

“Mass spectrum in Supersymmetric Scheme  
of Gelmini-Roncadelli”

M. C. Rodriguez

*Grupo de Física Teórica e Matemática  
Física*

*Departamento de Física*

*Universidade Federal Rural do Rio de  
Janeiro - UFRRJ*

*BR 465 Km 7, 23890-000*

*Seropédica, RJ, Brazil,*

*email: [marcoscrodriguez@ufrj.br](mailto:marcoscrodriguez@ufrj.br)*

## Plan

- Standard Model
- Scheme Gelmini-Roncadelli
- Majoron
- Possible Solution
- Supersymmetric Scheme of Gelmini-Roncadelli
- Mass Spectrum

## Standard Model

- We introduce only left-handed neutrinos

$$L_{iL} = \begin{pmatrix} \nu_{iL} \\ l_{iL} \end{pmatrix} \sim \left( \mathbf{1}, \mathbf{2}, -\frac{1}{2} \right)$$
$$l_{iR} \sim (\mathbf{1}, \mathbf{1}, -1) \quad i = 1, 2, 3$$

$$Q_{iL} = \begin{pmatrix} u_{iL} \\ d_{iL} \end{pmatrix} \sim \left( \mathbf{3}, \mathbf{2}, +\frac{1}{6} \right)$$
$$u_{iR} \sim \left( \mathbf{3}, \mathbf{1}, +\frac{2}{3} \right) \quad d_{iR} \sim \left( \mathbf{3}, \mathbf{1}, -\frac{1}{3} \right)$$

- One Scalar in doublet representation

$$\phi = \begin{pmatrix} \phi^+ \\ \phi^0 \end{pmatrix} \sim \left( \mathbf{1}, \mathbf{2}, +\frac{1}{2} \right)$$
$$\tilde{\phi} \equiv [(i\sigma_2) \phi^*] = \begin{pmatrix} (\phi^0)^* \\ -\phi^- \end{pmatrix} \sim \left( \mathbf{1}, \mathbf{2}, -\frac{1}{2} \right)$$

- vacuum expectation value (VEV)

$$\langle \phi \rangle \equiv \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ v \end{pmatrix} \quad \langle \tilde{\phi} \rangle = \frac{1}{\sqrt{2}} \begin{pmatrix} v \\ 0 \end{pmatrix}$$

- Lagrangian

$$\mathcal{L}_{SM} = \mathcal{L}_{SM}^Y - V(\phi) + \mathcal{L}_{SM}^{kin}$$

- Yukawa Couplings

$$\begin{aligned} \mathcal{L}_{SM}^Y = & \left[ g_{ij}^l (\bar{L}_{iL} \phi) l_{jR} + g_{ij}^d (\bar{Q}_{iL} \phi) d_{jR} \right. \\ & \left. + g_{ij}^u (\bar{Q}_{iL} \tilde{\phi}) u_{jR} + hc \right] \end{aligned}$$

- All the charged leptons get mass at tree level
- Top quark mass (CMS Collaboration- LHC)  
 $m_t = 172.25 \pm 0.08(\text{stat.}) \pm 0.62(\text{syst.}) \text{ GeV}$
- Neutrinos massless any order in perturbation theory

- Scalar Potential

$$V(\phi) = \mu^2|\phi|^2 + \lambda|\phi|^4$$

- Condition of Extremes

$$\left. \frac{\partial V(\phi)}{\partial \phi} \right|_{\langle \phi \rangle = v} = 0$$

- Shift in the neutral scalar field

$$\phi^0 \equiv \frac{1}{\sqrt{2}} (v + h^0 + iG^0)$$

- One Goldstone boson (CP-odd)

- One massive boson (CP-even)

$$M_{h^0}^2 = -2\mu^2$$

- Discovered in LHC

$$M_{h^0} = (125.20 \pm 0.11) \text{ GeV}$$

- Mass for Gauge Bosons

$$\mathcal{L}_{SM}^{kin} = (D_m \phi)^\dagger (D^m \phi)$$

$$D_m \phi = \left[ \partial_m - ig \sum_{i=1}^3 \left( \frac{\sigma^i}{2} \right) W_m^i - ig' \left( \frac{1}{2} \right) B_m \right] \phi$$

- Two Massive Gauge Bosons

$$M_{W^\pm}^2 = \frac{g^2 v^2}{4} = [(80.3505 \pm 0.0077) \text{ GeV}]^2$$

$$W^\pm = \frac{1}{\sqrt{2}} (W_m^1 \mp iW_m^2)$$

$$M_{Z^0}^2 = \left( \frac{g^2 + (g')^2}{4} \right) v^2 = \frac{M_{W^\pm}^2}{\cos^2 \theta_W}$$

$$\begin{pmatrix} Z_m^0 \\ A_m \end{pmatrix} = \begin{pmatrix} \cos \theta_W & -\sin \theta_W \\ \sin \theta_W & \cos \theta_W \end{pmatrix} \begin{pmatrix} W_m^3 \\ B_m \end{pmatrix}$$

$$\tan \theta_W \equiv \frac{g'}{g}$$

- Average Experimental Values

$$(M_{W^\pm})_{ave} = (80.4133 \pm 0.0080) \text{ GeV}$$

$$(M_{Z^0})_{ave} = (91.1875 \pm 0.0021) \text{ GeV}$$

$$\sin^2 \theta_W = 0.2324 \pm 0.0012$$

- Scheme Gelmini-Roncadelli [PLB99, 411, \(1981\)](#); [S. M. Bilenky, hep-ph/1210.3065](#) ( Neutrinos are massive )

$$\overline{L_{iL}^c} L_{jL} \sim (\mathbf{1}, \mathbf{1} \oplus \mathbf{3}, -1)$$

- 1-) Extra fermions in singlet  $N$  type I See-saw mechanism
- 2-) Extra scalars  $\Delta$  in triplets type II
- 3-) Extra fermions  $\Sigma$  in triplets type III

- New scalar

$$\begin{aligned} \Delta &\sim (\mathbf{1}, \mathbf{3}, 1) \\ \Delta &= \begin{pmatrix} \Delta^0 & \frac{h^+}{\sqrt{2}} \\ \frac{h^+}{\sqrt{2}} & H^{++} \end{pmatrix} \\ \langle \Delta \rangle &= \frac{1}{\sqrt{2}} \begin{pmatrix} V_\Delta & 0 \\ 0 & 0 \end{pmatrix} \end{aligned}$$

- Fermilab's CDF

$$(M_W)_{\text{CDF}} = (80.4335 \pm 0.0094) \text{ GeV}$$

- Masses for neutrinos

$$\begin{aligned}
 \mathcal{L}_{\Delta,L}^{\nu} &= g_{ij}^{\nu} \left[ \left( \overline{L}_{iL}^c \Delta L_{jL} \right) + hc \right] \\
 &= g_{ij}^{\nu} \left[ \overline{\nu}_{iL}^c \nu_{jL} \Delta^0 \right. \\
 &\quad + \left( \overline{\nu}_{iL}^c l_{jL} - \overline{l}_{iL}^c \nu_{jL} \right) \frac{h^+}{\sqrt{2}} \\
 &\quad \left. + \overline{l}_{iL}^c l_{jL} H^{++} + hc \right]
 \end{aligned}$$

- Neutrinos are Majorana Particles



- A. S. Barabash nucl-ex/1107.5663

- Experiments CUORE, GERDA, MAJORANA

- Masses in Gauge Bosons

$$M_W^2 = \frac{g^2 v^2}{4} (1 + 2R)$$

$$M_Z^2 = \frac{g^2 v^2}{4 \cos^2 \theta_W} (1 + 4R)$$

$$\rho \equiv \left( \frac{M_W^2}{M_Z^2 \cos^2 \theta_W} \right) = \frac{1 + 2R}{1 + 4R} \simeq 1 - 2R$$

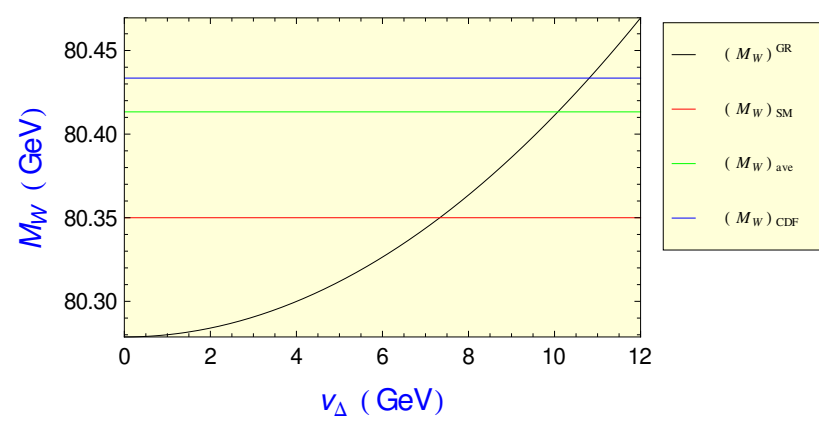
$$R = \left( \frac{v \Delta}{v} \right)^2$$

$$\rho^{SM} = 1$$

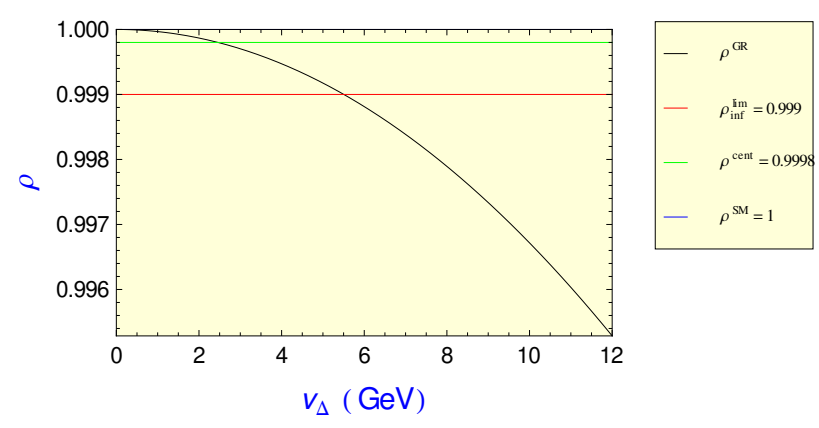
$$\rho_{EXP} = 0.9998 \pm 0.0008$$

- Some Numerical Results

•  $M_W$



•  $\rho$



- Scalar Potential (Majoron  $M^0$ )

$$\begin{aligned}
 V_G(\phi, \Delta) = & \mu^2(\phi^\dagger\phi) + M^2\text{Tr}(\Delta^\dagger\Delta) \\
 & + \lambda_1(\phi^\dagger\phi)^2 + \lambda_2 [\text{Tr}(\Delta^\dagger\Delta)]^2 \\
 & + \lambda_3\text{Tr}[(\Delta^\dagger\Delta)(\Delta^\dagger\Delta)] \\
 & + \lambda_4(\phi^\dagger\phi)\text{Tr}(\Delta^\dagger\Delta) \\
 & + i\lambda_5\epsilon_{ijk}(\phi^\dagger\sigma^i\phi)(\Delta^{j\dagger}\Delta^k)
 \end{aligned}$$

- CP-even two massive states

- CP- odd two Goldstone boson

$$(A, Z) \rightarrow (A, Z + 2) + 2e^- + M^0$$

- It is excluded by experimental data

- A. S. Barabash nucl-ex/1107.5663

- Possible Solution

- We can remove Majoron; E.Ma PRL80, 5716, (1998)

$$V(\phi, \Delta) = V_G(\phi, \Delta) + [\mu_M (\phi^\dagger \Delta \tilde{\phi}) + hc]$$

- Mass Spectrum

$$M_{h^0}^2 \approx 2\lambda_1 v^2 \text{ SMHiggs}$$

$$M_{H^0}^2 \approx \frac{\mu_M v^2}{\sqrt{2} V_\Delta}$$

$$M_{A^0}^2 \approx \frac{\mu_M}{\sqrt{2}} \left( \frac{4v_\Delta^2 + v^2}{V_\Delta} \right) = M_{H^0}^2 + 2\sqrt{2}\mu_M V_\Delta$$

- $V_\Delta \leq 3 \text{ GeV}$   $\mu \geq 10^0 \text{ GeV}$

$$400 \leq M_{H^0} \leq 1000 \text{ GeV}$$

$$400 \leq M_{A^0} \leq 1000 \text{ GeV}$$

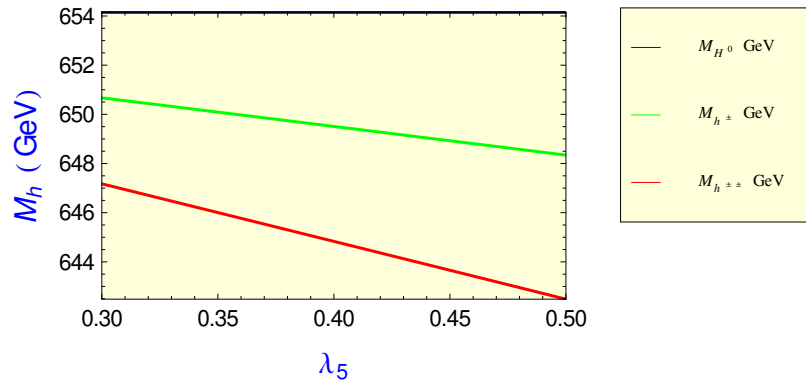
- Agree with Atlas results

- There are also charged scalars

$$M_{h^\pm}^2 = M_{H^0}^2 - \frac{\lambda_5}{4} v^2$$

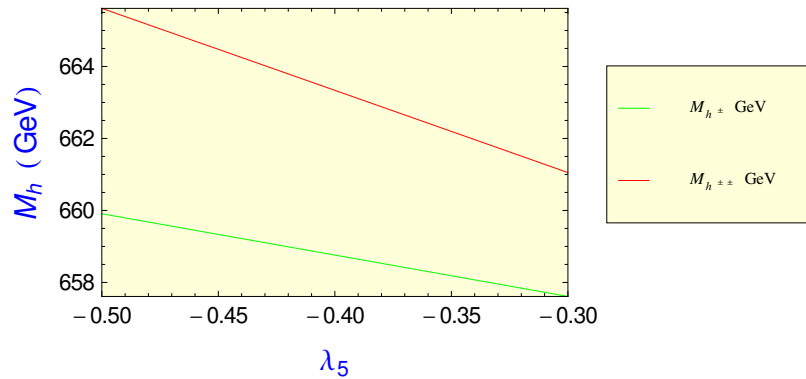
$$M_{h^{\pm\pm}}^2 = M_{H^0}^2 - \frac{\lambda_5}{2} v^2$$

- $\lambda_5 > 0$



$$M_{H^0} > M_{h^\pm} > M_{h^{\pm\pm}}$$

- $\lambda_5 < 0$



$$M_{h^{\pm\pm}} > M_{h^\pm} > M_{H^0}$$

- Some decays channels

$$H^{\pm\pm} \rightarrow l^\pm l^\pm$$

$$H^{\pm\pm} \rightarrow W^\pm W^\pm$$

$$H^{\pm\pm} \rightarrow H^\pm W^\pm \rightarrow \bar{b}b W^\pm W^\pm$$

- contain source of  $L$  and  $CP$  violation at high scale
- can not induce Leptogenesis Ambrosio PLB604, 199, (2004)

- It is simple to introduce it in SUSY

- A. V. Gladyshev and D. I. Kazakov [arXiv:1212.2548 [hep-ph]]

- Usual fermions Chiral Superfield

- Scalars Chiral Superfield

$$\begin{aligned}
 H_1 &= \begin{pmatrix} h_1^0 \\ h_1^- \end{pmatrix} & \langle H_1 \rangle &= \frac{1}{\sqrt{2}} \begin{pmatrix} v_1 \\ 0 \end{pmatrix} \\
 H_2 &= \begin{pmatrix} h_2^+ \\ h_2^0 \end{pmatrix} & \langle H_2 \rangle &= \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ v_2 \end{pmatrix}
 \end{aligned}$$

- Gauge bosons  $SM$  Vector Superfields

a-) Gluons  $g$ , superpartners gluinos  $\tilde{g}$

b-)  $SU(2)$  gauge  $W_i$ , superpartnes  $\tilde{W}_i$   $i = 1, 2, 3$

c-)  $U(1)$  gauge  $B_m$ , superpartner  $\tilde{B}$

- Superpotential

$$W_{RC}^{MSSM} = \mu (\hat{H}_1 \hat{H}_2) + f_{ij}^l (\hat{H}_1 \hat{L}_i) \hat{E}_j \\ + f_{ij}^d (\hat{H}_1 \hat{Q}_i) \hat{D}_j + f_{ij}^u (\hat{H}_2 \hat{Q}_i) \hat{U}_j$$

- Some Problems in the MSSM

a-) Neutrinos are massless

b-)  $\mu$  Problem

b1-) Singlet  $N$

$$t_N \hat{N} + \mu_N \hat{N} \hat{N} + \kappa \hat{N} \hat{N} \hat{N} + \lambda \hat{N} (\hat{H}_1 \hat{H}_2)$$

b2-) Triplet  $T$   $Y = 0$

$$\mu_T \text{Tr} [\hat{T} \hat{T}] + \lambda \text{Tr} [(\hat{H}_1 \hat{T} \hat{H}_2)]$$

c-) Strong  $CP$  Problem

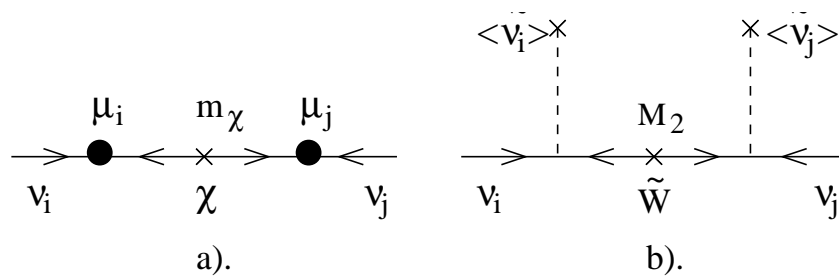
- Generate mass to neutrinos break  $R$ -Parity

- A. Yu. Smirnov hep-ph/0411194

- Superpotential

$$W_{RV}^{MSSM} = W_{RC}^{MSSM} + \mu_i \hat{L}_i \hat{H}_2 + \lambda'_{ijk} \hat{L}_i \hat{L}_j \hat{E}_k + \lambda''_{ijk} \hat{L}_i \hat{Q}_j \hat{D}_k$$

- one get mass tree-level (Majorana Particle)



- type I (gaugino  $U(1)$   $\tilde{B}$  )

- type III (wino  $\tilde{W}_3$  )

- Supersymmetric Scheme of Gelmini-Roncadelli  
A. Rossi PRD66, 075003, (2002)

- Usual fermions, Gauge bosons  $H_1, H_2$   
 $MSSM$

- Scalars

$$\Delta_1 = \begin{pmatrix} \Delta_1^0 & \frac{h_1^+}{\sqrt{2}} \\ \frac{h_1^+}{\sqrt{2}} & H_1^{++} \end{pmatrix} \quad \langle \Delta_1 \rangle = \frac{1}{\sqrt{2}} \begin{pmatrix} V_{\Delta_1} & 0 \\ 0 & 0 \end{pmatrix}$$

$$\Delta_2 = \begin{pmatrix} \Delta_2^{--} & \frac{h_2^-}{\sqrt{2}} \\ \frac{h_2^-}{\sqrt{2}} & \Delta_2^0 \end{pmatrix} \quad \langle \Delta_2 \rangle = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 & 0 \\ 0 & V_{\Delta_2} \end{pmatrix}$$

- $\Delta_1 \sim (1, \mathbf{3}, 1) \quad L = -2$

- $\Delta_2 \sim (1, \bar{\mathbf{3}}, -1) \quad L = 2$

- Leptogenesis is possible due to finite temperature effects

- Superpotential

$$\begin{aligned}
W_{SUSY}^{GR} &= W_{RC}^{MSSM} + \mu_{\Delta} Tr \left[ (\hat{\Delta}_1 \hat{\Delta}_2) \right] \\
&+ f_{ij}^N Tr \left[ \hat{L}_i \hat{\Delta}_1 \hat{L}_j \right] + \lambda_1 Tr \left[ \hat{H}_1 \hat{\Delta}_1 \hat{H}_1 \right] \\
&+ \lambda_2 Tr \left[ \hat{H}_2 \hat{\Delta}_2 \hat{H}_2 \right]
\end{aligned}$$

- $\Delta_1$  and  $\Delta_2$  degenerated  $\mu_{\Delta}$

- $CP$ -violation induce Leptogenesis by SSB

$$\begin{aligned}
-\mathcal{L}_{soft} &= m_{\Delta_1}^2 \Delta_1^\dagger \Delta_1 + m_{\Delta_2}^2 \Delta_2^\dagger \Delta_2 \\
&+ (BM_T \Delta_1 \Delta_2 + hc) + \dots
\end{aligned}$$

- $B$ -term remove degeneracy
- $T_-$  mass  $\mu_{\Delta}^2 + BM_T$  (unstable)
- $T_+$  mass  $\mu_{\Delta}^2 - BM_T$
- $T_-$  decay in Leptons **Lepton Asymmetry**  
Ambrosio PLB604, 199, (2004)

- Gauge bosons

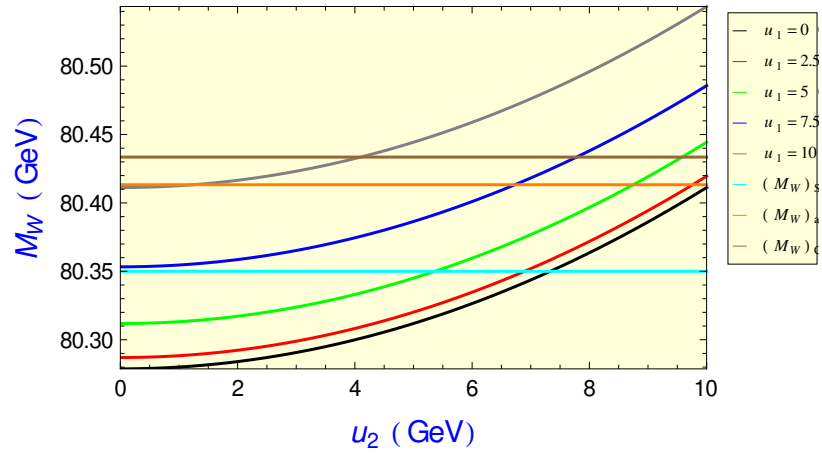
$$M_{W^\pm}^2 = \frac{g^2 v^2}{4} [1 + 2(u_1 + u_2)]$$

$$M_{Z^0}^2 = \frac{g^2 v^2}{4 \cos^2 \theta_W} [1 + 4(u_1 + u_2)]$$

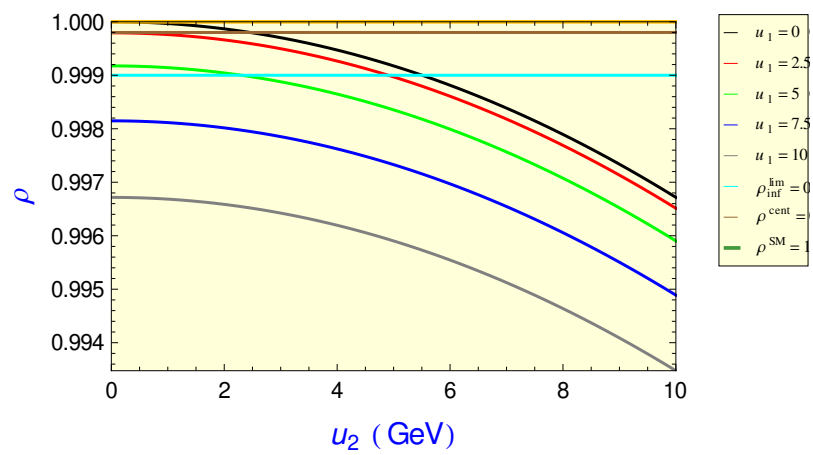
$$\rho \approx 1 - 2(u_1 + u_2)$$

$$u_1 = \left( \frac{V_{\Delta_1}}{v} \right)^2, \quad u_2 = \left( \frac{V_{\Delta_2}}{v} \right)^2$$

•  $M_W$



•  $\rho$



- $\lambda_{1,2}$  explicit break  $L$  similar to  $\mu_M$
- Charginos, Neutralinos and Sleptons Production
- Singlet/ Triplet

$$\begin{aligned}
& \lambda_T \hat{N} \text{Tr} \left[ \left( \hat{\Delta}_1 \hat{\Delta}_2 \right) \right] + \lambda_N \hat{N} \left( \hat{H}_1 \hat{H}_2 \right) \\
+ & \kappa \hat{N} \hat{N} \hat{N} + \lambda_1 \text{Tr} \left[ \left( \hat{H}_1 \hat{\Delta}_1 \hat{H}_2 \right) \right] \\
+ & \lambda_2 \text{Tr} \left[ \left( \hat{H}_1 \hat{\Delta}_2 \hat{H}_2 \right) \right]
\end{aligned}$$

- Both Mechanism are present in MSUSY331

1-) J. C. Montero, V. Pleitez and M. C. Rodriguez, *Phys. Rev.* **D65**, 035006, (2002);

2-) M. Capdequi-Peyranère and M.C. Rodriguez, *Phys. Rev.* **D 65**, 035001 (2002);

- M. C. Rodriguez *Int. J. Mod. Phys.***A39**, 2440001, (2024);

- M. C. Rodriguez *Int. J. Mod. Phys.***A40**, 2550092, (2025).

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