

update

Thessaloniki, Greece, 28 August - 4 September 2016

XIIIth Quark Confinement and the Hadronic Spectrum

[<https://indico.cern.ch/event/353906/overview>]

October 13, 2016

Sessions

1. Section A: **Vacuum Structure and Confinement**
2. Section B: **Light Quarks**
[Chiral and soft collinear effective theories; sum rules; lattice; **Schwinger-Dyson equations**; masses of light quarks; light-quark loops; structure functions; **phenomenology of light-hadron form factors**, experiments.]
3. Section C: **Heavy Quarks**
4. Section D: **Deconfinement**
5. Section E: **QCD and New Physics**
6. Section F: **Nuclear and Astroparticle Physics**
7. Section G: **Strongly Coupled Theories**
8. **Future Perspectives, Upgrades, Instrumentation**
9. **Statistical Methods for Physics Analysis in the XXI Century**
10. **Poster session**

8:30-10:30 Plenary: Session III – Aristotelis, Chair: *Gastao Krein*

8:30 Roy-Steiner analysis of pion nucleon-scattering and a precision determination of the sigma-term

Ulf-G. Meißner

Yes **9:00** Precision physics with QCD *No single word about APT. Interesting* *Antonio Pich*

9:30 Review of present experimental and theoretical status of the proton radius puzzle

Richard Hill

Yes **10:00** One and two nucleon matrix elements from lattice QCD for precision tests of the SM in NP environments

Andre Walker-Loud

10:30-11:00

Coffee Break

11:00-13:00 Plenary: Session IV – Aristotelis, Chair: *Joan Soto*

11:00 Hadron physics meets gravity

Felipe J. Llanes-Estrada

11:30 Flavour anomalies

Thomas Blake

12:00 ROUND TABLE: Flavour anomalies - New Physics or QCD effects?

*Marco Gersabeck
Roman Zwicky
Zhaofeng Liu
Thomas Blake
Lars Hofer
Sebastian Jaeger*

13:00-15:00

Lunch

VACUUM STRUCTURE AND CONFINEMENT A2	LIGHT QUARKS B2	LIGHT QUARKS B3	HEAVY QUARKS C2	DECONFINMENT D2	QCD AND NEW PHYSICS E2	STRONGLY COUPLED THEORIES G2
<i>Alexandros II</i> Chair: <i>Dmitry Antonov</i>	<i>Aristotelis II</i> Chair: <i>Nikolaos Stefanis</i>	<i>Amfitrion II</i> Chair: <i>Jose Luis Goity</i>	<i>Alexandros I</i> Chair: <i>Antonio Vairo</i>	<i>Aristotelis I</i> Chair: <i>Piotr Bozek</i>	<i>Amfitrion I</i> Chair: <i>Martha Constantinou, Felipe J. Llanes-Estrada, Marco Gersabeck</i>	<i>Erato</i> Chair: <i>Ilias Kyritsis</i>
Gauge engineering and propagators 17:30 <i>Axel Maas</i>	Meson Form Factors and Deep Exclusive Meson Production Experiments 17:30 <i>Tanja Horn</i>	Roy-Steiner-equation analysis of pion-nucleon scattering 17:30 <i>Jacobo Ruiz De Elvira</i>	Isospin-breaking in the decay constants of heavy mesons from QCD sum rules 17:30 <i>Dmitri Melikhov</i>	The flow paradigm 17:30 <i>Jean-Yves Ollitrault</i>	Perturbative and non-perturbative QCD parameters in Dispersive model. 17:30 <i>Mohammad Ebrahim Zomorrodian</i>	Strong dynamics on the lattice 17:30 <i>Daniel Nogradi</i>
From QCD's n-point functions to nucleon resonances 18:00 <i>Gernot Eichmann</i>	Inclusive Cross Sections, Parton Density Functions and the strong coupling at HERA 18:00 <i>Stefan Schmitt</i>	Unitary coupled channel approach to diffractive scattering and its application to axial vector states 18:00 <i>Ed Berger</i>	D and B mesons masses in chiral perturbation theory with heavy quark symmetry 17:50 <i>Mohammad Alhakami</i>	Overview of experimental results on collective flow with identified particles at RHIC and the LHC 18:00 <i>Panos Christakoglou</i>	Search for heavy resonances in vector boson scattering 17:45 <i>Guangyi Zhang</i> Measurement of the WZ boson pair production cross section at 13 TeV and limits on anomalous triple gauge couplings with the ATLAS detector 18:00 <i>Dimitrios Iliadis</i>	Infrared behaviors of two color gauge theory 18:00 <i>Kimmo Tuominen</i>
Three-point functions in Yang-Mills Theory and QCD in Landau gauge 18:30 <i>Adrian Lorenz Blum</i>	Nucleon structure functions and longitudinal spin asymmetries 18:20 <i>Harleen Dahiya</i>	The anomalous triangle singularity and its implications of threshold enhancements 18:30 <i>Qiang Zhao</i>	Approximate degeneracy of heavy-light mesons with the same L 18:10 <i>Takayuki Matsuki</i>	Collectivity I hydrodynamics 18:30 <i>Wojciech Florkowski</i>	Measurement of the ZZ(*) production cross section in the four lepton channel at 8 TeV and 13 TeV and limits on anomalous triple gauge couplings with the ATLAS detector 18:15 <i>Kostas Kordas</i>	Composite Higgs Dynamics on the Lattice 18:30 <i>Claudio Pica</i>
Chiral symmetry breaking in continuum QCD 18:50 <i>Mario Mitter</i>	Pion-photon transition form factor at low-mid momenta within collinear QCD 18:40 <i>Sergey Mikhailov</i>	Pion-eta scalar-isovector 3-coupled channel amplitude fitted to branching ratio as and threshold plus subthreshold parameters 19:00 <i>Robert Kaminski</i>	The bottom-quark mass from non-relativistic sum rules at NNNLO 18:30 <i>Jan Piclum</i>	Overview of collectivity in small systems 19:00 <i>Wei Li</i>	Break 18:30	Inverse magnetic catalysis in holographic models of QCD 19:00 <i>Kiminad Mamo</i>
Dyson-Schwinger approach to Hamiltonian QCD 19:10 <i>Davide Campagnari</i>	Neutral pion form factor measurement by the NA62 experiment 19:10 <i>Monica Pepe</i>	Properties of exotic and non-exotic quark-bilinears within the Dyson-Schwinger - Bethe-Salpeter equation approach 19:20 <i>Thomas Hilger</i>	Short-distance current correlators on the lattice 18:50 <i>Shoji Hashimoto</i>	Anisotropic hydrodynamics 19:30 <i>Michael Strickland</i>	Recent progress on QCD inputs for axion phenomenology 18:45 <i>Massimo D'elia</i>	Axion cosmology from lattice QCD 19:30 <i>Sandor Katz</i>
	Electromagnetic transition form factor and radiative corrections in decays of neutral pions 19:30 <i>Tomas Husek</i>		Experimental highlights: Heavy Quark Physics in Heavy-ion collisions at RHIC 19:10 <i>Rachid Nouicer</i>		Controlling quark mass determinations non-perturbatively in three-flavour QCD 19:05 <i>Patrick Fritzschn</i>	
					Constraining anomalous Higgs couplings at high and low energy 19:20 <i>Emanuele Mereghetti</i>	
					Observation of Anomalous Internal Pair Creation in 8Be: A Possible Signature of a Light, Neutral Boson 19:35 <i>Attila Krasznahorkay</i>	



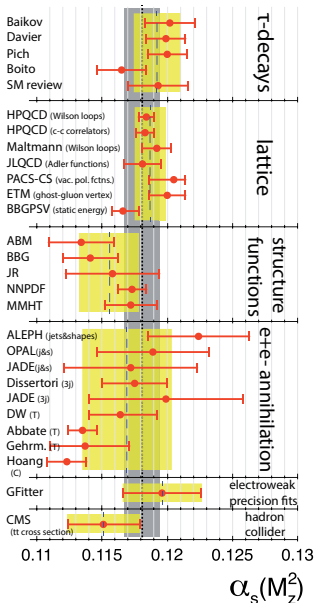
Precision Physics with QCD

Antonio Pich

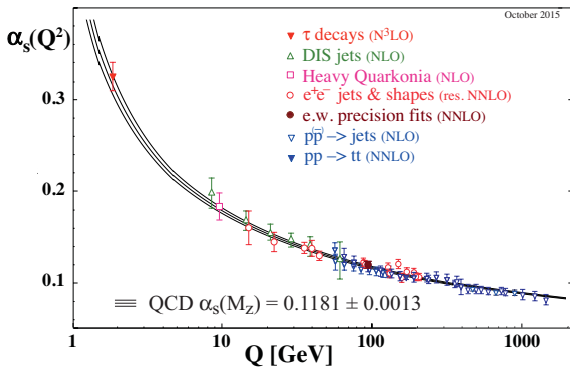
IFIC, Univ. Valencia – CSIC

XIIth Quark Confinement and the Hadron Spectrum
Thessaloniki, Greece, 29th August – 3th September 2016

PDG 2015



S. Bethke, G. Dissertori, G. Salam



See also: S. Alekhin et al., arXiv:1512.05194 [hep-ph]

New analysis of ALEPH data

Rodríguez-Sánchez, Pich, arXiv:1605.06830

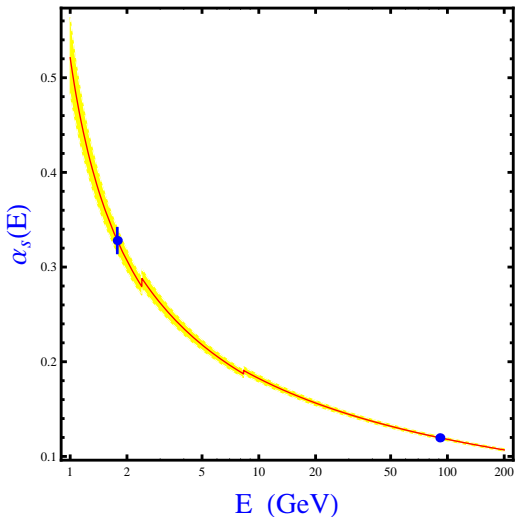
Method (V + A)	$\alpha_s(m_\tau^2)$		
	CIPT	FOPT	Average
ALEPH moments ¹	$0.339^{+0.019}_{-0.017}$	$0.319^{+0.017}_{-0.015}$	$0.329^{+0.020}_{-0.018}$
Mod. ALEPH moments ²	$0.338^{+0.014}_{-0.012}$	$0.319^{+0.013}_{-0.010}$	$0.329^{+0.016}_{-0.014}$
$A^{(2,m)}$ moments ³	$0.336^{+0.018}_{-0.016}$	$0.317^{+0.015}_{-0.013}$	$0.326^{+0.018}_{-0.016}$
s_0 dependence ⁴	0.335 ± 0.014	0.323 ± 0.012	0.329 ± 0.013
Borel transform ⁵	$0.328^{+0.014}_{-0.013}$	$0.318^{+0.015}_{-0.012}$	$0.323^{+0.015}_{-0.013}$
Combined value	0.335 ± 0.013	0.320 ± 0.012	0.328 ± 0.013



$$\alpha_s(M_Z^2) = 0.1197 \pm 0.0015$$

- $\omega_{kl}(x) = (1+2x)(1-x)^{2+k}x^l$ (k, l) = (0, 0), (1, 0), (1, 1), (1, 2), (1, 3)
- $\tilde{\omega}_{kl}(x) = (1-x)^{2+k}x^l$ (k, l) = (0, 0), (1, 0), (1, 1), (1, 2), (1, 3)
- $\omega^{(2,m)}(x) = (1-x)^2 \sum_{k=0}^m (k+1)x^k = 1 - (m+2)x^{m+1} + (m+1)x^{m+2}$, $1 \leq m \leq 5$
- $\omega^{(2,m)}(x)$ $0 \leq m \leq 2$, 1 single moment in each fit
- $\omega_a^{(1,m)}(x) = (1-x^{m+1})e^{-ax}$ $0 \leq m \leq 6$

α_s at N³LO from τ and Z



$$\alpha_s(m_\tau^2) = 0.328 \pm 0.013$$



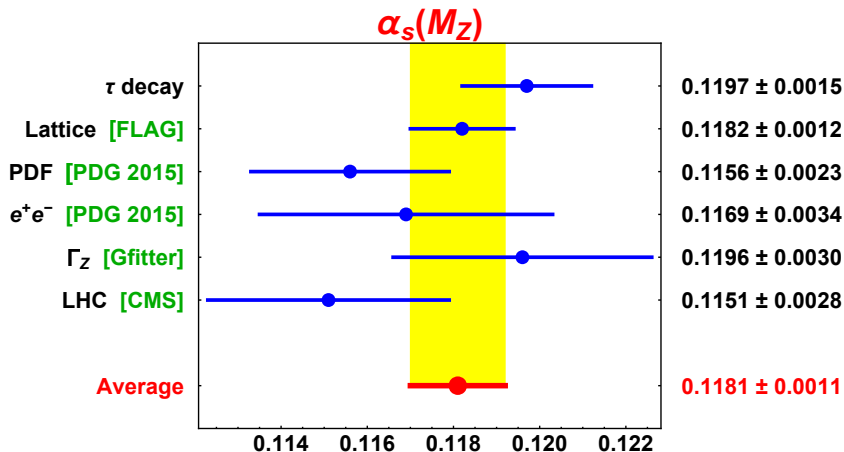
$$\alpha_s(M_Z^2) = 0.1197 \pm 0.0015$$

$$\alpha_s(M_Z^2)_{Z \text{ width}} = 0.1196 \pm 0.0030$$

**The most precise test of
Asymptotic Freedom**

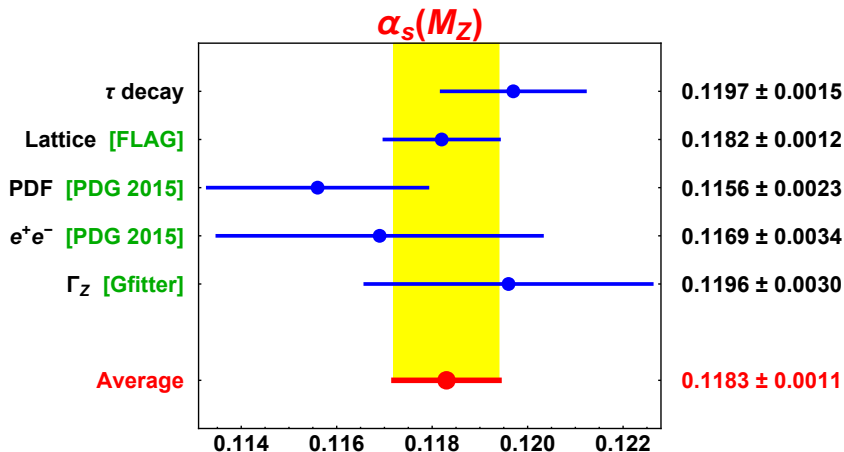
$$\alpha_s^\tau(M_Z^2) - \alpha_s^Z(M_Z^2) = 0.0001 \pm 0.0015_\tau \pm 0.0030_Z$$

$\alpha_s(M_Z^2)$: 2016 Average



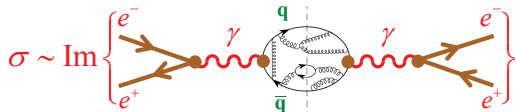
PDG 2015: $\alpha_s(M_Z^2) = 0.1181 \pm 0.0013$

$\alpha_s(M_Z^2)$: 2016 Average



PDG 2015: $\alpha_s(M_Z^2) = 0.1181 \pm 0.0013$

Inclusive Observables: $R_{ee}(s)$



$$R_{ee}(s) = 12\pi \operatorname{Im}\Pi_{em}(s)$$

$$\Pi_{em}^{\mu\nu}(q) \equiv i \int d^4x e^{iqx} \langle 0 | T [J_{em}^\mu(x) J_{em}^\nu(0)] | 0 \rangle = (-g^{\mu\nu} q^2 + q^\mu q^\nu) \Pi_{em}(q^2)$$

$$R_{ee} \equiv \frac{\Gamma(e^+e^- \rightarrow \text{hadrons})}{\Gamma(e^+e^- \rightarrow e^+e^-)} = \sum_q Q_q^2 N_C \left\{ 1 + \sum_{n \geq 1} F_n \left[\frac{\alpha_s(M_Z^2)}{\pi} \right]^n \right\} + \mathcal{O}\left(\frac{m_q^2}{s}, \frac{\Lambda^4}{s^2}\right)$$

Perturbative series known to $\mathcal{O}(\alpha_s^4)$: ($n_F = 5$)

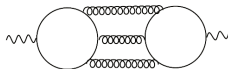
Baikov-Chetyrkin-Kühn-Ritinger

$$F_1 = 1 \quad , \quad F_2 = 1.9857 - 0.1153 n_F = 1.4092$$

$$F_3 = -6.63694 - 1.20013 n_F - 0.00518 n_F^2 - 1.2395 \eta = -12.805$$

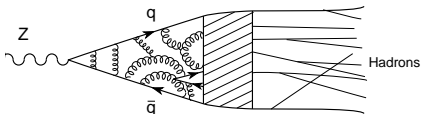
$$F_4^{\text{NS}} = -156.608 + 18.7748 n_F - 0.7974 n_F^2 + 0.0215 n_F^3 - 14.952 \eta = -80.434$$

$$\eta = \left(\sum_q Q_q \right)^2 / \left(N_C \sum_q Q_q^2 \right)$$



Singlet contributions

Z Hadronic Width



Vector + Axial

$$R_Z \equiv \frac{\Gamma(Z \rightarrow \text{hadrons})}{\Gamma(Z \rightarrow e^+e^-)} = R_Z^{\text{EW}} N_C \left\{ 1 + \sum_{n \geq 1} \tilde{F}_n \left[\frac{\alpha_s(M_Z^2)}{\pi} \right]^n \right\} + \mathcal{O}\left(\frac{m_q^2}{M_Z^2}, \frac{\Lambda^4}{M_Z^4}\right)$$

Perturbative series known to $\mathcal{O}(\alpha_s^4)$

Baikov-Chetyrkin-Kühn-Rittger

$$\left[+ \mathcal{O}\left(\alpha_s^2 \frac{m_b^4}{M_Z^4}, \alpha_s^2 \frac{m_b^2}{m_t^2}, \alpha_s^3 \frac{M_Z^2}{m_t^2}\right) \right]$$

Z-pole data (EW fit)

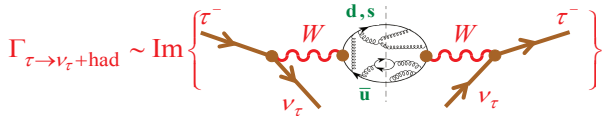


$$\alpha_s(M_Z^2) = 0.1196 \pm 0.0030$$

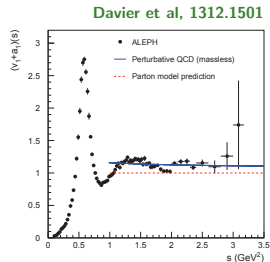
Gfitter 2014

Assumes validity of the EW Standard Model

τ Hadronic Width: R_τ



$$\Pi^{(J)}(s) \equiv |V_{ud}|^2 \left(\Pi_{ud,V}^{(J)}(s) + \Pi_{ud,A}^{(J)}(s) \right) + |V_{us}|^2 \Pi_{us,V+A}^{(J)}(s)$$



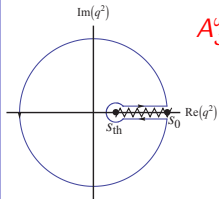
$$v_1 = 2\pi \text{Im}\Pi_{ud,V}^{(1)}(s) \quad , \quad a_1 = 2\pi \text{Im}\Pi_{ud,A}^{(1)}(s)$$

$$R_\tau = \frac{\Gamma[\tau^- \rightarrow \nu_\tau \text{hadrons}]}{\Gamma[\tau^- \rightarrow \nu_\tau e^- \bar{\nu}_e]} = R_{\tau,V} + R_{\tau,A} + R_{\tau,S}$$

$$= 12\pi \int_0^{m_\tau^2} \frac{ds}{m_\tau^2} \left(1 - \frac{s}{m_\tau^2}\right)^2 \left[\left(1 + 2\frac{s}{m_\tau^2}\right) \text{Im}\Pi^{(0+1)}(s) - 2\frac{s}{m_\tau^2} \text{Im}\Pi^{(0)}(s) \right]$$

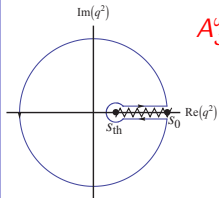
$$i \int d^4 x e^{iqx} \langle 0 | T \left[\mathcal{J}_{ij}^\mu(x) \mathcal{J}_{ij}^{\nu\dagger}(0) \right] | 0 \rangle = (-g^{\mu\nu} q^2 + q^\mu q^\nu) \Pi_{ij,\mathcal{J}}^{(1)}(q^2) + q^\mu q^\nu \Pi_{ij,\mathcal{J}}^{(0)}(q^2)$$

$$A_{\mathcal{J}}^\omega(s_0) \equiv \int_{s_{th}}^{s_0} \frac{ds}{s_0} \omega(s) \operatorname{Im} \Pi_{\mathcal{J}}^{(J)}(s) = \frac{i}{2} \oint_{|s|=s_0} \frac{ds}{s_0} \omega(s) \Pi_{\mathcal{J}}^{(J)}(s)$$



$$\Pi_{\mathcal{J}}^{(J)}(s) \approx \Pi_{\mathcal{J}}^{(J)}(s)^{\text{OPE}} = \sum_D \frac{\mathcal{O}_{D,\mathcal{J}}^{(J)}}{(-s)^{D/2}}$$

$$i \int d^4 x e^{iqx} \langle 0 | T [\mathcal{J}_{ij}^\mu(x) \mathcal{J}_{ij}^{\nu\dagger}(0)] | 0 \rangle = (-g^{\mu\nu} q^2 + q^\mu q^\nu) \Pi_{ij,\mathcal{J}}^{(1)}(q^2) + q^\mu q^\nu \Pi_{ij,\mathcal{J}}^{(0)}(q^2)$$



$$A_{\mathcal{J}}^\omega(s_0) \equiv \int_{s_{th}}^{s_0} \frac{ds}{s_0} \omega(s) \text{Im} \Pi_{\mathcal{J}}^{(J)}(s) = \frac{i}{2} \oint_{|s|=s_0} \frac{ds}{s_0} \omega(s) \Pi_{\mathcal{J}}^{(J)}(s)$$

$$\Pi_{\mathcal{J}}^{(J)}(s) \approx \Pi_{\mathcal{J}}^{(J)}(s)^{\text{OPE}} = \sum_D \frac{\mathcal{O}_{D,\mathcal{J}}^{(J)}}{(-s)^{D/2}}$$

$$\mathbf{R}_\tau = \mathbf{N}_C \mathbf{S}_{\text{EW}} (\mathbf{1} + \delta_P + \delta_{\text{NP}})$$

Braaten-Narison-Pich '92

$$= 6\pi i \oint_{|x|=1} (1-x)^2 \left[(1+2x) \Pi^{(0+1)}(m_\tau^2 x) - 2x \Pi^{(0)}(m_\tau^2 x) \right]$$

$$\delta_P = a_\tau + 5.20 a_\tau^2 + 26 a_\tau^3 + 127 a_\tau^4 + \dots \approx 20\%$$

Baikov-Chetyrkin-Kühn '08

$$a_\tau \equiv \alpha_s(m_\tau^2)/\pi, \quad \mathbf{S}_{\text{EW}} = 1.0201 (3)$$

Marciano-Sirlin, Braaten-Li, Erler

$$\delta_{\text{NP}} = -0.0064 \pm 0.0013 \quad (\text{Fitted from data})$$

Davier et al '14

Perturbative Contribution ($m_q = 0$)

$$a_\tau \equiv \frac{\alpha_s(m_\tau^2)}{\pi}$$

$$-s \frac{d}{ds} \Pi^{(0+1)}(s) = \frac{1}{4\pi^2} \sum_{n=0} K_n a_s (-s)^n \quad \rightarrow$$

$$\delta_P = \underbrace{\sum_{n=1} K_n A^{(n)}(\alpha_s)}_{\text{CIPT}} = \underbrace{\sum_{n=1} r_n a_\tau^n}_{\text{FOPT}}$$

$$A^{(n)}(\alpha_s) \equiv \frac{1}{2\pi i} \oint_{|x|=1} \frac{dx}{x} (1 - 2x + 2x^3 - x^4) \left(\frac{\alpha_s(-m_\tau^2 x)}{\pi} \right)^n = a_\tau^n + \dots$$

Perturbative Contribution ($m_q = 0$)

$$a_\tau \equiv \frac{\alpha_s(m_\tau^2)}{\pi}$$

$$-s \frac{d}{ds} \Pi^{(0+1)}(s) = \frac{1}{4\pi^2} \sum_{n=0} K_n a_s (-s)^n \quad \rightarrow$$

$$\delta_P = \underbrace{\sum_{n=1} K_n A^{(n)}(\alpha_s)}_{\text{CIPT}} = \underbrace{\sum_{n=1} r_n a_\tau^n}_{\text{FOPT}}$$

$$A^{(n)}(\alpha_s) \equiv \frac{1}{2\pi i} \oint_{|x|=1} \frac{dx}{x} (1 - 2x + 2x^3 - x^4) \left(\frac{\alpha_s(-m_\tau^2 x)}{\pi} \right)^n = a_\tau^n + \dots$$

1) The dominant corrections come from the contour integration

Large running of α_s along the circle $s = m_\tau^2 e^{i\phi}$, $\phi \in [-\pi, \pi]$

n	1	2	3	4	5
K_n	1	1.6398	6.37101	49.0757	?
r_n	1	5.2023	26.3659	127.079	$307.78 + K_5$
$r_n - K_n$	0	3.5625	19.9949	78.0029	307.78

Baikov-Chetyrkin-Kühn '08

Le Diberder-Pich '92

Perturbative Contribution ($m_q = 0$)

$$a_\tau \equiv \frac{\alpha_s(m_\tau^2)}{\pi}$$

$$-s \frac{d}{ds} \Pi^{(0+1)}(s) = \frac{1}{4\pi^2} \sum_{n=0} K_n a_s (-s)^n \quad \rightarrow$$

$$\delta_P = \underbrace{\sum_{n=1} K_n A^{(n)}(\alpha_s)}_{\text{CIPT}} = \underbrace{\sum_{n=1} r_n a_\tau^n}_{\text{FOPT}}$$

$$A^{(n)}(\alpha_s) \equiv \frac{1}{2\pi i} \oint_{|x|=1} \frac{dx}{x} (1 - 2x + 2x^3 - x^4) \left(\frac{\alpha_s(-m_\tau^2 x)}{\pi} \right)^n = a_\tau^n + \dots$$

2) CIPT gives rise to a well-behaved perturbative series

$a_\tau = 0.11$	$A^{(1)}(\alpha_s)$	$A^{(2)}(\alpha_s)$	$A^{(3)}(\alpha_s)$	$A^{(4)}(\alpha_s)$	δ_P
$\beta_{n>1} = 0$	0.14828	0.01925	0.00225	0.00024	0.20578
$\beta_{n>2} = 0$	0.15103	0.01905	0.00209	0.00020	0.20537
$\beta_{n>3} = 0$	0.15093	0.01882	0.00202	0.00019	0.20389
$\beta_{n>4} = 0$	0.15058	0.01865	0.00198	0.00018	0.20273
$\beta_{n>5} = 0$	0.15041	0.01859	0.00197	0.00018	0.20232
$\mathcal{O}(a_\tau^4)$ FOPT	0.16115	0.02431	0.00290	0.00015	0.22665

FOPT overestimates δ_P by 11%



PDFs from Jefferson Lab to the LHC

Wally Melnitchouk



JLab Angular Momentum (JAM) collaboration: <http://www.jlab.org/JAM>



CTEQ-JLab (CJ) collaboration: <http://www.jlab.org/CJ>

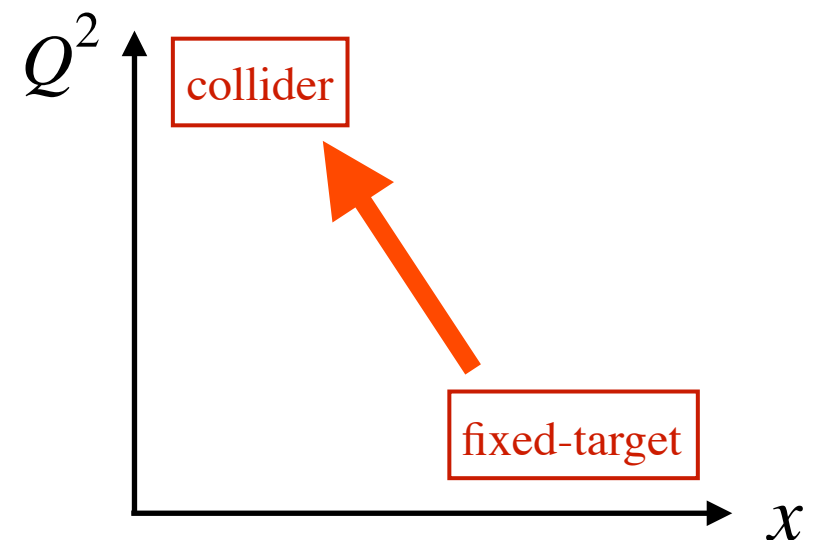
☀ Universality of PDFs allows data from many different processes (DIS, SIDIS, weak boson/jet production in pp , Drell-Yan, ...) to be analyzed simultaneously

→ global QCD analyses of spin-averaged ($f = f^\uparrow + f^\downarrow$) and spin-dependent ($\Delta f = f^\uparrow - f^\downarrow$) PDFs

☀ Precision PDFs needed to

- (1) understand basic structure of QCD bound states
- (2) compute backgrounds in searches for BSM physics

→ Q^2 evolution feeds low x , high Q^2 (“LHC”) from high x , low Q^2 (“JLab”)



Valence quarks & QCD models

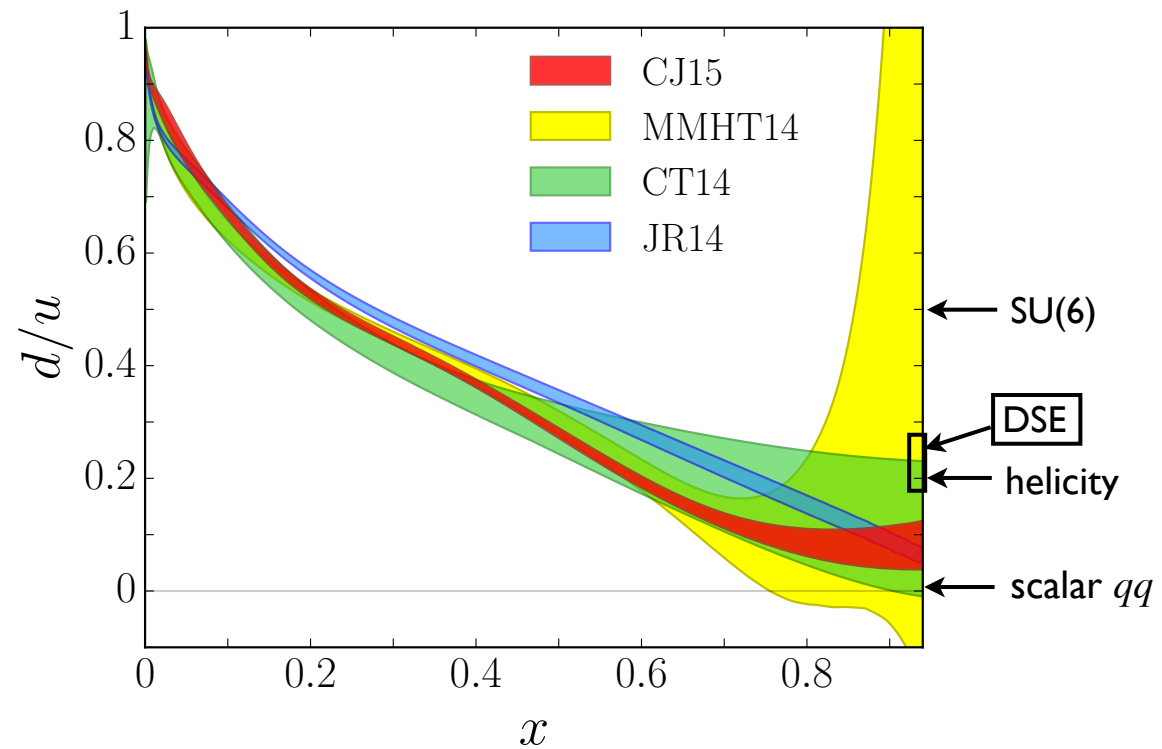
☀ Valence d/u ratio at high x of particular interest

→ testing ground for nucleon models in $x \rightarrow 1$ limit

- $d/u \rightarrow 1/2$
SU(6) symmetry
- $d/u \rightarrow 0$
 $S = 0$ qq dominance
(color-hyperfine interaction)
- $d/u \rightarrow 1/5$
 $S_z = 0$ qq dominance
(perturbative gluon exchange)
- $d/u \rightarrow 0.18 - 0.28$
DSE with qq correlations



Roberts

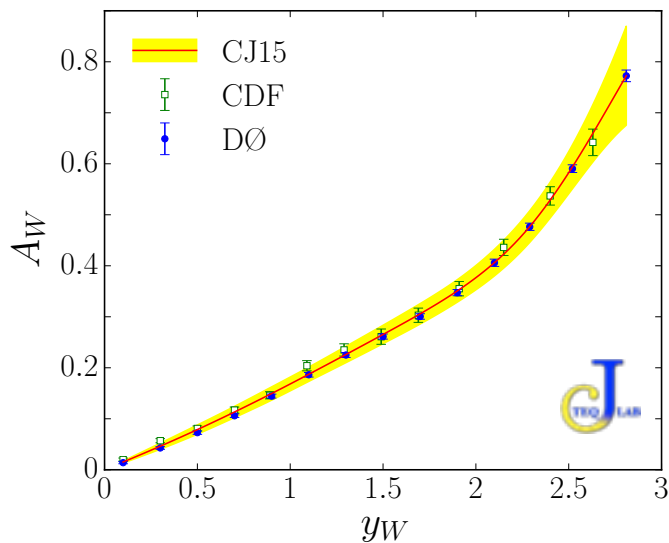


→ considerable uncertainty at high x from deuterium corrections (no free neutrons!)

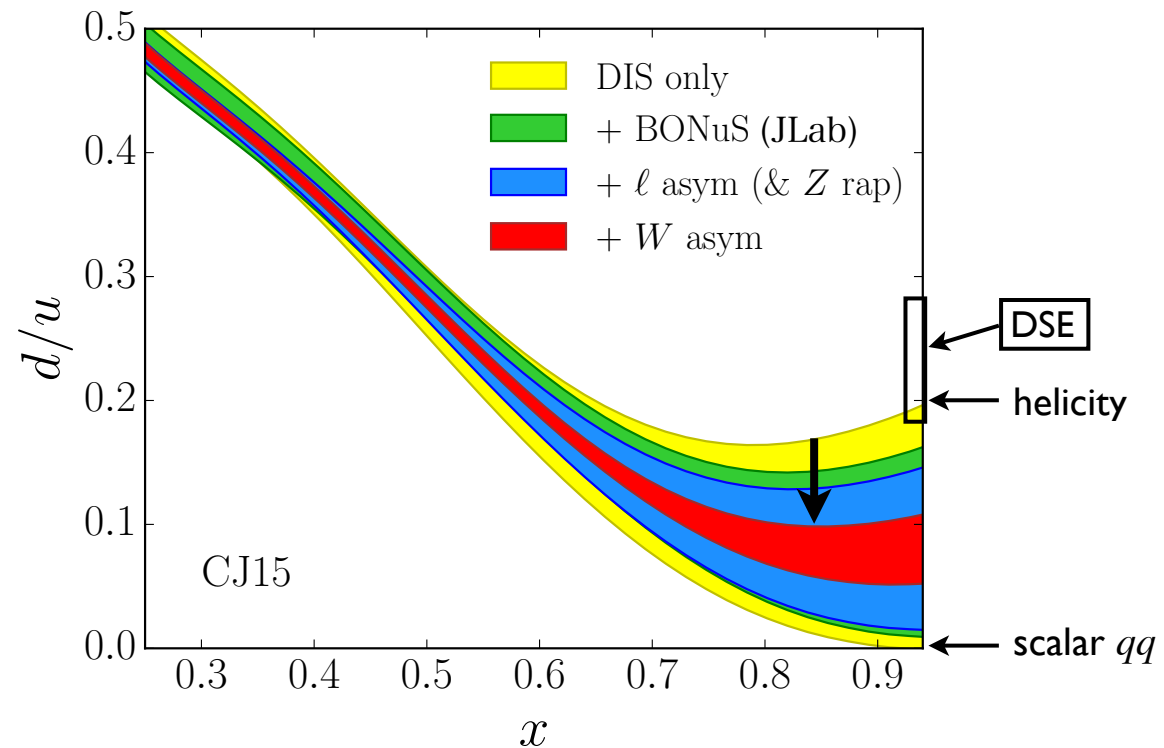
Valence quarks & QCD models

☀ Valence d/u ratio at high x of particular interest

→ significant reduction of PDF errors with new JLab tagged neutron & FNAL W -asymmetry data



Accardi et al. (2016)



→ extrapolated ratio at $x = 1$

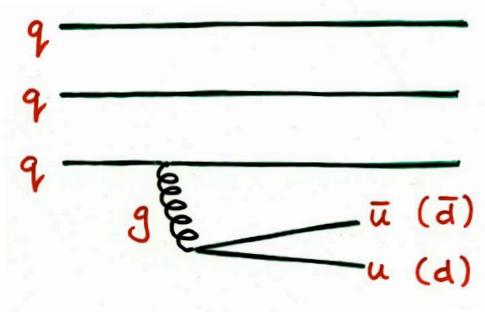
$$d/u \rightarrow 0.09 \pm 0.03$$

does not match any model!

→ upcoming experiments at JLab (MARATHON, BONuS, SoLID) will determine d/u up to $x \sim 0.85$

Light quark sea

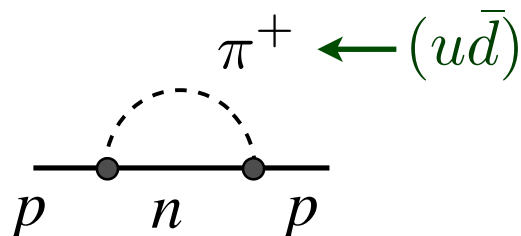
- From perturbative QCD expect symmetric $q\bar{q}$ sea generated by gluon radiation into $q\bar{q}$ pairs (if quark masses are the same)



→ since u and d quarks nearly degenerate, expect flavor-symmetric light-quark sea

$$\bar{d} \approx \bar{u}$$

- In 1984 Thomas made audacious suggestion that chiral symmetry of QCD (important at low energies) should have consequences for antiquark PDFs in the nucleon (at high energies)



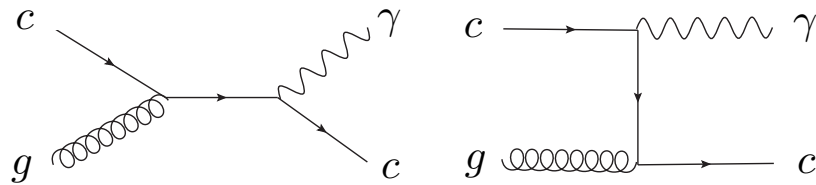
→ $\bar{d} > \bar{u}$

Charm in the nucleon



Associated prompt photon + charm production

$pp \rightarrow \gamma + c + X$ may reveal “intrinsic” charm component



Bednyakov et al. (2014)

→ “smoking gun” would be observation of asymmetric distributions $c(x) \neq \bar{c}(x)$

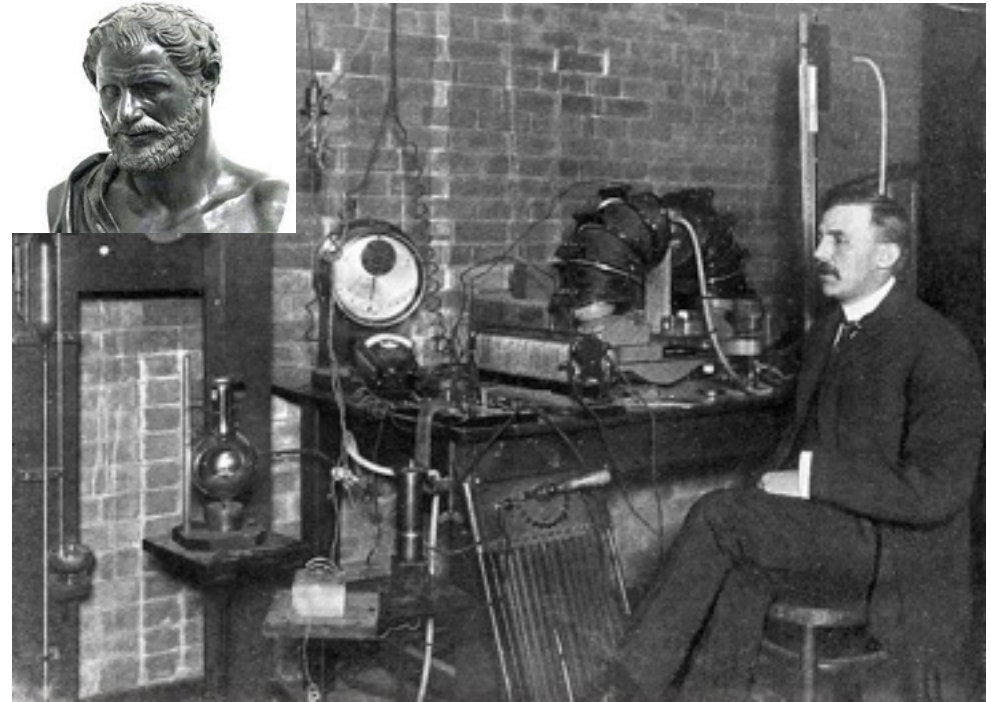
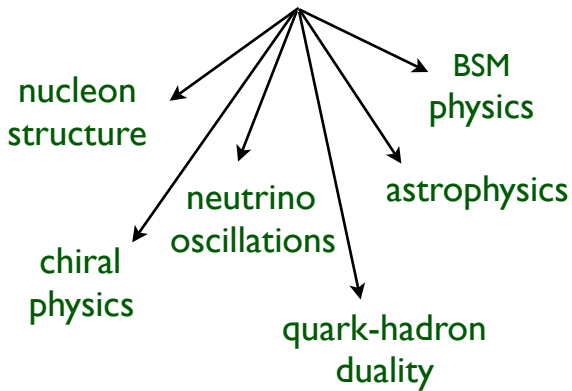
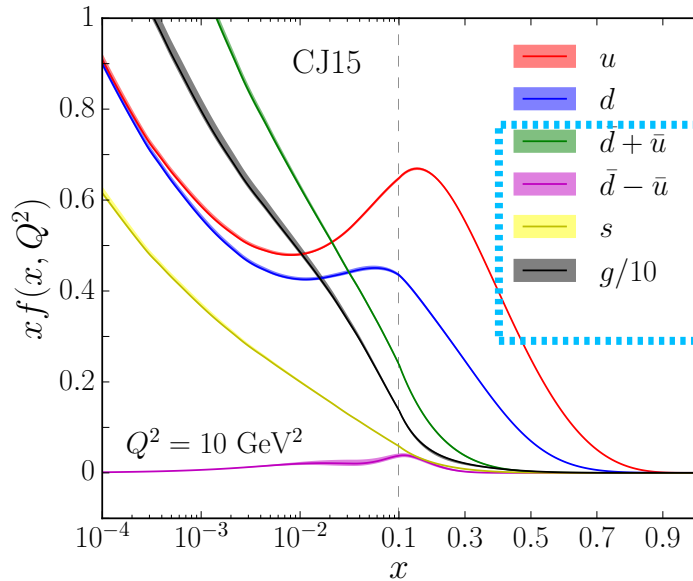


Tim Hobbs talk
Tue. 18:30



Outlook and new directions

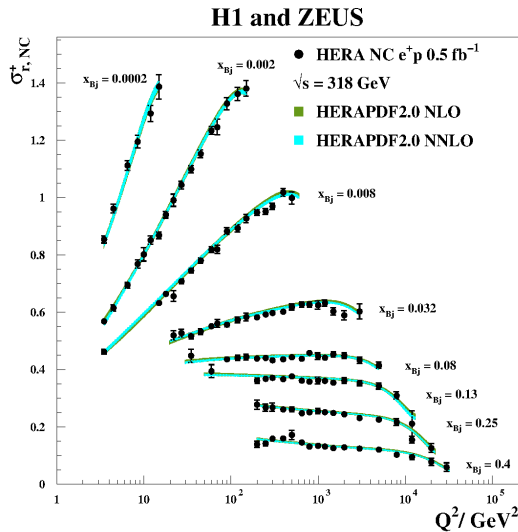
☀ Study of PDFs has brought together essential elements of nuclear and high-energy physics





XII Quark Confinement and the Hadron Spectrum

from 29 August 2016 to 3 September 2016
Europe/Athens timezone



HCHS2016
Thessaloniki, Greece

Stefan Schmitt, DESY
For the HERA collaborations
H1 and ZEUS



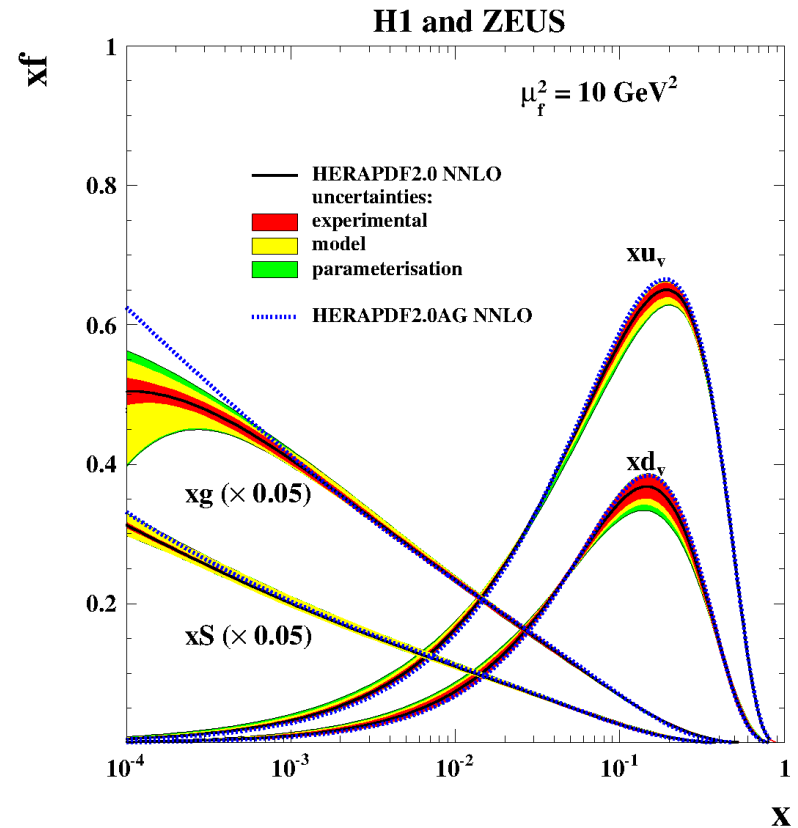


Outline

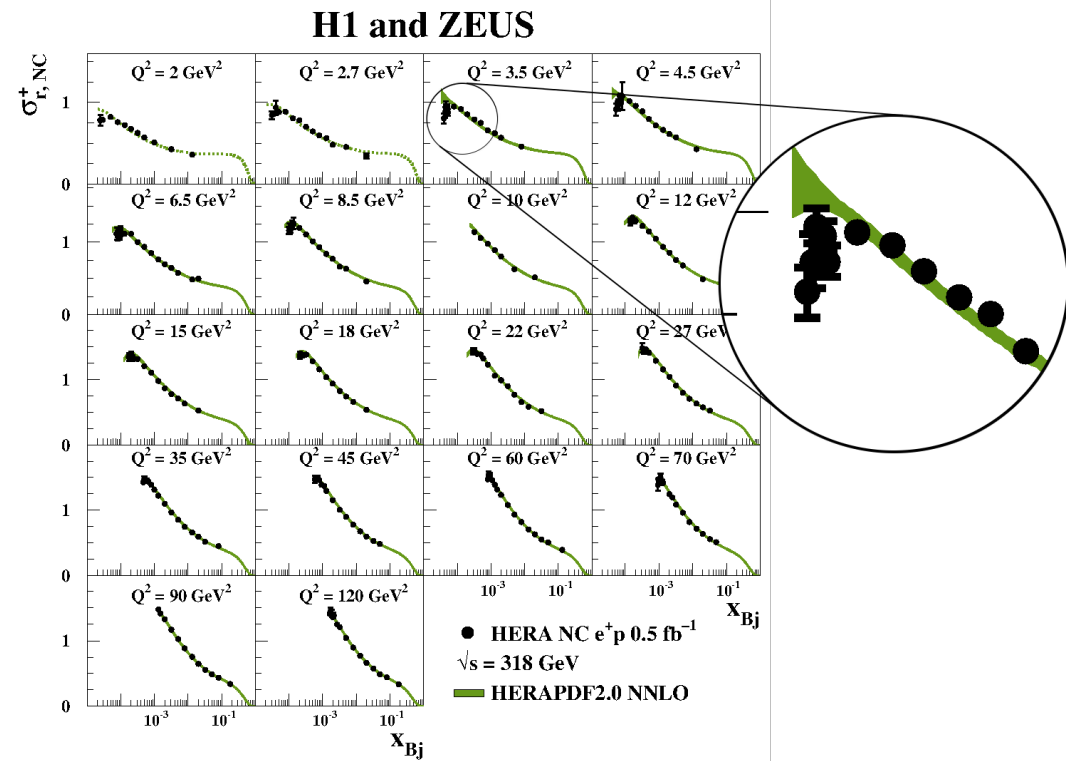


- The HERA collider
- Deep-inelastic scattering
- Data combination
- The combined HERA data
- The HERAPDF2.0 fit
- Jet production and α_s

- HERAPDF2.0 PDFs: family of fits based on HERA data alone, at NLO and NNLO
- All fit variants are available in the LHAPDF library
- Shown here:
 - Default NNLO fit with uncertainty bands: “HERAPDF2.0 NNLO”
 - Variant with non-negative gluon “HERAPDF2.0AG NNLO”



- HERAPDF2.0 PDFs: family of fits based on HERA data alone, at NLO and NNLO
- Overall good description of the data down to low Q^2
- Some deviations in the region of low x at low Q^2



- Recent publication of combined HERA inclusive cross section data: precision better than 1.5% for $Q^2 < 500 \text{ GeV}^2$
- A unique dataset probing the proton structure over more than five orders of magnitude in Q^2 and x
- Parton densities HERPDF2.0 derived from HERA data alone
- Together with DIS jet data, the strong coupling can be measured $\alpha_s(M_z) = 0.1183$
- Aim to reduce scale uncertainties on α_s from DIS jets in the near future using NNLO calculations

XII Quark Confinement & the Hadron Spectrum



X, Y, Z States

Marina Nielsen
Universidade de
São Paulo

Lots of X, Y and Z states observed by BaBar, Belle, BESIII, CDF, CLEOIII, CLEO-c, CMS, D0 and LHCb Collaborations













N. Branbilla et al., arXiv:1404.3723

State	M , MeV	Γ , MeV	J^{PC}	Process (mode)	Experiment ($\# \sigma$)	Year	Status
$X(3872)$	3871.68 ± 0.17	< 1.2	1^{++}	$B \rightarrow K(\pi^+\pi^-J/\psi)$ $p\bar{p} \rightarrow (\pi^+\pi^-J/\psi) \dots$ $pp \rightarrow (\pi^+\pi^-J/\psi) \dots$ $B \rightarrow K(\pi^+\pi^-\pi^0J/\psi)$ $B \rightarrow K(\gamma J/\psi)$ $B \rightarrow K(\gamma\psi(2S))$	Belle [810, 1030] (>10), BaBar [1031] (8.6) CDF [1032, 1033] (11.6), D0 [1034] (5.2) LHCb [1035, 1036] (np) Belle [1037] (4.3), BaBar [1038] (4.0) Belle [1039] (5.5), BaBar [1040] (3.5) LHCb [1041] (>10) BaBar [1040] (3.6), Belle [1039] (0.2) LHCb [1041] (4.4)	2003	Ok
$Z_c(3885)^+$	3883.9 ± 4.5	25 ± 12	1^{+-}	$Y(4260) \rightarrow \pi^-(D\bar{D}^*)^+$	Belle [1042] (6.4), BaBar [1043] (4.9) BES III [1044] (np)	2006	Ok
$Z_c(3900)^+$	3891.2 ± 3.3	40 ± 8	$?^{? -}$	$Y(4260) \rightarrow \pi^-(\pi^+J/\psi)$	BES III [1045] (8), Belle [1046] (5.2) T. Xiao <i>et al.</i> [CLEO data] [1047] (>5)	2013	NC!
$Y(3915)$	3918.4 ± 1.9	20 ± 5	$0/2^{?+}$	$B \rightarrow K(\omega J/\psi)$ $e^+e^- \rightarrow e^+e^-(\omega J/\psi)$	Belle [1088] (8), BaBar [1038, 1089] (19) Belle [1090] (7.7), BaBar [1091] (7.6)	2004	Ok
$\chi_{c2}(2P)$	3927.2 ± 2.6	24 ± 6	2^{++}	$e^+e^- \rightarrow e^+e^-(D\bar{D})$	Belle [1092] (5.3), BaBar [1093] (5.8)	2005	Ok
$X(3940)$	3942_{-8}^{+9}	37_{-17}^{+27}	$?^{?+}$	$e^+e^- \rightarrow J/\psi(D\bar{D}^*)$	Belle [1086, 1087] (6)	2005	NC!
$Y(4008)$	3891 ± 42	255 ± 42	1^{--}	$e^+e^- \rightarrow (\pi^+\pi^-J/\psi)$	Belle [1046, 1094] (7.4)	2007	NC!
$Z_c(4020)^+$	4022.9 ± 2.8	7.9 ± 3.7	$?^{? -}$	$Y(4260, 4360) \rightarrow \pi^-(\pi^+h_c)$	BES III [1048] (8.9)	2013	NC!
$Z_c(4025)^+$	4026.3 ± 4.5	24.8 ± 9.5	$?^{? -}$	$Y(4260) \rightarrow \pi^-(D^*\bar{D}^*)^+$	BES III [1049] (10)	2013	NC!
$\psi(4040)$	4039 ± 1	80 ± 10	1^{--}	$e^+e^- \rightarrow (D^{(*)}\bar{D}^{(*)}(\pi))$ $e^+e^- \rightarrow (\eta J/\psi)$	PDG [1] Belle [1095] (6.0)	1978	Ok
$Z(4050)^+$	4051_{-43}^{+24}	82_{-55}^{+51}	$?^{?+}$	$\bar{B}^0 \rightarrow K^-(\pi^+\chi_{c1})$	Belle [1096] (5.0), BaBar [1097] (1.1)	2008	NC!
$Y(4140)$	4145.8 ± 2.6	18 ± 8	$?^{?+}$	$B^+ \rightarrow K^+(\phi J/\psi)$	CDF [1098] (5.0), Belle [1099] (1.9), LHCb [1100] (1.4), CMS [1101] (>5) D0 [1102] (3.1)	2009	NC!

$\psi(4160)$	4153 ± 3	103 ± 8	1^{--}	$e^+ e^- \rightarrow (D^{(*)} \bar{D}^{(*)})$ $e^+ e^- \rightarrow (\eta J/\psi)$	PDG [1]	1978	Ok
$X(4160)$	4156^{+29}_{-25}	139^{+113}_{-65}	$?^{?+}$	$e^+ e^- \rightarrow J/\psi (D^* \bar{D}^*)$	Belle [1095] (6.5)	2013	NC!
$Z(4200)^+$	4196^{+35}_{-30}	370^{+99}_{-110}	1^{+-}	$\bar{B}^0 \rightarrow K^- (\pi^+ J/\psi)$	Belle [1087] (5.5)	2007	NC!
$Z(4250)^+$	4248^{+185}_{-45}	177^{+321}_{-72}	$?^{?+}$	$\bar{B}^0 \rightarrow K^- (\pi^+ \chi_{c1})$	Belle [1103] (7.2)	2014	NC!
$Y(4260)$	4250 ± 9	108 ± 12	1^{--}	$e^+ e^- \rightarrow (\pi\pi J/\psi)$	Belle [1096] (5.0), BaBar [1097] (2.0)	2008	NC!
				$e^+ e^- \rightarrow (f_0(980)J/\psi)$	BaBar [1104] [1105] (8), CLEO [1106] [1107] (11)	2005	Ok
				$e^+ e^- \rightarrow (\pi^- Z_c(3900)^+)$	Belle [1046] [1094] (15), BES III [1045] (np)		
				$e^+ e^- \rightarrow (\gamma X(3872))$	BaBar [1105] (np), Belle [1046] (np)	2012	Ok
$Y(4274)$	4293 ± 20	35 ± 16	$?^{?+}$	$B^+ \rightarrow K^+ (\phi J/\psi)$	BES III [1045] (8), Belle [1046] (5.2)	2013	Ok
					BES III [1108] (5.3)	2013	NC!
					CDF [1098] (3.1), LHCb [1100] (1.0), CMS [1101] (>3), D0 [1102] (np)	2011	NC!
$X(4350)$	$4350.6^{+4.6}_{-5.1}$	13^{+18}_{-10}	$0/2^{?+}$	$e^+ e^- \rightarrow e^+ e^- (\phi J/\psi)$	Belle [1109] (3.2)	2009	NC!
$Y(4360)$	4354 ± 11	78 ± 16	1^{--}	$e^+ e^- \rightarrow (\pi^+ \pi^- \psi(2S))$	Belle [1110] (8), BaBar [1111] (np)	2007	Ok
$Z(4430)^+$	4458 ± 15	166^{+37}_{-32}	1^{+-}	$\bar{B}^0 \rightarrow K^- (\pi^+ \psi(2S))$	Belle [1112] [1113] (6.4), BaBar [1114] (2.4)	2007	Ok
					LHCb [1115] (13.9)		
				$\bar{B}^0 \rightarrow K^- (\pi^+ J/\psi)$	Belle [1103] (4.0)	2014	NC!
$X(4630)$	4634^{+9}_{-11}	92^{+41}_{-32}	1^{--}	$e^+ e^- \rightarrow (\Lambda_c^+ \bar{\Lambda}_c^-)$	Belle [1116] (8.2)	2007	NC!
$Y(4660)$	4665 ± 10	53 ± 14	1^{--}	$e^+ e^- \rightarrow (\pi^+ \pi^- \psi(2S))$	Belle [1110] (5.8), BaBar [1111] (5)	2007	Ok

in 2014: 23 new states, many not confirmed
many candidates for exotic states

up to now: 9 reported charged states
which are not quark-antiquark states

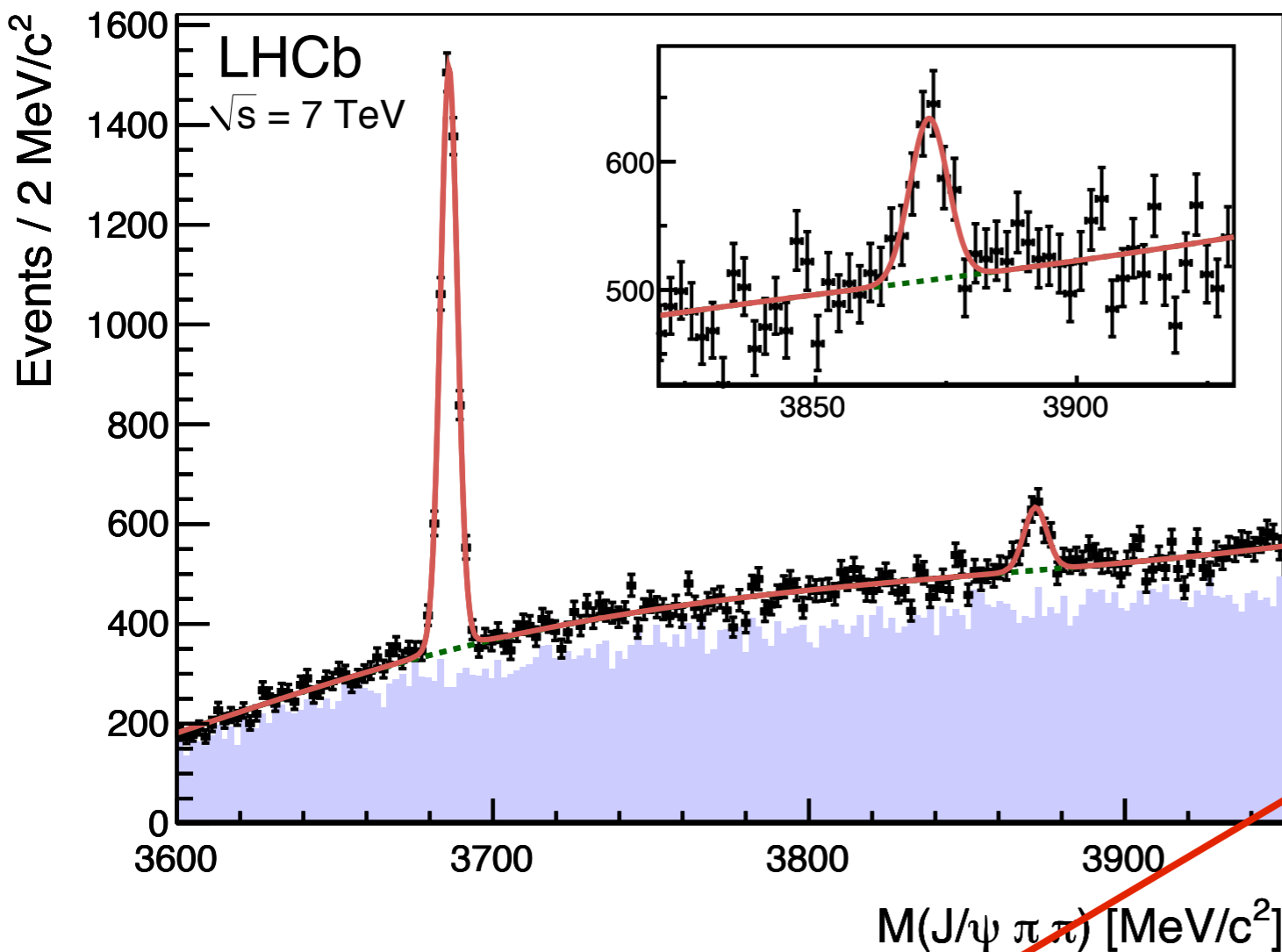
 <p>$Z^+(4430)$ 2007</p>  	 <p>$Z_1^+(4050)$ 2008</p> 	 <p>$Z_2^+(4250)$ 2008</p> 
<p>BES III</p> <p>$Z_c^+(3900)$ 2013</p> 	<p>$Z_c^+(4025)$ 2013</p> <p>BES III</p>	<p>$Z_c^+(4020)$ 2013</p> <p>BES III</p>
<p>$Z_c^+(3885)$ 2013</p> <p>BES III</p>	<p>$Z_c^+(4200)$ 2014</p> 	<div style="border: 2px dashed orange; padding: 5px;">  <p>$X^+(5568)$ 2016</p>   </div>

not a charmonium state

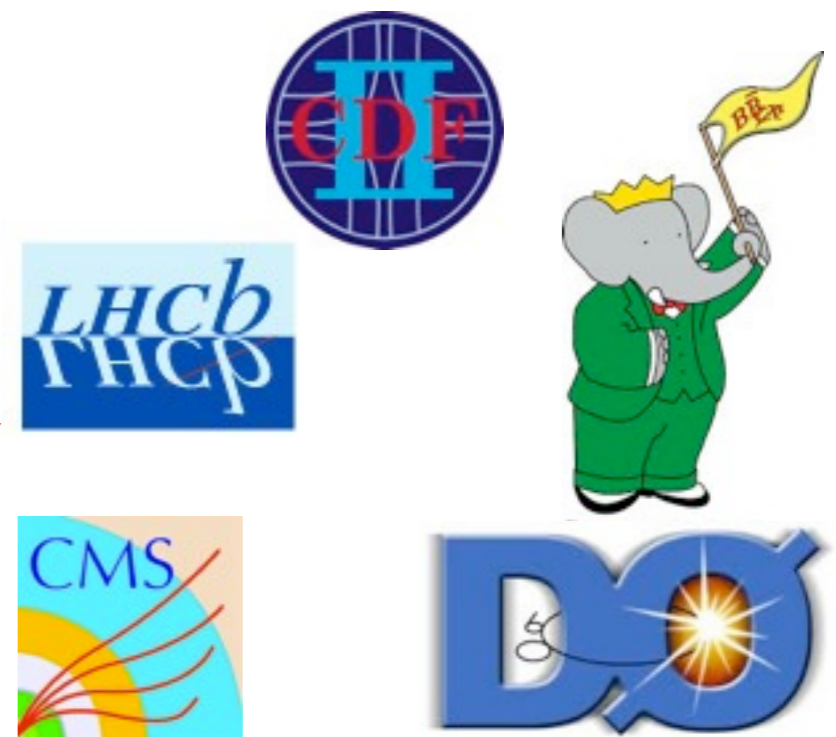
X(3872) @ KEK (PRL91(2003))

very narrow state observed in the decay: $B^\pm \rightarrow K^\pm (J/\psi \pi^+ \pi^-)$

best studied charmonium exotic candidate



$M_X = (3872.20 \pm 0.39) \text{ MeV}$
 $\Gamma < 2.3 \text{ MeV}$



$c\bar{c}$ spec. for $J^{PC} = 1^{++}$ (Barnes & Godfrey, PRD69 (2004))

- $2^3 P_1$ (3990)
- $3^3 P_1$ (4290)

$$\frac{X \rightarrow J/\psi \pi^+ \pi^- \pi^0}{X \rightarrow J/\psi \pi^+ \pi^-} = 0.8 \pm 0.3 \Rightarrow \text{strong isospin and G parity violation}$$

$$M(D^{*0} \bar{D}^0) = (3871 \pm 1)$$

X(3872): molecular $(D^{*0} \bar{D}^0 + \bar{D}^{*0} D^0)$ state (Swanson, Close, Voloshin, Wong ...)

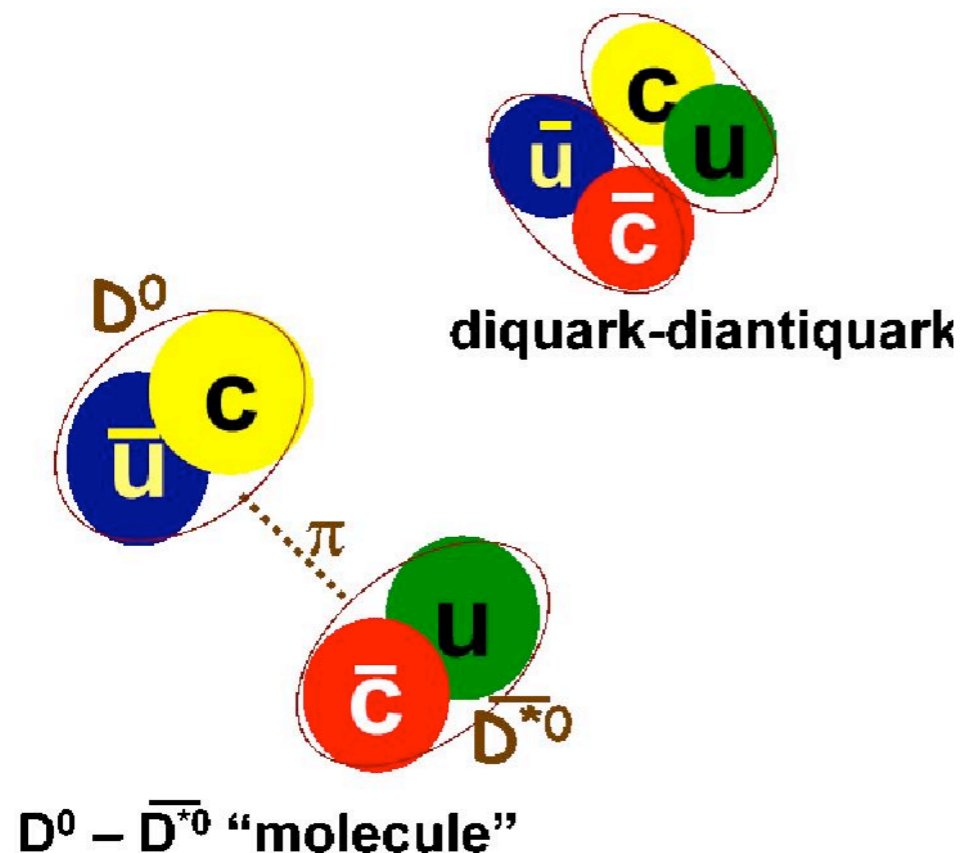
Maiani et al. (PRD71 (05)) tetraquark $J^{PC} = 1^{++}$ state

$$\frac{X \rightarrow J/\psi \pi^+ \pi^- \pi^0}{X \rightarrow J/\psi \pi^+ \pi^-} = 0.8 \pm 0.3 \rightarrow \text{strong isospin and G parity violation}$$

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Maiani et al. (PRD71 (05)) tetraquark $J^{PC} = 1^{++}$ state



molecular and tetraquark interpretations differ by the way quarks are organized in the state

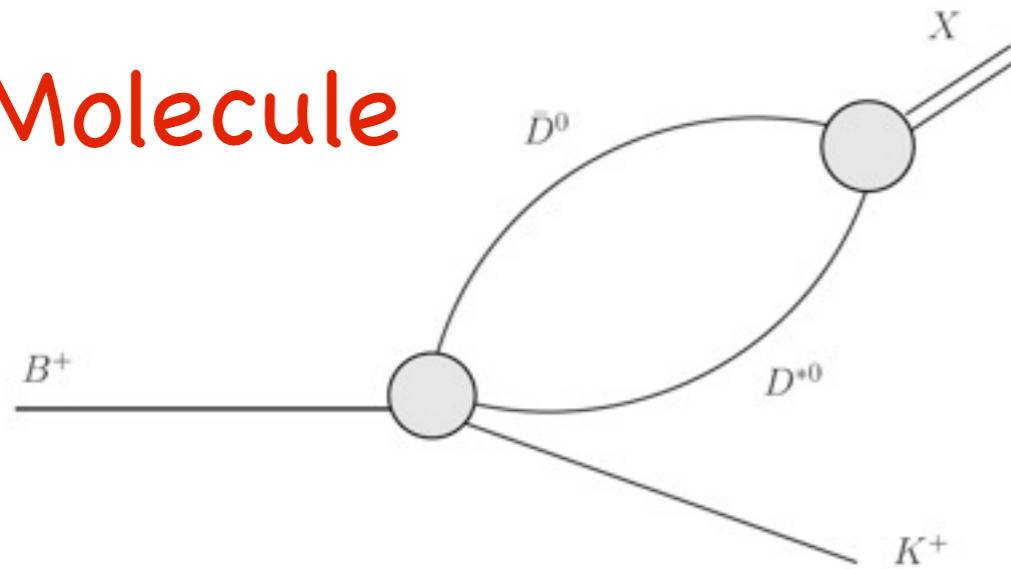
X(3872) production

B decays at B factories



$$B^{\pm} \rightarrow X(3872)K^{\pm}$$

Meson Molecule



Meson coalescence

Small binding energy

Agreement with data !

E. Braaten, M. Kusunoki, hep-ph/0404161

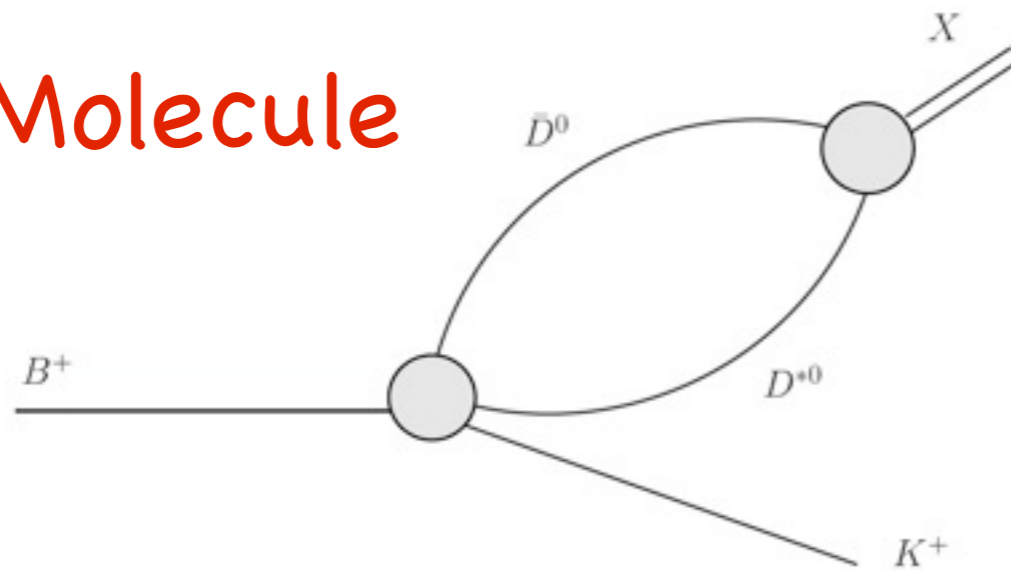
X(3872) production

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$$B^\pm \rightarrow X(3872)K^\pm$$

Meson Molecule



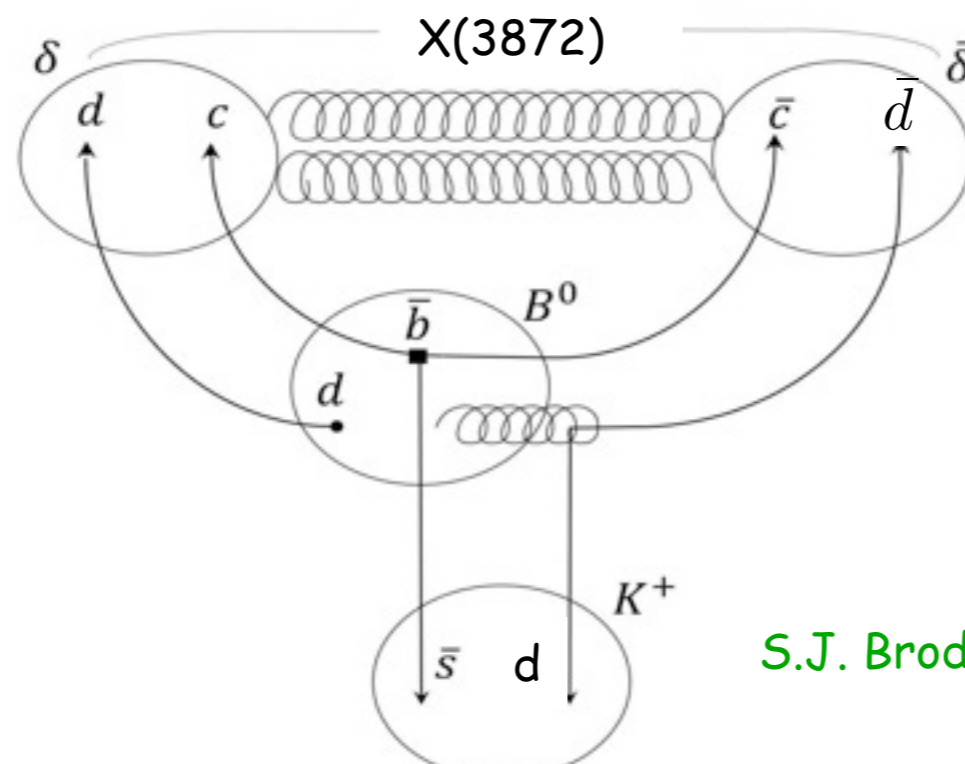
Meson coalescence

Small binding energy

Agreement with data !

E. Braaten, M. Kusunoki, hep-ph/0404161

Tetraquark



Diquark-antidiquark picture

Non-relativistic potential

Agreement with data !

S.J. Brodsky, D.S. Hwang, R.F. Lebed, arXiv:1406.7281

Conclusions

$X(3872) \rightarrow$ mixture χ_{c1} and a $D^*\bar{D}$ molecule

$Z_c^+(3900) \rightarrow J^P=1^+$ tetraquark state

$Z_c^+(3900)$ and $Z_c^+(3885) \rightarrow$ not the same state

$Z_c^+(4025) \rightarrow J^P=1^+,2^+ D^*\bar{D}^*$ resonance, or D-wave background

- Z^+ states need confirmation. A bump in the spectra near the threshold does not indicate, necessarily, the existence of a state

$X^+(5568) \rightarrow$ needs confirmation, probably not a real state

Questions?



Emergent phenomena and partonic structure in hadrons

Craig Roberts, Physics Division

Collaborators: 2013-Present

Students, Postdocs, Profs.

1. *S. HERNÁNDEZ (U Michoacán) ;*
2. *Jing CHEN (Peking U.)*
3. *Bo-Lin LI (Nanjing U.)*
4. *Ya LU (Nanjing U.)*
5. *Khépani RAYA (U Michoacán);*
6. *Chien-Yeah SENG (UM-Amherst) ;*
7. *Kun-lun WANG (PKU);*
8. *Chen CHEN (UNESP, São Paulo);*
9. *Zhu-Fang CUI (Nanjing U.) ;*
10. *J. Javier COBOS-MARTINEZ (U Michoacán);*
11. *Minghui DING (Nankai U.) ;*
12. *Fei GAO (Peking U.) ;*
13. *L. Xiomara Gutiérrez-Guerrero (Sonora U.);*
14. *Cédric MEZRAG (ANL, Irfu Saclay) ;*
15. *Mario PITSCHMANN (Vienna);*
16. *Si-xue QIN (ANL, U. Frankfurt am Main, PKU);*
17. *Eduardo ROJAS (Antioquia U.)*
18. *Jorge SEGOVIA (TU-Munich, ANL);*
19. *Chao SHI (ANL, Nanjing U.)*
20. *Shu-Sheng XU (Nanjing U.)*
21. *Adnan Bashir (U Michoacán);*
22. *Daniele Binosi (ECT*)*
23. *Stan Brodsky (SLAC);*
24. *Lei Chang (Nankai U.) ;*
25. *Ian Cloët (ANL) ;*
26. *Bruno El-Bennich (São Paulo);*
27. *Roy Holt (ANL);*
28. *Tanja Horn (Catholic U. America)*
29. *Yu-xin Liu (PKU);*
30. *Hervé Moutarde (CEA, Saclay) ;*
31. *Joannis Papavassiliou (U.Valencia)*
32. *M. Ali Paracha (NUST, Islamabad)*
33. *Alfredo Raya (U Michoacán);*
34. *Jose Rodriguez Qintero (U. Huelva) ;*
35. *Franck Sabatié (CEA, Saclay);*
36. *Sebastian Schmidt (IAS-FZJ & JARA);*
37. *Peter Tandy (KSU);*
38. *Tony Thomas (U.Adelaide) ;*
39. *Shaolong WAN (USTC) ;*
40. *Hong-Shi ZONG (Nanjing U)*

Epilogue

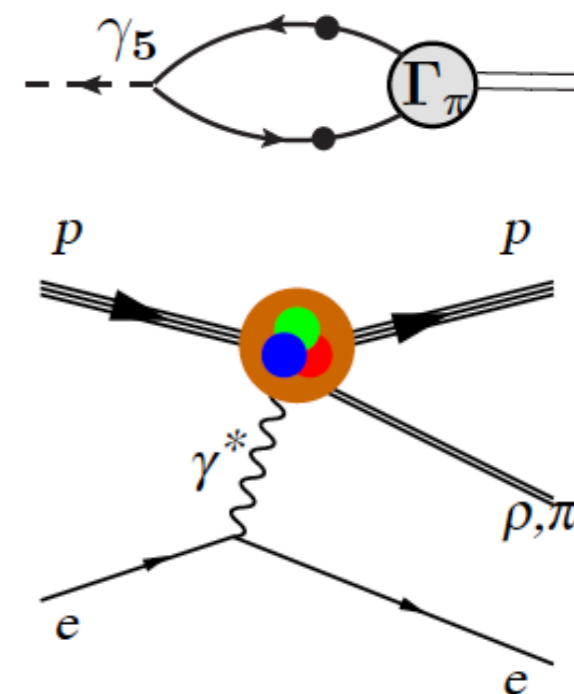
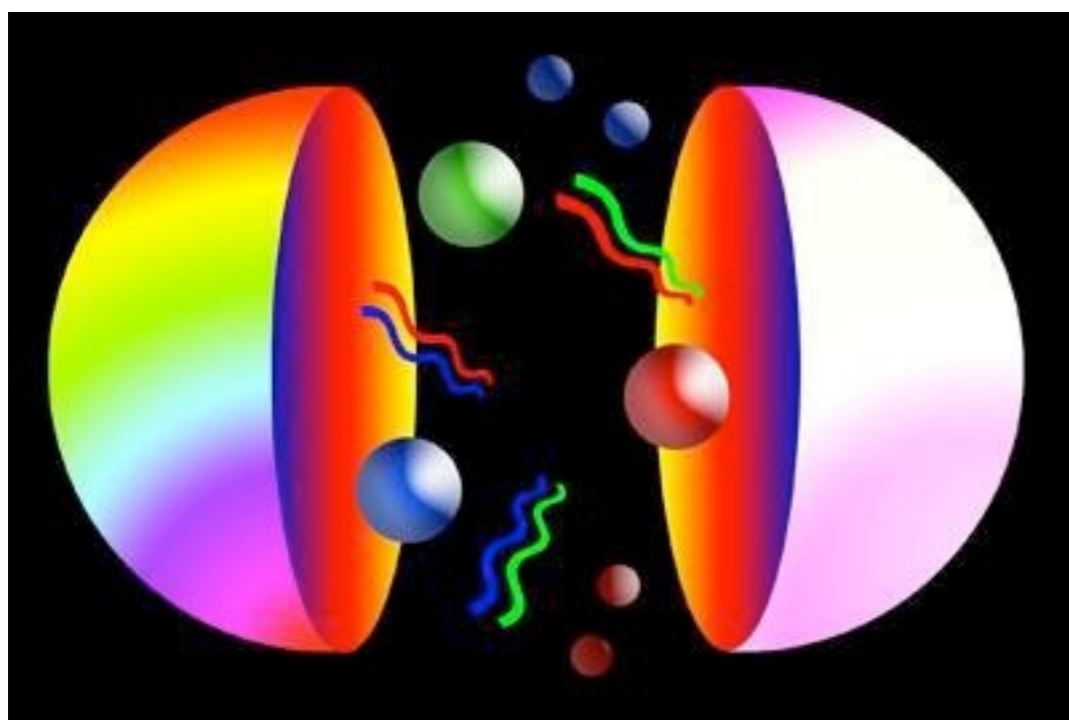
- Conformal anomaly ... *gluons and quarks acquire momentum-dependent masses* ... values are large in the infrared $m_g \propto 500$ MeV & $M_q \propto 350$ MeV ... underlies DCSB; and has numerous observable consequences
- Universe with light quarks \Rightarrow confinement is a dynamical phenomenon
Confinement and DCSB are intimately linked in real-QCD
- Origin and distribution of mass depend on the observer's preferred frame of reference and scale ... Contemporary and planned experiments, DCSB paradigm is the best way to explicate and understand the associated, emerging phenomena. Numerous verifiable predictions accessible
 - form factors, PDAs and PDFs, GPDs and TMDs, etc.
- What can experiments at an EIC add to this?
 - Valence-quark region will be accessible
 - However, focus is on low- x , where gluons dominate ... mass generation in the gluon sector ... must affect potential for gluon saturation; how?
- Ability to compute valence-quark PDAs and PDFs has provided many new insights ... must now begin to do the same for sea-quarks and glue

Pion and Kaon Properties from Dyson-Schwinger Eons



Peter C. Tandy

Dept of Physics
Kent State University USA



Topics

- DSE continuum approach to QCD
- Old work on pion and kaon properties and decays
- Parton distribution amplitudes and PDFs—mainly mesons as an example. DSE-model calculations with direct connection to QCD. Comparison to LQCD.
- Some applications to uv physics (Form Factors, HS behavior)
- PDFs including X. Ji's space-like correlator approximation for LQCD—a model investigation.



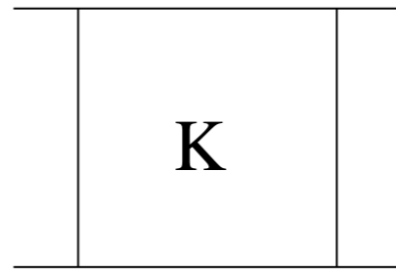
DSE Modeling of Hadron Physics

- Most common: Rainbow-ladder truncation of QCD's eqns of motion. Approximation to full BSE kernel now starting to produce results.....
- **Constrain modeling by preserving AV-Ward-Takahashi Id, V-WTI. [Color singlet] Naturally implements DCSB, conserved vector current, Goldstone Thm, PCAC...**
- RL truncation only good for ground state vector & pseudoscalar mesons, q-qq descriptions of baryons with AV and S diquarks.
- At the very least: DSE continuum QCD modeling suited for surveying the landscape quickly from large to small scales; finding out which underlying mechanisms are dominant. Applicable to all scales, high Q^2 form factors, etc. Do not expect ab initio final-precision QCD results, except in special cases. **[pion, kaon..]**
- Unifying DSE treatment of light front quantities (PDFs, GPDs, DA) with other aspects of hadron structure: masses, decays, charge form factors, transition form factors.....
- Pion & kaon q-qbar Bethe-Salpeter wavefn is very well known

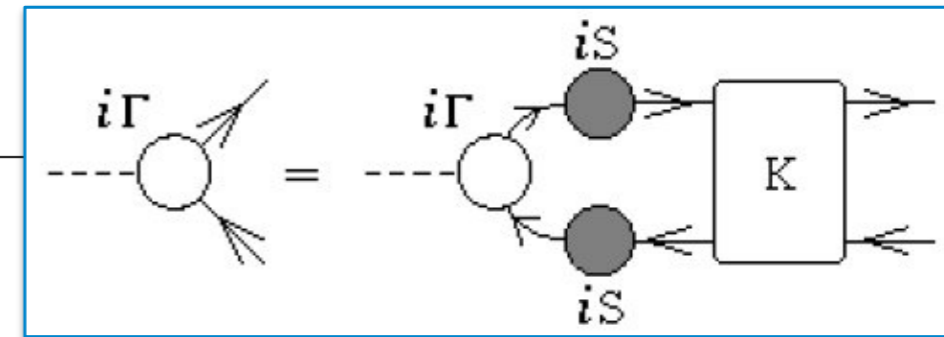
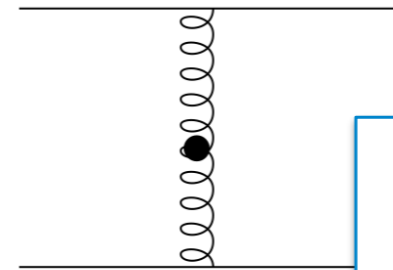
$$\text{AV - WTI : } m_q \rightarrow 0, P \rightarrow 0 \Rightarrow \Gamma_{\pi q\bar{q}}(k^2) = i\gamma_5 \frac{\frac{1}{4}\text{tr}S_0^{-1}(k)}{f_\pi} + \mathcal{O}(P)$$

Ladder-Rainbow Model

Landau gauge only



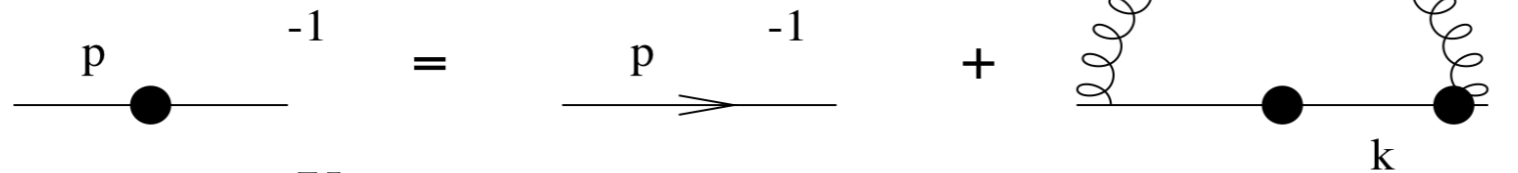
→



- $K_{\text{BSE}} \rightarrow -\gamma_\mu \frac{\lambda^a}{2} 4\pi\alpha_{\text{eff}}(q^2) D_{\mu\nu}^{\text{free}}(q) \gamma_\nu \frac{\lambda^a}{2}$

- $\alpha_{\text{eff}}(q^2) \xrightarrow{IR} \langle \bar{q}q \rangle_{\mu=1} \text{ GeV} = -(240\text{MeV})^3$, incl vertex dressing

- $\alpha_{\text{eff}}(q^2) \xrightarrow{UV} \alpha_s^{1-\text{loop}}(q^2)$



modern π, K qDSE-BSE strategy: Maris & Roberts, PRC56, 3369 (1997)

- P. Maris & P.C. Tandy, PRC60, 055214 (1999)

M_ρ, M_ϕ, M_{K^*} good to 5%, f_ρ, f_ϕ, f_{K^*} good to 10% [fit : m_π, m_K, f_π], f_K (2%)

An Ansatz for the FULL QCD kernel:
L. Chang, C.D. Roberts, PRL103,
081601 (2009), + S. Qin (2015).

A more modern RL kernel: S. Qin, L.
Chang, C.D. Roberts, D.J. Wilson, PRC84,
042202 (2011).

Summary of light meson results

$m_{u=d} = 5.5 \text{ MeV}$, $m_s = 125 \text{ MeV}$ at $\mu = 1 \text{ GeV}$

Pseudoscalar (PM, Roberts, PRC56, 3369)

	expt.	calc.
$-\langle qq \rangle_\mu^0$	$(0.236 \text{ GeV})^3$	$(0.241^\dagger)^3$
m_π	0.1385 GeV	0.138^\dagger
f_π	0.0924 GeV	0.093^\dagger
m_K	0.496 GeV	0.497^\dagger
f_K	0.113 GeV	0.109

Charge radii (PM, Tandy, PRC62, 055204)

r_π^2	0.44 fm ²	0.45
$r_{K^+}^2$	0.34 fm ²	0.38
$r_{K^0}^2$	-0.054 fm ²	-0.086

$\gamma\pi\gamma$ transition (PM, Tandy, PRC65, 045211)

$g_{\pi\gamma\gamma}$	0.50	0.50
$r_{\pi\gamma\gamma}^2$	0.42 fm ²	0.41

Weak K_{l3} decay (PM, Ji, PRD64, 014032)

$\lambda_+(e3)$	0.028	0.027
$\Gamma(K_{e3})$	$7.6 \cdot 10^6 \text{ s}^{-1}$	7.38
$\Gamma(K_{\mu3})$	$5.2 \cdot 10^6 \text{ s}^{-1}$	4.90

Vector mesons (PM, Tandy, PRC60, 055214)

$m_{\rho/\omega}$	0.770 GeV	0.742
$f_{\rho/\omega}$	0.216 GeV	0.207
m_{K^*}	0.892 GeV	0.936
f_{K^*}	0.225 GeV	0.241
m_ϕ	1.020 GeV	1.072
f_ϕ	0.236 GeV	0.259

Strong decay (Jarecke, PM, Tandy, PRC67, 035202)

$g_{\rho\pi\pi}$	6.02	5.4
$g_{\phi KK}$	4.64	4.3
$g_{K^* K\pi}$	4.60	4.1

Radiative decay (PM, nucl-th/0112022)

$g_{\rho\pi\gamma}/m_\rho$	0.74	0.69
$g_{\omega\pi\gamma}/m_\omega$	2.31	2.07
$(g_{K^* K\gamma}/m_{K^*})^+$	0.83	0.99
$(g_{K^* K\gamma}/m_{K^*})^0$	1.28	1.19

Scattering length (PM, Cotanch, PRD66, 116010)

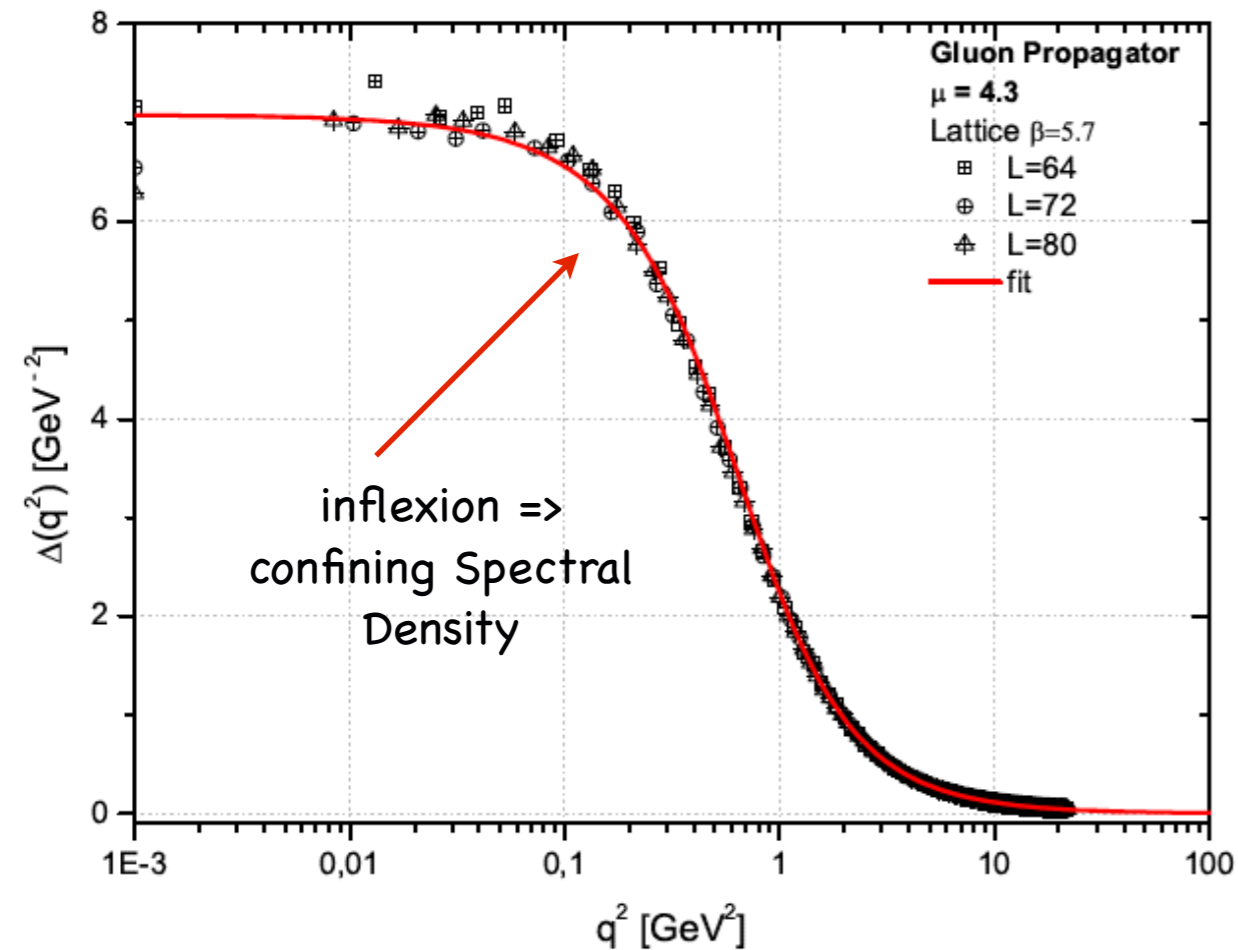
a_0^0	0.220	0.170
a_0^2	0.044	0.045
a_1^1	0.038	0.036



Modern Context for DSE Interaction Kernel

Landau gauge, lattice – QCD gluon propagator,
I.L.Bogolubisky *etal.*, PosLAT2007, 290 (2007)

$$\Rightarrow m_G(k^2) \quad m_G(0) \sim 0.38 \text{ GeV}$$



Bridging a gap between continuum-QCD and ab initio predictions of hadron observables

Daniele Binosi (ECT, Trento & Fond. Bruno Kessler, Trento), Lei Chang (Adelaide U., Sch. Chem. Phys.), Joannis Papavassiliou (Valencia U. & Valencia U., IFIC), Craig D. Roberts (Argonne, PHY). Dec 15, 2014. 6 pp. Published in *Phys.Lett.* B742 (2015) 183-188

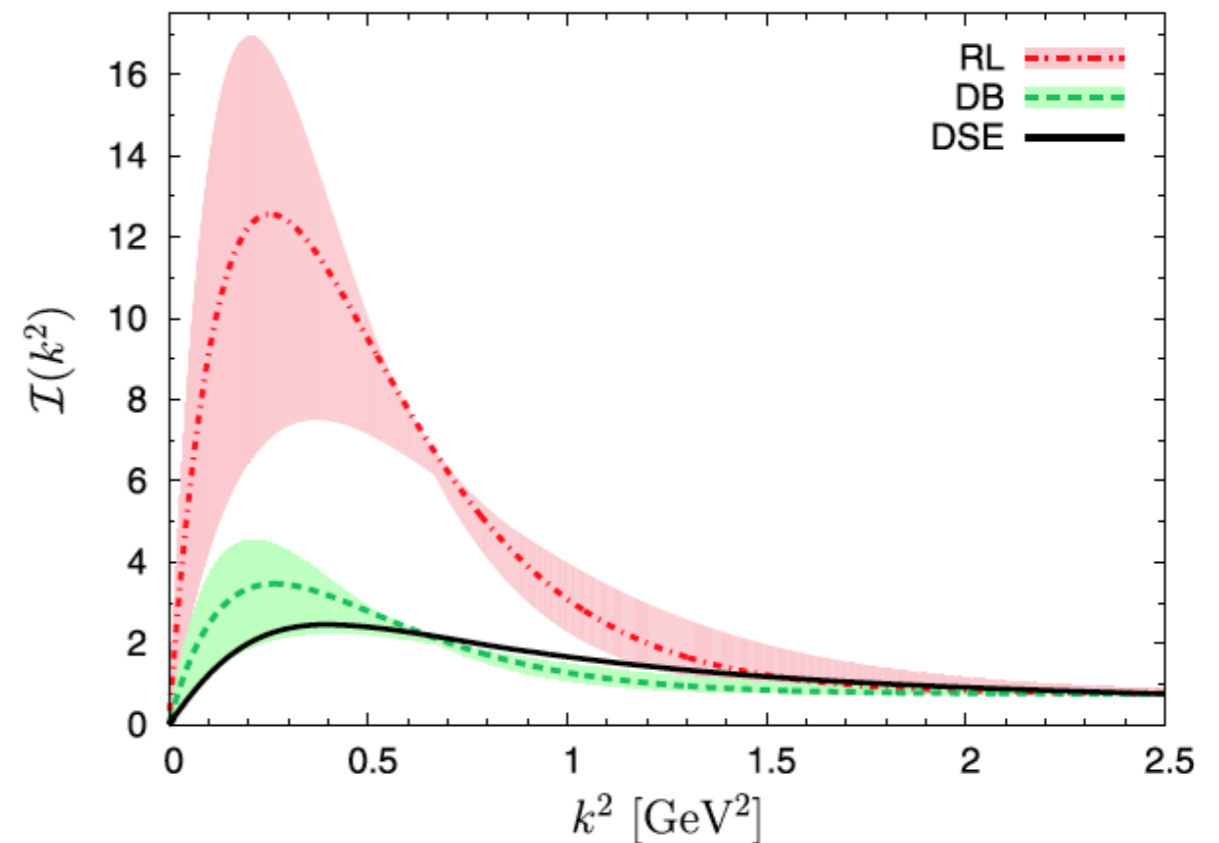


Table 1

Row 1 – Computed values determined from the interaction tension in Eq. (23), quoted in GeV; and Row 2 – the difference: $\varepsilon_\zeta := \zeta_I / \zeta_{I_d} - 1$. So as to represent the domain of constant ground-state physics, described in connection with Eq. (5), we list values obtained with bottom-up interactions using $\omega = 0.5, 0.6$ GeV.

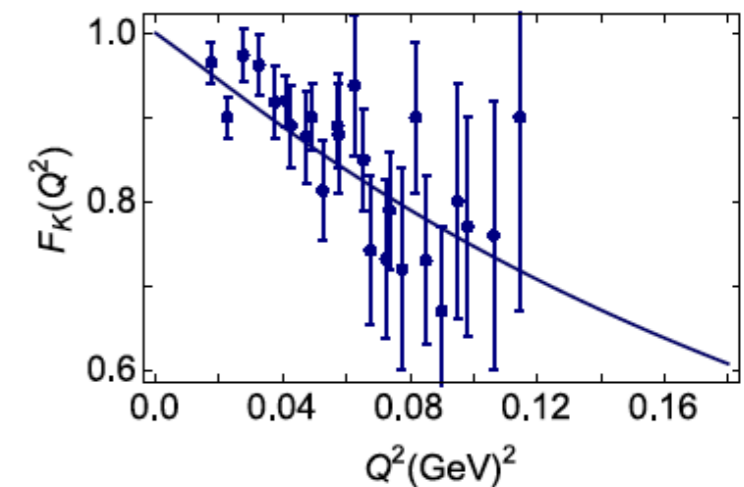
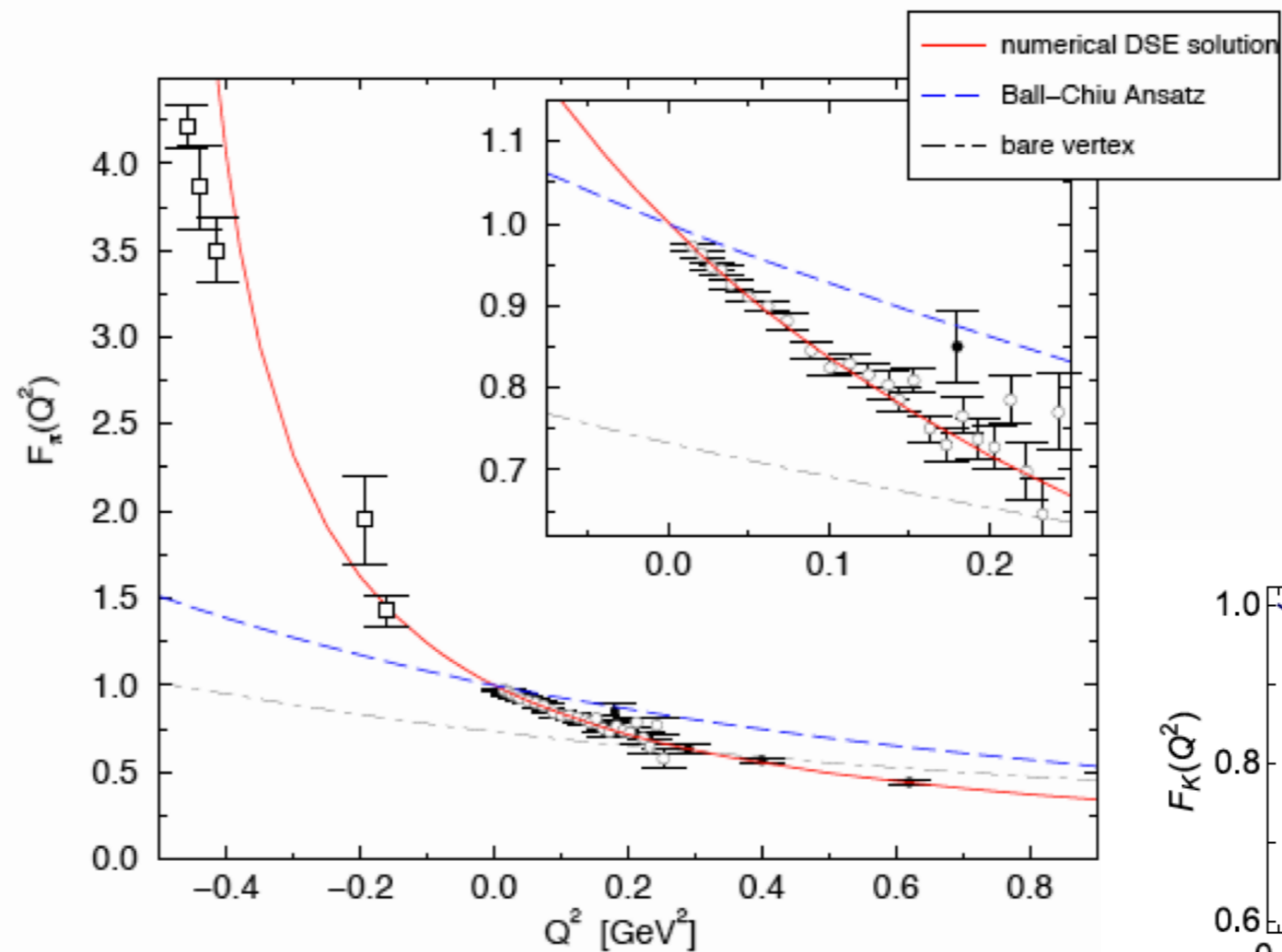
\mathcal{I}	\mathcal{I}_d	$\mathcal{I}_{DB}^{\omega=0.5}$	$\mathcal{I}_{DB}^{\omega=0.6}$	$\mathcal{I}_{RL}^{\omega=0.5}$	$\mathcal{I}_{RL}^{\omega=0.6}$
ζ_I	1.86	1.91	1.82	3.14	2.90
ε_ζ	0	2.8%	-2.4%	68.5%	55.8%

Pion $F(Q^2)$: Low Q^2

(P Maris & PCT, PRC 61, 045202 (2000))

(P. Maris & PCT, PRC 62, 0555204 (2000))

$$r_{\pi}^{\text{DSE}} = 0.68 \text{ fm} \quad r_{\pi}^{\text{expt}} = 0.663 \pm .006 \text{ fm}$$



$$\Gamma_{\pi} = \sqrt{1 - \alpha^2} \Gamma_{q\bar{q}}^{\text{RL}} + \alpha \Gamma_{\pi q\bar{q}}$$

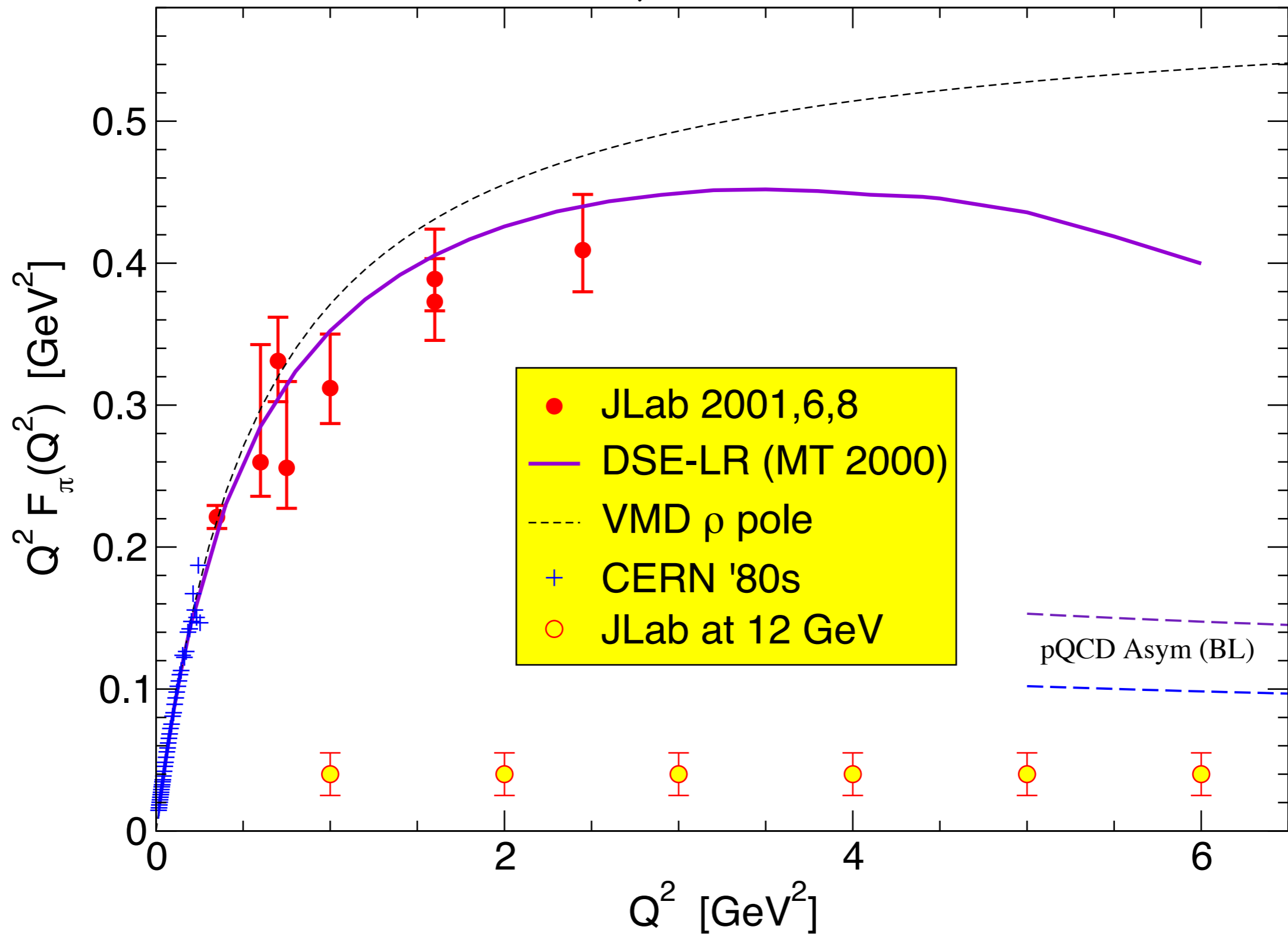
CPT: 18% effect

$$r_{\text{ch}}^2 = (1 - \alpha^2) r_{\text{RL}}^2 + \alpha^2 r_{\pi\text{-lp}}^2$$

DSE-RL: $r_{\text{RL}}^2 = r_{\text{ch}}^2 \Rightarrow \alpha^2 = 18\%$

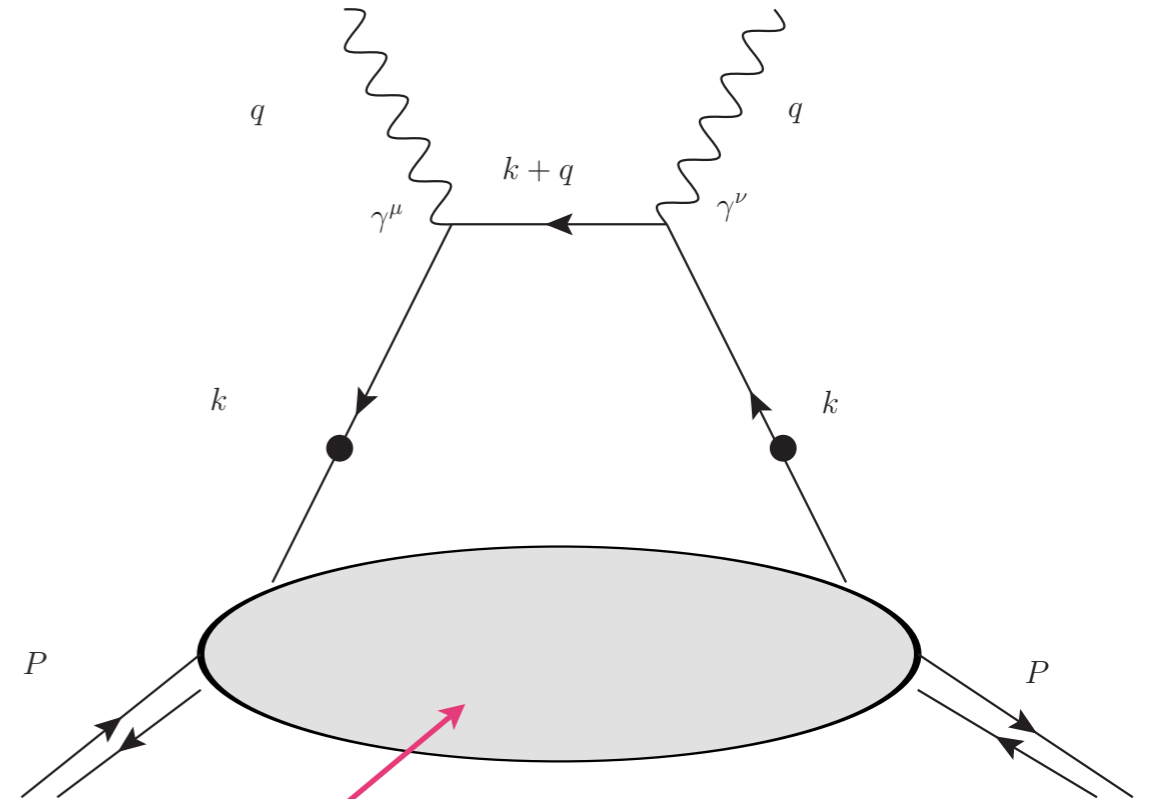


P. Maris and P.C. Tandy, PRC62, 055204, (2000)



Jab data: G. Huber et al., PRC78, 045203 (2008)

Parton Distribution Functions

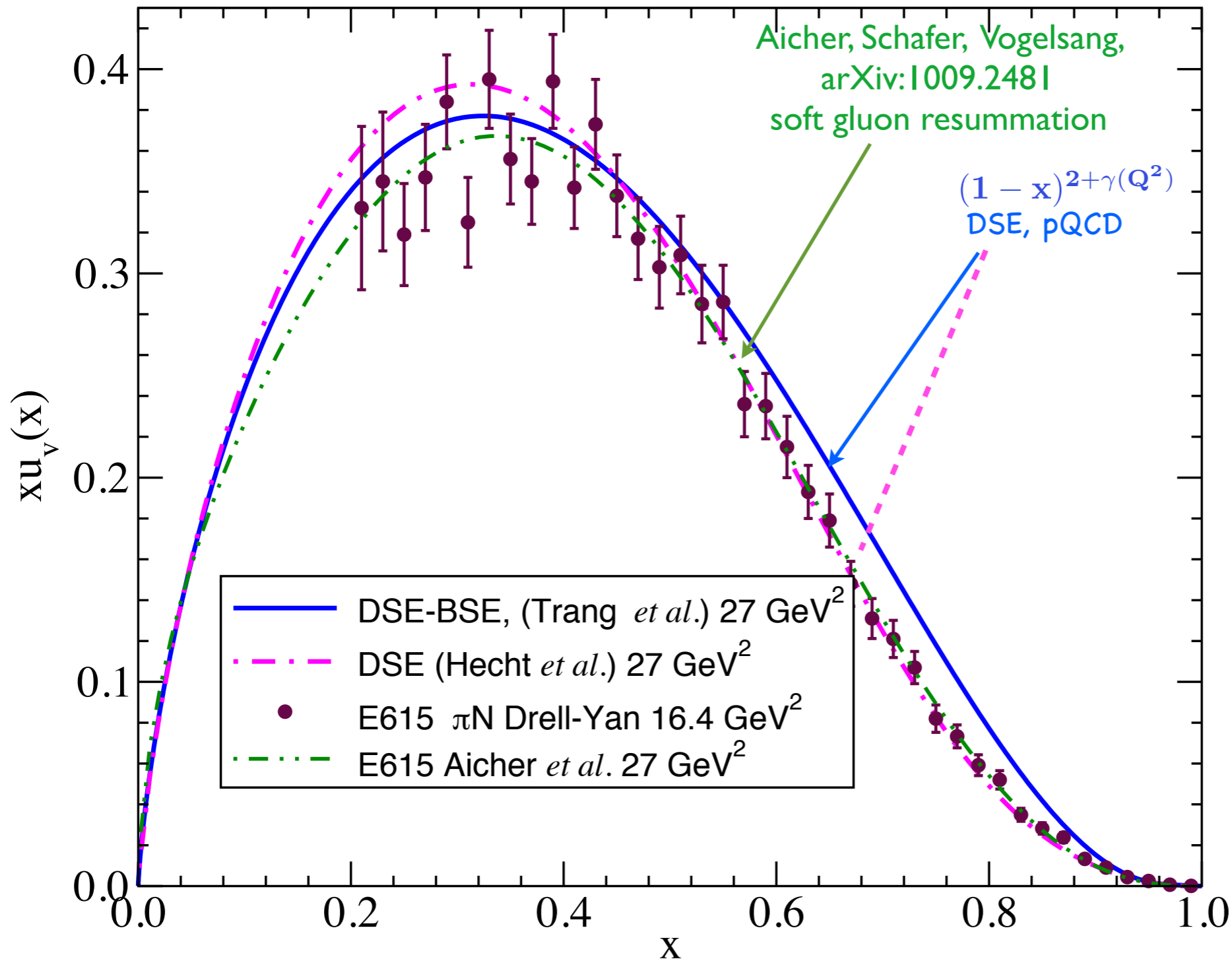


Covariant formulation
and calculation

$$\int d^4q \, F(q^2, q \cdot P, q \cdot k, k^2)$$

Pion Valence PDF

Nguyen, Bashir, Roberts, PCT, PRC 83 062201 (2011); arXiv:1102.2448



q_0
 prev PDF expt parm
 $(1-x)^{1.5}$
 CQM, duality.. $(1-x)^1$
 NJL (pt π) : $(1-x)^0$

One Lattice-QCD Moment Almost Determines Pion DA

PRL 111, 092001 (2013)

PHYSICAL REVIEW LETTERS

week ending
30 AUGUST 2013

Pion Distribution Amplitude from Lattice QCD

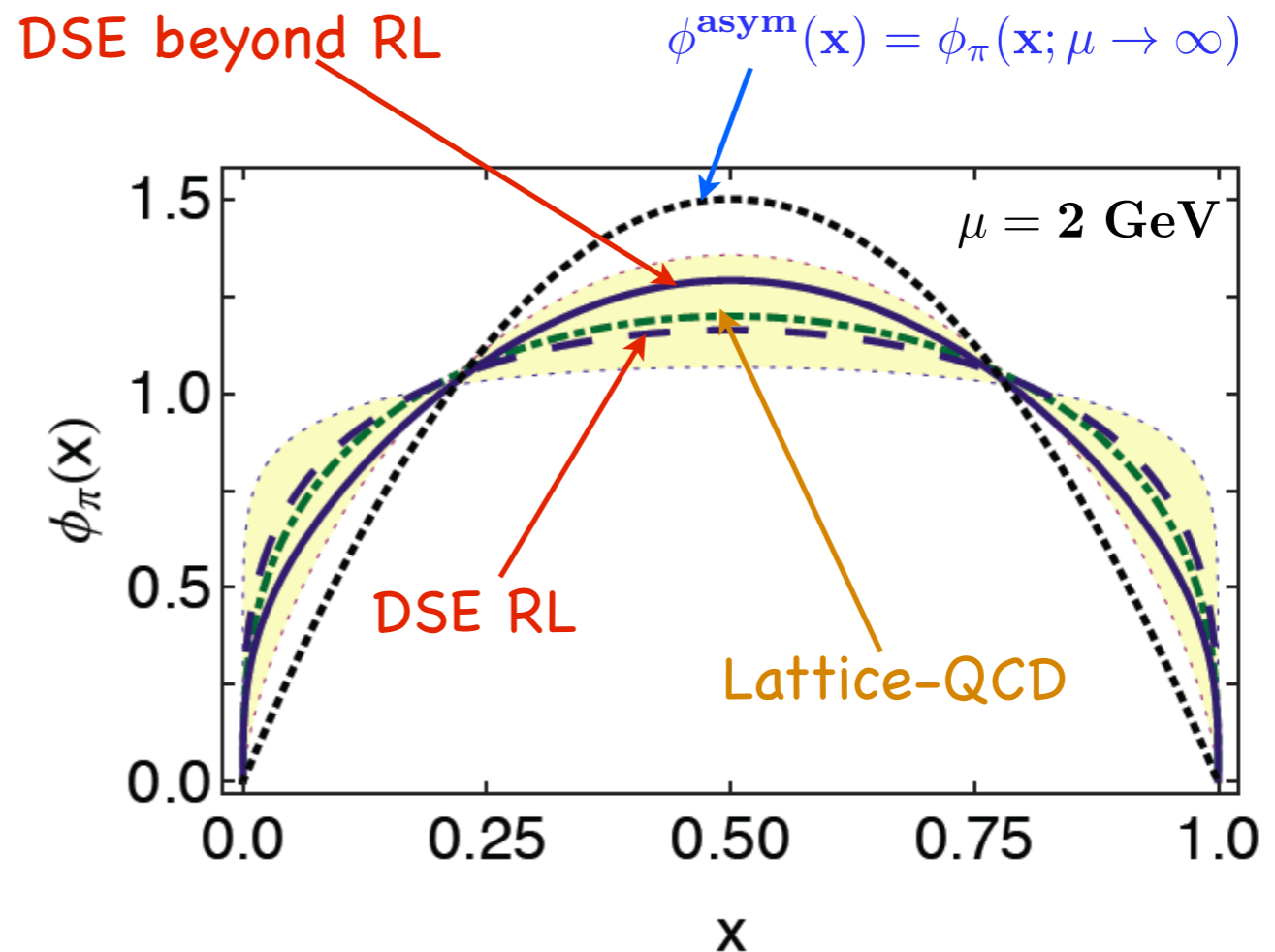
I. C. Cloët,¹ L. Chang,² C. D. Roberts,¹ S. M. Schmidt,³ and P. C. Tandy⁴

$$\phi_{\pi}^{\text{LQCD}}(\mathbf{x}; \mu = 2) = N \mathbf{x}^{\alpha} (1 - \mathbf{x})^{\alpha}$$

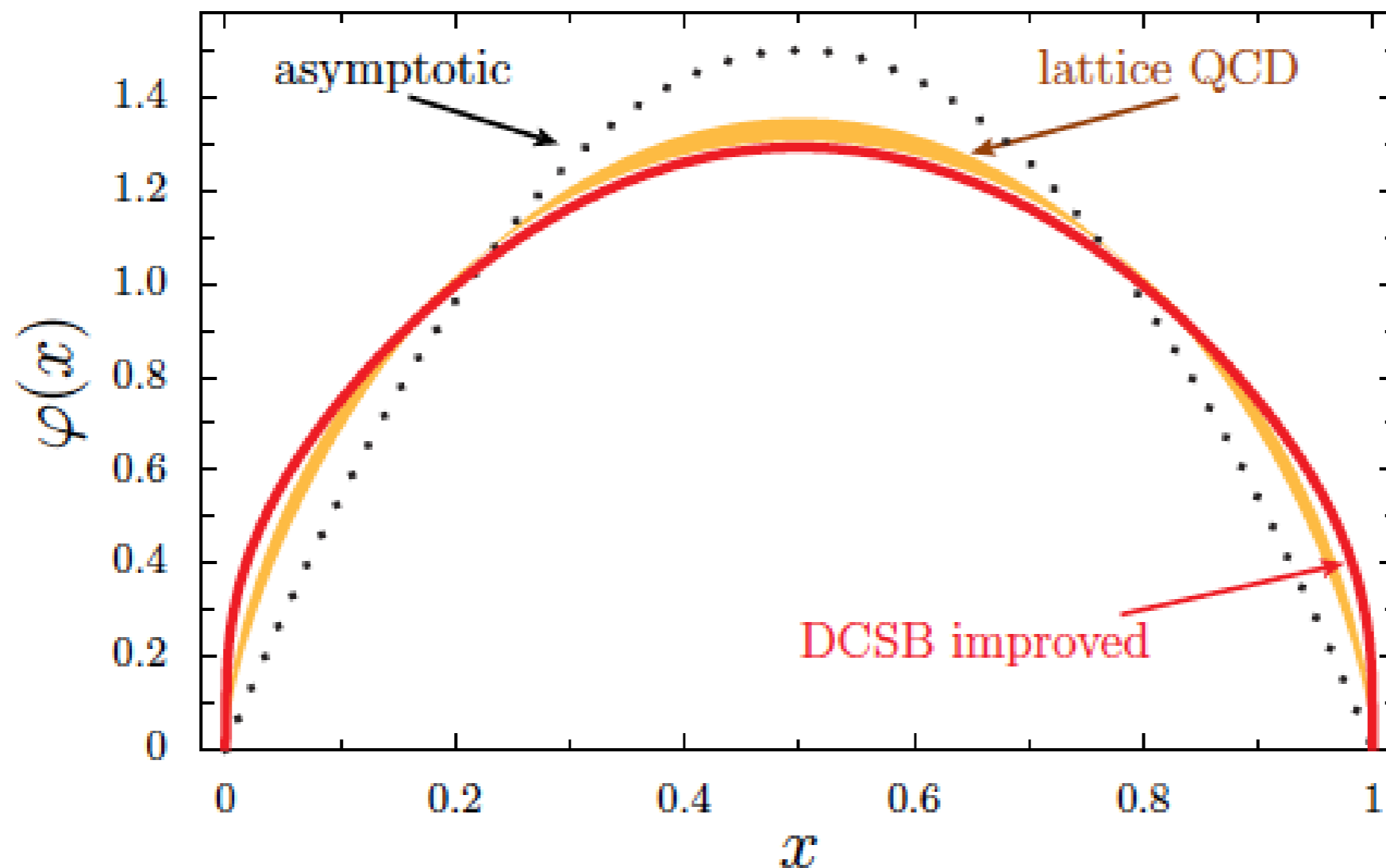
$$\alpha = 0.35 + 0.32 - 0.24$$

$$\langle (2\mathbf{x} - 1)^2 \rangle_{\mu=2}^{\text{LQCD}} = 0.27 \pm 0.04$$

V. Braun et al., PRD74, 074501 (2006)



Pion Distribution Amplitude



$$\langle (2x - 1)^2 \rangle_{\mu=2 \text{ GeV}}^{\text{LQCD}} = 0.2361 (41) (39)$$

V. Braun et al., arXiv:1503.03656 [hep-lat]

DSE prediction: 0.251



The Pion Charge Form Factor: Transition from npQCD to pQCD

$$F_\pi(Q^2 = uv) = \int_0^1 dx \int_0^1 dy \phi_\pi^*(x; Q) [\mathbf{T}_H(x, y; Q^2)] \phi_\pi(y; Q) + \text{NLO/higher twist} \dots$$

---LFQCD, Brodsky, LePage PRD (1980)

$$Q^2 \gg \Lambda_{\text{QCD}}^2 : Q^2 F_\pi(Q^2) \rightarrow 16 \pi f_\pi^2 \alpha_s(Q^2) \omega_\phi^2(Q^2) + \mathcal{O}(1/Q^2)$$

at $Q^2 \sim 3 - 4 \text{ GeV}^2$, $\Rightarrow 0.1$
 JLab expt, Theory $\Rightarrow 0.45$

$$\omega_\phi(Q^2) = \frac{1}{3} \int_0^1 dx \frac{\phi_\pi(x; Q)}{x}$$

$\rightarrow 1, Q^2 \rightarrow \infty$

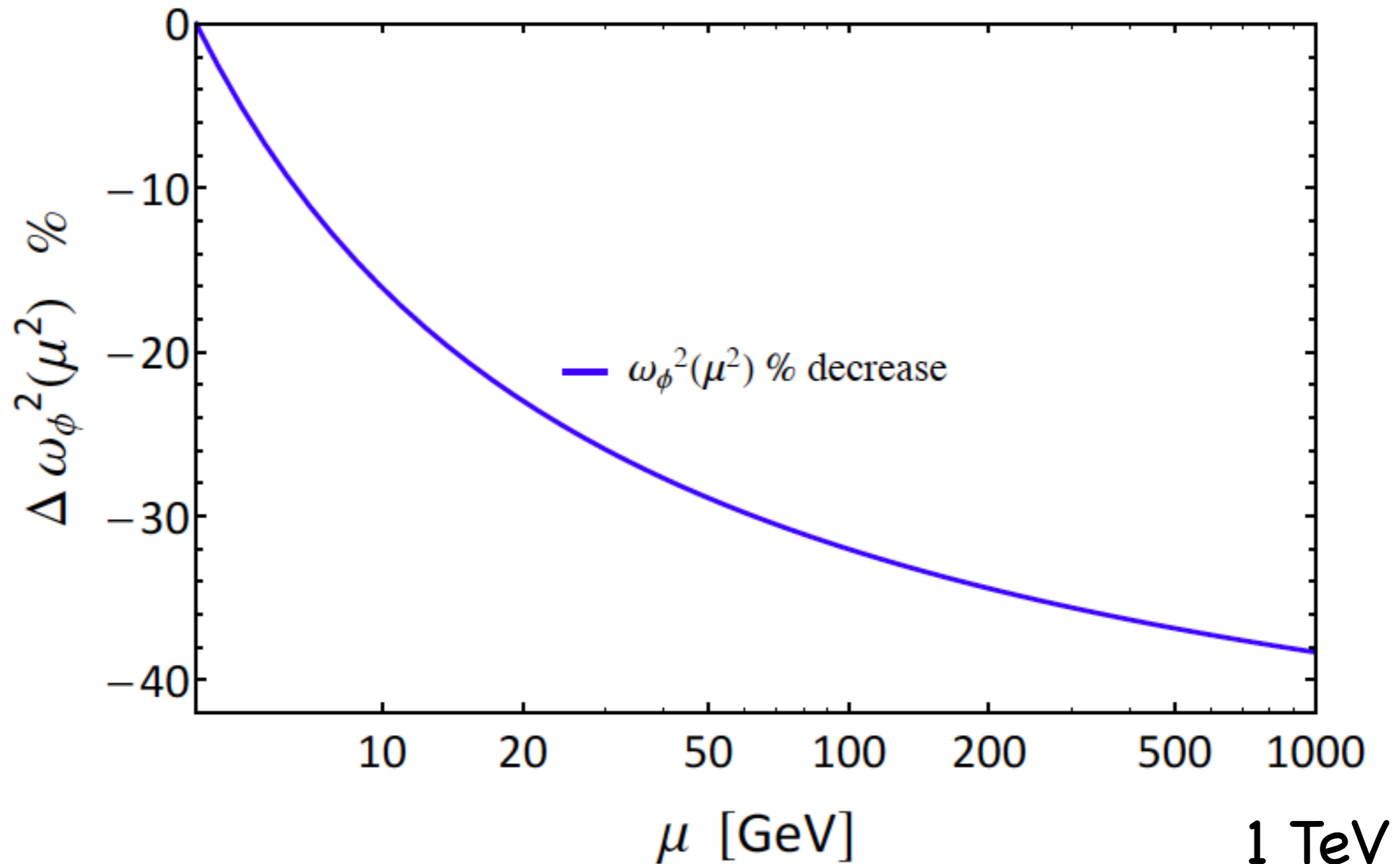
But, recent DSE theory $\Rightarrow \phi_\pi(x; \mu = 2 \text{ GeV}) \Rightarrow \omega_\phi^2 = 3.3$

Pion Electromagnetic Form Factor at Spacelike Momenta

L. Chang,¹ I. C. Cloët,² C. D. Roberts,² S. M. Schmidt,³ and P. C. Tandy⁴

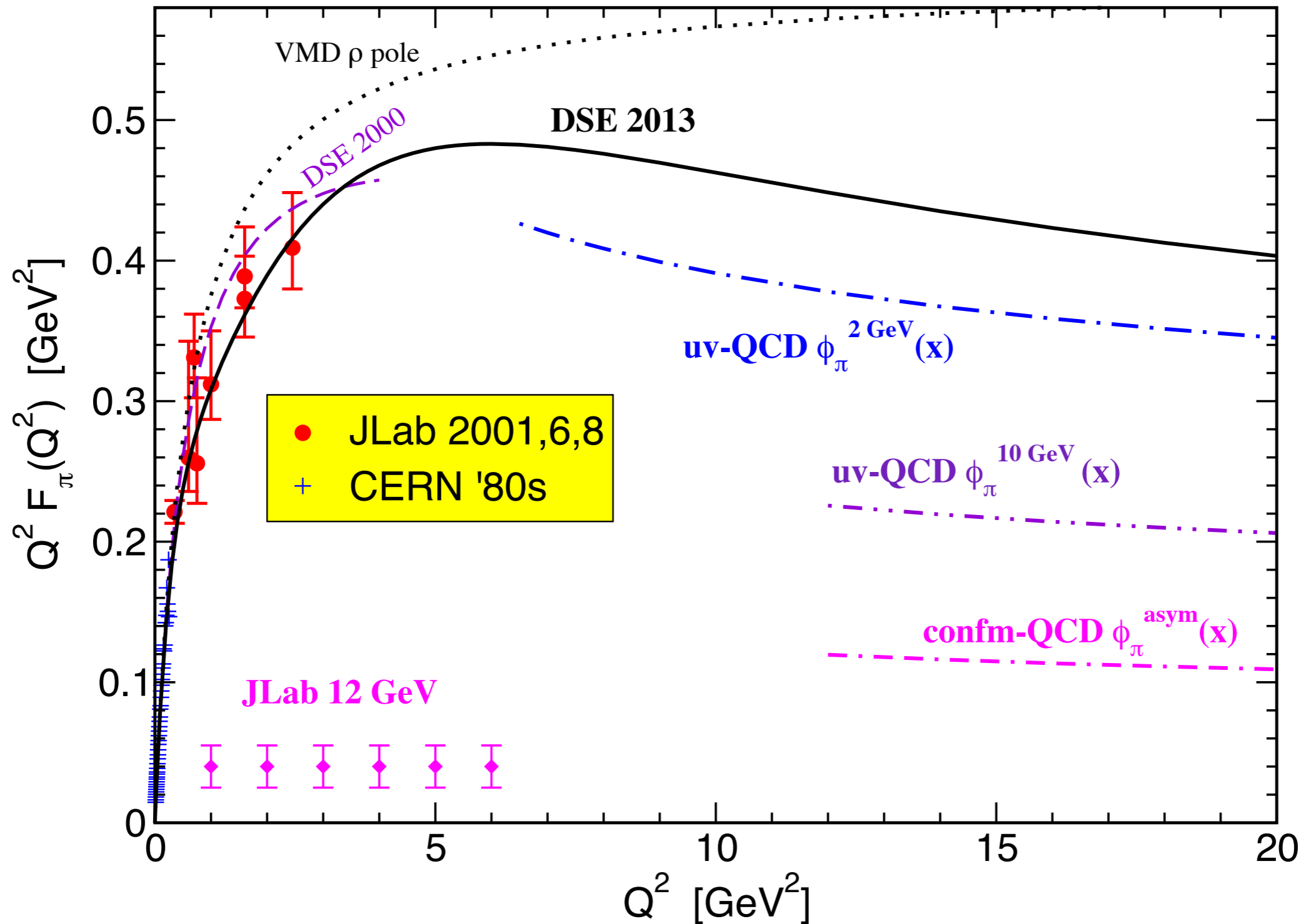
UV-QCD is not Asymptotic QCD

$$Q^2 \gg \Lambda_{\text{QCD}}^2 : Q^2 F_\pi(Q^2) \rightarrow 16 \pi f_\pi^2 \alpha_s(Q^2) \omega_\phi^2(Q^2) + \mathcal{O}(1/Q^2)$$



Pion Electromagnetic Form Factor at Spacelike Momenta

L. Chang,¹ I.C. Cloët,² C.D. Roberts,² S. M. Schmidt,³ and P. C. Tandy⁴

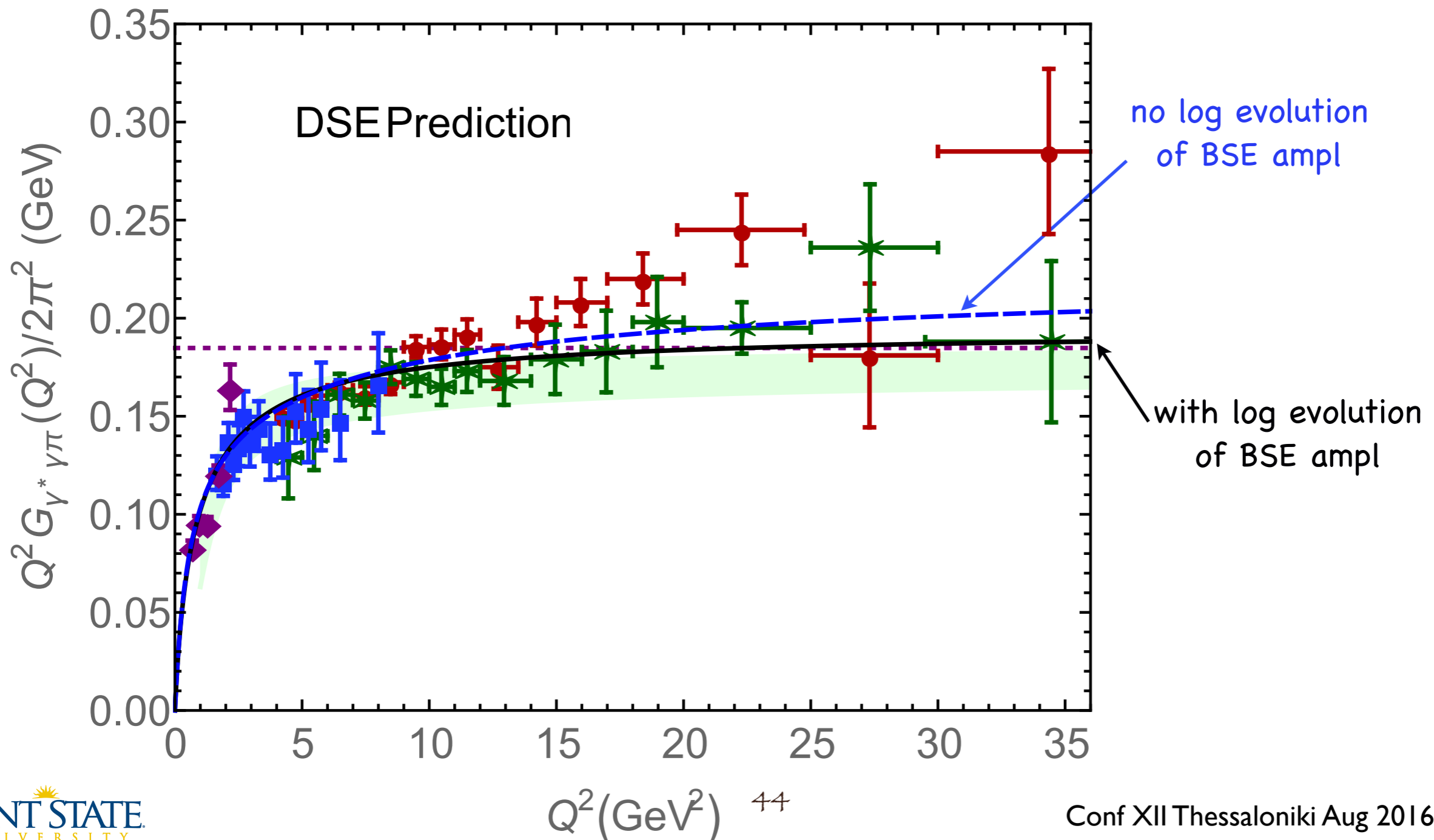


Jab data: G. Huber et al., PRC78, 045203 (2008)

Pion Transition Form Factor

K. Raya, L. Chang, A. Bashir, J.J.Cobos-Martinez, L.X. Gutierrez-Guerrero, C.D.Roberts, P.C.Tandy,
PRD93, 074017 (2016)

From unified treatment of DA, elastic FF, and transition FF



Summary

- **DSE approach** works extremely well for pion & kaon due to symmetry dominance.
- **Parton Distribution Amplitudes** (pion, kaon). **DSE approach shows good contact with available lattice-QCD moments.** Flavor symmetry breaking & dynamical chiral symmetry breaking evident and quantitative in the shapes.
- **Pion Transition & Elastic Form Factors** **DSE TFF calculation for all Q^2 —agrees with Belle not BaBar.** DSE eIFF— —Connection with ultraviolet /hard scattering QCD reconciled. Identify that the ultraviolet partonic behavior is within reach of proposed JLab pion FF experiments.
- **Parton Distribution Functions** (pion). Qualitative behavior of empirical data fits reproduced by DSE q - q bar + pion loop analysis.
- **Time to declare we understand the pion and kaon in QCD ?**
- **X. Ji's space-like correlator approach to PDFs**—a model investigation. Spurious anti-quark contributions seem unavoidable if $P_z < 2$ GeV. For $x > 0.8$, need $P_z > 4$ GeV for confidence in the qualitative shape. Further work in progress.

