



XVI WORKSHOP ON HIGH ENERGY SPIN PHYSICS  
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The momentum transfer dependence of the hadrons GPDs  
and Compton scattering at wide region of  $t$

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# Contents

- \* Introduction
- \* Nucleon structure
- \* Hadrons form-factors and GPDs
- \* New GPDs fitting of the electromagnetic form factors
  - \* transition form factor
- \* Real Compton Scattering
  - \* Elastic hadron scattering and recent LHC data
  - \* The structure of the nucleons in the impact parameter representation
- \* Results and Summery

A.Z. Dubnickova and S. Dubnicka

Hep-ph/0708.0162

“One doesn’t know explicit form of the nucleon matrix element of the EM current”

$$J_{\mu}^{EM} = \frac{2}{3} \bar{u} \gamma_{\mu} u - \frac{1}{3} \bar{d} \gamma_{\mu} d - \frac{1}{3} \bar{s} \gamma_{\mu} s.$$

$$J_{\mu}(P', s'; P, s) = \bar{u}(P', s') \Lambda_{\mu}(q, P) u(P, s) = \\ \bar{u}(P', s') (\gamma_{\mu} F_1(q^2) + \frac{1}{2M} i \sigma_{\mu\nu} q_{\nu} F_2(q^2)) u(P, s).$$

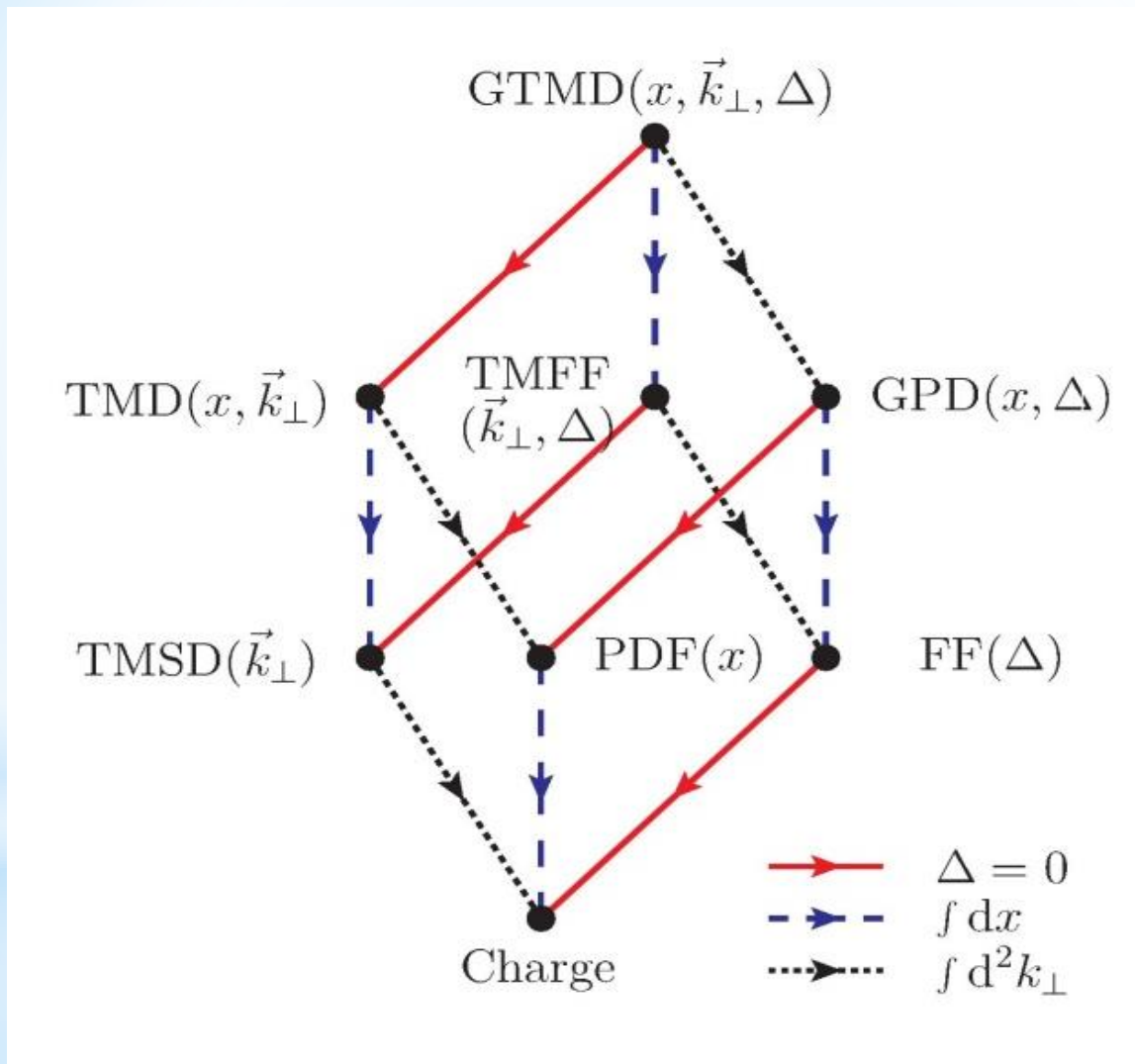
## Standard definitions

$$G_{Ep}(0) = 1; \quad G_{En}(0) = 0; \quad G_M(0) = (G_E(0) + k) = \mu;$$

$$\mu_p = (1 + 1.79) \frac{e}{2M}; \quad k_p = 1.79;$$

$$F_1^D(t) = \frac{4M_p^2 - t \mu_p}{4M_p^2 - t} G_D(t); \quad F_2^P(t) = \frac{1}{1 - t / 4M_p^2} G_D(t);$$

$$G_D(t) = \frac{\Lambda^2}{(\Lambda - t)^2}; \quad \Lambda = 0.71 \text{ GeV}^2;$$



# General Parton Distributions (GPDs)

## GPDs

limit  $Q_\gamma^2=0$ , and  $\xi=0$

X.Ji [Sum Rules \(1997\)](#)

$$\mathcal{F}_{\xi=0}(x;t) = \mathcal{F}(x;t)$$

$$F_1^q(t) = \int_{-1}^1 dx H^q(x, \xi, t);$$

$$F_2^q(t) = \int_{-1}^1 dx E^q(x, \xi, t);$$

$$\mathcal{H}^q(x;t) = H^q(x,0,t) + H^q(-x,0,t)$$

$$\mathcal{E}^q(x;t) = E^q(x,0,t) + E^q(-x,0,t)$$

$$F_1^q(t) = \int_0^1 dx \mathcal{H}^q(x, \xi, t);$$

$$F_2^q(t) = \int_0^1 dx \mathcal{E}^q(x, \xi, t);$$

$$\int_{-1}^1 dx \textcolor{red}{x} [H^q(x, \xi, t) + E^q(x, \xi, t)] = A_q(\Delta^2) + B_q(\Delta^2);$$

# General Parton Distributions (GPDs)

Sanielevici-Valin (1984) – Valon model – Phys.Rev.D29 (1984).

“matter form factor” (MFF) measures the interaction of a gluonic probe with the excited matter of the overlapping hadrons and should incorporate the static matter distributions of the participating hadrons...”

$$M_{AB}(s, t) = K_A(q^2) K_B(q^2) V(s, q^2);$$

$$K_p(q^2) = \frac{1}{3} \int_0^1 dx [2L_p^U(x) T_p^U(\vec{k}) + L_p^D(x) T_p^D(\vec{k})]; \quad \vec{k} = (1-x)\vec{q}.$$

$$L_p^U(x) = 7.98 x^{0.65} (1-x)^2; \quad L_p^D(x) = 6.01 x^{0.35} (1-x)^{2.3};$$

$$T_p^U(\vec{k}) = e^{-6.1k^2}; \quad T_p^D(\vec{k}) = e^{-3k^2}; \quad k^2 = (1-x)^2 q^2.$$

Why it is need know the  $t$ -dependence of GPDs in the wide region of the momentum transfer?

- Form factors in the wide region of  $t$  ( $x^{n-1}$ )

- (Compton - zero momentum -  $x^{-1}$
  - electromagnetic, - first momentum -  $x^0$
  - gravitomagnetic - second momentum -  $x^1$

- \* Tomography of the nucleons  
(impact parameter representation)  
require the integration on the whole region of  $t$

## Our ansatz

O.S., O. Terayev, Phys.Rev.D79:033003,2009  
Found.Phys.40:1042,2010

1. Simplest;
2. Not far from Gaussian representation
3. Satisfy the  $(1-x)^n$  ( $n \geq 2$ )
4. Valid for large  $t$

$$\mathcal{H}^q(x, t) \approx q(x) \exp\left[a + \frac{(1-x)^2}{x^{0.4}} t\right];$$

$q(x)$  is based on the MRST2002

$$u(x) = 0.262 x^{-0.69} (1-x)^{3.50} (1 + 3.83 x^{0.5} + 37.65 x);$$

$$d(x) = 0.061 x^{-0.65} (1-x)^{4.03} (1 + 49.05 x^{0.5} + 8.65 x);$$

TABLE I. The sets of the PDFs with its basic parameters.

| N   | Model    | Reference | $g_2^q(x)$ | Order, ( $Q_0^2$ ) |
|-----|----------|-----------|------------|--------------------|
| 1   | ABKM09   | [50]      | Eq. (36)   | NNLO (9.)          |
| 2a  | JR08a    | [46]      | Eq. (32)   | NNLO (0.55)        |
| 2b  | JR08b    | [46]      | Eq. (32)   | NNLO (2.)          |
| 3   | ABM12    | [51]      | Eq. (37)   | NNLO (9.)          |
| 4a  | KKT12a   | [48]      | Eq. (34)   | NLO (4.)           |
| 4b  | KKT12b   | [48]      | Eq. (34)   | NLO (4.)           |
| 5a  | GJR07d   | [52]      | Eq. (32)   | LO (0.3)           |
| 5b  | GJR07b   | [52]      | Eq. (32)   | NLO (0.3)          |
| 5c  | GJR07a   | [52]      | Eq. (32)   | NLO (2.)           |
| 5d  | GJR07c   | [52]      | Eq. (32)   | NLO (0.3)          |
| 6a  | MRST02   | [40]      | Eq. (32)   | NLO (1.)           |
| 6b  | MRST01   | [44]      | Eq. (32)   | NLO (1.)           |
| 7a  | GP08a    | [47]      | Eq. (33)   | NLO (0.5)          |
| 7b  | GP08b    | [47]      | Eq. (33)   | NNLO (1.5)         |
| 7c  | GP08c    | [47]      | Eq. (33)   | NLO (2.)           |
| 7d  | GP08d    | [47]      | Eq. (33)   | NNLO (0.5)         |
| 8a  | MRST09   | [43]      | Eq. (32)   | LO (1.)            |
| 8b  | MRST09   | [43]      | Eq. (32)   | NLO (1.)           |
| 8c  | MRST09   | [43]      | Eq. (32)   | NNLO (1.)          |
| 9   | MRST02P  | [49]      | Eq. (35)   | NLO (1.3)          |
| 10a | CJ12amin | [45]      | Eq. (32)   | NLO (1.7)          |
| 10b | CJ12am   | [45]      | Eq. (32)   | NLO (1.7)          |
| 10c | CJ12bmid | [45]      | Eq. (32)   | NLO (1.7)          |
| 10c | CJ12cmax | [45]      | Eq. (32)   | NLO (1.7)          |
| 11  | MRSTR4   | [40]      | Eq. (32)   | NLO (1.3)          |

O.S. – Phys.Rev.  
(D 89) (2014)

Martin – 2002 // H. KHANPOUR..-2012 (1205.5194)

$$x q_v(x, Q_0) = A_0 x^{A_1} (1-x)^{A_2} (1 + A_3 x^{A_4} + A_5 x^{A_6})$$

Pumplin et al. 2002 (CTEQ6M)

$$x q_v(x, Q_0) = A_0 x^{A_1} (1-x)^{A_2} e^{A_3} (1 + e^{A_4} x)^{A_5}$$

Martin et al. 2002 (MRST02) .– Martin -2009 (LO, NLO, NNLO)

$$x q_v(x, Q_0) = A_0 x^{A_1} (1-x)^{A_2} (1 + A_3 x^{0.5} + A_4 x)$$

Gluck-Pisano 2008

$$x q_v(x, Q_0) = A_0 x^{A_1} (1-x)^{A_2} (1 + A_3 x^{0.5} + A_4 x + A_5 x^{1.5})$$

Alekhin et al. 2012 (ABM12)

$$x q_v(x, Q_0) = \frac{2\delta_{qu} + \delta_{qd}}{N_q^\nu} x^{a_q} (1-x)^{b_q} x^{\gamma_{1,q}x + \gamma_{2,q}x^2 + \gamma_{3,q}x^3}$$

TABLE II. Experimental data of the electromagnetic form factors.

| N points | Proton            | References                                            |
|----------|-------------------|-------------------------------------------------------|
| 111      | $G_E^p$           | [53]; [55]; [56]; [57]; [58]; [59]; [54];             |
| 196      | $G_M^p$           | [53]; [55]; [60]; [56]; [61]; [62]; [59]; [54];       |
| 87       | $\mu G_E^p/G_M^p$ | [55]; [61]; [63]; [64]; [65]; [54];                   |
|          | neutron           |                                                       |
| 13       | $G_E^n$           | [66]; [67]; [68]; [69]; [70]; [71]; [72]; [73]; [74]; |
| 38       | $G_M^n$           | [75]; [76]; [77]; [78]; [79];                         |
| 6        | $\mu G_E^n/G_M^n$ | [80]; [68];                                           |

$$\mathcal{H}^u(x, t) \square u(x) \exp[2\alpha_1(\frac{(1-x)^{p_1}}{(x_0+x)^{p_2}}t)];$$

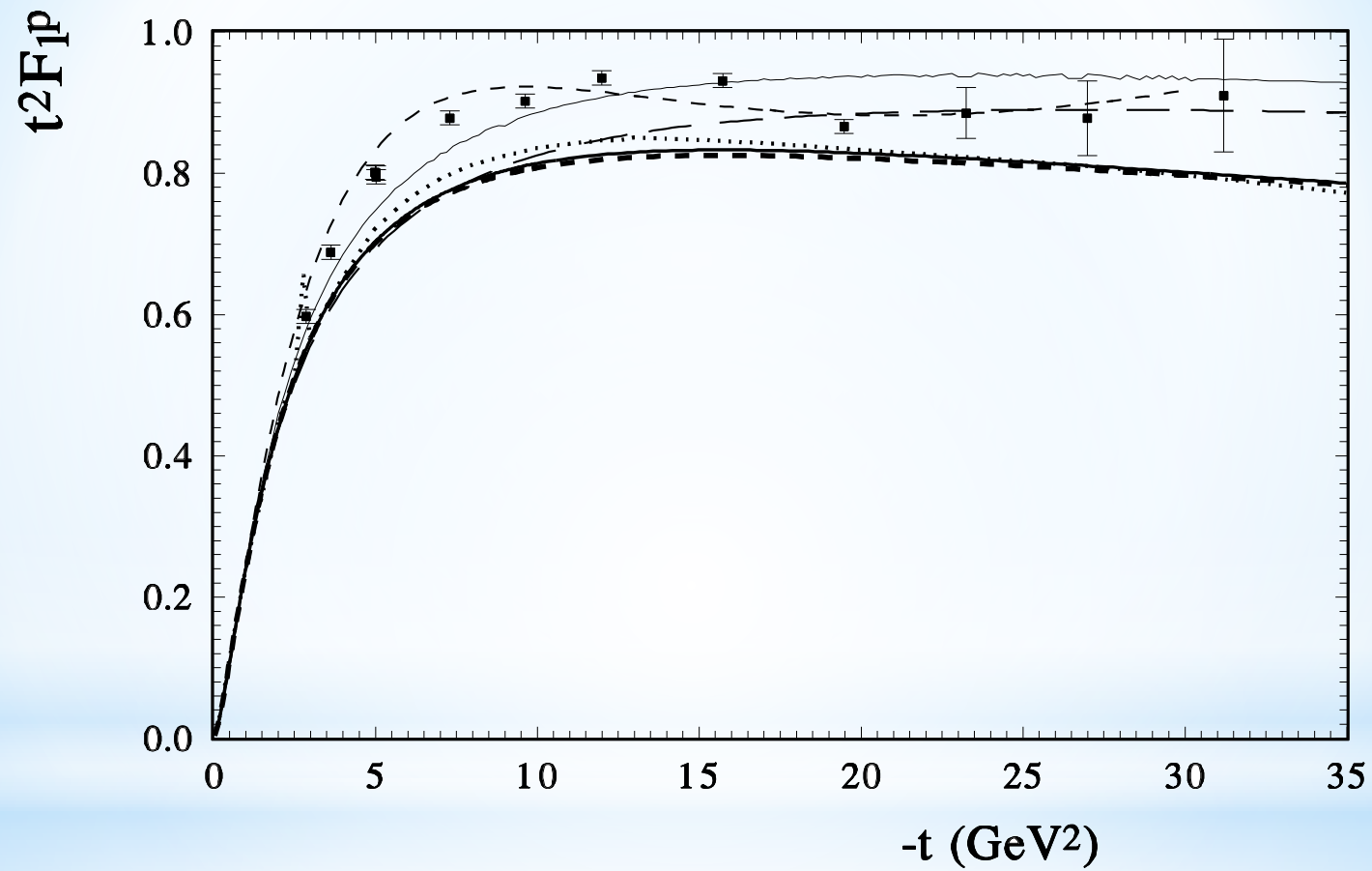
O.S., talk on Intern. Conf.  
 "SPIN in High Energy Physics"  
 ( 2012)

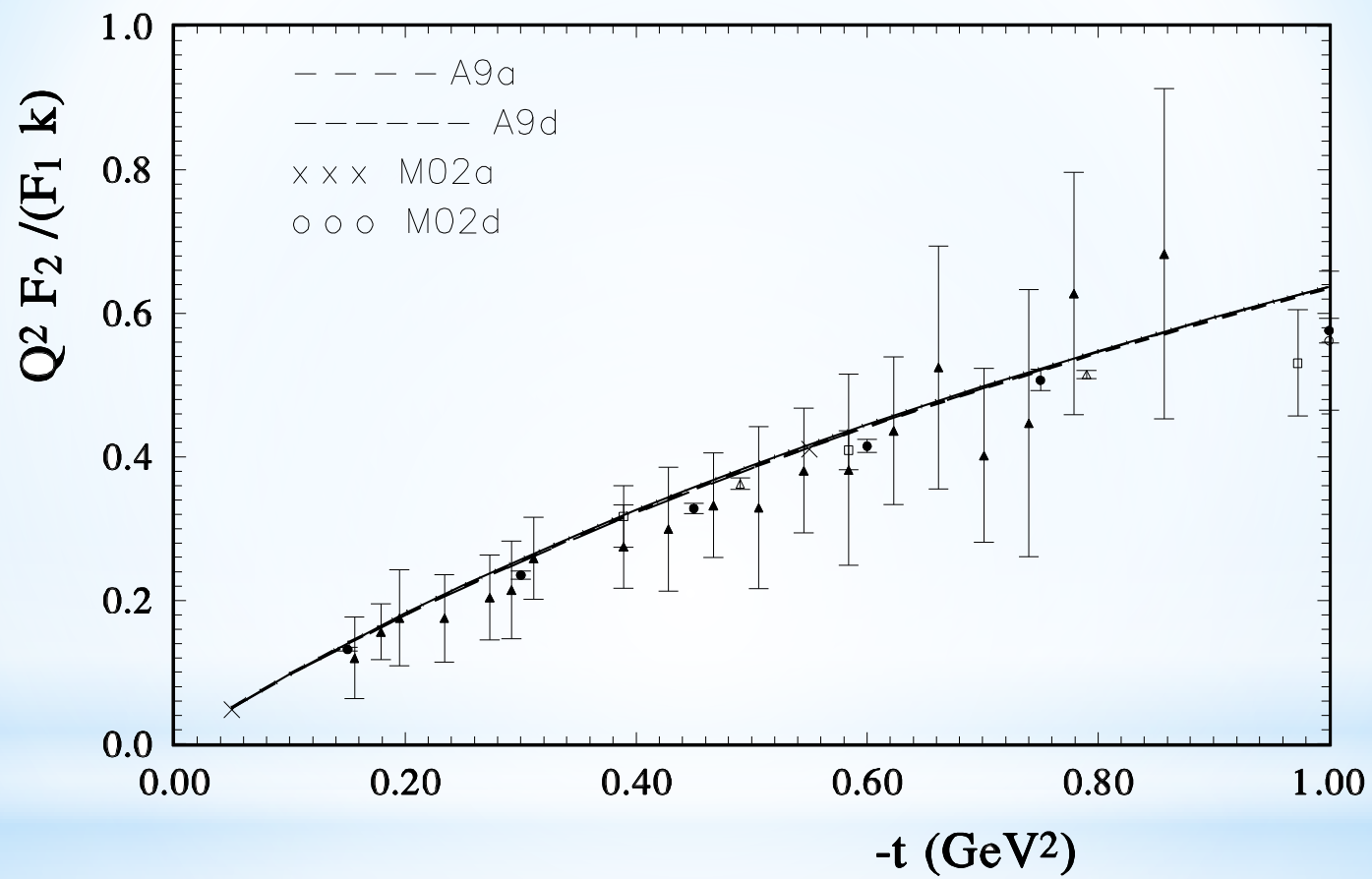
$$\mathcal{H}^d(x, t) \square d(x) \exp[2\alpha_1(\frac{(1-x)^{p_1(*k_d)}}{(x_0+x)^{p_2}}+d * x * (1-x)t]$$

|         | a1     | a2   | a3                                                                                | a4                                                                                | a5   | a6    | a7    | a8      | a9    |
|---------|--------|------|-----------------------------------------------------------------------------------|-----------------------------------------------------------------------------------|------|-------|-------|---------|-------|
|         | p1     | p2   |  |  | du   | dd    | x0    | k       | d     |
| Al-09   | 2.03   | 0.5  | 0.4                                                                               | 0.39                                                                              | 2.4  | -0.14 | 0.006 | 0.41    | -1.61 |
| Al-09-0 | 2.-fix | 0.5  | 0.38                                                                              | 0.39                                                                              | 2.6  | 0.03  | 0.007 | 1.-fix  | ----- |
| G-07-a  | 1.88   | 0.43 | 0.6                                                                               | 0.6                                                                               | 1.7  | -0.14 | 0.013 | 0.54    | -1.   |
| G-07-a0 | 2.-fix | 0.34 | 0.68                                                                              | 0.73                                                                              | 1.7  | -0.14 | 0.003 | 1 - fix | ----- |
| R4      | 1.89   | 0.51 | 0.5                                                                               | 0.43                                                                              | 2.6  | 0.5   | 0.01  | 0.35    | -2.   |
| R4-0    | 2.-fix | 0.42 | 0.57                                                                              | 0.56                                                                              | 2.2  | 0.15  | 0.005 | 1 - fix | ----- |
| M-09NN  | 1.92   | 0.4  | 0.57                                                                              | 0.66                                                                              | 0.93 | -1.1  | 0.008 | 0.58    | -0.61 |
| M-09NN  | 2- fix | 0.35 | 0.6                                                                               | 0.7                                                                               | 1.5  | -0.5  | 0.003 | 1. fix  | ----- |
| G07NL   | 1.49   | 0.35 | 0.6                                                                               | 0.71                                                                              | 0.58 | -1.05 | 0.007 | 0.89    | 0.46  |

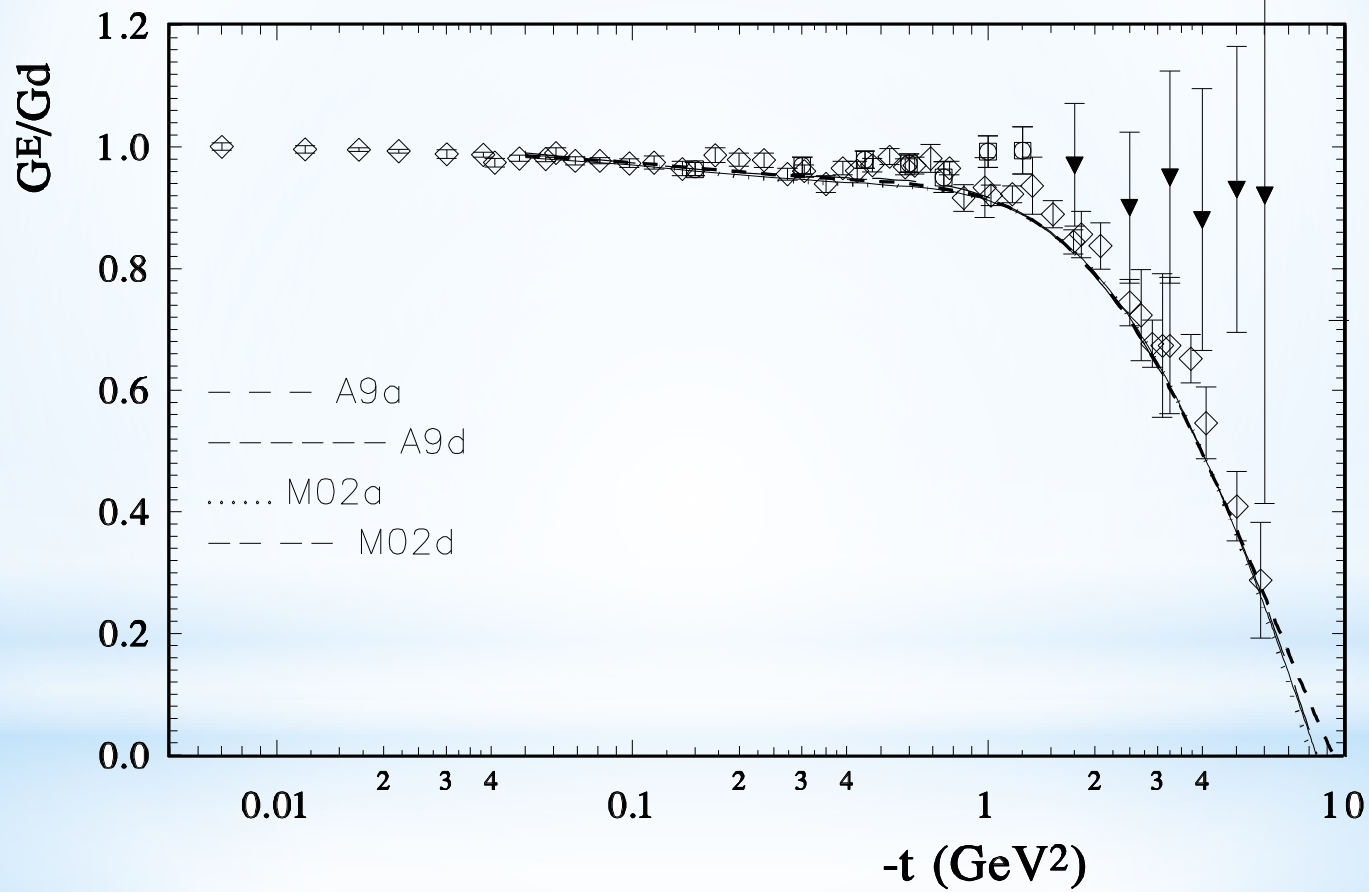
TABLE III. The sum of  $\chi^2$  for the different PDFs sets and with different number of the fitting parameters.

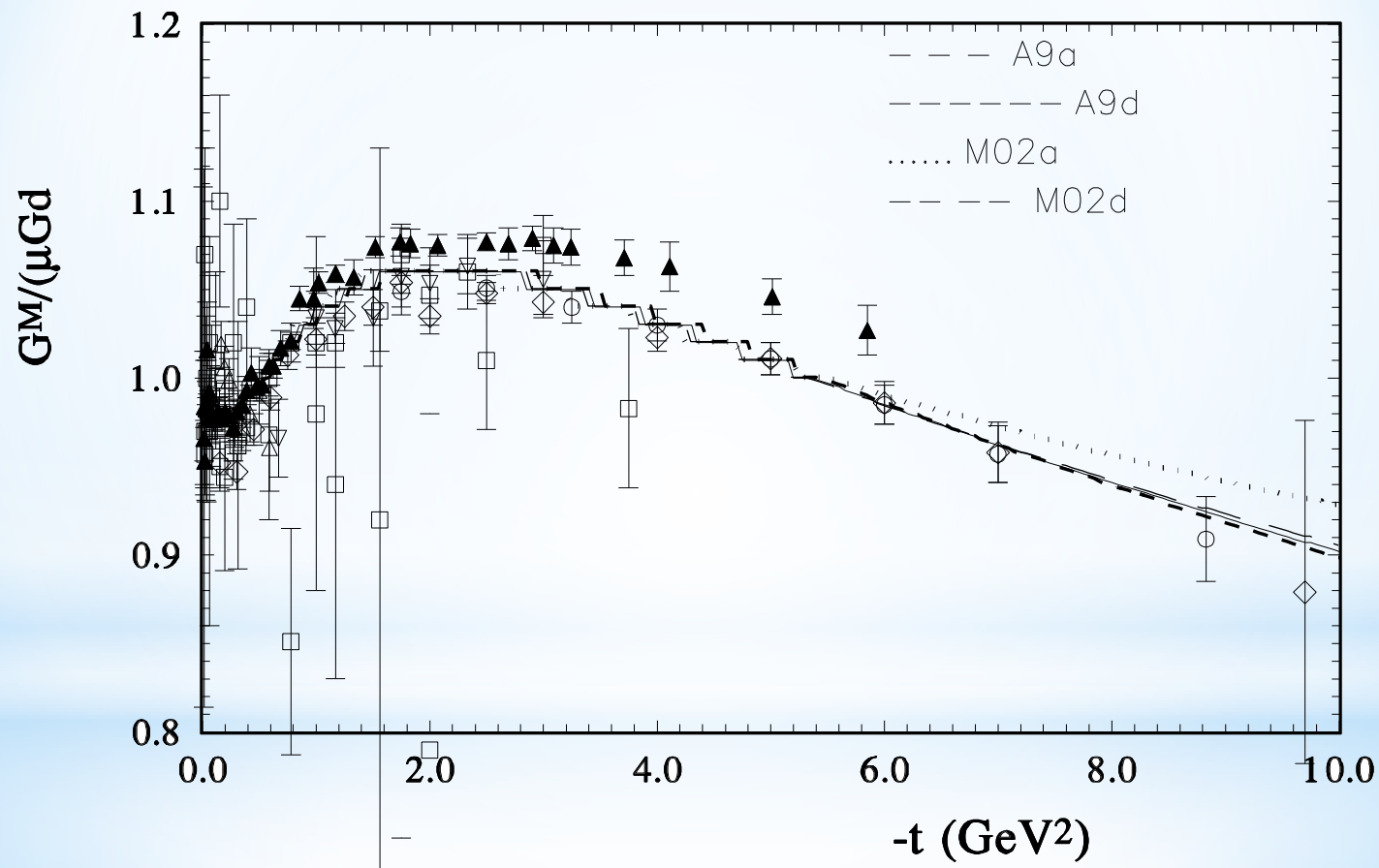
| N   | Model    | $\chi_0^2$ | $\chi_{+1p}^2$ | $\chi_{+1p}^2$ | $\chi_{+2p}^2$ | $\chi_{+3p}^2$ | $\chi_{+4p}^2$ |
|-----|----------|------------|----------------|----------------|----------------|----------------|----------------|
| 1   | ABKM09   | 984        | 984            | 953            | 936            | 903            | 872            |
| 2a  | JR08a    | 1119       | 861            | 891            | 861            | 860            | 857            |
| 2b  | JR08b    | 1242       | 1242           | 880            | 868            | 868            | 864            |
| 3   | ABM12    | 1036       | 1033           | 1031           | 1020           | 919            | 904            |
| 4a  | KKT12a 8 | 1170       | 1133           | 1170           | 1108           | 934            | 888            |
| 4b  | KKT12b   | 1074       | 1074           | 1064           | 1064           | 1036           | 988            |
| 5a  | GJR07d   | 1772       | 1042           | 1553           | 936            | 884            | 878            |
| 5b  | GJR07b   | 1172       | 1078           | 992            | 947            | 887            | 865            |
| 5c  | GJR07a   | 1215       | 1214           | 1079           | 1024           | 940            | 894            |
| 5d  | GJR07c   | 8423       | 1230           | 7279           | 1042           | 954            | 891            |
| 6a  | MRST02   | 1089       | 1041           | 1035           | 1013           | 932            | 905            |
| 6b  | MRST01   | 1167       | 1002           | 1129           | 999            | 898            | 873            |
| 7a  | GP08a    | 2189       | 1575           | 1495           | 1017           | 886            | 879            |
| 7b  | GP08b    | 1423       | 1382           | 1009           | 988            | 891            | 888            |
| 7c  | GP08c    | 1278       | 1226           | 991            | 974            | 898            | 892            |
| 7d  | GP08d    | 4587       | 2484           | 4575           | 3483           | 2388           | 2388           |
| 8a  | MRST09a  | 1785       | 1184           | 1598           | 1107           | 974            | 887            |
| 8b  | MRST09b  | 1382       | 1226           | 1149           | 1052           | 972            | 894            |
| 8c  | MRST09c  | 1260       | 1168           | 1005           | 960            | 930            | 881            |
| 9   | MR02P    | 1344       | 1187           | 1120           | 1044           | 946            | 875            |
| 10a | O12a     | 1523       | 1458           | 1080           | 1054           | 1007           | 932            |
| 10b | O12am    | 1534       | 1468           | 1077           | 1050           | 1007           | 932            |
| 10c | O12b     | 1377       | 1361           | 1134           | 1127           | 1052           | 958            |
| 10d | O12c     | 1366       | 1359           | 1192           | 1191           | 1085           | 981            |
| 11  | MRST02R4 | 2360       | 2358           | 1879           | 1819           | 1786           | 1780           |

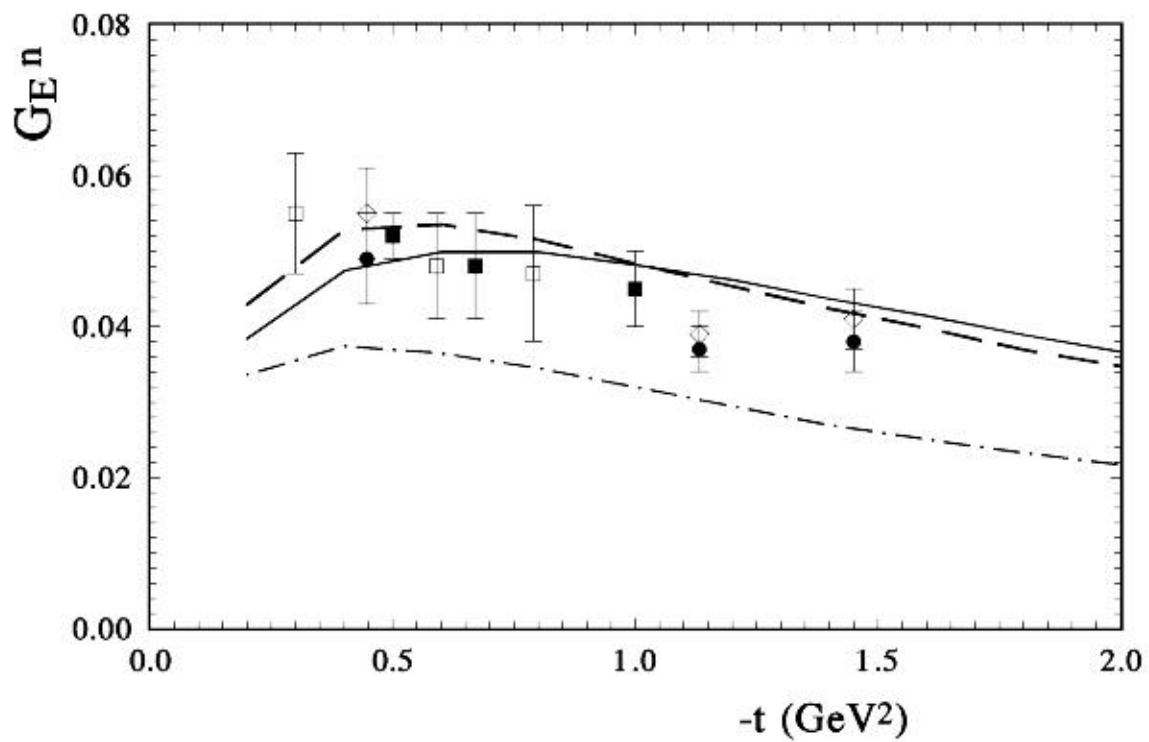


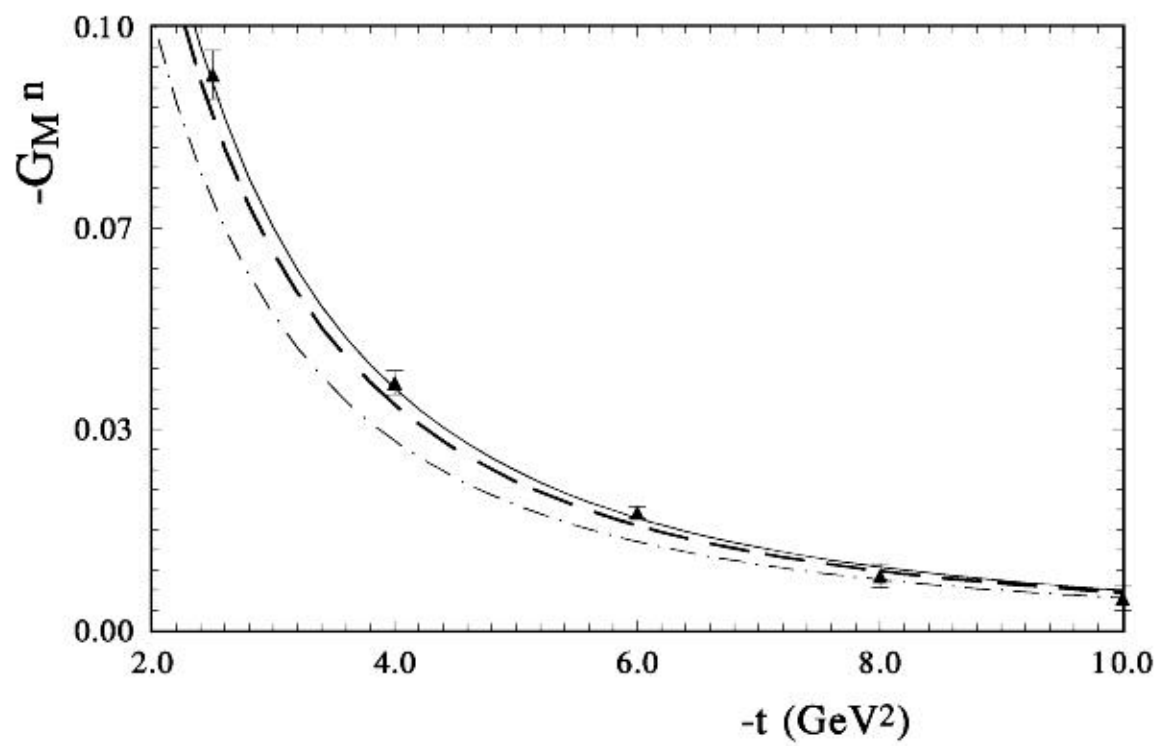


$$G_E^p(t) / G_d(t)$$





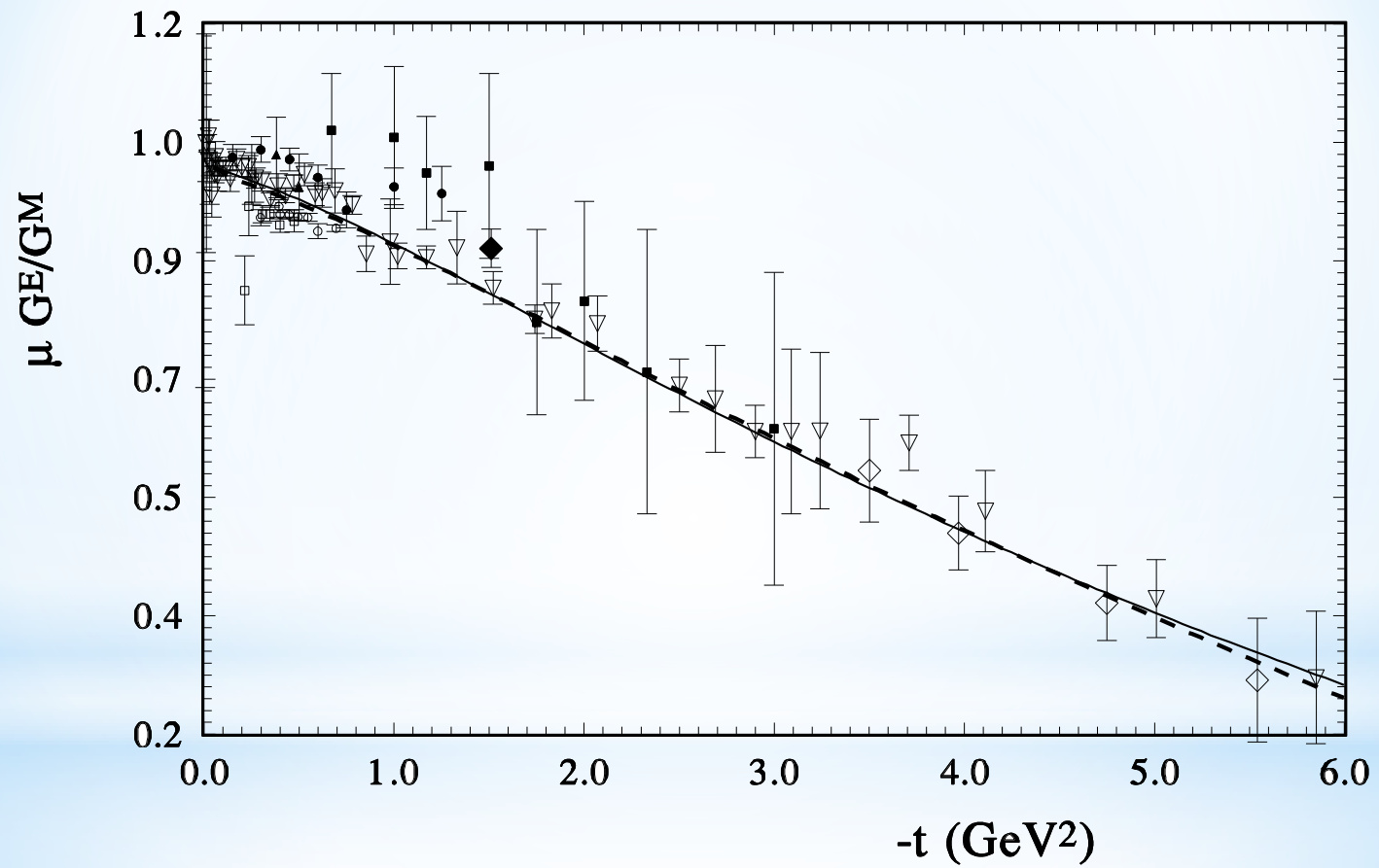




$G_M^n$

$$\mu G_{ep}/G_{Mp}$$

▽



- Form factors in the wide region of  $t$
- $(x^{n-1})$

(Compton - zero momentum -  $x^{-1}$

electromagnetic, - first momentum -  $x^0$

gravitomagnetic - second momentum -  $x^1$

## Magnetic transition form factor $G_M^* (\gamma^* N \Delta)$

We can also be used to estimate  $N \rightarrow \Delta$  transition form factors, provided one can relate the  $N \rightarrow \Delta$  transition GPDs.

For the magnetic  $N \rightarrow \Delta$  transition form factor  $G_M^*(t)$ , in the large  $N_c$  limit, the relevant  $N \rightarrow \Delta$  GPD can be expressed in terms of the isovector GPD

$E_u - E_d$ , yielding the sum rule

$$G_M^*(t) = \frac{G_M^*(0)}{k_V} \int_{-1}^1 dx \{E^u(x, \xi, t) - E^d(x, \xi, t)\};$$

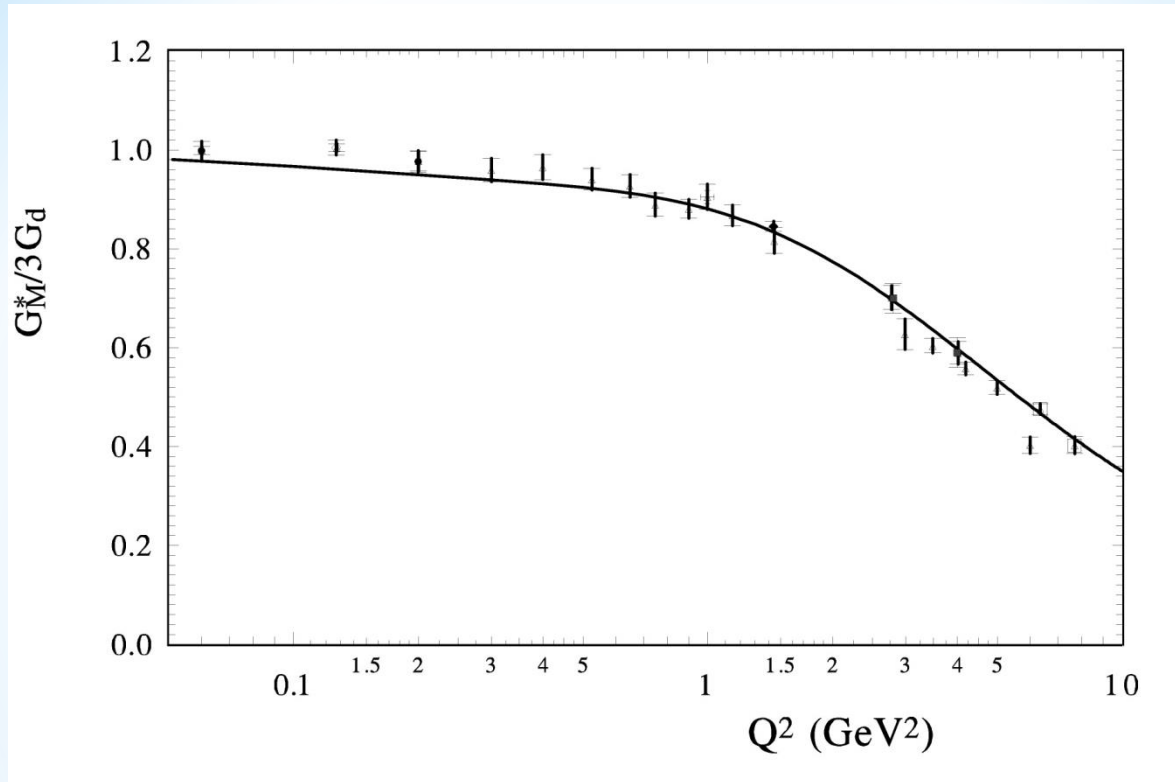
where  $k_V = k_p - k_n = 3.70$ ; and  $G_M^*(0) = k_V / \sqrt{3}$ ;

$$E^u(x, t) = u(x)_E \exp[2\alpha_1(\frac{(1-x)^{p_1}}{(x_0+x)^{p_2}}t)];$$

$$E^d(x, t) = d(x)_E \exp[2\alpha_1(\frac{(1-x)^{p_1(*k_d)}}{(x_0+x)^{p_2}} + d * x * (1-x)t]$$

All parameters are fixed

where  $k_v = k_p - k_n = 3.70$ ;



The Jones-Scadron convention is related to Ash conventional

$$G_{M,J-S}^*(Q^2) = G_{M,Ash}^*(Q^2) \sqrt{1 + \frac{Q^2}{(M+m)^2}};$$

$$\gamma p \rightarrow \gamma p$$

The differential cross section for the unpolarized cross section that reaction can be written as

$$\frac{d\sigma}{dt} = \frac{\pi\alpha_{em}^2}{s^2} \frac{(s-u)^2}{-us} \left[ R_V^2(t) - \frac{t}{4m^2} R_T^2(t) + \frac{t^2}{(s-u)^2} R_A^2(t) \right]$$

where  $R_V(t)$ ,  $R_T(t)$ ,  $R_A(t)$  are the form factors given by the  $1/x$  moments of corresponding GPDs

$H^q(x,t)$ ,  $E^q(x,t)$ ,  $\tilde{H}^q(x,t)$ .

The last is related with the axial form factors.

$$\frac{d\sigma}{dt} = \frac{2\pi\alpha_{em}^2}{s^2} \left[ -\frac{u}{s} - \frac{s}{u} \right] \left\{ \frac{1}{2} (R_V^2(t) + R_A^2(t)) - \frac{us}{s^2 + u^2} (R_V^2(t) + R_A^2(t)) \right\}$$

A. Radyushkin (1998)

$$R_A(t) \approx R_V(t)$$

M. Diehle, P. Kroll

$$\frac{R_V(t)}{R_A(t)} = \frac{F_2(t)}{F_1(t)} \approx \frac{2m}{\sqrt{-t}}.$$

S. Alekhin, J. Blumlein, S. Moch, Phys.Rev. D86 (2012)

$$x \, q_u = 4.649903 x^{0.712} (1-x)^{3.637} x^{0.593x-3.607x^2+3.718x^3}$$

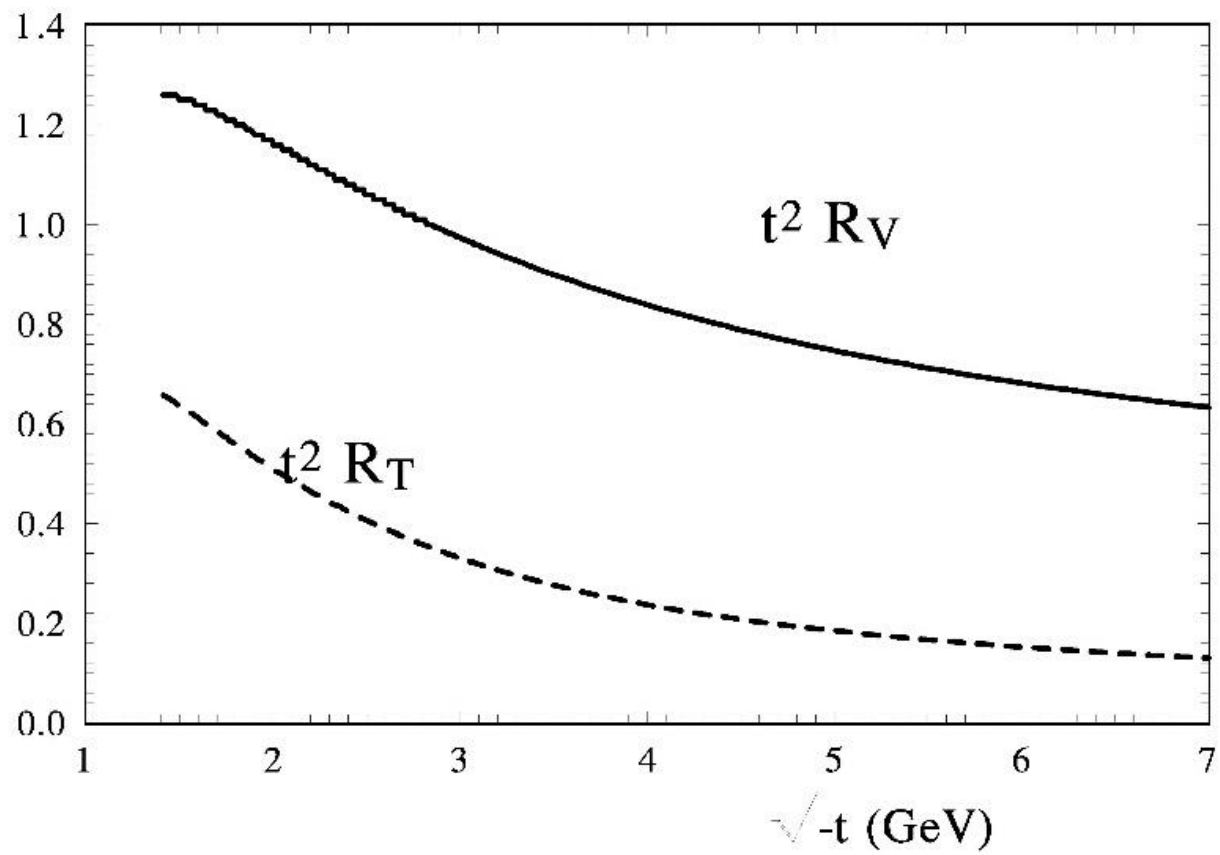
$$x \, q_d = 3.424394 x^{0.741} (1-x)^{5.123} x^{(1.122x-2.984x^2)}$$

$$R_V(t) = \sum_q e_q^2 \int \frac{dx}{x} dx \, H^q(x, \xi = 0, t)$$

$$= \frac{dx}{x} \{u(x) \exp[2\alpha_1(\frac{(1-x)^{p_1}}{(x_0+x)^{p_2}}t)] + d(x) \exp[2\alpha_1(\frac{(1-x)^{p_1(*k_d)}}{(x_0+x)^{p_2}}t)]\}$$

$$R_T(t) = \sum_q e_q^2 \int \frac{dx}{x} dx \, E^q(x, \xi = 0, t)$$

$$= \frac{dx}{x} \{u^e(x) \exp[2\alpha_1(\frac{(1-x)^{p_1}}{(x_0+x)^{p_2}}t)] + d^e(x) \exp[2\alpha_1(\frac{(1-x)^{p_1(*k_d)}}{(x_0+x)^{p_2}}t)]\}$$



$$R_A(t) = \sum_q e_q^2 \int \frac{dx}{x} \tilde{H}^q(x, \xi = 0, t)$$

F.Taghavi-Shahri, H. Khanpour .. 1603.03157 NNLO  $Q^2_0=4 \text{ GeV}^2$

$$x\Delta_q(x, Q_0) = N_q \eta_q x^{\alpha_q} (1-x)^{b_q} (1+c_q x);$$

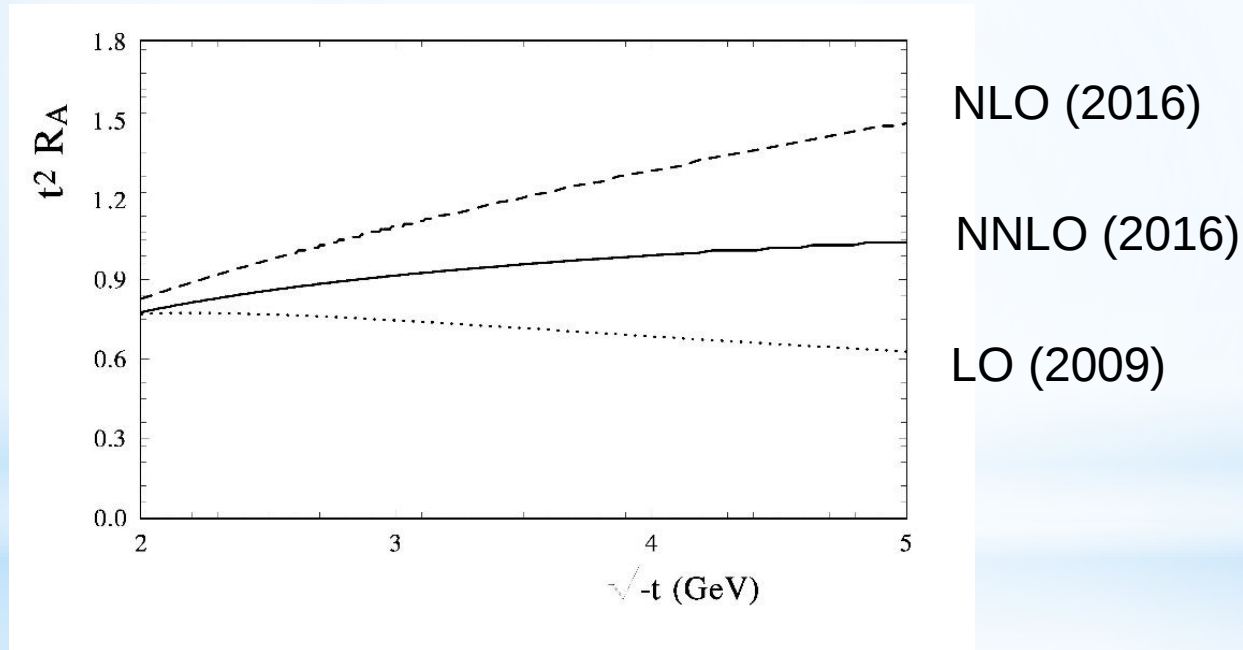
$$1/N_q = (1 + c_q \frac{a_q}{1+a_q+b_q}) B(a_q, b_q + 1);$$

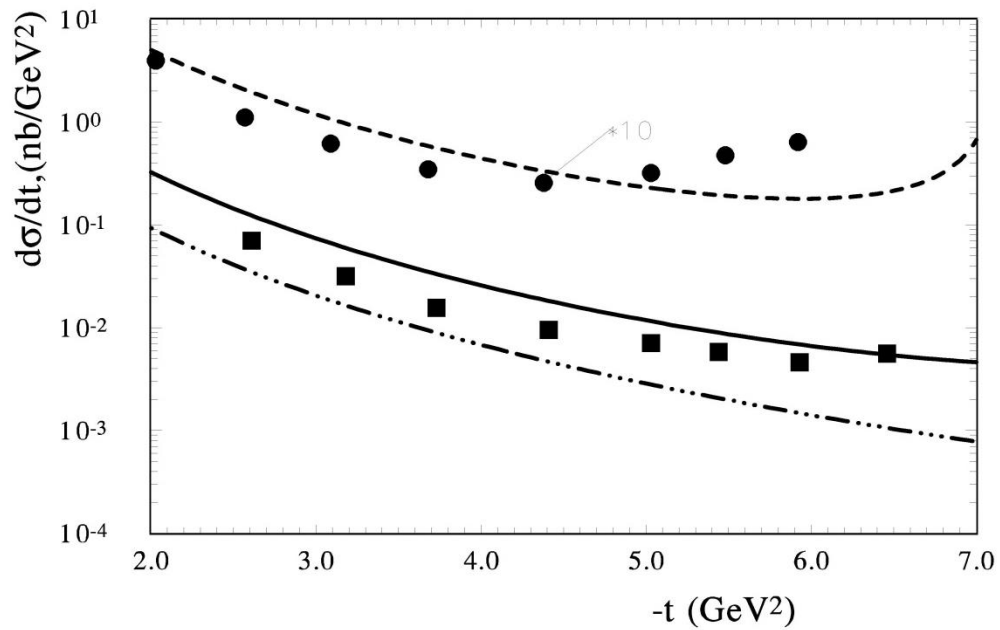
$$\text{Euler function } B(a,b) = \Gamma(a)\Gamma(b)/\Gamma(a+b) = \int_0^1 t^{a-1} (1-t)^{b-1} dt;$$

$$SU(3) \text{ flavor symmetry } \Delta \bar{q} \equiv \Delta \bar{u} = \Delta \bar{d} = \Delta \bar{s} = \Delta s;$$

$$R_A(t) = \sum_q e_q^2 \int \frac{dx}{x} dx \tilde{H}^q(x, \xi = 0, t)$$

$$= \frac{dx}{x} \left\{ \Delta u^e(x) \exp\left[ 2\alpha_1 \left( \frac{(1-x)^{p_1}}{(x_0+x)^{p_2}} t \right) \right] + \Delta d^e(x) \exp\left[ 2\alpha_1 \left( \frac{(1-x)^{p_1(*k_d)}}{(x_0+x)^{p_2}} t \right) \right] \right\}$$



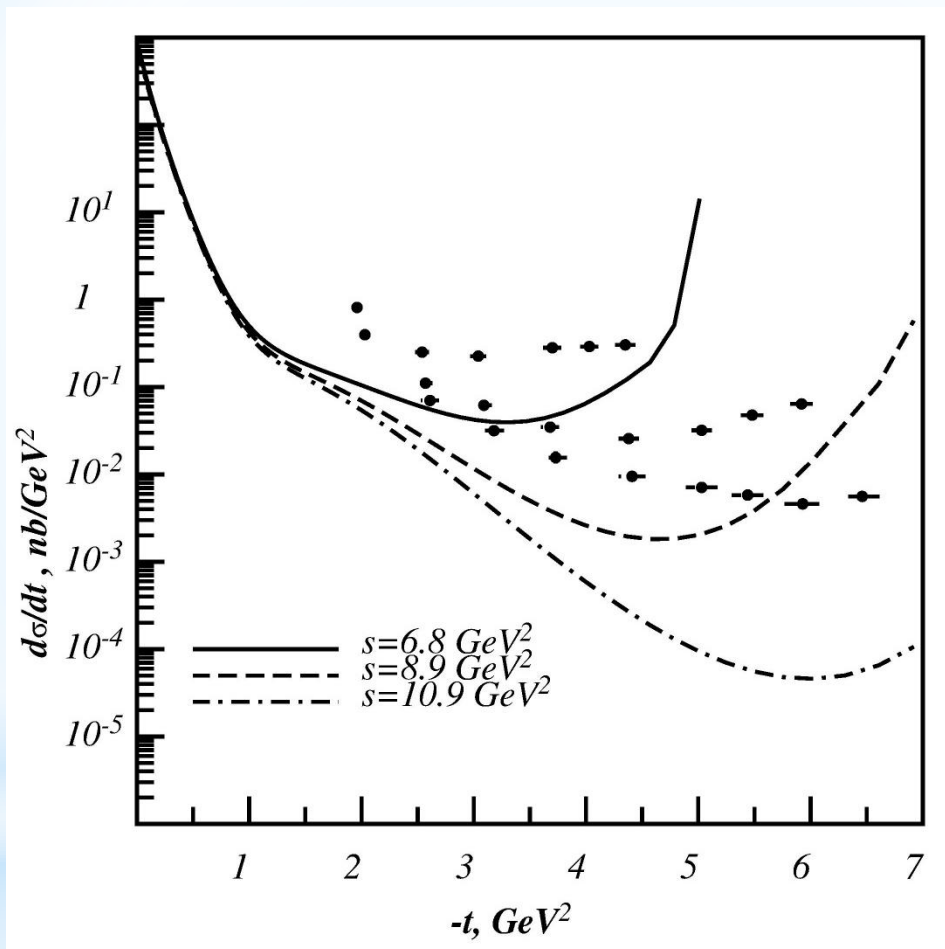


\*10  $S = 8.7 \text{ GeV}^2$

$S = 10.9 \text{ GeV}^2$

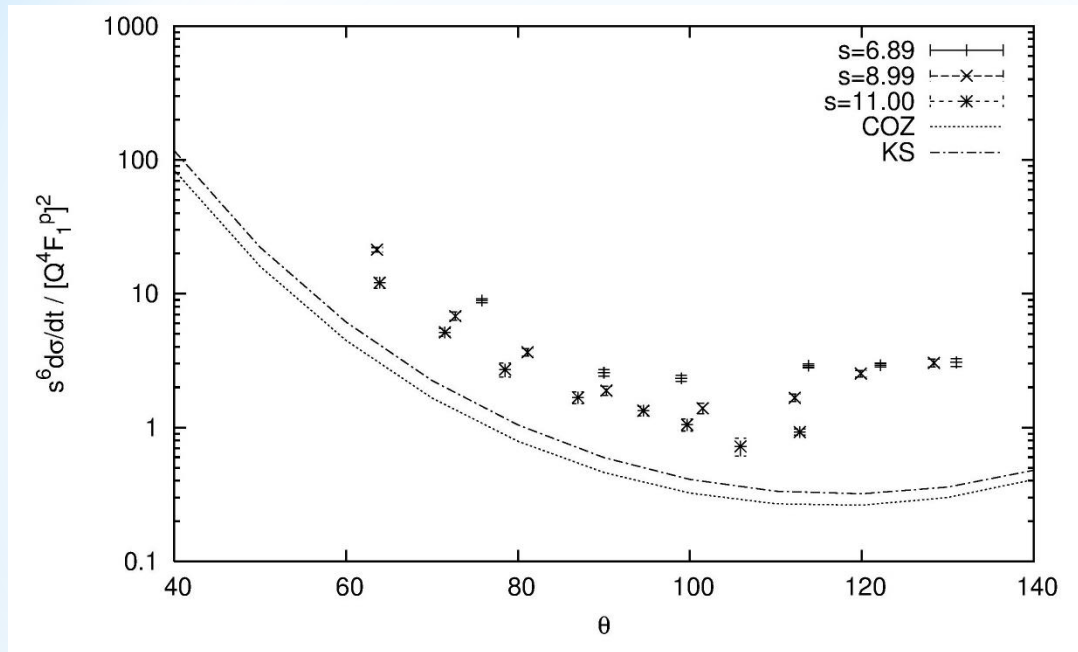
$S = 20. \text{ GeV}^2$

B. Kopeliovich,

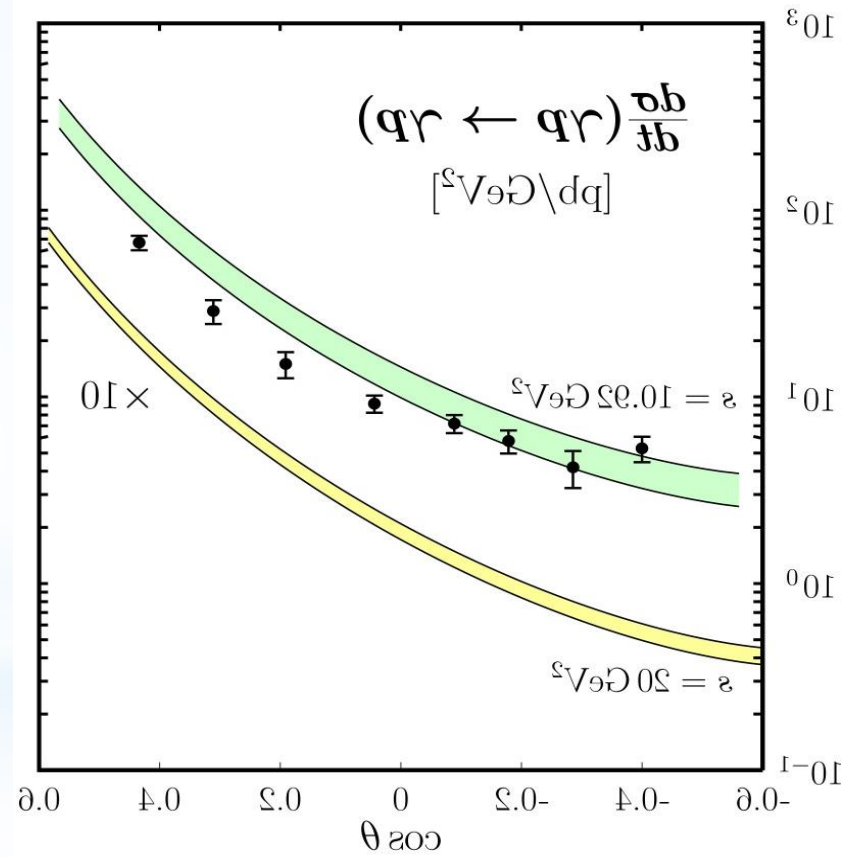
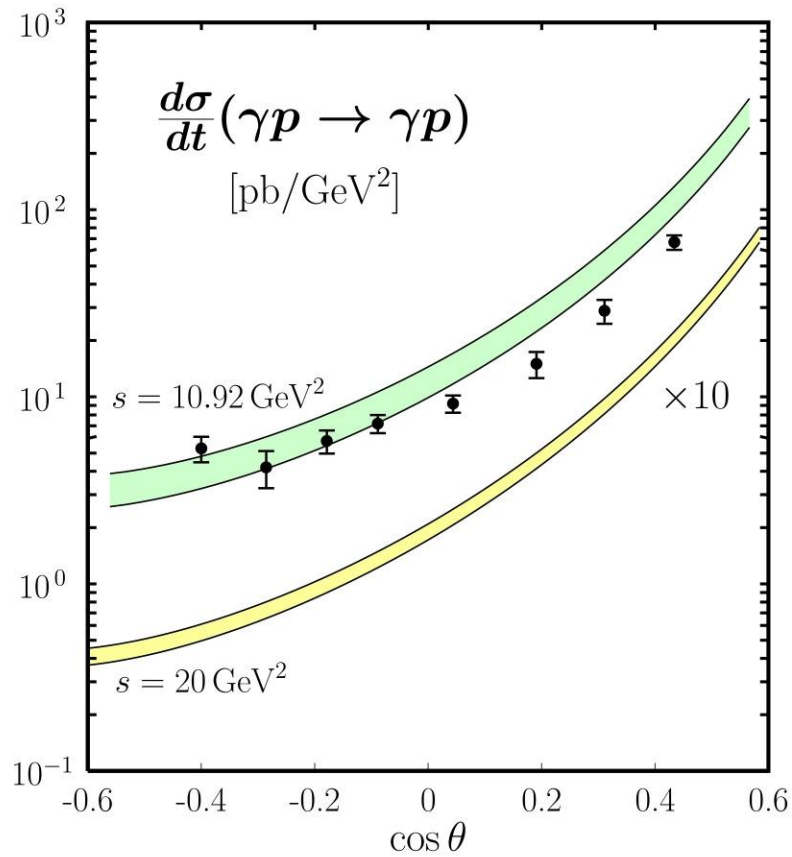


r. Thomson, A. Pang, Ch-R. Ji,

Phys.ReV., D73 (2006)



Diehl, P. Kroll (2013)



$$pp \rightarrow pp$$

General Parton Distributions -GPDs

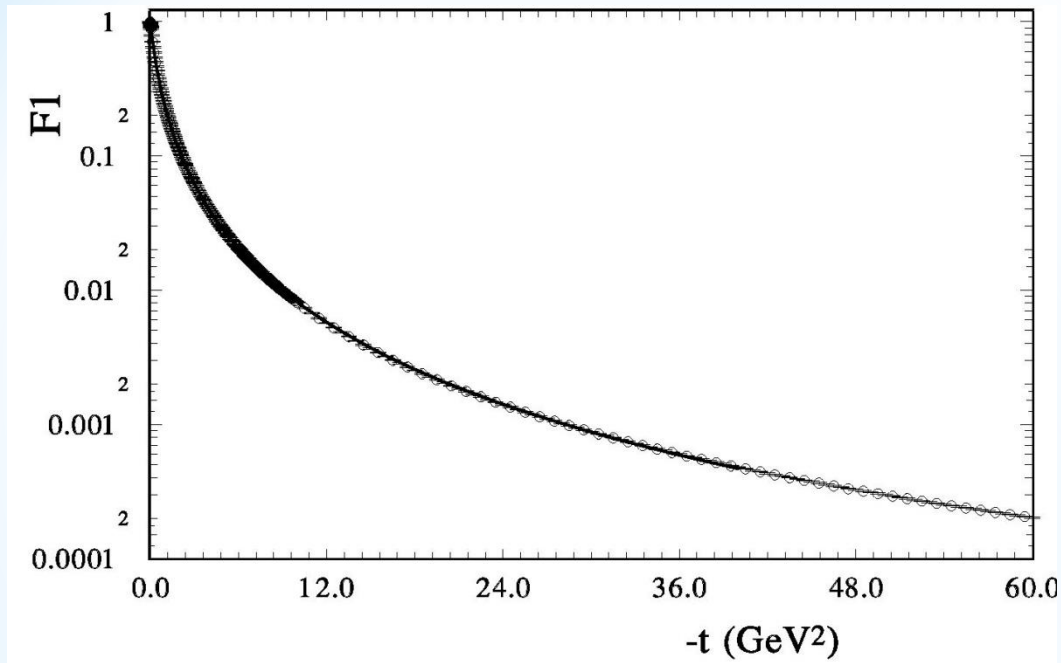
Electromagnetic  
form factors  
(charge  
distribution)

Gravitation  
form factors  
(matter distribution)

$$F_1^D(t) = \frac{4M_p^2 - t \mu_p}{4M_p^2 - t} G_D(t);$$

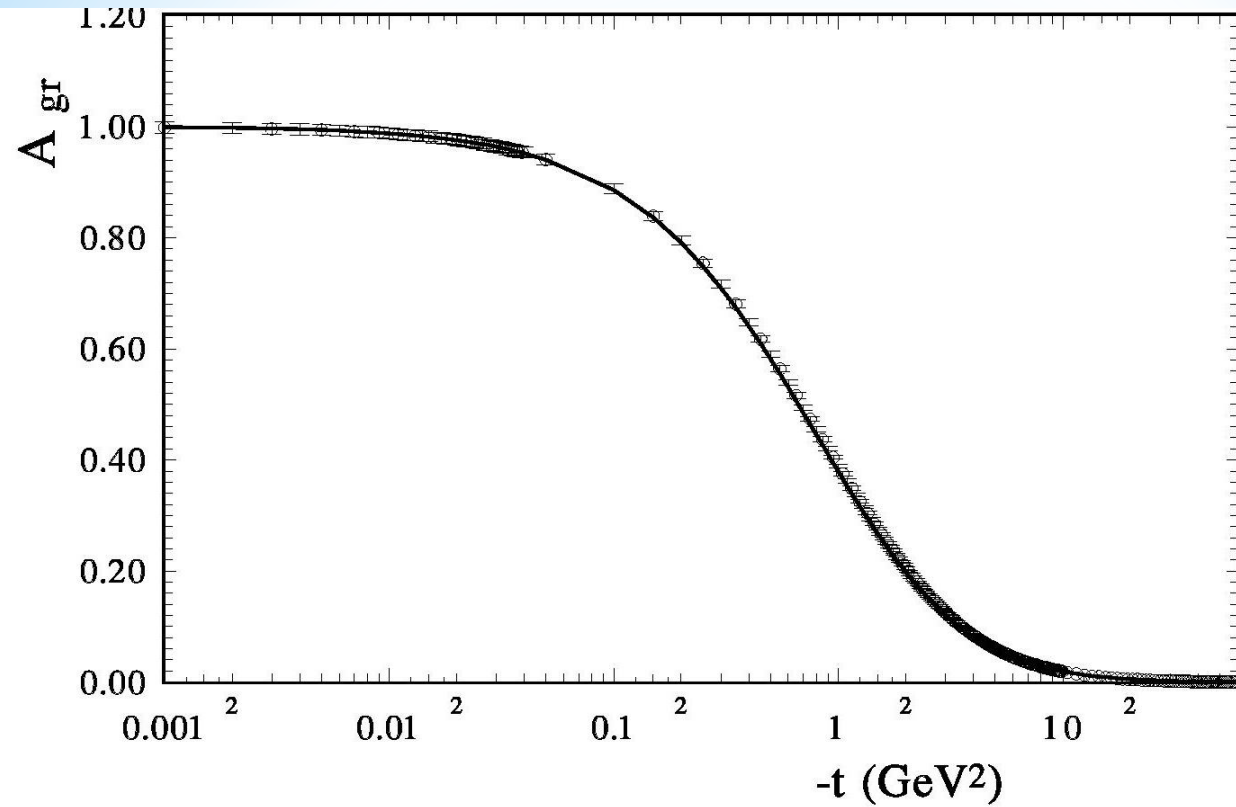
$$G_D(t) = \frac{\Lambda^4}{(\Lambda^2 - t)^2};$$

$$G_A(t) = \frac{\Lambda_A^4}{(\Lambda_A^2 - t)^2};$$



$$G_{em}(t) = \frac{\Lambda_{em}^4}{(\Lambda_{em}^2 + k_1 q - t + k_2 q^3)^2};$$

$$\Lambda_{em}^2 = 0.775 \text{ GeV}^2; k_1 = 0.06 \text{ GeV}; k_2 = 0.08 \text{ GeV}^{-1};$$



$$G_A(t) = \frac{\Lambda_A^4}{(\Lambda_A^2 - t)^2};$$

$$\Lambda_A^2 = 1.6 \pm 0.05 \text{ GeV}^2;$$

# Elastic scattering amplitude

$$pp \rightarrow pp$$

$$p\bar{p} \rightarrow p\bar{p}$$

$$\frac{d\sigma}{dt} = 2\pi[|\Phi|_1^2 + |\Phi|_2^2 + |\Phi|_3^2 + |\Phi|_4^2 + 4|\Phi|_5^2]$$

$$\Phi_i(s,t) = \Phi_i^h(s,t) + \Phi_i^e(t) e^{i\alpha\varphi}$$

$$\varphi(s,t) = \mp [\gamma + \ln(B(s,t)|t|/2) + \nu_1 + \nu_2]$$

$\gamma = 0,577\dots$  ( the Euler constant )

$\nu_1$  and  $\nu_2$  are small correction terms

Extending of model (HEGS)

$$\hat{s} = s / s_0 e^{-i\pi/2};$$

$$9 \leq \sqrt{s} \leq 8000 \text{ GeV}; \quad 0.00037 < |t| < 15 \text{ GeV}^2; \quad s_0 = 4m_p^2.$$

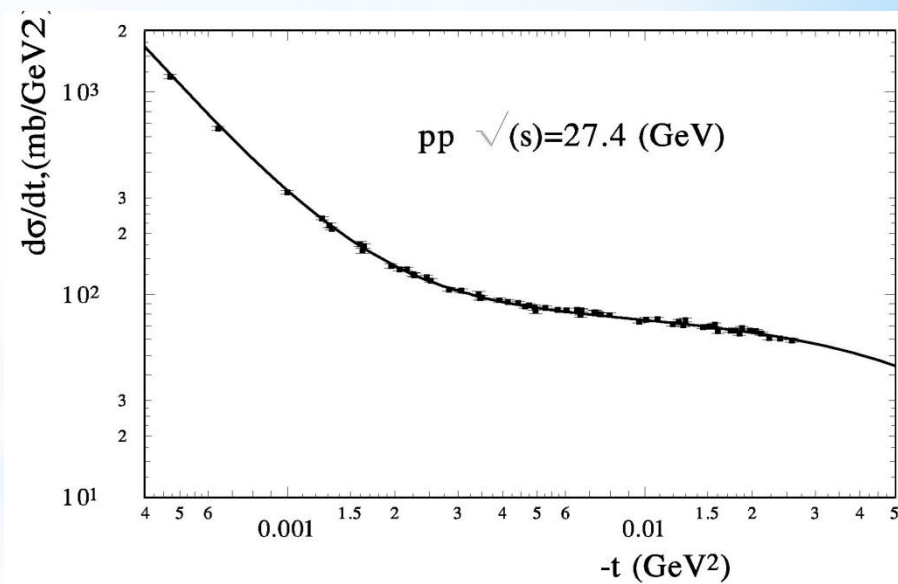
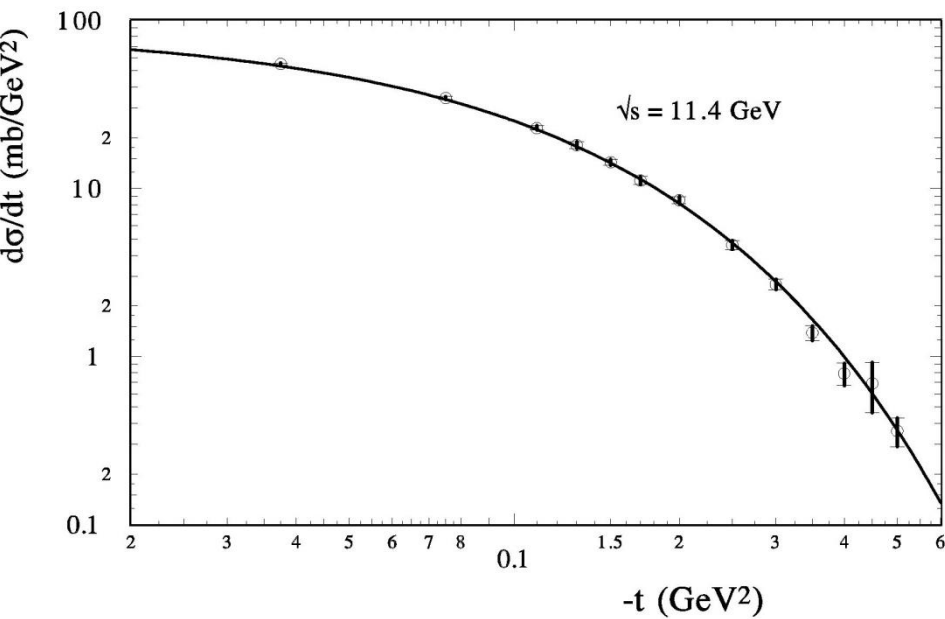
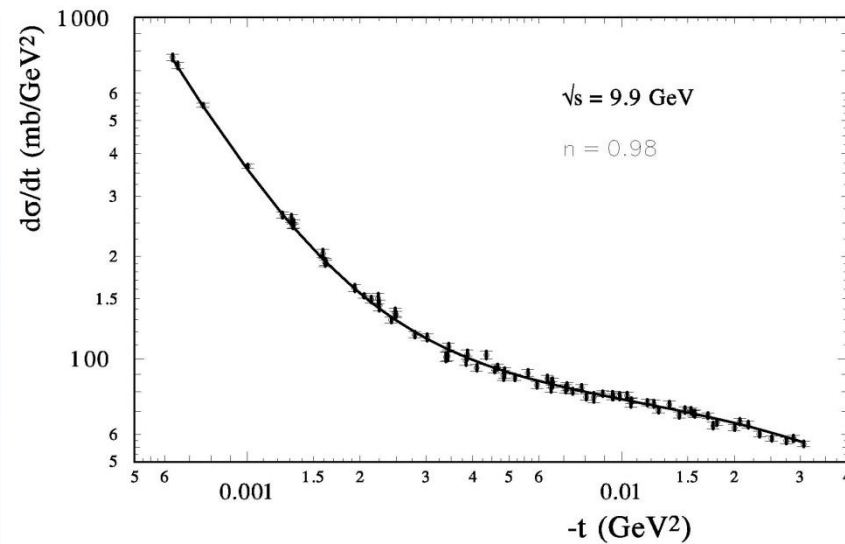
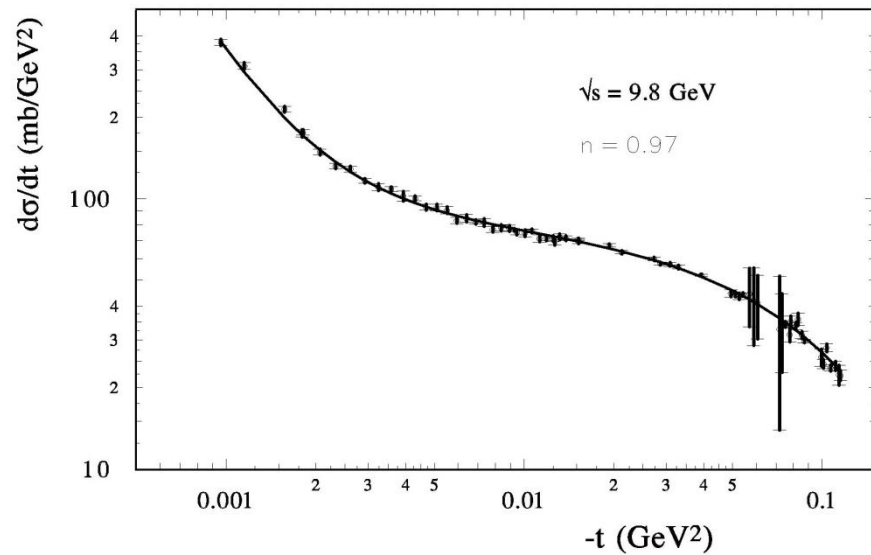
$$F_1^B(s, t) = h_2 G_{em}(t) (\hat{s})^{\Delta_1} e^{\alpha_1 t \ln(\hat{s})}; \quad F_3^B(s, t) = h_3 G_A(t)^2 (\hat{s})^{\Delta_1} e^{\alpha_1/4 t \ln(\hat{s})};$$

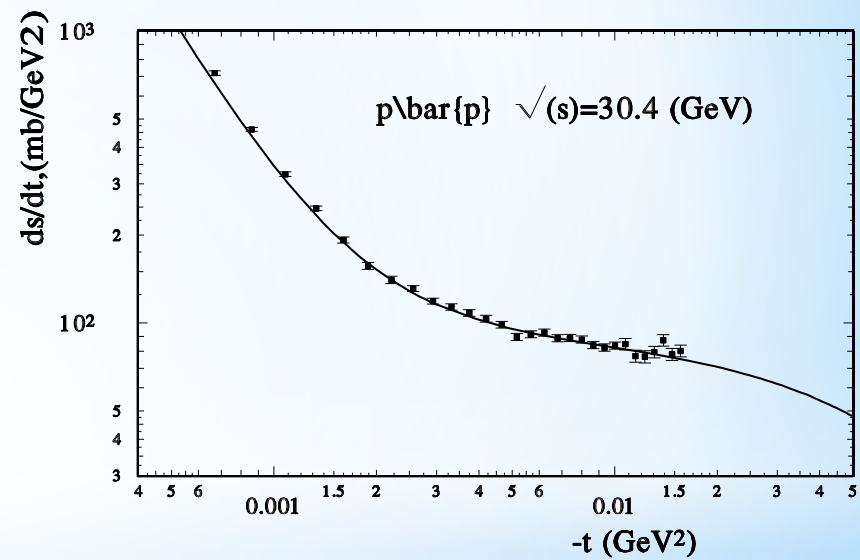
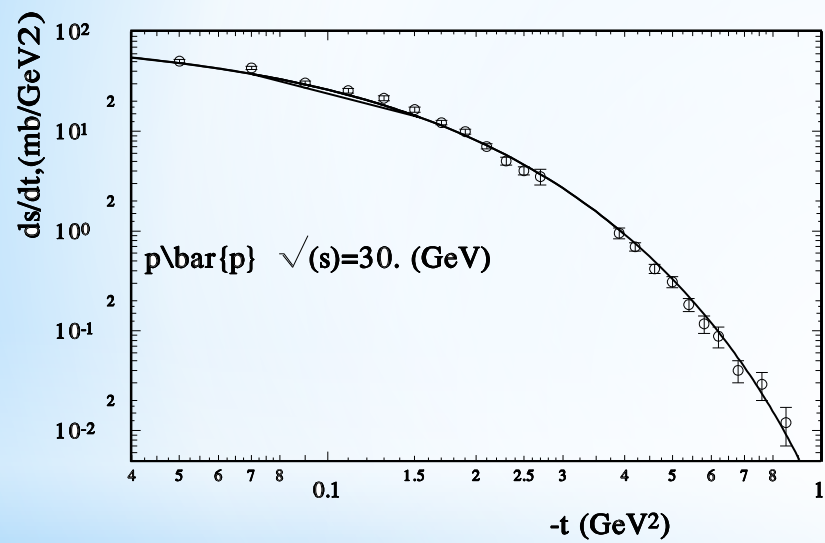
$$F^B(\hat{s}, t) = F_2^B(\hat{s}, t)(1 + R_1 / \sqrt{\hat{s}}) + F_3^B(\hat{s}, t)(1 + R_2 / \sqrt{\hat{s}}) + F_{odd}^B(s, t);$$

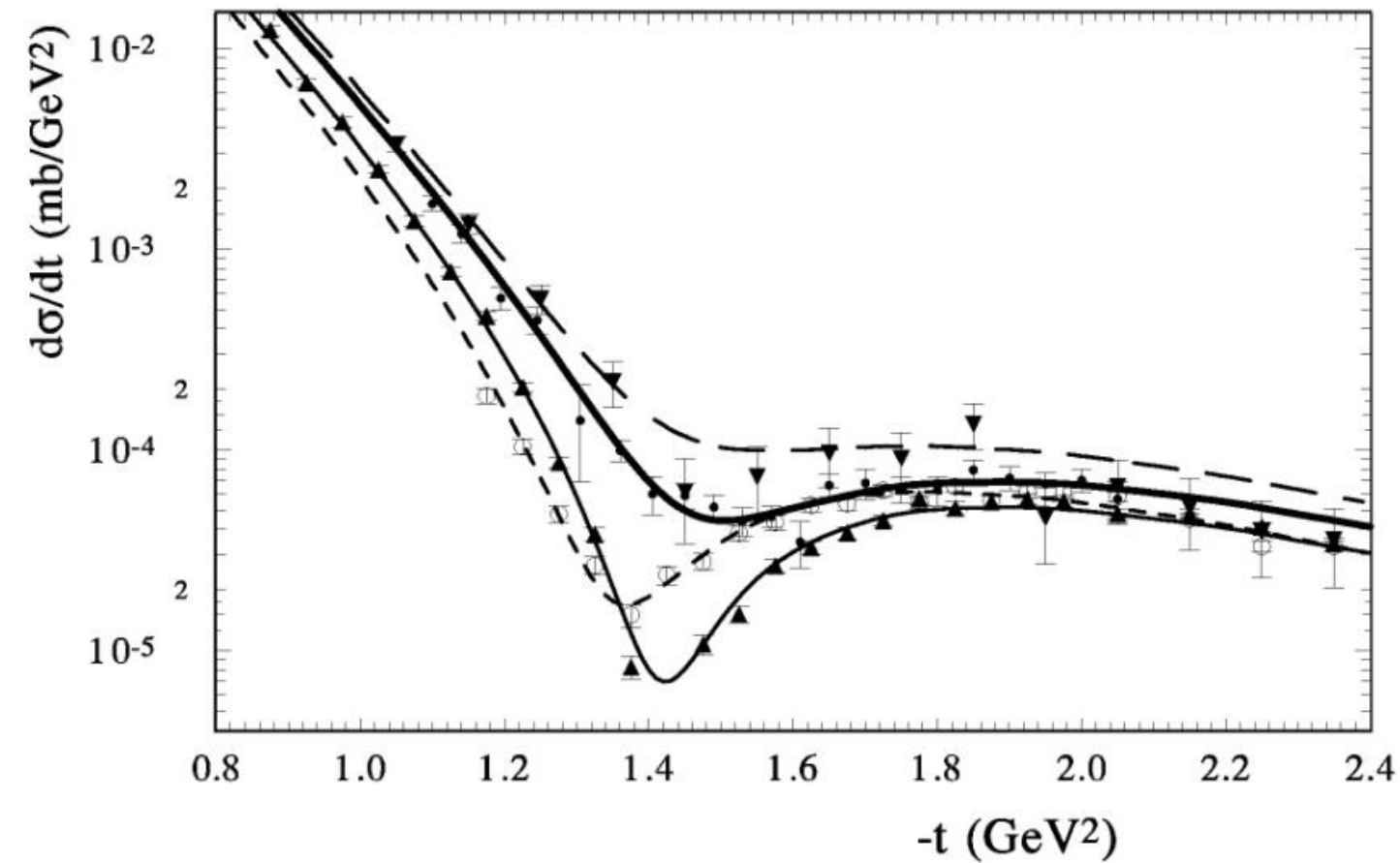
$$F_{Odd}^B(s, t) = h_{Odd} G_A(t)^2 (\hat{s})^{\Delta_1} \frac{t}{1 - r_o^2 t} e^{\alpha_1/4 t \ln(\hat{s})};$$

$$B(t) = (\alpha_1 + k_0 q e^{k_0 t \ln \hat{s}}) \ln \hat{s}.$$

$$F^{+-}(s, t) = h_{sf} q^3 G_{em}(t)^2;$$

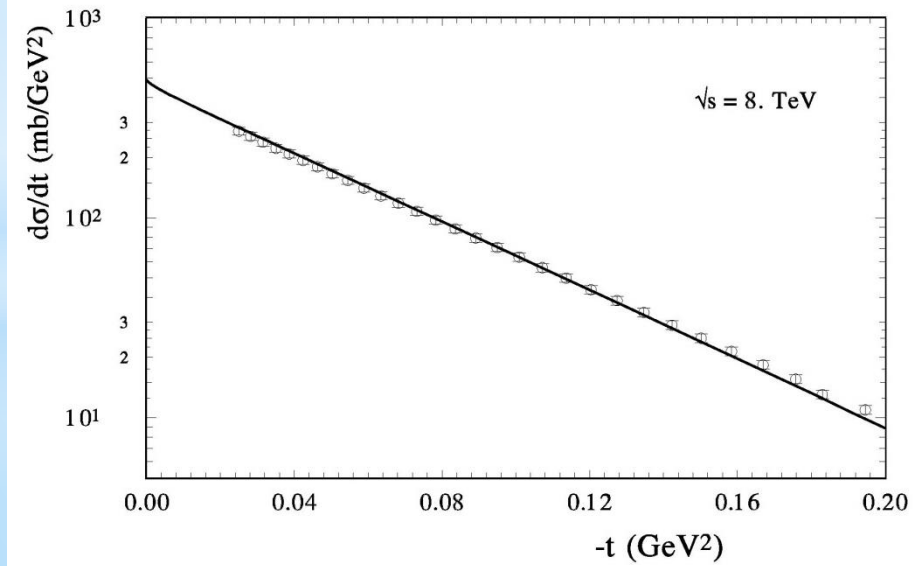
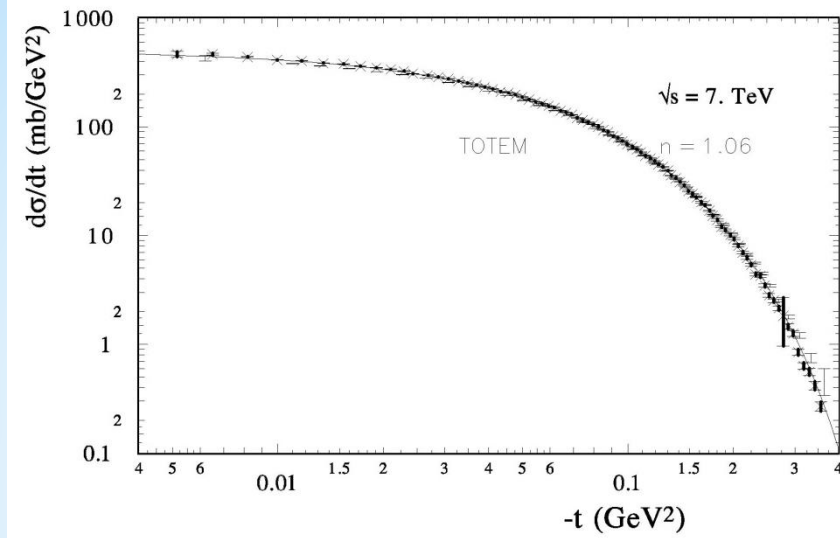


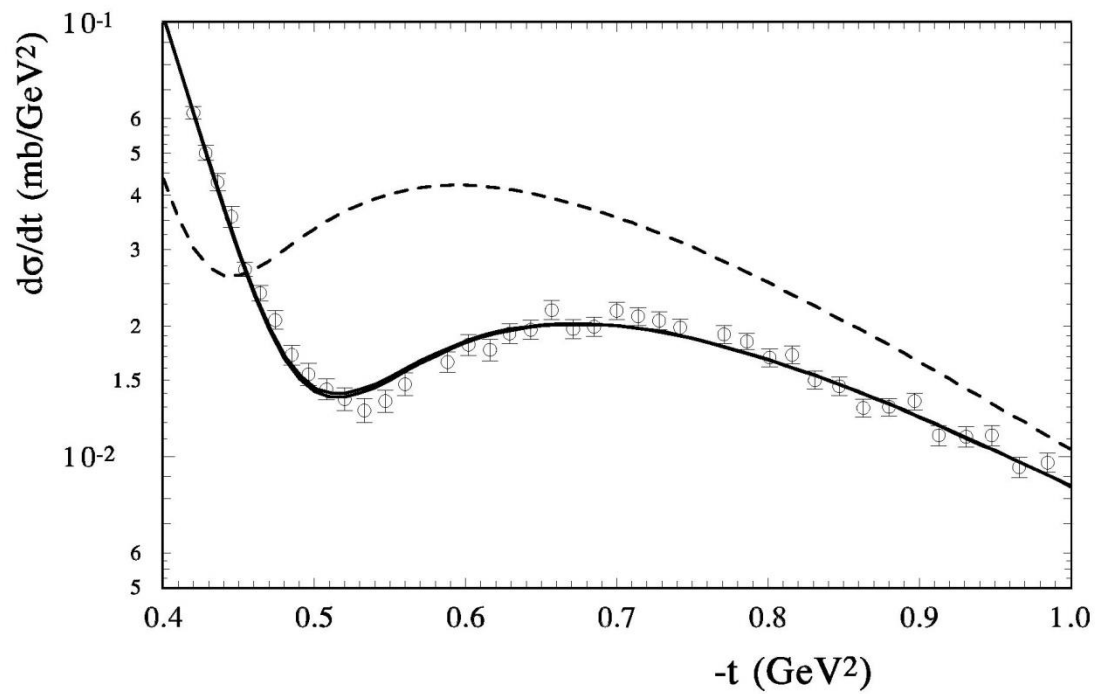
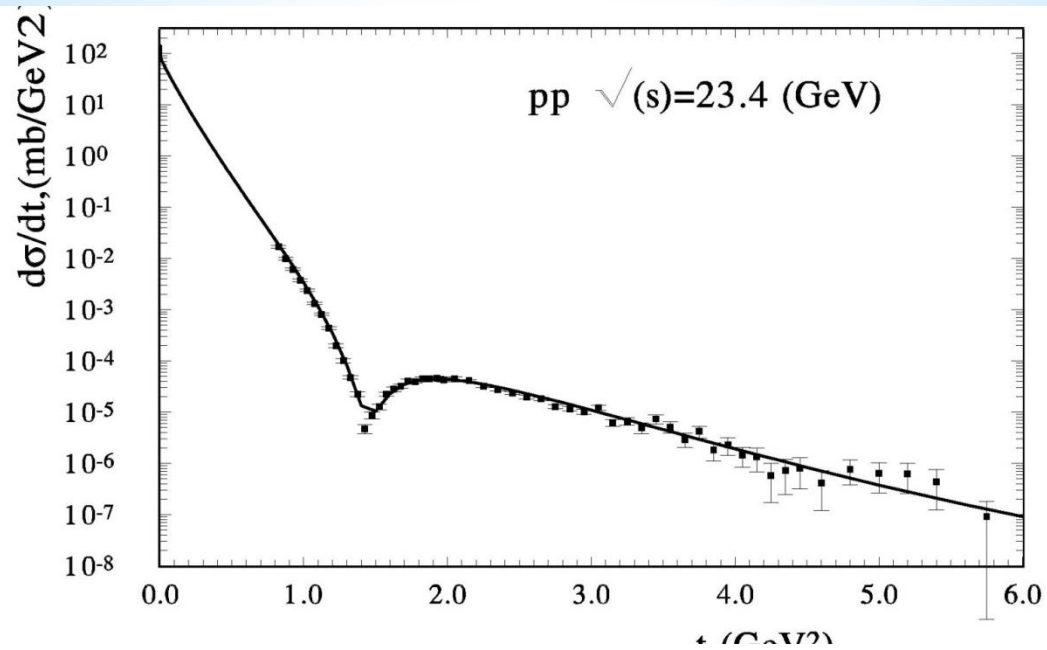




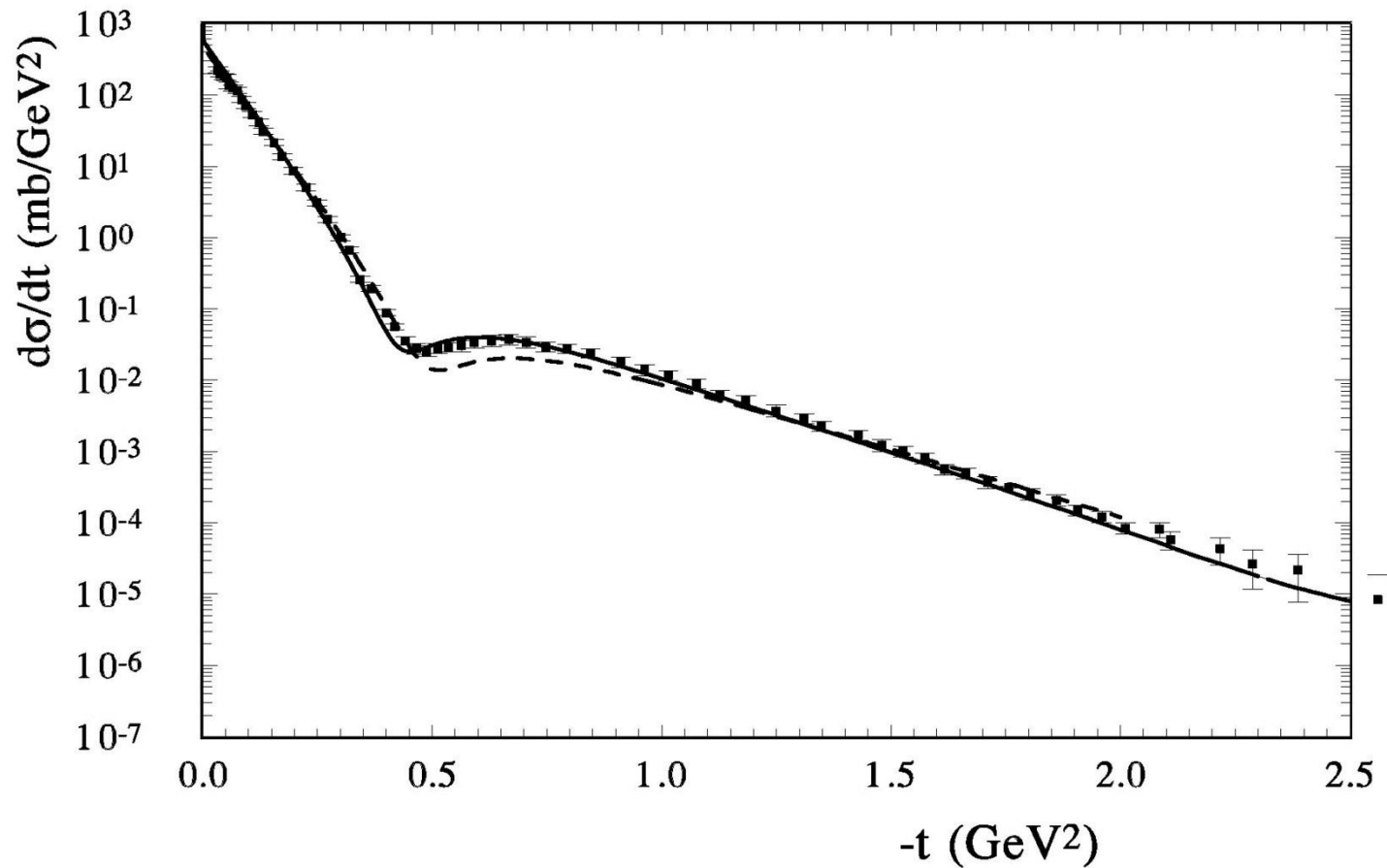
$\sqrt{s} = 9.8 \text{ GeV}$   
 $\sqrt{s} = 13.7 \text{ GeV}$   
 $\sqrt{s} = 30.4 \text{ GeV}$   
 $\sqrt{s} = 44.8 \text{ GeV}$

# TOTEM 7TeV





13 TeV (line and points) and 7 TeV – dashed line



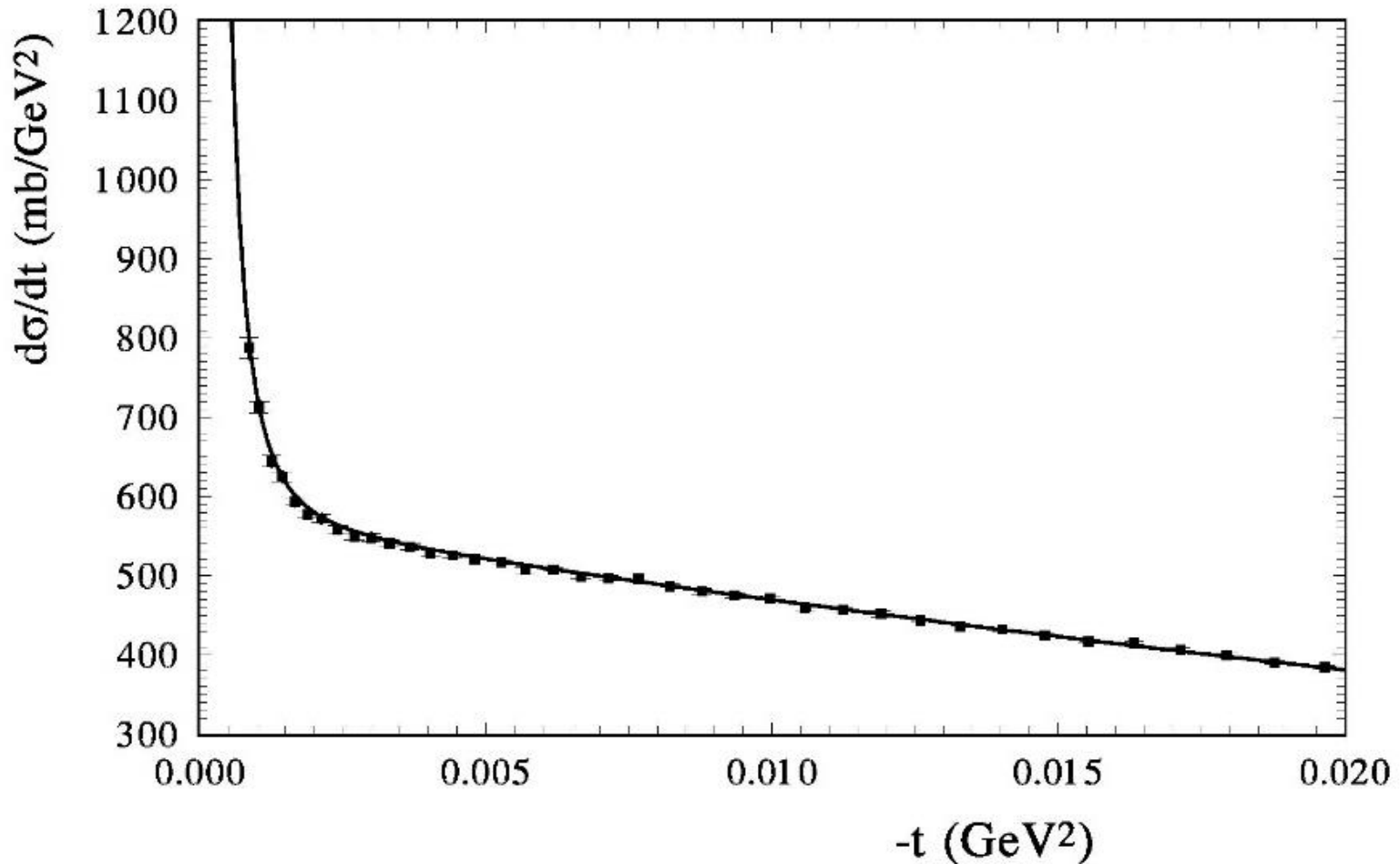
( The normalization of the 13 TeV data on the model calculations)

13 TeV (TOTEM) - (Mario Deile “EDS(Blois)-17, Prague, June 26-30, 2017 )  
+ HEGS model predictions O.V. S. Nucl.Phys. A,959 (2017); arxiv: 1609.08847

$t$  [0.0008 – 0.019]

$n=0.9$

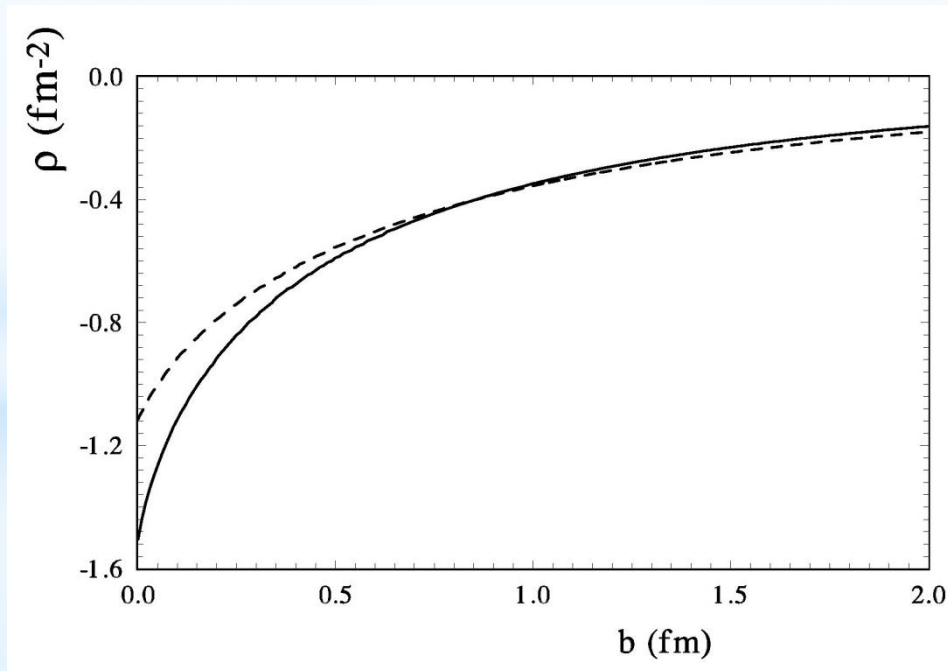
$\sqrt{s} = 13 \text{ TeV}, \beta^* = 2500 \text{ m}$



$$\rho(\vec{b}) = \sum_q e_q \frac{1}{2\pi} \int_0^\infty d^2 q \exp[i\vec{q} \cdot \vec{b}] \int_0^1 dx H_q(x, t, \xi=0).$$

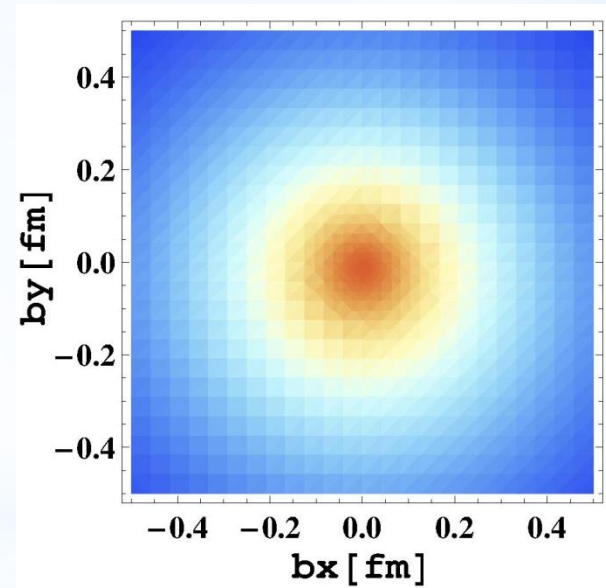
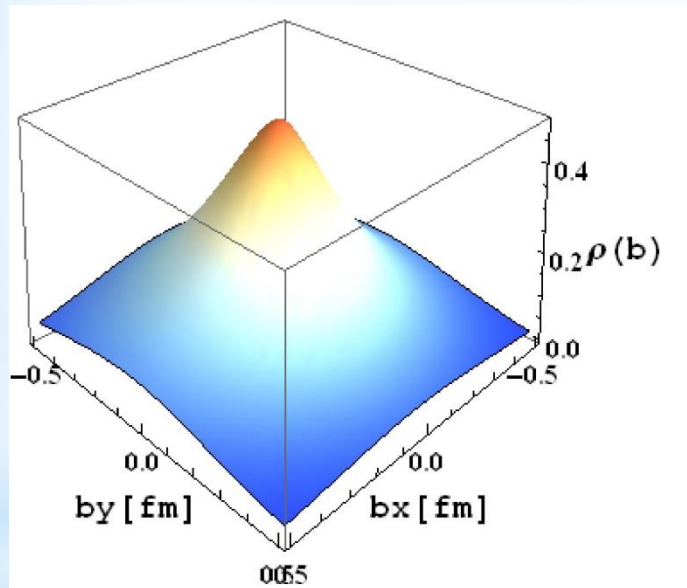
$$\rho_{G_E}(\vec{b}) = \frac{1}{2\pi} \int_0^\infty q dq J_0(qb) G_E(q^2)$$

The contribution in the density of the neutron  
u-quark (hard line) and (- d) – quark (dashed line)



## Quark transverse charge density of the proton

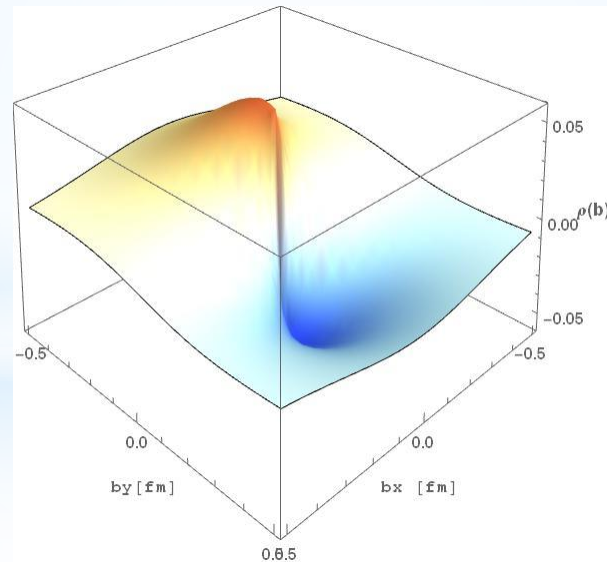
$$\rho_T^N(\vec{b}) = \rho_0^N(\vec{b}) + \sin(\phi) \frac{1}{2\pi} \int_0^\infty dq \frac{q^2}{2M_N} J_1(qb) F_2(q^2)$$

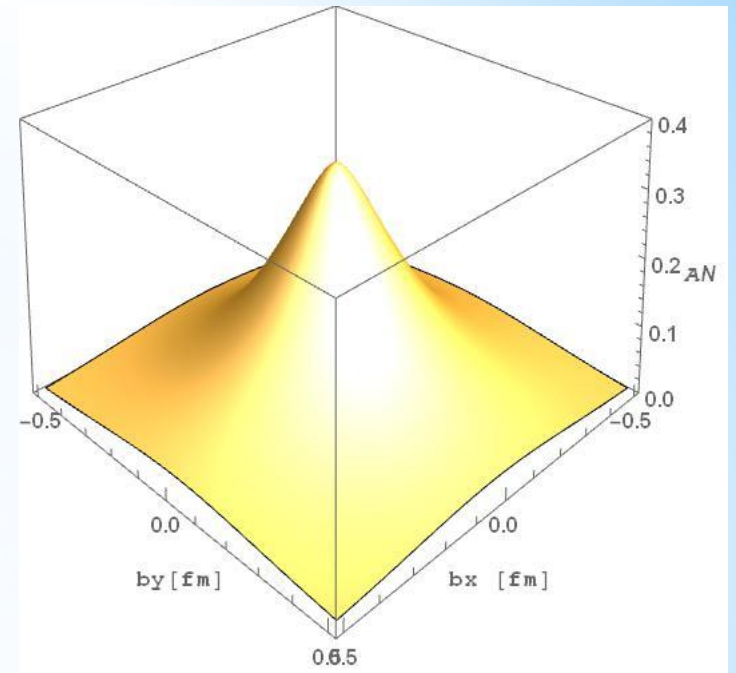
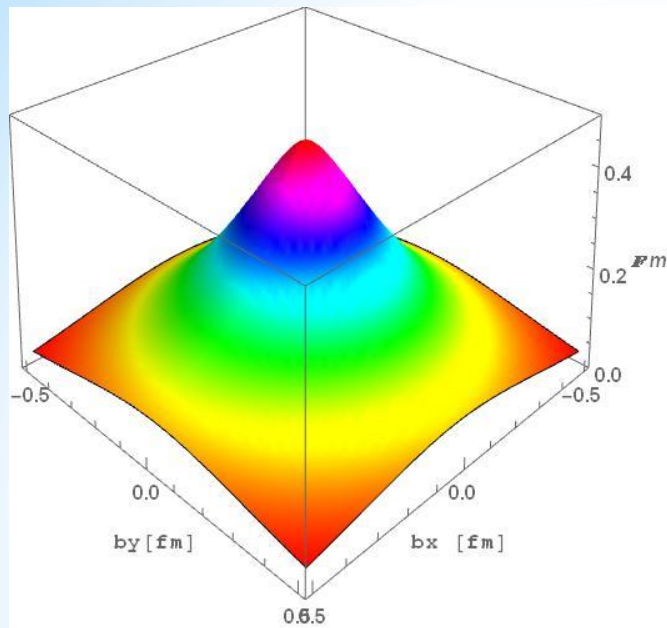


Angular-dependent contribution to quark transverse density of the proton

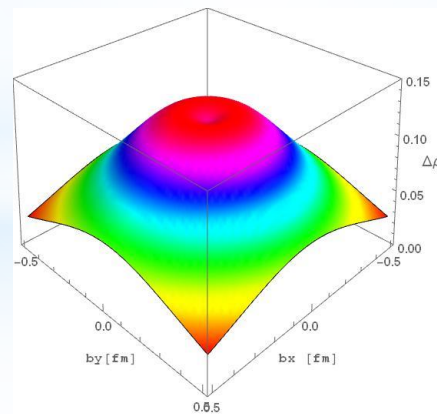
$$\Delta\rho(\vec{b}) = \rho_T^p(\vec{b}) - \rho_0^p(\vec{b});$$

$$\sin(\phi) \frac{1}{2\pi} \int_0^\infty dq \frac{q^2}{2M_N} J_1(qb) F_2(q^2)$$





$$\Delta\rho(\vec{b}) = F_1(\vec{b}) - A(\vec{b});$$



$$\langle r_{em}^2 \rangle \approx -\frac{6}{G(0)} \frac{dG}{dt} \approx \frac{1}{L_{em}^2}; \quad \langle r_{gr}^2 \rangle \approx -\frac{6}{A(0)} \frac{dA}{dt} \approx \frac{1}{L_{gr}^2};$$

$$L_{em}^2 = 0.71 \text{ GeV}^2; \quad L_{gr}^2 = 1.6 \text{ GeV}^2$$

$$\frac{r_{em}}{r_{gr}} \approx \sqrt{\frac{1/L_{em}^2}{1/L_{gr}^2}} \approx 1.5;$$

## Summary

- \* The **GPDs** reflect the basic properties of the hadron structure and gave some bridge between the many different reactions.
- The new form of the **t-dependence** of **GPDs** allow to obtain the different form factors, including Compton form factors, electromagnetic form factors, transition form factor, gravitomagnetic form factor.
- The our model **GPDs** leads to the well description of the **proton and neutron electromagnetic form factors** simultaneously.
- \* The compare the calculations and full row of the data shows the preference the “**Polarization**” case.

# Summary

- In result, the description of the **different** reaction based on **the same** representation of the hadron structure.
- Especially it is concern the **high energy elastic hadron scattering**
- \* The new High Energy Generalized Structure model (**HEGS**) gives the quantitatively description of the **elastic nucleon scattering** at high energy with only 6 fitting high energy parameters.

The predictions of the model based on the obtained **electromagnetic and gravitomagnetic form factors**, good coincide with the preliminary **data at 13 TeV**.

- The investigation of the nucleon structure show that the density of the matter more concentrated into nucleon than the charge density.
- \* The model open the new way to determine the true form of the **GPDs** and standard parton distributions

THANKS  
FOR YOUR  
ATTENTION