PARTICLES FASTER THAN LIGHT. IS IT POSSIBLE? IS IT DANGEROUS?

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OPERA:

$$(v-c)/c = [2.48 \pm 0.28 (stat) \pm 0.30 (sys)] \times 10^{-5}$$

MINOS:
$$(v-c)/c = [5.1 \pm 2.9] \times 10^{-5}$$

SN 1987A:
$$(v-c)/c < 2 \times 10^{-9}$$

Theoretical interpretation:

- A. Experiment is incorrect.
- B. Breaking of sacred principles.
- C. Normal quantum field theory, with some new neutrino interactions.

Faster than light possibilities:

- 1. Breaking of Lorenz symmetry. If CPT is broken in such a way that $m \neq \bar{m}$, then Lorenz is broken as well.
- 2. Breaking of spin-statistics relation leads to breaking of everything.
- 3. More modest, breaking of Lorenz but not other sacred principles.
- 4. Natural radiative correction to light propagation in gravitational field.

Drummond and Hathrell, 1980: radiative correction to light propagation in gravitational field (triangle graph)

$$L_{eff} = -rac{1}{4}F_{\mu
u}F^{\mu
u} + CR_{lphaeta\mu
u}F_{\mu
u}F^{lphaeta}$$

where $C = -\alpha/(360\pi m_e^2)$. C is divergent at $m_e = 0$.

There are also $RF_{\mu\nu}F^{\mu\nu}$ and $R_{\alpha\beta}F^{\mu\alpha}F^{\beta}_{\mu}$ terms, but they are absent in vacuum.

$$D_{\mu}\left[F_{
u}^{\mu}-4CR_{
ulphaeta}^{\mu}F^{lphaeta}
ight]=0$$

Characteristics of the Maxwell equations are modified so that one of light polarization propagates inside the cone, the other propagates outside the cone! Light propagates faster than light.

Quantum corrections to light propagation in external electric or magnetic field (Heisenberg-Euler): both polarizations are inside the cone.

Heisenberg-Euler correction to refrac-

Heisenberg-Euler correction to refraction index vanishes at $\omega \to \infty$

DH-correction does not vanish at $\omega \to \infty$! It leads to $n(\infty) < 1$.

Group velocity is determined by $n(\omega)$ at some fixed ω and can be larger than c (anomalous dispersion).

Front velocity must be smaller than c, so $n(\infty) \geq 1$

DH: the effective Lagrangian is valid only at low ω (we will see that it is not so) but dispersion relations leads to $n(\infty) < n(0)$ (we will see that it is not so too).

$$n(\omega) = n(0) + rac{2\omega}{\pi} \int rac{d\omega \, \mathcal{I}m \, n(\omega')}{\omega'(\omega' - \omega)}$$
 Thus if $\mathcal{I}m \, n(\omega) \geq 0, \, n(\infty) < n(0).$

However, $\mathcal{I}mn$ may be negative due to wave focusing in curved space-time:

$$\mathcal{I}m\,n=\lambda_s R_{1230}/2\omega^2$$

(AD, Khriplovich, 1983). In 2007 Shore made the same conclusion because of possible particle production but the effect seems to be negligible.

The DH correction to the refraction index is valid at any ω , because the $\gamma\gamma$ -graviton vertex is a function of only three variables k_1^2 , k_2^2 and q^2 and for on-mass-shell photons depends only on momentum transfer to gravitational field, Khriplovich, 1994.

The Heisenberg-Euler correction is 4leg amplitude and drops with rising photon frequency, ω .

The photon-photon scattering or photon scattering in external electromagnetic field drops down with energy.

Possible higher order corrections in electromagnetic interactions: could higher powers of α be compensated by a rise of the amplitude with the photon energy, ω ?

Negative, because of the known renormalizability of QED in external gravitational field.

Higher order in external gravitational field. The amplitude F^2R^n might contain derivatives ∂F which gives some factors proportional to ω , but power counting and renormalizability demand that the amplitudes are normalized to photon energy and not to electron mass in complete analogy to photon scattering in electromagnetic field.

Higher orders in virtual graviton exchange (quantum gravity) may contain terms of the type:

$$C_g lpha(\partial F)(\partial F)R/m_{Pl}^2.$$

Constant C_g is small but at $\omega > m_{Pl}$ this correction can be large.

However, if there is renormalizable quantum gravity (super-strings, branes...), the corrections must be small.

Recent criticism:

1. Hollowood, Shore claimed: "..novel non-analytical behavior due to vacuum polarization, which invalidates Kramers-Kronig dispersion relation." because of generic focusing of geodesics. A new non-perturbative singularity in refraction index in the complex ω plane.

2. Dubovsky, Nicolis, Trincherini, Villadoro: classical theory does not admit superluminous propagation. Quantum field theory respects general principles of classical theory, if there are no quantum anomalies. "Anomalies arise due to UV effects and exhibit themselves as localized terms in position space" and cannot influence spacelike separated commutators.

AD, Zakharov, 1970: anomalies are equally infrared phenomenon and the anomalous amplitude is infrared singular, i.e. long-ranged. E.g. the vertex VVA has $1/q^2$ -singularity. Imaginary part of the amplitude is $\sim m^2/q^4$ and vanishes for m=0, but real part is $\sim 1/q^2 \neq 0$ if m=0.

The same is known to be true for the energy-momentum tensor.

Imaginary part of the triangle diagram:

$$\begin{split} &\mathcal{I} m A_{\alpha\beta\mu\nu} = -\frac{e^2}{8} \int d\tau_2 Tr \left\{ (R_{\mu}\gamma_{\nu} + R_{\nu}\gamma_{\mu}) \right. \\ &\left[\frac{1}{p_1 k_1} (\not p_2 - m) \gamma_{\beta} (\not p_1 - \not k_1 + m) \gamma_{\alpha} (\not p_1 + m) \right. \\ &\left. \frac{1}{p_1 k_2} (\not p_2 - m) \gamma_{\alpha} (\not p_1 - \not k_2 + m) \gamma_{\beta} (\not p_1 + m) \right] \right\} \end{split}$$

$$\mathcal{I}m\,C(q^2)=rac{2\pilpha m^2}{q^4} imes \ \left[6V-\left(3-V^2
ight)ln\left(rac{1+V}{1-V}
ight)
ight],$$
 where $V=\sqrt{1-4m^2/q^2}.$ $\mathcal{I}m\,C(q^2)=0 \,\, ext{for}\,\,m=0 \,\, ext{but} \ \mathcal{R}e\,C(q^2)
eq 0 \,\, ext{for}\,\,m=0.$

$$C(q^2) = rac{1}{\pi} \int_{4m^2}^{\infty} rac{dz}{z-q^2} \mathcal{I}m\,C(z)$$

Thus for small q^2 :

$$C(0)=rac{4\pilpha}{45m^2}.$$

Only acausal amplitude is purely anomalous, the other ones contain both anomalous and non-anomalous terms.

Is it possible to violate causality? There are reference frames in which the signal, which is causal in some other frame, looks acausal (AD, I. Novikov, 1998).

Special relativity, "normal" tachyons. Tachyon is emitted at (t_1, x_1) and registered at (t_2, x_2) :

$$t_2 - t_1 = (x_2 - x_1)/u > 0$$

Here u > 1 is the tachyon velocity. Causality is not violated. Go to another frame with velocity V:

$$x' = \gamma(x - Vt), \quad t' = \gamma(t - Vx),$$

where $\gamma = 1/\sqrt{1 - V^2}$.

In the new frame:

$$t_2' - t_1' = \gamma(t_2 - t_1)(1 - Vu)$$

Thus $u' = \infty$ for V = 1/u,

infinite energy for u = const > 1.

For V > 1/u, $t'_2 - t'_1 < 0$, i.e. tachyon propagates backward in time

Is it possible that in some reference frame the signal "returns" the the place of origin before it was emitted? YES!

Let us consider two tachyon sources, moving in opposite directions with velocity V. The first of them emits tachyon in direction of the other and at the moment when the second one received the signal it "shoot" back with another tachyon. If V = 1/u tachyons propagate with infinite velocity and the signal returns instantly. If V > 1/u, the signal returns before it was emitted.

Light propagation in GR.

Metric, e.g. Schwatzschild:

$$ds^2 = a^2(r)dt^2 - b^2(r)(dx^2 + dy^2 + dz^2)$$

where $r^2 = x^2 + y^2 + z^2$,
 $a^2 = (1 - r_g/4r)^2/(1 + r_g/4r)^2$, and
 $b^2 = (1 + r_g/4r)^4$. The explicit form
of a and b is not essential.

Change of coordinates: One of the spatial coordinate lines, l, is the trajectory of the superluminal photon in this metric and the coordinate running along this trajectory we denote as l. The other two, x_{\perp} , are orthogonal (in three-D sense). The metric along this trajectory, where $x_{\perp} = 0$, can be written in the form:

$$ds^2 = A^2(l)dt^2 - B^2(l)dl^2$$

New coordinate frame moving w.r.t. the original one with velocity V along l at large distances from the center. The corresponding coordinate transformation can be chosen as

$$t' = \gamma \left[t - Vl - Vf(l) \right]$$
 $l' = \gamma \left[l + f(l) - Vt \right]$

The function f(l) is chosen in such a way so that the crossed terms dt'dl' do not appear in the metric. It can be achieved if

$$f(l) = \int^l dl \left(rac{B}{A} - 1
ight)$$

In this moving frame the metric is:

$$ds^2 = A^2 \left(dt^{'2} - dl^{'2} \right)$$

where A should be substituted as a function of l' and t'.

The motion of the tachyonic photon in the original frame satisfies the condition:

$$u=rac{Bdl}{Adt}=1+\delta u$$

The overshoot of c:

$$\delta u = rac{lpha r_g
ho}{30 \pi r^4 m_e^2}$$

The effect may be large for small BHs with $r_g < 1/m_e$.

E.g. for $M_{BH}=10^{14}~{
m g}$ and $au\sim t_U,$ $r_g\approx 1/{
m GeV}.$

Possible implications: BH evaporation and information loss?