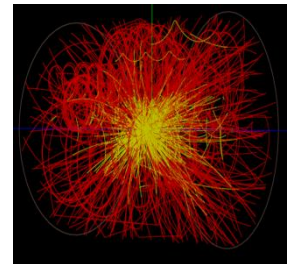
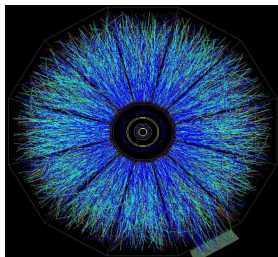


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**Beam Energy Scan at RHIC**  
&  
Search for Signatures of Phase Transition  
and Critical Point in  $z$ -scaling approach

M. Tokarev  
JINR, Dubna, Russia



in collaboration  
with Yu.Panebratsev, I.Zborovský, A.Kechechyan,  
A.Alakhverdyants, A.Aparin

# Contents

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- Introduction
- **BES** at RHIC
- **z**-Scaling (ideas, definitions, properties,...)
- Self-similarity of hadron production in **pp** & **AA**
- Energy loss in **pp** & **AA**
- Signatures of **phase transition** & **Critical Point**
- Conclusions

# Motivation

---

“Scaling” and “Universality” are concepts developed to understanding critical phenomena. Scaling means that systems near the critical points exhibiting self-similar properties are invariant under transformation of a scale. According to universality, quite different systems behave in a remarkably similar fashion near the respective critical points. Critical exponents are defined only by symmetry of interactions and dimension of the space.

H.Stanley, G.Barenblatt,...

Dense, strongly-coupled matter and an almost perfect liquid with partonic collectivity has been created in HIC at RHIC.

Experimental study of phase structure of QCD matter started ...

STAR, PHENIX, PHOBOS, BRAHMS - White papers - Nucl. Phys. A757 (2005)

USA-NSAC 2007 Long-range plan

# Self-similarity principle

- The self-similarity of a pattern means that it is similar to a part of itself.
- Physical description in terms of self-similarity parameters constructed as suitable combinations of some physical quantities.

## Self-similarity parameters ( $Re$ , $\Pi$ , $M$ ,...):

### Hydrodynamics

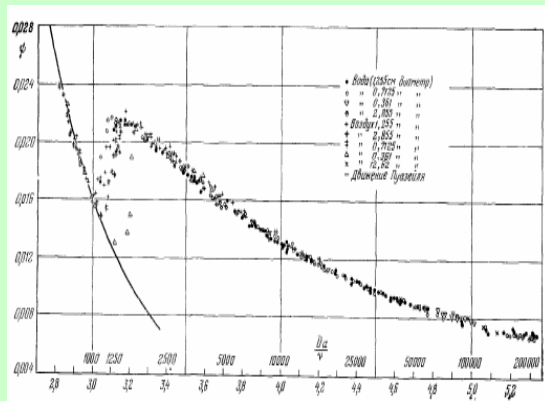
$$Re = dU\rho/\mu$$

d-diameter

U-velocity of the fluid

$\rho$ -density of the fluid

$\mu$ -viscosity of the fluid



### Point explosion

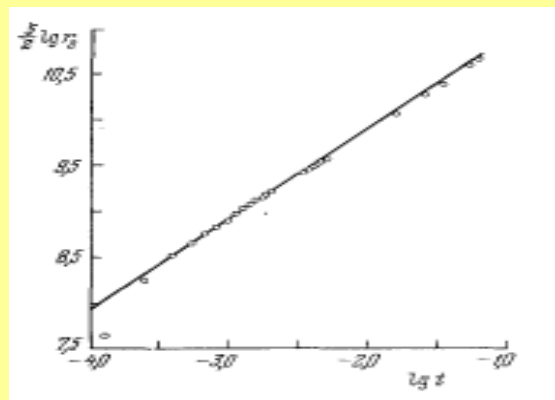
$$\Pi = r(Et^2/\rho)^{-1/5}$$

r-radius of the front wave

E-energy of the explosion

t-elapsed time

$\rho$ -density of the environment

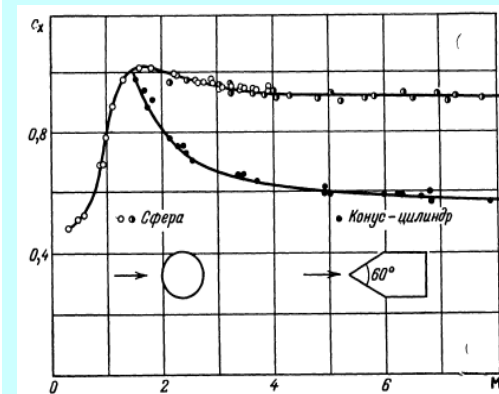


### Aerodynamics

$$M = v/c$$

v - velocity of medium

c - velocity of sound



# Thermodynamic potentials

Gibbs potential

$G(T,p)$

$$G(\lambda^{a_\varepsilon} \varepsilon, \lambda^{a_p} p) = \lambda G(\varepsilon, p)$$

Scaled temperature

Helmholtz potential

$F(T,V)$

$$F(\lambda^{a_\varepsilon} \varepsilon, \lambda^{a_v} V) = \lambda F(\varepsilon, V)$$

$$\varepsilon \equiv (T - T_c) / T_c$$

Internal energy

$U(S,V)$

$$U(\lambda^{a_s} S, \lambda^{a_v} V) = \lambda U(S, V)$$

Ferromagnetics

Enthalpy

$E(S,p)$

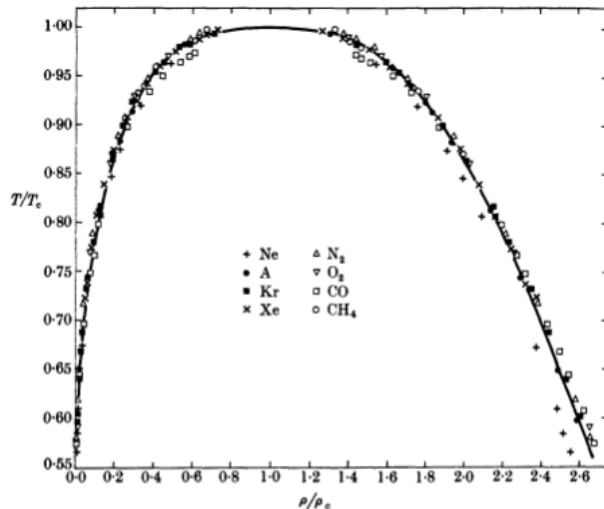
$$E(\lambda^{a_s} S, \lambda^{a_p} p) = \lambda E(S, p)$$

$$p \rightarrow H$$

$$V \rightarrow M$$

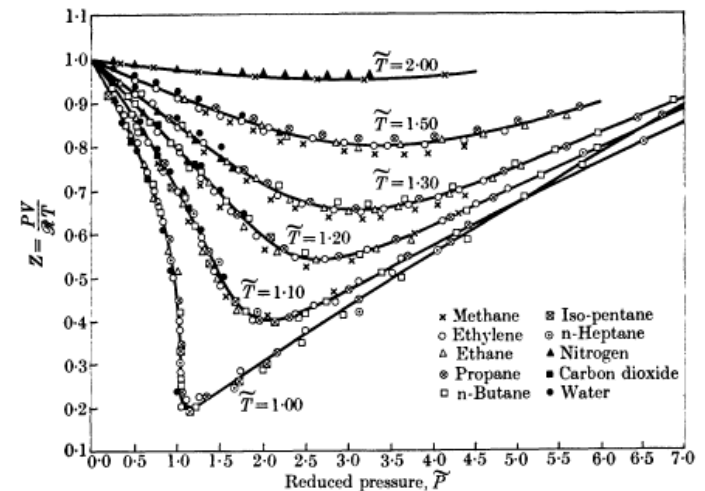
If one of the thermodynamic potentials is a generalized homogeneous function, then all thermodynamic potentials are GHPs.

Scaled density vs. scaled temperature



Data collapse

Compressibility vs. scaled pressure



All curves of this family can be “collapsed” onto a single curve.

# Critical exponents

## Fluid systems

$$c_V \sim |\varepsilon|^{-\alpha}$$

$$\rho_L - \rho_G \sim |\varepsilon|^\beta$$

$$K_T \sim |\varepsilon|^{-\gamma} \quad \text{compressibility}$$

$$K_T = -\frac{1}{V} \left( \frac{\partial^2 G}{\partial p^2} \right)_T$$

$$c_p = -T \left( \frac{\partial^2 G}{\partial T^2} \right)_p$$

$$\alpha_p = \frac{1}{V} \left( \frac{\partial^2 G}{\partial T \partial p} \right)_p$$

Scaled temperature

$$\varepsilon \equiv (T - T_c) / T_c$$

## Magnetic systems

$$c_H \sim |\varepsilon|^{-\alpha'}$$

$$M_H \sim |\varepsilon|^{\beta'}$$

$$\chi_T \sim |\varepsilon|^{-\gamma'}$$

$$c_H = -T \left( \frac{\partial^2 G}{\partial T^2} \right)_H$$

$$M_H = \left( \frac{\partial G}{\partial H} \right)_T$$

$$\chi_T = -\frac{1}{V} \left( \frac{\partial^2 G}{\partial H^2} \right)_T$$

specific heat

magnetization

susceptibility

## Dynamic properties

Transport of number of particles, energy, charge,...

## Transport coefficients

$$\Lambda(\text{thermal conductivity}) \sim \varepsilon^{-a}, \quad \varepsilon > 0$$

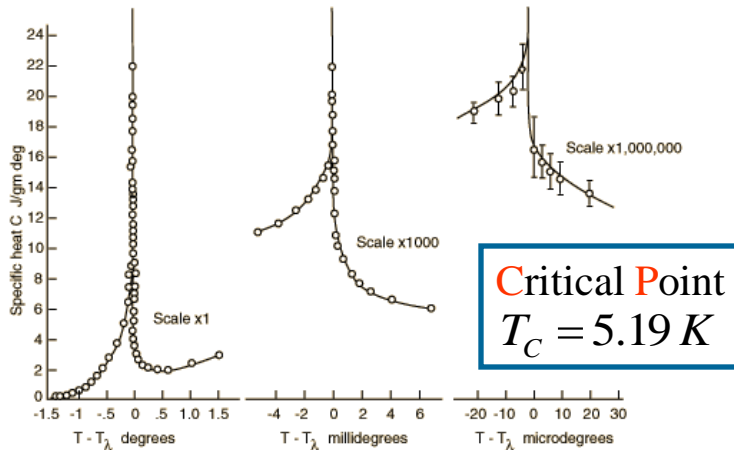
$$\eta(\text{shear viscosity}) \sim \varepsilon^{-b}, \quad \varepsilon > 0$$

$$\zeta(\text{bulk viscosity}) \sim \varepsilon^{-c}, \quad \varepsilon > 0$$

Critical exponents  $\alpha, \beta, \gamma, \delta, \dots$  define the behavior of physics quantities close to the **Critical Point**

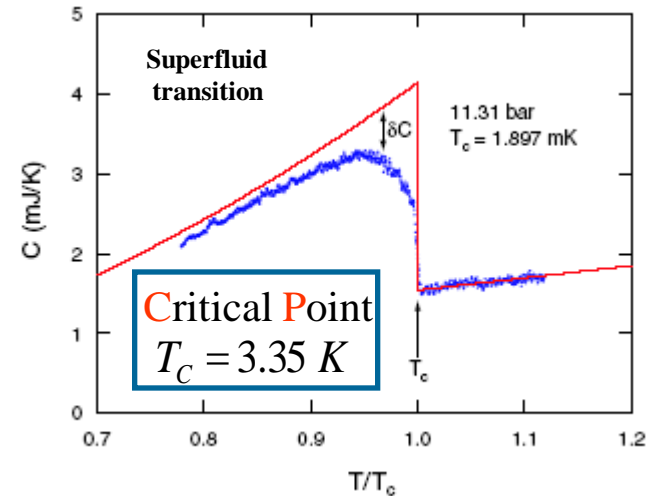
# Discontinuity of specific heat near a **Critical Point**

## Specific heat of liquid $^4\text{He}$



H.E. Stanley, 1971

## Heat capacity of liquid $^3\text{He}$



H. Choi et al., PRL 96, 125301 (2006)

- Near a critical point the singular part of thermo-dynamic potentials is a Generalized Homogeneous Function (GHF).
- The Gibbs potential  $G(\lambda^{a_\varepsilon} \varepsilon, \lambda^{a_p} p) = \lambda G(\varepsilon, p)$  is GHF of  $(\varepsilon, p)$ .

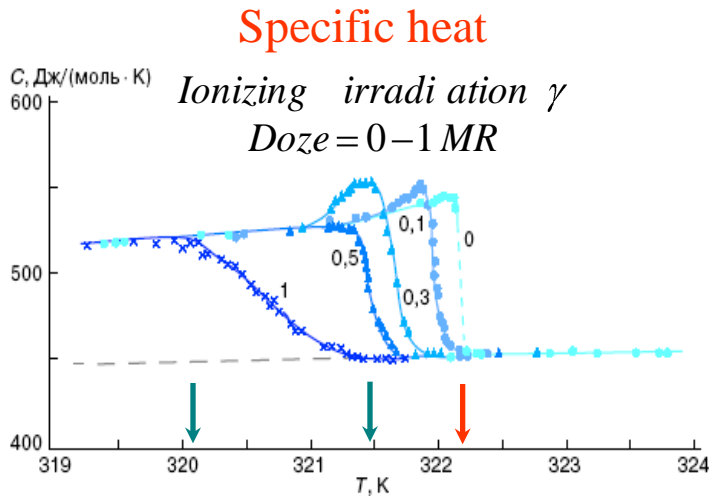
$$c_V \sim |\varepsilon|^{-\alpha} \quad \varepsilon \equiv (T - T_c) / T_c \quad c_V = -T(\partial^2 G / \partial T^2)_V$$

Critical exponents define the behavior of thermodynamical quantities close to the **Critical Point**.

# Defects influence upon phase transition

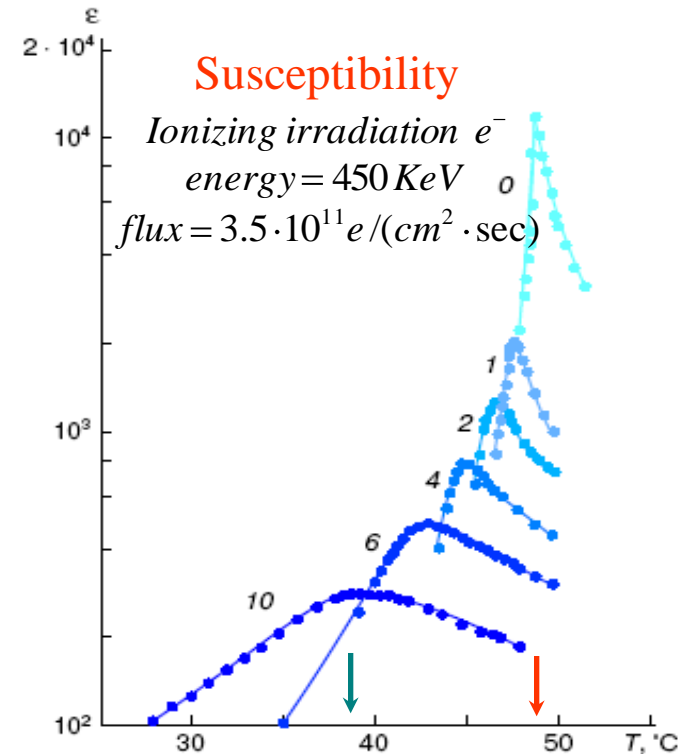
## Defects smear phase transitions

Ferroelectric crystal  
 $(CH_2NH_2COOH)_3 \cdot H_2SO_4$



**Critical Point**  
 $T_C = 49.2^0 C$

*Ferroelectric crystals*  
 $BaTiO_3$   
 $KNaC_4H_4O_6 \cdot 4H_2O$   
 $(CH_2NH_2COOH)_3 \cdot H_2SO_4$



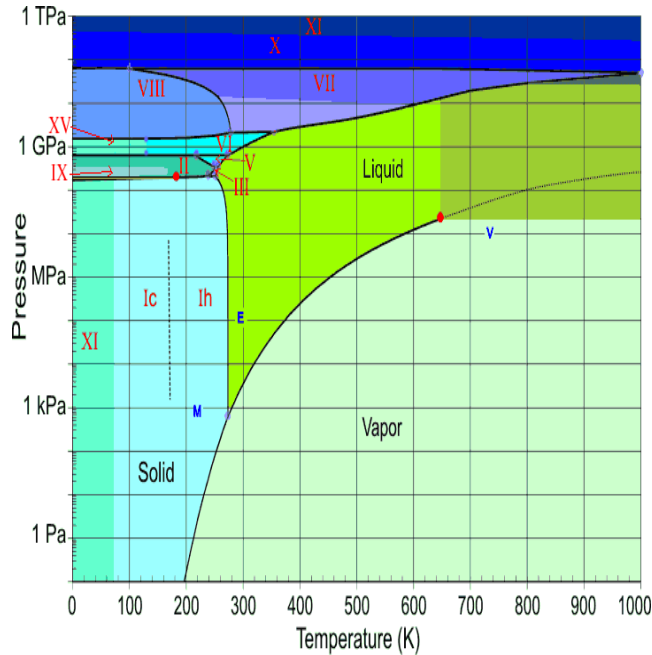
- Modification of crystal properties due to directed implantation of impurities or ionizing irradiation
- Anomalies of the properties in the region of the phase transitions

B.A.Strukov, Phase transitions,...(1996)

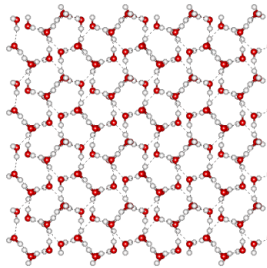


# Phase Diagram of Strongly Interacting Matter

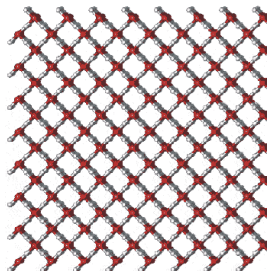
The phase diagram of water is established



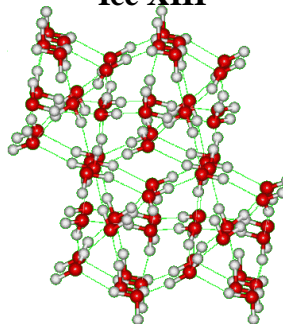
**Ice III**



**Ice X**

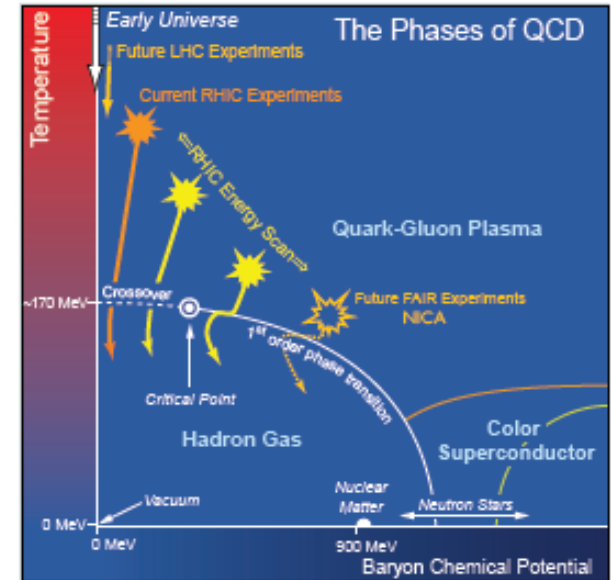


**Ice XIII**



- Phases (ice I-XV, liquid, vapor)
- Phase boundaries
- Phase transitions
- Triple Point (16)
- Critical Point (2)

The phase diagram of strongly interacting nuclear matter is under study



- Phases - ?
- Phase boundaries - ?
- Phase transitions - ?
- Triple Point - ?
- Critical Point - ?



# The Relativistic Heavy Ion Collider



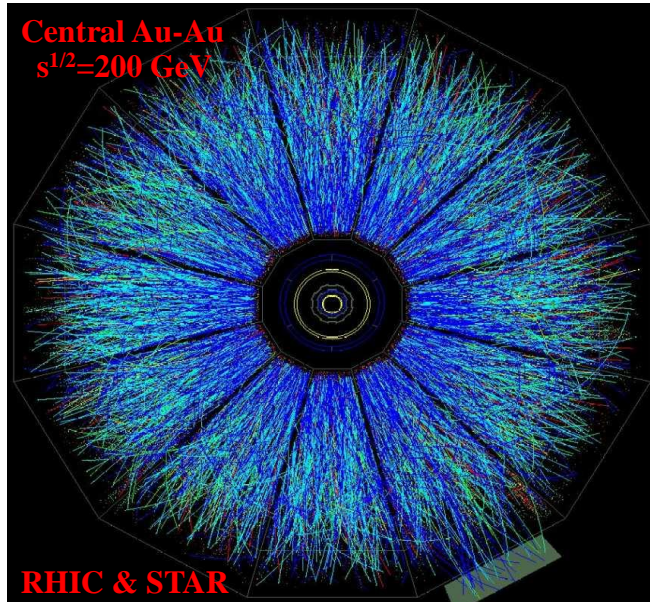
- 3.83 km circumference
- Two separated rings
- 120 bunches/ring
- 106 ns bunch crossing time
- A+A, p+A, p+p
- Maximum Beam Energy :
  - 500 GeV for p+p
  - 200A GeV for Au+Au
- Luminosity
  - Au+Au:  $2 \times 10^{26} \text{ cm}^{-2} \text{ s}^{-1}$
  - p+p :  $2 \times 10^{32} \text{ cm}^{-2} \text{ s}^{-1}$
- Beam polarizations
  - P=70%

Nucleus-nucleus collisions (AuAu, CuCu, dAu, CuAu, UU, ...  $\sqrt{s_{NN}}=7.7\text{-}200 \text{ GeV}$ )  
Polarized proton-proton collisions



# Main goal of investigations in relativistic **AA** collisions is search for and study new state of nuclear matter

..., AGS, SPS, RHIC, LHC, ...

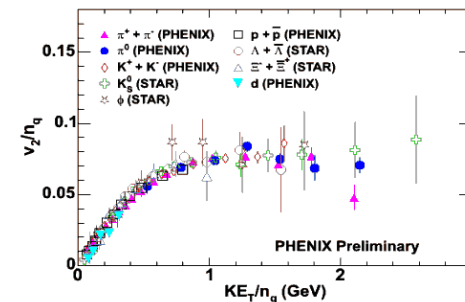
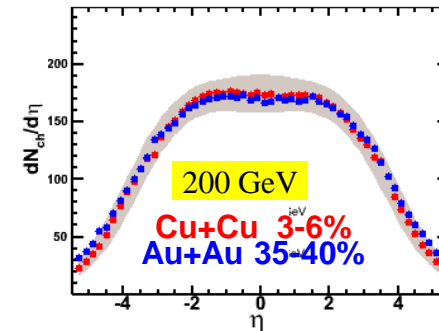
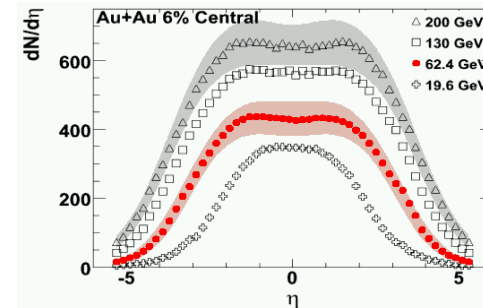


..., **NICA, FAIR**, ...

- High energy-density and very strong interacting matter was created at **RHIC**.
- **RHIC** data on  $dN_{ch}/d\eta$ ,  $v_2$ ,  $R_{CP}$ , ... exhibit scaling laws.
- Transition to the new state of matter does not manifest abrupt changes in observables.

“White papers”

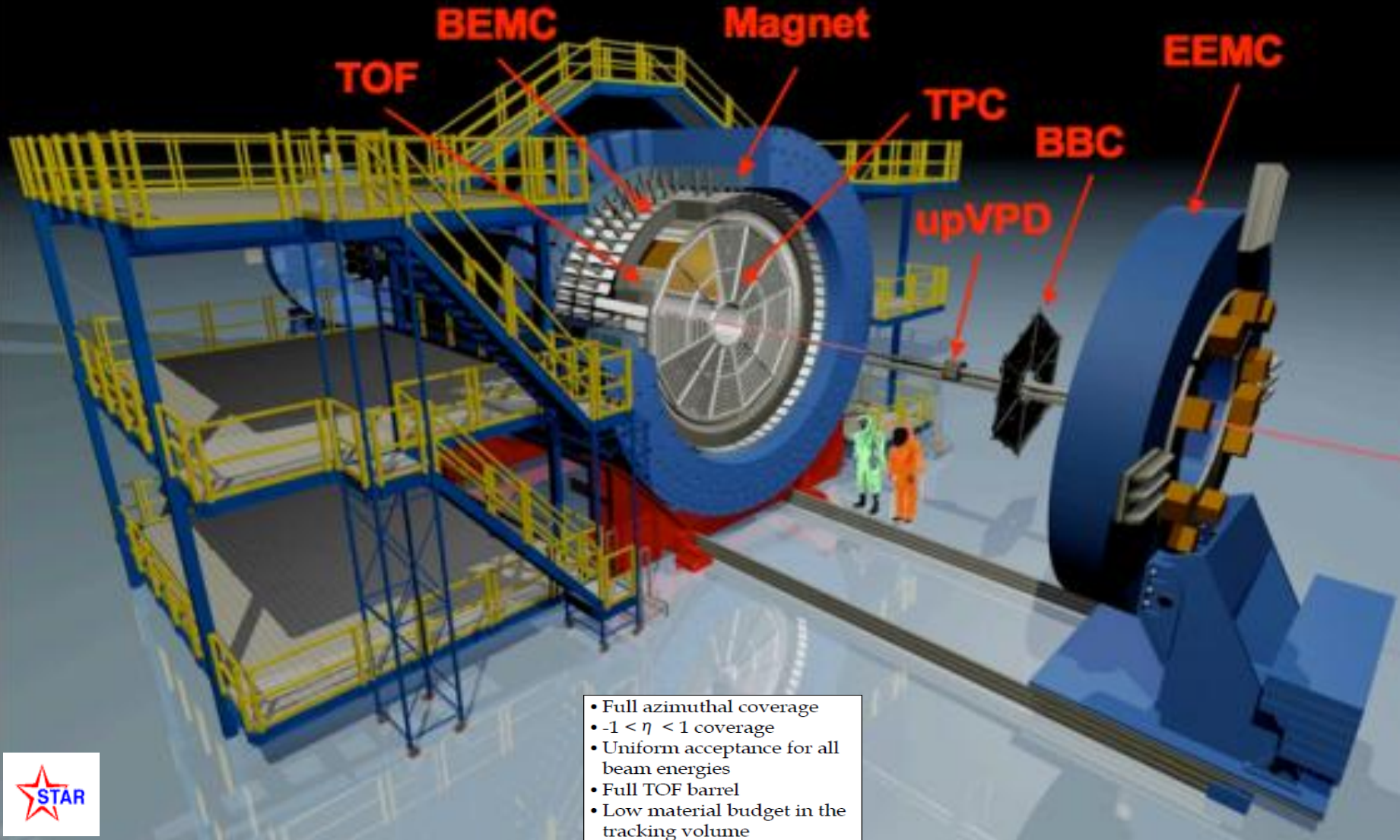
**STAR, PHENIX, PHOBOS & BRAHMS**



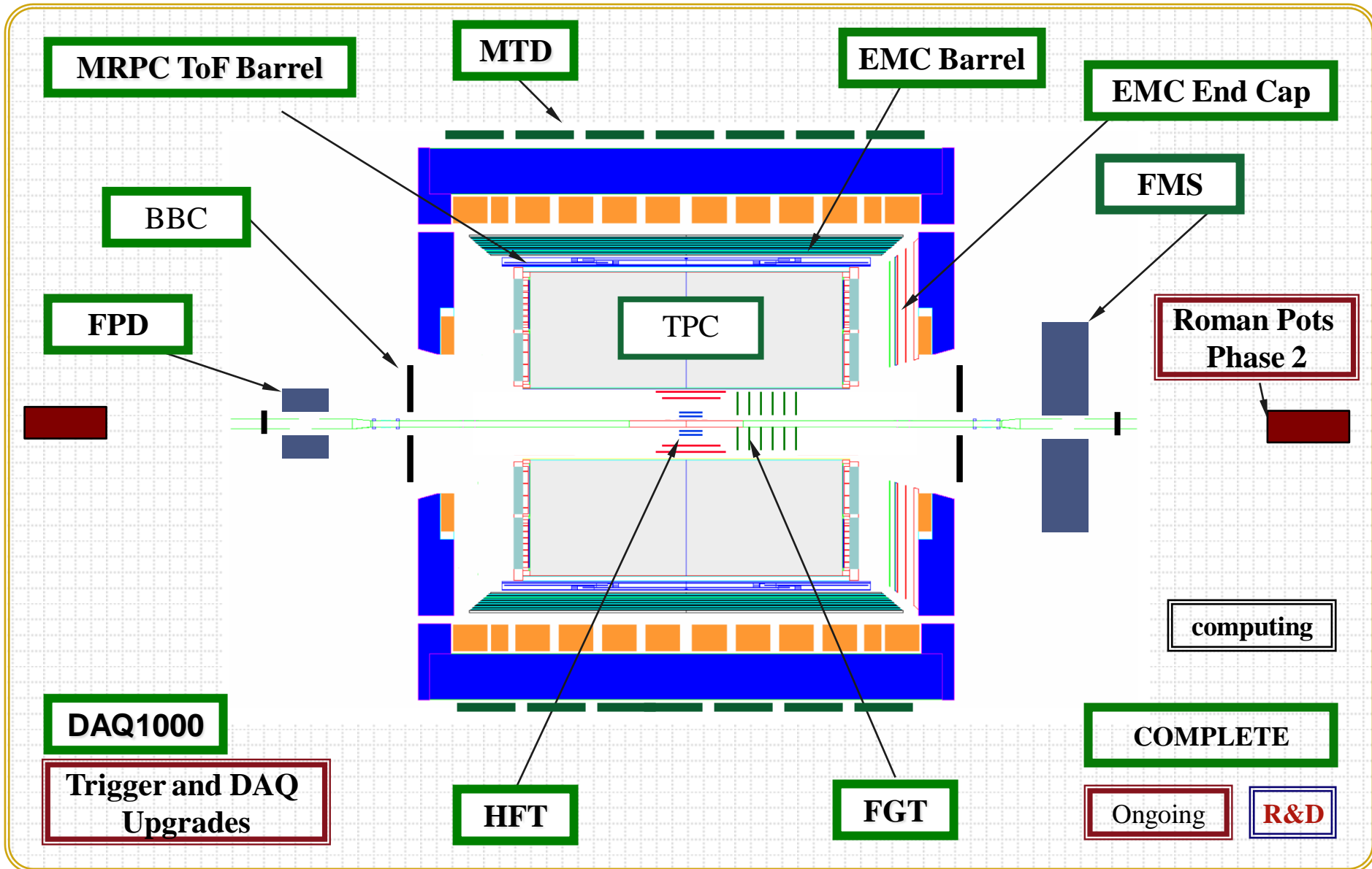
- What kind of interacting matter is created ?
- Thermodynamics, hydrodynamics, ...
- Phase transition, critical point, ...
- Self-similarity of created matter, ...



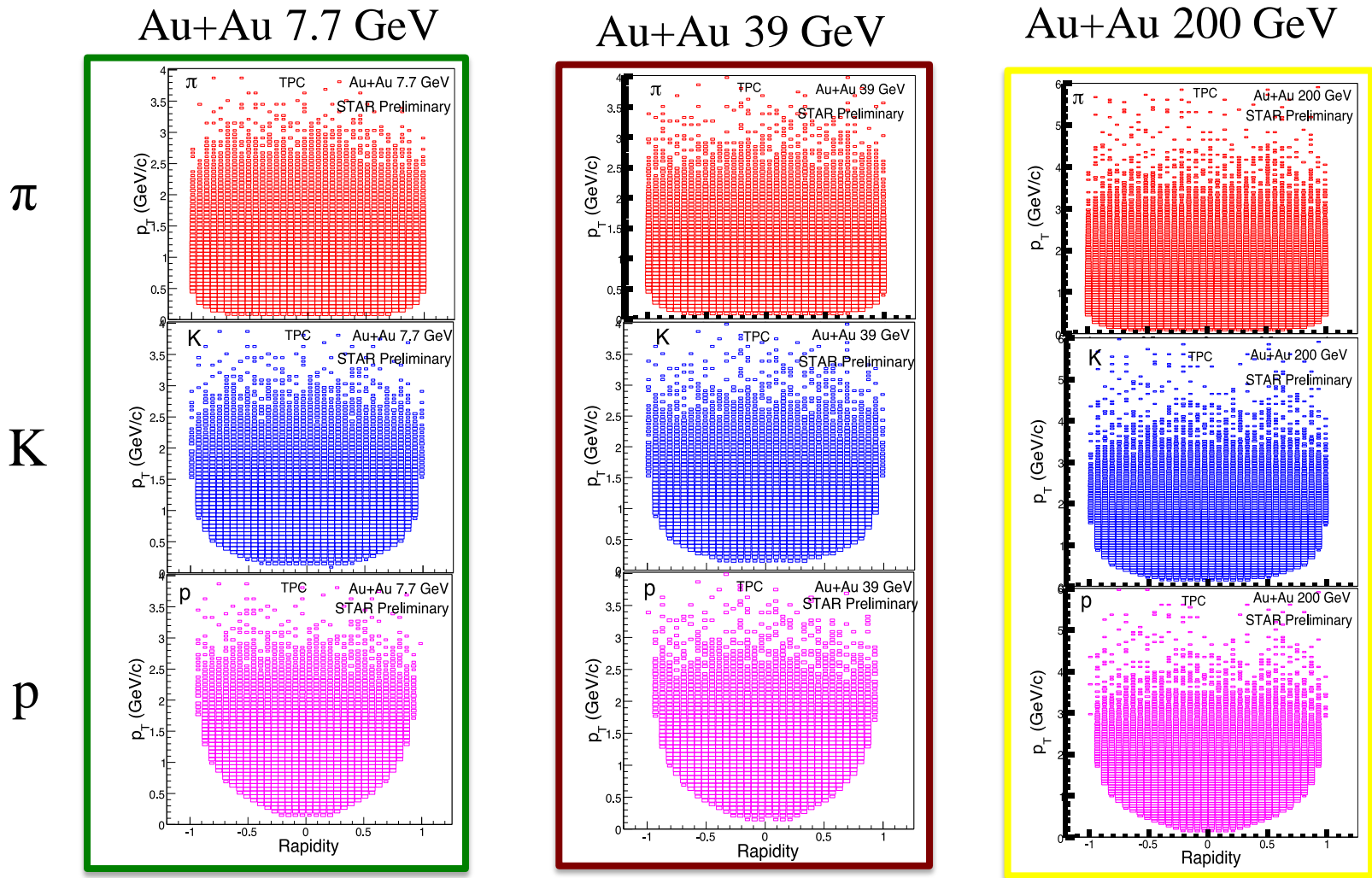
# The Solenoid Tracker At RHIC (STAR)



# STAR Detector



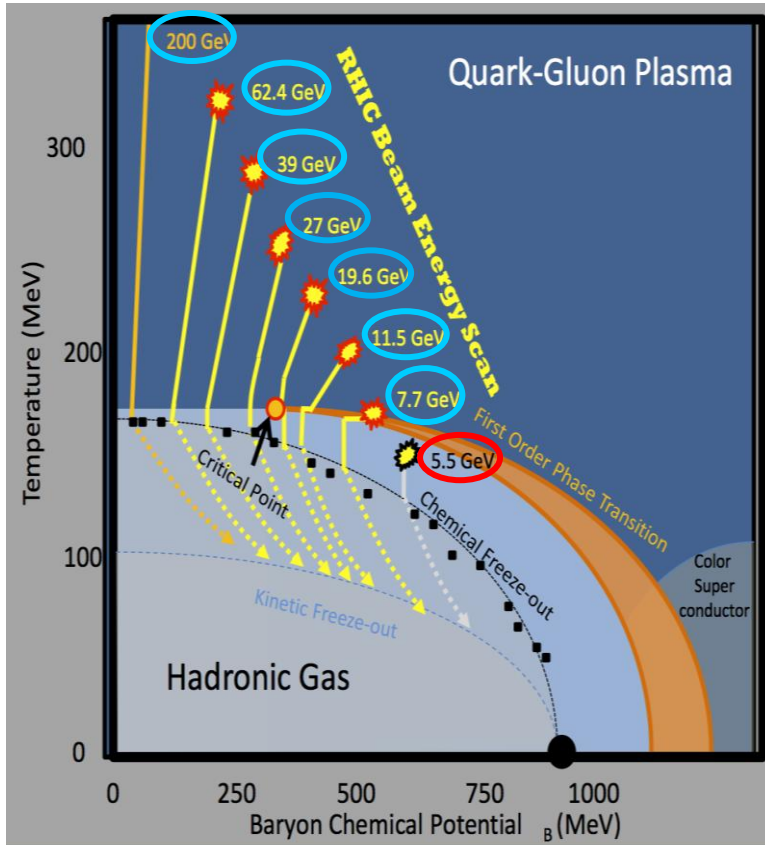
# Identified Particle Acceptance at STAR



Homogeneous acceptance for all energies.

# Beam Energy Scan at RHIC

Systematic study of AuAu collisions



STAR Note SN0493.

Phys. Rev. C 81, 024911 (2010).

Phys.At.Nucl., 2011, V.74, №5, p.769.

## Motivation

Search for phase transition and critical point of strongly interacting matter

- Elliptic & directed flow  $v_2, v_1$
- Azimuthally-sensitive femtoscopy
- Fluctuation measures:  
 $\langle K/\pi \rangle, \langle p/\pi \rangle, \langle p_T \rangle, \langle N_{ch} \rangle \dots$

Search for turn-off of new phenomena seen at higher RHIC energies

- Constituent-quark-number scaling of  $v_2$
- Hadron suppression in central collisions  $R_{AA}$
- Ridge ( $\Delta\phi$ - $\Delta\eta$  correlations)
- Local parity violation

STAR Collaboration:

*An Experimental Exploration of the QCD Phase*

*Diagram: The Search for the Critical Point*

*and the Onset of Deconfinement*

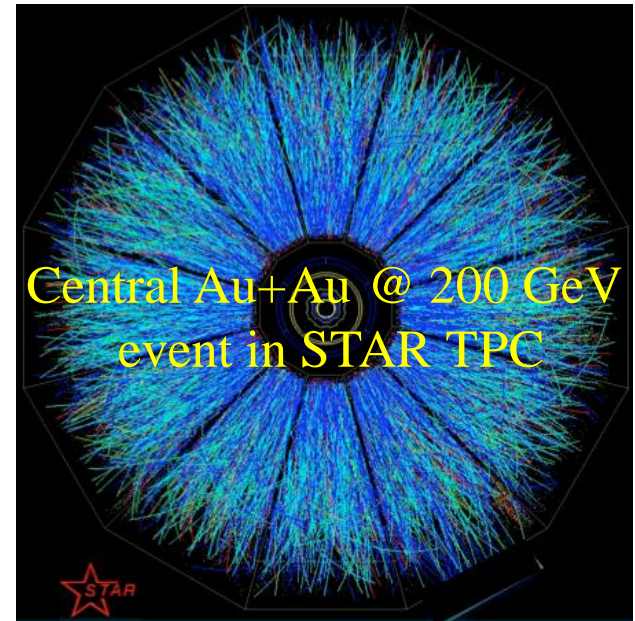
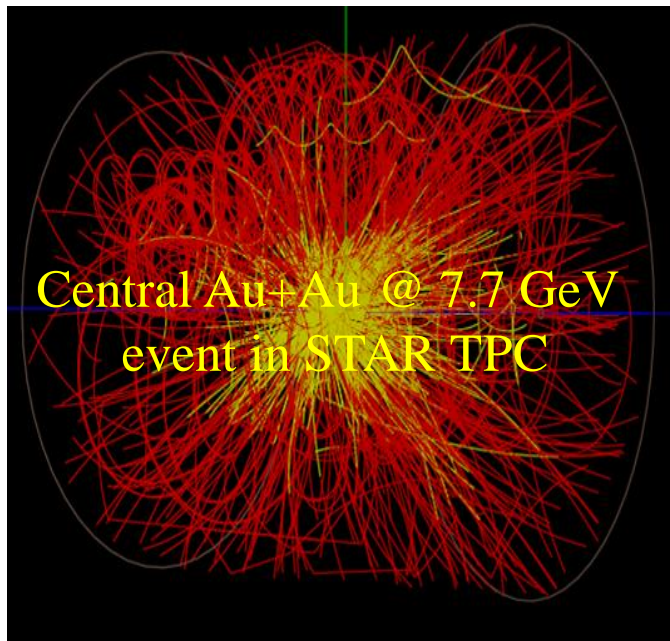
arXiv:1007.2613v1 [nucl-ex]

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# Beam Energy Scan Program at STAR RHIC

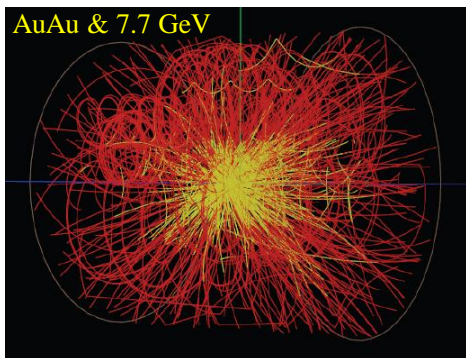
- signatures for a phase transition
- signatures for a critical point
- boundary of phase diagram





**RHIC beam energy scan with Au+Au:**

$\sqrt{s_{NN}} = 7.7, 11.5, 19.6, 27, 39, 62, 130, 200 \text{ GeV}$



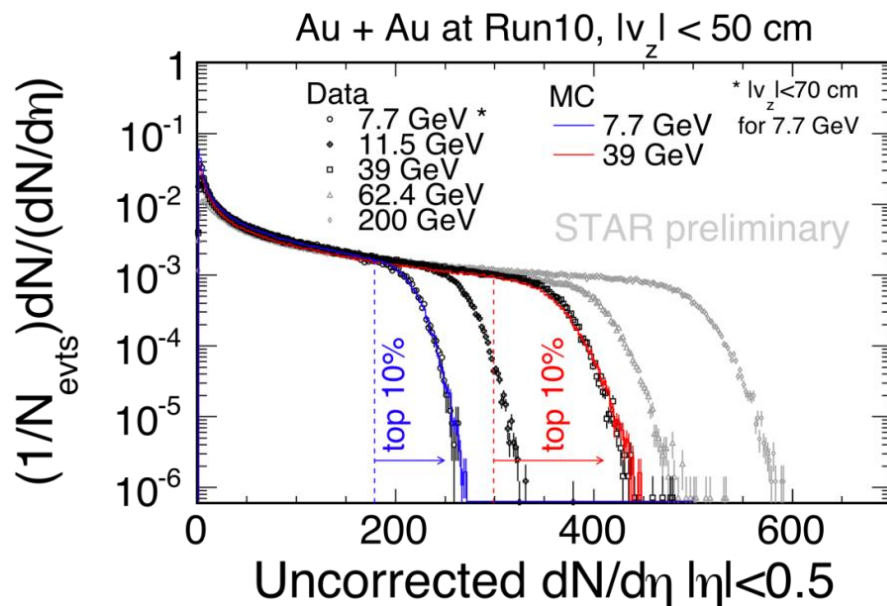
## Experimental Study of the QCD Phase Diagram and Search for the Critical Point

STAR Note SN0493, Phys. Rev. C 81, 024911 (2010)

STAR Run 10,11

Multiplicity distribution

$\sqrt{s_{NN}}$ (GeV)	$\mu_B$ (MeV)	MB Events in Millions
5.0	550	
7.7	410	4.3
11.5	300	11.7
19.6	230	35.8
27	151	70.4
39	112	130.4
62.4	73	67.3
130	36	
200	24	

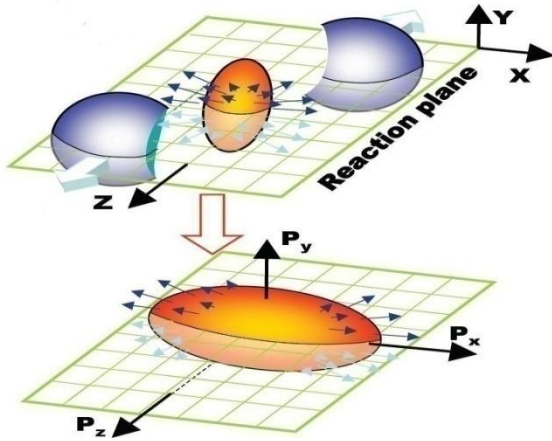


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# Flow of nuclear matter

collectivity of partonic degree of freedom

# Directed ( $v_1$ ) & Elliptic ( $v_2$ ) flow in AuAu collisions



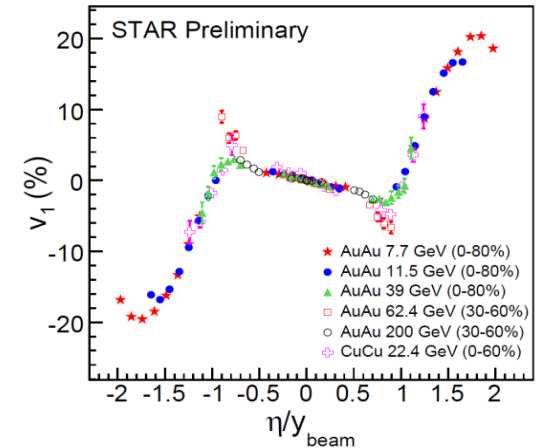
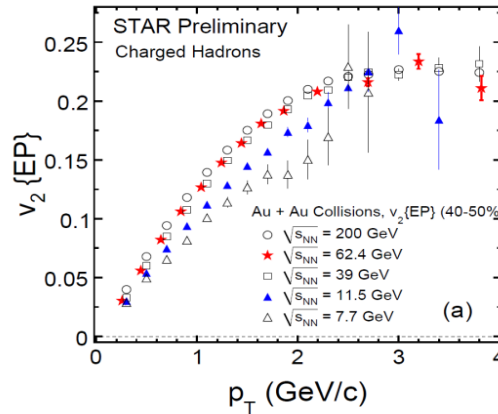
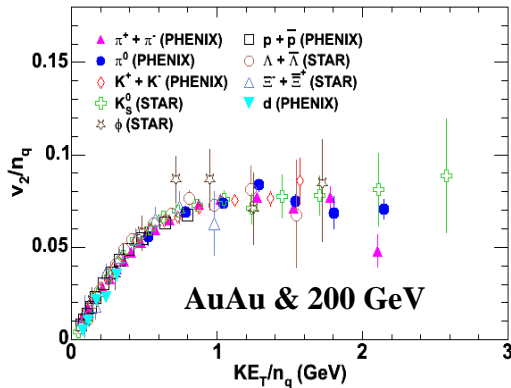
Coordinate-Space  
Anisotropy  
↓  
Momentum-Space  
Anisotropy

Fourier expansion  
of the momenta distribution

$$E \frac{d^3N}{d^3p} \propto \left( 1 + \sum_{n=1}^{\infty} 2v_n \cos n(\phi - \Psi_r) \right)$$

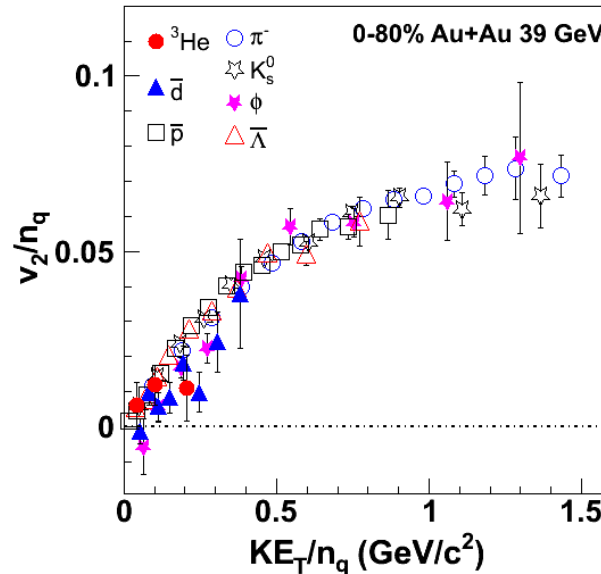
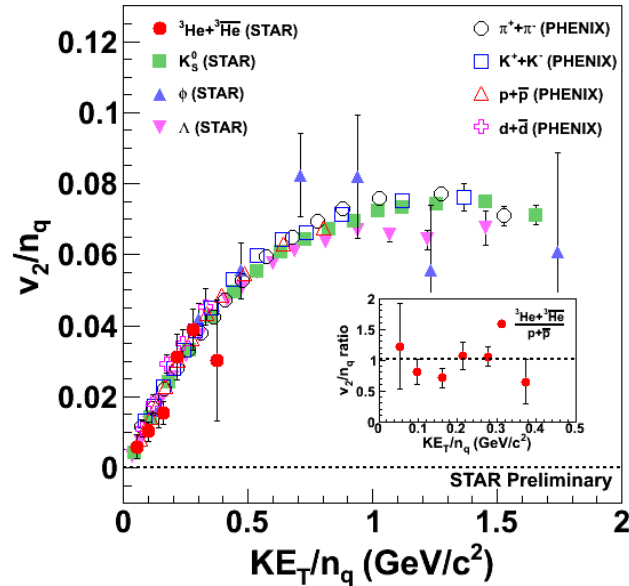
$$v_n = \langle \cos n(\phi - \Psi_r) \rangle$$

$$\phi = \tan^{-1} \left( \frac{p_y}{p_x} \right)$$



- $v_1$  ( $y$ ) sensitive to baryon transport, space momentum correlations and QGP formation.
- $v_2$  provides the possibility to gain information about the degree of thermalization of the hot, dense medium.
- The breaking of  $v_2$  number of quark scaling will indicate a transition from partonic to hadronic degrees of freedom.

# NCQ scaling: Au+Au 200 & 39 GeV



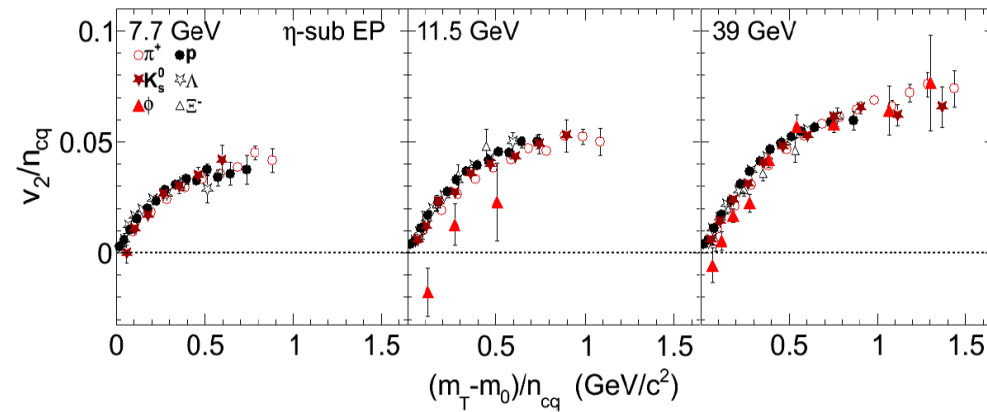
Flow vs.  
 - energy  
 - centrality  
 - particle mass

$v_2$  of light nuclei scaled to the number of constituent quarks (NCQ) of their constituent nucleons, are consistent with NCQ scaled  $v_2$  of baryons and mesons

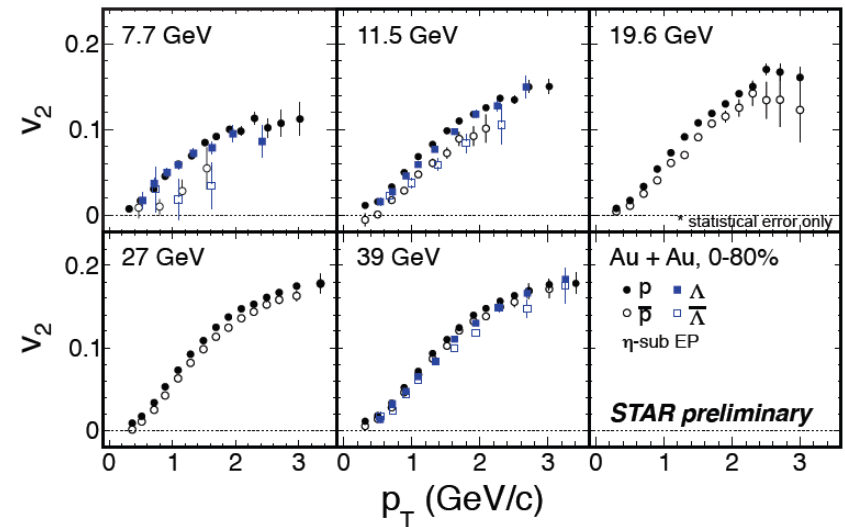
NCQ scaling holds good for  $v_2$  of light nuclei in Au+Au 39 GeV

# BES @ NCQ scaling of $v_2$

AuAu @ 7.7, 11.5, 39



AuAu @ 7.7, 11.5, 19.6, 27, 39



- Universal trend for most of particles
- $\phi$  meson  $v_2$  indicates strange quark collectivity becomes weaker with decreasing beam energy

- Difference of  $v_2(p_T)$  between particles and antiparticles.

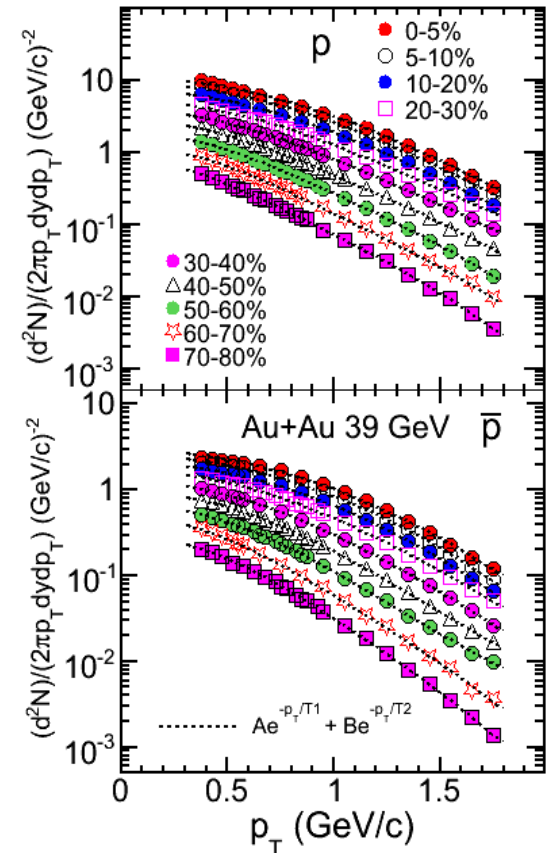
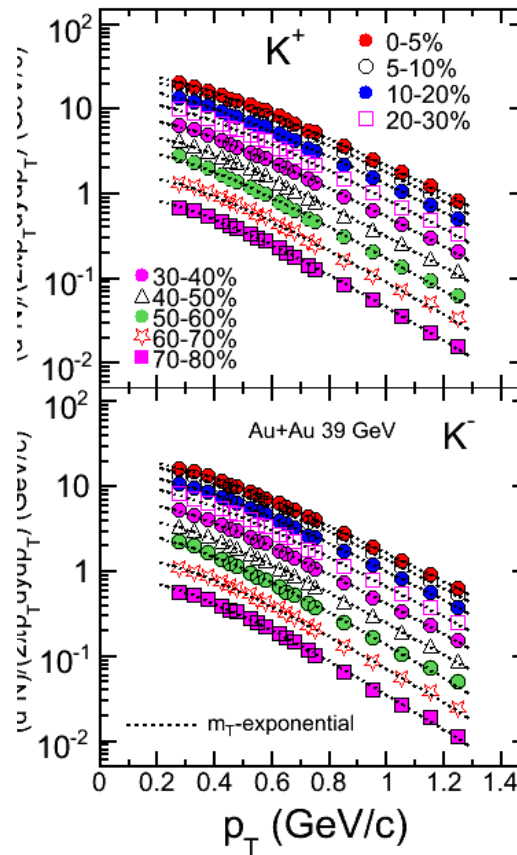
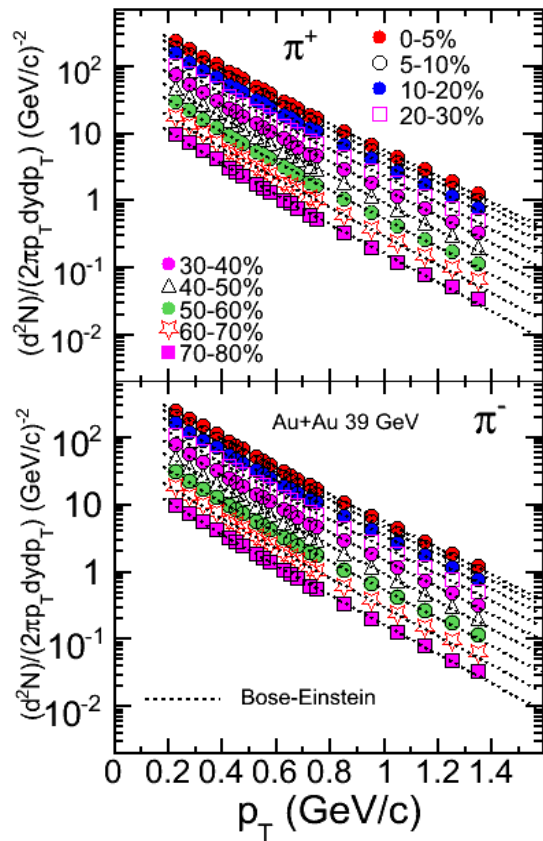
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# Spectra

probing QCD phase diagram  
with identified particles:  $\pi^{+/-}$ ,  $K^{+/-}$  and  $\bar{p}/p$   
in STAR BES program



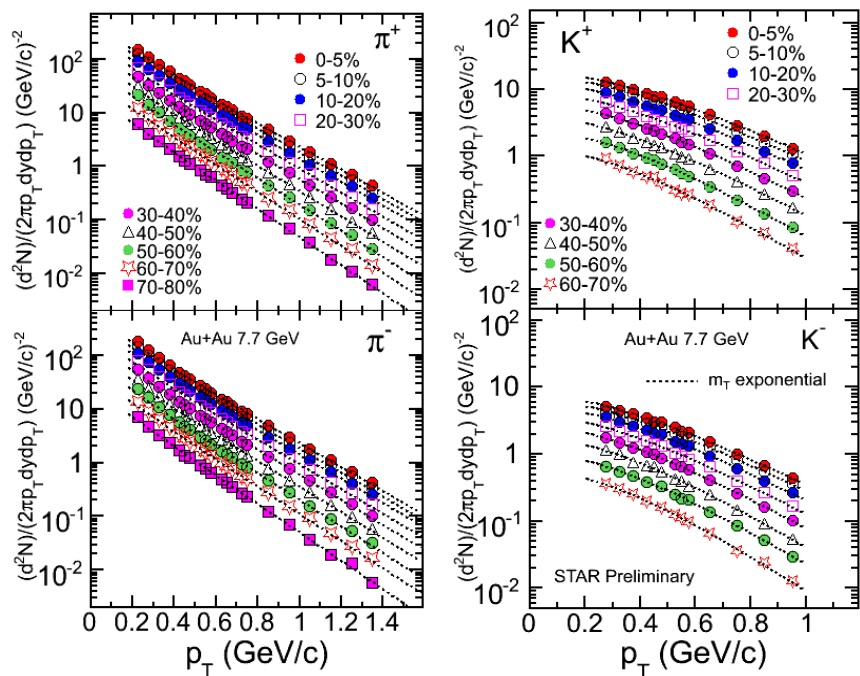
## Au+Au @ 39 GeV



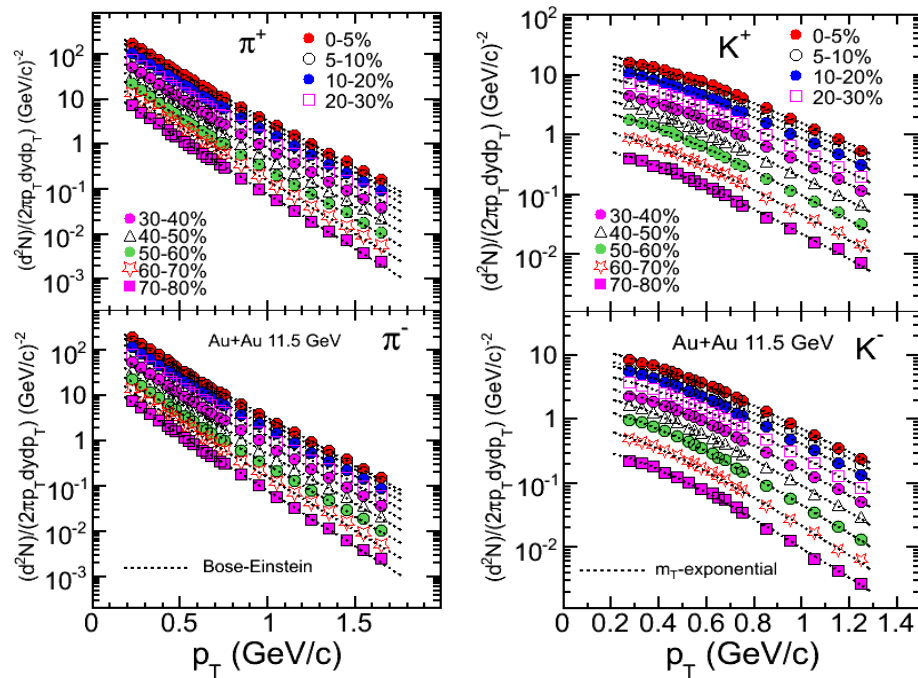
- BES spectra obtained with **TPC** and **TOF**:
  - ✓ Consistent with dE/dx in overlapping range



Au+Au @ 7.7 GeV

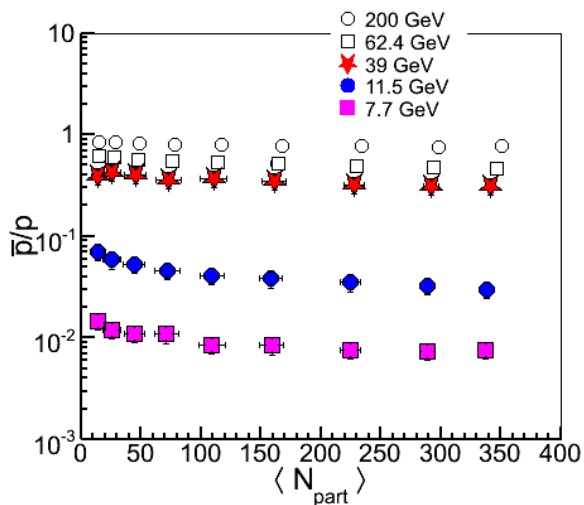
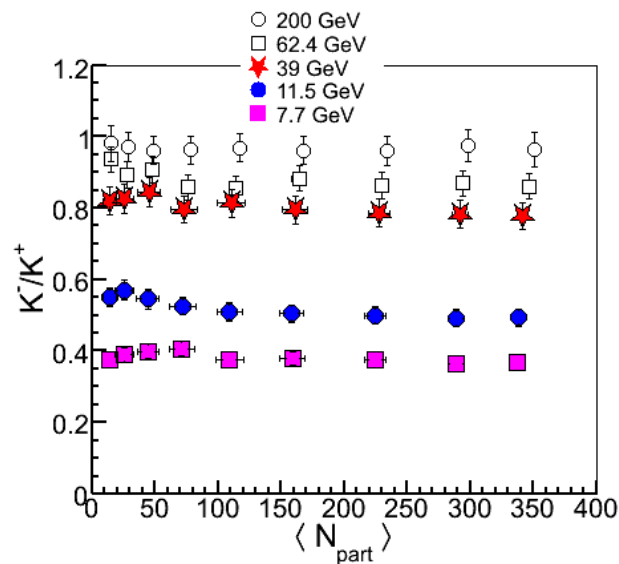
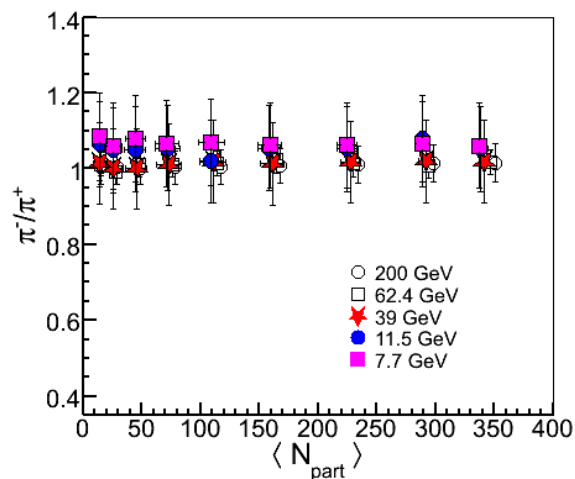


Au+Au @ 11.5 GeV



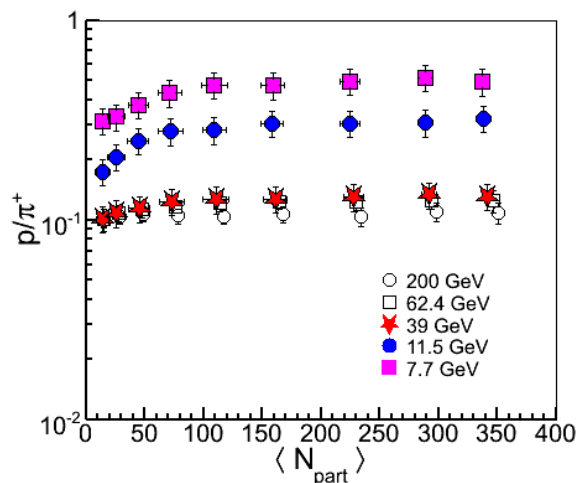
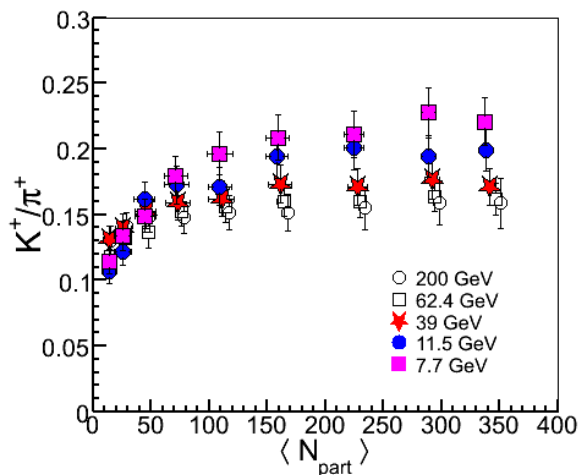
➤ Spectra of identified particle up to 1.5 GeV/c.

AuAu @ 7.7, 11.5, 39, 62.4, 200 GeV

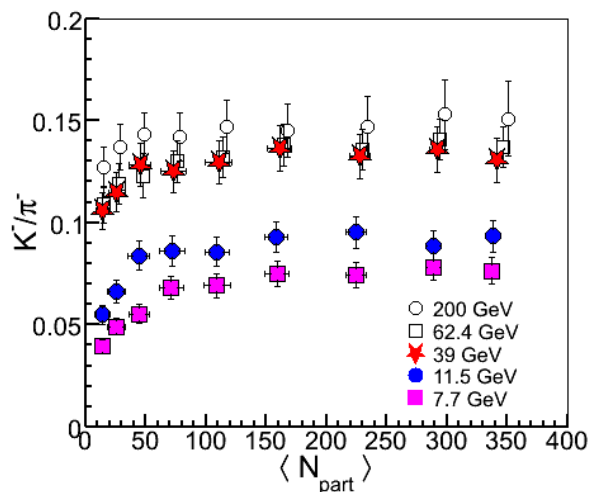
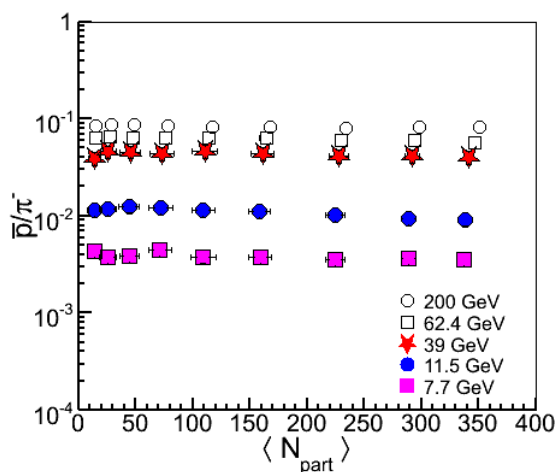


- Ratios are flat vs. centrality
- Ratios increase vs. energy  $\sqrt{s_{NN}}$

AuAu @ 7.7, 11.5, 39, 62.4, 200 GeV



➤  $K^+/\pi^+$  and  $p/\pi^+$  ratios increases with decrease in energy



➤  $K^-/\pi^-$  and  $p^-/\pi^-$  ratios increases with energy

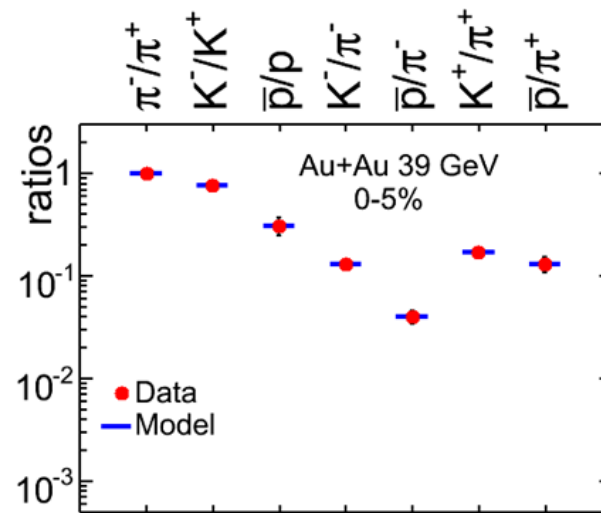
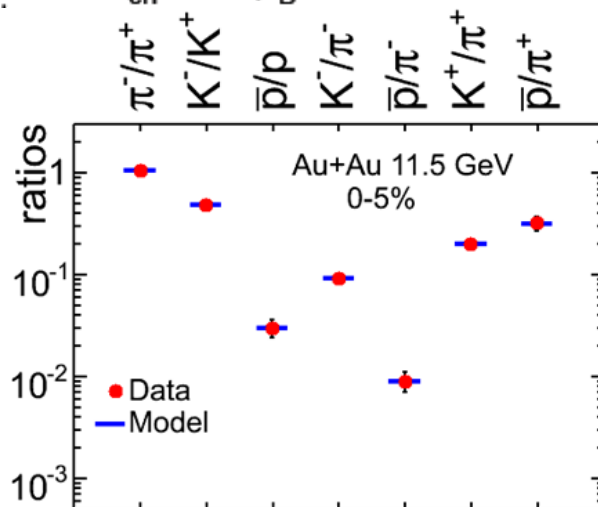
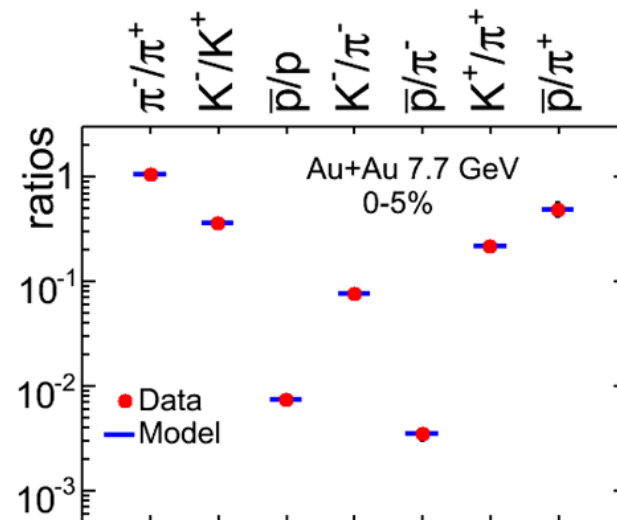
## Statistical-Thermal Model (THERMUS):

$$n = \frac{1}{V} \frac{\partial(T \ln Z)}{\partial \mu} = \frac{VT m_i^2 g_i}{2\pi^2} \sum_{k=1}^{\infty} \frac{(\pm 1)^{k+1}}{k} (e^{\beta k \mu_i}) K_2\left(\frac{km_i}{T}\right)$$

$\beta = 1/T$ ;  $-1(+1)$  for fermions (bosons),  $Z =$  partition function;  
 $m_i =$  mass of hadron species  $i$ ;  $V =$  volume;  $T =$  Temperature;  
 $K_2 =$  2<sup>nd</sup> order Bessel function;  $g_i =$  degeneracy;  $\mu_i =$  chemical potential

- ✦ Fitted particle ratios with THERMUS
- ✦ Used grand-canonical approach
- ✦ Two main parameters:  $T_{ch}$  and  $\mu_B$

S. Wheaton & J. Cleymans, hep-ph/0407174;  
 S. Wheaton, J. Cleymans & M. Hauer, comp. phys. Comm. 180 (2009) 84.

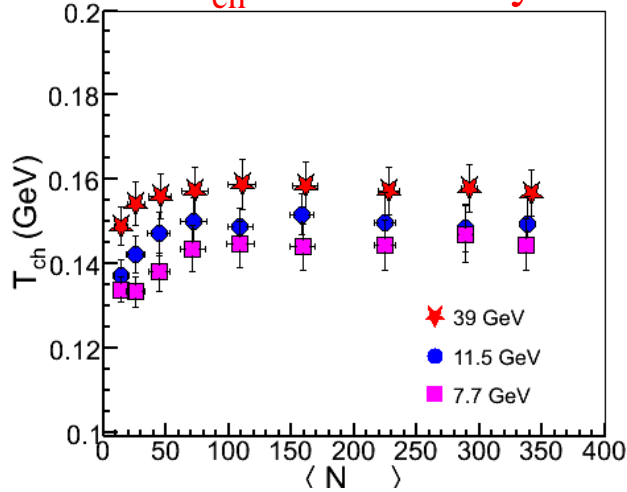


$$\langle n_i \rangle = \frac{(2J_i + 1) V}{(2\pi)^3} \int d^3p \frac{1}{\gamma_s^i \exp[(E_i - (\mu_B + \mu_S + \mu_Q))/T] \pm 1}$$



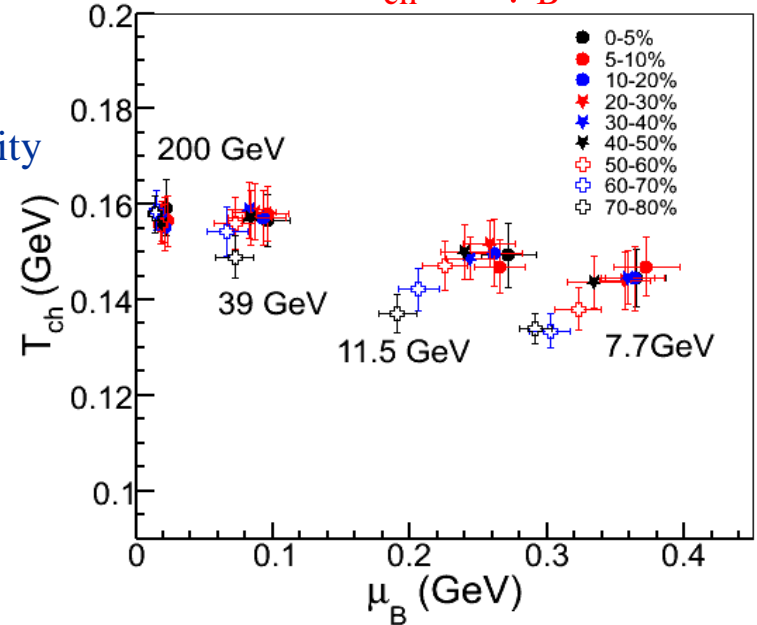
# BES @ Chemical Freeze-out

### $T_{ch}$ vs. centrality

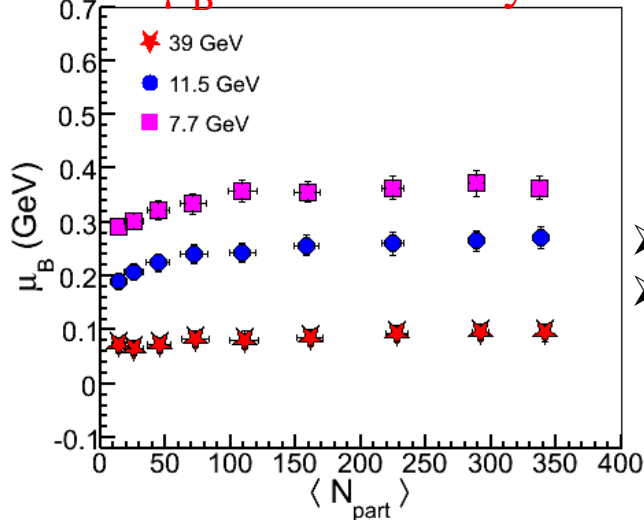


- $T_{ch}$  increases with energy
- $T_{ch}$  saturates with centrality

### $T_{ch}$ vs. $\mu_B$



### $\mu_B$ vs. centrality



- $\mu_B$  decreases as energy increases
- $\mu_B$  saturates with centrality

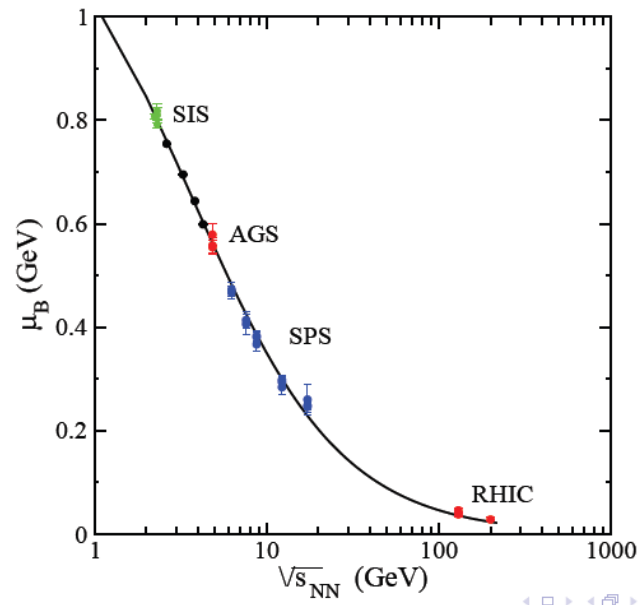
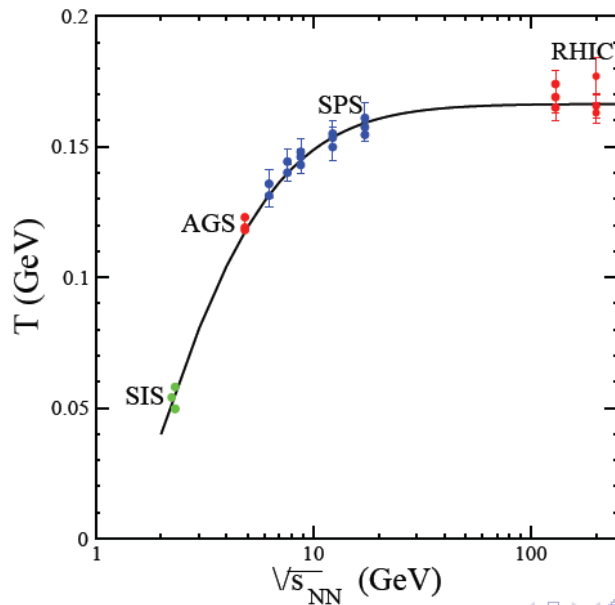
Phase boundary depends on centrality



# Statistical thermodynamical model

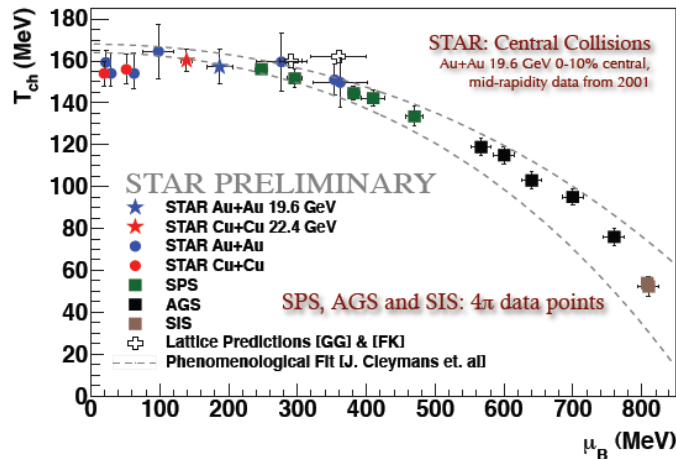
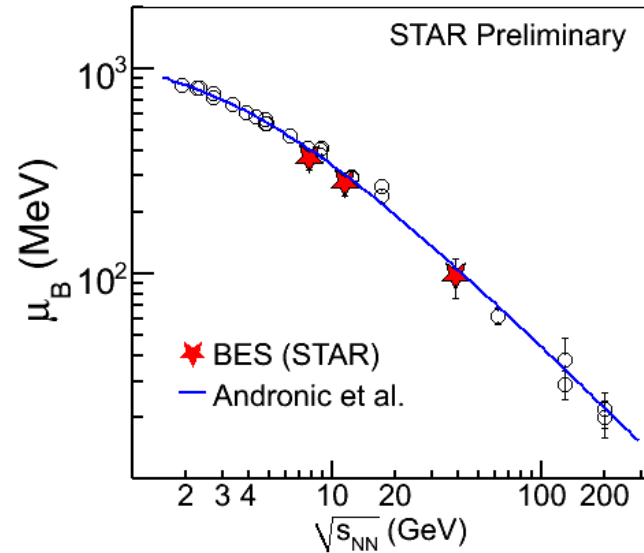
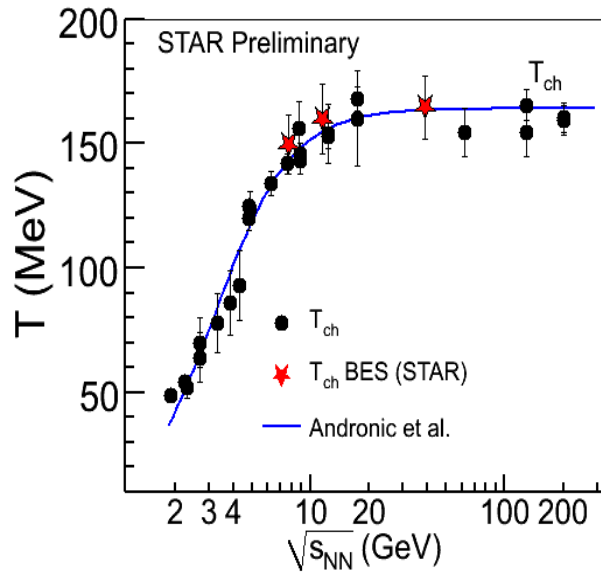
Particle ratio fitted by thermal model to extract Chemical freeze-out temperature ( $T$ ) and baryon chemical potential ( $\mu_B$ ).

J. Cleymans et al, Phys. Rev. C73 (2006) 034905



- Smooth dependence of  $T_{ch}$  and  $\mu_B$  on energy
- $T_{ch}$  is flat for  $\sqrt{s_{NN}} > 20$  GeV
- $\mu_B$  is tending to zero if  $\sqrt{s_{NN}} \rightarrow \infty$
- RHIC:  $\mu_B \approx 24$  MeV at  $\sqrt{s_{NN}} = 200$  GeV
- LHC:  $\mu_B \approx 0.87$  MeV at  $\sqrt{s_{NN}} = 5500$  GeV

# Data @ Stat-Thermo Model



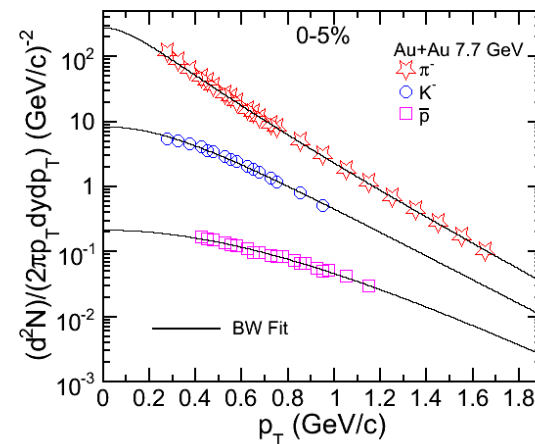
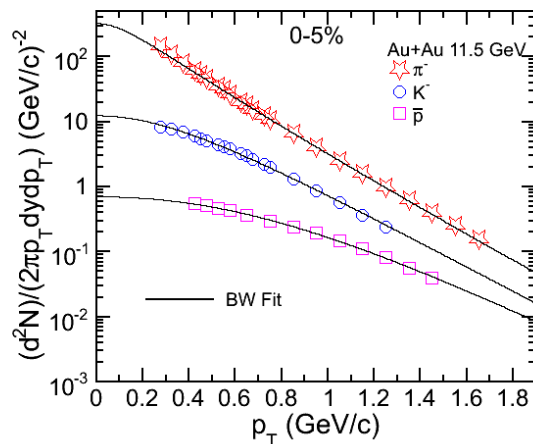
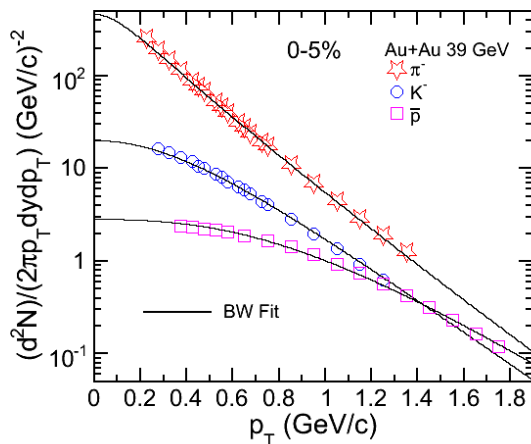
Smooth dependence everywhere.



# BES @ Kinetic Freeze-out

Blast-Wave (BW) Model:

$$\frac{dN}{p_T dp_T} \propto \int_0^R r dr m_T I_0 \left( \frac{p_T \sinh \rho(r)}{T_{kin}} \right) \times K_1 \left( \frac{m_T \cosh \rho(r)}{T_{kin}} \right)$$



- ✧ Spectra are fitted simultaneously with BW
- ✧ Two main parameters:  $T_{kin}$  and  $\langle \beta \rangle$

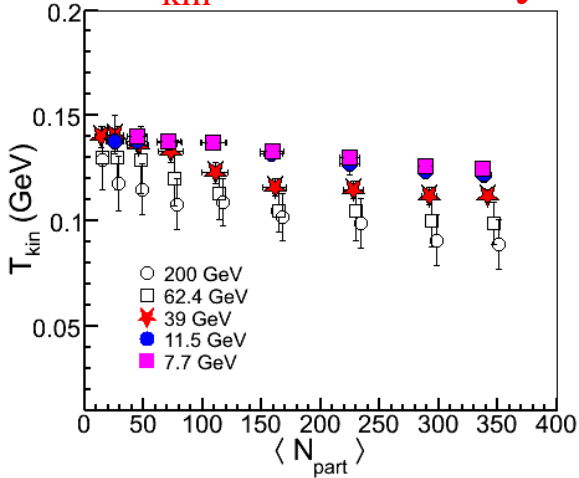






# BES @ Kinetic Freeze-out

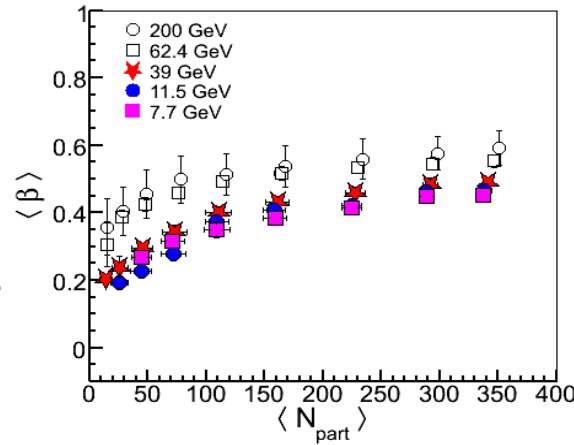
## $T_{kin}$ vs. centrality



$T_{kin}$

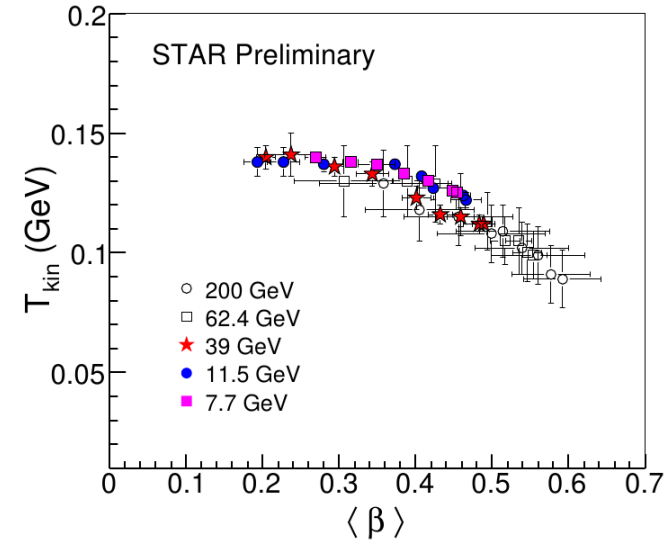
- decreases as energy increases
- saturates with centrality

## $\langle \beta \rangle$ vs. centrality



$\langle \beta \rangle$

- increases with energy
- saturates with centrality



## Smooth behavior

$T_{kin}$  vs. centrality  
 $\langle \beta \rangle$  vs. centrality  
 $T_{kin}$  vs.  $\langle \beta \rangle$



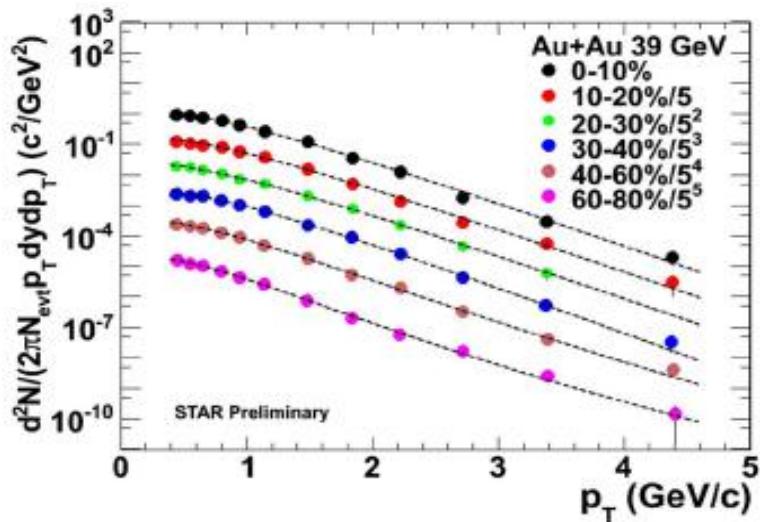
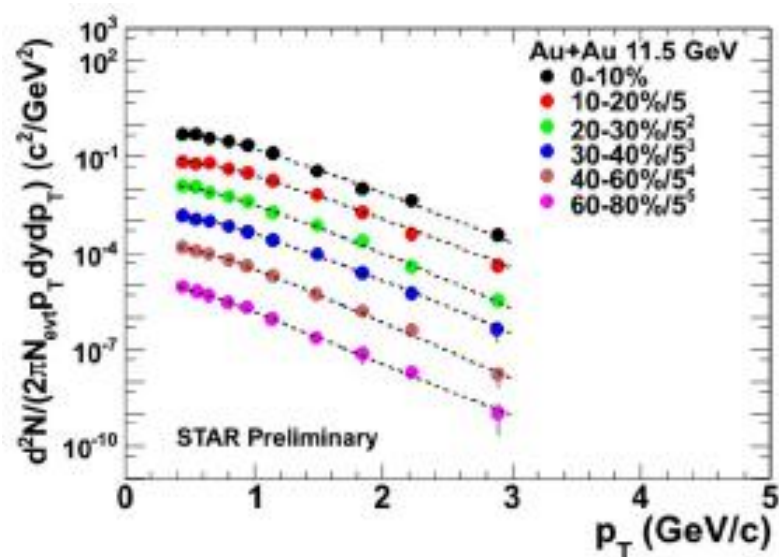
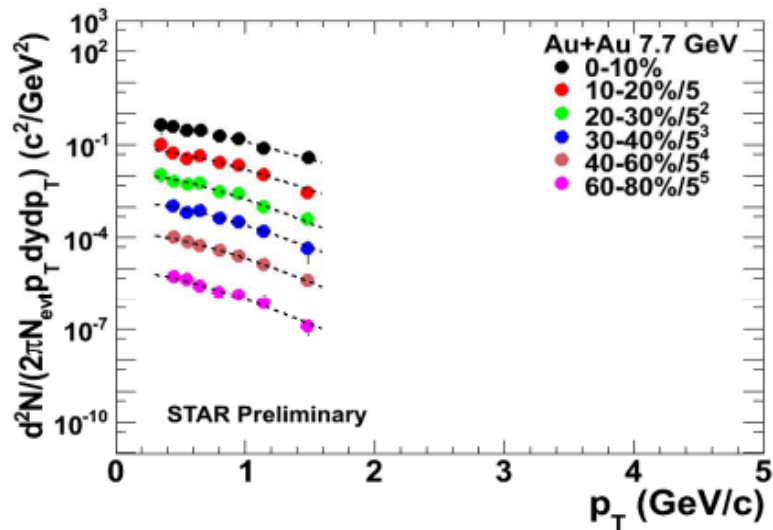
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# Spectra

probing QCD phase diagram  
with identified particles:  $\phi$ ,  $K_S^0$ ,  $\Lambda$ ,  $\Xi$ ,  $\Omega$ , ...  
in STAR BES program

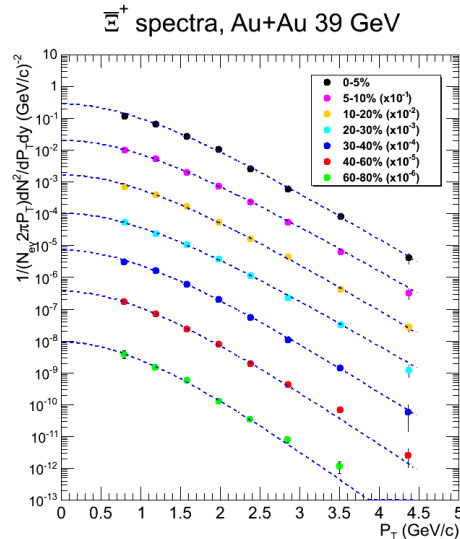
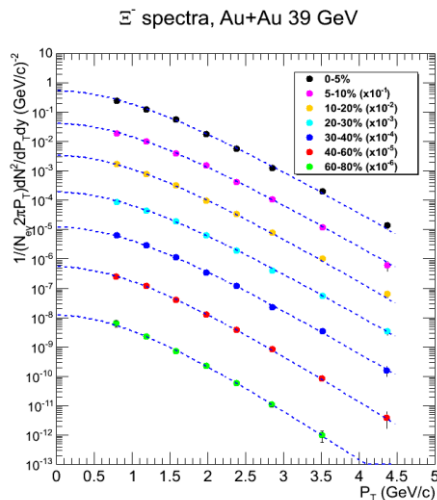
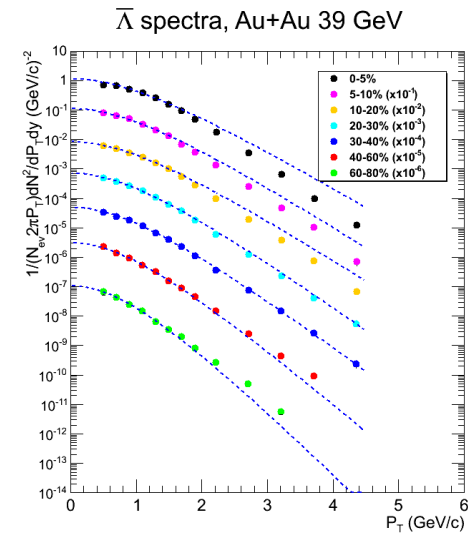
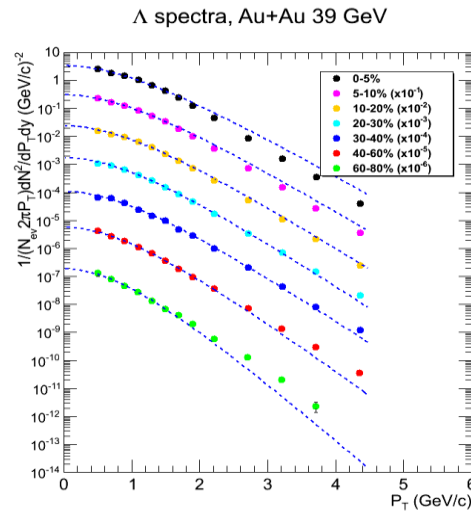
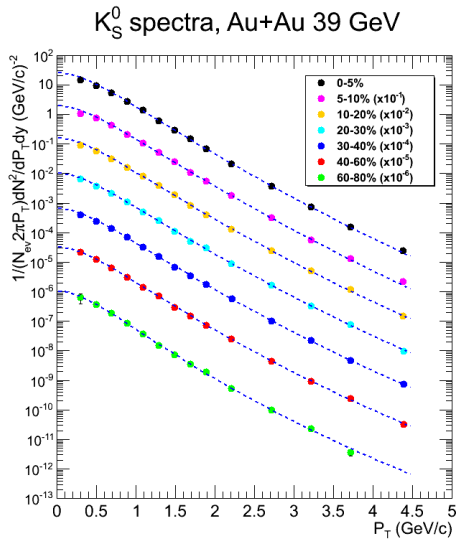


# Spectra from $\phi \rightarrow K^+K^-$ decay channel



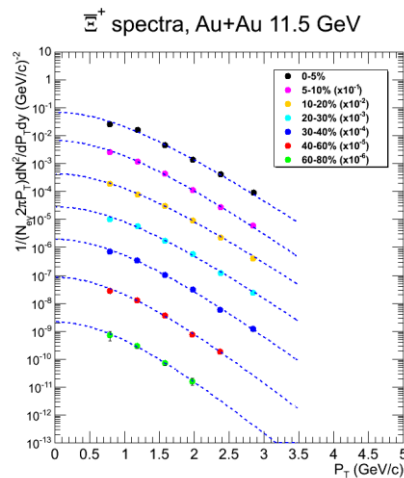
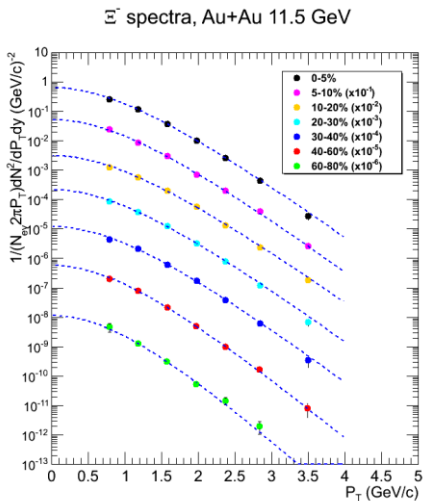
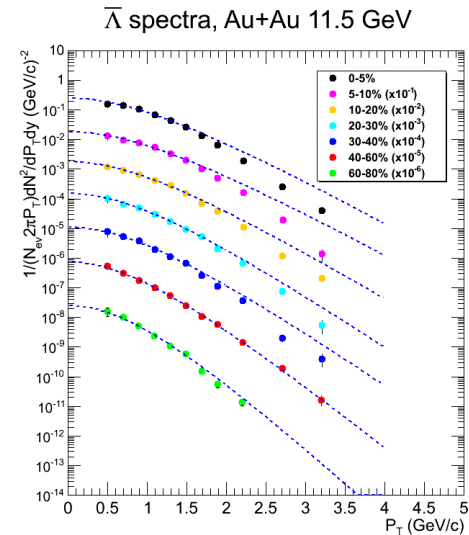
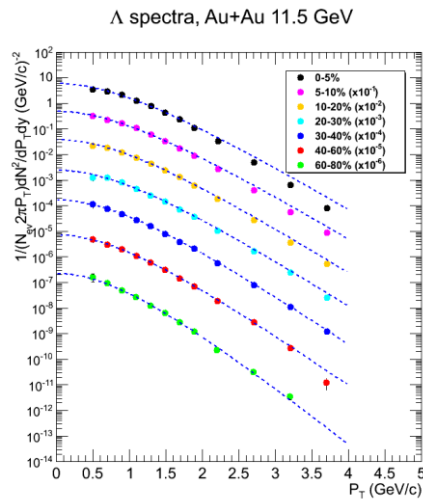
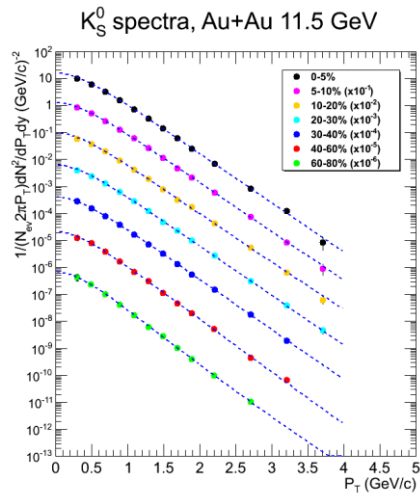
Transverse momentum spectra are well described by the Levy function with parameters  $T$  &  $n$

$$\frac{1}{2\pi p_T} \frac{d^2N}{dp_T dy} = \frac{dN/dy}{2\pi n T (nT + m(n-2))} \left(1 + \frac{\sqrt{p_T^2 + m^2} - m}{nT}\right)^{-n}$$



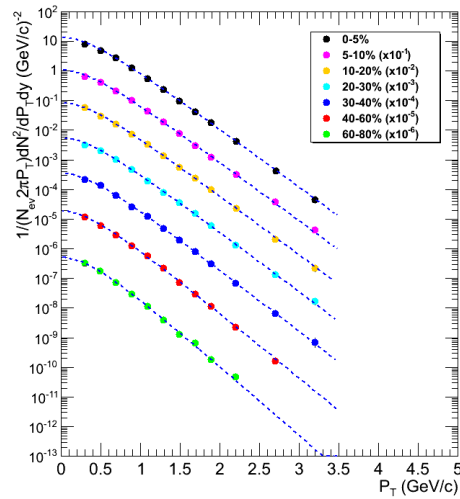
$\sqrt{s}=39$  GeV

$\Lambda$  spectra are weak decay  
feed-down corrected:  
~ 20% for  $\Lambda$   
~ 25% for anti- $\Lambda$

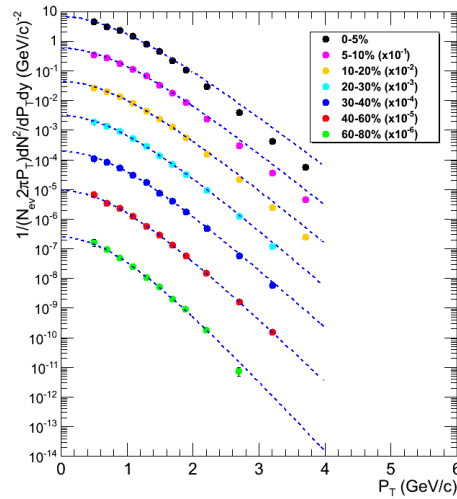


$\sqrt{s}=11.5$  GeV  
 $\Lambda$  spectra are weak decay  
 feed-down corrected:  
 $\sim 15\%$  for  $\Lambda$   
 $\sim 27\%$  for anti- $\Lambda$

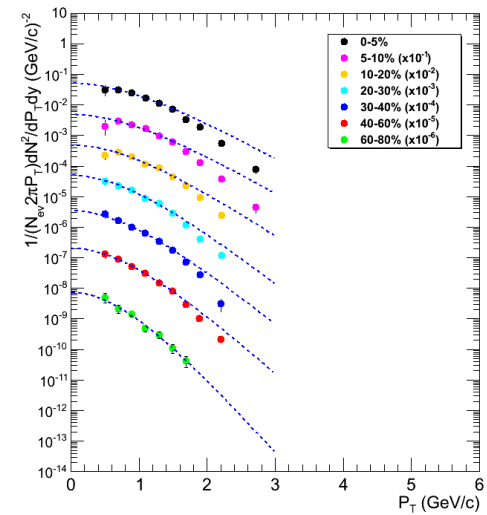
$K_S^0$  spectra, Au+Au 7.7 GeV



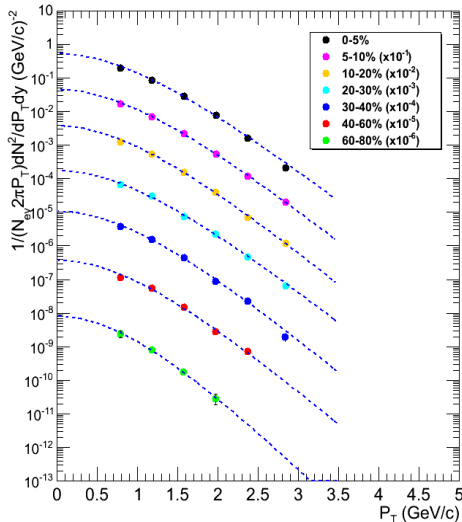
$\Lambda$  spectra, Au+Au 7.7 GeV



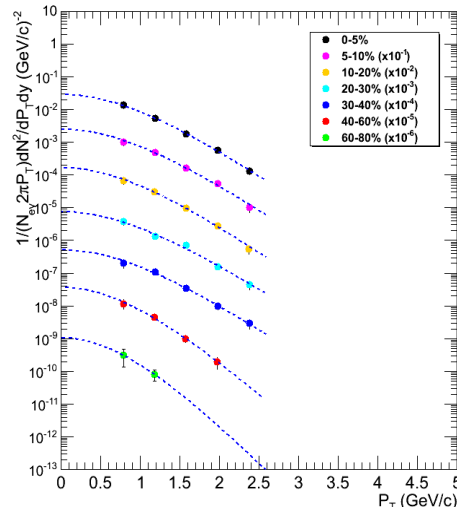
$\bar{\Lambda}$  spectra, Au+Au 7.7 GeV



$\Xi^-$  spectra, Au+Au 7.7 GeV



$\Xi^+$  spectra, Au+Au 7.7 GeV



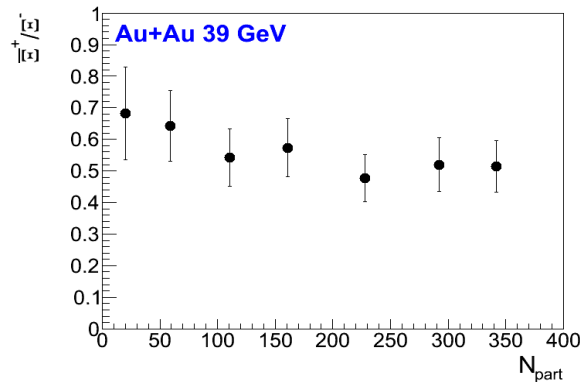
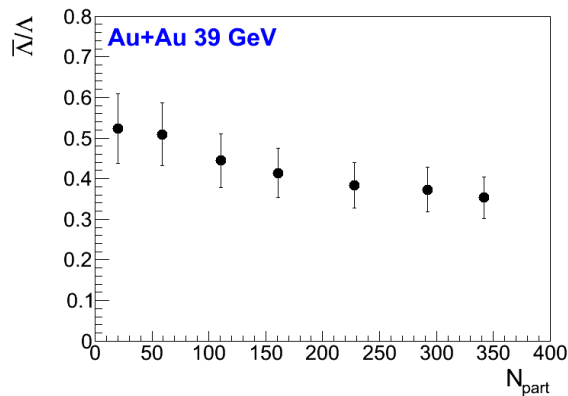
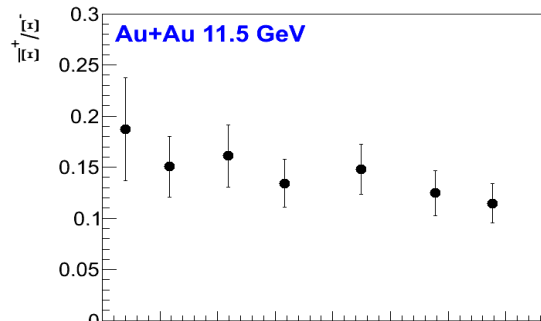
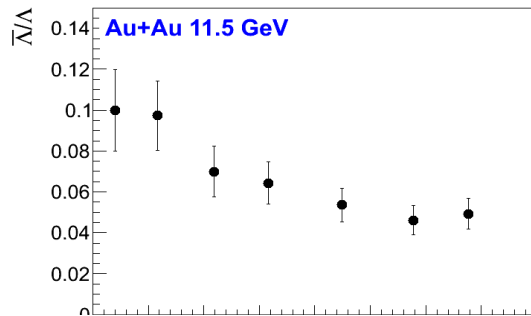
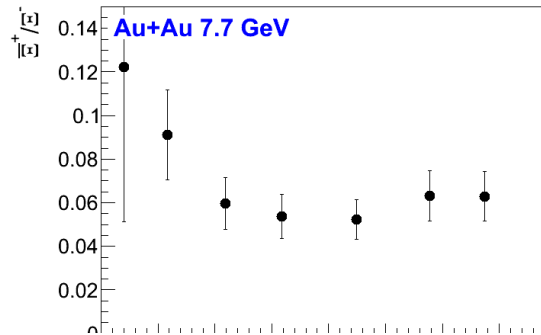
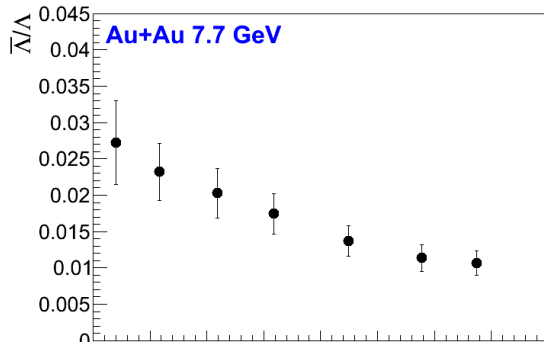
$\sqrt{s}=7.7$  GeV

$\Lambda$  spectra are weak decay

feed-down corrected:

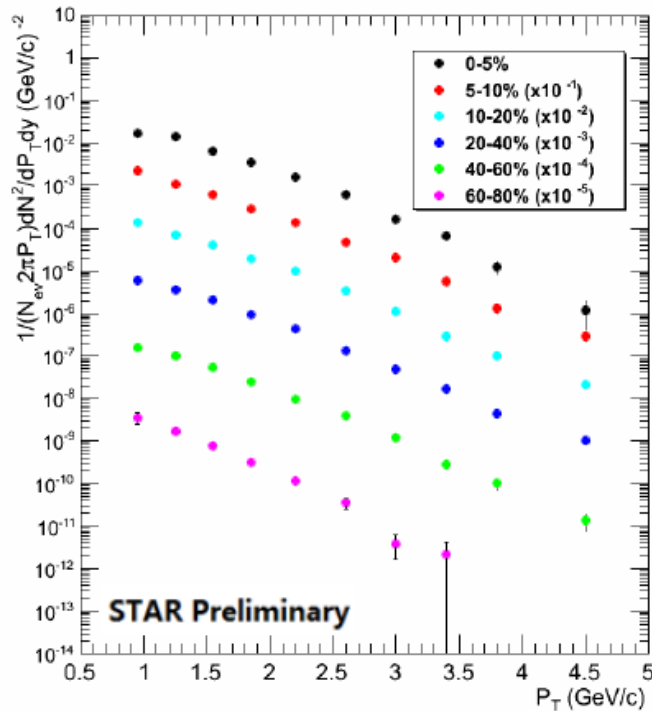
~ 11% for  $\Lambda$

~ 35% for anti- $\Lambda$

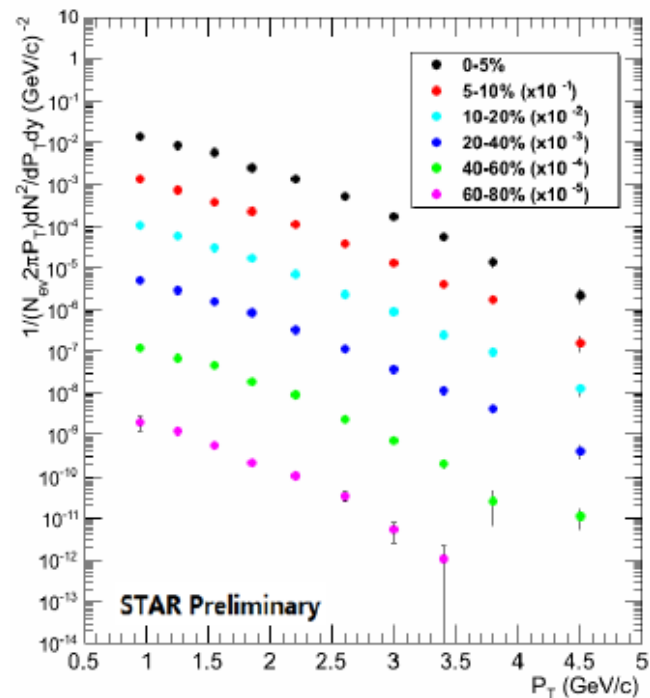


- Ratio decreases with the increase of centrality.
- Ratio decreases with energy.
- Ratio increases with mass.

$\Omega^-$  spectra, Au+Au 39 GeV



$\bar{\Omega}^+$  spectra, Au+Au 39 GeV



Strangeness vs. energy, centrality,...

Dependence of signature of phase transition  
near a Critical Point over a range  $\sqrt{s_{NN}} = 7.7-39$  GeV on flavor.

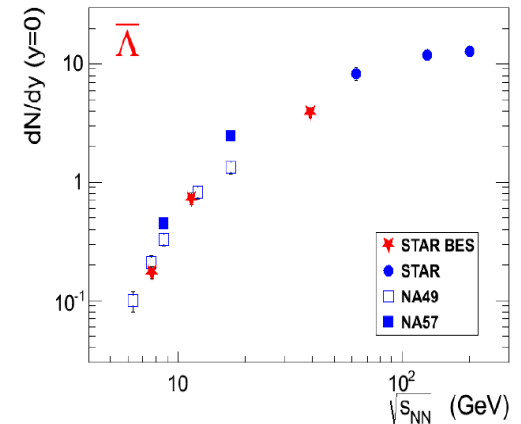
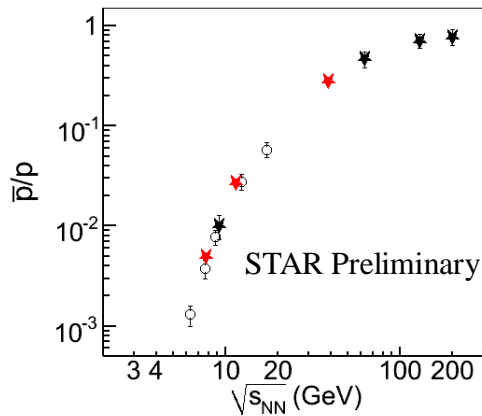
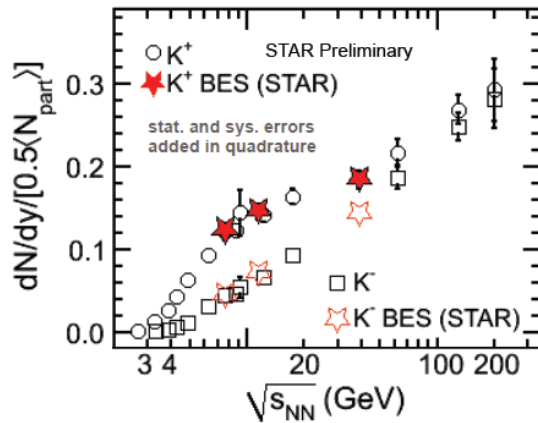
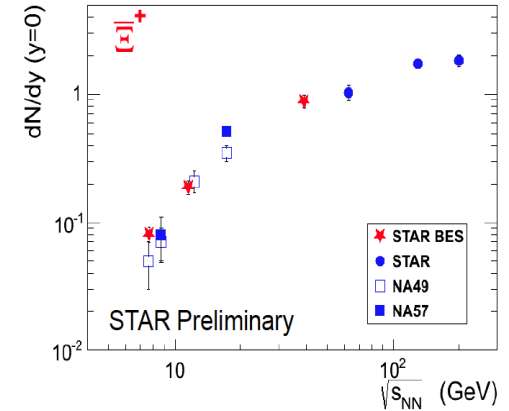
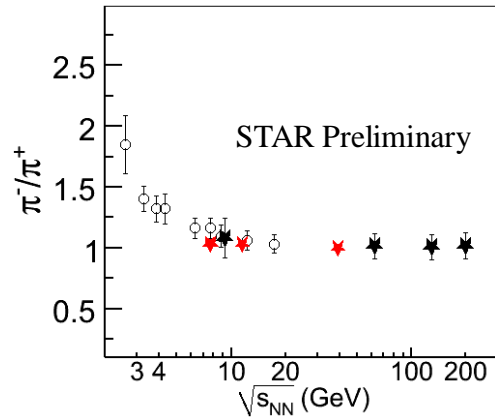
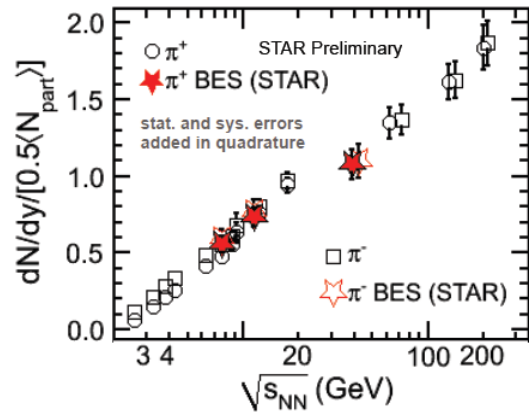


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## Comparison with other data

probing QCD phase diagram  
with identified particles:  $\pi$ ,  $\varphi$ ,  $K^\pm$ ,  $K_S^0$ ,  $\Lambda$ ,  $\Xi$ ,  $\Omega$ , ...  
in STAR BES program

# Spectra, particle ratios,... vs. energy, centrality

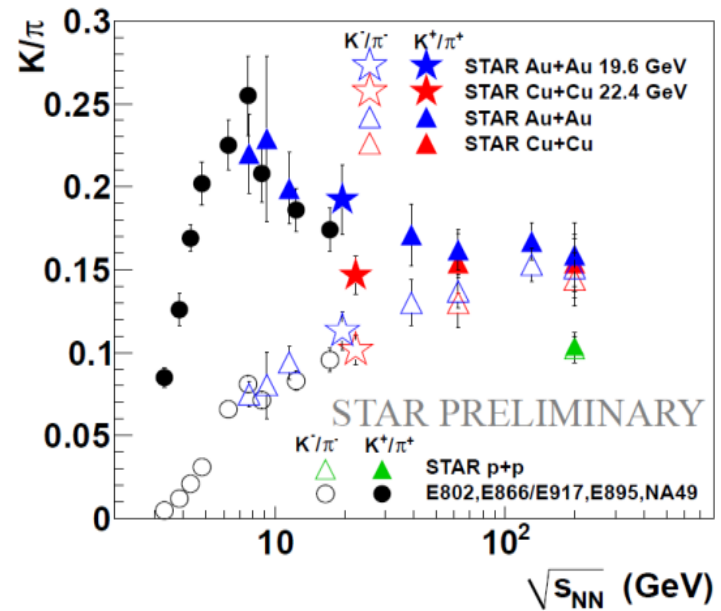
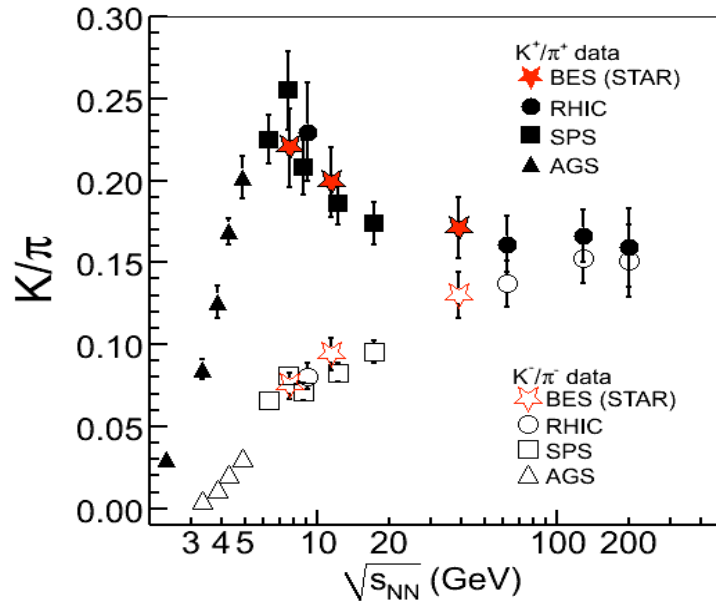


- General tendencies of new data are preserved
- Smooth dependencies are observed

A.Schmah, CPOD, Wuhan, China, Nov. 2011  
 M.Mitrovski, EPIC@LHC, Bari, July, 2011  
 L. Kumar, ICPAQGP 2010

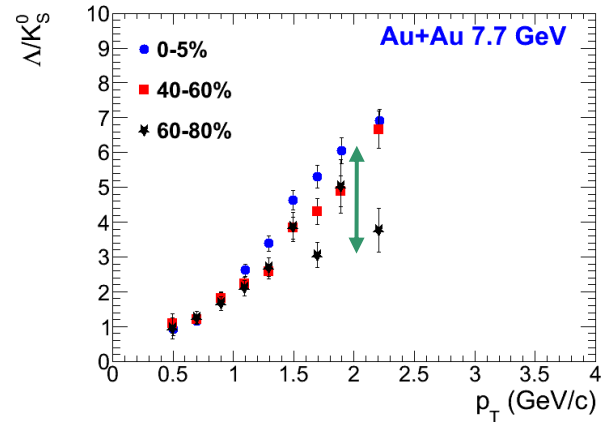
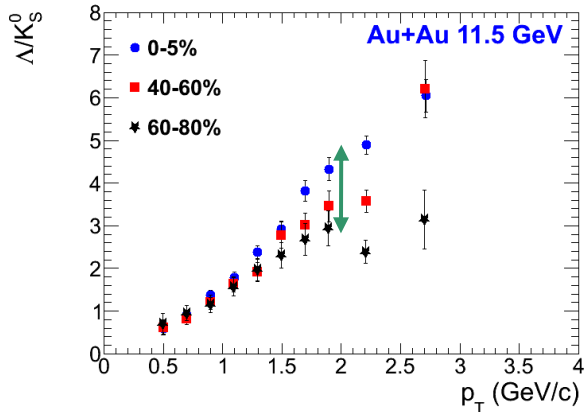
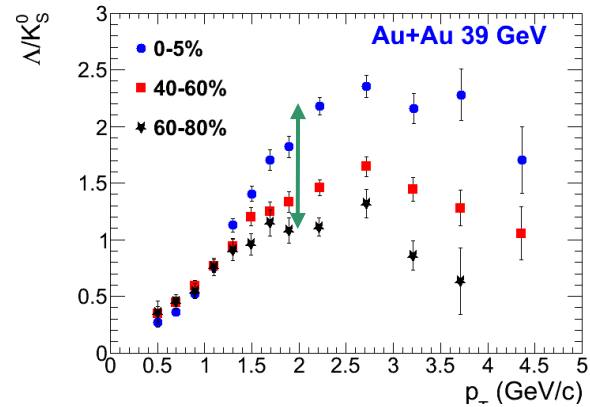
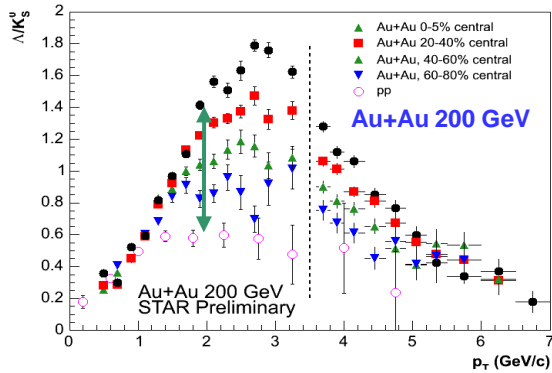


# Ratio $K/\pi$ vs. energy



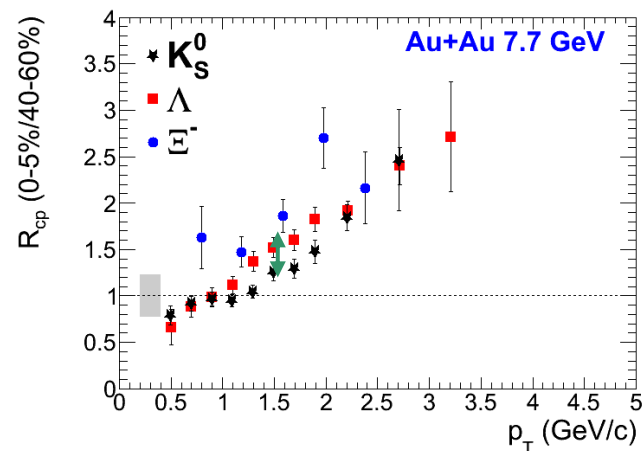
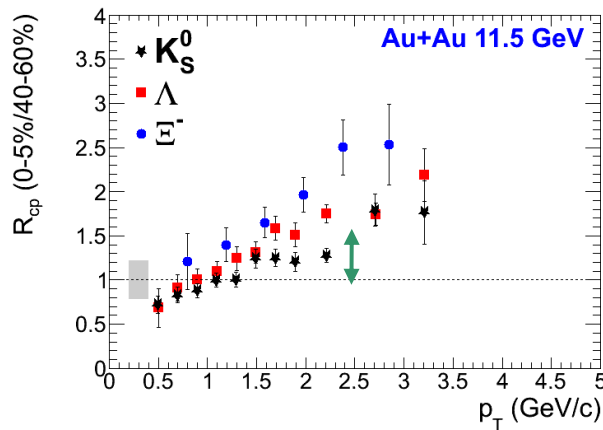
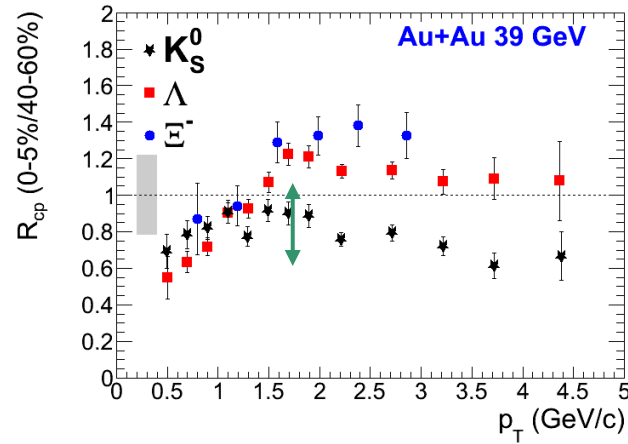
- Agreement with AGS, SPS data
- Enhanced  $K^+/\pi^+$  in comparison with  $K^-/\pi^-$

# $\Lambda/K^0_S$ ratio vs. energy and centrality



Ratio increases as the beam energy decreases.

# $R_{CP}$ ratio vs. energy and centrality

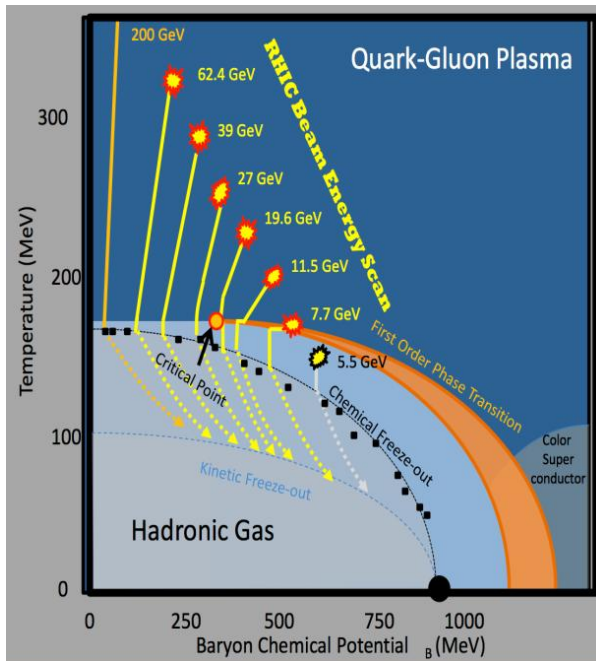


Baryon-meson splitting increases with energy.

# Beam Energy Scan in AuAu collisions at RHIC

PHASE I – completed with huge success !

(7.7, 11.5, 19.6, 27, 39 and 39 GeV runs) + 62 & 200 GeV



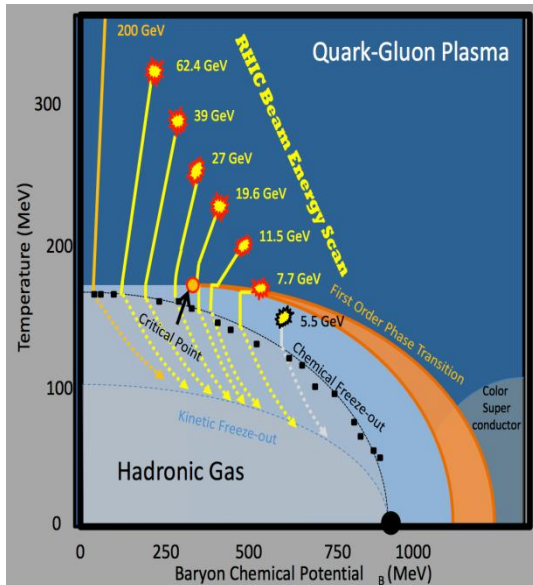
$\sqrt{s_{NN}}$ (GeV)	Good events in Million MB
5.0	
7.7	4.3
11.5	11.7
19.6	35.8
27	70.4
39	130.4

+ ~ 67.3 M @ 62.4 GeV

Extended  $\mu_B$  range covered by RHIC :  
20 ~ 400 MeV ( $\sqrt{s_{NN}} = 200 - 7.7$  GeV)

# Conclusions

- **B**eam **E**nergy **S**can program in **AuAu** collisions at **RHIC** was reviewed.
  - Experimental data and comparison with some models were presented.
  - **BES (I)** data demonstrate a smooth behavior vs. energy and centrality.
- No indications on discontinuity → more sophisticated analysis is required.
- High- $p_T$  spectra of charged hadrons at  $\sqrt{s_{NN}} = 7.7, 11.5, 19.6, 27, 39$  GeV are soon expected from **BES (I)** at **RHIC**.



The obtained results may be of interest in searching for a **Critical Point** and signatures of phase transition in hadron matter produced at **SPS, RHIC** and **LHC** in present, and **FAIR & NICA** in future.

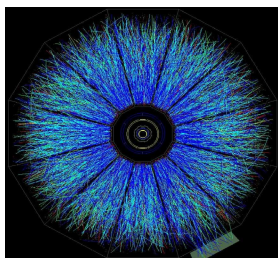


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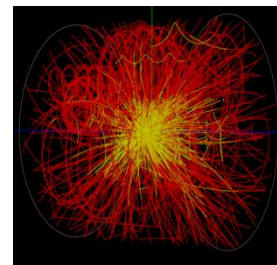
# **z**-Scaling & Search for Signatures of **Phase Transition** and **Critical Point**

**M. Tokarev**

JINR, Dubna, Russia



Письма в ЭЧАЯ, 7 (2010) 271.  
Phys.Part.Nucl.Lett., 8 (2011) 533.  
Phys.At.Nucl., 75 (2012) 700.



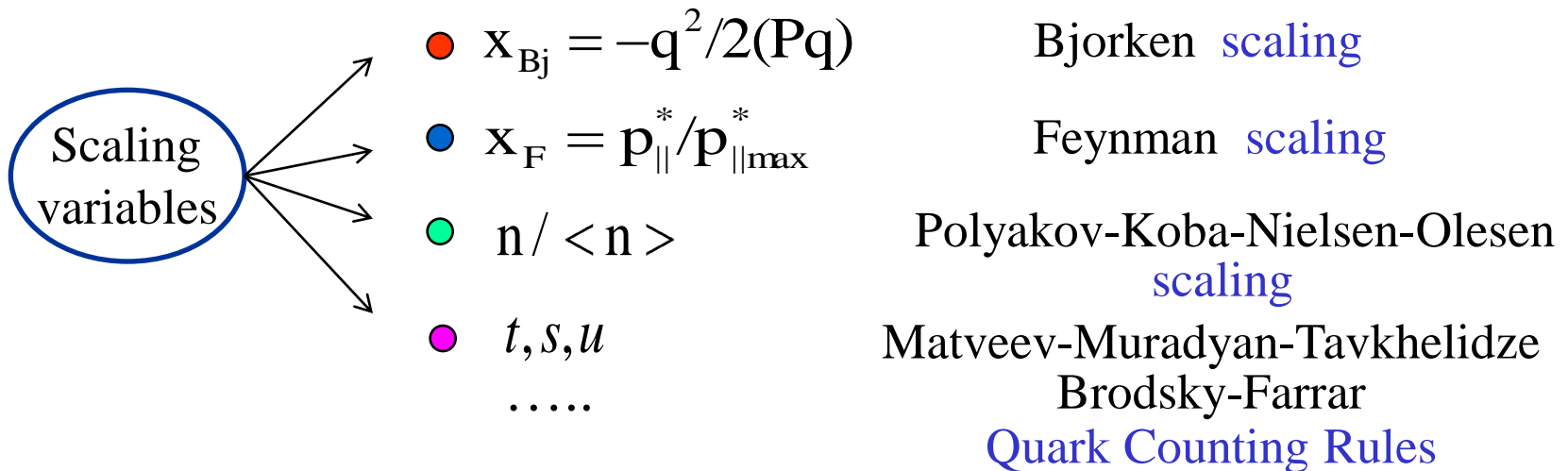
in collaboration  
with Yu.Panebratsev, I.Zborovský, A.Kechechyan,  
A.Aлахverdyan, A.Aparin

# Contents

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- Introduction
- BES at RHIC
- z-Scaling (ideas, definitions, properties,...)
- Self-similarity of hadron production in pp & AA
- Energy loss in pp & AA
- Signatures of phase transition & Critical Point
- Conclusions

# Regularities in high energy interactions



- These scaling regularities have restricted range of validity.
- Violation of the scaling laws can be indication of new physics.

New regularity - **z-Scaling**  
Universal description of inclusive particle cross sections  
over a wide kinematical region

(central+fragmentation region,  $p_T > 0.5 \text{ GeV}/c$ ,  $s^{1/2} > 20 \text{ GeV}$ )

**z-Scaling** reveals self-similar properties in hadron, jet and direct photon production in high energy hadron and nucleus collisions.

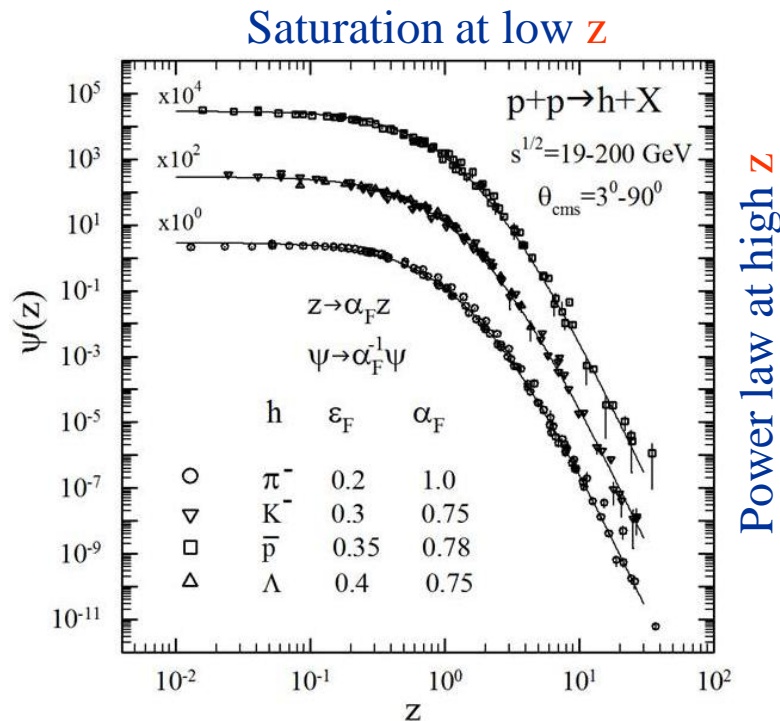
# Scaling & Universality & Saturation

Inclusive cross sections of  $\pi^-, K^-, \bar{p}, \Lambda$  in pp collisions

FNAL:  
PRD 75 (1979) 764

ISR:  
NPB 100 (1975) 237  
PLB 64 (1976) 111  
NPB 116 (1976) 77  
(low  $p_T$ )  
NPB 56 (1973) 333  
(small angles)

STAR:  
PLB 616 (2005) 8  
PLB 637 (2006) 161  
PRC 75 (2007) 064901



Energy scan of spectra at U70, ISR, SppS, SPS, HERA, FNAL(fixed target), Tevatron, RHIC, LHC

MT & I.Zborovsky  
Phys.Rev.D75,094008(2007)  
Int.J.Mod.Phys.A24,1417(2009)

- Energy & angular independence
- Flavor independence ( $\pi, K, \bar{p}, \Lambda$ )
- Saturation for  $z < 0.1$
- Power law  $\Psi(z) \sim z^{-\beta}$  for high  $z > 4$

Scaling – “collapse” of data points onto a single curve.

Scaled particle yield ( $\Psi$ ) vs. scaled variable ( $z$ ).

Universality classes – hadron species ( $\epsilon_F, \alpha_F$ ).



# Goals

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Development of **z**-scaling approach for description of hadron production in inclusive reactions to search for signatures of new state of nuclear matter (phase transitions, critical point, ...)

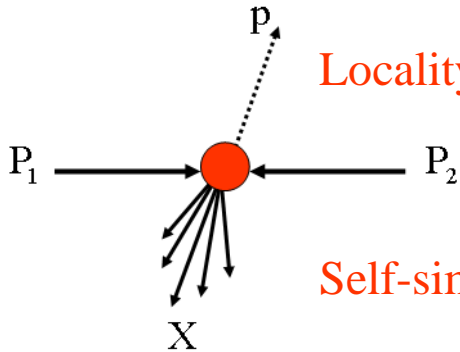
Analysis of **AA** experimental data obtained at RHIC & SPS to verify properties of **z**-scaling observed in **pp** &  $\bar{p}p$  collisions at U70, ISR,  $S\bar{p}pS$ , SPS and Tevatron.

Estimation of constituent energy loss in central **AA** collisions vs. collision energy, centrality, transverse momentum over the range  $\sqrt{s_{NN}} = 7.7-200$  GeV

**Problem:** Impurities and defects smear phase transition. Low energy loss region is preferable for search for CP.

# z-Scaling

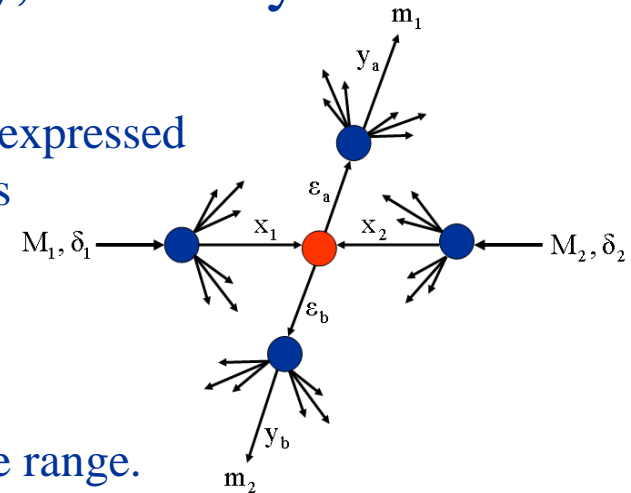
**Principles:** locality, self-similarity, fractality



**Locality:** collisions of hadrons and nuclei are expressed via interactions of their constituents (partons, quarks and gluons,...).

**Self-similarity:** interactions of the constituents are mutually similar.

**Fractality:** the self-similarity over a wide scale range.



## Hypothesis of z-scaling:

$s^{1/2}, p_T, \theta_{\text{cms}}$  Inclusive particle distributions can be described in terms of constituent sub-processes and parameters characterizing bulk properties of the system.

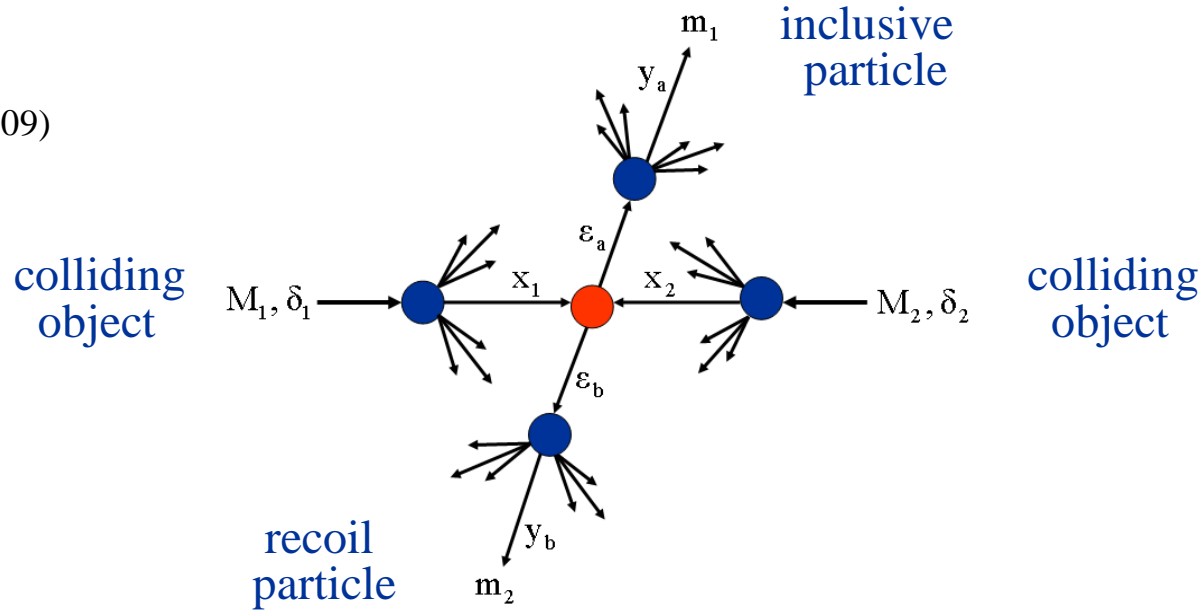
$x_1, x_2, y_a, y_b$   
 $\delta_1, \delta_2, \epsilon_a, \epsilon_b, c$

$Ed^3\sigma/dp^3$  Scaled inclusive cross section of particles depends in a self-similar way on a single scaling variable  $z$ .

$\Psi(z)$

# Locality of hadron interactions

M.T. & I.Zborovský  
 Part.Nucl.Lett.312(2006)  
 PRD75,094008(2007)  
 Int.J.Mod.Phys.A24,1417(2009)  
 J.Phys.G: Nucl.Part.Phys.  
 37,085008(2010)



## Constituent subprocess

$$(\mathbf{x}_1 M_1) + (\mathbf{x}_2 M_2) \Rightarrow (m_1/y_a) + (\mathbf{x}_1 M_1 + \mathbf{x}_2 M_2 + m_2/y_b)$$

Kinematical condition (4-momentum conservation law):

$$(\mathbf{x}_1 P_1 + \mathbf{x}_2 P_2 - p/y_a)^2 = M_X^2$$

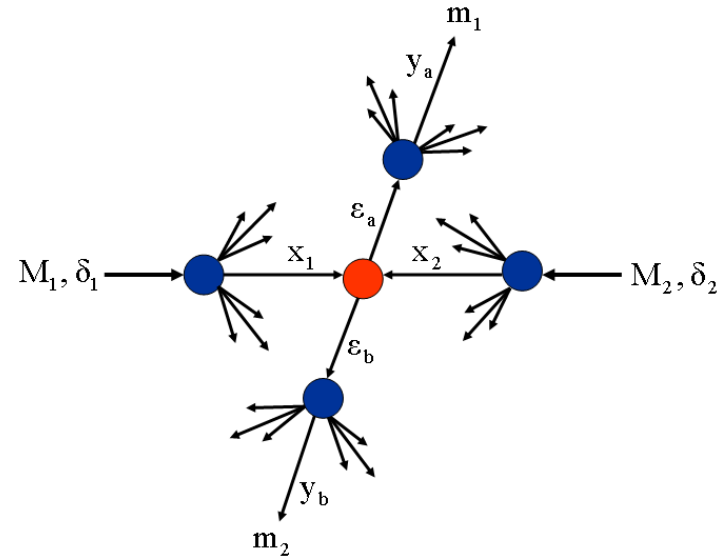
Recoil mass:  $M_X = \mathbf{x}_1 M_1 + \mathbf{x}_2 M_2 + m_2/y_b$



# Self-similarity parameter $Z$

$$Z = z_0 \cdot \Omega^{-1}$$

$$z_0 = \frac{s_{\perp}^{1/2}}{(dN_{\text{ch}}/d\eta|_0)^c m}$$



- $\Omega^{-1}$  is the minimal resolution at which a constituent subprocess can be singled out of the inclusive reaction
- $s_{\perp}^{1/2}$  is the transverse kinetic energy of the subprocess consumed on production of  $m_1$  &  $m_2$
- $dN_{\text{ch}}/d\eta|_0$  is the multiplicity density of charged particles at  $\eta = 0$
- $c$  is a parameter interpreted as a “specific heat” of created medium
- $m$  is an arbitrary constant (fixed at the value of nucleon mass)

# Fractal measure $z$

The fractality is reflected in definition of  $z$

$$z = z_0 \Omega^{-1}$$

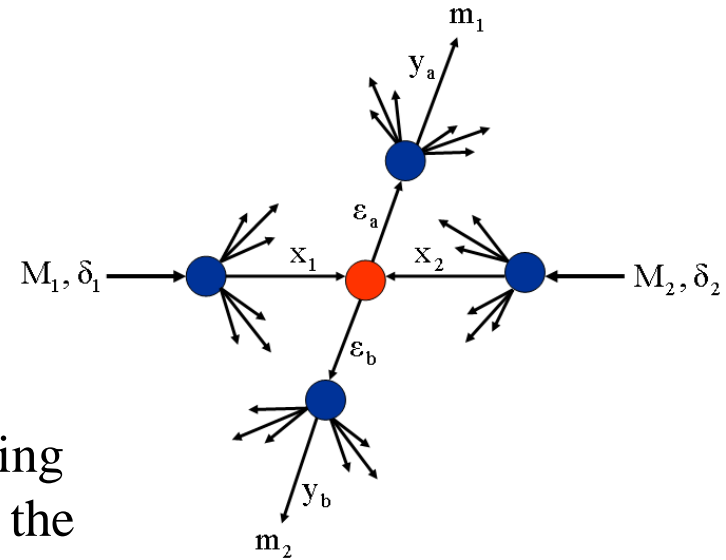
$$\Omega = (1 - x_1)^{\delta_1} (1 - x_2)^{\delta_2} (1 - y_a)^{\varepsilon_a} (1 - y_b)^{\varepsilon_b}$$

$\Omega$  is relative number of configurations containing a sub-process with fractions  $x_1, x_2, y_a, y_b$  of the corresponding 4-momenta

$\delta_1, \delta_2, \varepsilon_a, \varepsilon_b$  are parameters characterizing structure of the colliding objects and fragmentation process, respectively

$\Omega^{-1}(x_1, x_2, y_a, y_b)$  characterizes resolution at which a constituent sub-process can be singled out of the inclusive reaction

$z(\Omega) \Big|_{\Omega^{-1} \rightarrow \infty} \rightarrow \infty$  The fractal measure  $z$  diverges as the resolution  $\Omega^{-1}$  increases.



# Momentum fractions $x_1, x_2, y_a, y_b$

**Principle of minimal resolution:** The momentum fractions  $x_1, x_2$  and  $y_a, y_b$  are determined in a way to minimize the resolution  $\Omega^{-1}$  of the fractal measure  $z$  with respect to all constituent sub-processes taking into account 4-momentum conservation:

$$\Omega = (1 - x_1)^{\delta_1} (1 - x_2)^{\delta_2} (1 - y_a)^{\varepsilon_a} (1 - y_b)^{\varepsilon_b}$$

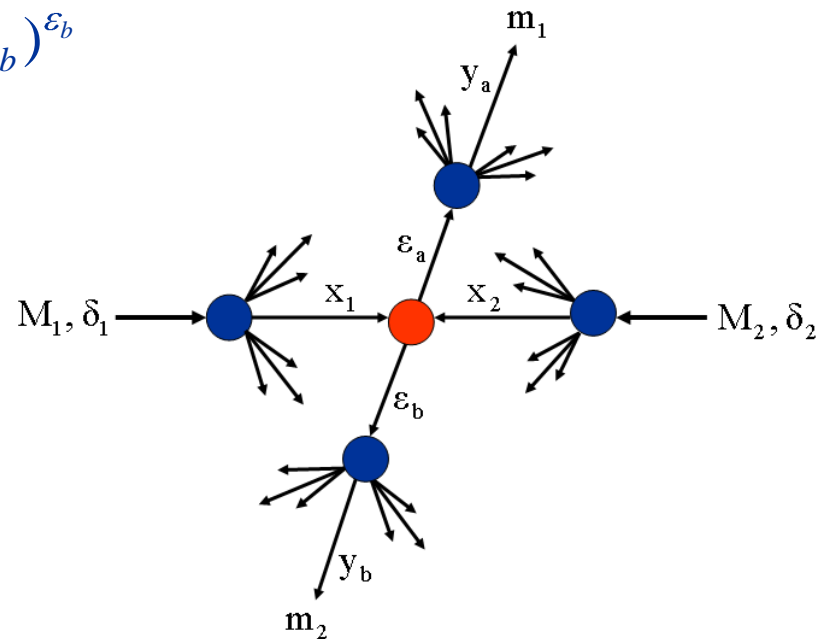
$$\begin{cases} \partial\Omega / \partial x_1 |_{y_a=y_a(x_1, x_2, y_b)} = 0 \\ \partial\Omega / \partial x_2 |_{y_a=y_a(x_1, x_2, y_b)} = 0 \\ \partial\Omega / \partial y_b |_{y_a=y_a(x_1, x_2, y_b)} = 0 \end{cases}$$

**Momentum conservation law)**

$$(x_1 P_1 + x_2 P_2 - p / y_a)^2 = M_X^2$$

**Recoil mass**

$$M_X = x_1 M_1 + x_2 M_2 + m_2 / y_b$$



# Transverse kinetic energy $s_{\perp}^{1/2}$ consumed on production of $m_1$ & $m_2$

$$s_{\perp}^{1/2} = y_1 (s_{\lambda}^{1/2} - M_1 \lambda_1 - M_2 \lambda_2) - m_1 + y_2 (s_{\chi}^{1/2} - M_1 \chi_1 - M_2 \chi_2) - m_2$$

energy consumed  
for the inclusive particle  $m_1$

energy consumed  
for the recoil particle  $m_2$

**Decomposition:**  $x_{1,2} = \lambda_{1,2} + \chi_{1,2}$

$$\lambda_{1,2} = \kappa_{1,2} / y_1 + v_{1,2} / y_2$$

$$\chi_{1,2} = (\mu_{1,2}^2 + \omega_{1,2}^2)^{1/2} \mp \omega_{1,2}$$

$$\omega_{1,2} = \mu_{1,2} U, \quad U = \frac{\alpha - 1}{2\sqrt{\alpha}} \xi, \quad \alpha = \frac{\delta_2}{\delta_1}$$

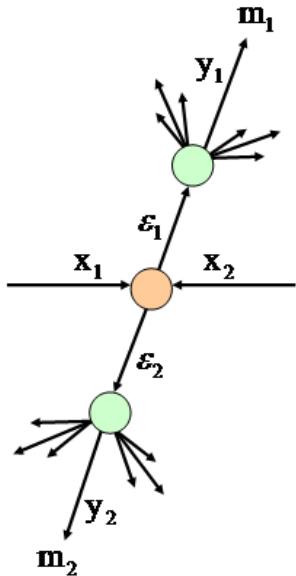
$$\xi^2 = (\lambda_1 \lambda_2 + \lambda_0) / [(1 - \lambda_1)(1 - \lambda_2)]$$

$$\kappa_{1,2} = \frac{(P_{2,1} P)}{(P_2 P_1)}, \quad v_{1,2} = \frac{M_{2,1} m_2}{(P_2 P_1)}$$

$$\mu_{1,2}^2 = \alpha^{\pm 1} (\lambda_1 \lambda_2 + \lambda_0) \frac{1 - \lambda_{1,2}}{1 - \lambda_{2,1}}$$

$$\lambda_0 = \bar{v}_0 / y_2^2 - v_0 / y_1^2$$

$$\bar{v}_0 = \frac{0.5 m_2^2}{(P_1 P_2)}, \quad v_0 = \frac{0.5 m_1^2}{(P_1 P_2)}$$

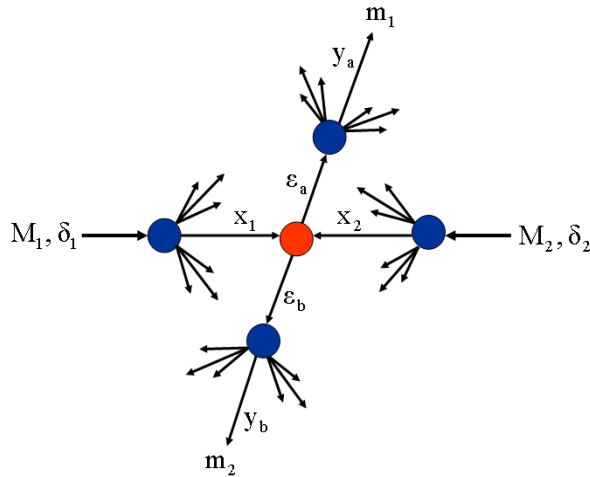


$$s_{\lambda} = (\lambda_1 P_1 + \lambda_2 P_2)^2$$

$$s_{\chi} = (\chi_1 P_1 + \chi_2 P_2)^2$$

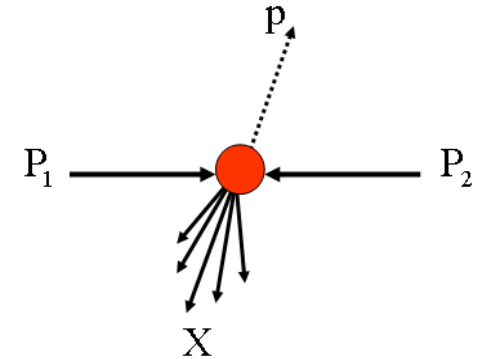
All dimensionless quantities are expressed via relativistic invariants.

# Scaling function $\Psi(z)$



$$\int_0^{\infty} \Psi(z) dz = 1$$

$$z \rightarrow \alpha_F z, \quad \Psi \rightarrow \alpha_F^{-1} \Psi$$



$$\Psi(z) = \frac{\pi}{(dN/d\eta) \cdot \sigma_{inel}} \cdot J^{-1} \cdot E \frac{d^3\sigma}{dp^3} \iff \int E \frac{d^3\sigma}{dp^3} dy d^2p_{\perp} = \sigma_{inel} \cdot N$$

- $\sigma_{in}$  - inelastic cross section
- $N$  - average multiplicity of the corresponding hadron species
- $dN/d\eta$  - pseudorapidity multiplicity density at angle  $\theta$  ( $\eta$ )
- $J(z, \eta; p_T^2, y)$  - Jacobian
- $E d^3\sigma/dp^3$  - inclusive cross section

The scaling function  $\Psi(z)$  is probability density to produce an inclusive particle with the corresponding  $z$ .

# Properties of $\Psi(z)$ in $pp$ & $\bar{p}p$ collisions

- Energy independence of  $\Psi(z)$  ( $\sqrt{s} > 20 \text{ GeV}$ )
- Angular independence of  $\Psi(z)$  ( $\theta_{\text{cms}} = 3^\circ - 90^\circ$ )
- Multiplicity independence of  $\Psi(z)$  ( $dN_{\text{ch}}/d\eta = 1.5 - 26$ )
- Power law,  $\Psi(z) \sim z^{-\beta}$ , at high  $z$  ( $z > 4$ )
- Flavor independence of  $\Psi(z)$  ( $\pi, K, \phi, \Lambda, \dots, D, J/\psi, B, \Upsilon, \dots$ )
- Saturation of  $\Psi(z)$  at low  $z$  ( $z < 0.1$ )

These properties reflect self-similarity, locality, and fractality of the hadron interaction at constituent level. It concerns the structure of the colliding objects, interactions of their constituents, and fragmentation process.

M.T. & I.Zborovsky  
Phys.At.Nucl. 70,1294(2007)  
Phys.Rev. D75,094008(2007)  
Int.J.Mod.Phys. A24,1417(2009)  
J. Phys.G: Nucl.Part.Phys. 37,085008(2010)

# z-Scaling & Heavy Ion Collisions

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z-Scaling reflects self-similarity, locality and fractality of particle production at a constituent level.

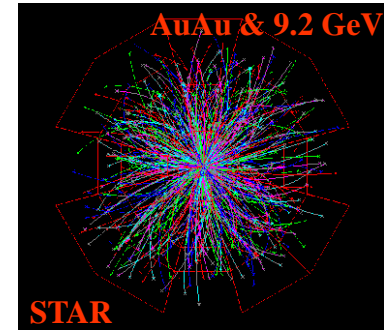
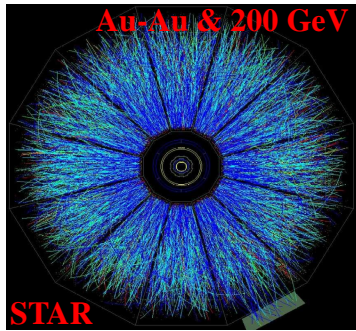
The variable  $z$  is a self-similarity parameter.

New tool in searching for signatures of new state of nuclear matter created in HIC at high energy and high multiplicity density (phase transition, critical point, QGP...)

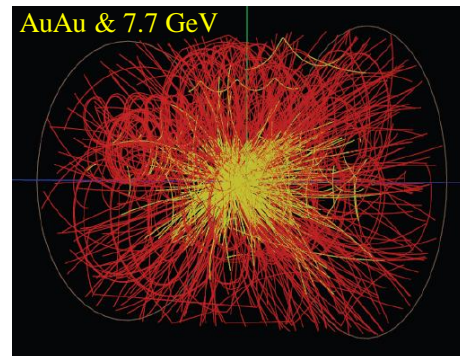
- Scaling in  $pp / \bar{p}p$  collisions is a reference frame for AA collisions.
- Observed scaling features in AA are sensitive characteristics of nuclear matter and signatures of new medium created in HIC.
- Change of parameters of z-scaling can indicate a phase transition.

Analysis of experimental data on charged hadrons produced in AuAu collisions at  $\sqrt{s_{NN}} = 7.7-200$  GeV at RHIC to search for CP & estimation of particle energy loss.



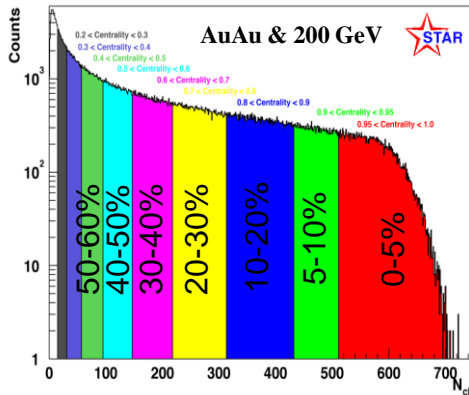


## Self-similarity of hadron production in $pp$ & $AA$ collisions



# Self-similarity parameter $z$ in AA collisions

$$z = z_0 \Omega^{-1} \quad z_0 = \frac{s_{\perp}^{1/2}}{(dN_{ch}/d\eta|_0)^c m_N} \quad \Omega = (1-x_1)^{\delta_{A1}} (1-x_2)^{\delta_{A2}} (1-y_a)^{\varepsilon} (1-y_b)^{\varepsilon}$$



## Ingredients of $z$ characterizing AA collisions:

- $dN_{ch}/d\eta|_0$  - multiplicity density in AA collisions
- $c$  - “specific heat” in AA collisions
- $\delta_A$  - nucleus fractal dimension
- $\varepsilon$  - fragmentation dimension in AA collisions

These quantities characterize properties of medium created in AA collisions.

## Additivity of fractal dimensions $\delta_A$ in pA collisions: $\delta_A = A\delta$

consistent with  $z$ -scaling in pD, pBe, pTi, pW collisions

This property is connected with factorization of  $\Omega = \dots(1-x_1)(1-x_2)^{A\delta} \dots$   
for small values of  $x_2 \equiv x_A \equiv x_N/A$ .

$$\delta_{A1} = A_1 \delta \quad \& \quad \delta_{A2} = A_2 \delta \quad \text{for AA collisions}$$

MT  
I.Zborovsky  
Yu.Panebratsev  
G.Skoro  
PRC 59 (1999) 2227



# Variable $z$ & Entropy $S$

$$z = z_0 \Omega^{-1}$$

$$z_0 = \frac{s_{\perp}^{1/2}}{(dN_{ch}/d\eta|_0)^c m_N} \quad \Omega = (1-x_1)^{\delta_1} (1-x_2)^{\delta_2} (1-y_a)^{\varepsilon} (1-y_b)^{\varepsilon}$$

$$z \cong \frac{s_{\perp}^{1/2}}{W}$$

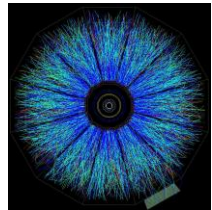
$W = (dN_{ch}/d\eta|_0)^c \cdot \Omega$  - relative number of such constituent configurations which contain the configuration  $\{x_1, x_2, y_a, y_b\}$

Statistical entropy:

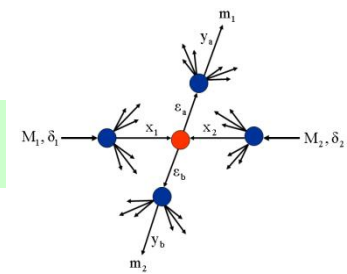
$$S = \ln W$$

Thermodynamical entropy for ideal gas:

$$S = c_V \ln T + R \ln V + S_0$$



$$S = c \cdot \ln(dN_{ch}/d\eta|_0) + \ln[(1-x_1)^{\delta_1} (1-x_2)^{\delta_2} (1-y_a)^{\varepsilon} (1-y_b)^{\varepsilon}] + \ln W_0$$



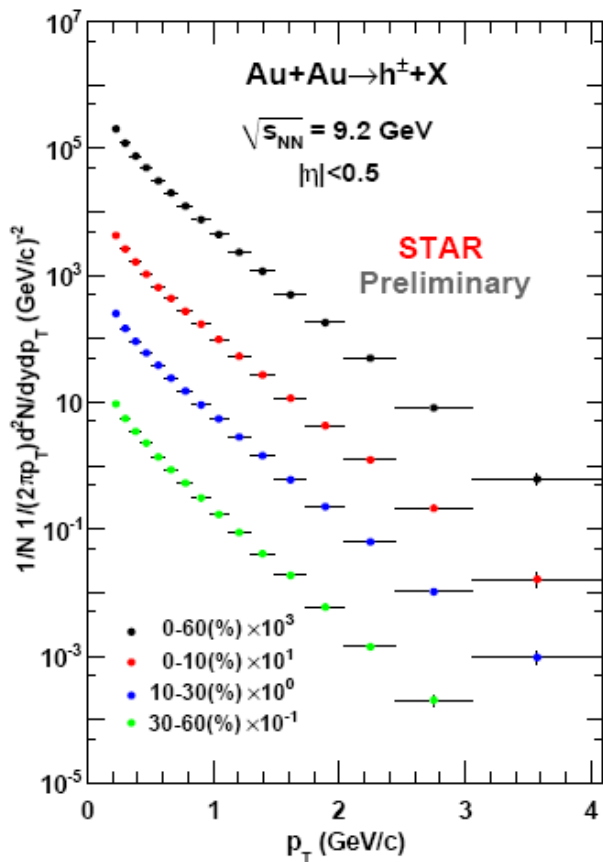
- $dN_{ch}/d\eta|_0$  characterizes “temperature” of the colliding system.
- Provided local equilibrium,  $dN_{ch}/d\eta|_0 \sim T^3$  for high temperatures and small  $\mu$ .
- $c$  has meaning of a “specific heat” of the produced medium.
- Fractional exponents  $\delta_1, \delta_2, \varepsilon$  are fractal dimensions in the space of  $\{x_1, x_2, y_a, y_b\}$ .
- Entropy increases with  $dN_{ch}/d\eta|_0$  and decreases with increasing resolution  $\Omega^{-1}$ .

Maximal entropy  $S \Leftrightarrow$  minimal resolution  $\Omega^{-1}$  of the fractal measure  $z$



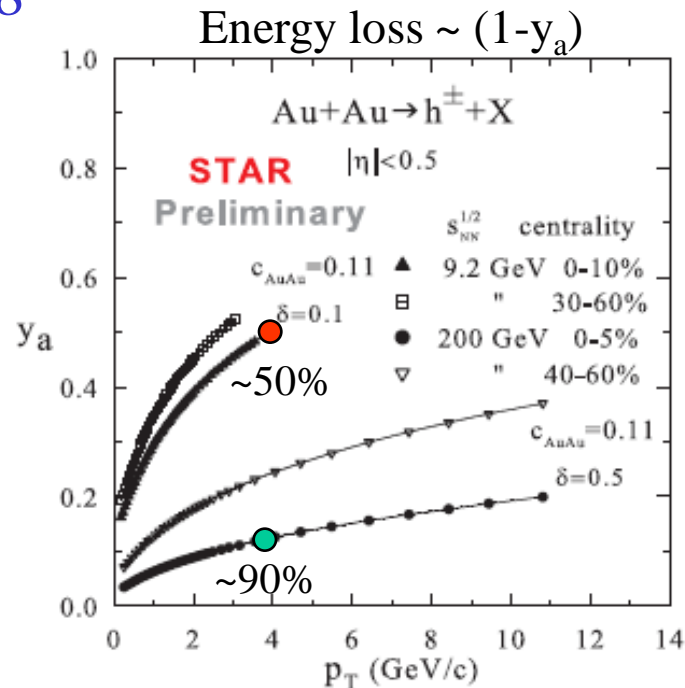
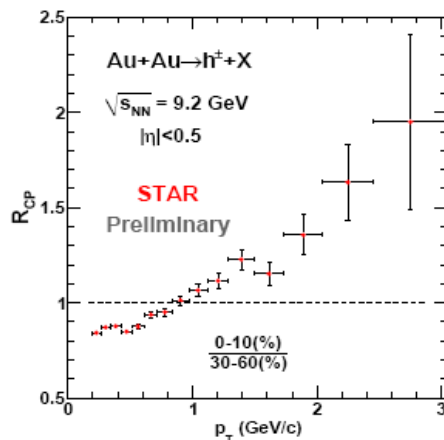
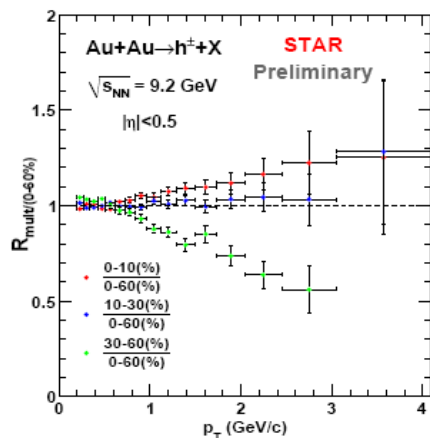
# High- $p_T$ Spectra of Charged Hadrons in Au+Au Collisions at $\sqrt{s_{NN}} = 9.2$ GeV in STAR

STAR test Run 2008



STAR: Phys. At. Nucl., 2011,  
V.74, No5, p.769

STAR, PRC 81 (2010) 024911

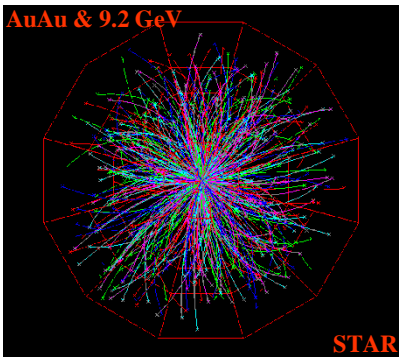


Data sample (2008)

~ 4000 events (!!!)

- High- $p_T$  spectra vs. centrality
- $R_{CP}$  ratio vs.  $p_T$
- Energy loss vs.  $p_T$ ,  $dN/d\eta$

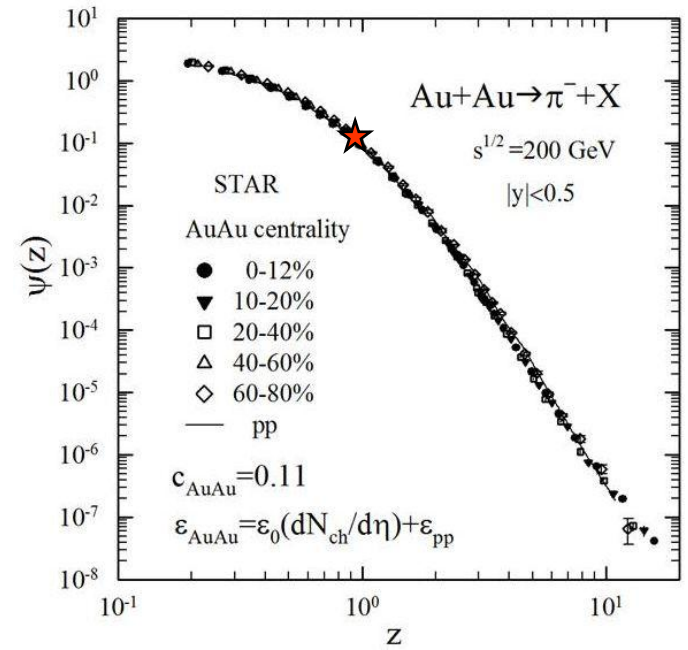
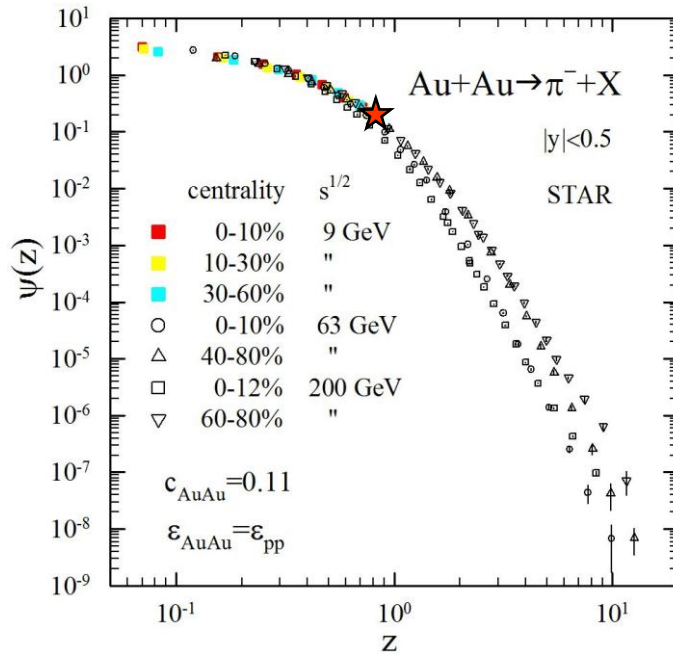
# Energy scan of spectra in AuAu collisions



STAR  
PLB 637 (2006) 161  
PRL 97 (2006) 152301  
PLB 655 (2007) 104

STAR  
PRC 81 (2010) 024911

## $\pi^-$ in AuAu at 9.2 & 63, 200 GeV



$$z = \frac{s_{\perp}^{1/2}}{(dN_{ch}/d\eta|_0)^c} \Omega^{-1}$$

$$\Omega = (1-x_1)^{\delta_A} (1-x_2)^{\delta_A} (1-y_a)^{\epsilon} (1-y_b)^{\epsilon}$$

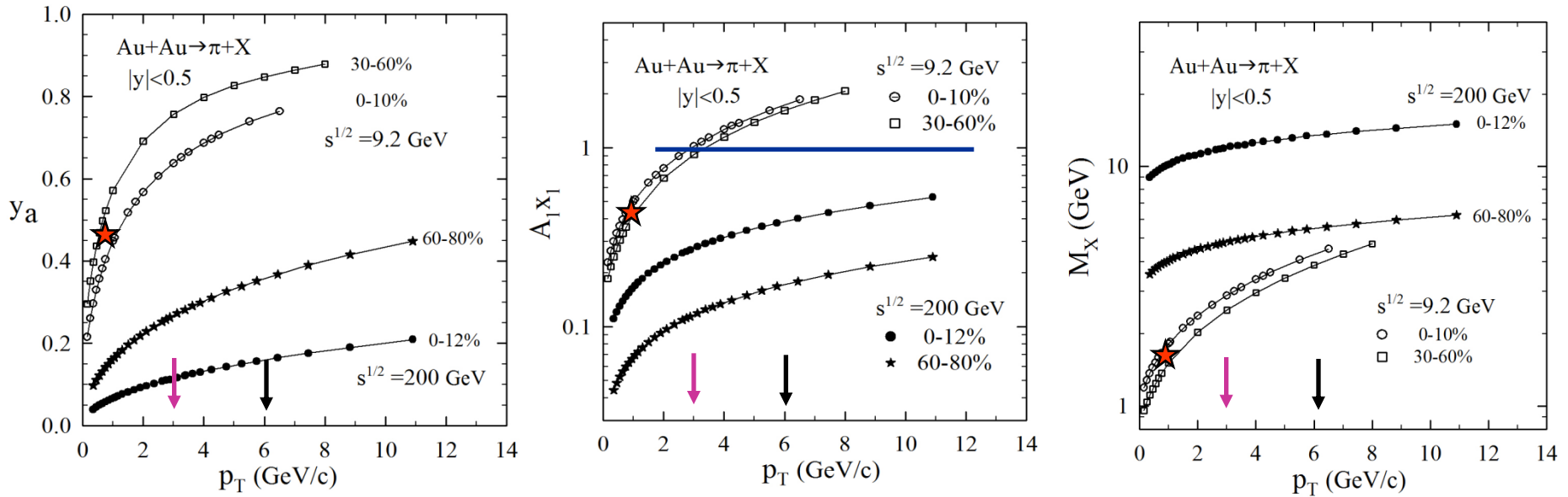
$$\delta_A = A\delta$$

- Saturation of  $\Psi(z)$  for  $z < 0.1$
- Power law for  $z > 4$
- Centrality dependence of  $\Psi(z)$  at high  $z$
- Fractal dimension  $\epsilon$  depends on centrality
- Spectra at high  $p_T$  are sensitive to  $c$ - $\delta$  correlation



# Energy losses $\sim(1-y_a)$ vs. energy, centrality, $p_T$

## $\pi^-$ in AuAu at 9.2 & 200 GeV



- $y_a$  increases with  $p_T \Rightarrow$  energy losses decreases with  $p_T$
- $y_a$  decreases with centrality  $\Rightarrow$  energy losses increase with centrality
- $x_1$  is independent of centrality at 9.2 GeV
- $M_X$  increases with  $p_T$ ,  $\sqrt{s_{NN}}$  and centrality

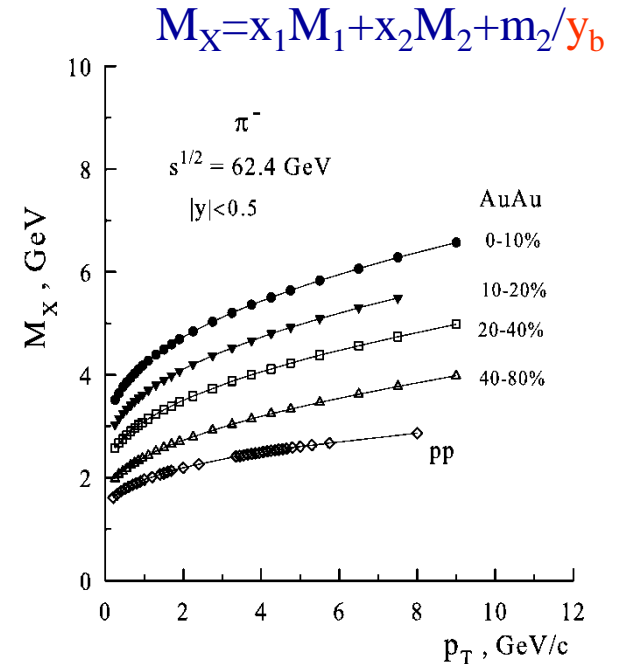
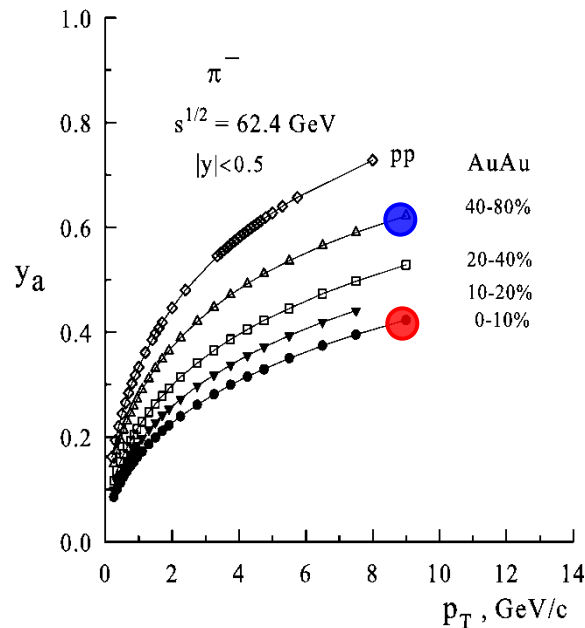
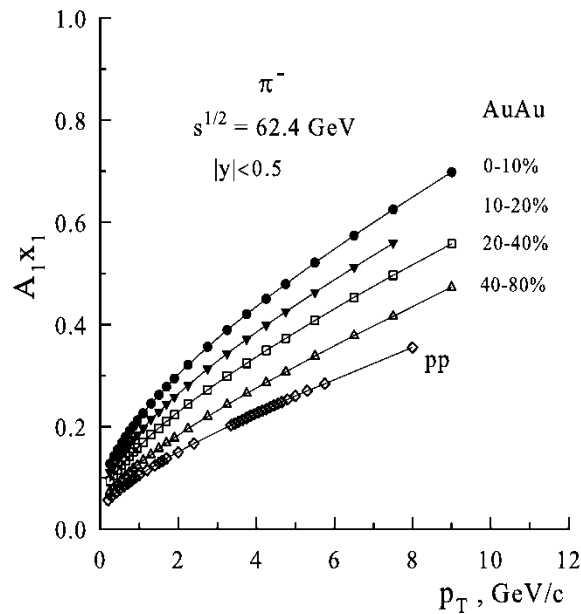
Smaller energy losses  $\Rightarrow$  better localization of a **Critical Point**

Cumulative region ( $A_1 x_1 > 1$ ) is most preferable to search for a **Critical Point**

# Momentum fractions $x_1$ , $y_a$ & recoil mass $M_X$

STAR

$\pi^-$  in AuAu at 62.4 GeV



- $p_T$  dependence of  $x_1$  is dependent of centrality
- $y_a$  increases with  $p_T \Rightarrow$  energy losses decrease with  $p_T$
- $y_a$  decreases with centrality  $\Rightarrow$  energy losses increase with centrality
- $M_X$  increases with  $p_T$ ,  $s^{1/2}$  and centrality

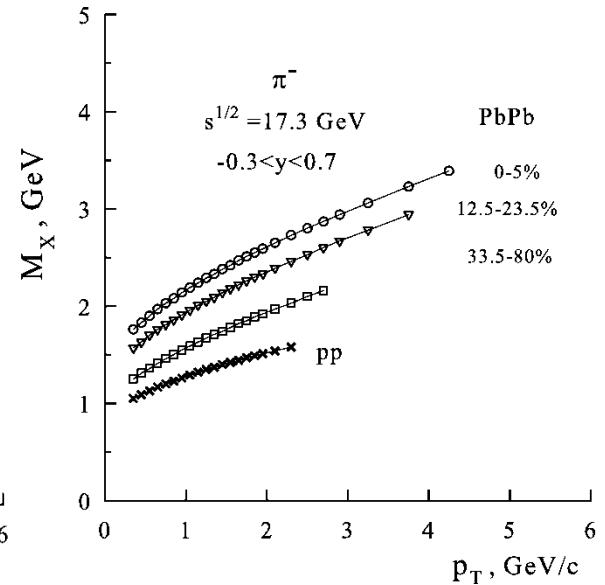
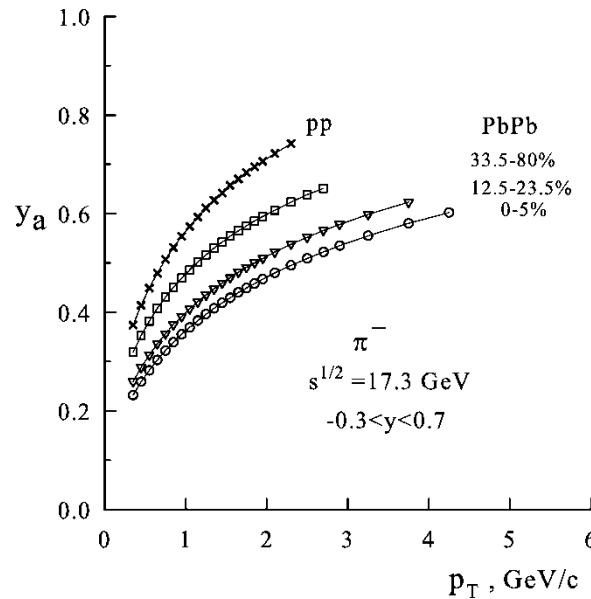
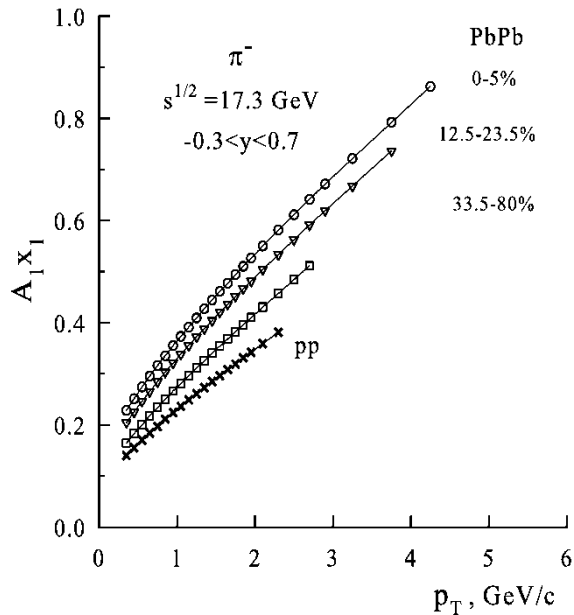


# Momentum fractions $x_1$ , $y_a$ & recoil mass $M_X$

NA49

$\pi^-$  in PbPb at 17.3 GeV

$$M_X = x_1 M_1 + x_2 M_2 + m_2 / y_b$$

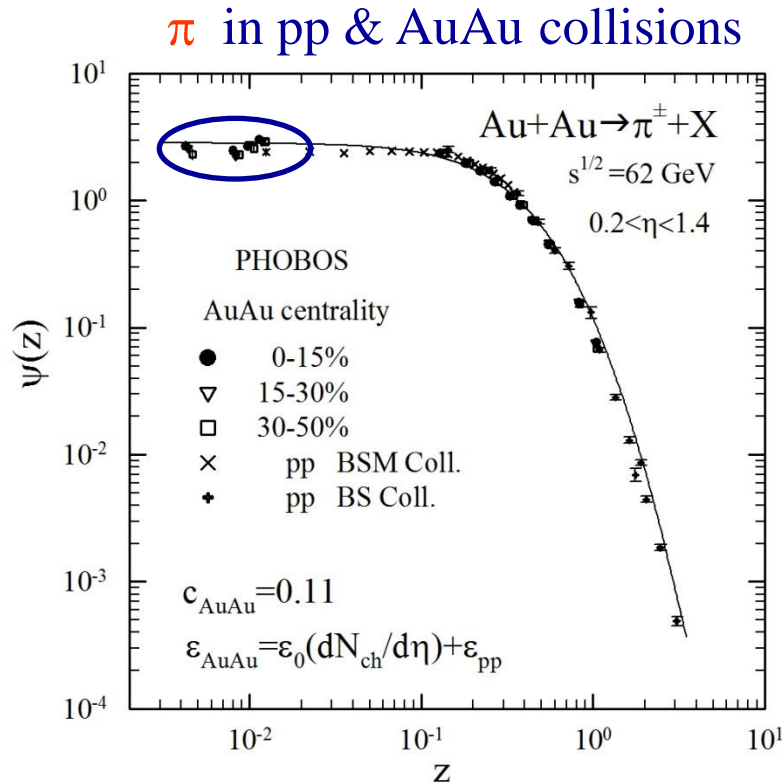


- $p_T$  dependence of  $x_1$  is dependent of centrality
- $y_a$  increases with  $p_T \Rightarrow$  energy losses decrease with  $p_T$
- $y_a$  decreases with centrality  $\Rightarrow$  energy losses increase with centrality
- $M_X$  increases with  $p_T$ ,  $s^{1/2}$  and centrality

# Saturation of $\Psi(z)$ at low $z$ in AuAu collisions

PHOBOS:  
PRC 75 (2007) 024910

ISR:  
NPB 100 (1975) 237  
PLB 64 (1976) 111 (low  $p_T$ )



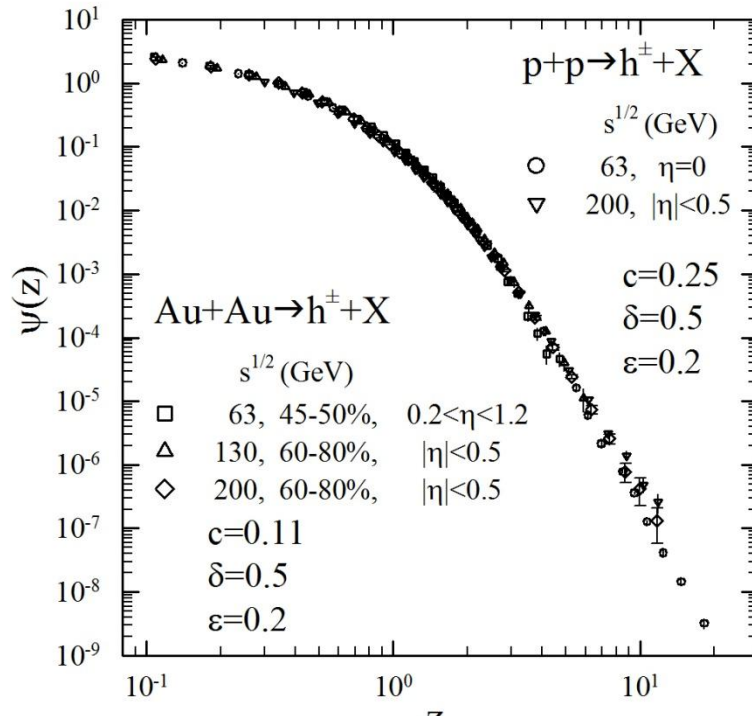
$$z \cong \frac{s_{\perp}^{1/2}}{(dN_{ch}/d\eta|_0)^c}$$

at low  $z$  (low  $p_T$ )

- The saturation of  $\Psi(z)$  in AuAu for  $z < 0.1$
- The centrality (multiplicity) independence of  $\Psi(z)$  in AuAu
- Restoration of the shape of  $\Psi(z)$  over a wide  $z$ -range

# Self-similarity in peripheral AuAu collisions

## Charged hadrons in pp & AA @ 63, 130, 200 GeV



ISR: NPB 208 (1982)1

STAR: PRL 89 (2002) 202301;  
 PRL 91 (2003) 172302

PHOBOS: PRL 94 (2005) 082304

**pp collisions:**

$dN_{ch}/d\eta|_0$  for non-single-diffractive events

**AA collisions:**

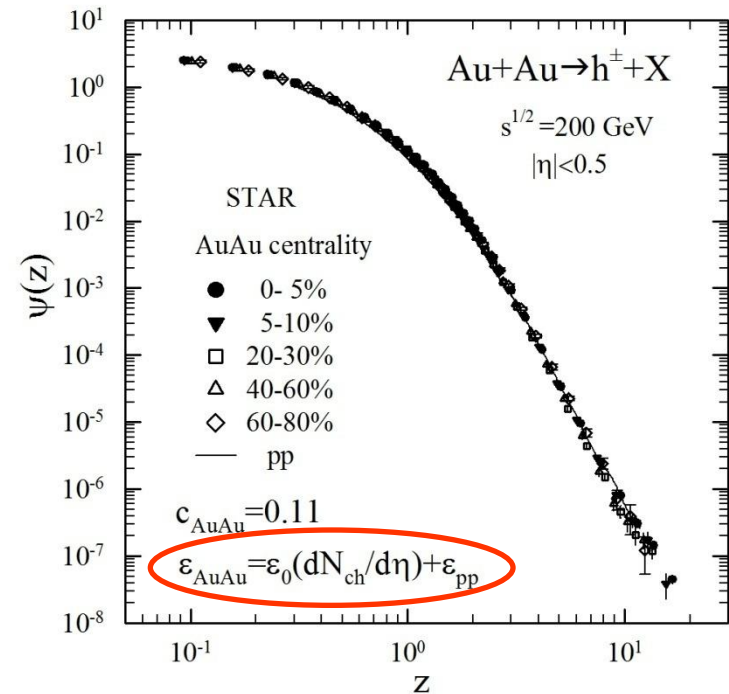
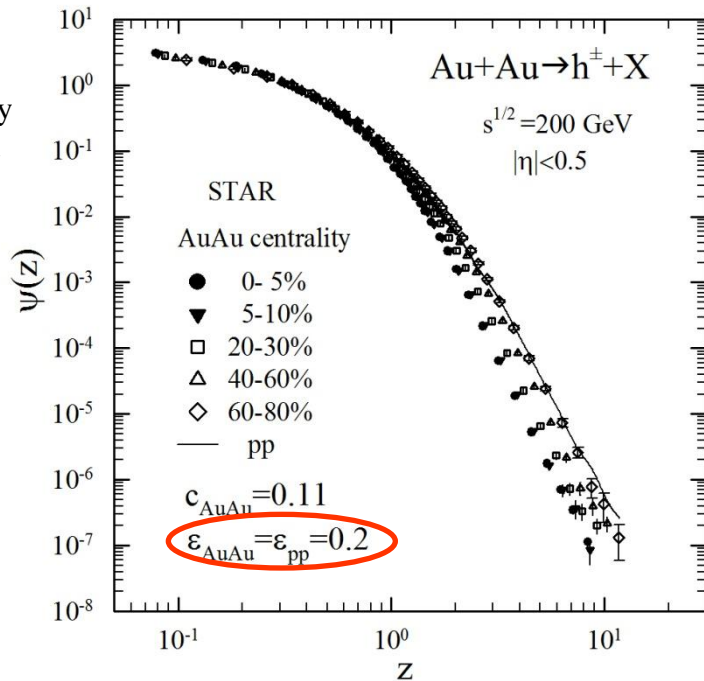
$dN_{ch}/d\eta|_0$  for corresponding AA centrality

- The energy independence of  $\Psi(z)$  in peripheral AuAu
- The same shape of  $\Psi(z)$  for pp & peripheral AuAu
- “Specific heat”  $c_{AuAu} = 0.11 < c_{pp} = 0.25$
- The same  $\epsilon$  in pp & peripheral AuAu

# Multiplicity dependence of fragmentation dimension $\epsilon_{AA}$

## Charged hadrons in central AuAu collisions at 200 GeV

STAR: PRL 91 (2003) 172302



Centrality dependence (decrease)  
 of  $\Psi(z)$  in central AuAu collisions  
 for  $\epsilon_{\text{AuAu}} = \epsilon_{\text{pp}}$

- The same  $\Psi(z)$  in pp & AuAu for all centralities
- Dimension  $\epsilon_{\text{AuAu}}$  depends on multiplicity
- “Specific heat”  $c_{\text{AuAu}} = 0.11$  for all centralities

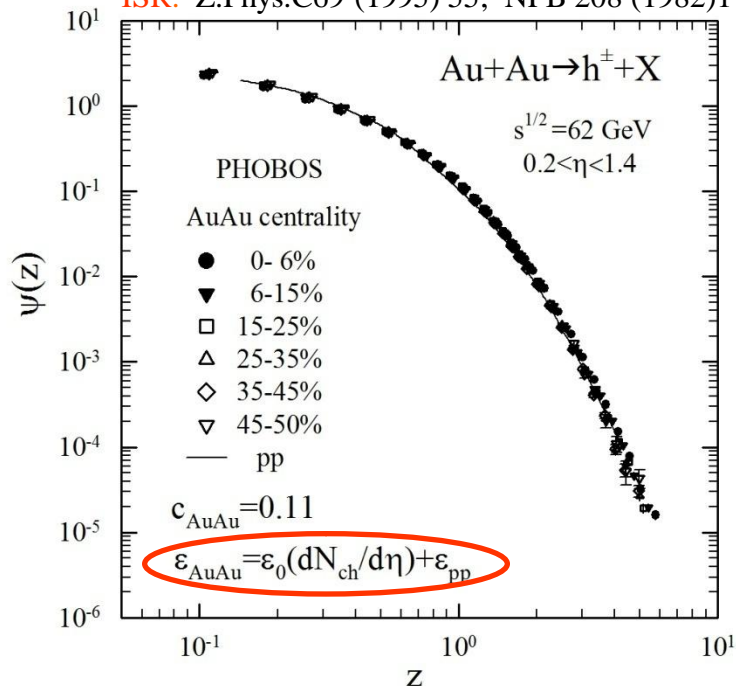
Multiplicity dependence of fragmentation process in HIC

# Self-similarity in AuAu collisions

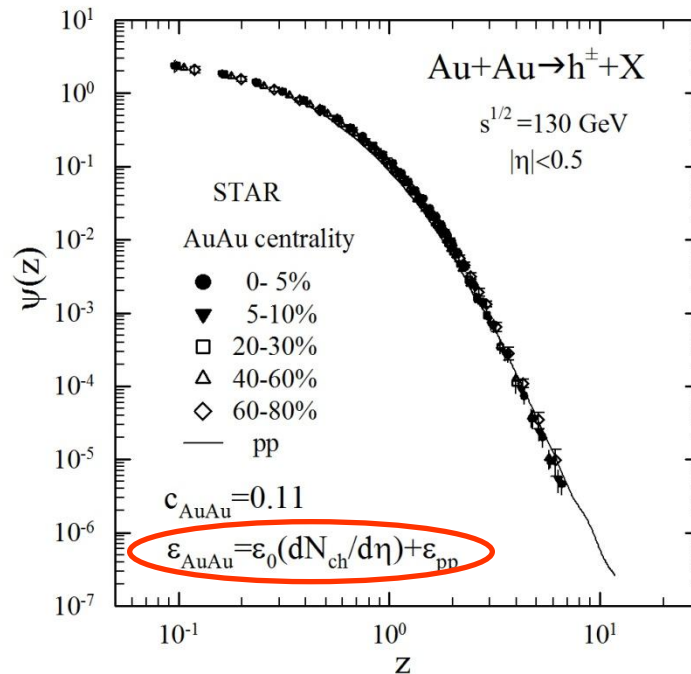
## Charged hadrons in pp & AuAu @ 62, 130 GeV

PHOBOS: PRL 94 (2005) 082304

ISR: Z.Phys.C69 (1995) 55; NPB 208 (1982)1



STAR: PRL 89 (2002) 202301; PRL 91 (2003) 172302



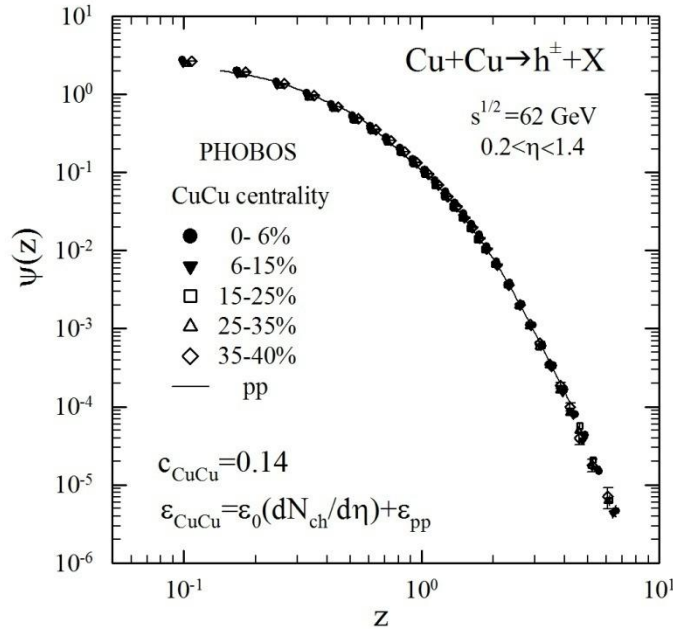
- The same  $\Psi(z)$  in AuAu & pp for  $\epsilon_{\text{AuAu}}$  is dependent of AuAu multiplicity
- “Specific heat”  $c_{\text{AuAu}} = 0.11$  (constant with  $s^{1/2}$ )
- $\epsilon_0$  increases with  $s^{1/2}$ :  $\epsilon_0(62\text{GeV}) = 0.0018 < \epsilon_0(130\text{GeV}) = 0.0022 < \epsilon_0(200\text{GeV}) = 0.0028$

Restoration of self-similarity in central AuAu collisions

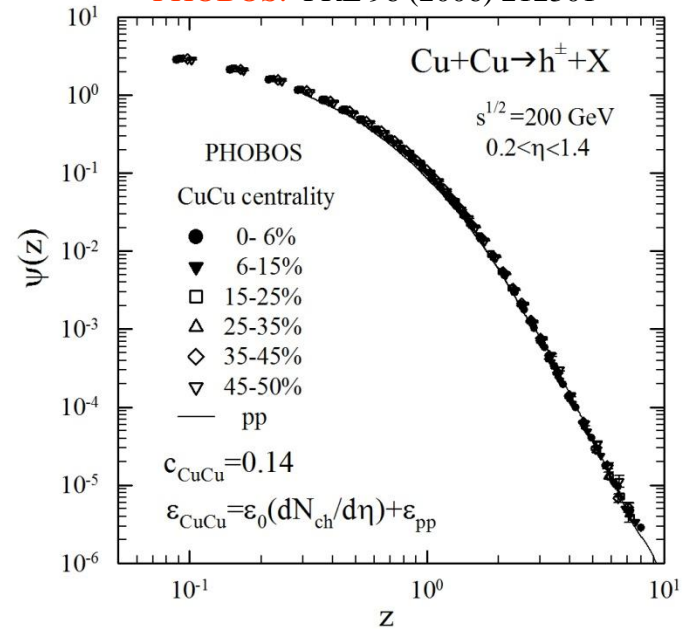
# Self-similarity in CuCu collisions

## Charged hadrons in pp & CuCu @ 62, 200 GeV

ISR: Z.Phys.C69 (1995) 55; NPB 208 (1982) 1



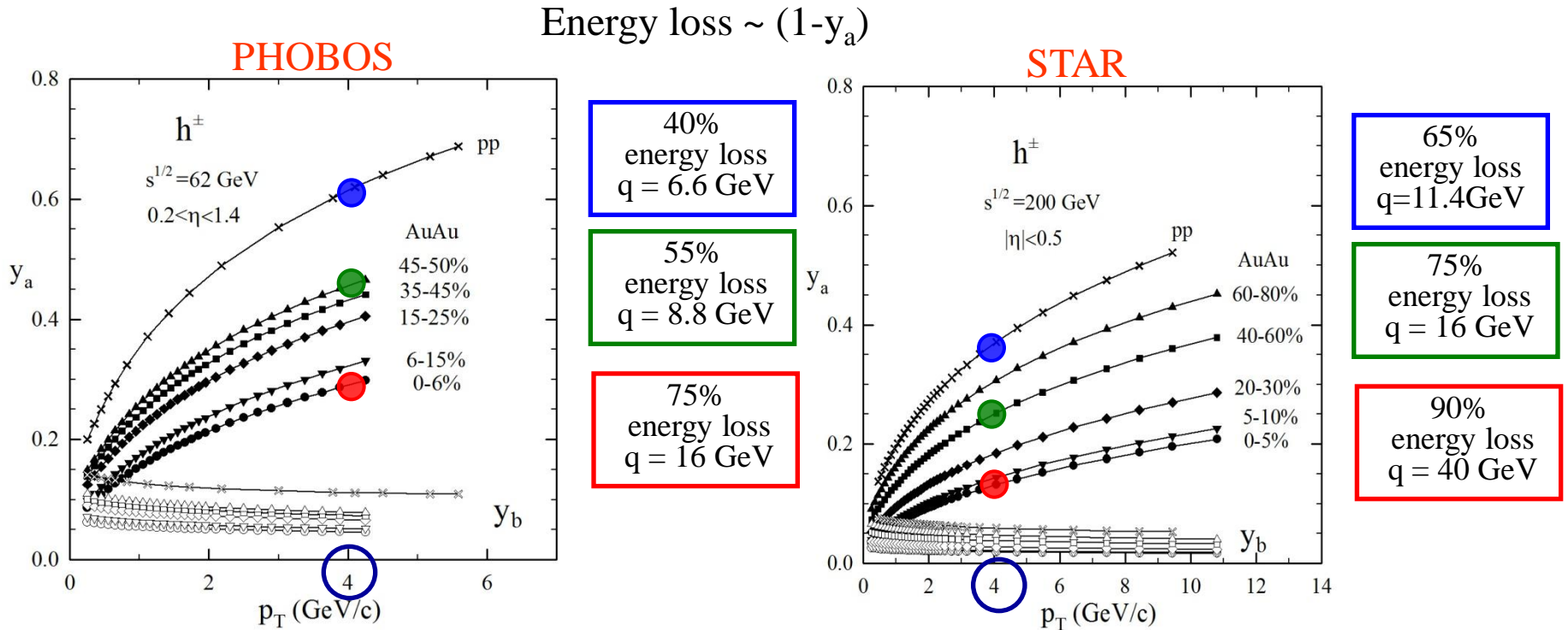
PHOBOS: PRL 96 (2006) 212301



- The same  $\Psi(z)$  in CuCu & pp for  $\epsilon_{\text{CuCu}}$  is dependent of CuCu multiplicity
- “Specific heat”  $c_{\text{CuCu}} = 0.14$  is independent of  $s^{1/2}$
- $\epsilon_0$  increases with  $s^{1/2}$ :  $\epsilon_0(62\text{GeV}) = 0.005 < \epsilon_0(200\text{GeV}) = 0.008$  (CuCu)

Restoration of self-similarity in central CuCu collisions

# Energy losses in pp & AuAu

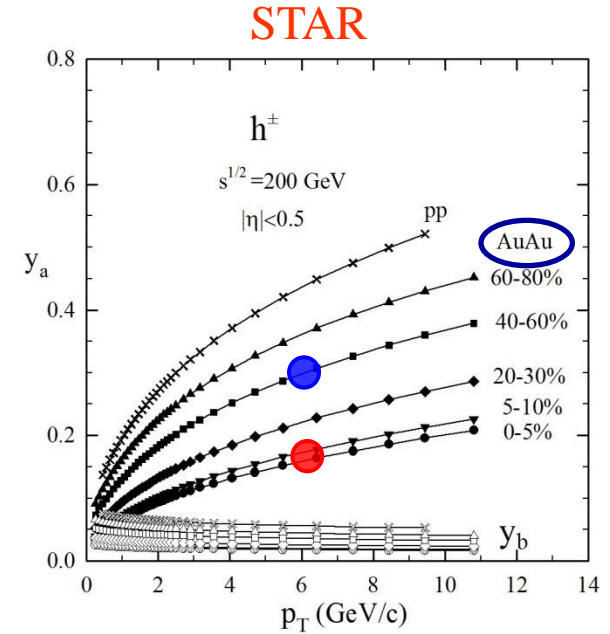
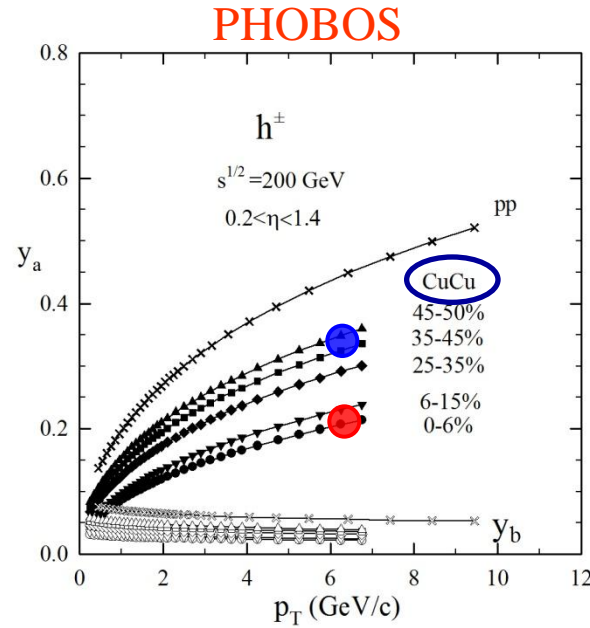
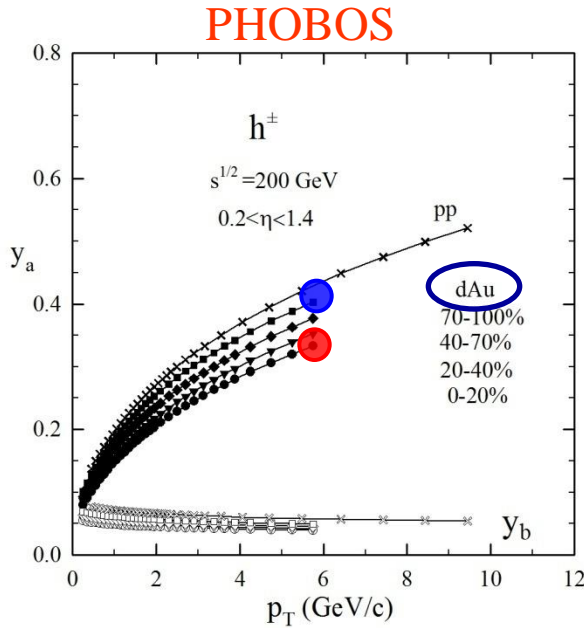


- $y_a$  increases with  $p_T \Rightarrow$  energy losses decrease with  $p_T$
- $y_a$  decreases with  $s^{1/2} \Rightarrow$  energy losses increase with  $s^{1/2}$
- $y_a$  decreases as centrality increases  $\Rightarrow$  energy losses increase with centrality
- $y_b$  is flat with  $p_T \Rightarrow$  weak dependence of  $M_X$  on  $p_T$
- $y_b \ll y_a$  for  $p_T > 1 \text{ GeV/c} \Rightarrow$  soft (high multiplicity) recoil  $M_X$



# Energy losses in dAu, CuCu, AuAu @ 200 GeV

Energy loss  $\sim (1-y_a)$



- $y_a$  increases with  $p_T \Rightarrow$  energy losses decrease with  $p_T$
- $y_a$  decreases with  $s^{1/2} \Rightarrow$  energy losses increase with  $s^{1/2}$
- $y_a$  decreases as centrality increases  $\Rightarrow$  energy losses increase with centrality
- $y_b$  is flat with  $p_T \Rightarrow$  weak dependence of  $M_X$  on  $p_T$
- $y_b \ll y_a$  for  $p_T > 1 \text{ GeV/c} \Rightarrow$  soft (high multiplicity) recoil  $M_X$
- $y_b$  increases with  $m \Rightarrow$  harder recoil  $M_X$  for heavy particles

# Energy scan of spectra in AuAu collisions

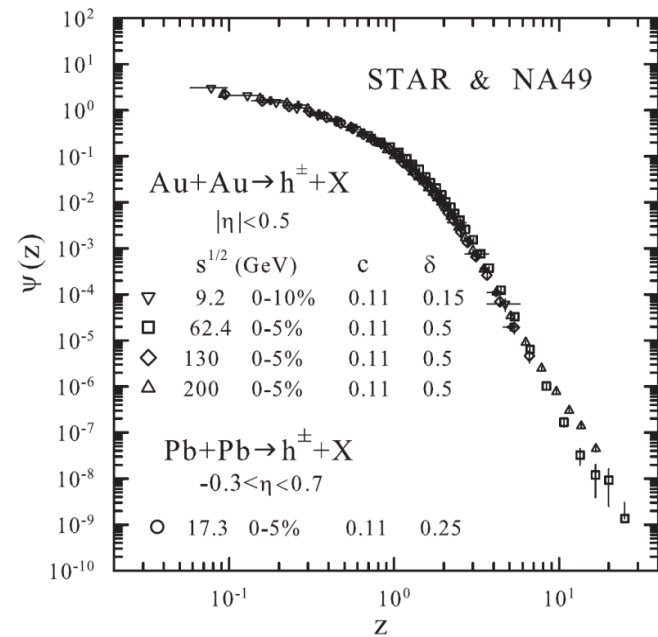
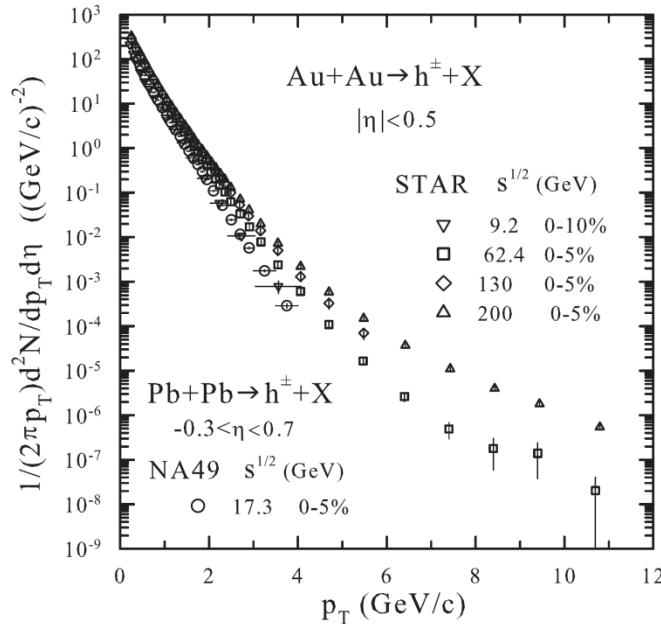
## Charged hadrons in central AuAu collisions at 200, 130, 62.4, 9.2 GeV

STAR:

PRL 89 (2002) 202301

PRL 91 (2003) 172302

arXiv:1004.5582



$\pi$  at SPS & RHIC



MT & I.Zborovsky  
 Phys.Part.Nucl.Lett.  
 7(2010)171

- Energy scan of the spectra:  $\sqrt{s_{NN}} = 9 - 200$  GeV
- Centrality dependence of the spectra at high  $p_T$
- Power law for all centralities for  $p_T > 2$  GeV/c
- Fragmentation ( $\epsilon$ ) depends on centrality

Change of the parameters  $c, \delta, \epsilon \Rightarrow$  indication on new properties of matter

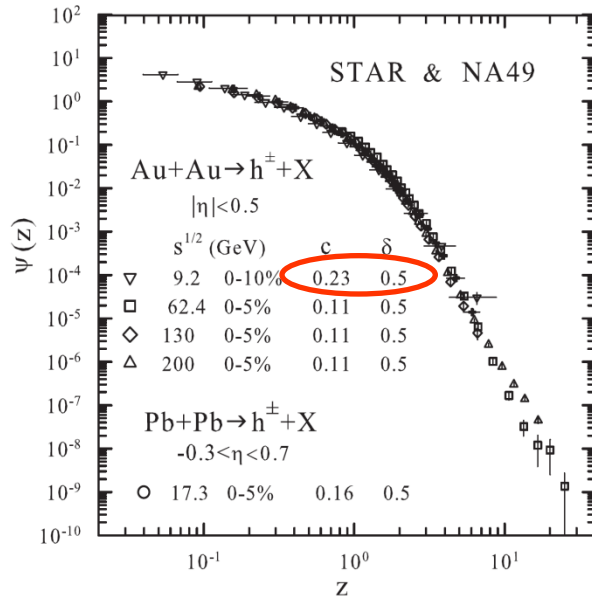
Discontinuity of the parameters  $c, \delta, \epsilon \Rightarrow$  indication of existence of CP



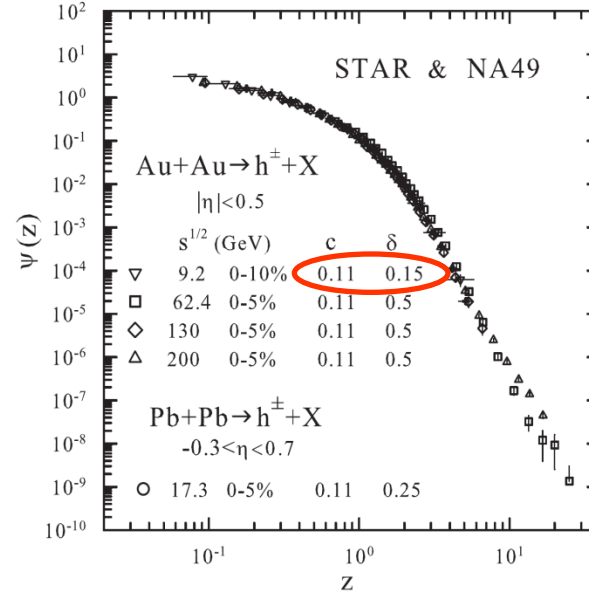
# Charged hadrons in central AuAu collisions

## Spectra in $z$ presentation - two scenarios

### I Large specific heat $c$ & large $\delta$



### II Small specific heat $c$ & small $\delta$



$$z = \frac{s_{\perp}^{1/2}}{(dN_{ch}/d\eta|_0)^c m_N} \cdot \Omega^{-1}$$

$$\Omega = (1-x_1)^{\delta_A} (1-x_2)^{\delta_A} (1-y_a)^\varepsilon (1-y_b)^\varepsilon$$

$$\delta_A = A\delta$$

- The same  $\Psi(z)$  for all centralities & energy (universality)  
 $\varepsilon_{AuAu}$  depends on multiplicity density
- Scenarios of interaction: large / small “specific heat”
- Correlation of  $c$ ,  $\varepsilon$ ,  $\delta$
- Centrality dependence of the spectra constraints  $c$
- Different scenarios in high- $z$  range ( $p_T > 6$  GeV/c)

# Energy losses in AuAu collisions $\sim (1-y_a)$

## Momentum fractions $y_a, y_b$ in different scenarios

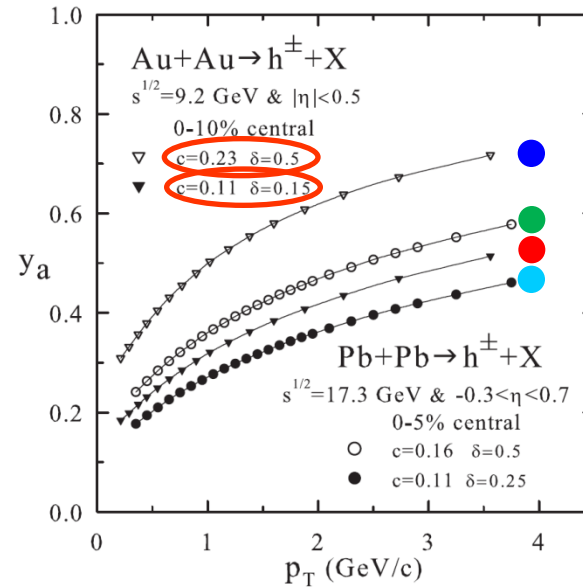
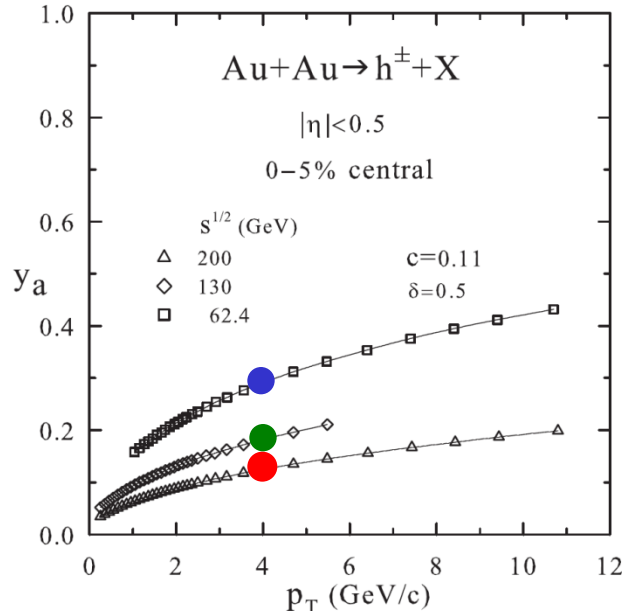
I Large specific heat  $c$  & large  $\delta$  :  $c=0.23, \delta=0.5$

II Small specific heat  $c$  & small  $\delta$  :  $c=0.11, \delta=0.11$

70%  
energy loss  
 $q \approx 5.7$  GeV

82%  
energy loss  
 $q \approx 22$  GeV

89%  
energy loss  
 $q \approx 36$  GeV



28%  
energy loss  
 $q \approx 5.6$  GeV

40%  
energy loss  
 $q \approx 6.7$  GeV

45%  
energy loss  
 $q \approx 7.3$  GeV

55%  
energy loss  
 $q \approx 8.9$  GeV

- $y_a$  increases with  $p_T \Rightarrow$  energy losses decrease with  $p_T$
- $y_a$  decreases with  $\sqrt{s_{NN}} \Rightarrow$  energy losses increase with  $\sqrt{s_{NN}}$
- $y_a$  decreases as centrality increases  $\Rightarrow$  energy losses increase with centrality
- $y_b$  is flat with  $p_T \Rightarrow$  weak dependence of  $M_X$  on  $p_T$
- $y_b \ll y_a$  for  $p_T > 1$  GeV/c  $\Rightarrow$  soft (high multiplicity) recoil  $M_X$

Energy losses ( $c=0.23, \delta=0.5$ ) < Energy losses ( $c=0.11, \delta=0.15$ )

Smaller energy losses  $\Rightarrow$  better localization of a Critical Point.....

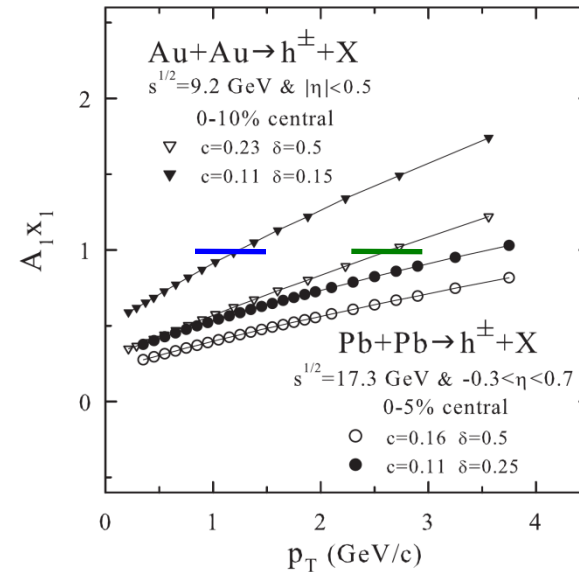
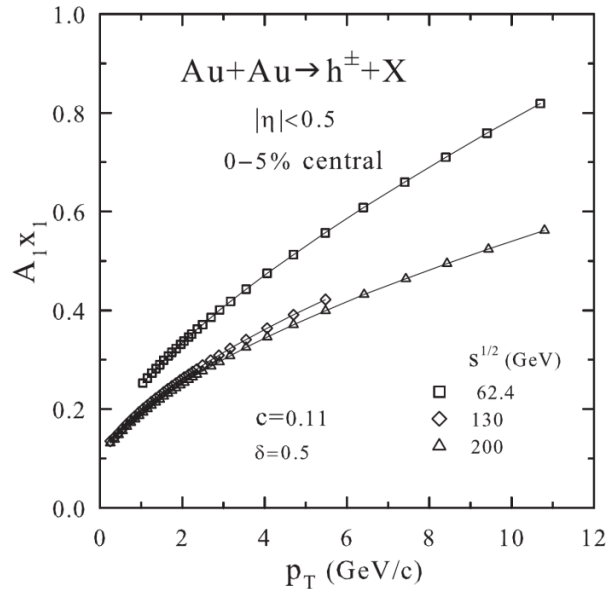


# Momentum fraction $x_1 A_1$ in AuAu collisions

## Different scenarios

I Large specific heat  $c$  & large  $\delta$  :  $c=0.23, \delta=0.5$

II Small specific heat  $c$  & small  $\delta$  :  $c=0.11, \delta=0.11$



- Cumulative region at  $p_T > 2.5$  GeV/c
- Smaller energy losses
- Not smeared sub-structure

- Cumulative region at  $p_T > 1.5$  GeV/c
- Larger energy losses
- Smeared sub-structure

Smaller energy losses  $\Rightarrow$  better localization of a Critical Point

Cumulative region ( $x_1 A_1 > 1$ ) is most preferable to search for a Critical Point

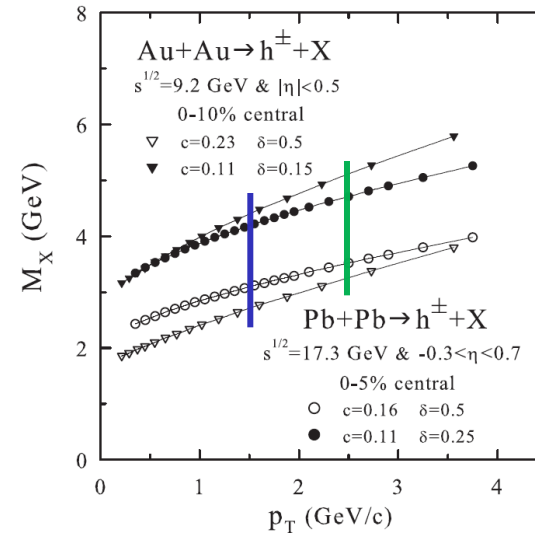
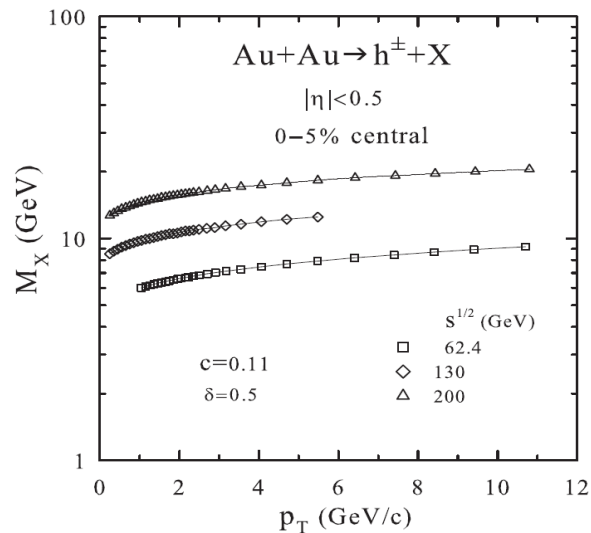
# Recoil mass $M_X$

## Recoil mass in different scenarios

$$M_X = x_1 M_1 + x_2 M_2 + m/y_b$$

I Large specific heat  $c$  & large  $\delta$  :  $c=0.23$ ,  $\delta=0.5$

II Small specific heat  $c$  & small  $\delta$  :  $c=0.11$ ,  $\delta=0.11$



➤ Cumulative region at  $p_T > 2.5$  GeV/c

➤ Smaller energy losses

➤ Not smeared sub-structure

➤ Smaller multiplicity in the way-side

➤ Cumulative region at  $p_T > 1.5$  GeV/c

➤ Larger energy losses

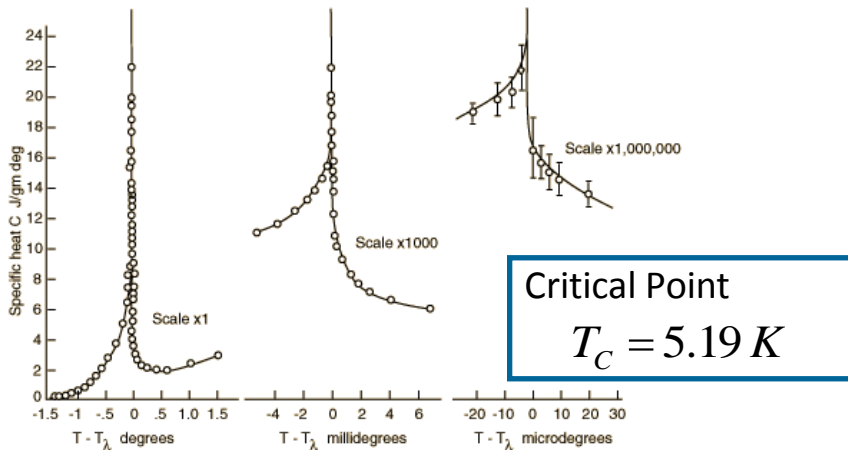
➤ Smeared sub-structure

➤ Larger multiplicity in the way-side

$M_X$  increases with  $p_T$ ,  $\sqrt{s_{NN}}$ , centrality due to decrease of the fraction  $y_b$

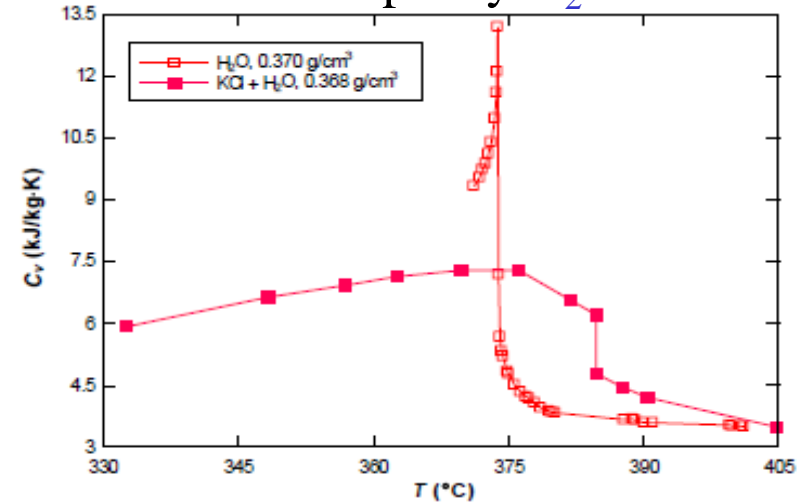
# Discontinuity and Smearing near a Critical Point

## Heat capacity $^4\text{He}$



H.E. Stanley, 1971

## Heat capacity $\text{H}_2\text{O}$



N.G. Polikhronidi et al. *Int.J.Thermophysics*  
2001, 22, (1), 189-200.

$$c_v = -T(\partial^2 G / \partial T^2)_V$$

G - Gibbs potential

$$\varepsilon \equiv (T - T_c) / T_c$$

$\varepsilon$  - scaled temperature

$$c_v \sim |\varepsilon|^{-\alpha}$$

$\alpha$  - critical exponent

- Discontinuity of heat capacity near a Critical Point
- Impurities smear the region of localization of a Critical Point
- Region with small energy loss is of most preferable for search for localization of a Critical Point



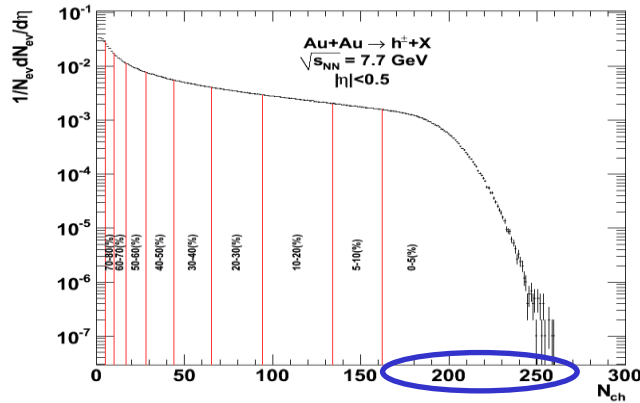
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## Signatures of phase transition and Critical Point:

- **Discontinuity** of the parameters:  
“specific heat”-  $c$ , fractal dimension –  $\delta$
- **Enhancement** of  $c$ - $\delta$  correlation
- **Energy loss** is a contamination factor leading to the smearing of the phase transition

# MC UrQMD study of hadron spectra in AuAu at high $p_T$

## Multiplicity distribution

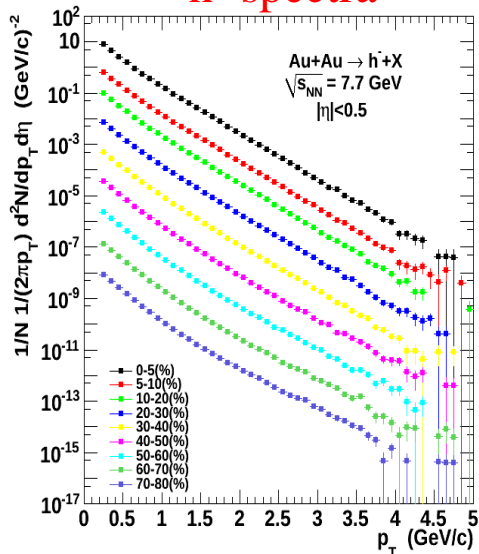


AuAu @ 7.7 GeV

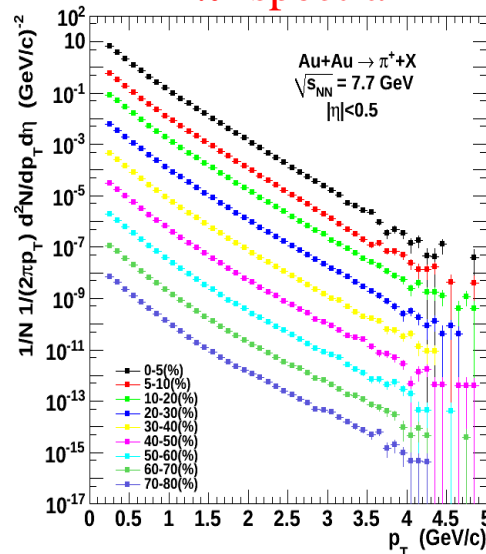
Centrality, %	0-5	5-10	10-20	20-30	30-40	40-50	50-60	60-70	70-80
$\langle N_{ch} \rangle$	182	148	113	79	54	36	23	14	8

10 Mevts

## $h^-$ spectra



## $\pi^+$ spectra



## Centrality dependence of spectra

- High energy density
- Sensitivity of particle formation to state of nuclear medium at high  $p_T$
- Small energy loss

$$\varepsilon = \frac{E_T}{\pi R^2 \tau A^{2/3}} \frac{dN_{ch}}{d\eta}$$

# Energy loss in AuAu collisions at $\sqrt{s_{NN}}=7.7$ GeV

Energy loss  $\Delta E/E \sim (1-y_a)$

STAR

PRL 91 (2003) 172302  
ЯФ 74 (2011) 1

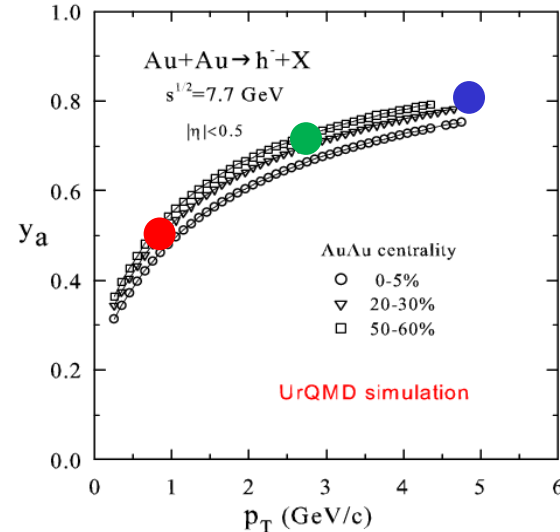
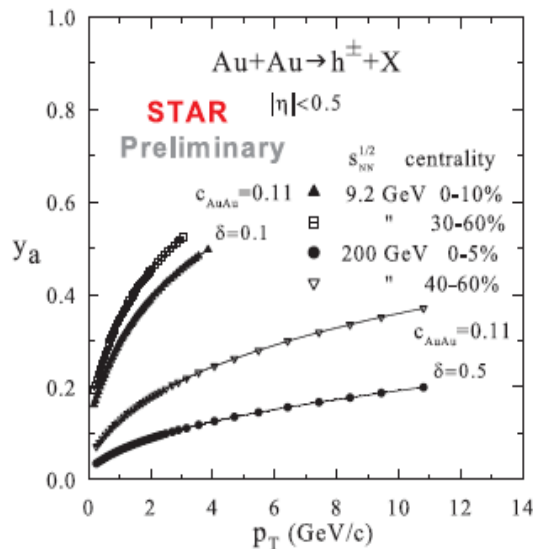
z-Scaling

M.T.

I.Zborovsky

PRD 75(2007) 094008  
IJMPA 24 (2009) 1417

.....



Energy loss 20%  
p<sub>T</sub> = 5 GeV/c  
q<sub>T</sub> ≈ 6.3 GeV/c

Energy loss 30%  
p<sub>T</sub> = 3 GeV/c  
q<sub>T</sub> ≈ 4.3 GeV/c

Energy loss 50%  
p<sub>T</sub> = 1 GeV/c  
q<sub>T</sub> ≈ 2 GeV/c

$\Delta E$  – constituent energy loss,  $E(q)$  – constituent energy (momentum)  
 $y_a$  – constituent energy fraction carried away by inclusive particle.

Less energy loss better localization of a Critical Point.

- Energy loss increases with energy and centrality and decreases as transverse momentum  $p_T$  increases.
- High- $p_T$  region ( $>4$  GeV/c) at  $\sqrt{s_{NN}} = 5-40$  GeV is of more preferable for search for phase transition and a Critical Point.

# Conclusions

- Results of analysis of experimental data on charged hadrons produced in **Heavy Ion** collisions at  $\sqrt{s_{NN}}=7.7-200$  GeV at **RHIC** in the framework of **z**-scaling were presented.
- Search for signatures of phase transition of nuclear matter and **Critical Point** in the approach was discussed.
- The constituent energy loss in **AuAu** collisions vs. energy and centrality collisions was estimated.
- Discontinuity & correlation of **c,  $\delta$**  as a signatures of phase transition and **Critical Point** in nucleus-nucleus collisions was discussed.
- High- $p_T$  spectra of charged hadrons at  $\sqrt{s_{NN}}=7.7, 11.5, 19.6, 27, 39$  GeV are soon expected from **BES** at **RHIC**.

The obtained results may be of interest in searching for a **Critical Point** and signatures of phase transition in hadron matter produced at **SPS, RHIC** and **LHC** in present, and **FAIR & NICA** in future.

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*Thank You for Attention !!!*