



*Bogoliubov Laboratory of
Theoretical Physics*
JINR

Dubna, 25 September 2019



**Joint Institute for Nuclear
Research**

SCIENCE BRINGING NATIONS
TOGETHER

Investigating relativistic proton-nucleus collisions and the influence of electromagnetic fields on final hadronic observables

Lucia Oliva



Collaborators:

Elena Bratkovskaya, Pierre Moreau, Vadim Voronyuk



Helmholtzzentrum für Schwerionenforschung GmbH



Dynamics of quarks and gluons described by the Quantum Chromodynamics (QCD)

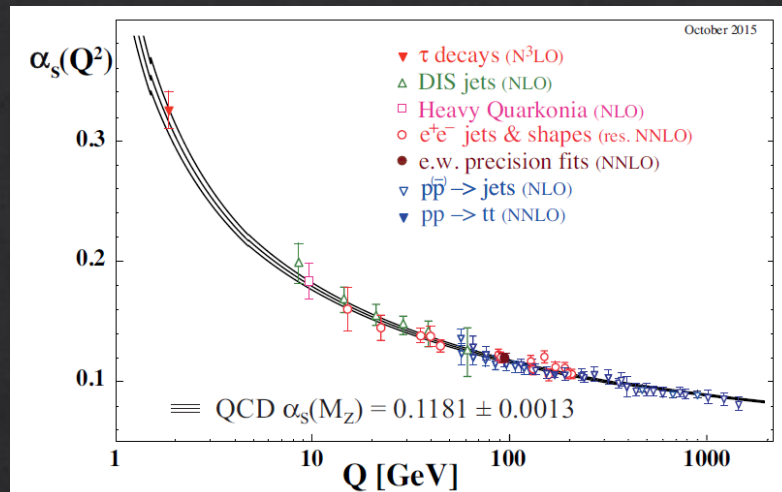
$$\mathcal{L}_{cl} = \bar{q}_i^\alpha (i\gamma^\mu D_\mu - m)_{\alpha\beta}^{ij} q_j^\beta - \frac{1}{4} F_{\mu\nu}^a F_a^{\mu\nu}$$

QCD LAGRANGIAN

QCD predicts that at very high energy quarks and gluons became weakly interacting

QUARK-GLUON PLASMA (QGP)

Collins and Perry, PRL 34 (1975) 1353



PDG, Chin. Phys. C 38, 010009 (2014-2015)

ASYMPTOTIC FREEDOM

Dynamics of quarks and gluons described by the Quantum Chromodynamics (QCD)

$$\mathcal{L}_{cl} = \bar{q}_i^\alpha (i\gamma^\mu D_\mu - m)_{\alpha\beta}^{ij} q_j^\beta - \frac{1}{4} F_{\mu\nu}^a F_a^{\mu\nu}$$

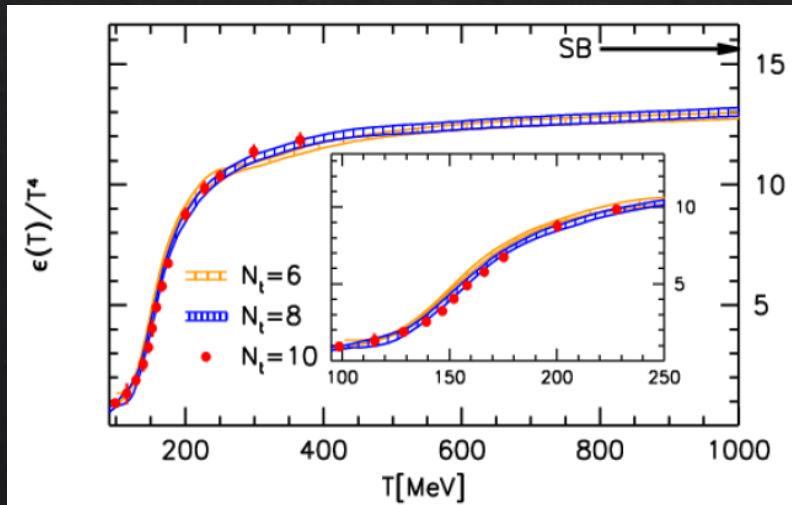
QCD LAGRANGIAN

QCD predicts that at very high energy quarks and gluons became weakly interacting

QUARK-GLUON PLASMA (QGP)

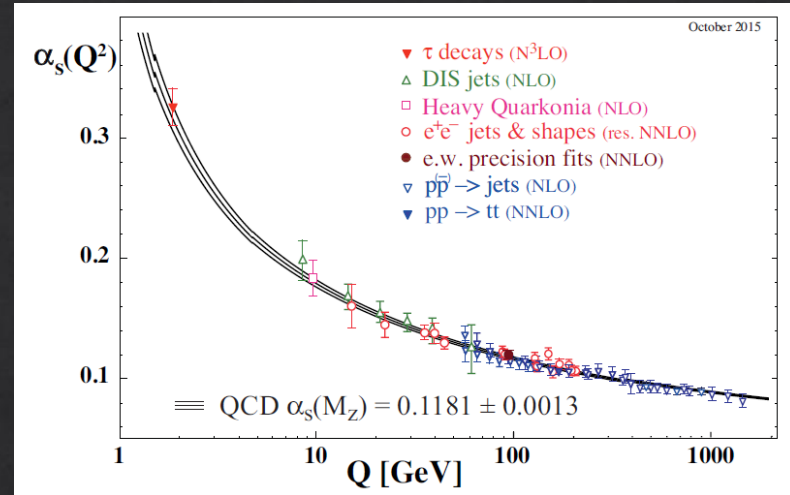
Collins and Perry, PRL 34 (1975) 1353

Phenomenological models and lattice QCD indicates the existence of a transition from hadronic matter to QGP at large energy density $\epsilon \sim 0.5 - 1 \text{ GeV}/\text{fm}^3$



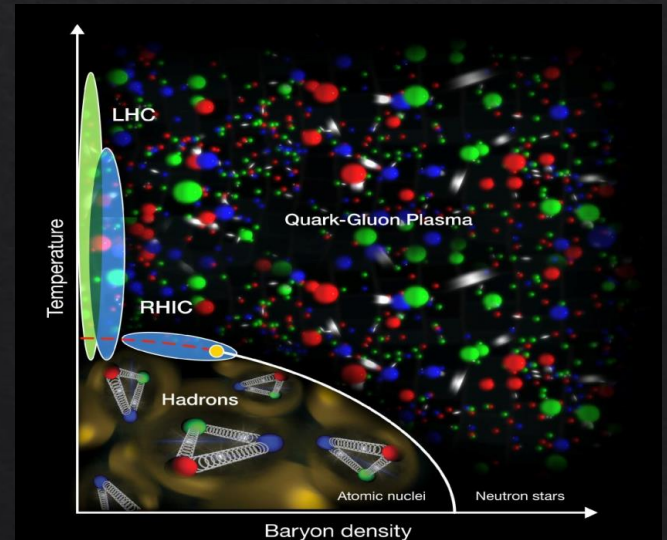
at $\mu = 0$
CROSSOVER
 $T_c \approx 155 \text{ MeV}$

Borsanyi et al., J. High Energy. Phys. 11 (2010) 077

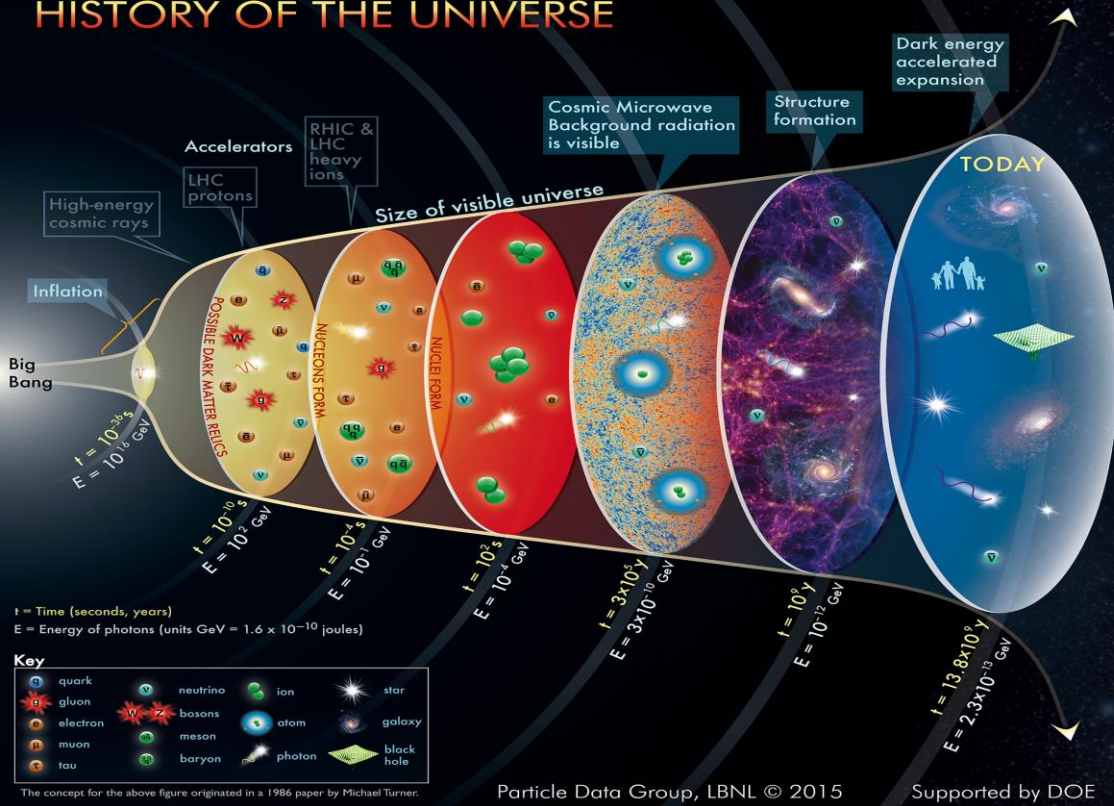


PDG, Chin. Phys. C 38, 010009 (2014-2015)

ASYMPTOTIC FREEDOM

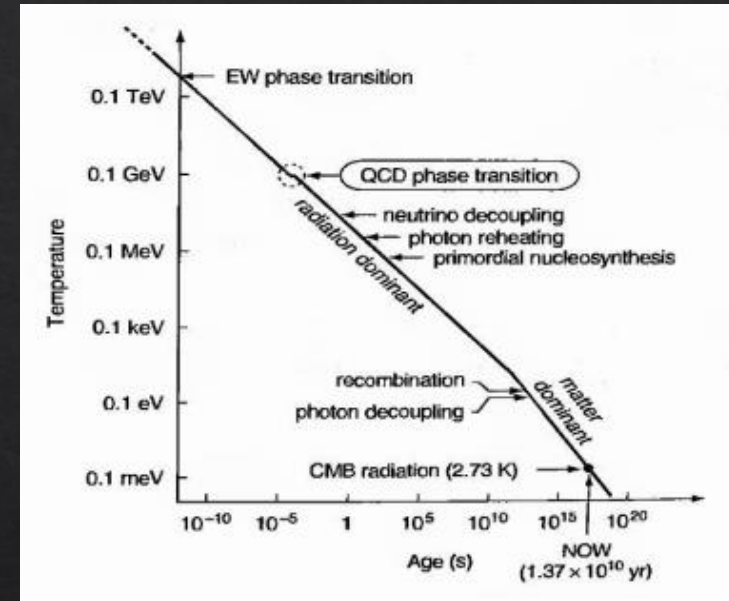


HISTORY OF THE UNIVERSE



QGP at high temperature and low net baryon density in the **EARLY UNIVERSE** up to $\sim 10 \mu\text{s}$ after the Big Bang

$$T_c \approx 155 \text{ MeV} \approx 2 \cdot 10^{12} \text{ K}$$

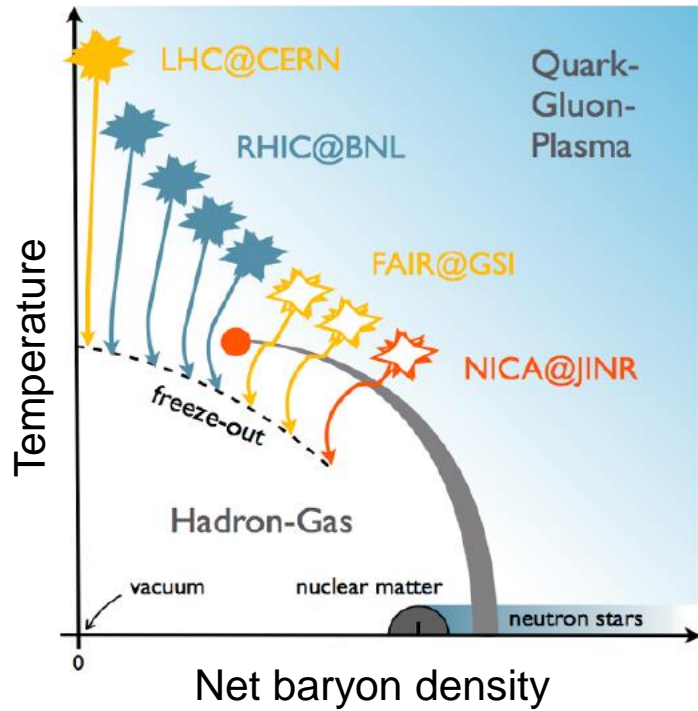


QGP at low temperature and high net baryon density in the core of **NEUTRON STARS**

$$\rho_c \approx 5-10 \rho_{\text{nm}} \approx 0.8-1.6 \text{ fm}^{-3} \approx 10^{45} \text{ particles/m}^3$$



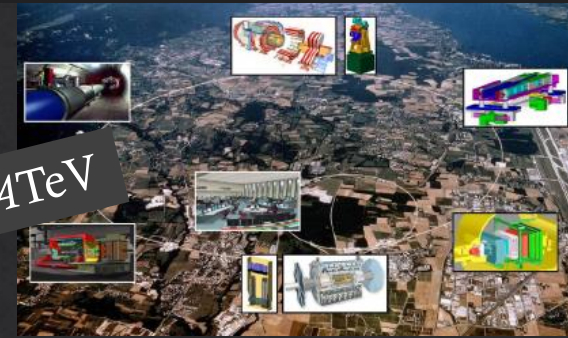
QCD PHASE DIAGRAM



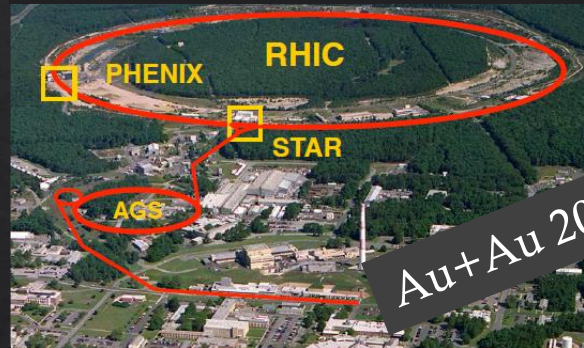
High energy heavy ion collisions

- ✓ allow to experimentally investigate the **QCD PHASE DIAGRAM**
- ✓ recreate the extreme condition of temperature and density required to form the **QUARK-GLUON PLASMA**

Large Hadron Collider (LHC)



Relativistic Heavy Ion Collider (RHIC)



Facility for Antiproton and Ion Research (FAIR)

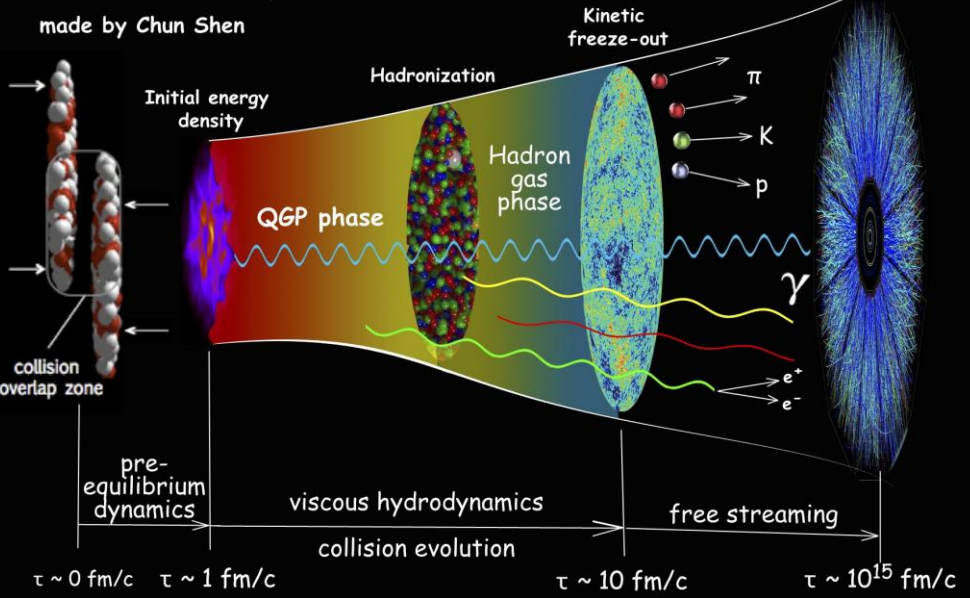
Au+Au 11 AGeV



Au+Au 30 AGeV

Nuclotron-based Ion Collider Facility (NICA)

Relativistic Heavy-Ion Collisions



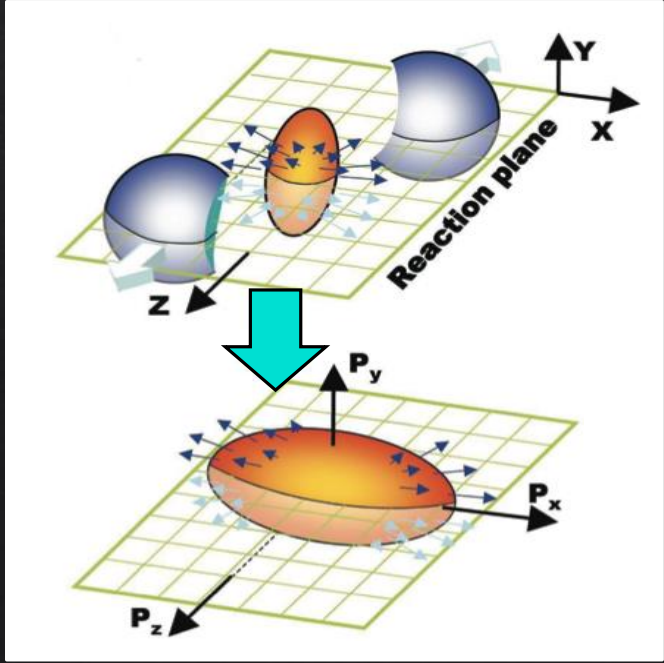
EXPANDING FIREBALL

- ❖ $t \sim 10\text{-}20 \text{ fm/c} \sim 10^{-23}\text{-}10^{-22} \text{ s}$
- ❖ $x \sim 10 \text{ fm} \sim 10^{-14} \text{ m}$
- ❖ $T_{in} \sim 300\text{-}600 \text{ MeV} \sim 10^{12} \text{ K}$

Quark-Gluon Plasma

hydrodynamical behaviour with very low η/s and collective flows

$$\frac{dn}{d\phi} \propto 1 + \sum_n 2v_n(p_T) \cos[n(\phi - \Psi_n)]$$



eccentricity

$$\epsilon = \frac{\langle y^2 - x^2 \rangle}{\langle y^2 + x^2 \rangle}$$

$$v_2 = \left\langle \frac{p_x^2 - p_y^2}{p_x^2 + p_y^2} \right\rangle$$

elliptic flow

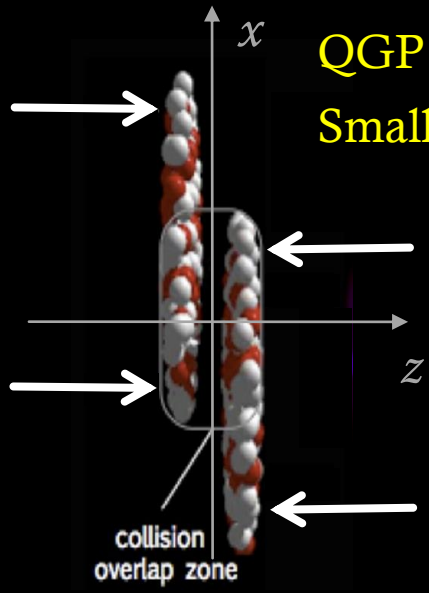
$$4\pi\eta/s \approx 1 - 2$$

almost perfect fluid



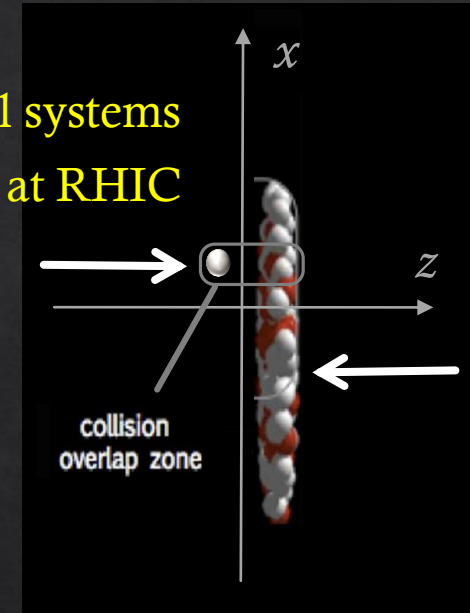
$$\eta/s_{\text{qgp}} \ll \eta/s_{\text{water}} \ll \eta/s_{\text{pitch}}$$

QGP initially expected only in high energy collisions of two heavy ions
 Small colliding systems initially regarded as control measurements



Signatures of collective flow found in small systems
 p+Pb collisions at LHC, p/d/³He+Au at RHIC

PHENIX Coll., Nature Phys. 15 (2019) 214



nature
 physics

LETTERS

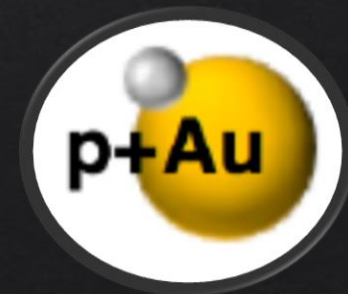
<https://doi.org/10.1038/s41567-018-0360-0>

Creation of quark-gluon plasma droplets with three distinct geometries

PHENIX Collaboration^{*}

Experimental studies of the collisions of heavy nuclei at relativistic energies have established the properties of the quark-gluon plasma (QGP), a state of hot, dense nuclear matter in which quarks and gluons are not bound into hadrons¹⁻⁴. In this state, matter behaves as a nearly inviscid fluid⁵ that efficiently translates initial spatial anisotropies into correlated momentum anisotropies among the particles produced, creating a common velocity field pattern known as collective flow. In recent years, comparable momentum anisotropies have been measured in small-system proton-proton (p+p) and proton-nucleus (p+A) collisions, despite expectations that the volume and lifetime of the medium produced would be too small to form a QGP. Here we report on the observation of elliptic and triangular flow patterns of charged particles produced in proton-gold (p+Au), deuteron-gold (d+Au) and helium-gold (³He+Au) collisions at a nucleon-nucleon centre-of-mass energy $\sqrt{s_{NN}} = 200$ GeV. The unique combination of three distinct initial geometries and two flow patterns provides unprecedented model discrimination. Hydrodynamical models, which include the formation of a short-lived QGP droplet, provide the best simultaneous description of these measurements.

**COLLECTIVITY
 IN SMALL SYSTEMS
 AS SIGN OF
 QGP DROPLETS?**

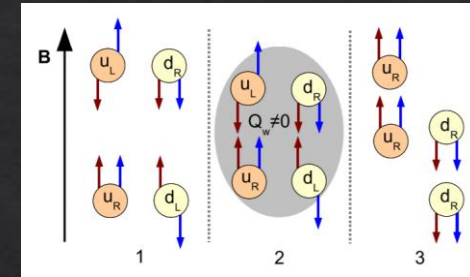


proton-induced collisions
 at top RHIC energy

Very intense magnetic fields in the early stage of HICs

Many interesting phenomena in HICs driven by the electromagnetic fields (EMF)

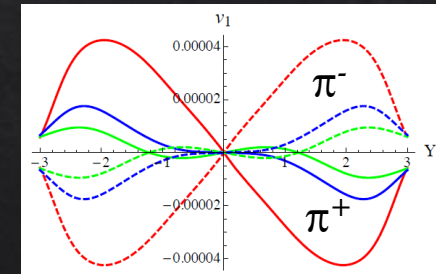
CHIRAL MAGNETIC EFFECT



$$J_m = \frac{e^2}{2\pi^2} \mu_5 B$$

Kharzeev, McLerran and Warringa, NPA 803 (2008) 227

CHARGE-ODD DIRECTED FLOW

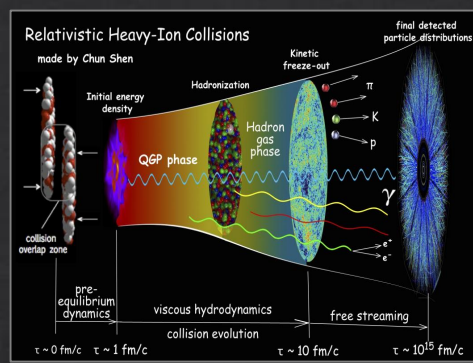


$$v_1^+(y, p_T) \neq v_1^-(y, p_T)$$

$$F_{em} = q(E + v \times B)$$

Gursoy, Kharzeev and Rajagopal, PRC 89 (2014) 054905
 Voronyuk, Toneev, Voloshin and Cassing, PRC 90 (2014) 064903
 Das, Plumari, Greco et al., PLB 768 (2017) 260

In p+Au collisions?



HICs

$\sim 10^{18}-10^{19}$ G



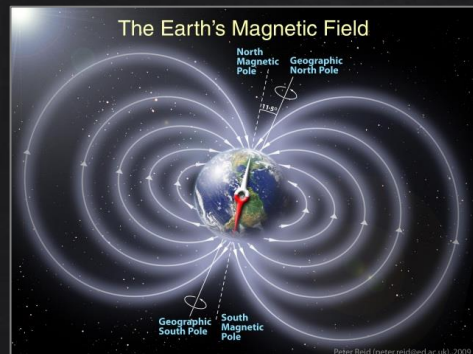
magnetars

$\sim 10^{14}-10^{15}$ G



laboratory

$\sim 10^6$ G



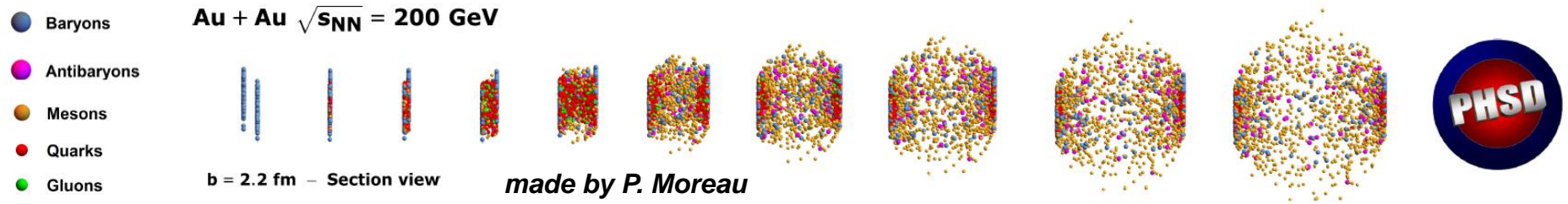
Earth's field

~ 1 G

PHSD: Parton-Hadron-String Dynamics

non-equilibrium transport approach to describe large and small colliding systems

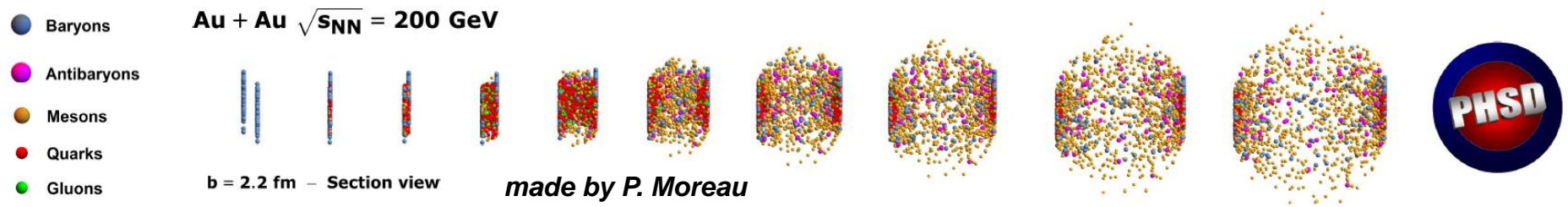
To study the phase transition from hadronic to partonic matter and QGP properties from a microscopic origin



PHSD: Parton-Hadron-String Dynamics

non-equilibrium transport approach to describe large and small colliding systems

To study the phase transition from hadronic to partonic matter and QGP properties from a microscopic origin

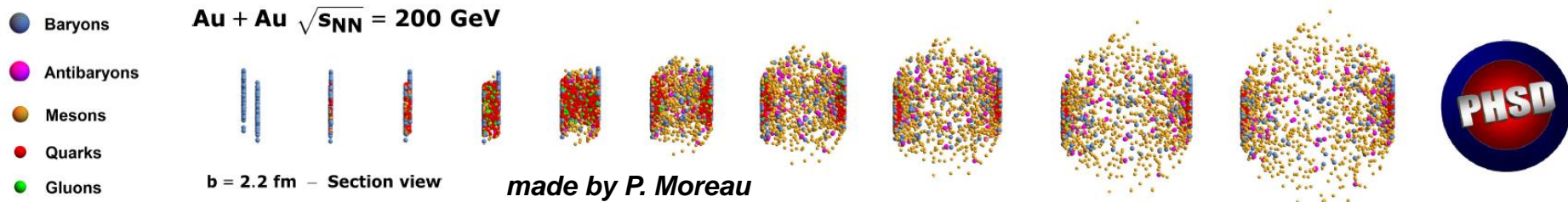


- **INITIAL A+A COLLISIONS:** nucleon-nucleon collisions lead to the formation of strings that decay to pre-hadrons
- **FORMATION OF QGP:** if the energy density is above ϵ_c pre-hadrons dissolve in massive quarks and gluons + mean-field potential

PHSD: Parton-Hadron-String Dynamics

non-equilibrium transport approach to describe large and small colliding systems

To study the phase transition from hadronic to partonic matter and QGP properties from a microscopic origin

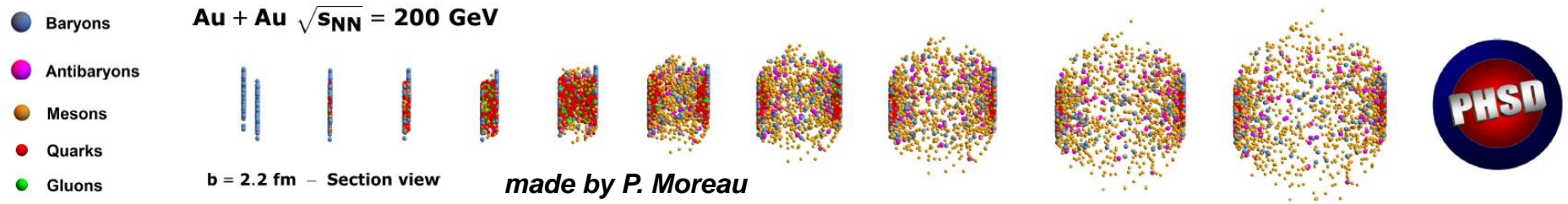


- **INITIAL A+A COLLISIONS:** nucleon-nucleon collisions lead to the formation of strings that decay to pre-hadrons
- **FORMATION OF QGP:** if the energy density is above ϵ_c pre-hadrons dissolve in massive quarks and gluons + mean-field potential
- **PARTONIC STAGE:** evolution based on Generalized Transport Equations with parton properties defined by the Dynamical Quasi-Particle Model

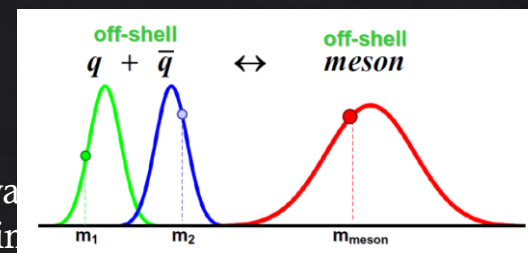
PHSD: Parton-Hadron-String Dynamics

non-equilibrium transport approach to describe large and small colliding systems

To study the phase transition from hadronic to partonic matter and QGP properties from a microscopic origin



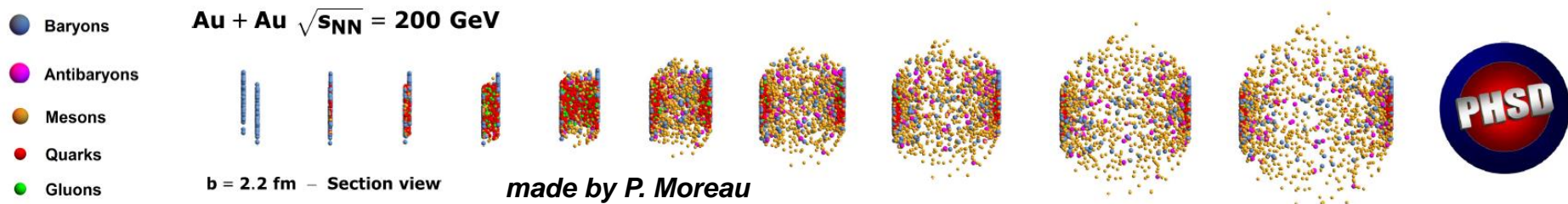
- **INITIAL A+A COLLISIONS:** nucleon-nucleon collisions lead to the formation of strings that decay to pre-hadrons
- **FORMATION OF QGP:** if the energy density is above ϵ_c pre-hadrons dissolve in massive quarks and gluons + mean-field potential
- **PARTONIC STAGE:** evolution based on Generalized Transport Equations with parton properties defined by the Dynamical Quasi-Particle Model
- **HADRONIZATION:** massive off-shell partons with broad spectral functions hadronize to off-shell baryon and mesons



PHSD: Parton-Hadron-String Dynamics

non-equilibrium transport approach to describe large and small colliding systems

To study the phase transition from hadronic to partonic matter and QGP properties from a microscopic origin



- **INITIAL A+A COLLISIONS:** nucleon-nucleon collisions lead to the formation of strings that decay to pre-hadrons
- **FORMATION OF QGP:** if the energy density is above ϵ_c pre-hadrons dissolve in massive quarks and gluons + mean-field potential
- **PARTONIC STAGE:** evolution based on Generalized Transport Equations with parton properties defined by the Dynamical Quasi-Particle Model
- **HADRONIZATION:** massive off-shell partons with broad spectral functions hadronize to off-shell baryon and mesons
- **HADRONIC PHASE:** evolution based on Generalized Transport Equations with hadron-hadron interactions

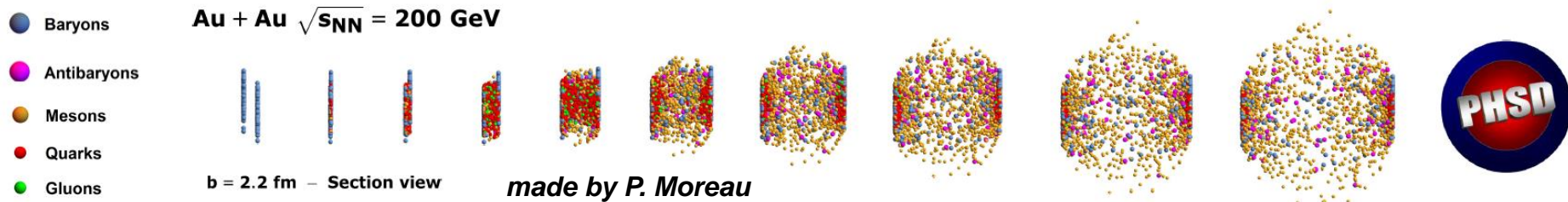
Cassing and Bratkovskaya, PRC 78 (2008) 034919; NPA831 (2009) 215

Cassing, EPJ ST 168 (2009) 3; NPA856 (2011) 162

PHSD: Parton-Hadron-String Dynamics

non-equilibrium transport approach to describe large and small colliding systems

To study the phase transition from hadronic to partonic matter and QGP properties from a microscopic origin



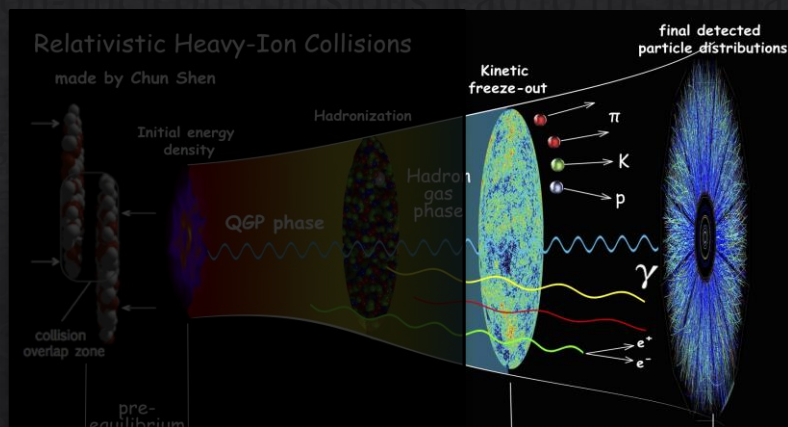
➤ INITIAL A+A COLLISIONS

➤ FORMATION OF QGP

➤ PARTONIC STAGE

➤ HADRONIZATION

➤ HADRONIC PHASE



good description of A–A collisions
from the lower SPS to the top LHC energies
for bulk and electromagnetic observables

Generalized Transport Equations (GTE)

After the first order gradient expansion of the Wigner transformed Kadanoff-Baym equations and separation into the real and imaginary parts one obtains GTE which describes the dynamics of broad strongly interacting quantum states

$$\underbrace{\diamond \{P^2 - M_0^2 - \text{Re}\Sigma_{XP}^{\text{ret}}\}}_{\text{drift term}} \underbrace{\{S_{XP}^<\}}_{\text{Vlasov term}} - \underbrace{\diamond \{\Sigma_{XP}^<\} \{ \text{Re}S_{XP}^{\text{ret}} \}}_{\text{backflow term}} = \underbrace{\frac{i}{2} [\Sigma_{XP}^> S_{XP}^< - \Sigma_{XP}^< S_{XP}^>]}_{\text{collision term = 'gain' - 'loss' term}}$$

$$\diamond \{F_1\} \{F_2\} := \frac{1}{2} \left(\frac{\partial F_1}{\partial X_\mu} \frac{\partial F_2}{\partial P^\mu} - \frac{\partial F_1}{\partial P_\mu} \frac{\partial F_2}{\partial X^\mu} \right) \quad \text{off-shell behavior}$$

GTE govern the propagation of the Green functions $i S_{XP}^< = A_{XP} N_{XP}$

Dressed propagators (S_q, Δ_g)

$$S = (P^2 - \Sigma^2)^{-1}$$

with complex self-energies (Σ_q, Π_g):

$$\Sigma = m^2 - i2\gamma\omega$$

- ❖ the real part describes a dynamically generated mass (m_q, m_g)
- ❖ the imaginary part describes the interaction width (γ_q, γ_g)

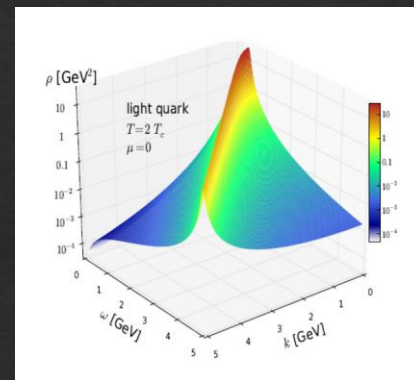
number of particles
particle spectral function

Dynamical QuasiParticle Model (DQPM)

The DQPM describes QGP in terms of interacting quasiparticle: massive quarks and gluons with Lorentzian spectral functions

$$A_j(\omega, \mathbf{p}) = \frac{\gamma_j}{\tilde{E}_j} \left(\frac{1}{(\omega - \tilde{E}_j)^2 + \gamma_j^2} - \frac{1}{(\omega + \tilde{E}_j)^2 + \gamma_j^2} \right)$$

$$\tilde{E}_j = p^2 + m^2 - \gamma^2$$



GLUONS

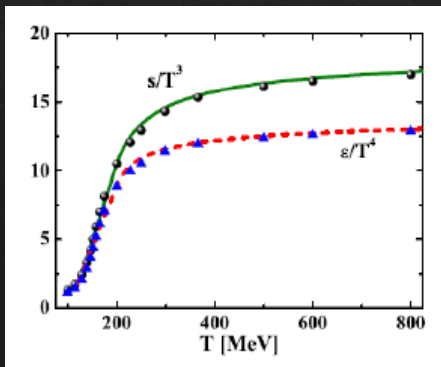
QUARKS

MASSES

$$m_g^2 = \frac{g^2}{6} \left(N_c + \frac{1}{2} N_f \right) T^2, \quad m_q^2 = g^2 \frac{N_c^2 - 1}{8N_c} T^2$$

WIDTHS

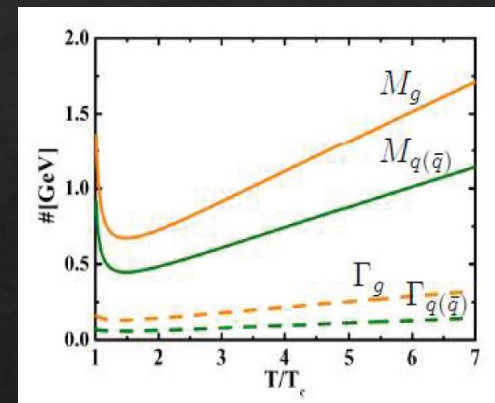
$$\gamma_g = \frac{1}{3} N_c \frac{g^2 T}{8\pi} \ln\left(\frac{2c}{g^2} + 1\right), \quad \gamma_q = \frac{1}{3} \frac{N_c^2 - 1}{2N_c} \frac{g^2 T}{8\pi} \ln\left(\frac{2c}{g^2} + 1\right)$$



$$g^2(T/T_c) = \frac{48\pi^2}{(11N_c - 2N_f) \ln(\lambda^2(T/T_c - T_s/T_c)^2)}$$

RUNNING COUPLING

parameters from fit
of lattice QCD
thermodynamics



Peshier, PRD 70 (2004) 034016

Peshier and Cassing, PRL 94 (2005) 172301

Cassing, NPA 791 (2007) 365; NPA 793 (2007)

PHSD extended to include chemical potential dependence of scattering cross section

Moreau, Soloveva, LO, Song, Cassing and Bratkovskaya, PRC 100 (2019) 014911

PHSD + electromagnetic fields



PHSD has been extended including the dynamical formation and evolution of the retarded electromagnetic field (EMF) and its influence on the quasi-particle (QP) dynamics

Voronyuk *et al.*, PRC 83 (2011) 054911

Toneev *et al.*, PRC 85 (2012) 034910; PRC 86 (2012) 064907; PRC 95 (2017) 034911

TRANSPORT EQUATION

$$\left\{ \frac{\partial}{\partial t} + \left(\frac{\mathbf{p}}{p_0} + \nabla_{\mathbf{p}} U \right) \nabla_{\mathbf{r}} + (-\nabla_{\mathbf{r}} U + e\mathbf{E} + e\mathbf{v} \times \mathbf{B}) \nabla_{\mathbf{p}} \right\} f = C_{\text{coll}}(f, f_1, \dots, f_N)$$

Lorentz force

MAXWELL EQUATIONS

$$\nabla \cdot \mathbf{B} = 0 \quad \nabla \times \mathbf{E} = -\frac{\partial \mathbf{B}}{\partial t} \quad \nabla \cdot \mathbf{E} = 4\pi\rho \quad \nabla \times \mathbf{B} = \frac{\partial \mathbf{E}}{\partial t} + \frac{4\pi}{c}\mathbf{j}$$

charge distribution

electric current

consistent solution of particle and field evolution equations

retarded electromagnetic fields

$$\mathbf{B} = \nabla \times \mathbf{A}, \quad \mathbf{E} = -\nabla\Phi - \frac{\partial\mathbf{A}}{\partial t}$$

General solution of the wave equation for the electromagnetic potentials

$$\mathbf{A}(\mathbf{r}, t) = \frac{1}{4\pi} \int \frac{\mathbf{j}(\mathbf{r}', t') \delta(t - t' - |\mathbf{r} - \mathbf{r}'|/c)}{|\mathbf{r} - \mathbf{r}'|} d^3r' dt'$$

$$\Phi(\mathbf{r}, t) = \frac{1}{4\pi} \int \frac{\rho(\mathbf{r}', t') \delta(t - t' - |\mathbf{r} - \mathbf{r}'|/c)}{|\mathbf{r} - \mathbf{r}'|} d^3r' dt'$$

$$\mathbf{r}' \equiv \mathbf{r}(t')$$

$$t' = t - \frac{|\mathbf{r} - \mathbf{r}'|}{c}$$

Liénard-Wiechert potentials for a moving point-like charge

$$\Phi(\mathbf{r}, t) = \frac{e}{4\pi} \left[\frac{1}{R(1 - \mathbf{n} \cdot \boldsymbol{\beta})} \right]_{\text{ret}} \quad \mathbf{A}(\mathbf{r}, t) = \frac{e}{4\pi} \left[\frac{\boldsymbol{\beta}}{R(1 - \mathbf{n} \cdot \boldsymbol{\beta})} \right]_{\text{ret}}$$

ret: evaluated at the times t'

$$\mathbf{R} = \mathbf{r} - \mathbf{r}'$$

$$\mathbf{n} = \frac{\mathbf{R}}{R}$$

$$\boldsymbol{\beta} = \frac{\mathbf{v}}{c}$$

retarded electromagnetic fields

Retarded electric and magnetic fields for a moving point-like charge

$$\mathbf{E}(\mathbf{r}, t) = \frac{e}{4\pi} \left[\frac{\mathbf{n} - \boldsymbol{\beta}}{(1 - \mathbf{n} \cdot \boldsymbol{\beta})^3 \gamma^2 R^2} + \frac{\mathbf{n} \times ((\mathbf{n} - \boldsymbol{\beta}) \times \dot{\boldsymbol{\beta}})}{(1 - \mathbf{n} \cdot \boldsymbol{\beta})^3 cR} \right]_{\text{ret}} \quad \mathbf{B}(\mathbf{r}, t) = [\mathbf{n} \times \mathbf{E}(\mathbf{r}, t)]_{\text{ret}}$$

elastic Coulomb
scatterings

inelastic bremsstrahlung
processes

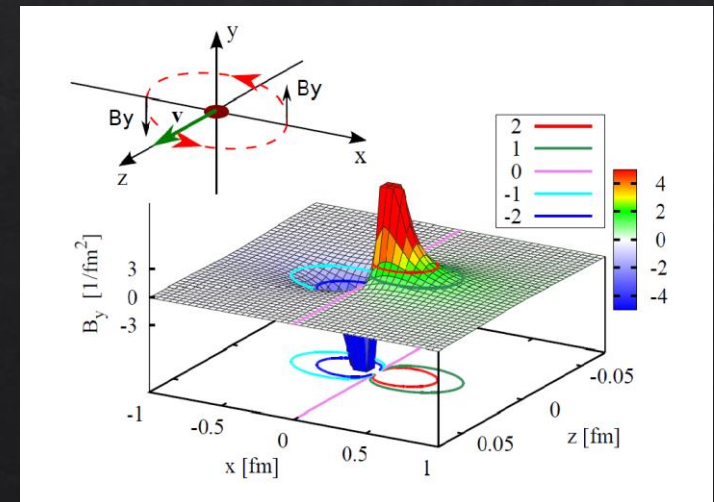
$$\mathbf{R} = \mathbf{r} - \mathbf{r}' \quad \mathbf{n} = \frac{\mathbf{R}}{R} \quad \boldsymbol{\beta} = \frac{\mathbf{v}}{c}$$

Neglecting the acceleration

$$e\mathbf{E}(t, \mathbf{r}) = \alpha_{em} \frac{1 - \beta^2}{[(\mathbf{R} \cdot \boldsymbol{\beta})^2 + R^2(1 - \beta^2)]^{3/2}} \mathbf{R}$$

$$e\mathbf{B}(t, \mathbf{r}) = \alpha_{em} \frac{1 - \beta^2}{[(\mathbf{R} \cdot \boldsymbol{\beta})^2 + R^2(1 - \beta^2)]^{3/2}} \boldsymbol{\beta} \times \mathbf{R}$$

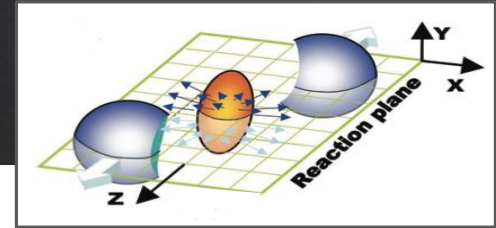
magnetic field created by a
single freely moving charge



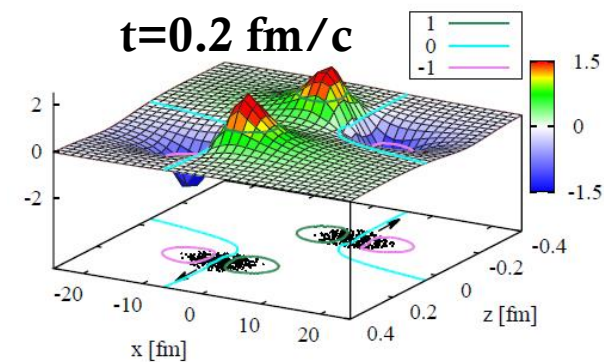
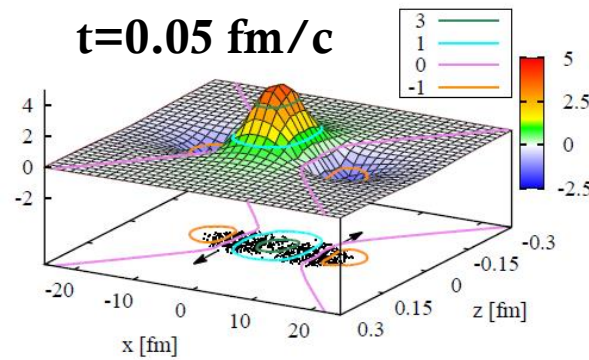
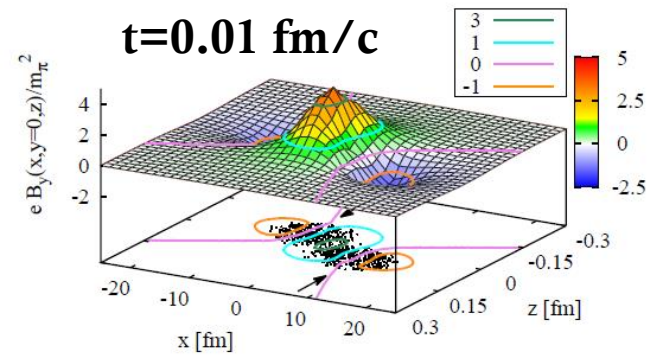
Voronyuk *et al.* (HSD), PRC 83 (2011) 054911

electromagnetic fields in HICs

in a nuclear collision the magnetic field is a superposition of solenoidal fields from different moving charges

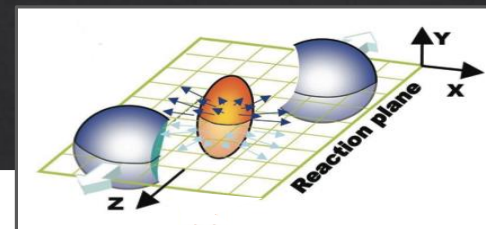


Au+Au @RHIC 200 GeV - b = 10 fm

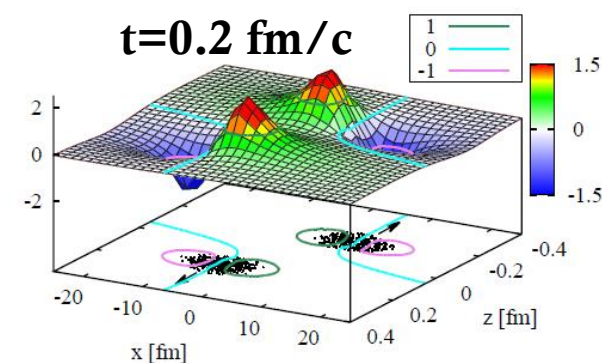
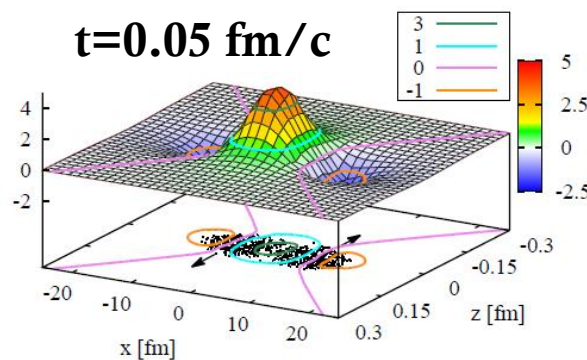
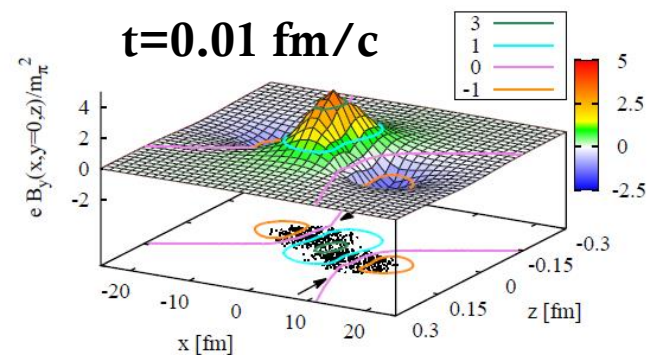


electromagnetic fields in HICs

in a nuclear collision the magnetic field is a superposition of solenoidal fields from different moving charges

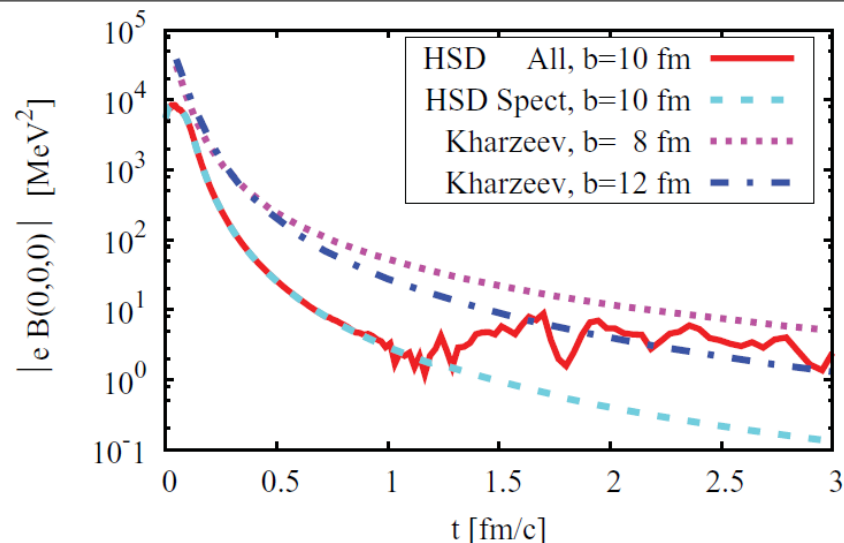


Au+Au @RHIC 200 GeV - b = 10 fm



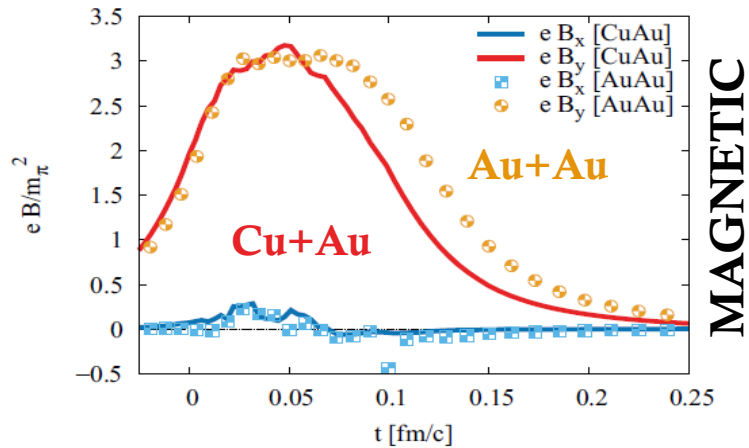
MAGNETIC FIELD

- ❖ dominated by the y-component
- ❖ maximal strength reached during nuclear overlapping time
- ❖ only due to spectators up to $t \sim 1$ fm/c
- ❖ drops down by three orders of magnitude and become comparable with that from participants

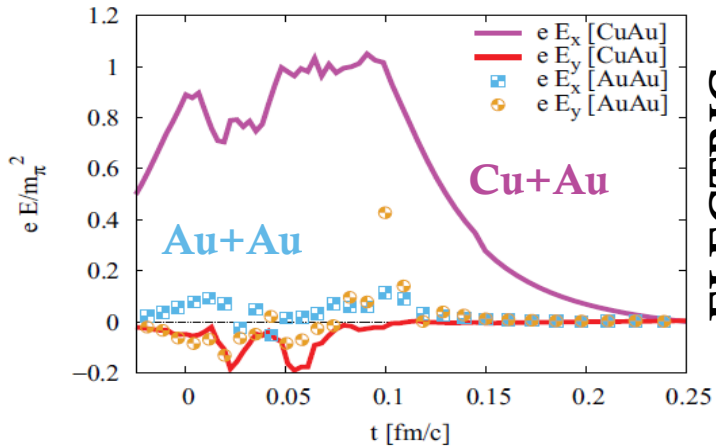


electromagnetic fields in HICs

RHIC 200 GeV - $b = 7$ fm



MAGNETIC



ELECTRIC

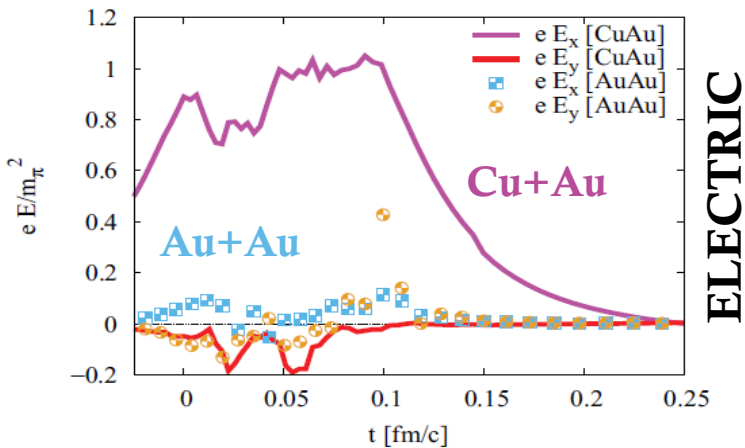
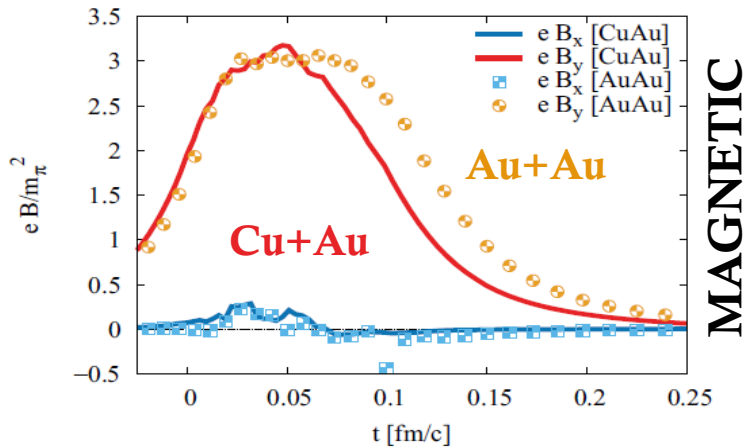
- ✓ **SYMMETRIC SYSTEMS (e.g. Au+Au)**
transverse momentum increments due to electric and magnetic fields compensate each other
- ✓ **ASYMMETRIC SYSTEMS (e.g. Cu+Au)**
an intense electric fields directed from the heavy nuclei to light one appears in the overlap region

Voronyuk *et al.* (PHSD), PRC 90 (2014) 064903

Toneev *et al.* (PHSD), PRC 95 (2017) 034911

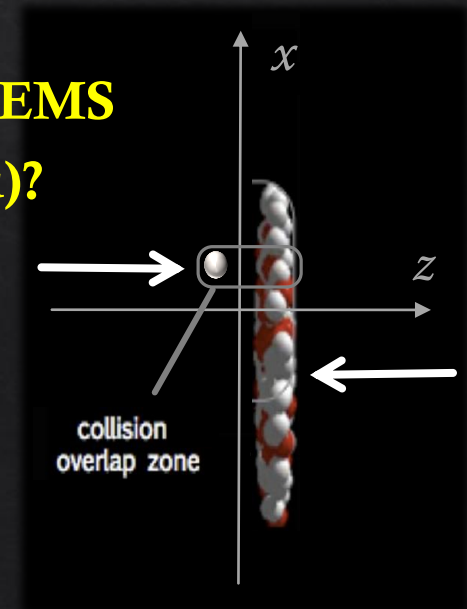
electromagnetic fields in HICs

RHIC 200 GeV - $b = 7$ fm



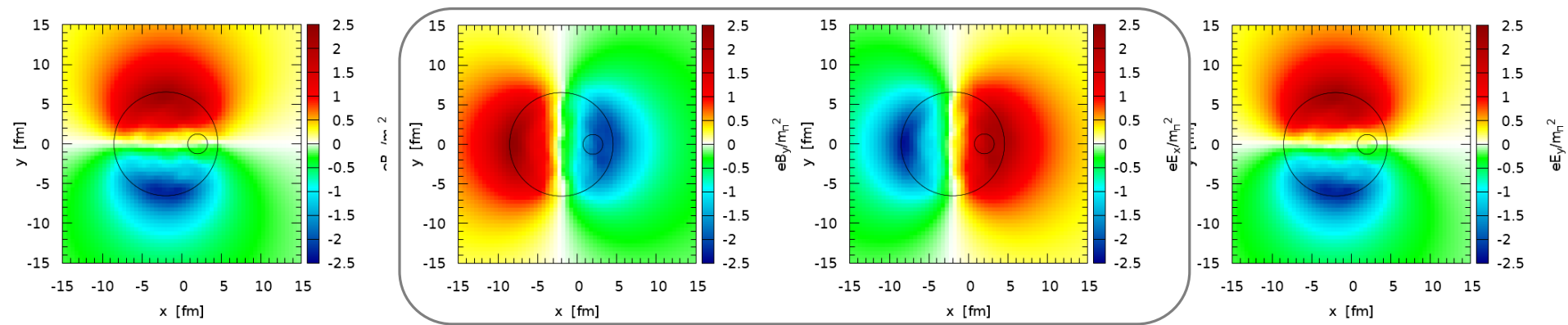
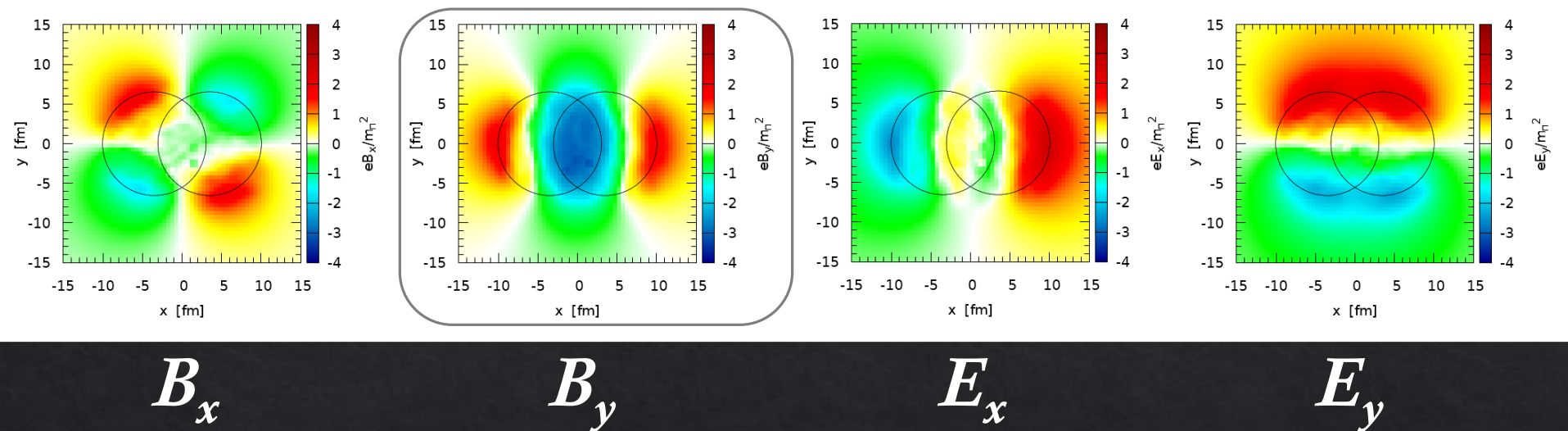
- ✓ **SYMMETRIC SYSTEMS** (e.g. Au+Au)
transverse momentum increments due to electric and magnetic fields compensate each other
- ✓ **ASYMMETRIC SYSTEMS** (e.g. Cu+Au)
an intense electric fields directed from the heavy nuclei to light one appears in the overlap region

SMALL SYSTEMS
(e.g. p+Au)?



p+Au: electromagnetic fields

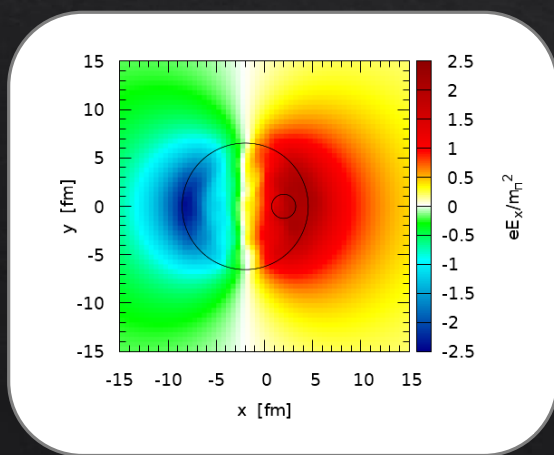
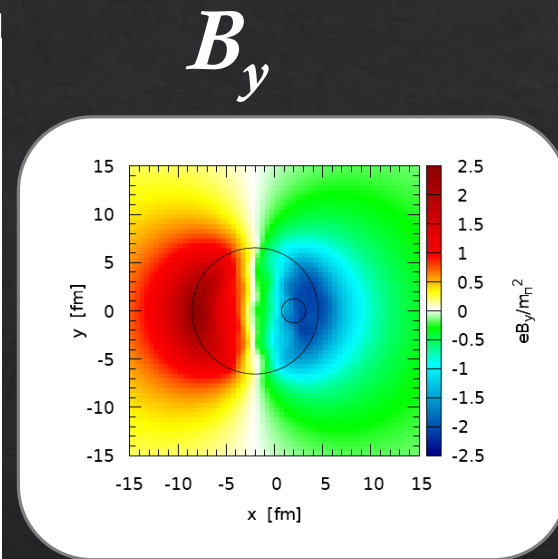
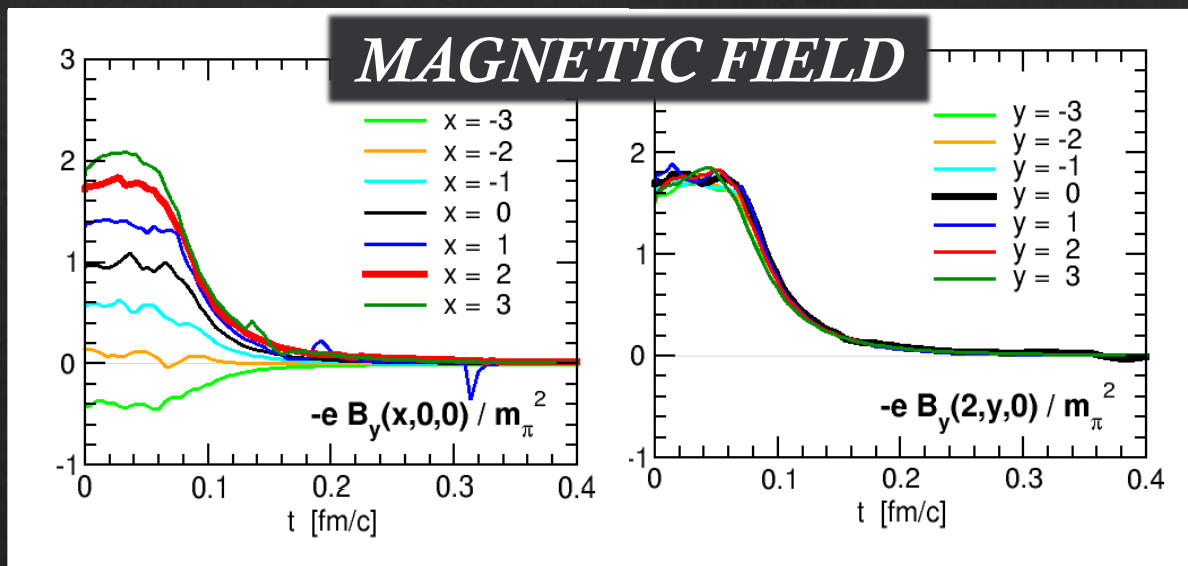
Au+Au @ RHIC 200 GeV $b=7$ fm



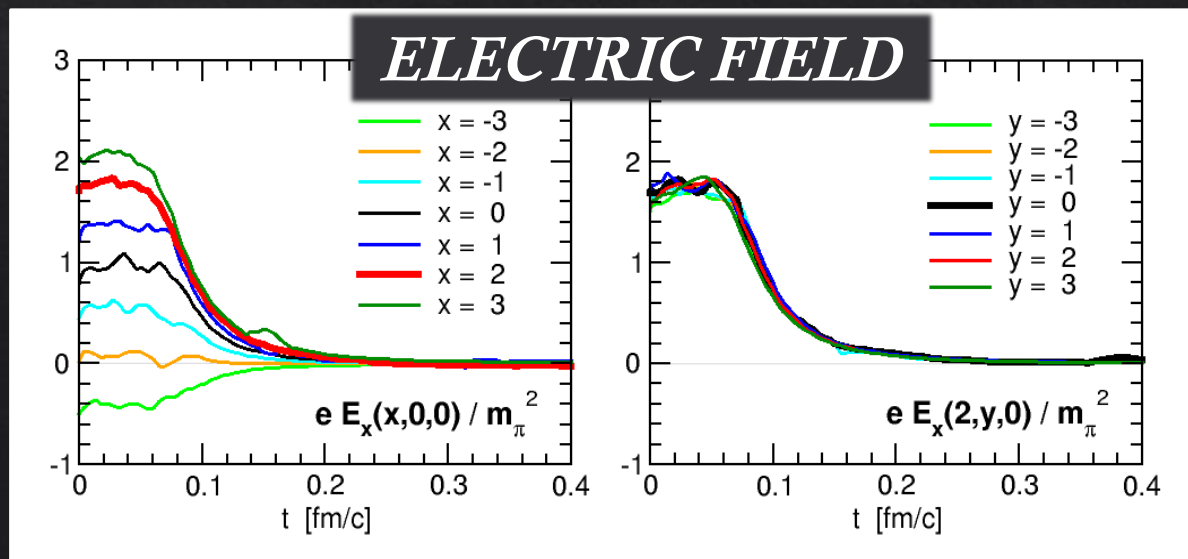
p+Au @ RHIC 200 GeV $b=4$ fm

p+Au: electromagnetic fields

p+Au @ RHIC 200 GeV $b=4$ fm

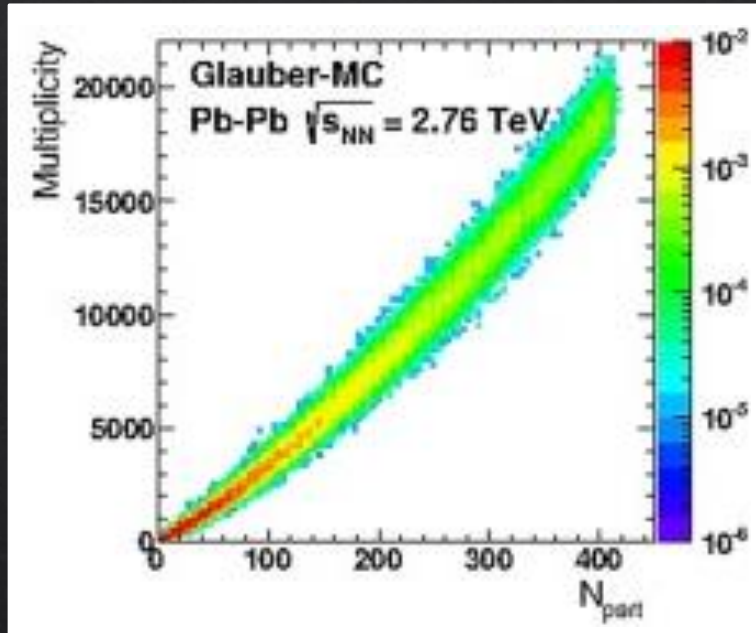


E_x



centrality in small systems

In heavy ion collisions centrality characterizes the amount of overlap or size of the fireball in the collision region

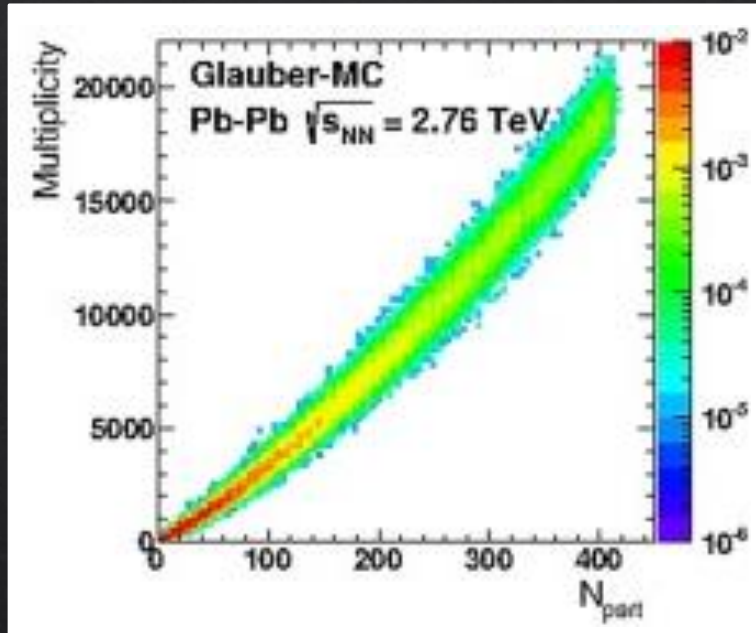


ALICE, NPA 932 (2014) 399

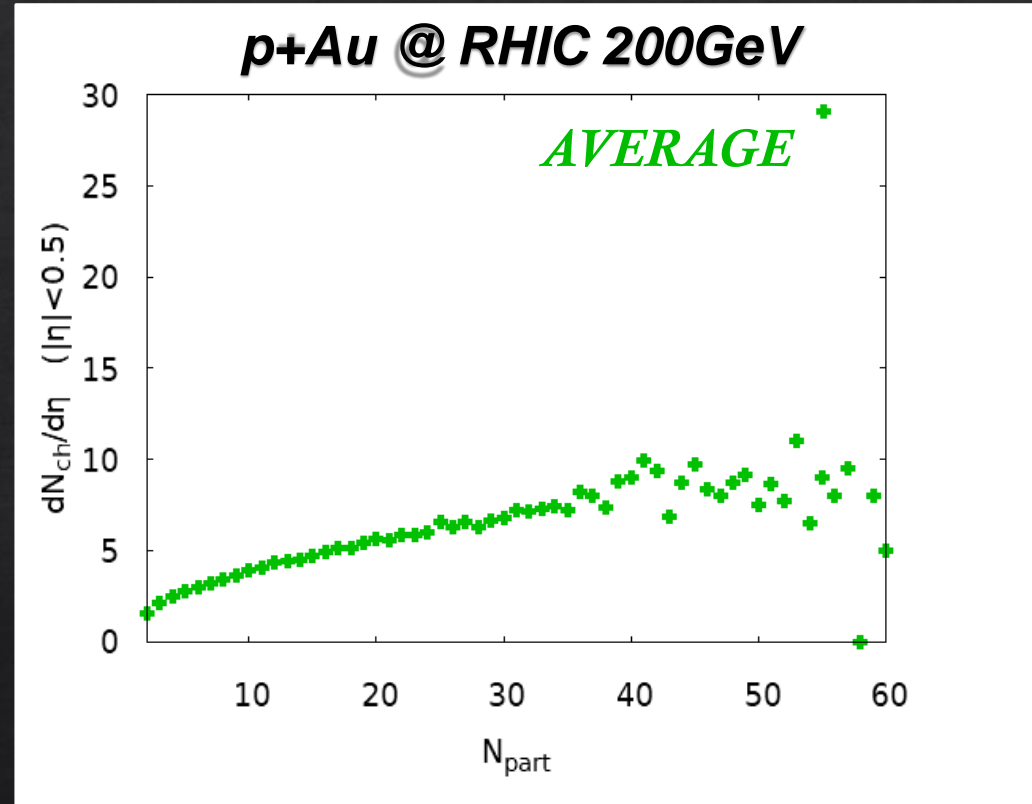
Correlation between participant number and charged particle multiplicity at midrapidity

p+Au: centrality determination

In heavy ion collisions centrality characterizes the amount of overlap or size of the fireball in the collision region



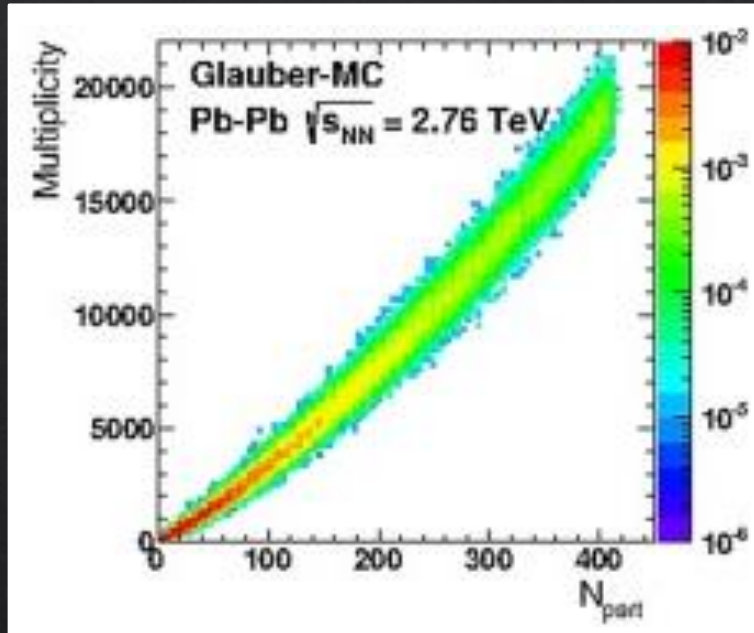
ALICE, NPA 932 (2014) 399



Correlation between participant number and charged particle multiplicity at midrapidity

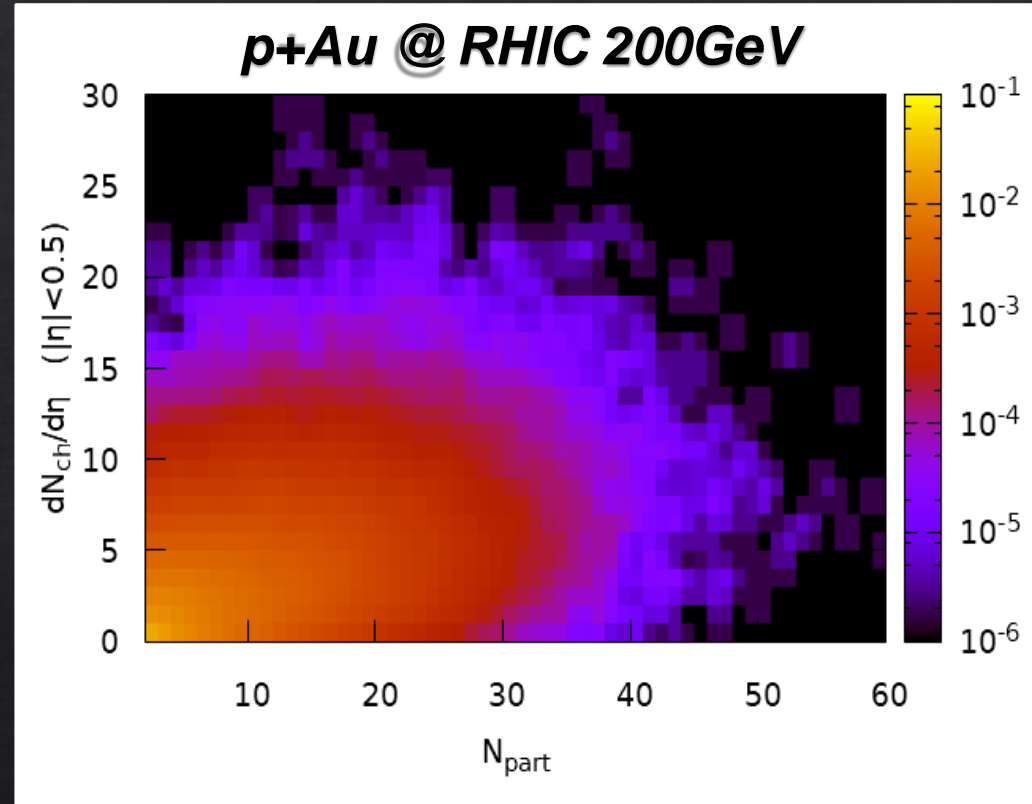
p+Au: centrality determination

In heavy ion collisions centrality characterizes the amount of overlap or size of the fireball in the collision region



ALICE, NPA 932 (2014) 399

LO, Moreau, Voronyuk and Bratkovskaya, 1909.06770



Correlation between participant number and charged particle multiplicity at midrapidity

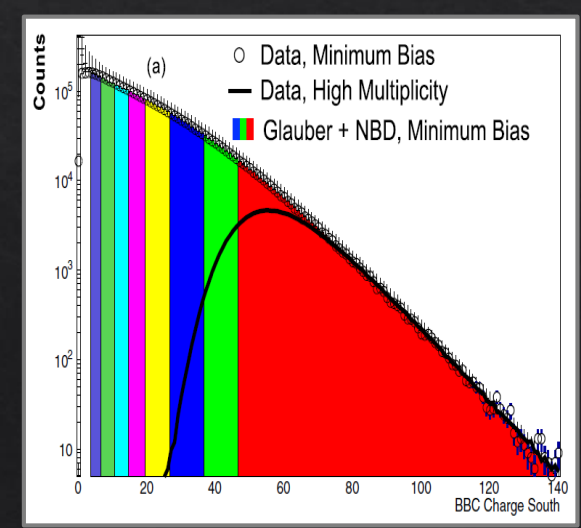
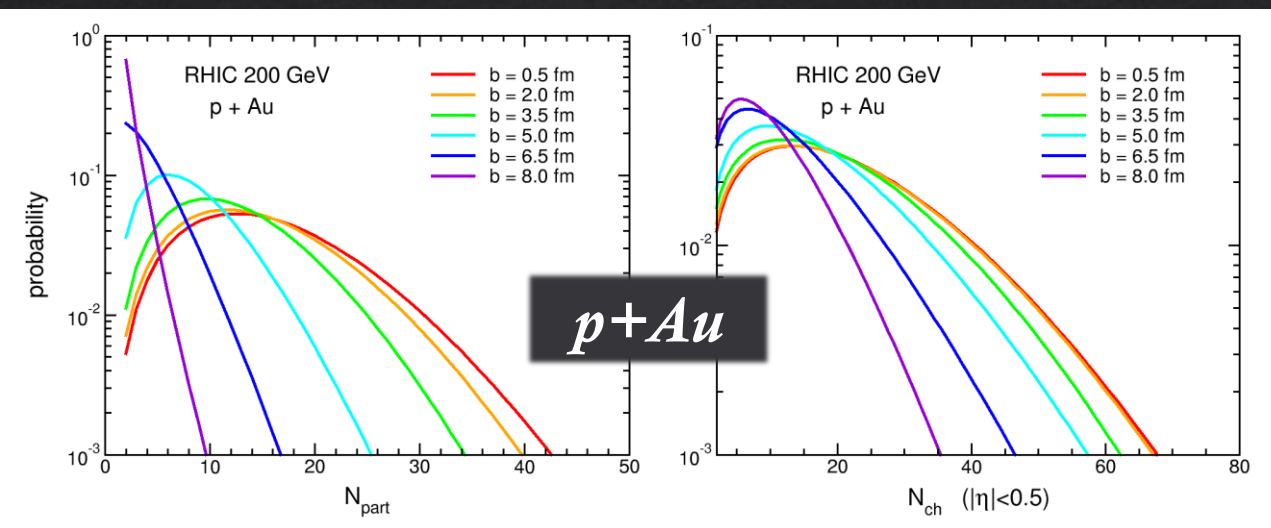
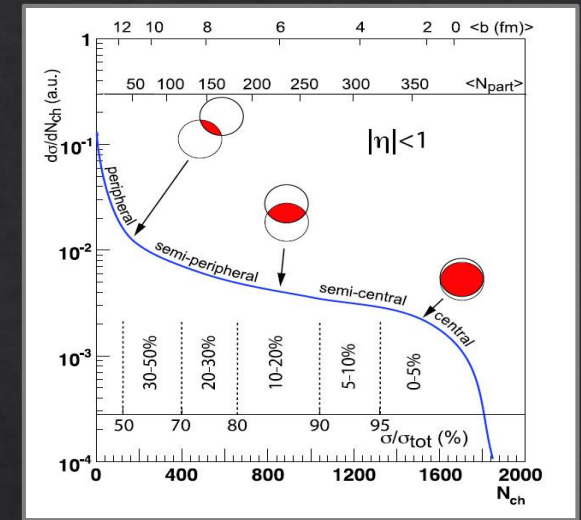
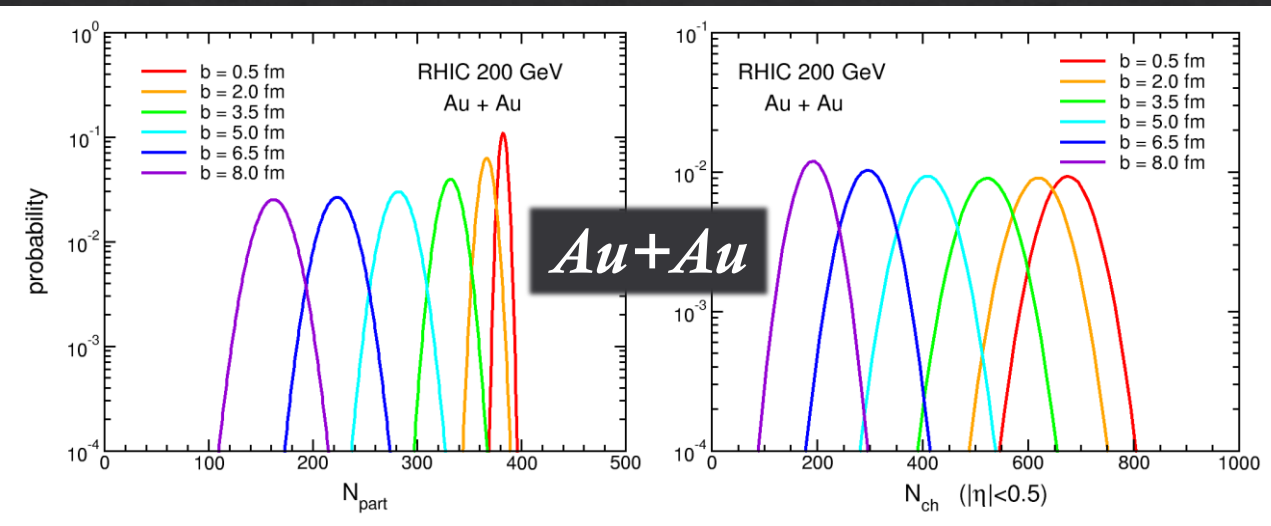
BUT

large dispersion in both quantities in p+A respect to A+A collisions

Centrality in small systems

LO, Moreau, Voronyuk and Bratkovskaya, 1909.06770

Miller *et al.*, ARNPS 57 (2007) 205



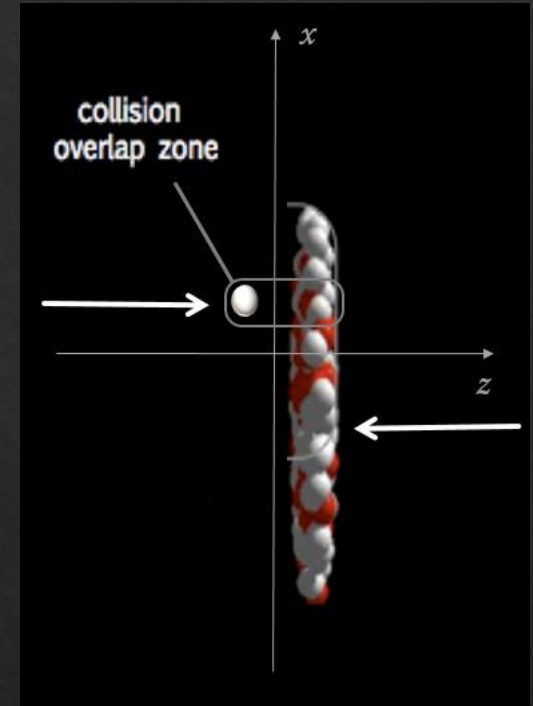
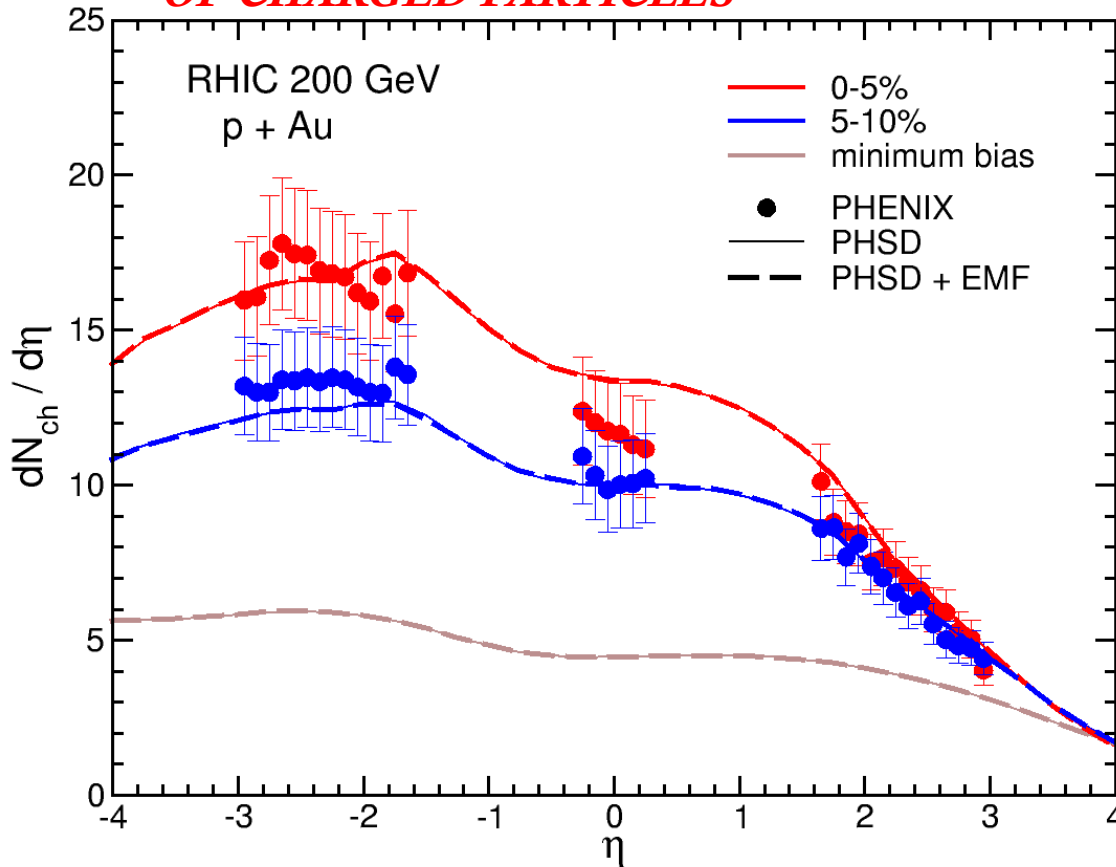
Multiplicity fluctuation in the final state mixes events from different impact parameters!

PHENIX, PRC 95 (2017) 034910

p+Au: rapidity distributions

Exp. Data: PHENIX Collaboration, PRL 121 (2018) 222301

PSEUDORAPIDITY DISTRIBUTION OF CHARGED PARTICLES

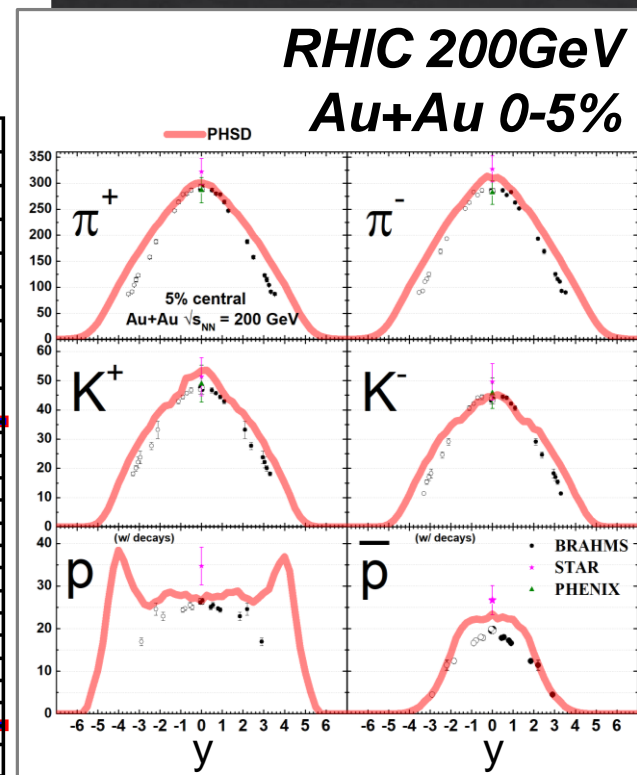
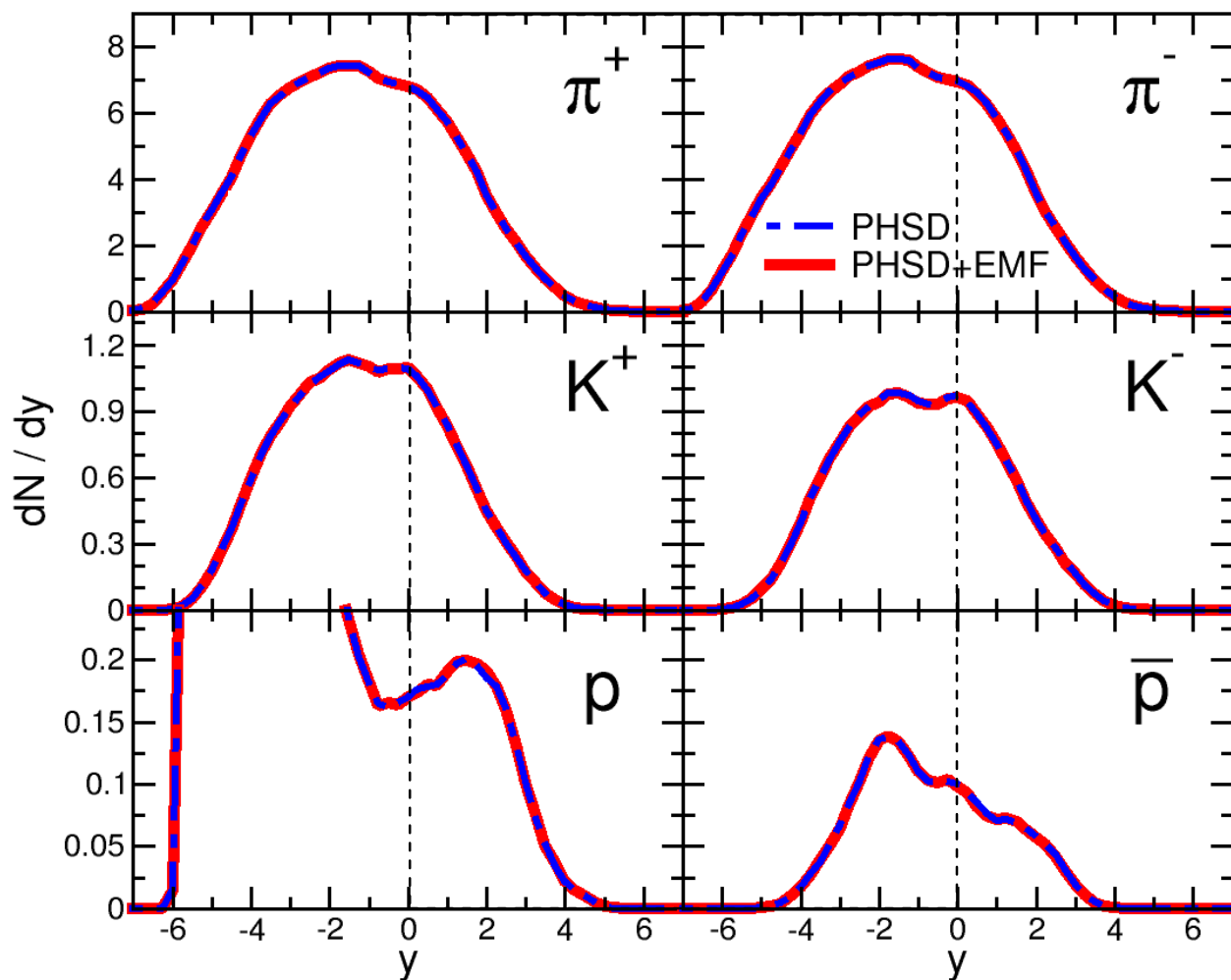


- enhanced particle production in the Au-going directions
- asymmetry increases with centrality of the collision

LO, Moreau, Voronyuk and Bratkovskaya, 1909.06770

p+Au: rapidity distributions

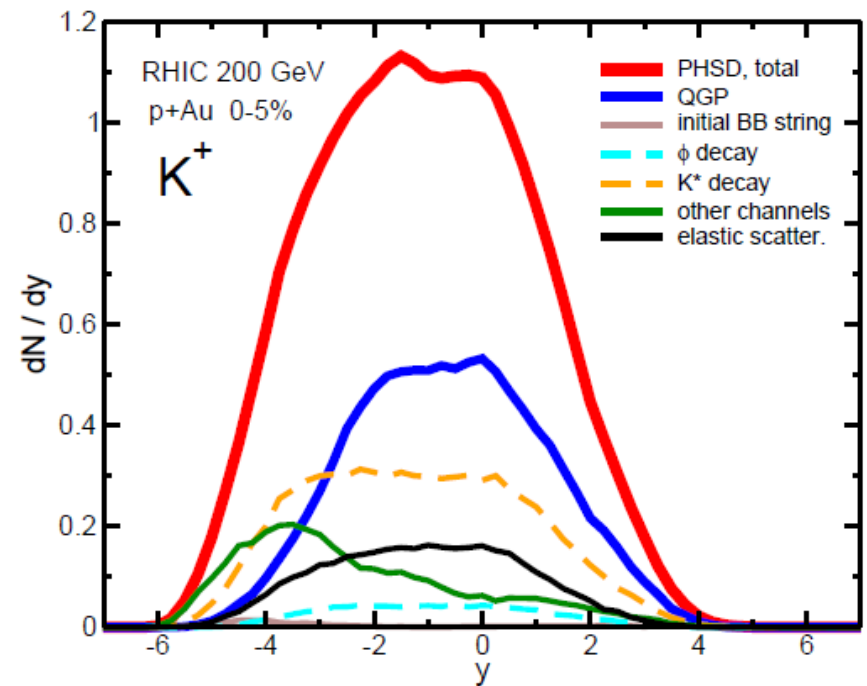
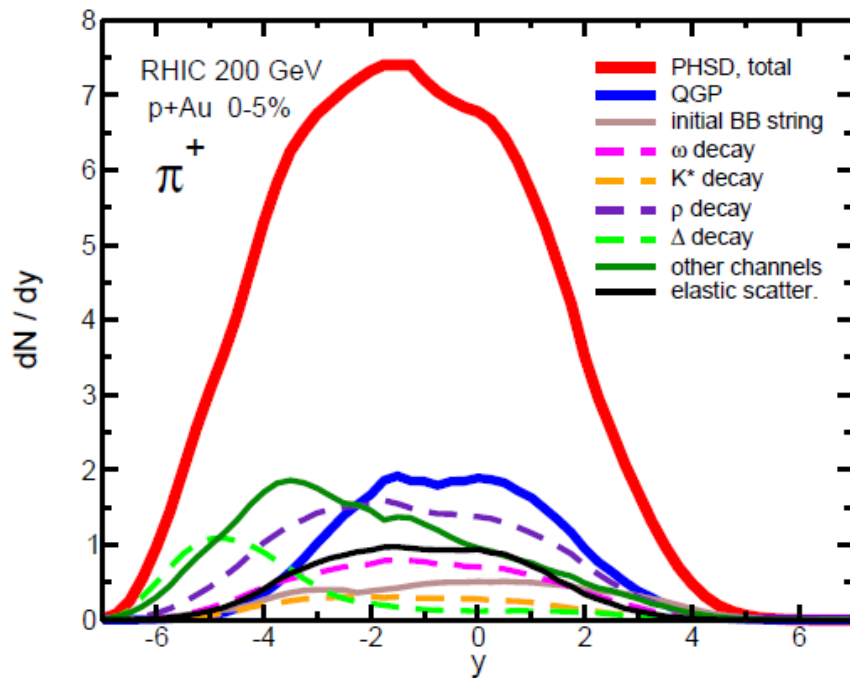
RAPIDITY DISTRIBUTION OF IDENTIFIED PARTICLES RHIC 200GeV
p+Au 0-5%



**symmetric
colliding system**

p+Au: rapidity distributions

RAPIDITY DISTRIBUTION OF IDENTIFIED PARTICLES channel decomposition



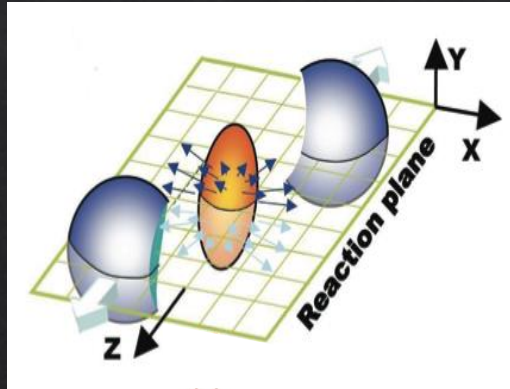
large amount of particles escapes from the medium
just after production from QGP hadronization
without further rescattering

Anisotropic radial flow

A DEEPER INSIGHT...INITIAL-STATE FLUCTUATIONS

Not a simple almond shape

➤ odd harmonics = 0

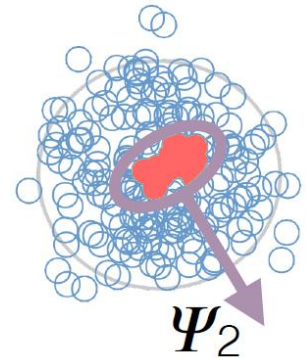


$$E \frac{d^3 N}{d^3 p} = \frac{1}{2\pi} \frac{d^2 N}{p_T dp_T dy} \left(1 + 2 \sum_{n=1}^{\infty} v_n(p_T, y) \cos(n(\phi - \Psi_r)) \right)$$

$$v_n = \langle \cos(n(\phi - \Psi_r)) \rangle$$

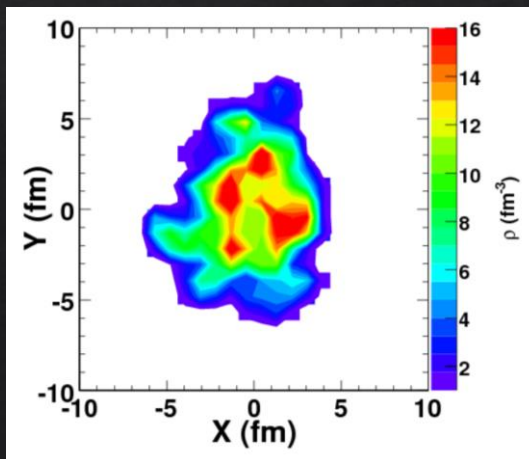


ELLIPTICITY

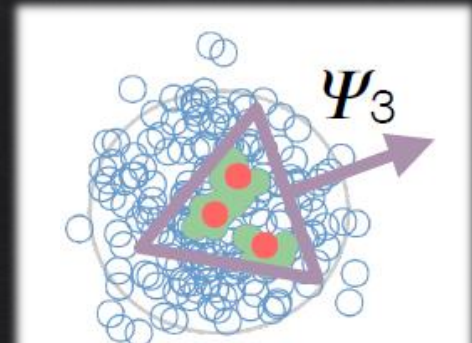


But a “lumpy” profile due to fluctuations of nucleon position in the overlap region

➤ odd harmonics ≠ 0



Plumari et al., PRC 92 (2015) 054902



TRIANGULARITY

Anisotropic radial flow

A DEEPER INSIGHT...FINITE EVENT MULTIPLICITY

azimuthal particle distributions
w.r.t. the reaction plane

$$\frac{dN}{d\varphi} \propto 1 + \sum_n 2v_n(p_T) \cos[n(\varphi - \Psi_n)]$$

n-th order
flow harmonics

$$v_n = \frac{\langle \cos[n(\varphi - \Psi_n)] \rangle}{\text{Res}(\Psi_n)}$$

event-plane angle resolution
(three-subevent method)

Important especially for small
colliding system, e.g. p+A

n-th order
event-plane angle

$$\Psi_n = \frac{1}{n} \text{atan2}(Q_n^y, Q_n^x)$$

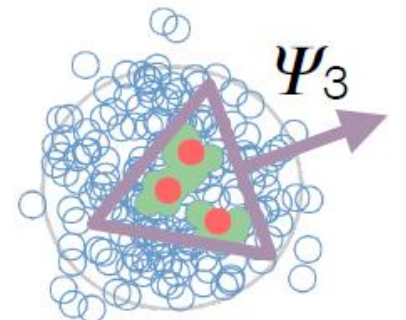
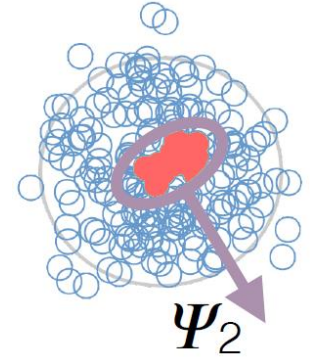
$$Q_n^x = \sum_i \cos[n\varphi_i]$$

$$Q_n^y = \sum_i \sin[n\varphi_i]$$

Since the finite number of particles produces limited resolution in the determination of Ψ_n , the v_n must be corrected up to what they would be relative to the real reaction plane

Poskanzer and Voloshin,
PRC 58 (1998) 1671

ELLIPTICITY

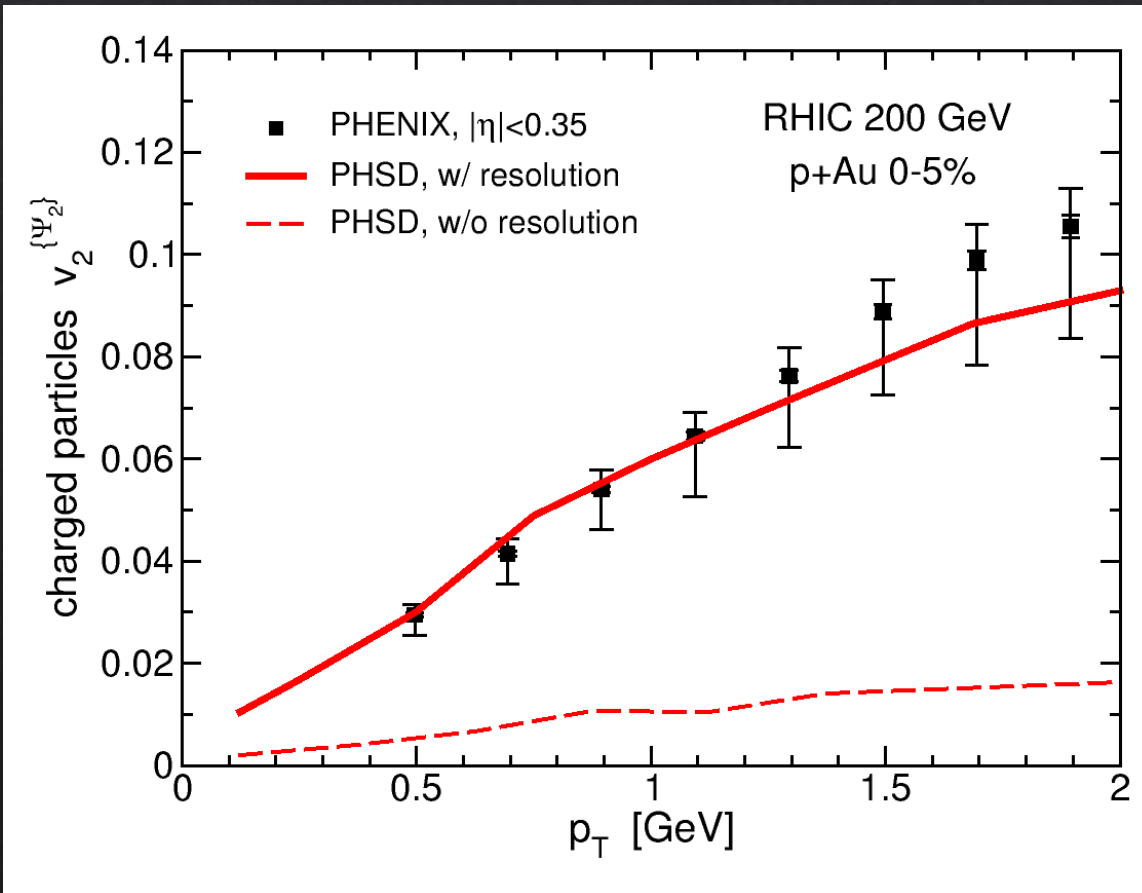


TRIANGULARITY

p+Au: elliptic flow

ELLIPTIC FLOW OF CHARGED PARTICLES

$$v_2(p_T) = \frac{\langle \cos[2(\varphi(p_T) - \Psi_2)] \rangle}{Res(\Psi_2)}$$



Event-plane angle
in $-3 < \eta < -1$:
 $Res(\Psi_2^{PHSD}) = 0.175$
 $Res(\Psi_2^{PHENIX}) = 0.171$

magnitude correlated with
the determination of the
reaction plane

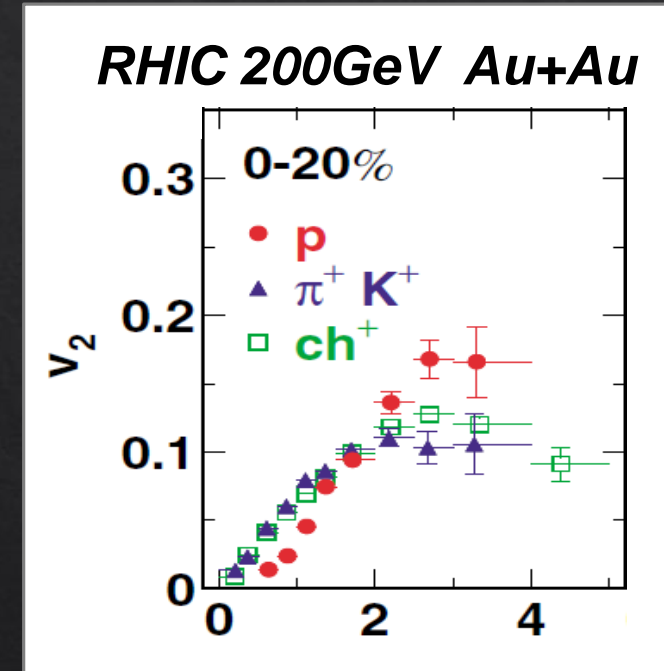
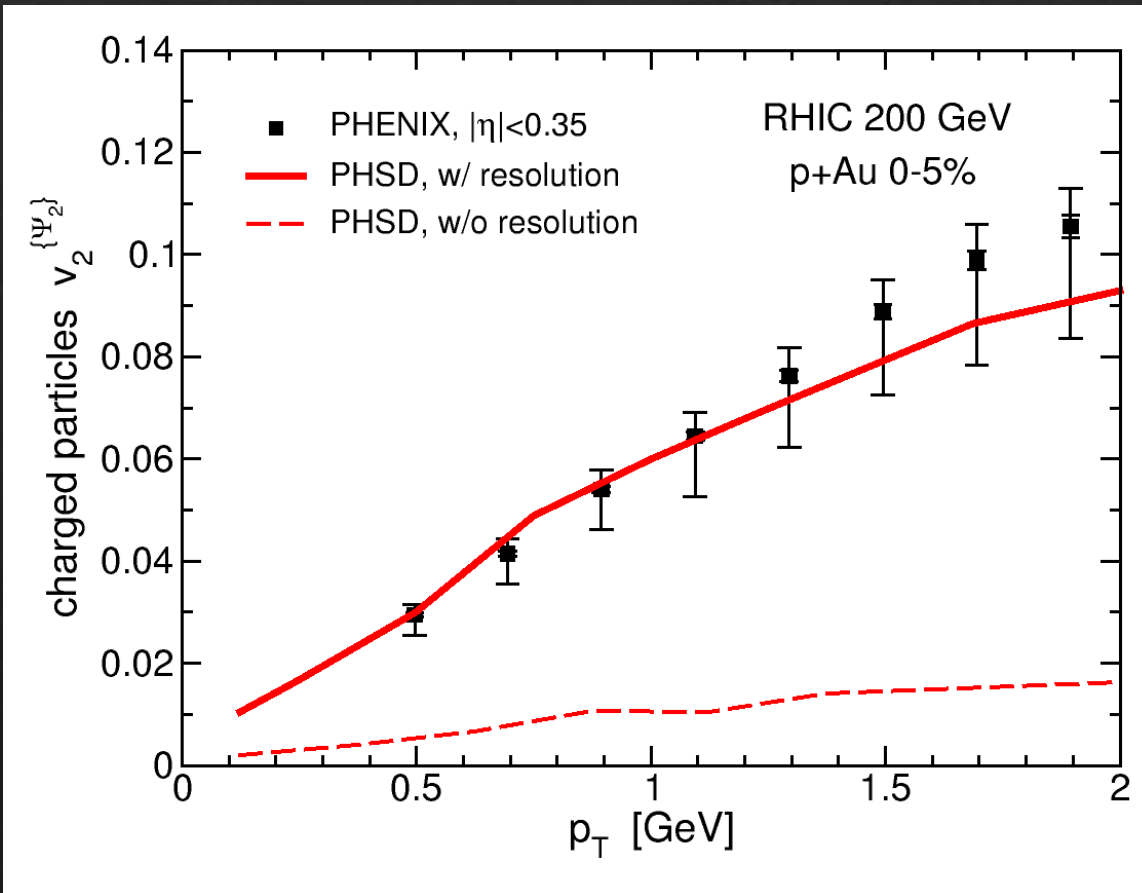
LO, Moreau, Voronyuk and Bratkovskaya, 1909.06770

Exp. data: Aidala et al. (PHENIX Collaboration), PRC 95 (2017) 034910

p+Au: elliptic flow

ELLIPTIC FLOW OF CHARGED PARTICLES

$$v_2(p_T) = \frac{\langle \cos[2(\varphi(p_T) - \Psi_2)] \rangle}{Res(\Psi_2)}$$



PHENIX, PRL 91 (2003) 182301

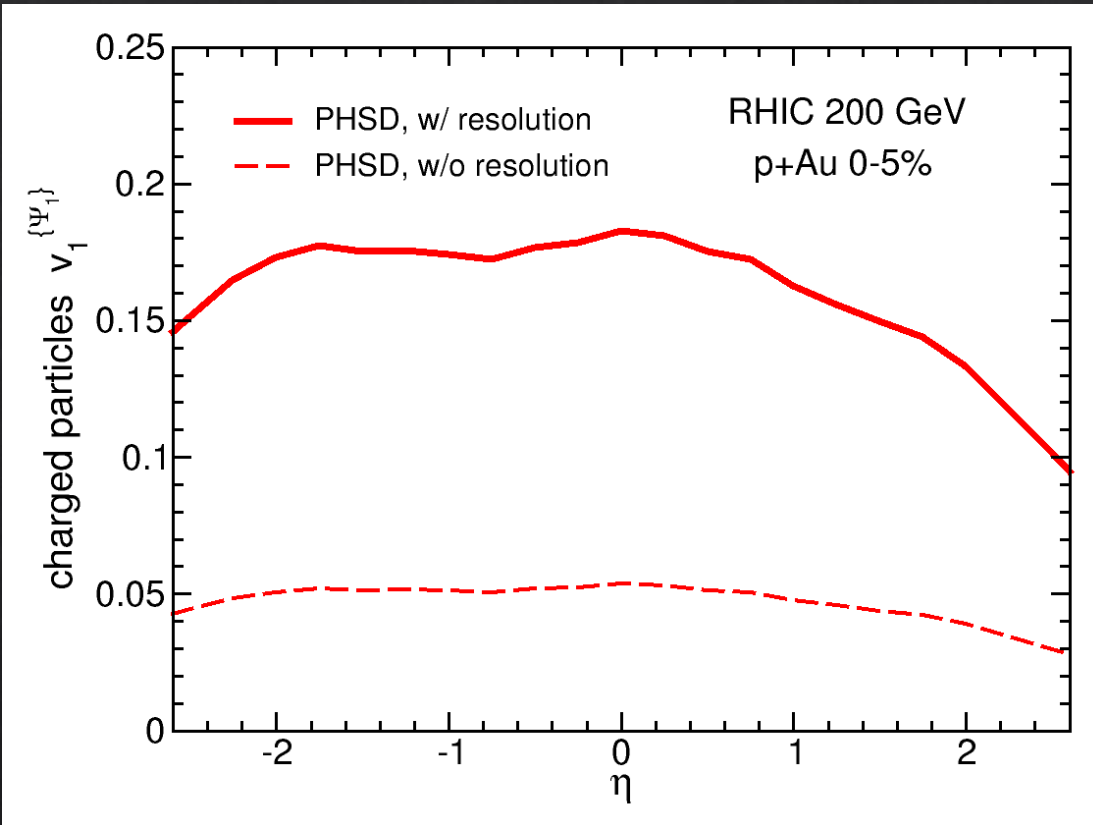
comparable to that found in large colliding systems

LO, Moreau, Voronyuk and Bratkovskaya, 1909.06770

Exp. data: Aidala et al. (PHENIX Collaboration), PRC 95 (2017) 034910

p+Au: directed flow

pseudorapidity dependence of the DIRECTED FLOW OF CHARGED PARTICLES



$$v_1(\eta) = \frac{\langle \cos[\varphi(\eta) - \Psi_1] \rangle}{Res(\Psi_1)}$$

Event-plane angle

in $-4 < \eta < -3$:

$$Res(\Psi_1^{PHSD}) = 0.397$$

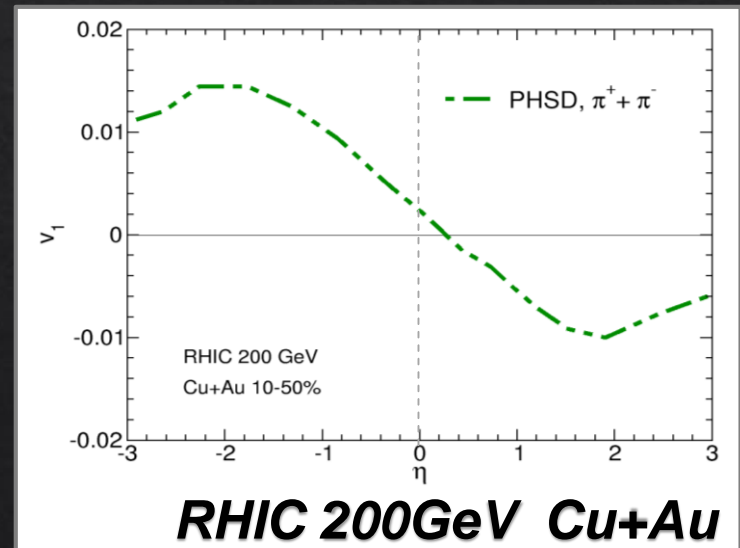
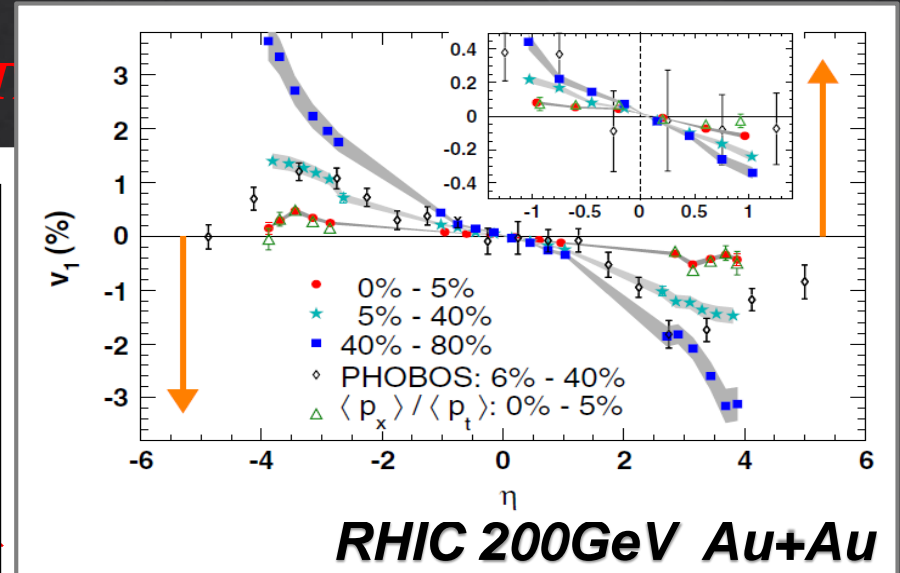
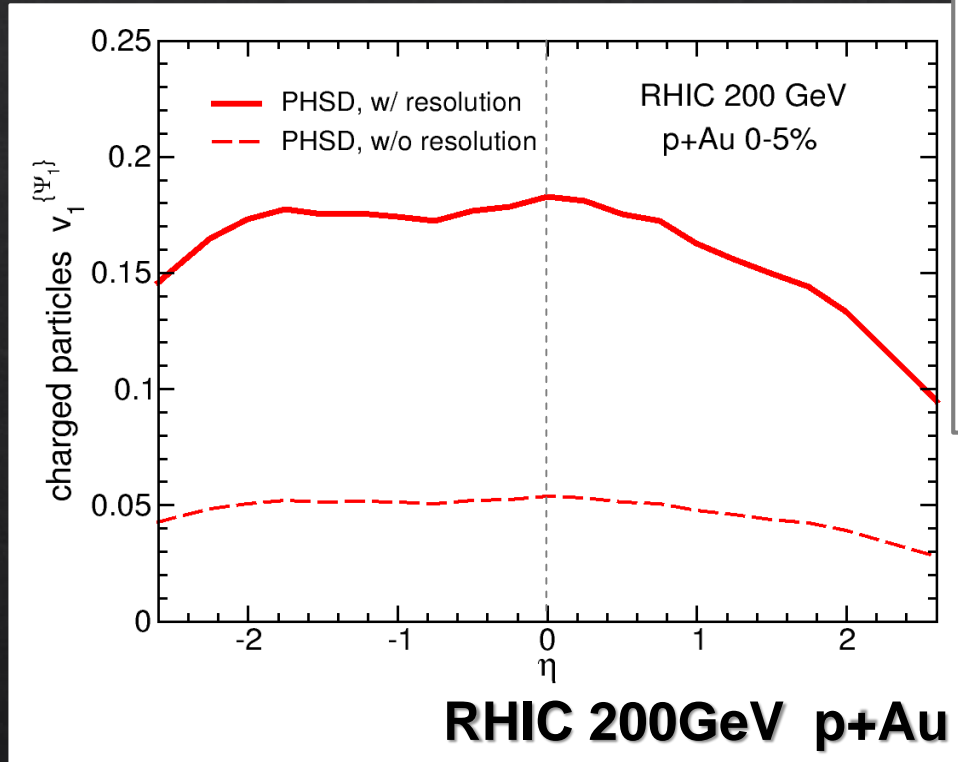
magnitude correlated with
the determination of the
reaction plane

LO, Moreau, Voronyuk and Bratkovskaya, 1909.06770

p+Au: directed flow

STAR Collaboration, PRL 101 (2008) 252301

*pseudorapidity dependence of the
DIRECTED FLOW OF CHARGED PART*



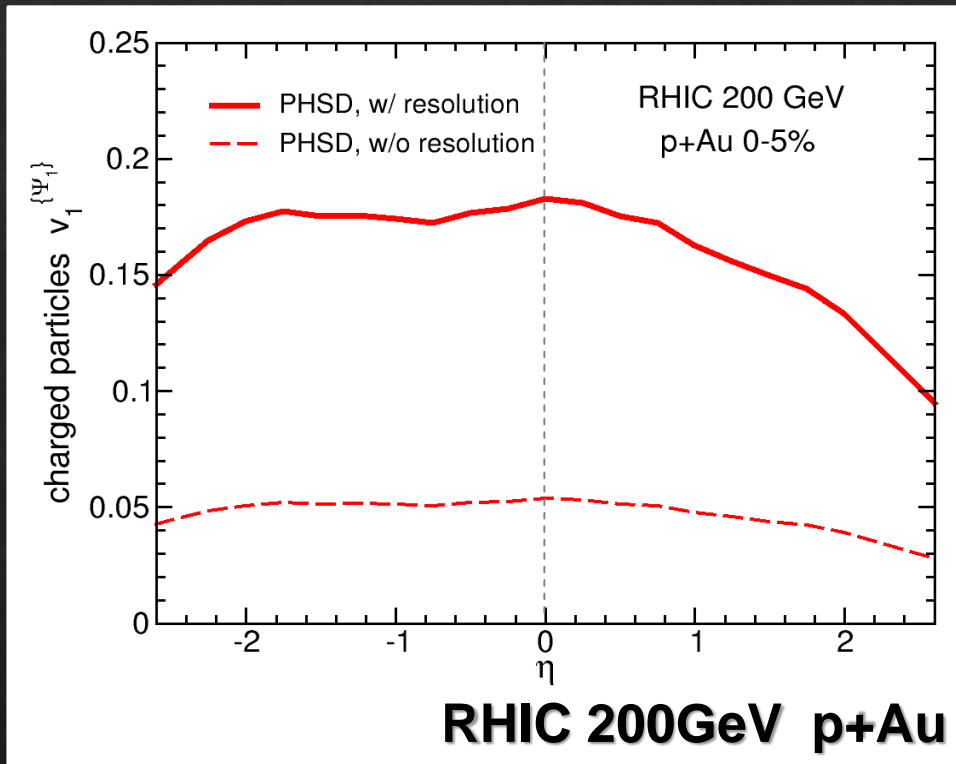
LO, Moreau, Voronyuk and Bratkovskaya, 1909.06770

Voronyuk *et al.*, PRC 90 (2014) 064903

Toneev *et al.*, PRC 95 (2017) 034911

p+Au: directed flow

pseudorapidity dependence of the DIRECTED FLOW OF CHARGED PARTICLES



LO, Moreau, Voronyuk and Bratkovskaya, 1909.06770



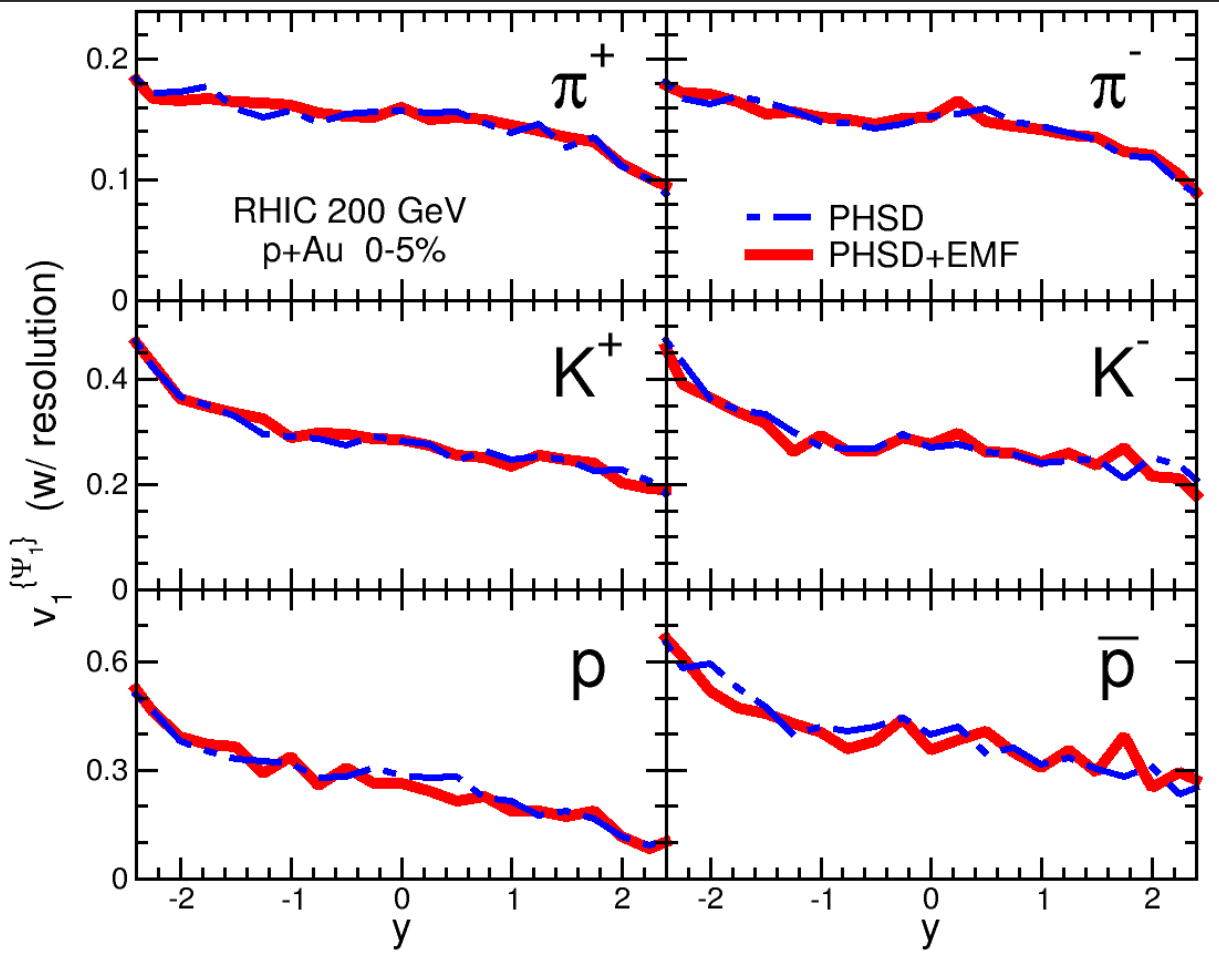
**SPLITTING OF POSITIVELY AND NEGATIVELY
CHARGED PARTICLES INDUCED BY THE ELECTROMAGNETIC FIELD?**

p+Au: directed flow

*rapidity dependence of the
DIRECTED FLOW OF IDENTIFIED PARTICLES*

$$v_1(\eta) = \frac{\langle \cos[\varphi(\eta) - \Psi_1] \rangle}{Res(\Psi_1)}$$

LO, Moreau, Voronyuk and Bratkovskaya, 1909.06770



**SPLITTING
INDUCED BY
THE EM FIELD?**

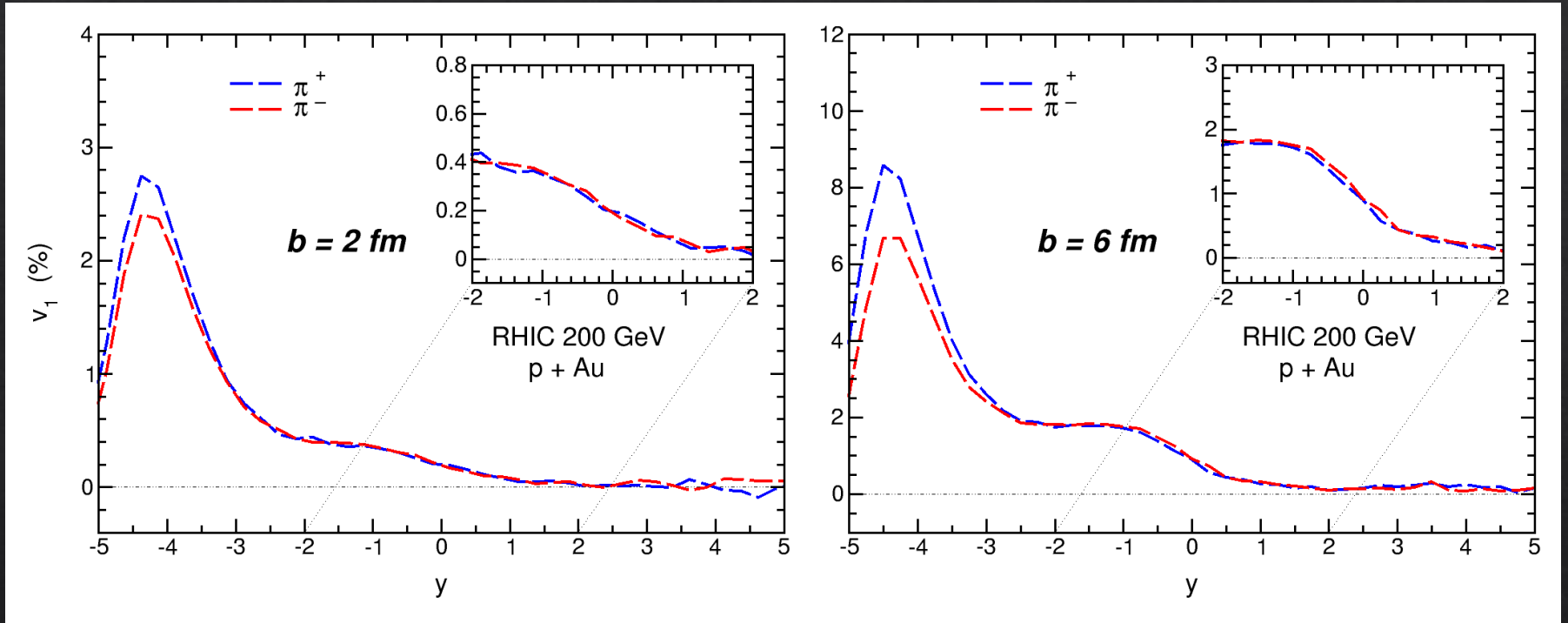
no visible changes
with and without
electromagnetic fields
for 5% central collisions

BUT...

p+Au: directed flow

*rapidity dependence of the
DIRECTED FLOW OF PIONS*

$$v_1(y) = \langle \cos[\varphi(y)] \rangle$$



LO, Moreau, Voronyuk and Bratkovskaya, 1909.06770

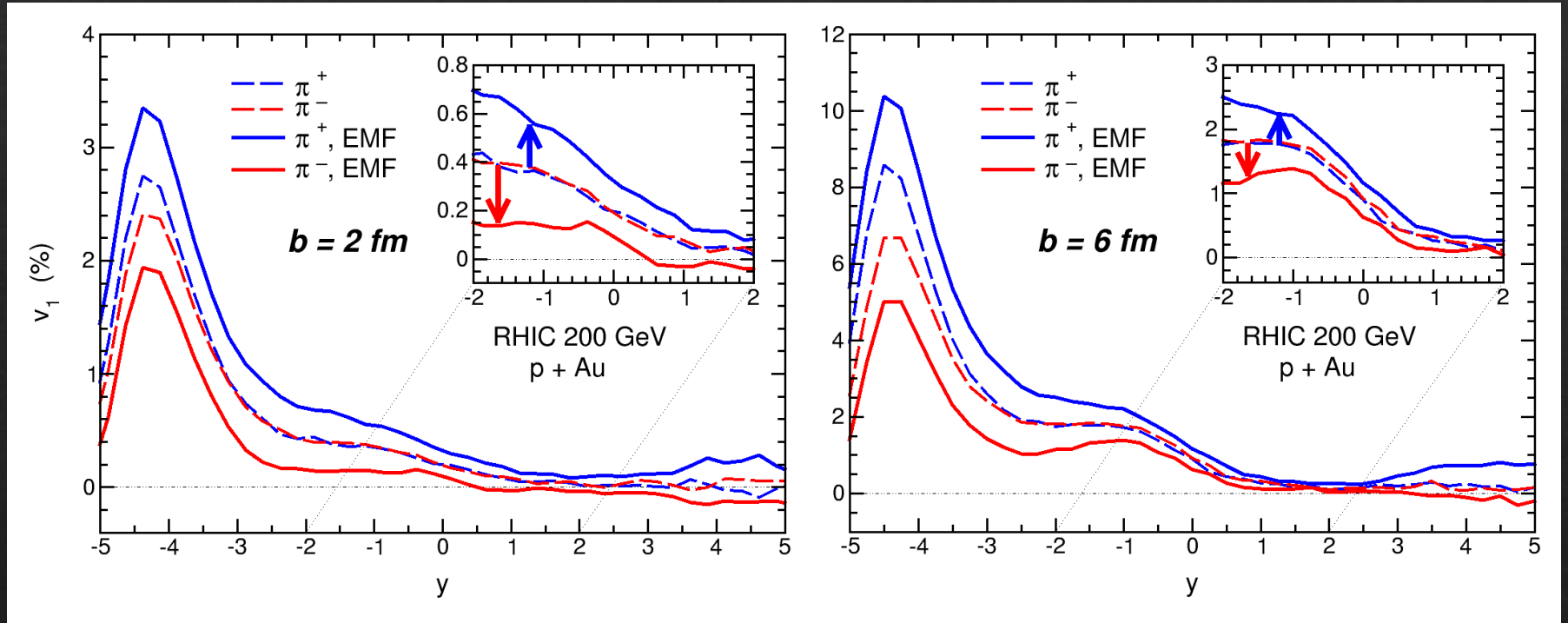


**SPLITTING
INDUCED BY
THE EM FIELD?**

p+Au: directed flow

*rapidity dependence of the
DIRECTED FLOW OF PIONS*

$$v_1(y) = \langle \cos[\varphi(y)] \rangle$$



LO, Moreau, Voronyuk and Bratkovskaya, 1909.06770



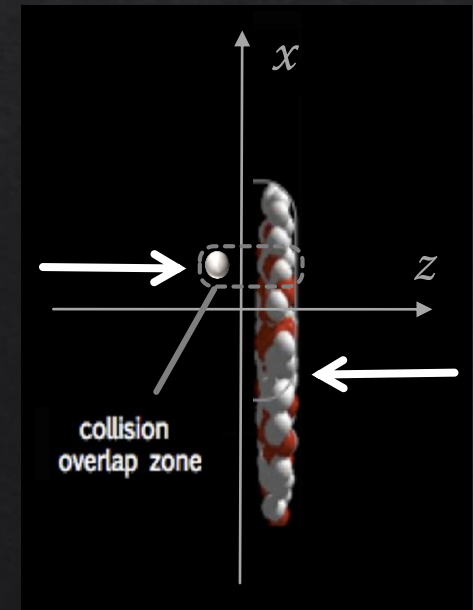
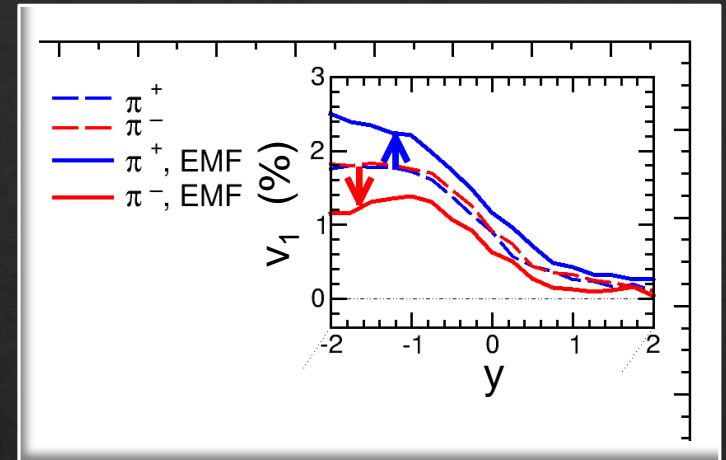
**Splitting of π^+ and π^-
induced by the
electromagnetic field**

p+Au: directed flow

*rapidity dependence of the
DIRECTED FLOW OF PIONS*

collective sideways deflection of particles

$$v_1 = \langle \cos\varphi \rangle = \langle p_x/p_T \rangle$$

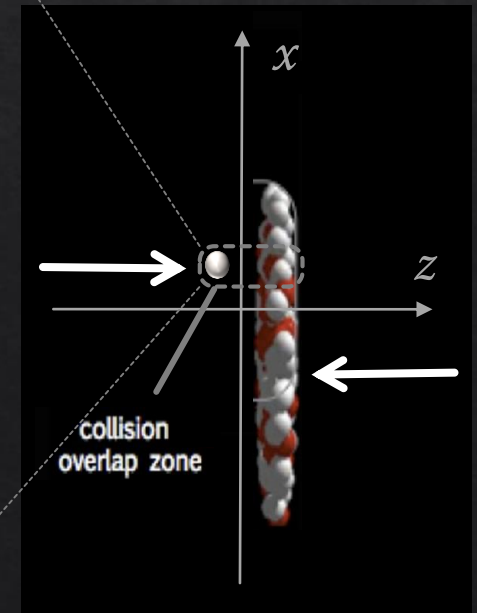
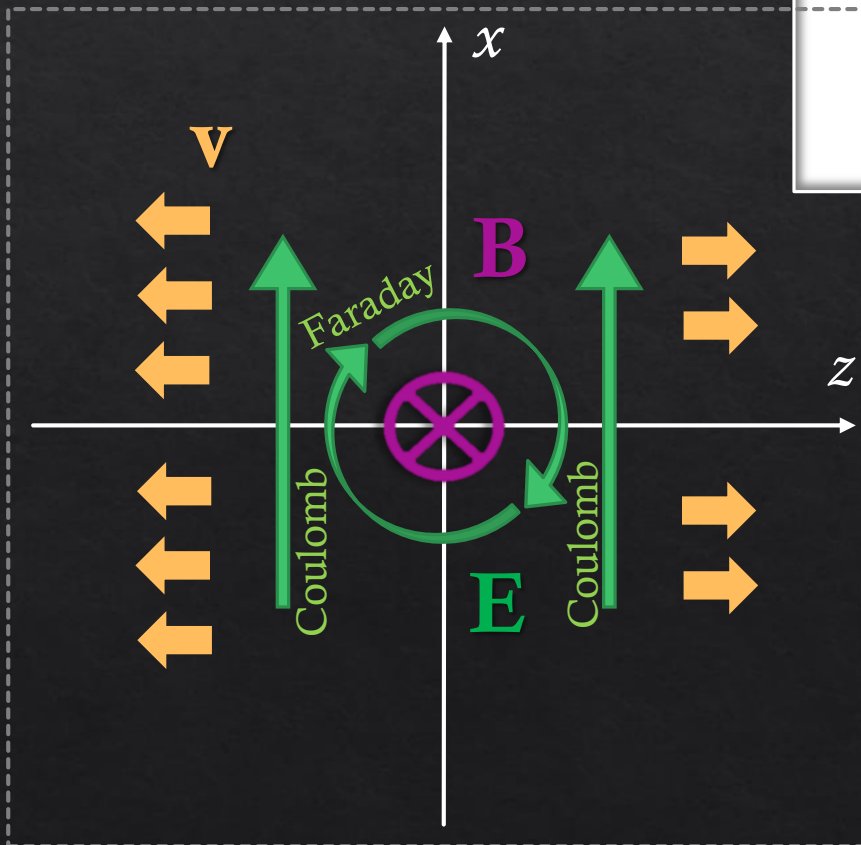
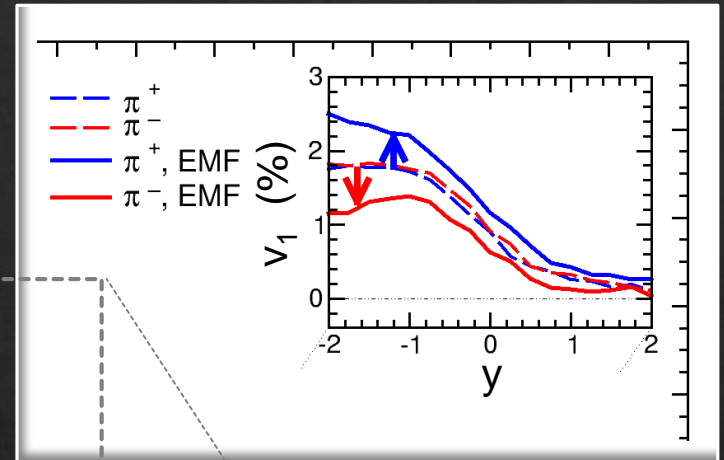


p+Au: directed flow

*rapidity dependence of the
DIRECTED FLOW OF PIONS*

collective sideways deflection of particles

$$v_1 = \langle \cos\phi \rangle = \langle p_x/p_T \rangle$$



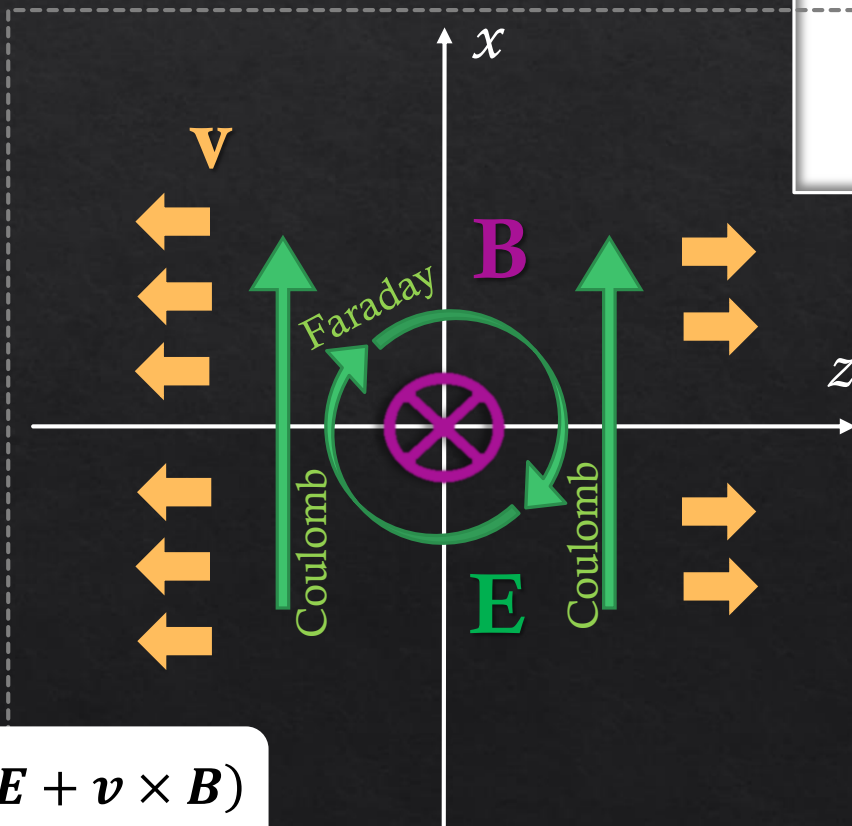
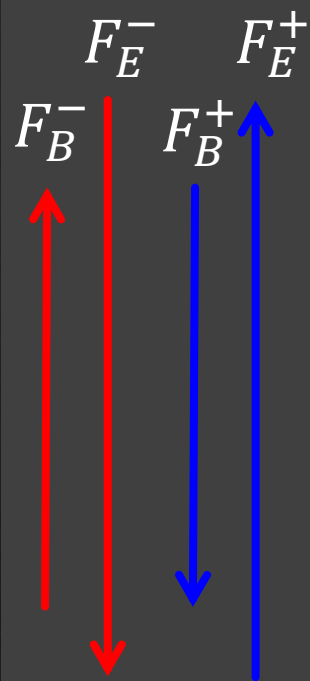
p+Au: directed flow

*rapidity dependence of the
DIRECTED FLOW OF PIONS*

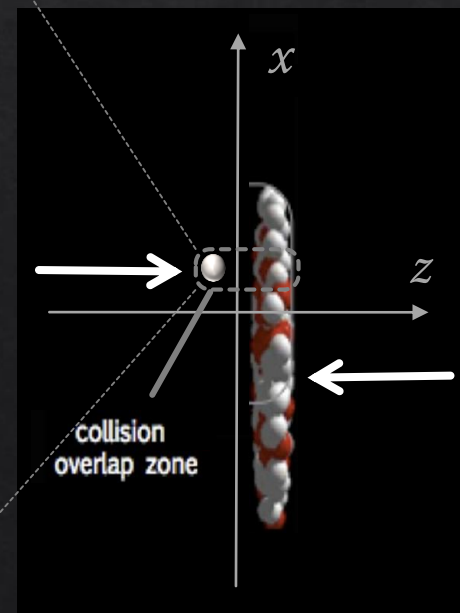
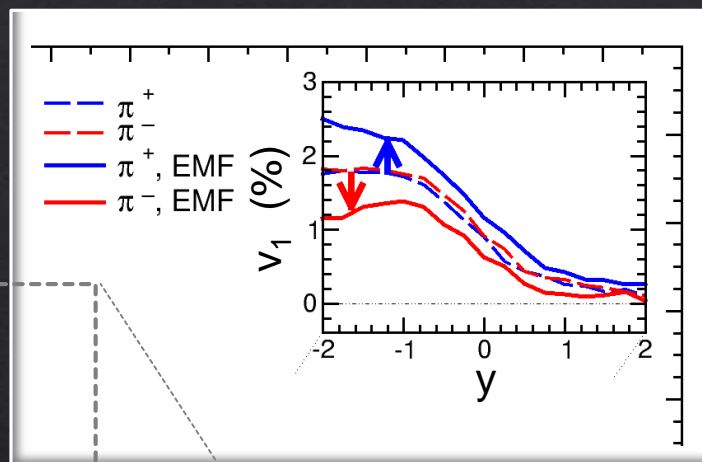
collective sideways deflection of particles

$$v_1 = \langle \cos\phi \rangle = \langle p_x/p_T \rangle$$

$$\eta < 0$$



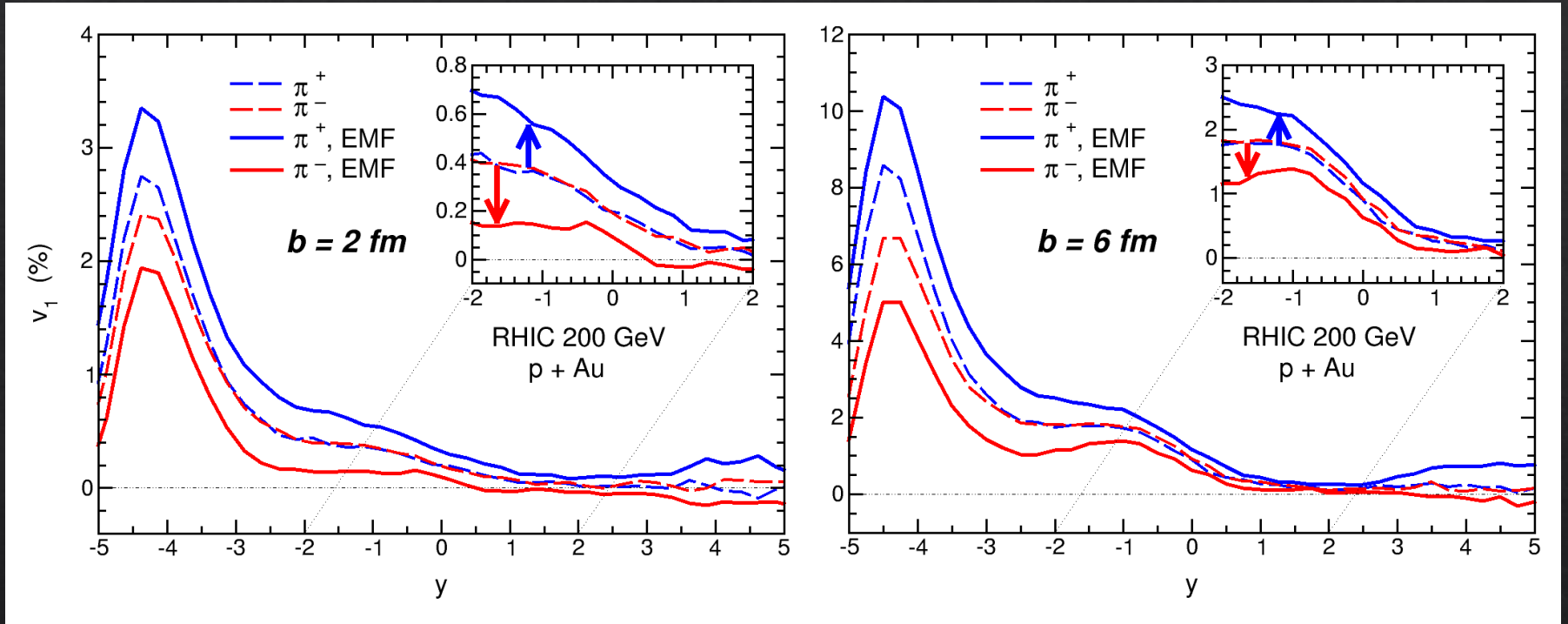
$$F_{Lorentz} = q(\mathbf{E} + \mathbf{v} \times \mathbf{B})$$



p+Au: directed flow

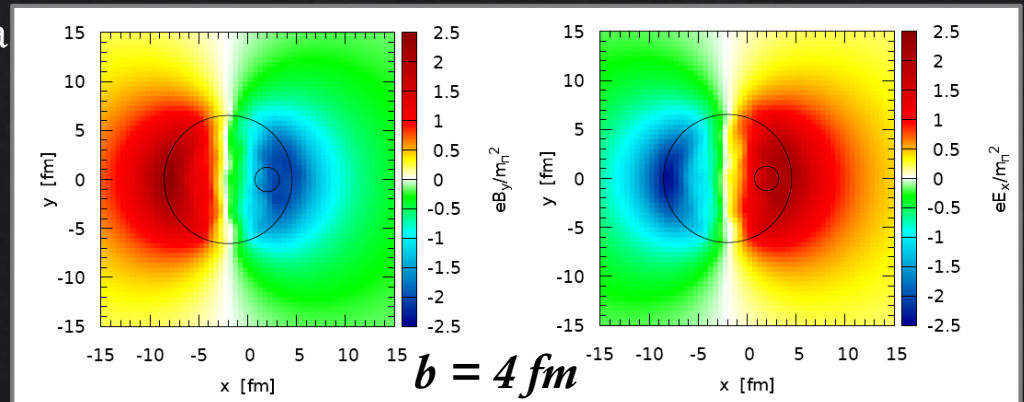
rapidity dependence of the
DIRECTED FLOW OF PIONS

$$v_1(y) = \langle \cos[\varphi(y)] \rangle$$



LO, Moreau, Voronyuk and Bratkovskaya

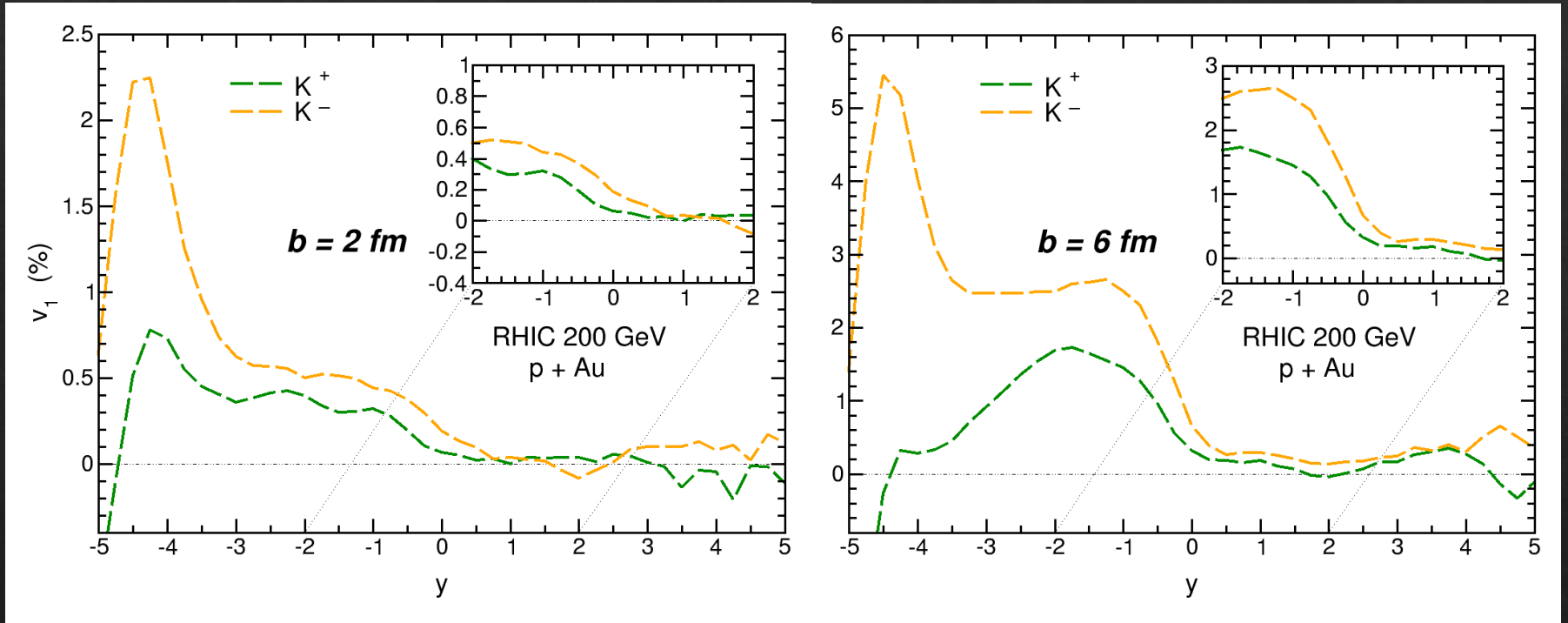
**Splitting of π^+ and π^-
induced by the
electromagnetic field**



p+Au: directed flow

*rapidity dependence of the
DIRECTED FLOW OF KAONS*

$$v_1(y) = \langle \cos[\varphi(y)] \rangle$$

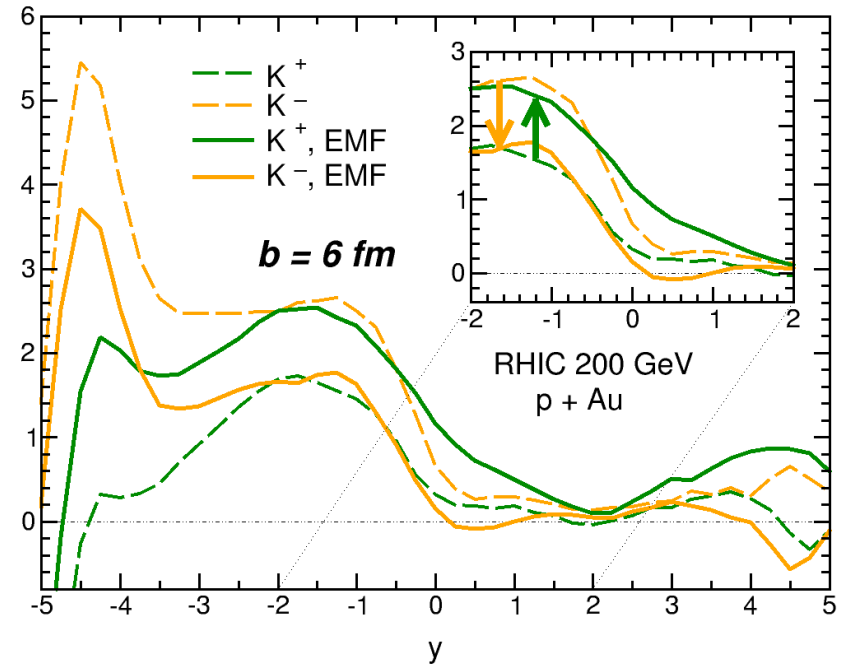
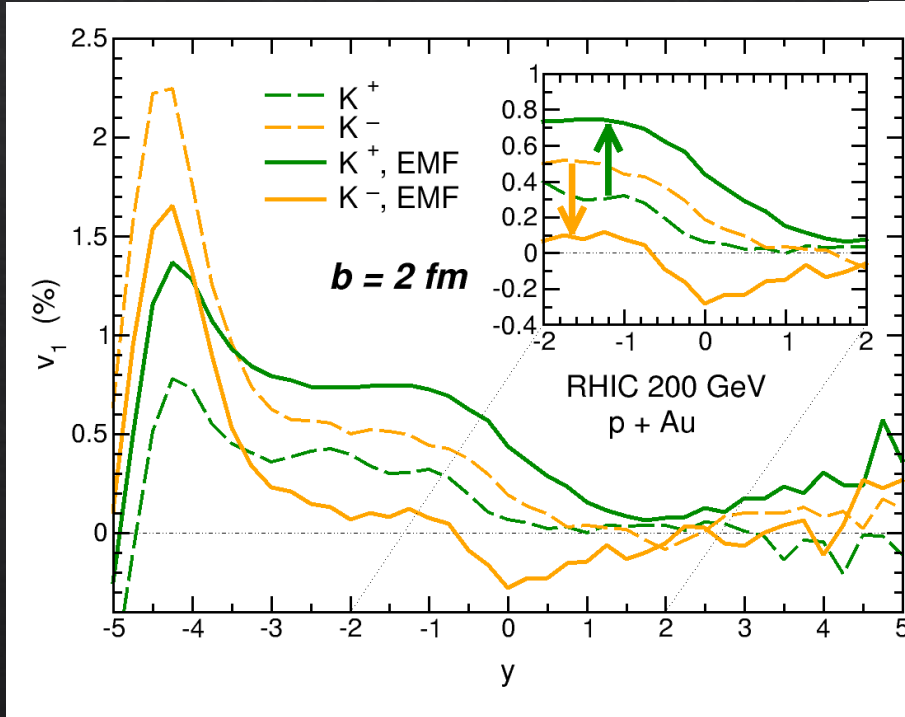


LO, Moreau, Voronyuk and Bratkovskaya, 1909.06770

p+Au: directed flow

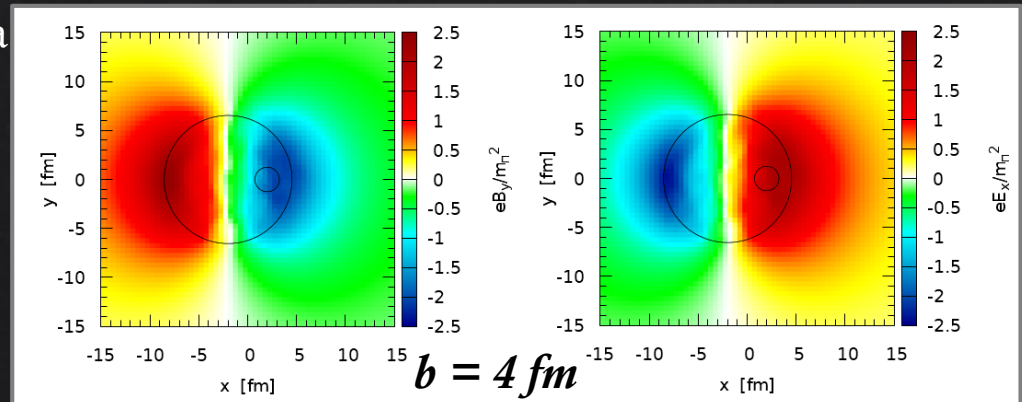
rapidity dependence of the
DIRECTED FLOW OF KAONS

$$v_1(y) = \langle \cos[\varphi(y)] \rangle$$



LO, Moreau, Voronyuk and Bratkovskaya

**Splitting of K^+ and K^-
induced by the
electromagnetic field**



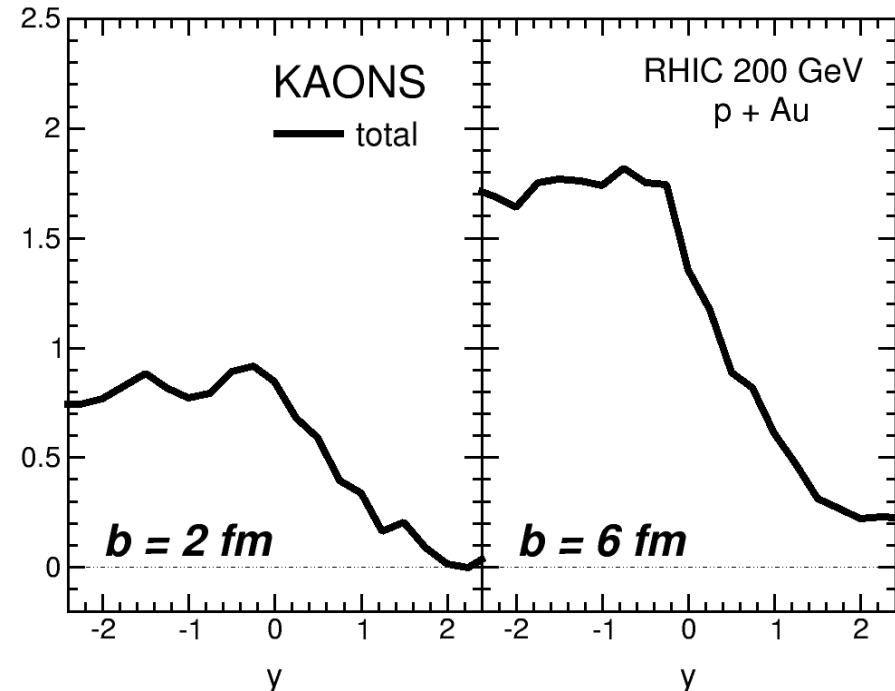
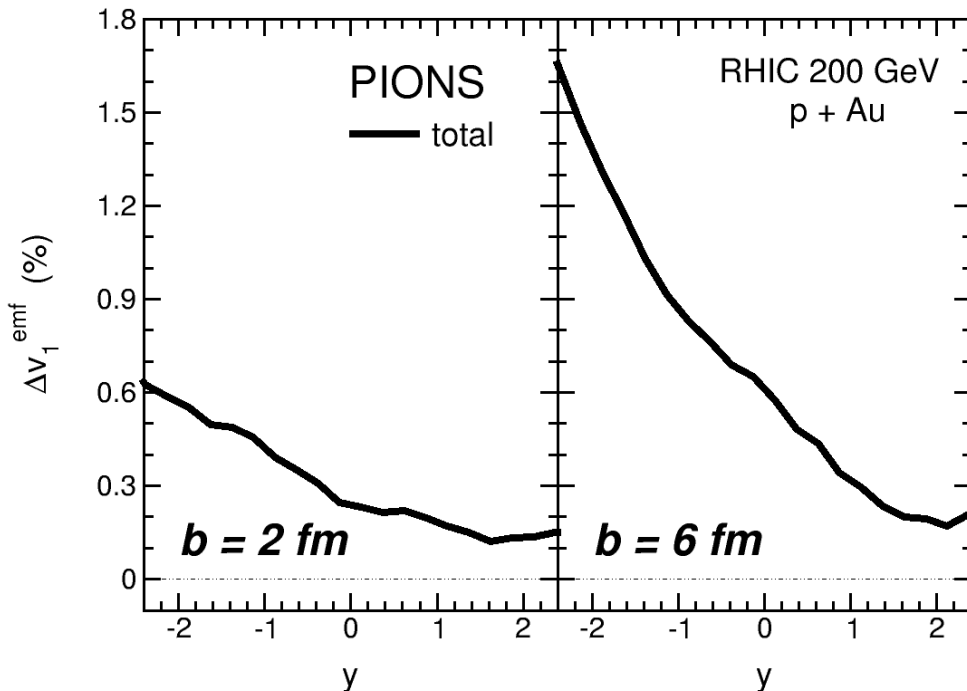
p+Au: directed flow

ELECTROMAGNETICALLY-INDUCED SPLITTING in the directed flow of hadrons with same mass and opposite charge

$$\Delta v_1^{emf} \equiv \Delta v_1^{(PHSD+EMF)} - \Delta v_1^{(PHSD)}$$

$$\Delta v_1 \equiv v_1^+ - v_1^-$$

LO, Moreau, Voronyuk and Bratkovskaya, 1909.06770



- magnitude increasing with impact parameter
- larger splitting for kaons than for pions

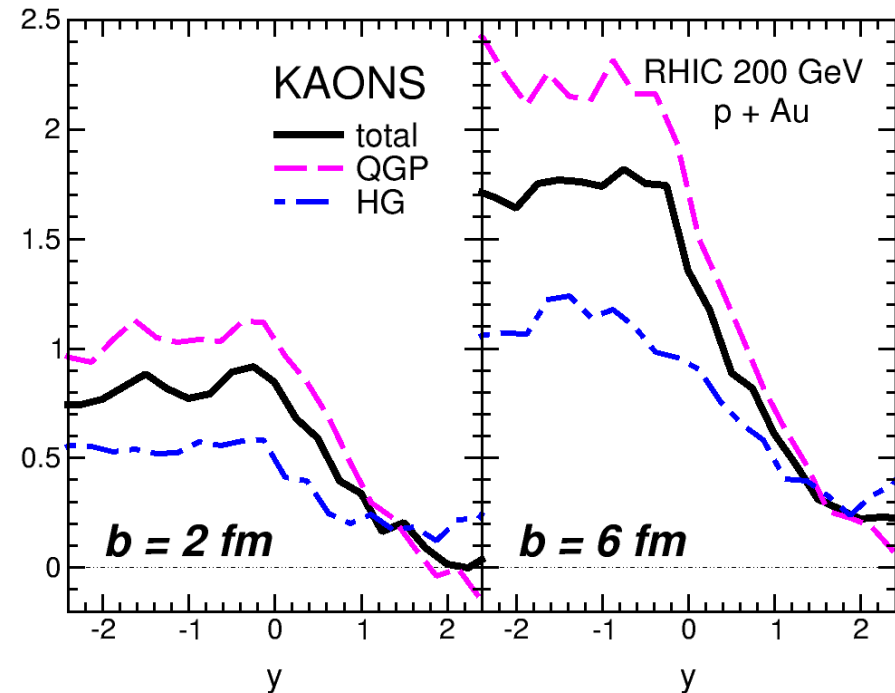
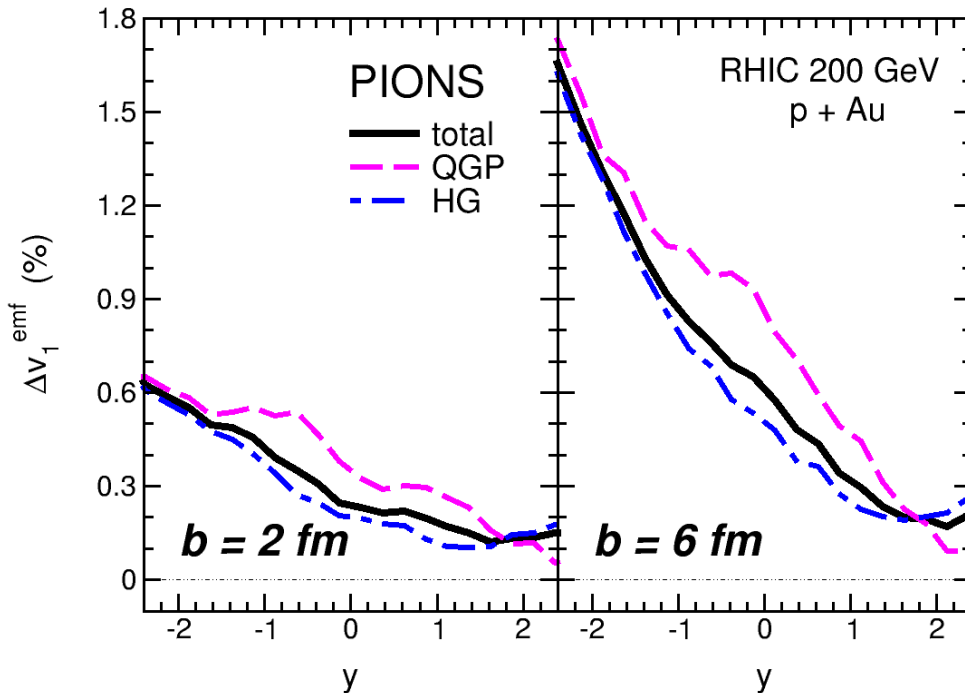
p+Au: directed flow

ELECTROMAGNETICALLY-INDUCED SPLITTING in the directed flow of hadrons with same mass and opposite charge

$$\Delta v_1^{emf} \equiv \Delta v_1^{(PHSD+EMF)} - \Delta v_1^{(PHSD)}$$

$$\Delta v_1 \equiv v_1^+ - v_1^-$$

LO, Moreau, Voronyuk and Bratkovskaya, 1909.06770



➤ **splitting generated at partonic level higher than that induced in the hadronic phase, especially for kaons**

CONCLUDING....

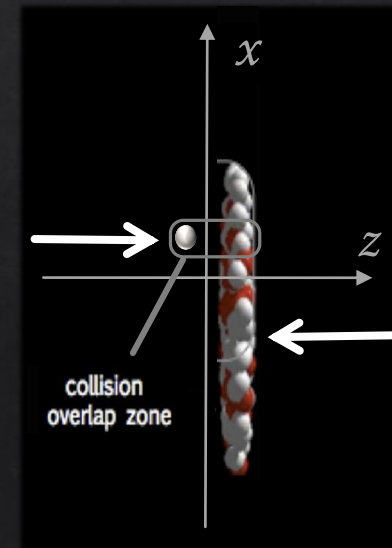


The Parton-Hadron-String-Dynamics (PHSD) approach describes the entire dynamical evolution of large and small colliding systems within one single theoretical framework

PHSD includes in a consistent way the intense electromagnetic fields produced in the very early stage of the collision

Study of p+Au collisions at top RHIC energy:

- ✓ **the electric field is strongly asymmetric inside the overlap region**
- ✓ asymmetry of charged-particle rapidity distributions increasing with centrality
- ✓ collectivity as signal of quark-gluon plasma formation
- ✓ **effect of electromagnetic fields in directed flow of mesons: splitting between positively and negatively charged particle**
- ✓ **electromagnetically-induced splitting generated in the deconfined phase larger than that produced in the hadronic phase**

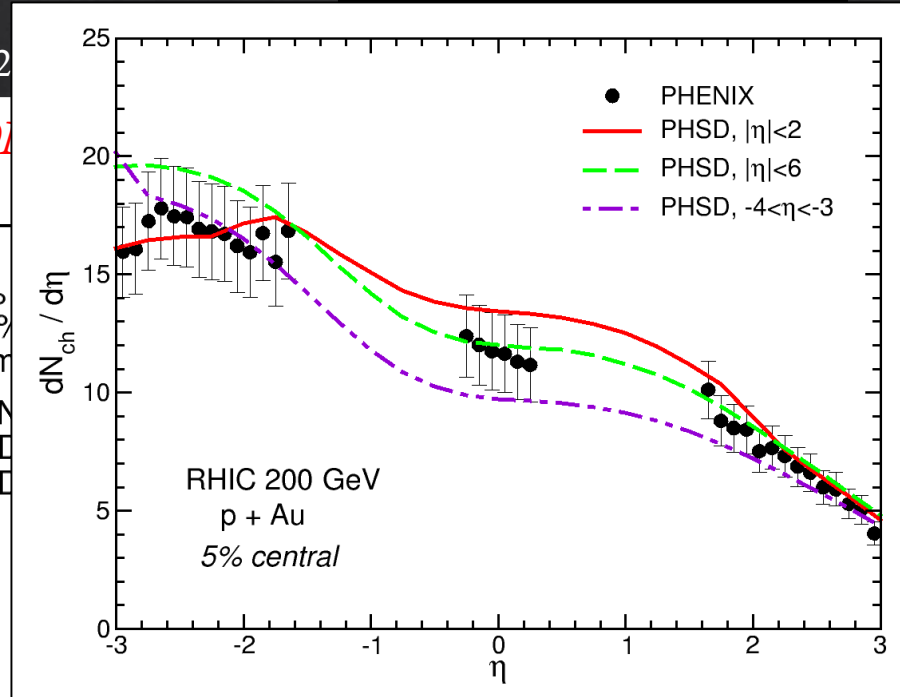
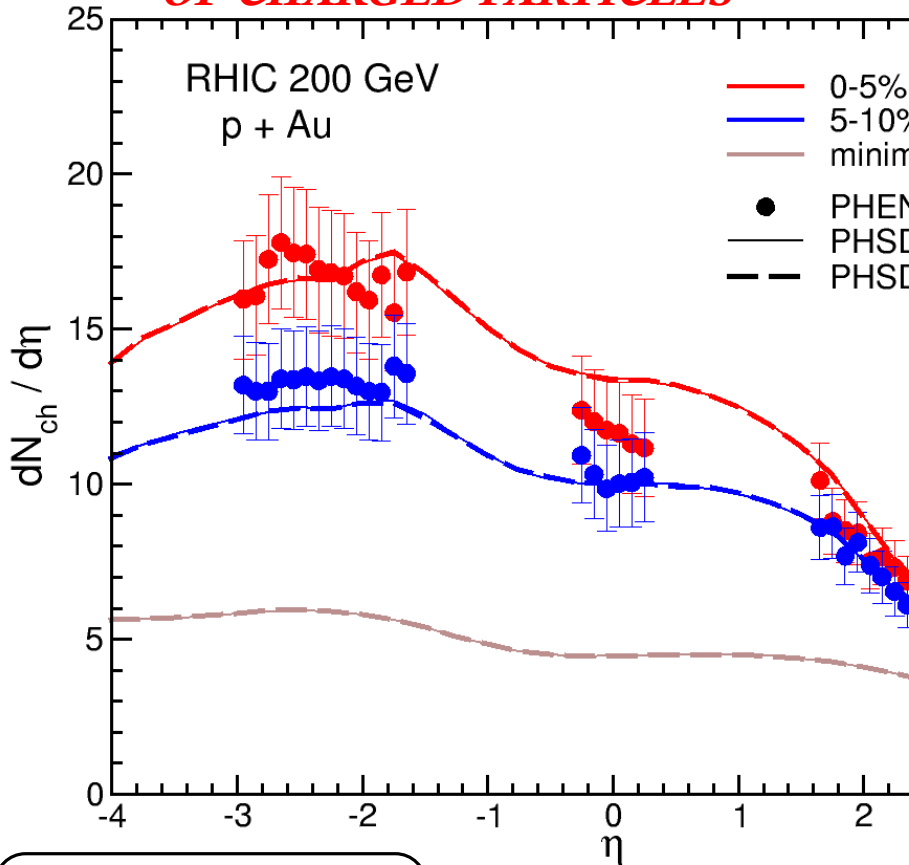


*Thank you
for your attention!*

p+Au collisions @ RHIC 200 GeV

Exp. Data: PHENIX Collaboration, PRL 121 (2018) 222

PSEUDORAPIDITY DISTRIBUTION OF CHARGED PARTICLES



$$\eta = -\ln\left(\tan\frac{\theta}{2}\right)$$

- enhanced particle production in the Au-going directions
- asymmetry increases with centrality of the collision