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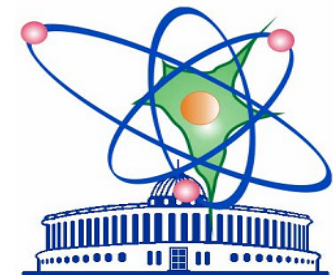
# The properties of parton-hadron matter from heavy-ion collisions

**Elena Bratkovskaya**

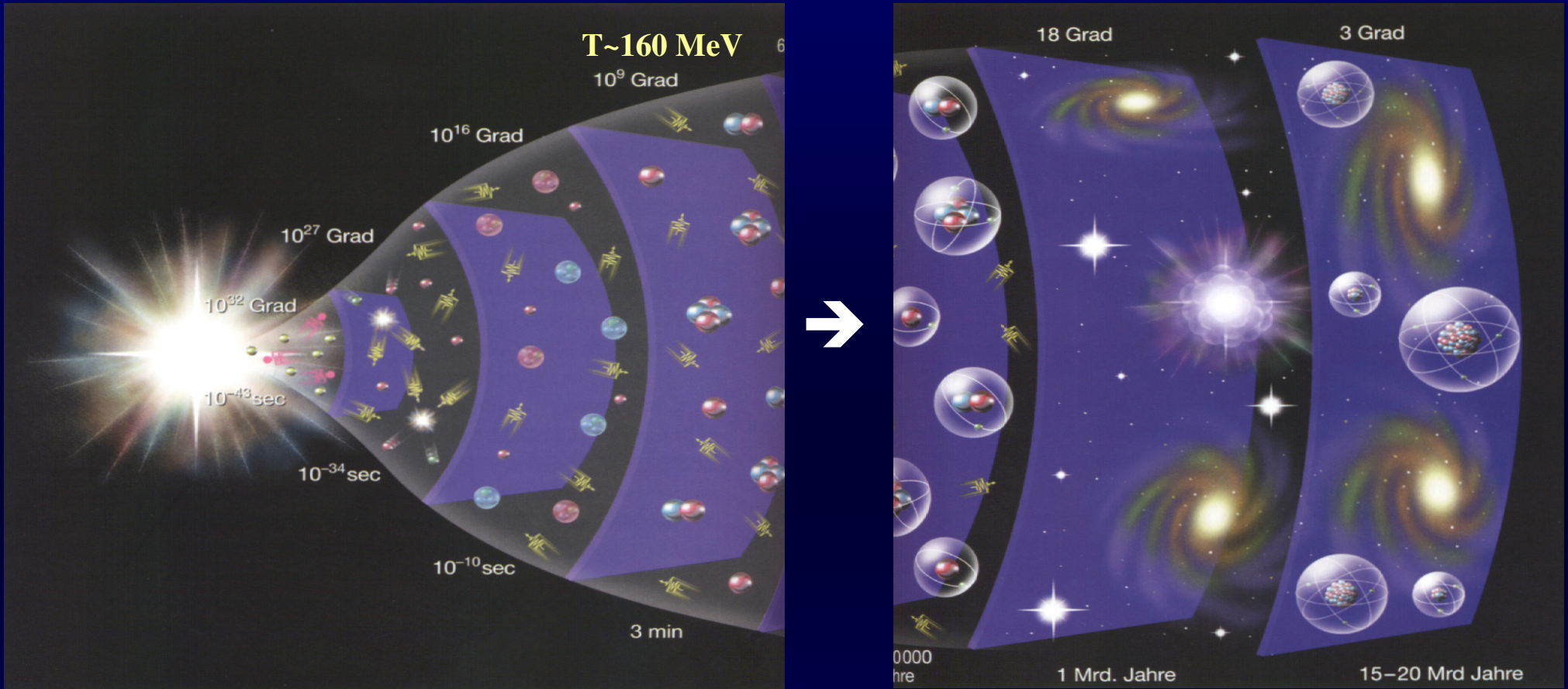
**Institut für Theoretische Physik & FIAS, Uni. Frankfurt**



BLTP, 7 August, 2013



# From Big Bang to Formation of the Universe



*time*

$10^{-3}$  sec  
quarks  
gluons  
photons

3 min  
nucleons  
deuterons  
 $\alpha$ -particles

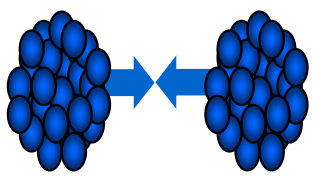
300000 years  
atoms

15 Mrd years  
our Universe



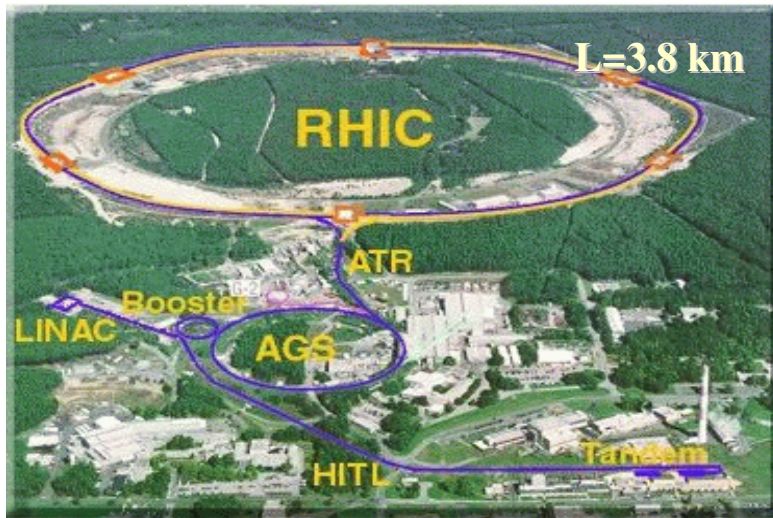
Can we go back in time ?



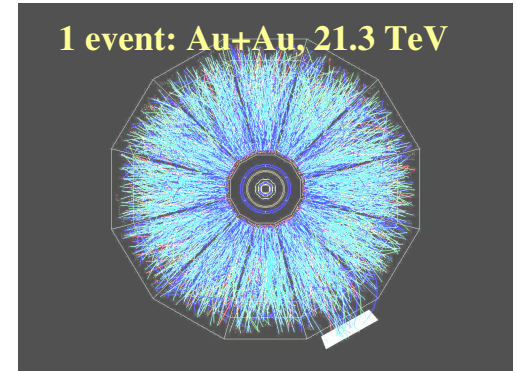
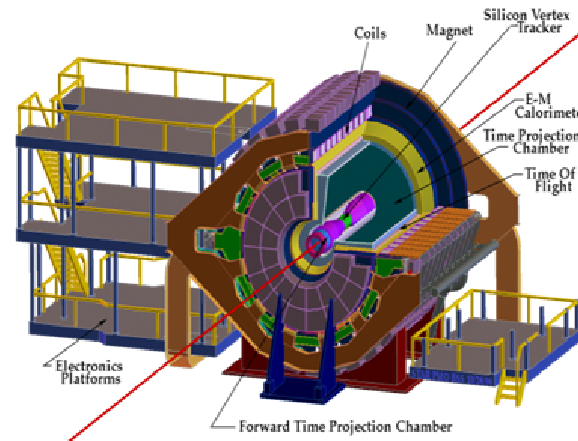


# Heavy-ion accelerators

- **Relativistic-Heavy-Ion-Collider – RHIC - (Brookhaven): Au+Au at 21.3 A TeV**

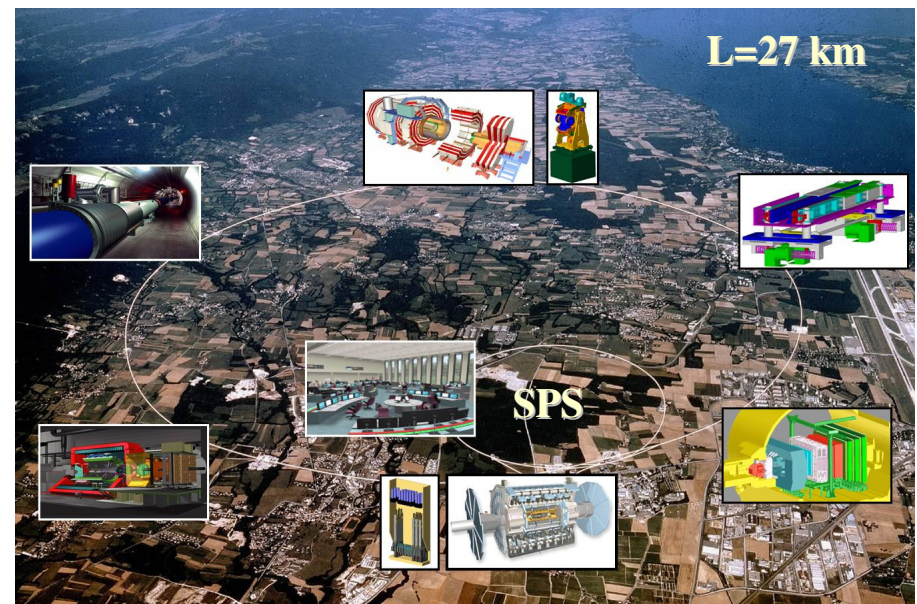
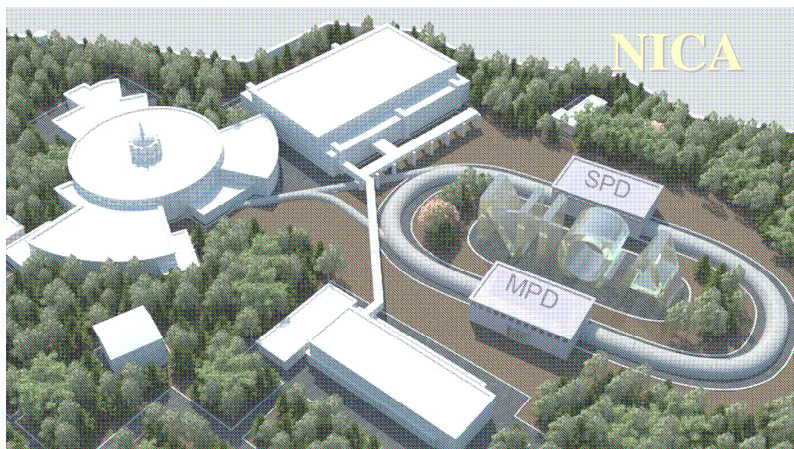


## STAR detector at RHIC



- **Large Hadron Collider - LHC - (CERN): Pb+Pb at 574 A TeV**

- **Future facilities: FAIR (GSI), NICA (Dubna)**

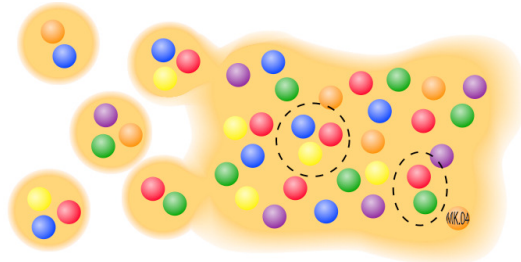


# The QGP in Lattice QCD

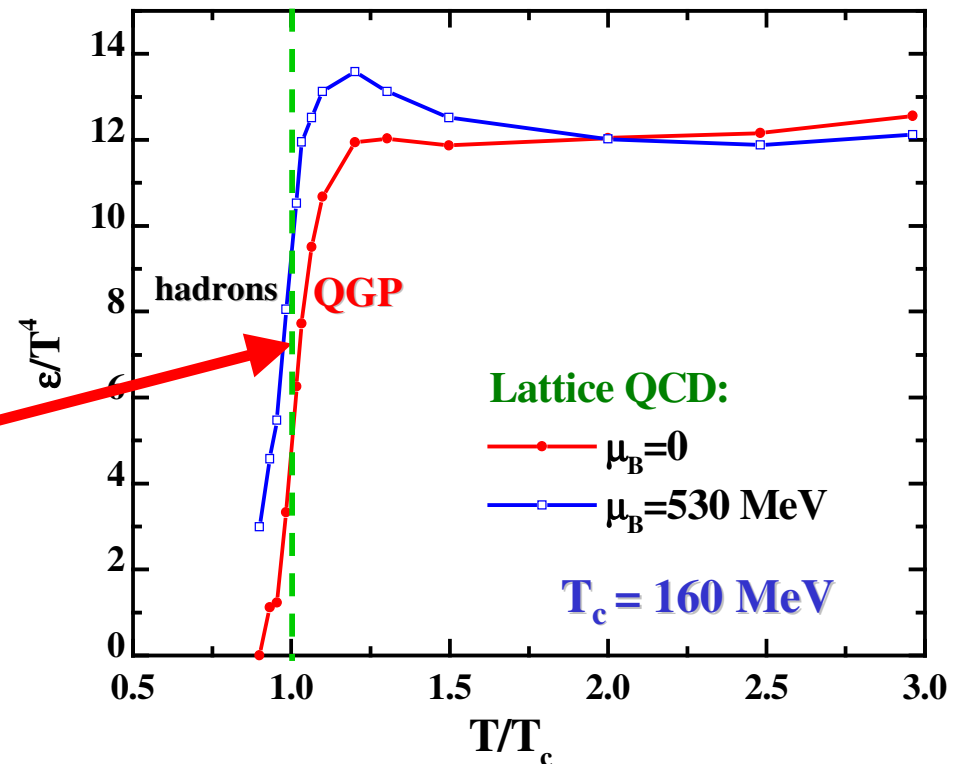
## Quantum Chromo Dynamics :

predicts strong increase of the **energy density  $\epsilon$**  at a critical temperature  **$T_C \sim 160$  MeV**

$\Rightarrow$  Possible **phase transition** from hadronic to **partonic matter** (quarks, gluons) at critical energy density  **$\epsilon_C \sim 0.5$  GeV/fm<sup>3</sup>**



## Lattice QCD: energy density versus temperature



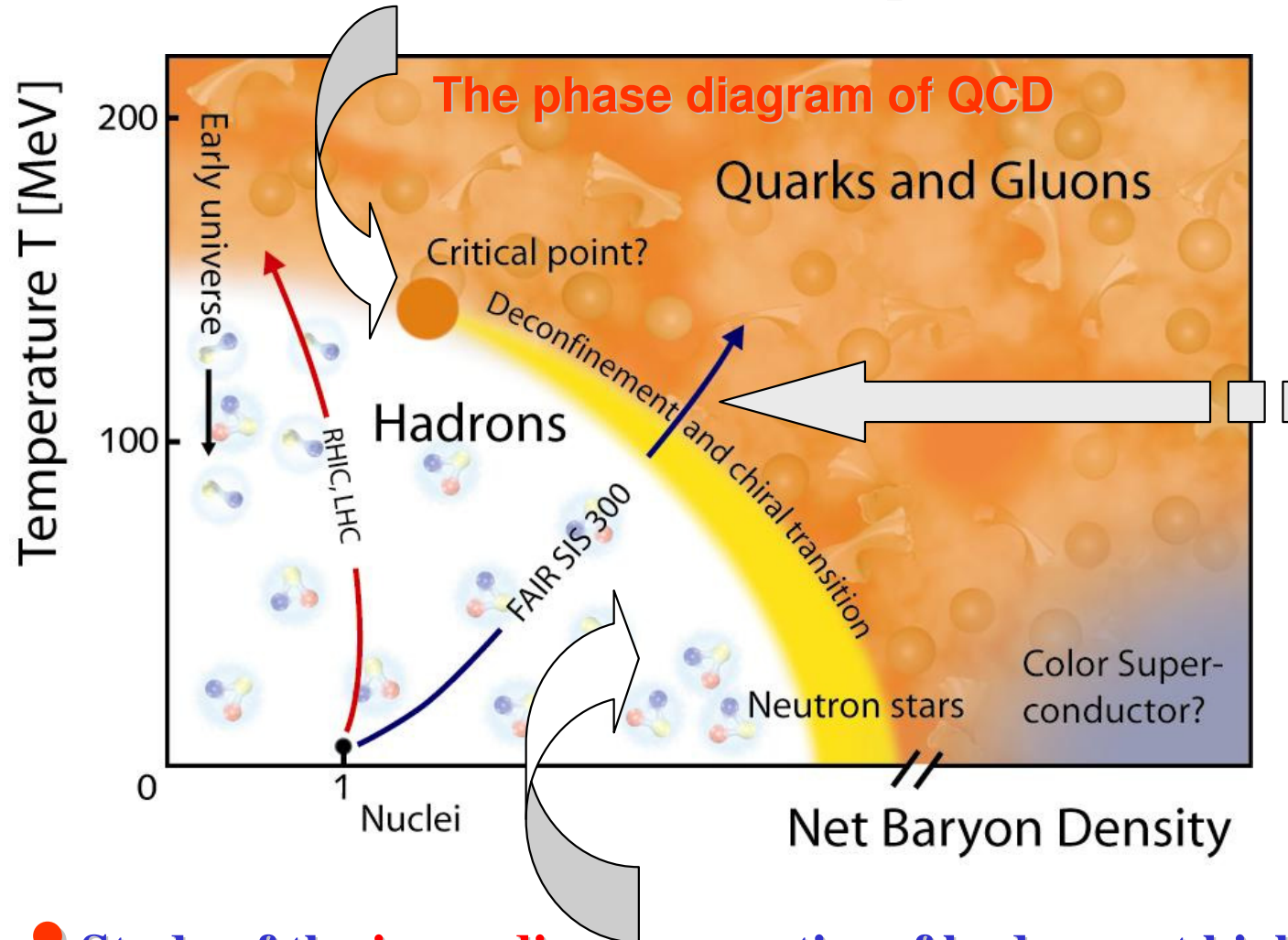
Z. Fodor et al., PLB 568 (2003) 73

**Critical conditions -  $\epsilon_C \sim 0.5$  GeV/fm<sup>3</sup>,  $T_C \sim 160$  MeV - can be reached in heavy-ion experiments at bombarding energies  $> 5$  GeV/A**



# The holy grail of heavy-ion physics:

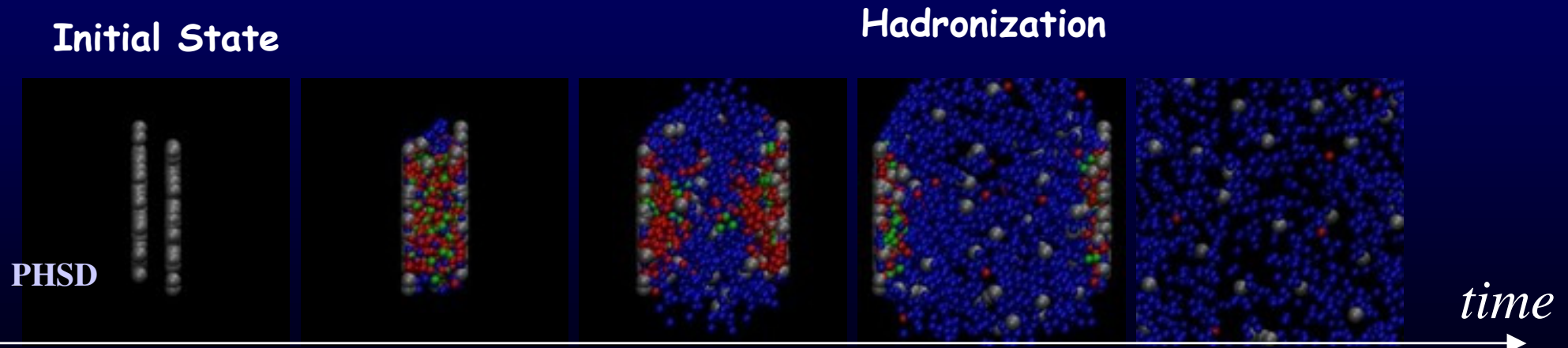
- Search for the **critical point**



- Study of the **phase transition** from hadronic to partonic matter – **Quark-Gluon-Plasma**

- Study of the **in-medium** properties of hadrons at high baryon density and temperature

# „Little Bangs‘ in the Laboratory



Au+Au

Quark-Gluon-Plasma ?

hadron  
degrees  
of freedom



quarks and gluons



hadron  
degrees  
of freedom

How can we prove that an equilibrium QGP has been created in central heavy-ion collisions ?!

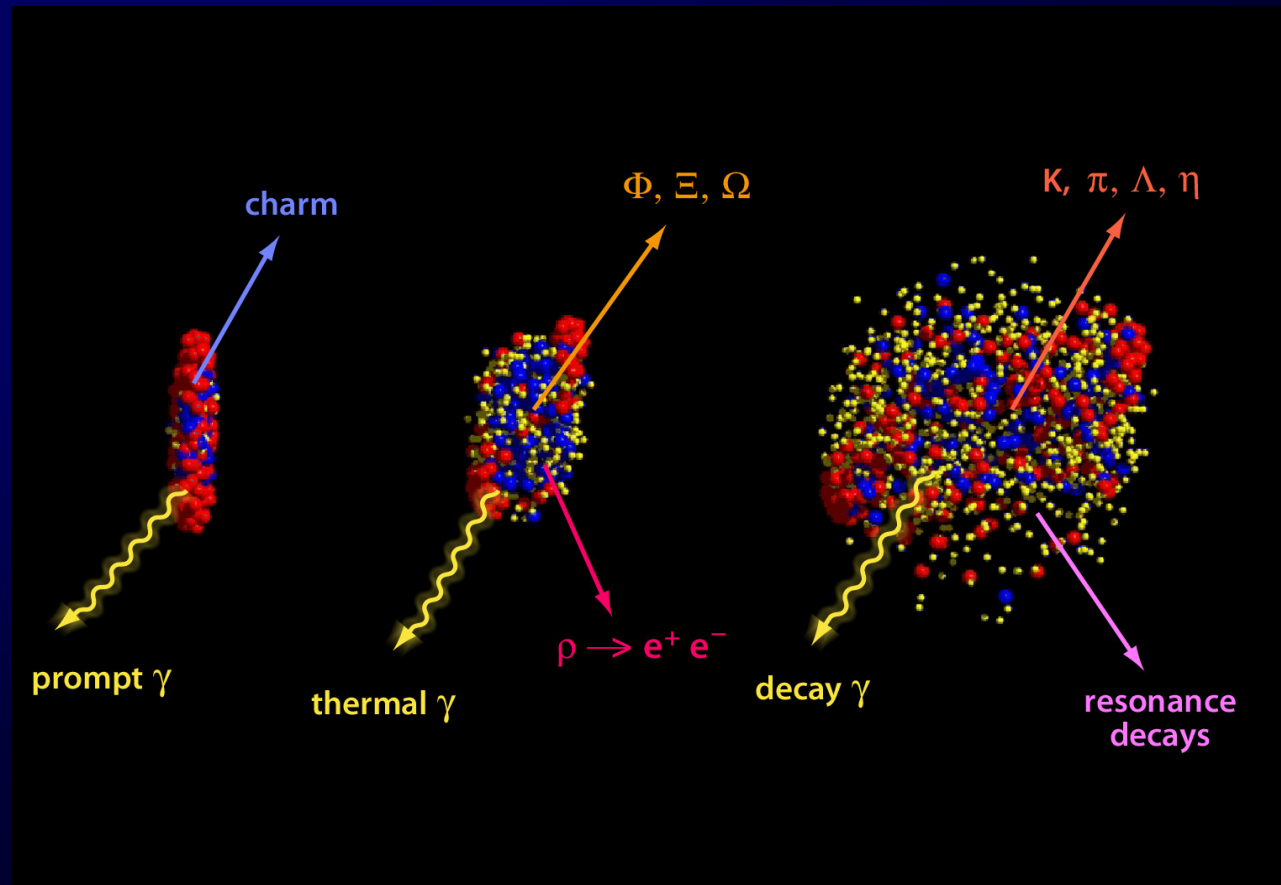
## Signals of the phase transition:

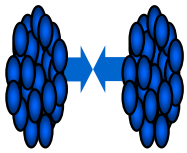
- Multi-strange particle enhancement in A+A
- Charm suppression
- Collective flow ( $v_1, v_2$ )
- Thermal dileptons
- Jet quenching and angular correlations
- High  $p_T$  suppression of hadrons
- Nonstatistical event by event fluctuations and correlations
- ...

**Experiment:** measures final hadrons and leptons

How to learn about physics from data?

Compare with theory!





# Basic models for heavy-ion collisions

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- **Statistical models:**

basic assumption: system is described by a (grand) canonical ensemble of non-interacting fermions and bosons in **thermal and chemical equilibrium**

[ -: no dynamics]

- **Ideal hydrodynamical models:**

basic assumption: conservation laws + equation of state; assumption of local thermal and chemical equilibrium

[ -: - simplified dynamics]

- **Transport models:**

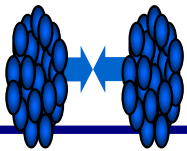
based on transport theory of relativistic quantum many-body systems -

Actual solutions: Monte Carlo simulations

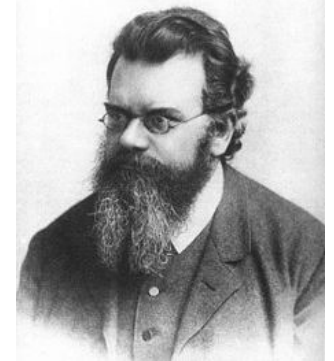
[+: full dynamics | -: very complicated]

→ Microscopic transport models provide a unique **dynamical** description of **nonequilibrium** effects in heavy-ion collisions





# Semi-classical BUU equation



Ludwig Boltzmann

**Boltzmann -Uehling-Uhlenbeck equation** (non-relativistic formulation)

- propagation of particles in the **self-generated Hartree-Fock mean-field potential**  $U(\vec{r},t)$  with an on-shell **collision term**:

$$\frac{\partial}{\partial t} f(\vec{r}, \vec{p}, t) + \frac{\vec{p}}{m} \vec{\nabla}_{\vec{r}} f(\vec{r}, \vec{p}, t) - \vec{\nabla}_{\vec{r}} U(\vec{r}, t) \vec{\nabla}_{\vec{p}} f(\vec{r}, \vec{p}, t) = \left( \frac{\partial f}{\partial t} \right)_{coll}$$

**collision term:**  
elastic and  
inelastic reactions

$f(\vec{r}, \vec{p}, t)$  is the **single particle phase-space distribution function**

- probability to find the particle at position  $r$  with momentum  $p$  at time  $t$

□ self-generated **Hartree-Fock mean-field potential**:

$$U(\vec{r}, t) = \frac{1}{(2\pi\hbar)^3} \sum_{\beta_{occ}} \int d^3 r' d^3 p V(\vec{r} - \vec{r}', t) f(\vec{r}', \vec{p}, t) + (Fock \text{ term})$$

□ **Collision term** for  $1+2 \rightarrow 3+4$  (let's consider fermions) :

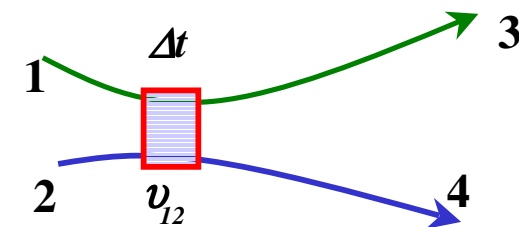
$$I_{coll} = \frac{4}{(2\pi)^3} \int d^3 p_2 d^3 p_3 \int d\Omega |v_{12}| \delta^3(\vec{p}_1 + \vec{p}_2 - \vec{p}_3 - \vec{p}_4) \cdot \frac{d\sigma}{d\Omega}(1+2 \rightarrow 3+4) \cdot P$$

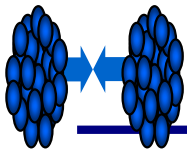
Probability including **Pauli blocking of fermions**:

$$P = \underline{f_3 f_4 (1 - f_1)(1 - f_2)} - \underline{f_1 f_2 (1 - f_3)(1 - f_4)}$$

**Gain term:  $3+4 \rightarrow 1+2$**

**Loss term:  $1+2 \rightarrow 3+4$**





# Dynamical description of strongly interacting systems

□ Semi-classical BUU → solution for weakly interacting systems of particles

How to describe **strongly interacting systems?!**

□ Quantum field theory →

**Kadanoff-Baym dynamics** for resummed(!) single-particle Green functions  $S^<$

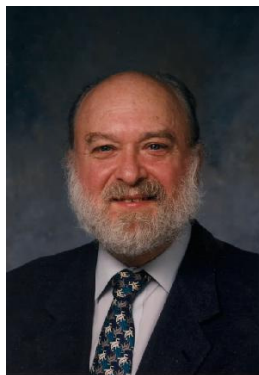
$$\hat{S}_{0x}^{-1} S_{xy}^< = \sum_{xz}^{ret} \odot S_{zy}^< + \sum_{xz}^< \odot S_{zy}^{adv} \quad (1962)$$

Green functions  $S^</math>/self-energies  $\Sigma$ :$

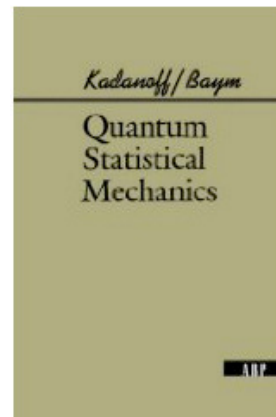
Integration over the intermediate spacetime

$$\left\{ \begin{aligned} iS_{xy}^< &= \eta \langle \{ \Phi^+(y) \Phi(x) \} \rangle \\ iS_{xy}^> &= \langle \{ \Phi(y) \Phi^+(x) \} \rangle \\ iS_{xy}^c &= \langle T^c \{ \Phi(x) \Phi^+(y) \} \rangle - \text{causal} \\ iS_{xy}^a &= \langle T^a \{ \Phi(x) \Phi^+(y) \} \rangle - \text{anticausal} \end{aligned} \right.$$

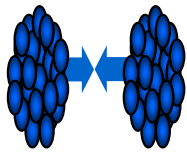
$$\begin{aligned} S_{xy}^{ret} &= S_{xy}^c - S_{xy}^< = S_{xy}^> - S_{xy}^a - \text{retarded} & \hat{S}_{0x}^{-1} &\equiv -(\partial_x^\mu \partial_\mu^x + M_0^2) \\ S_{xy}^{adv} &= S_{xy}^c - S_{xy}^> = S_{xy}^< - S_{xy}^a - \text{advanced} \\ \eta &= \pm 1 (\text{bosons / fermions}) \\ T^a (T^c) &- (\text{anti-})\text{time - ordering operator} \end{aligned}$$



Leo Kadanoff



Gordon Baym



# From Kadanoff-Baym equations to generalized transport equations

After the **first order gradient expansion of the Wigner transformed Kadanoff-Baym equations** and separation into the real and imaginary parts one gets:

## Generalized transport equations (GTE):

$$\underbrace{\diamond \{ P^2 - M_0^2 - \text{Re} \Sigma_{XP}^{\text{ret}} \}}_{\text{drift term}} \underbrace{\{ S_{XP}^< \}}_{\text{Vlasov term}} - \underbrace{\diamond \{ \Sigma_{XP}^< \} \{ \text{Re} S_{XP}^{\text{ret}} \}}_{\text{backflow term}} = \frac{i}{2} \left[ \underbrace{\Sigma_{XP}^> S_{XP}^<}_{\text{collision term = 'loss' term}} - \underbrace{\Sigma_{XP}^< S_{XP}^>}_{\text{'gain' term}} \right]$$

**Backflow term** incorporates the **off-shell** behavior in the particle propagation  
**! vanishes in the quasiparticle limit**  $A_{XP} \rightarrow \delta(p^2 - M^2)$

□ GTE: Propagation of the Green's function  $iS_{XP}^< = A_{XP} N_{XP}$ , which carries information not only on the **number of particles** ( $N_{XP}$ ), but also on their **properties**, interactions and correlations (via  $A_{XP}$ )

**Spectral function:** 
$$A_{XP} = \frac{\Gamma_{XP}}{(P^2 - M_0^2 - \text{Re} \Sigma_{XP}^{\text{ret}})^2 + \Gamma_{XP}^2/4}$$

$\Gamma_{XP} = -\text{Im} \Sigma_{XP}^{\text{ret}}$  – **width of spectral function**

= **reaction rate** of particle (at phase-space position  $XP$ )

4-dimensional generalization of the Poisson-bracket:

$$\diamond \{ F_1 \} \{ F_2 \} := \frac{1}{2} \left( \frac{\partial F_1}{\partial X_\mu} \frac{\partial F_2}{\partial P^\mu} - \frac{\partial F_1}{\partial P_\mu} \frac{\partial F_2}{\partial X^\mu} \right)$$





# The baseline concepts of HSD

## HSD – Hadron-String-Dynamics transport approach:

→ solution of the **generalized off-shell transport equations** for the phase-space density  $f_i(r,p,t)$  with **collision terms**  $I_{coll}$  describing:

### Low energy collisions:

- binary  $2 \leftrightarrow 2$  and  $2 \leftrightarrow 3$  reactions
- $1 \leftrightarrow 2$  : formation and decay of baryonic and mesonic **resonances**

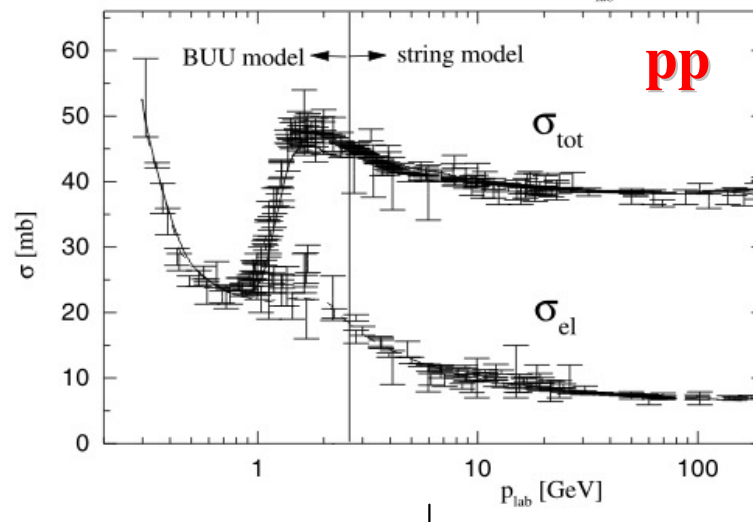
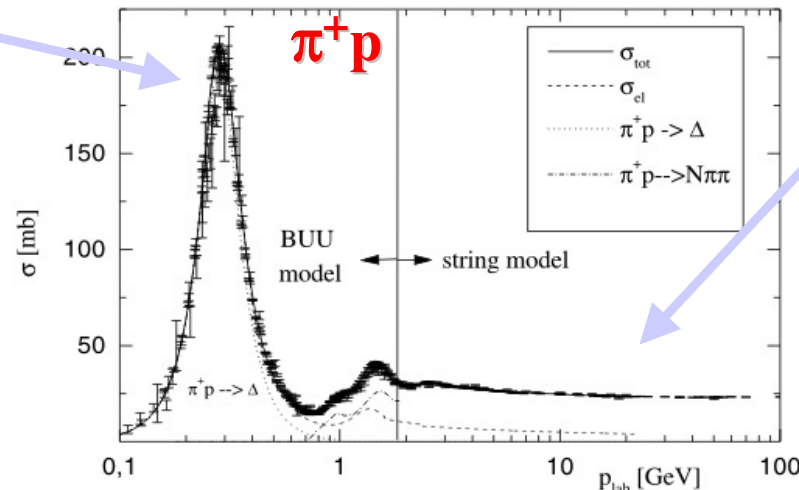
$BB \leftrightarrow B'B'$   
 $BB \leftrightarrow B'B'm$   
 $mB \leftrightarrow m'B'$   
 $mB \leftrightarrow B'$   
 $mm \leftrightarrow m'm'$   
 $mm \leftrightarrow m'$  ...

### Baryons:

$B = p, n, \Delta(1232),$   
 $N(1440), N(1535), \dots$

### Mesons:

$M = \pi, \eta, \rho, \omega, \phi, \dots$



### High energy collisions: (above $s^{1/2} \sim 2.5$ GeV)

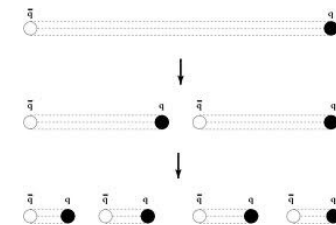
#### Inclusive particle production:

$BB \rightarrow X, mB \rightarrow X$

$X = \text{many particles}$

described by

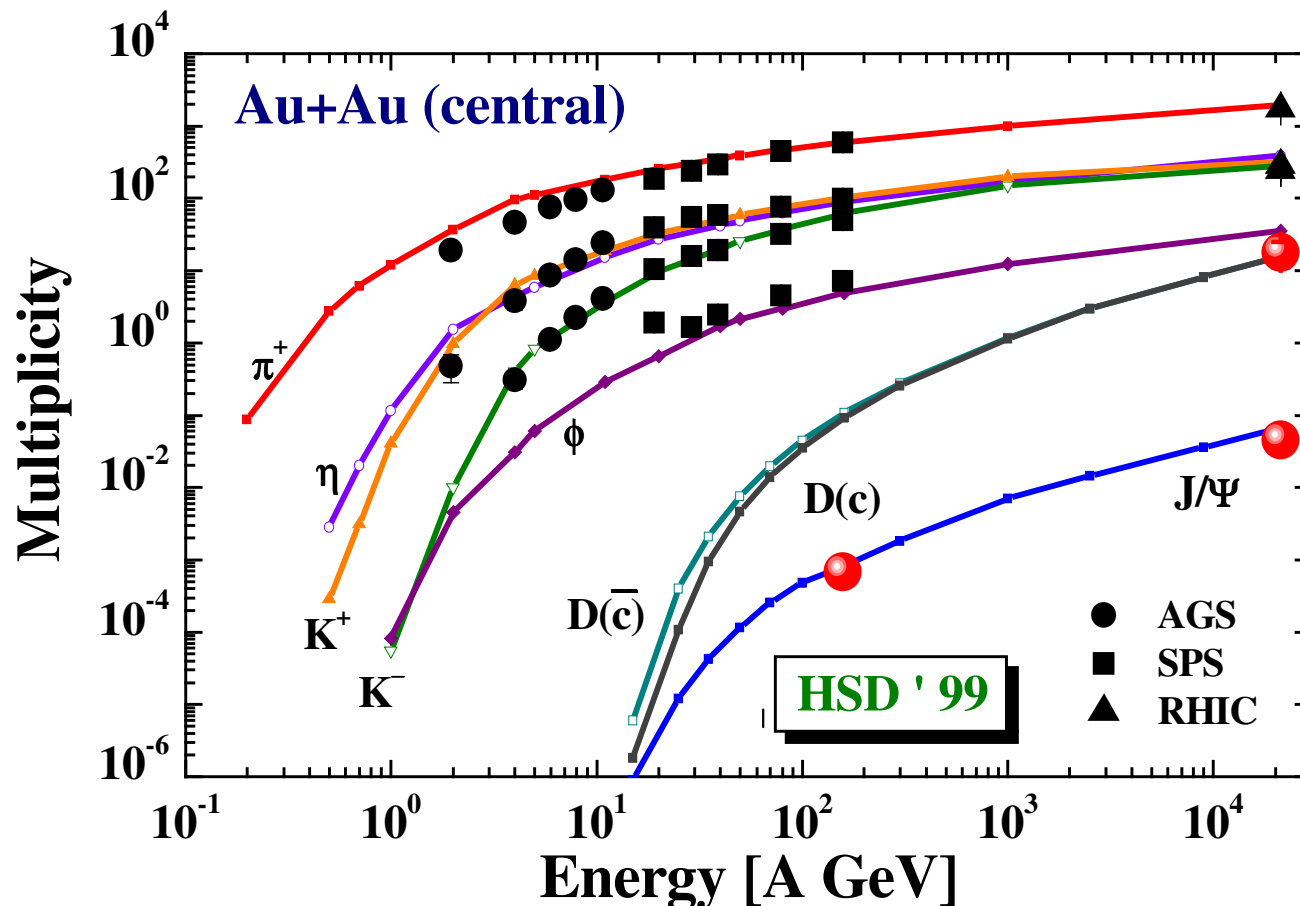
**strings** (= excited color singlet states  $q-qq, q-qbar$ )  
**formation and decay**





# HSD – a microscopic off-shell transport model for heavy-ion reactions

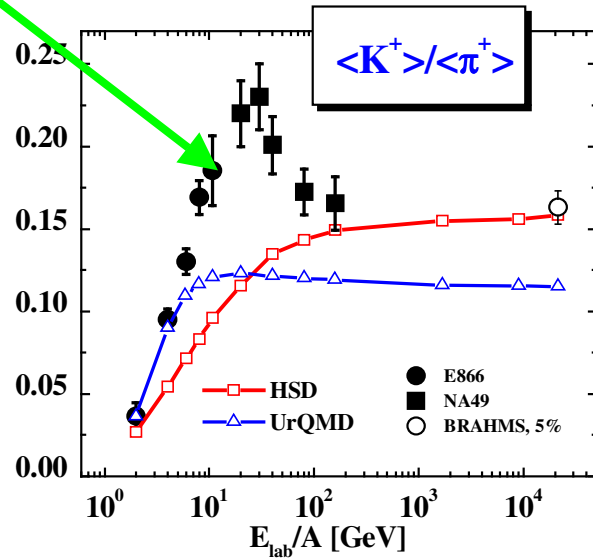
- very good description of particle production in **pp, pA,  $\pi$ A, AA reactions**
- unique description of nuclear dynamics from **low (~100 MeV) to ultrarelativistic (>20 TeV) energies**



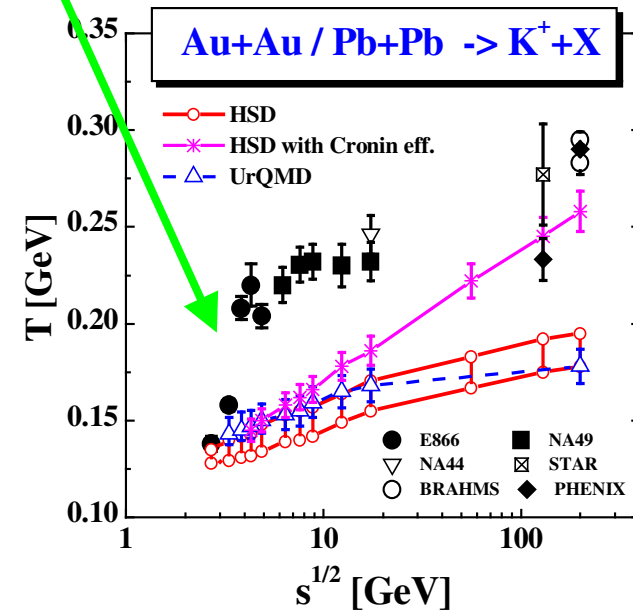
# Hadron-string transport models (HSD, UrQMD)

## versus observables

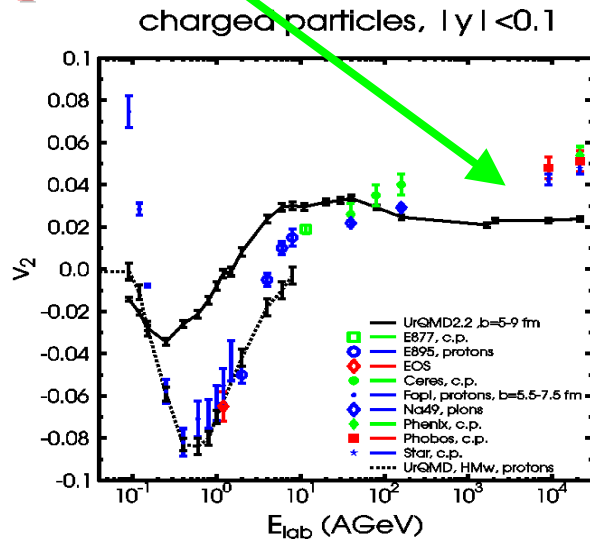
□ ,horn' in  $K^+/\pi^+$



□ ,step' in slope T



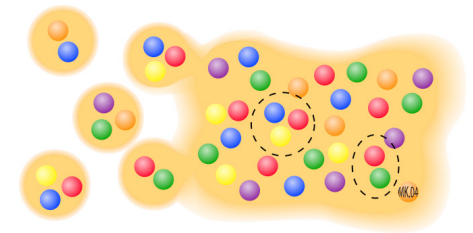
□ elliptic flow



Exp. data are not reproduced in terms of the hadron-string picture  
 => evidence for **partonic degrees of freedom**



# Goal: microscopic transport description of the **partonic** and **hadronic** phase



## Problems:

- ❑ How to model a **QGP phase** in line with IQCD data?
- ❑ How to solve the **hadronization problem**?

## Ways to go:

### pQCD based models:

- QGP phase: pQCD cascade
  - hadronization: quark coalescence
- AMPT, HIJING, BAMPS

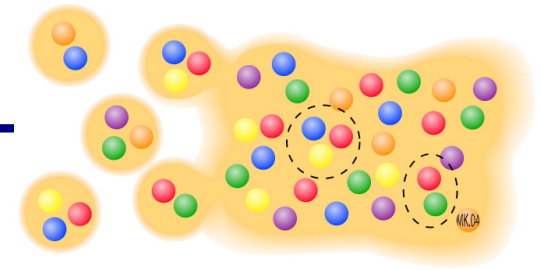
### ‘Hybrid’ models:

- QGP phase: **hydro** with QGP EoS
  - hadronic freeze-out: after burner  
- hadron-string transport model
- Hybrid-UrQMD

- **microscopic** transport description of the **partonic** and **hadronic phase** in terms of strongly interacting dynamical **quasi-particles** and off-shell hadrons

→ PHSD

# From hadrons to partons



In order to study the **phase transition** from hadronic to partonic matter – **Quark-Gluon-Plasma** – we **need a consistent non-equilibrium (transport) model with**

- **explicit parton-parton interactions** (i.e. between quarks and gluons) beyond strings!

- **explicit phase transition** from hadronic to partonic degrees of freedom

- **IQCD EoS** for partonic phase

**Transport theory:** off-shell Kadanoff-Baym equations for the Green-functions  $S_h^<(x,p)$  in phase-space representation for the **partonic and hadronic phase**



**Parton-Hadron-String-Dynamics (PHSD)**

**QGP phase** described by

**Dynamical QuasiParticle Model (DQPM)**

W. Cassing, E. Bratkovskaya, PRC 78 (2008) 034919;  
NPA831 (2009) 215;  
W. Cassing, EPJ ST 168 (2009) 3

A. Peshier, W. Cassing, PRL 94 (2005) 172301;  
Cassing, NPA 791 (2007) 365; NPA 793 (2007)

# Dynamical QuasiParticle Model (DQPM) - Basic ideas:

DQPM describes QCD properties in terms of ,resummed' single-particle Green's functions – in the sense of a two-particle irreducible (2PI) approach:

Gluon propagator:  $\Delta^{-1} = P^2 - \Pi$

gluon self-energy:  $\Pi = M_g^2 - i2\Gamma_g \omega$

Quark propagator:  $S_q^{-1} = P^2 - \Sigma_q$

quark self-energy:  $\Sigma_q = M_q^2 - i2\Gamma_q \omega$

- the resummed properties are specified by complex self-energies which depend on temperature:
  - the real part of self-energies ( $\Sigma_q, \Pi$ ) describes a dynamically generated mass ( $M_q, M_g$ );
  - the imaginary part describes the interaction width of partons ( $\Gamma_q, \Gamma_g$ )
- space-like part of energy-momentum tensor  $T_{\mu\nu}$  defines the potential energy density and the mean-field potential (1PI) for quarks and gluons
- 2PI framework guarantees a consistent description of the system in- and out-of equilibrium on the basis of Kadanoff-Baym equations



# The Dynamical QuasiParticle Model (DQPM)

**Properties** of interacting quasi-particles: massive quarks and gluons ( $g, q, q_{\text{bar}}$ ) with Lorentzian spectral functions :

$$\rho_i(\omega, T) = \frac{4\omega\Gamma_i(T)}{\left(\omega^2 - \bar{p}^2 - M_i^2(T)\right)^2 + 4\omega^2\Gamma_i^2(T)}$$

$(i = q, \bar{q}, g)$

■ Modeling of the quark/gluon masses and widths → HTL limit at high T

■ quarks:

$$\text{mass: } M_{q(\bar{q})}^2(T) = \frac{N_c^2 - 1}{8N_c} g^2 \left( T^2 + \frac{\mu_q^2}{\pi^2} \right)$$

$$\text{width: } \Gamma_{q(\bar{q})}(T) = \frac{1}{3} \frac{N_c^2 - 1}{2N_c} \frac{g^2 T}{8\pi} \ln\left(\frac{2c}{g^2} + 1\right)$$

■ gluons:

$$M_g^2(T) = \frac{g^2}{6} \left( \left( N_c + \frac{N_f}{2} \right) T^2 + \frac{N_c}{2} \sum_q \frac{\mu_q^2}{\pi^2} \right)$$

$$\Gamma_g(T) = \frac{1}{3} N_c \frac{g^2 T}{8\pi} \ln\left(\frac{2c}{g^2} + 1\right)$$

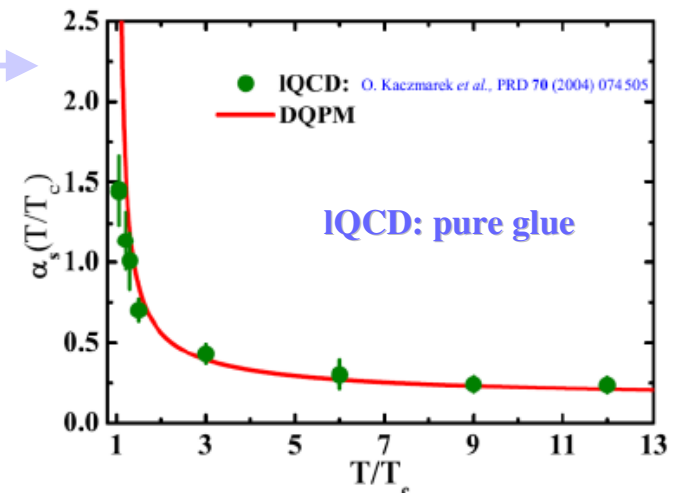
$N_c = 3, N_f = 3$

■ running coupling (pure glue):

$$\alpha_s(T) = \frac{g^2(T)}{4\pi} = \frac{12\pi}{(11N_c - 2N_f) \ln[\lambda^2(T/T_c - T_s/T_c)^2]}$$

□ fit to lattice (IQCD) results (e.g. entropy density)

with 3 parameters:  $T_s/T_c = 0.46$ ;  $c = 28.8$ ;  $\lambda = 2.42$   
(for pure glue  $N_f = 0$ )



DQPM: Peshier, Cassing, PRL 94 (2005) 172301;  
Cassing, NPA 791 (2007) 365; NPA 793 (2007)

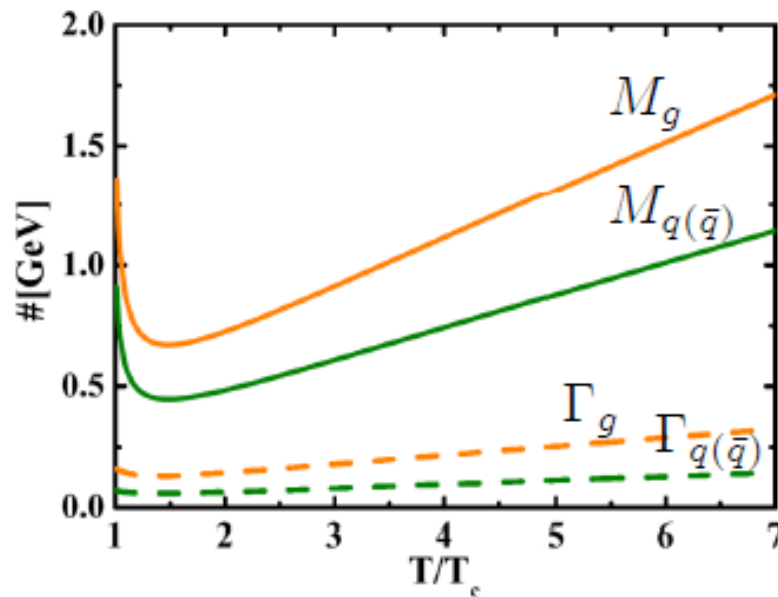
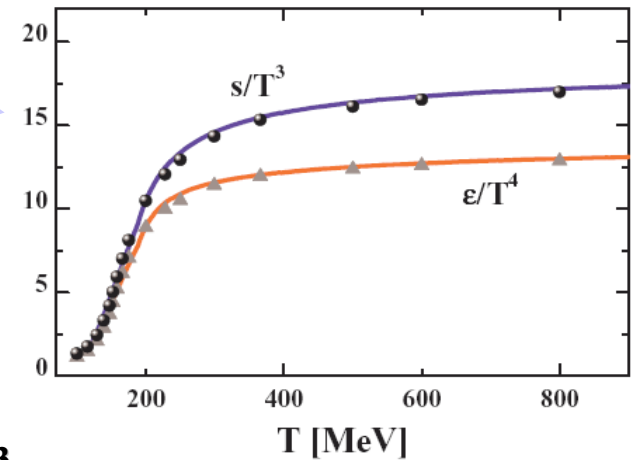
# The Dynamical QuasiParticle Model (DQPM)

➤ **fit to lattice (IQCD) results** (e.g. entropy density)

\* BMW IQCD data S. Borsanyi et al., JHEP 1009 (2010) 073

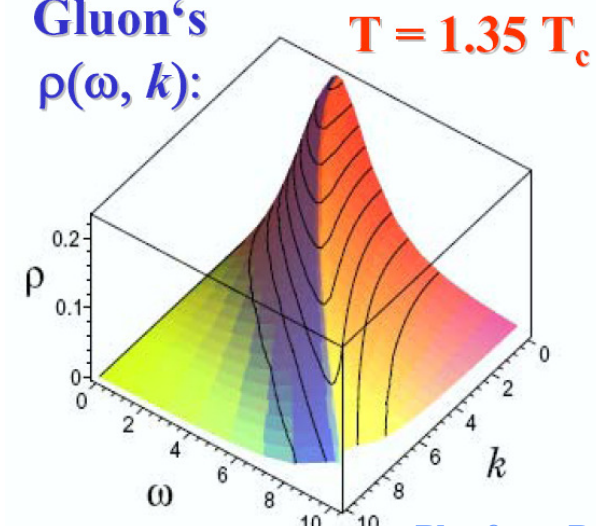
➔ **Quasiparticle properties:**

■ **large width and mass for gluons and quarks**



$T_C = 158 \text{ MeV}$   
 $\epsilon_C = 0.5 \text{ GeV/fm}^3$

Gluon's  
 $\rho(\omega, k):$



Plot from Peshier,  
 PRD 70 (2004)  
 034016

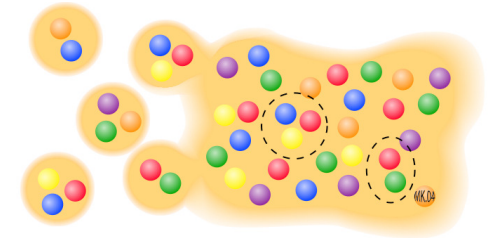
- **DQPM matches well lattice QCD**
- **DQPM provides mean-fields (1PI) for gluons and quarks as well as effective 2-body interactions (2PI)**
- **DQPM gives transition rates for the formation of hadrons → PHSD**

# I. PHSD - basic concept

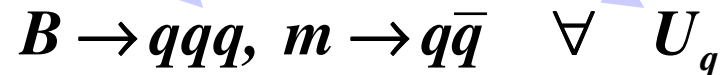
## I. From hadrons to QGP:

- **Initial A+A collisions** – as in HSD:
  - **string** formation in primary NN collisions
  - **string decay to pre-hadrons** ( $B$  - baryons,  $m$  - mesons)

- **Formation of QGP stage by dissolution of pre-hadrons**  
(all new produced secondary hadrons)  
into **massive colored quarks + mean-field energy**



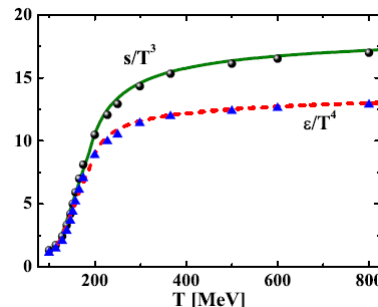
**QGP phase:**  
 $\epsilon > \epsilon_{\text{critical}}$



based on the **Dynamical Quasi-Particle Model (DQPM)** which defines  
**quark spectral functions**, i.e. masses  $M_q(\epsilon)$  and widths  $\Gamma_q(\epsilon)$

+ **mean-field potential  $U_q$**  at given  $\epsilon$  – local energy density

( $\epsilon$  related by IQCD EoS to  $T$  - temperature in the local cell)



W. Cassing, E. Bratkovskaya, PRC 78 (2008) 034919;  
NPA831 (2009) 215; EPJ ST 168 (2009) 3; NPA856 (2011) 162.





# II. PHSD - basic concept

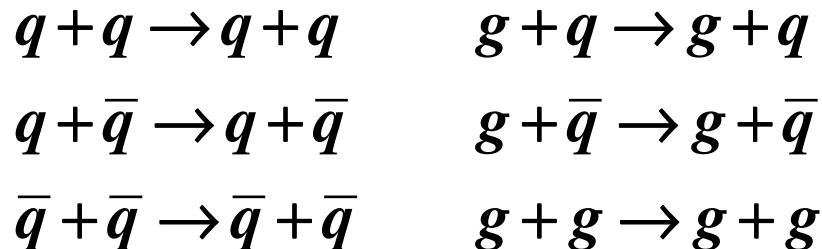
## II. Partonic phase - QGP:

quarks and gluons (= ,dynamical quasiparticles‘)

with off-shell spectral functions (width, mass) defined by the DQPM

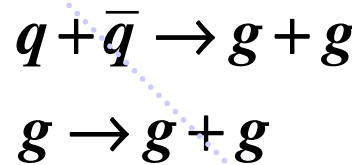
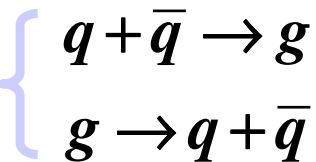
- in **self-generated mean-field potential** for quarks and gluons  $U_q, U_g$  from the DQPM
- **EoS of partonic phase: ,crossover‘** from lattice QCD (fitted by DQPM)
- **(quasi-) elastic and inelastic** parton-parton interactions: using the effective cross sections from the DQPM

- **(quasi-) elastic collisions:**

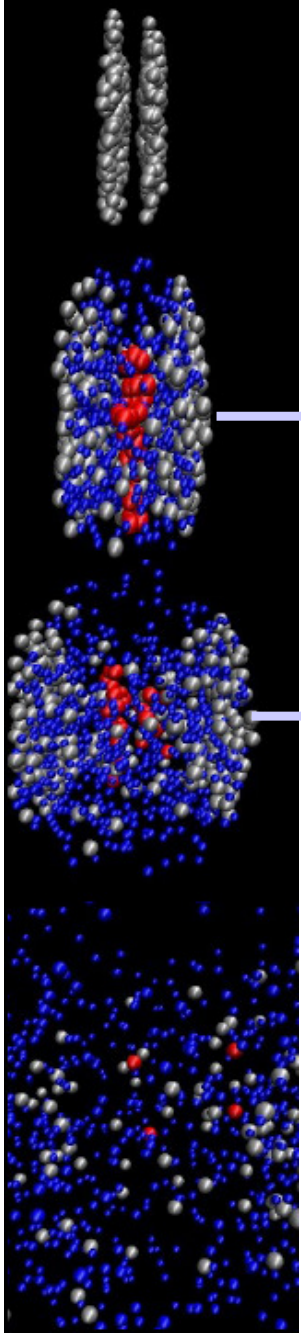
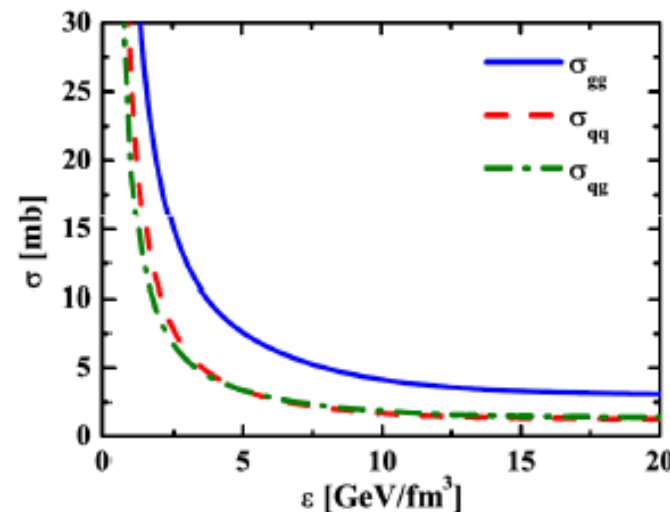


- **inelastic collisions:**

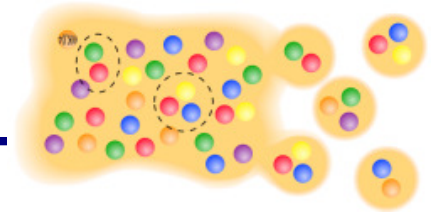
(Breit-Wigner cross sections)



suppressed (<1%)  
due to the large  
mass of gluons



# III. PHSD - basic concept



## III. Hadronization:

□ **Hadronization:** based on DQPM

- **massive, off-shell (anti-)quarks** with broad spectral functions hadronize to **off-shell mesons and baryons or color neutral excited states - ,strings‘** (strings act as ,doorway states‘ for hadrons)

$$g \rightarrow q + \bar{q}, \quad q + \bar{q} \leftrightarrow \text{meson ('string' )}$$

$$q + q + q \leftrightarrow \text{baryon ('string' )}$$

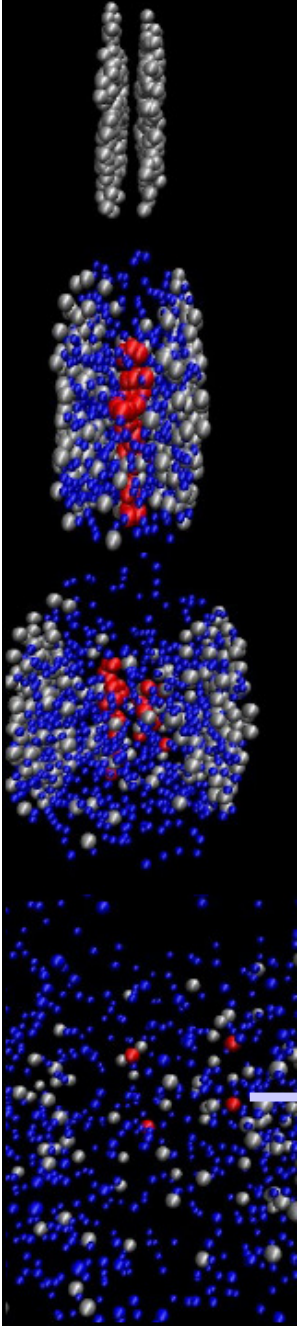
- Local covariant off-shell **transition rate** for q+qbar fusion  
 → **meson formation:**

$$\frac{dN^{q+\bar{q} \rightarrow m}}{d^4x d^4p} = \text{Tr}_q \text{Tr}_{\bar{q}} \delta^4(p - p_q - p_{\bar{q}}) \delta^4\left(\frac{x_q + x_{\bar{q}}}{2} - x\right) \delta(\text{flavor, color})$$

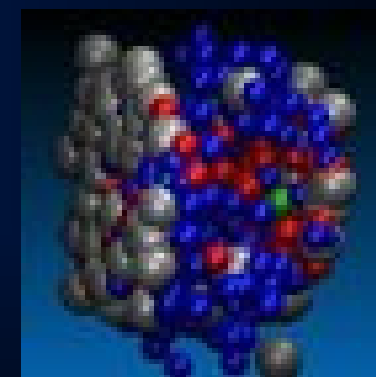
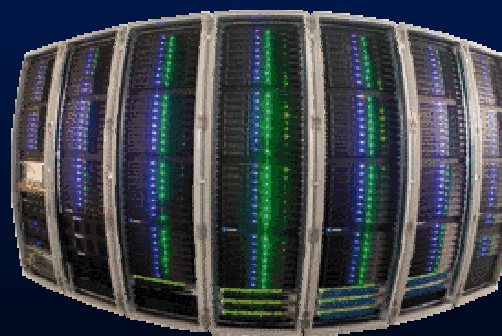
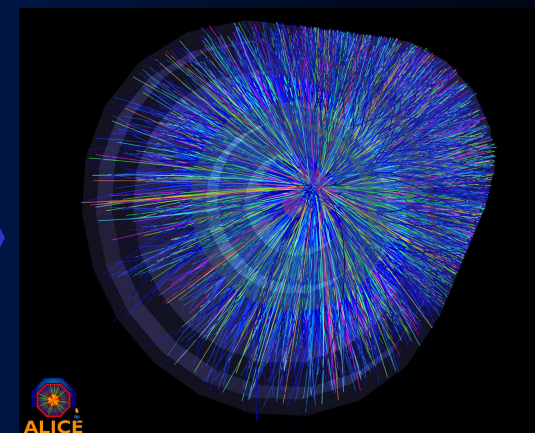
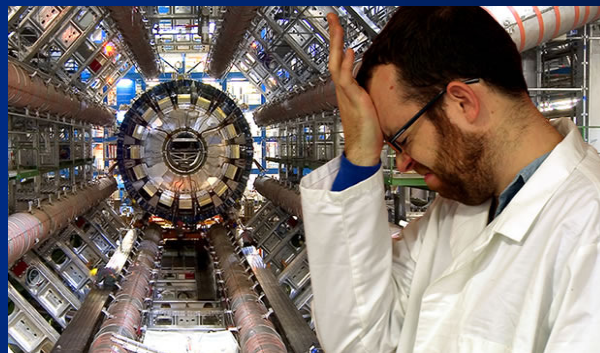
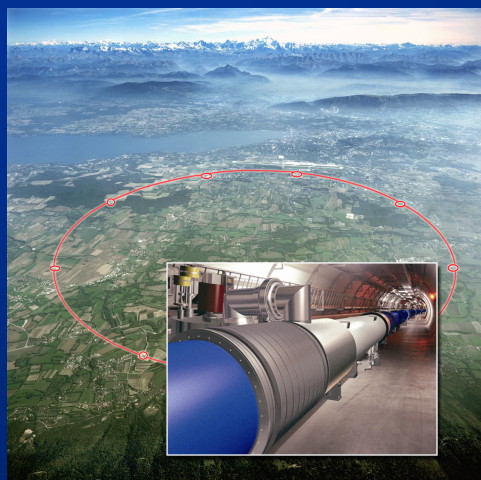
$$\cdot N_q(x_q, p_q) N_{\bar{q}}(x_{\bar{q}}, p_{\bar{q}}) \cdot \omega_q \rho_q(p_q) \cdot \omega_{\bar{q}} \rho_{\bar{q}}(p_{\bar{q}}) \cdot |M_{q\bar{q}}|^2 \underline{W_m(x_q - x_{\bar{q}}, p_q - p_{\bar{q}})}$$

- $N_j(x,p)$  is the phase-space density of parton j at space-time position x and 4-momentum p
- $W_m$  is the phase-space distribution of the formed ,pre-hadrons‘ (Gaussian in phase space)
- $|M_{q\bar{q}}|^2$  is the effective quark-antiquark interaction from the DQPM

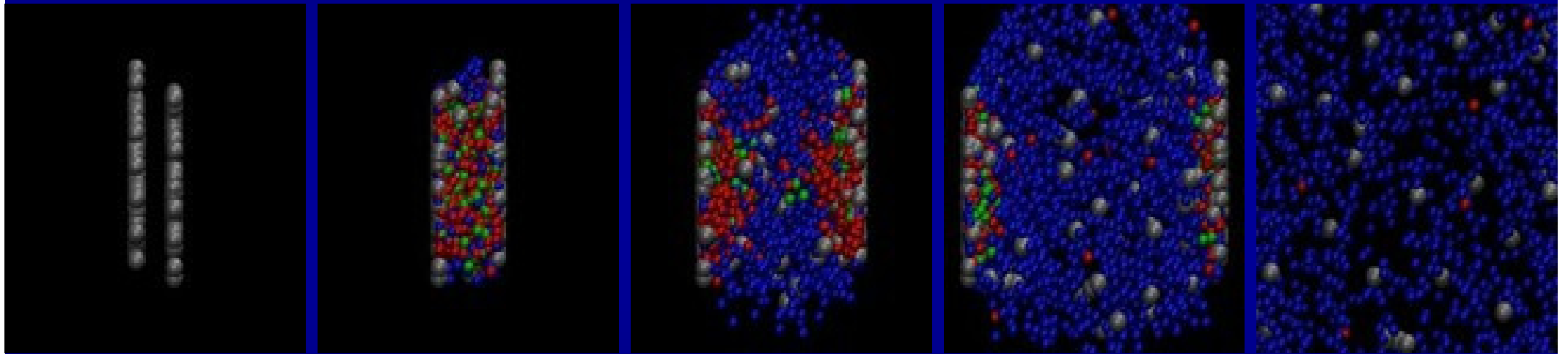
## IV. Hadronic phase: hadron-string interactions – off-shell HSD



# PHSD – ,femto‘ accelerator

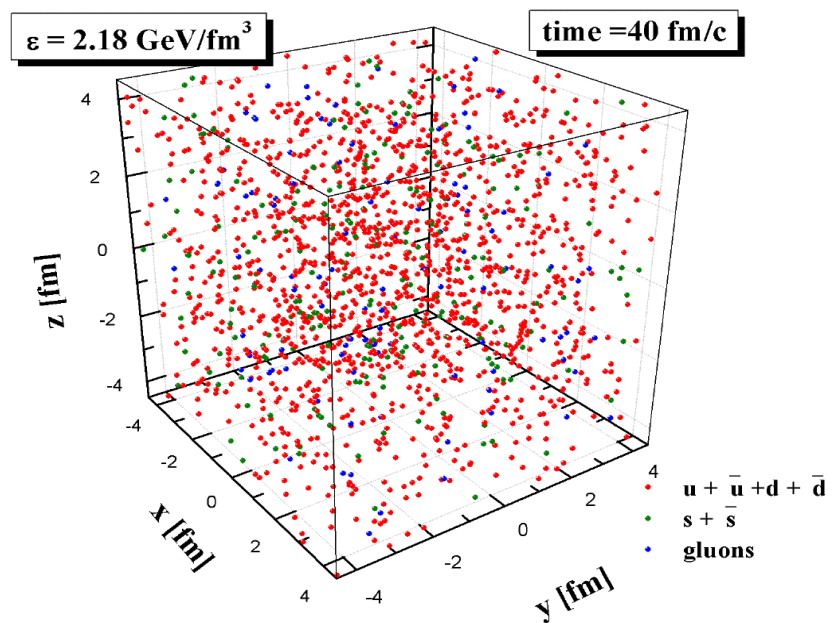


# Au+Au, 21.3 TeV, central





# Properties of QGP in-equilibrium using PHSD





# Properties of parton-hadron matter in-equilibrium

V. Ozvenchuk et al., PRC 87 (2013) 024901, arXiv:1203.4734

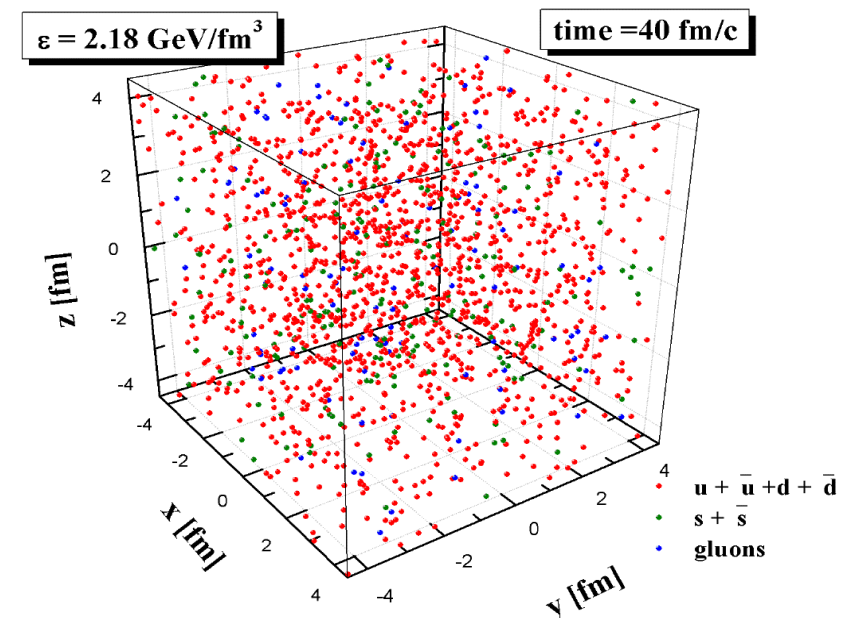
V. Ozvenchuk et al., PRC 87 (2013) 064903, arXiv:1212.5393

## The goal:

- study of the dynamical equilibration of QGP within the non-equilibrium off-shell PHSD transport approach
- transport coefficients (shear and bulk viscosities) of strongly interacting partonic matter
- particle number fluctuations (scaled variance, skewness, kurtosis)

## Realization:

- Initialize the system in a finite box with periodic boundary conditions with some energy density  $\varepsilon$  and chemical potential  $\mu_q$
- Evolve the system in time until equilibrium is achieved





# Properties of parton-hadron matter – shear viscosity

$\eta/s$  using **Kubo formalism** and the **relaxation time approximation** (,kinetic theory‘)

□  $T=T_c$ :  $\eta/s$  shows a **minimum** ( $\sim 0.1$ ) close to the critical temperature

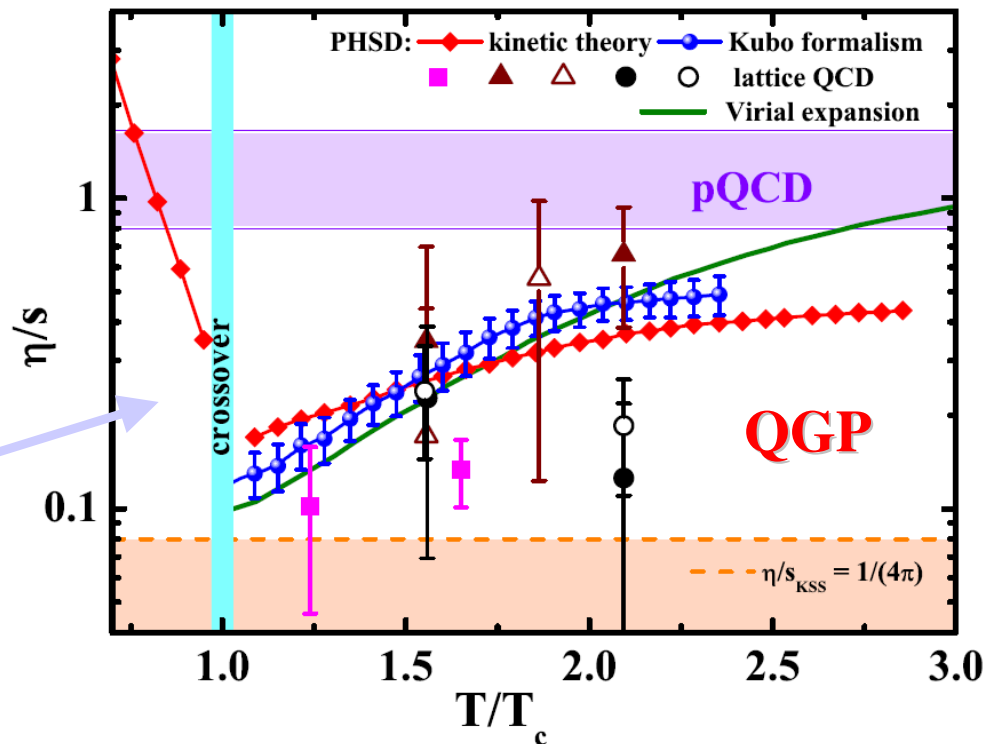
□  $T>T_c$ : **QGP - pQCD limit** at higher temperatures

□  $T<T_c$ : fast increase of the ratio  $\eta/s$  for **hadronic matter** →

- lower interaction rate of hadronic system
- smaller number of degrees of freedom (or entropy density) for hadronic matter compared to the QGP



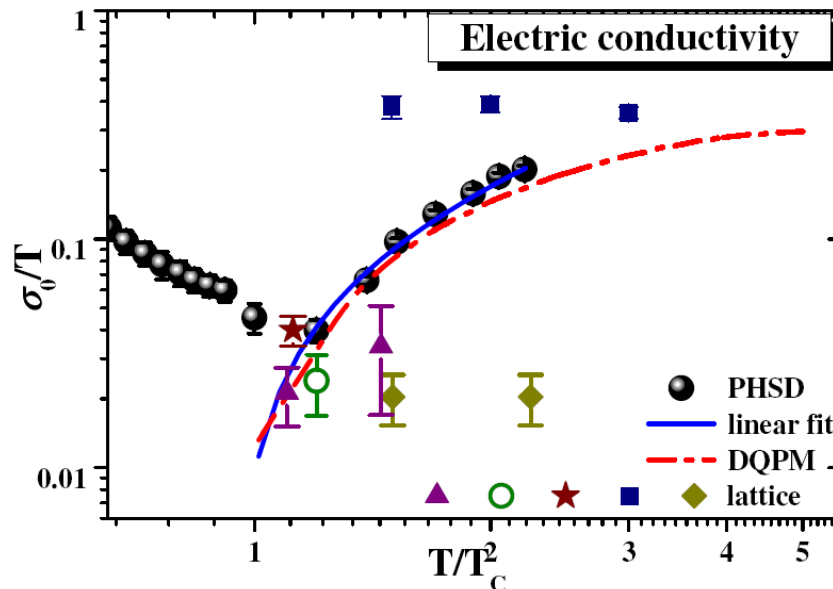
**QGP in PHSD = strongly-interacting liquid**



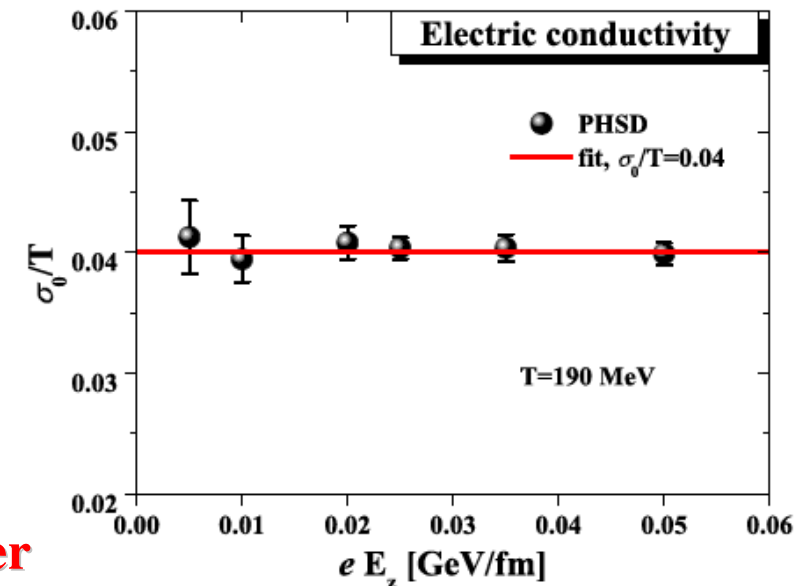
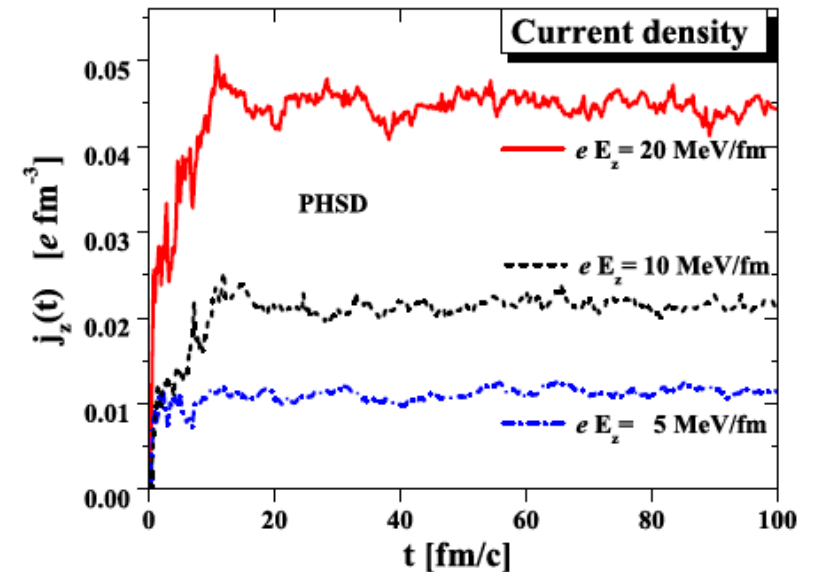
Virial expansion: S. Mattiello, W. Cassing, Eur. Phys. J. C 70, 243 (2010).

- The response of the strongly-interacting system in equilibrium to an **external electric field**  $eE_z$  defines the **electric conductivity**  $\sigma_0$ :

$$\frac{\sigma_0}{T} = \frac{j_{eq}}{E_z T}, \quad j_z(t) = \frac{1}{V} \sum_j eq_j \frac{p_z^j(t)}{M_j(t)}$$

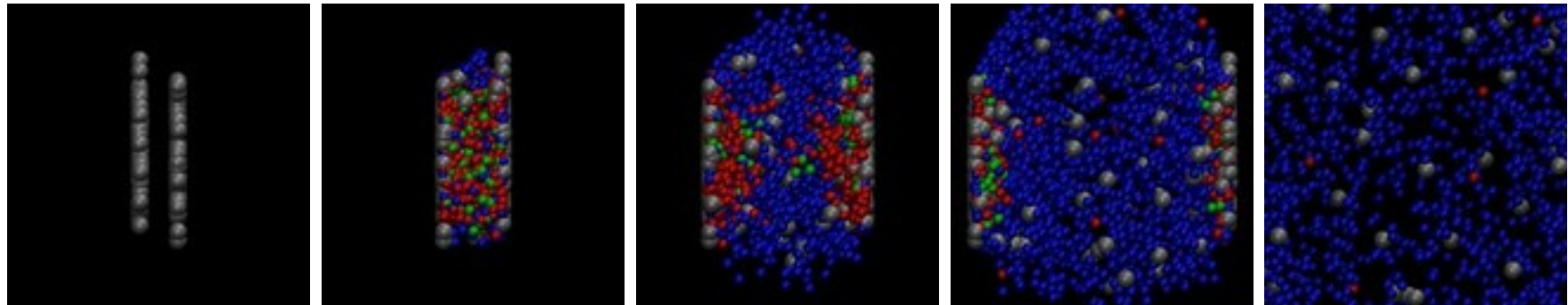


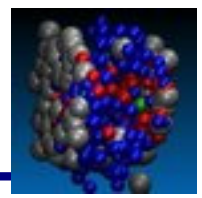
- the **QCD matter** even at  $T \sim T_c$  is a **much better electric conductor than Cu or Ag** (at room temperature) by a factor of **500** !



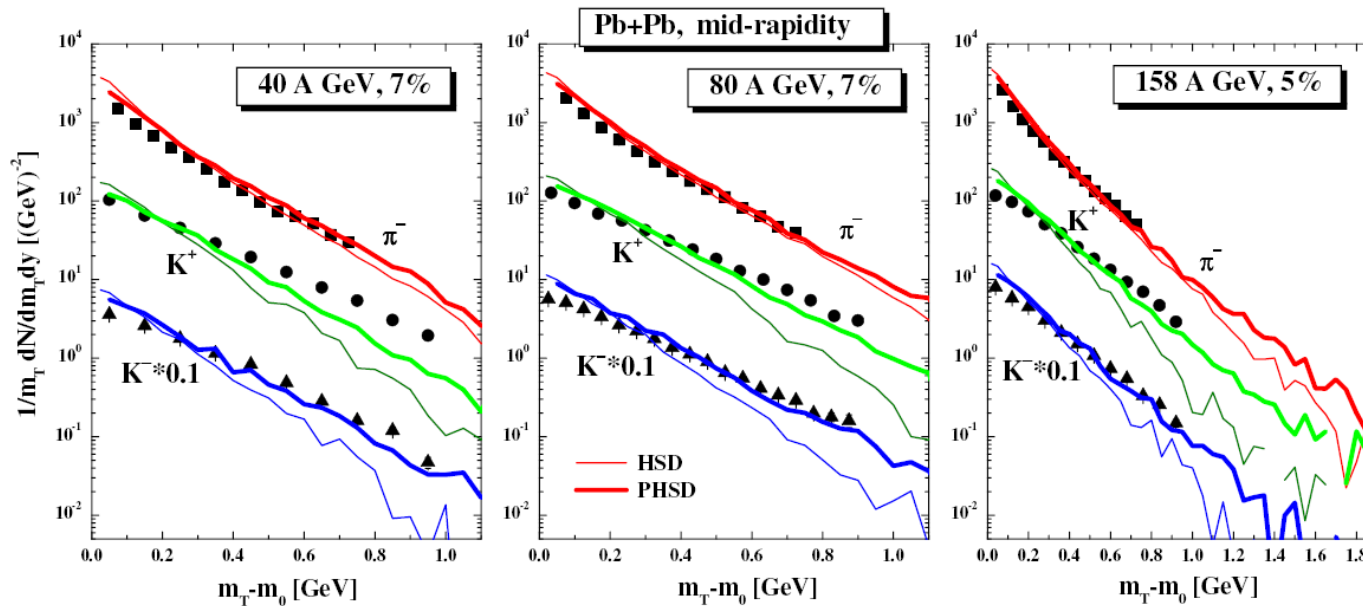


**Bulk properties:  
rapidity,  $m_T$ -distributions,  
multi-strange particle enhancement in Au+Au**

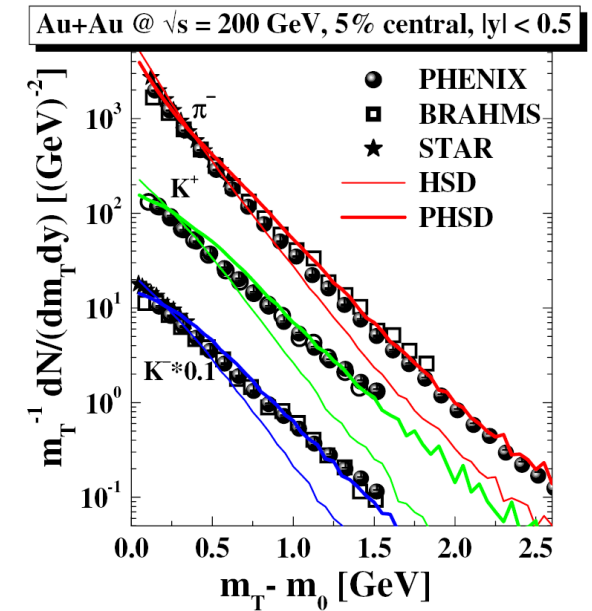




## Central Pb + Pb at SPS energies



## Central Au+Au at RHIC

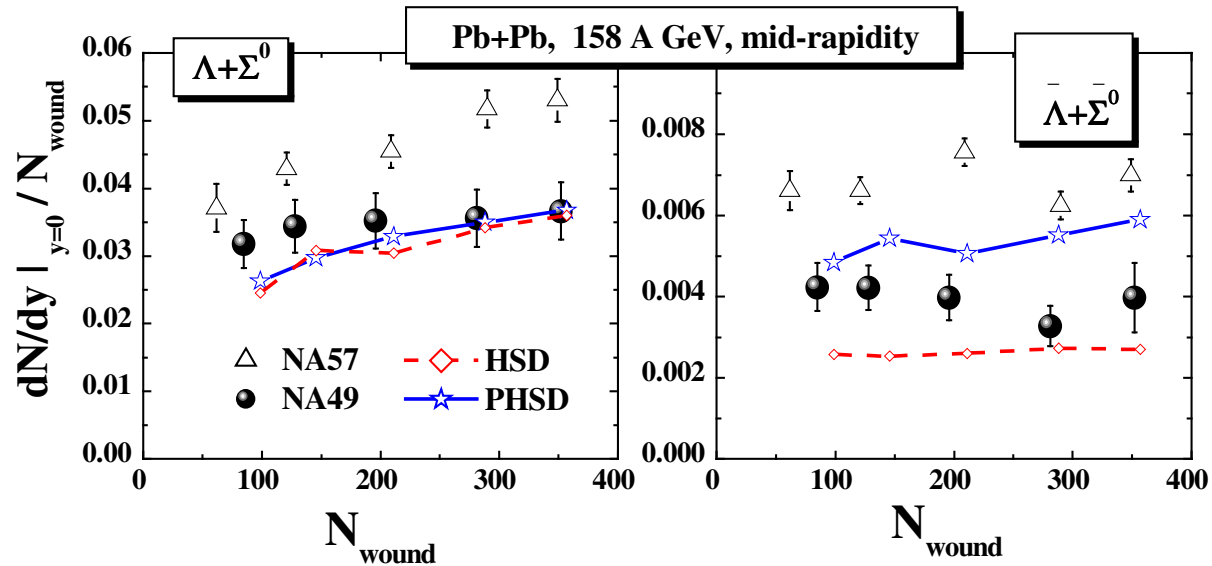


- PHSD gives **harder  $m_T$  spectra** and works better than HSD at **high energies**
  - RHIC, SPS (and top FAIR, NICA)
- however, at low SPS (and low FAIR, NICA) energies the effect of the partonic phase decreases due to the decrease of the partonic fraction



# Centrality dependence of (multi-)strange (anti-)baryons

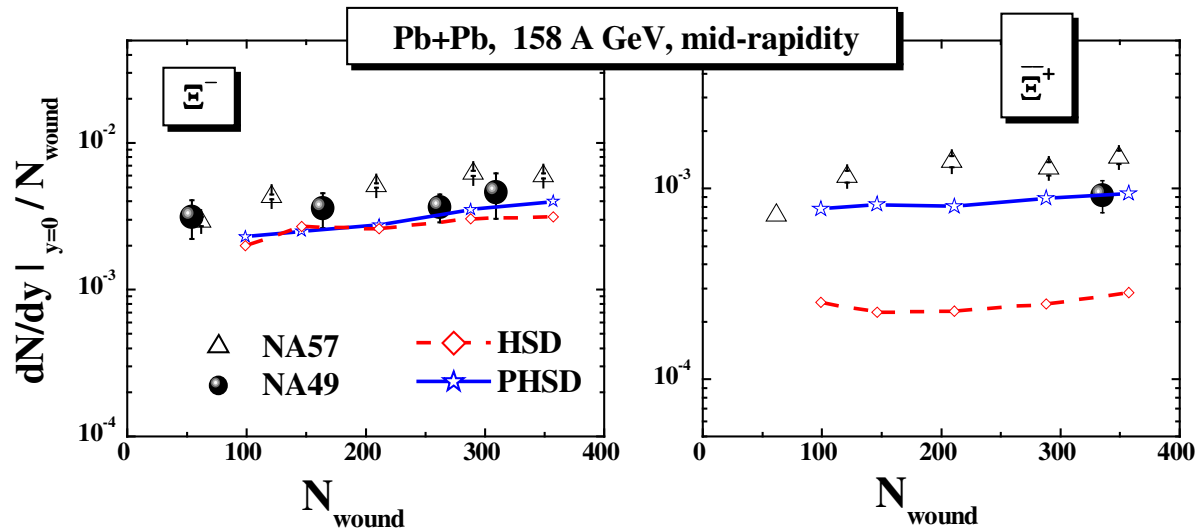
strange  
baryons  
 $\Lambda + \Sigma^0$



strange  
antibaryons

$\bar{\Lambda} + \bar{\Sigma}^0$

multi-strange  
baryon  
 $\Xi^-$

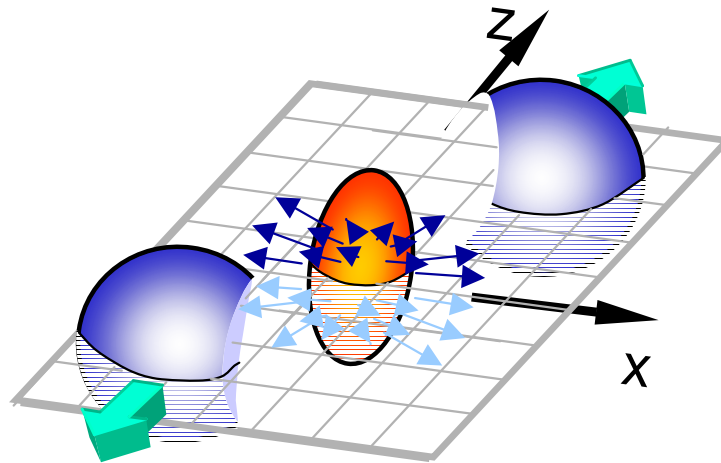


multi-strange  
antibaryon

$\bar{\Xi}^+$

→ enhanced production of (multi-) strange antibaryons in PHSD relative to HSD

**Collective flow:  
anisotropy coefficients ( $v_1, v_2, v_3, v_4$ )  
in A+A**





# Anisotropy coefficients

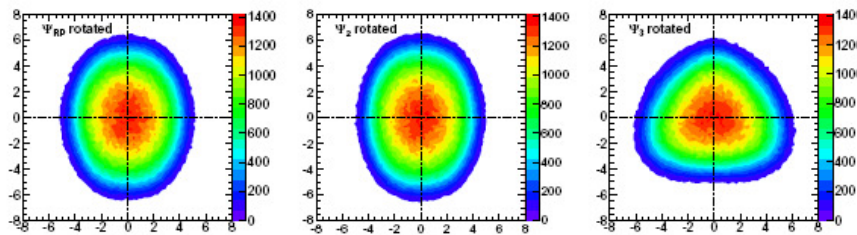
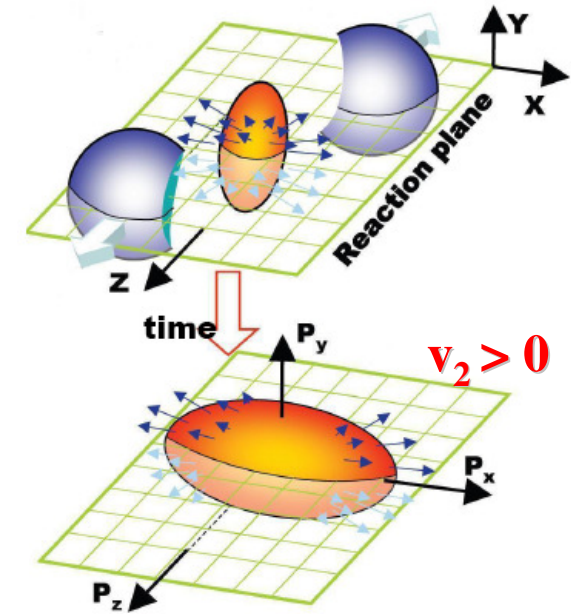
Non central Au+Au collisions :

interaction between constituents leads to a **pressure gradient** => spatial asymmetry is converted to an asymmetry in momentum space => **collective flow**

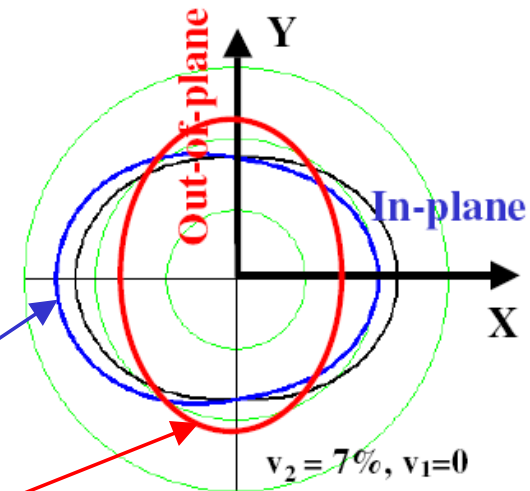
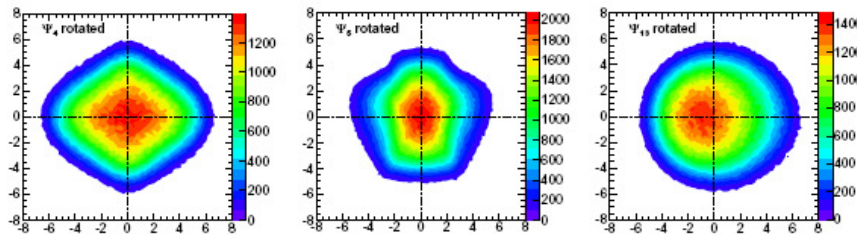
$$\frac{dN}{d\varphi} \propto \left( 1 + 2 \sum_{n=1}^{+\infty} v_n \cos[n(\varphi - \psi_n)] \right)$$

$$v_n = \langle \cos n(\varphi - \psi_n) \rangle, \quad n = 1, 2, 3, \dots$$

$v_1$ : directed flow  
 $v_2$ : elliptic flow  
 $v_3$ : triangular flow.....



from S. A. Voloshin, arXiv:1111.7241



$v_2 > 0$  indicates **in-plane** emission of particles

$v_2 < 0$  corresponds to a **squeeze-out** perpendicular to the reaction plane (**out-of-plane** emission)

$$v_2 = 7\%, v_1 = 0$$

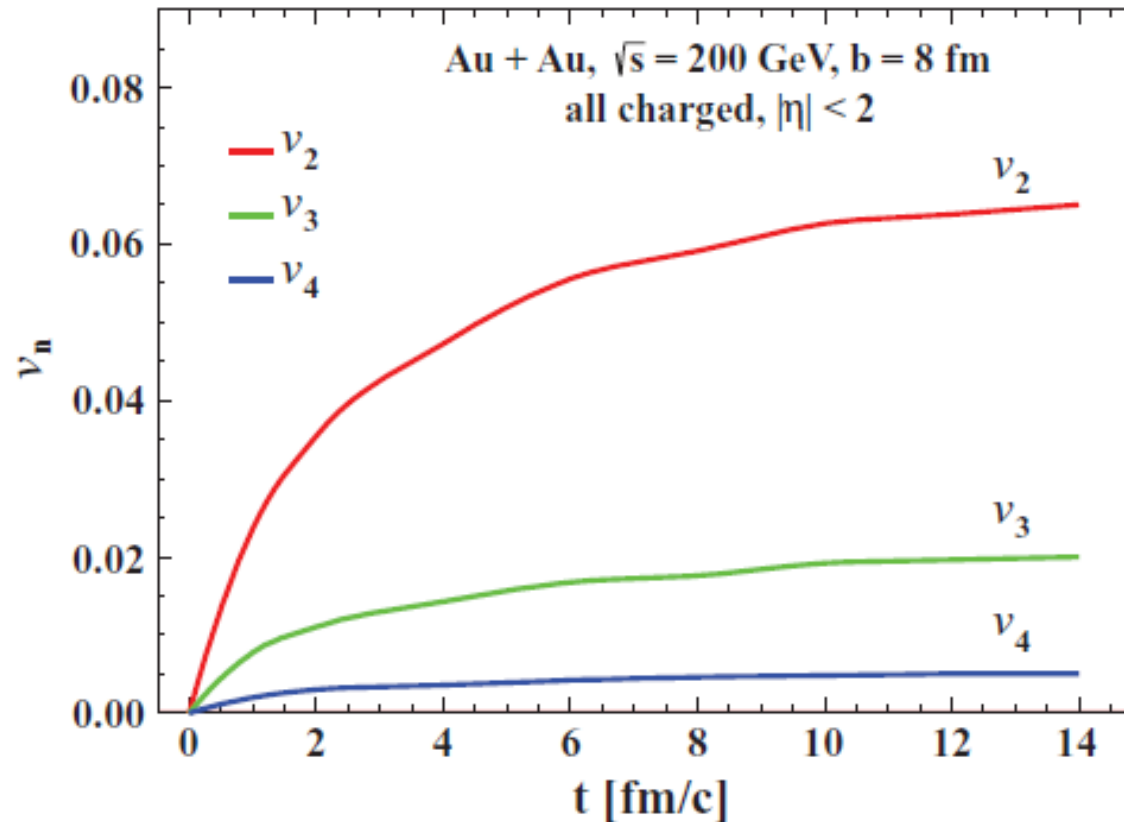
$$v_2 = 7\%, v_1 = -7\%$$

$$v_2 = -7\%, v_1 = 0$$



# Development of azimuthal anisotropies in time

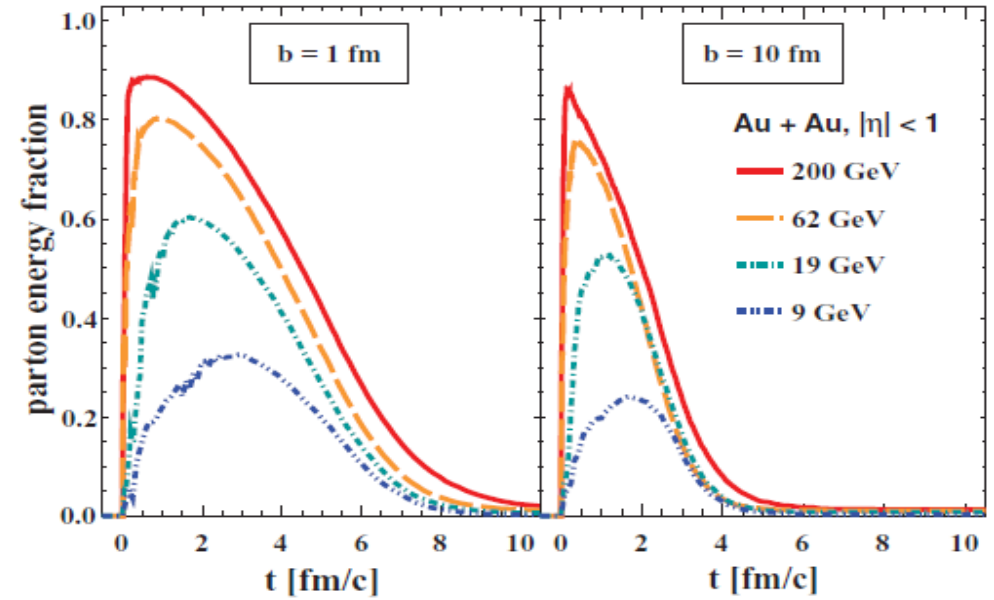
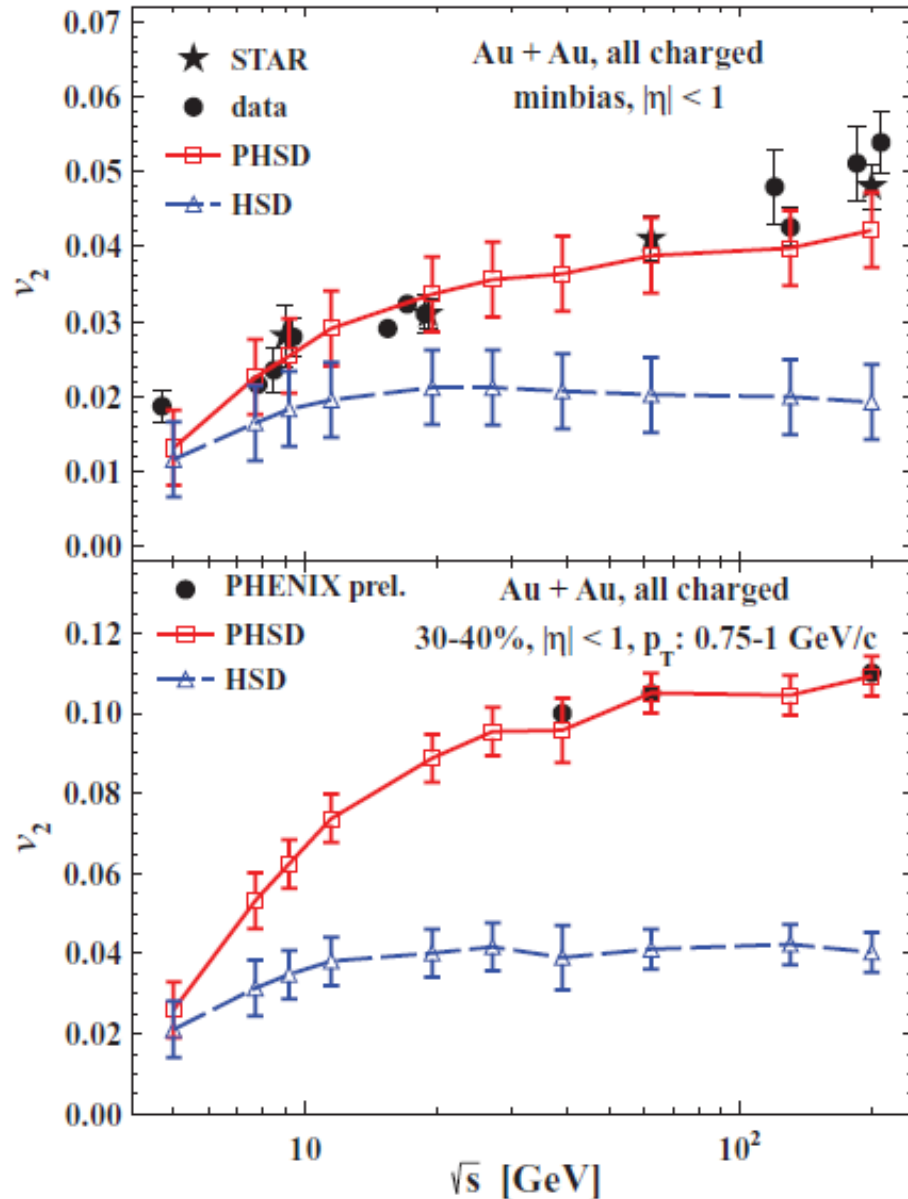
Time evolution of  $v_n$  for Au + Au collisions at  $\sqrt{s} = 200$  GeV with impact parameter  $b = 8$  fm.



- Flow coefficients **reach their asymptotic values** by the time of 6–8 fm/c after the beginning of the collision

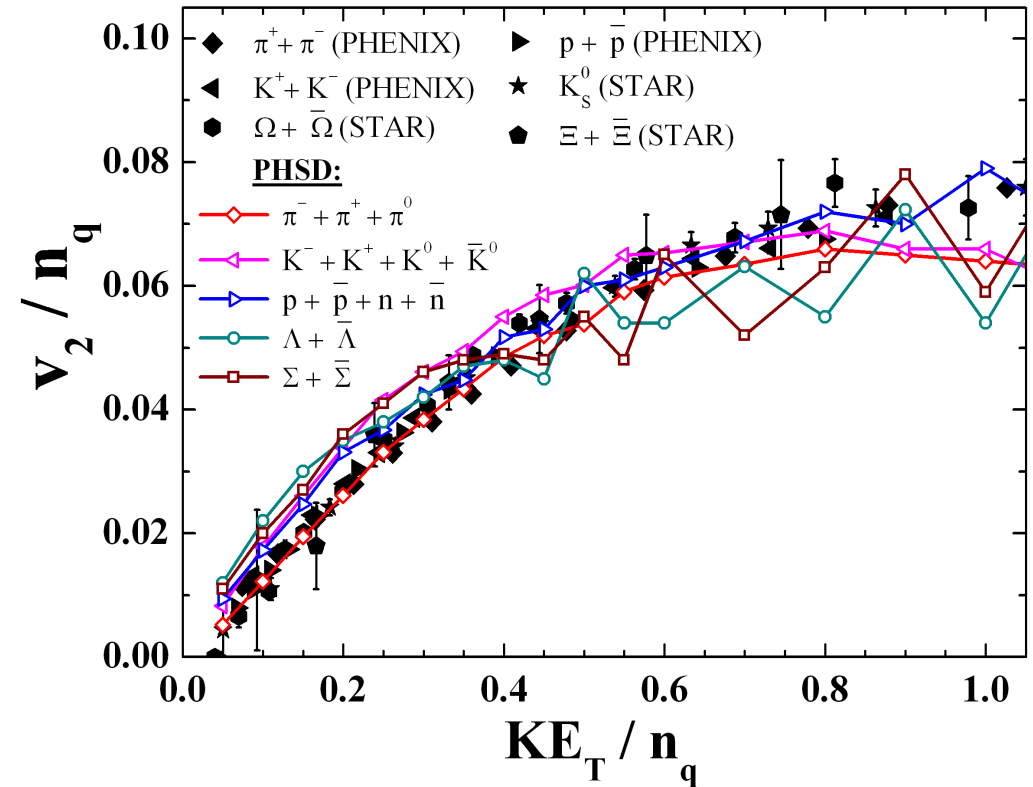
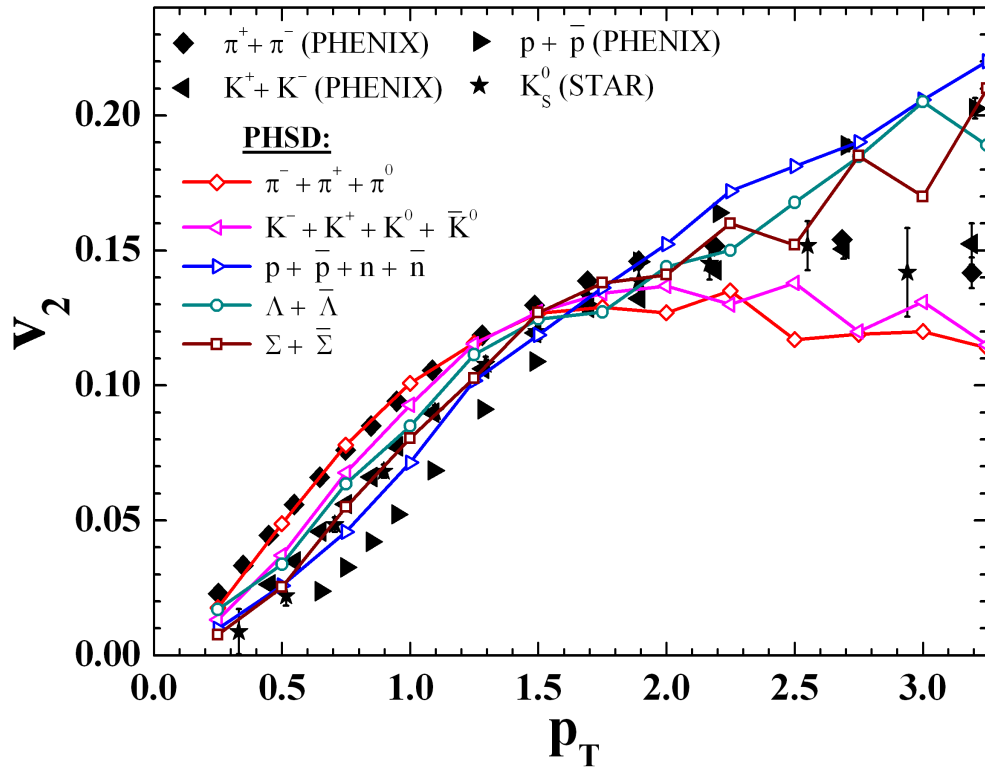


# Elliptic flow $v_2$ vs. collision energy for Au+Au



- $v_2$  in PHSD is larger than in HSD due to the repulsive scalar mean-field potential  $U_s(\rho)$  for partons
- $v_2$  grows with bombarding energy due to the increase of the parton fraction

# Scaling properties: quark number scaling

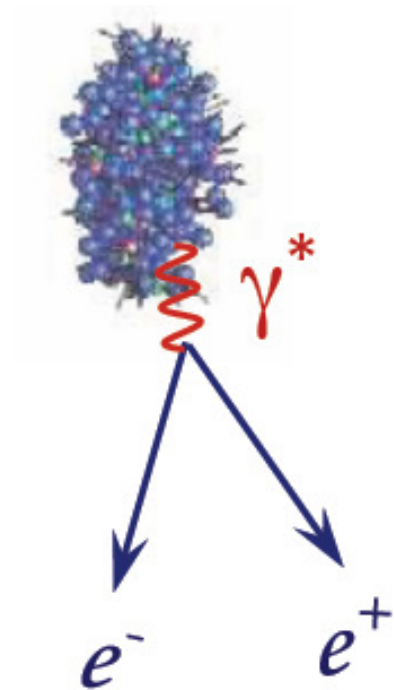


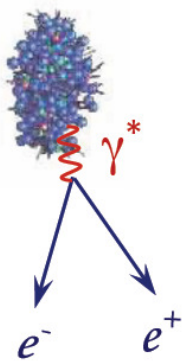
- The mass splitting at low  $p_T$  is approximately reproduced as well as the meson-baryon splitting for  $p_T > 2 \text{ GeV}/c$  !
- The scaling of  $v_2$  with the number of constituent quarks  $n_q$  is roughly in line with the data at RHIC.

E. Bratkovskaya, W. Cassing, V. Konchakovski, O. Linnyk, NPA856 (2011) 162

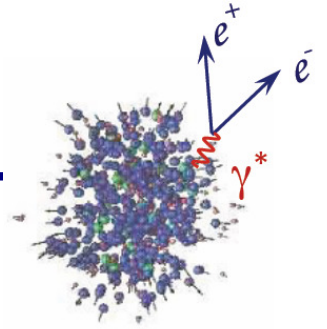


# Dileptons





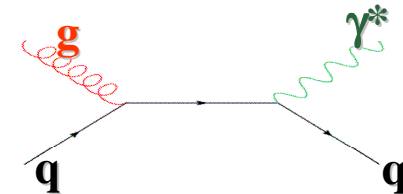
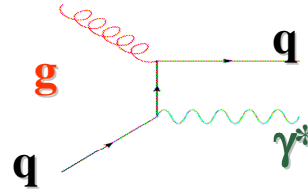
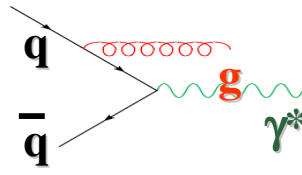
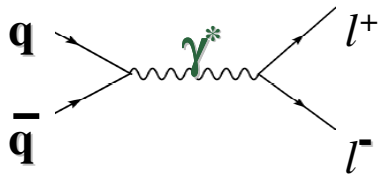
# Electromagnetic probes: dileptons and photons



➤ Dileptons are emitted from different stages of the reaction and not much effected by final-state interactions

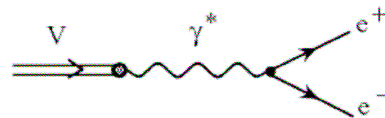
## Dilepton sources:

■ from the QGP via partonic (q,qbar, g) interactions:

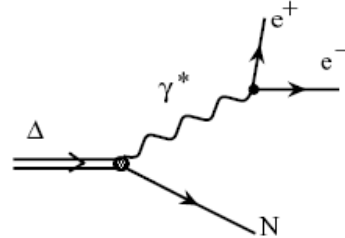


■ from hadronic sources:

• direct decay of vector mesons ( $\rho, \omega, \phi, J/\Psi, \Psi'$ )



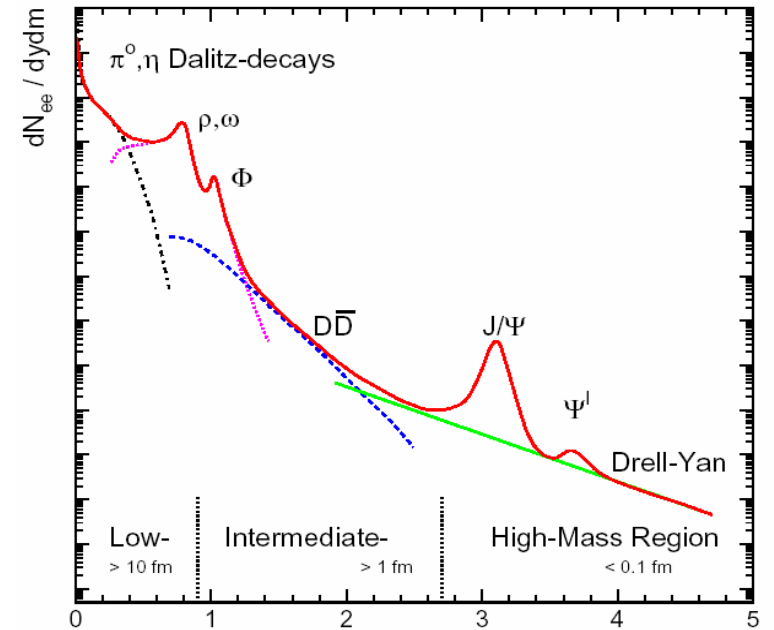
• Dalitz decay of mesons and baryons ( $\pi^0, \eta, \Delta, \dots$ )



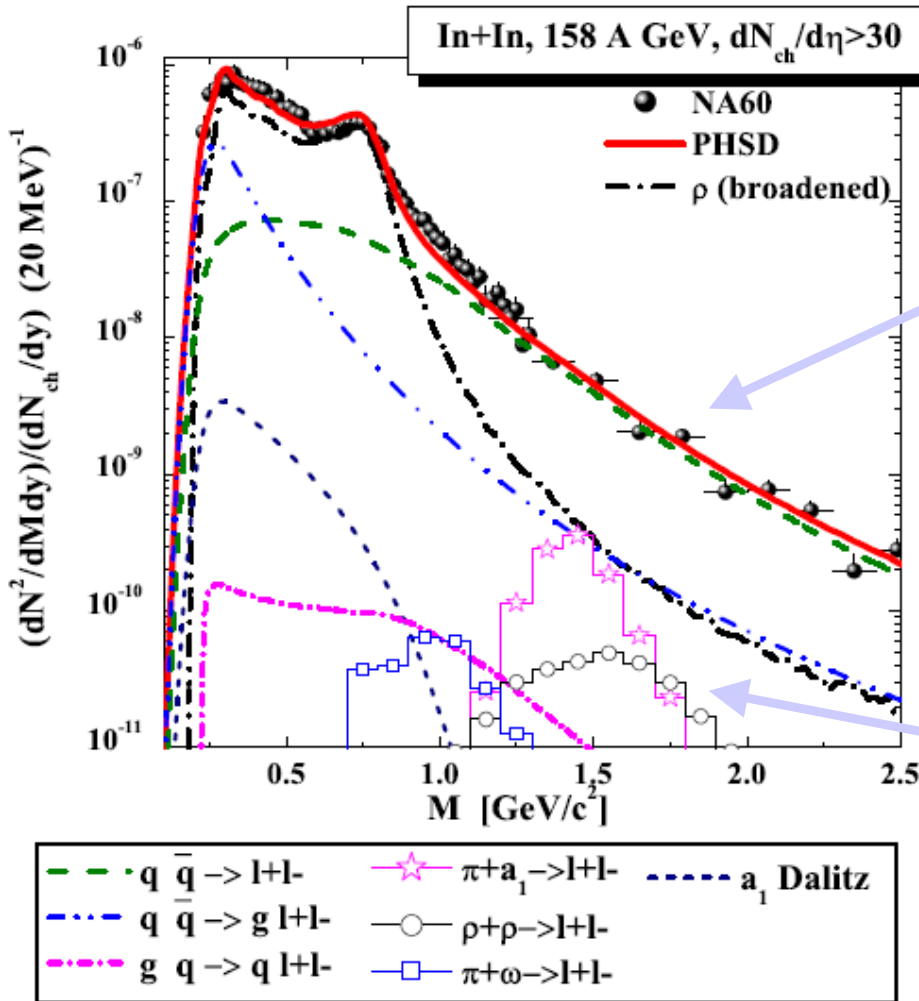
• correlated D+Dbar pairs

• radiation from multi-meson reactions ( $\pi+\pi, \pi+\rho, \pi+\omega, \rho+\rho, \pi+a_1$ ) - ,4π'

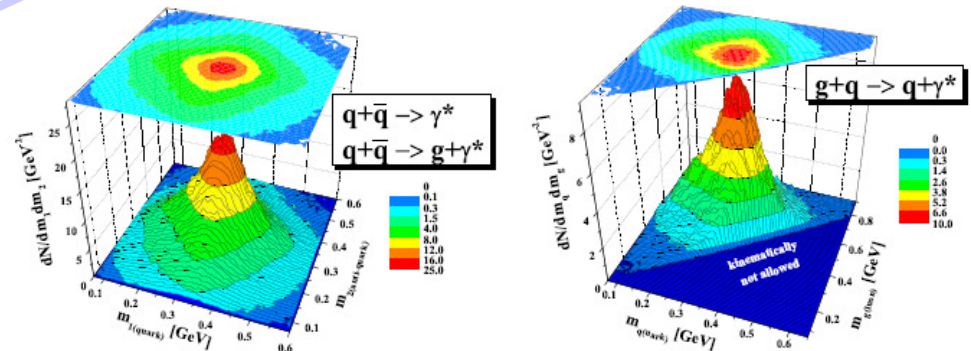
➔ Dileptons are an ideal probe to study the properties of the hot and dense medium



## Acceptance corrected NA60 data



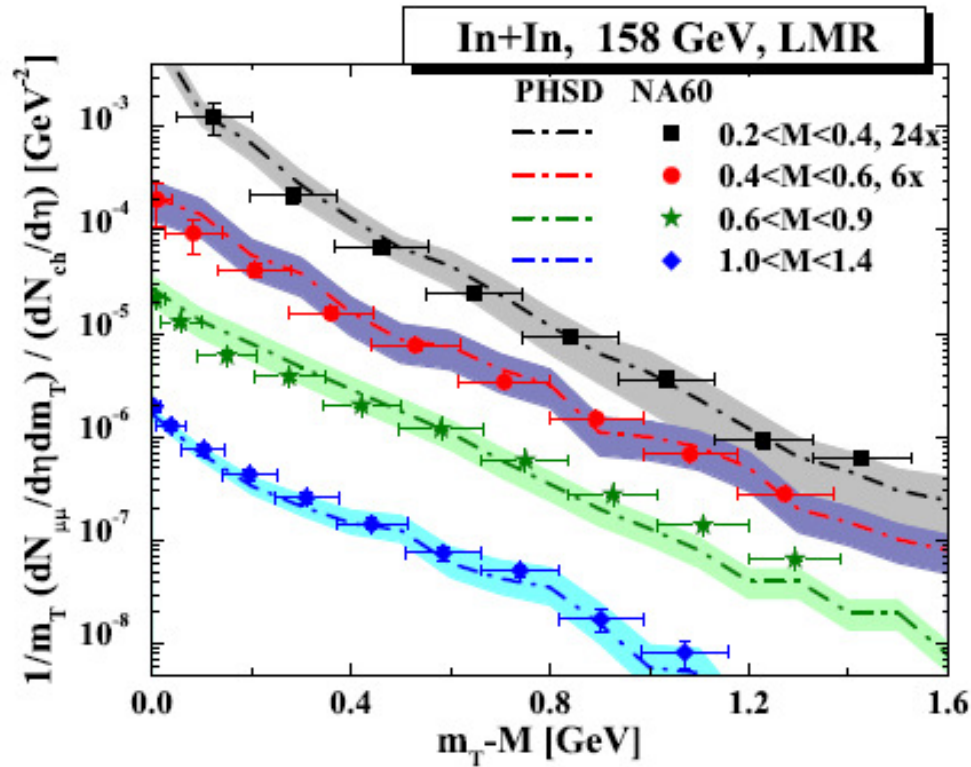
■ Mass region above 1 GeV is dominated by **partonic radiation** !



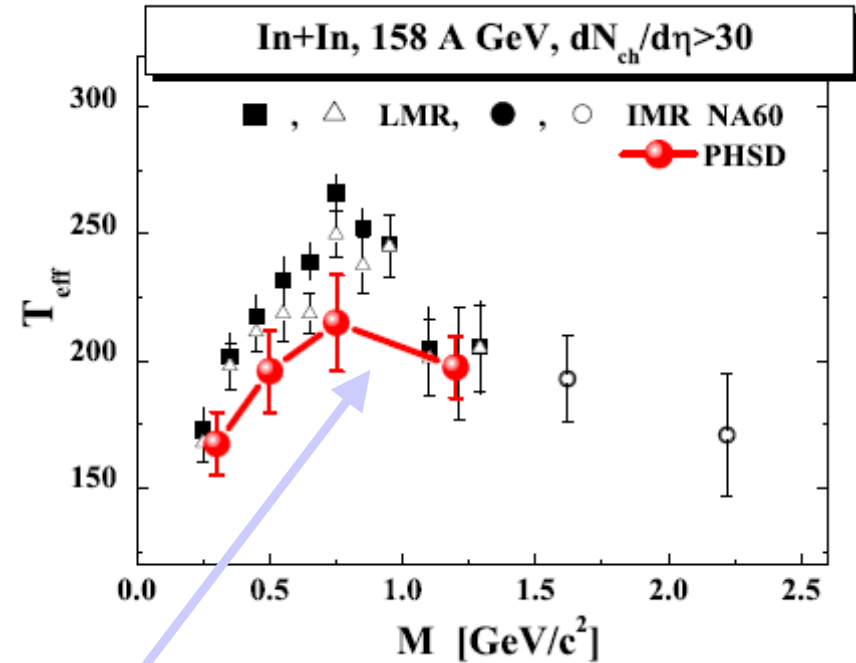
■ Contributions of **“4 $\pi$ ”** channels (radiation from multi-meson reactions) are **small**

O. Linnyk, E.B., V. Ozvenchuk, W. Cassing and C.-M. Ko, PRC 84 (2011) 054917

# NA60: $m_T$ spectra



- Inverse slope parameter  $T_{\text{eff}}$  for dilepton spectra vs NA60 data



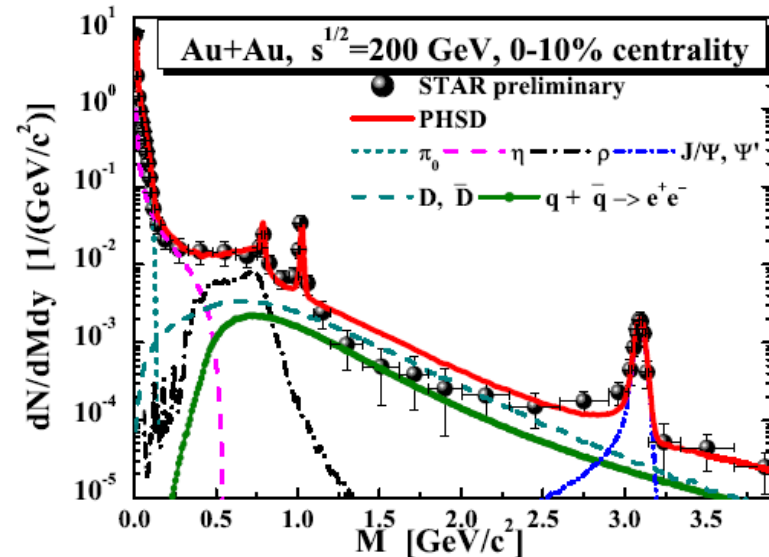
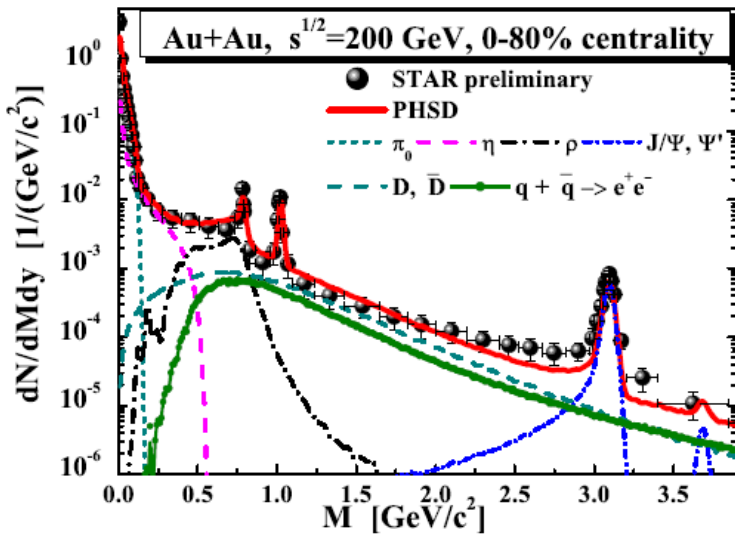
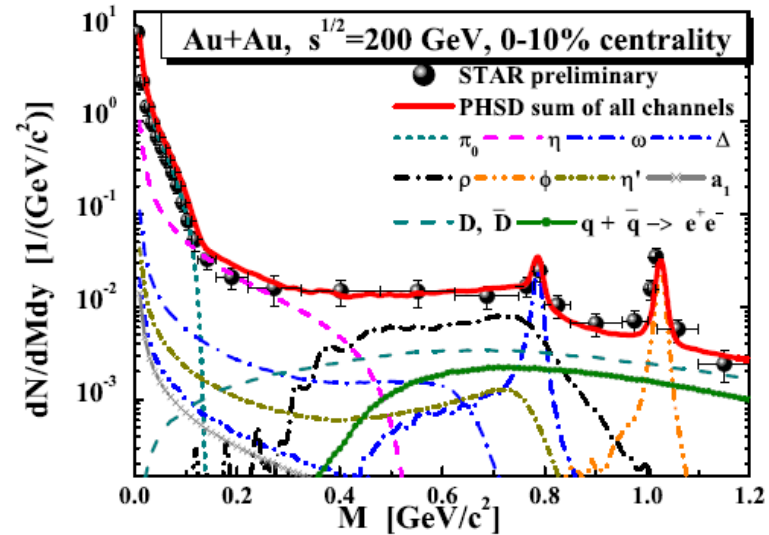
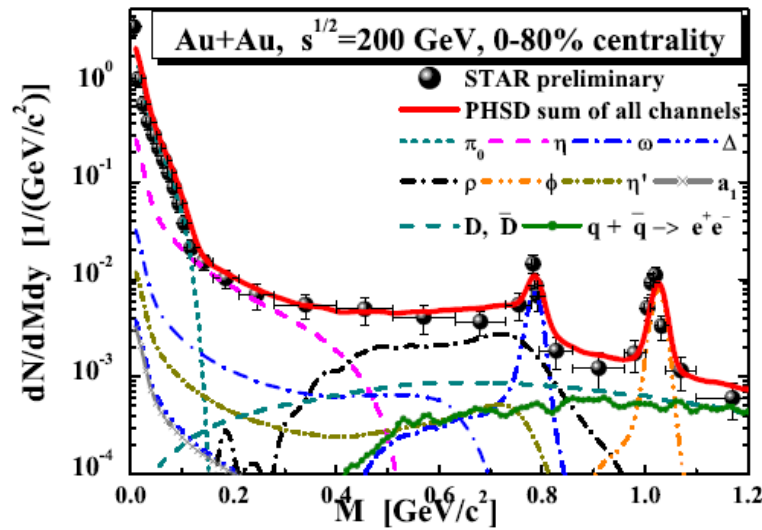
## Conjecture:

- spectrum from sQGP is softer than from hadronic phase since quark-antiquark annihilation occurs dominantly before the collective radial flow has developed (cf. NA60)

O. Linnyk, E.B., V. Ozvenchuk, W. Cassing and C.-M. Ko, PRC 84 (2011) 054917



# STAR: mass spectra

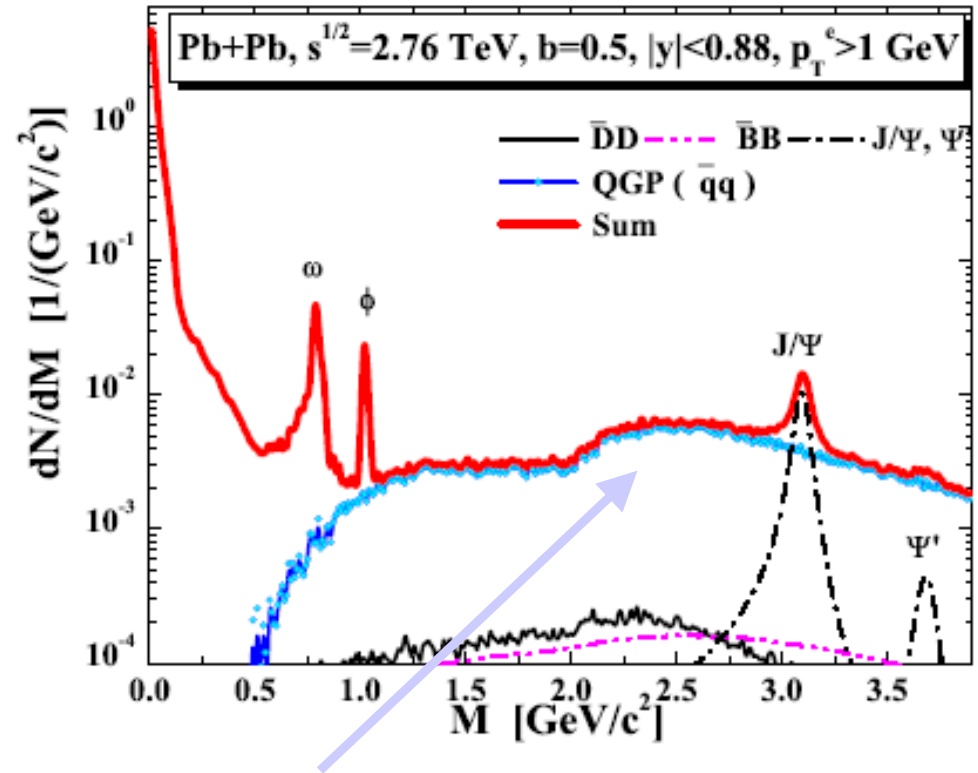
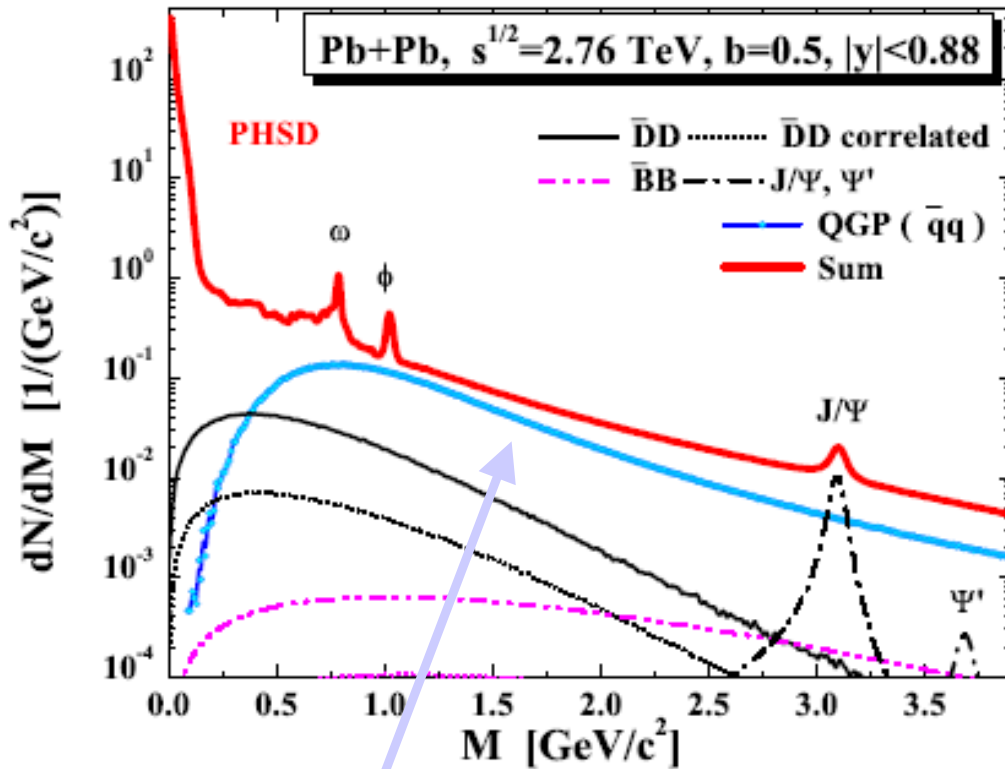


- The partonic channels dominate at  $M > 1$  GeV





# LHC: mass spectra with exp. cuts



■ QGP( $q\bar{q}$ ) dominates at  $M > 1.2$  GeV !

■  $p_T$  cut enhances the signal of QGP( $q\bar{q}$ )

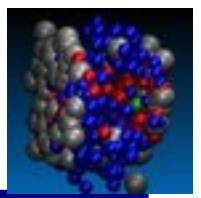
**D-, B-mesons:** from Pol-Bernard Gossiaux and Jörg Aichelin

**J/ $\Psi$ ,  $\Psi'$ :** from C.M. Ko and T. Song

O. Linnyk, W. Cassing, J. Manninen, E.B., P.B. Gossiaux, J. Aichelin, T. Song, C.-M. Ko, Phys.Rev. C87 (2013) 014905; arXiv:1208.1279



# Summary



- **PHSD** provides a consistent description of **off-shell parton dynamics** in line with the **lattice QCD equation of state** (from the BMW collaboration)

- **PHSD** versus **experimental observables**:

  - enhancement of meson  $m_T$  slopes (at top SPS and RHIC)

  - strange antibaryon enhancement (at SPS)

  - partonic emission of high mass dileptons at SPS and RHIC

  - enhancement of collective flow  $v_2$  with increasing energy

  - quark number scaling of  $v_2$  (at RHIC)

  - ...

⇒ **evidence for strong nonhadronic interactions in the early phase of relativistic heavy-ion reactions**

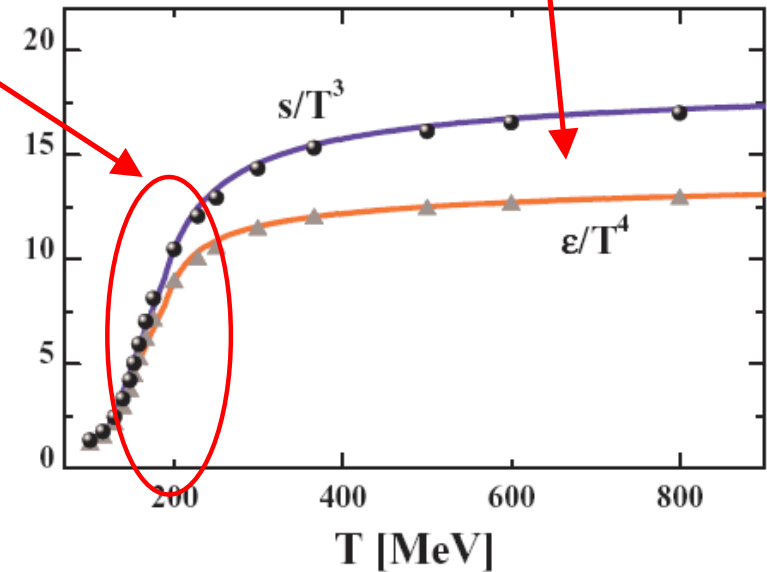
⇒ **formation of the sQGP!**

# Outlook - Perspectives

What is the stage of matter close to  $T_c$  :

- ❑ 1st order phase transition?
- ❑ ,Mixed‘ phase = interaction of partonic and hadronic degrees of freedom?  
(V.D. Toneev et al.)

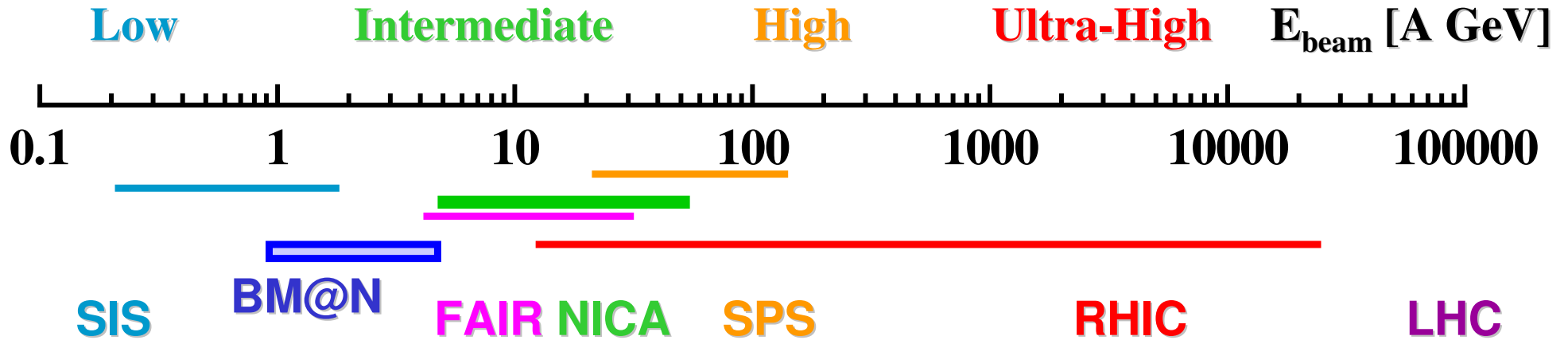
Lattice EQS for  $\mu=0$   
 → ,crossover‘ ,  $T > T_c$



Open problems:

- How to describe a **first-order phase transition** in transport models?
- How to describe parton-hadron interactions in a **,mixed‘ phase**?

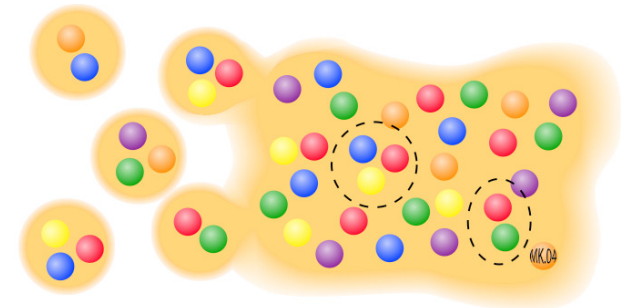
# HIC experiments



**Baryonic matter**  
 ||  
 Meson and baryon spectroscopy  
 In-medium effects  
 EoS

**„Mixed“ phase:**  
 hadrons (baryons, mesons) +  
 quarks and gluons  
 ||  
 In-medium effects  
 Chiral symmetry restoration  
 Phase transition to sQGP  
 Critical point in the QCD phase diagram

**QGP: quarks and gluons**  
 ||  
 Properties of sQGP





# PHSD group

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**Volodya Konchakovski (Giessen Univ.)**

**Olena Linnyk (Giessen Univ.)**

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