

Measurements of the ratio R_{dp} of the quasi-elastic $nd \rightarrow pnn$ to the elastic $np \rightarrow pn$ charge-exchange process yields at 0° over 0.55 - 2.0 GeV neutron beam energy

Measurements were carried out at the Nuclotron of the Veksler and Baldin Laboratory of High Energies of the Joint Institute for Nuclear Research (JINR) at the neutron beam kinetic energies 0.55, 0.8, 1.0, 1.2, 1.4, 1.8 and 2.0 GeV.

The obtained $R_{dp} = d\sigma/d\Omega(nd) / d\sigma/d\Omega(np)$ values remain nearly constant with energy.

The new data are compared with existing ones, measured at energies below 1 GeV, and with calculations using the invariant amplitude sets for the solutions of the GW/VPI phase-shift analyses.

The investigations are being carried out under the program of the first priority JINR project "Delta-Sigma" experiment.

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“The theory of the nucleon-nucleon (NN) interaction in the range of about 1-10 GeV is one of the most pressing open questions of modern nuclear/particle physics.

Below that energy range, chiral effective field theory applies as well as meson theory.

At very high energies (~ 100 GeV) perturbative QCD can be used.

But it is the “intermediate” region of a few GeV where theory has big problems.

For our understanding of the fundamental NN interaction on a broad scale, it is vital to have data for np spin observables in the GeV region”.

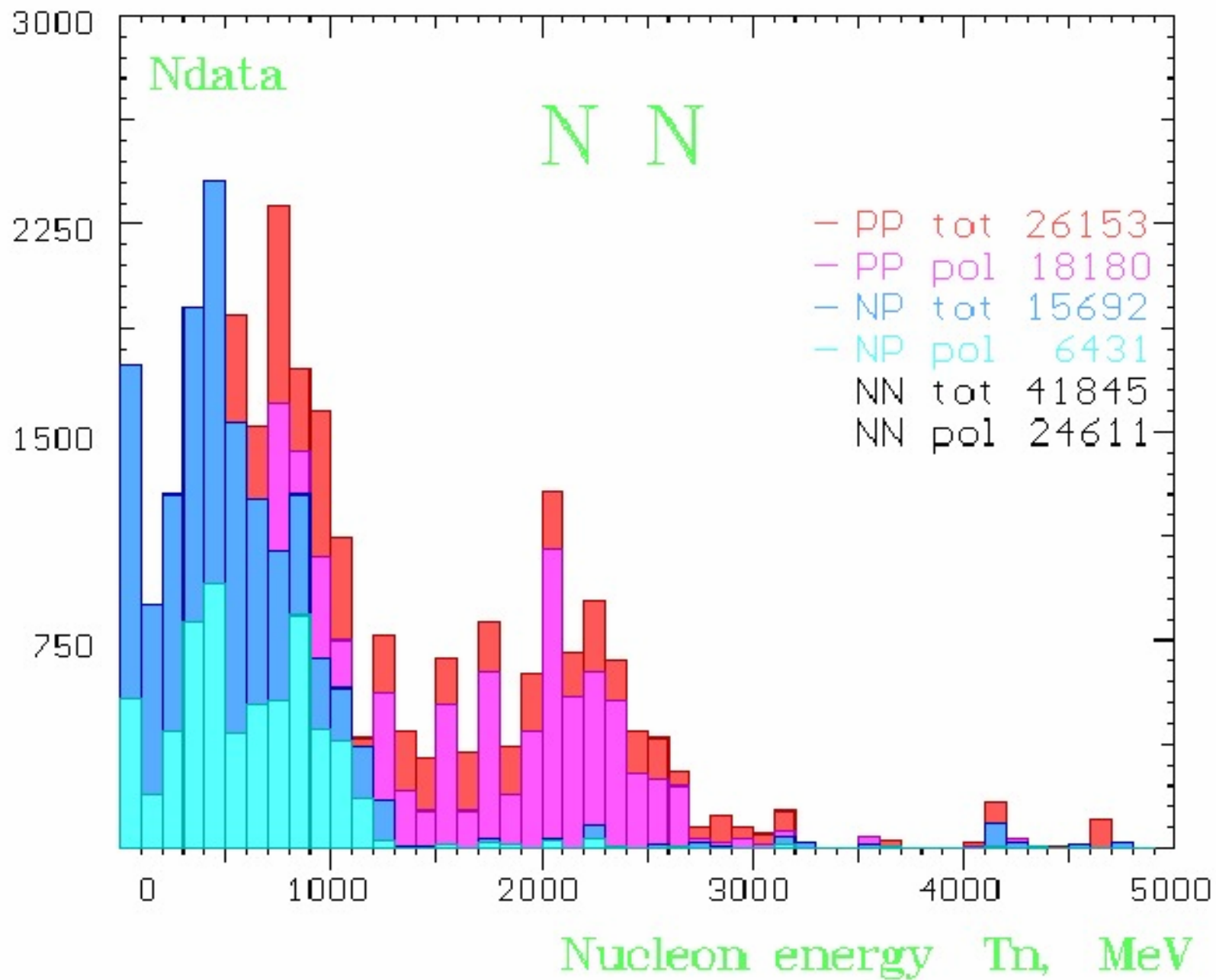
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The aim of the project "**Delta-Sigma**" Experiment

(see Ref.[30] in arXiv:0706.2195 [nucl-th])

is to extend the investigations of **NN** interaction over a new high **1.2 – 3.7 GeV** energy region of free polarized neutron beams, **provided at present**

only by the JINR VBLHEP accelerator Nuclotron.



The main task of the "**Delta-Sigma**" **Experiment** is **determination** for the first time the imaginary and real parts of spin-dependent **forward scattering np amplitudes** over **1.2 – 3.7 GeV** energy region.

To reach this aim, a sufficient data set on energy dependencies of **np** spin-dependent observables have to be obtained for **direct and simple reconstruction** of these **amplitudes**.

The Delta-Sigma experiment research program

1. Using longitudinally (L) and transverse (T) polarized neutron beams and polarized proton target to measure the energy dependencies of
 - a) the total cross section differences $\Delta\sigma_L(np)$ and $\Delta\sigma_T(np)$ for parallel and antiparallel directions of beam and target polarizations, with energy steps of 100–200 MeV and expected statistical errors of 1 mb.

The observables $\Delta\sigma_L(np)$ and $\Delta\sigma_T(np)$ are linearly related to the imaginary parts of the two spin-dependent forward scattering invariant amplitudes **c** and **d** via optical theorems and allow to extract these imaginary parts.

- b) the spin-correlation parameters $A_{00kk}(np)$ and $A_{00nn}(np)$ with expected statistical errors of 0.02 – 0.05 (simultaneously with and independently of the $\Delta\sigma_{L,T}(np)$ measurements) .

The $A_{00kk}(np)$ and $A_{00nn}(np)$ values will be obtained from a registration of yields of elastic charge exchange process $np \rightarrow pn$ at 0° angle. They are related to the real parts of the amplitudes mentioned above and data to be obtained will be used to extract these real parts.

The Delta-Sigma experiment research program

2. Using high intensity unpolarised neutron beam and liquid hydrogen and deuterium targets to measure

c) the ratio $R_{dp} = [d\sigma/d\Omega(nd \rightarrow pnn)] / [d\sigma/d\Omega(np \rightarrow pn)]$ for elastic charge exchange process $np \rightarrow pn$ at 0° angle on deuterium and hydrogen targets with 5% statistical errors at the same energies as for i. 1.

Experimental observable R_{dp} is the ratio of a quasi-elastic nd scattering differential cross section to the free np elastic scattering one.

The values of R_{dp} can give one additional relation between spin-dependent NN -amplitudes and a set of such data allows to avoid one uncertainty of extraction of amplitudes real parts.

The data set on energy behaviors of spin-dependent observables $\Delta\sigma_{L,T}(np)$, $A_{00kk}(np)$, $A_{00nn}(np)$ and R_{dp} will be obtained for the first time over the energy range of neutron beam of 1.2–3.7 GeV.

Besides the direct amplitude reconstruction, this data set will be used to extend the NN phase shift analysis to higher energies and to verify the dynamical model predictions.

Accelerators and tools

- The **Synchrotron** and **Nuclotron VBLHE, JINR**.

Relativistic 1 – 5 GeV

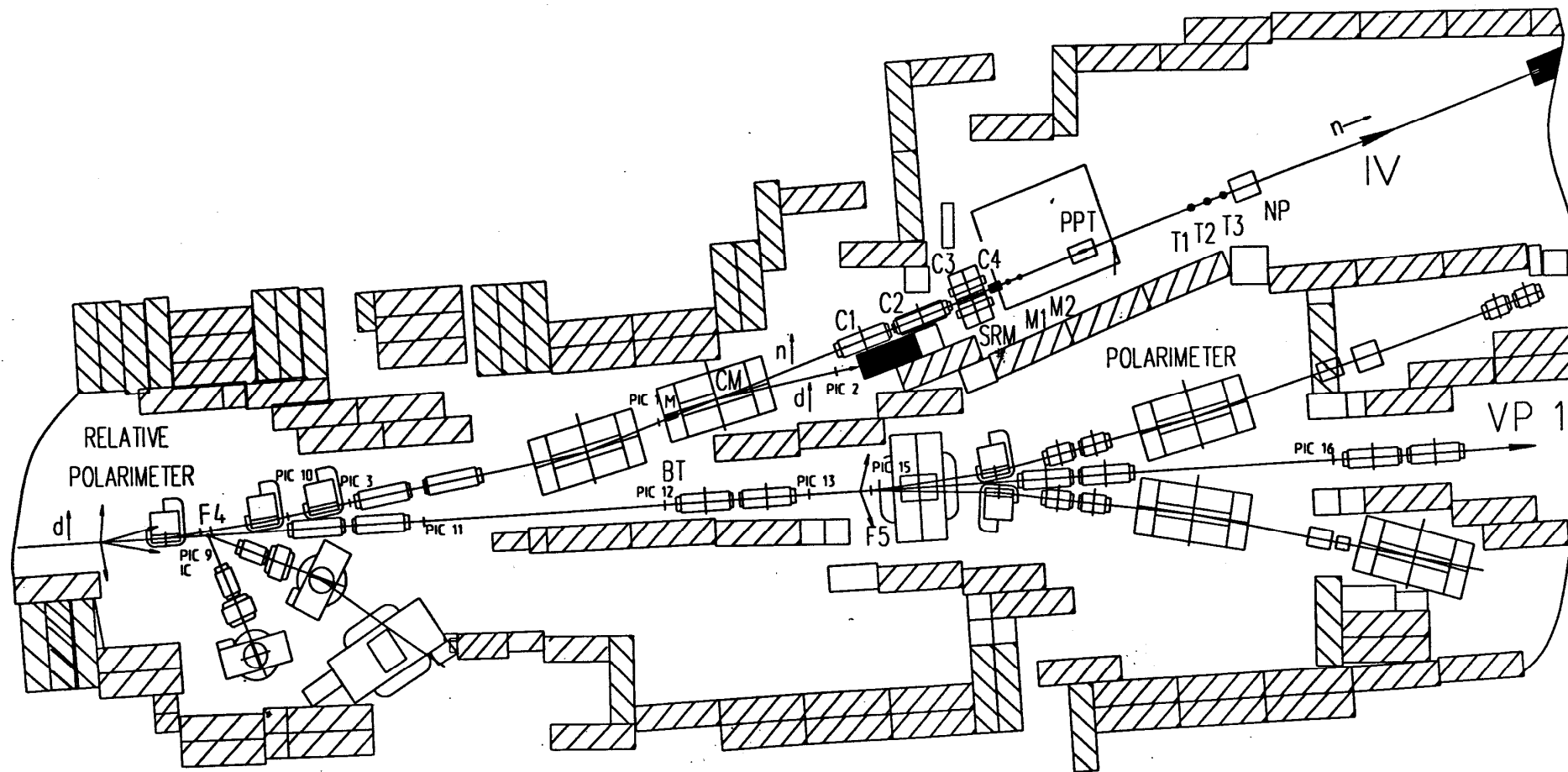
polarized neutron beams with average polarization value of **0.53**,
orientation of polarization **L** or **T** and
reversion of polarization direction from cycle to cycle;
unpolarized neutron beam with high intensity
(4×10^6 n/cycle at $T_n = 2$ GeV).

- **Large (140 cm³) polarized proton target** with polarization value of **0.7–0.8**.
- **Cryogenic hydrogen H₂ and deuterium D₂ targets (L = 30 cm)**.
- **“Delta-Sigma” set-up** with:
 - monitor and transmission neutron detectors;
 - magnetic spectrometer with proportional chambers;
 - detectors for target surrounding;
 - time-of-flight system;
 - adequate data acquisition system.

Accelerators and tools

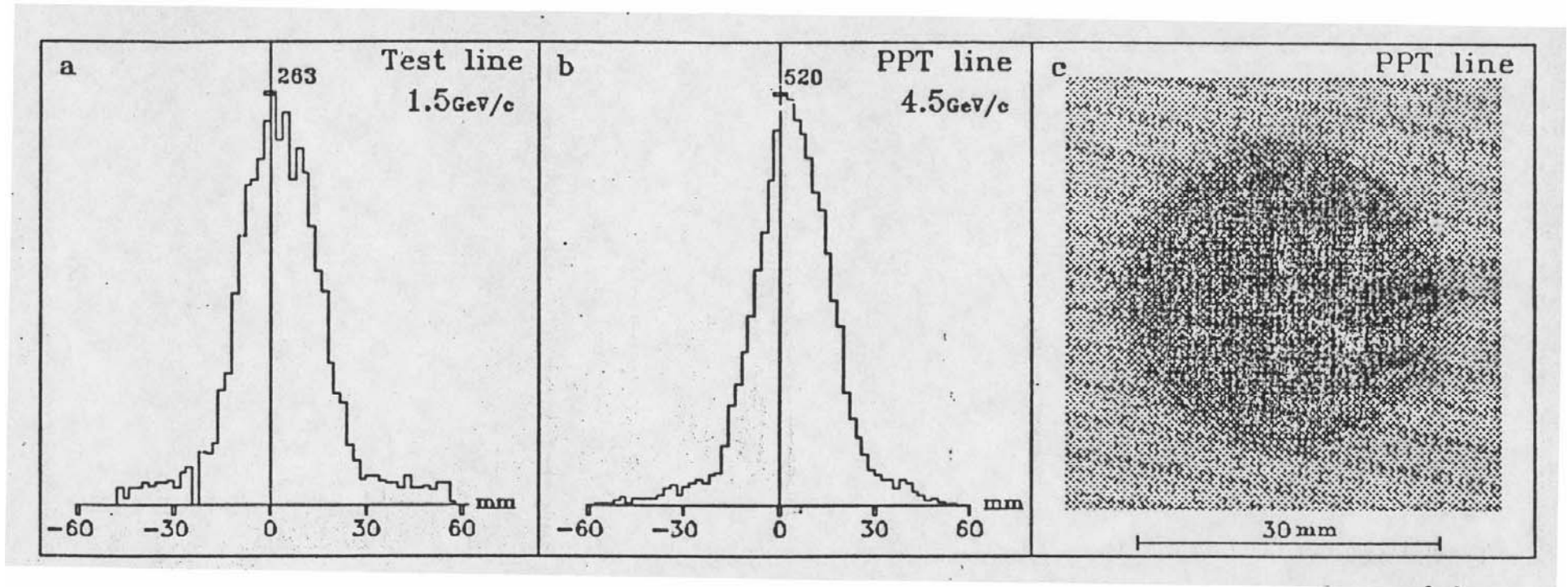
Polarized Beams and Targets at the Nuclotron

- The Nuclotron and Nuclotron-M VBLHEP, JINR.
 - Relativistic $1 - 6 \text{ GeV}/A$
 - ❖ polarized deuteron beam
 - with intensity $1 \times 10^8 \text{ d/cycle}$ from ion source POLARIS (Nuclotron)
 - expected in near future $1 \times 10^{10} \text{ d/cycle}$ using new polarized deuteron ions source (Nuclotron-M).
 - ❖ polarized neutron beams with
 - average polarization value of 0.53 ,
 - orientation of polarization L or T and
 - reversion of polarization direction cycle by cycle;
 - neutron beam intensity $4 \times 10^6 \text{ n/cycle}$ at $T_n = 2 \text{ GeV}$
 - using new polarized deuteron ions source.
- Large (140 cm^3) polarized proton target
 - with polarization value of $0.7-0.8$.
- Cryogenic hydrogen H_2 and deuterium D_2 targets ($L = 34 \text{ cm}$).



DELTA-SIGMA Setup at the Polarized Neutron Beams of the JINR VBLHE

VP 1 – beam line of polarized deuterons; **1V** – beam line of polarized neutrons;
BT – beryllium neutron production target; **IC** – ionization chamber;
PIC 1-3, 9-16 – multiwire proportional/ionization chambers; **CM** – sweeping magnet;
C1-C4 – set of neutron beam collimators; **SRM** – neutron spin rotating magnet;
PPT – polarized proton target; **NP** – neutron profilometer



- The beam of free quasi-monochromatic neutrons is obtained by break-up at 0° of deuterons in the Beryllium target BT ($20 \text{ cm} \times 8 \times 8 \text{ cm}^2$).
- Neutron beam is formed by a set of collimators C1–C4.
- The deuteron beam momentum P_d is known with accuracy of $\sim 1\%$.
- The neutron beam has the momentum $P_n = P_d / 2$ with a gaussian momentum spread of FWHM $\sim 5\%$.
- Intensity of prepared neutron beam at $T_n = 2.0 \text{ GeV}$ was $\sim 4 \cdot 10^6 \text{ n/cycle}$.



SPIN-Praha-2008

V. Sharov

Accelerators and tools

□ **“Delta-Sigma” set-up**

with:

- **monitor and transmission neutron detectors;**
- **magnetic spectrometer with proportional chambers;**
- **detectors for target surrounding;**
- **time-of-flight system;**
- **adequate data acquisition system.**

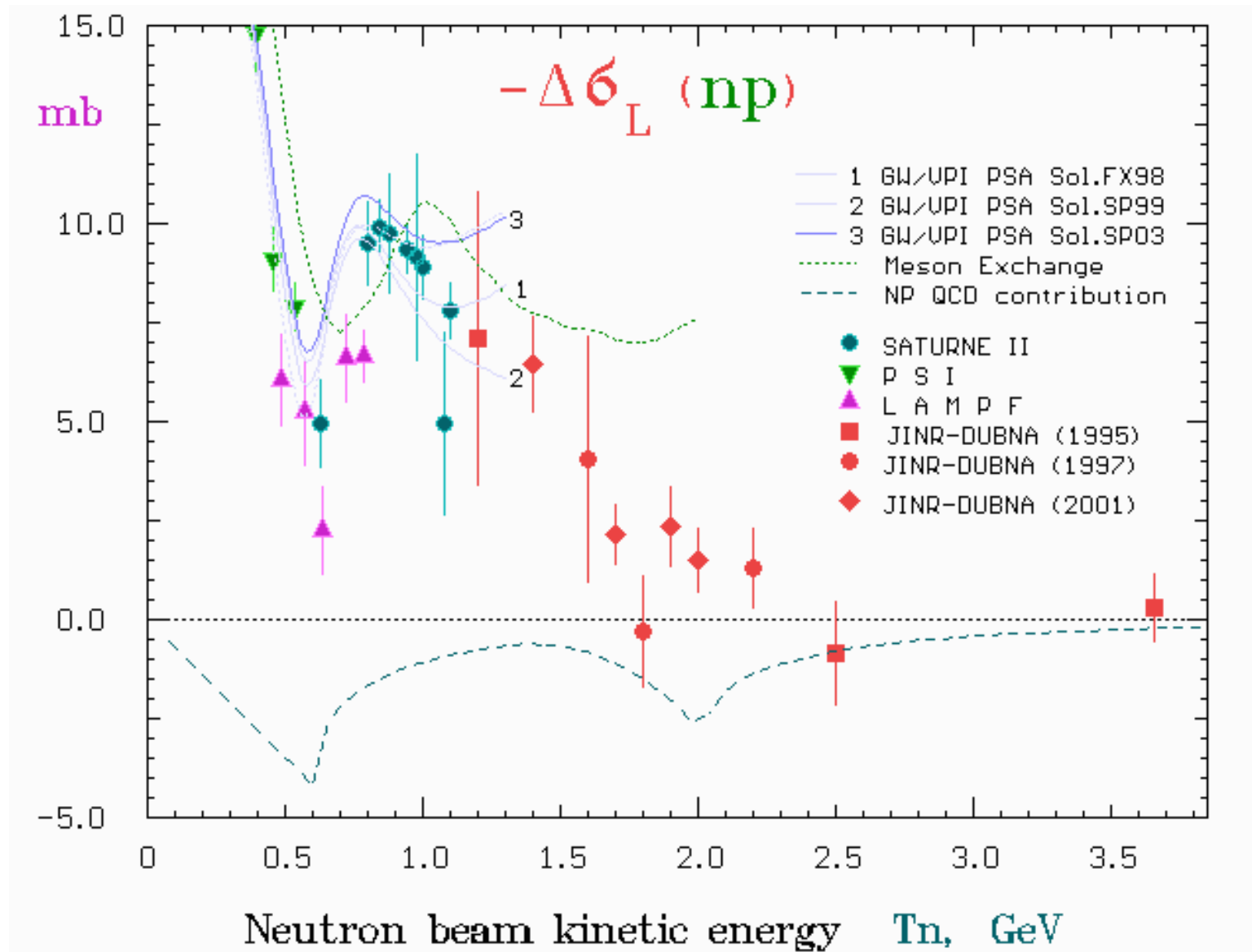
Measurements of the $-\Delta\sigma_L$ (np) energy dependence were in the main completed using L-polarized neutron beam at the **Synchrotron** facility and the Dubna L-polarized proton target .

Results were published in:

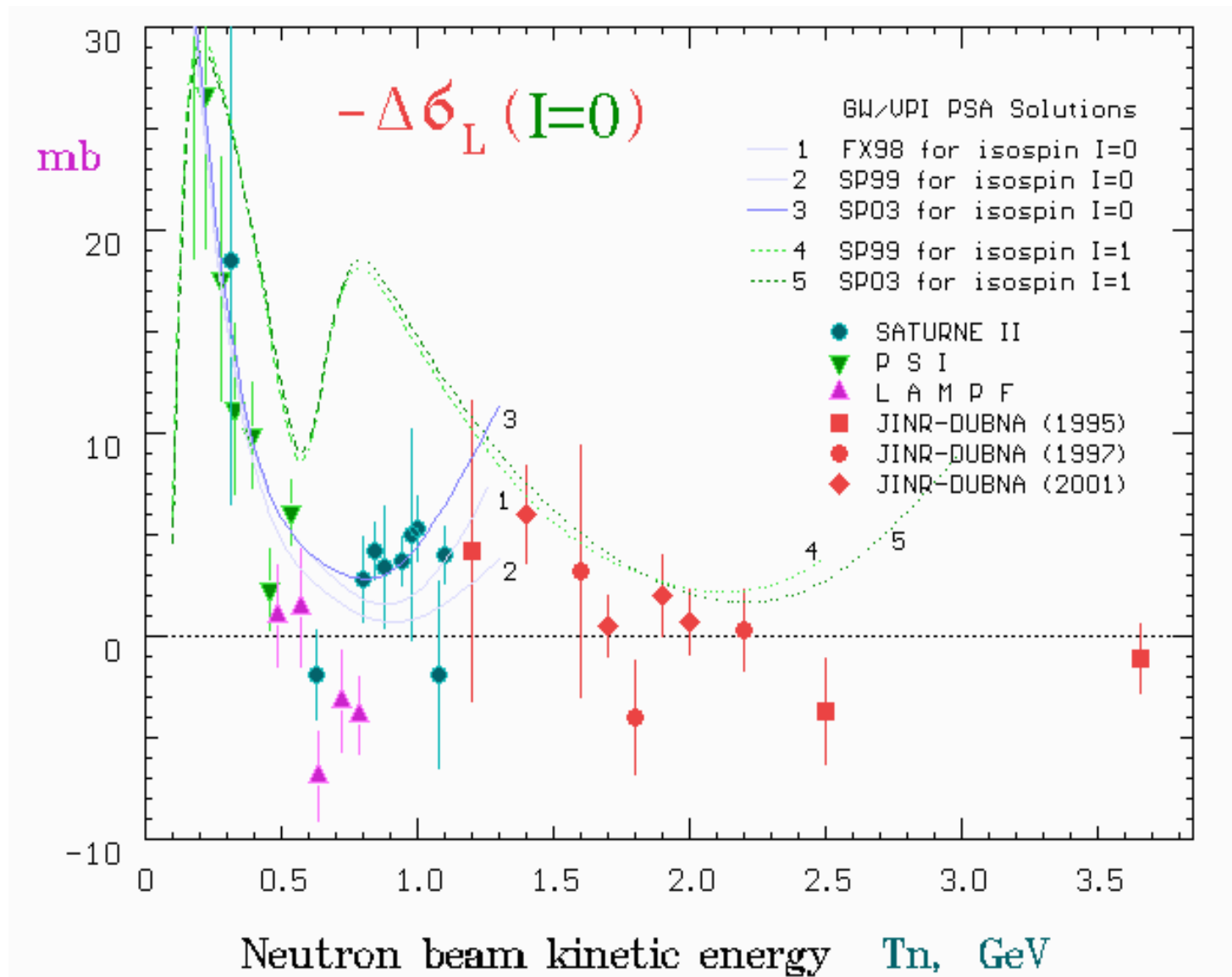
References on $-\Delta\sigma_L$ (np) results

1. B.P.Adiasevich, V.G.Antonenko, S.A.Averichev, L.S.Azhgirey et al.
Zeitschrift fur Physik C71 (1996) 65.
2. V.I.Sharov, S.A.Zaporozhets, B.P.Adiasevich, V.G.Antonenko et al.
JINR Rapid Communications 3[77]-96 (1996) 13.
3. V.I.Sharov, S.A.Zaporozhets, B.P.Adiasevich, N.G.Anischenko et al.
JINR Rapid Communications 4[96]-99 (1999) 5.
4. V.I.Sharov, S.A.Zaporozhets, B.P.Adiasevich, N.G.Anischenko et al.
European Physical Journal C13 (2000) 255.
5. V.I.Sharov, N.G.Anischenko, V.G.Antonenko, S.A.Averichev et al.
European Physical Journal C37 (2004) 79-90.
6. V.I.Sharov, N.G.Anischenko, V.G.Antonenko, S.A.Averichev et al.
Yadernaya Fizika v.68, №11 (2005) 1858-1873.
Physics of Atomic Nuclei v.68, №11 (2005) 1796-1811.

Energy Dependence of the $-\Delta\sigma_L$ (np) Observable Obtained with Free Neutron Polarized Beams

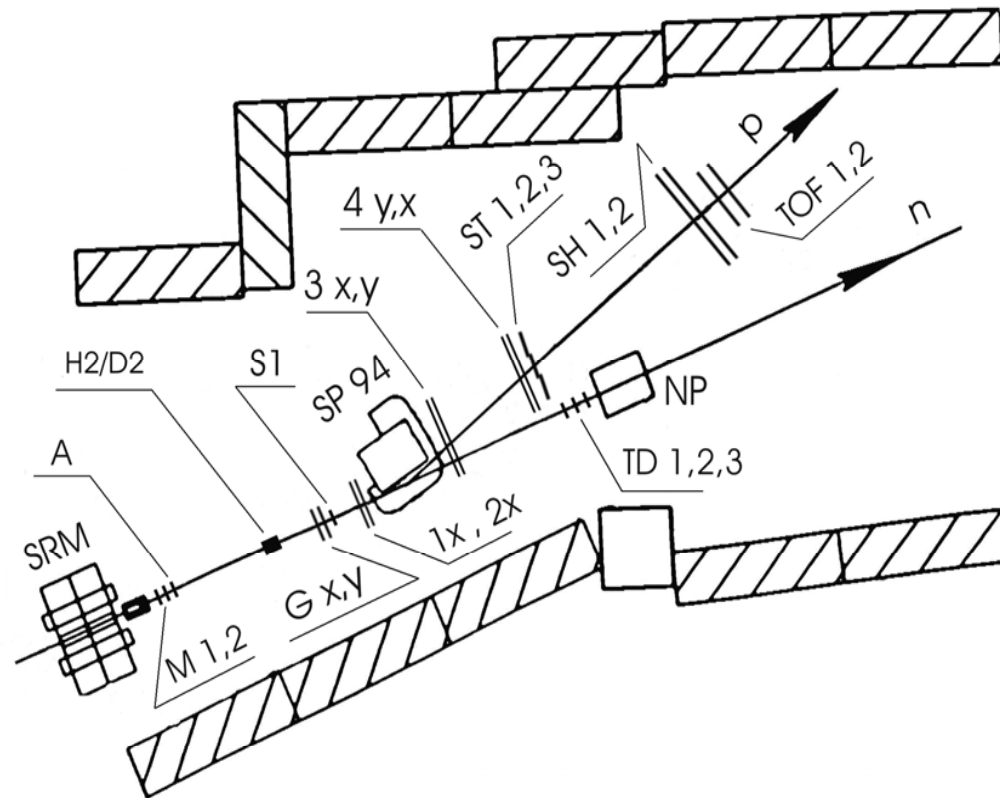


Energy Dependence of the $-\Delta\sigma_L (I=0)$



Measurements of the $\Delta\sigma_{L,T}(np)$ and $A_{00kk}(np)$ and $A_{00nn}(np)$ energy dependences using L and T orientations of beam and target polarizations will be possible in the near future when the new high intensity source of polarized deuterons will be put in operation at the Nuclotron and when the T mode of target polarization will be ready.

During the last period, in frame of the project experimental program, the studies of elastic $np \rightarrow pn$ charge exchange process were carried out using high intensity unpolarized neutron beams and cryogenic H_2 and D_2 targets ($l=34$ cm). The results of these measurements will be presented below.



Spectrometer of the “Delta-Sigma” set-up

- The magnetic spectrometer consist of the analyzing dipole **SP94**, two sets of multiwire proportional chambers **PCs**: **Gx, Gy, 1x, 2x** before and **PCs**: **3x, 3y, 4x, 4y** after **SP94** for momentum analysis of detected secondaries;
- Time-of flight system **S1, TOF1,2** for particle identification;
- Liquid **H₂ / D₂** or solid **CH₂ / CD₂** targets inserted in the neutron beam line instead of the **PPT** and surrounded by a device **DTS** for detecting charged recoils and gammas;
- Trigger counters **A, S1, ST1,2,3**.

Systematical errors.

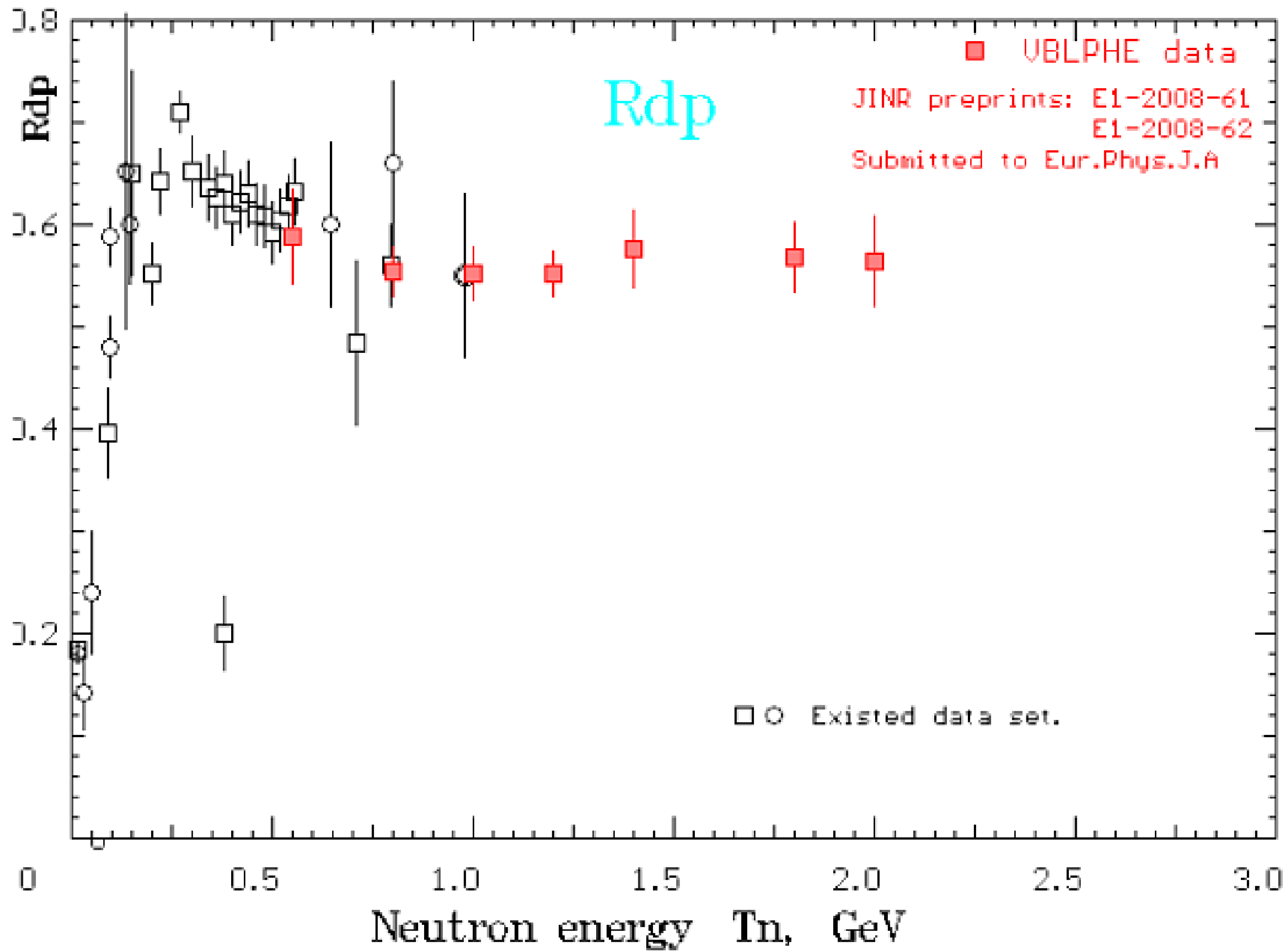
Estimations for data at $T_n = 1.4$ GeV.

Sources of systematic error	Absolute values of the Rdp error
1. Total PC efficiency	0.0027
2. Trigger PC efficiency	0.0026
3. Efficiency of the DTS	0.0179
4. Efficiency of TOF	0.0034
5. Error in shift determination of the H2 and D2 elastic peak center positions	0.0177
6. Number of H/D nuclei in the targets	0.0014
Total:	0.0257

Values of $R_{dp} = d\sigma/d\Omega (nd) / d\sigma/d\Omega (np)$.

Total errors are the quadratic sums of statistical and systematic uncertainties.

NN	Tn,	Pn,	R_{dp}	Errors		
	GeV	GeV/c		Stat.	Syst.	Total
1	0.550	1.1559	0.589	0.024	0.039	0.046
2	0.800	1.4640	0.554	0.017	0.016	0.023
3	1.000	1.6968	0.553	0.011	0.023	0.026
4	1.200	1.9222	0.551	0.011	0.019	0.022
5	1.400	2.1426	0.576	0.028	0.026	0.038
6	1.800	2.5734	0.568	0.016	0.029	0.033
7	2.000	2.7854	0.564	0.014	0.042	0.045



Nucleon-Nucleon Formalism

Throughout the project and results publications we used the NN formalism and notations for elastic nucleon-nucleon scattering observables from

Bystricky J., Lehar F., Winternitz P. J. Phys. (Paris). 1978. v.39. p. 1.

Assuming parity conservation, time-reversal invariance, the Pauli principle, and isospin invariance, the nucleon-nucleon scattering matrix can be written in term of only **five invariant amplitudes**

$M(\mathbf{k}', \mathbf{k}) =$

$$\frac{1}{2} [(a+b) + (a-b)(\boldsymbol{\sigma}_1, \mathbf{n})(\boldsymbol{\sigma}_2, \mathbf{n}) + (c+d)(\boldsymbol{\sigma}_1, \mathbf{m})(\boldsymbol{\sigma}_2, \mathbf{m}) + (c-d)(\boldsymbol{\sigma}_1, \mathbf{l})(\boldsymbol{\sigma}_2, \mathbf{l}) + e(\boldsymbol{\sigma}_1 + \boldsymbol{\sigma}_2, \mathbf{n})], \quad (1)$$

where $\boldsymbol{\sigma}_1$ and $\boldsymbol{\sigma}_2$ are the Pauli 2x2 matrices acting on the first and second nucleon wave functions, and \mathbf{k} and \mathbf{k}' are unit vectors in the direction of the incident and scattered particles, respectively. The invariant amplitudes a , b , c , d and e are complex functions of two variables, e. g., the center of mass (c. m.) energy k and scattering angle θ .

In the forward direction at $\theta=0$, total angular momentum conservation implies that $e=0$ and $a-b=c+d$. Similarly at 180° one obtains $e=0$ and $a-b=c-d$.

The center of mass basis vectors are given by

$$\mathbf{l} = (\mathbf{k}' + \mathbf{k}) / (|\mathbf{k}' + \mathbf{k}|), \quad \mathbf{m} = (\mathbf{k}' - \mathbf{k}) / (|\mathbf{k}' - \mathbf{k}|), \quad \mathbf{n} = (\mathbf{k}' \times \mathbf{k}) / (|\mathbf{k}' \times \mathbf{k}|). \quad (2)$$

For the pp , nn , and np interactions, the scattering matrix can be written in term of two matrices M_0 and M_1 having the same form as Eq. (1)

$$\mathbf{M}(\mathbf{k}', \mathbf{k}) = \frac{1}{4} \mathbf{M}_0 [1 - (\tau_1, \tau_2)] + \frac{1}{4} \mathbf{M}_1 [3 + (\tau_1, \tau_2)], \quad (3)$$

where τ_1 and τ_2 are isosinglet and isotriplet scattering matrices. Ignoring electromagnetic interaction, one can write

$$\mathbf{M}(pp \rightarrow pp) = \mathbf{M}(nn \rightarrow nn) = \mathbf{M}_1, \quad (4a)$$

$$\mathbf{M}(np \rightarrow np) = \mathbf{M}(pn \rightarrow pn) = \frac{1}{2} (\mathbf{M}_1 + \mathbf{M}_0), \quad (4b)$$

$$\mathbf{M}(np \rightarrow pn) = \mathbf{M}(pn \rightarrow np) = \frac{1}{2} (\mathbf{M}_1 - \mathbf{M}_0). \quad (4c)$$

This formalism uses a four-subscript notation X_{srbt} for experimental quantities. Subscripts s , r , b , and t refer to the polarization components of the scattered, recoil, beam, and target particles, respectively.

For any c. m. observable X_{pqik} , the following expression holds

$$d\sigma/d\Omega X_{pqik} = \frac{1}{4} \text{Tr} (\sigma_{1p} \sigma_{2q} \mathbf{M} \sigma_{1i} \sigma_{2k} \mathbf{M}^+), \quad (5)$$

where

$$d\sigma/d\Omega = I_{0000} = \frac{1}{4} \text{Tr} (\mathbf{M} \mathbf{M}^+), \quad (6)$$

is the unpolarized differential cross section.

Experimental observable

$$R_{dp} = d\sigma/d\Omega(nd \rightarrow pnn) / d\sigma/d\Omega(np \rightarrow pn) \quad (7)$$

is the ratio of a quasi-elastic **nd** charge-exchange process yield to the free elastic **np** one.

In frame of impulse approximation following by

L.I. Lapidus, J. Exp. Theor. Phys. 32, 1957, 1437,

N.W. Dean, Phys. Rev. D 5, 1972, 1661; 2832,

the differential cross section $d\sigma/d\Omega(nd \rightarrow pnn)$ at $t \rightarrow 0$ can be expressed

$$d\sigma/d\Omega(nd) = (2/3) \cdot d\sigma/d\Omega^{SD}(np), \quad (8)$$

where $d\sigma/d\Omega^{SD}(np)$ is the “spin-dependent” part of the $np \rightarrow np$ differential cross section.

This gives

$$R_{dp} = (2/3) \cdot d\sigma/d\Omega^{SD}(np) / d\sigma/d\Omega(np). \quad (9)$$

Using the invariant NN amplitudes formalism

J. Bystricky, F. Lehar, P. Winternitz, J. Phys. (Paris). 1978. v.39. p. 1,

the $R_{dp}(0, \pi)$ can be expressed via invariant NN amplitudes as

(F. Lehar. Private communication)

$$R_{dp}(0, \pi) = (2/3) \cdot [0.25 \cdot |a - b|^2 + 0.5 \cdot (|c|^2 + |d|^2)] / 0.5 \cdot (|a|^2 + |b|^2 + |c|^2 + |d|^2). \quad (10)$$

The values of R_{dp} can give one additional relation between spin-dependent NN-amplitudes and a set of such data allows to avoid one uncertainty of extraction of amplitudes real parts.

Estimations of the R_{dp} values were performed by formula (10) using the invariant amplitudes data sets for the elastic $np \rightarrow np$ and $pp \rightarrow pp$ scattering at $\theta_{CM} = \pi$.

The amplitudes data sets were received from I.I. Strakovsky for the GW/VPI phase-shift analysis (PSA) solutions: SM97

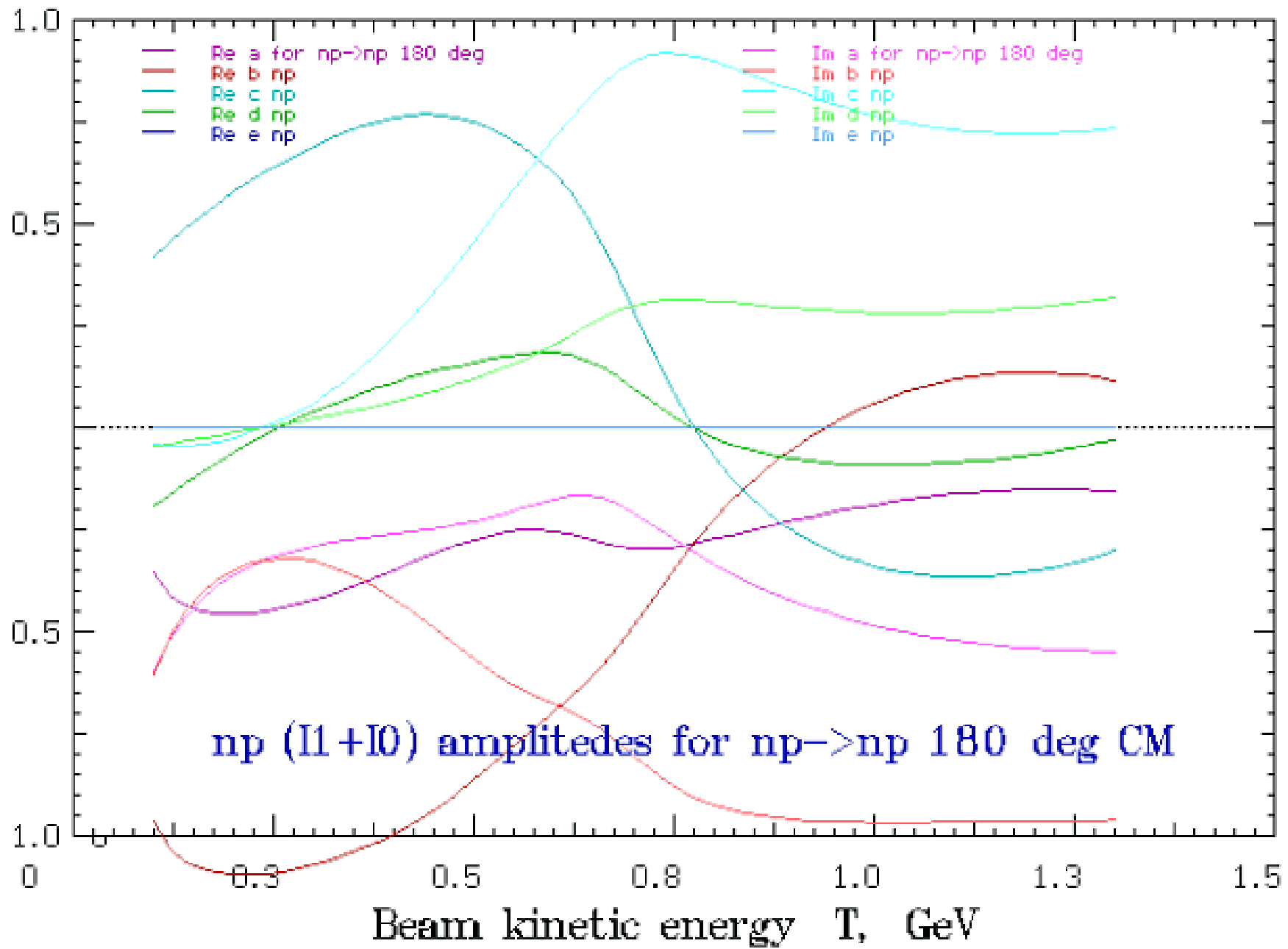
R.A.Arndt, C.H.Oh, I.I.Strakovsky, R.L.Workman, and F.Dohrmann, “Nucleon-nucleon elastic scattering analysis to 2.5 GeV”, *Phys. Rev. C* 56, 3005 (1997) [nucl-th/9706003].

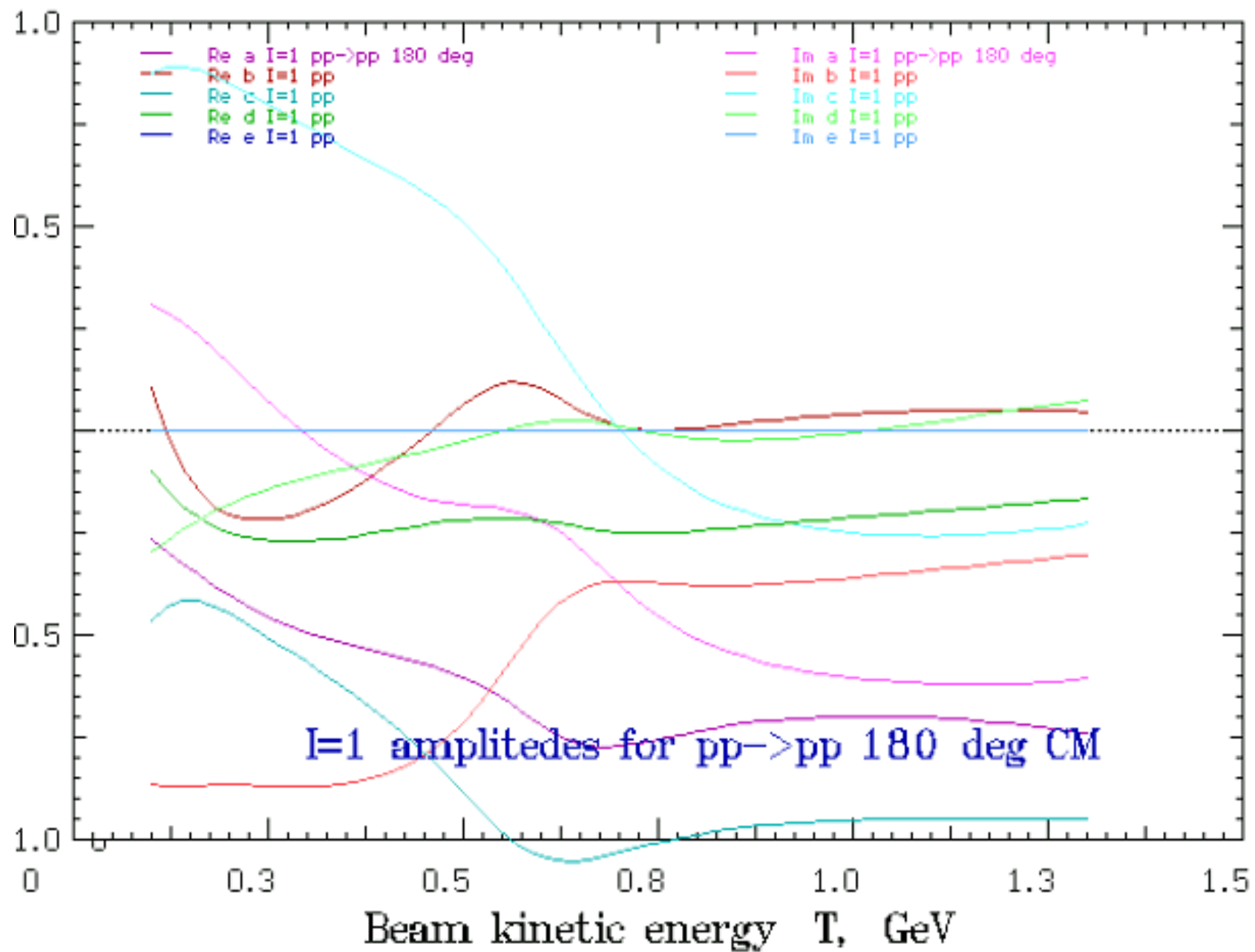
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R.A.Arndt, I.I.Strakovsky, and R.L.Workman, “Nucleon-nucleon elastic scattering to 3 GeV”, *Phys. Rev. C* 62, 034005 (2000) [nucl-th/0004039].

SP07

R.A.Arndt, W.J.Briscoe, I.I.Strakovsky, and R.L.Workman, “Updated analysis of NN elastic scattering to 3 GeV”, *Phys. Rev. C* 76, 025209 (2007); arXiv:0706.2195 [nucl-th].





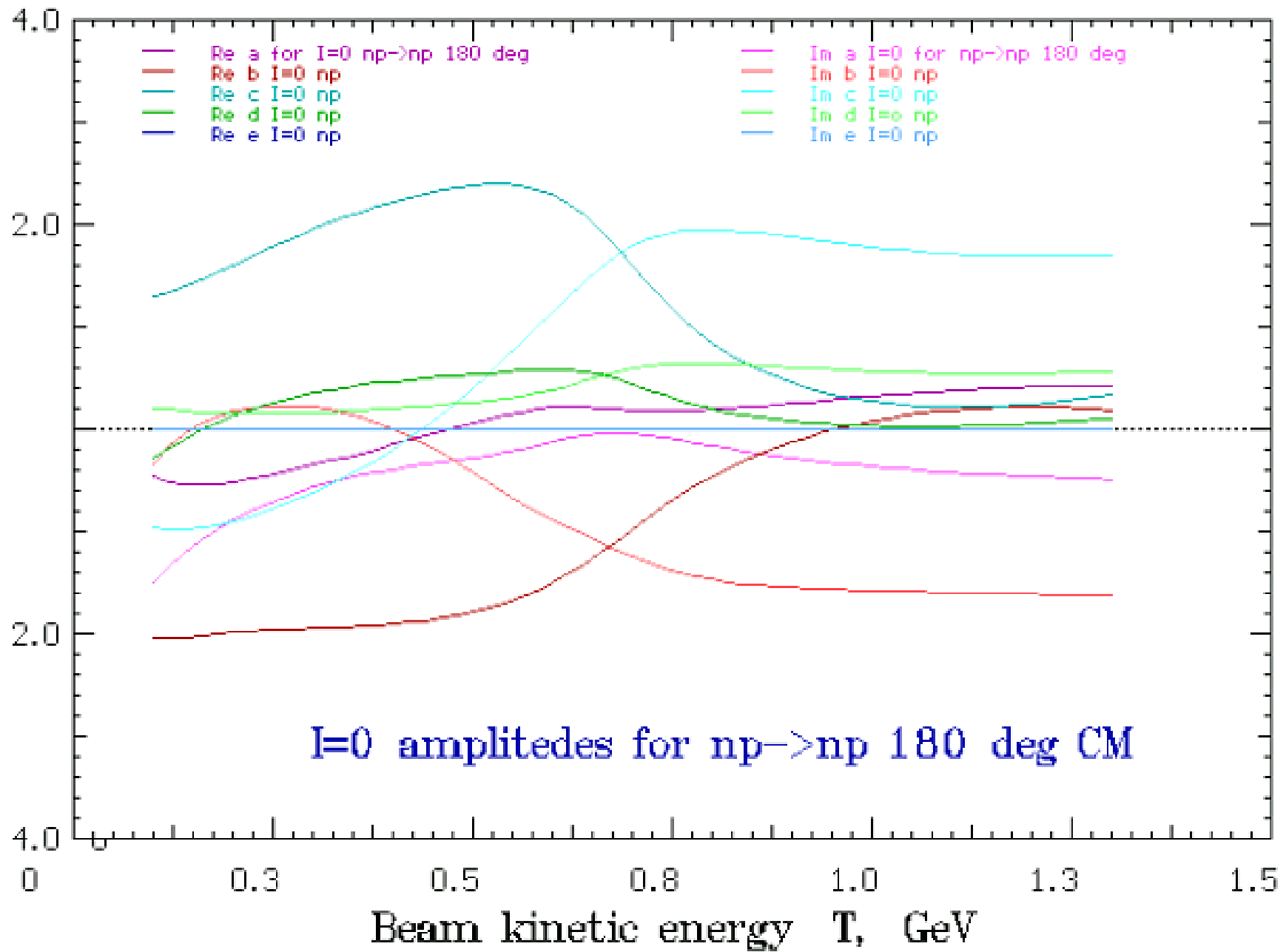
The amplitudes $np \rightarrow np$ are the mixture of pure isospin $l=1$ and $l=0$ states amplitudes according Eq. (4b)

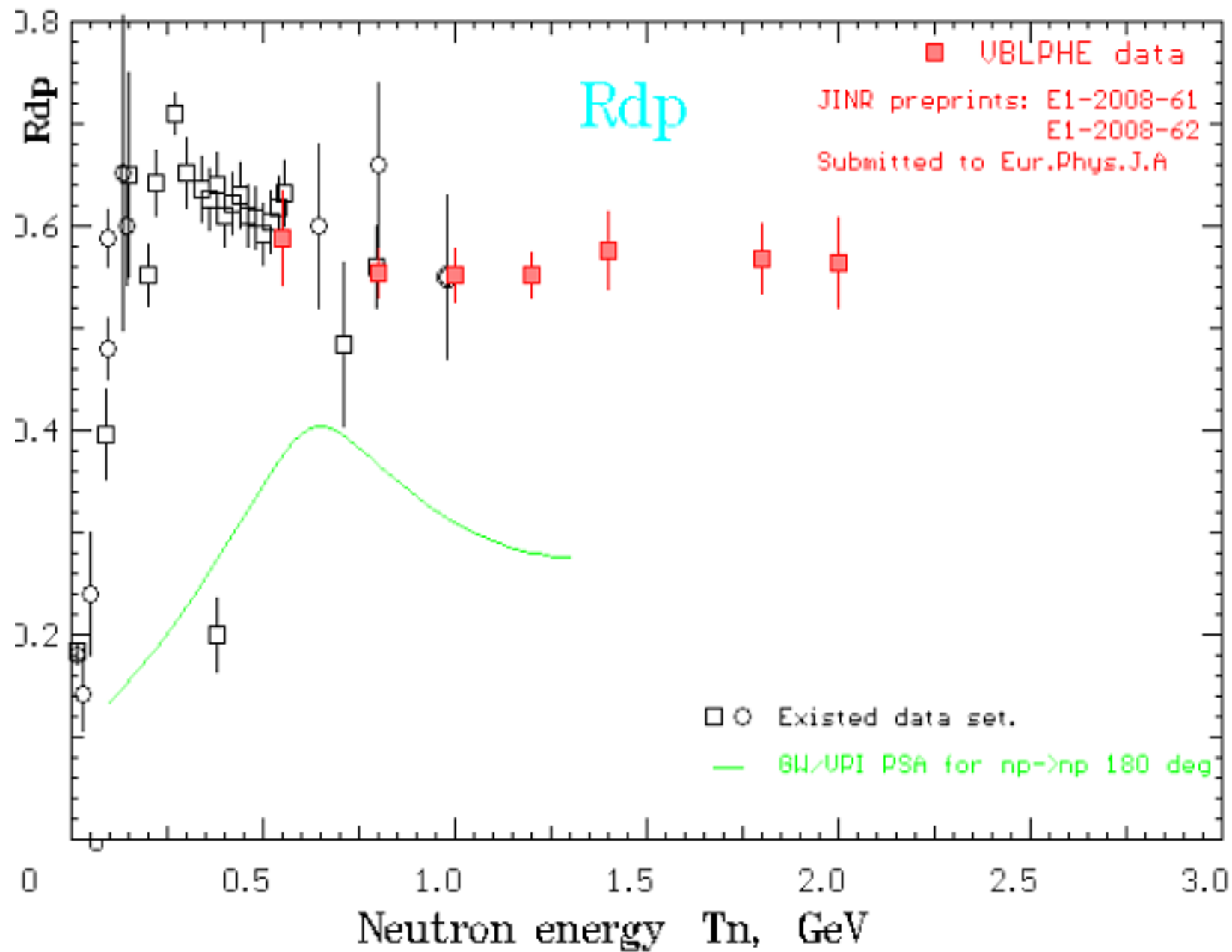
$$\text{Amp}(np) = \frac{1}{2} (\text{Amp}(l=1(pp)) + \text{Amp}(l=0)) \quad (11)$$

and $\text{Amp}(l=0) = 2 \text{Amp}(np) - \text{Amp}(l=1(pp))$. (12)

Using existed $\text{Amp}(np)$ and $\text{Amp}(l=1(pp))$ sets one can obtained the $\text{Amp}(l=0)$ set by Eq. (12).

The R_{dp} values for the elastic $np \rightarrow np$ scattering at $\theta_{CM} = \pi$ one can obtained by Eq. (10) using either $\text{Amp}(np)$ set or $\frac{1}{2} (\text{Amp}(l=1) + \text{Amp}(l=0))$ one.



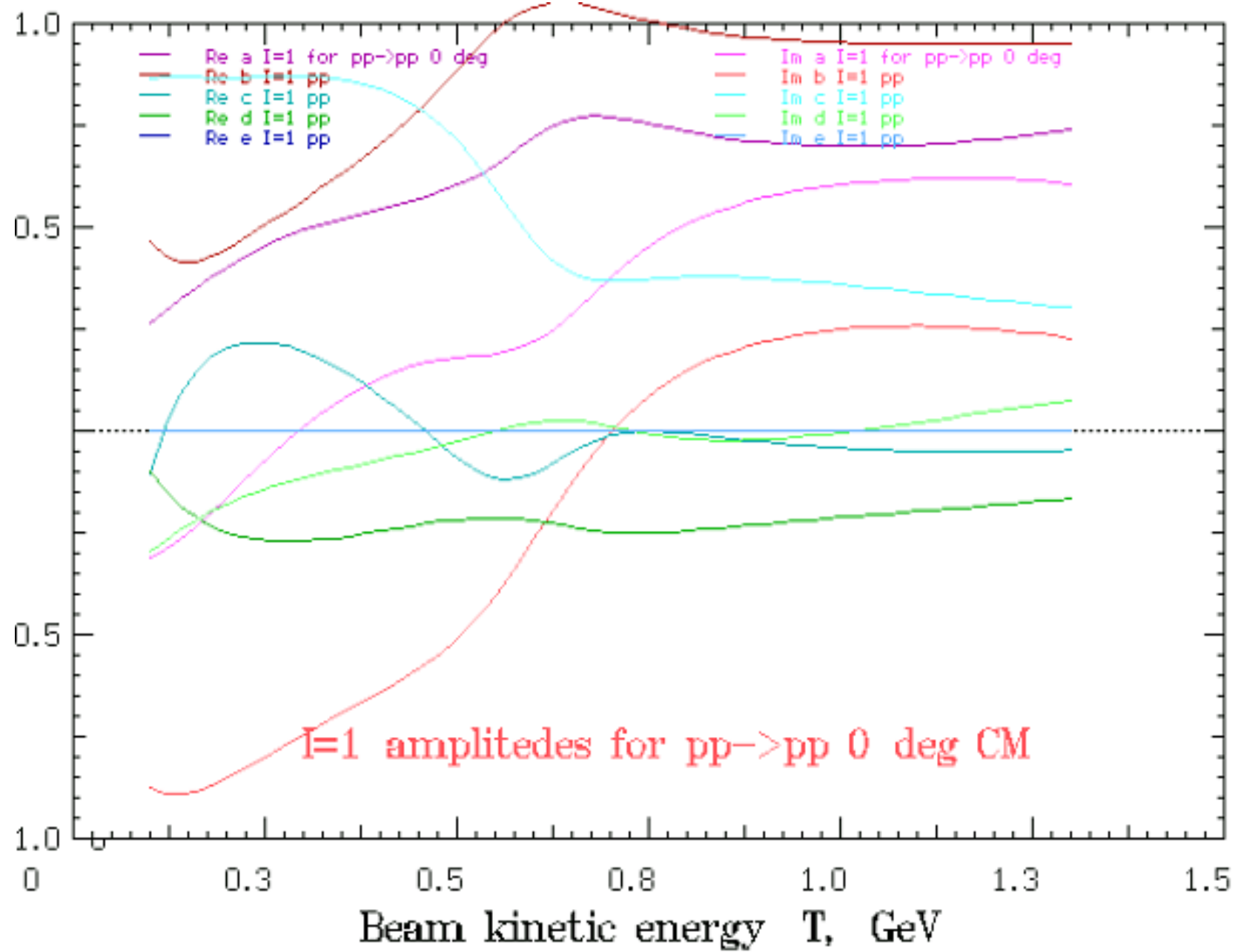


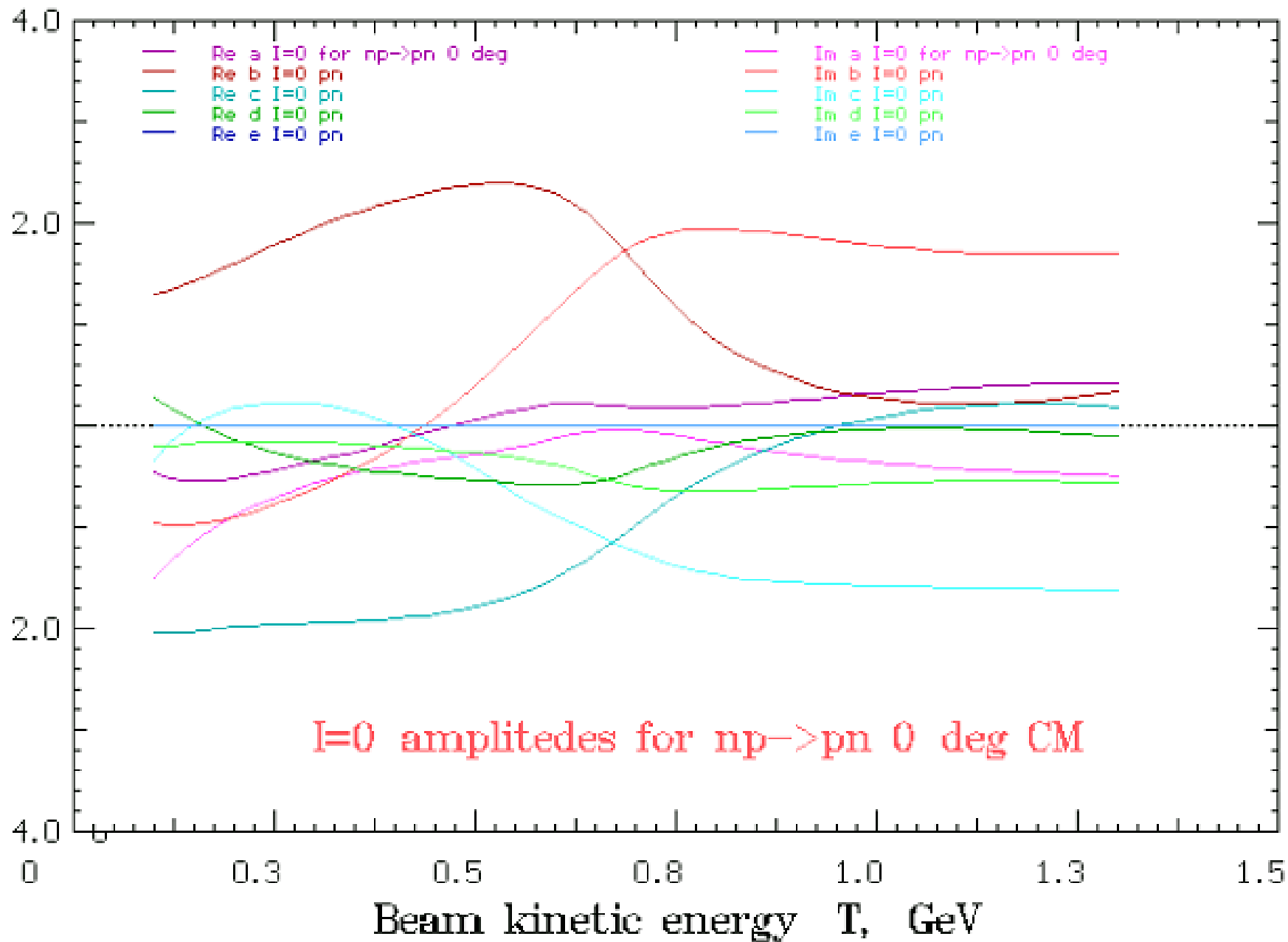
To obtain the R_{dp} values for the elastic $np \rightarrow pn$ charge exchange at $\theta_{CM} = 0$ one needs to perform the $k' \rightarrow -k'$ and $n \rightarrow p$ transformations of the **Amp (l=1)** and **Amp (l=0)** sets according to Table 1.

(J. Bystricky, F. Lehar, P. Winternitz, J. Phys. (Paris). 1978. v.39. p. 1)

Table 1. Symmetry properties of the NN invariant amplitudes.

l=0 amplitudes	l=1 amplitudes
$a_0(\theta) = + a_0(\pi - \theta)$	$a_1(\theta) = - a_1(\pi - \theta)$
$b_0(\theta) = + c_0(\pi - \theta)$	$b_1(\theta) = - c_1(\pi - \theta)$
$c_0(\theta) = + b_0(\pi - \theta)$	$c_1(\theta) = - b_1(\pi - \theta)$
$d_0(\theta) = - d_0(\pi - \theta)$	$d_1(\theta) = + d_1(\pi - \theta)$
$e_0(\theta) = - e_0(\pi - \theta)$	$e_1(\theta) = + e_1(\pi - \theta)$





The scattering matrix simplifies at the forward $\theta_{CM} = 0$ and backward $\theta_{CM} = \pi$ angles.

The amplitudes at these angles satisfy

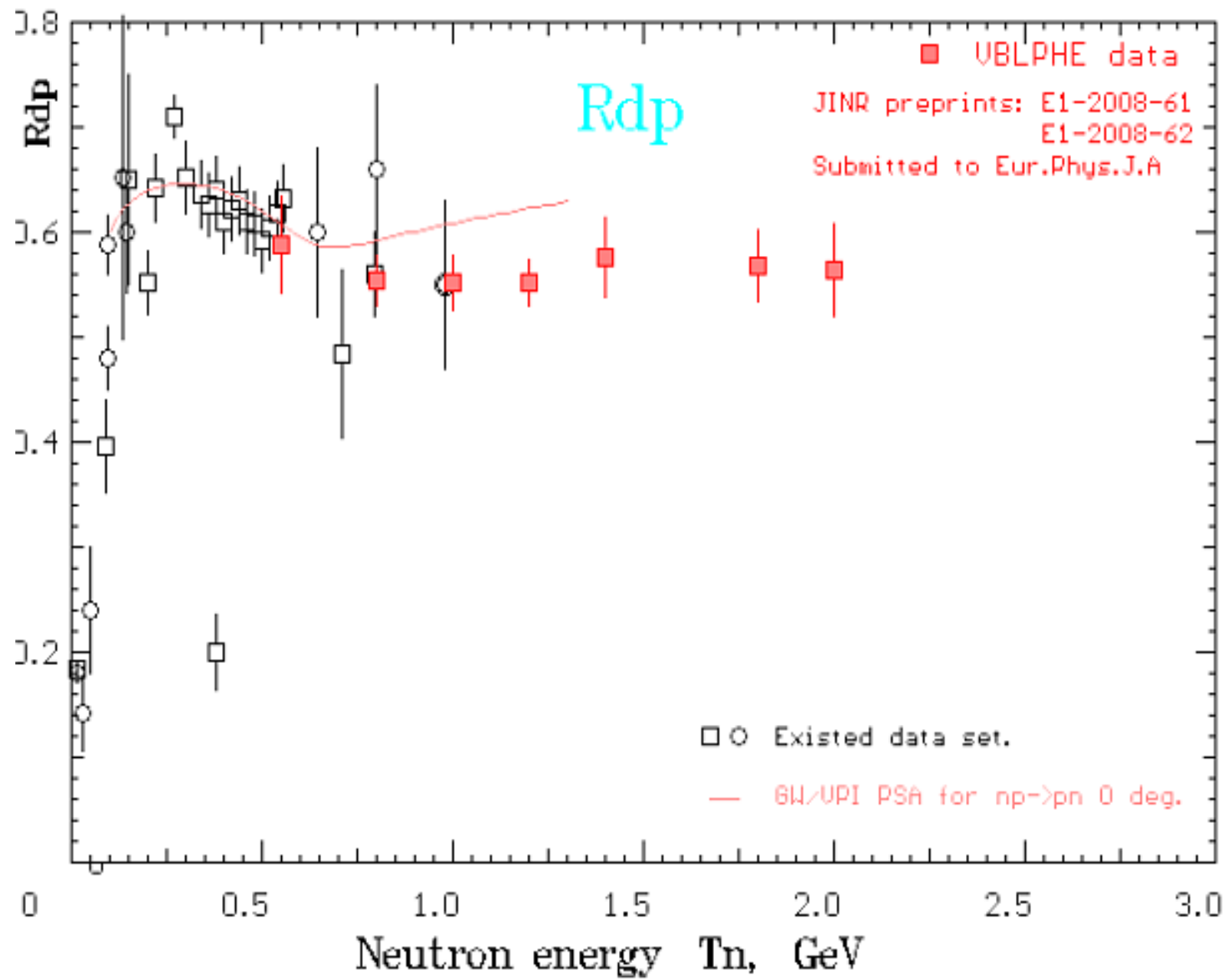
$$\begin{aligned} a(0) - b(0) &= c(0) + d(0), & e(0) &= 0, \\ a(\pi) - b(\pi) &= c(\pi) - d(\pi), & e(\pi) &= 0. \end{aligned}$$

The $np \rightarrow np$ elastic scattering and $np \rightarrow pn$ charge exchange differential cross sections are given by

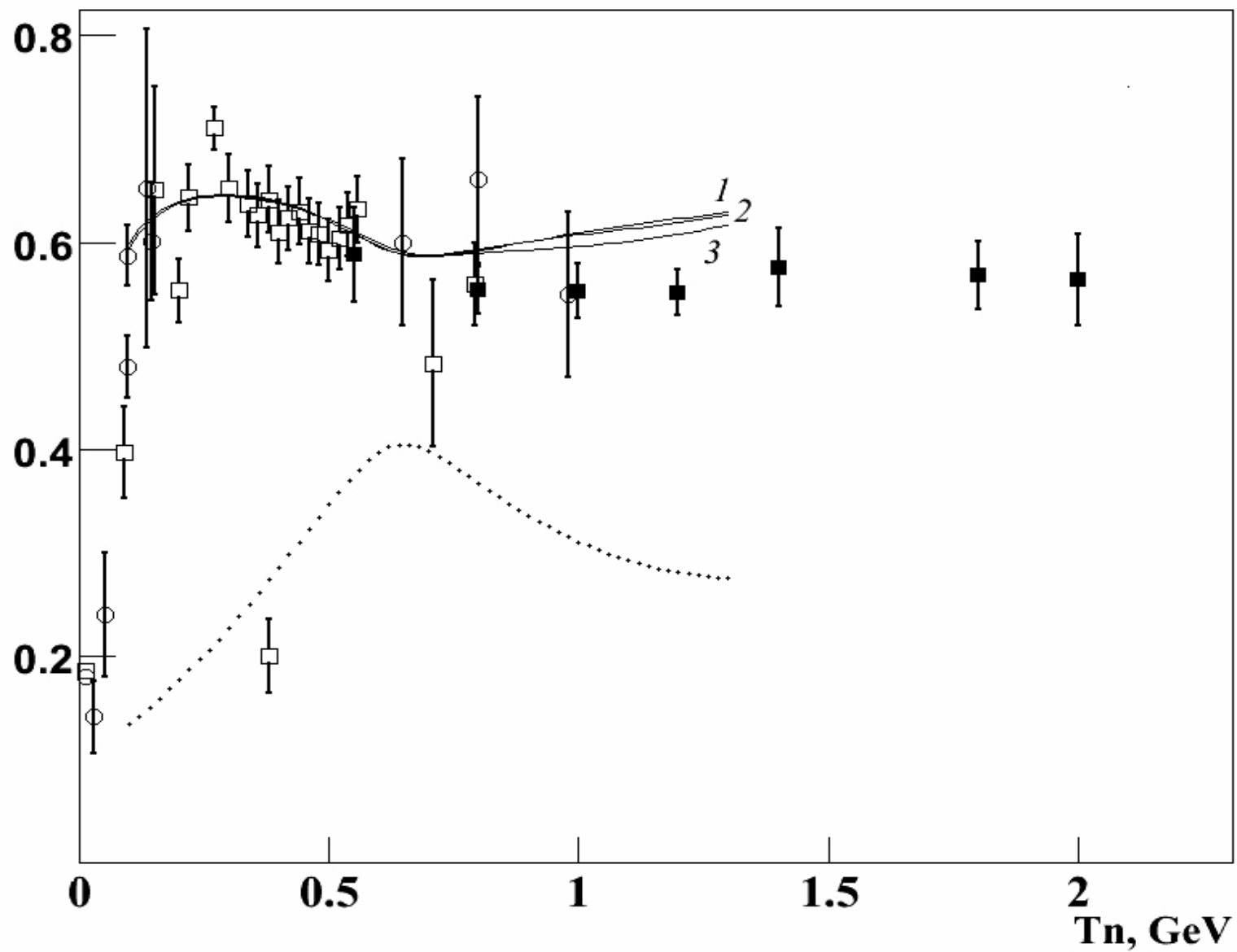
$$d\sigma/d\Omega = \frac{1}{2} (|a|^2 + |b|^2 + |c|^2 + |d|^2 + |e|^2)$$

and equal each other.

The R_{dp} values for the elastic $np \rightarrow pn$ charge exchange at $\theta_{CM} = 0$ one can obtain by Eq. (10) using $\frac{1}{2} (\text{Amp } (l=1) - \text{Amp } (l=0))$ set of the transformed **NN** amplitudes.



$$R_{dp} = (d\sigma/d\Omega)(nd) / (d\sigma/d\Omega)(np)$$



Conclusions

1. **New results** at $\theta_{CM} = 0$ for $R_{dp} = d\sigma/d\Omega(nd) / d\sigma/d\Omega(np)$ – the ratio of a quasi-elastic $nd \rightarrow pnn$ charge exchange yield to the free elastic $np \rightarrow pn$ one at **0.55, 0.8, 1.0, 1.2, 1.4, 1.8** and **2.0 GeV** are presented.
2. Estimations of the R_{dp} values by formula (10) using the invariant amplitudes data sets for the elastic $np \rightarrow np$ and $pp \rightarrow pp$ scattering at $\theta_{CM} = \pi$ were performed.
3. Calculated R_{dp} values with the set of invariant amplitudes data for the elastic $np \rightarrow np$ scattering at $\theta_{CM} = \pi$ disagree with experimental data.
4. Calculated R_{dp} values with the set of invariant amplitudes data for the elastic $np \rightarrow pn$ charge exchange at $\theta_{CM} = 0$ agree with experimental data.
5. It is confirmed that the $nd \rightarrow pnn$ process yield caused by the spin-dependent part of the elastic $np \rightarrow pn$ charge exchange process at $\theta_{CM} = 0$.
6. It is shown that the Eq. (10) gives one additional relation between spin-dependent **NN**-amplitudes and obtained experimental R_{dp} results **can be used** to avoid one uncertainty of extraction of amplitudes real parts.
7. The R_{dp} measurements at the energies above 2 GeV are planned to continue.