Transverse Single Spin Asymmetries in hard scattering processes

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based on collaboration with

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- Motivations: experimental evidence of SSAs. From $p^{\uparrow}p \rightarrow hX$ to $\ell p^{\uparrow} \rightarrow \ell' hX$
- Theoretical approaches to SSAs:
- Transverse Moment Dependent approach vs. Higher-Twist formalism
- TMD approach in a parton model and in QCD
- TMD functions and their role in azimuthal and SSAs: Phenomenology
- Extraction of Sivers, Collins and transversity functions
- SSAs: From SIDIS to pp collisions
- Conclusions and outlook

SSAs: QCD expectations vs. data

SSAs in pQCD

Kane, Pumplin, Repko 1978

$$\hat{a}_N = \frac{d\hat{\sigma}^{a^{\uparrow}b \to cd} - d\hat{\sigma}^{a^{\downarrow}b \to cd}}{d\hat{\sigma}^{a^{\uparrow}b \to cd} + d\hat{\sigma}^{a^{\downarrow}b \to cd}} \sim \operatorname{Im}[A_{\operatorname{flip}} A_{\operatorname{no-flip}}^*]$$

requires:

- helicity flip at the partonic level but helicity is conserved in massless QCD
- relative phase between helicity amplitudes but Born amplitudes are real.

$$\Rightarrow \hat{a}_N \propto \alpha_s \frac{m}{\sqrt{s}}$$

 $p^{\uparrow}p \to hX$: $A_N = \frac{d\sigma^{\uparrow} - d\sigma^{\downarrow}}{d\sigma^{\uparrow} + d\sigma^{\downarrow}}$ [transverse w.r.t. production plane] $\hat{a}_N \to A_N$: further dilution

pQCD: $A_N \simeq$ few % at large energy scales!

What do experimental data say?



 A_N data for $pp \to \pi X$: (left) at $\sqrt{s} = 20$ GeV [E704 coll. (1991)], (right) at $\sqrt{s} = 200$ GeV [STAR coll. (2004)]

$\ell p^{\uparrow} \rightarrow \ell' \pi X$: A_{UT} [HERMES coll. 2006]



Experimental observation: large SSAs!

Theoretical approaches in QCD

- 1. Spin and transverse momentum dependent (TMD) distributions: azimuthal asymmetries in the soft part
- 2. Higher-twist functions in collinear pQCD

...a brief overview



Nucleon structure in a collinear picture: $p_q = xP_N$ and $S = 0, (+), (\uparrow)$ three leading twist quantities \Rightarrow complete description of quark momentum and spin:

- unpolarized parton distribution: $q(x) = q_{+/+} + q_{-/+}$
- longitudinally polarized distribution: $\Delta q(x) = q_{+/+} q_{-/+}$
- transversely polarized distribution: $\Delta_T q(x) = q_{\uparrow\uparrow\uparrow} q_{\downarrow\uparrow\uparrow}$ $[h_1^q, \delta q]$

Three independent forward quark-nucleon amplitudes $(N \rightarrow qX)$:



 $\hat{F}^{\lambda_q,\lambda_q'}_{\lambda_N,\lambda_N'}(x, \mathbf{k}_{\perp})$ Helicity conservation, Parity, Rotational invariance

 \rightarrow 3 + 5 independent amplitudes i.e. \rightarrow 3 + 5 spin and TMD distributions Helicity formalism (each direction refers to the particle helicity frame)

$$\begin{aligned} f_q(x, \mathbf{k}_{\perp}) &= (F_{++}^{++} + F_{++}^{--}) & \text{unpolarized} \\ \Delta f_{s_z/+}(x, \mathbf{k}_{\perp}) &= (F_{++}^{++} - F_{++}^{--}) & \text{helicity} \\ \Delta f_{s_x/+}(x, \mathbf{k}_{\perp}) &= 2 \operatorname{Re} F_{++}^{+-} \\ \Delta' \hat{f}_{s_y/\uparrow}(x, \mathbf{k}_{\perp}) &= (F_{+-}^{+-} - F_{+-}^{-+}) \sin(\phi_{\uparrow} - \phi_q) \Rightarrow \text{transversity} \\ \Delta \hat{f}_{s_x/\uparrow}(x, \mathbf{k}_{\perp}) &= (F_{+-}^{+-} + F_{+-}^{-+}) \cos(\phi_{\uparrow} - \phi_q) \\ \Delta \hat{f}_{s_z/\uparrow}(x, \mathbf{k}_{\perp}) &= 2 \operatorname{Re} F_{+-}^{++} \cos(\phi_{\uparrow} - \phi_q) , \\ \Delta \hat{f}_{q/\uparrow}(x, \mathbf{k}_{\perp}) &= 4 \operatorname{Im} F_{+-}^{++} \sin(\phi_{\uparrow} - \phi_q) & \text{Sivers} \\ \Delta f_{s_y/N}(x, \mathbf{k}_{\perp}) &= -2 \operatorname{Im} F_{++}^{+-} & \text{Boer} - \text{Mulders} \end{aligned}$$

NOTICE: $\Delta \equiv$ difference of quark spin directions [except for Sivers funct.] Other notation (Amsterdam group): $f_1, g_{1L}, h_{1L}^{\perp}, h_{1T}, h_{1T}^{\perp}, g_{1T}, f_{1T}^{\perp}, h_1^{\perp}$



• Boer-Mulders function $[ImF_{++}^{+-}] h_1^{\perp}$

Boer, Mulders 1998



(Sivers '90, Anselmino, Boglione, Murgia '95): parton model with k_{\perp} effects assuming TMD factorization

$$A_{N}(pp \to \pi X) = \frac{d\sigma^{\uparrow} - d\sigma^{\downarrow}}{d\sigma^{\uparrow} + d\sigma^{\downarrow}} = \frac{d\Delta\sigma}{2d\sigma^{\mathrm{unp}}}$$

$$d\Delta\sigma^{\mathrm{Sivers}} \propto \sum_{a,b,c} \Delta \hat{f}_{a/p^{\uparrow}}(x_{a}, \mathbf{k}_{\perp a}) \otimes f_{b/p}(x_{b}, \mathbf{k}_{\perp b}) \otimes d\hat{\sigma}^{ab \to cd}(x, \mathbf{k}_{\perp}) \otimes D_{\pi/c}(z, \mathbf{k}_{\perp \pi})$$

$$= \int_{a,b,c}^{a,b,c} \int_{a,b,c}^{a$$

Fit of E704 data: (left) leading k_{\perp} (ABM), (right) full k_{\perp} [UD & F.Murgia 2004]



T-odd but safe: final state interactions between h X

SSAs in $pp \rightarrow CX$: generalized parton model (TMD approach)

$$d\sigma^{\uparrow} - d\sigma^{\downarrow} = \sum_{a,b,c} \left\{ \Delta \hat{f}_{a/p^{\uparrow}} \otimes f_{b/p} \otimes d\hat{\sigma} \otimes D_{\pi/c} \qquad \text{Sivers} \right. \\ \left. + h_1^{a/p} \otimes f_{b/p} \otimes \Delta \hat{\sigma} \otimes \Delta \hat{D}_{\pi/c^{\uparrow}} \qquad \text{Collins} \\ \left. + h_1^{a/p} \otimes \Delta \hat{f}_{b^{\uparrow}/p} \otimes \Delta' \hat{\sigma} \otimes D_{\pi/c} \right\} \qquad \text{Boer - Mulders}$$

Complete structure and full k_{\perp} - kinematics in the helicity formalism

[Anselmino et al. 06].

Higher-Twist approach

Alternative approach to SSAs in $A^{\uparrow}B \rightarrow CX$: $A_N \simeq m/\sqrt{s}$

Twist-three formalism [Efremov-Terayev '82, Qiu-Sterman '91, Koike et al. 2000]

$$d\sigma^{\uparrow} - d\sigma^{\downarrow} = \sum_{abc} \phi_{a/A^{\uparrow}}^{(3)}(x_1, x_2) \otimes \phi_{b/B}(x') \otimes \hat{H} \otimes D_{c \to C}(z)$$

+
$$\sum_{abc} h_1^{a/A}(x) \otimes \phi_{b/B}(x') \otimes \hat{H}' \otimes D_{c \to C}^{(3)}(z_1, z_2)$$

+
$$\sum_{abc} h_1^{a/A}(x) \otimes \phi_{b/B}^{(3)}(x'_1, x'_2) \otimes \hat{H}'' \otimes D_{c \to C}(z)$$

 $\Phi^{(3)}, D^{(3)}$: higher-twist partonic correlations (rather than PDFs or FFs) \hat{H} : elementary interactions for $ab \rightarrow cd$ process

Strong analogy to A_N in terms of TMD distributions.

$$\Phi_{a/p^{\uparrow}}^{(3)}(x_1, x_2) \sim \int \frac{dy^-}{4\pi} e^{ixp^+y^-} \langle P, \boldsymbol{S}_T | \, \overline{\psi}_a(0) \gamma^+ \\ \times \left[\int dy_2^- \epsilon_{\rho\sigma\alpha\beta} \, S_T^{\rho} \, p_1^{\alpha} \, p_2^{\beta} \, F^{\sigma+}(y_2) \right] \psi_a(y^-) \, | P, \boldsymbol{S}_T \rangle$$

• *TWO* parton momentum fractions, x_1, x_2 , and an external gluonic field $F^{\mu\nu}$; $\Phi^{(3)} \to T(x_1, x_2)$ (in the twist-three factorization proof)

• \hat{H} involves two terms

- $\delta(x_1 - x_2)$: gluon momentum set to zero \rightarrow Soft Gluon Pole ($\rightarrow x_1 = x_2 = x$)

- $\delta(x_i)$: quark momentum set to zero \rightarrow *Soft Fermion Pole*

 A_N is large at large x_F (valence region of p^{\uparrow}) Only SGP enters with dT(x,x)/dx: leading effect if $T(x,x) \simeq (1-x)^{\beta}$ at large xRecent developments [Kouvaris et al. '06, Koike et al. '07]. Phenomenology of Twist-three vs. TMD approach in $pp \rightarrow \pi X$

Twist-3 **collinear** factorization:

- 3 valence contributions: (one from each hadron in $p^{\uparrow}p \rightarrow \pi + X$)

- pQCD at NLO describes unpol. cross sections at large energies (200 GeV, RHIC), fails at moderate energies (20 GeV, E704)

- GLOBAL fit of A_N data (high and low energy data): GOOD description
 - using LO unpol. cross sections
 - rescaling E704 calculation of A_N
 - neglecting the potentially large contribution from chiral-odd FF.
- low energy data: problems both for the unpol. cross section and SSA description
- fit of all available data by a simple parametrization of T(x, x)

Generalized parton model with k_{\perp}

- no factorization proof
- Sivers effect able to describe the large x_F E704 data
- fair description of low and high-energy unpol. cross section data at LO
- fit on E704 A_N data: GOOD description
- predictions for RHIC in terms of Sivers effect:

GOOD for neutral pions (STAR), problems for charged pions (BRAHMS)



Left: $A_N(p^{\uparrow}p \to \pi^0 + X)$ at $\sqrt{s} = 200$ GeV: Sivers effect (GPM approach, dashed line) and twist-3 calculations (dotted line). Right: $A_N(p^{\uparrow}p \to \pi^{\pm} + X)$ at $\sqrt{s} = 200$ GeV for two scattering angles 2.3⁰ (left) and 4⁰ (right). Dotted line: Sivers effect; solid line: twist-three approach.

It seems that:

Twist-3 can describe all data; Sivers effect fails in describing high energy data.

but

TMD approach: Sivers effect from low-energy data to PREDICT high energy SSA Twist-3 function fitted on ALL data (handling with the low energy data)

So, can the Sivers effect do a better job for high energy SSA data?

Need of a global fit: in progress...

Back on it later on

TMD approach in QCD

"T-odd" distributions: T-reversal invariance $\Rightarrow \Delta f_{\uparrow} = -\Delta f_{\uparrow} \rightarrow \mathbf{0} \ (A^+ = 0 \text{ gauge})$



Brodsky, Hwang, Schmidt 2001 final state interactions in DIS through soft gluon rescattering: leading twist effect. - Model for the Sivers asymmetry

- Need of quark orbital angular momentum.

Soft gluons \leftrightarrow gauge link for gauge-invariant parton density [*Collins, Ji, Yuan, ...*]

$$\mathcal{P}\exp\left(-ig_s\int_{\xi^-}^{\infty}dz^-\,\hat{A}^+(z^-,\xi_\perp)
ight)$$

T-reversal invariance implies [modified universality]

$$\Delta f_{\uparrow}|_{\text{future}} = -\Delta f_{\uparrow}|_{\text{past}} \implies \Delta f_{\uparrow}|_{\text{DIS}} = -\Delta f_{\uparrow}|_{\text{DY}}$$



Transverse Single Spin Asymmetries in hard scattering processes

• TMD factorization proved for

DY, SIDIS, [and e^+e^- annihilation] processes in the two-scale regime:

- large Q^2 (i.e. boson virtuality)
- small q_T (lepton-pair or final hadron transverse momentum) [*Collins*, *Ji*, *Ma*, *Yuan*, *Belitsky* '04]
- gauge links \rightarrow universality of Collins function (*Collins & Metz '04, Yuan '08*)
- $\int d\mathbf{k}_{\perp} k_{\perp}^2 / (2M^2) f_{1T}^{\perp}(x, k_{\perp}) = T(x, x)$ [Boer, Mulders, Piljman '03]

- a step forward: equivalence of Twist-three and TMD approach for SIDIS and DY in the region where both apply: $\Lambda_{QCD} \ll q_T \ll Q$ (*Ji*, *Qiu*, *Vogelsang*, *Yuan '06*)

• Universality breaking effects in TMD approach for $pp \rightarrow hh + X$ (*Collins-Qiu, Vogelsang-Yuan, Mulders et al.* '07) [disappearing for $\int dk_{\perp}$!!!] $pp \rightarrow h + X$ still under debate

TMD approach and SSAs: phenomenology

• DY processes, $pp \rightarrow \ell^+ \ell^- + X$:

$$d\sigma \simeq 1 + \lambda \cos^2 \theta + \mu \sin 2\theta \cos \phi + \frac{\nu}{2} \sin^2 \theta \cos 2\phi$$

puzzling in LO and NLO collinear pQCD, explained in TMD approach: $d\sigma \simeq \text{Boer-Mulders} \otimes \text{Boer-Mulders} \cos 2\phi$ 0.45



• SSA in $p^{\uparrow}p \rightarrow \ell^+\ell^- + X$: $A_N \simeq \Delta^N f_{q/p\uparrow} \otimes f_{\bar{q}/p\uparrow} \sin(\phi - \phi_{\uparrow}) + \hat{a}_{TT} \Delta_T q \otimes \Delta^N f_{\bar{q}\uparrow/p} \sin(\phi + \phi_{\uparrow})$ (different azimuthal dependences \rightarrow separable) NO DATA

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SIDIS

• azimuthal dependence in $\ell p \rightarrow \ell' h + X$ $d\sigma \simeq \Delta^N f_{q^{\uparrow}/p} \otimes \Delta^N D_{h/q^{\uparrow}} d\Delta \hat{\sigma} \cos 2\phi_h$ + $f_{q/p} \otimes D_{h/q} d\hat{\sigma} \cos \phi_h$ [Cahn effect]

• SSA in $\ell p^{\uparrow} \rightarrow \ell' h + X$

 $A_{UT} \simeq d\sigma(\phi_S) - d\sigma(\phi_S + \pi)$



different azimuthal dependences \rightarrow separation of Sivers and Collins effects

$$A_{UT}^{\sin(\phi_h \pm \phi_S)} = 2 \frac{\int d\phi_S \, d\phi_h \, [d\sigma^{\uparrow} - d\sigma^{\downarrow}] \sin(\phi_h \pm \phi_S)}{\int d\phi_S \, d\phi_h \, [d\sigma^{\uparrow} + d\sigma^{\downarrow}]}$$

• Azimuthal correlations in $e^+e^- \rightarrow h_1h_1 + X$: Collins effect



Experimental Program: Belle @ KEK [FIRST EVIDENCE]

Extraction of Sivers, Collins and transversity functions

Sivers function: u, d and sea (latest analysis) quarks

Collins function: favoured and unfavoured FFs: $u \to \pi^+$ and $d \to \pi^+$

Transversity: u and d quarks

simple ansatz: $Nx^{a}(1-x)^{b} \times$ [Gaussian] k_{\perp} dependence

Other similar analysis from Vogelsang & Yuan, Efremov et al.

New (Anselmino et al. '08) vs. Old (Anselmino et al. 05) fits

- larger data set and more accurate data both for Collins and Sivers asymmetries
- new FF set: from KRE (Kretzer 2000) to DSS (De Florian, Sassot, Stratman '07)

in particular for the Sivers effect:

- old fit: up and down Sivers functions & independent large x behaviour x^+ +
- new fit: up, down and sea $[A_{UT}^{K^+} > A_{UT}^{\pi^+}]$ & same large x behaviour

Notice: covered experimental region: x < 0.3



Comparison of three FF sets.

• Sivers effect in SIDIS: NEW analysis [completed]

Anselmino et al. 2008



Fit of HERMES data [*Diefenthaler et al. 2006*],

(deuterium target)

KAON SSAs



Fit of HERMES data [Diefenthaler et al. 2006],

Comparison of fits adopting different FFs

• Collins effect in SIDIS: NEW analysis [preliminary]

Anselmino et al. 2008



Preliminary fit of [left] HERMES data [*Diefenthaler et al. 2007*] (hydrogen target) and [right] COMPASS data [*Alekseev et al. 2008*] (deuterium target).

• Collins effect in $e^+e^- \rightarrow \pi\pi + X$ NEW analysis [preliminary]

Anselmino et al. 2008



Preliminary fit of data on $e^+e^- \rightarrow h_1h_2 X$ from Belle Collaboration. [Ogawa et al. 2007].





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Sivers function: valence quarks



Burkardt sum rule [Burkardt '04]: $\sum_{a} \langle k_{\perp}^{a} \rangle = 0 \quad \langle k_{\perp}^{a} \rangle \equiv \int d^{2}k_{\perp}k_{\perp}\hat{f}_{a/p^{\uparrow}}$ $\langle k_{\perp}^{u} \rangle = 96 \text{ MeV } \langle k_{\perp}^{d} \rangle = -113 \text{ MeV } \langle k_{\perp}^{\text{sea}} \rangle = -14 \text{ MeV}$ \Rightarrow little room for the gluon Sivers function

Collins function [NEW preliminary analysis]

Anselmino et al. 2008



Consistent with other extractions [Efremov et al. 2006, Vogelsang & Yuan 2005] $A_{UT}^{\pi^+}(p) \simeq 4\Delta_T u \,\Delta^N D_{\text{fav}} + \Delta_T d \,\Delta^N D_{\text{unf}}$ $A_{UT}^{\pi^-}(p) \simeq 4\Delta_T u \,\Delta^N D_{\text{unf}} + \Delta_T d \,\Delta^N D_{\text{fav}}$ larger $|A_{UT}^{\pi^-}| \Rightarrow$ large and negative unfav. FF

Transversity function [NEW analysis: upgrade of 2007 First extraction]

Anselmino et al. 2008



Errors strongly reduced! $\Delta_T u$: larger; Tensor charge: $\delta u = 0.59^{+0.14}_{-0.13}$ $\delta d = -0.20^{+0.05}_{-0.07}$ at $Q^2 = 0.8 \text{ GeV}^2$



Transversity: Comparison with models

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SSAs: from SIDIS to *pp* **collisions**

Adopting Sivers & Collins functions as in the old fits with KRE set (*Boglione, UD, Murgia '08*)



PREDICTIONS and comparison to STAR $A_N(\pi^0)$ data.

Notice: extrapolation to large x region (uncovered in SIDIS).

A better strategy: use of pp data and fit to SIDIS data.



Sivers effect from SIDIS + pp scan ($\chi_{dof} \simeq 1.2$)

- A global description of A_{UT}^{Sivers} and A_N (in terms of Sivers effect) seems possible.
- Collins effect (reassessed!: Yuan '08): in progress (new fit and scan)
- GOAL (future): a complete global analysis of Sivers and Collins effects in SIDIS, e^+e^- and $pp \rightarrow hX$.
- A guidance to look for universality breaking effects (future)
- intermediate goal: disentangling Sivers and Collins effect in pp collisions

 $pp \rightarrow jet(\gamma) + X \text{ or } pp \rightarrow jet \gamma + X$ (Sivers effect) $pp \rightarrow jet \pi + X$ (Collins effect) [Yuan '08, UD-Murgia '08 (in progress)] and naturally

$pp \rightarrow \ell^+ \ell^- + X$ (safe process)

Importance of A_N in DY integrated over lepton angular variables clean access to Sivers effect: Anselmino, UD, Murgia '03, Efremov et al. '05, Vogelsang-Yuan '05, Anselmino et al. '05

- modified universality (change of sign w.r.t. SIDIS): crucial test (Collins '02)
- small and intermediate x region at RHIC
- large x region at COMPASS (uncovered in SIDIS)



COMPASS:
$$\pi^- p^{\uparrow}$$
: $\bar{u}u \to \ell^+ \ell^-$

- Sign: definite !
- access to large x region.

Conclusions

- Azimuthal and transverse SSAs: powerful tool, recent and important progress
- extractions of Sivers, transversity and Collins functions from SIDIS and e^+e^- :
- Collins effect as a polarimeter to access $\Delta_T q$. Large (negative) unfavoured FF.
- First extraction of transversity distribution: u and d smaller than their Soffer bounds
- Sizeable Sivers function for valence quarks; little room for gluon Sivers function;

Conclusions

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Open issues:

- Q^2 -evolution of TMDs
- modified universality: to be checked [$\Delta f_{\uparrow}|_{\rm DIS} = -\Delta f_{\uparrow}|_{\rm DY}$]
- SSAs in SIDIS: binning in x, z, P_{\perp} and error correlation matrix
 - large (low) x region still uncovered [JLAB(COMPASS)]
- SSAs in $p^{\uparrow}p \rightarrow CX$: disentangling TMD approach and Twist-3 formalism
- SSAs in $p^{\uparrow}p \rightarrow \text{jet } \pi X$: universality and separation of Sivers and Collins effects