THE ROLE OF CONSTITUENT QUARK MASS IN THE STANDARD MODEL

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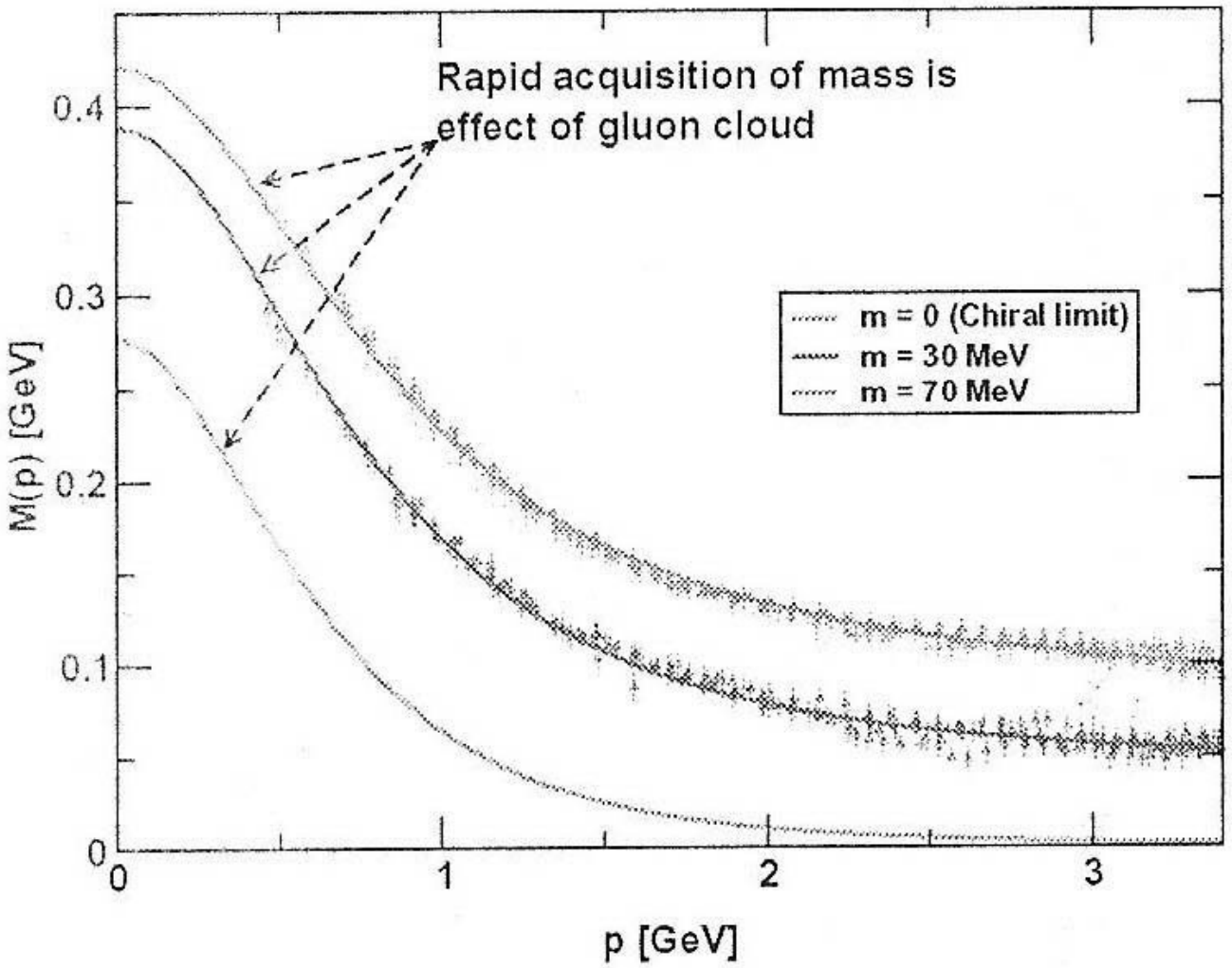


Fig.1. QCD gluon-quark-dressing effect calculated with Dyson-Schwinger Equation [9,13-17], initial masses m=0, 30 and 70 MeV; the constituent-quark mass arisses from a cloud of low-momentum gluons attaching themselves to the current-quark; this is dynamical chiral symmetry breacking: an nonperturbative effect that generates a quark mass from nothing even at chiral limit m=0, bottom curve) [9]..

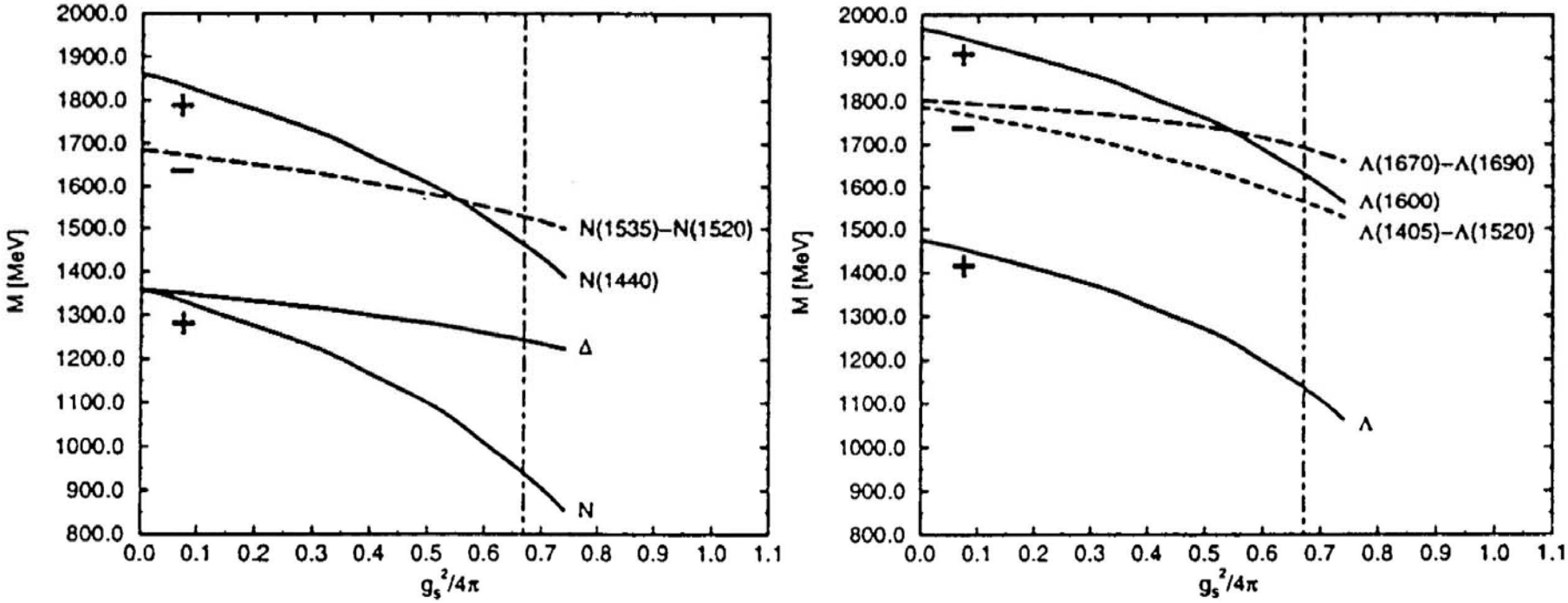


Fig.2. Calculation of nonstrange baryon masses (left) and Λ-hyperon masses as a function of interaction strength within GBECQM – Goldstone Boson Exchange interaction Constituent Quark Model [19]; initial baryon mass 1350 MeV=3×450 MeV=$3M_q$ is near the bottom "+" on the left vertical axis.

Table 1. Discussed in the literature closeness of masses or mass differences to the integer numbers (k) of the pion mass value $m_\pi^\pm$=139.5 MeV or to $2m_\pi^\pm+m_\pi^\circ=\kappa_T$=409 MeV.

Particle	Λ	Ω	(bb)(2S-1S)	(bb)(4S-2S)	ΔE_B
Mass or ΔM (MeV)	1115.683(6)	1672.45(29)	10023-9460 =563	10579-10023 =556	408.9
km_π or $2m_\pi^\pm+m_\pi^\circ=\kappa_T$	1116 k=8	1672 k=12	558 k=4	558 k=4	409 κ_T
difference, reference	0, [1,23-26]	0, [1,25,26]	-5, [1,26]	-2, [1,27]	0, [28]

Table 2. Discussed in the literature closeness of particle masses or mass differences to the integer numbers (k) of the nucleon Δ-excitation parameter Δ_Δ=147 MeV [23].

Particle	(cc) (2S-1S)	(cc) (1S)	Ξ^-	ω_3-ω	K_3^*-$K^*(892)$	ΔE_B
Mass or ΔM (MeV)	3686.1-3096.9 =589.2 k=4	3096.92(1) 3087 k=21	1321.3 k=9	1667(4)-782.7 884(4) k=6	1776(7)-891.7 =884(7) k=6	441.5 (Fig.4) k=4
$k\Delta M_\Delta$	588	588	1323	882	882	441
diff., ref.	1,[1,25,29]	1,[1,25,29]	-2,[??]	2(4),[1,25,29]	2(7),[1,25,29]	0,[28]

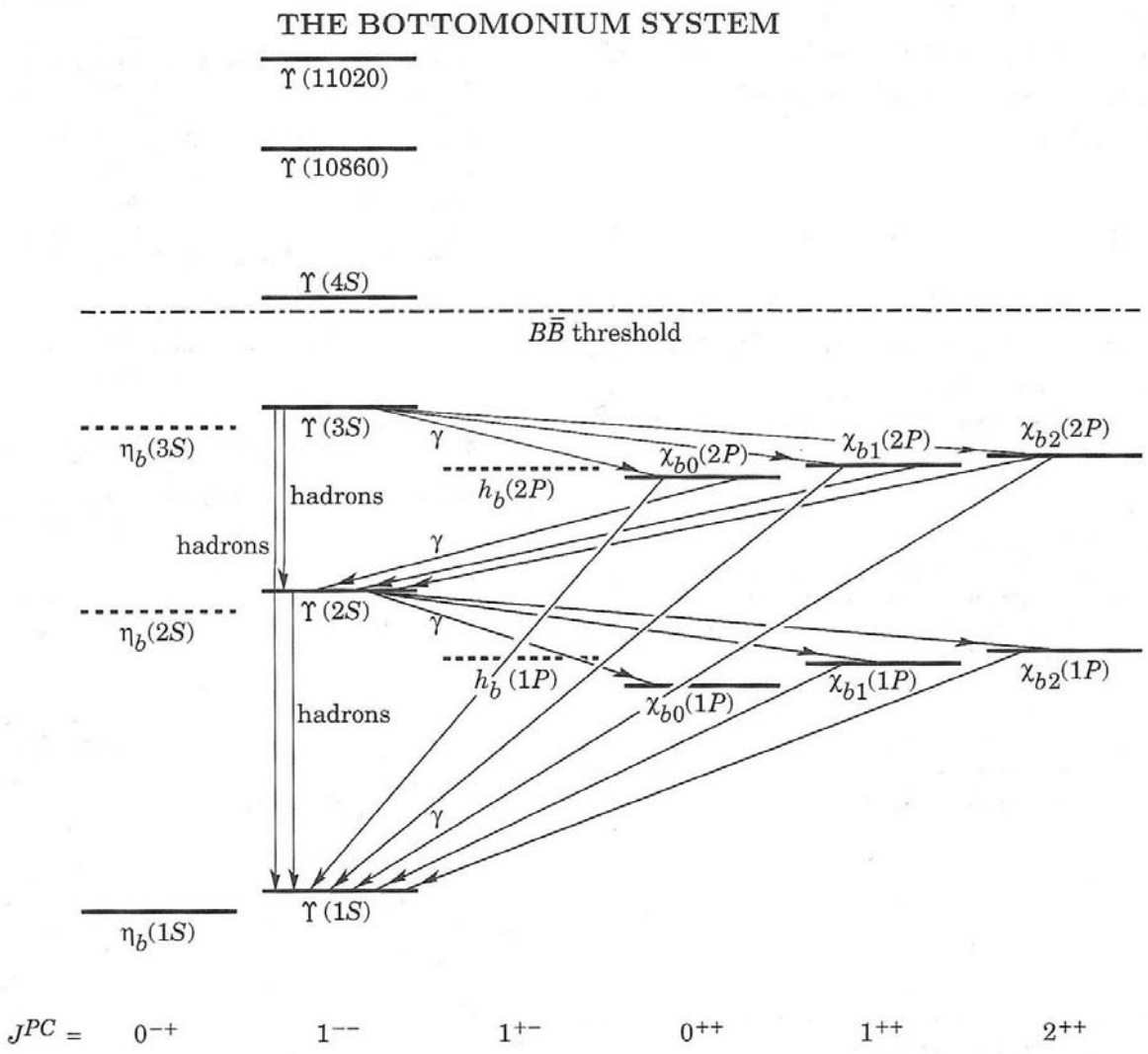
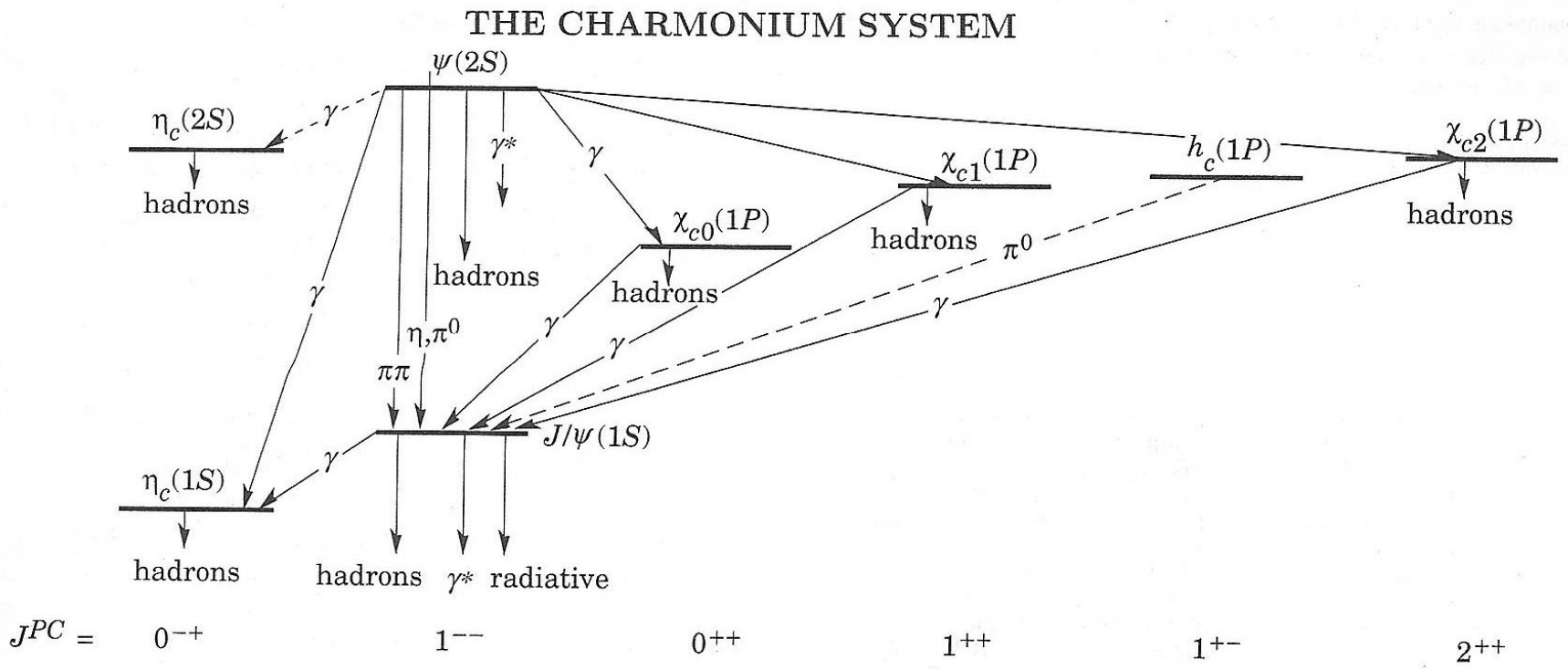


Fig.3. *Top* Mesons of (bb)-structure with radial excitations n=1 and n=1-3 close to $4m_\pi$ [1,27]; *Bottom* Mesons of (cc)-structure with radial excitation (n=1) close to $4\Delta M_\Delta$=4×147 MeV=588 MeV.



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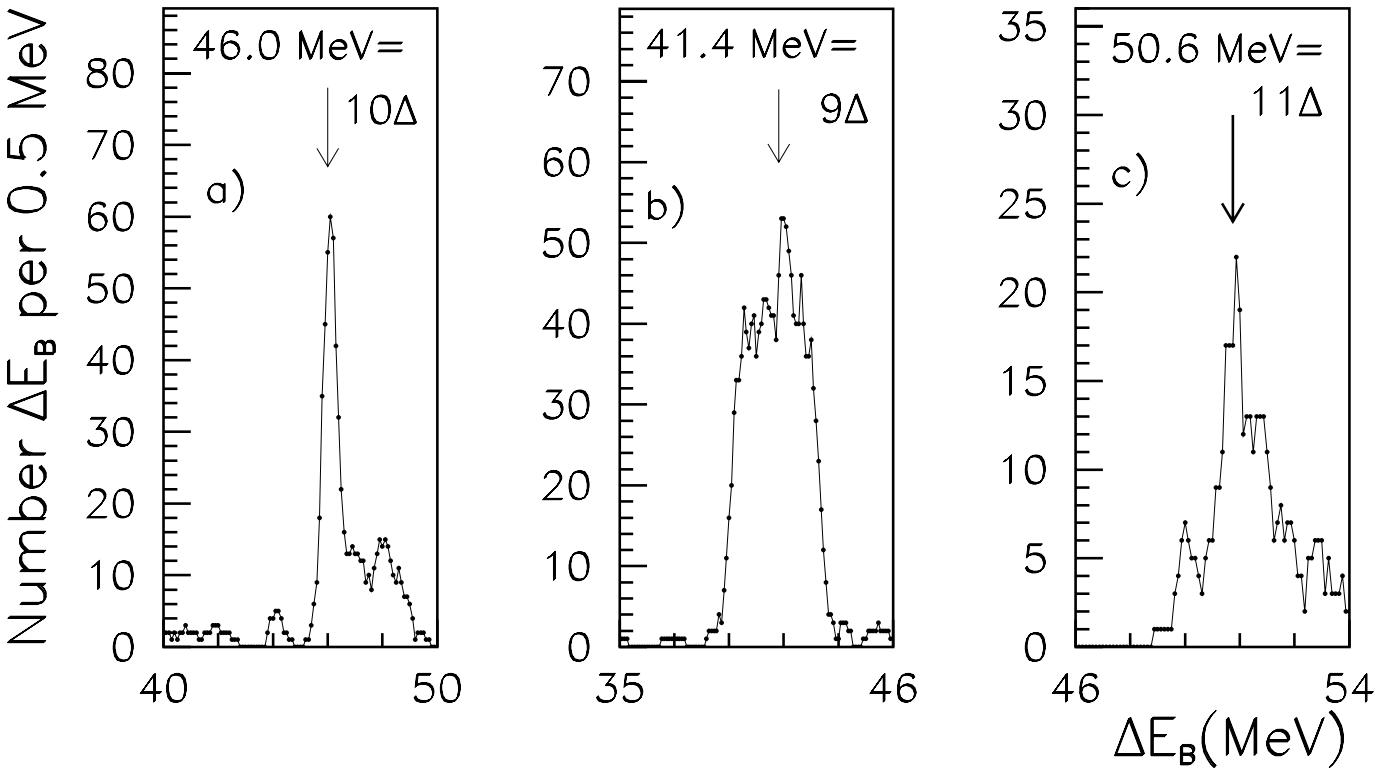
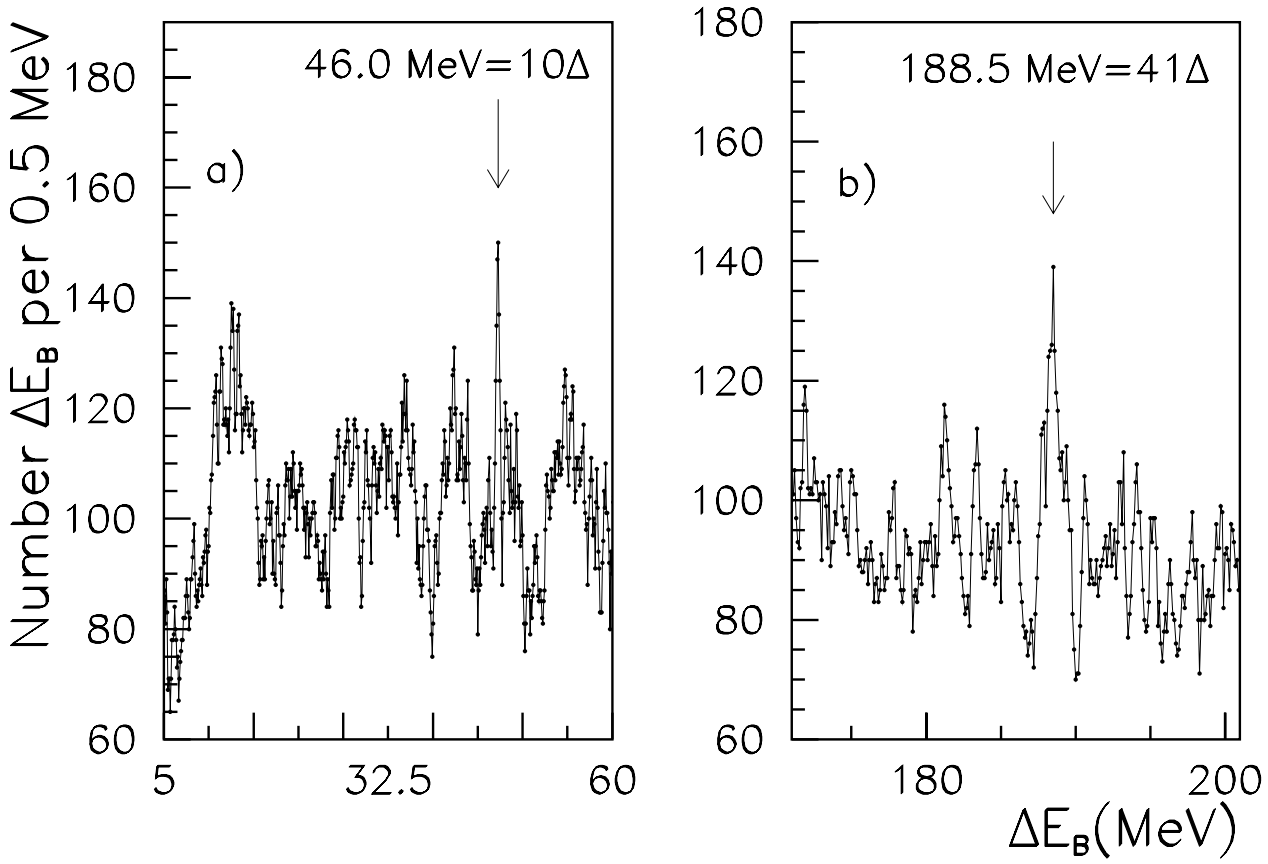


Fig. 4, *Top:* Distribution of ΔE_B in nuclei with $\Delta Z=2$, $\Delta N=4$, $Z=50$-58, 64-82 and $Z\leq 28$ [26] *Bottom:* The same in all even-even and nuclei [26], in even-even nuclei with $Z\leq 58$ [29].



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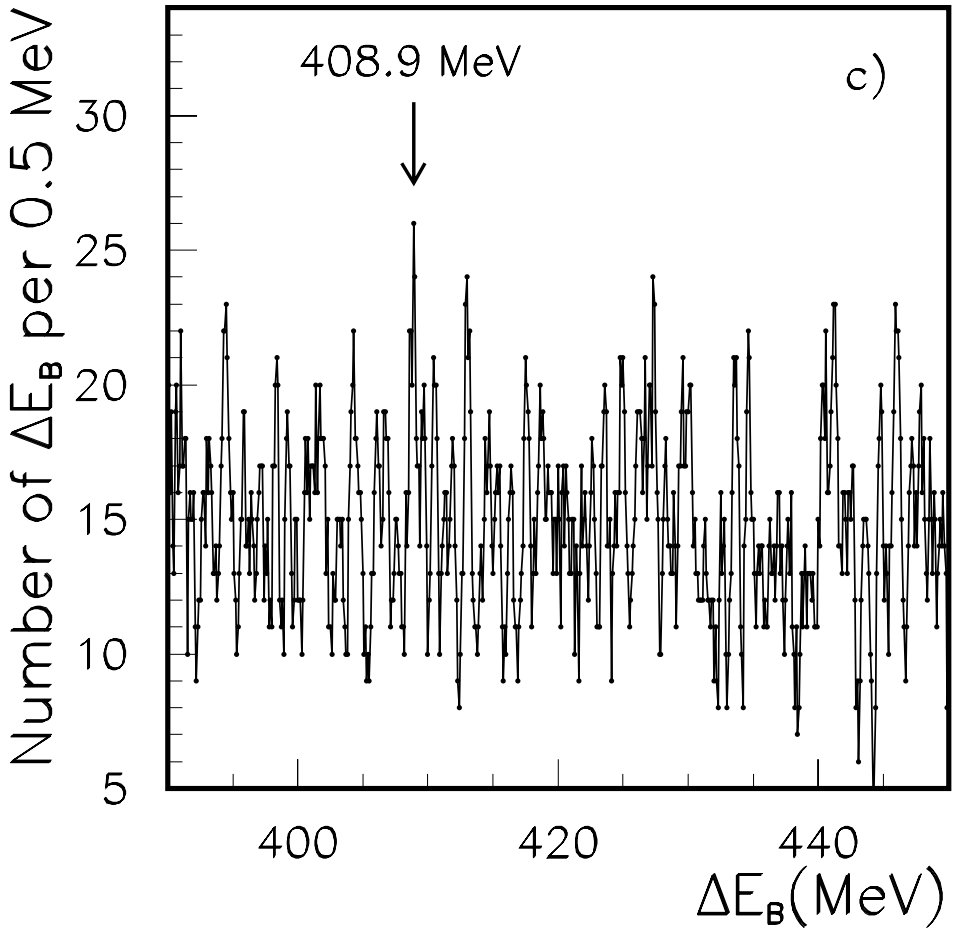

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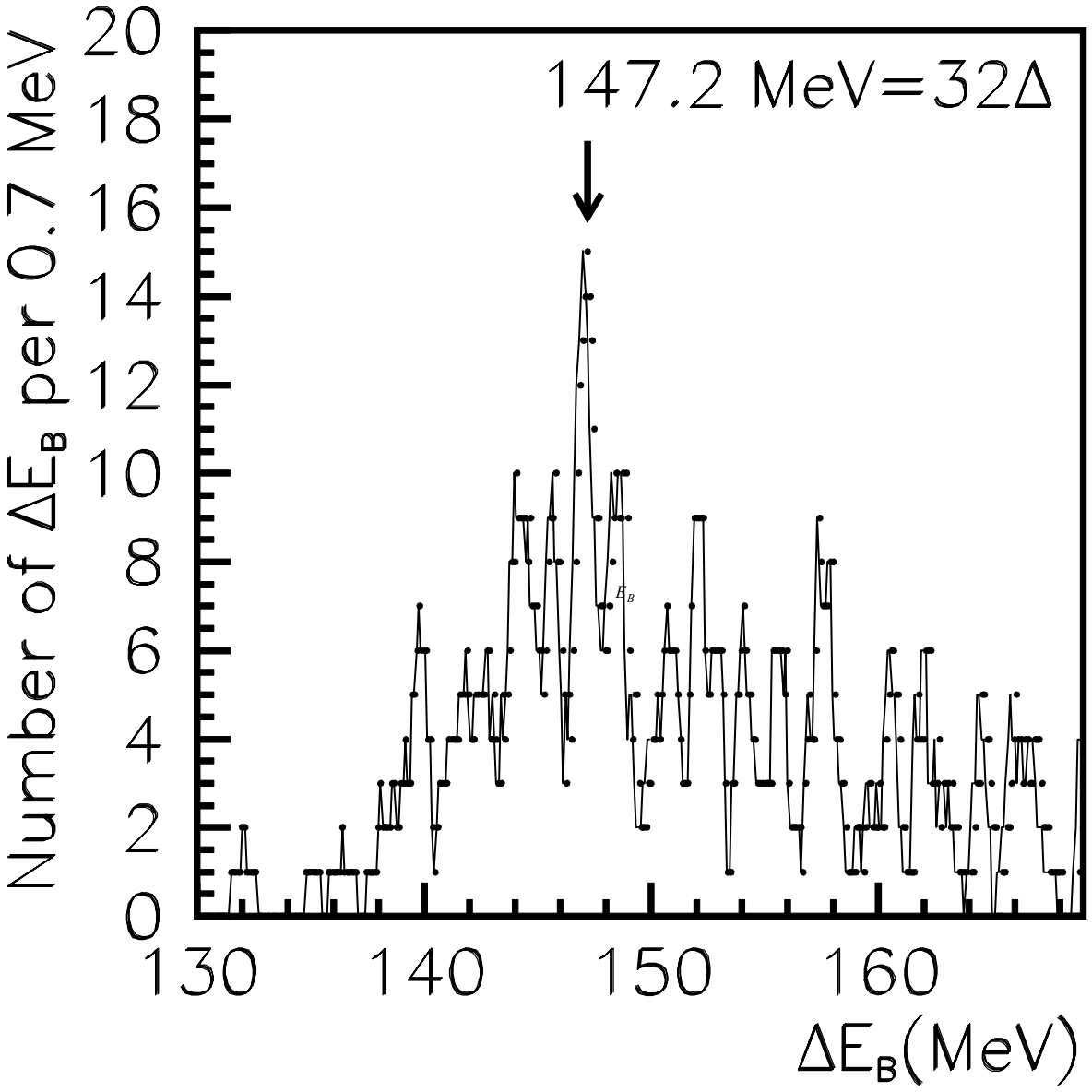
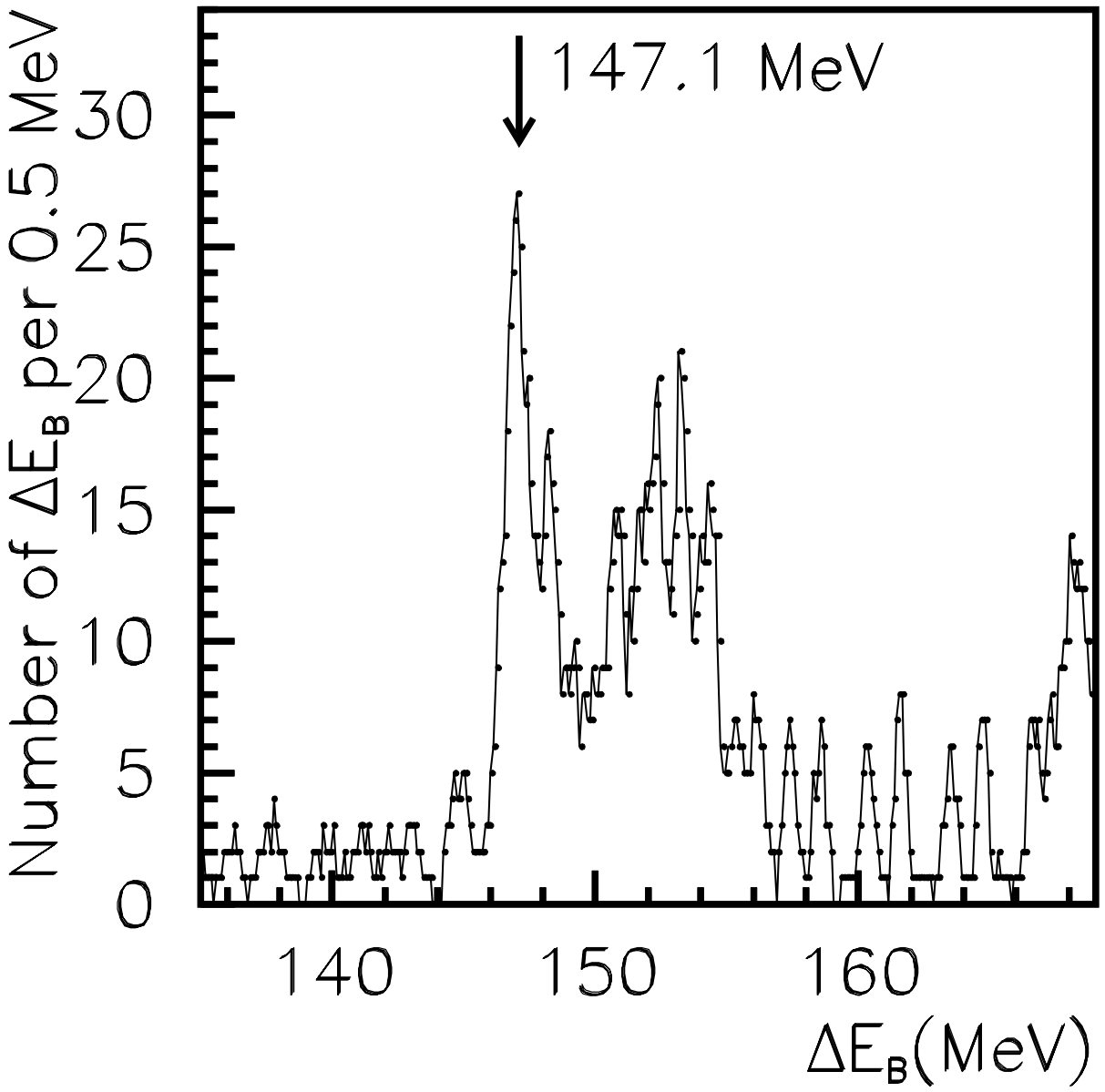


Z less 26 ΔE_B (4α)



Heavy nuclei

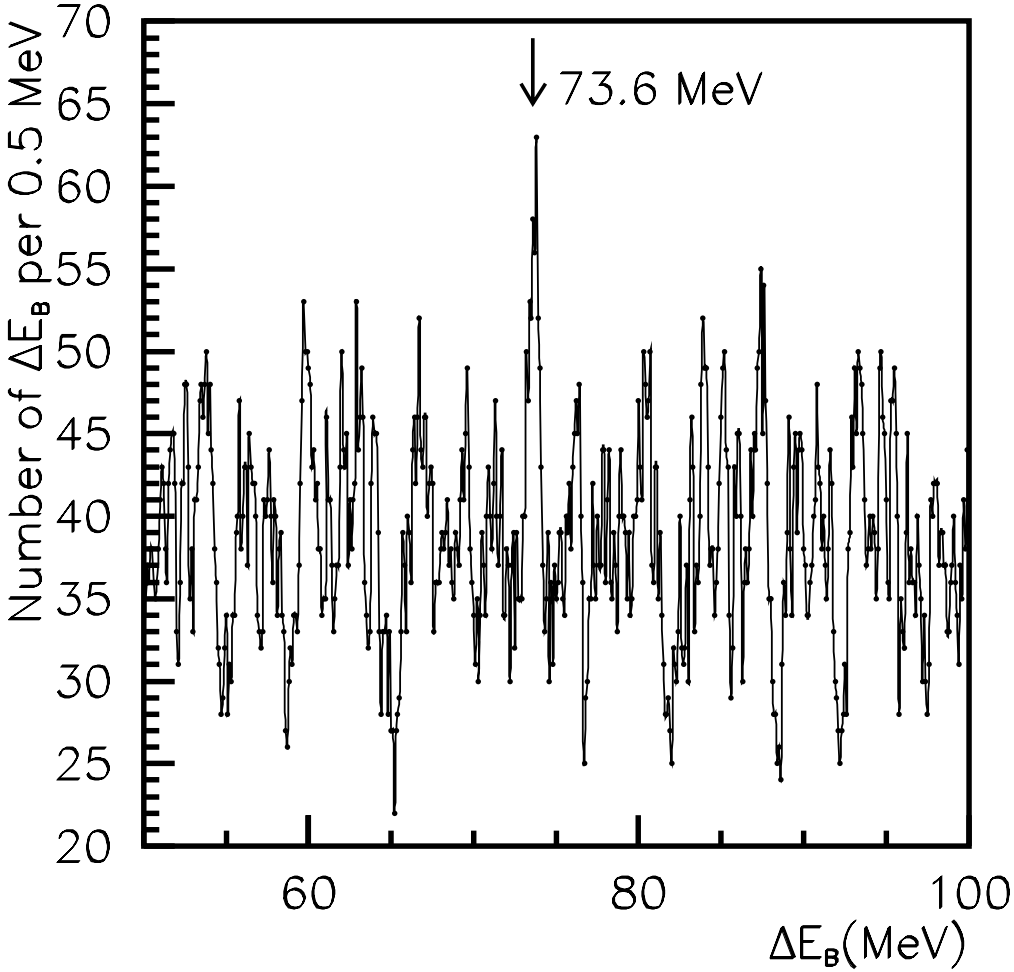
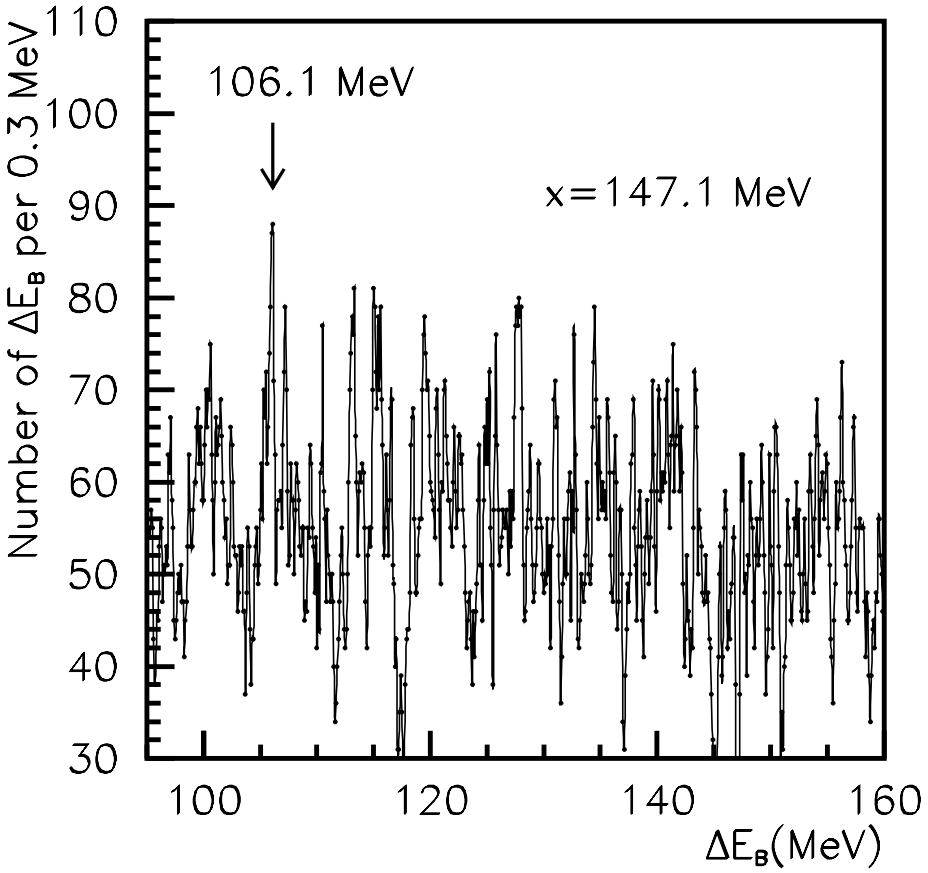


Fig. 5, *top:* Distribution of ΔEB in nuclei with ΔZ≤26; 4α- 2α-config. and all nuclei [6]); *center*: Distribution of adjacent intervals $\Delta E_{B\text{-}AIM}$ in nuclei with Z≤26 for x=147.2 and 73.6 MeV [6]); *bottom*: Distribution of ΔE_B in nuclei with ΔZ=8, ΔN=14 (Z=50-82); Distribution of $\Delta E_{B\text{-}AIM}$ in nuclei with ΔZ=65-81 for x=147.1 MeV [6]; Distribution of ΔE_B in all odd-odd nuclei [26].



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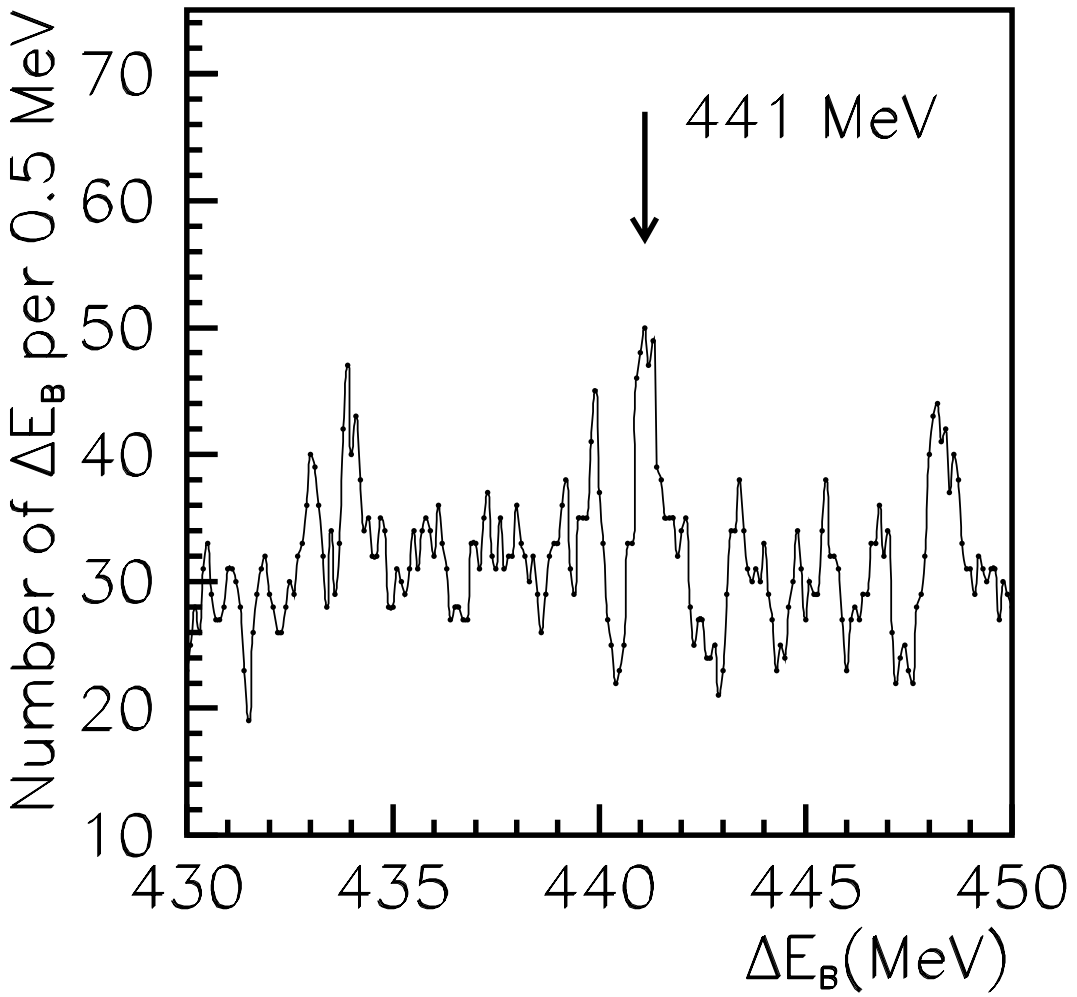

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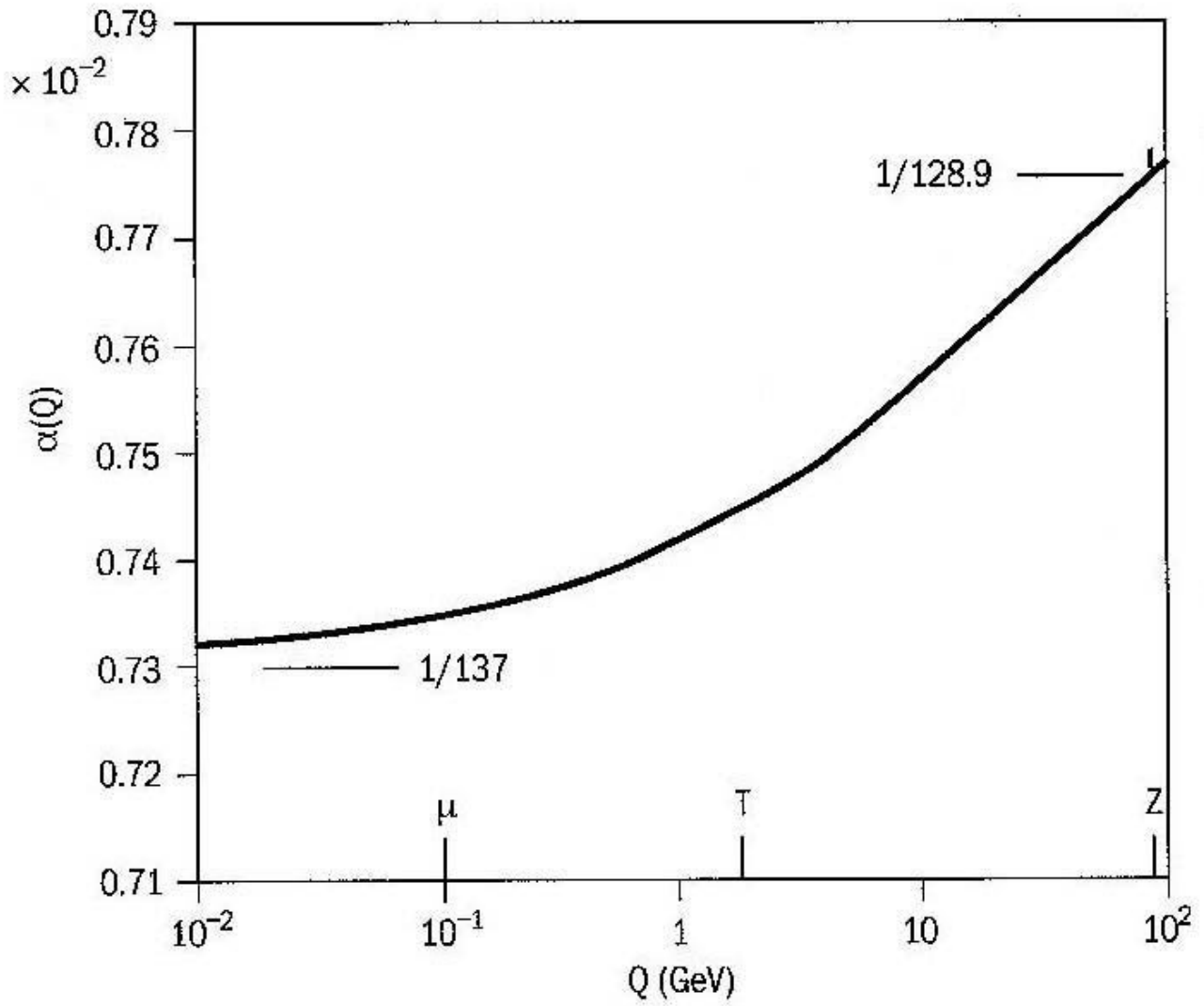


Fig.6. Momentum transfer evolution of QED effective electron charge squired. The momotonically rising theoretical curve is confronted with precise measurements at the Z mass at CERN LEP collider

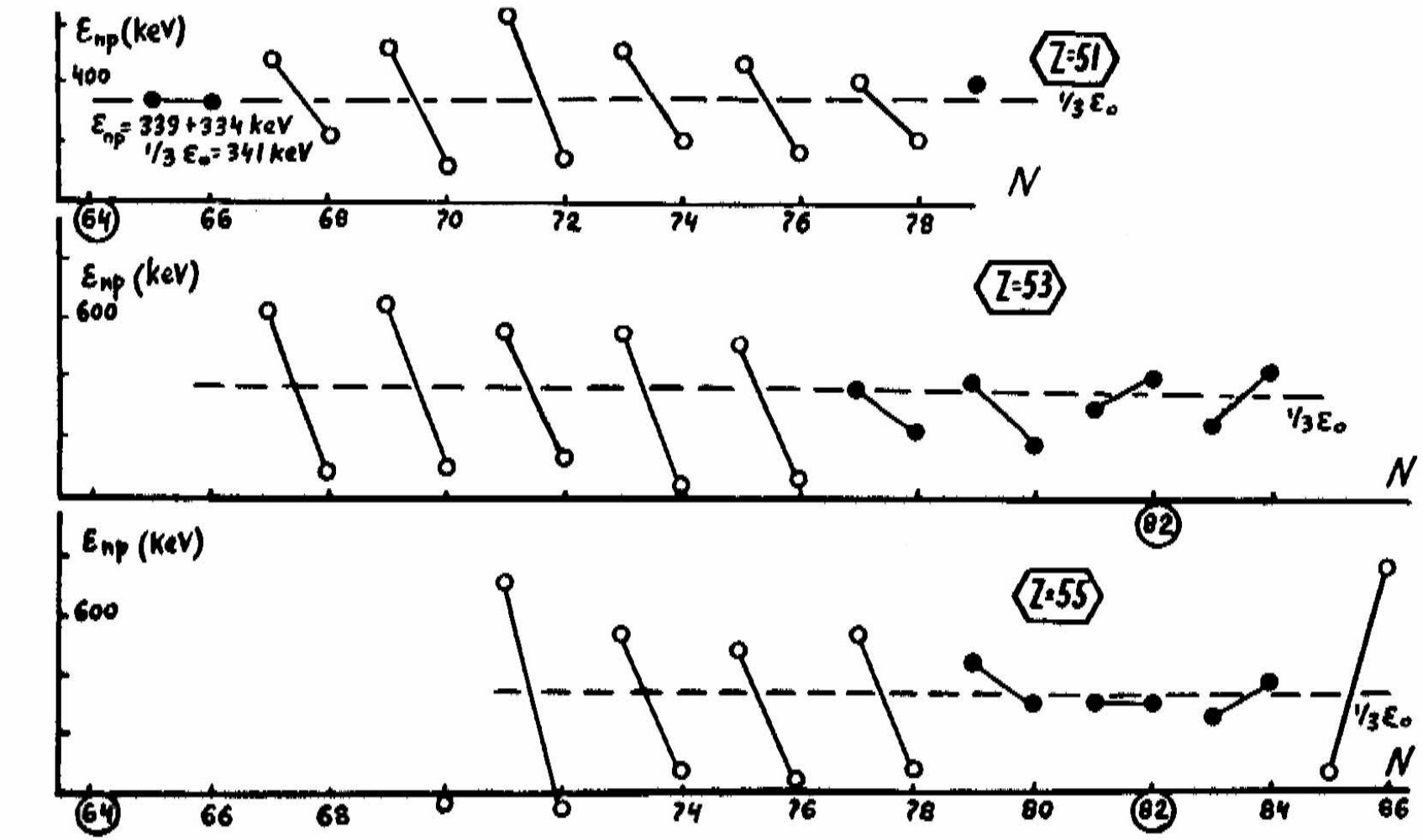
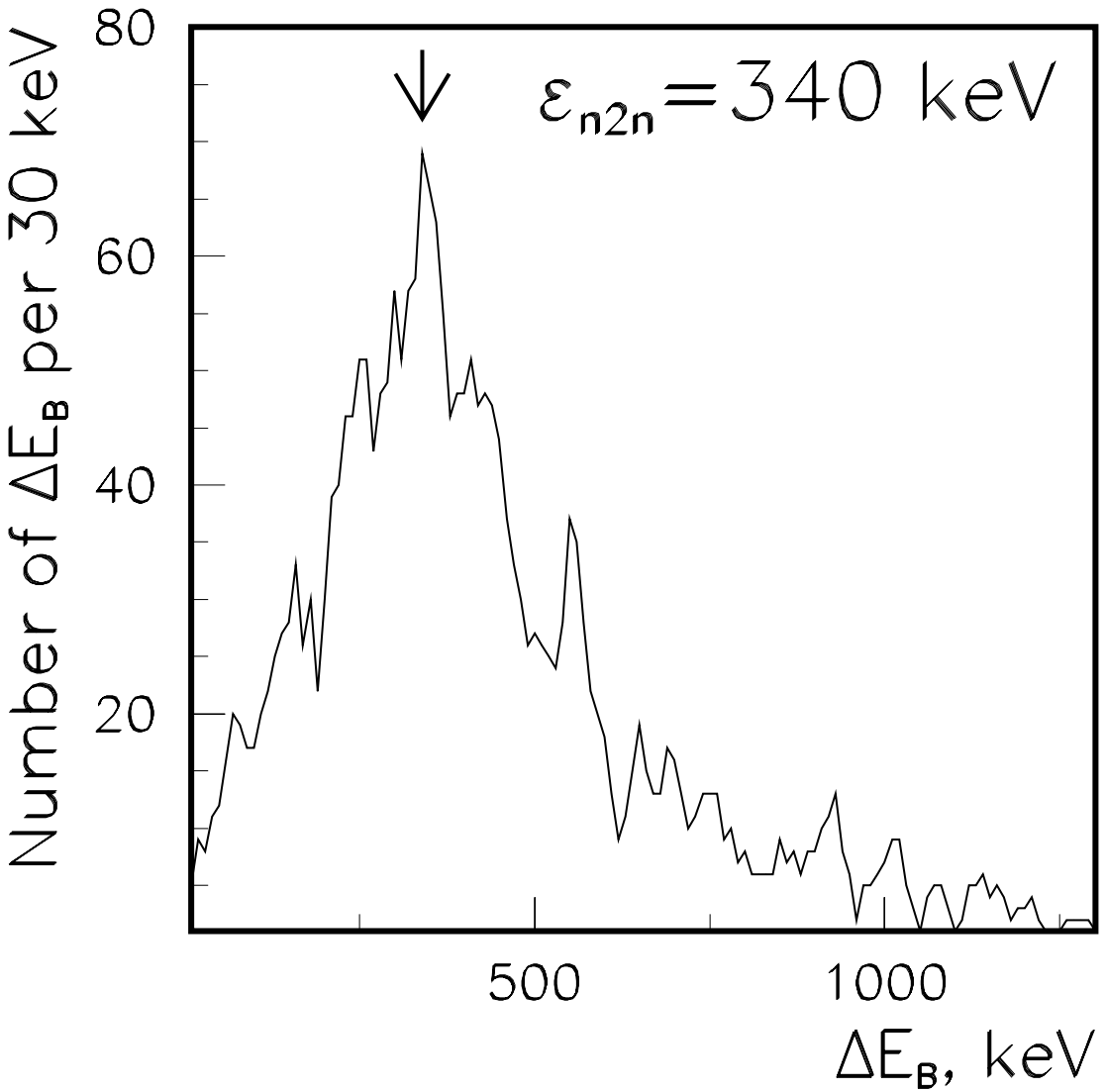
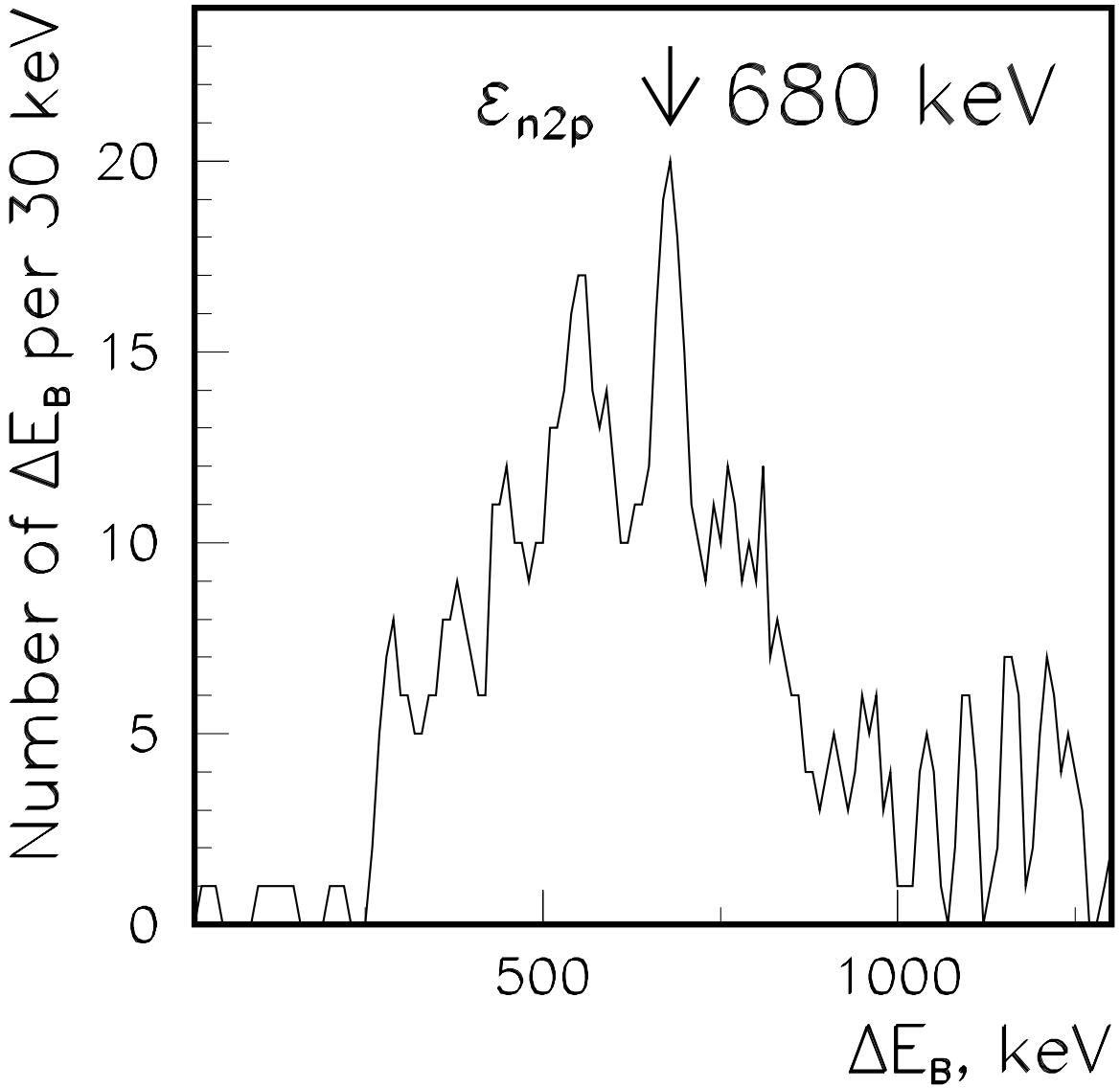
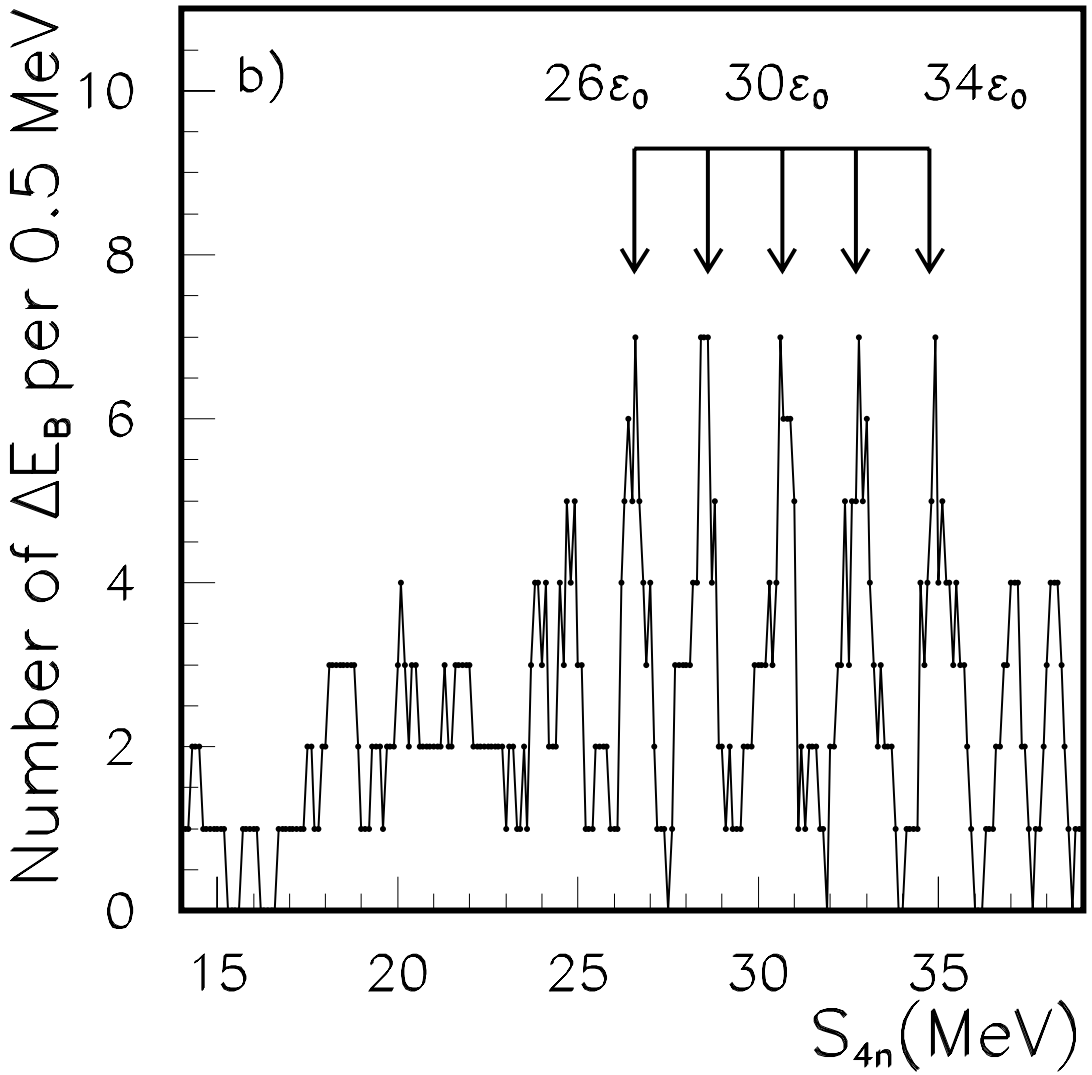
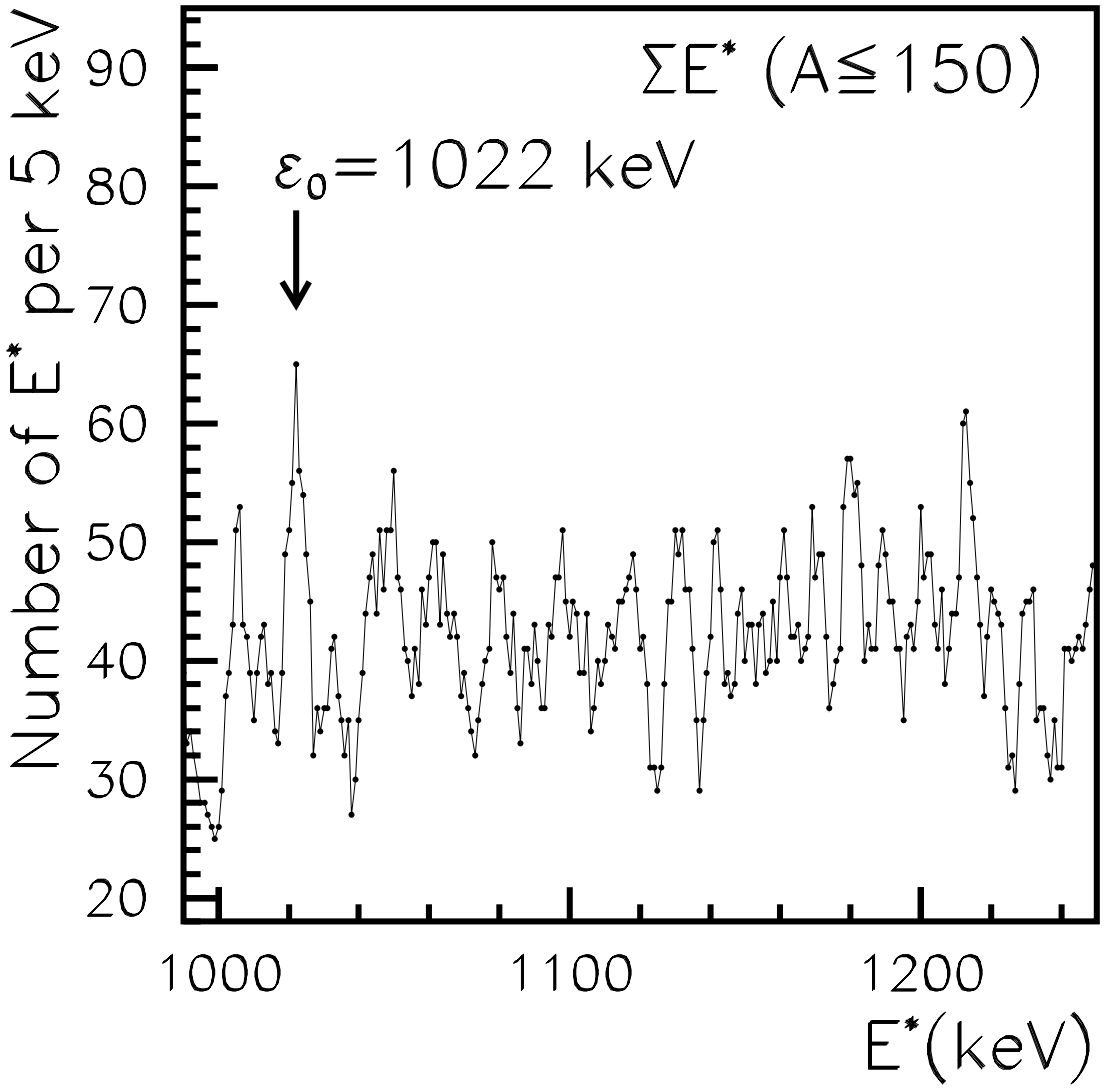


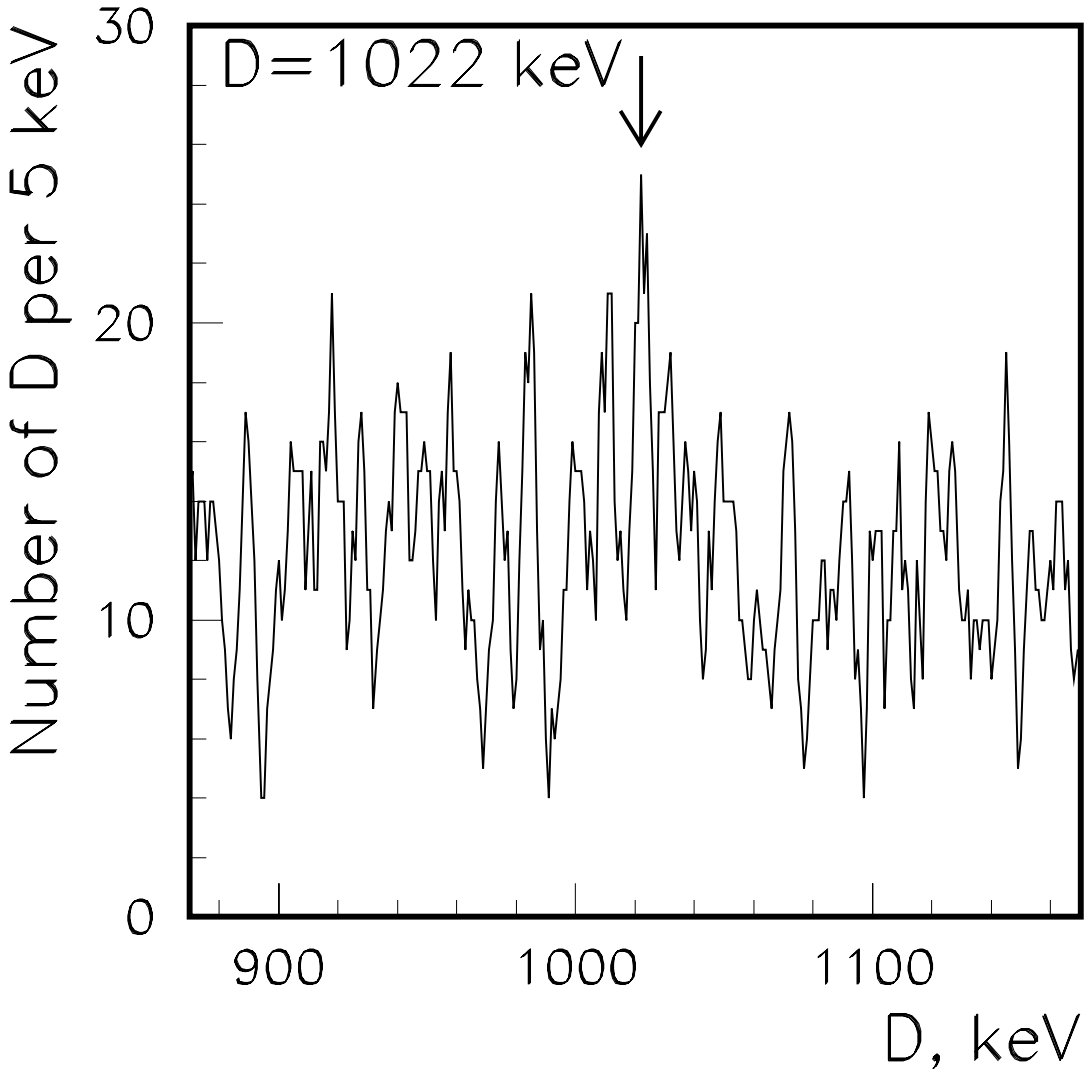
Fig.7. Parameters of the residual interaction ε_{np} from differences of S_p in Z-odd nuclei ($\Delta N = 1$). The value $\varepsilon_o/3$=341 keV is given by horizontal line

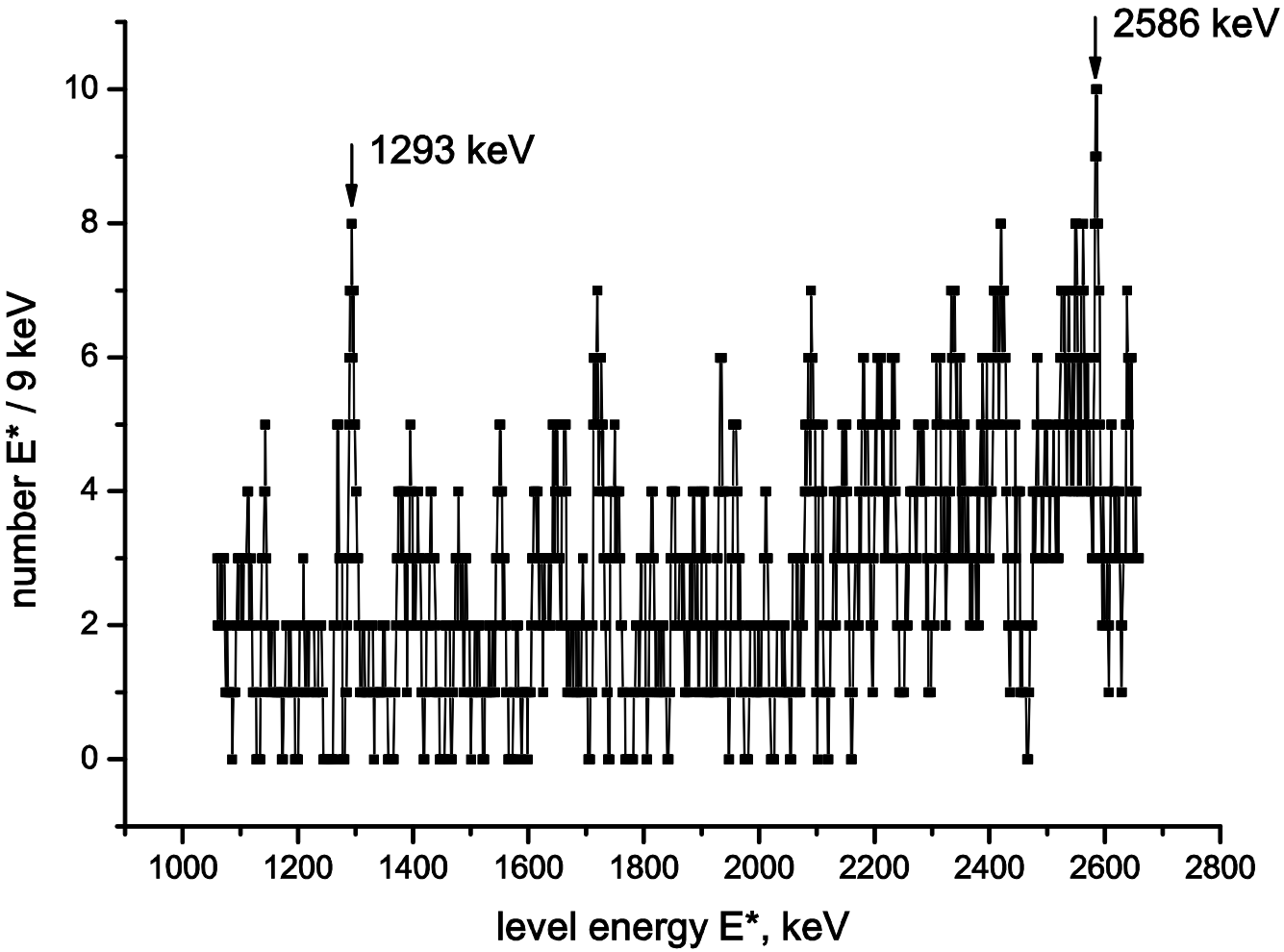

80
60
40
20
Number of $\Delta E_в$ per 30 keV
ε_{n2n}=340 keV
500
1000
$\Delta E_в$, keV

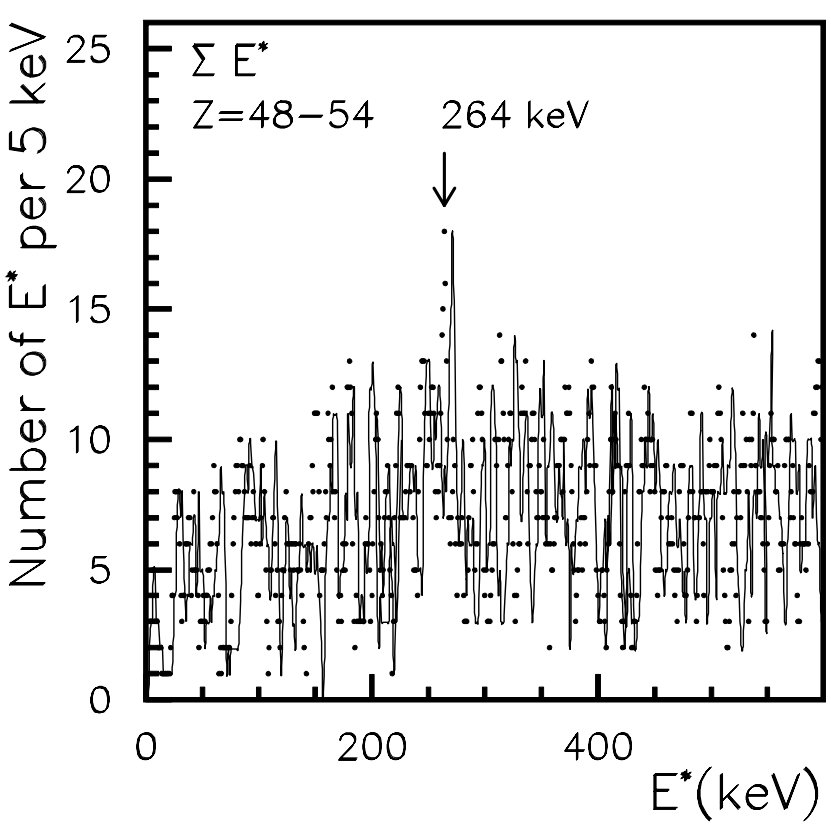

ε_{n2p} ↓ 680 keV
Number of $\Delta E_в$ per 30 keV
0
5
10
15
20
500
1000
$\Delta E_в$, keV

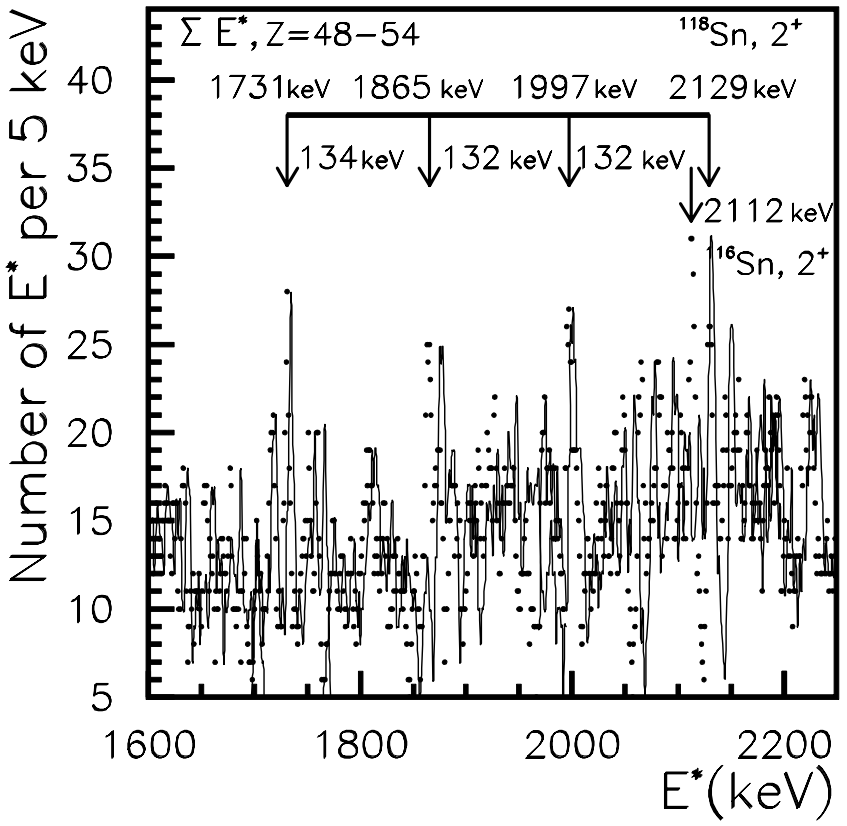

b)
26ε₀
30ε₀
34ε₀
Number of ΔE_B per 0.5 MeV
0
2
4
6
8
10
15
20
25
30
35
S_4n(MeV)

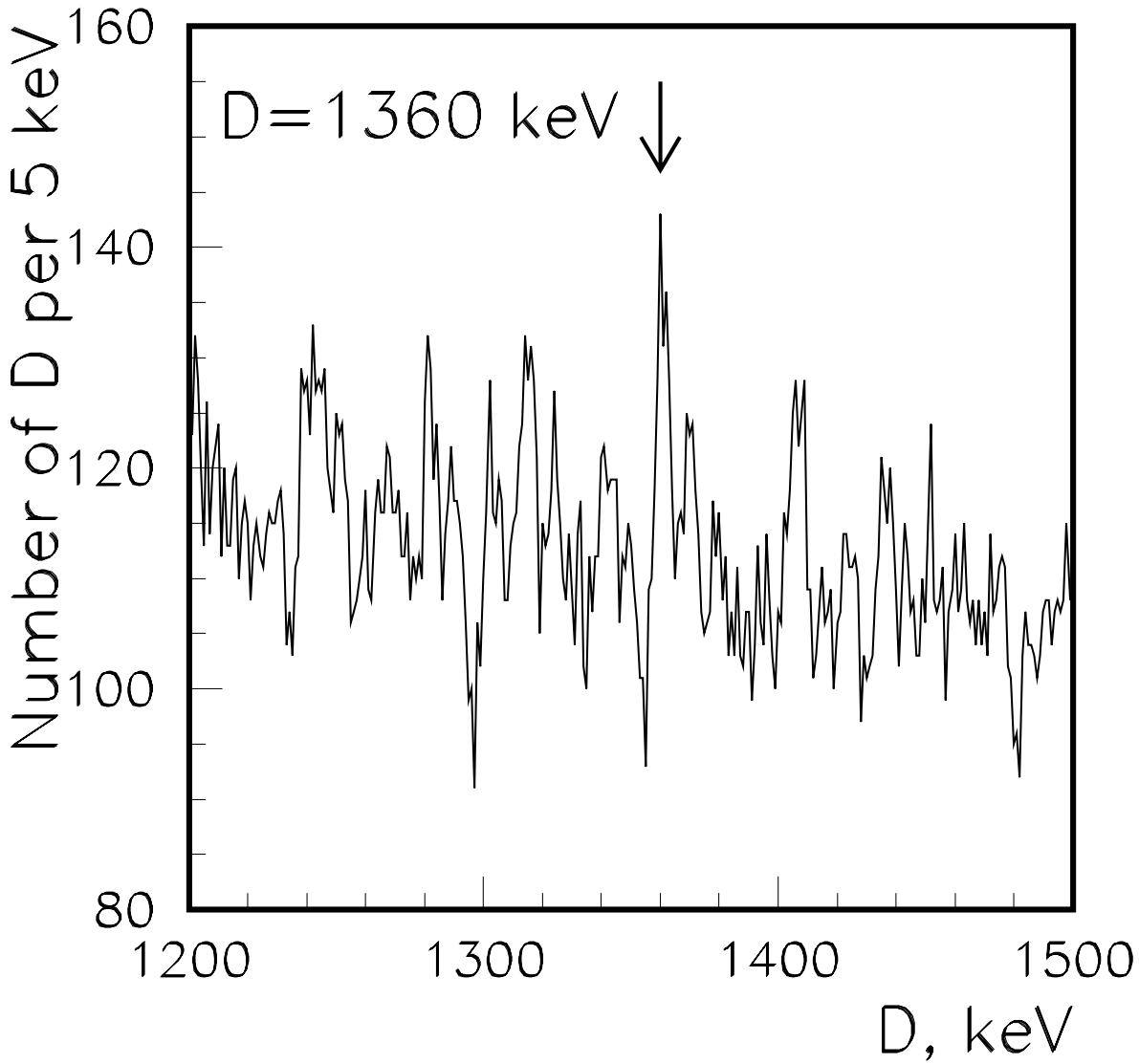

ΣE* (A≦150)
ε0=1022 keV
Number of E* per 5 keV
90
80
70
60
50
40
30
20
1000
1100
1200
E*(keV)

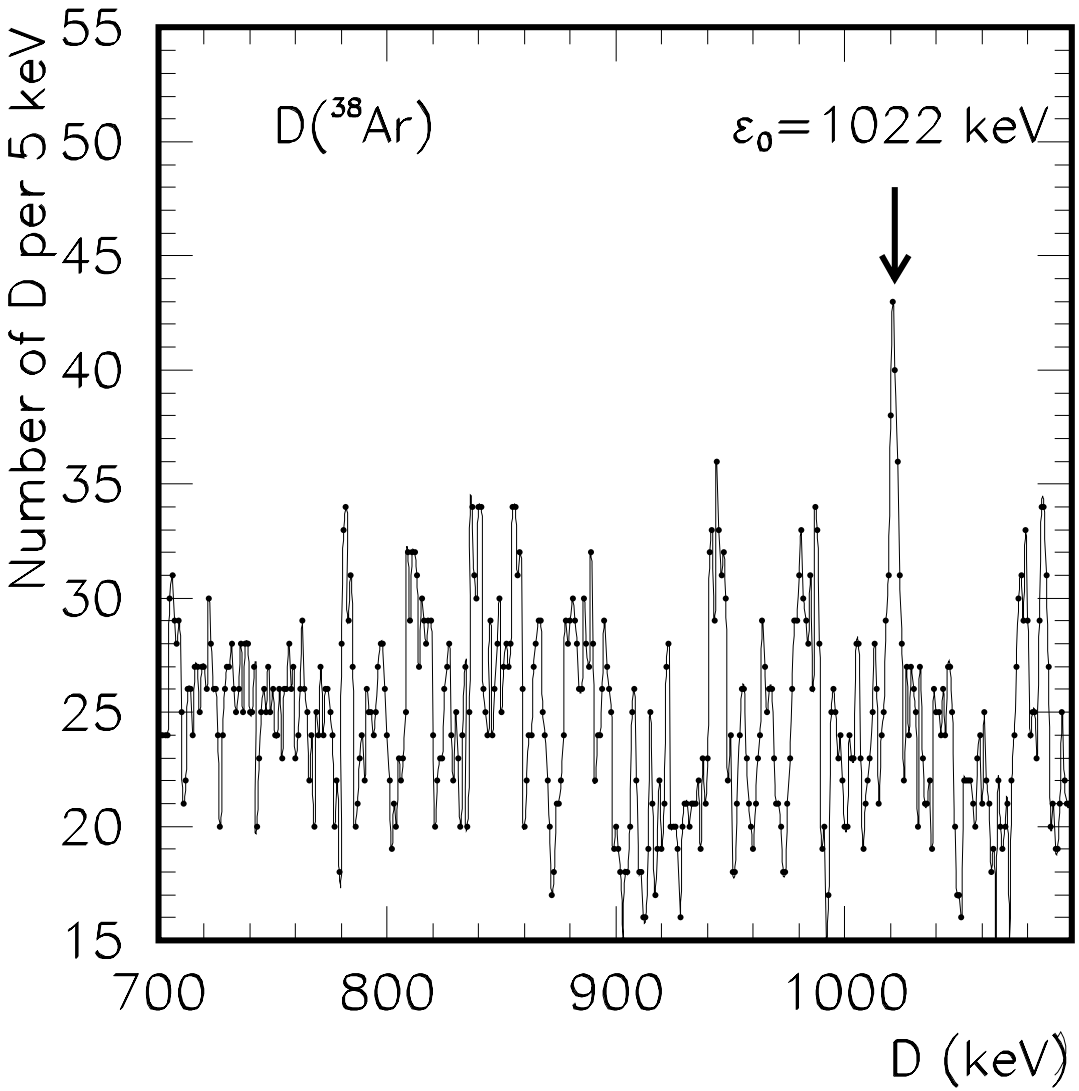

D=1022 keV
Number of D per 5 keV
30
20
10
0
900
1000
1100
D, keV

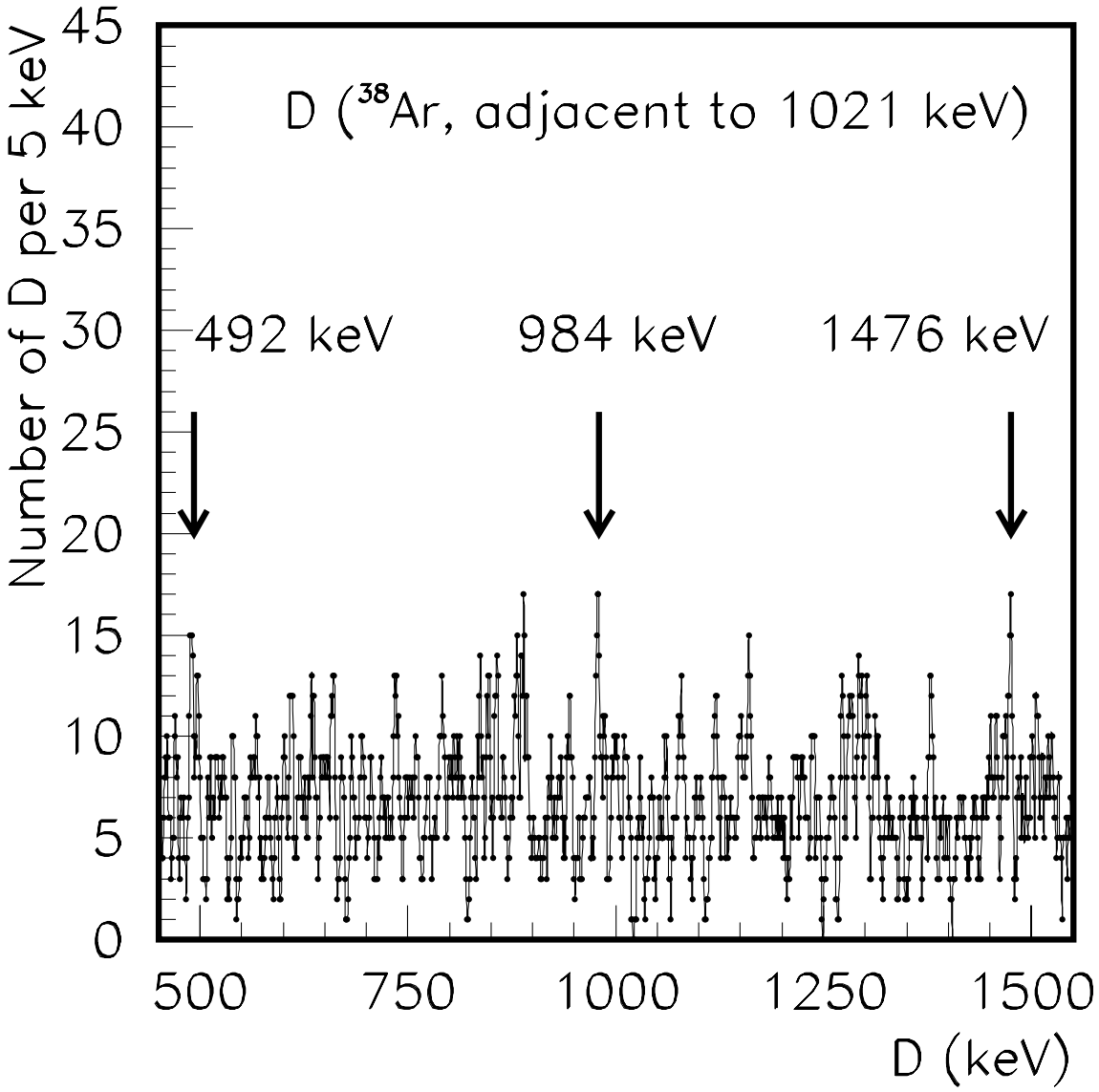

2586 keV
1293 keV
number E* / 9 keV
0
2
4
6
8
10
1000
1200
1400
1600
1800
2000
2200
2400
2600
2800
level energy E*, keV

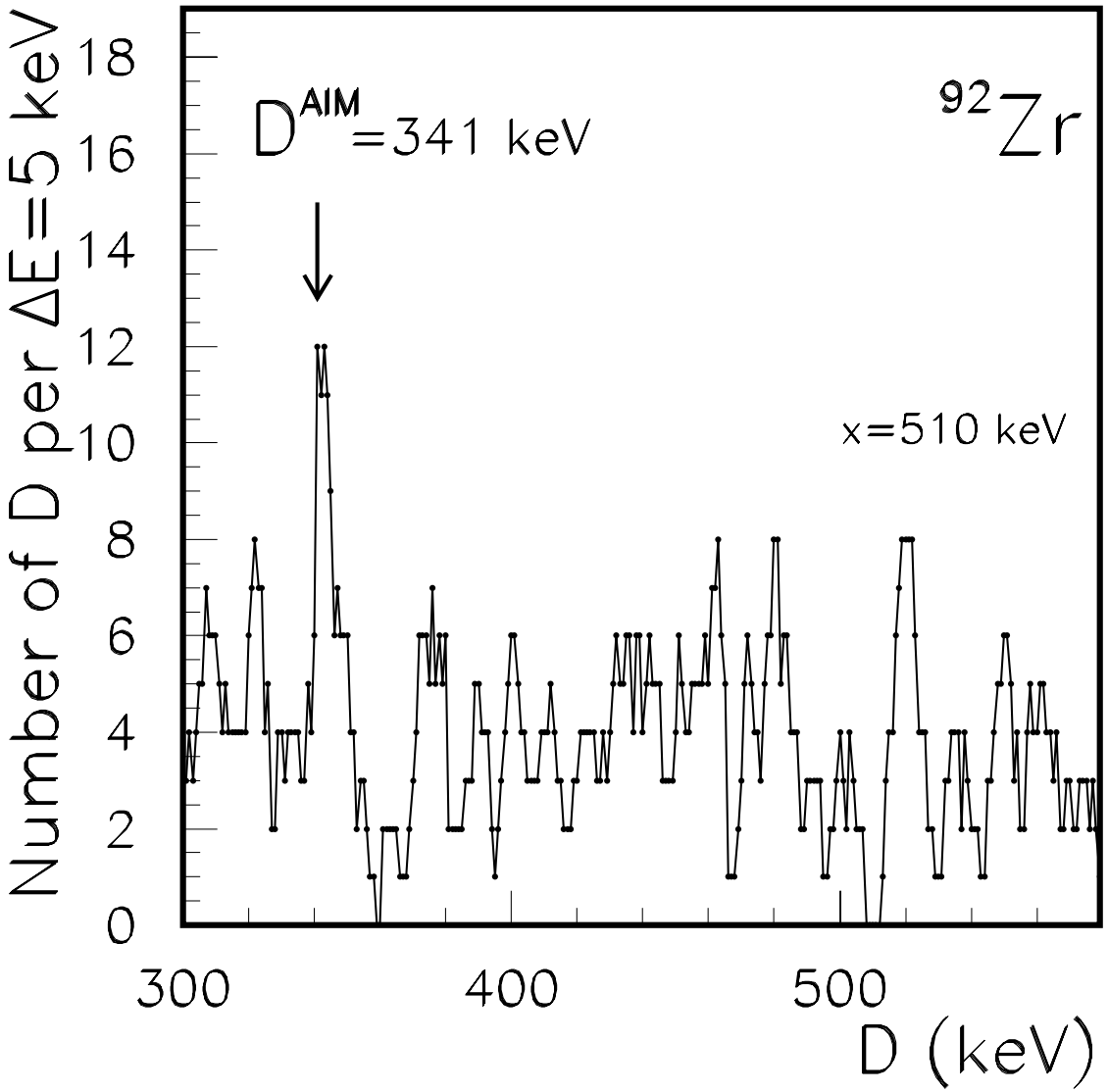

Σ E*
Z=48–54
264 keV
Number of E* per 5 keV
E*(keV)
0
5
10
15
20
25
0
200
400


Σ E*, Z=48–54
118Sn, 2+
1731keV
1865 keV
1997 keV
2129 keV
134keV
132 keV
132 keV
2112 keV
116Sn, 2+
Number of E* per 5 keV
E*(keV)
5
10
15
20
25
30
35
40
1600
1800
2000
2200


D=1360 keV
Number of D per 5 keV
160
140
120
100
80
1200
1300
1400
1500
D, keV


D(38Ar)
ε0=1022 keV
Number of D per 5 keV
55
50
45
40
35
30
25
20
15
700
800
900
1000
D (keV)


D (^{38}Ar, adjacent to 1021 keV)
492 keV
984 keV
1476 keV
Number of D per 5 keV
0
5
10
15
20
25
30
35
40
45
500
750
1000
1250
1500
D (keV)


Number of D per ΔE=5 keV
0
2
4
6
8
10
12
14
16
18
300
400
500
D (keV)
D^AIM=341 keV
92Zr
x=510 keV

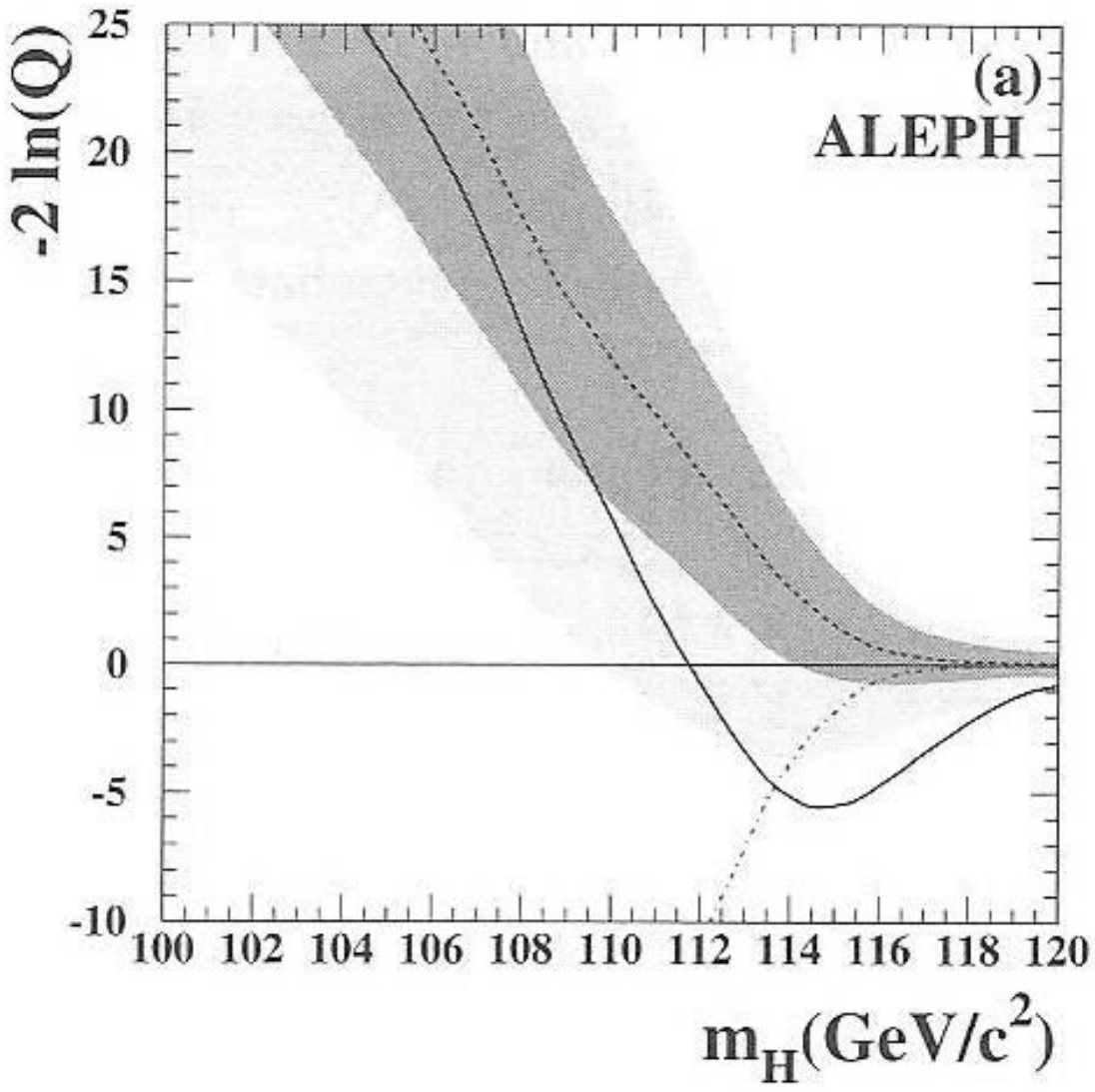


Fig.8. ALEPH results with about 3 standard deviation at mass 115 GeV; observed (solid line) and the expected behaviors of the test statistic (dark region) are presented and discussed in [1].

Table 3. Representation of parameters of tuning effects in particle masses (upper part) and in nuclear data by the expression $(n \times m_e(\alpha/2\pi)^x) \times m$ with $\alpha=137^{-1}$ [5]. Asterisk marks stable intervals observed in low-energy excitations and neutron resonances; ε_{np}=340 keV is discussed in the text, Fig.7

x	m	n=1/8	n=1	n=13	n=16	n=17	n=18
-1	1			M_Z=91.188	M_H=115		
GeV	3				$2m_t$=348		
0	1	$2m_e$	$16m_e$	m_μ=105.658		m_π-m_e	147=ΔM_Δ
MeV	1	ε_o	δ	106.4=ΔE_B	130=ΔE_B	140=ΔE_B	147=ΔE_B
	3				M''_q=$m_\rho/2 \approx m_\omega/2$	M'_q=420	M_q=441=ΔE_B
1	1	1.2*	9.48=δ'*	123*	152*	161*	170*
keV	2			246*	303*	321*	ε_{np}=340=$\varepsilon_o/3$
	3			368*	455*	481*	511=$\varepsilon_o/2$
	8	9.5*	76*	984, Fig.8	1212*	1293=D_o	1360, Fig.8
2	1		11*	143*	176*	187*	D in neutron
eV	4	5.5*	44*	572*		750 - 1500*	resonances

Lepton ratio as the distinguished parameter

Earlier, as a realization of Nambu's suggestion to search for empirical mass relations needed for SM-development, it was noticed in [5,6] that

1) the well-known lepton ratio L=$m\mu/me$=206.77 becomes the integer 207=9*23=13*16-1 after a small QED radiative correction applied to me (it becomes $m\mu/me(1-\alpha/2\pi)$=207.01)

2) the same ratio L=207 exists between masses of vector bosons MZ=91.188(2) GeV and MW=80.40(3) GeV and two above discussed estimates of baryon/meson constituent quark masses Mq=441 MeV=$m\Xi_c/3=(3/2)(m_\Delta-m_N)$ and $M''q=m\rho/2$=775.5(4) MeV/2=387.8(2) MeV

[1] (MZ/441 MeV=206.8; $MW/(m_\rho/2)$=207.3 [5,6]). The origin of these effects should be considered in the complex analysis of tunung effects in particle masses and in nuclear data [5,6].

Conclusions

The QCD-based estimates of the constituent quark masses ($M0\ q$=420 MeV, Mq=441 MeV, $M''q$) could play important role in the description of Standard Model dynamics if the observed now empirical relations in particle masses (and value MH) would be confirmed in the experiment.

Nuclear data can provide some important additional information on fundamental properties of strong nucleon interactions and nuclear matter as well as general properties of fermion systems.