

# Quark helicity distributions in COMPASS experiment at CERN

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on behalf of the COMPASS collaboration

SYMMETRIES AND SPIN (SPIN-Praha-2008)  
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- 1 COMPASS experiment
  - Spectrometer setup
  - Physics motivation and used methods

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  - Inclusive asymmetry  $A_1^d$
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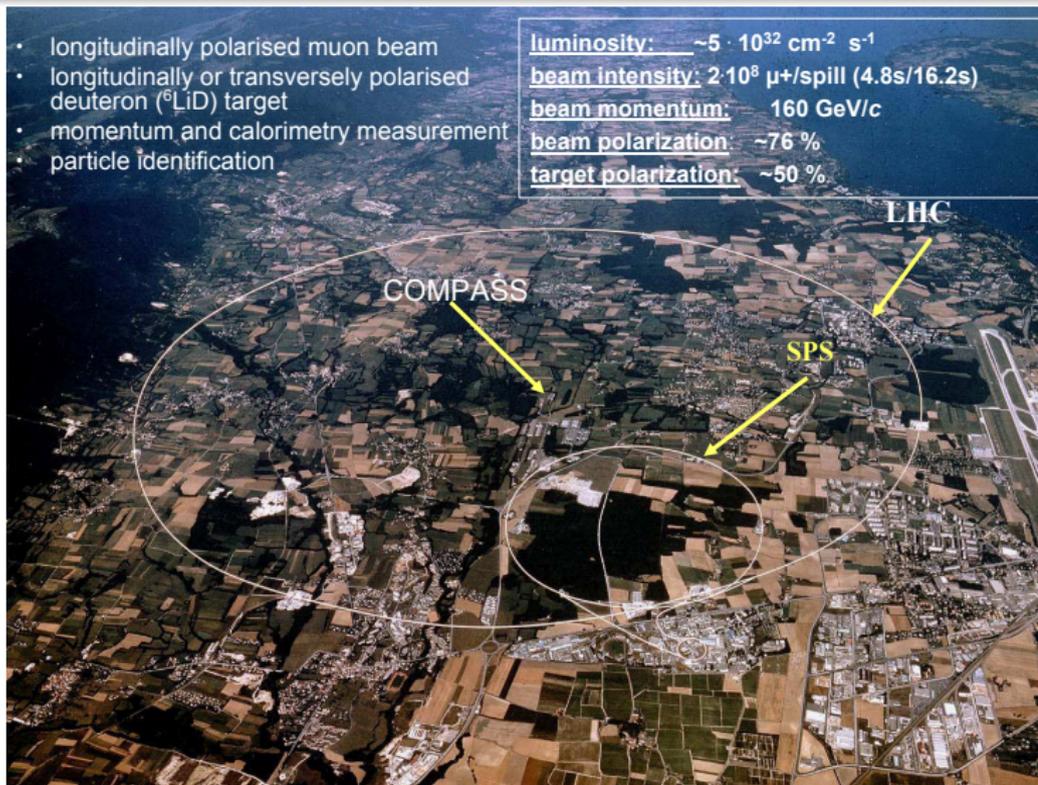
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- 4 Estimation of statistical precision with 2006&2007 data

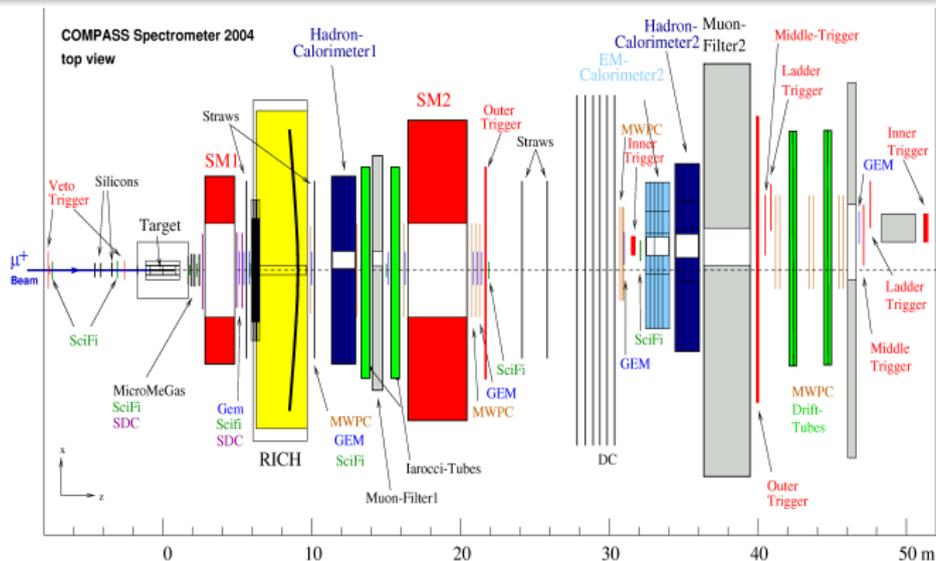
# COMPASS experiment at CERN

- longitudinally polarised muon beam
- longitudinally or transversely polarised deuteron ( $^6\text{LiD}$ ) target
- momentum and calorimetry measurement
- particle identification

luminosity:  $\sim 5 \cdot 10^{32} \text{ cm}^{-2} \text{ s}^{-1}$   
beam intensity:  $2 \cdot 10^8 \mu\text{+}/\text{spill} (4.8\text{s}/16.2\text{s})$   
beam momentum: 160 GeV/c  
beam polarization:  $\sim 76 \%$   
target polarization:  $\sim 50 \%$



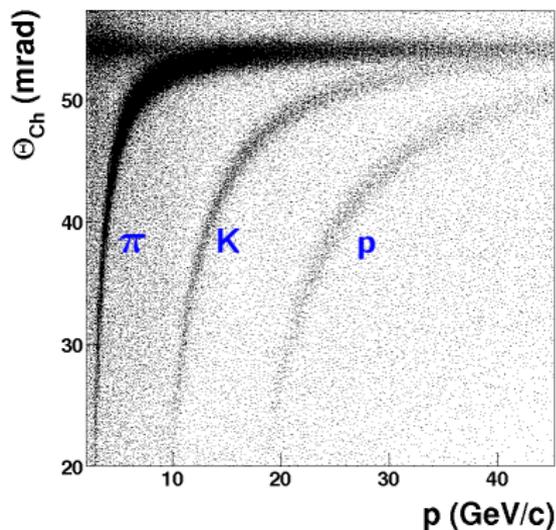
# COMPASS spectrometer



- Two parts of spectrometer (60m length in total)
- About 350 detector planes of different type
- Polarized beam:  $\mu^+$  ( $P_B=80\%$  at 160GeV)
- Polarized target:  ${}^6\text{LiD}$  ( $P_T=50\%$ ) and  $\text{NH}_3$  ( $P_T=90\%$ )
- Particle identification by RICH, ECALs, HCALs and  $\mu$ -filter

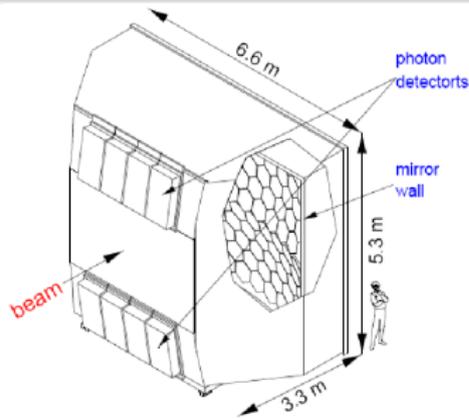


# Ring Imaging Cherenkov detector

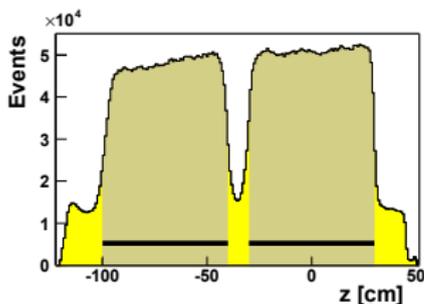
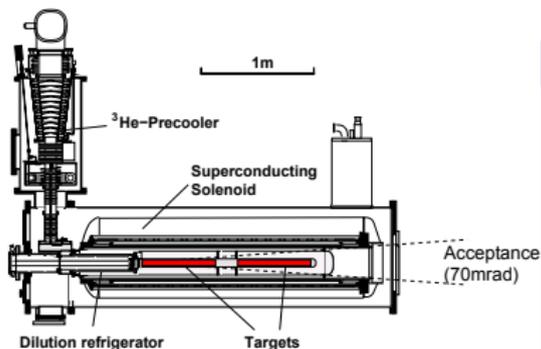


## RICH features

- $\pi$ ,  $K$ ,  $p$  separation from 2, 9, 18 GeV up to 50 GeV
- 116 spherical mirrors (21 m<sup>2</sup>)
- 80 m<sup>3</sup> C<sub>4</sub>F<sub>10</sub>,  $n=1.00153$
- $\langle n \rangle = 15$



# The polarized target (2002-2004)



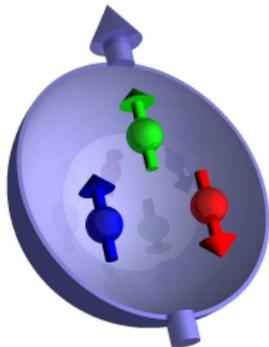
## Target features

- target material  $^6\text{LiD}$
- Dynamic Nuclear Polarization technique
- polarization about 50%
- acceptance: 70 mrad
- solenoid field: 2.5T
- temperature ( $^3\text{He}$ ,  $^4\text{He}$ ): 50mK
- two cells with opposite polarization
- target length: 60 cm each cell
- dilution factor  $\approx 0.4$

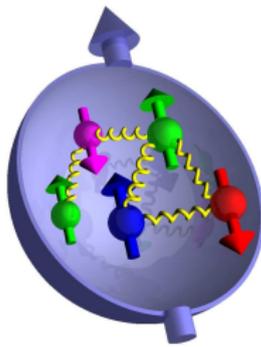
# The spin of the nucleon

## Angular momentum conservation

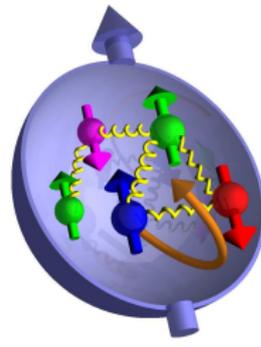
$$\frac{1}{2} = \frac{1}{2}\Delta\Sigma + \Delta G + L_q + L_g$$



Constituent (naive)  
parton model:  
 $\Delta\Sigma = \Delta u_v + \Delta d_v = 1$



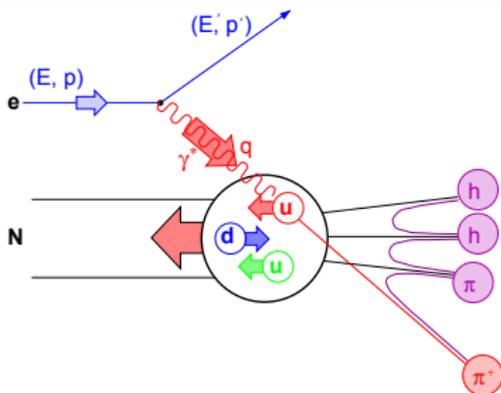
Is contribution from  
gluons important  
as in unpolarized  
case?



Full description  
should take into  
account orbital  
angular momenta



# Deep inelastic scattering



Kinematical variables:

- $Q^2 = -q^2$
- $\nu = E - E'$
- $x = Q^2/2M\nu$
- $y = \nu/E$
- $z = E_h/\nu$

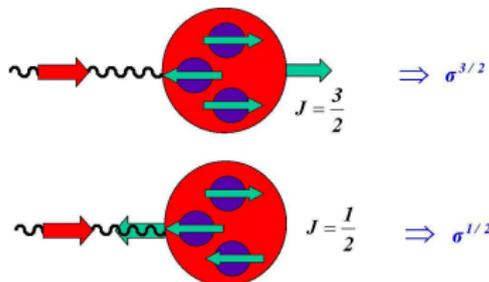
## Inclusive cross-section

$$\frac{d^2\sigma}{d\Omega dE'} = c_1 F_1(x, Q^2) + c_2 F_2(x, Q^2) + c_3 g_1(x, Q^2) + c_4 g_2(x, Q^2)$$

where  $g_1, g_2$  and  $F_1, F_2$  are spin **dependent** and spin **independent** structure functions.



# Polarized deep inelastic scattering



Quark densities in QPM:

- $q(x) = q^+(x) + q^-(x)$
- $\Delta q(x) = q^+(x) - q^-(x)$

$q^+(x), q^-(x)$ : quarks polarized parallel (antiparallel) to nucleon spin

- Photon-nucleon asymmetry:

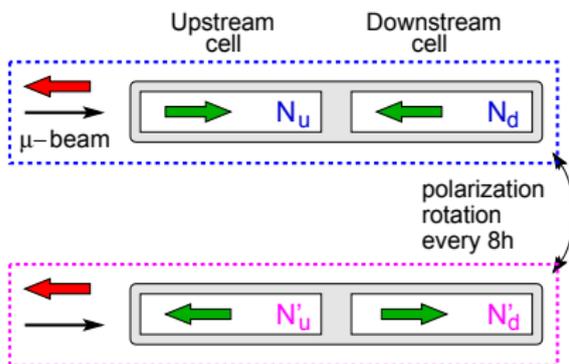
$$A_1 = \frac{\sigma_{1/2} - \sigma_{3/2}}{\sigma_{1/2} + \sigma_{3/2}} = \frac{\sum_q e_q^2 \Delta q}{\sum_q e_q^2 q} = \frac{g_1}{F_1} = \frac{2x(1+R)}{F_2} g_1, \quad R = \sigma_L / \sigma_T$$

- Longitudinal asymmetry:

$$A_{\parallel} = \frac{\sigma^{\uparrow\downarrow} - \sigma^{\uparrow\uparrow}}{\sigma^{\uparrow\downarrow} + \sigma^{\uparrow\uparrow}} \approx DA_1 \implies g_1 = \frac{A_{\parallel}}{D} \cdot \frac{F_2}{2x(1+R)}$$



# Experimental asymmetry



- Target cells polarized in opposite direction
- Acceptance for both cells is not the same
- Polarization reversed every 8 hours

Experimental asymmetry:

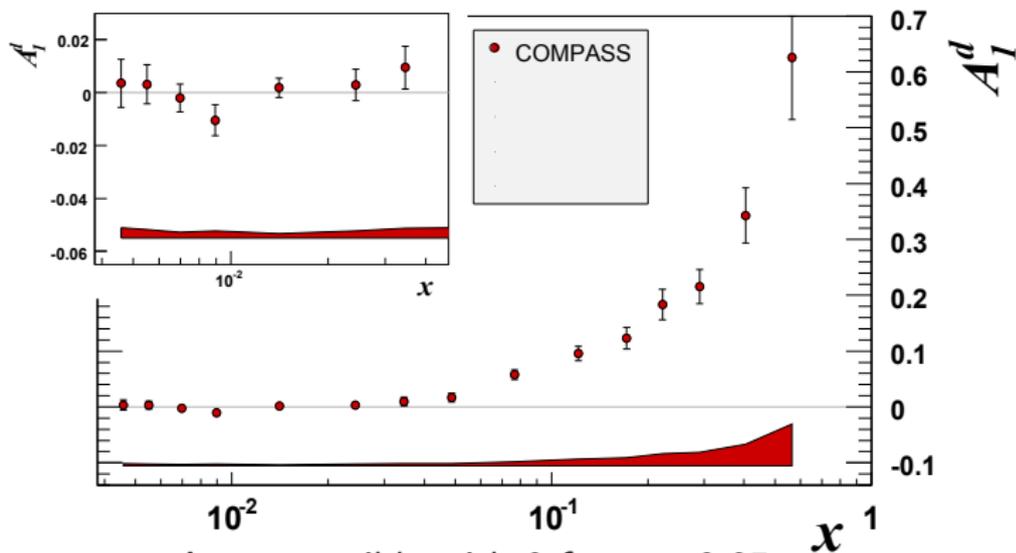
$$A_{exp} = \frac{1}{2} \left( \frac{N_u - N_d}{N_u + N_d} + \frac{N'_d - N'_u}{N'_d + N'_u} \right) = f P_B P_T A_{||}$$

$P_B, P_T$  - beam and target polarization

$f$  - dilution factor



# Inclusive asymmetry for $Q^2 > 1 \text{ GeV}^2$

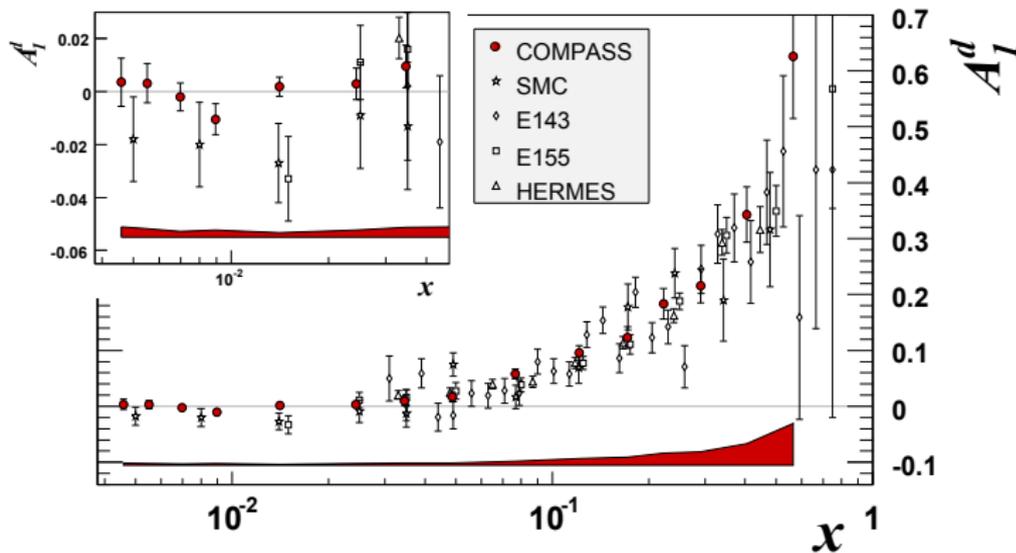


$Q^2 > 1 \text{ GeV}^2$   
 $0.004 < x < 0.7$   
 $0.1 < y < 0.9$   
 $\sim 10^8$  events

- $A_1$  compatible with 0 for  $x < 0.05$
- Large asymmetry at large  $x$
- Sys. errors:  $P_B(5\%), P_T(5\%), f(3\%), D(6\%) \Rightarrow \delta A_1 \approx 0.1 A_1$
- Results from 2002-2004, published in PLB 647 (2007) 8



# Inclusive asymmetry for $Q^2 > 1\text{GeV}^2$ , comparison



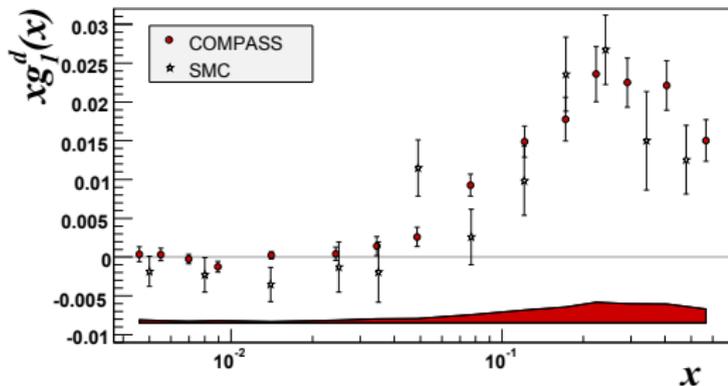
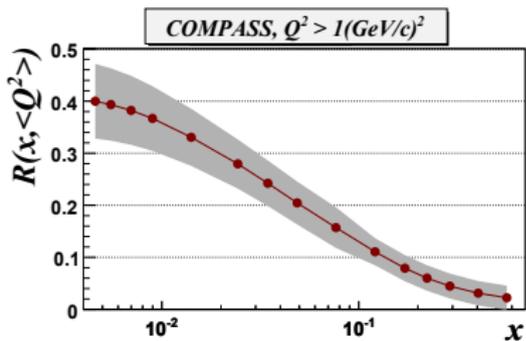
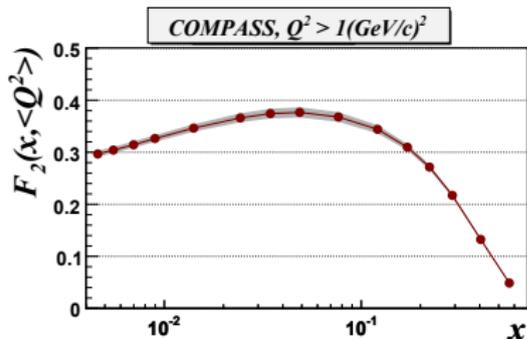
$Q^2 > 1\text{GeV}^2$   
 $0.004 < x < 0.7$   
 $0.1 < y < 0.9$   
 $\sim 10^8$  events

- Good agreement with previous experiments
- Significant improvement at low  $x$  region
- No tendency towards negative values at  $x < 0.03$



# Parametrization of $F_2$ and $R$

$$g_1 = \frac{F_2}{2x(1 + R)} A_1$$



# NLO QCD analysis

$$\Delta\Sigma = \Delta u + \Delta d + \Delta s, \quad \Delta q_3 = \Delta u - \Delta d, \quad \Delta q_8 = \Delta u + 2\Delta d - \Delta s$$

- Spin dependent structure function  $g_1$ :

$$g_1^d(x, Q^2) = \frac{1}{2} \langle e^2 \rangle [C_q^S \otimes \Delta\Sigma + C_q^{NS} \otimes \Delta q^{NS} + 2n_f C_G \otimes \Delta G]$$

- DGLAP equations:

$$\frac{d}{dt} \Delta q^{NS} = \frac{\alpha_s(t)}{2\pi} P_{qq}^{NS} \otimes \Delta q^{NS}, \quad t = \log\left(\frac{Q^2}{\Lambda^2}\right)$$

$$\frac{d}{dt} \begin{pmatrix} \Delta\Sigma \\ \Delta G \end{pmatrix} = \frac{\alpha_s(t)}{2\pi} \begin{pmatrix} P_{qq}^S & 2n_f P_{qG}^S \\ P_{Gq}^S & P_{GG}^S \end{pmatrix} \otimes \begin{pmatrix} \Delta\Sigma \\ \Delta G \end{pmatrix}$$

- Input parametrization at fixed  $Q_0^2$ :

$$(\Delta\Sigma, \Delta q_3, \Delta q_8, \Delta G) = \eta \frac{x^\alpha (1-x)^\beta (1+\gamma x)}{\int_0^1 x^\alpha (1-x)^\beta (1+\gamma x) dx}$$

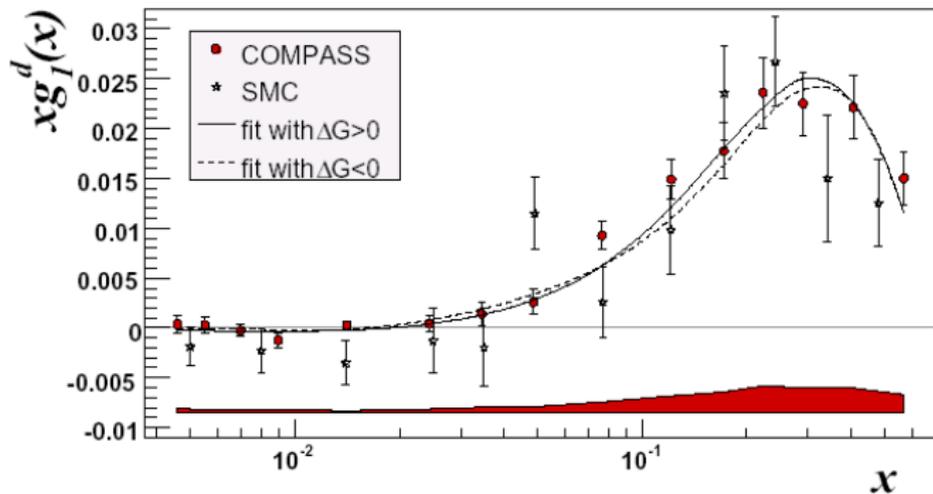
- Minimization routine:

$$\chi^2 = \sum_{i=1}^N \frac{[g_1^{calc}(x, Q^2) - g_1^{exp}(x, Q^2)]^2}{[\sigma_{stat}^{exp}(x, Q^2)]^2}$$

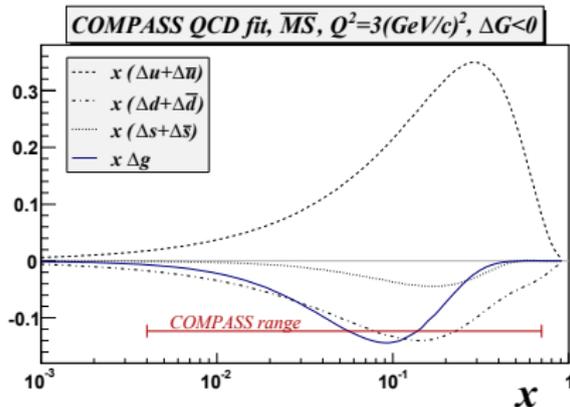
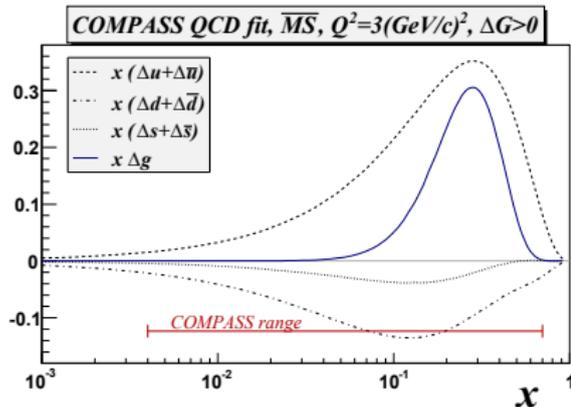


# QCD fits

- Two different approaches in NLO  $\overline{\text{MS}}$  scheme have been used
  - Numerical integration in  $(x, Q^2)$  space (PRD 58 (1998) 112002)
  - Solution of DGLAP in space of moments (PRD 70 (2004) 074032)
- Fit to world data (9 experiments, 230 points in total)
- Two solutions describe data equally well:  $\Delta G < 0$  and  $\Delta G > 0$



# Polarized parton distributions



- Quark distributions are quite similar for two solutions
- Polarization of quarks  $\eta_\Sigma = \int \Delta q_{Si}(x) dx$   
 $\eta_\Sigma = 0.30 \pm 0.01(\text{stat}) \pm 0.02(\text{evol})$



# First moment of $g_1$

- COMPASS data only

$$\Gamma_1^N(Q^2 = 3\text{GeV}^2) = \int_0^1 g_1^N(x) dx =$$

$$0.0502 \pm 0.0028(\text{stat}) \pm 0.0020(\text{evol}) \pm 0.0051(\text{syst})$$

- data for  $0.004 < x < 0.7$ , QCD fit used for extrapolation
- contribution from unmeasured region about 4%
- Extracting  $a_0$  from the first moment of  $g_1^N$  (NLO QCD):

$$\Gamma_1^N(Q^2) = \frac{1}{9} \left( 1 - \frac{\alpha_s(Q^2)}{\pi} + \mathcal{O}(\alpha_s^2) \right) \left( a_0(Q^2) + \frac{1}{4} a_8 \right)$$

- From hyperon  $\beta$  decays assuming  $SU(3)_f$

$$a_8 = 0.585 \pm 0.025 \quad (\text{Y.Goto et. al., PRD62(2000)034017})$$

- Quark polarization at  $Q^2 = 3\text{GeV}^2$ :

$$a_0 = 0.35 \pm 0.03(\text{stat}) \pm 0.05(\text{syst})$$

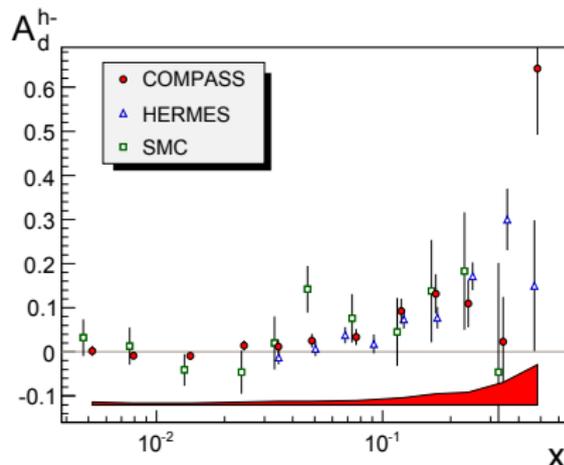
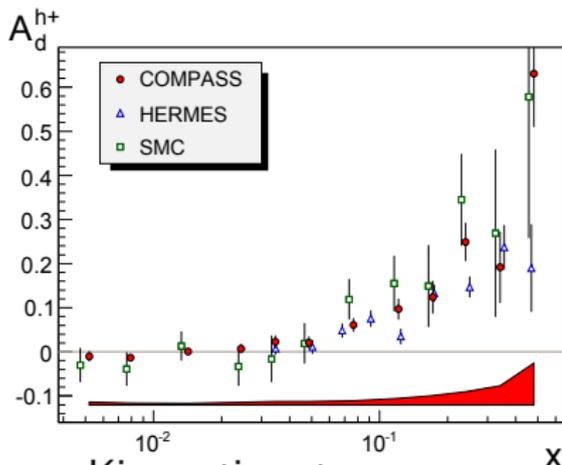
$$\eta_\Sigma = 0.30 \pm 0.01(\text{stat}) \pm 0.02(\text{evol})$$



# Single hadron asymmetries

$$A^h = \frac{\sigma_{\downarrow\downarrow}^h - \sigma_{\uparrow\uparrow}^h}{\sigma_{\uparrow\downarrow}^h + \sigma_{\downarrow\uparrow}^h} \xrightarrow{\text{QPM}}$$

$$\frac{\sum_q e_q^2 (\Delta q(x) D_q^h + \Delta \bar{q}(x) D_{\bar{q}}^h)}{\sum_q e_q^2 (q(x) D_q^h + \bar{q}(x) D_{\bar{q}}^h)}$$



- Kinematic cuts:

$$Q^2 > 1(\text{GeV}/c)^2, 0.1 < y < 0.9, 0.2 < z < 0.85$$

- Final statistics:  $N^+ = 30 \cdot 10^6$ ,  $N^- = 25 \cdot 10^6$ ,  
 $\text{corr}(N^+, N^-) \approx 20\%$



# Difference asymmetry

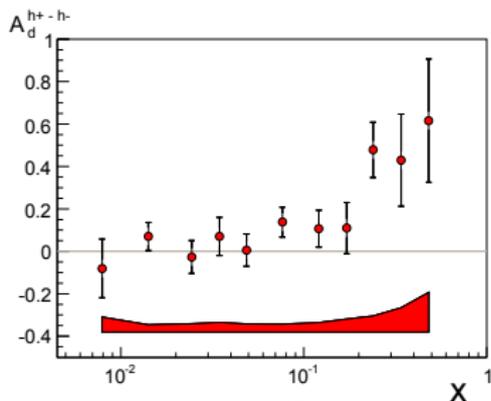
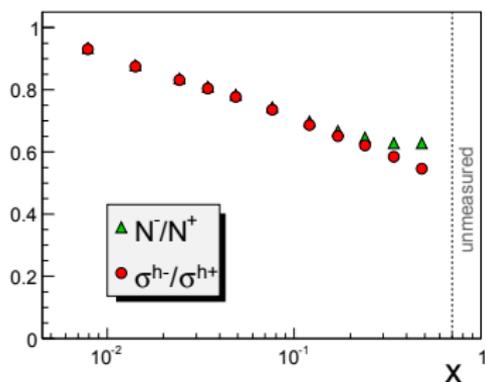
- Definition:  $A^{h^+-h^-} = \frac{(\sigma_{\uparrow\downarrow}^{h^+} - \sigma_{\uparrow\downarrow}^{h^-}) - (\sigma_{\uparrow\uparrow}^{h^+} - \sigma_{\uparrow\uparrow}^{h^-})}{(\sigma_{\uparrow\downarrow}^{h^+} - \sigma_{\uparrow\downarrow}^{h^-}) + (\sigma_{\uparrow\uparrow}^{h^+} - \sigma_{\uparrow\uparrow}^{h^-})}$

- In LO FF cancel out. For a deuteron target:

$$A_d^{\pi^+-\pi^-}(x) = A_d^{K^+-K^-}(x) = \frac{\Delta u_v(x) + \Delta d_v(x)}{u_v(x) + d_v(x)}$$

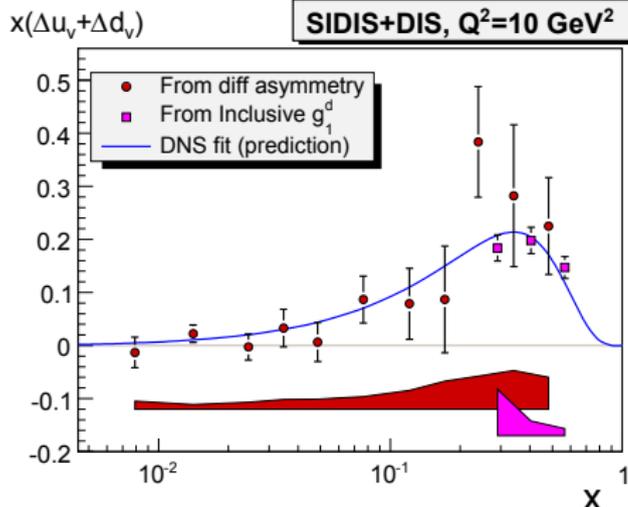
- $A^{h^+-h^-}$  calculated from  $A^{h^+}$  and  $A^{h^-}$ :

$$A^{h^+-h^-} = \frac{1}{1-r}(A^{h^+} - rA^{h^-}), \quad r = \frac{\sigma_{\uparrow\downarrow}^{h^-} + \sigma_{\uparrow\uparrow}^{h^-}}{\sigma_{\uparrow\downarrow}^{h^+} + \sigma_{\uparrow\uparrow}^{h^+}} = \frac{\sigma^{h^-}}{\sigma^{h^+}} = \frac{N^-/a^-}{N^+/a^+}$$



# Valence quark distribution

$$x(\Delta x_v(x) + \Delta d_v(x)) = \frac{x(u_v(x) + d_v(x))}{(1+R(x))(1-1.5\omega_D)} A^{h^+ - h^-}(x), \quad \omega_D = 0.05 \pm 0.01$$



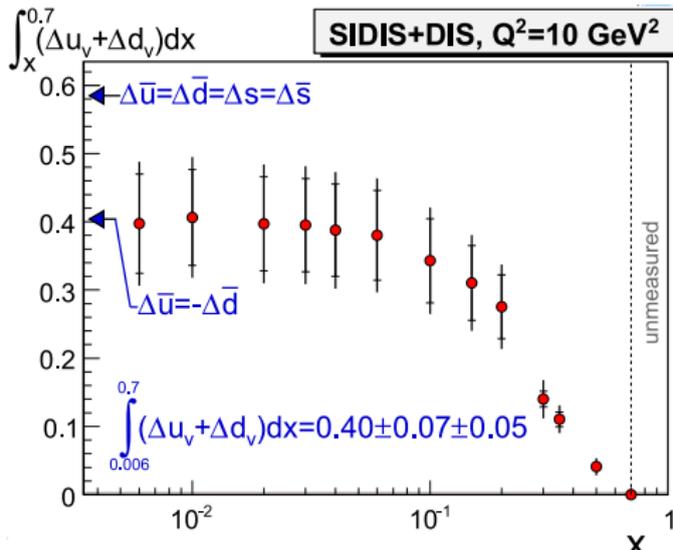
- evolved to  $Q^2 = 10 \text{ (GeV/c)}^2$
- using LO DNS parameterization (PRD 71(2005)094018)
- DNS predicts COMPASS data
- for  $u_v + d_v$  MRST04(LO) used

sea very small at large  $x$ , with inclusive asymmetry much better precision

$$\Delta u_v + \Delta d_v = \frac{36}{5} \frac{g_1^d(x, Q^2)}{(1 - 1.5\omega_D)} - \left[ 2(\Delta \bar{u} + \Delta \bar{d}) + \frac{2}{5}(\Delta \bar{s} + \Delta \bar{c}) \right]$$



# Estimate for the first moment (LO)



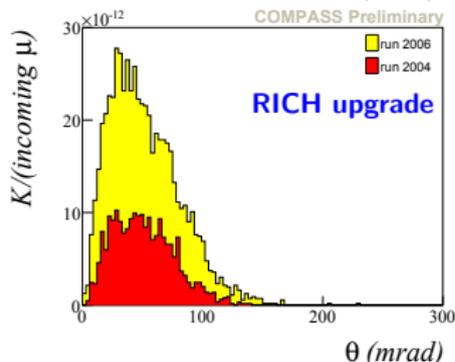
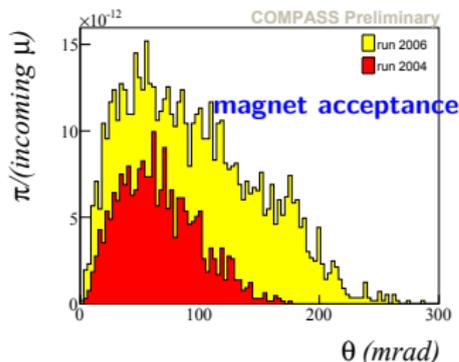
- First moment  
 $\Gamma_v = \int_0^1 (\Delta u_v(x) + \Delta d_v(x)) dx$
- Contribution from  $x > 0.7$  about 0.004 (DNS fit)
- $\Gamma_v$  (DIS+SIDIS) is  $2.5\sigma_{stat}$  away from the symmetric sea scenario, asymmetric sea favoured



# Estimation of the statistical errors with 2006 and 2007 data



## 2006 setup

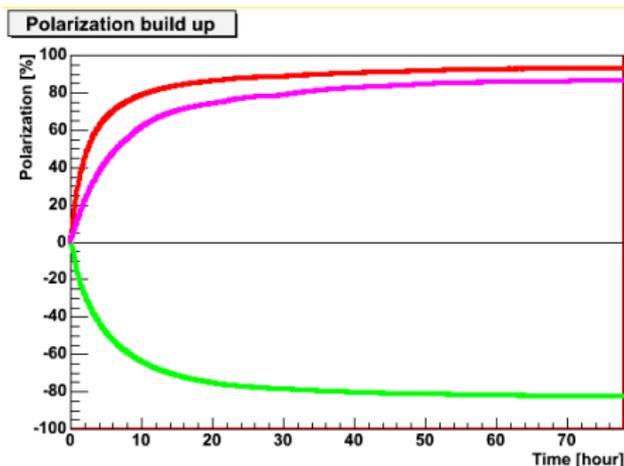


- New target magnet:
  - angular acceptance increased to 180mrad
  - 3 cells used to reduce false asymmetries
- RICH upgrade
- ECAL1 included
- RICH Wall - preshower for ECAL1
- more large angle trackers in first stage
- gain mainly in high  $x$  and  $Q^2$

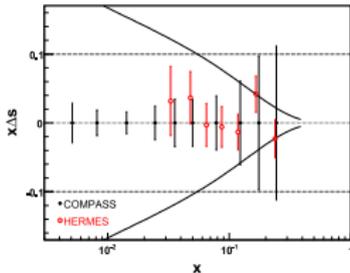
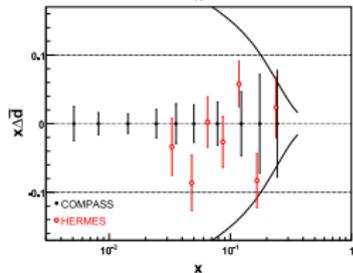
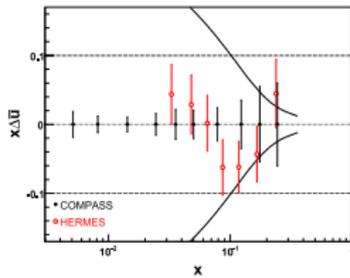
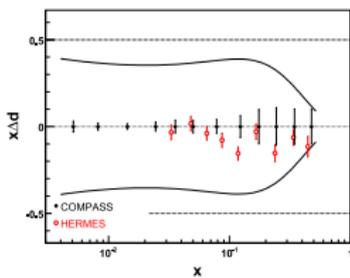
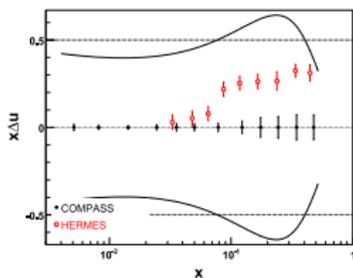


## 2007 setup

- New target material:  $\text{NH}_3$ 
  - proton data will allow to distinguish  $u$  and  $d$  polarization
  - very high polarization (90%)
- new trigger using ECAL1
- longitudinal and transverse polarization



# Expectations with 2007 (proton) and 2002-2006 (deuteron) data



	0.004 – 0.03	0.004 – 0.7
$\delta(\delta u_V)$	0.020	0.07
$\delta(\delta d_V)$	0.036	0.11
$\delta(\delta \bar{u})$	0.013	0.04
$\delta(\delta \bar{d})$	0.017	0.05
$\delta(\delta s)$	0.003	0.09



# Summary

- Analysis of 2002-2004 deuteron data has been presented
- QCD fits to world data give for quark and gluon contributions:

$$\eta_{\Sigma}(Q_0^2 = 3(\text{GeV}/c)^2) = 0.30 \pm 0.01(\text{stat}) \pm 0.02(\text{evol})$$

- From the first moment of  $g_1^d$  we obtained quark contribution to the nucleon spin (at  $Q^2 = 3\text{GeV}$ ):

$$\Delta\Sigma = 0.35 \pm 0.03(\text{stat}) \pm 0.05(\text{syst})$$

- $\Delta u_v$  and  $\Delta d_v$  have been extracted from difference asymmetry for  $x < 0.3$  and from  $g_1^d$  for  $x > 0.3$
- $\int_{0.006}^{0.7} (\Delta u_v + \Delta d_v) dx = 0.4 \pm 0.07(\text{stat}) \pm 0.05(\text{syst})$
- Analysis of 2006 and 2007 data is in progress - update of analysis soon

