

Astrophysical Constraints on the Nuclear Matter Equation of State

Helmholtz International Summerschool

Nuclear Theory and Astrophysical Applications

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Part 1: Neutron Stars - Masses and Radii

Part 2: Consistence with modern Equations of State

Overview

- ➔ relativistic mean field (RMF): Walecka
- ➔ parameterisation of realistic models
- ➔ neutron star constraints (last session)
- ➔ symmetric matter: flow constraint
- ➔ cooling neutron stars: direct Urca
- ➔ quark matter phase transition

Walecka model for dense nuclear matter

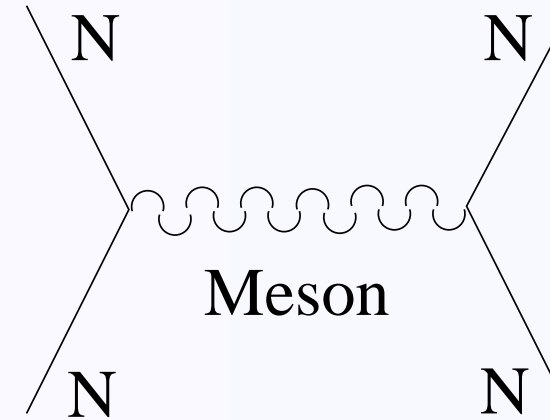
Meson exchange model

example: scalar (σ) meson

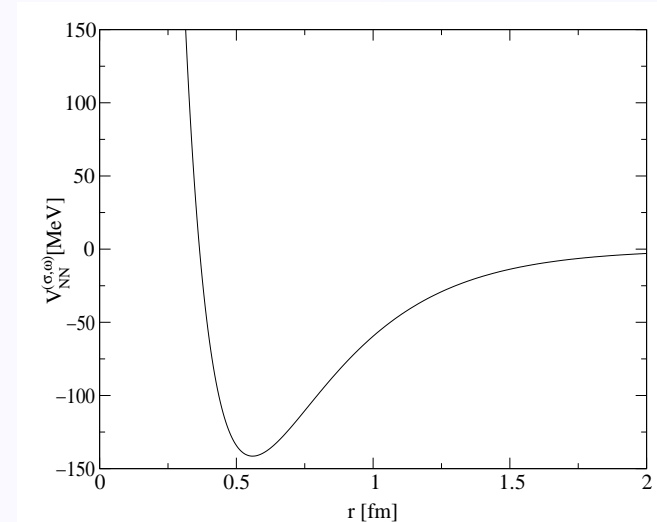
$$(-\Delta + m_\sigma^2)\sigma(\vec{r}) = -g_\sigma\delta(\vec{r})$$

$$\Rightarrow \sigma(r) = -\frac{g_\sigma}{4\pi} \frac{e^{-m_\sigma r}}{r}$$

$$V_{NN}^{(\sigma)}(r) = g_\sigma\sigma(r) = -\frac{g_\sigma^2}{4\pi} \frac{e^{-m_\sigma r}}{r}$$



Meson	I^π	T	S	M[MeV]
π^0, π^\pm	0^-	1	0	140
σ	0^+	0	0	≈ 500
K^0, K^\pm	0^-	1/2	± 1	495
η	0^-	0	0	550
ρ^0, ρ^\pm	1^-	1	0	770
ω	1^-	0	0	780
δ	0^+	1	0	900



Walecka model for dense nuclear matter

Field theoretical formulation: Lagrangian and Path Integral for Partition Function

$$\mathcal{Z}_{gk}(T, V, \{\mu_i\}) = \int [d\bar{\Psi}][d\Psi] \exp \left\{ \int_0^{\beta=1/T} d\tau \int_V d^3\vec{x} (\mathcal{L}_0 + \mathcal{L}_I + \mu_p \Psi_p^+ \Psi_p + \mu_n \Psi_n^+ \Psi_n) \right\}$$

$$\mathcal{L}_0(\tau, \vec{x}) = \bar{\Psi}(\tau, \vec{x}) (i\gamma_\mu \partial_\mu - m_N) \Psi(\tau, \vec{x})$$

$$\mathcal{L}_I(\tau, \vec{x}) = j_{\omega_\mu}(\tau, \vec{x}) \frac{G_\omega}{2} j_{\omega_\mu}(\tau, \vec{x}) - j_\sigma(\tau, \vec{x}) \frac{G_\sigma}{2} j_\sigma(\tau, \vec{x})$$

$$\begin{aligned} j_\sigma(\tau, \vec{x}) &= \bar{\Psi}(\tau, \vec{x}) \Psi(\tau, \vec{x}) \\ j_{\omega_\mu}(\tau, \vec{x}) &= \bar{\Psi}(\tau, \vec{x}) \gamma_\mu \Psi(\tau, \vec{x}) \end{aligned} \quad \Psi = \begin{pmatrix} \psi_n \\ \psi_p \end{pmatrix}; \quad \psi_n = \begin{pmatrix} u_{n, \uparrow} \\ u_{n, \downarrow} \\ v_{n, \uparrow} \\ v_{n, \downarrow} \end{pmatrix} \left. \begin{array}{l} \text{Neutron} \\ \text{Antineut.} \end{array} \right\}$$

$\mu_n = \mu_p \quad \rightarrow \quad$ symmetric nuclear matter

$\mu_n \neq 0; \mu_p = 0 \quad \rightarrow \quad$ pure neutron matter

$\mu_n = \mu_p + \mu_{e^-} \quad \rightarrow \quad$ neutron star matter (β -equilibrium)

Walecka model for dense nuclear matter

Evaluation of the Path Integral: Hubbard-Stratonovich trick

$$\exp\left(-(\bar{\Psi}\Psi) \frac{G_\sigma}{2} (\bar{\Psi}\Psi)\right) = (\det G_\sigma^{-1})^{\frac{1}{2}} \int [d\sigma] \exp\left(\frac{\sigma^2}{2G_\sigma} + \sigma \bar{\Psi}\Psi\right)$$

Effective action quadratic \implies Gaussian Path Integral

$$\mathcal{S} \equiv \int_0^\beta d\tau \int d^3\vec{x} \left\{ \bar{\Psi}(\vec{x}, \tau) \left(-\gamma_0 \frac{\partial}{\partial \tau} + i\vec{\gamma}\vec{\nabla} - m_N + \gamma_0\mu + \sigma - \gamma_0\omega_0 \right) \Psi(\vec{x}, \tau) + \frac{\sigma^2}{2G_\sigma} - \frac{\omega_0^2}{2G_{\omega_0}} \right\}$$

Fourier representation: $\Psi(\vec{x}, \tau) = \sqrt{\frac{T}{V}} \sum_n \sum_{\vec{p}} e^{i(\vec{p}\vec{x} + \omega_n\tau)} \Psi_n(\vec{p})$, with $\omega_n \equiv \pi T(2n + 1)$

$$\begin{aligned} & \int_0^\beta d\tau \int d^3\vec{x} \bar{\Psi}(\vec{x}, \tau) \left(-\gamma_0 \frac{\partial}{\partial \tau} + i\vec{\gamma}\vec{\nabla} - m_N + \gamma_0\mu + \sigma - \gamma_0\omega_0 \right) \Psi(\vec{x}, \tau) \\ &= \beta \sum_n \sum_{\vec{p}} \bar{\Psi}_n(\vec{p}) (-\gamma_\mu p_\mu - m_N^*) \Psi_n(\vec{p}) = \sum_n \sum_{\vec{p}} \bar{\Psi}_n(\vec{p}) G^{-1}[\sigma, \omega_0] \Psi_n(\vec{p}) \end{aligned}$$

Effective mass $m_N^* = m_N - \sigma$, chemical potential $\mu^* = \mu - \omega_0$ and quasiparticle propagator

$$G^{-1}[\sigma, \omega] = -\beta(\gamma_\mu p_\mu + m_N^*) , \quad p_0 = i\omega_n - \mu^*$$

Walecka model for dense nuclear matter

Evaluate fermionic Path Integral and mean field approximation:

$$\begin{aligned}
 \mathcal{Z}_{gk}(T, V, \{\mu_i\}) &= \mathcal{N} \prod_{n, \vec{p}} \int [d\bar{\Psi}_n][d\Psi_n][d\sigma][d\omega_0] \exp \left\{ \sum_{n, \vec{p}} \bar{\Psi}_n G^{-1}[\sigma, \omega_0] \Psi_n + \frac{\sigma^2}{2G_\sigma} - \frac{\omega_0^2}{2G_{\omega_0}} \right\} \\
 &= \int [d\sigma][d\omega_0] \exp \left\{ Tr \ln G^{-1}[\sigma, \omega_0] + \frac{\sigma^2}{2G_\sigma} - \frac{\omega_0^2}{2G_{\omega_0}} \right\} \\
 &= \exp \left\{ Tr \ln G^{-1}[\bar{\sigma}, \bar{\omega}_0] + \frac{\bar{\sigma}^2}{2G_\sigma} - \frac{\bar{\omega}_0^2}{2G_{\omega_0}} \right\}
 \end{aligned}$$

Stationarity condition: $\partial \ln \mathcal{Z}_{gk} / \partial \bar{\sigma} = \partial \ln \mathcal{Z}_{gk} / \partial \bar{\omega}_0 = 0$ corresponds to

$$\bar{\sigma} = -G_\sigma Tr G[\bar{\sigma}, \bar{\omega}_0] = G_\sigma n_s, \quad \bar{\omega}_0 = -G_\omega Tr \gamma_0 G[\bar{\sigma}, \bar{\omega}_0] = G_\omega n.$$

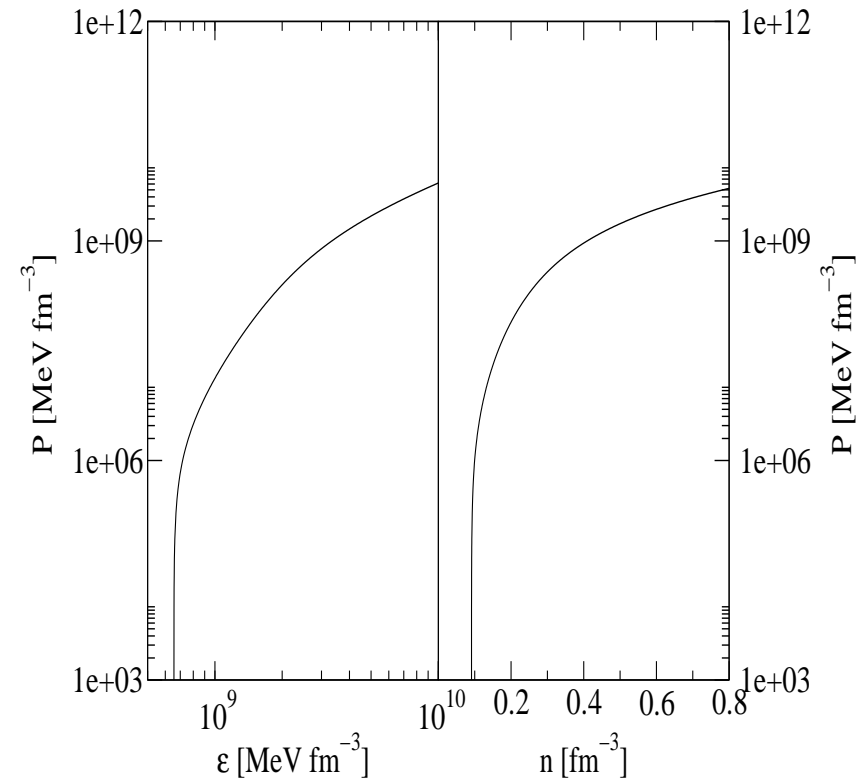
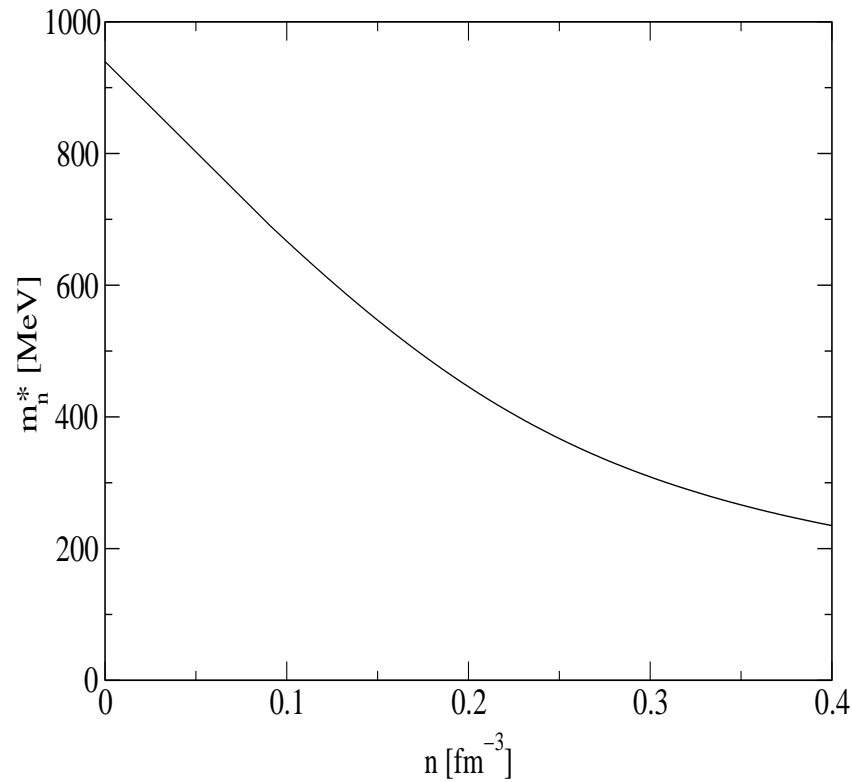
Thermodynamics: $\Omega(T, V, \mu) = -T \ln \mathcal{Z}_{gk} = -pV$

$$p(\mu, T) = \frac{1}{2} G_\omega n^2 - \frac{1}{2} G_\sigma n_s^2 + 4T \int \frac{d^3 \vec{p}}{(2\pi)^3} \left[\ln \left(1 + e^{-\beta(E^* - \mu^*)} \right) + \ln \left(1 + e^{-\beta(E^* + \mu^*)} \right) \right]$$

$$n = 4 \int \frac{d^3 \vec{p}}{(2\pi)^3} [f_-(E^*) - f_+(E^*)], \quad n_s = 4 \int \frac{d^3 \vec{p}}{(2\pi)^3} \frac{m_N^*}{E^*} [f_-(E^*) - f_+(E^*)]$$

Quasiparticle properties $E^* = \sqrt{\vec{p}^2 + m_N^{*2}}$, $m_N^* = m_n - G_\sigma n_s$, $\mu^* = \mu - G_\omega n$.

Walecka model for dense nuclear matter



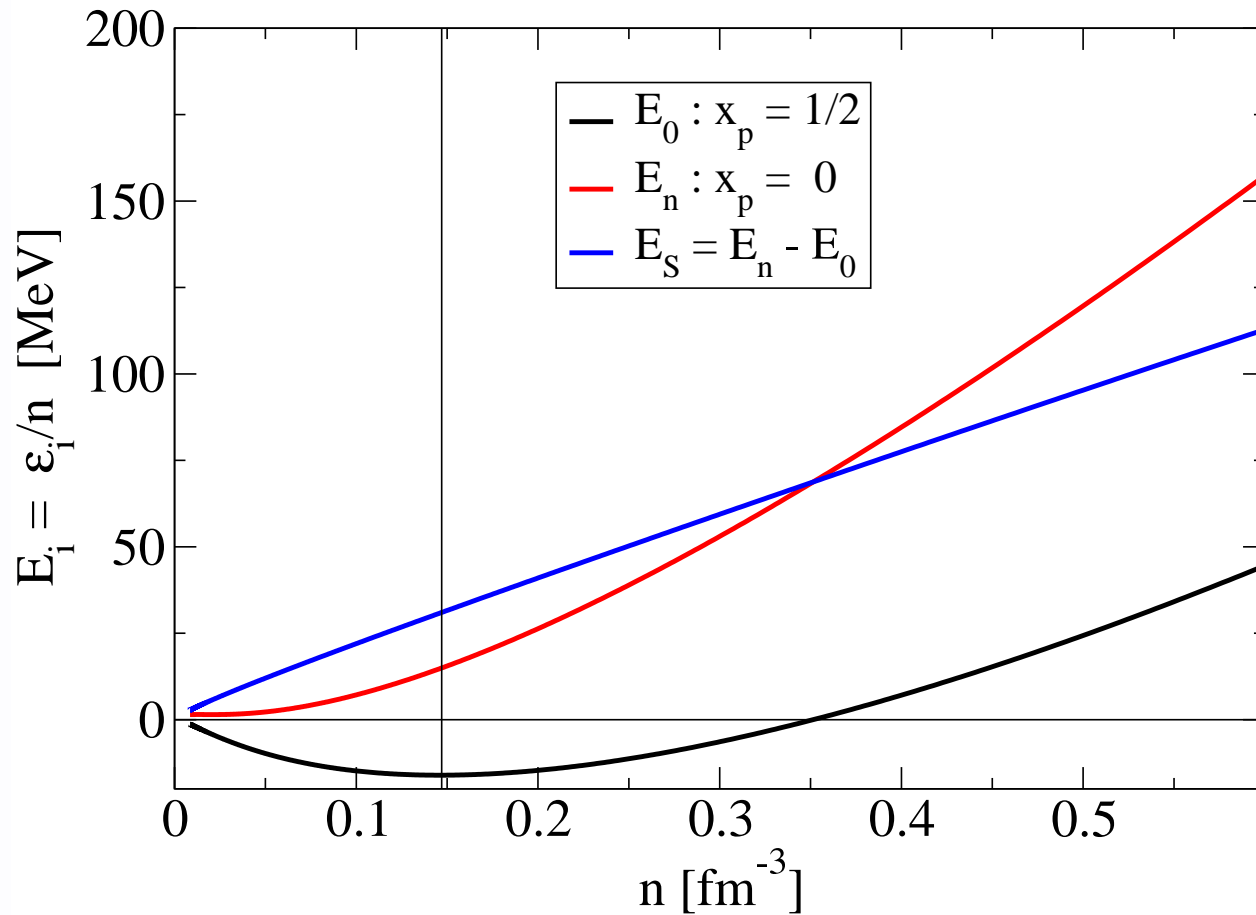
Further reading, e.g.,

Kapusta: 'Finite temperature field theory'

Glendenning: 'Compact Stars'

Symmetry Energy

Energy per particle in symmetric ($E_0(n)$) and neutron matter ($E_n(n)$) \rightarrow symmetry energy



(Link to Bethe-Weizsäcker : $E_0(n_0) \approx a_{vol}$, $E_S(n_0) \approx a_{sym}$)

Exploring the Limits - The EoS

Several approaches to describe dense nuclear matter

➔ **relativistic** Equations of State at $T = 0$ K

$$\varepsilon(n_n, n_p, n_e, n_\mu) \rightarrow \varepsilon_h(n_n, n_p) + \sum_{e,\mu} \varepsilon_i(n_i),$$

$$\mu_i = \frac{d\varepsilon}{dn_i}, P = \sum_{n,p,e,\mu} \mu_i n_i - \varepsilon_h - \varepsilon_l$$

➔ expanding energy per particle in terms of

neutron-proton asymmetry $\beta = \frac{n_n - n_p}{n_n + n_p} = 1 - 2x_p$, $n = n_n + n_p$

➔
$$\frac{B}{A}(n_n, n_p) \rightarrow \frac{B}{A}(n, \beta) = E_0(n) + \beta^2 E_S(n)$$

$$\varepsilon_h(n, \beta) = n \frac{B}{A}(n, \beta), \quad P_h(n, \beta) = n^2 \frac{\partial}{\partial n} \frac{B}{A}(n, \beta),$$

$$\mu_{n,p}(n, \beta) = \left(1 + n \frac{\partial}{\partial n}\right) E_0(n) - \left(\beta^2 \mp 2\beta - \beta^2 n \frac{\partial}{\partial n}\right) E_S(n).$$

Equations of State

➔ Phenomenological (RMF)

NL ρ , NL $\rho\delta$

non linear σ terms

(σ self interactions)

ρ - (and δ -) Mesons

DD, D³C, DD-F

density dependent couplings ($\Gamma_i \rightarrow \Gamma_i(n)$)

KVR, KVOR

density dependent mass of σ -Meson

➔ ab initio

DBHF

relativistic Dirac-Brueckner-Hartree-Fock

free N-N interaction explicitly given

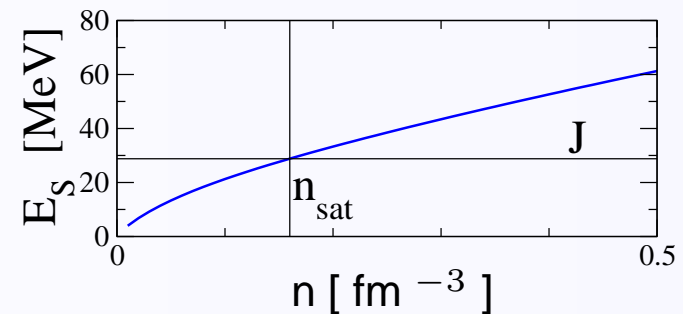
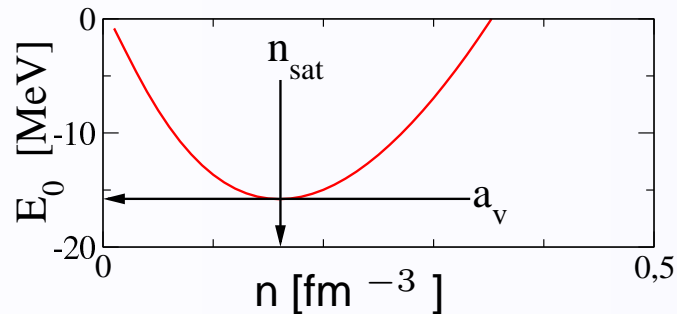
medium effects: T-Matrix (ladder approximation)

Exploring the Limits - The EoS beyond saturation

$$E(n, \beta) = E_0(n) + \beta^2 E_S(n) \approx a_V + \frac{K}{18}\epsilon^2 - \frac{K'}{162}\epsilon^3 + \dots + \beta^2 \left(J + \frac{L}{3}\epsilon + \dots \right) + \dots$$

$$\epsilon = (n - n_{sat})/n \quad \beta = (n_n - n_p)/(n_n + n_p)$$

	n_{sat}	a_V	K	K'	J	L	m_D/m
	[fm ⁻³]	[MeV]	[MeV]	[MeV]	[MeV]	[MeV]	
exp.	0.16 ± 0.01	-16 ± 1	200 – 300		25 – 35		0.6 – 1.0
NL ρ	0.1459	-16.062	203.3	576.5	30.8	83.1	0.603
NL $\rho\delta$	0.1459	-16.062	203.3	576.5	31.0	92.3	0.603
DBHF	0.1779	-16.160	201.6	507.9	33.7	69.4	0.684
DD	0.1487	-16.021	240.0	-134.6	32.0	56.0	0.565
D ³ C	0.1510	-15.981	232.5	-716.8	31.9	59.3	0.541
KVR	0.1600	-15.800	250.0	528.8	28.8	55.8	0.800
KVOR	0.1600	-16.000	275.0	422.8	32.9	73.6	0.800
DD-F	0.1469	-16.024	223.1	757.8	31.6	56.0	0.556



Exploring the Limits - The EoS beyond saturation

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$$\epsilon = (n - n_{sat})/n \quad \beta = (n_n - n_p)/(n_n + n_p)$$

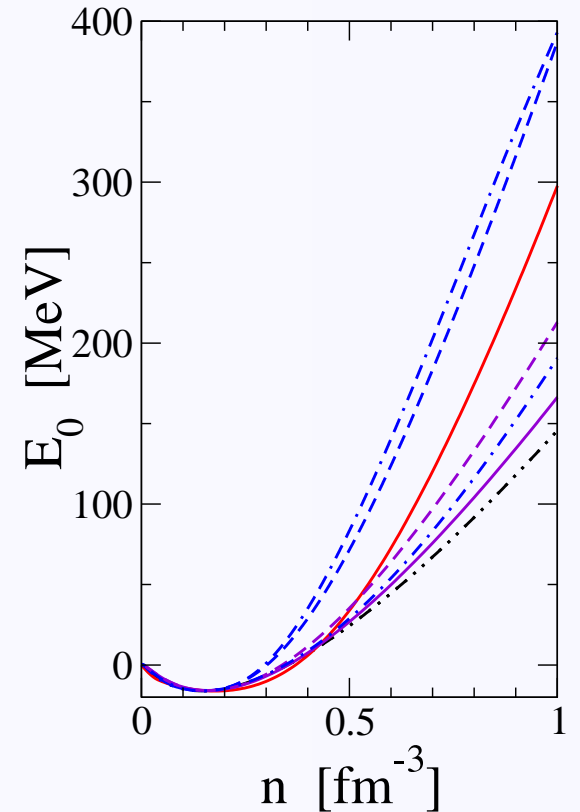
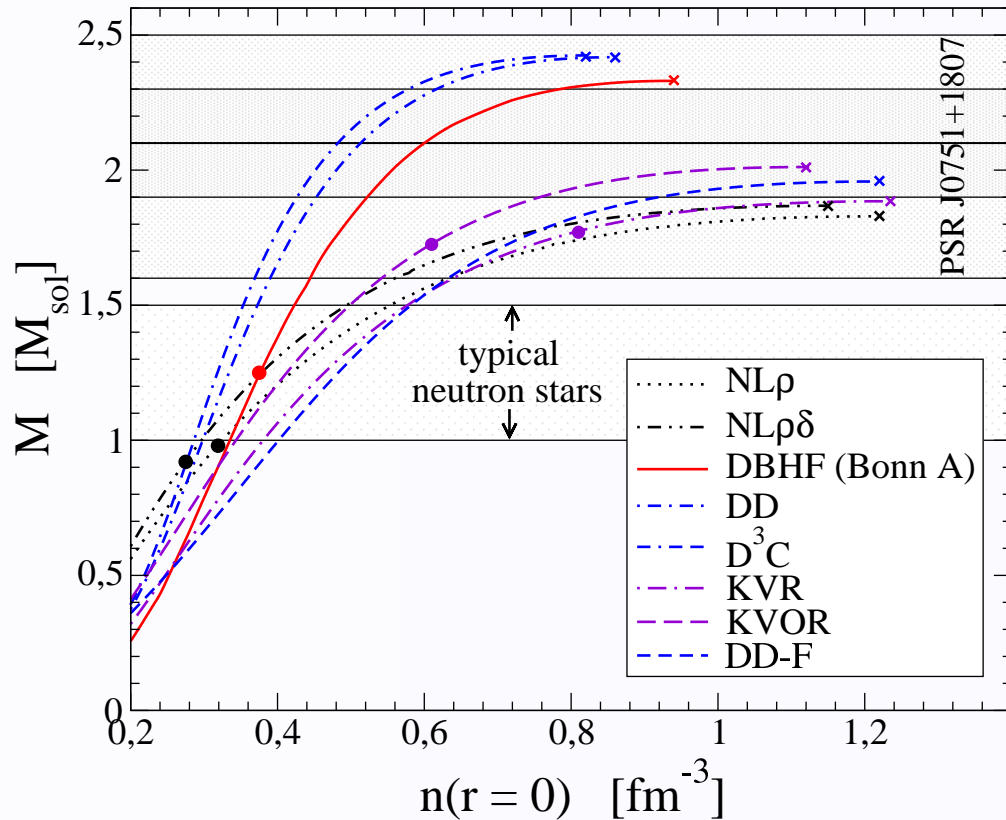
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δ_{rel}	22%	2%	36%	±!	17%	65%	33%

Higher order terms are **barely constrained!**

How to select the 'good' model?

New quality of astrophysical measurements! **Constraints from NSs!**

Maximum Neutron Star Masses



$M(n)$ correlated to $E_0(n)$

stiff: higher M_{max} at smaller densities

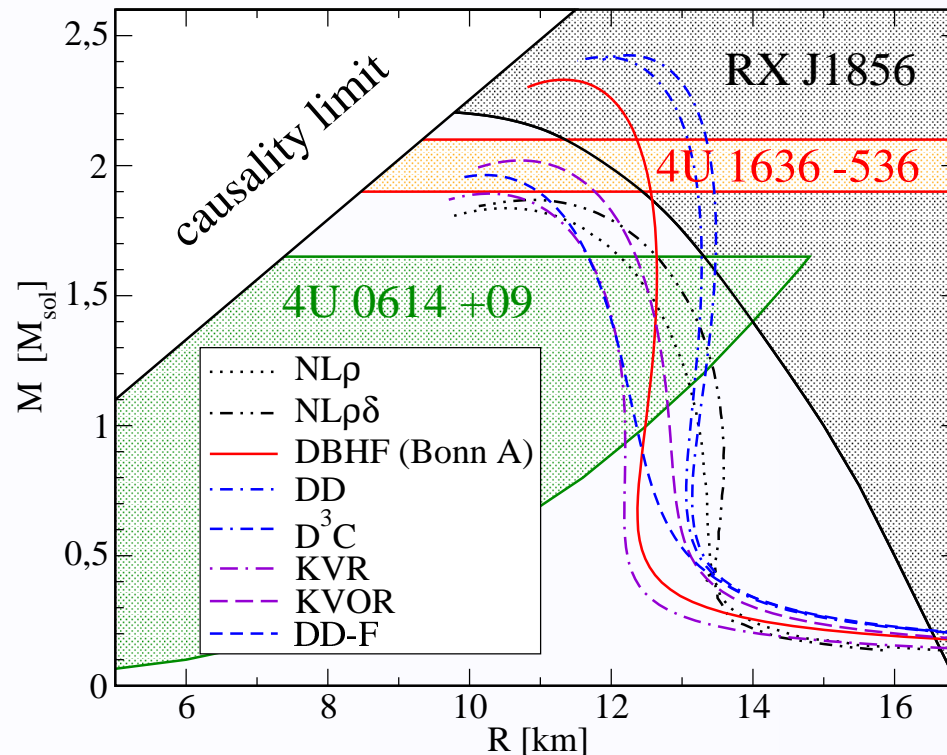
soft: smaller M_{max} at higher densities

M-R Constraints

RXJ1856 black body spectrum: $T_\infty = 57 \text{ eV}$

measurement of distance: 60 pc (2002) \rightarrow 117 pc (2004)

\rightarrow photospheric radius: $R_\infty = R(1 - R/R_S)^{-1/2}$ $R_S = 2GM$



Mass Radius Constraints

QPO : M-R upper limits

ISCO : max. mass constraint

RXJ1856: M-R lower limits

each region...

\rightarrow represents a different object

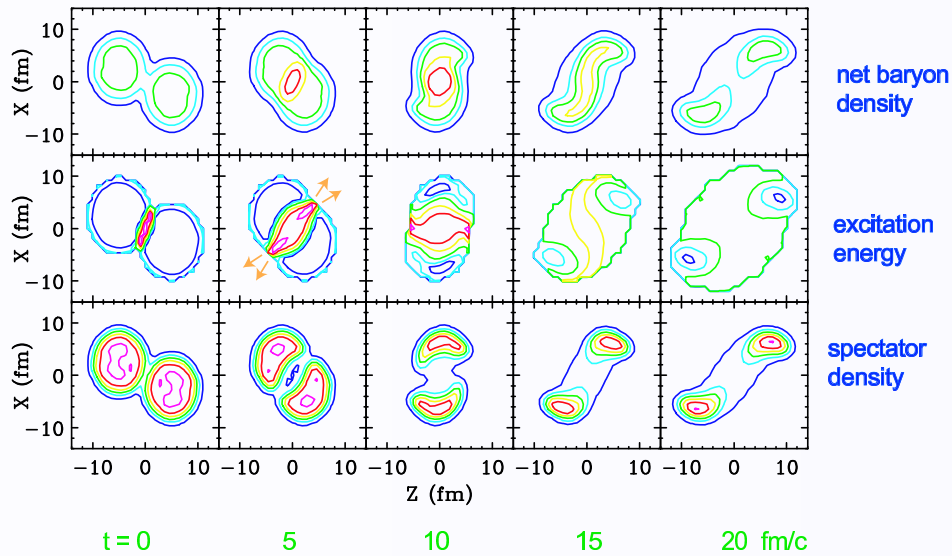
\rightarrow should be touched at least once

J. Trümper et al., Nucl. Phys. Proc. Suppl. 132, 560 (2004)

D. Barret, J.-F. Olive, M.C. Miller, Mon. Not. Roy. Astron. Soc. 361, 855 (2005)

Elliptic Flow in HIC

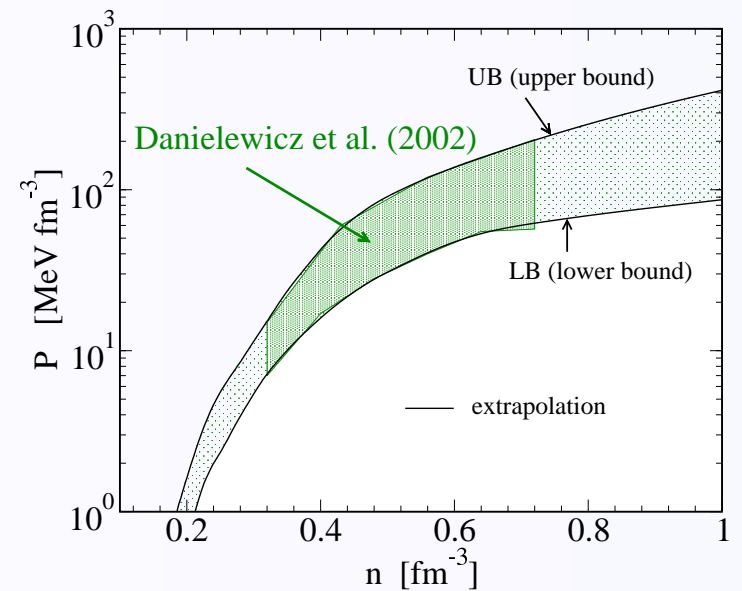
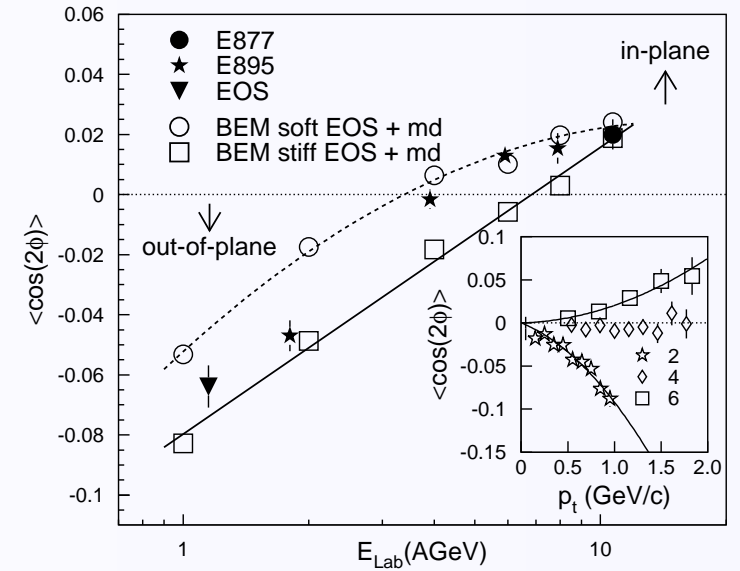
Heavy Ion Collisions:



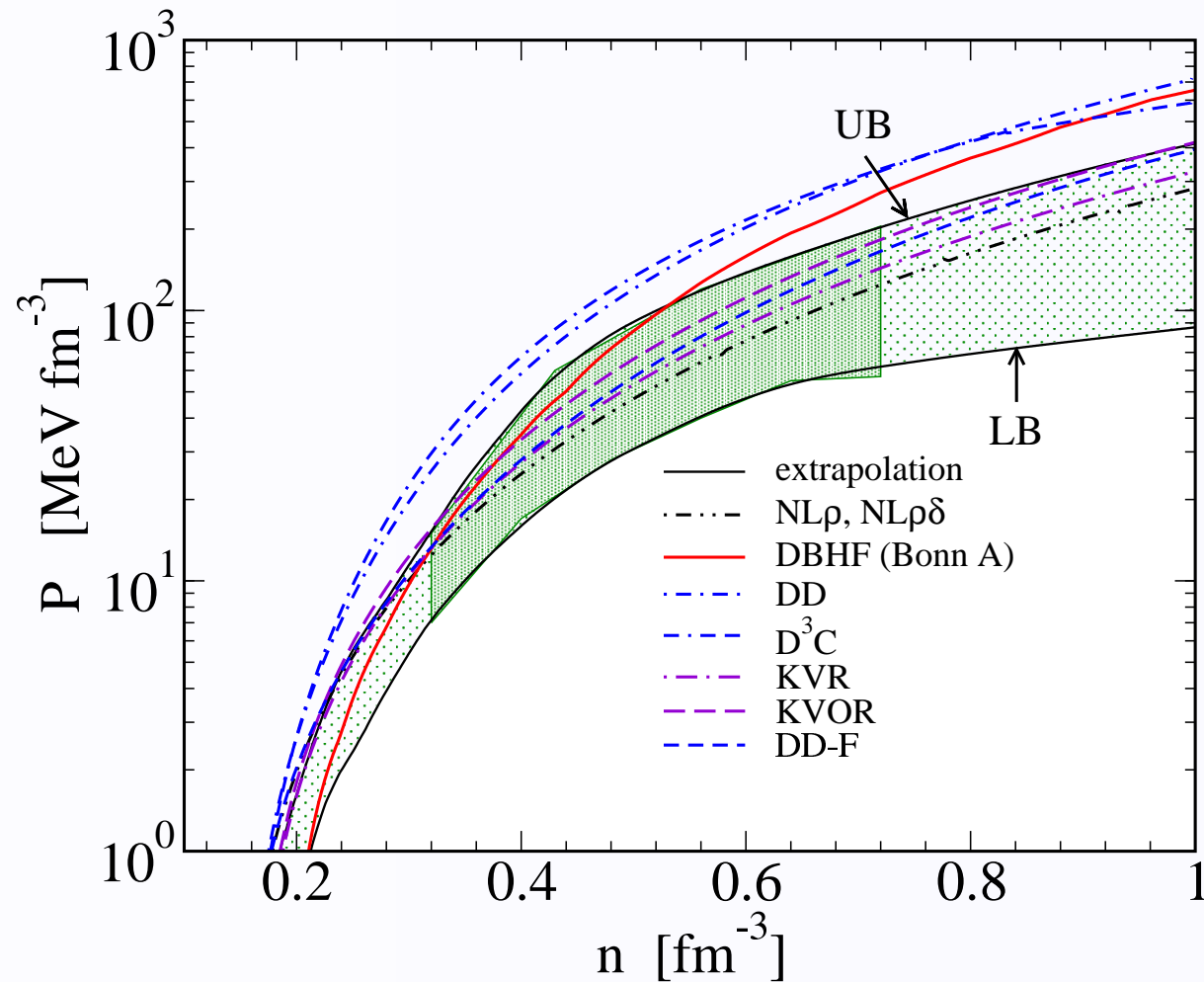
P. Danielewicz et al., Science 298, 1592 (2002)

Flow data constrain EoS up to $n \approx 4n_0$

→ finite range of possible $P(n)$ for given n



Flow Constraint



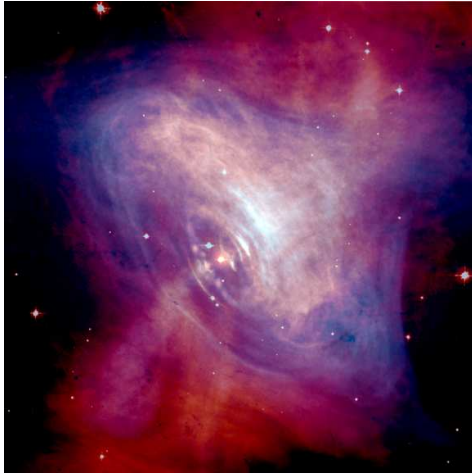
→ fulfilled for soft $NL\rho, NL\rho\delta, KVR, KVOR, DD-F$;

DBHF at low densities; DD, D^3C fail

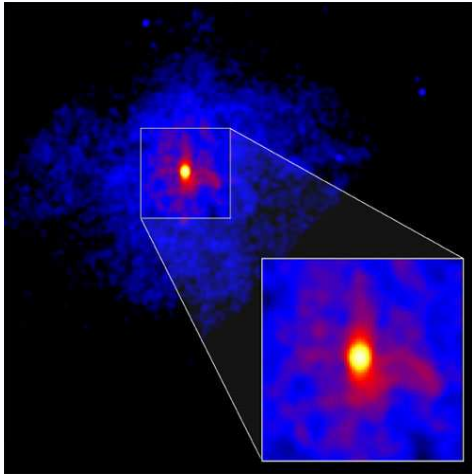
Neutron Star Cooling

Pulsars in SN remnants:

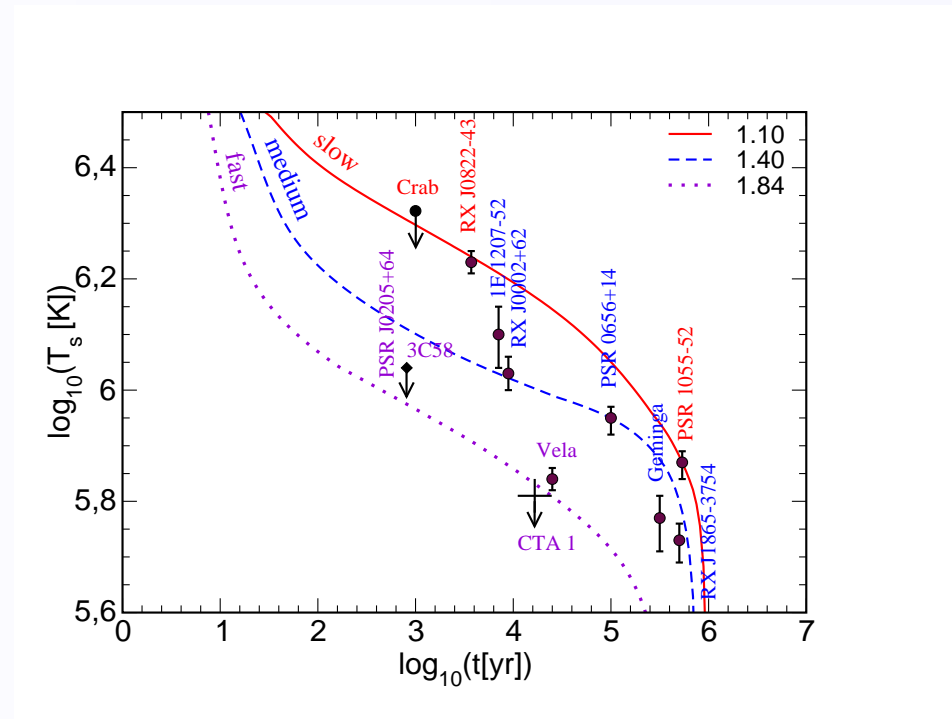
1054 - Crab



1181 - 3C58



Classification of cooling compact stars

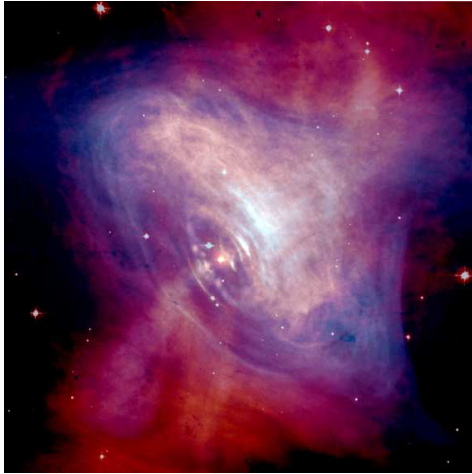


Blaschke et al. (2004)

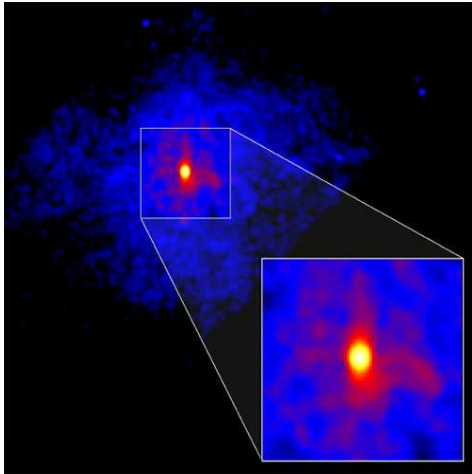
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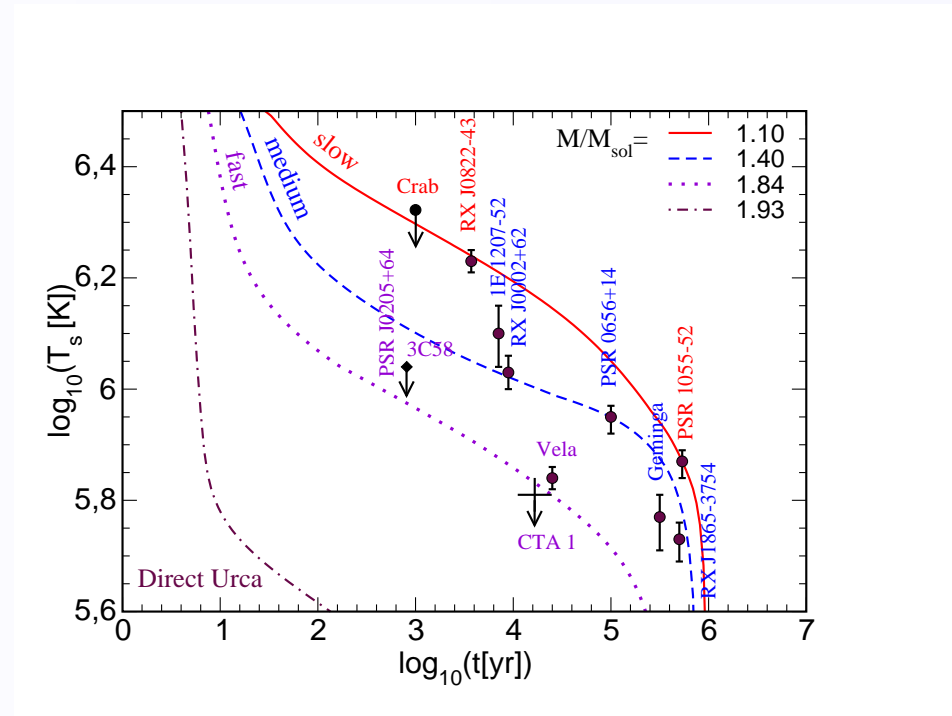
1054 - Crab



1181 - 3C58



Classification of cooling compact stars



Blaschke et al. (2004)

parameter \rightarrow neutron star mass

Direct Urca: $n \rightarrow p + e^- + \bar{\nu}_e$

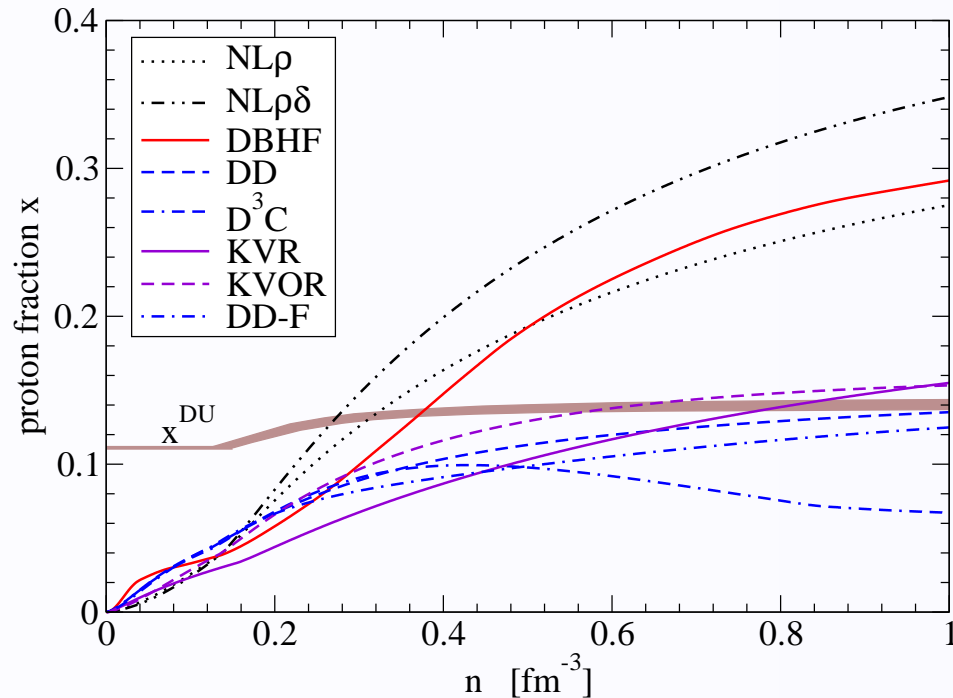
Direct Urca Process → Rapid Cooling

$n \rightarrow p + e + \bar{\nu}_e$ implies $p_n \leq p_p + p_e$, same for muons: $e \leftrightarrow \mu$
 charge neutrality: $n_p = n_e + n_\mu$, i.e. $p_p^3 = p_e^3 + p_\mu^3$ results in

$$x_p \geq x_{DU}(x_e) = [1 + (1 + x_e^{1/3})^3]^{-1} \quad x_e = n_e / (n_e + n_\mu)$$

➔ no muons: $x_{DU} = 11.1\%$

➔ relativistic limit ($n_e = n_\mu$): $x_{DU} = 14.8\%$



$E_S(n)$:

soft for DU onset at high n

NL ρ , NL $\rho\delta$, DBHF :

DU occurs below $2.5 n_0$

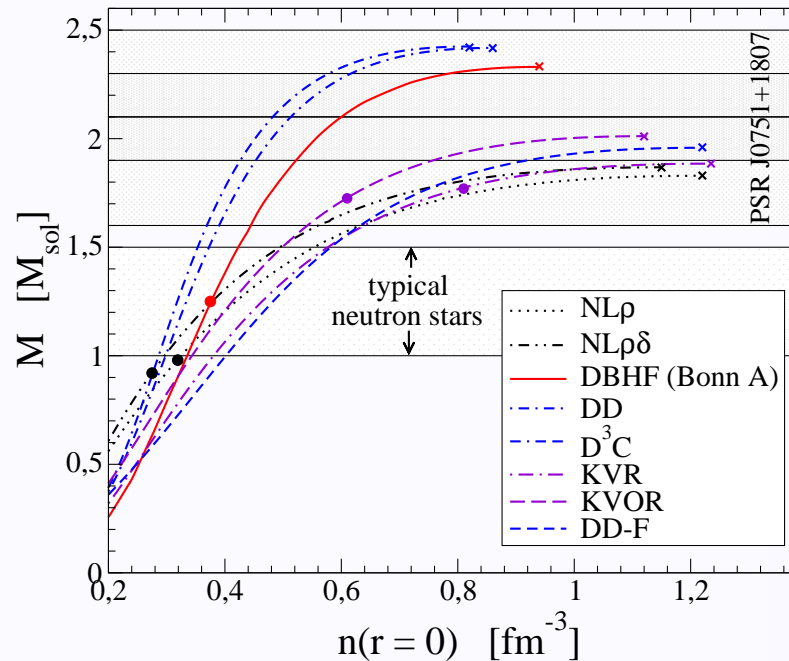
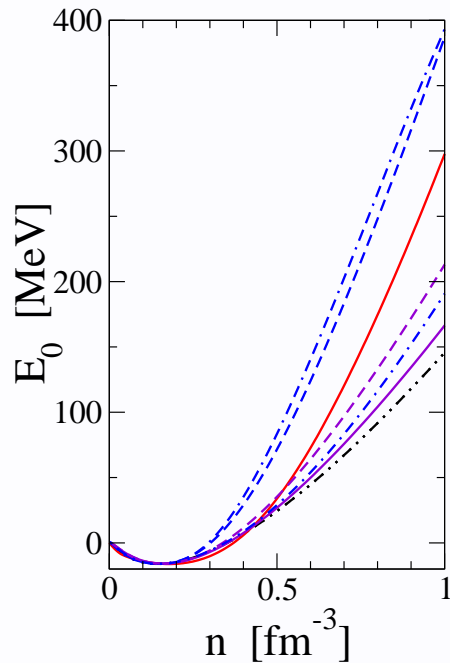
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$$x_p \geq x_{DU}(x_e) = [1 + (1 + x_e^{1/3})^3]^{-1} \quad x_e = n_e / (n_e + n_\mu)$$

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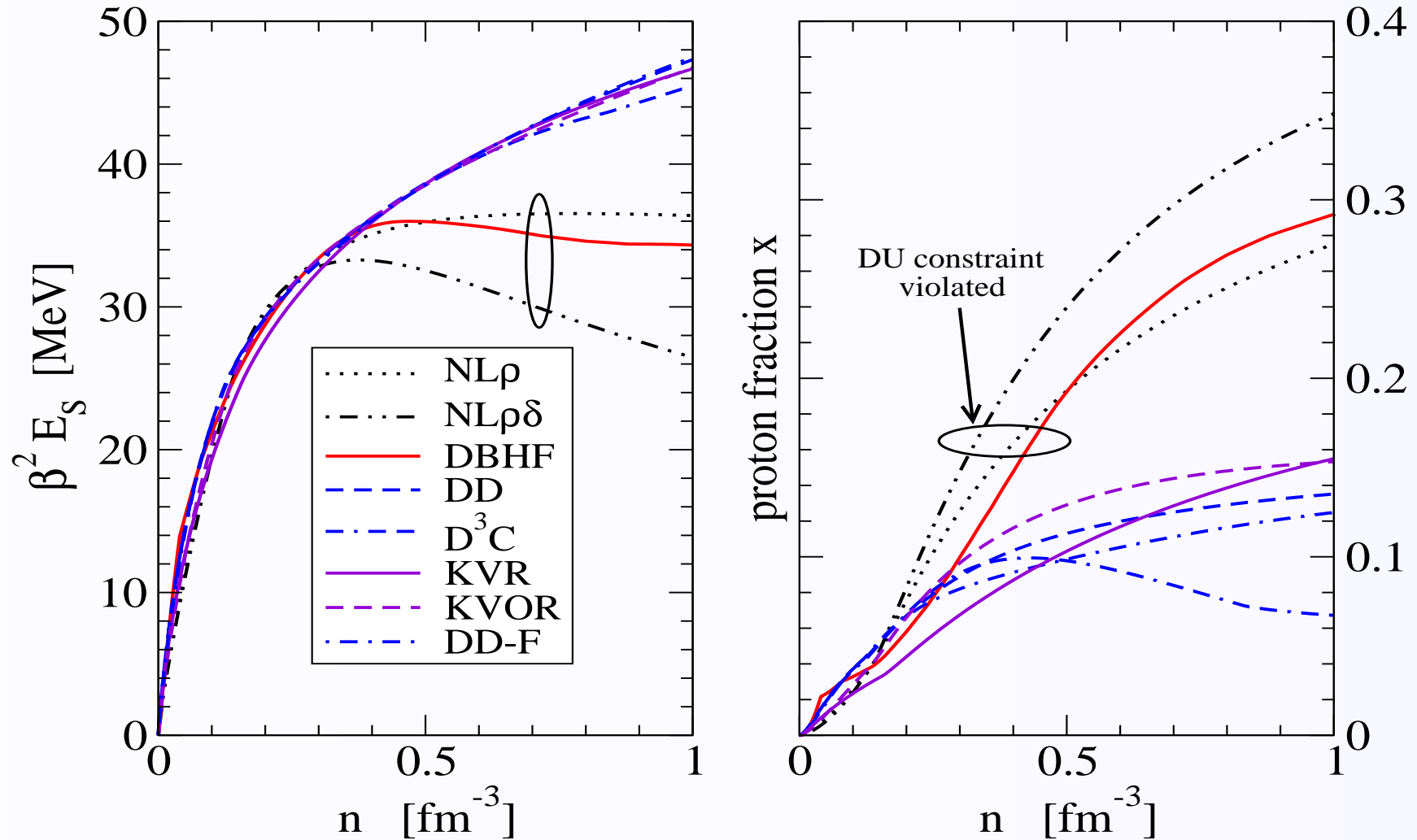


$E_S(n)$:
 soft for DU onset at high n

NL ρ , NL $\rho\delta$, DBHF :
 DU occurs below $2.5 n_0$

$$M_{DU} < 1.3 M_\odot$$

Consequences: Universality conjecture for $\beta^2 E_S(n)$



Exclude NL ρ , NL $\rho\delta$, DBHF since DU constraint violated ($M_{DU} < M_{\text{typ}}$)

\rightarrow universal $\beta^2 E_S$

Exploring the Limits: Nuclear Matter beyond Saturation

Model	$M_{\max} \geq 1.9 M_{\odot}$	$M_{\max} \geq 1.6 M_{\odot}$	$M_{\text{DU}} \geq 1.5 M_{\odot}$	$M_{\text{DU}} \geq 1.35 M_{\odot}$	4U 1636-536 (u)	4U 1636-536 (l)	RX J1856 (A)	RX J1856 (B)	J0737 (no loss)	J0737 (loss 1%)	SIS+AGS flow constr.	SIS flow+ K^+ constr.	No. of passed strong tests	No. of passed weak tests
NL $_{\rho}$	-	+	-	-	-	-	-	-	-	-	+	+	1	2
NL $_{\rho\delta}$	-	+	-	-	-	-	-	-	-	-	+	+	1	2
DBHF	+	+	-	-	+	+	-	+	-	+	-	+	2	5
DD	+	+	+	+	+	+	-	+	-	-	-	-	3	4
D ³ C	+	+	+	+	+	+	-	+	-	-	-	-	3	4
KVR	o	+	+	+	-	o	-	-	-	+	+	+	3	5
KVOR	+	+	+	+	-	+	-	-	-	o	+	+	3	5
DD-F	+	+	+	+	-	+	-	-	-	+	+	+	3	5

Complementary scheme with strong (left columns) and weak (right columns) constraints

Favourite EsoS: DBHF, KVR, KVOR, DD-F; **None passes all constraints !**

Exploring the Limits - Summary

- ➔ High density EoS testing scheme
 - ★ set of constraints from HIC flow and new astrophysical observations
 - ★ complementary tests for $E_0(n)$ and $E_S(n)$
- ➔ Present-day conclusions
 - ★ “soft” $E_S(n)$ (NS cooling, direct Urca)
 - ★ $\beta^2 E_S(n)$ shows universal behaviour
 - ★ “stiff” $E_0(n)$ at intermediate densities (maximum masses)
 - ★ “soft” $E_0(n)$ at high densities (flow data)
- ➔ Open: transition to quark matter?
 - ★ does quark matter in compact stars contradict observations?
 - ★ might a phase transition to quark matter
solve problems of hadronic EoS (DBHF→DU, flow)?
 - ★ how to prove a possible quark core in NSs?

Quark Matter - NJL-type Model EoS

$$\mathcal{L}[\bar{q}, q] = \bar{q} (i\not{\partial} - \hat{m} + \hat{\mu}\gamma^0) q + G_S \left[\sum_{a=0,3,8} (\bar{q}\tau_a q)^2 - \eta_V (\bar{q}\gamma^0 q)^2 + \eta_D \sum_{A=2,5,7} (\bar{q}i\gamma_5\tau_A\lambda_A C\bar{q}^T)(q^T iC\gamma_5\tau_A\lambda_A q) \right]$$

Bosonization (Hubbard-Stratonovich trick) \rightarrow Mean-field approximation

$$\Omega_{MF}(T, \mu) = \frac{1}{8G_S} \left[\sum_{i=u,d,s} (m_i^* - m_i)^2 - \frac{2}{\eta_V} (2\omega_0^2 + \phi_0^2) + \frac{2}{\eta_D} \sum_{A=2,5,7} |\Delta_{AA}|^2 - \int \frac{d^3p}{(2\pi)^3} \sum_{a=1}^{18} [E_a + 2T \ln(1 + e^{-E_a/T})] \right] + \Omega_l - \Omega_0$$

Dispersion E_a : Eigenvalues of Nambu-Gorkov Propagator

$$\tilde{S}^{-1}(p_0, \vec{p}) = \begin{pmatrix} \not{p} - \hat{M}(p) - \hat{\mu}^*\gamma_0 & \Delta\gamma_5\tau_2\lambda_2 \\ -\Delta^*\gamma_5\tau_2\lambda_2 & \not{p} - \hat{M}(p) + \hat{\mu}^*\gamma_0 \end{pmatrix}.$$

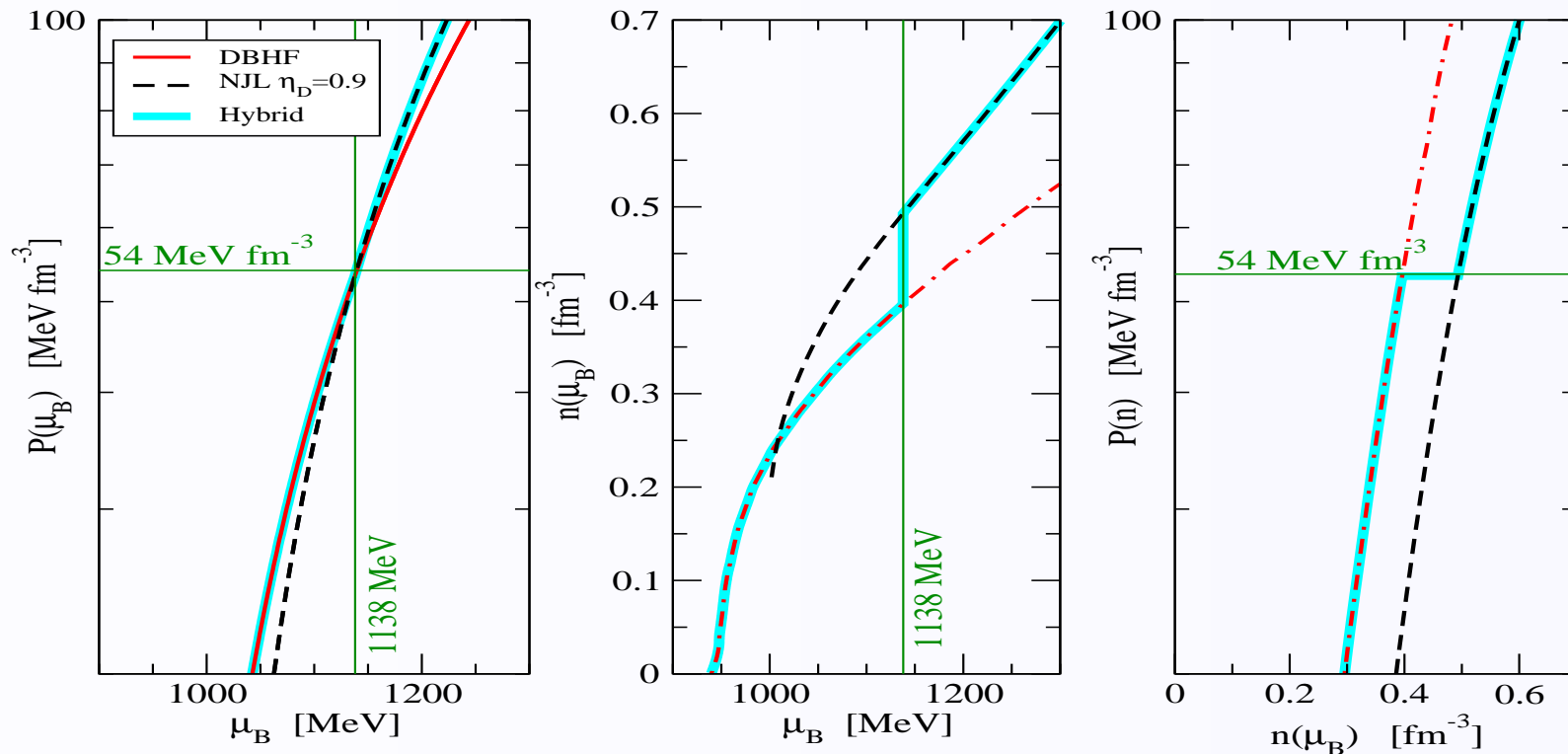
Vector coupling : renormalizes chemical potentials

$$\hat{\mu}^* = \text{diag}_f(\mu_u - G_S\eta_V\omega_0, \mu_d - G_S\eta_V\omega_0, \mu_s - G_S\eta_V\phi_0)$$

$$\eta_V = G_V/G_S, \quad \eta_D = G_D/G_S$$

Phase Transition to Quark Matter

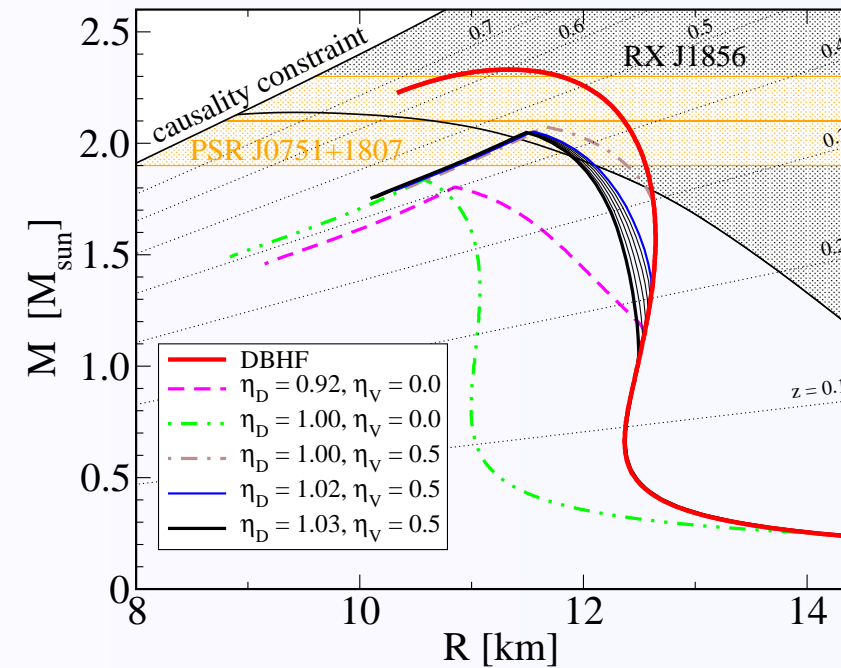
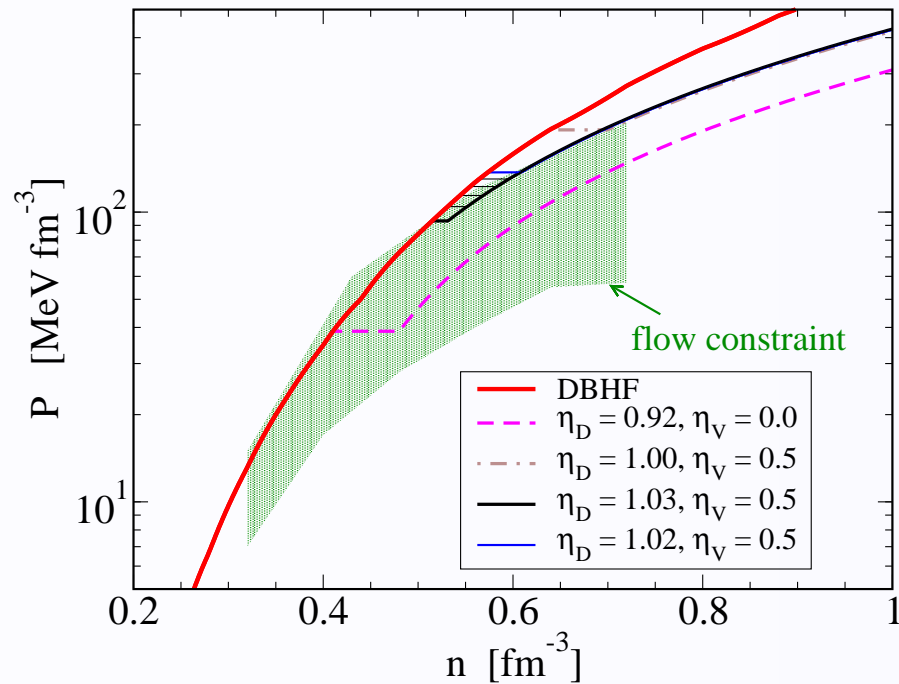
➔ traditional: two-phase construction



➔ “masquerade” problem: quark and hadron eos almost identical!

➔ challenge: hadrons as quark bound states

Quark Matter - NJL-type Model EoS



Vector coupling (η_V):

quark matter stiffness \rightarrow high density limit

Diquark coupling (η_D):

shifts transition density \rightarrow fine tuning

Flow constraint fulfilled!

mass and radius constraints:

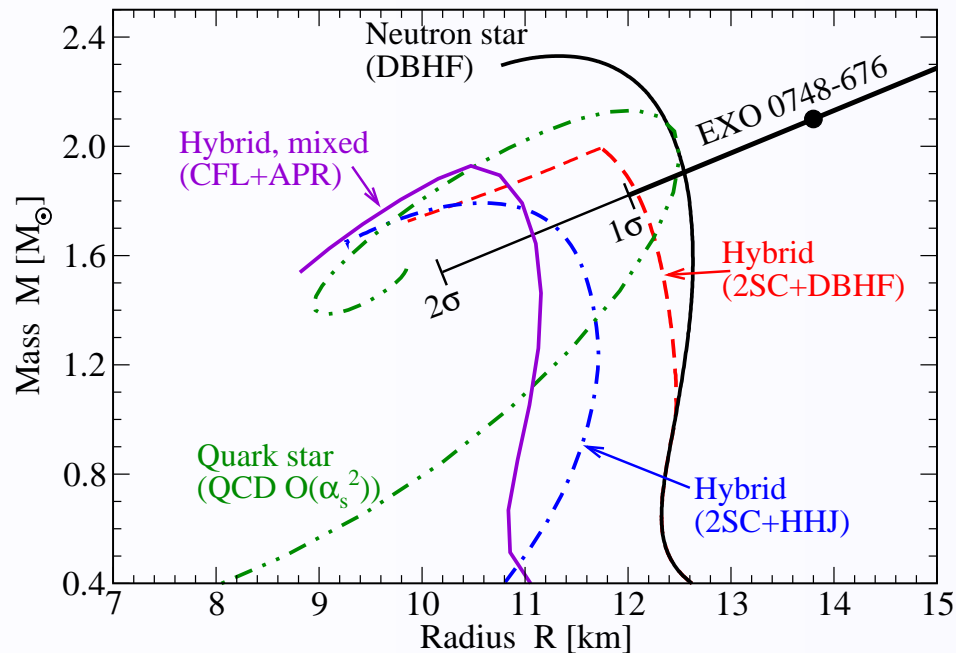
fulfilled for both pure and hybrid NSs

possible: QM cores in typical NSs

($1.0 \dots 1.5 M_\odot$)

How to distinguish?

Quark Matter - EXO 0748



The EXO constraint¹

3 Observables, 3 Unknowns

$$F_{edd} = \frac{GM}{D^2 \kappa_{es}} \left(1 - \frac{2GM}{R}\right)^{1/2}$$

$$F_{cool}/\sigma T_c^4 = f_\infty^2 \frac{R^2}{D^2} \left(1 - \frac{2GM}{R}\right)^{-1}$$

$$z = \left(1 - \frac{2GM}{R}\right)^{-1/2} - 1$$

Conclusion 1: Stiff EoS for NS matter

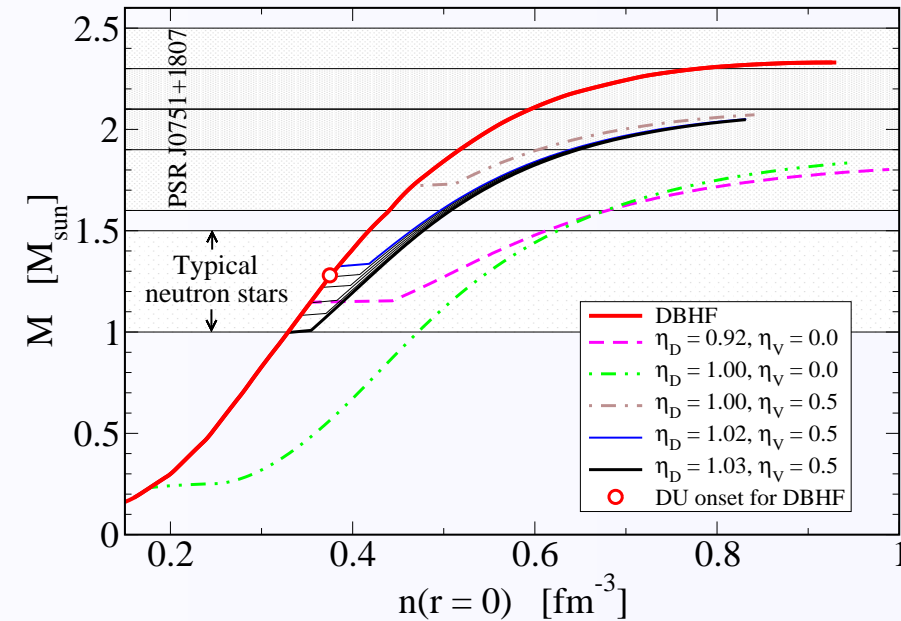
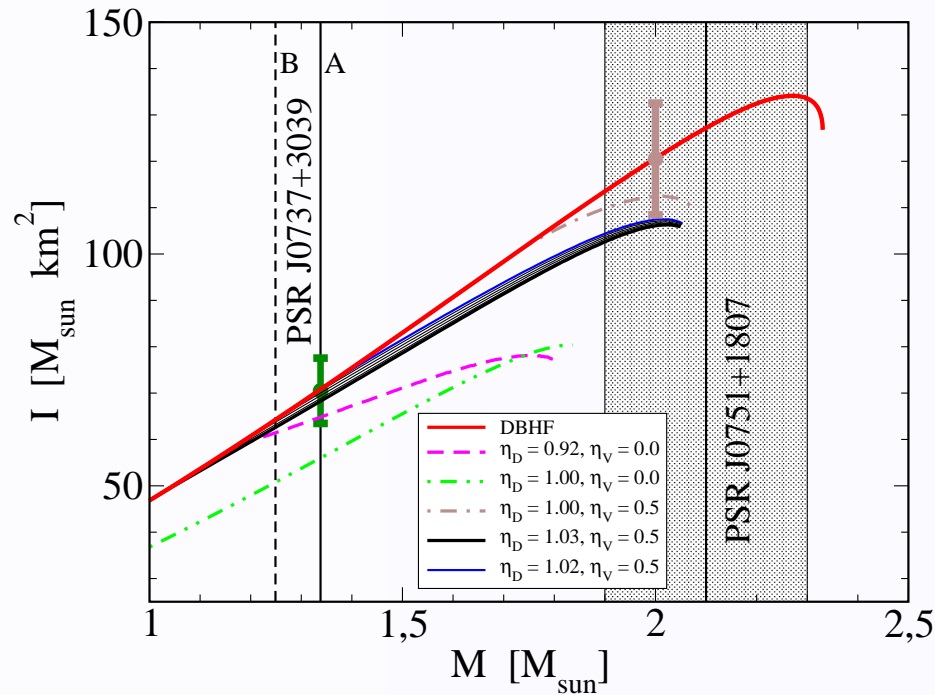
Conclusion 2: No quark matter in NS

BUT:

- Conclusion 2: several examples for QM EoS in accordance with EXO²
- redshift measurement ($z = 0.35$) has not been confirmed³ : 2 ↔ 3
- **However:** a measured point in $M - R$ plane would be a serious constraint!

¹ F.Özel (2006), ² M. Alford et al.(2007), ³ M. Mendez, priv. comm.

Quark Matter - NJL-type Model EoS



Moment of inertia:

expected to be measured for PSR J0737

(within 10% accuracy)

→ sorts out NM EoS, but not QM

Based on macroscopic properties!

Thermal evolution:

DU suppressed in QM

→ different cooling behavior

Blaschke et al., ApJ 533, 406 (2000)

Jaikumar et al., PRC 73, 042801 (2006)

Account for microscopic processes!

Quark Matter - Summary

- ➔ Constraints as a tool to adjust free parameters of effective NJL model
 - ★ vector coupling → sufficient stiffness
 - ★ diquark coupling → fine tuning of critical density
 - ★ G_V, G_D are model dependent
- ➔ Quark matter can not be excluded by high density EoS constraints!
 - ★ if QM exists in NS its **EoS is stiff**
- ➔ How to distinguish between pure and hybrid NS configurations?
 - ★ macroscopic quantities (M, R, I) → masquerade
 - ★ **microscopic information needed** → cooling

Collaborators

➔ *Rostock Group:* D. Blaschke, H. Grigorian, G. Röpke

➔ *Equations of State*

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