

Relativistic description of atomic nuclei

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Content

- **I. Covariant density functional theory**
- **II. Applications**

Content I

● Relativistic density functional theory

- * concept of density functional theory
 - Hohenberg-Kohn theorem
 - Kohn-Sham theory
- * covariant density functionals
 - relativistic fields
 - non-relativistic limit
 - pseudospin symmetry
 - effective Lagrangian
 - equations of motion
 - relativistic saturation mechanism
- * relativistic pairing

Hohenberg-Kohn theorem

We consider a realistic manybody system with the kinetic energy \hat{T} and two-body interaction $V(r_i, r_k)$ in an external field $U(r)$. In this case the expectation value of the exact energy

$$E_{HK}[\rho(\mathbf{r})] = \langle \hat{T} + \hat{V} \rangle$$

is given by a **universal functional** $E_{HK}[\rho]$, which does only depend on the **local density** $\rho(r)$, and not on the external potential $U(r)$.

The ground state is determined by minimizing $E_{HK}[\rho]$ with respect to ρ

Kohn-Sham theorem

For the same system the expectation value of the exact energy is also given by a functional

$$E_{KS}[\rho(\mathbf{r}), \tau(\mathbf{r})] = \langle \hat{T} + \hat{V} \rangle$$

is given by a **universal functional** $E_{KS}[\rho]$, which does depend on $\rho(\mathbf{r})$ and on the kinetic energy density

$$\tau(\mathbf{r}) = \nabla_r \nabla_{r'} \langle a^+(\mathbf{r}) a(\mathbf{r}') \rangle \Big|_{\mathbf{r}=\mathbf{r}'}$$

Summary on exact density functionals:

formally exact

in practice

| | | |
|-----------------|--|-------------------|
| Kohn-Hohenberg: | $E[\rho(\mathbf{r})]$ | no shell effects |
| Kohn-Sham: | $E[\rho(\mathbf{r}), \tau(\mathbf{r})]$ | no $l \cdot s$, |
| Skyrme: | $E[\rho(\mathbf{r}), \tau(\mathbf{r}), \mathbf{J}(\mathbf{r})]$ | no pairing |
| Gogny: | $E[\rho(\mathbf{r}), \tau(\mathbf{r}), \mathbf{J}(\mathbf{r}), \mathbf{\kappa}(\mathbf{r})]$ | no config. mixing |

generalized mean field: no configuration mixing,
no two-body correlations

local density:
$$\rho(\mathbf{r}) = \langle \Phi | a^\dagger(\mathbf{r}) a(\mathbf{r}) | \Phi \rangle = \sum_{i=1}^A |\varphi_i(\mathbf{r})\rangle \langle \varphi_i(\mathbf{r})|$$

kinetic energy density:
$$\tau(\mathbf{r}) = \sum_{i=1}^A |\nabla \varphi_i(\mathbf{r})\rangle \langle \nabla \varphi_i(\mathbf{r})|$$

pairing density:
$$\kappa(r) = \langle \Phi | \mathbf{a}(r, s) \mathbf{a}(r, -s) | \Phi \rangle$$

two-body density:
$$\rho_2(\mathbf{r}, \mathbf{r}') = \langle \Phi | a^\dagger(\mathbf{r}) a(\mathbf{r}) a^\dagger(\mathbf{r}') a(\mathbf{r}') | \Phi \rangle$$

Non-local density functional theory:

$$E = \langle \Psi | \hat{H} | \Psi \rangle = \langle \Phi | \hat{H}_{eff} | \Phi \rangle = E[\hat{\rho}]$$

$|\Phi\rangle$ Slater determinant $\Leftrightarrow \hat{\rho}$ density matrix

$$|\Phi\rangle = \mathbf{A}(\varphi_1(\mathbf{r}_1) \cdots \varphi_A(\mathbf{r}_A)) \quad \hat{\rho}(\mathbf{r}, \mathbf{r}') = \sum_{i=1}^A |\varphi_i(\mathbf{r})\rangle \langle \varphi_i(\mathbf{r}')|$$

Mean field:

$$\hat{h} = \frac{\delta E}{\delta \hat{\rho}}$$

Eigenfunctions:

$$\hat{h}|\varphi_i\rangle = \varepsilon_i|\varphi_i\rangle$$

Interaction:

$$\hat{V} = \frac{\delta^2 E}{\delta \hat{\rho} \delta \hat{\rho}}$$

Extensions: Pairing correlations, Covariance
Relativistic Hartree Bogoliubov (RHB)

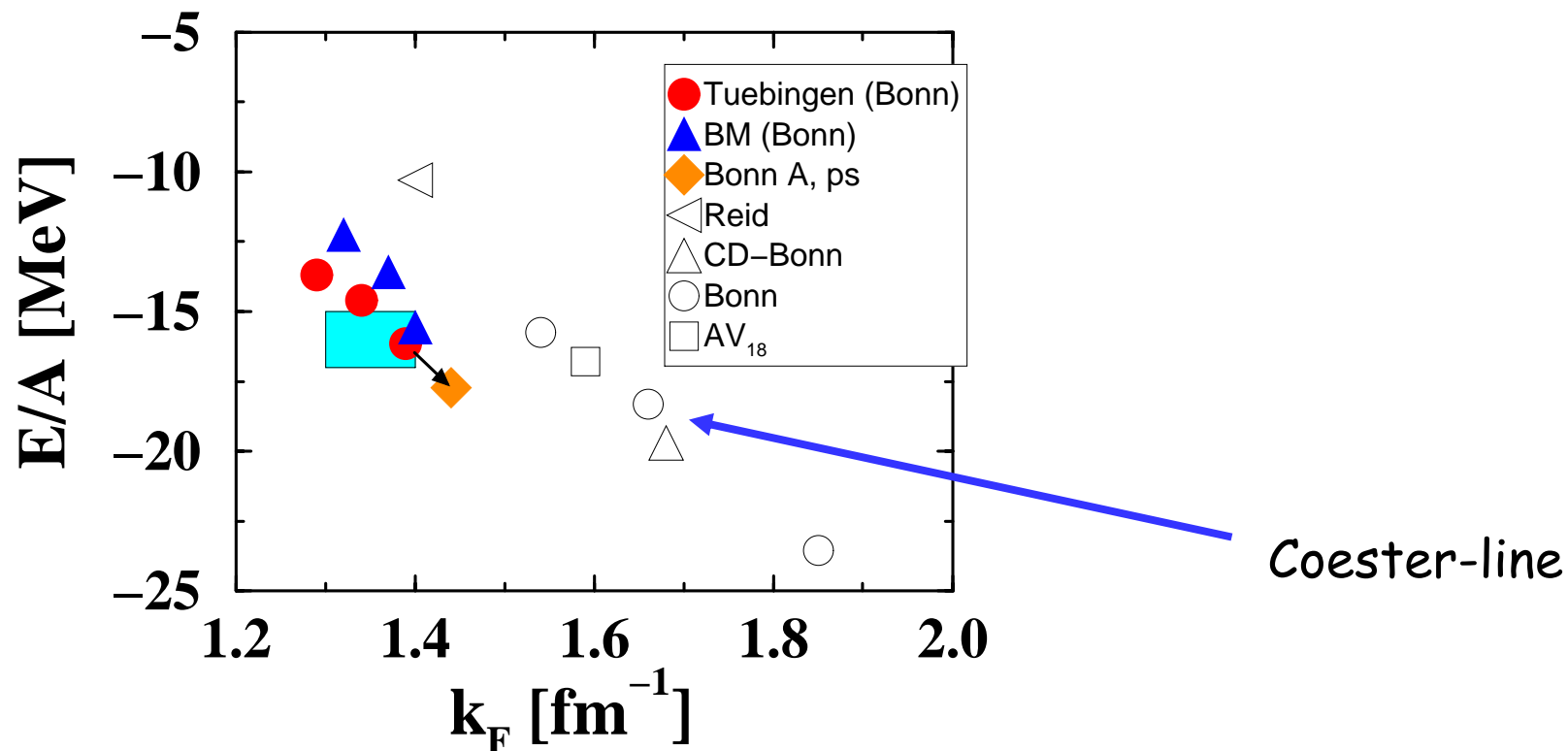
Covariant density functional theory:

Why covariant ?

- 1) no relativistic kinematic necessary: $\sqrt{p_F^2 + m_N^2} = m_N \sqrt{1 + 0.075}$
- 2) non-relativistic DFT works well
- 3) technical problems:
 - no harmonic oscillator
 - no exact soluble models
 - double dimension
 - huge cancellations V-S
 - no variational method
- 4) conceptual problems:
 - treatment of Dirac sea
 - no well defined many-body theory

Why covariant?

- 1) Large spin-orbit splitting in nuclei
- 2) Large fields $V \approx 350$ MeV, $S \approx -400$ MeV
- 3) Success of Relativistic Brueckner
- 4) Success of intermediate energy proton scatt.
- 5) relativistic saturation mechanism
- 6) consistent treatment of time-odd fields
- 7) Pseudo-spin Symmetry
- 8) Connection to underlying theories ?
- 9) As many symmetries as possible



Relativistic densities:

In the **relativistic treatment**, one has to deal with four-component Dirac spinor wave functions. Consequently, there are 16 independent bilinear covariants:

$$\bar{\psi}(\mathbf{r})\Gamma\psi(\mathbf{r})$$

This gives the following local densities:

$$\Gamma^s = 1$$

scalar density

$$\Gamma_{\mu}^v = \gamma_{\mu}$$

vector density

$$\Gamma_{\mu\nu}^t = (i/2)(\gamma_{\mu}\gamma_{\nu} - \gamma_{\nu}\gamma_{\mu})$$

tensor density

$$\Gamma^{\rho} = \gamma_5$$

pseudoscalar density

$$\Gamma_{\mu}^a = \gamma_{\mu}\gamma_5$$

axial density

(which have isoscalar and isovector components.) In most applications, only three densities are required:

$$\bar{\psi}\psi \quad (\sigma)$$

$$\bar{\psi}\gamma^{\mu}\psi \quad (\omega)$$

$$\bar{\psi}\gamma^{\mu}\vec{\tau}\psi \quad (\rho)$$

Dirac equation:

$$\begin{pmatrix} m + V - S & \vec{\sigma}(\vec{p} - \vec{V}) \\ \vec{\sigma}(\vec{p} - \vec{V}) & -m + V + S \end{pmatrix} \begin{pmatrix} g \\ f \end{pmatrix}_i = \epsilon_i \begin{pmatrix} g \\ f \end{pmatrix}_i$$

scalar potential

$S(\mathbf{r})$

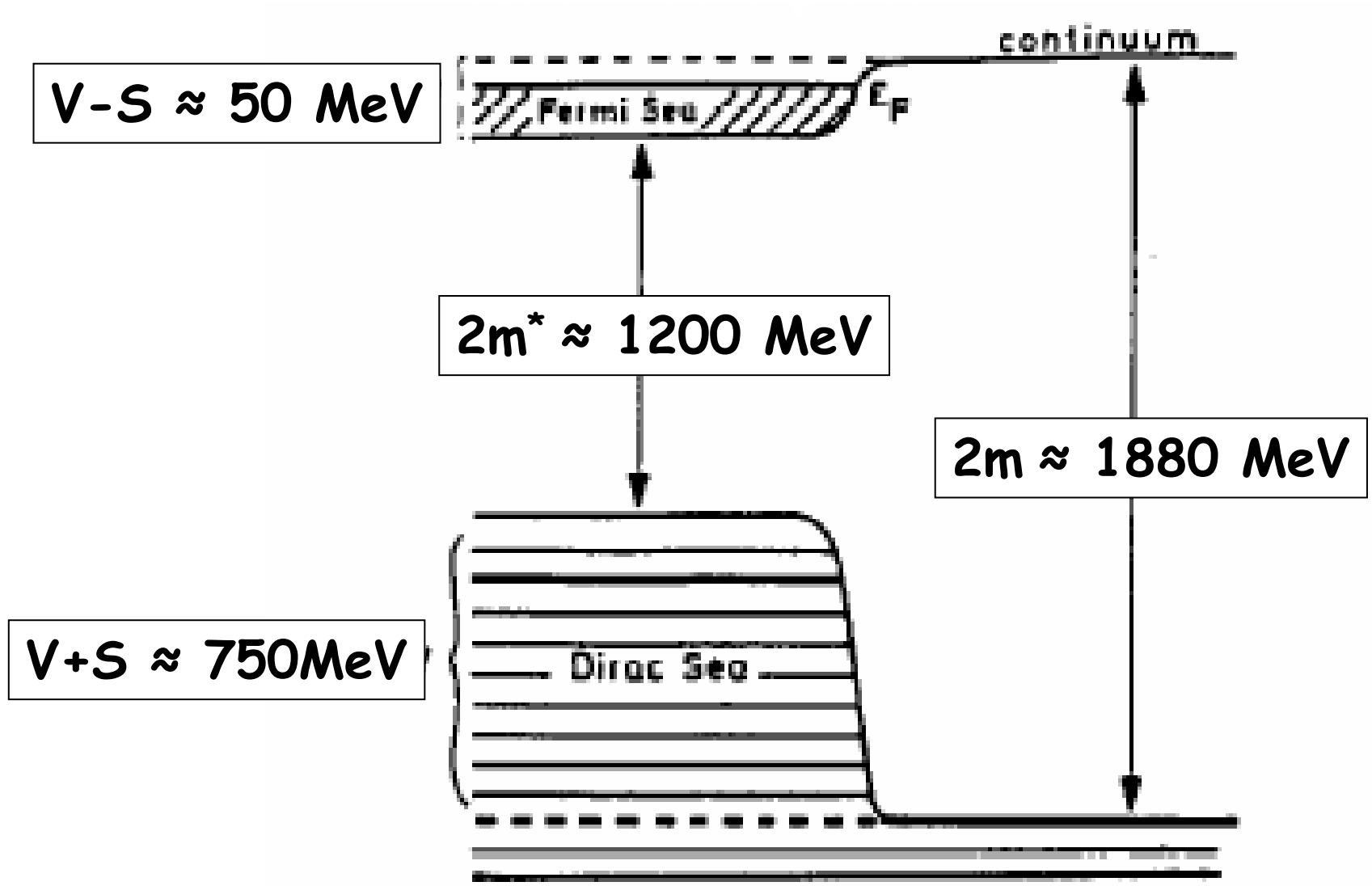
vector potential (time-like)

$V(\mathbf{r})$

vector potential (space-like)

$\vec{V}(\mathbf{r})$

vector space-like corresponds to magnetic potential (nuclear magnetism)
is time-odd and vanishes in the ground state of even-even systems



Elimination of small components:

$$(\varepsilon \rightarrow m+\varepsilon)$$

$$f_i(\mathbf{r}) = \frac{1}{\varepsilon_i + 2m - W_+} \vec{\sigma} \vec{p} g_i(\mathbf{r})$$

$$W_{\pm} = V \pm S$$

$$\left\{ \vec{\sigma} \vec{p} \frac{1}{\varepsilon_i + 2\tilde{m}(\mathbf{r})} \vec{\sigma} \vec{p} + W_- \right\} g_i(\mathbf{r}) = \varepsilon_i g_i(\mathbf{r})$$

$$\tilde{m}(\mathbf{r}) = m - \frac{1}{2} W_+$$

for $|\varepsilon_i| \ll 2\tilde{m}$

$$m^*(\mathbf{r}) = m - S$$

$$\left\{ \vec{p} \frac{1}{2\tilde{m}} \vec{p} + \frac{1}{4\tilde{m}^2} \frac{1}{r} \frac{\partial W_+}{\partial r} \vec{l} \vec{s} + W_- \right\} g_i(\mathbf{r}) \approx \varepsilon_i g_i(\mathbf{r})$$

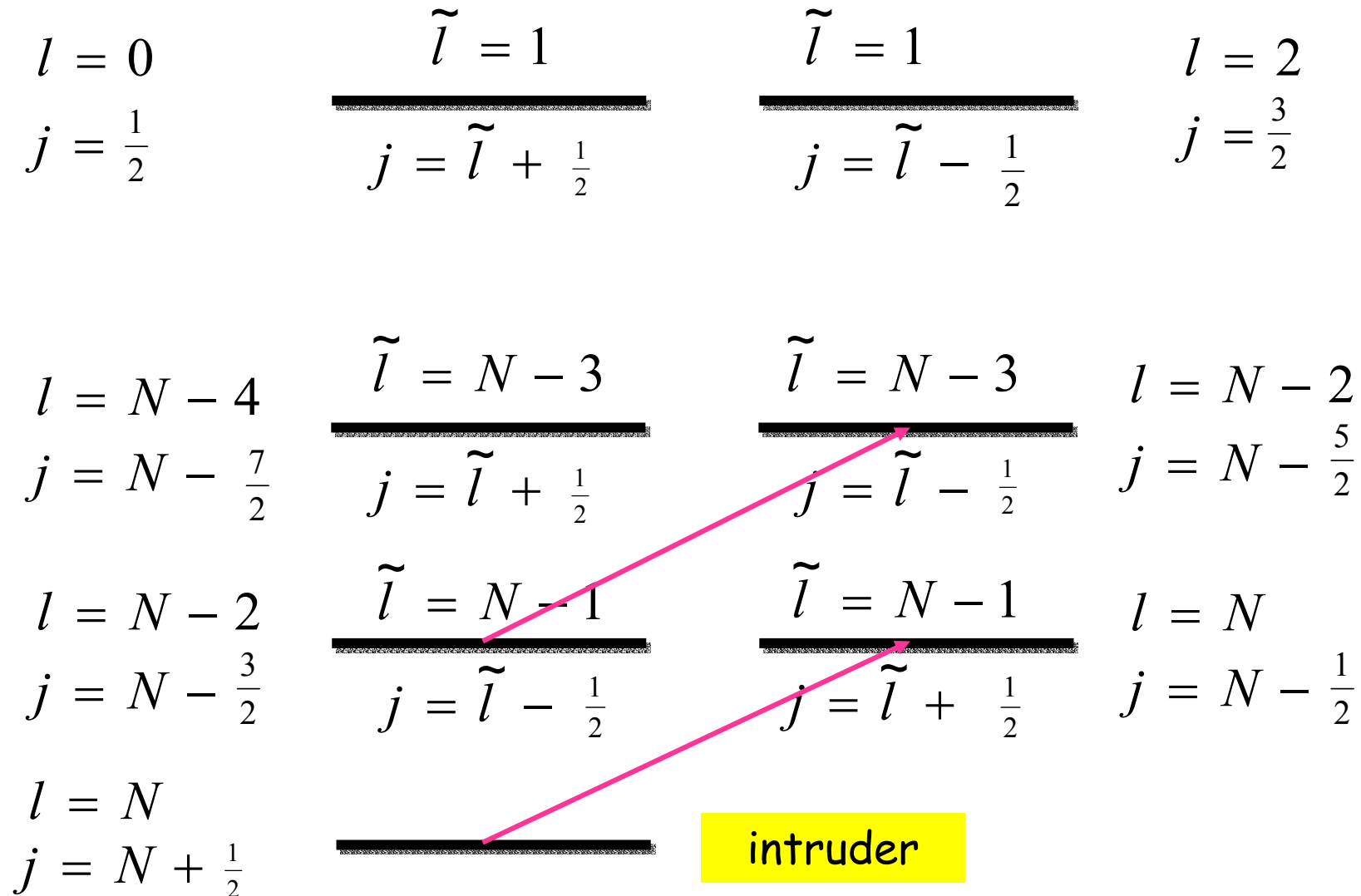
Pseudospin:

A.Arima, M.Harvey,K.Shimizu, PLB 30 (1969) 517

K.T.Hecht,A.Alder, NPA 137 (1969) 129

J.N.Ginocchio, PRL 78 (1997) 436

Oscillator-shell N



Elimination of large components:

$(\varepsilon \rightarrow m+\varepsilon)$

$$g_i(\mathbf{r}) = \vec{\sigma}\vec{p} \frac{1}{\varepsilon_i - W_-} \vec{\sigma}\vec{p} f_i(\mathbf{r})$$

$g(\mathbf{r})$ has pseudo-spin quantumnumbers

$$\left\{ \vec{\sigma}\vec{p} \frac{1}{\varepsilon_i - W_-} \vec{\sigma}\vec{p} + W_+ - 2m \right\} f_i(\mathbf{r}) = \varepsilon_i f_i(\mathbf{r})$$

$$\left\{ \vec{p} \frac{1}{\varepsilon_i - W_-} \vec{p} + \frac{1}{(\varepsilon_i - W_-)^2} \frac{1}{r} \frac{\partial W_-}{\partial r} \vec{l}\vec{s} + W_+ - 2m \right\} g_i(\mathbf{r}) = \varepsilon_i g_i(\mathbf{r})$$

For $V=S$ is $W_-=0$, i.e. **pseudo-spin orbit spitting** vanishes

J.N.Ginocchio, PRL 78 (1997) 436

QCD-sum rules: $V \approx S$

Furnstahl et al, PRC 46 (1992) 1507

Antinucleons have spin symmetry and no spin-orbit splitting

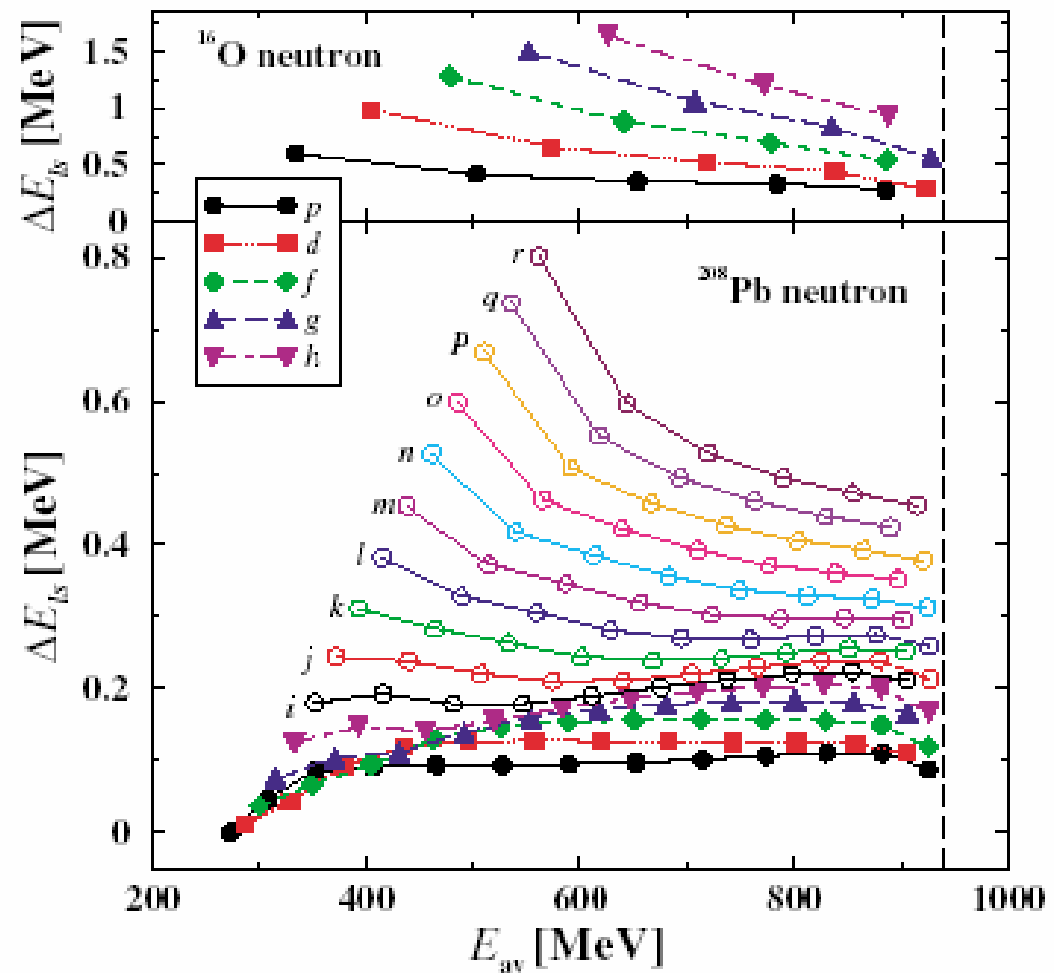
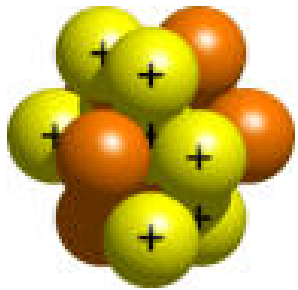
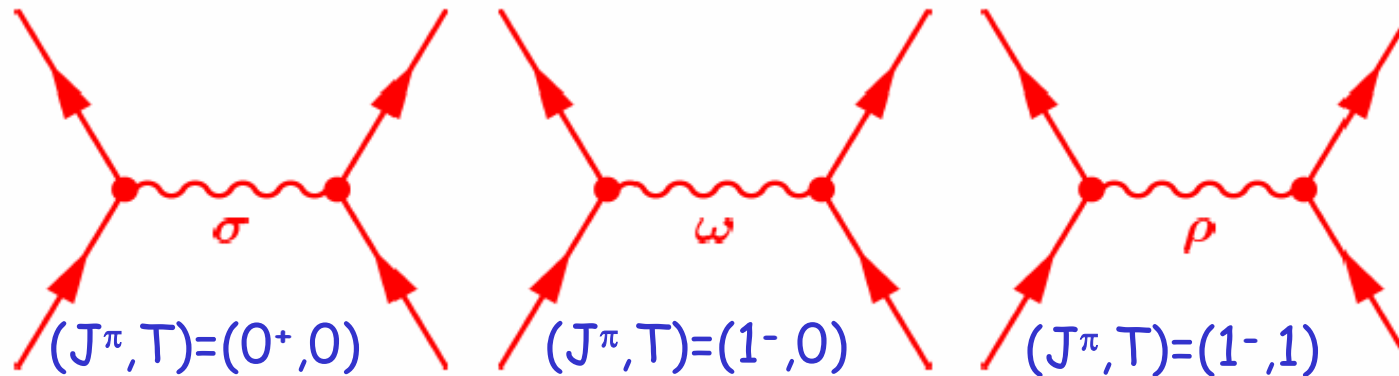


FIG. 2 (color online). Spin-orbit splitting $\epsilon_A(nl_{l-1/2}) - \epsilon_A(nl_{l+1/2})$ in antineutron spectra of ^{16}O and ^{208}Pb versus the average energy of a pair of spin doublets. The vertical dashed line shows the continuum limit.

Covariant density functional theory



Nucleons are coupled by exchange of mesons through an effective Lagrangian (EFT)



$$S(\mathbf{r}) = g_\sigma \sigma(\mathbf{r})$$

Sigma-meson:
attractive scalar field

$$V(\mathbf{r}) = g_\omega \omega(\mathbf{r}) + g_\rho \vec{\tau} \vec{\rho}(\mathbf{r}) + eA(\mathbf{r})$$

Omega-meson:
short-range repulsive

Rho-meson:
isovector field

LAGRANGIAN DENSITY

free Dirac particle

free meson fields

free photon field

$$\mathcal{L} = \bar{\psi}(i\gamma \cdot \partial - m)\psi + \frac{1}{2}(\partial\sigma)^2 - \frac{1}{2}m_\sigma^2\sigma^2 - \frac{1}{4}\Omega_{\mu\nu}\Omega^{\mu\nu} + \frac{1}{2}m_\omega^2\omega^2 - \frac{1}{4}\vec{R}_{\mu\nu}\vec{R}^{\mu\nu} + \frac{1}{2}m_\rho^2\vec{\rho}^2 - \frac{1}{4}F_{\mu\nu}F^{\mu\nu} - g_\sigma\bar{\psi}\sigma\psi - g_\omega\bar{\psi}\gamma \cdot \omega\psi - g_\rho\bar{\psi}\gamma \cdot \vec{\rho}\vec{\tau}\psi - e\bar{\psi}\gamma \cdot A\frac{(1-\tau_3)}{2}\psi$$

interaction terms

Parameter:

meson masses: $m_\sigma, m_\omega, m_\rho$

meson couplings: $g_\sigma, g_\omega, g_\rho$

Equations of motion:

$$\partial_\mu \frac{\partial L}{\partial(\partial_\mu q_k)} - \frac{\partial L}{\partial q_k} = 0.$$

for the nucleons we find the Dirac equation

$$(\gamma^\mu (i\partial_\mu - V_\mu) - m + S)\psi_i = 0.$$

No-sea approxim. !

for the mesons we find the Klein-Gordon equation

$$\begin{aligned}(\partial^\nu \partial_\nu + m_\sigma^2)\sigma &= -g_\sigma \rho_s \\(\partial^\nu \partial_\nu + m_\omega^2)\omega_\mu &= g_\omega j_\mu \\(\partial^\mu \partial_\mu + m_\rho^2)\vec{\rho}_\mu &= g_\rho \vec{j}_\mu \\ \partial^\nu \partial_\nu A_\mu &= e j_\mu^{(em)}\end{aligned}$$

$$\rho_s(x) = \sum_{i=1}^A \bar{\Psi}_i(x) \Psi_i(x)$$

$$j_\mu(x) = \sum_{i=1}^A \bar{\Psi}_i(x) \gamma_\mu \Psi_i(x)$$

$$\vec{j}_\mu(x) = \sum_{i=1}^A \bar{\Psi}_i(x) \vec{\tau} \gamma_\mu \Psi_i(x)$$

$$j_\mu^{(em)}(x) = \sum_{i=1}^A \bar{\Psi}_i(x) \frac{1}{2} (1 - \tau_3) \gamma_\mu \Psi_i(x)$$

The static limit (with time reversal invariance)

for the nucleons we find the **static Dirac equation**

$$(\vec{\alpha}\vec{p} + V + \beta(m - S))\psi_i = \varepsilon_i\psi_i.$$

$$S = -g_s\sigma, \quad V = g_\omega\omega_0 + g_\rho\rho_0 + eA_0$$

for the mesons we find the **Helmholtz equations**

No-sea approxim. !

$$\begin{aligned}(-\Delta + m_\sigma^2)\sigma &= -g_\sigma\rho_s \\(-\Delta + m_\omega^2)\omega_0 &= g_\omega\rho_B \\(-\Delta + m_\rho^2)\rho_0^3 &= g_\rho\rho^3 \\-\Delta A_0 &= e\rho^{(em)}\end{aligned}$$

$$\begin{aligned}\rho_s &= \sum_{i=1}^A \bar{\psi}_i\psi_i \\ \rho_B &= \sum_{i=1}^A \psi_i^+\psi_i \\ \rho^3 &= \sum_{i=1}^A \psi_i^+\tau_3\psi_i \\ \rho^{(em)} &= \sum_{i=1}^A \psi_i^+\frac{1}{2}(1 - \tau_3)\psi_i\end{aligned}$$

Relativistic saturation mechanism:

We consider only the σ -field, the origin of attraction
its source is the scalar density

$$m_\sigma^2 \sigma = -g_\sigma \sum_{i=1}^A \bar{\Psi}_i \Psi_i = -g_\sigma \sum_{i=1}^A (g_i^+ g_i - f_i^+ f_i)$$

for **high densities**, when the collapse is close, the Dirac gap $\approx 2m^*$ decreases, the small components f_i of the wave functions increase and reduce the scalar density, i.e. the source of the σ -field, and therefore also scalar attraction.

$$f_i(\mathbf{r}) = \frac{1}{\varepsilon_i + 2\tilde{m}} \vec{\sigma} \vec{k} g_i(\mathbf{r})$$

$$m_\sigma^2 \sigma \approx -g_\sigma \rho_B - 2 \sum_{i=1}^A f_i^+ f_i = -g_\sigma \rho_B + \frac{1}{\tilde{m}} \sum_{i=1}^A \nabla g_i^+ \nabla g_i$$

In the non-relativistic case, Hartree with Yukawa forces
would lead to collapse

Symmetric nuclear matter:

$$[\alpha \mathbf{k} + \beta (m - S)] \psi = [E - V] \psi$$

with $m^* = m - S$ and $E^* = \sqrt{\mathbf{k}^2 + m^{*2}}$ and $E = E^* + V$

we have plane wave solutions of the Dirac equation:

$$\psi(\mathbf{k}) = \sqrt{\frac{E^* + m^*}{2m^*}} \begin{pmatrix} 1 \\ \frac{\boldsymbol{\sigma} \mathbf{k}}{E^* + m^*} \end{pmatrix} \chi$$

the ω -field is given by the density:

$$V = g_\omega \omega_0 = \left(\frac{g_\omega}{m_\omega} \right)^2 \rho_B$$

the σ -field has to be determined from a non-linear equation, which gives saturation:

$$\begin{aligned} S = -g_\sigma \sigma = m - m^* &= \frac{g_\sigma^2}{m_\sigma^2} \rho_s = \gamma \frac{g_\sigma^2}{m_\sigma^2} \int \frac{d^3 k}{(2\pi)^3} \frac{m^*}{E^*(k)} \\ &= \frac{\gamma}{4\pi^2} \frac{g_\sigma^2}{m_\sigma^2} m^* \left[k_F E_F^* - m^{*2} \ln \left(\frac{k_F}{m^*} + \frac{E_F^*}{m^*} \right) \right] \end{aligned}$$

One needs only 2 constants:

$$G_\sigma = \left(\frac{g_\sigma}{m_\sigma} \right)^2 = 11,75 \text{ fm}^2$$

$$G_\omega = \left(\frac{g_\omega}{m_\omega} \right)^2 = 8,61 \text{ fm}^2$$

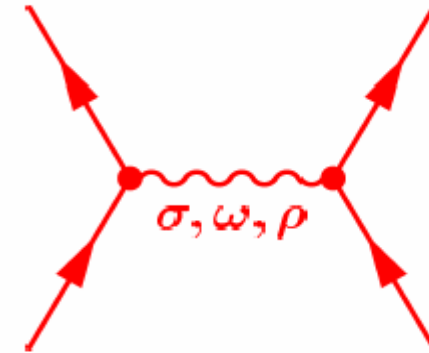
Relativistic Pairing:

One has to quantize the meson fields:

Fermion fields:
$$\int d^3r \hat{\bar{\psi}}(\alpha \mathbf{p} - \beta m)\hat{\psi}$$

Boson fields:
$$\sum_{\mu} \omega^{\mu} a_{\mu}^{+} a_{\mu}$$

Interaction:
$$- \sum_{\mu} \hat{\bar{\psi}} \Gamma^{\mu} \hat{\psi} \hat{\phi}_{\mu}$$



neglect retardation

Eliminate the meson operators:
$$\hat{\phi}_{\mu}(\mathbf{r}) = \frac{g_{\mu}}{4\pi} \int d^3r' \frac{e^{-m_{\mu}|\mathbf{r}-\mathbf{r}'|}}{|\mathbf{r}-\mathbf{r}'|} \hat{\bar{\psi}}(\mathbf{r}') \Gamma^{\mu} \hat{\psi}(\mathbf{r}')$$

Formulation in Green's functions:

Gorkov factorization

$$\langle \psi_1^+ \psi_2^+ \psi_3 \psi_4 \rangle \approx \langle \psi_1^+ \psi_4 \rangle \langle \psi_2^+ \psi_3 \rangle - \langle \psi_1^+ \psi_3 \rangle \langle \psi_2^+ \psi_4 \rangle + \langle \psi_1^+ \psi_2^+ \rangle \langle \psi_3 \psi_4 \rangle$$

direct term

exchange term

pairing term

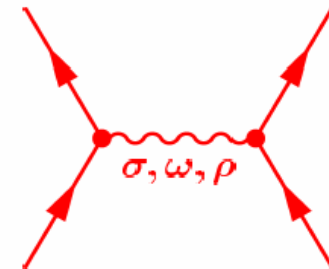
Relativistic HFB equations:

$$\begin{pmatrix} \hat{h} & \hat{\Delta} \\ -\Delta^* & -\hat{h}^* \end{pmatrix} \begin{pmatrix} U_k(\mathbf{r}) \\ V_k(\mathbf{r}) \end{pmatrix} = \begin{pmatrix} U_k(\mathbf{r}) \\ V_k(\mathbf{r}) \end{pmatrix} E_k$$

$$\hat{h} = \vec{\alpha}(\vec{p} - \vec{V}) + V + \beta(m - S)$$

$$\hat{\Delta} = \begin{pmatrix} \hat{\Delta}_{++} & \hat{\Delta}_{+-} \\ \hat{\Delta}_{-+} & \hat{\Delta}_{--} \end{pmatrix} = \beta\Delta_s + \Delta_0 + \vec{\alpha}\vec{\Delta}$$

$$\Delta_{ab}(\vec{r}, \vec{r}') = \frac{1}{2} \sum_{c,d} V_{abcd}^{pp}(\vec{r}, \vec{r}') \kappa_{cd}(\vec{r}, \vec{r}')$$



Pairing in nuclear matter:

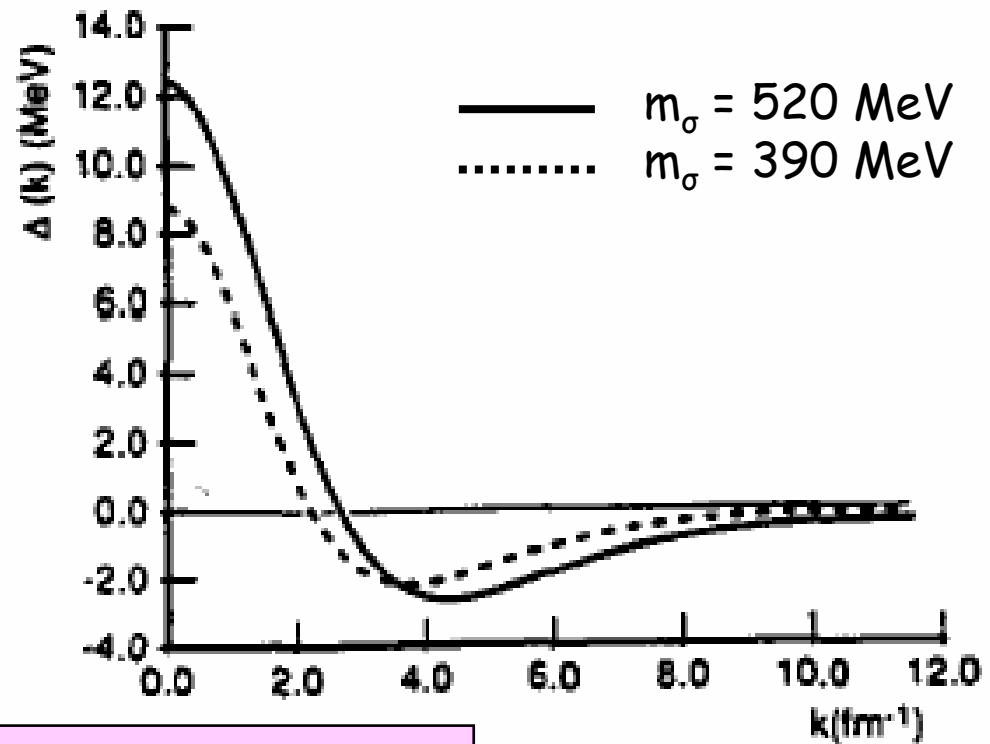
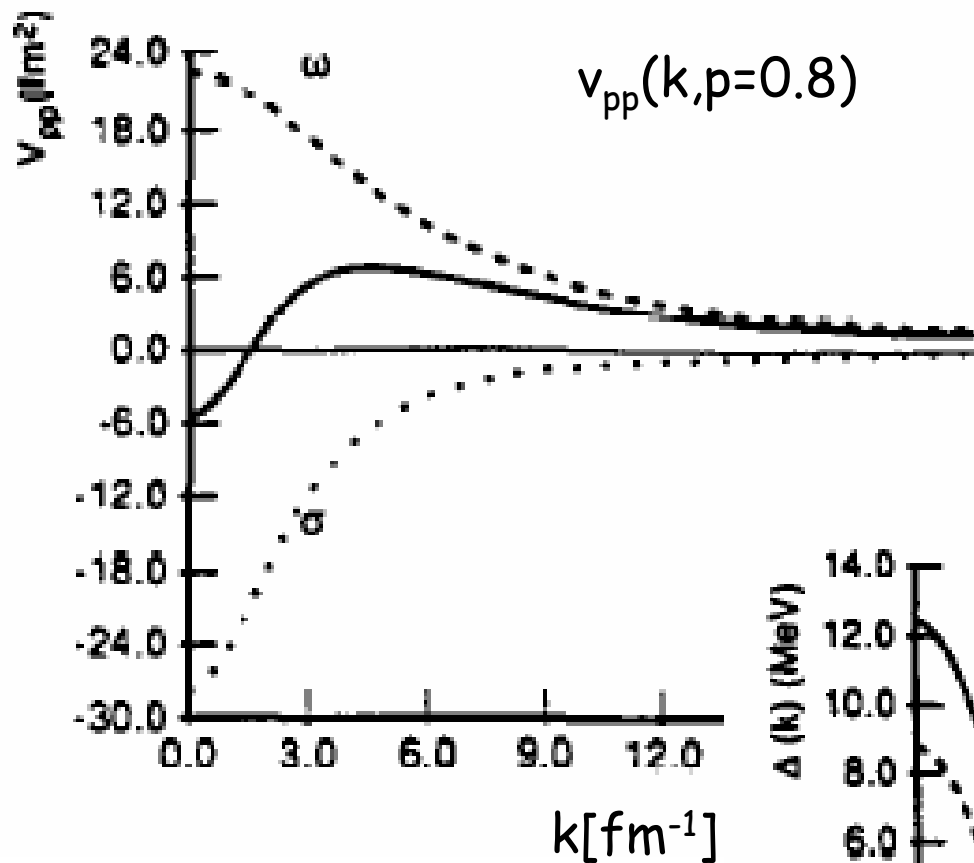
RMF+BCS

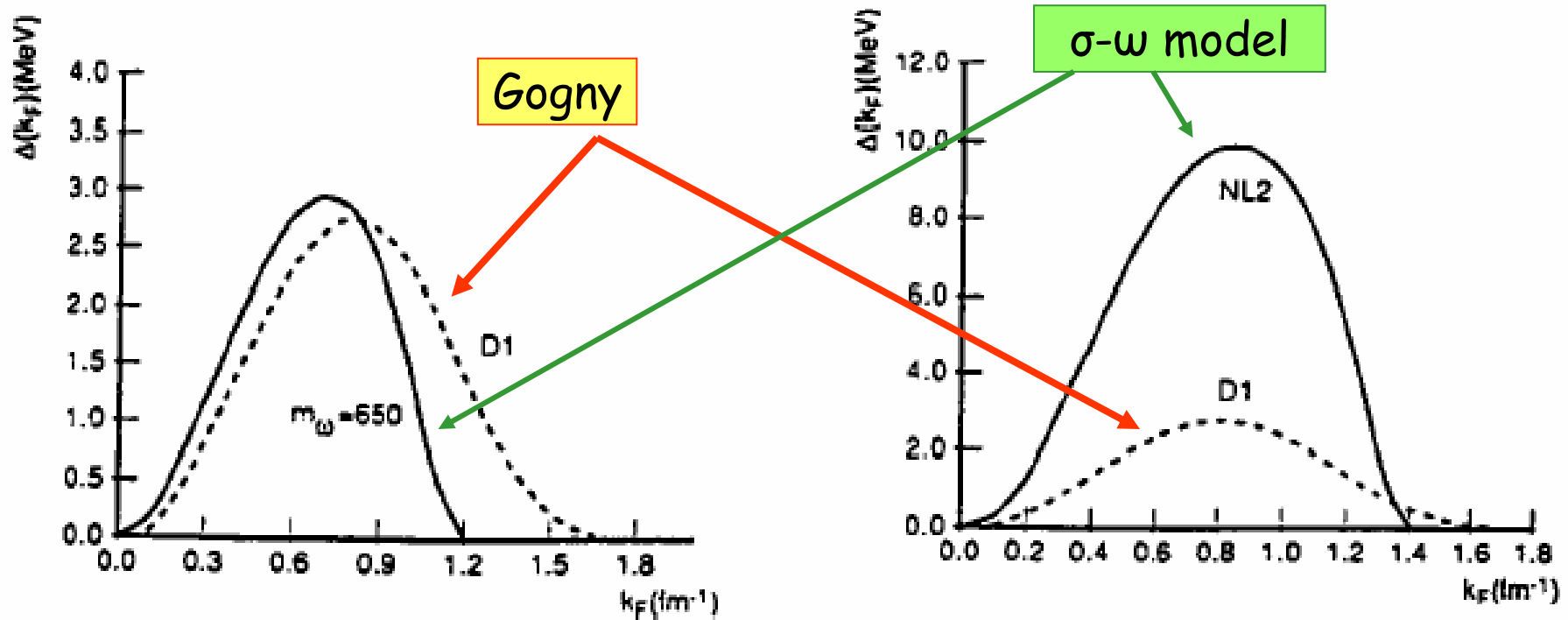
Gap equation: $\Delta = v_{\kappa} = v_{\mu\nu}$

1S_0 - Channel

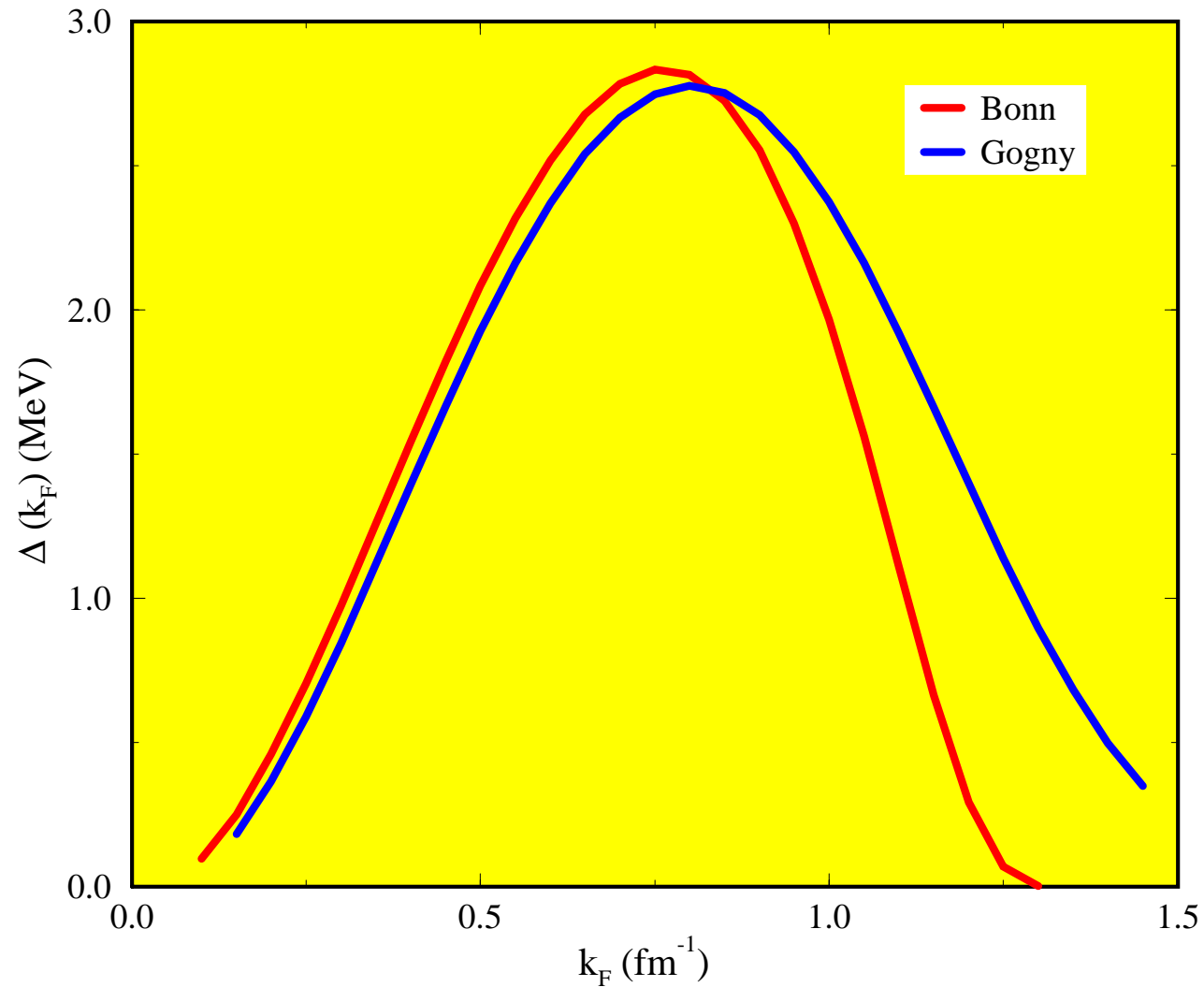
$$\Delta(p) = -\frac{1}{4\pi^2} \int_0^\infty v_{pp}(p, k) \frac{\Delta(k)}{\sqrt{(\varepsilon(k) - \lambda)^2 + \Delta^2(k)}} k^2 dk$$

$$v_{pp}^\omega(p, k) = \frac{g_\omega^2}{2E^*(p)E^*(k)} \frac{m^*{}^2 + p^2 + k^2 - (E^*(p) - E^*(k))^2}{pk} \ln \left(\frac{(p+k)^2 + m_\omega^2}{(p-k)^2 + m_\omega^2} \right)$$

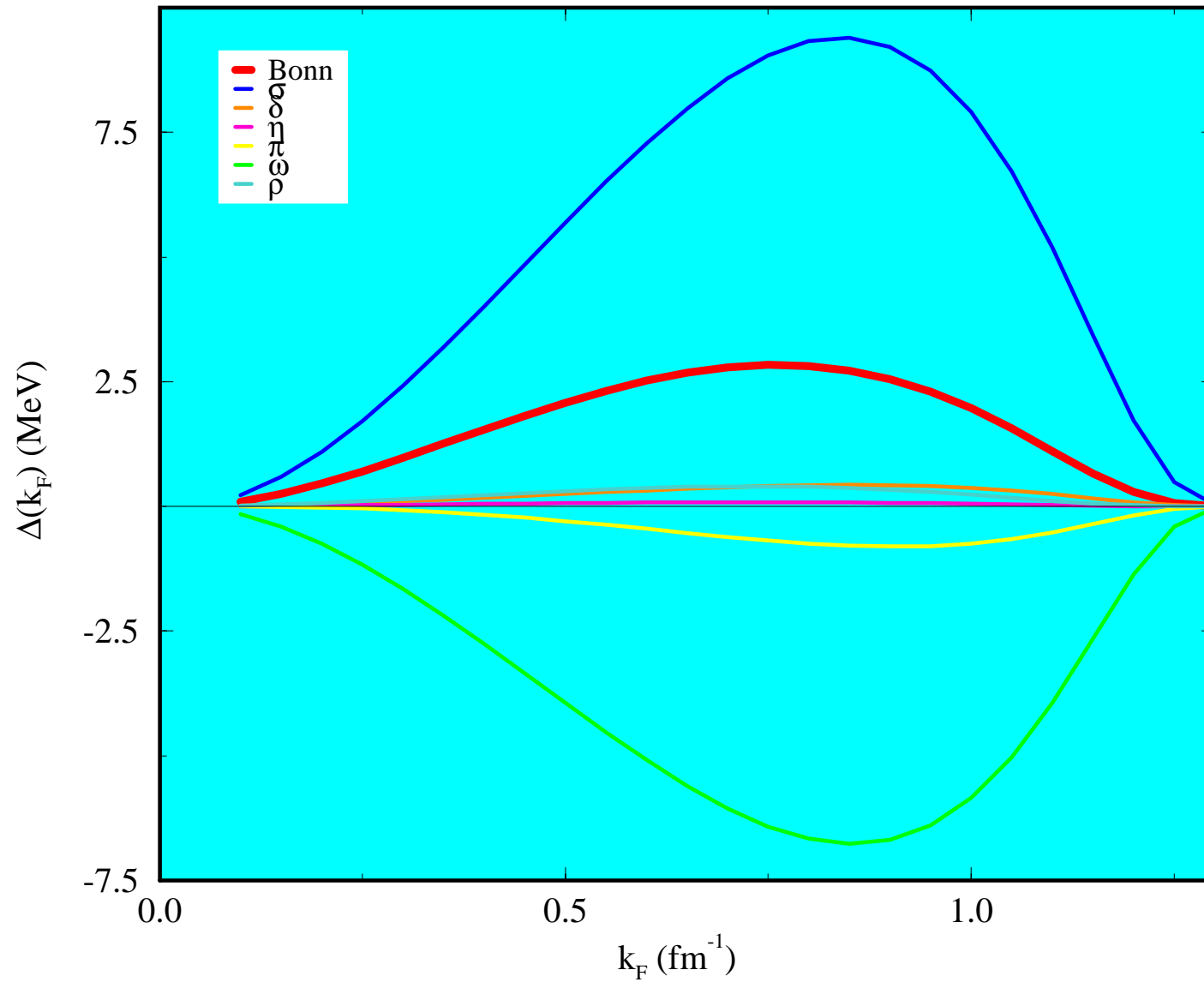




All relativistic forces, e. g. NL1, NL2, ... **overestimate** nuclear pairing by a factor 3, because they do not have a cut off in momentum space

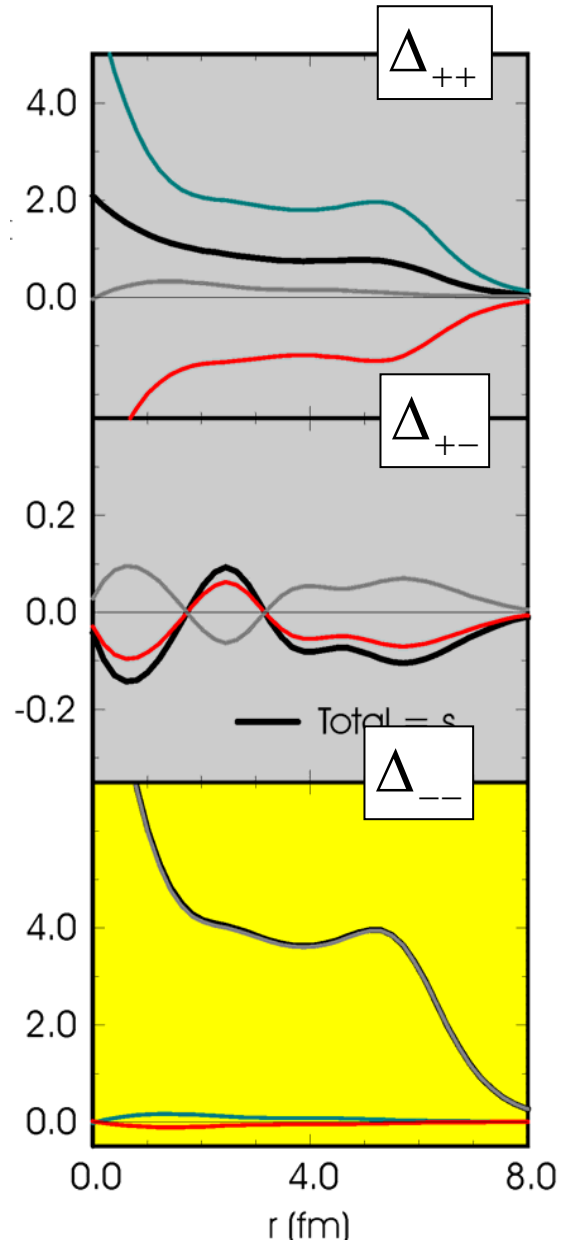


free NN-forces, which reproduce the phase shift in the 1S0 channel, give pairing similar to the Gogny force



contributions of the various meson fields in the B-potential to pairing

Relativistic structure of pairing



$$\mathbf{H} = \begin{pmatrix} m+V-S & \sigma\mathbf{p} & \Delta_{++} & \Delta_{+-} \\ \sigma\mathbf{p} & -m-V-S & \Delta_{-+} & \Delta_{--} \\ \Delta_{++} & \Delta_{+-} & -m-V+S & -\sigma\mathbf{p} \\ \Delta_{-+} & \Delta_{--} & -\sigma\mathbf{p} & m+V+S \end{pmatrix}$$

$$\Delta_{+-} = \Delta_{-+} \ll \Delta_{++} \ll \sigma\mathbf{p}$$

therefore we neglect Δ_{+-}

- total
- scalar
- vector time-like
- vector spacelike

Relativistic Hartree Bogoliubov (RHB):

| A | E/A | | E _{pair} | | |
|-----|--------|--------|-------------------|--------|--------|
| | expt. | RHB | Gogny | RHB | Gogny |
| 112 | -8.513 | -8.558 | -8.419 | -22.84 | -19.04 |
| 116 | -8.523 | -8.563 | -8.437 | -22.75 | -19.39 |
| 120 | -8.505 | -8.538 | -8.417 | -21.89 | -17.92 |
| 124 | -8.467 | -8.487 | -8.378 | -19.68 | -14.94 |
| 128 | -8.418 | -8.414 | -8.326 | -13.97 | -9.45 |
| 132 | -8.355 | -8.319 | -8.283 | 0.00 | 0.00 |

$$\hat{h} = \frac{\delta E'_{\text{RMF}}}{\delta \hat{\rho}}$$

$$\hat{\Delta} = \frac{\delta E_{\text{GOG}}}{\delta \hat{\kappa}}$$

$$E[\rho, \kappa] = E_{\text{RMF}}[\rho] + E_{\text{Gogny}}[\kappa]$$

Conclusions part I:

- 1) density functional theory is in principle exact
- 2) microscopic derivation of $E(\rho)$ very difficult
- 3) Lorentz symmetry gives essential constraints
 - large spin orbit splitting
 - relativistic saturation
 - unified theory of time-odd fields
- 4) pairing effects are non-relativistic

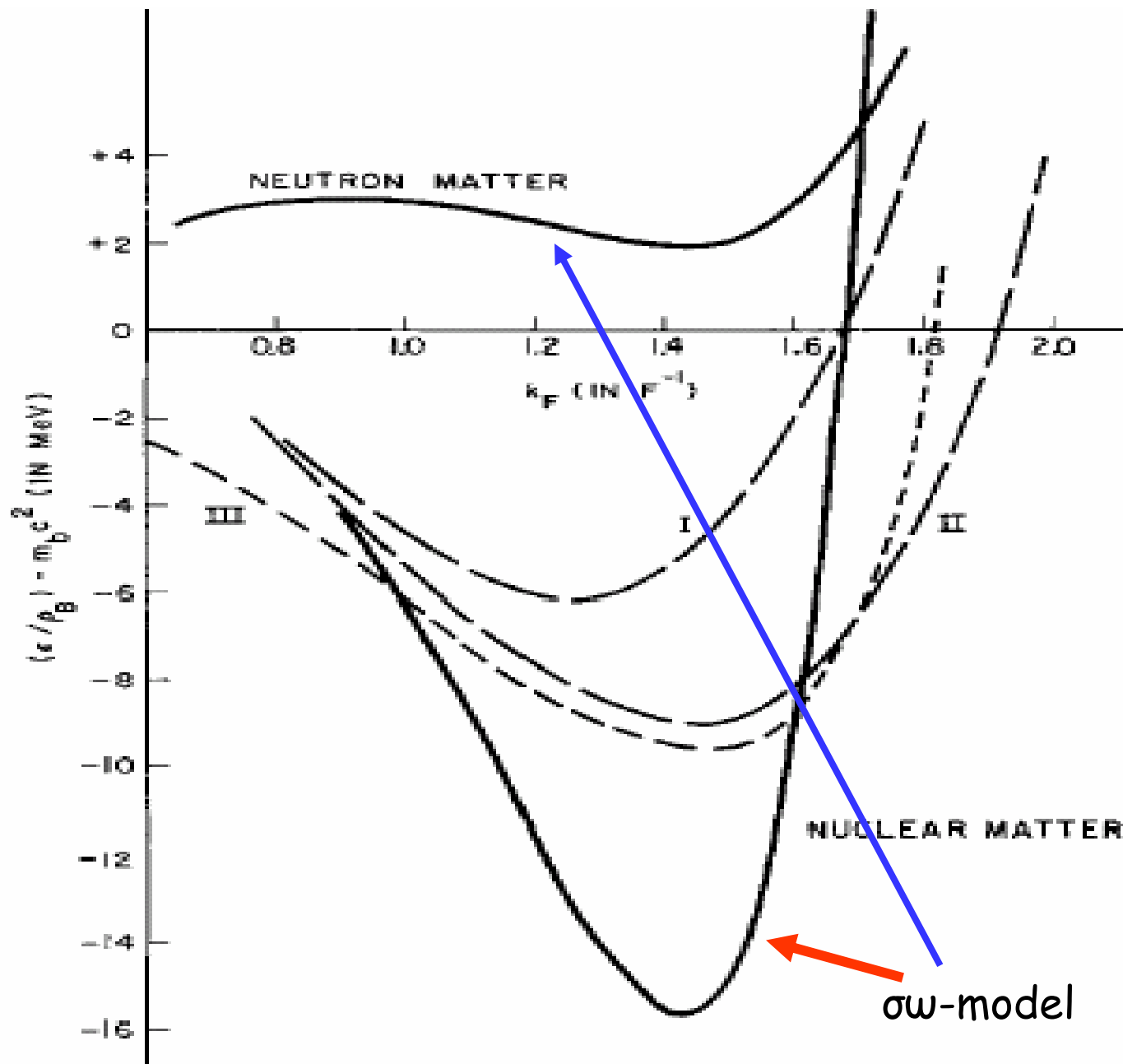
Content II

● Ground state properties

- * nuclear matter
- * masses, radii, deformations
- * shell quenching
- * neutron skins and halo phenomena
- * proton emitters
- * superheavy elements

● Vibrational excitations

- * breathing modes (incompressibility)
- * giant dipole modes (symmetry energy)
- * pygmy resonances
- * isobaric analog resonances
- * Gamov-Teller resonances



Effective density dependence:

non-linear potential:

NL1, NL3..

Boguta and Bodmer, NPA. 431, 3408 (1977)

$$\frac{1}{2}m_{\sigma}^2\sigma^2 \Rightarrow U(\sigma) = \frac{1}{2}m_{\sigma}^2\sigma^2 + \frac{1}{3}g_2\sigma^3 + \frac{1}{4}g_3\sigma^4$$

density dependent coupling constants:

R.Brockmann and H.Toki, PRL 68, 3408 (1992)

S.Typeel and H.H.Wolter, NPA 656, 331 (1999)

$$g_o, g_{\omega}, g_{\rho} \Rightarrow g_o(\rho), g_{\omega}(\rho), g_{\rho}(\rho)$$

new

$$g \rightarrow g(\rho(r))$$

DD-ME1, DD-ME2

Parameterization of density dependence

MICROSCOPIC: Dirac-Brueckner calculations

saturation density

PHENOMENOLOGICAL:

$$g_i(\rho) = g_i(\rho_{\text{sat}}) f_i(x)$$

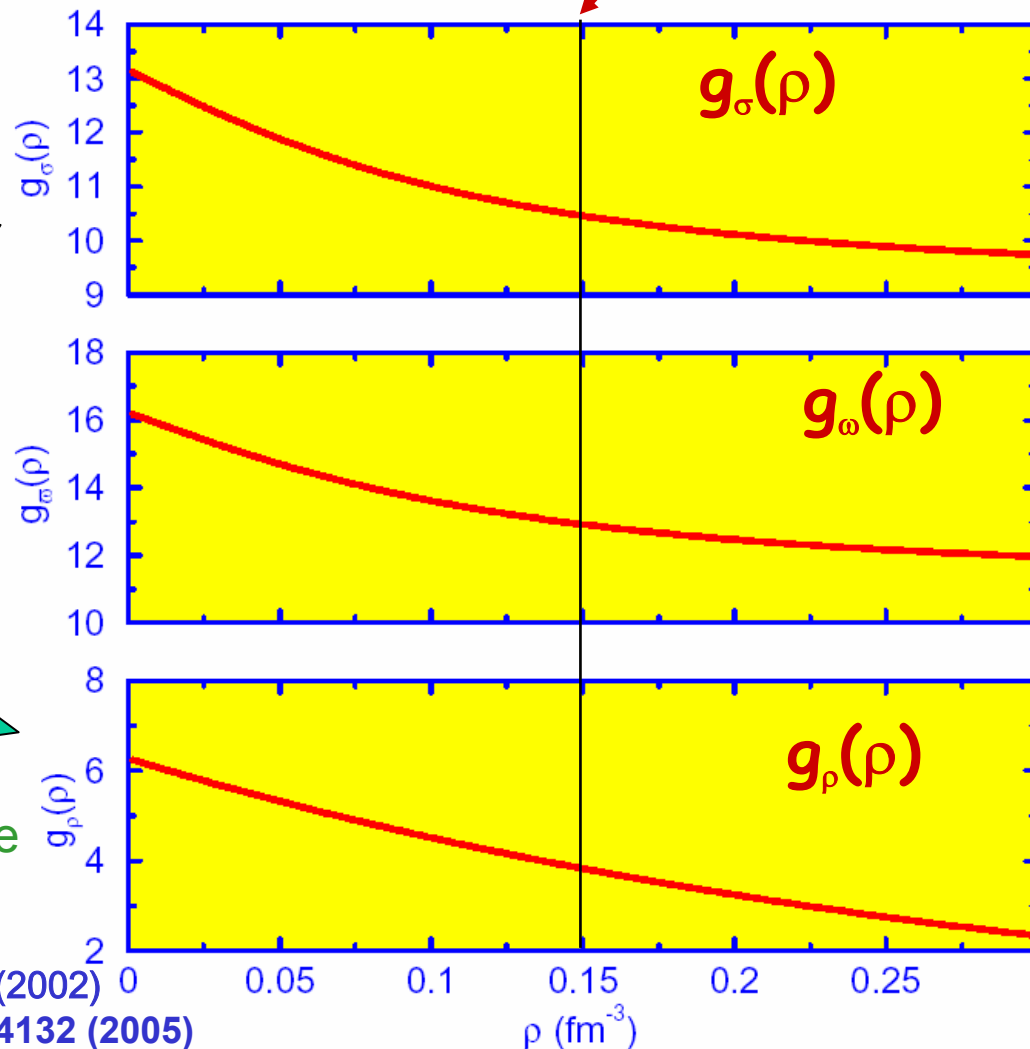
$$f_i(x) = a_i \frac{1 + b_i(x + d_i)^2}{1 + c_i(x + d_i)^2}$$

$$i = \sigma, \omega$$

$$g_\rho(\rho) = g_\rho(\rho_{\text{sat}}) e^{-a_\rho(x-1)}$$

$$x = \rho / \rho_{\text{sat}}$$

4 parameters for density dependence



Typel and Wolter, NPA 656, 331 (1999)

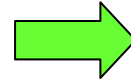
Niksic, Vretenar, Finelli, Ring, PRC 66, 024306 (2002)

Lalazissis, Niksic, Vretenar, Ring, PRC 71 024132 (2005)

How many parameters ?

7 parameters

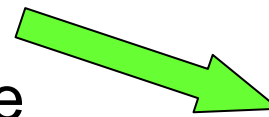
symmetric nuclear matter: $E/A, \rho_0$



$$\frac{g_\sigma}{m_\sigma}$$

$$\frac{g_\omega}{m_\omega}$$

finite nuclei (N=Z): $E/A,$ radii
spinorbit for free



$$m_\sigma$$

Coulomb (N≠Z):

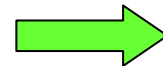
a_4



$$\frac{g_\rho}{m_\rho}$$

density dependence: T=0

K_∞

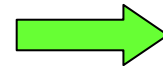


$$g_2$$

$$g_2$$

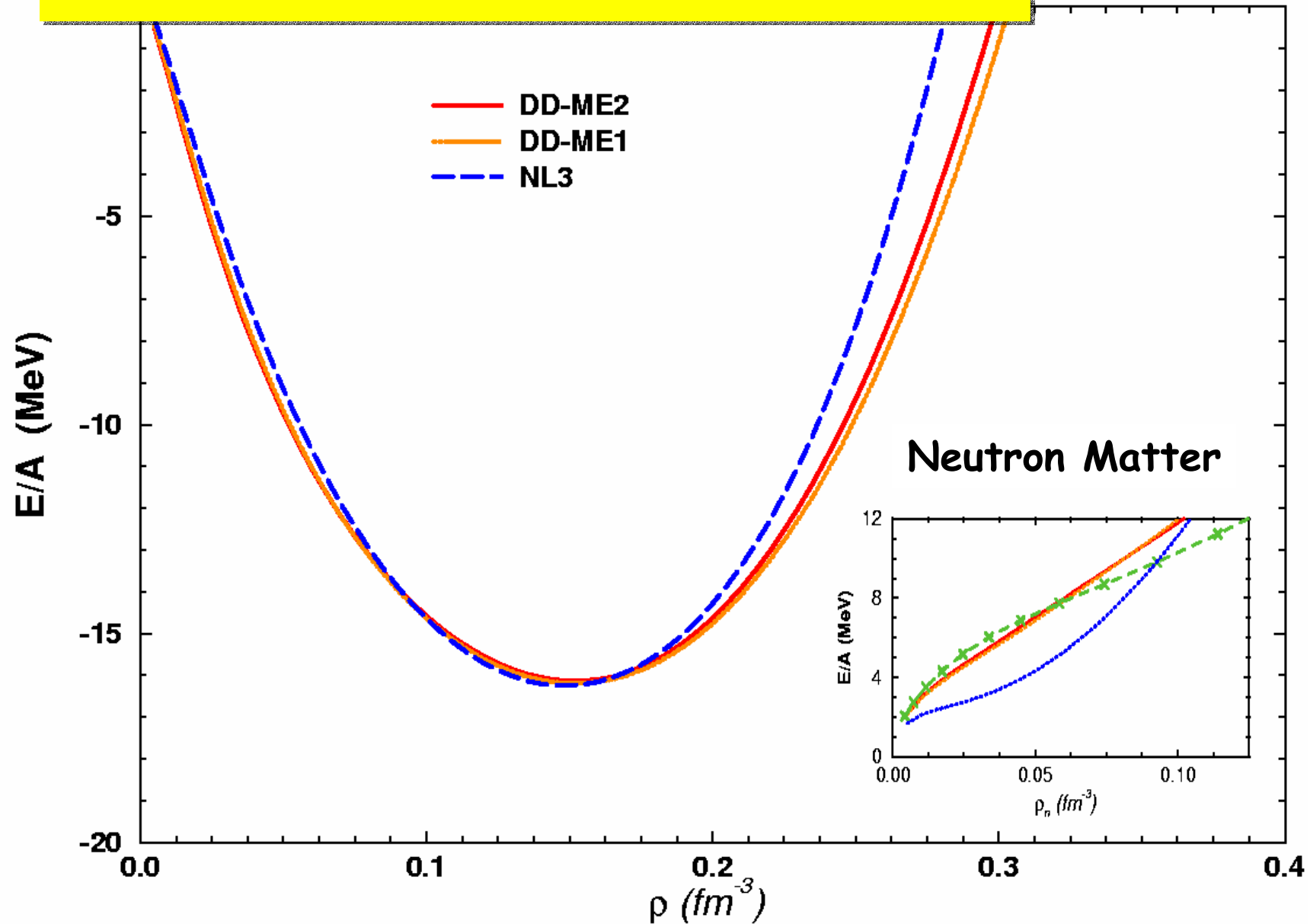
T=1

$r_n - r_p$



$$a_\rho$$

Nuclear matter equation of state



Symmetry energy

$$\alpha \equiv \frac{N-Z}{N+Z}$$

$$E(\rho, \alpha) = E(\rho, 0) + S_2(\rho)\alpha^2 + S_4(\rho)\alpha^4 + \dots$$

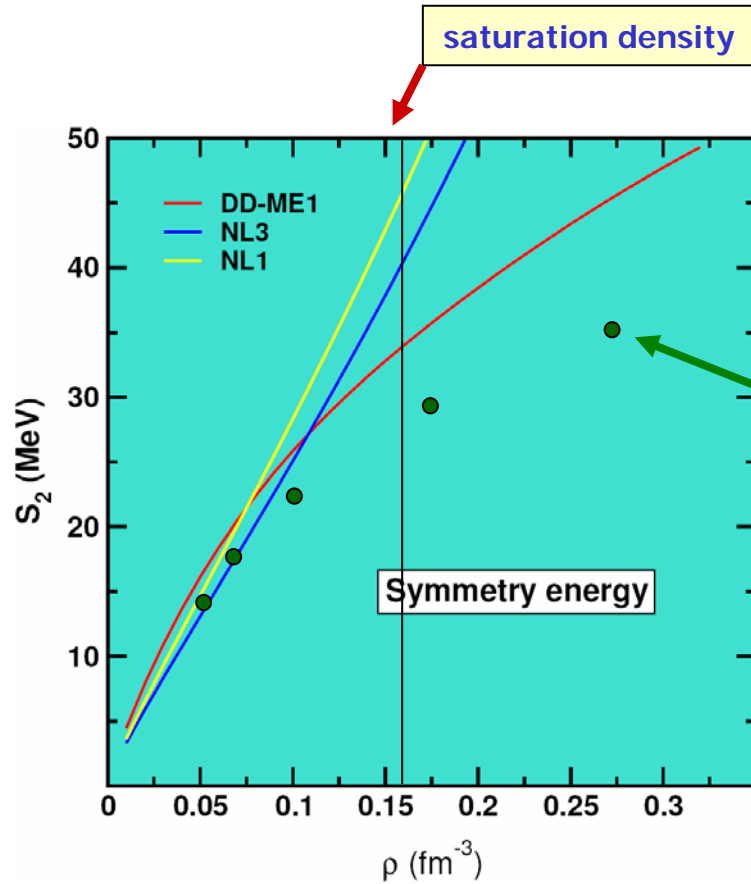
$$S_2(\rho) = a_4 + \frac{p_0}{\rho_{\text{sat}}^2} (\rho - \rho_{\text{sat}}) + \frac{\Delta K_0}{18\rho_{\text{sat}}^2} (\rho - \rho_{\text{sat}})^2 + \dots$$

empirical values:

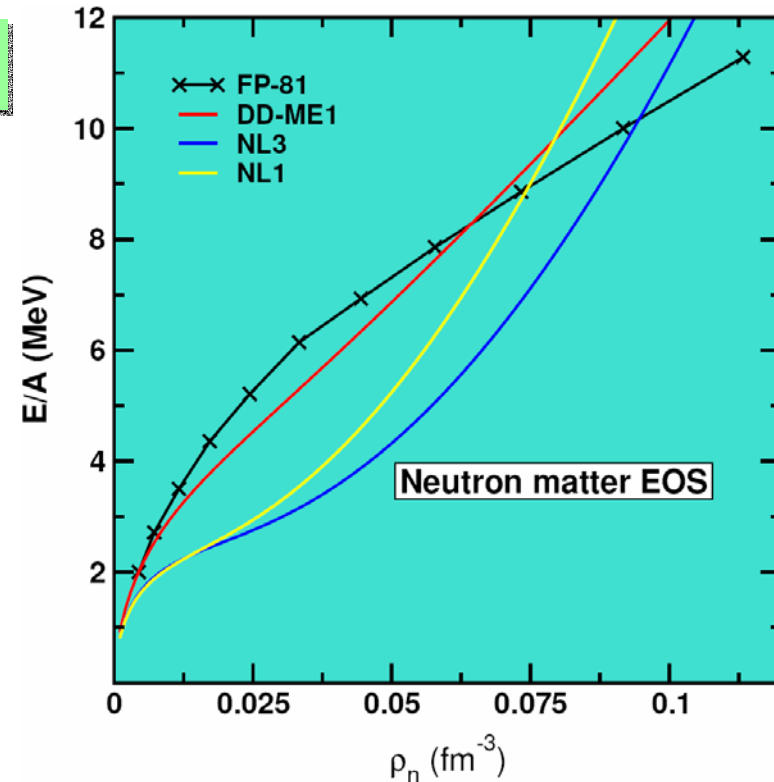
$$30 \text{ MeV} \leq a_4 \leq 34 \text{ MeV}$$

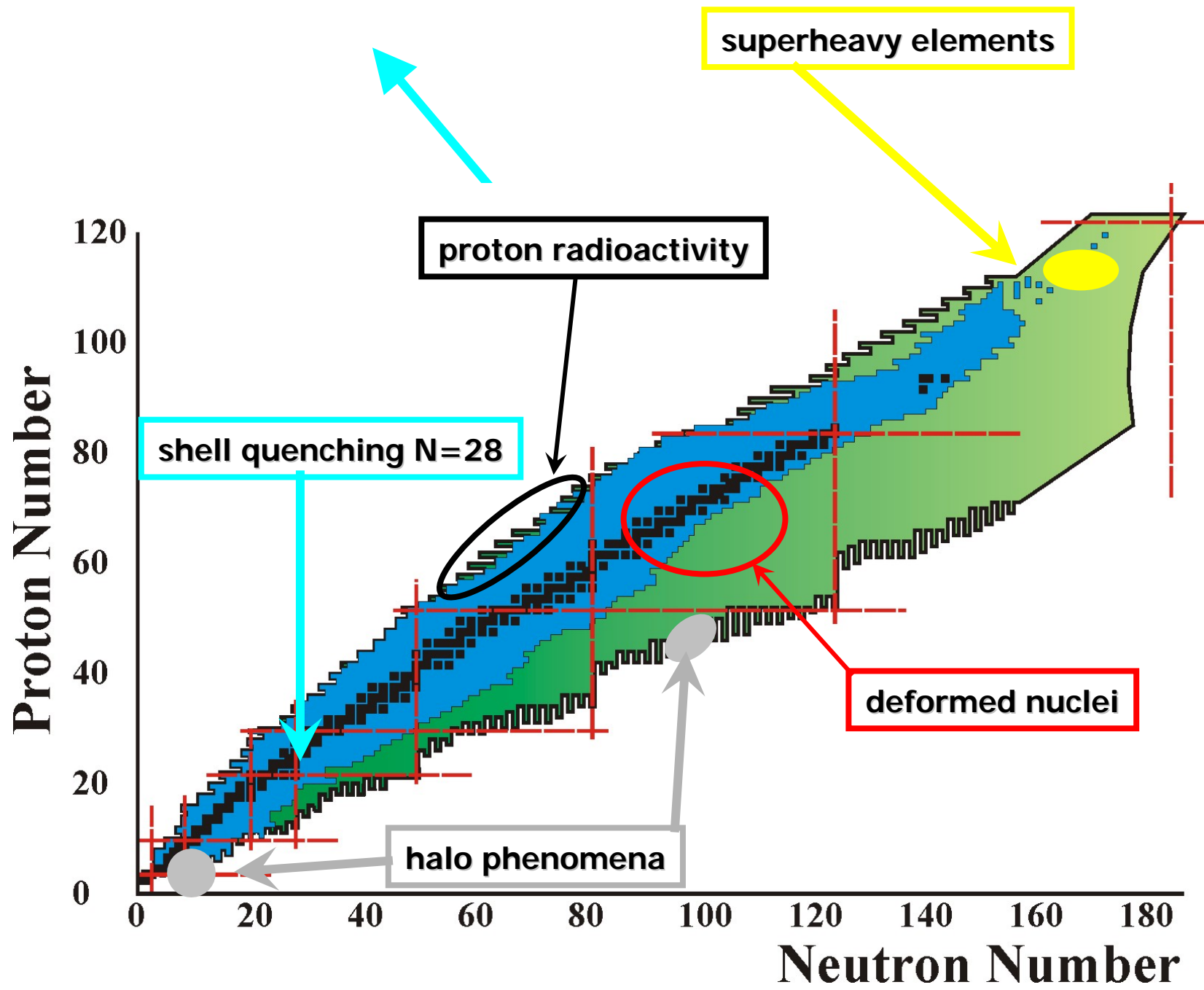
$$2 \text{ MeV/fm}^3 < p_0 < 4 \text{ MeV/fm}^3$$

$$-200 \text{ MeV} < \Delta K_0 < -50 \text{ MeV}$$



| | DD-ME1 | NL3 | NL1 |
|--------------------------|--------|------|------|
| $a_4(\text{MeV})$ | 33.1 | 37.9 | 43.7 |
| $p_0(\text{MeV/fm}^3)$ | 3.26 | 5.92 | 7.0 |
| $\Delta K_0(\text{MeV})$ | -128.5 | 52.1 | 67.3 |





superheavy elements

proton radioactivity

shell quenching N=28

deformed nuclei

halo phenomena

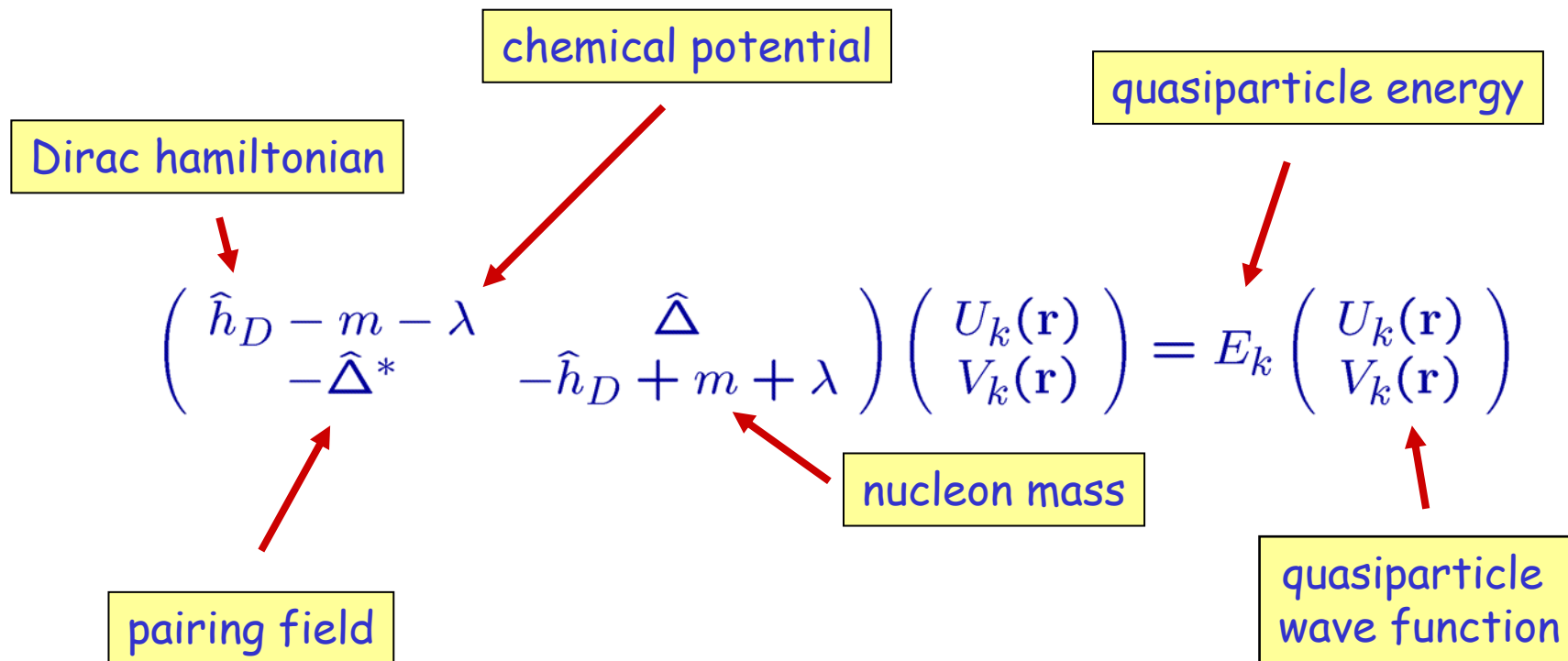
Proton Number

Neutron Number

Relativistic Hartree Bogoliubov theory (RHB)

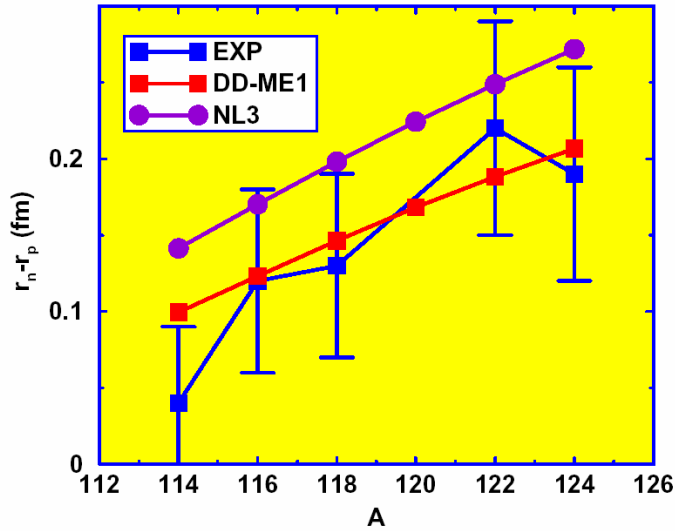
Ground-state properties of weakly bound nuclei far from stability

→ Unified description of mean-field and pairing correlations

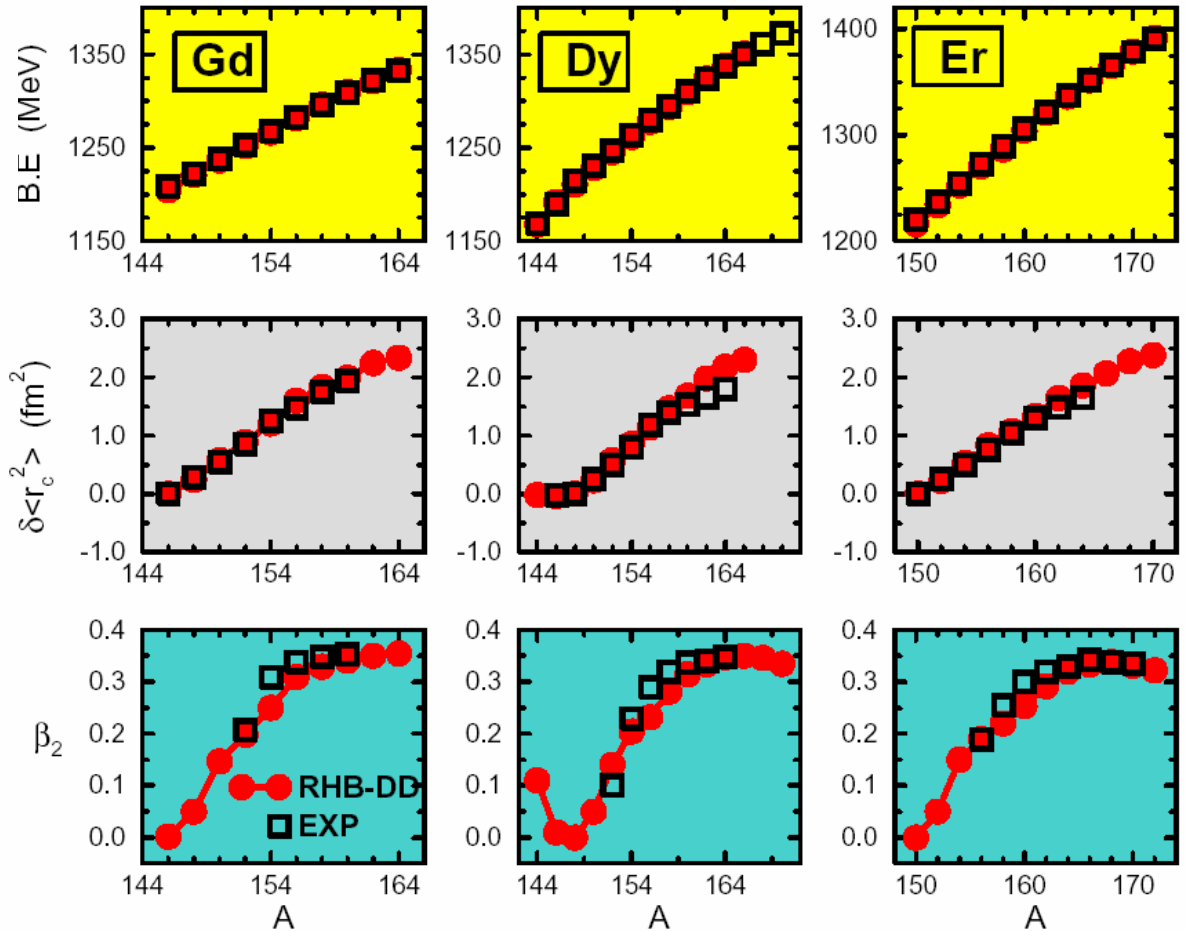


$$\Delta_{ab}(\vec{r}, \vec{r}') = \frac{1}{2} \sum_{c,d} V_{abcd}^{pp}(\vec{r}, \vec{r}') \kappa_{cd}(\vec{r}, \vec{r}')$$

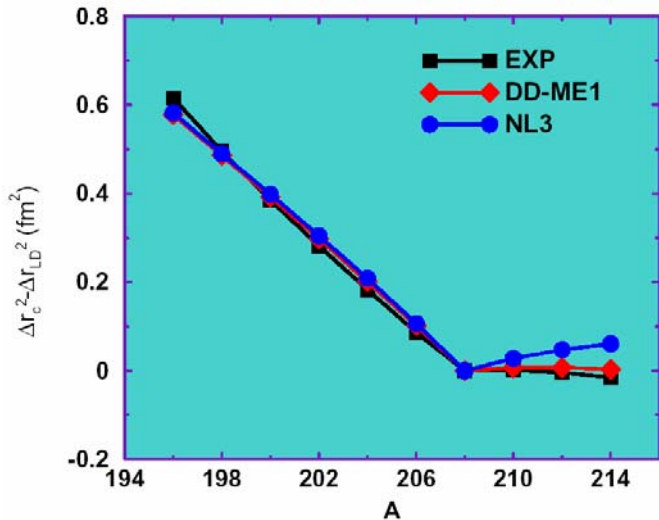
Ground state properties of finite nuclei



Binding energies, charge isotope shifts, and quadrupole Deformations of Gd, Dy, and Er isotopes.

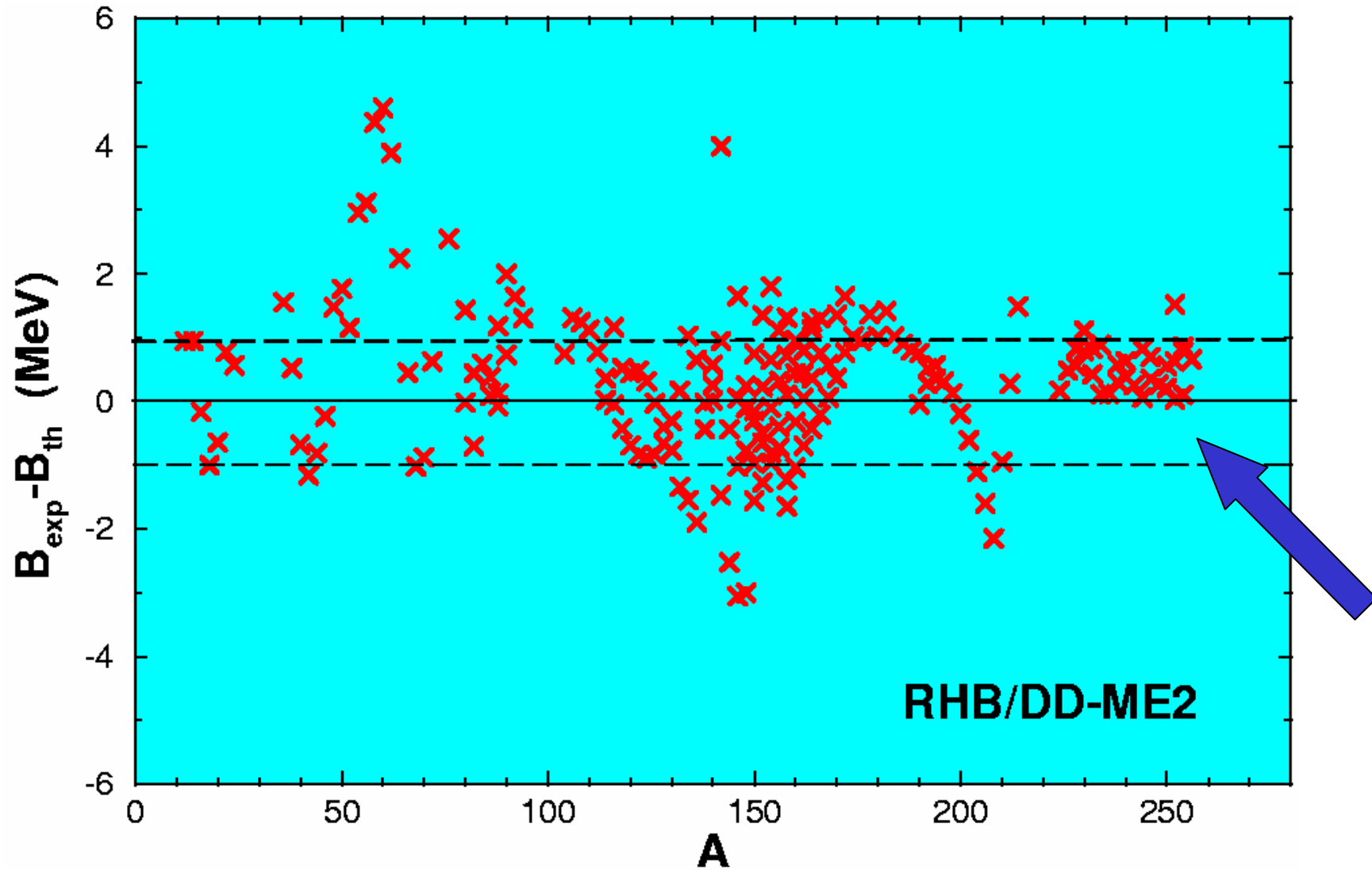


Charge isotope shifts in even-A Pb isotopes.



rms-deviations: masses: $\Delta m = 900$ keV
radii: $\Delta r = 0.015$ fm

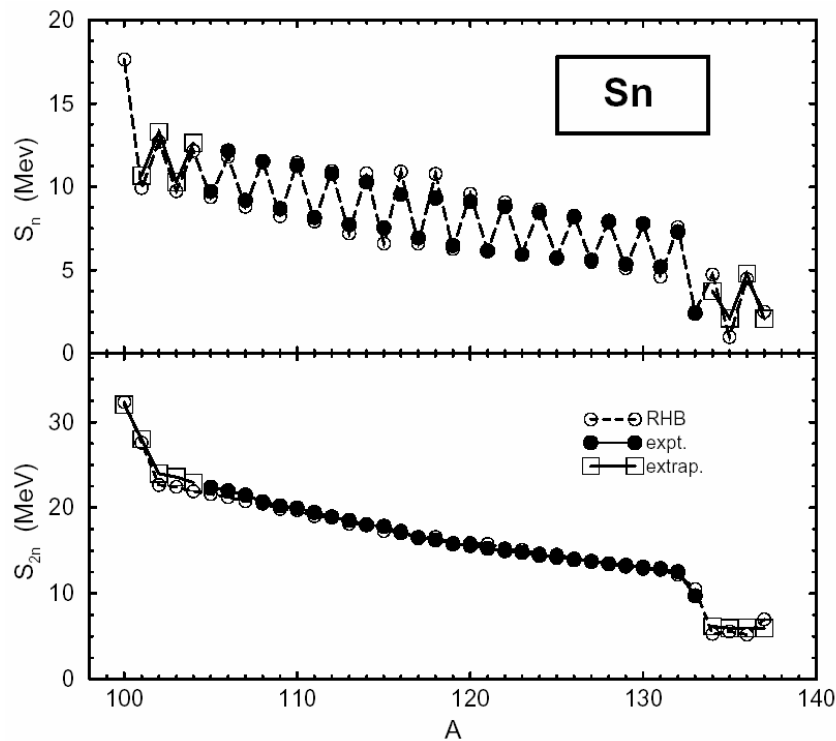
Lalazissis, Niksic, Vretenar, Ring, PRC submitted



ground state properties of Ni and Sn isotopes

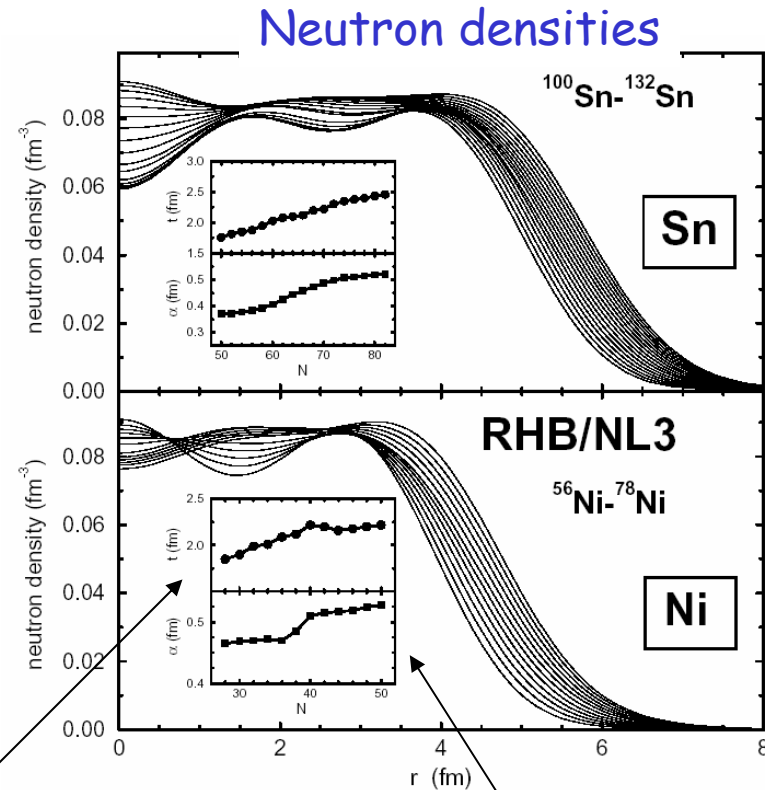
Lalazisis, Vretenar, Ring, Phys. Rev. C57, 2294 (1998)

combination of the NL3 effective interaction for the RMF Lagrangian, and the Gogny interaction with the parameter set D1S in the pairing channel.



One- and two-neutron separation energies

surface thickness



surface diffuseness α

$$\rho(r) = \rho_0 \left(1 + \exp\left(\frac{r-R_0}{\alpha}\right) \right)^{-1}$$

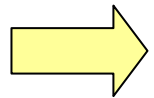
reduction of the spin-orbit potential

The **spin-orbit potential** originates from the addition of two large fields: the field of the vector mesons (short range repulsion), and the scalar field of the sigma meson (intermediate attraction).

$$V_{s.o.} \approx \frac{1}{r} \frac{\partial}{\partial r} V_{ls}(r)$$

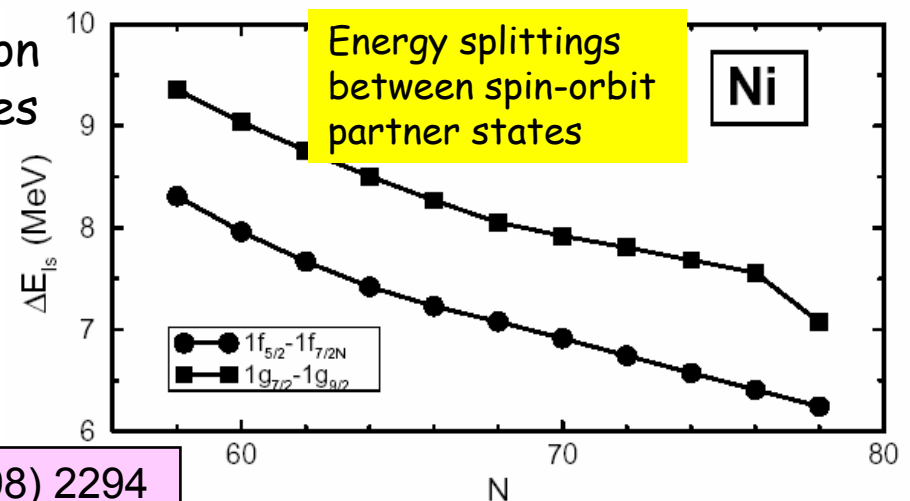
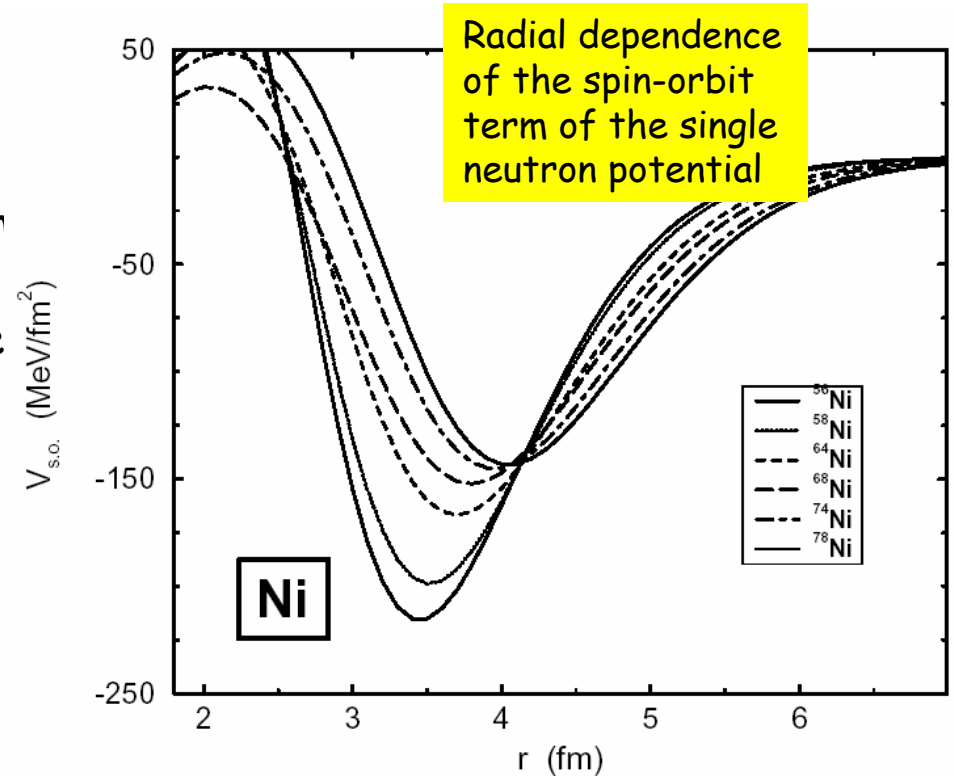
$$V_{ls} = \frac{m}{m_{eff}} (V + S)$$

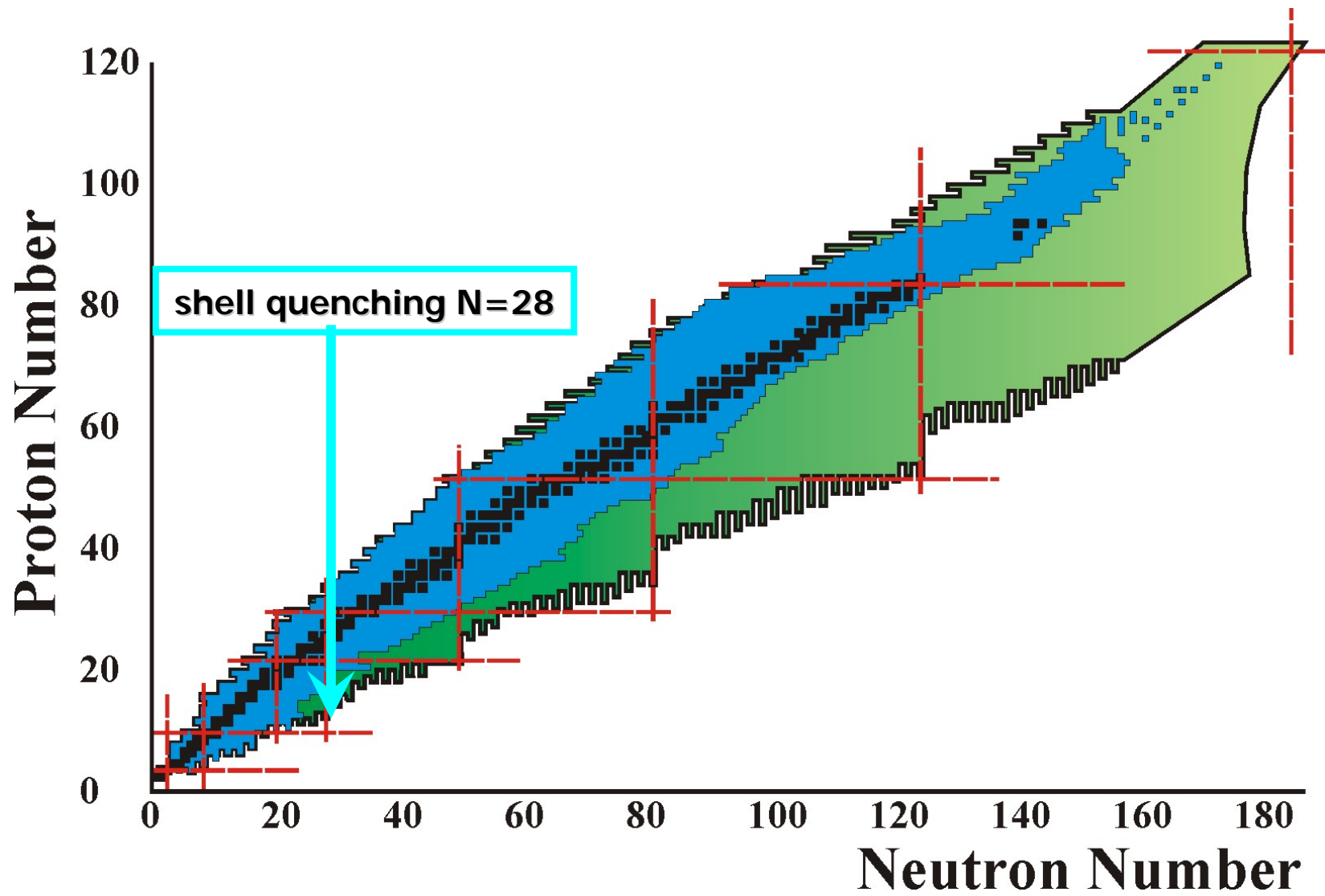
weakening of the effective single-neutron spin-orbit potential in neutron-rich isotopes



reduced energy spacings between spin-orbit partners

$$\Delta E_{ls} = E_{n,l,j=l-1/2} - E_{n,l,j=l+1/2}$$





Shape coexistence in the deformed N=28 region

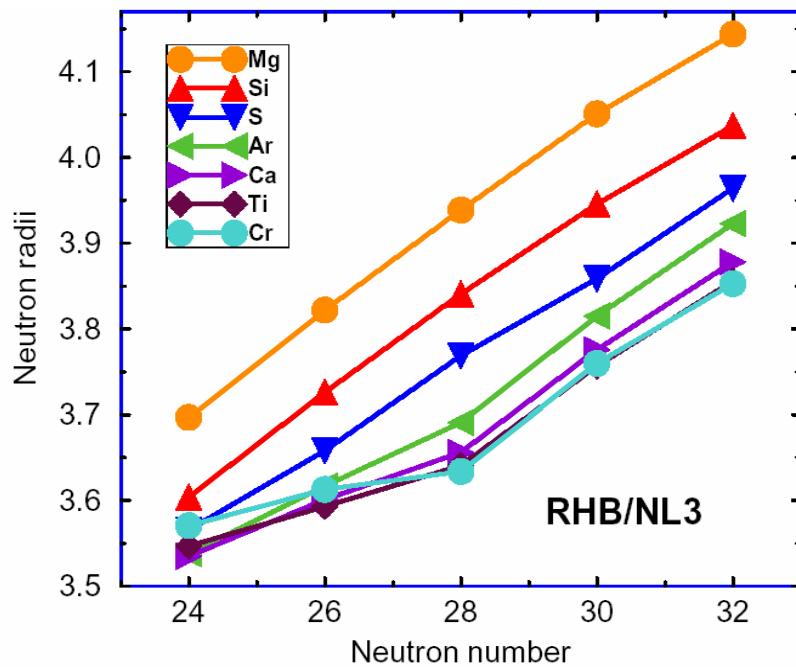
Lalazisis, Vretenar, Ring, Stoitsov, Robledo, Phys. Rev. C60, 014310 (1999)



RHB description of neutron rich N=28 nuclei. NL3+D1S effective interaction.

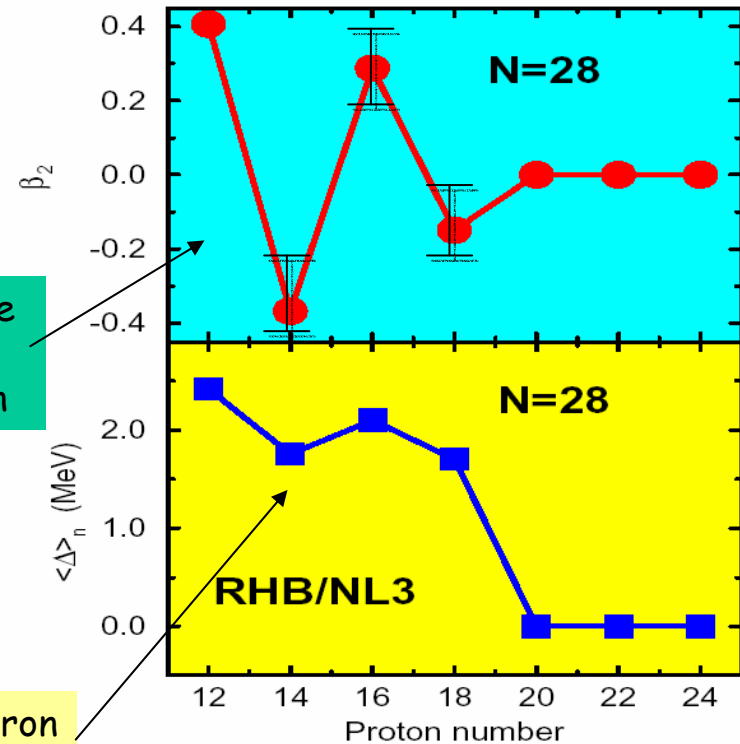
Strong suppression of the spherical N=28 shell gap.

1f7/2 → fp core breaking → Shape coexistence



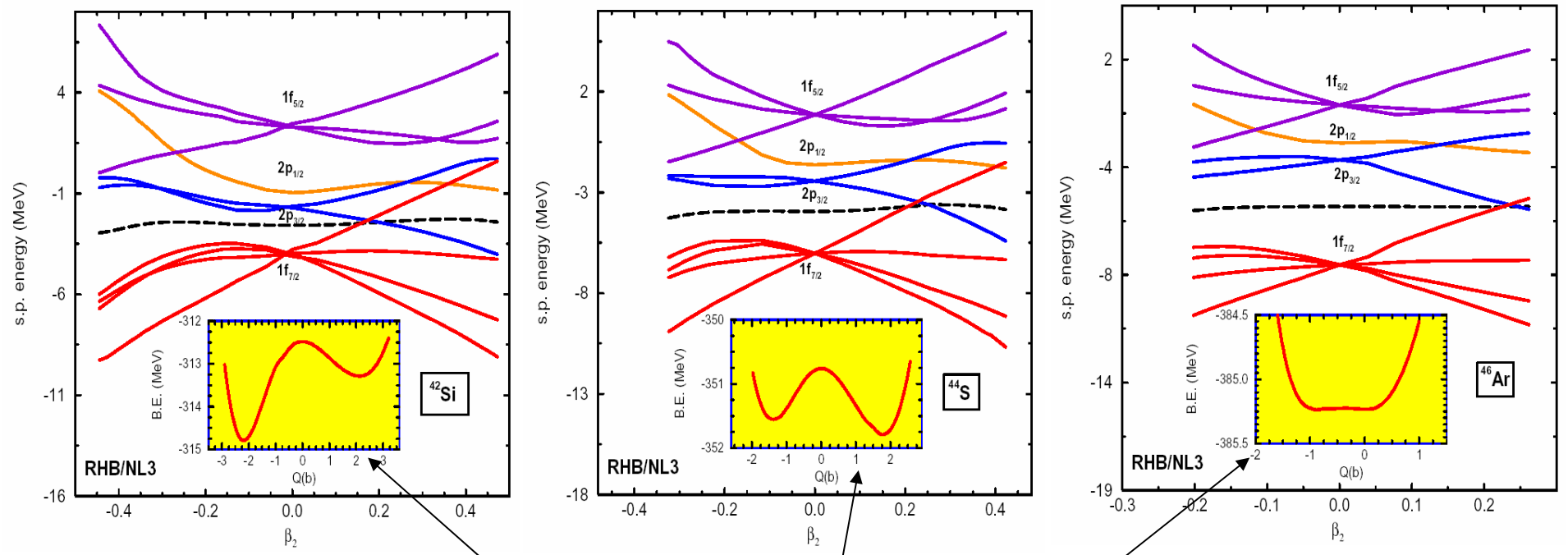
Ground-state quadrupole deformation

Average neutron pairing gaps





Neutron single-particle levels for ^{42}Si , ^{44}S , and ^{46}Ar as functions of the quadrupole deformation. The energies in the canonical basis correspond to ground-state RHB solutions with constrained quadrupole deformation.

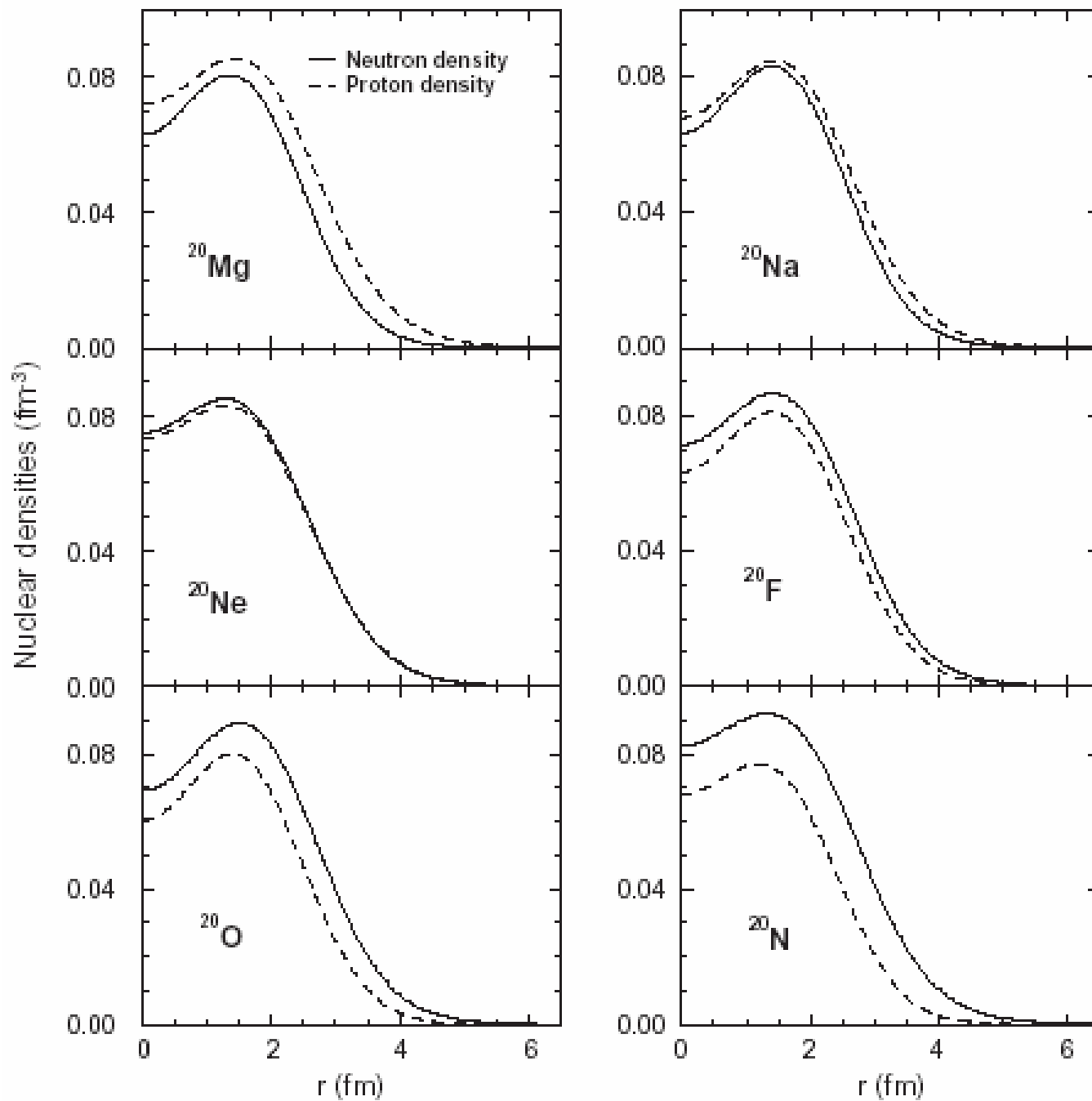


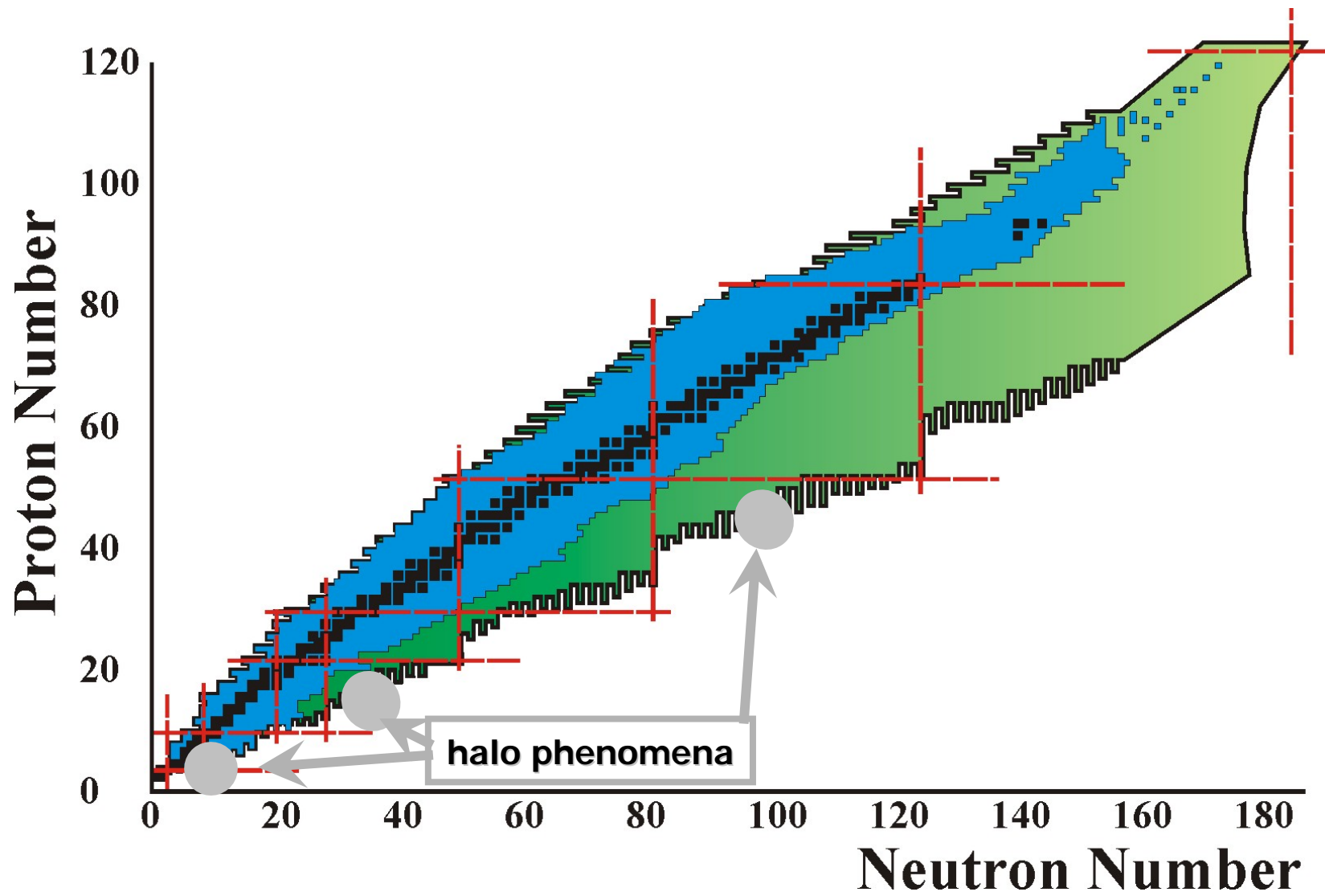
Total binding energy curves

SHAPE COEXISTENCE

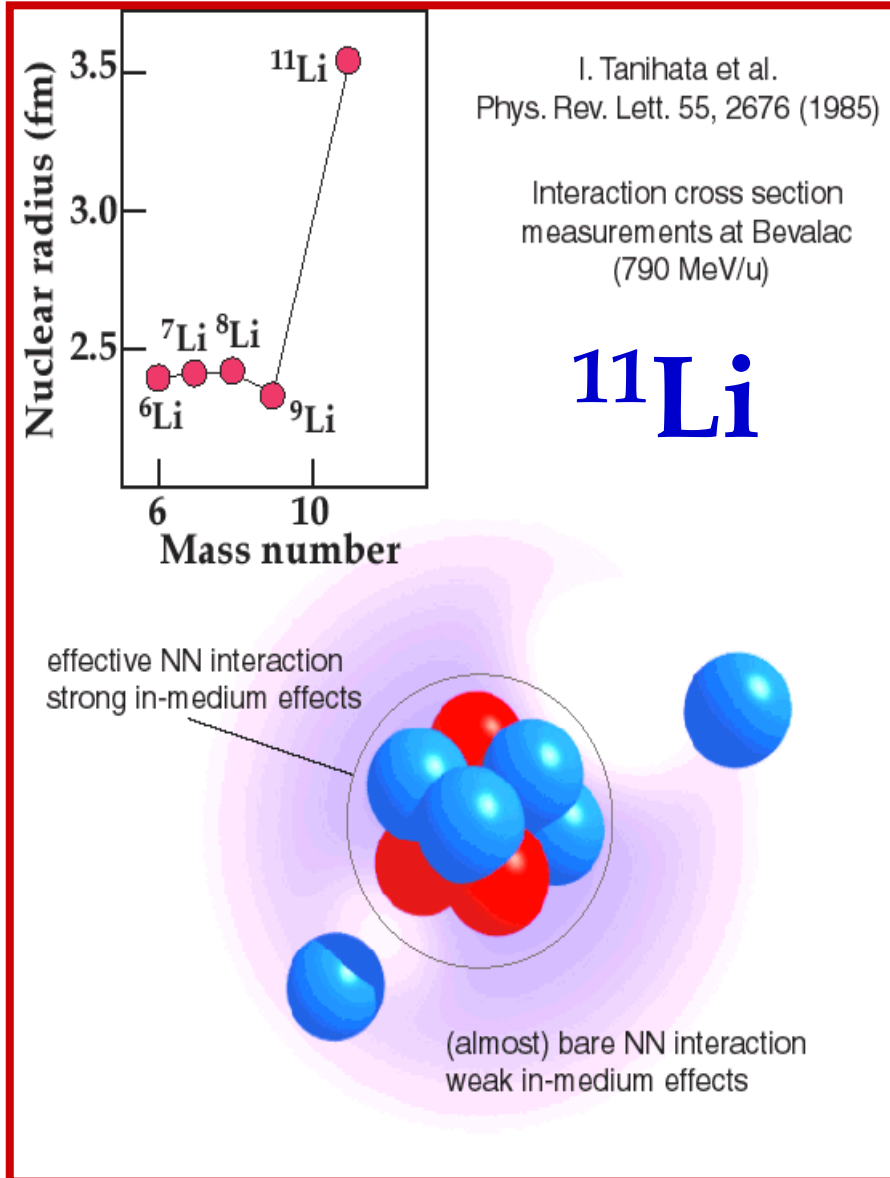
Evolution of the shell structure, shell gaps and magicity with neutron number!

proton- and
neutron skins





Neutron halo's



Mean field theory of halo's: (RHB in the continuum)

advantages:

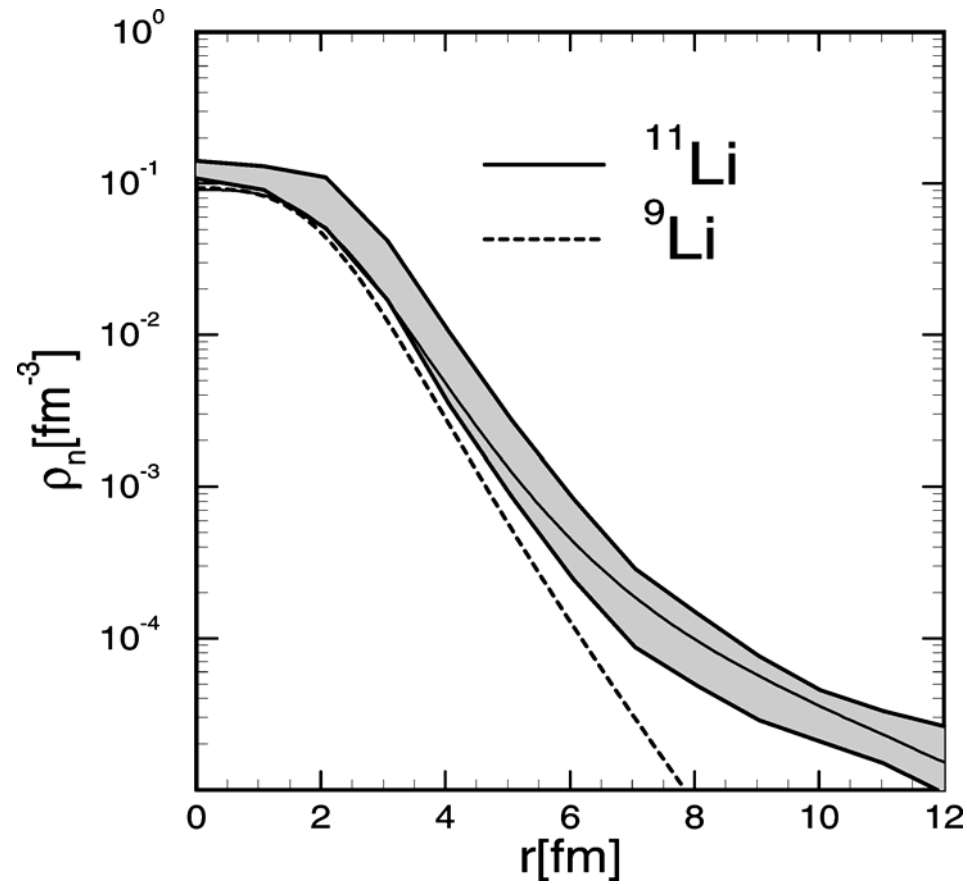
- * residual interaction by pairing
- * self-consistent description
- * universal parameters
- * polarization of the core
- * treatment of the continuum

problems:

- * center of mass motion
- * boundary conditions at infinity

Densities in Li-isotopes

J. Meng and P. Ring , PRL 77, 3963 (1996)
J. Meng and P. Ring , PRL 80, 460 (1998)



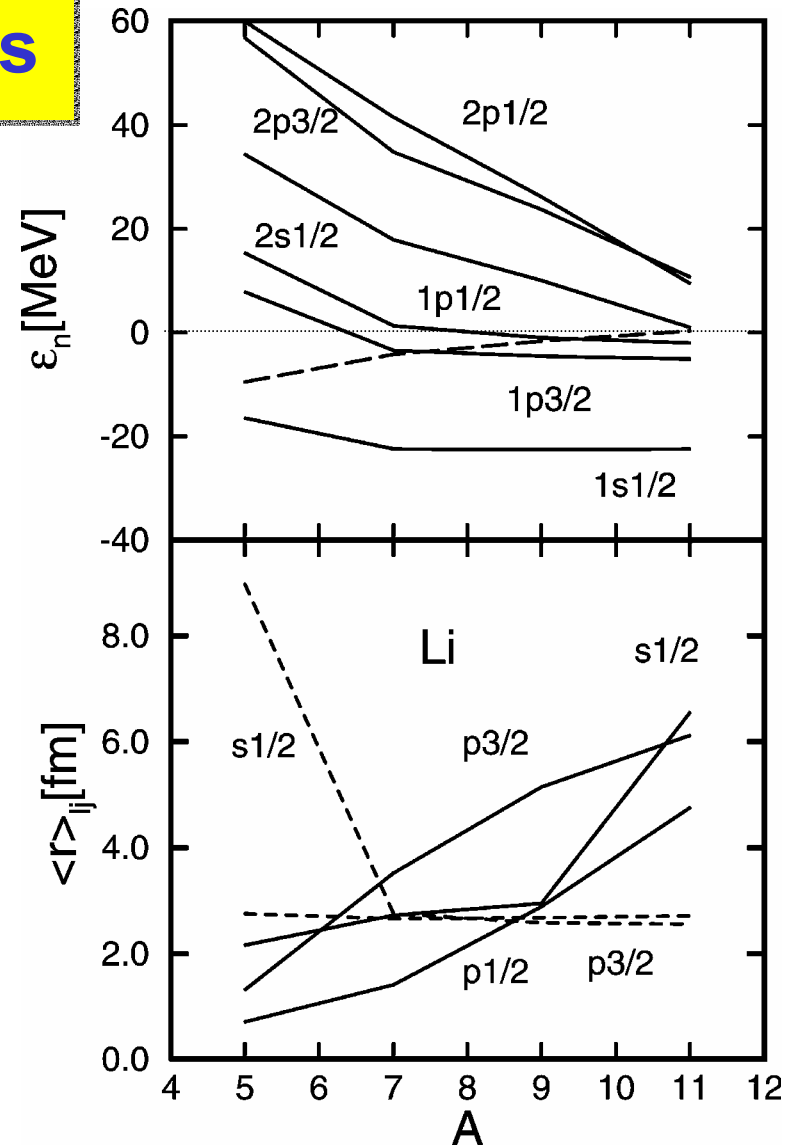
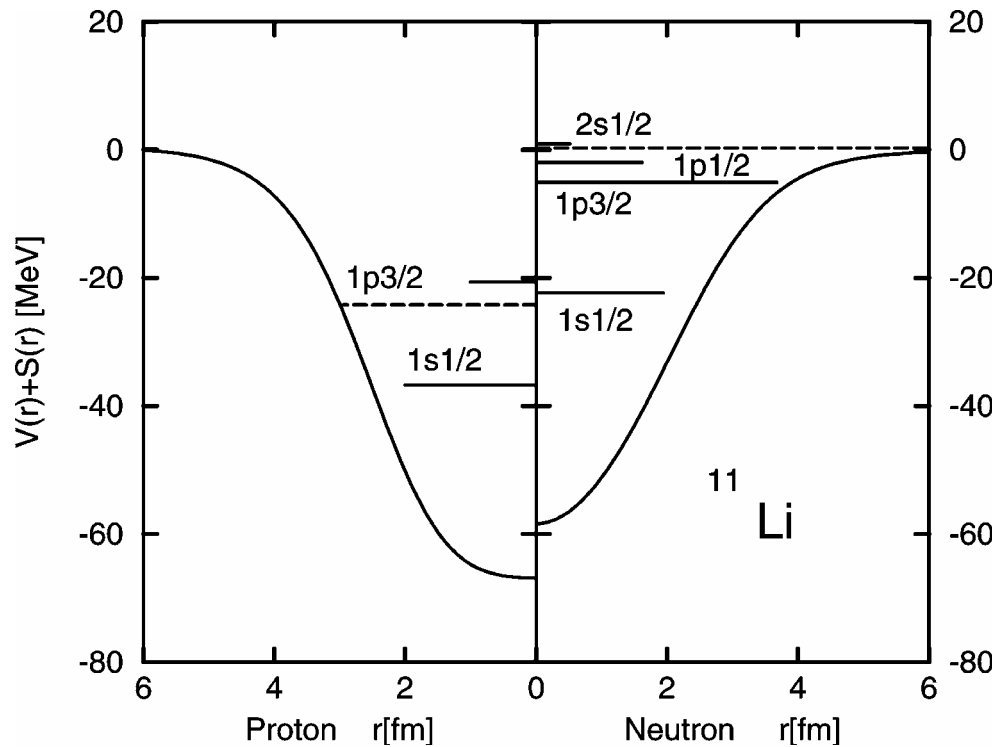
rel. Hartree-Bogoliubov
in the continuum
density dependent δ -pairing

canonical basis in Li-isotopes

- * eigenstates of the density matrix
- * wavefunction has BCS-type

$$|\Phi\rangle = \prod_n (u_n + v_n a_n^+ a_n^+) |-\rangle$$

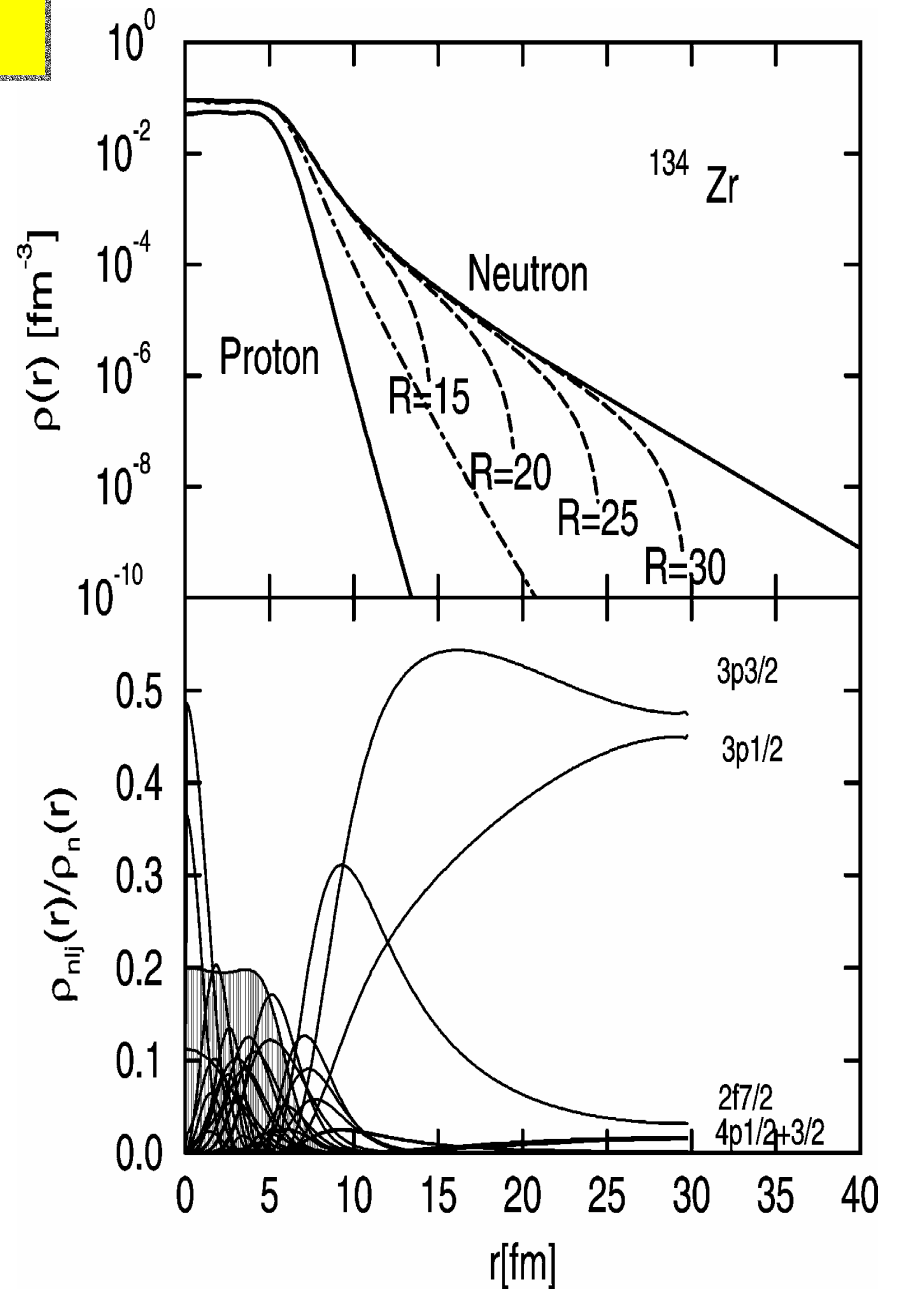
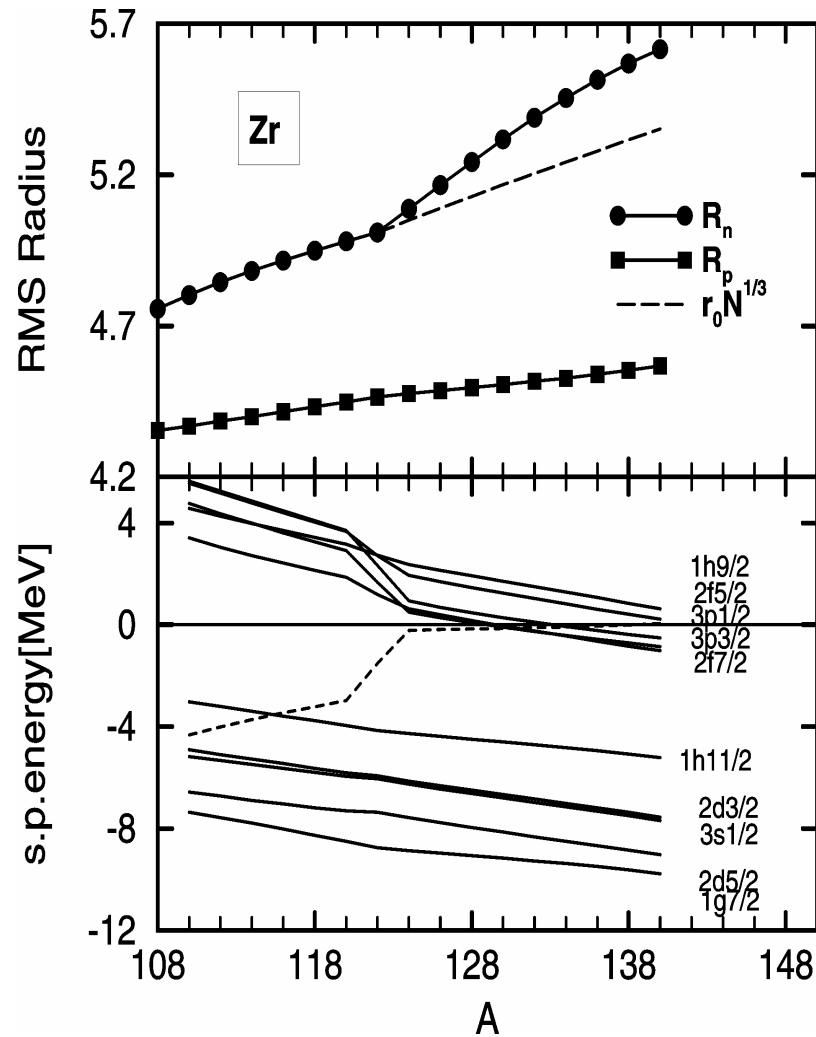
$$\varepsilon_n = \langle n|h|n\rangle, \quad \Delta_n = \langle n|\Delta|n\rangle$$

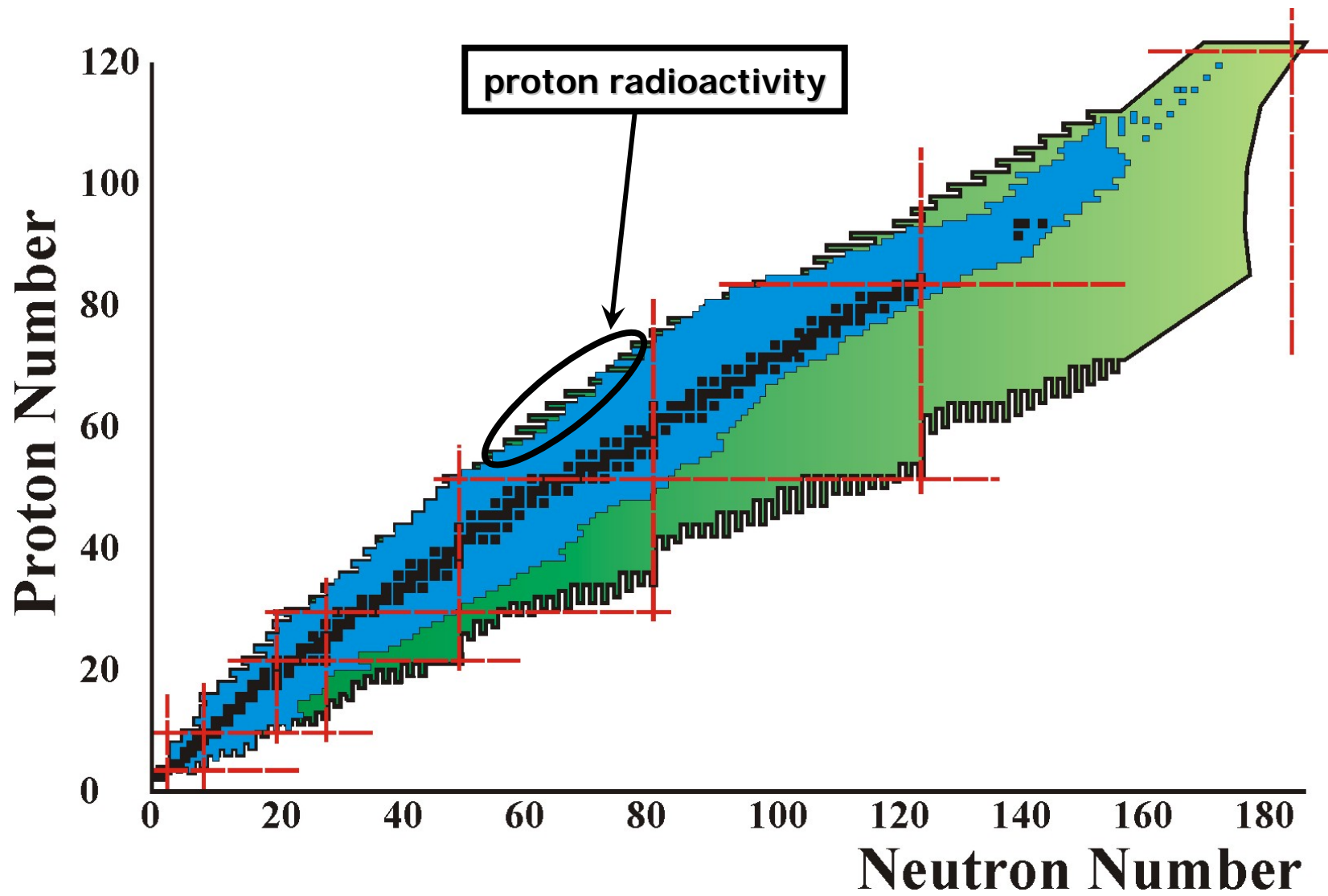


J. Meng and P. Ring, PRL 77, 3963 (1996)

Giant halo in the Zr region:

J. Meng and P. Ring, PRL 80, 460 (1998)

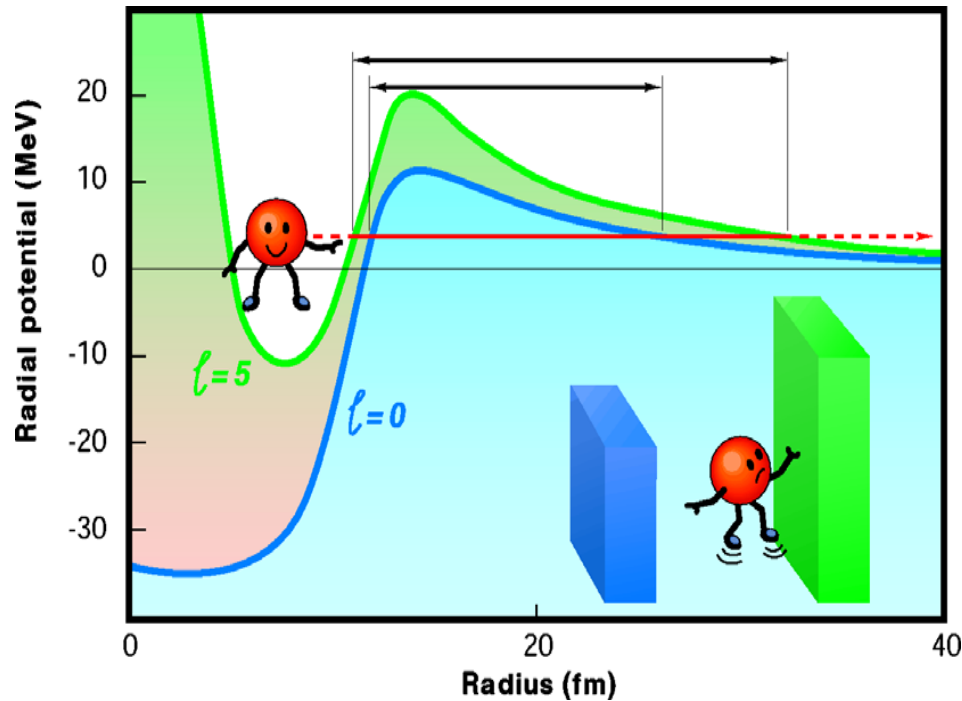




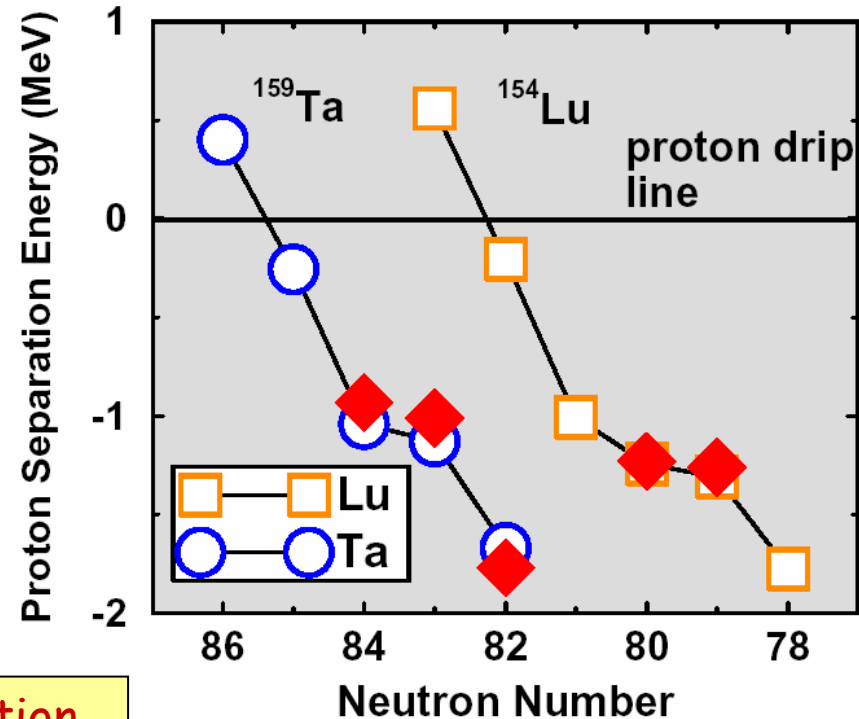
Nuclei at the proton drip line:

Vretenar, Lalazissis, Ring, Phys.Rev.Lett. 82, 4595 (1999)

characterized by exotic ground-state decay modes such as the direct emission of charged particles and β -decays with large Q-values.



Ground-state proton emitters

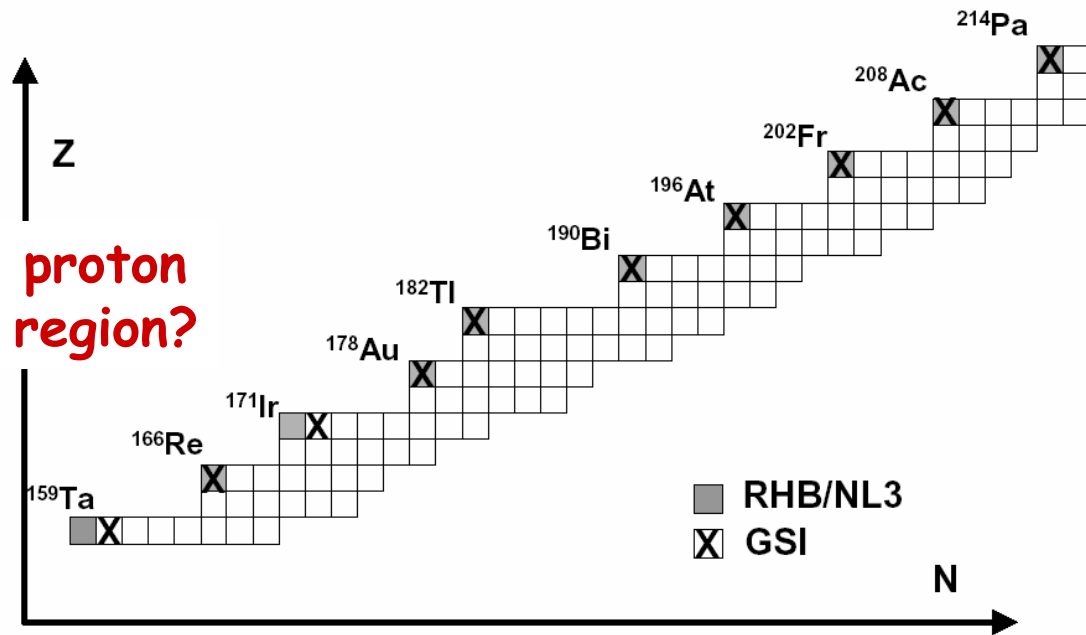


Self-consistent RHB calculations \rightarrow separation energies, quadrupole deformations, odd-proton orbitals, spectroscopic factors

Lalazissis, Vretenar, Ring
Phys.Rev. C60, 051302 (1999)

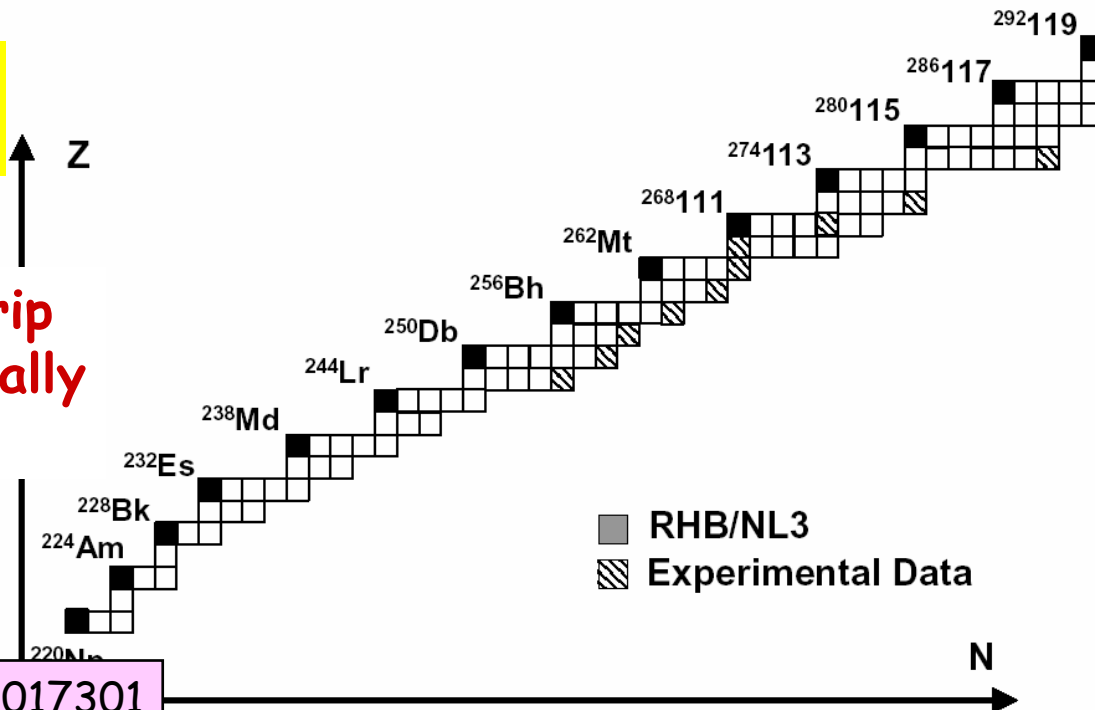
The proton drip-line in the sub-Uranium region.

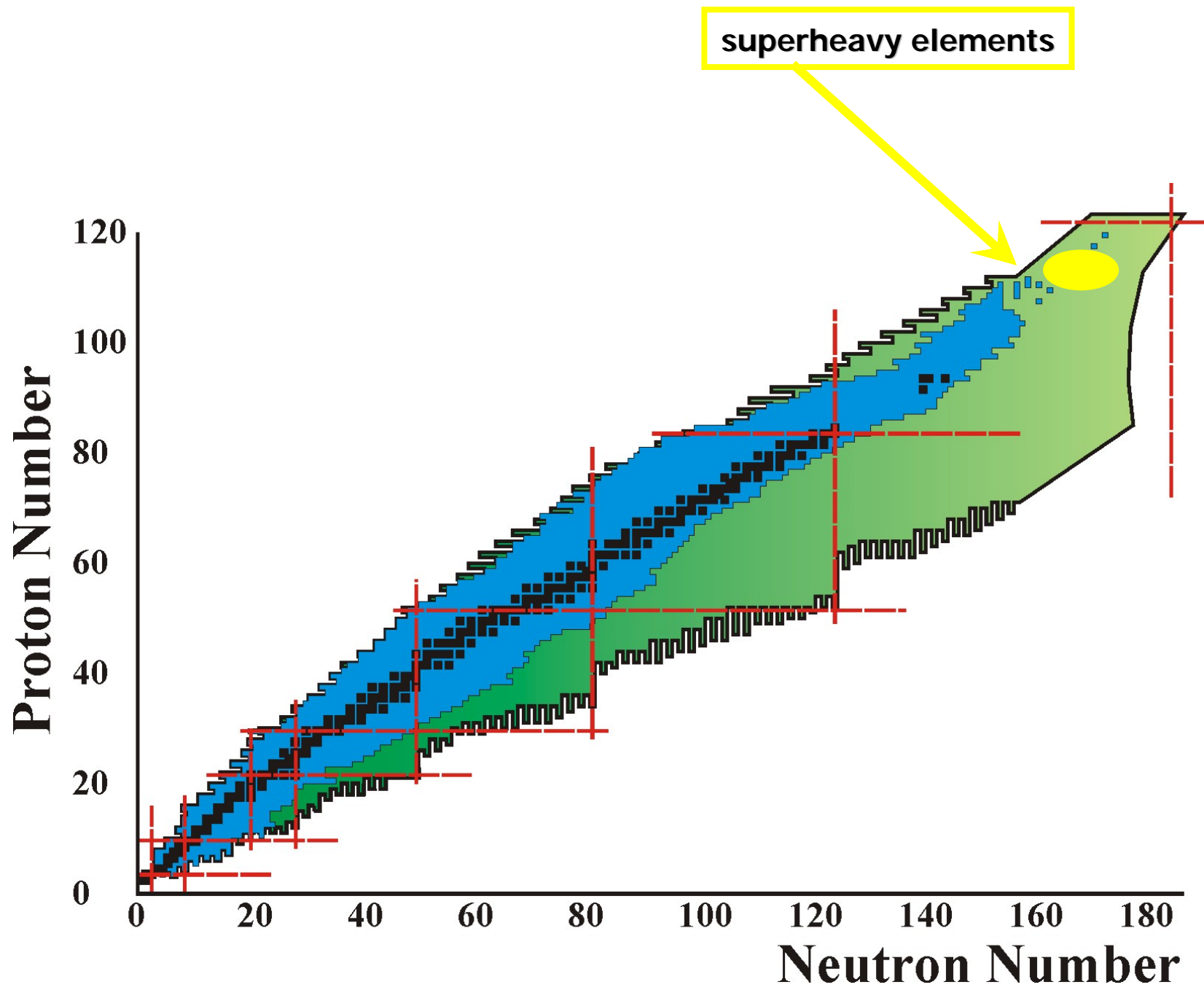
Possible ground-state proton emitters in this mass region?



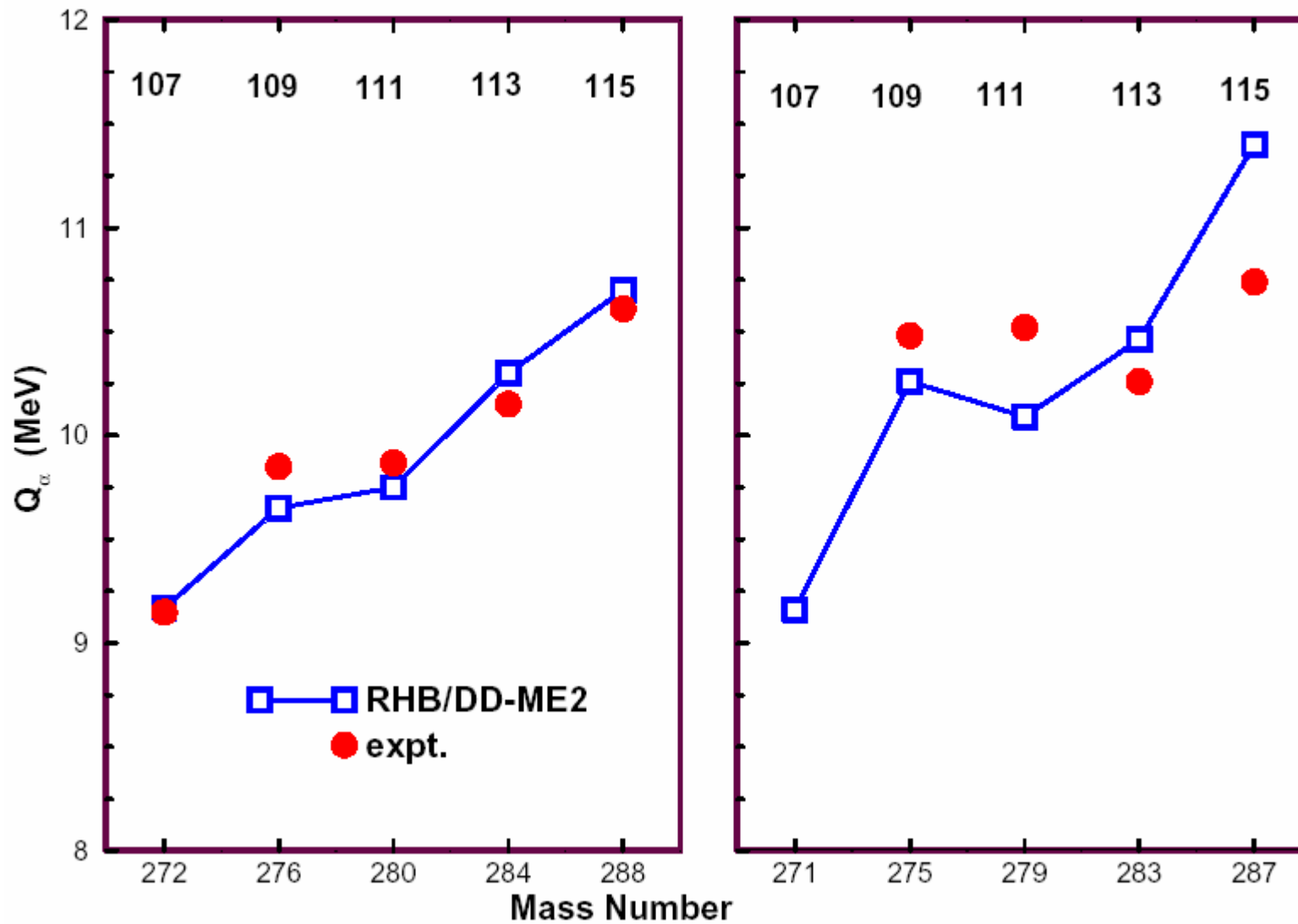
The proton drip-line in the region of superheavy elements.

How far is the proton-drip line from the experimentally known superheavy nuclei?



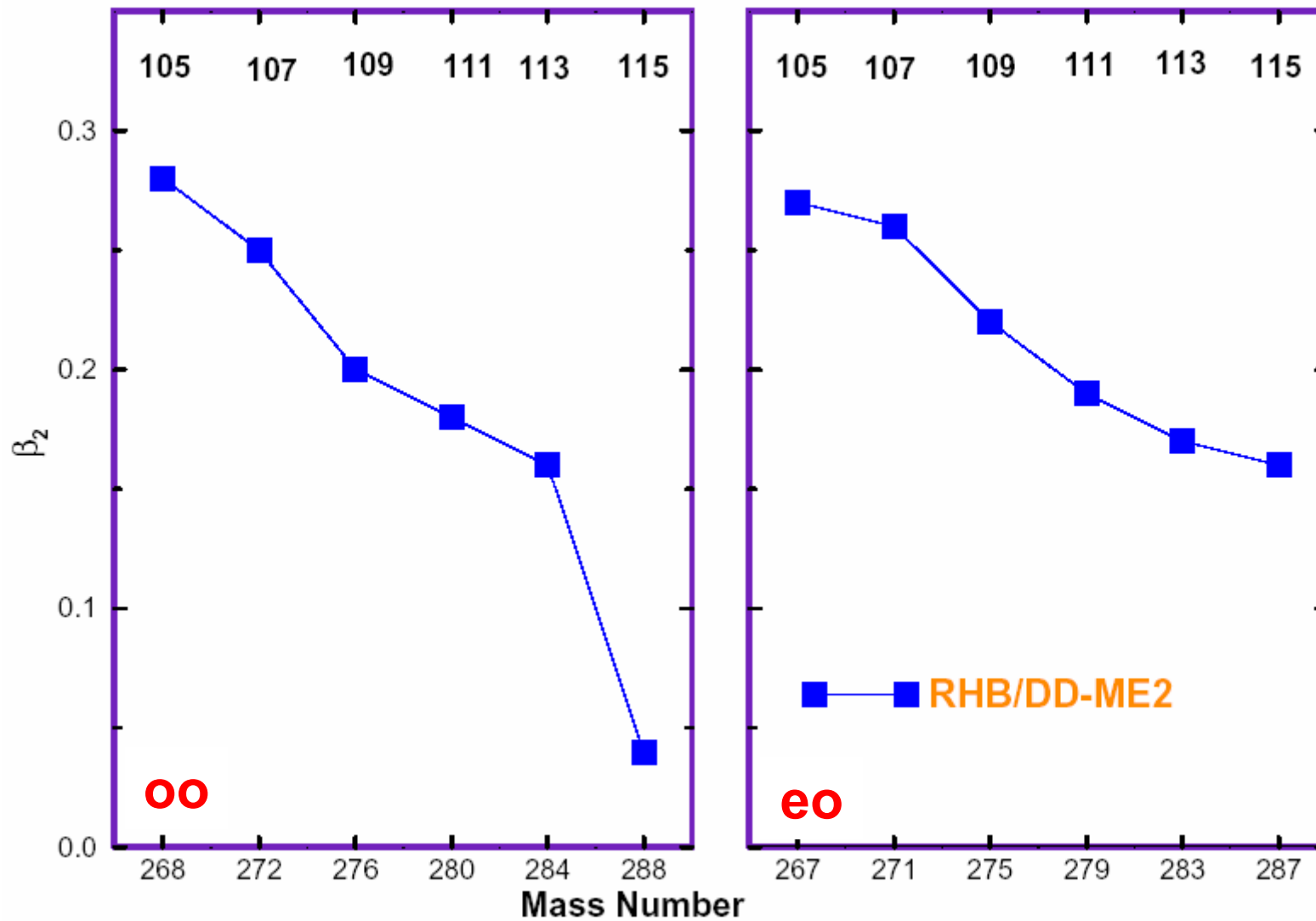


Superheavy Elements: Q_α -values



● Exp: Yu.Ts.Oganessian *et al*, PRC 69, 021601(R) (2004)

Superheavy elements: Quadrupole deformations



RHB/DD-ME2

Time dependent mean field theory:

$$\delta \int dt \left\{ \langle \Phi(t) | i\partial_t | \Phi(t) \rangle - E[\hat{\rho}(t)] \right\} = 0$$



$$i\partial_t \hat{\rho} = [\hat{h}(\hat{\rho}) + \hat{f}, \hat{\rho}]$$

$$i\partial_t \psi_i(t) = \left(\vec{\alpha} \left(\frac{1}{i} \vec{\nabla} - \vec{V} \right) + V + \beta(m - S) \right) \psi_i(t)$$

No-sea approxim. !

$$[-\Delta + m_\sigma^2] \sigma(t) = -g_\sigma \rho_s(t)$$

$$\rho_s = \sum_{i=1}^A \bar{\psi}_i \psi_i$$

$$[-\Delta + m_\omega^2] \omega_0(t) = g_\omega \rho_B(t)$$

$$\rho_B = \sum_{i=1}^A \psi_i^+ \psi_i$$

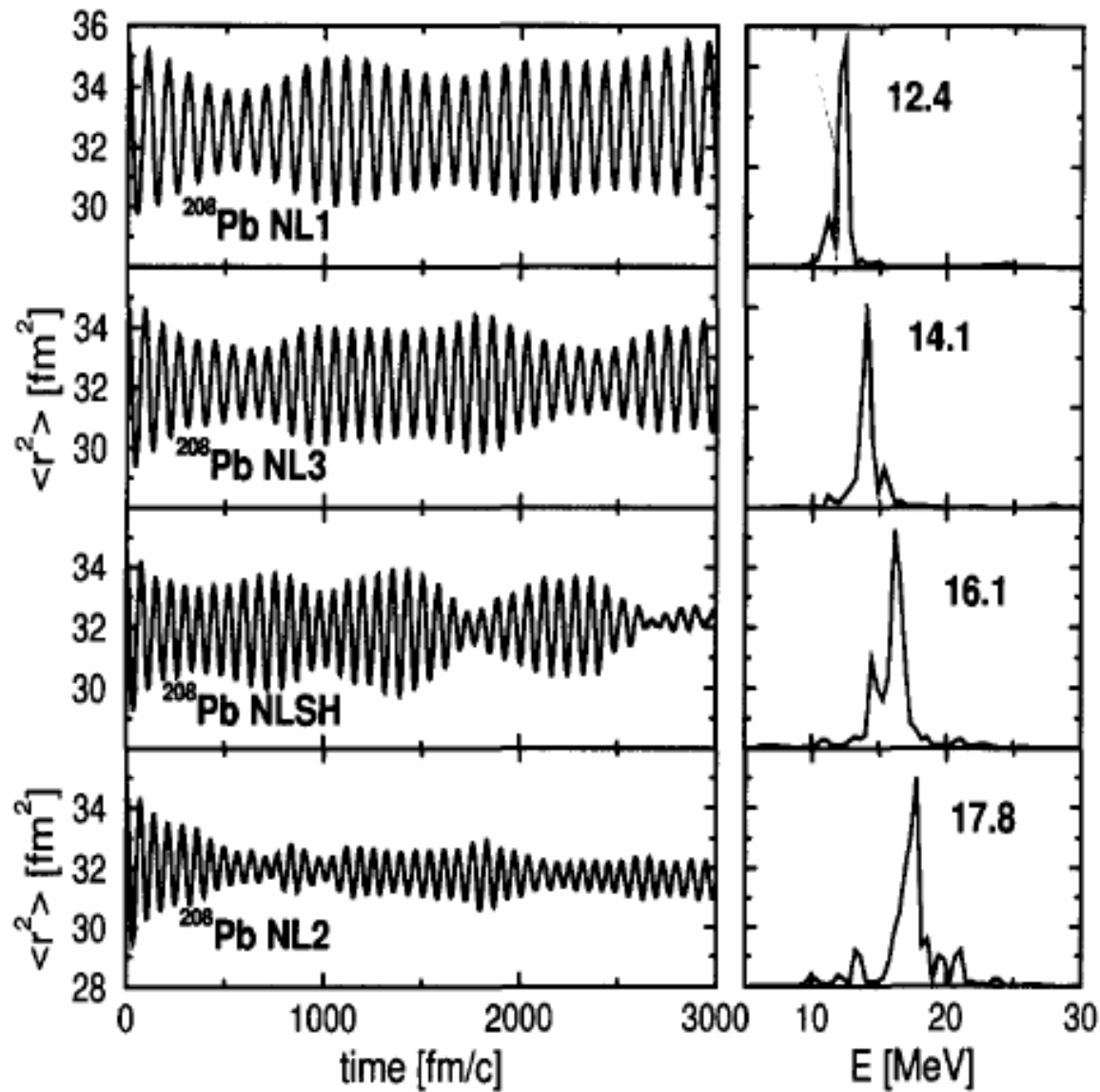
$$[-\Delta + m_\omega^2] \vec{\omega}(t) = g_\omega \vec{j}_B(t)$$

$$\vec{j}_B = \sum_{i=1}^A \bar{\psi}_i \vec{\alpha} \psi_i$$

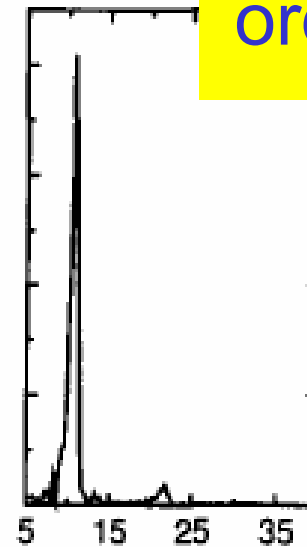
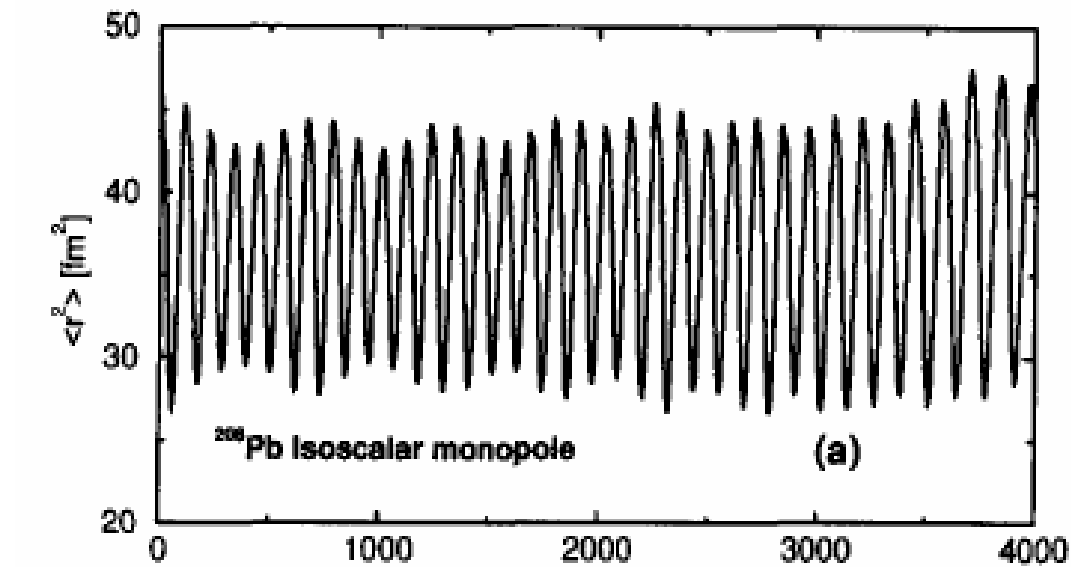
and similar equations for the ρ - and A -field

$$\langle \Phi(t) | r^2 | \Phi(t) \rangle$$

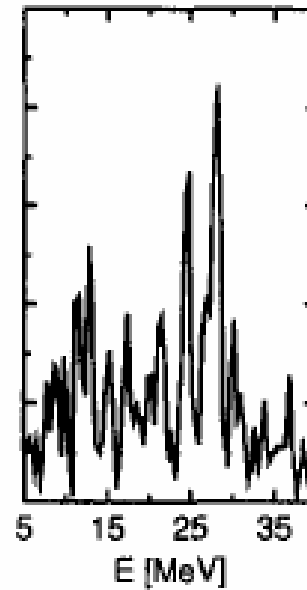
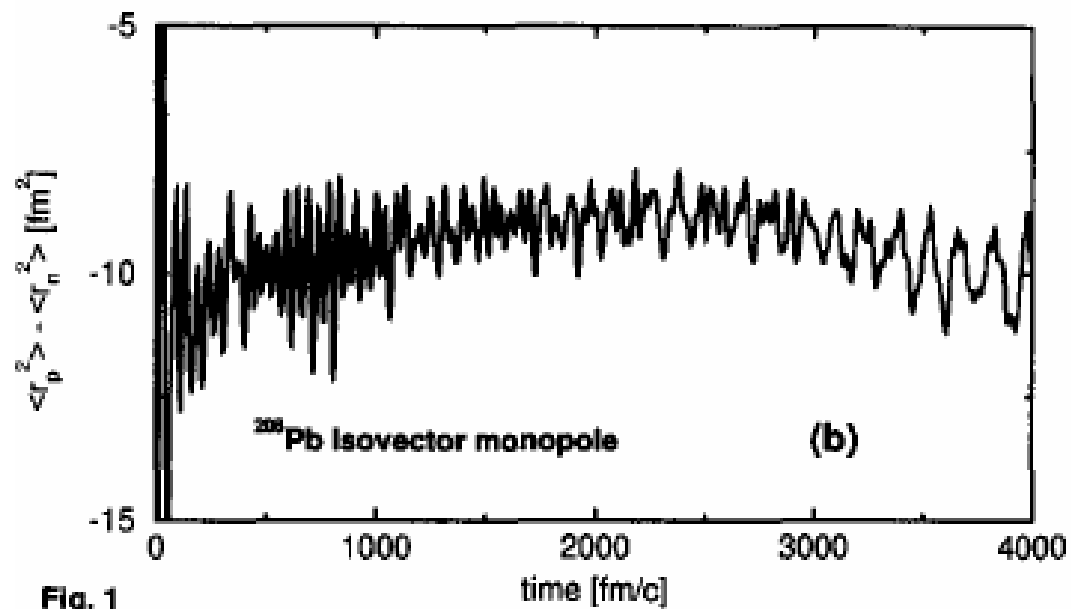
breathing mode: ^{208}Pb



order and chaos



GMR: T=0



GMR: T=1

Fig. 1

Relativistic RPA for excited states

Small amplitude limit:

$$\hat{\rho}(t) = \hat{\rho}^{(0)} + \delta\hat{\rho}(t)$$

ground-state density

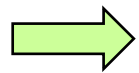
$$\begin{pmatrix} A & B \\ -B^* & -A^* \end{pmatrix} \begin{pmatrix} X \\ Y \end{pmatrix} = \hbar\omega \begin{pmatrix} X \\ Y \end{pmatrix}$$

$\delta\rho_{ph}, \delta\rho_{\alpha h}$

$\delta\rho_{hp}, \delta\rho_{h\alpha}$

RRPA matrices:

$$A_{minj} = (\epsilon_n - \epsilon_i)\delta_{mn}\delta_{ij} + \frac{\partial h_{mi}}{\partial \rho_{nj}}, \quad B_{minj} = \frac{\partial h_{mi}}{\partial \rho_{jn}}$$



the same effective interaction determines the Dirac-Hartree single-particle spectrum and the residual interaction

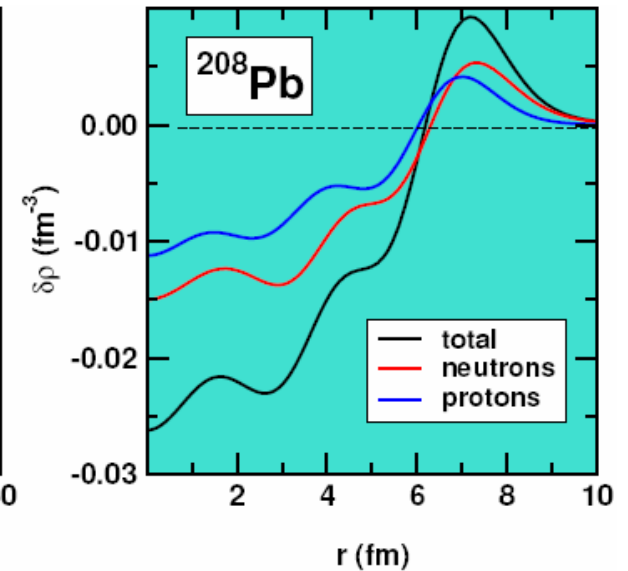
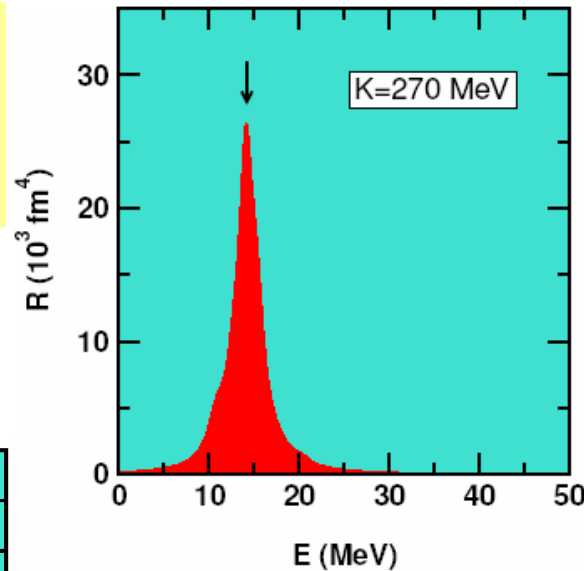
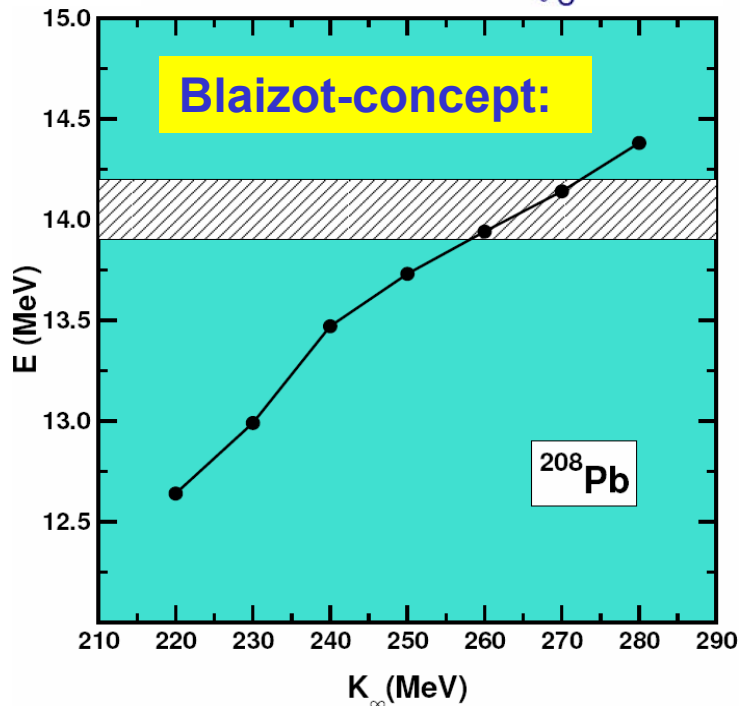
Interaction:

$$\hat{V} = \frac{\delta^2 E}{\delta \hat{\rho} \delta \hat{\rho}}$$

Isoscalar Giant Monopole Resonance: IS-GMR

The ISGMR represents the essential source of experimental information on the nuclear incompressibility

$$K_0 = p_f^2 \left. \frac{d^2 E/A}{dp_f^2} \right|_{p_{f0}}$$



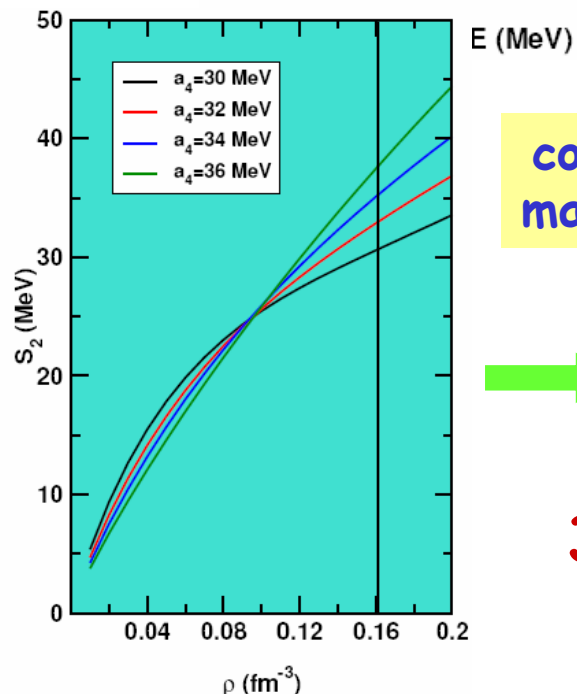
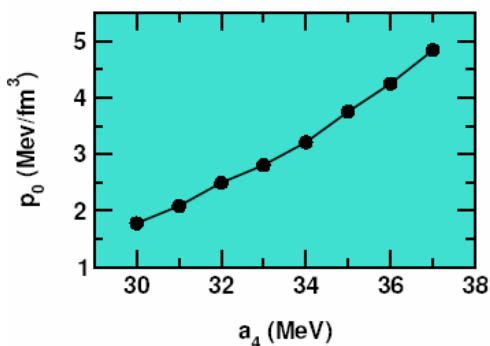
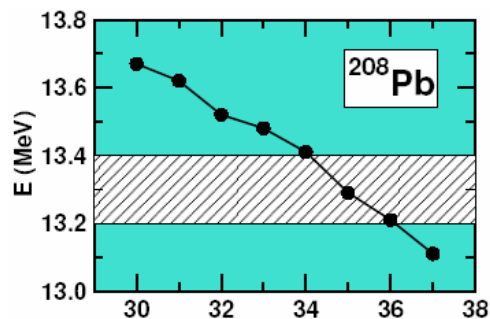
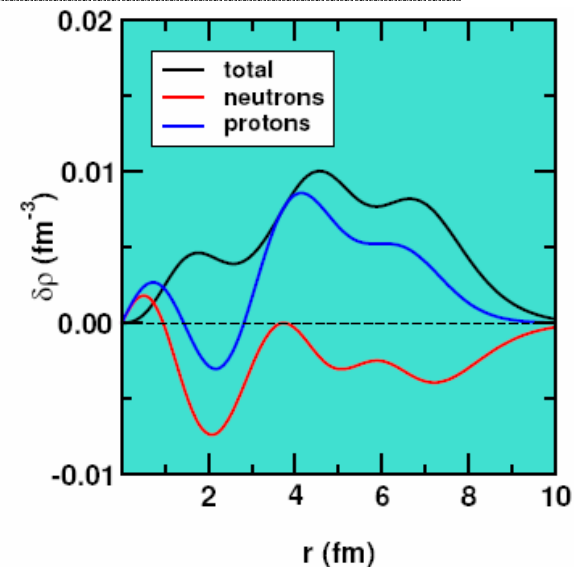
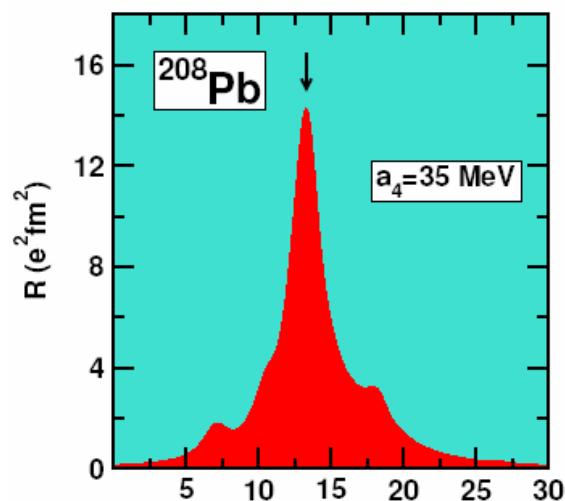
constraining the nuclear matter compressibility

RMF models reproduce the experimental data only if

$$250 \text{ MeV} \leq K_0 \leq 270 \text{ MeV}$$

Isovector Giant Dipole Resonance: IV-GDR

the IV-GDR represents one of the sources of experimental informations on the nuclear matter symmetry energy

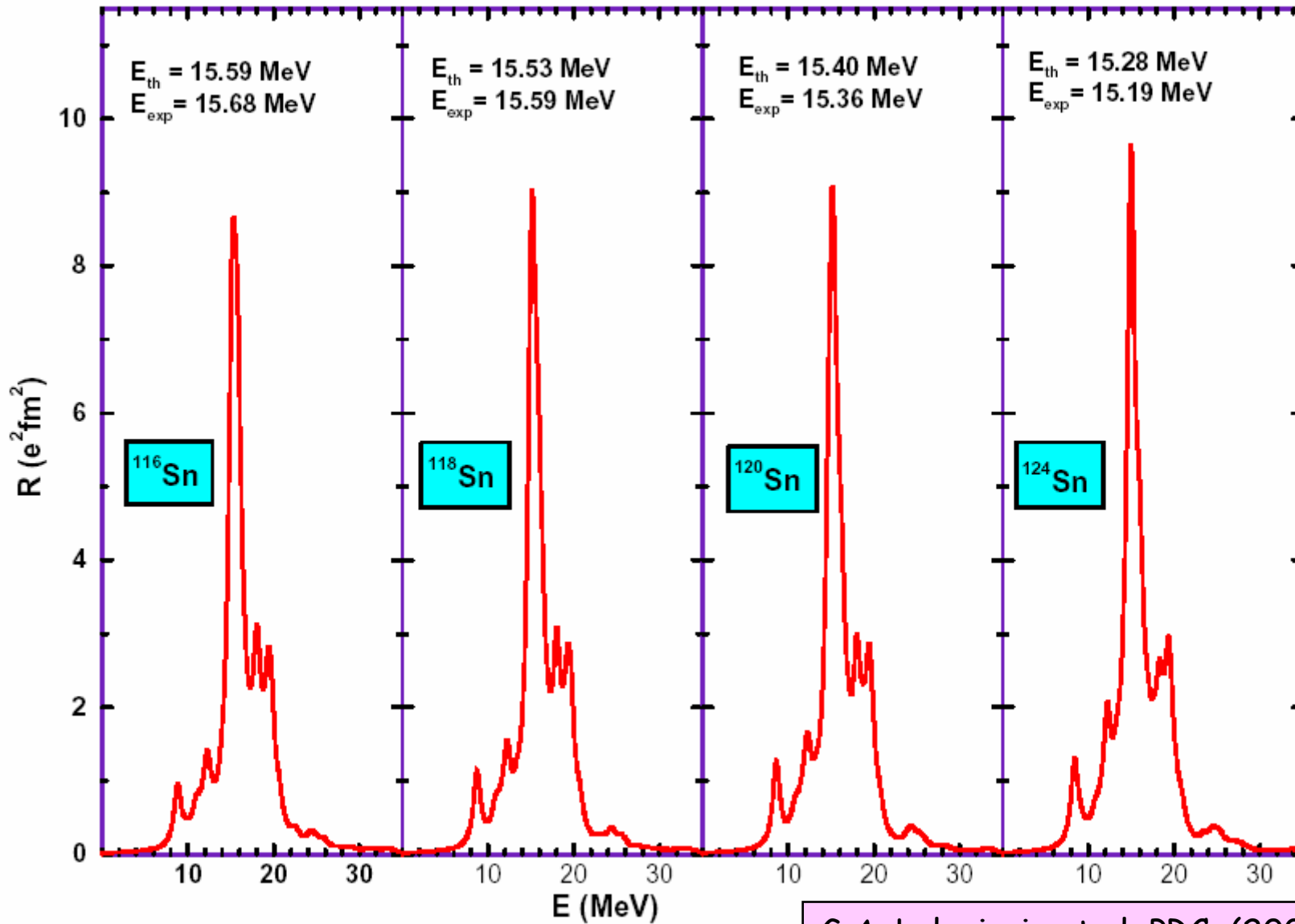


constraining the nuclear matter symmetry energy

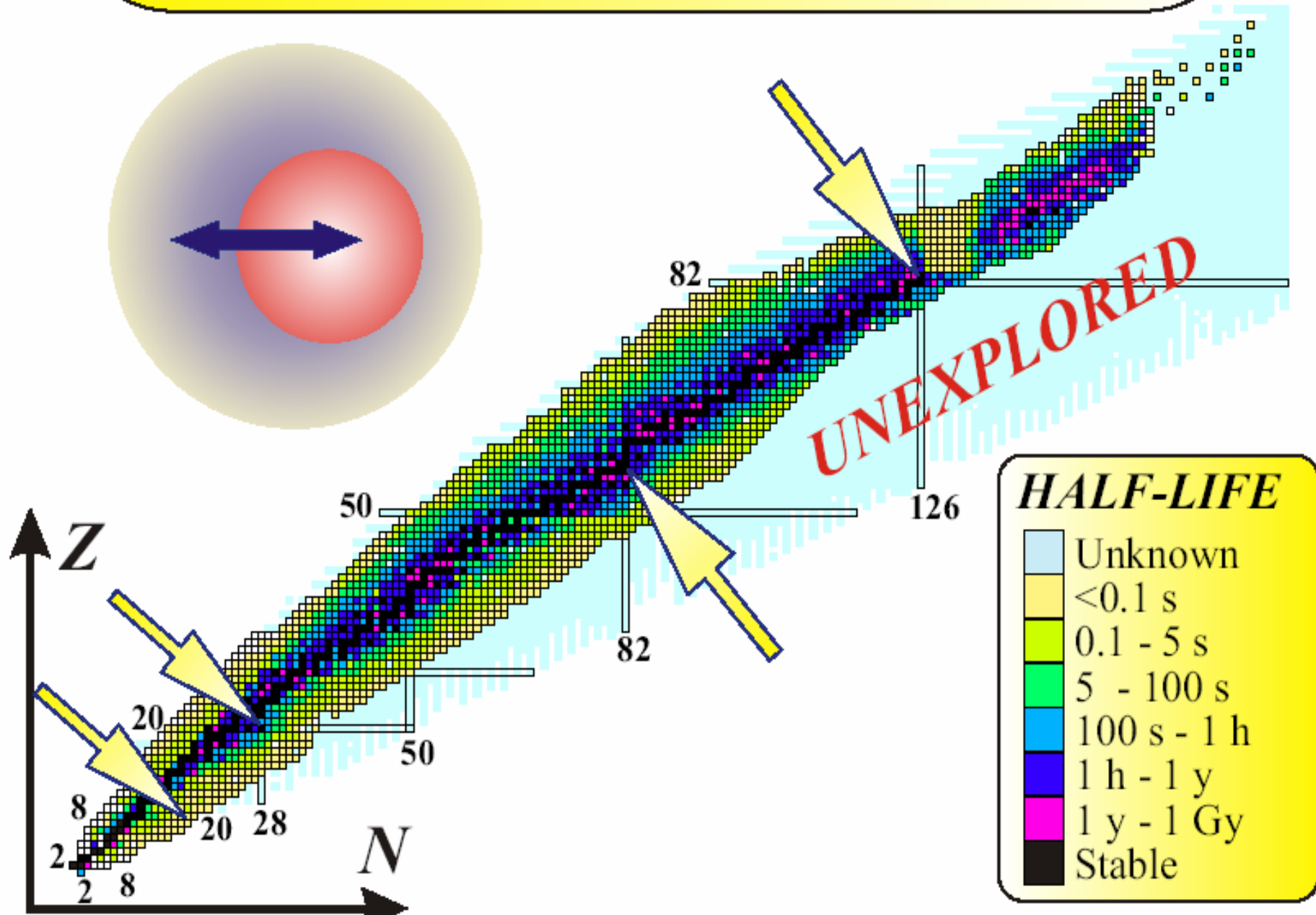
the position of IV-GDR is reproduced if

$$32 \text{ MeV} \leq a_4 \leq 36 \text{ MeV}$$

IV-GDR in Sn-isotopes



Experimental indications of the soft dipole mode



Photoneutron Cross Sections for Unstable Neutron-Rich Oxygen Isotopes

A. Leistenschneider, T. Aumann, K. Boretzky, D. Cortina, J. Cub, U. Datta Pramanik, W. Dostal, Th. W. Elze, H. Emling, H. Geissel, A. Grünschoß, M. Hellstr, R. Holzmann, S. Ilievski, N. Iwasa, M. Kaspar, A. Kleinböhl, J. V. Kratz, R. Kulesa, Y. Leifels, E. Lubkiewicz, G. Münzenberg, P. Reiter, M. Rejmund, C. Scheidenberger, C. Schlegel, H. Simon, J. Stroth, K. Stümmerer, E. Wajda, W. Walus, and S. Wan

Institut für Kernphysik, Johann Wolfgang Goethe-Universität, D-60486 Frankfurt, Germany
Gesellschaft für Schwerionenforschung (GSI), D-64291 Darmstadt, Germany
Institut für Kernchemie, Johannes Gutenberg-Universität, D-55099 Mainz, Germany
Institut für Kernphysik, Technische Universität, D-64289 Darmstadt, Germany
Instytut Fizyki, Uniwersytet Jagielloński, PL-30-059 Kraków, Poland
Sektion Physik, Ludwig-Maximilians-Universität, D-85748 Garching, Germany
 (Received 19 December 2000)

The dipole response of stable and unstable neutron-rich oxygen nuclei of masses $A=17$ to $A=22$ has been investigated experimentally utilizing **electromagnetic excitation in heavy-ion collisions at beam energies about 600 MeV/nucleon**. A kinematically complete measurement of the neutron decay channel in inelastic scattering of the secondary beam projectiles from a Pb target was performed. Differential electromagnetic excitation cross sections $d\sigma/dE$ were derived up to 30 MeV excitation energy. **In contrast to stable nuclei, the deduced dipole strength distribution appears to be strongly fragmented and systematically exhibits a considerable fraction of low-lying strength.**

DOI: 10.1103/PhysRevLett.86.2560

The study of the response of a nucleus to a clear or electromagnetic field is a central topic in nuclear physics. The properties of the nuclear dipole response at excitation energies above the par- tial dipole resonance of stable nuclei is dominated by the response of various multipolarities, with the giant resonance strength being the most prominent. For stable nuclei, the dipole strength distribution is concentrated in the giant resonance region, which is located at excitation energies of about 10–20 MeV. For neutron-rich nuclei, more pronounced effects, in particular a fragmentation of the dipole strength towards lower excitation energies, have been observed in the giant resonance region. The dipole strength depends strongly on the effective dipole response of exotic nuclei can be investigated on the isospin dependence of the nucleon-nucleon interaction [7].

Systematic experimental information on the dipole response of exotic nuclei, however, is scarce. For some light halo nuclei, low dipole strength has been observed in electromagnetic excitation experiments [8–11]. For the one-neutron halo nucleus ^{11}Li [11], the observed dipole strength at low excitation energies was interpreted as a threshold effect, involving the neutron being captured into the continuum. For ^{11}Li and ^6He , a coherent dipole resonance of neutrons against the core was observed. The appearance of a collective dipole resonance was also predicted for heavy nuclei [19,20], located at excitation energies of about 10 MeV. This dipole resonance (GDR) [19],

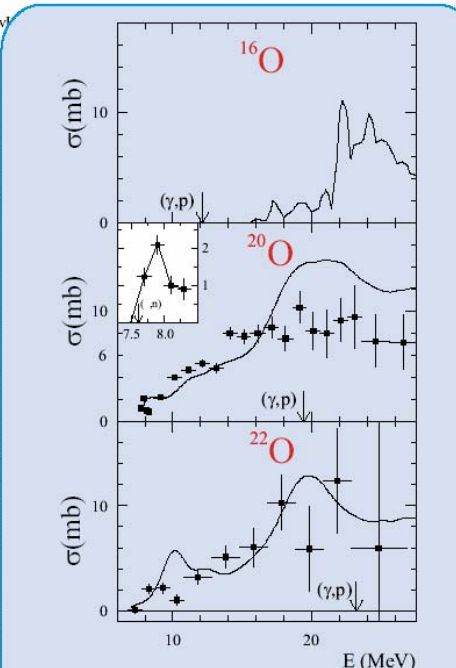


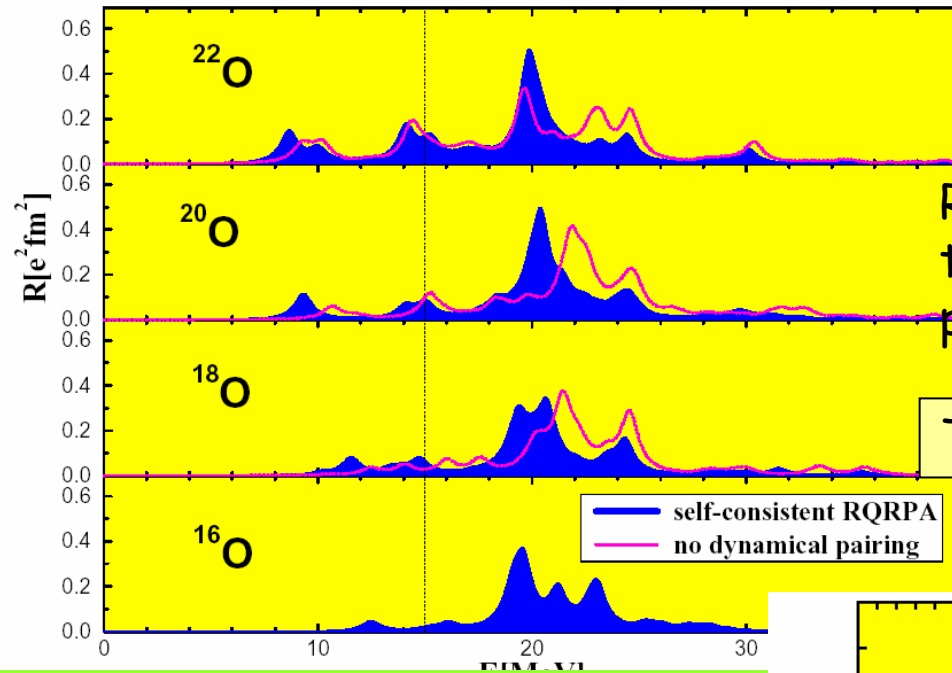
FIG. 2. Photoneutron cross sections σ for ^{16}O (upper panel) and for the unstable isotopes ^{20}O (lower panels) as extracted from the measured electromagnetic excitation cross section (symbols). The inset displays the cross section near the neutron threshold on an expanded energy scale. The thresholds for decay channels involving protons (which were not observed in the present experiment) are indicated by arrows.

DOI: 10.1103/PhysRevLett.86.2560

may arise from the fact that neutrons vibrate against the core, passing that a systematic fragmentation of the dipole strength in neutron-rich nuclei is observed. From physical aspects, e.g., calculations in the ^{16}O nucleus in the (γ, n) -process of the giant resonance [21]. For neutron-rich nuclei, the dipole strength is fragmented and lower lying resonances and lower lying strength have been investigated systematically. For all neutron-rich oxygen isotopes, one may expect a dipole strength to be concentrated in the giant resonance region. For ^{16}O , the dipole strength is concentrated in the giant resonance region, and about 4 MeV for the ^{16}O nucleus. Thus the dipole strength might be good candidates for

investigation. We use the electromagnetic excitation cross section for high targets. Similar to stable nuclei, it is mostly sensitive to electric dipole (E1) contributions. For neutron-rich nuclei, the weighted sum rule for E1 contributions is arbitrarily at an excitation energy of about 10 MeV. For electromagnetic excitation cross sections, respectively (calculated for a Pb target). It was demonstrated that the dipole strength is fragmented and lower lying strength is observed. This dipole strength is fragmented and lower lying strength is observed. This dipole strength is fragmented and lower lying strength is observed.

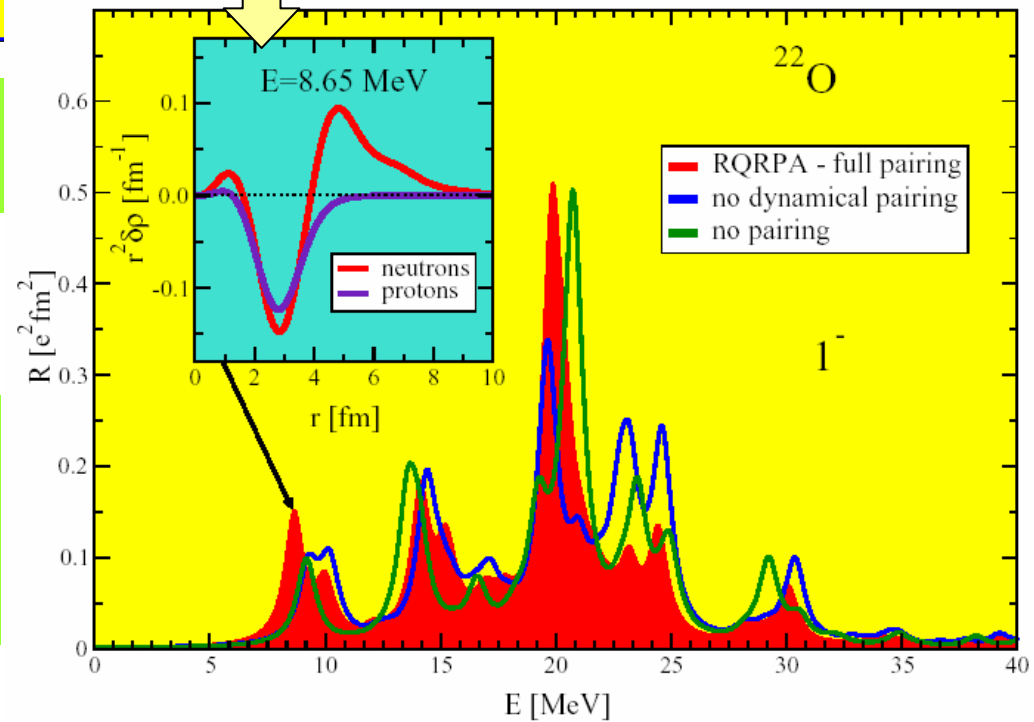
Resolution of IV dipole strength in Oxygen isotopes

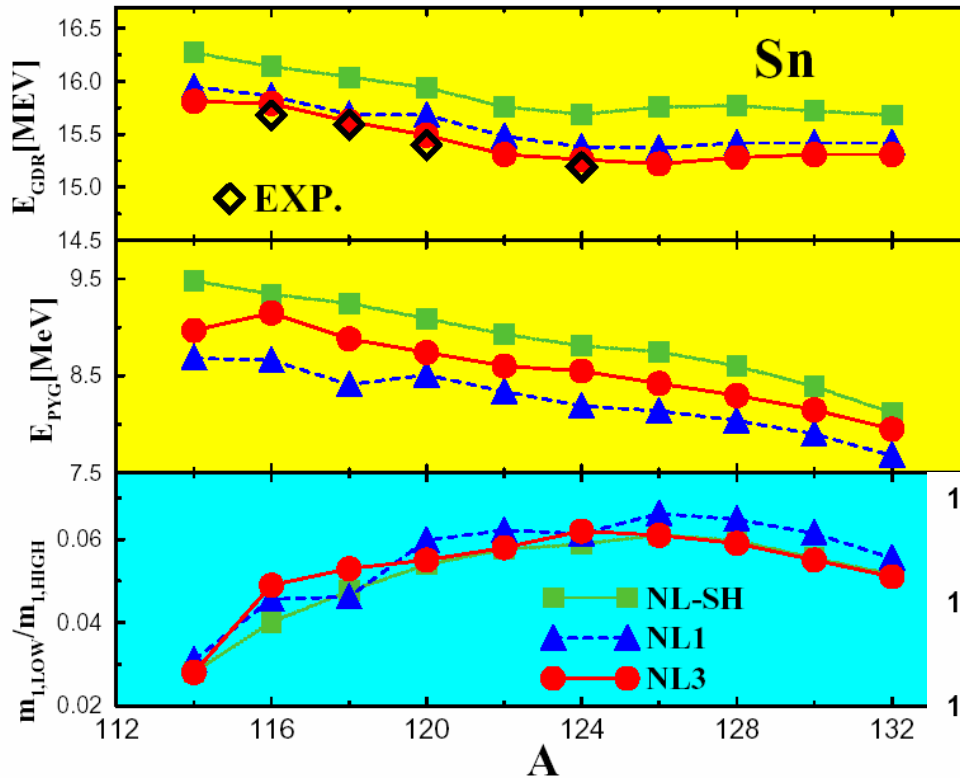


RHB + RQRPA calculations with the NL3 relativistic mean-field plus D1S Gogny pairing interaction.

What is the structure of low-lying strength below 15 MeV?

Effect of pairing correlations on the dipole strength distribution





Mass dependence of GDR and Pygmy dipole states in Sn isotopes. Evolution of the low-lying strength.

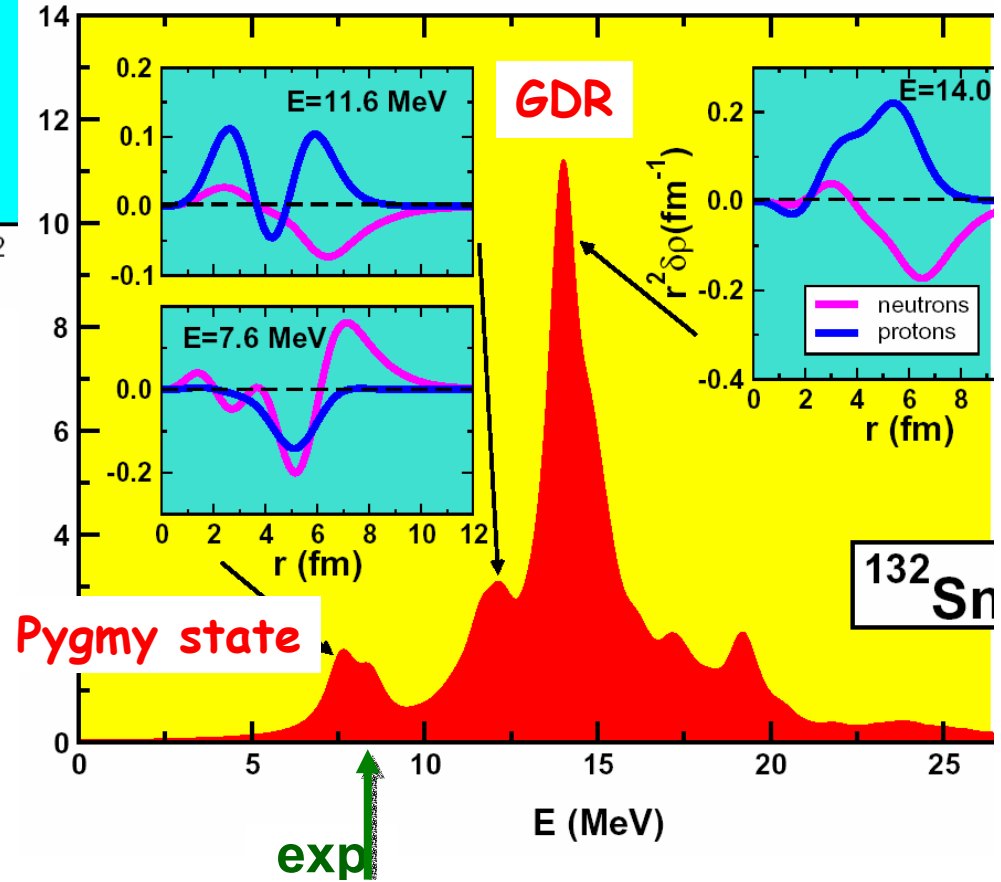
Isvector dipole strength in ^{132}Sn .

Nucl. Phys. A692, 496 (2001)

Distribution of the neutron particle-hole configurations for the peak at 7.6 MeV (1.4% of the EWSR)

^{132}Sn at 7.6 MeV

| | |
|-------|-----------------------------------|
| 28.2% | $2d_{3/2} \rightarrow 2f_{5/2}$ |
| 21.9% | $2d_{5/2} \rightarrow 2f_{7/2}$ |
| 19.7% | $2d_{3/2} \rightarrow 3p_{1/2}$ |
| 10.5% | $1h_{11/2} \rightarrow 1i_{13/2}$ |
| 3.5% | $2d_{5/2} \rightarrow 3p_{3/2}$ |
| 1.9% | $1g_{7/2} \rightarrow 2f_{5/2}$ |
| 1.5% | $1g_{7/2} \rightarrow 1h_{9/2}$ |
| 0.6% | $1g_{7/2} \rightarrow 2f_{7/2}$ |
| 0.6% | $2d_{3/2} \rightarrow 3p_{3/2}$ |

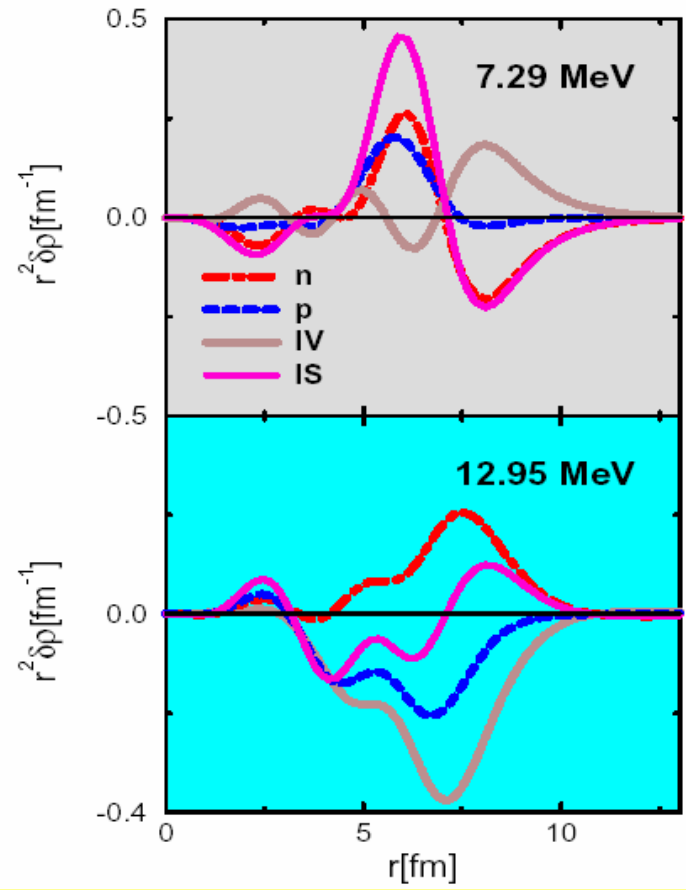
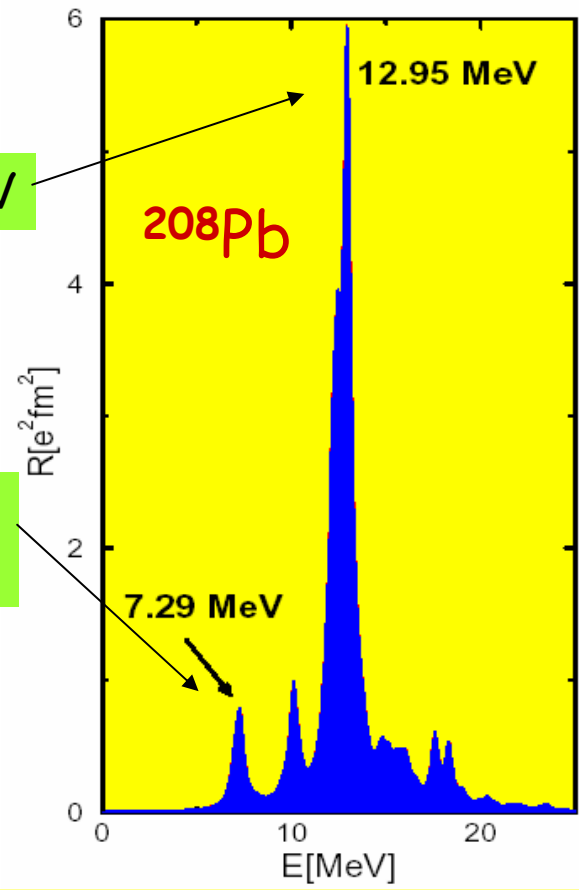


^{132}Sn

IV Dipole Strength for ^{208}Pb and transition densities for the peaks at 7.29 MeV and 12.95 MeV
 Phys. Rev. C63, 047301 (2001)

Exp GDR at 13.3 MeV

Exp PYGMY centroid at 7.37 MeV



In heavier nuclei low-lying dipole states appear that are characterized by a more distributed structure of the RQRPA amplitude.

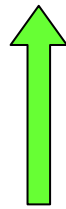
Among several single-particle transitions, a single collective dipole state is found below 10 MeV and its amplitude represents a coherent superposition of many neutron particle-hole configurations.

Spin-Isospin Resonances: IAR - GTR

Z, N

$Z+1, N-1$

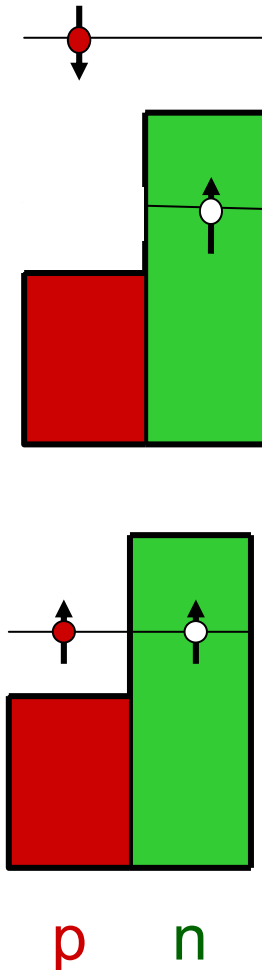
$$|\text{GTR}\rangle = S_- T_+ |Z, N\rangle$$



spin flip σ

$$|Z, N\rangle \longrightarrow |\text{IAR}\rangle = T_+ |Z, N\rangle$$

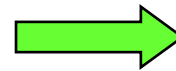
isospin flip τ



$$E_{\text{GTR}} - E_{\text{IAR}} \sim \Delta(l \cdot s) \sim \frac{dV}{dr} \sim \text{neutron skin} = r_n - r_p$$

Spin-Isospin Resonances: IAS and GTR

charge-exchange excitations



proton-neutron
relativistic QRPA

π and ρ -meson exchange
generate the spin-isospin
dependent interaction terms

$$\mathcal{L}_{\pi N} = -\frac{f_{\pi}}{m_{\pi}} \bar{\psi} \gamma_5 \gamma_{\mu} \partial^{\mu} \vec{\pi} \vec{\tau} \psi$$

the Landau-Migdal zero-range
force in the spin-isospin channel

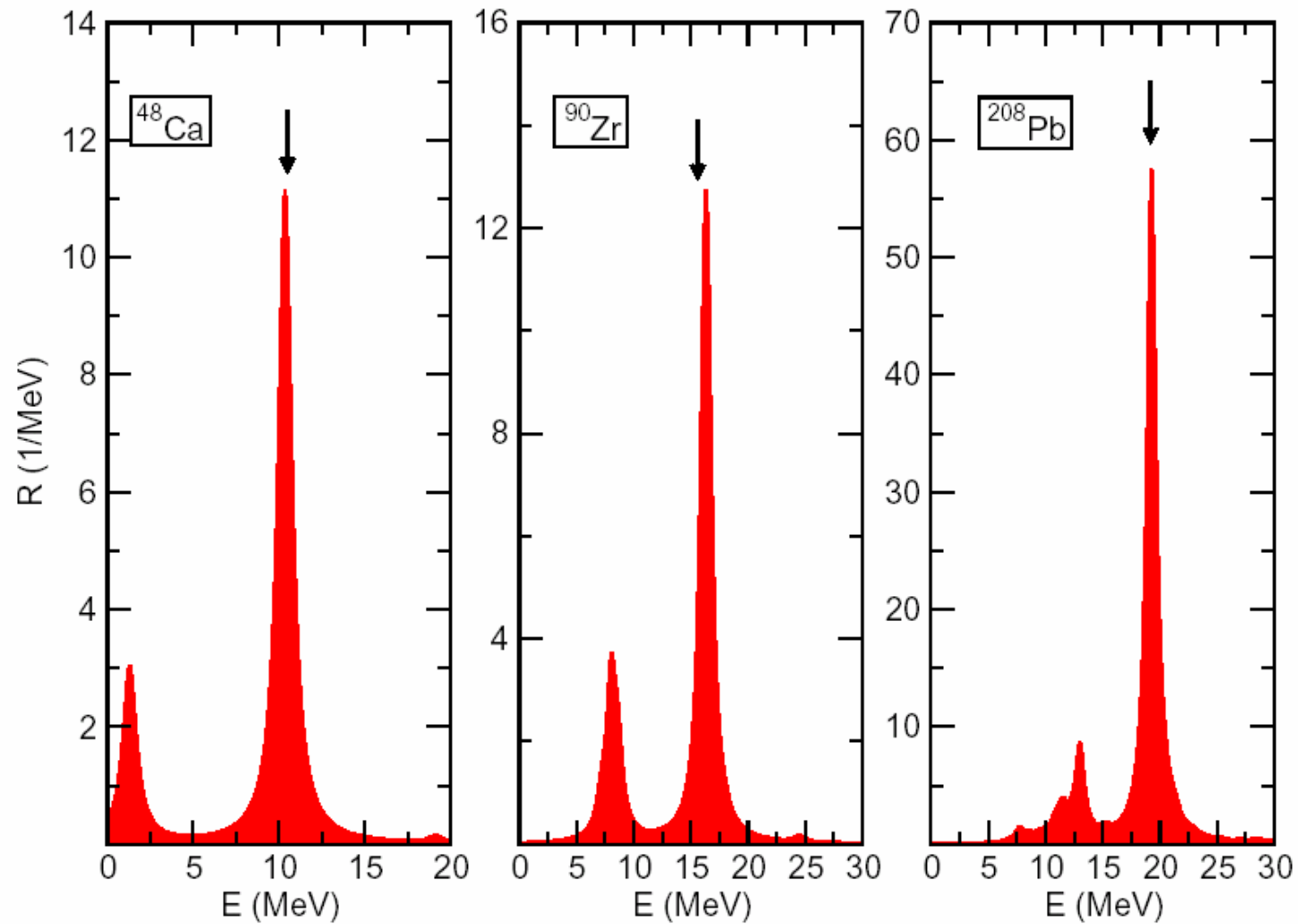
$$V(1, 2) = g'_0 \left(\frac{f_{\pi}}{m_{\pi}} \right)^2 \vec{\tau}_1 \cdot \vec{\tau}_2 \Sigma_1 \cdot \Sigma_2 \delta(r_1 - r_2) \quad (g'_0=0.55)$$

GAMOW-TELLER RESONANCE: $S=1 \quad T=1 \quad J^{\pi} = 1^{+}$

ISOBARIC ANALOG STATE: $S=0 \quad T=1 \quad J^{\pi} = 0^{+}$

GT-Resonances

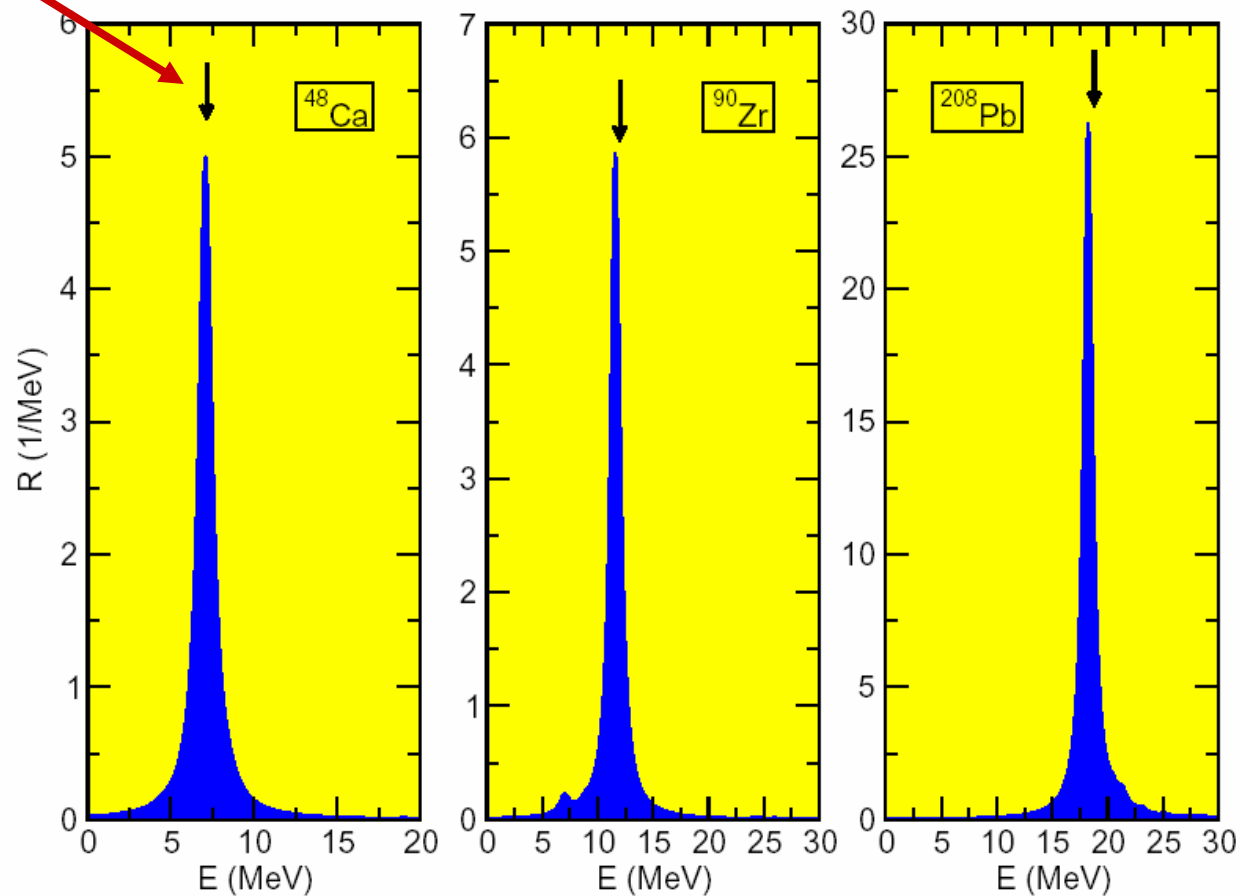
N. Paar, T. Niksic, D. Vretenar, P. Ring, PR C69, 054303 (2004)



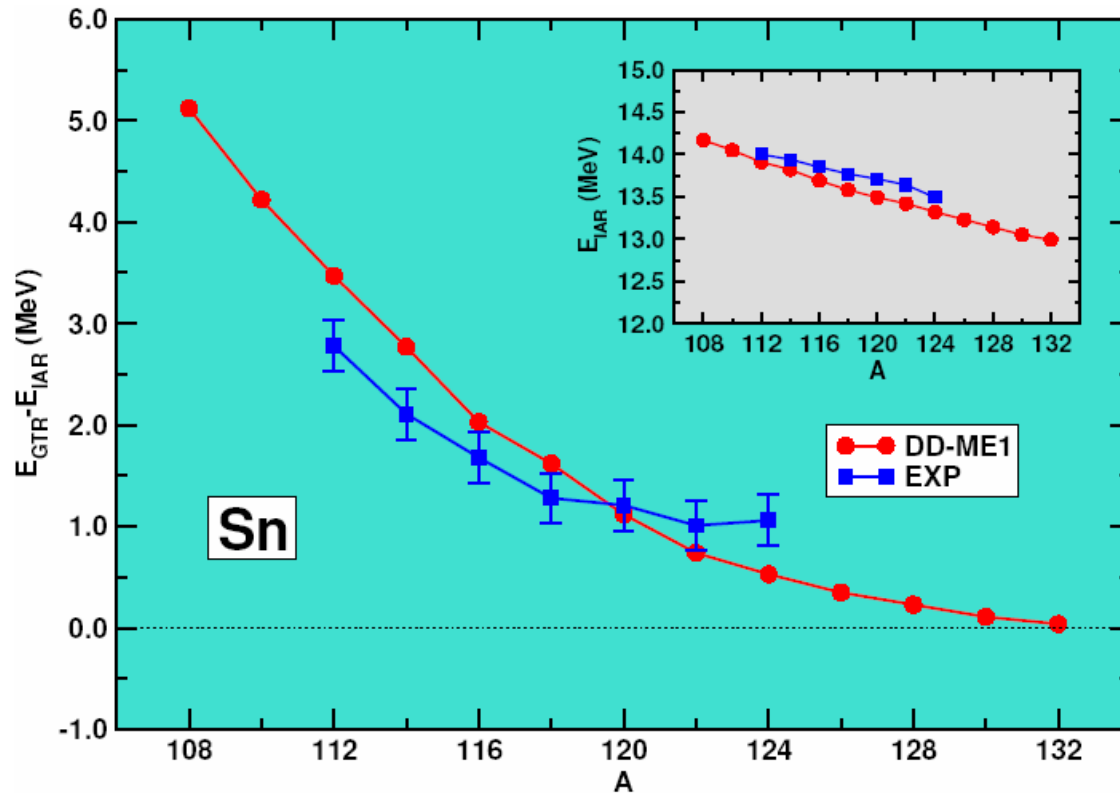
Isobaric Analog Resonance: IAR

N. Paar, T. Niksic, D. Vretenar, P. Ring, PR C69, 054303 (2004)

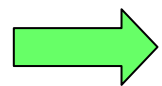
experiment



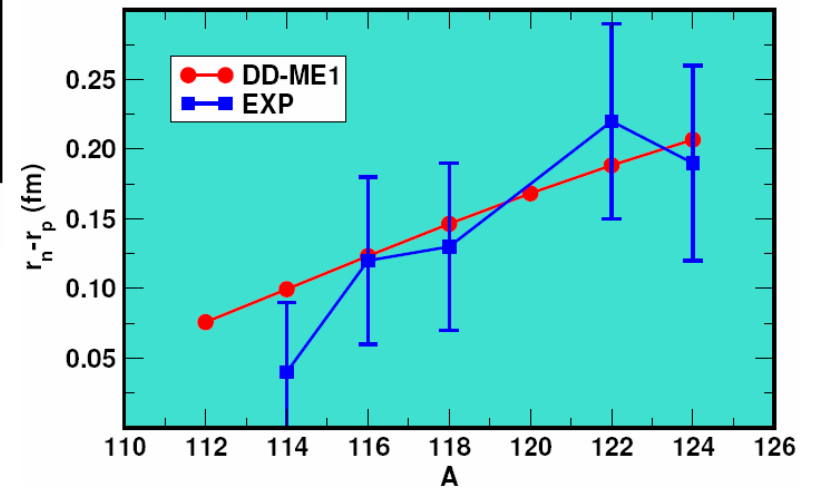
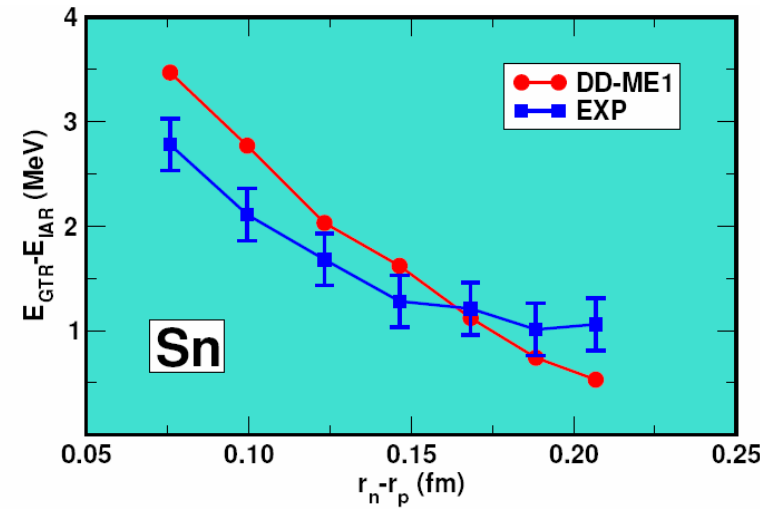
Neutron skin and IAR/GRT



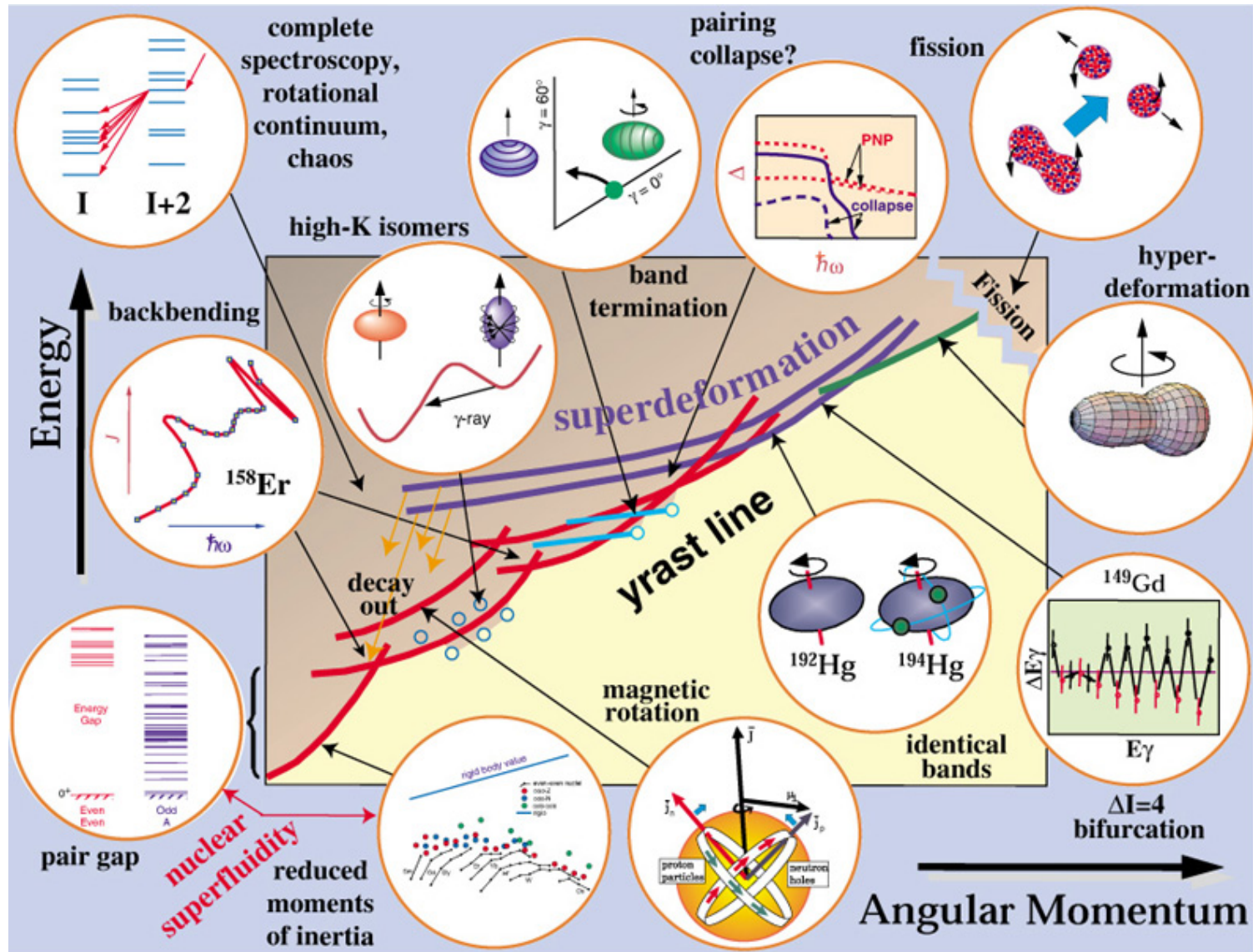
The isotopic dependence of the energy spacings between the GTR and IAS



direct information on the evolution of the neutron skin along the Sn isotopic chain



nuclei at high large angular velocities:



Physical observables in rotating nuclei:

$$E_\gamma(I) = E(I + 2) - E(I)$$

Angular velocity Ω :

$$\Omega = \frac{dE}{dJ} = \frac{\Delta E}{\Delta I} = \frac{E_\gamma(I)}{2}$$

Kinematic moment of inertia $J^{(1)}$

$$J^{(1)}(\Omega) = \frac{J}{\Omega} = \frac{2I - 1}{E_\gamma}$$

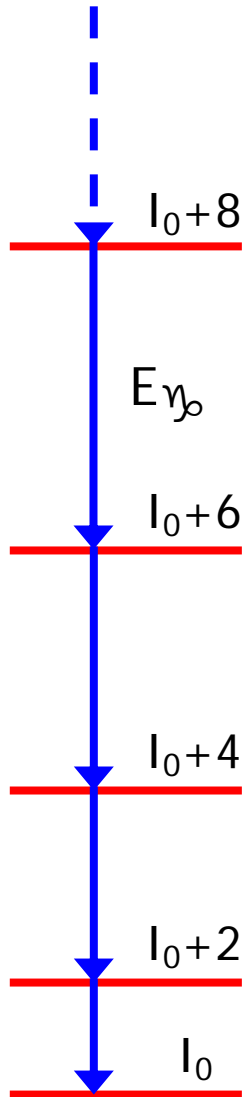
Dynamic moment of inertia $J^{(2)}$

$$J^{(2)}(\Omega) = \frac{dJ}{d\Omega} = \frac{4}{E_\gamma(I) - E_\gamma(I - 2)}$$

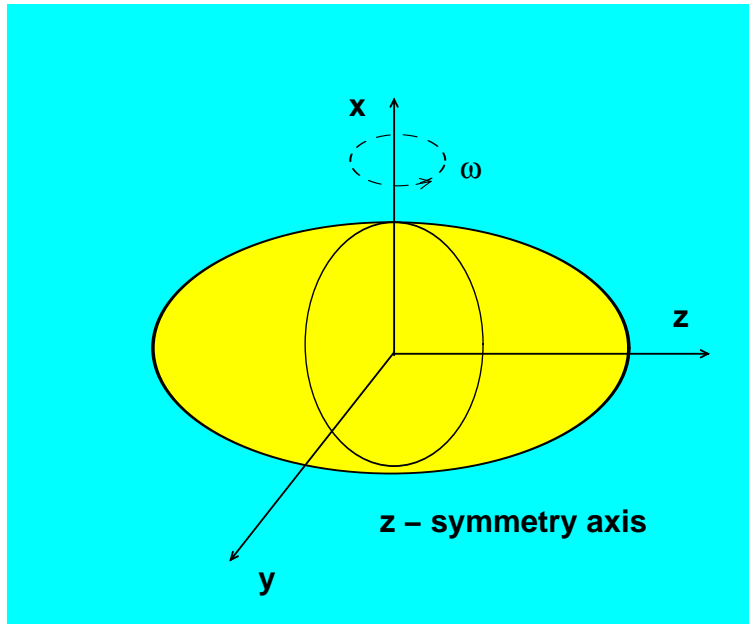
Charge quadrupole moment

Relative quantities: relative (effective) alignment, relative charge quadrupole moments:

1. measure an effect introduced by a particle(s) in single-particle orbital(s)
2. includes direct contribution ($\langle i|O|i \rangle$) and polarization effects on "core"



How to describe rotating nuclei ?



Rigid rotor: rotational excitation energies $E(I)$ obey 'the $I(I+1)$ rule'; I is spin

$$E(I) = \frac{\hbar^2}{2J} I(I+1)$$

J is moment of inertia

- Nuclei do not rotate as rigid bodies
- Quantum mechanics forbids collective rotation around the symmetry axis

Laboratory frame: potential V is time-dependent
 Rotating frame: potential V^* is time-independent

Transformation to rotating frame → CRANKING MODEL

$$\langle \Psi | \hat{J}_x | \Psi \rangle = \sqrt{I(I+1)}$$

$$\langle \Psi | \hat{J}_x | \Psi \rangle = \sum_i \langle i | \hat{j}_x | i \rangle$$

$$\hat{H}' = \hat{H} - \Omega \hat{J}_x$$

The cranked relativistic Hartree+Bogoliubov theory

1. The CRHB equations for the fermions in the rotating frame (one-dimensional cranking approximation)

$$\begin{pmatrix} \hat{h}_D - \lambda_\tau - \Omega \hat{J}_x & \hat{\Delta} \\ -\hat{\Delta}^* & \hat{h}_D + \lambda_\tau + \Omega \hat{J}_x \end{pmatrix} \begin{pmatrix} U_k \\ V_k \end{pmatrix} = E_k \begin{pmatrix} U_k \\ V_k \end{pmatrix}$$

Coriolis term

$$\hat{h}_D = \alpha(-i\vec{\nabla} - \vec{V}(\vec{r})) + V_0(\vec{r}) + \beta(m - S(\vec{r}))$$

Magnetic potential

$$\vec{V}(\vec{r}) = g_\omega \vec{\omega}(\vec{r}) + g_\rho \tau_3 \vec{\rho}(\vec{r}) + e \frac{1-\tau_3}{2} \vec{A}(\vec{r})$$

- space-like components of vector mesons
- behaves in Dirac equation like a magnetic field

Nuclear magnetism

2. Klein-Gordon equations for mesons:

$$\left\{ -\Delta - (\Omega \hat{L}_x)^2 + m_\omega^2 \right\} \omega_0(\vec{r}) = g_\omega \rho_V^{is}(\vec{r})$$

$$\left\{ -\Delta - (\Omega \hat{L}_x)^2 + m_\sigma^2 \right\} \sigma(\vec{r}) = -g_\sigma \rho_S(\vec{r}) - g_2 \sigma^2(\vec{r}) - g_3 \sigma^3(\vec{r})$$

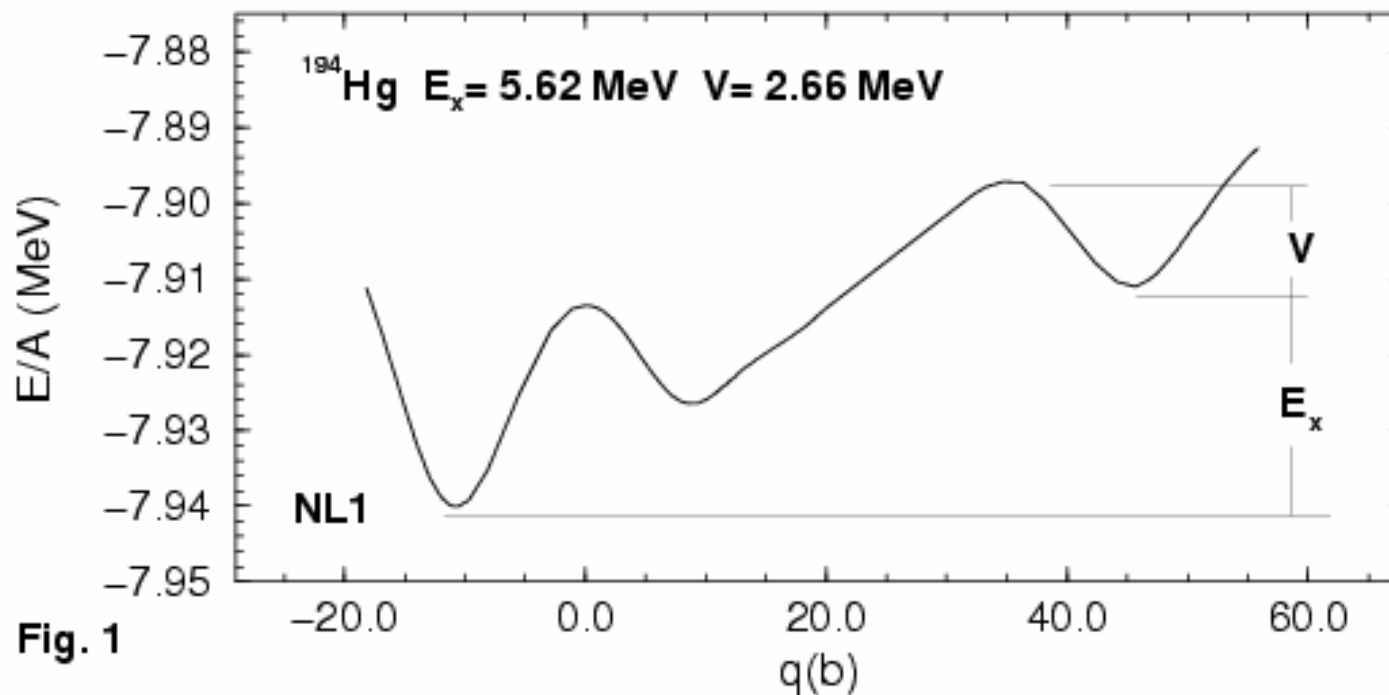
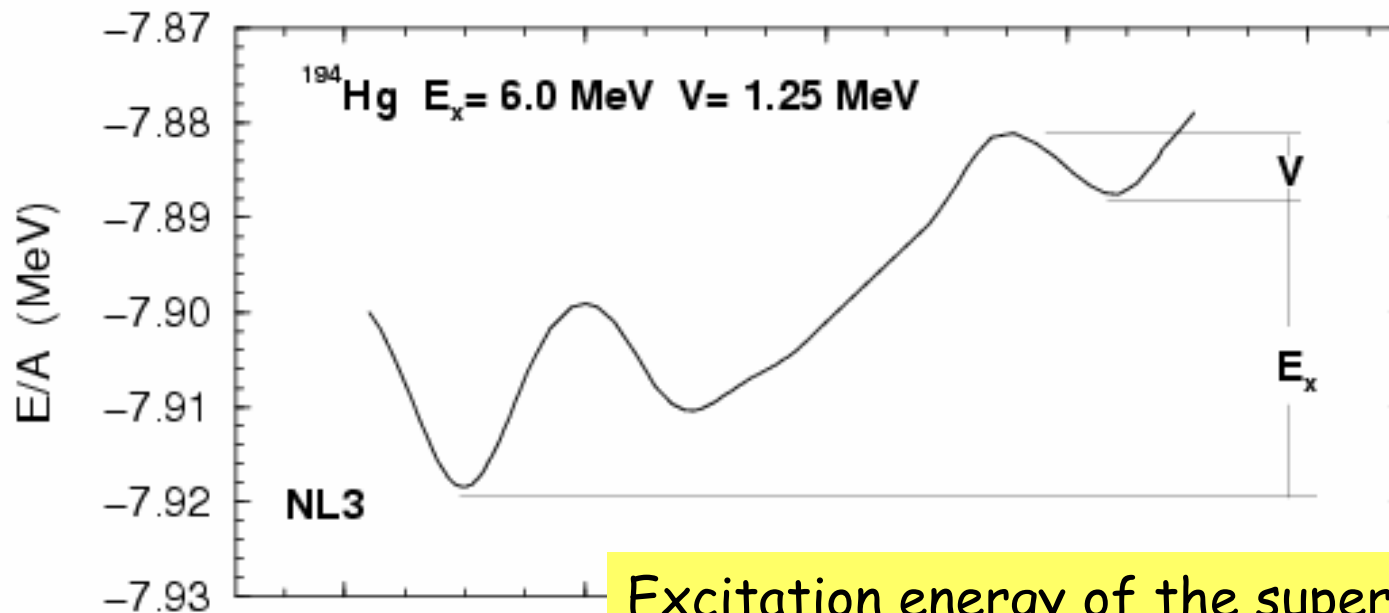
$$\left\{ -\Delta - (\Omega(\hat{L}_x + S_x))^2 + m_\omega^2 \right\} \vec{\omega}(\vec{r}) = g_\omega \vec{j}^{is}(\vec{r})$$

Two sources of time-reversal symmetry breaking:

- Coriolis term
- magnetic potential

"time-odd" mean fields in non-relativistic theory

^{194}Hg



| | |
|---------|--------------|
| Exp: | $E_x = 6.02$ |
| NL3: | $= 6.0$ |
| NL1: | $= 5.6$ |
| Gogny: | $= 6.9$ |
| Skyrme: | $= 5.0$ |
| WS: | $= 4.6$ |

Fig. 1

A.V.Afanasjev, P. Ring, J. König

Phys. Rev. C60 (1999) 051303; Nucl. Phys. A 676 (2000) 196

N=110

N=112

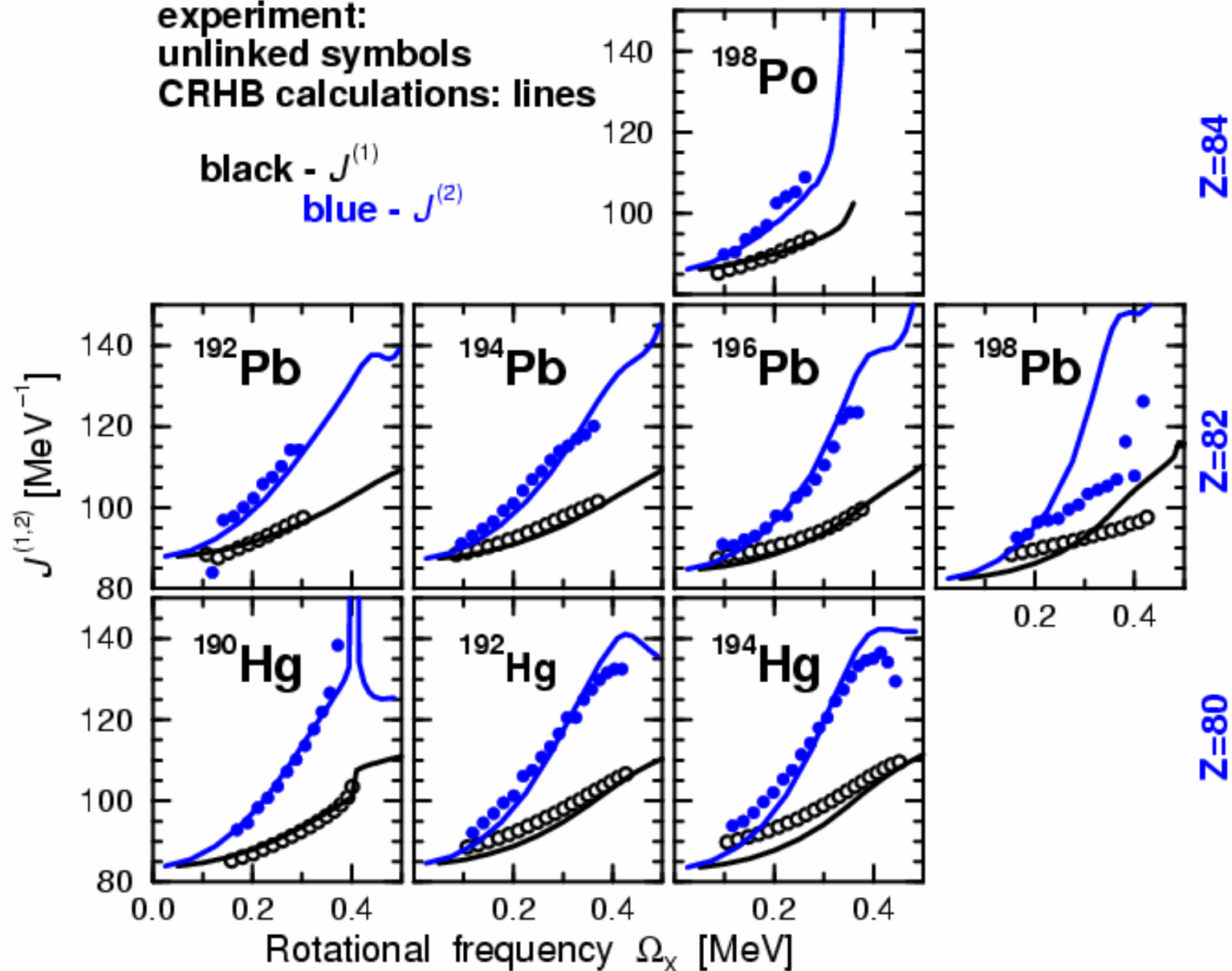
N=114

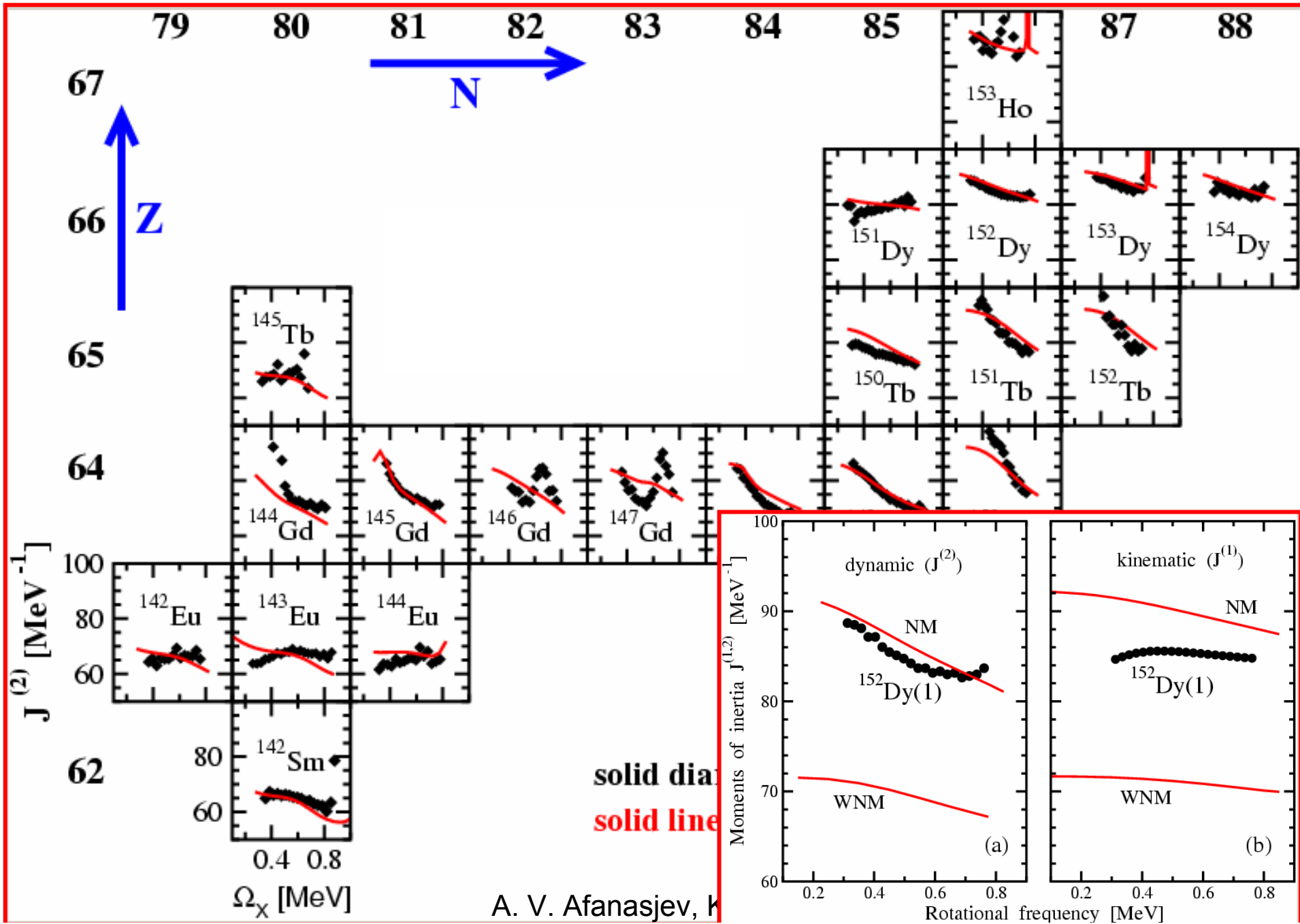
N=116

experiment:
unlinked symbols
CRHB calculations: lines

black - $J^{(1)}$

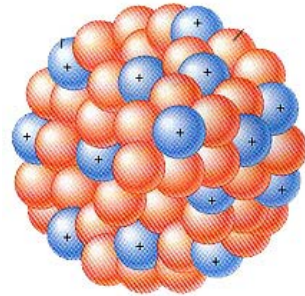
blue - $J^{(2)}$





TOWARD THE UNIVERSAL ENERGY DENSITY FUNCTIONAL

Structure of
heavy
neutron-rich
nuclei



Covariant Density Functional Theory

Next generation **universal energy density functionals** constrained by bulk properties of nuclei, nuclear excitations, nuclear and neutron matter EOS -> microscopic description of.

- ground-state properties of all nuclei
- extended asymmetric nuclear matter
- low-energy vibrations
- rotational spectra
- small-amplitude vibrations
- large-amplitude adiabatic properties

- Applications in astrophysics
- r-process
 - supernova explosions
 - neutrino-matrix-elements

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