Resonance dynamics and reconstruction in hadronic channels



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Helmholtz International Center



Outline



- Quick UrQMD reminder
- Resonance kinematics
 - How deep can we look into heavy ion collisions using resonances? (does high transverse momentum change anything?)
 - Baryons @ low energies
 - a1
- Conclusions

Motivation



- Several physical effects are density driven, e.g.
 - vector meson spectral function broadening
 - chiral phase transition
 - QGP phase transition
 - quarkyonic matter





The tool - UrQMD

 10^{3}

10²

10

103

10²

- Ultra Relativistic Quantum Molecular Dynamics
- Non equilibrium transport model
- All hadrons and resonances up to 2.2 GeV included
- Particle production via string excitation and -fragmentation
- Cross sections are fitted to available experimental data or calculated via detailed balance or the additive quark model
- Does account for canonical suppression

No explicit implementation of in-medium modifications!



Phys.Rev.C69:054907,2004 Phys.Rev.C74:034902,2006



The tool - UrQMD

nucleon	Δ	Λ	Σ	[1]	Ω
N938	Δ_{1232}	Λ_{1116}	Σ_{1192}	Ξ_{1317}	Ω_{1672}
N_{1440}	Δ_{1600}	Λ_{1405}	Σ_{1385}	Ξ_{1530}	
N_{1520}	Δ_{1620}	Λ_{1520}	Σ_{1660}	Ξ_{1690}	
N_{1535}	Δ_{1700}	Λ_{1600}	Σ_{1670}	Ξ_{1820}	
N_{1650}	Δ_{1900}	Λ_{1670}	Σ_{1775}	Ξ_{1950}	
N_{1675}	Δ_{1905}	Λ_{1690}	Σ_{1790}	Ξ_{2025}	
N_{1680}	Δ_{1910}	Λ_{1800}	Σ_{1915}		
N_{1700}	Δ_{1920}	Λ_{1810}	Σ_{1940}		
N_{1710}	Δ_{1930}	Λ_{1820}	Σ_{2030}		
N_{1720}	Δ_{1950}	Λ_{1830}			
N_{1900}		Λ_{1890}			
N_{1990}		Λ_{2100}			
N_{2080}		Λ_{2110}			
N_{2190}					
N_{2200}					
N_{2250}					



The tool - UrQMD

0-+	1	0++	1^{++}
π	ρ	a_0	a_1
K	K^*	K_0^*	K_1^*
η	ω	f_0	f_1
η'	ϕ	f_0^*	$\int f_1'$
1+-	2^{++}	$(1^{})^*$	$(1^{})^{**}$
b_1	a_2	$ ho_{1450}$	$ ho_{1700}$
K_1	K_2^*	K_{1410}^{*}	K_{1680}^*
h_1	f_2	ω_{1420}	ω_{1662}
h_1'	f_2'	ϕ_{1680}	ϕ_{1900}



Dileptonic and hadronic decays





Rescattering

• well known effect, studied in

- statistical hadronization models
- ➡ transport models
- hydrodynamical models





Rescattering

well known effect, studied in ⇒ experiment



Markert et al. [STAR], J.Phys.G35:044029,2008



Reach in density

- Normalized density spectrum
- Most resonances originate from very low density





Reconstruction probability

Probability to reconstruct resonances from a certain density





рт dependence





p_T dependence

- difference in p_T spectrum between observable and all decayed
- percentage of reconstructable resonances produced at ρ >2 ρ 0 increases with p_T





First conclusion

High pT resonances might shed some light on the dense phase of heavy ion collisions!

(but are they really what we want to measure?)





What is the deal about them at low energies?



p meson in C+C @ 2AGeV

At low energies (~2 AGeV) contributions from baryon resonance decays are dominant.

N*₁₅₂₀ contributes via the decay chain: N*₁₅₂₀ \rightarrow N + ρ $\rho \rightarrow \pi^{+}\pi^{-}$ or $\rho \rightarrow e^{+}e^{-}$ to the low mass part of the ρ meson mass spectrum.



SV, M. Bleicher, Phys.Rev.C74:014902,2006



p meson mass distribution

At higher energies the contribution from baryonic resonance decays become less important.





p meson at higher energies

Due to the dependence on the baryon density the mass of the ρ meson is rapidity dependent.

The ρ meson mass drops towards higher rapidity.





Second conclusion

Controlling baryon kinematics is important

(otherwise some spectra seem more interesting than they are)



Measuring Chiral Symmetry

- Can we observe a chirally restored phase? (and how?)
- What happens to the ρ meson in the medium? What happens to the a₁ meson?
- What can we learn from reasonable hadronic dynamics (without a chirally restored phase)?



V. Koch, Int.J.Mod.Phys.E6:203-250,1997



The a₁ meson mass is expected to be equal to the mass of the ρ meson, in case of chiral symmetry restoration.

Problem: It is hard to measure.

	Mode	Fraction (Γ_i/Γ)	
Г1	$\pi^+\pi^-\pi^0$		
Γ ₂	$\pi^{0}\pi^{0}\pi^{0}$		
Γ ₃	$(ho\pi)_{S-wave}$	seen	
Γ ₄	$(ho\pi)_{D- ext{wave}}$	seen	
Γ ₅	$(ho(1450)\pi)_{S- ext{wave}}$	seen	
Г ₆	$(ho(1450)\pi)_{D- ext{wave}}$	seen	
Γ ₇	$\sigma\pi$	seen	
Г ₈	$f_0(980)\pi$	not seen	
F٩	$f_0(1370)\pi$	seen	
Γ ₁₀	$f_2(1270)\pi$	seen	
Γ_{11}	$K\overline{K}^{*}(892) + cc$	seen	
Γ_{12}	$\pi\gamma$	seen	

a1(1260) DECAY MODES



Idea: Check the mass distribution from the transport code.





Next: trigger on the decay channel $a_1 \rightarrow \gamma \pi$ (assumed width = 640keV)





\rightarrow Mass dependent branching ratios

$$\Gamma_{i,j}(M) = \Gamma_R^{i,j} \frac{M_R}{M} \left(\frac{\langle p_{i,j}(M) \rangle}{\langle p_{i,j}(M_R) \rangle} \right)^{2l+1} \frac{1.2}{1 + 0.2 \left(\frac{\langle p_{i,j}(M) \rangle}{\langle p_{i,j}(M_R) \rangle} \right)^{2l}}$$

Low mass a₁ favors $\gamma \pi$ decay, not $\rho \pi$

Trigger on a₁ $\rightarrow \gamma \pi$ = trigger on low mass a₁ mesons

H. Sorge, Phys.Rev.C52:3291,1995



a₁ meson – a sketch!

Below 900 MeV $\gamma \pi$ decay is dominant, $\rho \pi$ is kinematically suppressed.

Branching ratio folded with BW distribution





Full model calculation









Take home messages

- Experimentally reconstructable resonances are sensitive to the high density region if measured at high p_T (however, medium modification gets weaker)
- Beware of baryon kinematics

(i.e. even calculations w/o explicit medium modification have a medium)

• $a_1 \rightarrow \gamma \pi$ might not be the golden channel (mass dependent branching ratios may surprise you)

the end



Take home messages

 Experimentally reconstructable resonances are not sensitive to the high density region unless measured at high p_T

Beware of baryons kinematics

• $a_1 \rightarrow \gamma \pi$ might not be the golden channel







BACKUP SLIDES



рт dependence

- average transverse momentum depends on density
- reconstructable resonances have higher p_T





Idea: Check the mass distribution from the transport code.





Next: trigger on the decay channel $a_1 \rightarrow \gamma \pi$. (assumed BR = 0.1)





a1 meson - density

Density at the point of decay of the a_1 meson





p meson at higher energies




Formation time

- formation time is mass and p_T dependent
- shaded areas indicate the estimated lifetime of the partonic phase





Cross sections

$$\sigma_{1,2\to3,4}(\sqrt{s}) \sim (2s_3+1)(2s_4+1) \frac{\langle p_{3,4} \rangle}{\langle p_{1,2} \rangle} \frac{1}{\sqrt{s}} |M(m_3,m_4)|^2$$

Global fit with the same kind of matrix element for 5 channels

$$NN \to NN^*, N\Delta^*, \Delta\Delta, \Delta N^*, \Delta\Delta^*$$

$$|M(m_3, m_4)|^2 = A \frac{1}{(m_4 - m_3)^2 (m_4 + m_3)^2}$$

Data from elementary reactions are needed as an input into theory! (HADES?)





Cross sections

 $NN \to N\Delta_{1232}, NN^*, N\Delta^*, \Delta_{1232}\Delta_{1232}, \Delta_{1232}N^*, \text{ and } \Delta_{1232}\Delta^*$

parametrized via

$$\sigma_{1,2\to 3,4}(\sqrt{s}) \sim (2s_3+1)(2s_4+1) \frac{\langle p_{3,4} \rangle}{\langle p_{1,2} \rangle} \frac{1}{\sqrt{s}} |M(m_3, m_4)|^2$$

Global fit with the same kind of matrix element of

$$NN \to NN^*, N\Delta^*, \Delta_{1232}\Delta_{1232}, \Delta_{1232}N^*, \text{ and } \Delta_1$$

$$|M(m_3, m_4)|^2 = A \frac{1}{(m_4 - m_3)^2 (m_4 + m_3)^2}$$

Data from elementary reactions are needed as an input into theory! (HADES?)





Dileptonic and hadronic decays

Dileptons	Hadrons
do not interact strongly with the surrounding medium	suffer from final state interactions
originate from various sources in various mass regions (note: Dalitz decays)	originate from various sources in various mass regions
Typical branching ratios on the order of 10 ⁻⁴ - 10 ⁻⁵	Typical branching ratios on the order of 0.1 - 1
when measured reflect the integrated collision history	when measured reflect the late stage (after freezeout) of the collision



Dilepton spectra





Dilepton spectra

The comparison to the data gives a reasonable explaination of the 400-600 MeV region.

Note: No explicit in-medium modifications have been implemented.



HADES collaboration, Phys. Rev. Lett.98, 052302, 2007 D. Schumacher, S.Vogel, M. Bleicher, in preparation



Dilepton approaches

1) Shining

- Evaluate lifetime of the resonance, weight accordingly
- 2) Full weight only when resonance decays ignore absorbed resonances
 - Weight decayed resonance with vacuum width / BR
- 3) Full weight when absorbed/decayed
 - Weight all decayed/absorbed resonances with vacuum width / BR (most optimistic approach)



Dilepton via shining

- Dileptons are emitted throughout the whole resonance evolution ("time-integration method" or "shining")
- \Rightarrow Resonances do not have to decay to emit dileptons



Pictures from:

http://www.th.physik.uni-frankfurt.de/~brat/hsd.html

,Virtual' - time int. method:



Calculate probability P(t) to emit e+e- pair at each time t and integrate P(t) over time!

Heinz and Lee, Nucl.Phys.A544:503-508,1992 Ko and Li. Nucl.Phys.A582:731-748.1995



Dilepton sources

- Bremsstrahlung
- Dalitz decays
- π^0 , η , η' , ω , Δ ...
- Direct decays





Dalitz decay (vector meson)

(pseudoscalar meson)

- ρ, ω, φ ...
- Thermal dileptons



Dalitz decay (Δ)

Direct decay



Dilepton sources

Pseudoscalar mesons: $\frac{dN_{A \rightarrow \gamma e^+ e^-}}{dM}$

$$= \frac{4\alpha}{3\pi M} \sqrt{1 - \frac{4m_e^2}{M^2}} \left(1 + \frac{2m_e^2}{M^2}\right) \left(1 - \frac{M^2}{m_A^2}\right)^3$$
$$\times |F_{AB}(M^2)|^2 \frac{\Gamma_{A \to 2\gamma}}{\Gamma_{tot}} \langle N_A \rangle$$

Vector mesons:

$$\frac{dN_{A\to Be^+e^-}}{dM} = \frac{2\alpha}{3\pi M} \sqrt{1 - \frac{4m_e^2}{M^2}} \left(1 + \frac{2m_e^2}{M^2}\right) |F_{AB}(M^2)|^2 \frac{\Gamma_{A\to 2\gamma}}{\Gamma_{tot}} \langle N_A \rangle \\ \times \left(\left(1 + \frac{M^2}{m_A^2 - m_B^2}\right)^2 - \left(\frac{2m_A M}{m_A^2 - m_B^2}\right)^2 \right)^{3/2}$$

Direct decays:

$$BR(V \to e^+e^-) = \frac{\Gamma_{V \to e^+e^-}(M)}{\Gamma_{tot}}$$

$$\Gamma_{V \to e^+e^-}(M) = \frac{\Gamma_{V \to e^+e^-}(m_V)}{m_V} \frac{m_V^4}{M^3} \sqrt{1 - \frac{4m_e^2}{M^2}} \left(1 + 2\frac{m_e^2}{M^2}\right)$$



Dilepton sources

Δ baryon:

$$\frac{dN_{e^+e^-}}{dM} = \int \frac{dN_{\Delta \to Ne^+e^-}}{dM} (M_{\Delta}) \frac{dN_{\Delta}}{dM_{\Delta}} dM_{\Delta} = \int \frac{2\alpha}{3\pi M} \frac{\Gamma(M_{\Delta}, M)}{\Gamma_{\Delta 0}^{tot}} \frac{dN_{\Delta}}{dM_{\Delta}} dM_{\Delta}$$

$$\Gamma(M_{\Delta}, M) = \frac{\lambda^{1/2}(M^2, m_N^2, M_{\Delta}^2)}{16\pi M_{\Delta}^2} m_N [2\mathcal{M}_t(M, M_{\Delta}) + \mathcal{M}_l(M, M_{\Delta})]$$

$$\lambda(m_A^2, m_1^2, m_2^2) = (m_A^2 - (m_1 + m_2)^2)(m_A^2 - (m_1 - m_2)^2)$$

$$\mathcal{M}_l = (efg)^2 \frac{m_\Delta^2}{9m_N} M^2 4(m_\Delta - m_N - q_0)$$

 $\begin{aligned} \mathcal{M}_t = (efg)^2 \frac{m_\Delta^2}{9m_N} [q_0^2(5m_\Delta - 3(q_0 + m_N)) - M^2(m_\Delta + m_N + q_0)] \\ \text{L.G. Landsberg, Phys.Rept.128:301-376,1985} \\ \text{P. Koch, Z. Phys. C57:283-304, 1993} \end{aligned}$



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Breit-Wigner





Measuring resonances

- Since resonances decay on timescales of several fm they cannot be measured directly
- Resonances are measured via their decay products, cross section follows a Breit-Wigner law





Measuring resonances in p+p*

Correlate all protons and kaons in the event, plot invariant mass.

Lots of uncorrelated pairs → background subtraction needed Nentries 500 400 300 200 100 background normalized: $\Delta m = 1.6-2.1$ [GeV/c 0 1.4 1.5 1.6 1.8 1.9 2 2.11.7 2.2 $m_{inv}(p K^{-}) [GeV/c^{2}]$





Measuring resonances in A+A®

Different methods to subtract the background lead to slightly different results.



Measuring resonances in A+A®



 $m_{inv}(p K) [GeV/c^2]$

Correlate all protons and kaons in the event, plot invariant mass.

Peak?



Density calculation

• Lorentz-transform the CF density to the frame where the three-current vanishes (Eckart frame)

$$\vec{\beta}_{CF} = \frac{\sum_{j=1}^{N} \left(\frac{\vec{p}_j}{E_j}\right) \cdot P_j}{\sum_{j=1}^{N} P_j}$$



The zero-component of the transformed four-current is the relevant density



Density calculation

- Local baryon density is the zeroth component of the baryon four-current $\ j^\mu = (\rho_B, \vec{j})$ when the baryon is at rest
- UrQMD calculates in the Computational Frame (CF), which is usually the CMS (due to symmetry)
- $j_{CF}^{\mu}=(\rho_{B_{CF}},\vec{j}_{CF})$ can be calculated as a sum over Gaussians

$$\rho_{CF}(\vec{r_i}) = \sum_{j=1}^{N} \left(\frac{1}{\sqrt{2\pi\sigma}}\right)^3 \gamma_z e^{\left(-\frac{(x-x_0)^2 + (y-y_0)^2 + (z-z_0)^2 \gamma_z^2}{2\sigma^2}\right)} \\ = \sum_{j=1}^{N} P_j$$



Dileptons







Baryon resonances @ decay





Baryon resonances @ production

Density evaluated at point of production At higher density resonances become more reconstructable again (p_T effect?) Roughly scales with lifetime of the resonance







Baryon resonances @ production

 p_T cut applied ($p_T > 2GeV$)

"Reconstructability" increases at higher density Problem: High p_T resonances might not be the most interesting to study







Density distribution







Density distribution





Integral values







Cross sections

$$\sigma_{1,2\to3,4}(\sqrt{s}) \sim (2s_3+1)(2s_4+1) \frac{\langle p_{3,4} \rangle}{\langle p_{1,2} \rangle} \frac{1}{\sqrt{s}} |M(m_3,m_4)|^2$$

Global fit with the same kind of matrix element

$$|M(m_3, m_4)|^2 = A \frac{1}{(m_4 - m_3)^2 (m_4 + m_3)^2}$$





Gain/Loss rates of ρ mesons

SiS energies: Most gain from decay AGS and FAIR energies: More gain from collisions In the early stage - loss by absorption dominant Decays set in in the late stage







Gain/Loss terms

- Resonances can stem from two processes
 - Collisions (e.g. $\pi\pi \to \rho$)
 - Decays of heavier resonances (e.g. $N^*_{1520} \rightarrow N + \rho$)
- Resonances can be destroyed by two processes

• Decays (e.g.
$$ho
ightarrow e^+ e^-$$
)

• Absorption (e.g.
$$N + \rho \rightarrow N^*_{1520}$$
)



Integral values

- Consistency check: Sum of gain and collision agree
- Difference gives the number of resonances in the system







a₁ meson

What about the other channels?

Experimentally not feasible:

Higher mass resonances are either not known or the decay channel analyses contradict each other (further exp. studies certainly useful!).

	Mode	Fraction (Γ_i/Γ)
Γ ₁	$\pi^+\pi^-\pi^0$	
Γ ₂	$\pi^{0}\pi^{0}\pi^{0}$	
۲ ₃	$(ho\pi)_{S- ext{wave}}$	seen
Г ₄	$(ho\pi)_{D-wave}$	seen
Γ ₅	$(ho(1450)\pi)_{S- ext{wave}}$	seen
Г ₆	$(ho(1450)\pi)_{D- ext{wave}}$	seen
Γ ₇	$\sigma \pi$	seen
Г ₈	$f_0(980)\pi$	not seen
Г9	$f_0(1370)\pi$	seen
Γ ₁₀	$f_2(1270)\pi$	seen
Γ ₁₁	<i>K</i> K *(892)+ c.c.	seen
Γ_{12}	$\pi\gamma$	seen

a1(1260) DECAY MODES



Gain/Loss rates of ρ mesons





Which percentage can you reconstruct at a given density?



Clear ordering with lifetime, saturates at higher densities.



16

14

[fm]

18

20

Time evolution of ho_B

6

 $\begin{array}{l} E_{lab} = 2 \ A \ G \ e \ V \\ E_{lab} = 11 \ A \ G \ e \ V \\ E_{lab} = 30 \ A \ G \ e \ V \end{array}$ Central Pb+Pb (Au+Au) collisions 5 Averaged over all 4 hadron positions ρ₈/ρ₀ 2 0 2 6 8 10 12 0 Δ

Density?





Most resonances are from the low density region of the collision.


рт dependence (exp)

- average transverse momentum depends on centrality as well
- more central \Rightarrow more transverse momentum



Markert et al. [STAR], J.Phys.G35:044029,2008



Motivation

- Before including those density-driven effects into theoretical models one should check:
 - the maximum density which is reached in heavy ion collisions
 - the behaviour of the system without any medium effects
 - from what stage is the information one can gather experimentally from? and how?