

Of Cookbooks and Fairy Tales:

How neutrinos could make

the Universe we see

Sacha Davidson, IPN de Lyon, France

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 $\approx H \approx$ baryons

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\Rightarrow Question : where did that excess come from ?

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- ▶ (only theory explaining coherent temperature fluctuations in microwave background that arrive from causally disconnected regions today...)
- ▶ "60 e-folds" inflation $\equiv V_U \rightarrow > 10^{90} V_U$

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3. created/generated/cooked after inflation...

One number : $\left. \frac{n_B - n_{\bar{B}}}{n_\gamma} \right|_0 \simeq 6 \times 10^{-10}$
...many recipes...

Leptogenesis \equiv non-equil. generation of Y_L
"sphalerons" redistribute to Y_B

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1. preliminaries

3 ingredients

fast $B \leftrightarrow L$ at $T > m_W$ in the Standard Model

observe m_ν , but no p decay \Rightarrow leptogenesis?

2. the matter excess in the type I seesaw (**heavy**, hierarchical N_R)

the fairy tale

\sim estimates

can it be tested? or is it a physicists fairytale? There is a wolf...

3. ν MSM (type 1 seesaw with $m_N < m_W$)

is testable(?)

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to be produced after inflation (dilutes previous asym)

Three ingredients to prepare in the early U (old russian recipe)

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Present in the SM quarks, observed in Kaons and Bs, searched for in leptons (...T2K, future expts)

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From end inflation \rightarrow BBN, Universe is an expanding, cooling thermal bath, so non-equilibrium from :
 - ▶ slow interactions : $\tau_{\text{int}} \gg \tau_U = \text{age of Universe}$ ($\Gamma_{\text{int}} \ll H$)
 - ▶ phase transitions :

ingredient 1 : Does the SM conserve B ?

B, L are global symmetries of the SM Lagrangian (q, ℓ doublets, e, u, d singlets)

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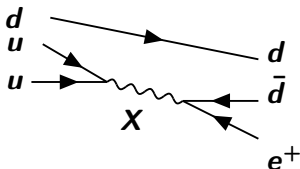
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Consider adding "X" with \mathcal{B} interactions :



$$\Gamma(p \rightarrow e^+ \pi) \sim \frac{\alpha^2 m_p^5}{m_X^4} \sim \left(\frac{10^{16} \text{ GeV}}{m_X} \right)^4 \times 10^{33} \text{ yrs}$$

ingredient 1 : But the SM *does not* conserve $B + L$...

in QFT, there is the axial anomaly...

...anomalously, the fermion current associated to a classical symmetry is not conserved.

see Polyakov,
"Gauge Fields + Strings,"
6.3=qualitative effects of instantons

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And $B + L$ is anomalous. Formally, for one generation (α colour) :

$$\sum_{\substack{SU(2) \\ \text{singlets}}} \partial^\mu (\bar{\psi} \gamma_\mu \psi) + \partial^\mu (\bar{\ell} \gamma_\mu \ell) + \partial^\mu (\bar{q}^\alpha \gamma_\mu q_\alpha) \propto \frac{1}{64\pi^2} W_{\mu\nu}^A \widetilde{W}^{\mu\nu A}.$$

where integrating the RHS over space-time counts “winding number” of the $SU(2)$ gauge field configuration.

\Rightarrow Field configurations of non-zero winding number are sources of a doublet lepton and three (for colour) doublet quarks for each generation.

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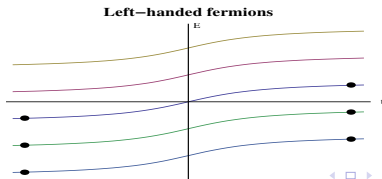
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thanks to V Rubakov

SM B+L violation : rates

't Hooft
Kuzmin Rubakov+
Shaposhnikov

At $T = 0$ is tunneling process (from winding # to next, "instanton") :

$$\Gamma \propto e^{-8\pi/g^2}$$

At $0 < T < m_W$, can climb over the barrier :

$$\Gamma_{\cancel{B+L}} \sim \begin{matrix} e^{-m_W/T} & T < m_W \\ \alpha^5 T & T > m_W \end{matrix}$$

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*** SM $\cancel{B+L}$ is $\Delta B = \Delta L = 3 (= N_f)$. No proton decay! ***

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One observation to fit, many new parameters...

\Rightarrow prefer BSM motivated by other data $\Leftrightarrow m_\nu \Leftrightarrow$ seesaw!

(uses non-pert. SM $B \not{L}$)

- add 3 singlet N to the SM in charged lepton and N mass bases, at scale $> M_i$:

$$\mathcal{L} = \mathcal{L}_{SM} + \lambda_{\alpha J} \bar{N}_J \ell_\alpha \cdot \phi - \frac{1}{2} \bar{N}_J M_J N_J^c$$

add 18 parameters :
 M_1, M_2, M_3

18 - 3 (ℓ phases) in λ

M_i unknown ($\not\propto v = \langle \phi^0 \rangle$), and Majorana (\mathbb{Z}). \mathcal{CP} in $\lambda_{\alpha J} \in \mathbf{C}$.

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- at low scale, for $M \gg m_D = \lambda v$, light ν mass matrix

$$\nu_{L\alpha} \xrightarrow{\nu \lambda^{\alpha A}} \times \xrightarrow{M_A} \times \xleftarrow{\nu \lambda^{\beta A}} \nu_{L\beta}$$

N_A

9 parameters :
 m_1, m_2, m_3

6 in U_{MNS}

$$[m_\nu] = \lambda M^{-1} \lambda^T v^2$$

for $\lambda \sim h_t, M \sim 10^{15} \text{ GeV}$
 $\lambda \sim 10^{-7}, M \sim 10 \text{ GeV} \quad \sim .05 \text{ eV}$

“natural” $m_\nu \ll m_f : m_\nu \propto \lambda^2$, and $M > v$ allowed.

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- at low scale, Higgs mass contribution

$$\delta m_\phi^2 \simeq - \sum_I \frac{[\lambda^\dagger \lambda]_{II}}{8\pi^2} M_I^2 \sim \frac{m_\nu M_I^3}{8\pi^2 v^4} v^2$$

for $M \gtrsim 10^7$ GeV $> v^2$ tuning problem

(? adding particles to cancel 1 loop...but higher loop? Need symmetry to cancel ≥ 2 loop?)
 \Rightarrow do seesaw with $M_I \lesssim 10^8$ GeV?

(NB, in this talk, ϕ = Higgs, H = Hubble)

Leptogenesis in the type 1 seesaw : usually a Fairy Tale

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Buchmuller et al
Covi et al
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Once upon a time, a Universe was born.

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The adventure begins after inflationary expansion of the Universe :

- 1 Assuming its hot enough, a population of N s appear, because they like the heat.
- 2 As the temperature drops below M , the N population decays away.
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If this asymmetry can escape the big bad wolf of thermal equilibrium...

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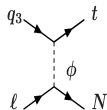
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- 4 If this asymmetry can escape the big bad wolf of thermal equilibrium...
- 5 the lepton asym gets partially reprocessed to a baryon asym by non-perturbative $B + L$ -violating SM processes ("sphalerons")

And the Universe lived happily ever after, containing many photons. And for every 10^{10} photons, there were 6 extra baryons (wrt anti-baryons).

Estimate something : $\mathbb{P} + \text{dynamics}$ Suppose $M_1 \ll M_{2,3}, T_{\text{reheat}} > M_1 \sim 10^9 \text{ GeV}$

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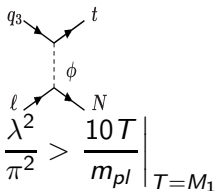


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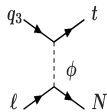
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Suppose satisfied...

Later, Lepton asym is produced in N decay if there is \mathcal{CP} , and it is “out of equilibrium”. Naive \mathcal{PE} condition, $\Gamma_{decay} < H(T = M)$:

$$\Gamma_{decay} = \frac{[\lambda\lambda^\dagger]_{11} M_1}{8\pi} < \frac{10 T^2}{m_{pl}} \Big|_{T=M_1}$$

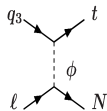
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Get thermal density $n_N \simeq n_\gamma$ if $M_1 \lesssim T$, and $\tau_{prod} < \tau_U$:

$$\Gamma_{prod} \sim \sigma v n \sim \frac{h_t^2 \lambda^2}{T^2} \frac{T^3}{\pi^2} \sim \frac{h_t^2 \lambda^2}{\pi^2} T > H \simeq \frac{10 T^2}{m_{pl}}, \Rightarrow \frac{\lambda^2}{\pi^2} > \frac{10 T}{m_{pl}} \Big|_{T=M_1}$$



Suppose satisfied...

Later, Lepton asym is produced in N decay if there is \mathcal{CP} , Lepton asym can survive after **inverse decays** ("washout") become rare enough

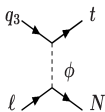
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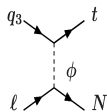
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so (1/3 is from SM $B \neq L$, $s \sim g_* n_\gamma$, ϵ_α is lepton asym in decay)

$$\frac{n_B - n_{\bar{B}}}{s} \sim \frac{1}{3} \sum_{\alpha} \epsilon_\alpha \frac{n_N(T_\alpha)}{g_* n_\gamma} \sim 10^{-3} \epsilon \frac{H}{\Gamma} \quad (\text{want } 10^{-10})$$

Estimate ϵ , the CP and L asymmetry in decays

Recall (in **S**-matrix) $CP : \langle \phi \ell | \mathbf{S} | N \rangle \rightarrow \langle \bar{\phi} \bar{\ell} | \mathbf{S} | \bar{N} \rangle = \langle \bar{\phi} \bar{\ell} | \mathbf{S} | N \rangle$, ($\bar{\eta}$ = anti- η)

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finite temp : Beneke et al 10

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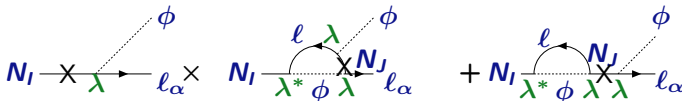
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Just try to calculate ϵ_1 ?

- no asym at tree
- asym at tree \times loop, if \mathcal{CP} from complex cpling *and* on-shell particles in the loop (divergences cancel in diff, need Im part of Feynman param integrtn)

\mathcal{CP} , complex couplings, loops unitarity and all that... (estimate ϵ , no loop calc)

1 the S-matrix $\mathbf{S} \equiv \mathbf{1} + i\mathbf{T}$ is CPT invariant

Kolb+Wolfram,
NPB '80, Appendix

$$\langle \overline{\phi\ell} | \mathbf{S} | N \rangle = \langle N | \mathbf{S} | \phi\ell \rangle \quad (= \langle \phi\ell | \mathbf{S}^\dagger | N \rangle^*)$$

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2 We are interested in a \mathcal{CP} asymmetry :

$$\epsilon \propto \int d\Pi \left(|\langle \phi\ell | \mathbf{T} | N \rangle|^2 - |\langle \overline{\phi\ell} | \mathbf{T} | N \rangle|^2 \right)$$

SO (this formula exact, if I kept 2s and sums)

$$\epsilon \propto \text{Im} \left\{ \langle \phi\ell | \mathbf{T}^\dagger | N \rangle \langle N | \mathbf{T}\mathbf{T}^\dagger | \phi\ell \rangle \right\}$$

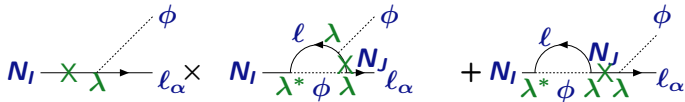
\Rightarrow need complex cplings, and on-shell particles in a loop

Estimating ϵ for hierarchical N_j

Consider simple case : $M_1 \ll M_{2,3}$. Suppose lepton asym generated in \mathcal{CP} decays of N_1 :

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(NB, no intermediate N_1 because cplg combo real)

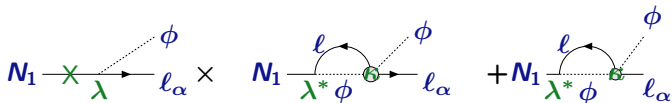


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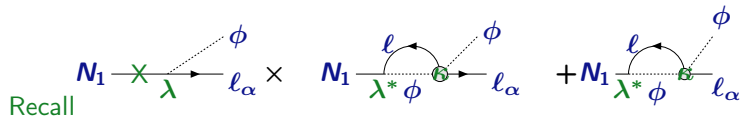


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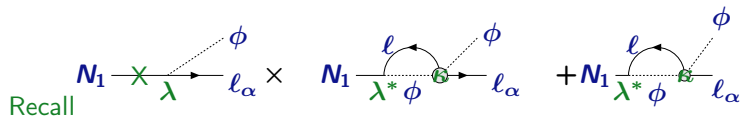


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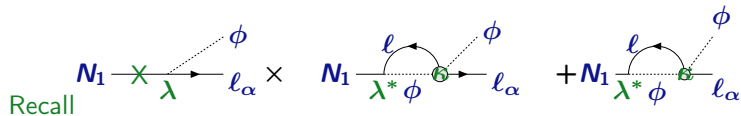
because $\langle \phi l | \mathbf{T} | N \rangle = \mathcal{M}(N \rightarrow \phi l) (2\pi)^4 \delta^4(\sum p_i - \sum p_f)$

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Recall

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$$\epsilon_1 < \frac{3}{8\pi} \frac{m_\nu^{\max} M_1}{v^2} \sim 10^{-6} \frac{M_1}{10^9 \text{GeV}} \gtrsim 10^{-6}$$

so for $M_1 \ll M_{2,3}$, need $M_1 \gtrsim 10^9$ GeV to obtain sufficient ϵ

Ouff : summary about simplest model and going beyond

1. type 1 seesaw model with hierarchical N_i :

suppose scattering in thermal bath produces abundance of $N_1 \sim T^3$,
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credibility enhanced if measure Majorana m_ν ($0\nu 2\beta$)
and if measure \mathcal{CP} in the lepton sector
and if measure $T_{reheat} > 10^9$ GeV

grav waves? BuchmullerDomcke etal
CMB? Martin etal

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1. $M_I \sim M_J \Leftrightarrow$ resonantly enhance ϵ ... up to $\epsilon \lesssim 1$.
2. But at lower T , age of Universe is longer, is there sufficient out-of-equilibrium?
 - 1) want to reproduce neutrino masses

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2) need to decay before Electroweak PT (to profit from sphalerons)...
...more restrictive : need $\mathcal{P}E$. Only keep the asym produced by N_s
who decay after inverse decays $\Gamma_{ID}(\phi\ell \rightarrow N)$ go out of equilibrium
(must happen before EWPT) :

$$\Gamma_{ID} \sim e^{-M/T} \Gamma(N \rightarrow \phi\ell) < H \quad \Rightarrow \quad M \gtrsim 10 T_c$$

Fairy tale works for degen N_I for $M_I \gtrsim \text{TeV}$

(but are $M_I \sim \text{TeV}$ any more detectable than $M_I \sim 10^9$ GeV?)

ν MSM : type 1 seesaw below 100 GeV gives BAU and DM

Asaka + Shaposhnikov
thesis Canetti

...

ingredients : SM +

$$N_{2,3} : 100 \text{ MeV} \lesssim M_{2,3} \lesssim 10 \text{ GeV}, \Delta M \lesssim \begin{cases} 10^{-6} \text{ eV} & Y_B, \Omega_{DM} \\ \text{keV} & Y_B, \text{NOT } \Omega_{DM} \end{cases}$$

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tests :

N_1 as DM : X-rays from DM decay, WDM bounds (depend on momentum distribution)

$N_{2,3}$: beam dump, SHIP

How does asym generation work? (very simplified!)

1 at $T \lesssim TeV$ (recall $\lambda \lesssim 10^{-7}$) , produce N_2, N_3 via Yukawa interaction
 $\lambda \overline{N} \ell \cdot \phi$

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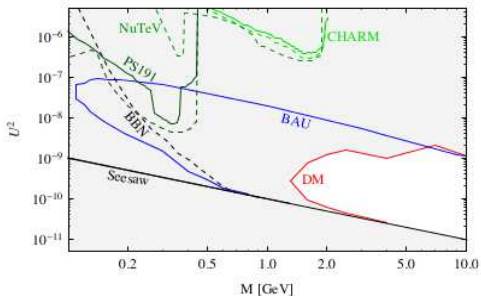
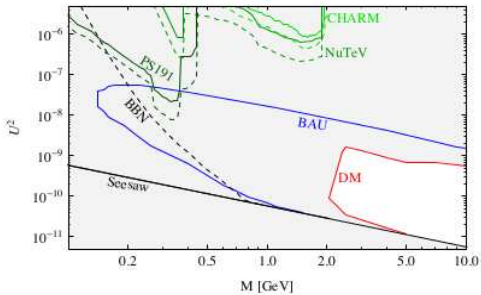
at $\tau_U \sim \tau_{OSC}$, 1,2,3 are *coherent*, so CPV from $\lambda - \Delta M^2 - \lambda$ gives
flavour asymms in $\nu_{L\alpha}$ (to small)

lepton number in $\ell_L + N_R$ is conserved (actually, L_{SM} + helicity of N_i)

from $\tau_{OSC} \rightarrow \tau_{EWPT}$, asymms in $\nu_{L\alpha}$ seed asymms in $N \rightarrow$ asymms in
 $\nu_{L\alpha}$ (enough asym)

...works also in detailed calculations with all available technology...
(eg also include lepton number violating interactions)

Teresi Hambye
Eijima + Shaposhnikov
Ghiglieri + Laine



$$U^2 = \text{Tr}[\lambda M^{-2} \lambda^\dagger]$$

Summary

The visible Universe today is made of baryonic matter, and negligible anti-matter. This excess should be produced during the evolution of the Universe — after inflation, (and before BigBangNucleosynthesis).

The three required ingredients are B number violn, C+CP violn, and a departure from thermal equilibrium. All are present in the SM of particle phys and cosmo...but noone has figured out how to combine them to generate the observed asym. Therefore the matter excess is taken as *evidence for Beyond-theStandard-Model Physics*.

Leptogenesis is a class of recipes, that use majorana neutrino mass models to generate the matter excess. The “new physics” in the lepton sector should generate a lepton asymmetry in the early Universe (before the Electroweak Phase Transition), and the non-perturbative SM B+L violn will partially reprocess it to a baryon excess.

- * efficient, to use the BSM for m_ν to generate the Baryon Asym.
- * using SM B+L violn ($\Delta B = \Delta L = 3$) avoids proton lifetime bound
- * *it works* ...rather well, for a wide range of parameters

The Excess of Matter over Antimatter in the Universe

Introduction

The matter excess — where did it come from?

Outline

Required Ingredients

Ingredient 1 : B is not conserved

Leptogenesis in the type I seesaw