

# **Tests of the Standard Model**

**Joachim Mnich**

**CERN EP**

**International Europhysics Conference  
on High Energy Physics 1999**

**Tampere, 15 – 21 July 1999**

## Outline

---

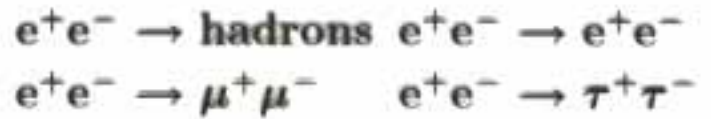
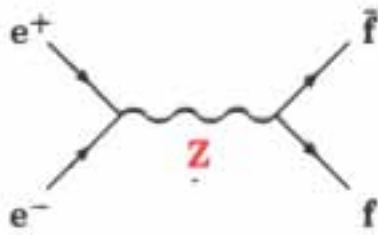
- Precision measurements at the Z resonance
- Fermion-pair production above the Z
- Production of neutral bosons pairs  $e^+e^- \rightarrow \gamma\gamma$ ,  $e^+e^- \rightarrow ZZ$  and the couplings of the neutral gauge bosons
- The properties of the  $W^\pm$  boson
- Interpretation in the Standard Model and limits on the Higgs boson

### New results from

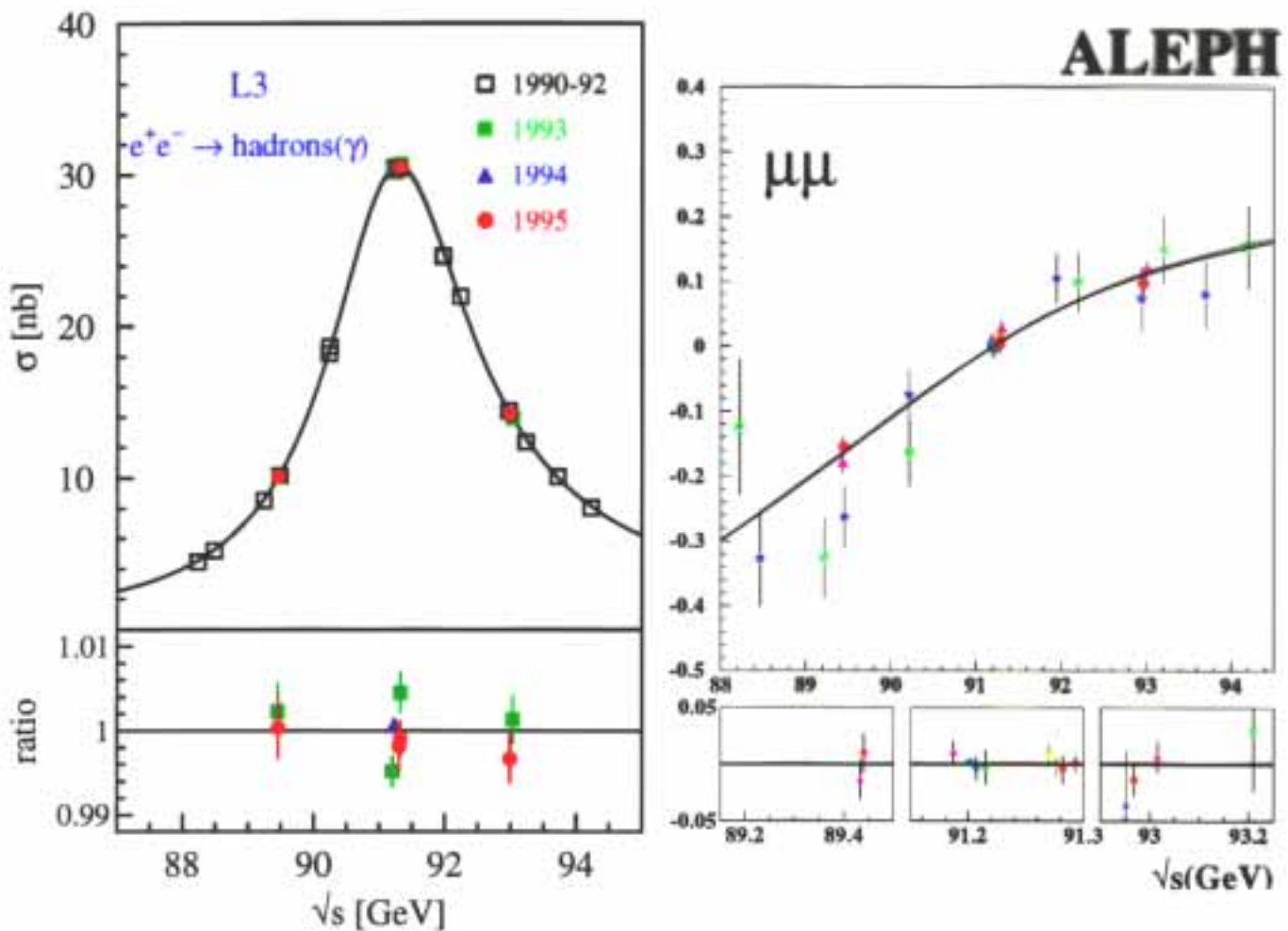
- LEP up to  $\sqrt{s} = 196$  GeV
- SLD
- CDF and DØ
- HERA

**Most of the results are preliminary**

## Z lineshape



- Precision measurements of total cross sections and leptonic forward-backward asymmetries at LEP:



- 17 million Z decays observed at LEP (1989 – 1995)
- Finalizing the analyses of the experiments
- Determination of Z parameters

## Z lineshape

---

- Improvements on theoretical calculations

ZFITTER 6.10 (D. Bardin et al.)

TOPAZ0 4.4 (G. Passarino et al.)

ALIBABA (W. Beenaker et al.) for  $e^+e^- \rightarrow e^+e^-(\gamma)$

### ZFITTER & TOPAZ0 calculate

- QED and QCD corrections

ISR:  $\mathcal{O}(\alpha^2), \mathcal{O}(\alpha^3 L^3)$   $L = \ln(s/m_e^2)$  FSR:  $\mathcal{O}(\alpha), \mathcal{O}(\alpha\alpha_s), \mathcal{O}(\alpha_s^3)$

+ interference

- Electroweak

leading two-loop  $\mathcal{O}(G_F^2 m_t^4)$ , sub-leading two-loop  $\mathcal{O}(G_F^2 m_t^2 m_Z^2)$

- Mixed QCD  $\times$  EW

$\mathcal{O}(\alpha\alpha_s)$ , leading  $\mathcal{O}(\alpha\alpha_s^2)$

Contributions from G. Degrossi et al., S. Jadach et al.,  
B. Kniehl, J. Kühn et al., G. Montagna et al.

### $\Rightarrow$ Small theoretical uncertainties:

- Uncertainties on QED corrections of Z lineshape:

$$\Delta m_Z = \pm 0.3 \text{ MeV}$$

$$\Delta \Gamma_Z = \pm 0.5 \text{ MeV}$$

$$\Delta \sigma_{\text{had}}^0 / \sigma_{\text{had}}^0 = \pm 2 \cdot 10^{-4}$$

- Very good agreement between ZFITTER and TOPAZ0:

$$\leq 10^{-4} \text{ (peak)} \quad \leq 3 \cdot 10^{-4} \text{ (off - peak)}$$

- SM parameter uncertainty

$$\Delta m_Z = \pm 0.3 \text{ MeV}$$

- $0.54 - 0.61 \cdot 10^{-3}$  on the luminosity measurement  
(B. Ward et al.)

## Measurement of Z parameters

---

- Experiments determine 9 parameter from total cross sections and forward-backward asymmetries
- Combination of the four LEP experiments:

$$m_Z \quad 91\,187.2 \pm 2.1 \text{ MeV}$$

$$\Gamma_Z \quad 2\,499.4 \pm 2.4 \text{ MeV}$$

---

$$\sigma_{\text{had}}^0 \quad 41.544 \pm 0.037 \text{ nb}$$

$$R_e \quad 20.803 \pm 0.049$$

$$R_\mu \quad 20.786 \pm 0.033$$

$$R_\tau \quad 20.764 \pm 0.045$$

---

$$A_{\text{FB}}^{0,e} \quad 0.0145 \pm 0.0024$$

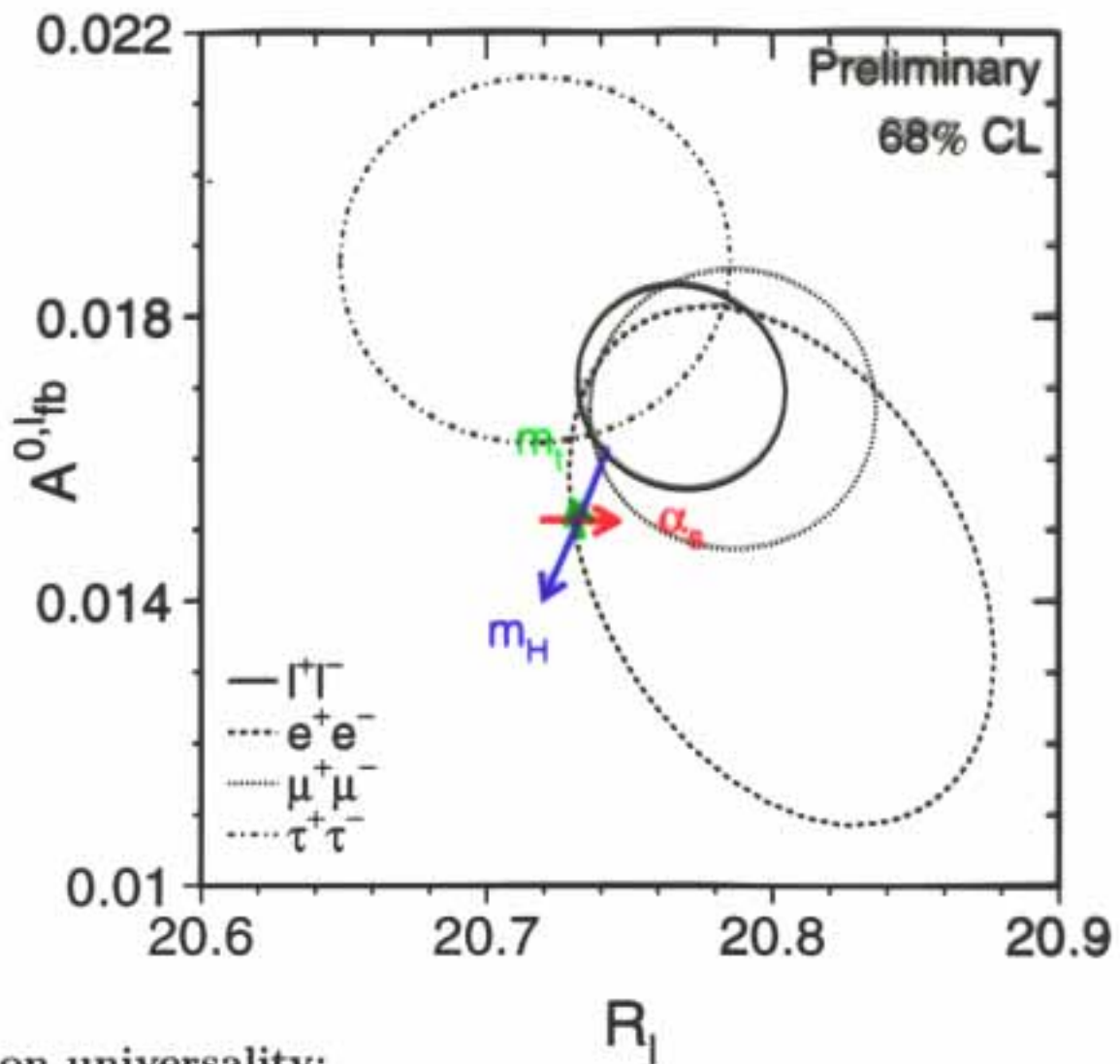
$$A_{\text{FB}}^{0,\mu} \quad 0.0167 \pm 0.0013$$

$$A_{\text{FB}}^{0,\tau} \quad 0.0188 \pm 0.0017$$

(+ small correlations)

$$\sigma_{\text{had}}^0 = \frac{12\pi}{m_Z^2} \frac{\Gamma_e \Gamma_{\text{had}}}{\Gamma_Z^2}, \quad R_\ell = \frac{\Gamma_{\text{had}}}{\Gamma_\ell},$$
$$A_{\text{FB}}^{0,\ell} = \frac{3}{4} A_e A_\ell, \quad A_\ell = \frac{2\bar{g}_V^\ell \bar{g}_A^\ell}{(\bar{g}_V^\ell)^2 + (\bar{g}_A^\ell)^2}$$

## Measurement of Z parameters



Lepton universality:

$$R_\ell = 20.768 \pm 0.024 \quad A_{\text{FB}}^{0,\ell} = 0.01701 \pm 0.00095$$

$$(\alpha_s = 0.1229 \pm 0.0036_{-0}^{+0.0033}(m_H))$$

Partial decay widths:

$$\Gamma_{\text{had}} = 1743.9 \pm 2.0 \text{ MeV}$$

$$\Gamma_\ell = 83.958 \pm 0.089 \text{ MeV}$$

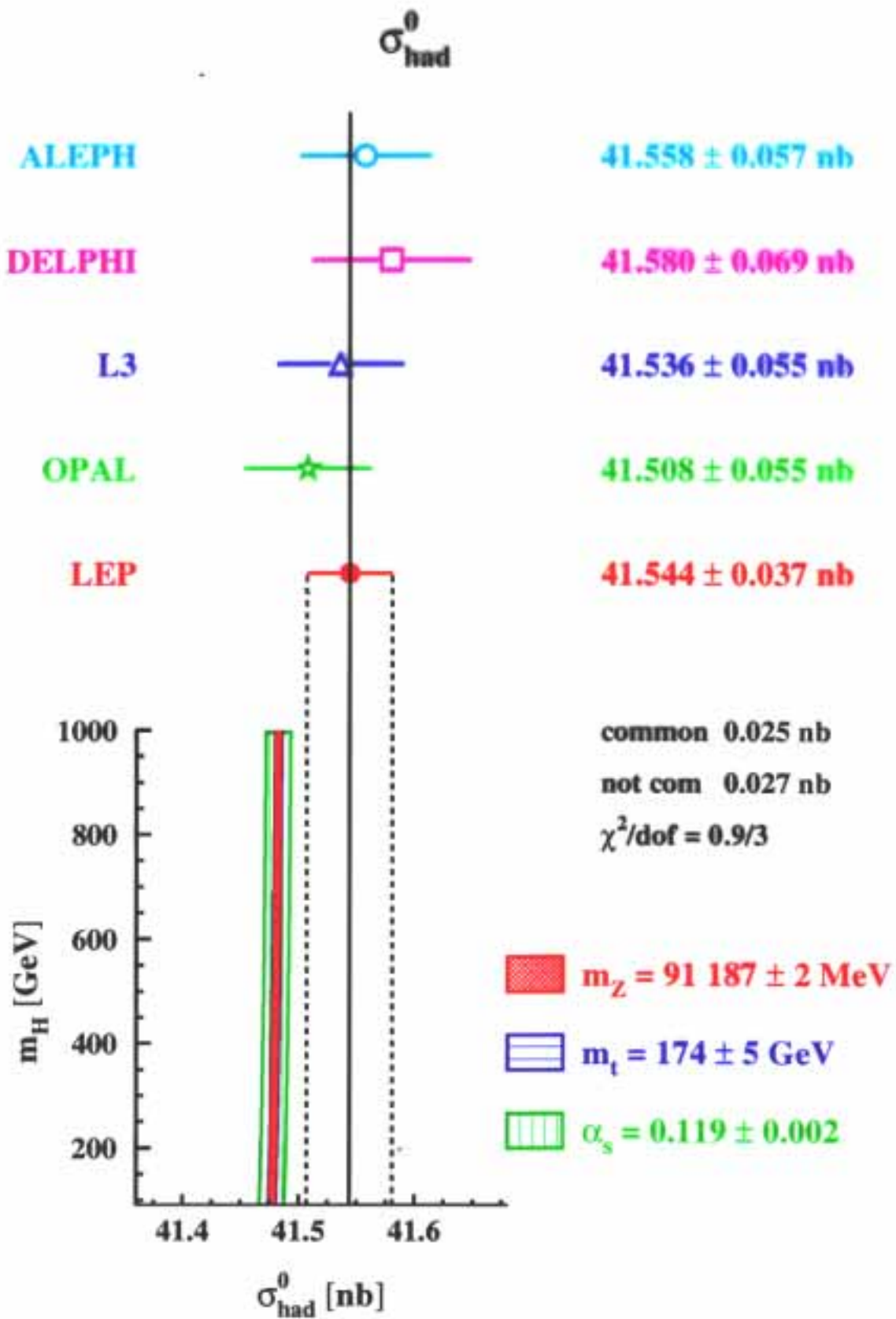
$$\Gamma_{\text{inv}} = 498.80 \pm 1.5 \text{ MeV}$$

$$\Delta\Gamma_{\text{inv}} < 2.0 \text{ MeV} \quad 95\% \text{ CL}$$

Number neutrino families:

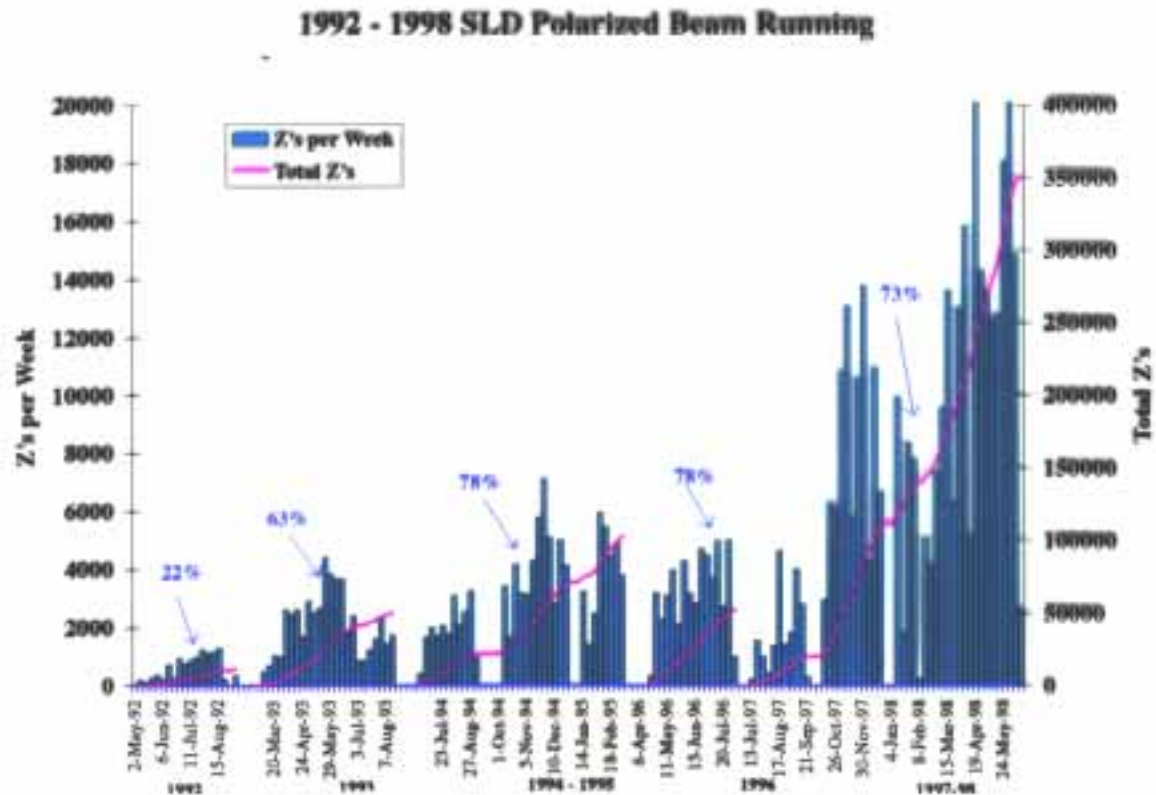
$$N_\nu = 2.9835 \pm 0.0083$$

## Measurements of the hadronic pole cross section



## Z couplings to leptons

- SLD: 550k  $e^+e^- \rightarrow \text{hadrons}(\gamma)$  events collected in total Polarized  $e^-$  beam



Left-right asymmetry  $A_{LR}$  in  $e^+e^- \rightarrow \text{hadrons}$

$$A_e = 0.1510 \pm 0.0025$$

Left-right forward-backward asymmetries  $e^+e^- \rightarrow \ell^+\ell^-$ :

$$A_e = 0.1504 \pm 0.0072$$

$$A_\mu = 0.120 \pm 0.019$$

$$A_\tau = 0.142 \pm 0.019$$

$$A_\ell = 0.1459 \pm 0.0063$$

Measurement of the effective weak mixing angle:

$$\sin^2 \bar{\theta}_W = 1 - 4 \frac{\bar{g}_V^\ell}{\bar{g}_A^\ell} = 0.23109 \pm 0.00029$$

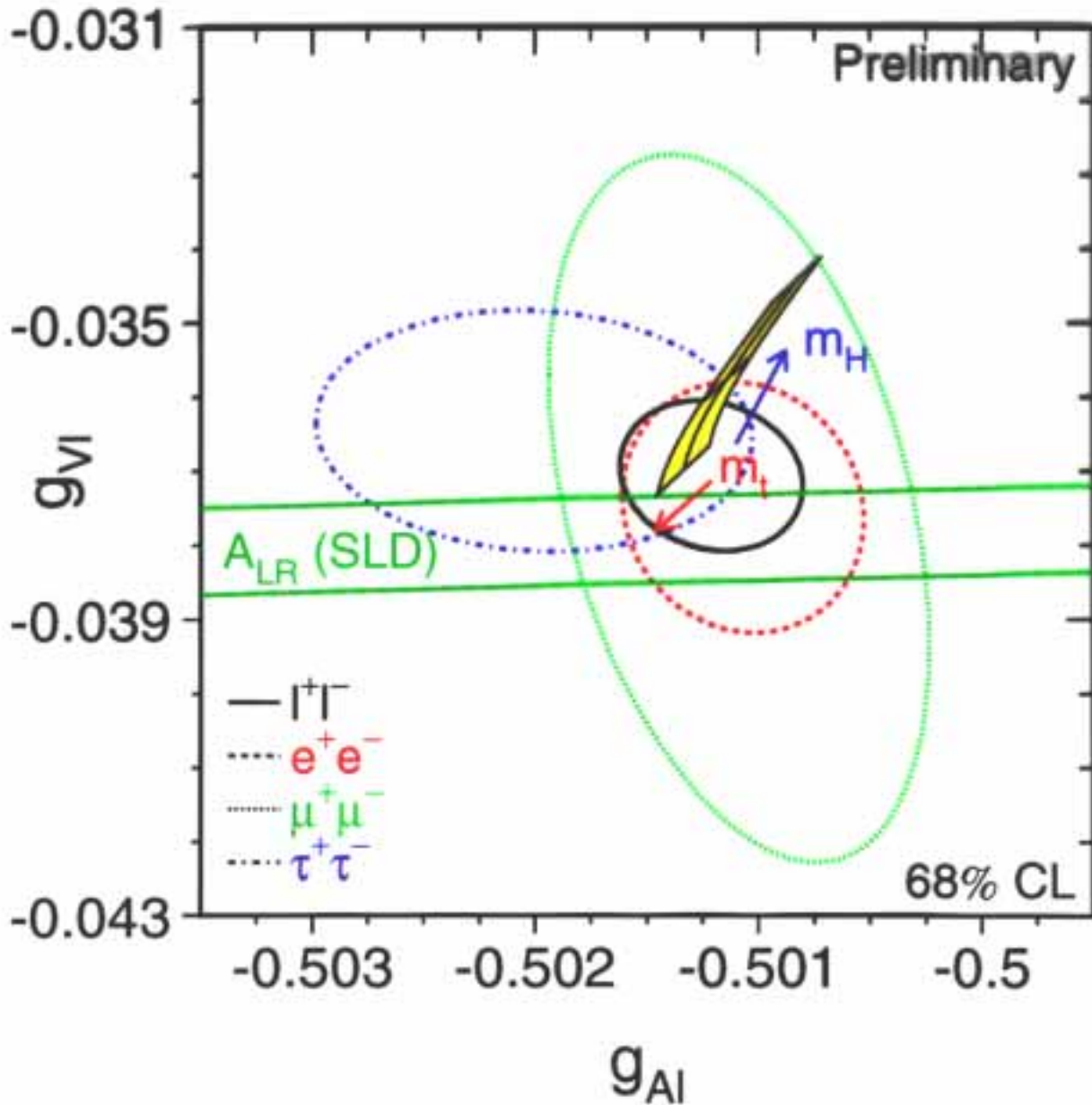


## Test of lepton universality

Include LEP tau polarization measurements:

$$A_e = 0.1483 \pm 0.0051$$

$$A_\tau = 0.1425 \pm 0.0044$$



Ratios of neutral current coupling constants (LEP & SLD):

$$\bar{g}_A^\mu / \bar{g}_A^e = 1.0001 \pm 0.0014 \quad \bar{g}_V^\mu / \bar{g}_V^e = 0.981 \pm 0.082$$

$$\bar{g}_A^\tau / \bar{g}_A^e = 1.0019 \pm 0.0015 \quad \bar{g}_V^\tau / \bar{g}_V^e = 0.964 \pm 0.032$$

## Z couplings to quarks

### Measurements of

- Cross sections ( $R_b, R_c$ ) at LEP & SLD

$$R_q = \Gamma_q / \Gamma_{\text{had}} \quad \Gamma_q \propto (\bar{g}_A^q)^2 + (\bar{g}_V^q)^2$$

- Forward-backward asymmetries at LEP

$$A_{\text{FB}}^{0,b}, A_{\text{FB}}^{0,c}$$

- Left-right forward-backward asymmetries

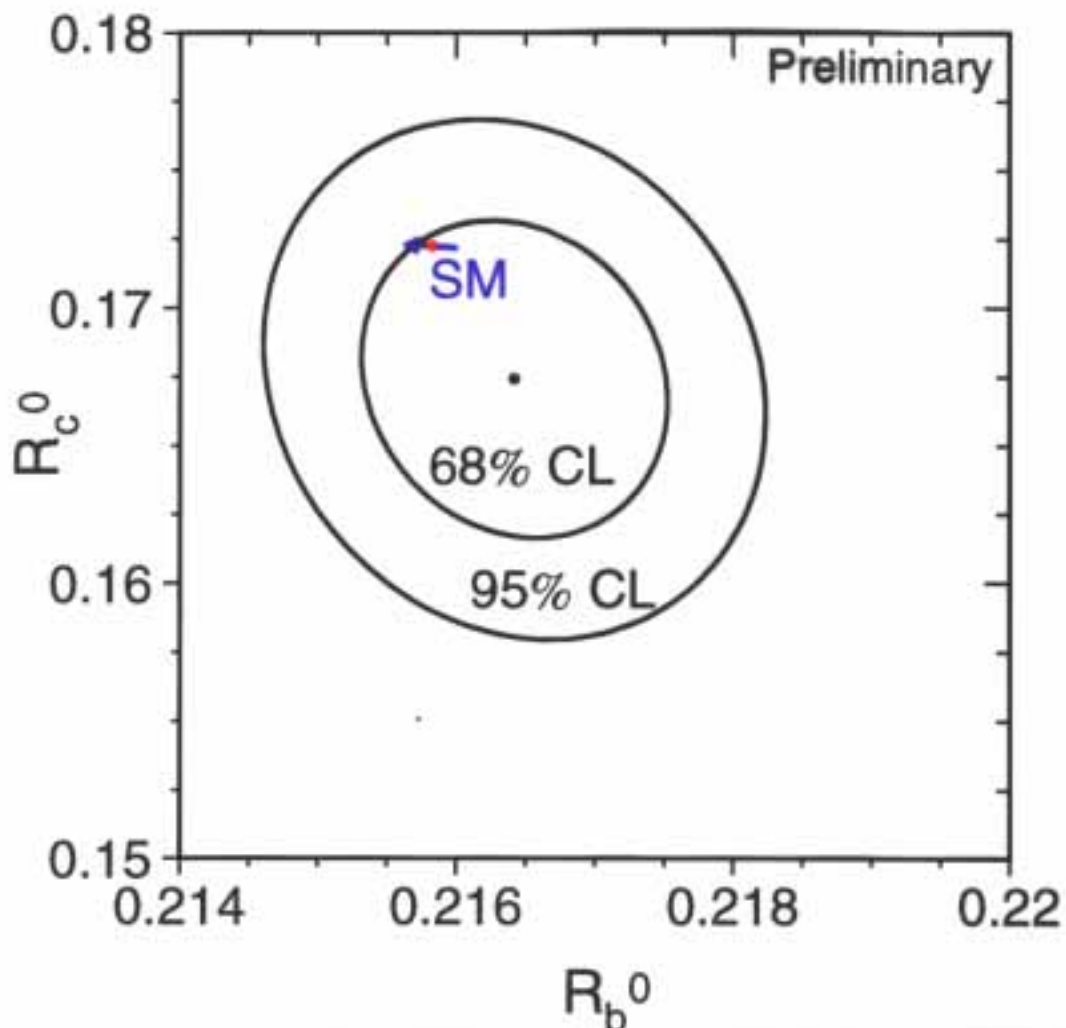
$$A_b, A_c \quad A_q = \frac{2\bar{g}_A^q\bar{g}_V^q}{(\bar{g}_A^q)^2 + (\bar{g}_V^q)^2}$$

### Combined fit to LEP & SLD data:

$$R_b = 0.21642 \pm 0.00073 \quad R_c = 0.1674 \pm 0.0038$$

$$A_{\text{FB}}^{0,b} = 0.0984 \pm 0.0020 \quad A_{\text{FB}}^{0,c} = 0.0691 \pm 0.0037$$

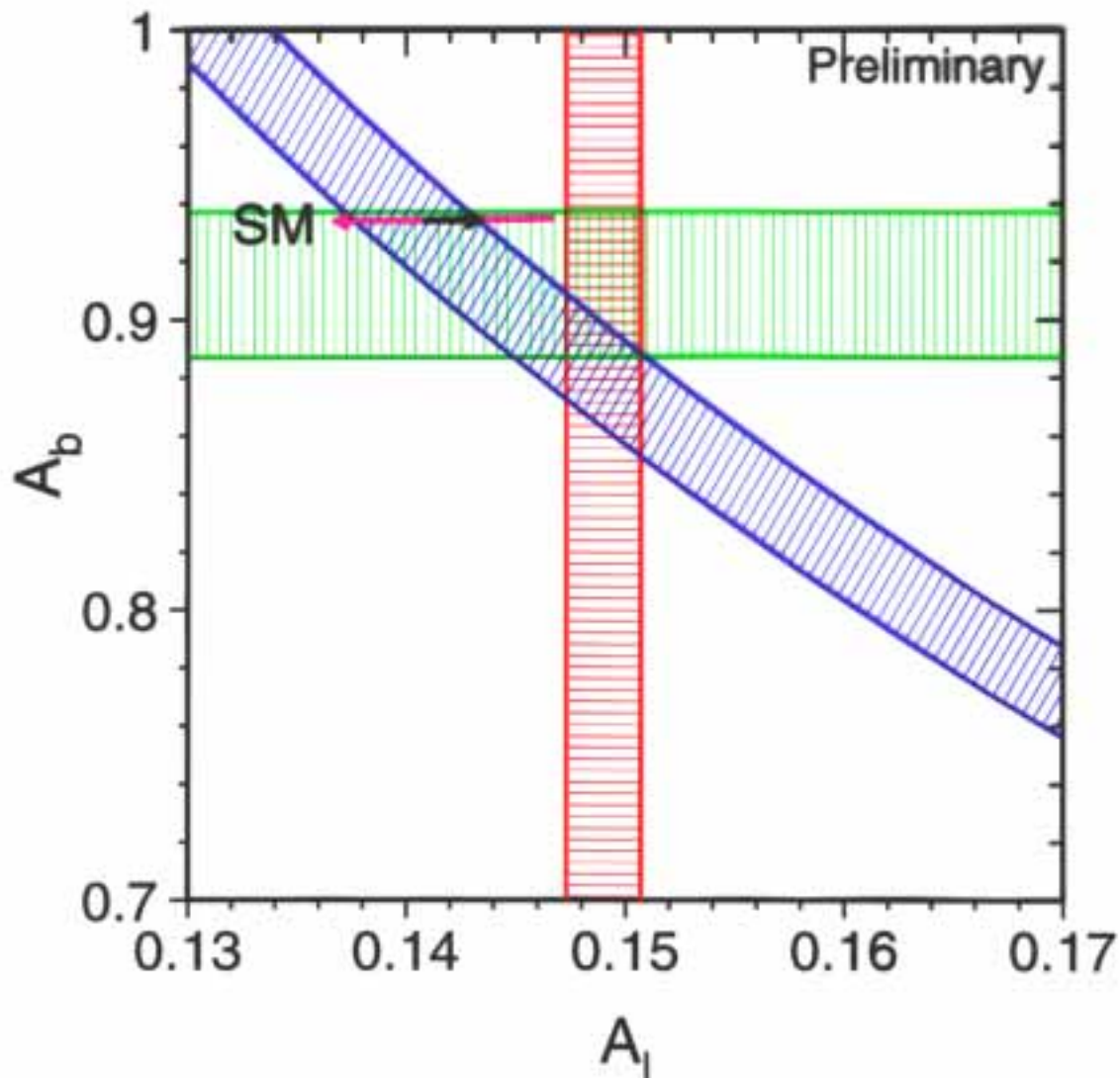
$$A_b = 0.912 \pm 0.025 \quad A_c = 0.630 \pm 0.026$$



## Z couplings to quarks

Comparison of

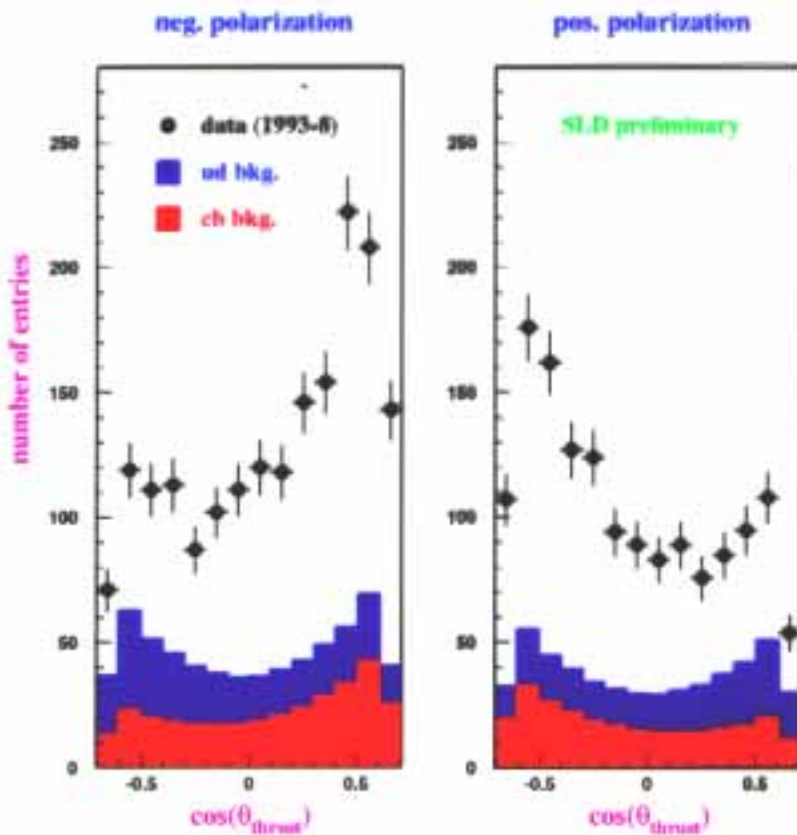
- $A_b$  (left-right forward-backward asymmetry)
- $A_\ell$  ( $A_{LR}, A_{FB}^{0,\ell}$ , tau-polarization)
- $A_{FB}^{0,b} = \frac{3}{4} A_\ell A_b$
- SM ( $m_H, m_t$ )



	LEP	SLD	LEP & SLD	SM
$A_\ell$	$0.1471 \pm 0.0026$		$0.1490 \pm 0.0017$	
$A_b$	$0.892 \pm 0.024$	$0.912 \pm 0.025$	$0.893 \pm 0.016$	0.935
$A_c$	$0.624 \pm 0.035$	$0.630 \pm 0.026$	$0.625 \pm 0.021$	0.668

## Z couplings to s-quarks

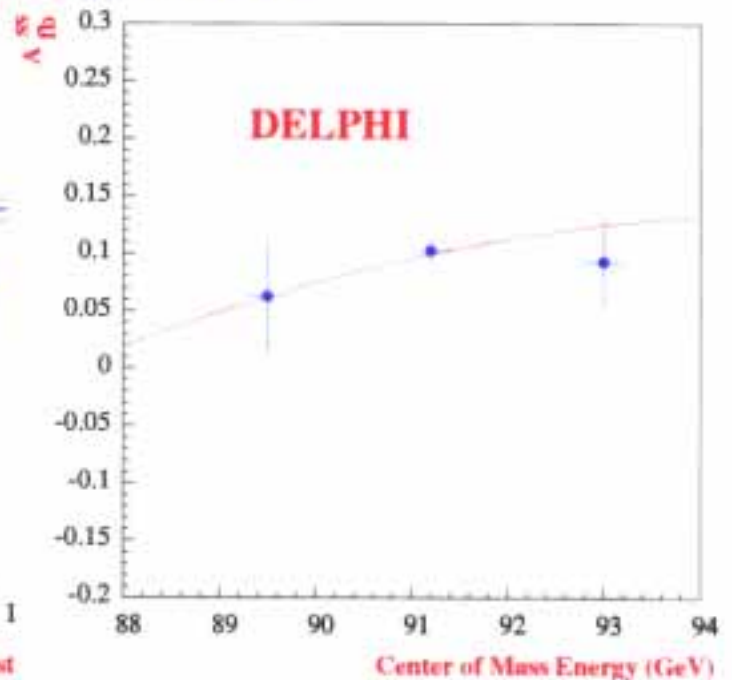
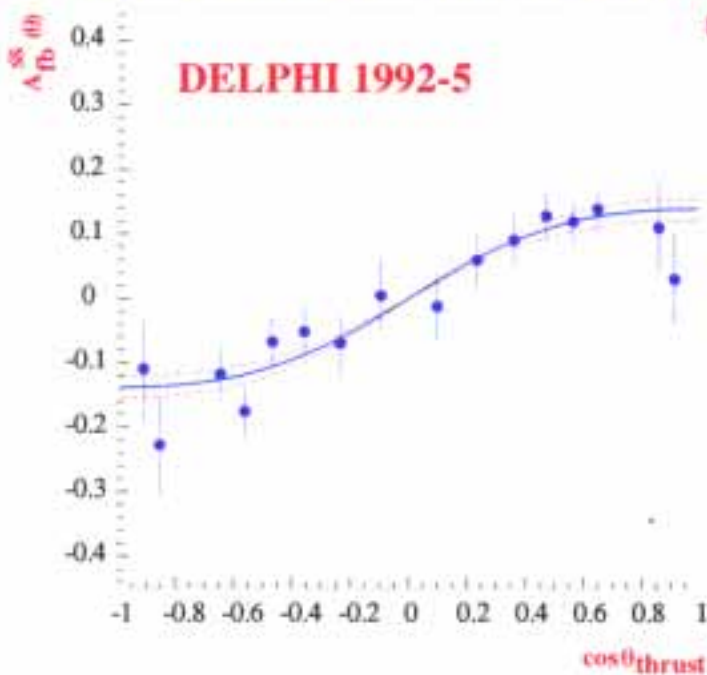
Identify  $e^+e^- \rightarrow s\bar{s}$  by high momentum  $K^+$ ,  $K_s$ ,  $\Lambda^0$  in hadronic events



SLD:

$$A_s = 0.85 \pm 0.06 \pm 0.07$$

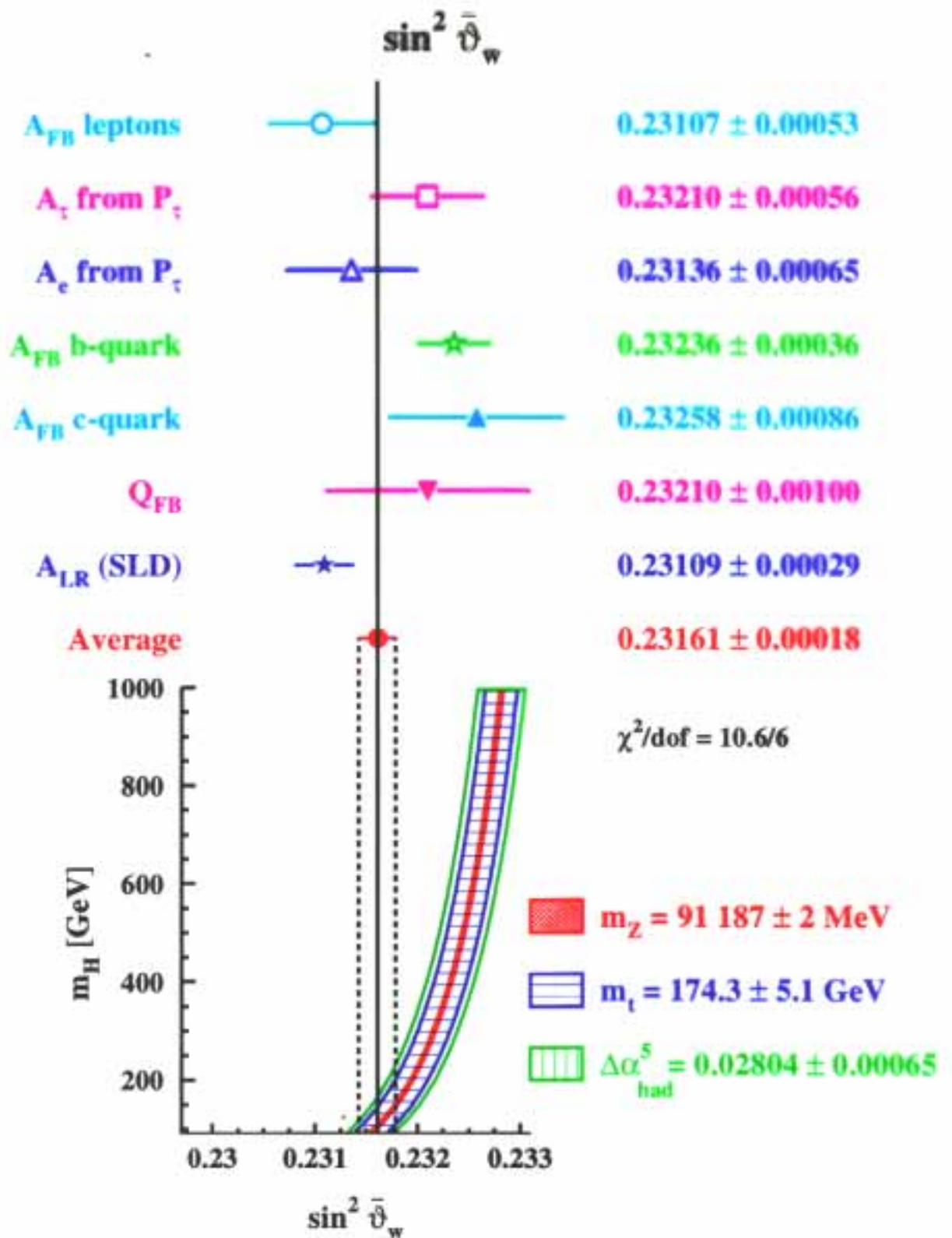
## DELPHI: Forward-backward asymmetry



$$A_{FB}^{0,s} = 0.1008 \pm 0.0113 \pm 0.0040$$

## Effective electroweak mixing angle $\sin^2 \bar{\theta}_W$

### Measurements of the effective electroweak mixing angle

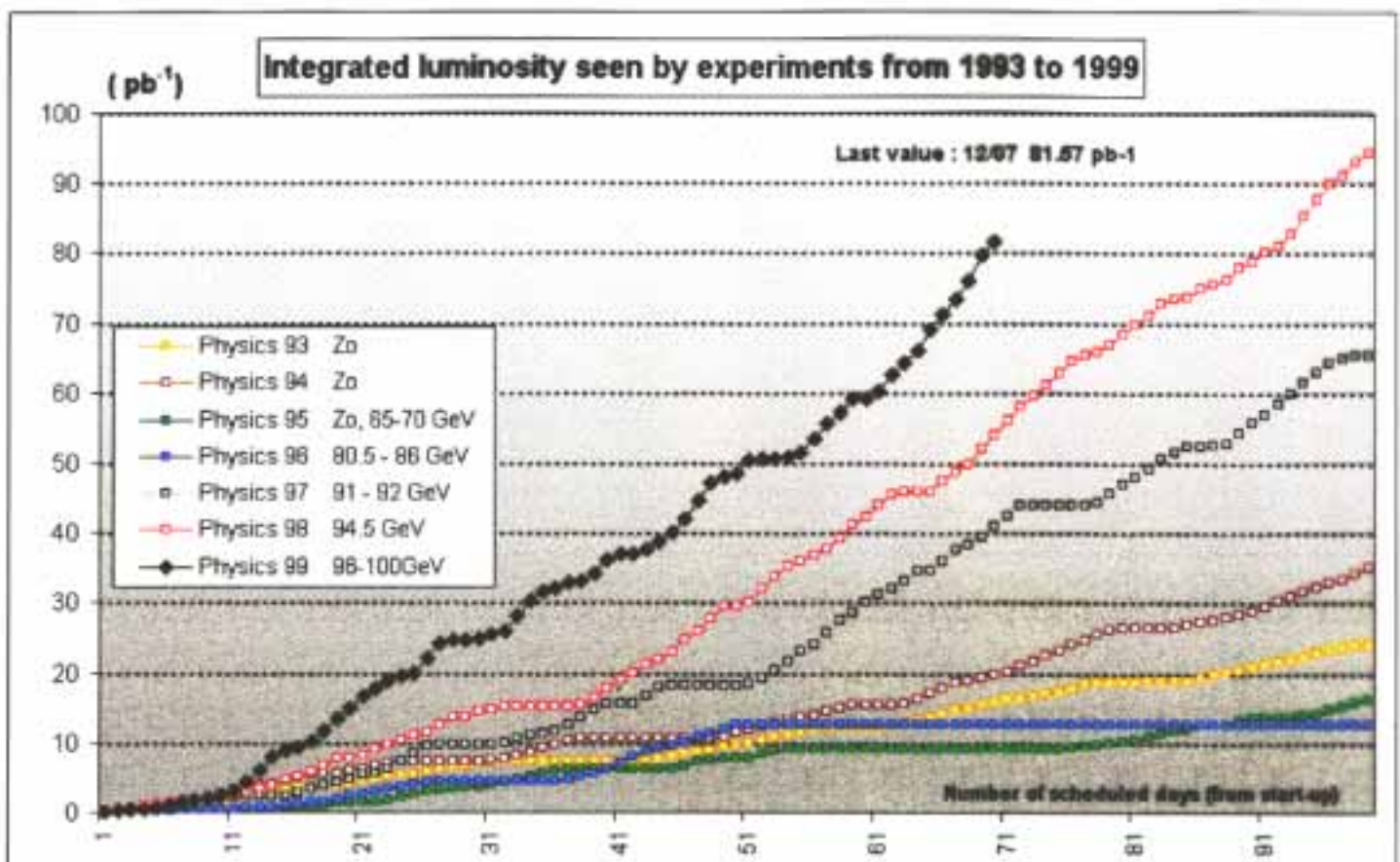


## $e^+e^- \rightarrow f\bar{f}$ above the Z resonance

### • LEP II: Physics above the Z resonance

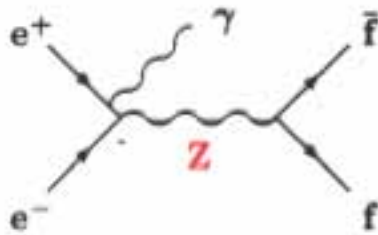
Centre-of-mass energies and approximate luminosities per experiment:

Year	$\sqrt{s}$	$\int \mathcal{L} dt$
1995	130 – 140 GeV	5 pb <sup>-1</sup>
1996	161/172 GeV	21 pb <sup>-1</sup>
1997	183 GeV	55 pb <sup>-1</sup>
	130/136 GeV	7 pb <sup>-1</sup>
1998	189 GeV	180 pb <sup>-1</sup>
1999	192 GeV	27 pb <sup>-1</sup>
	196 GeV	> 20 pb <sup>-1</sup>



$e^+e^- \rightarrow f\bar{f}$  above the Z resonance

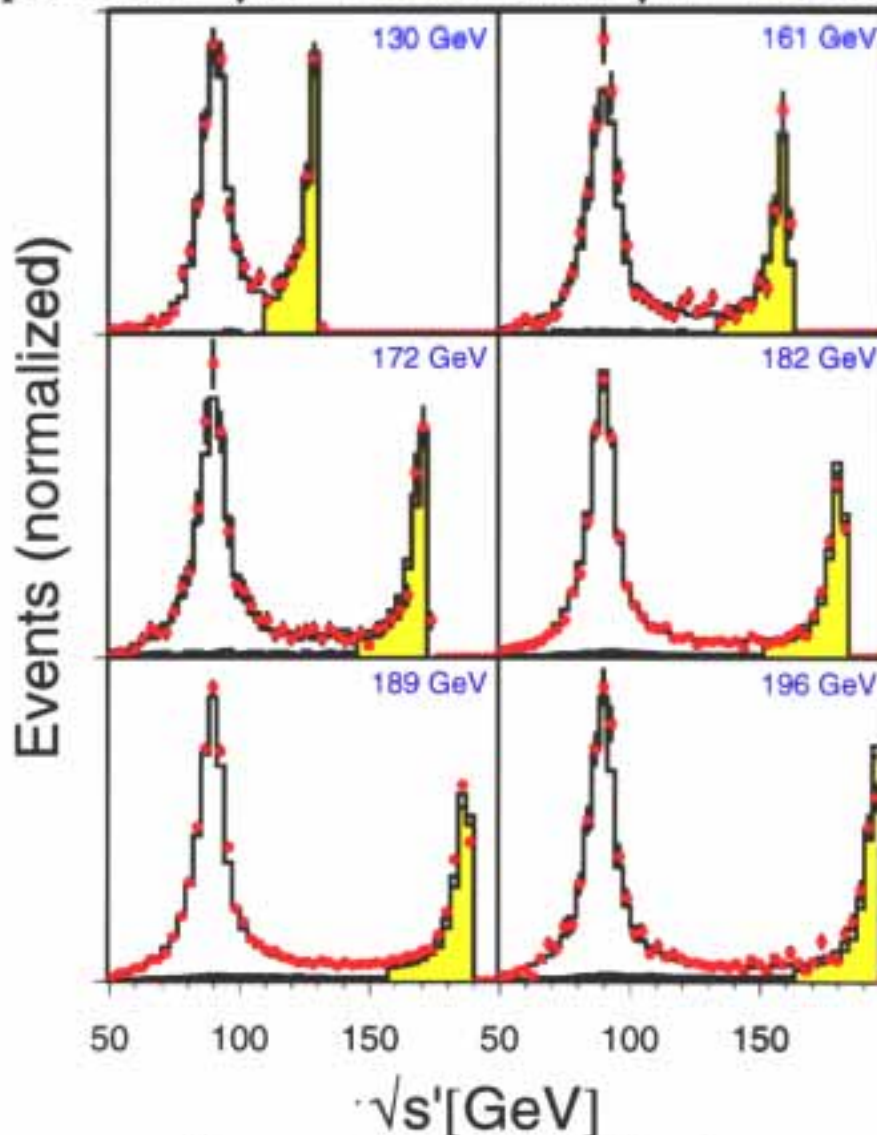
Important contribution from initial state radiation:



'Return-to-the-Z'

Effective cms energy  $\sqrt{s'}$  in  $e^+e^- \rightarrow \text{hadrons}(\gamma)$

Data samples from  $\sqrt{s} = 130 \text{ GeV}$  to  $\sqrt{s} = 196 \text{ GeV}$ :

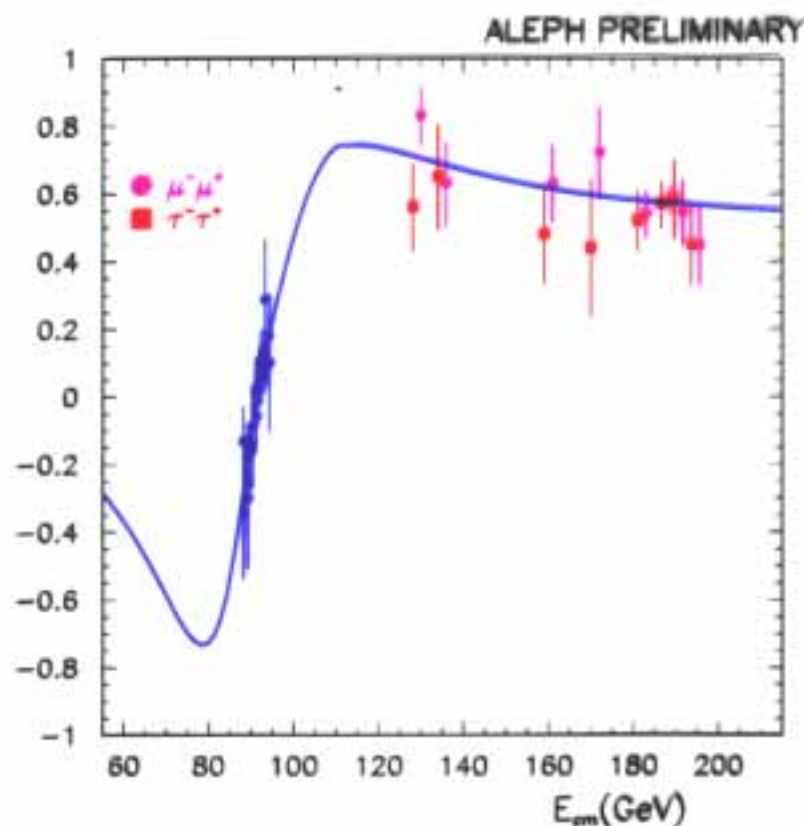


Measure cross sections and asymmetries for

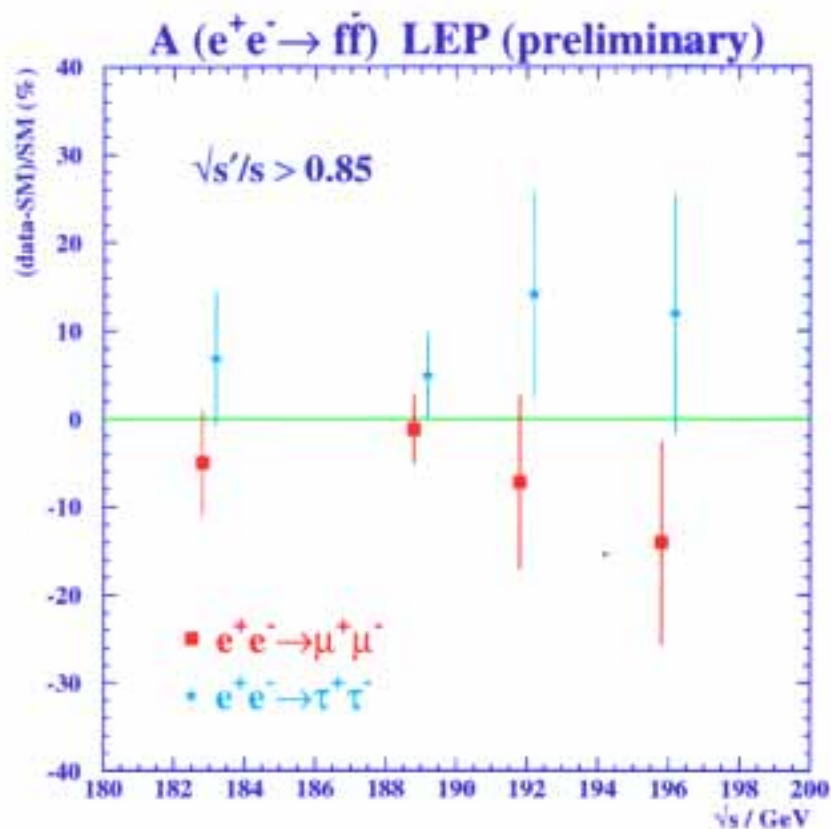
- Inclusive sample
- High energy sample  $\sqrt{s'} > 0.85\sqrt{s}$

# $e^+e^- \rightarrow f\bar{f}$ above the Z resonance

- Leptonic forward-backward asymmetries up to  $\sqrt{s} = 196$  GeV



$\sqrt{s'}/\sqrt{s} > 0.9$

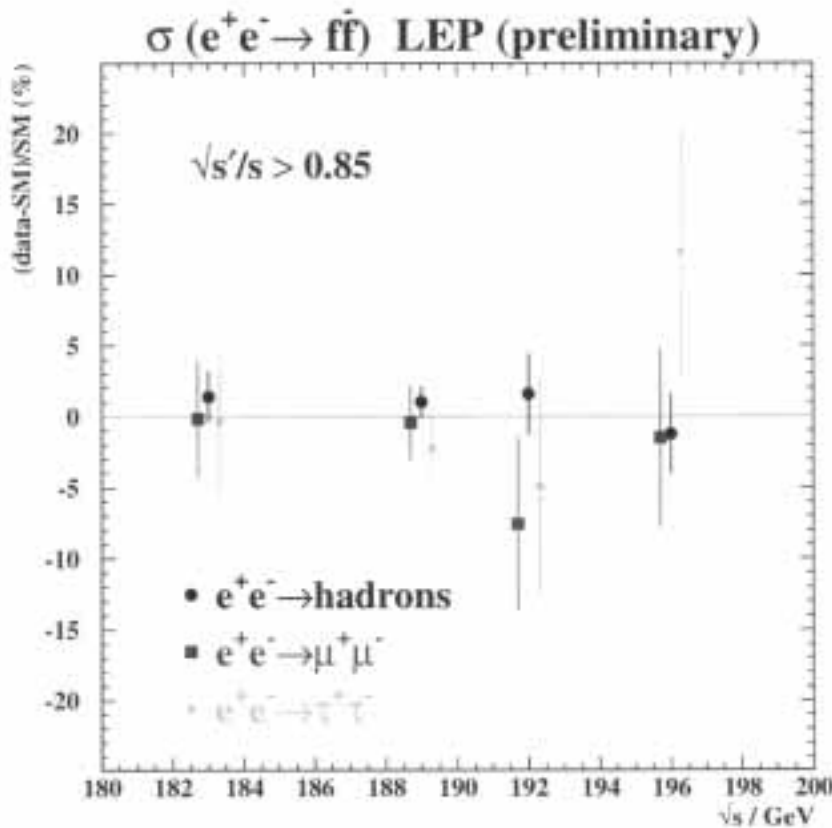
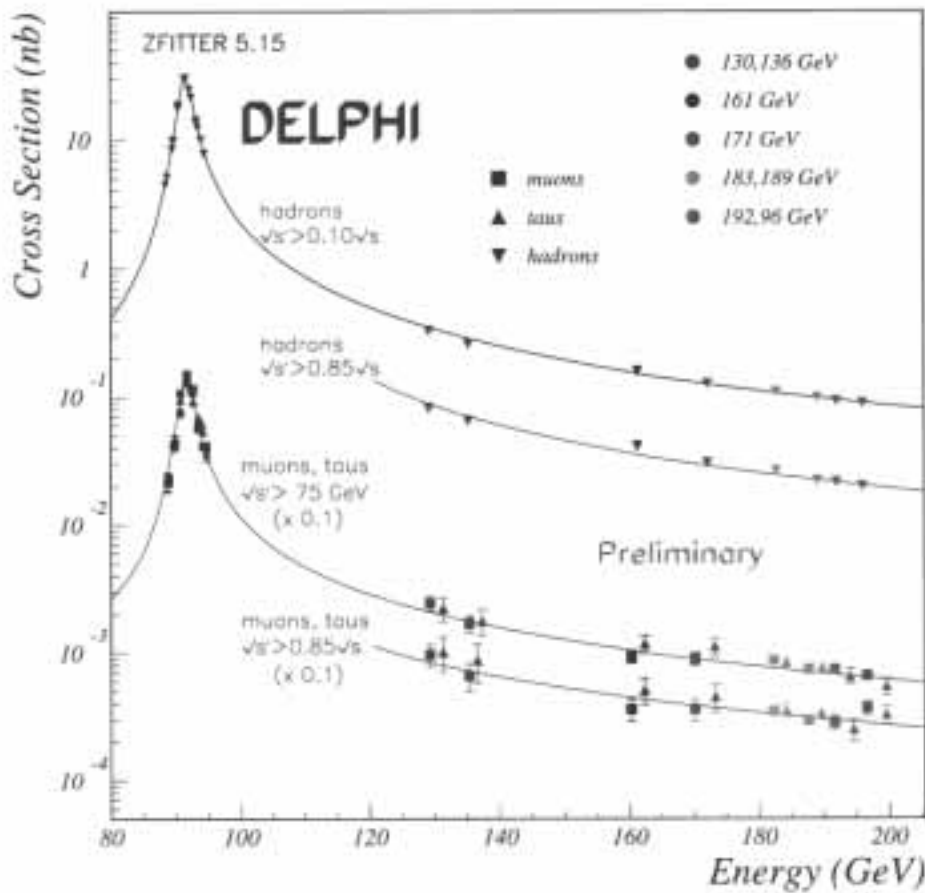


LEP combination  
 $183 \text{ GeV} \leq \sqrt{s} \leq 196 \text{ GeV}$   
(Difference to SM)



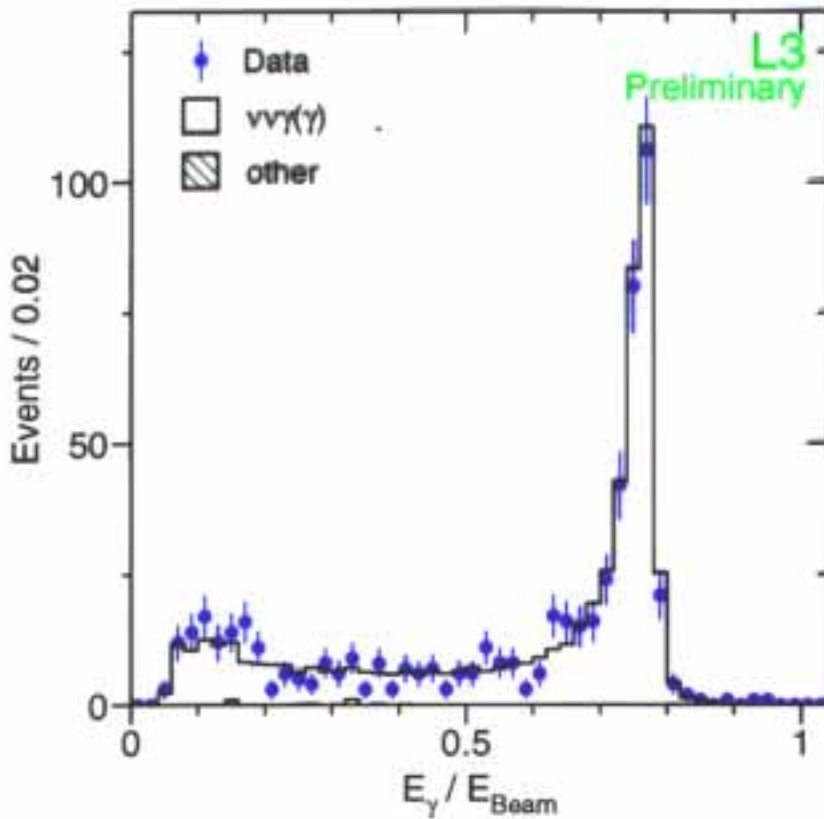
# $e^+e^- \rightarrow f\bar{f}$ above the Z resonance

- Quark- and lepton-pair cross sections up to  $\sqrt{s} = 196$  GeV



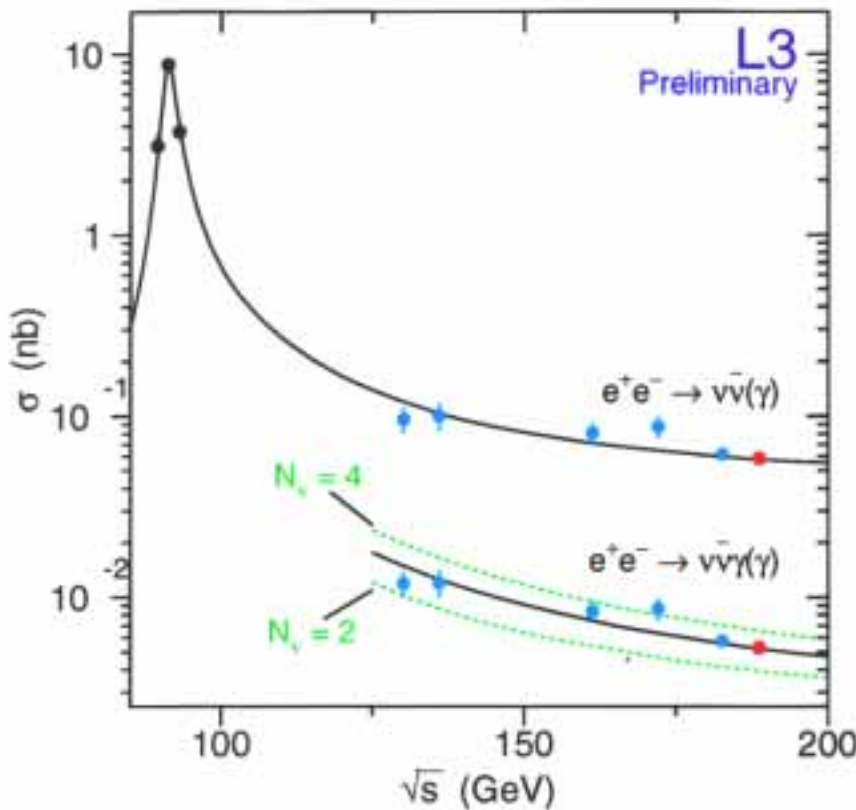
LEP combination  
 $183 \text{ GeV} \leq \sqrt{s} \leq 196 \text{ GeV}$   
 (Difference to SM)

## Cross section $e^+e^- \rightarrow \nu\bar{\nu}$ from single photon events



$\sqrt{s} = 189 \text{ GeV}$   
 $\approx 500$  events per experiment

	$\sigma^{\text{meas}} / \sigma^{\text{SM}}$
ALEPH	$1.017 \pm 0.053$
DELPHI	$0.965 \pm 0.088$
L3	$0.994 \pm 0.044$
OPAL	$0.908 \pm 0.053$



# of neutrino species

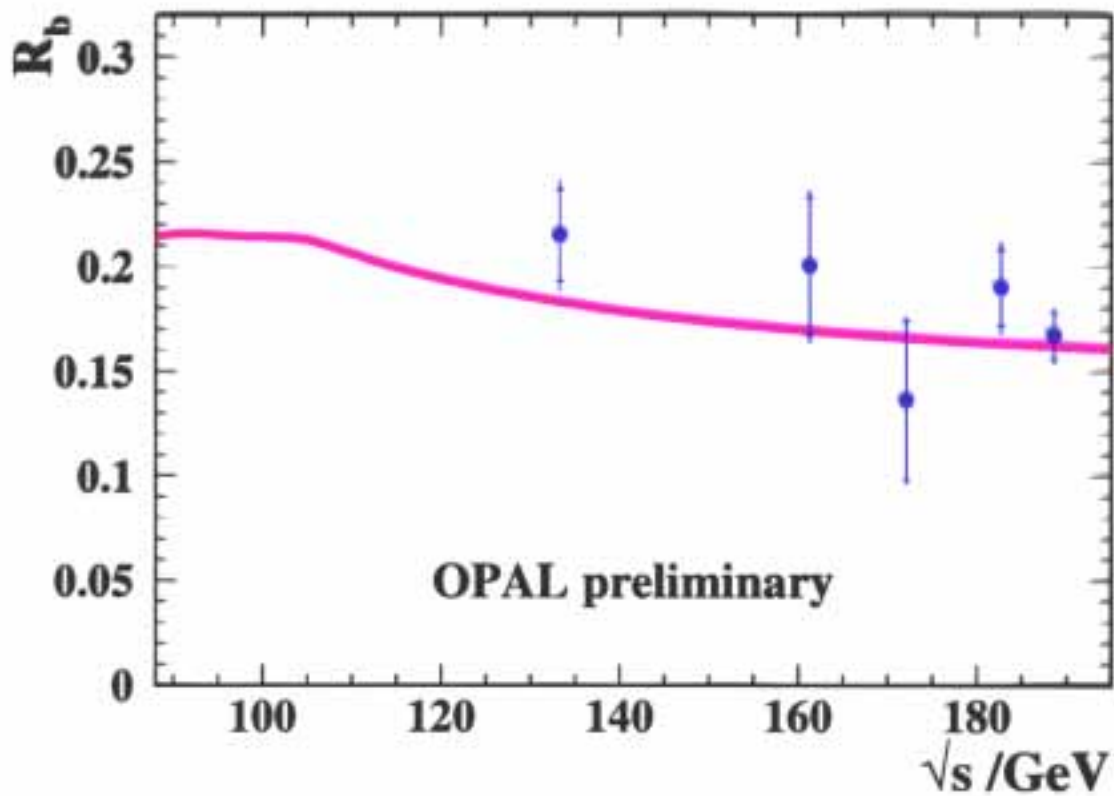
L3	$3.05 \pm 0.12$
DELPHI	$2.83 \pm 0.19$
<b>LEP II</b>	<b><math>2.99 \pm 0.10</math></b>

**LEP I**

single $\gamma$	$3.00 \pm 0.08$
lineshape	$2.9835 \pm 0.0083$

## Production of b- and c-quarks above the Z resonance

- Measurement of  $R_b = \sigma(e^+e^- \rightarrow b\bar{b})/\sigma(e^+e^- \rightarrow q\bar{q})$

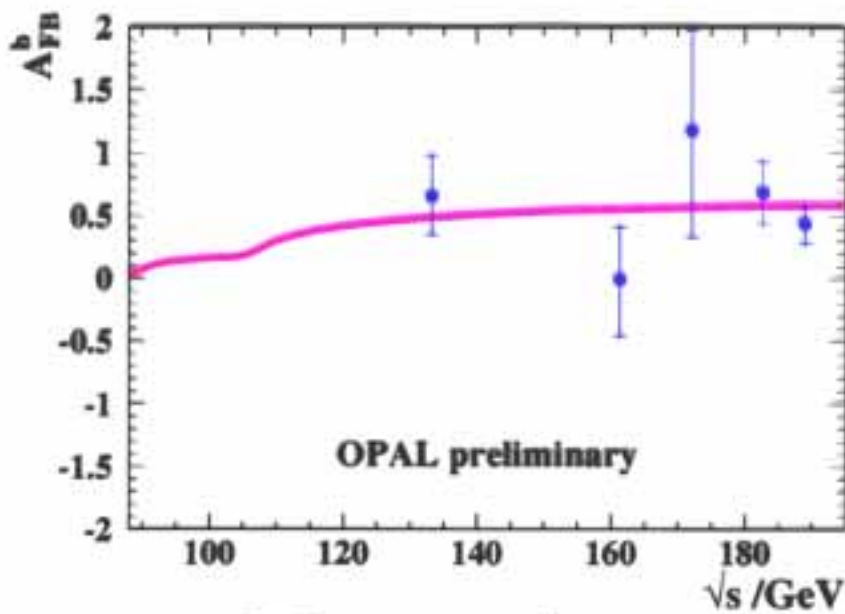


Compilation of measurements at  $\sqrt{s} = 189$  GeV:

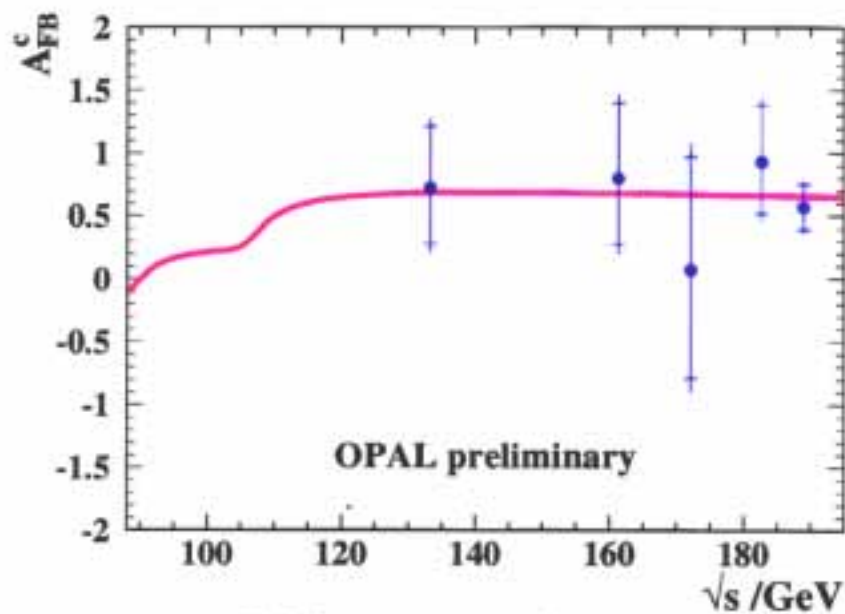
	$R_b$
ALEPH	$0.151 \pm 0.011^{+0.002}_{-0.004}$
DELPHI	$0.167 \pm 0.012$
L3	$0.163 \pm 0.012 \pm 0.010$
OPAL	$0.167 \pm 0.011 \pm 0.008$
LEP	$0.161 \pm 0.007$
SM	0.168

## Production of b- and c-quarks above the Z resonance

- Measurement of forward-backward asymmetries



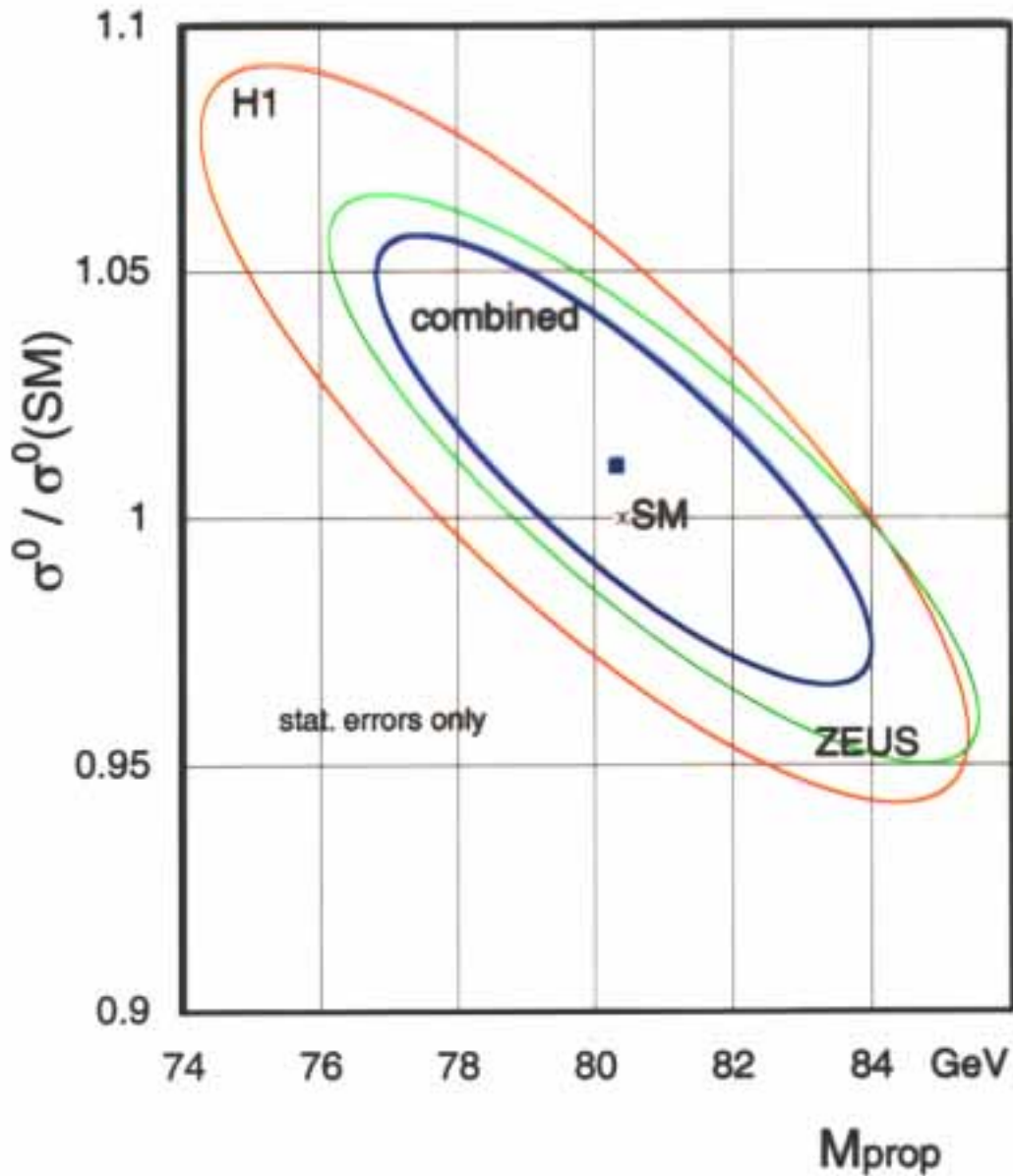
189 GeV	$A_{FB}^b$
ALEPH	$0.34 \pm 0.19 \pm 0.02$
L3	$0.66 \pm 0.23 \pm 0.08$
OPAL	$0.43 \pm 0.15 \pm 0.08$
LEP	$0.44 \pm 0.12$
SM	0.58



189 GeV	$A_{FB}^c$
OPAL	$0.57 \pm 0.18 \pm 0.09$
SM	0.65

## Space-like W exchange

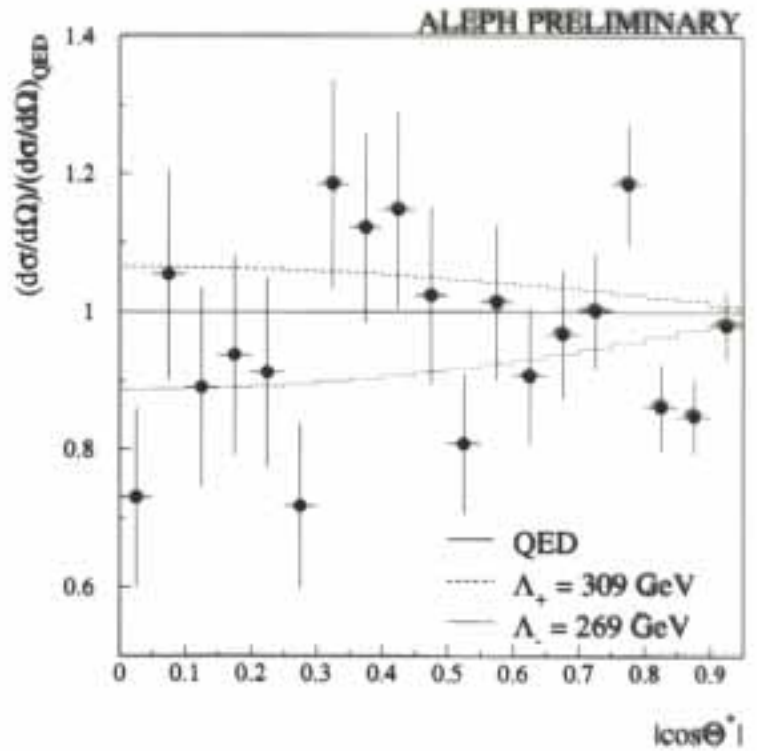
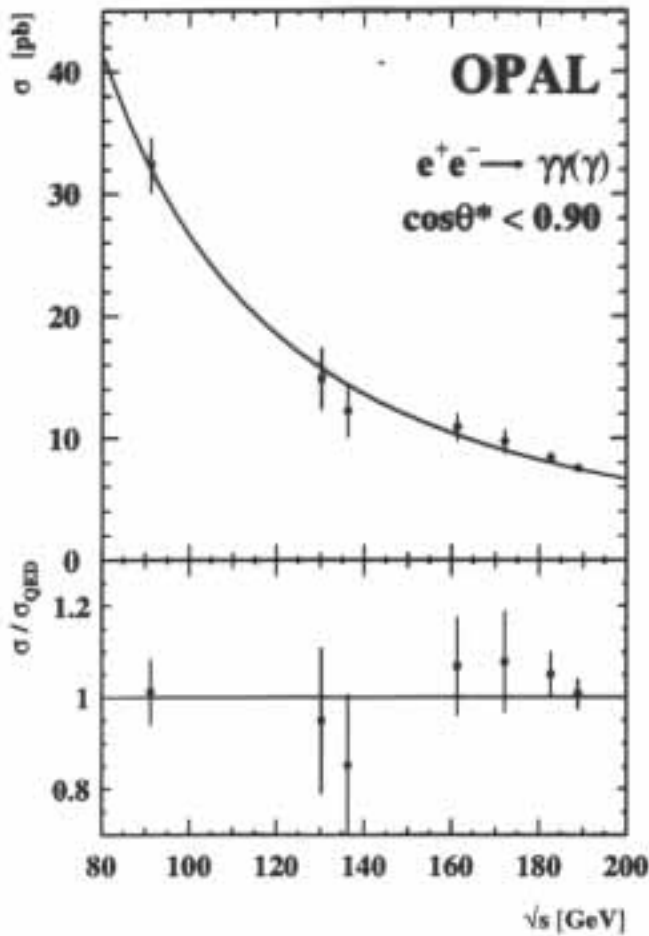
$$\frac{d\sigma}{dQ^2} = \sigma_0 \left( \frac{M_{prop}^2}{M_{prop}^2 + Q^2} \right)^2 \Phi W$$



$$\begin{aligned} \text{H1 : } M_{\text{prop}} &= 80.9 \pm 3.3 \pm 1.7 \pm 3.7 \text{ GeV} \\ \text{ZEUS : } M_{\text{prop}} &= 81.4^{+2.7}_{-2.6} \pm 2.0^{+3.3}_{-3.0} \text{ GeV} \end{aligned}$$

## Production of neutral boson pairs

- Test of QED in  $e^+e^- \rightarrow \gamma\gamma(\gamma)$



Lower limits on QED cut-off parameter

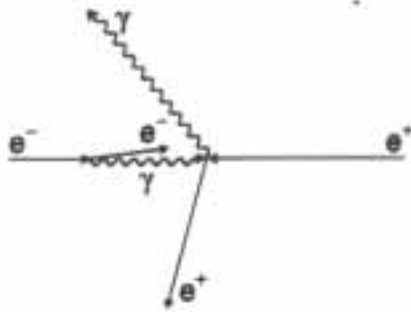
$$\left(\frac{d\sigma}{d\Omega}\right)_{\Lambda_{\pm}} = \left(\frac{d\sigma}{d\Omega}\right)_{\text{Born}} + \frac{\alpha^2 s}{2\Lambda_{\pm}^4} (1 + \cos^2\theta)$$

and mass of excited electrons  $m_{e^*}$  for equal  $e^*e\gamma$  and  $ee\gamma$  couplings (189 GeV data)

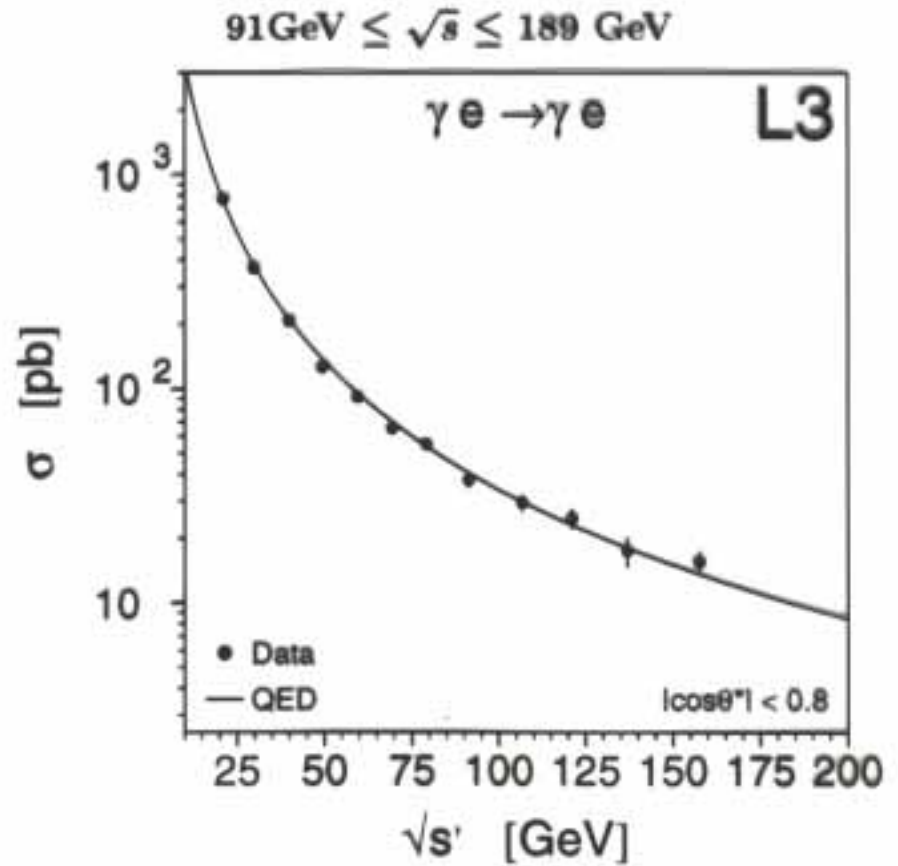
	$\Lambda_+$	$\Lambda_-$	$m_{e^*}$ [GeV]
ALEPH	309	269	335
DELPHI	284	278	262
L3	289	291	292
OPAL	304	295	306

## Electron-boson scattering at LEP

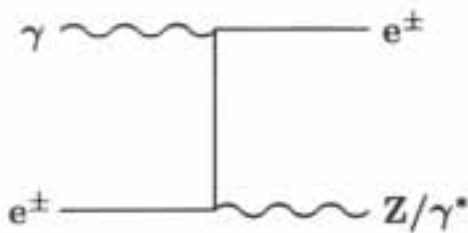
- Compton scattering  $e^\pm \gamma \rightarrow e^\pm \gamma$



6000 events  
 $\sqrt{s'} \leq 160$  GeV

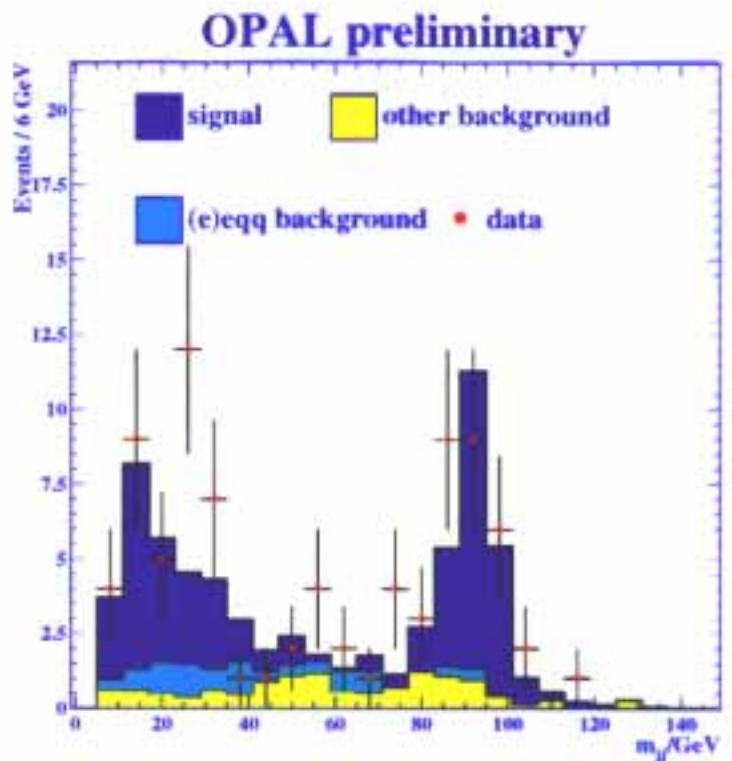


- Electroweak Compton scattering  $e^\pm \gamma \rightarrow e^\pm Z/\gamma^*$



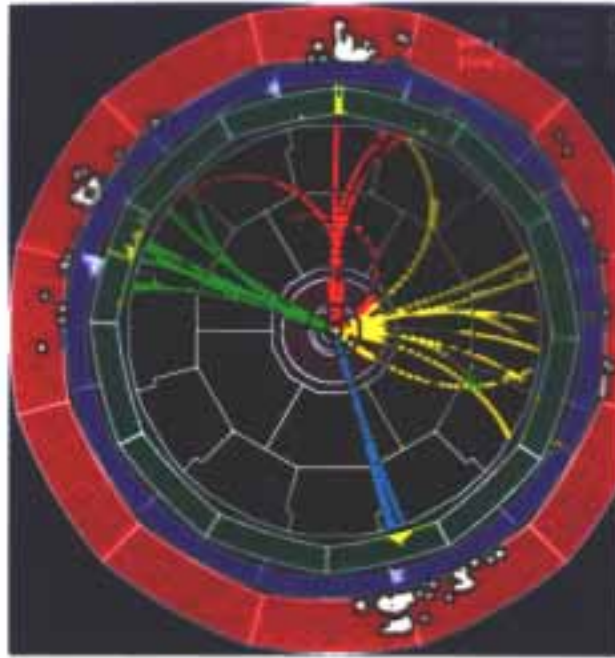
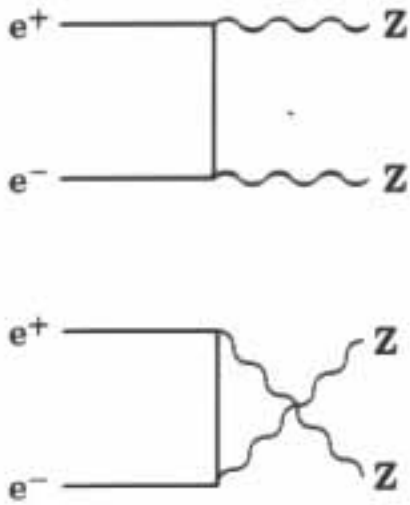
OPAL:  $Z/\gamma^* \rightarrow$  hadrons  
 2 jets and isolated electron

$m_{jj}$ [GeV]	5 – 60	> 60
	$\gamma^*e$	$Ze$
data	52	38
$\sigma$ [pb]	$4.6 \pm 0.9$	$1.5 \pm 0.3$
$\sigma^{\text{SM}}$ [pb]	3.06	1.19

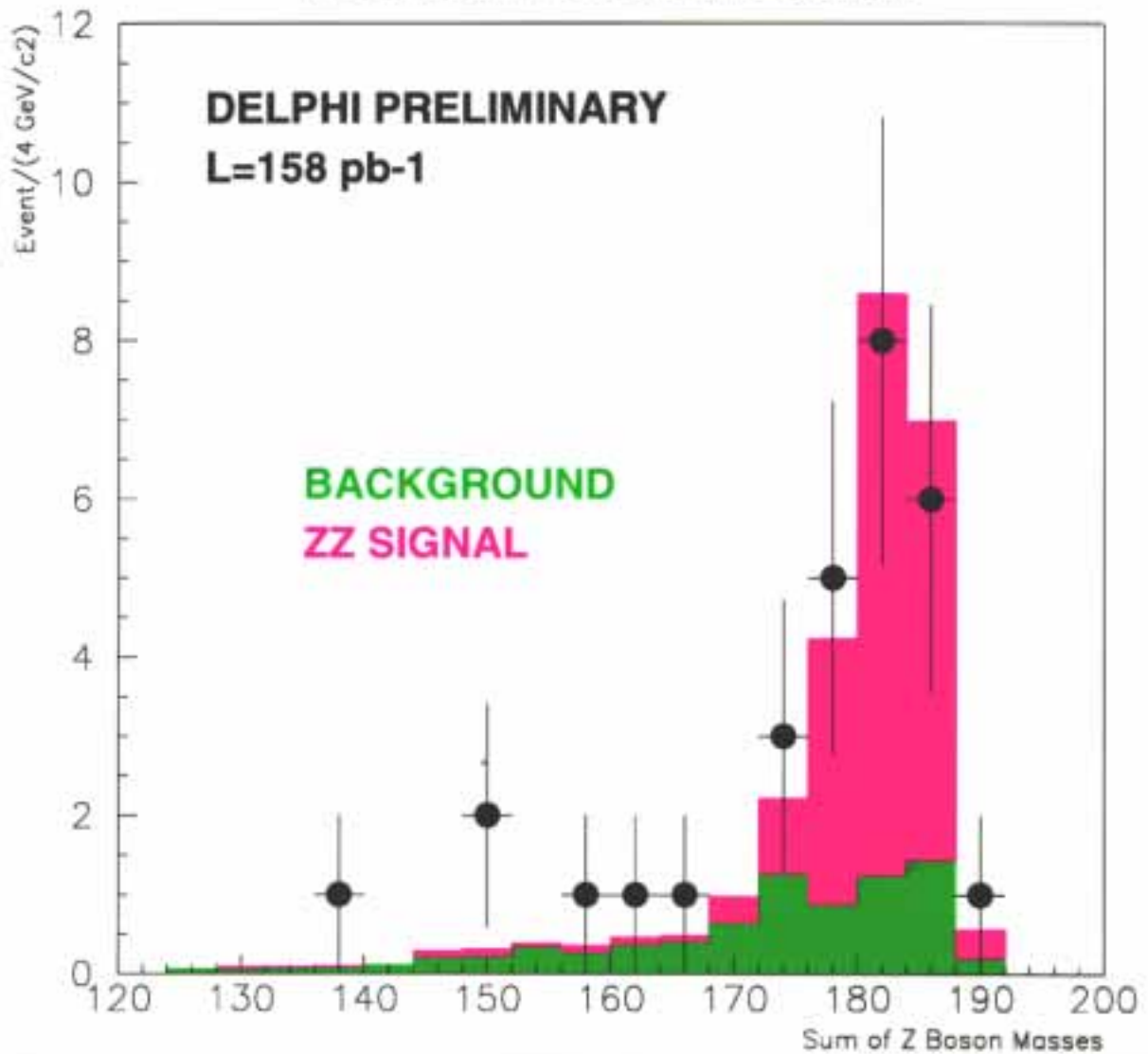


# Production of Z-boson pairs

## Signal definition



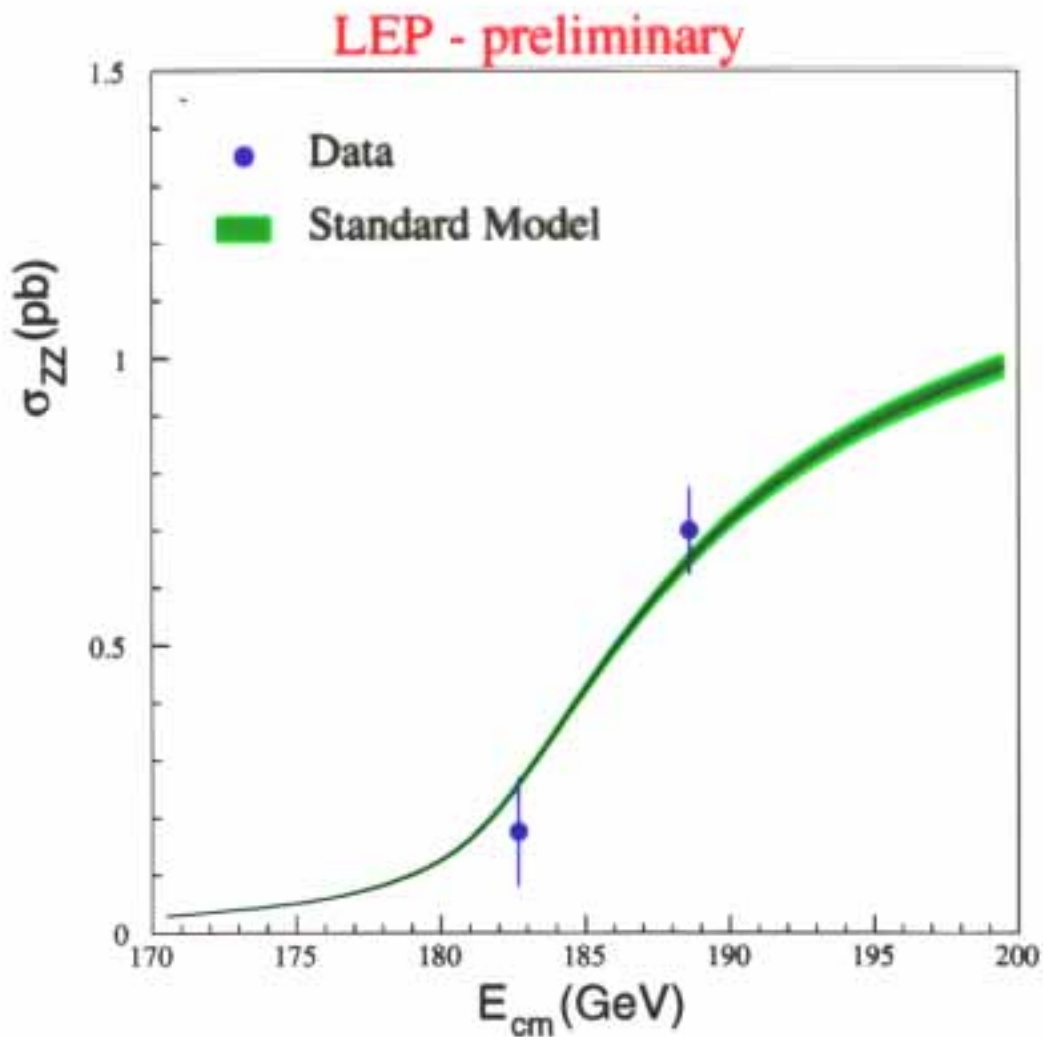
## ZZ MASS RECONSTRUCTION





## Cross section $e^+e^- \rightarrow ZZ$

- Combined LEP cross sections



- $e^+e^- \rightarrow ZZ$  probes  $ZZZ$  and  $ZZ\gamma$  vertices



4 coupling parameter  $f_i^V$ ;  $V = \gamma, Z$   
 $i = 4$  CP violating  
 $i = 5$  C & P violating

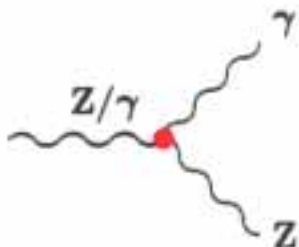
Typical limits:

$$|f_4^Z| < 2 \quad |f_4^\gamma| < 1$$

$$|f_5^Z| < 5 \quad |f_5^\gamma| < 3$$

## Testing the Z and $\gamma$ couplings

- $e^+e^- \rightarrow Z/\gamma \rightarrow f\bar{f}\gamma$  probes ZZ $\gamma$  and Z $\gamma\gamma$  vertices



8 coupling parameter  $h_i^V$ ;  $V = \gamma, Z$

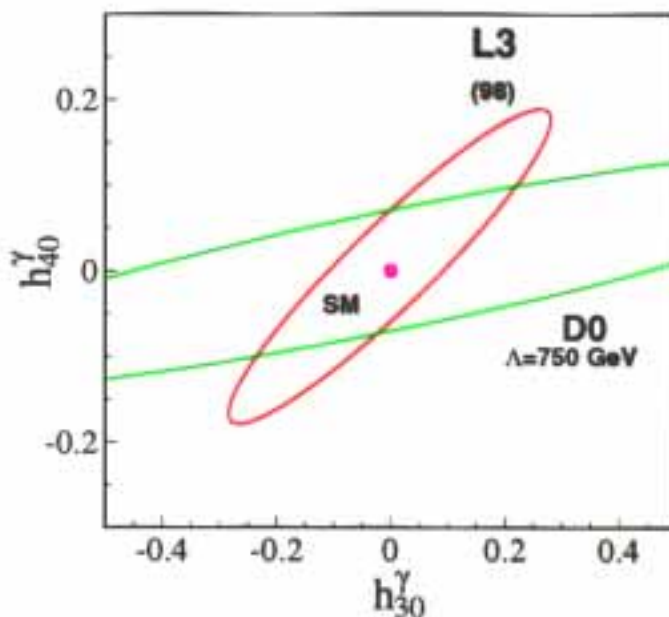
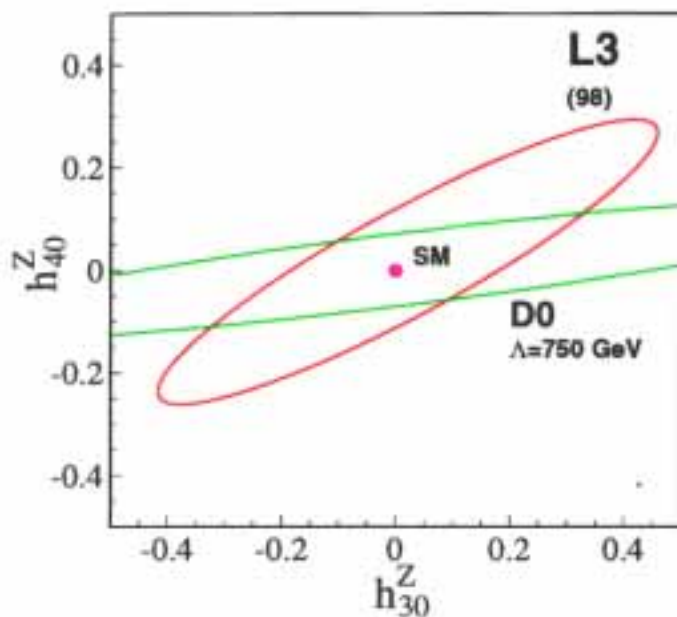
$i = 1, 2$  CP violating

$i = 3, 4$  CP conserving

Study of rate and differential distributions in  $e^+e^- \rightarrow q\bar{q}\gamma$  and  $e^+e^- \rightarrow \nu\bar{\nu}\gamma$  events

- Z $\gamma$  production at the Tevatron:

study of  $p\bar{p} \rightarrow e^+e^-\gamma, \mu^+\mu^-\gamma$  events (D $\emptyset$ )



•  $e^+e^- \rightarrow ZZ$

DELPHI:

$$\begin{aligned} -2.67 < f_4^Z < +2.67 & \quad -1.59 < f_4^\gamma < +1.58 \\ -7.09 < f_5^Z < +5.71 & \quad -3.90 < f_5^\gamma < +3.87 \end{aligned}$$

L3:

$$\begin{aligned} -1.9 < f_4^Z < +1.9 & \quad -1.1 < f_4^\gamma < +1.1 \\ -4.9 < f_5^Z < +4.7 & \quad -3.0 < f_5^\gamma < +2.9 \end{aligned}$$

OPAL:

$$\begin{aligned} -2.0 < \Re\{f_4^Z\} < +2.0 & \quad -1.2 < \Re\{f_4^\gamma\} < +1.2 \\ -5.1 < \Re\{f_5^Z\} < +5.1 & \quad -3.2 < \Re\{f_5^\gamma\} < +3.0 \\ -2.0 < \Im\{f_4^Z\} < +1.9 & \quad -1.2 < \Im\{f_4^\gamma\} < +1.2 \\ -5.2 < \Im\{f_5^Z\} < +5.4 & \quad -3.2 < \Im\{f_5^\gamma\} < +3.0 \end{aligned}$$

•  $e^+e^- \rightarrow q\bar{q}\gamma$  and  $e^+e^- \rightarrow \nu\bar{\nu}\gamma$

DELPHI ( $e^+e^- \rightarrow q\bar{q}\gamma$  only):

$$|h_{30}^Z| < 0.38 \quad |h_{30}^\gamma| < 0.23 \quad (\Lambda = 1000 \text{ GeV})$$

L3:

$$\begin{aligned} -0.09 < h_1^Z < 0.20 & \quad -0.09 < h_1^\gamma < 0.08 \\ -0.12 < h_2^Z < 0.06 & \quad -0.05 < h_2^\gamma < 0.07 \\ -0.16 < h_3^Z < 0.15 & \quad -0.09 < h_3^\gamma < 0.07 \\ -0.09 < h_4^Z < 0.10 & \quad -0.05 < h_4^\gamma < 0.06 \end{aligned}$$

•  $Z\gamma$  production at the Tevatron

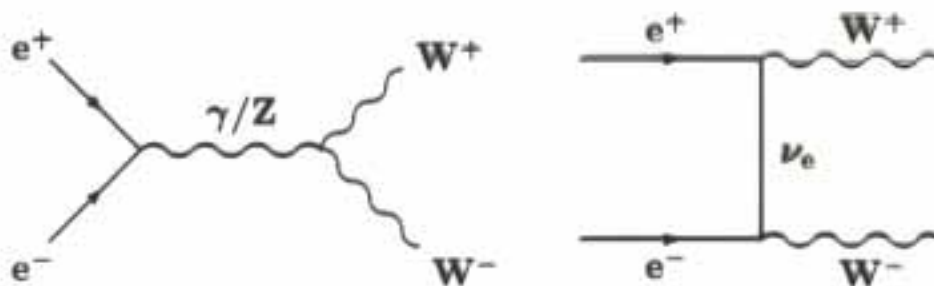
DØ:

$$\begin{aligned} |h_{30}^Z| < 0.36 & \quad |h_{30}^\gamma| < 0.37 \\ |h_{40}^Z| < 0.05 & \quad |h_{40}^\gamma| < 0.05 \quad (\Lambda = 750 \text{ GeV}) \end{aligned}$$

$$h_i^V = \frac{h_{i0}^V}{\left(1 + \frac{s}{\Lambda^2}\right)^3} \quad i = 1, 3 \quad \quad h_i^V = \frac{h_{i0}^V}{\left(1 + \frac{s}{\Lambda^2}\right)^4} \quad i = 2, 4$$

## Production of W bosons at LEP

- W-pair production at LEP  $e^+e^- \rightarrow W^+W^-(\gamma)$ :



Event samples (per experiment):

161 GeV  $\leq \sqrt{s} \leq$  189 GeV  $\approx$  3500

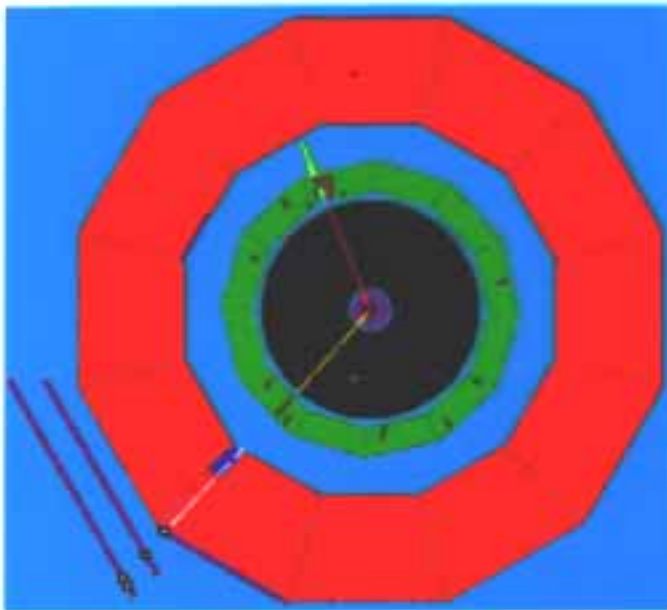
192 GeV  $\leq \sqrt{s} \leq$  196 GeV  $\approx$  1000

Three different event topologies:

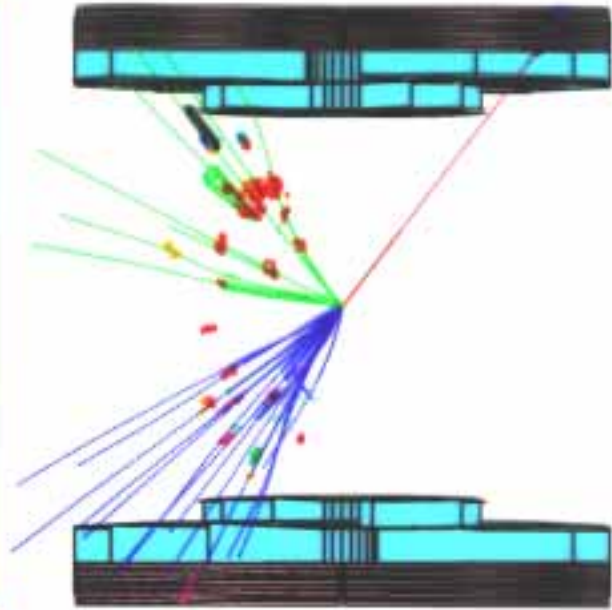
- $W^+W^- \rightarrow \ell\nu\ell\nu$ ,  $\ell = e, \mu, \tau$  ( $\approx$  11%)  
two energetic, acoplanar leptons
- $W^+W^- \rightarrow q\bar{q}\ell\nu$  ( $\approx$  44%)  
two jets plus isolated energetic lepton  
or jet for  $W^+W^- \rightarrow q\bar{q}\tau\nu$
- $W^+W^- \rightarrow q\bar{q}q\bar{q}$  ( $\approx$  46%)  
four jets of similar energy  
severe background from QCD:  
 $e^+e^- \rightarrow q\bar{q} + \text{gluons}$  ( $\approx$  100 pb)  
neural networks, likelihood analyses

$e^+e^- \rightarrow W^+W^-$  candidates at  $\sqrt{s} = 189$  GeV

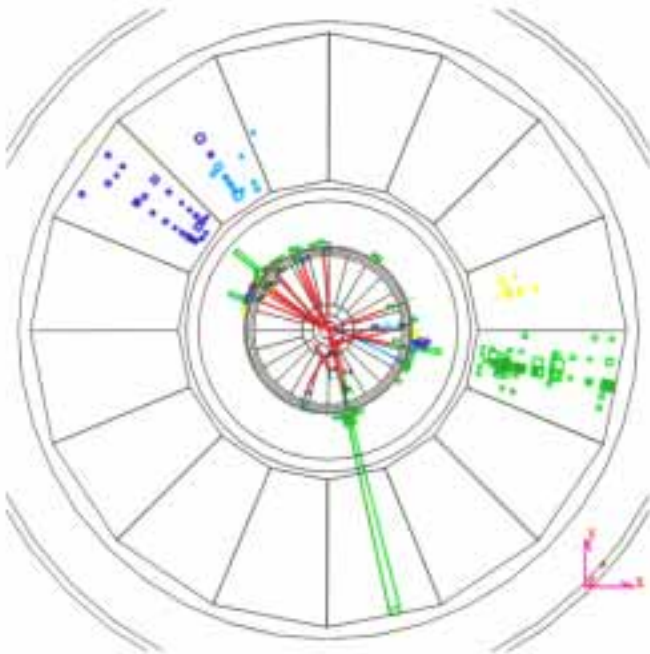
$e^+e^- \rightarrow \nu\bar{\nu}\nu\bar{\nu}$



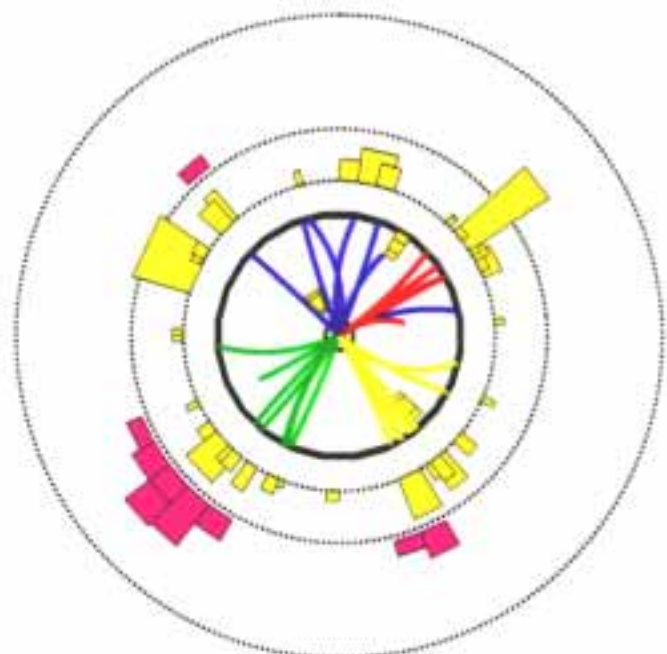
$e^+e^- \rightarrow q\bar{q}\mu\nu$



$e^+e^- \rightarrow q\bar{q}e\nu$

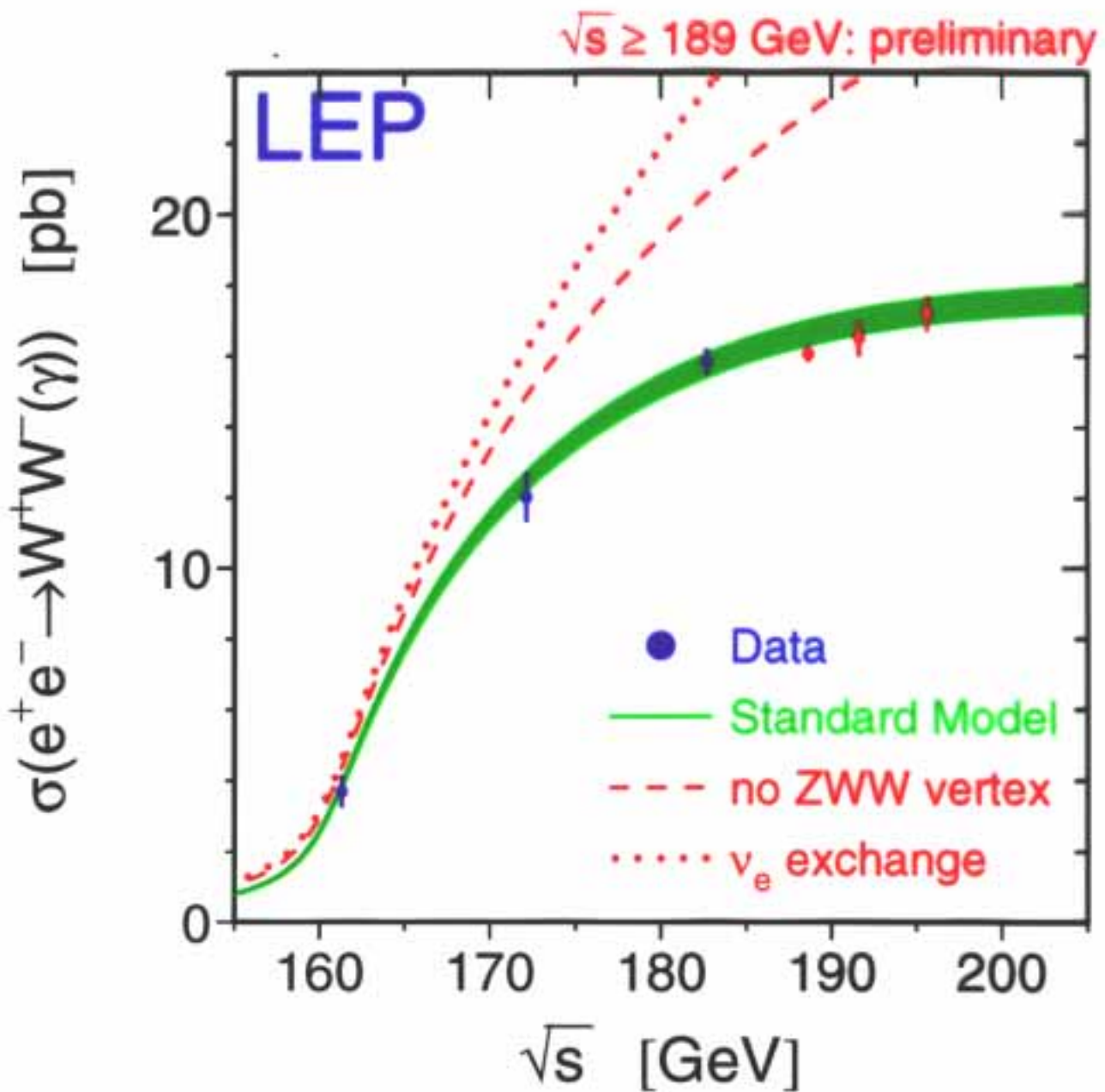


$e^+e^- \rightarrow q\bar{q}q\bar{q}$



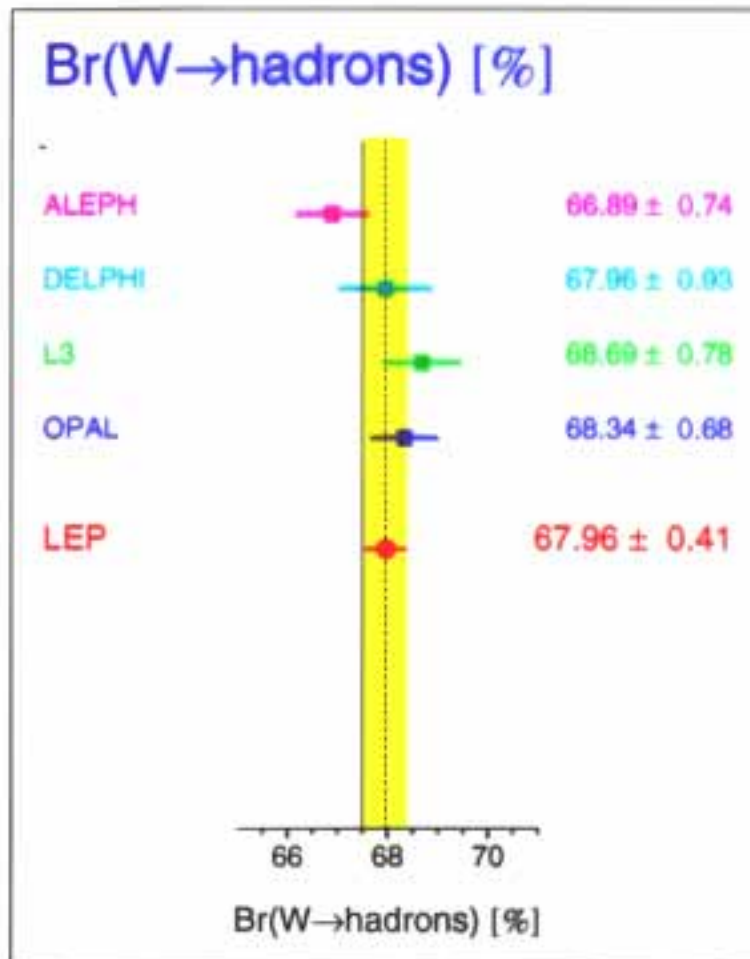
## W-pair production cross section

Combined LEP cross section measurement  $e^+e^- \rightarrow WW$  for  $161 \text{ GeV} \leq \sqrt{s} \leq 196 \text{ GeV}$



- Very good agreement with SM  
2% theoretical error
- ZWW vertex exist

## Hadronic W branching ratio



### Determination of $|V_{cs}|$

- indirectly from hadronic branching ratio

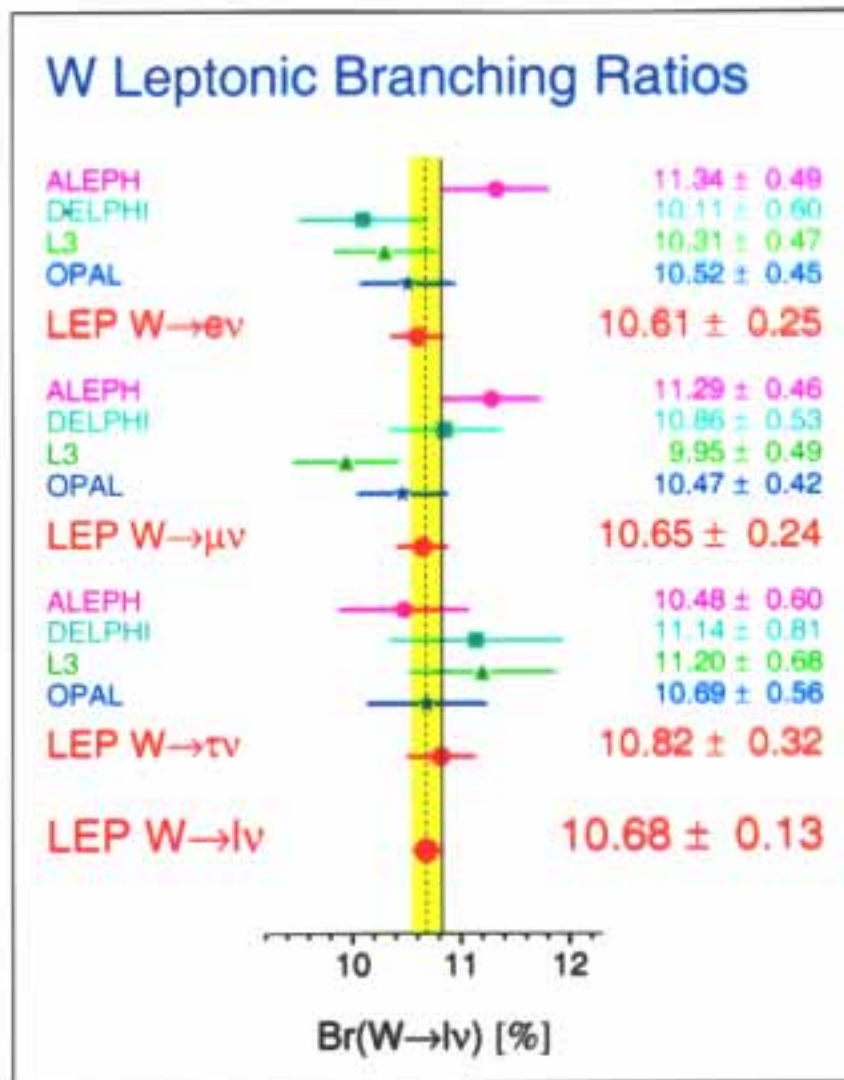
$$\frac{BR_{\text{had}}}{1 - BR_{\text{had}}} = \sum_{\substack{i=u,c \\ j=d,s,b}} |V_{ij}|^2 \left(1 + \frac{\alpha_s}{\pi}\right)$$

**LEP:  $|V_{cs}| = 0.997 \pm 0.020$**

- directly by charm tagging (189 GeV)

	$\Gamma(W \rightarrow cX)/\Gamma(W \rightarrow \text{had})$	$ V_{cs} $
ALEPH	$0.51 \pm 0.05 \pm 0.03$	$1.00 \pm 0.11 \pm 0.07$
OPAL	$0.47 \pm 0.04 \pm 0.06$	$0.91 \pm 0.07 \pm 0.11$

## Leptonic W branching ratios



Charged current lepton universality ( $Q^2 = m_W^2$ ):

$$g_\mu/g_e = 1.001 \pm 0.016$$

$$g_\tau/g_e = 1.010 \pm 0.022$$

$$g_\tau/g_\mu = 1.008 \pm 0.021$$

$$\text{CDF} : BR(W \rightarrow e\nu) = 0.1037 \pm 0.0022$$

$$\text{D}\emptyset : BR(W \rightarrow e\nu) = 0.1080 \pm 0.0030$$

$$\text{D}\emptyset : g_\tau/g_e = 0.98 \pm 0.03$$



## Charged current lepton universality in $\tau$ decays

- Measurements of tau leptonic branching fractions:

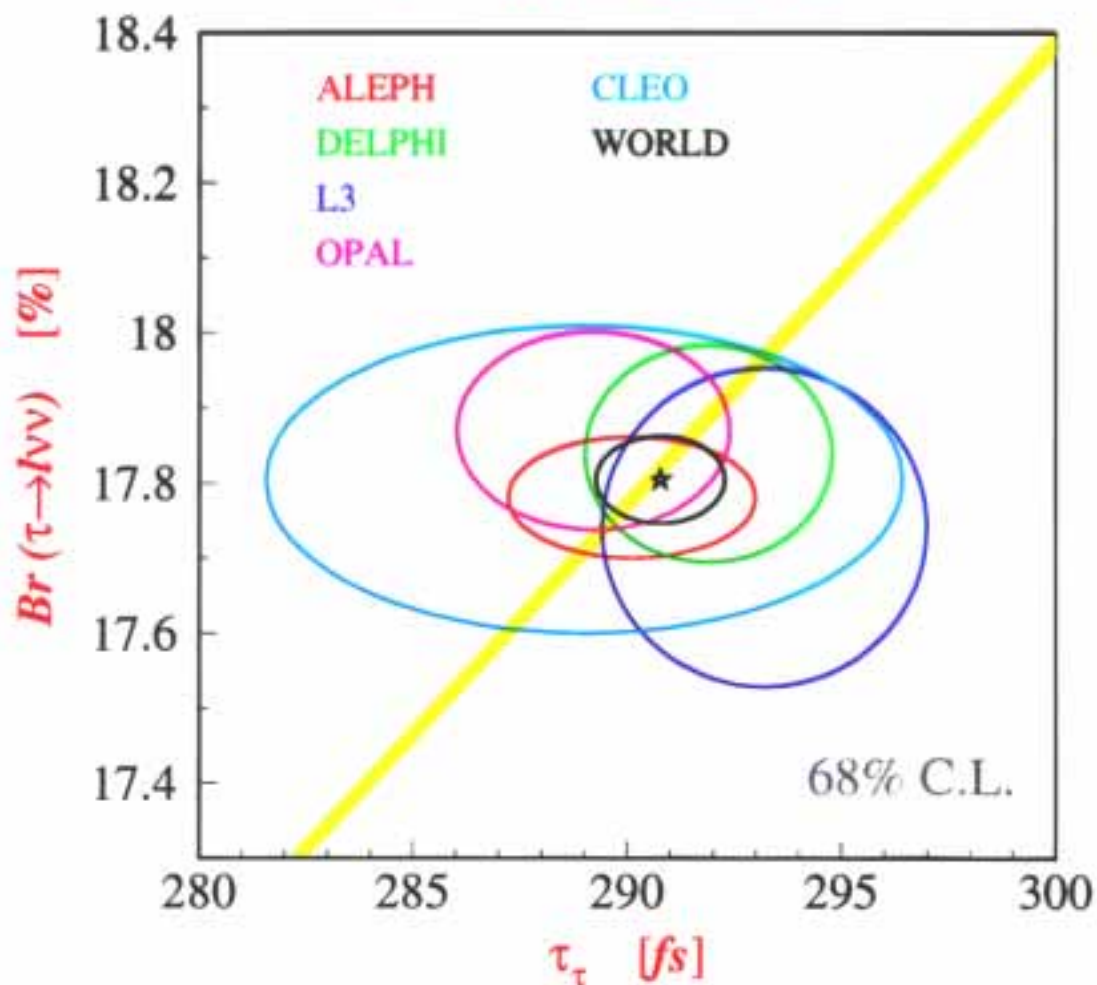
$$BR(\tau \rightarrow e \nu_e \nu_\tau) = (17.791 \pm 0.054)\%$$

$$BR(\tau \rightarrow \mu \nu_\mu \nu_\tau) = (17.333 \pm 0.054)\%$$

$$\Rightarrow BR(\tau \rightarrow \ell \nu_\ell \nu_\tau) = (17.805 \pm 0.039)\% \quad (\text{massless } \ell)$$

- Tau lifetime:

$$\tau_\tau = 290.77 \pm 0.99 \text{ fs}$$



Universality of couplings ( $Q^2 = m_\tau^2$ ):

$$g_\mu/g_e = 1.0006 \pm 0.0023$$

$$g_\tau/g_\mu = 0.9997 \pm 0.0024$$

## Couplings of the W boson

---

### Triple gauge boson vertices $\gamma WW$ and $ZWW$



Most general Lorentz invariant ansatz:  
 $2 \times 7$  complex couplings

Assume real couplings,  
C-, P- and CP invariance,  
charge of  $W^\pm (= \pm e)$   
no change of tree-level boson  
propagators

$\Rightarrow$  3 coupling parameter to be studied:

$$g_1^Z, \kappa_\gamma, \lambda_\gamma$$

SM values:

$$g_1^Z = 1, \quad \kappa_\gamma = 1, \quad \lambda_\gamma = 0$$

Deviations from Standard Model would

- at LEP

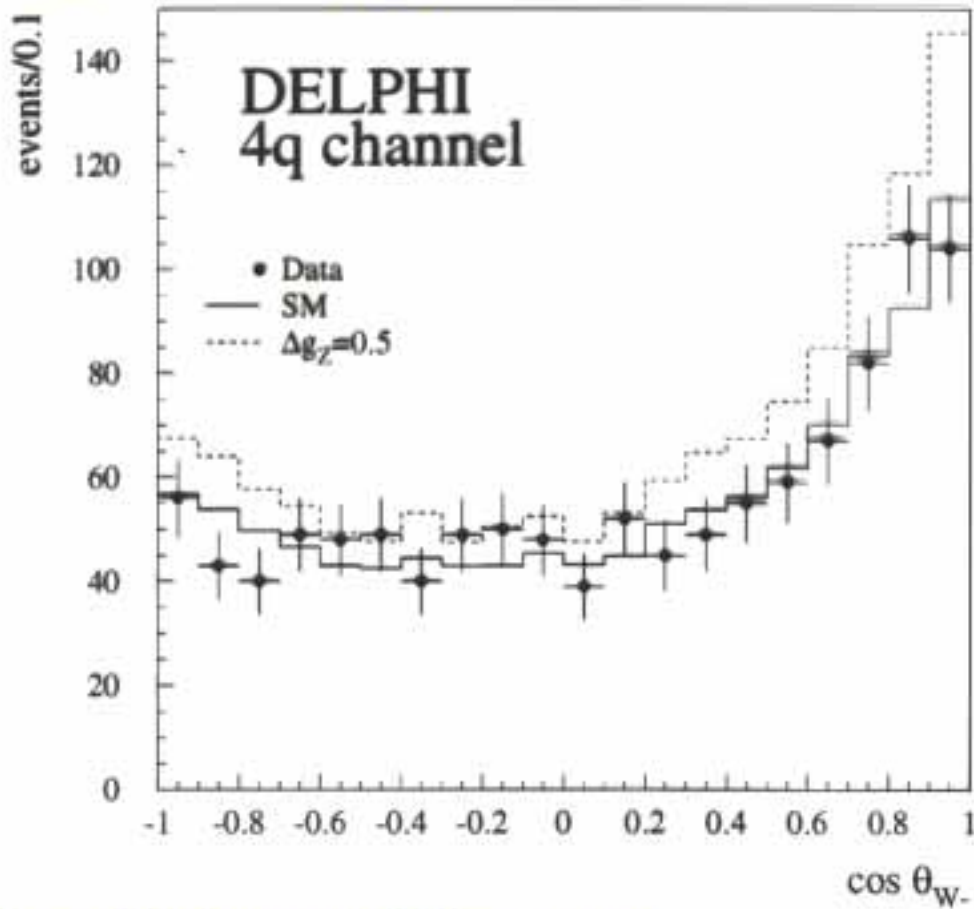
- increase  $e^+e^- \rightarrow WW$  cross section
- modify W production angles
- modify W polarization

- at Tevatron

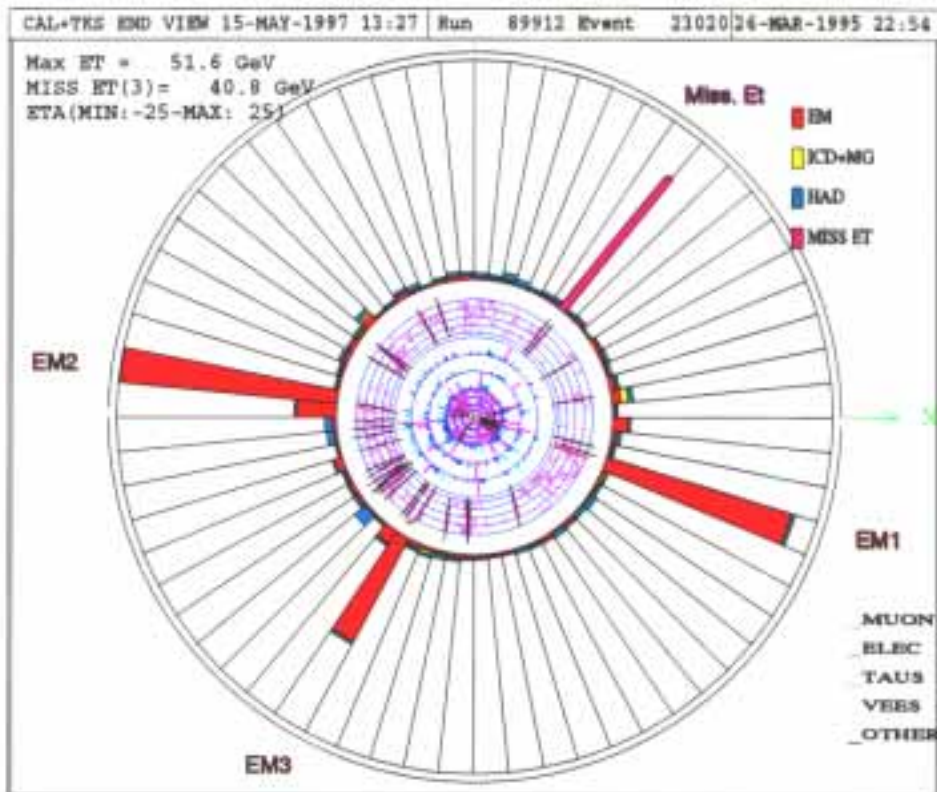
- enhanced boson pair production  $W\gamma, WW, WZ$

# Signature of anomalous triple boson couplings

## • $\cos \Theta_W$ in $WW \rightarrow q\bar{q}q\bar{q}$ events



## • $D\bar{D}$ candidate event $ZW \rightarrow eee\nu$



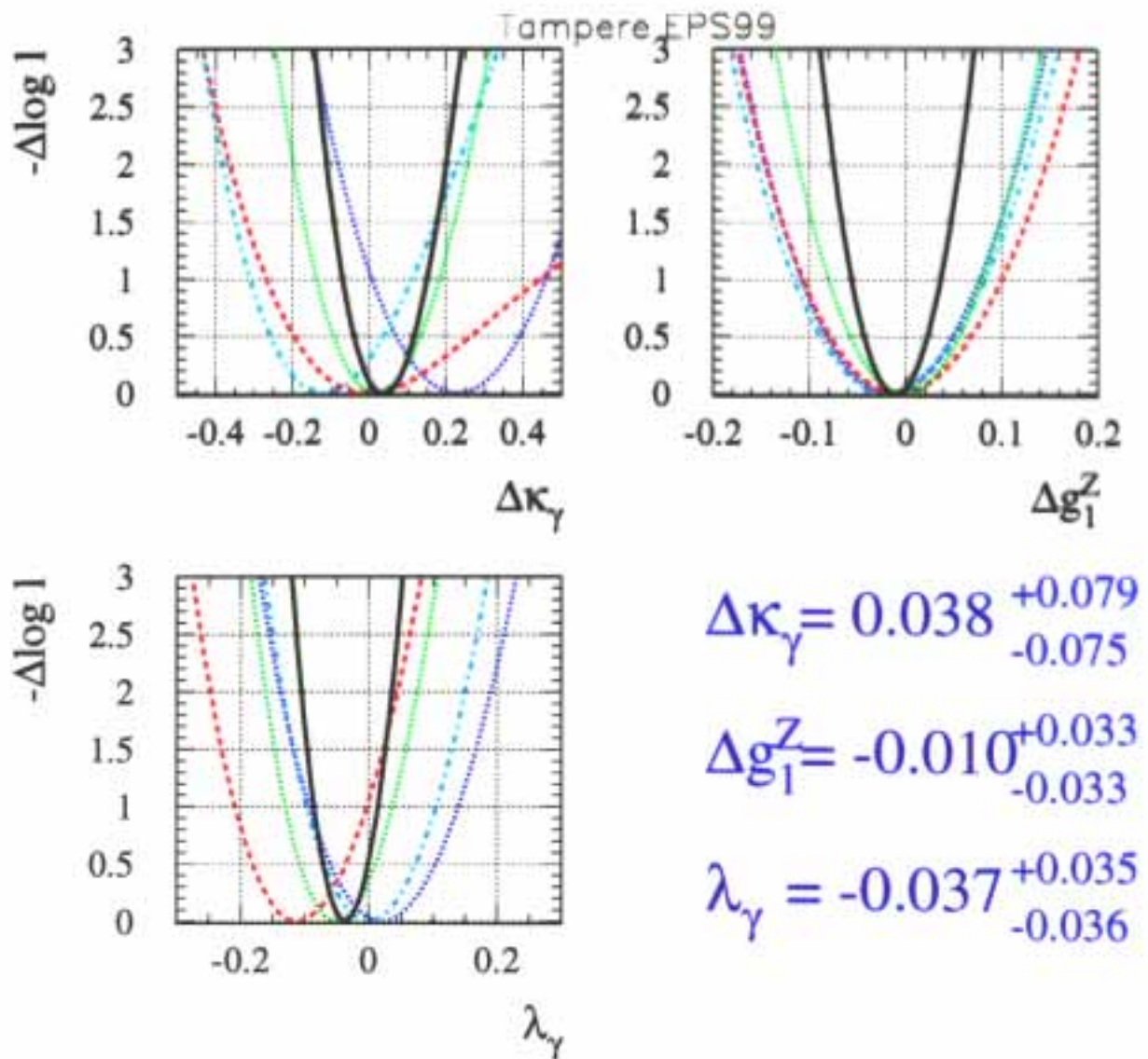
$M_T(2) = 74.7 \text{ GeV}$

$M_{13} = 93.6 \text{ GeV}$

## Limits on anomalous triple boson couplings

- LEP combination ( $e^+e^- \rightarrow WW$  up to 189 GeV)

**ALEPH + DELPHI + L3 + OPAL**



Result from DØ:

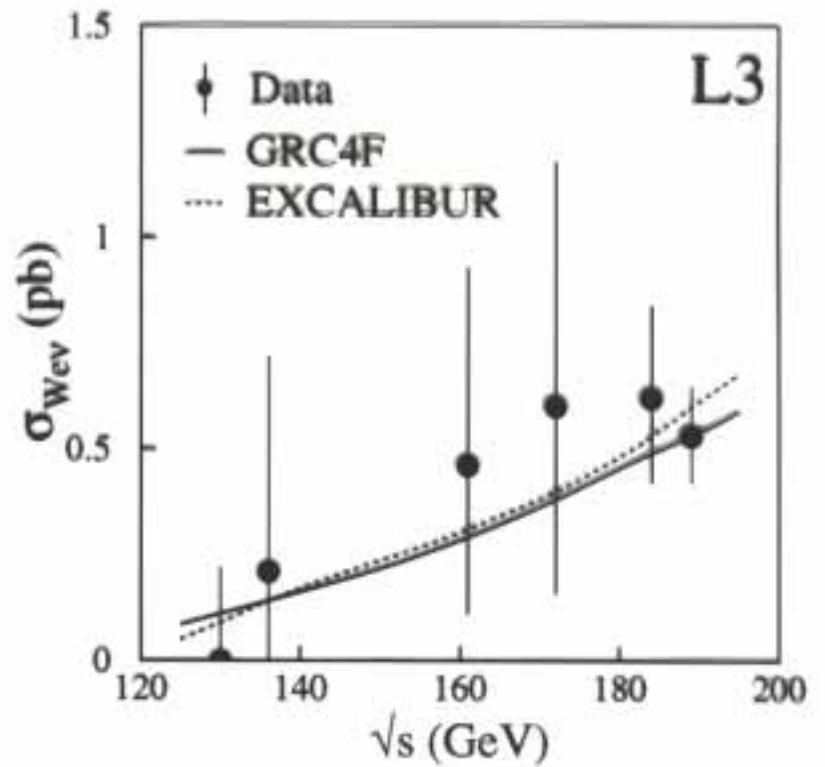
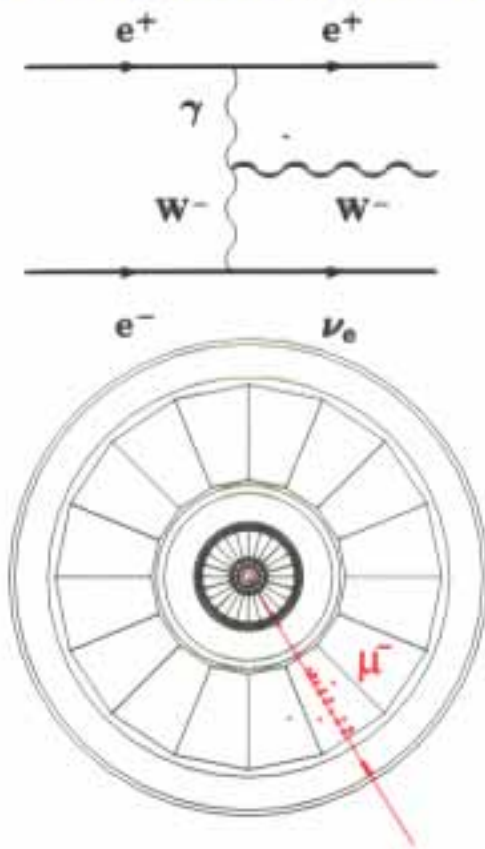
$$\Delta\kappa_\gamma = -0.08 \pm 0.34$$

$$\lambda_\gamma = 0.00^{+0.10}_{-0.09}$$

( $\Delta$  denotes deviation from SM value)

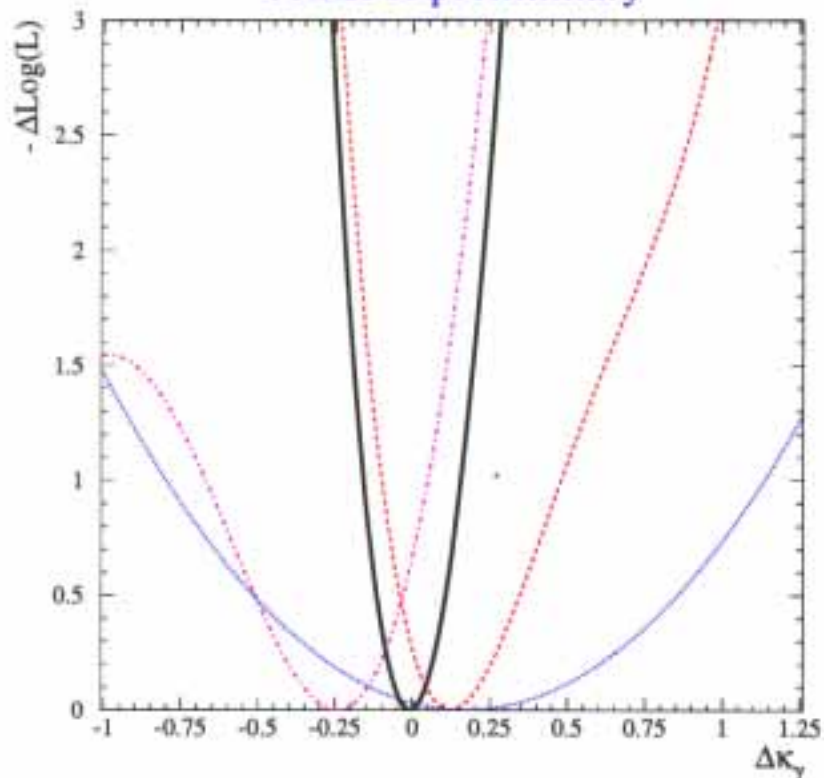
## Single W production at LEP

- More information on  $\gamma WW$  vertex from single W events:



- and from single photon events

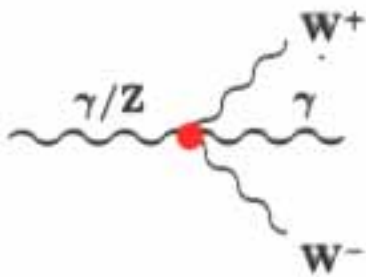
ALEPH preliminary



WW  
single W  
single  $\gamma$   
total

## Quartic boson couplings

- $e^+e^- \rightarrow WW\gamma$  probes quartic boson vertices  
 $WW\gamma\gamma$  and  $WWZ\gamma$



Genuine quartic gauge boson couplings:

6 dimensional operators

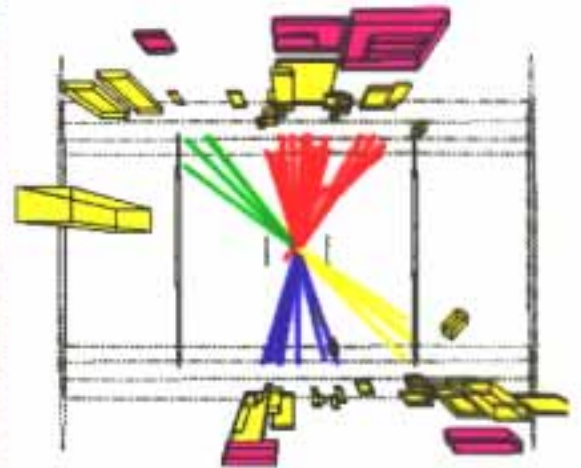
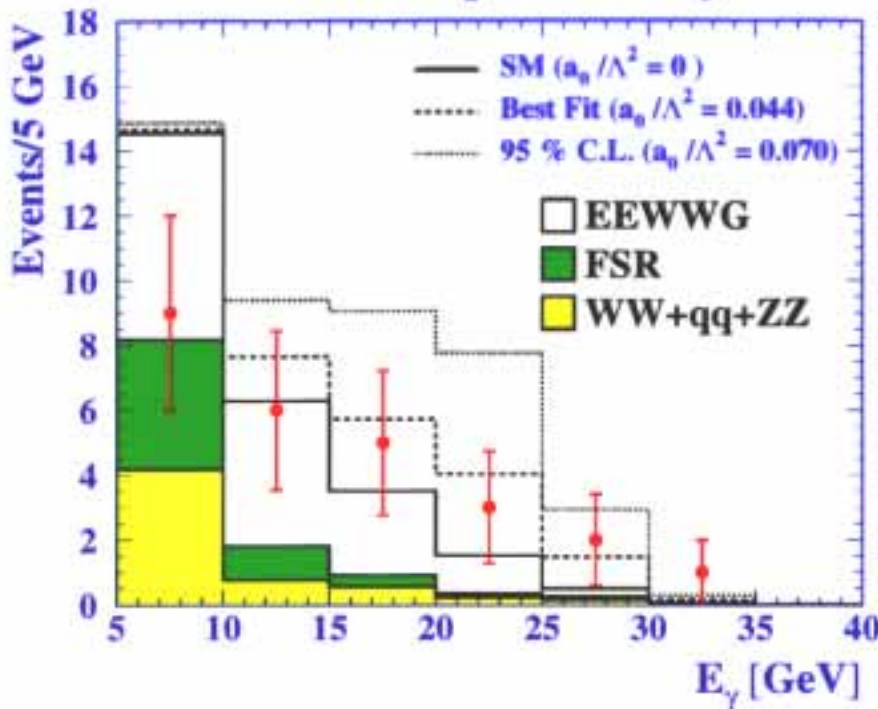
$$a_0/\Lambda^2, a_c/\Lambda^2, a_n/\Lambda^2$$

OPAL: 17 candidates with  $E_\gamma \geq 10$  GeV

$$\sigma_{WW\gamma} = 136 \pm 37 \pm 8 \text{ fb}$$

$$\sigma_{WW\gamma}^{\text{SM}} = 85 - 105 \text{ fb}$$

### OPAL preliminary



Combine with  $e^+e^- \rightarrow \nu\bar{\nu}\gamma\gamma$ :

$$-0.065 \text{ GeV}^{-2} < a_0/\Lambda^2 < +0.065 \text{ GeV}^{-2} \quad WW\gamma\gamma$$

$$-0.13 \text{ GeV}^{-2} < a_c/\Lambda^2 < +0.17 \text{ GeV}^{-2} \quad WW\gamma\gamma$$

$$-0.61 \text{ GeV}^{-2} < a_n/\Lambda^2 < +0.57 \text{ GeV}^{-2} \quad WWZ\gamma$$

(More stringent indirect limits exist on  $a_0$  and  $a_c$ )

## Longitudinally polarized W bosons

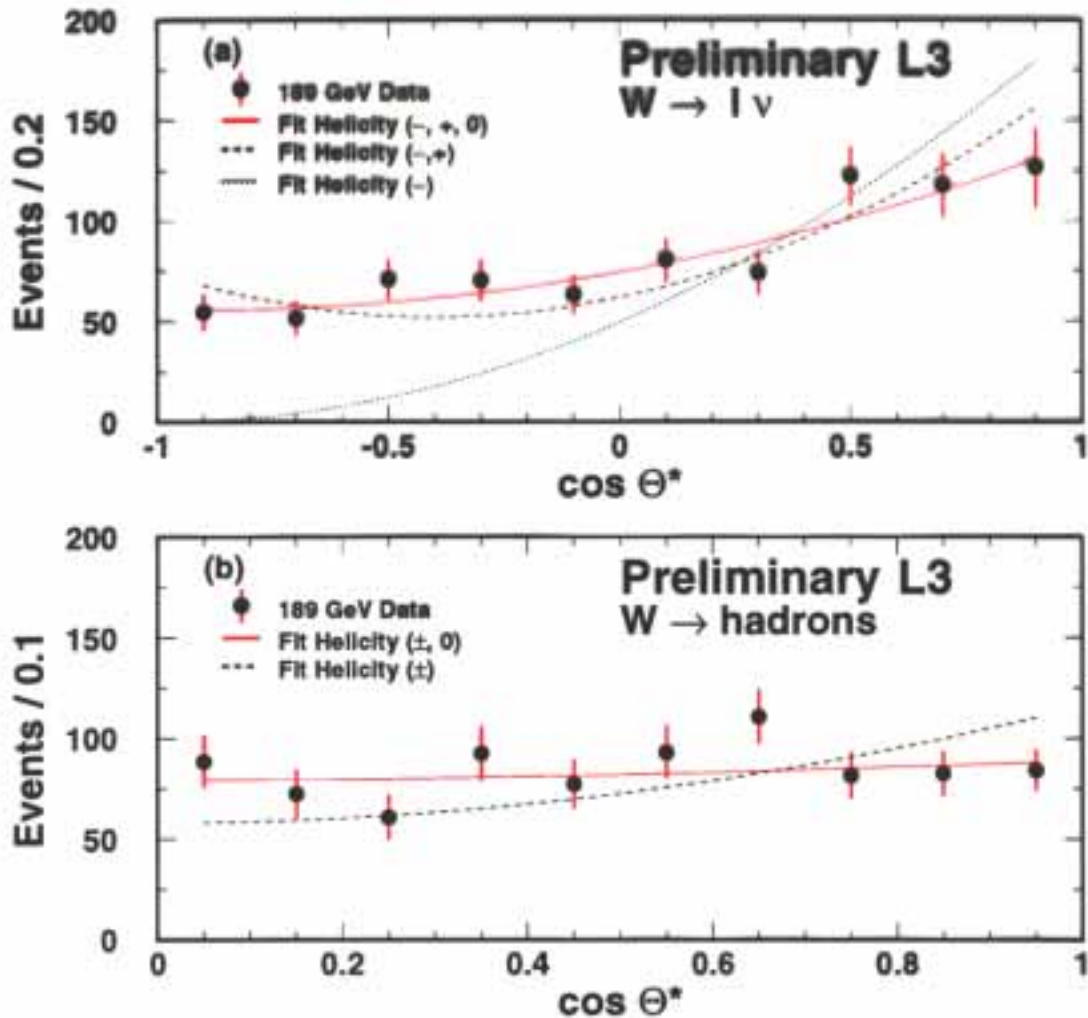
Massive gauge bosons have three polarization states

- transverse (- +)
- longitudinal (0)

Lepton (quark) angle in W rest frame  $\theta^*$ :

$\propto (1 \pm \cos \theta^*)^2$  transverse W

$\propto \sin^2 \theta^*$  longitudinal W



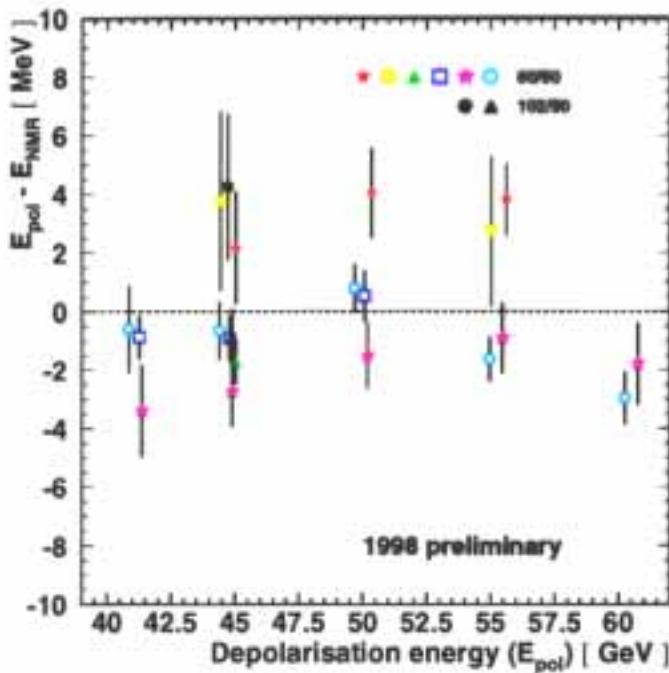
Fraction of longitudinally polarized W bosons:

183 GeV	$0.276 \pm 0.092 \pm 0.03$
189 GeV	$0.244 \pm 0.048 \pm 0.03$
SM	0.26

Top quark decays: CDF  $0.51 \pm 0.37 \pm 0.12$  (SM: 0.70)

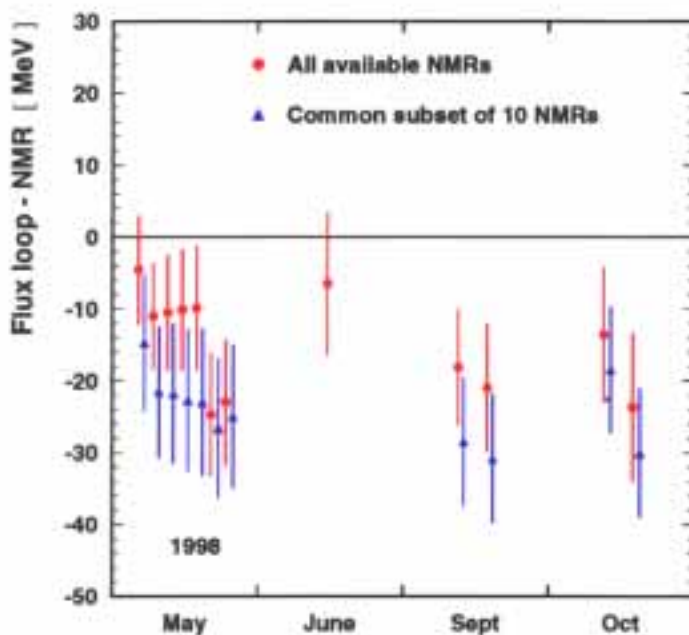
## W mass measurement at LEP

- $m_W$  determined from invariant mass distribution in  $e^+e^- \rightarrow WW$  events
  - Impose energy and momentum conservation in kinematic fit to improve mass resolution
  - Absolute scale determined by LEP beam energy



Resonant depolarisation  
 $E_b \leq 61$  GeV

Precision  $\mathcal{O}(1 \text{ MeV})$



Extrapolate to  $E_b = 94.5$  GeV  
using magnetic measurements  
NMR probes, flux loop

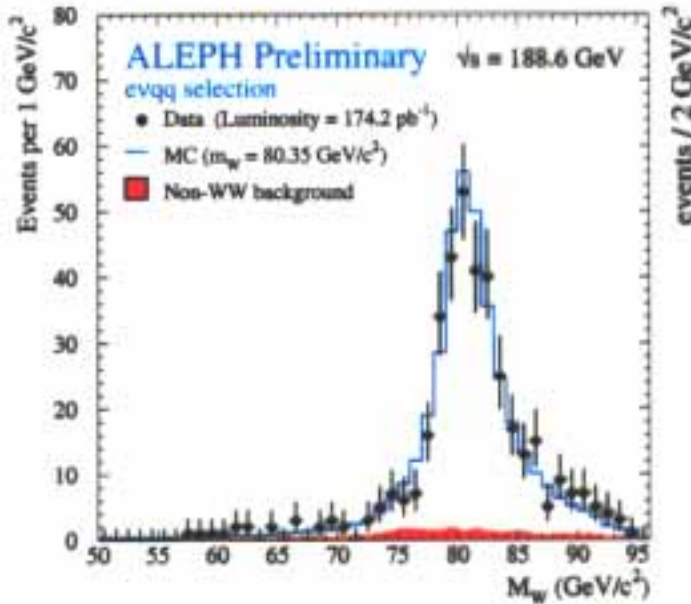
$$\Rightarrow \Delta E_b = \pm 20 \text{ MeV}$$



# Invariant mass distributions after kinematic fit

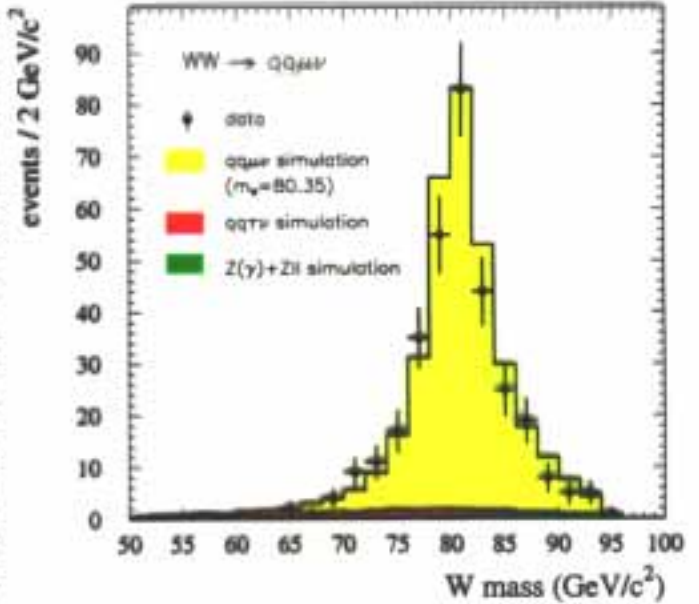
Data at  $\sqrt{s} = 189$  GeV:

$WW \rightarrow q\bar{q}e\nu$

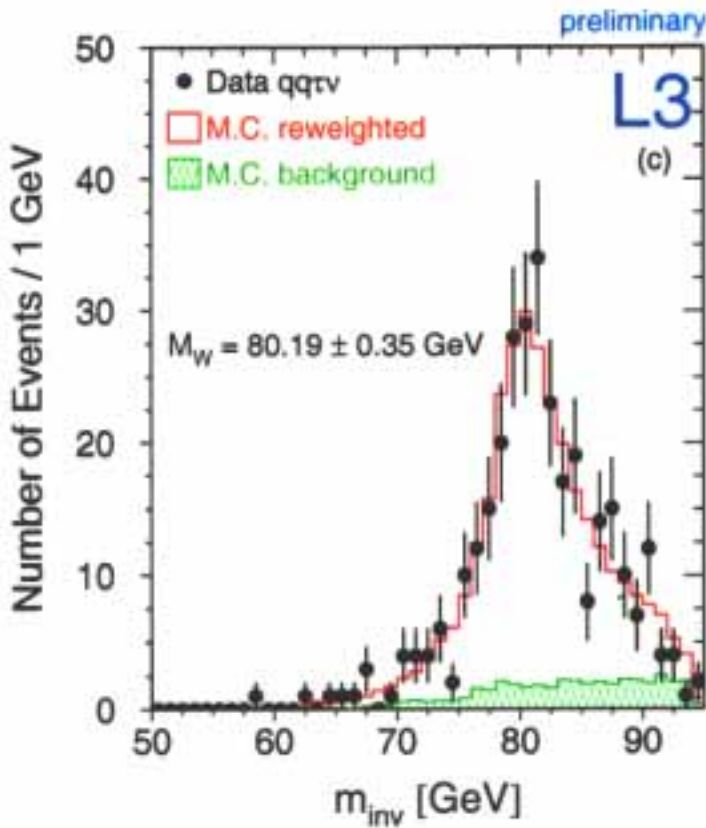


$WW \rightarrow q\bar{q}\mu\nu$

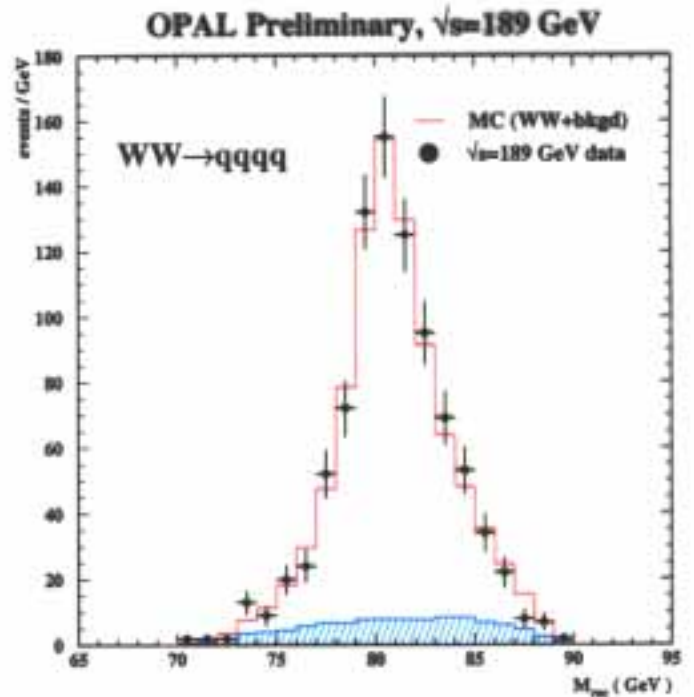
DELPHI



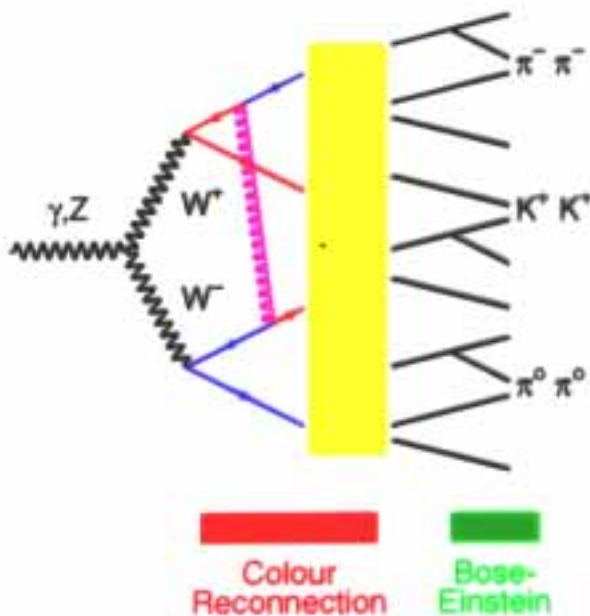
$WW \rightarrow q\bar{q}\tau\nu$



$WW \rightarrow q\bar{q}q\bar{q}$



## Final state interactions in $e^+e^- \rightarrow WW$



### • Colour reconnection

- Hadronisation scale  $\mathcal{O}(1 \text{ fm})$  much larger than W decay length  $\mathcal{O}(0.1 \text{ fm})$
- Gluons carry momentum between quarks from different W bosons
- Impact on reconstructed  $m_W$

### • Investigate charge multiplicity:

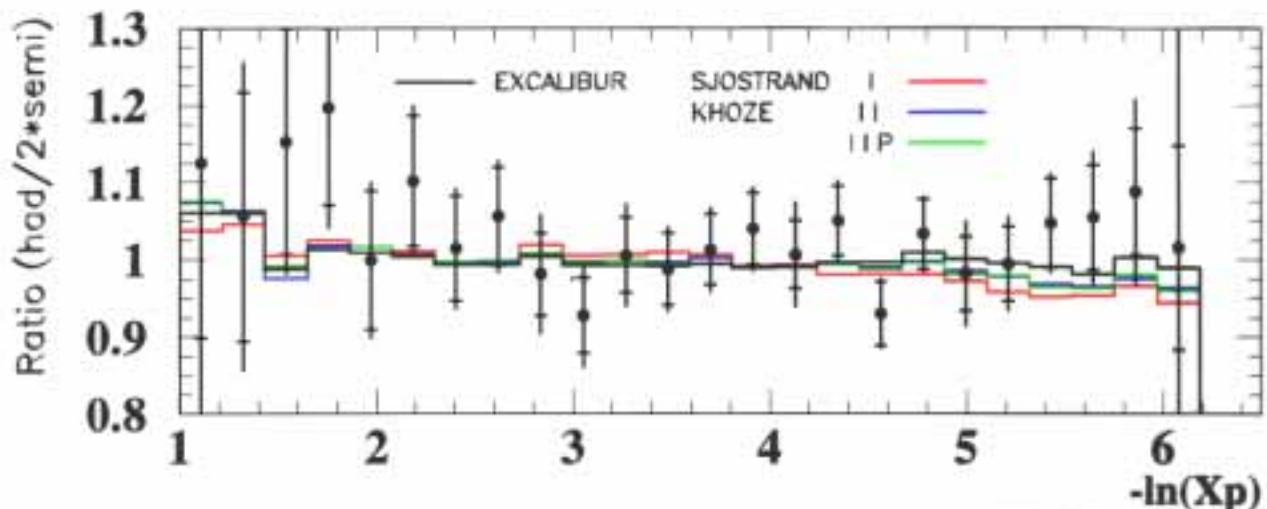
$$\Delta n_{\text{ch}} = \langle n_{\text{ch}}^{\text{qqqq}} \rangle - 2 \langle n_{\text{ch}}^{\text{qq}\ell\nu} \rangle \quad r_{\text{ch}} = \frac{\langle n_{\text{ch}}^{\text{qqqq}} \rangle}{2 \langle n_{\text{ch}}^{\text{qq}\ell\nu} \rangle}$$

ALEPH	$\Delta n_{\text{ch}}$	$+0.52 \pm 0.52$
DELPHI	$r_{\text{ch}}$	$+0.977 \pm 0.017 \pm 0.027$
L3	$\Delta n_{\text{ch}}$	$-0.23 \pm 0.40 \pm 0.52$
OPAL*	$\Delta n_{\text{ch}}$	$+0.7 \pm 0.8 \pm 0.6$

\* 183 GeV

### • compatible with no or small effect

e.g. ALEPH result for scaled momentum  $x_p$ :



Estimated systematic error on  $m_W$ : 25 – 70 MeV

• Bose-Einstein correlation of decay hadrons

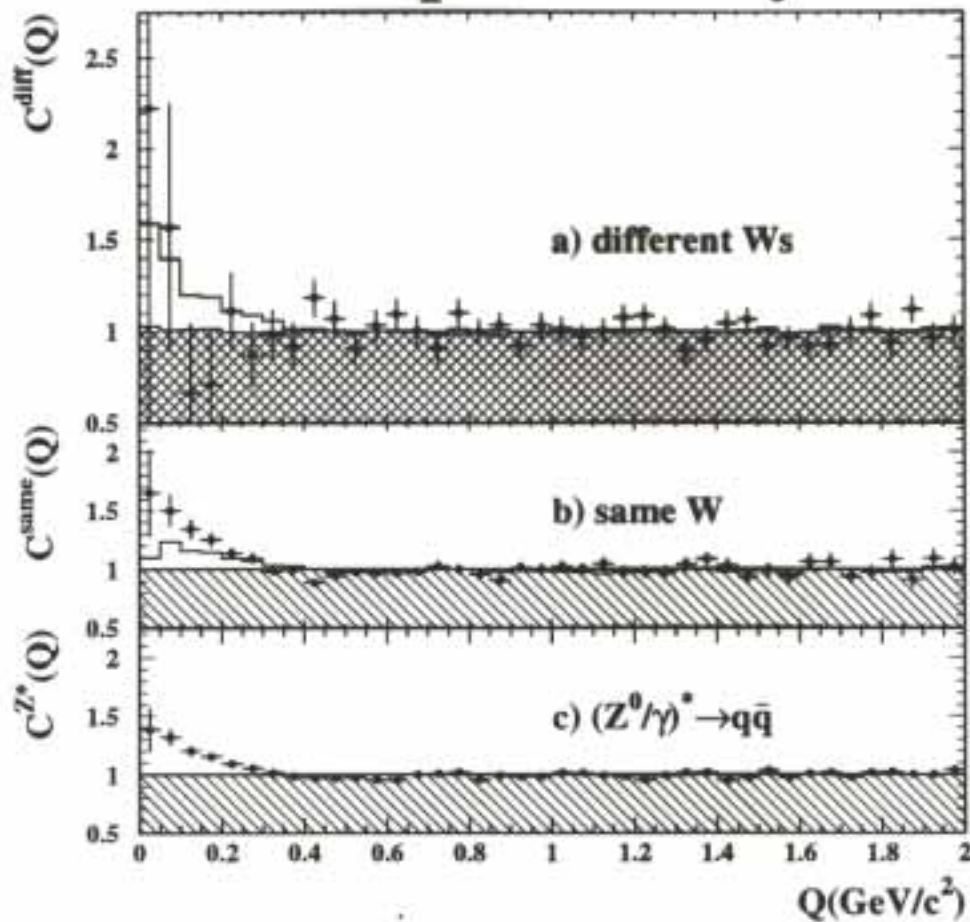
may lead to momentum transfer between decay products of different  $W$  bosons

Study correlation function:

$$C(Q) = N [1 + \lambda \exp(-Q^2 R^2)] \quad Q^2 = -(p_1 - p_2)^2$$

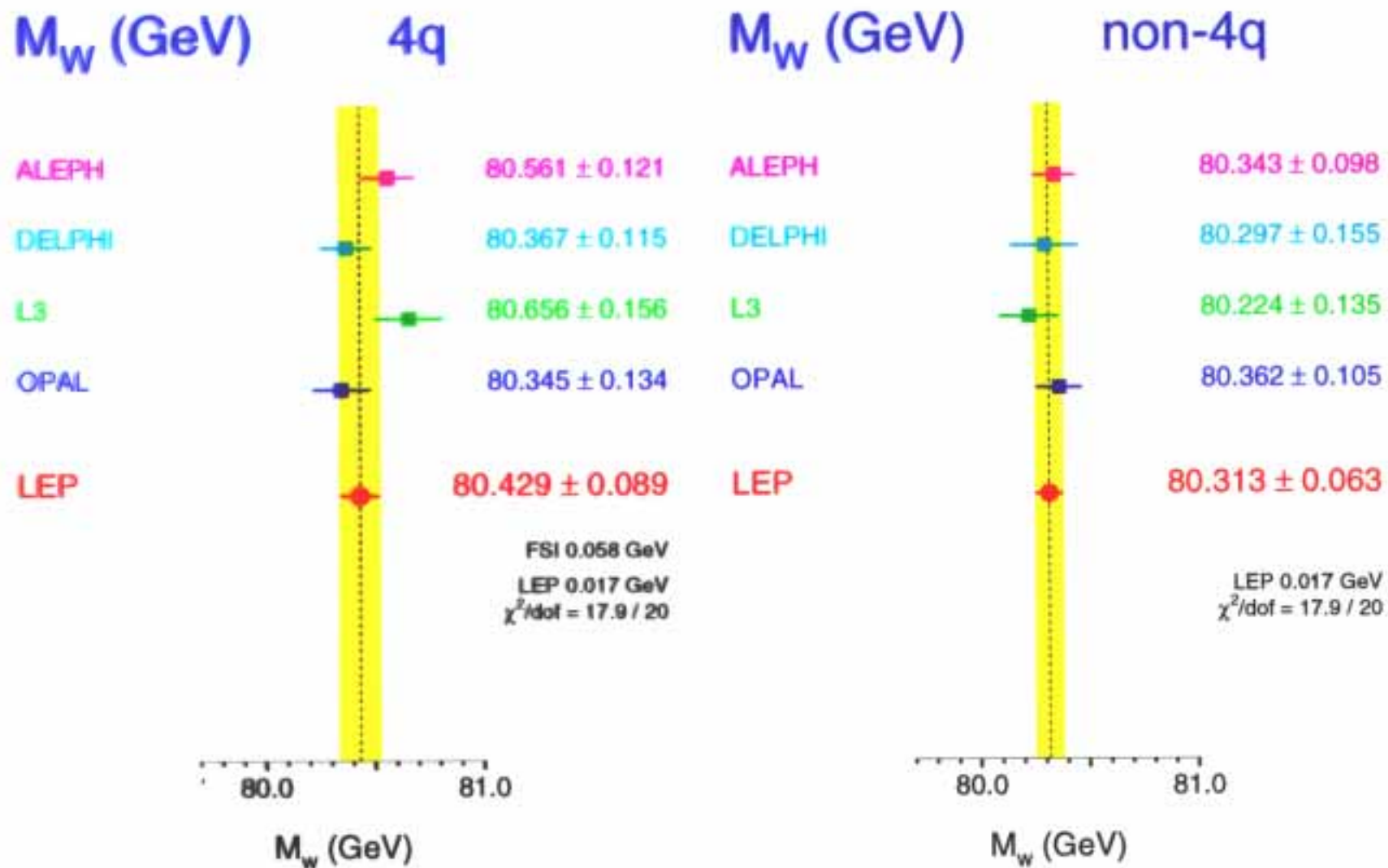
Correlations established in hadronic  $Z$  decays and in decays of the same  $W$

**OPAL preliminary**



Estimated systematic error on  $m_W$ : 20 – 60 MeV

## W mass results from LEP



Combined LEP W mass measurement including 189 GeV data:

$$m_W = 80.350 \pm 0.056 \text{ GeV}$$

## W mass from the Tevatron

- CDF & DØ results from complete Run I data set

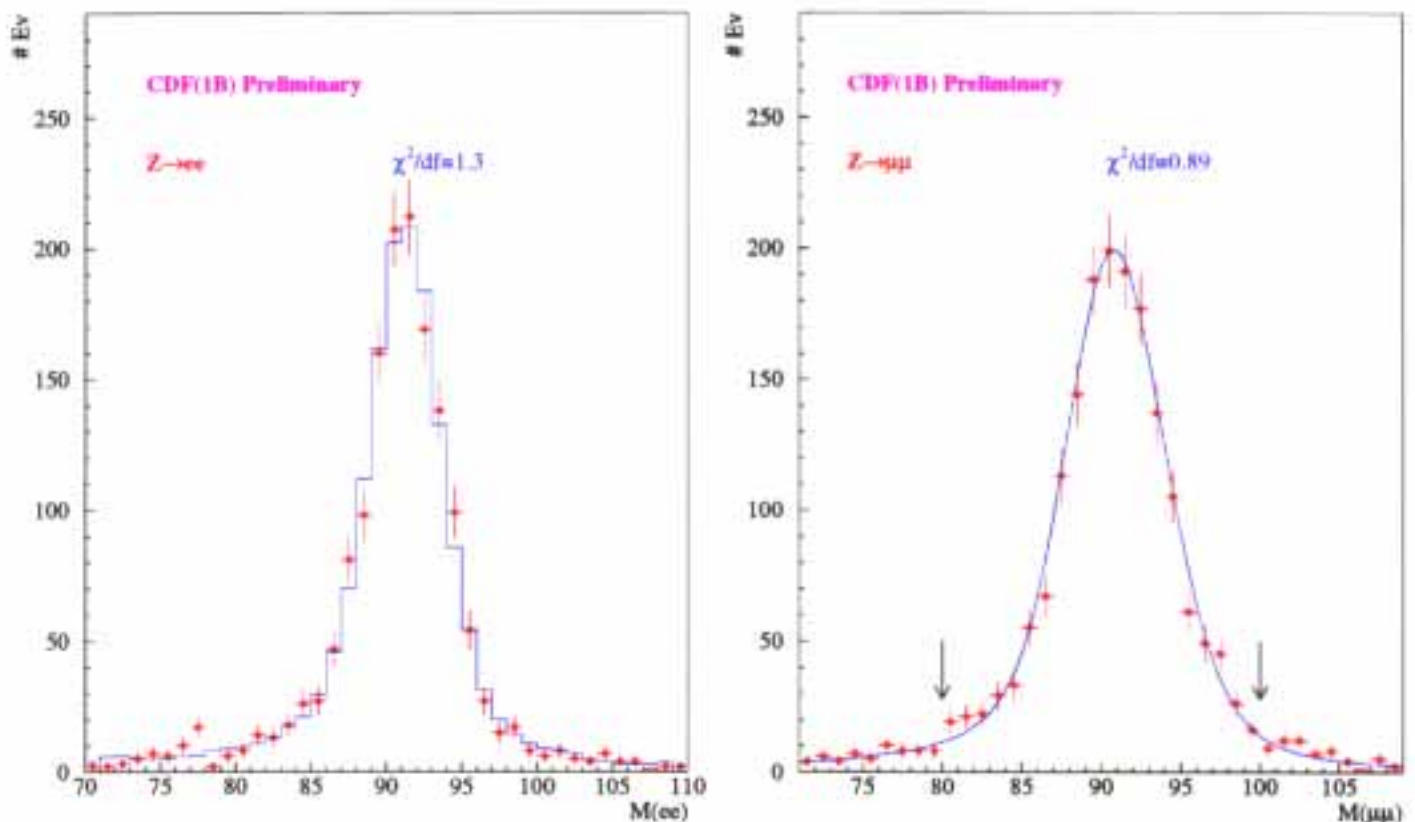
### Events used for $m_W$ measurement

30k  $W \rightarrow e\nu$  and 15k  $W \rightarrow \mu\nu$  (CDF)

45k  $W \rightarrow e\nu$ , incl. 11k in end calorimeter (DØ)

- Fit transverse mass or transverse momentum distributions of  $W \rightarrow \ell\nu$  ( $\ell = e, \mu$ ) events
- Fix energy scale with  $Z \rightarrow \ell^+\ell^-$  events

### Example CDF:



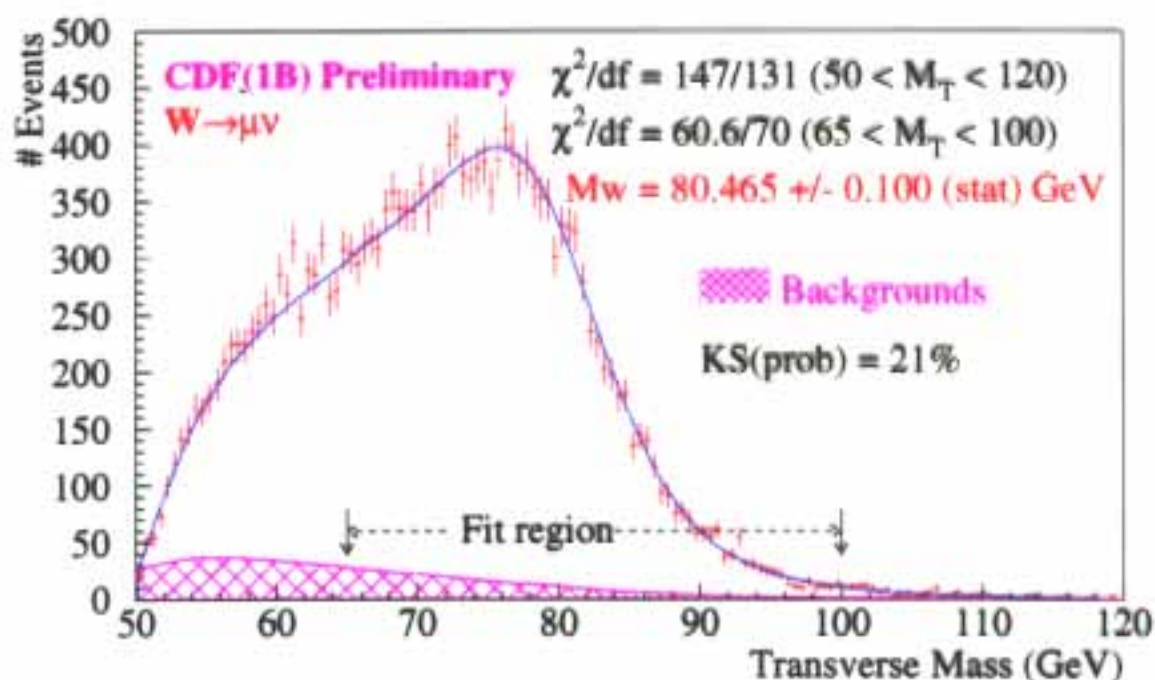
### Z statistics is dominant systematic error on $m_W$ :

CDF:  $\pm 75$  MeV ( $W \rightarrow e\nu$ )     $\pm 85$  MeV ( $W \rightarrow \mu\nu$ )

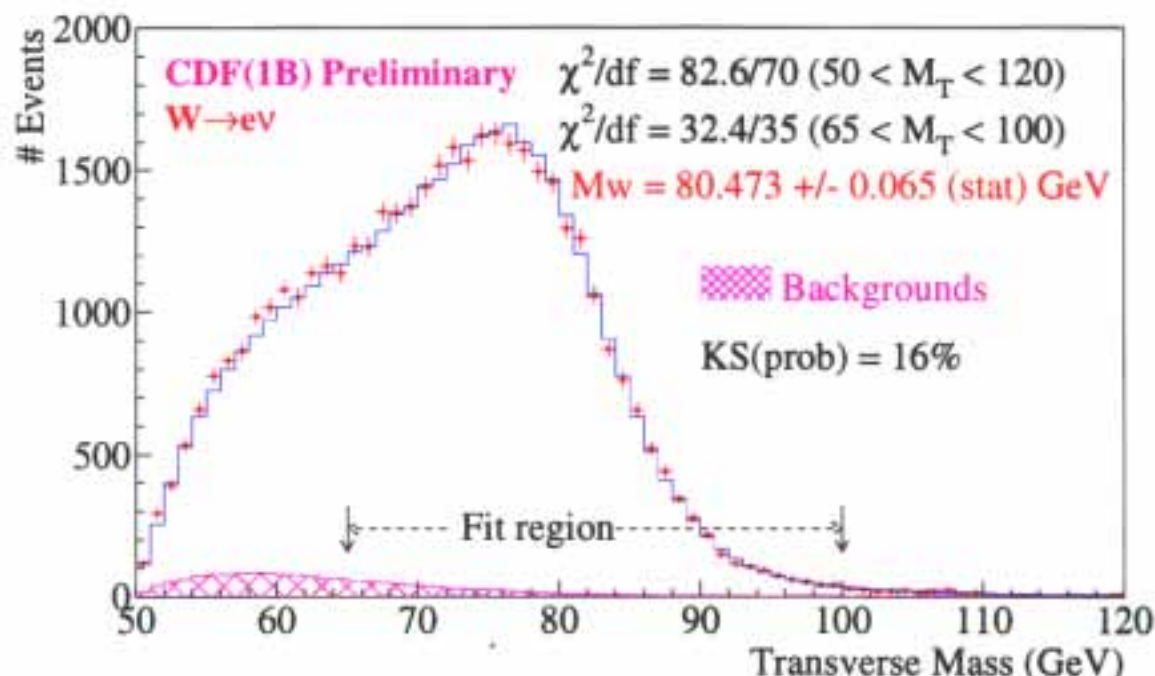
DØ:  $\pm 59$  MeV

## W mass measured by CDF

- CDF transverse mass distributions:



- New result from W → eν:

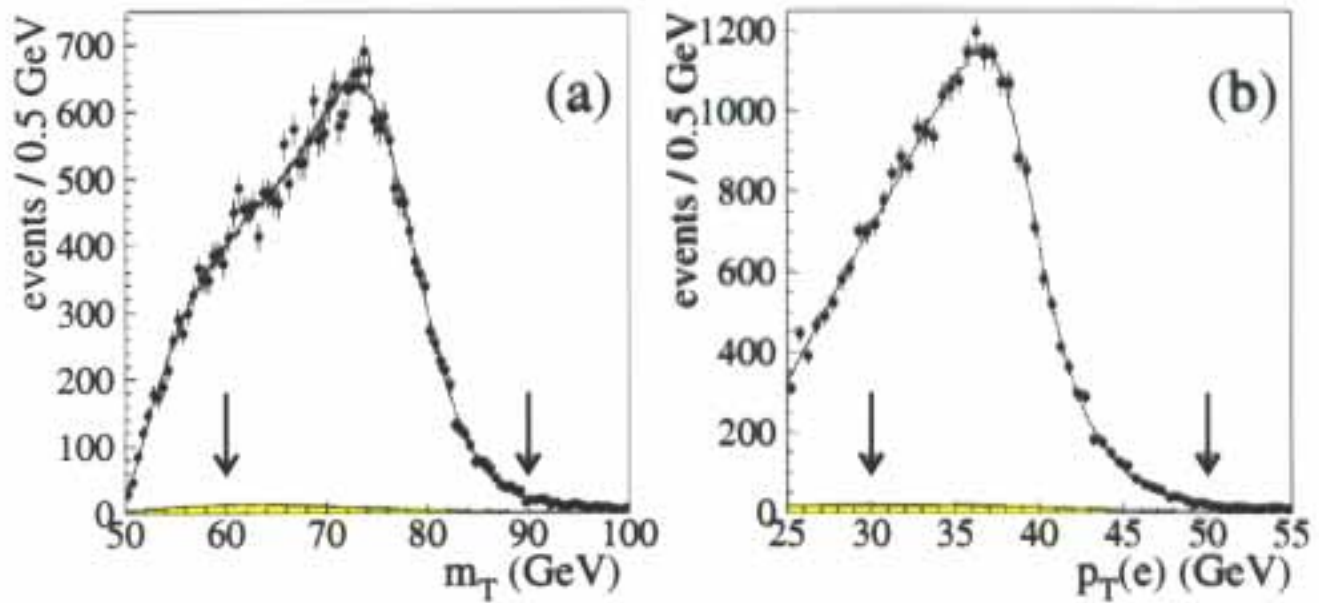


Combined CDF result:

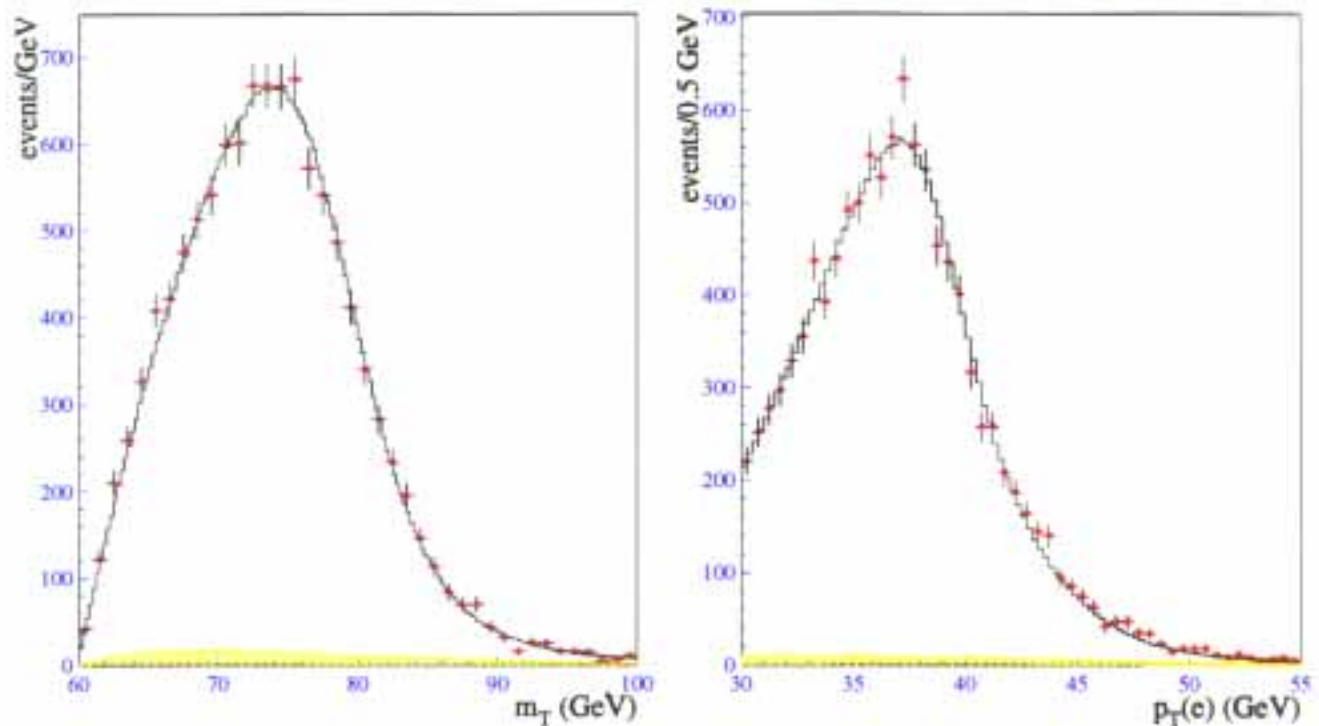
$$m_W = 80.433 \pm 0.079 \text{ GeV}$$

## W mass measured by DØ

- DØ transverse mass and momentum distributions:



- New: including endcap electrons ( $1.5 < |\eta| < 2.5$ )



Combined DØ result:

$$m_W = 80.474 \pm 0.093 \text{ GeV}$$

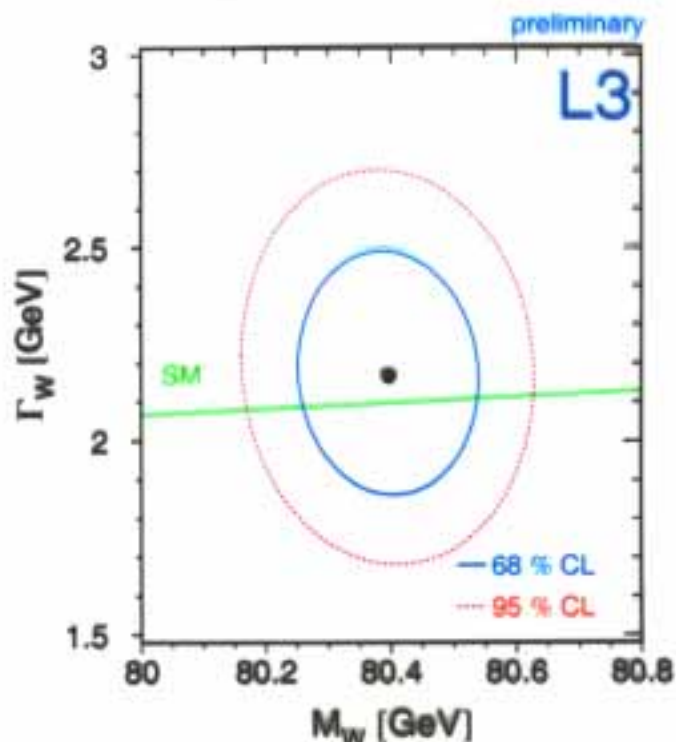
## Measurements of the W width

- Direct determination

- LEP: fit to invariant mass distributions:

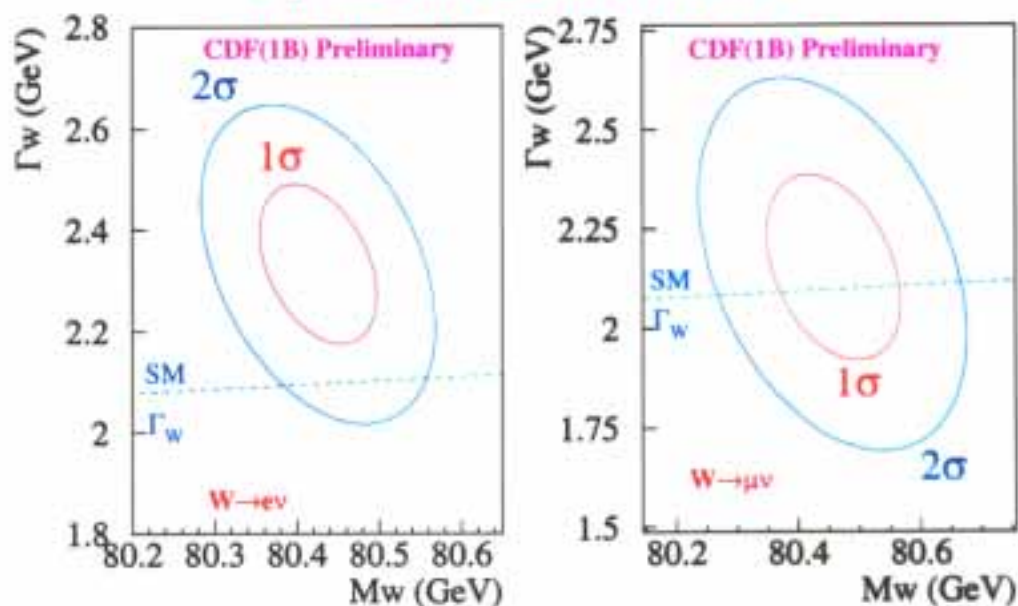
	$\Gamma_W$ [GeV]
L3	$2.12 \pm 0.25$
DELPHI*	$2.48 \pm 0.41$
OPAL*	$1.84 \pm 0.38$
SM	2.08

\* 183 GeV data



- CDF: high end of transverse mass distributions

$$\Gamma_W = 2.055 \pm 0.125 \text{ GeV}$$



- Indirect measurement from

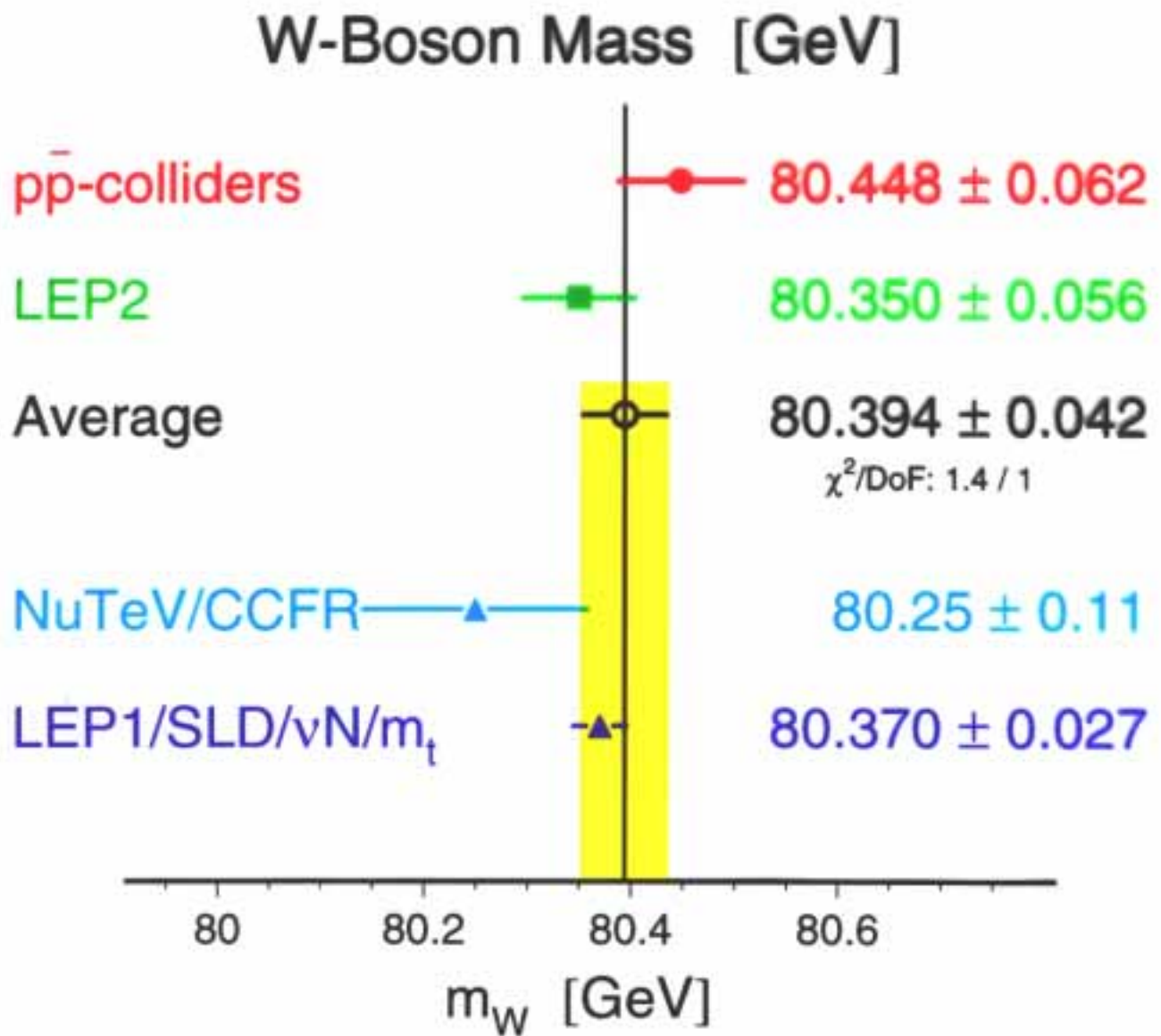
$$\frac{\sigma(p\bar{p} \rightarrow W + X) BR(W \rightarrow \ell\nu)}{\sigma(p\bar{p} \rightarrow Z + X) BR(W \rightarrow \ell\ell)} = \left(\frac{\sigma_W}{\sigma_Z}\right)^{SM} \left(\frac{\Gamma_Z}{\Gamma_{Z \rightarrow \ell\ell}}\right)^{LEP} \frac{\Gamma_{W \rightarrow \ell\nu}^{SM}}{\Gamma_W}$$

$$\text{CDF : } \Gamma_W = 2.179 \pm 0.046 \text{ GeV}$$

$$\text{D}\Phi : \Gamma_W = 2.107 \pm 0.054 \text{ GeV}$$



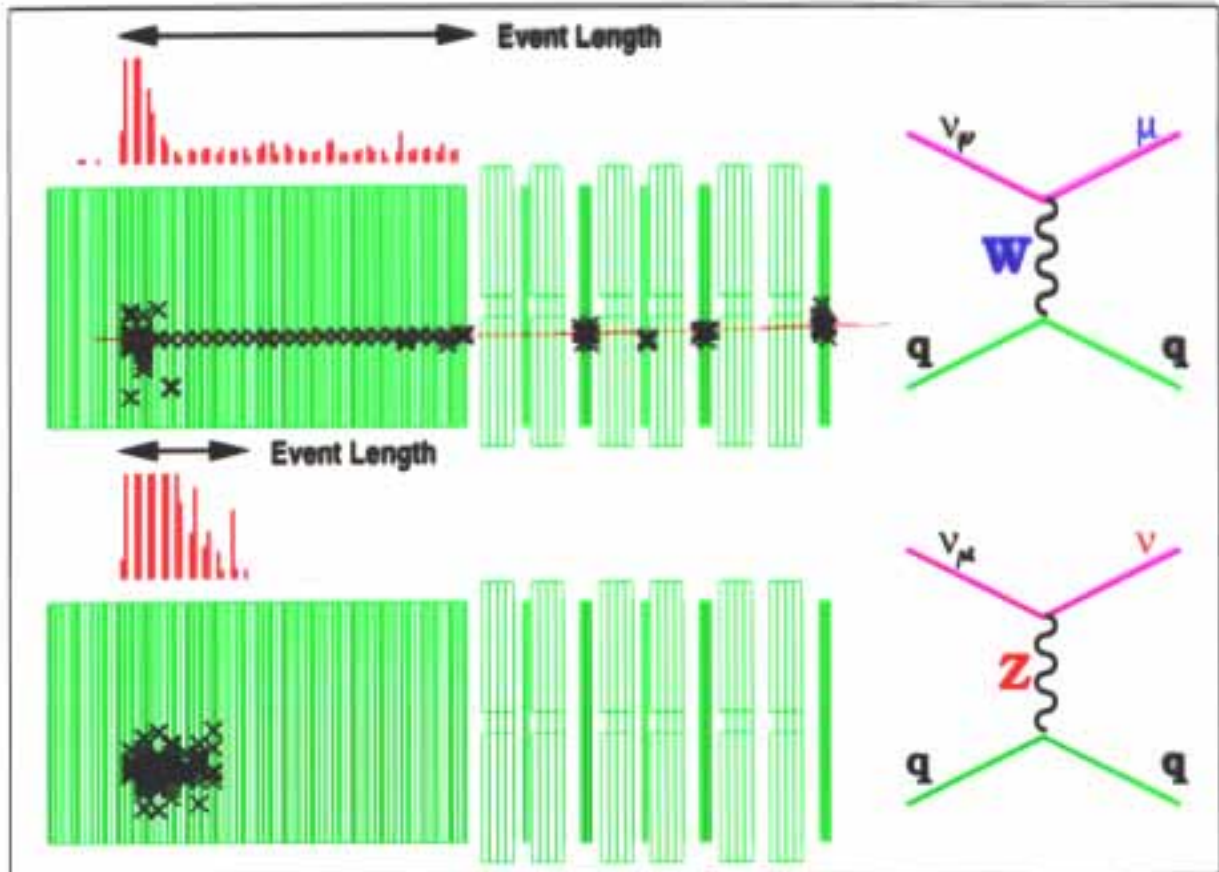
## Comparison of W mass measurements



## W mass from neutrino-nucleon scattering

- Ratio of neutral to charged current cross section measures

$$\sin^2 \theta_W = 1 - \left( \frac{m_W}{m_Z} \right)^2$$



- Experimentally measure

$$R^- = \frac{\sigma_{NC}^{\nu} - \sigma_{NC}^{\bar{\nu}}}{\sigma_{CC}^{\nu} - \sigma_{CC}^{\bar{\nu}}}$$

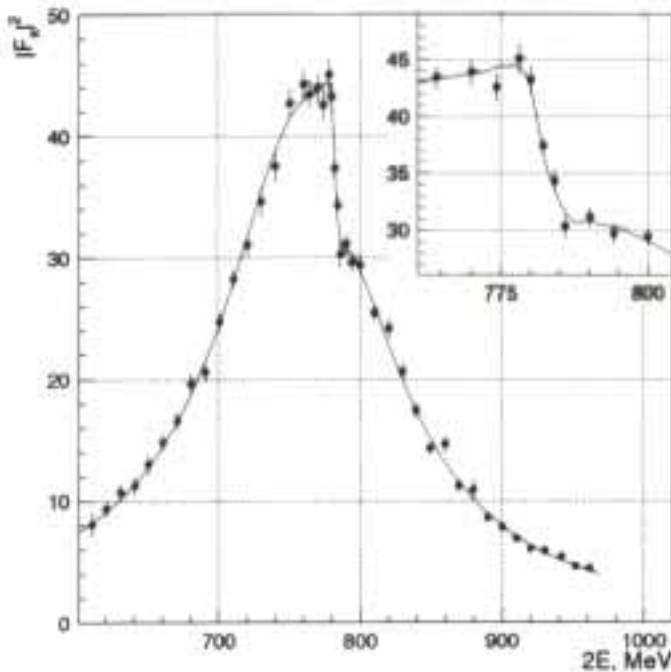
Sea quark contribution cancel:  $\sigma_{\nu q} = \sigma_{\bar{\nu} \bar{q}}$      $\sigma_{\nu \bar{q}} = \sigma_{\bar{\nu} q}$

*NUTeV*     $\sin^2 \theta_W = 0.2253 \pm 0.0019 \pm 0.0010$

$$\implies m_W = 80.25 \pm 0.11 \text{ GeV}$$

## Cross section measurements $e^+e^- \rightarrow \text{hadrons}$ at low energy

- CMD-2 at VEPP in Novosibirsk  
 $\sigma(e^+e^- \rightarrow \pi^+\pi^-)$  around the  $\rho$   
 $630 \text{ MeV} \leq \sqrt{s} \leq 810 \text{ MeV}$

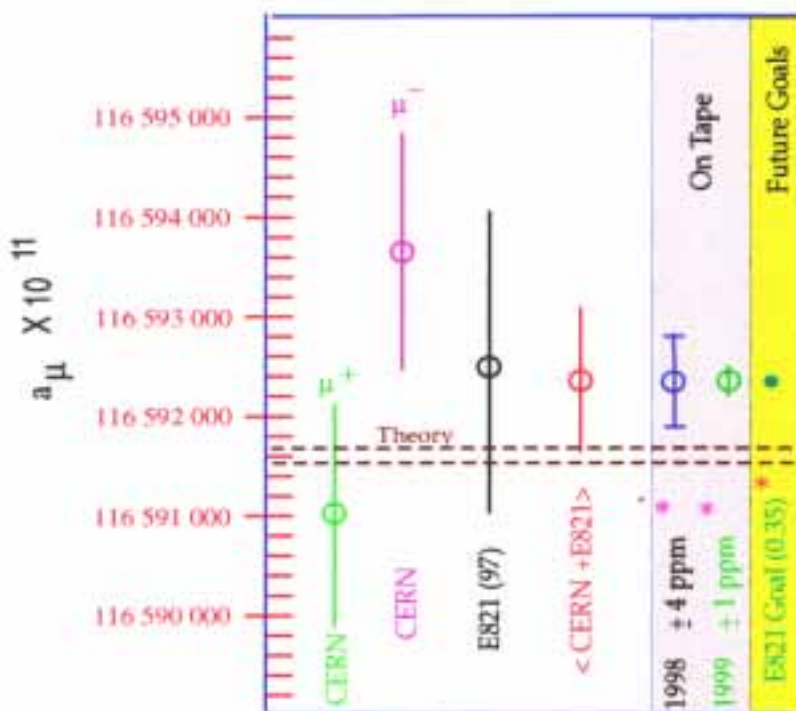


Improved determination of

$$a_\mu^{\text{had}} = (29.03 \pm 0.41) \cdot 10^{-9}$$

(combined with previous measurements)

- BNL E821 measurement of  $a_\mu = \frac{1}{2} (g_\mu - 2)$



First result from 1997  
 pilot run:

$$a_\mu = 1165925(15) \times 10^{-9}$$

Expected precision:

$$\pm 0.35 \cdot 10^{-9}$$

\* projected errors with current value

## Cross section measurements $e^+e^- \rightarrow \text{hadrons}$ at low energy

- Interpretation of electroweak measurements requires  $\alpha(m_Z)$
- Contribution of 5 light quarks to vacuum polarization

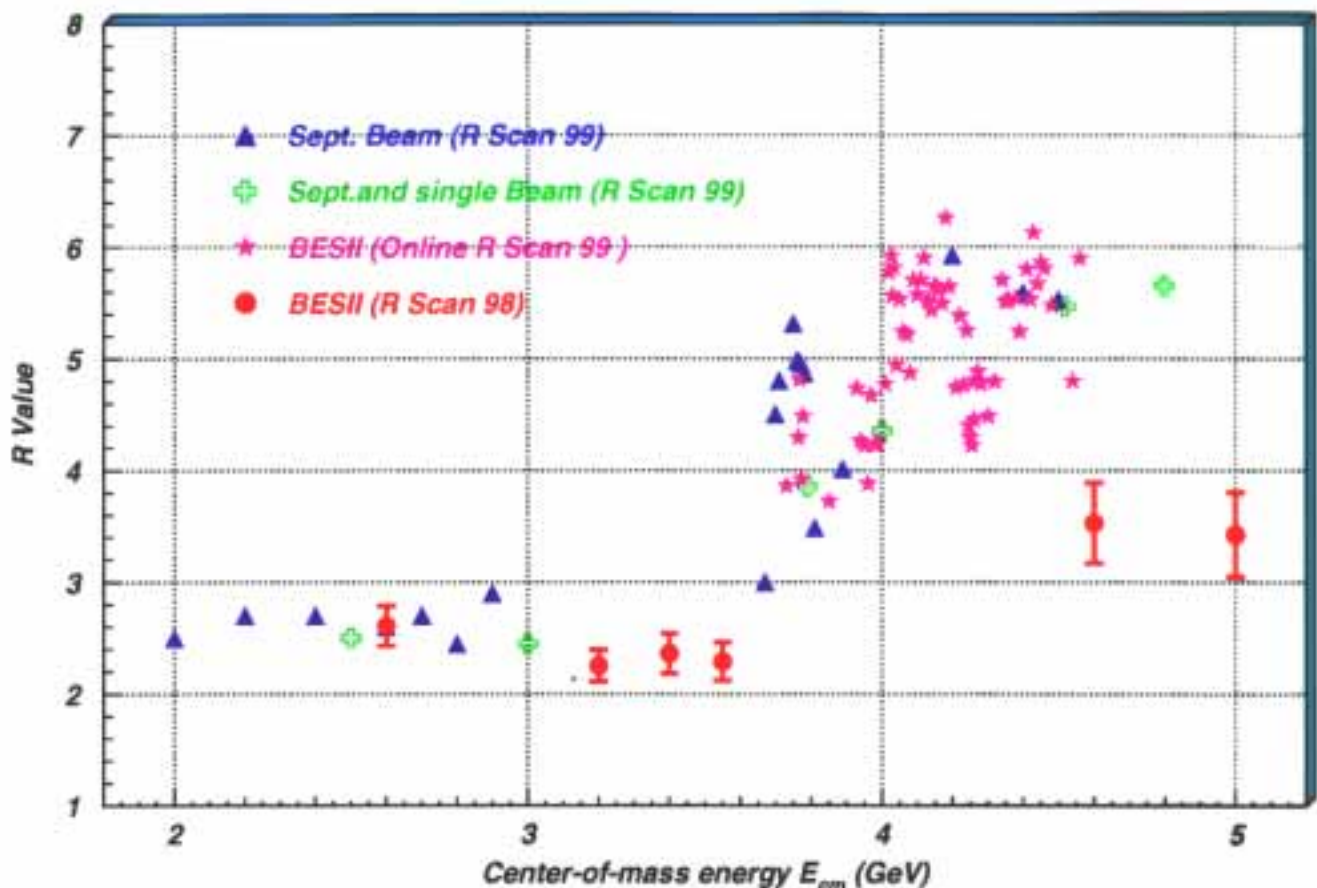
$$\Delta\alpha_{\text{had}}^{(5)} = 0.02804 \pm 0.00065$$

Limited by knowledge of  $R(s) = \frac{\sigma_{\text{had}}}{\sigma_{\mu\mu}}$  at low energy

BES experiment:

- Energy range  $2 \text{ GeV} \leq \sqrt{s} \leq 5 \text{ GeV}$
- Measure  $R$  to 6 – 10%
- Structures near charm threshold

$R$  scan performed in 1999 (85 points)



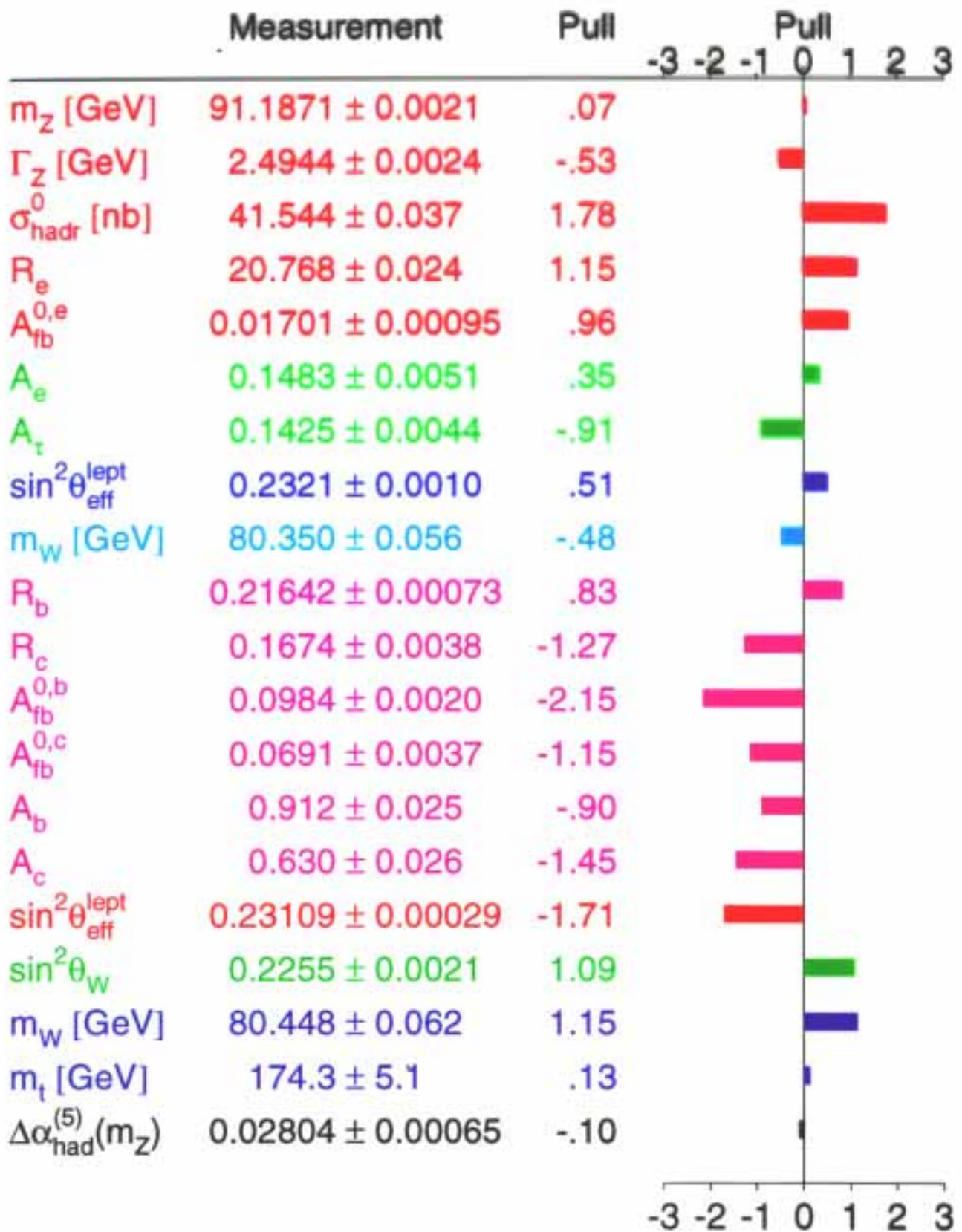
Analysis is ongoing ...

## Interpretation of precision data in the SM

- Observables at the Z from LEP & SLC
- $m_W$  from LEP II and CDF & DØ
- $\sin^2\theta_W$  from  $\nu$ -nucleon scattering
- $m_t = 174.3 \pm 5.1$  GeV (CDF & DØ)
- Hadronic contribution to running of  $\alpha$ :  $\Delta\alpha_{\text{had}}^{(5)} = 0.02804 \pm 0.00065$

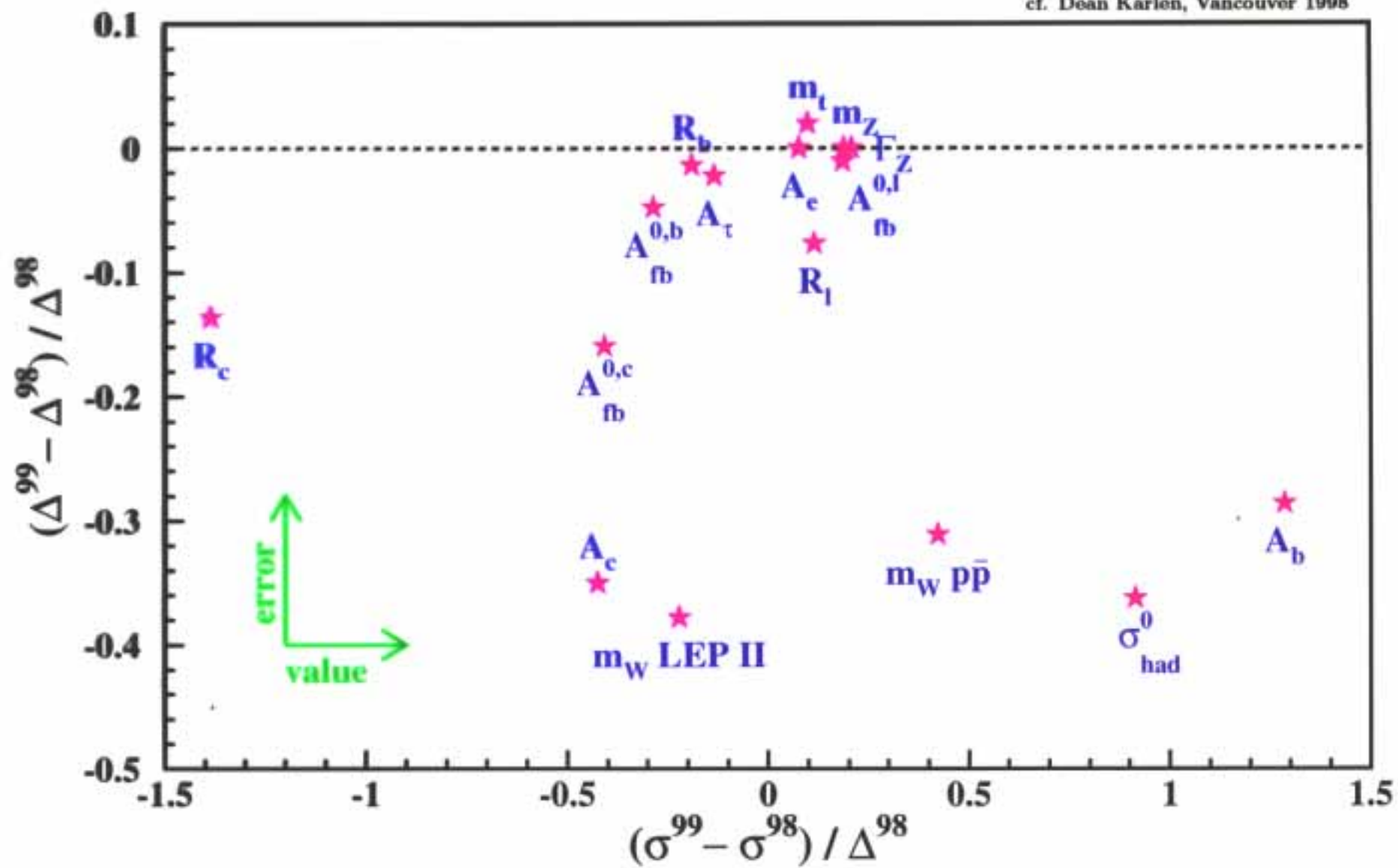
	LEP including LEP II $m_W$	all data except $m_W$ and $m_t$	all data except $m_W$	all data
$m_t$ [GeV]	$172_{-11}^{+14}$	$167_{-9}^{+12}$	$173.2 \pm 4.8$	$173.6 \pm 4.6$
$m_H$ [GeV]	$143_{-87}^{+284}$	$68_{-36}^{+118}$	$102_{-52}^{+92}$	$92_{-45}^{+78}$
$\log(m_H/\text{GeV})$	$2.15_{-0.41}^{+0.48}$	$1.83_{-0.32}^{+0.43}$	$2.01_{-0.31}^{+0.28}$	$1.96_{-0.30}^{+0.27}$
$\alpha_s$	$0.120 \pm 0.003$	$0.119 \pm 0.003$	$0.119 \pm 0.003$	$0.119 \pm 0.003$
$\chi^2/\text{d.o.f.}$	11/9	20/12	20/13	22/15
$\sin^2\bar{\theta}_W$	$0.23187 \pm 0.00021$	$0.23161 \pm 0.00018$	$0.23162 \pm 0.00018$	$0.23159 \pm 0.00016$
$\sin^2\theta_W$	$0.2238 \pm 0.0006$	$0.2234 \pm 0.0007$	$0.2232 \pm 0.0005$	$0.2231 \pm 0.0004$
$m_W$ [GeV]	$80.340 \pm 0.032$	$80.356 \pm 0.035$	$80.370 \pm 0.027$	$80.377 \pm 0.022$

# Tampere 1999

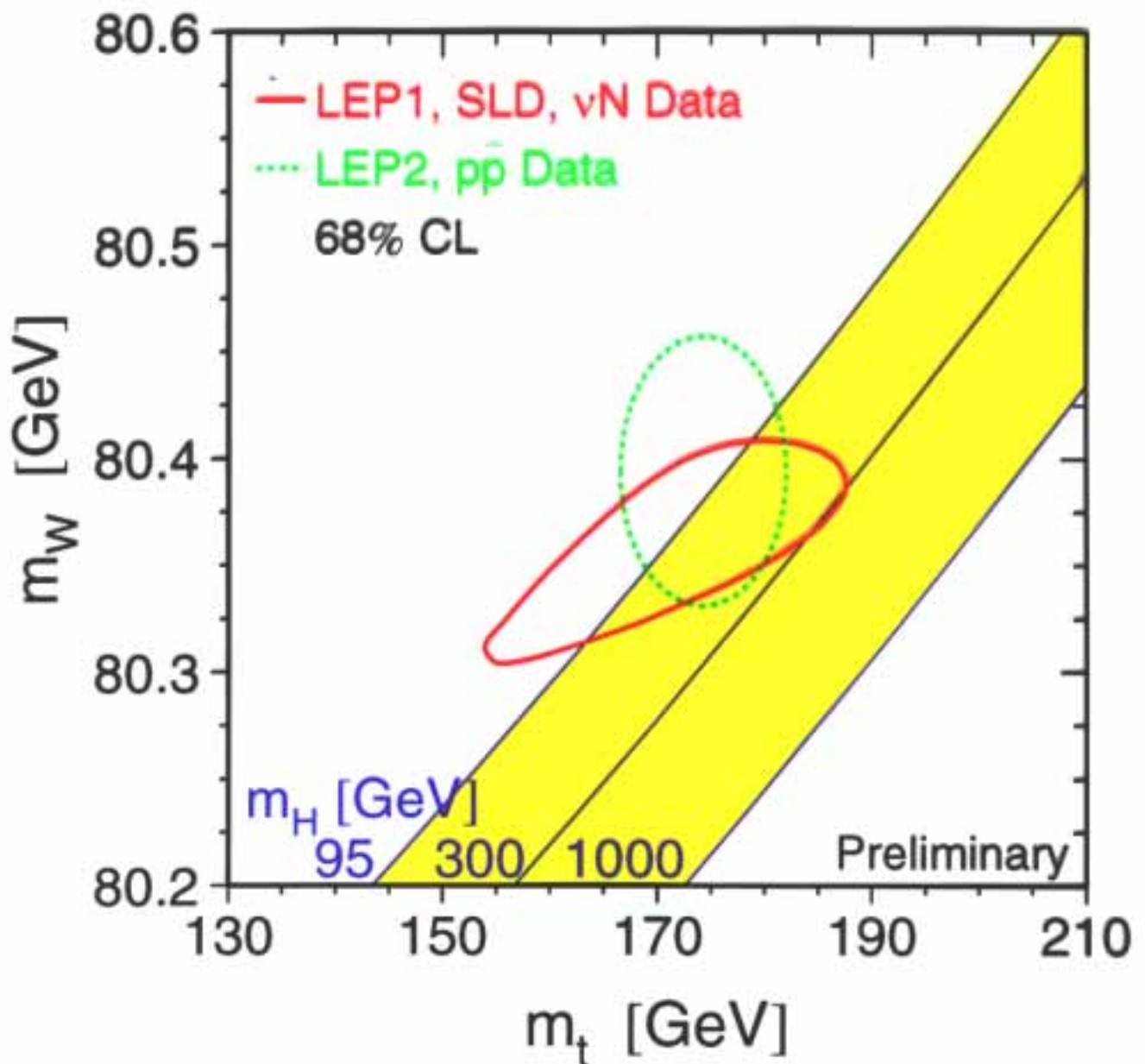


## Changes of measurements since summer 1998

cf. Dean Karlen, Vancouver 1998



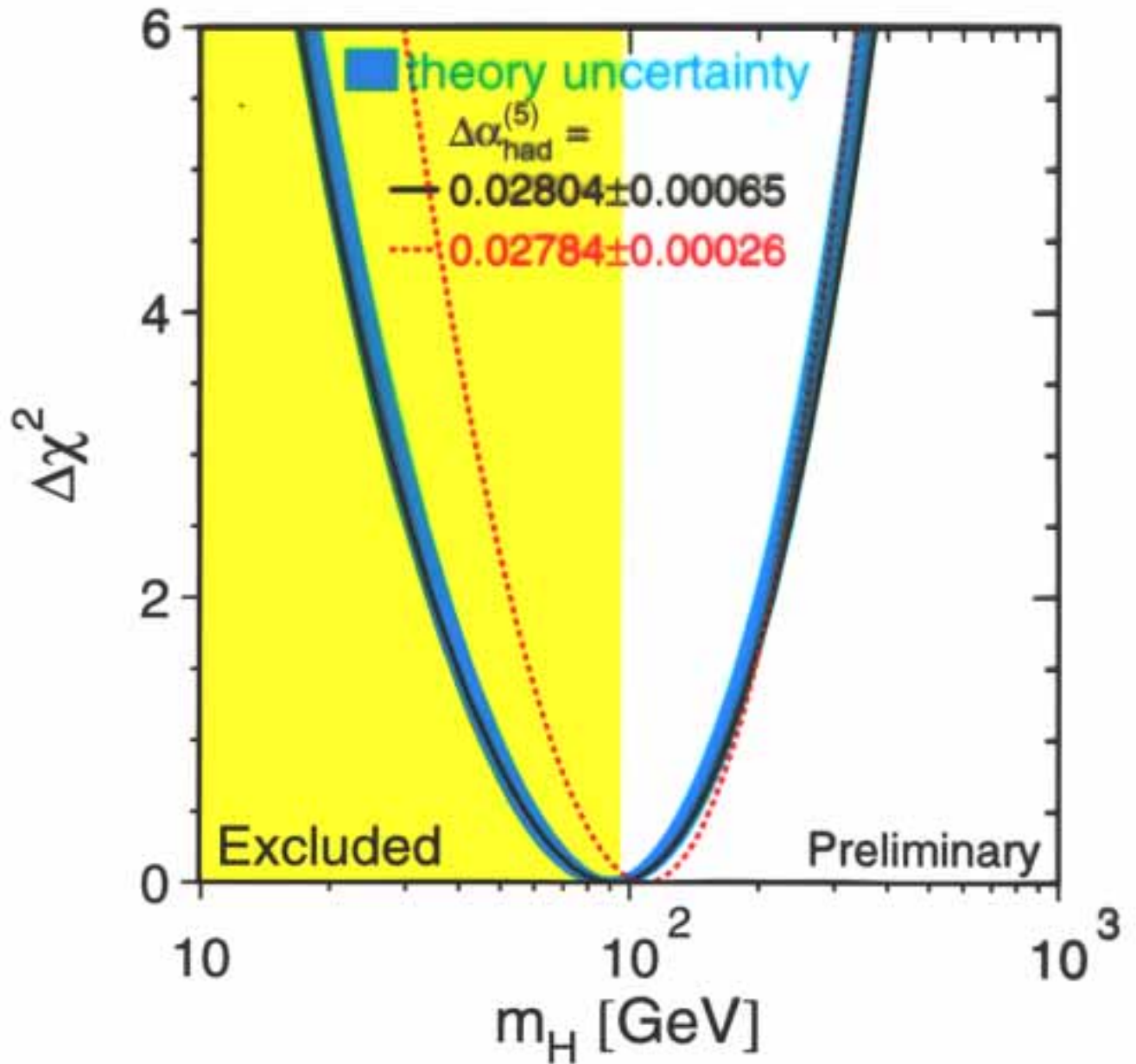
## Comparison of direct and indirect measurements



- Good agreement between direct and indirect determinations of  $m_t$  and  $m_W$   
The SM is correct at the one-loop level
- Data prefer a light Higgs boson



## The mass of the Higgs boson



Electroweak precision data:

$$m_H < 245 \text{ GeV} \quad 95\% \text{ CL}$$

Search for Higgs production at LEP:

$$m_H > 95.2 \text{ GeV} \quad 95\% \text{ CL}$$

## Conclusions and outlook

---

- 10 years of Z physics completed at LEP & SLD
- Rapid progress in W physics

$$m_W = 80.394 \pm 0.042 \text{ GeV}$$

from LEP & Tevatron

- Study of boson self couplings

### Near future

- LEP:  $\sqrt{s} = 200 \text{ GeV}$
- Improvement on  $\alpha(m_Z)$
- HERA
- Tevatron Run II

### Far future

- LHC
- Linear collider
- ...

**The Standard Model still works**

**The Higgs boson is light**

## Acknowledgements

---

Many thanks for results, plots and help to

- all colleagues from theory and experiments
- the LEP Electroweak Working Group
- and in particular to

**Alessandro Ballestrero**

**Dimitry Bardin**

**Igor Boyko**

**Bob Clare**

**Pablo Garcia-Abia**

**Martin Grünewald**

**Atul Gurtu**

**John Holt**

**Paul de Jong**

**Ashutosh Kotwal**

**Mark Lancaster**

**Eric Lançon**

**Clara Matteuzzi**

**Kevin McFarland**

**Martin von der Mey**

**Klaus Mönig**

**Monica Pepe-Altarelli**

**Günter Quast**

**Eusebio Sanchez**

**Mark Thompson**

**Pat Ward**

**Stephane Willocq**

**Yongsheng Zhu**

*Eckhard Elsen*