



# THE STANDARD MODEL AND BEYOND'24

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# The Universe

Улыбающееся лицо



10 сантиметров

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Улыбающееся лицо



10 сантиметров

# The Standard Model

SU(3)

SU(2)

U(1)

Particles

Three Generations of Matter (Fermions)

	I	II	III		
mass→	3 MeV	1.24 GeV	172.5 GeV	0	125.7 GeV
charge→	$\frac{2}{3}$	$\frac{2}{3}$	$\frac{2}{3}$	0	0
spin→	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	1	0
name→	<b>u</b> up	<b>c</b> charm	<b>t</b> top	<b>γ</b> photon	<b>H</b> Higgs
	6 MeV	95 MeV	4.2 GeV	0	0
	$-\frac{1}{3}$	$-\frac{1}{3}$	$-\frac{1}{3}$	0	0
	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	1	2
Quarks	<b>d</b> down	<b>s</b> strange	<b>b</b> bottom	<b>g</b> gluon	<b>G</b> Graviton
	<2 eV	<0.19 MeV	<18.2 MeV	90.2 GeV	
	0	0	0	0	
	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	1	
	<b>ν<sub>e</sub></b> electron neutrino	<b>ν<sub>μ</sub></b> muon neutrino	<b>ν<sub>τ</sub></b> tau neutrino	<b>Z<sup>0</sup></b> weak force	
	0.511 MeV	106 MeV	1.78 GeV	80.4 GeV	
	-1	-1	-1	±1	
	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	1	
Leptons	<b>e</b> electron	<b>μ</b> muon	<b>τ</b> tau	<b>W<sup>±</sup></b> weak force	

Bosons (Forces)

Forces

Electromagnetic

Strong

Weak

Гравитация

# THE STANDARD MODEL OF FUNDAMENTAL INTERACTIONS

## THE PRINCIPLES

- Three gauged symmetries  $SU(3) \times SU(2) \times U(1)$
- Three families of quarks and leptons ( $\underline{3} \times \underline{2}$ ,  $\underline{3} \times \underline{1}$ ,  $\underline{1} \times \underline{2}$ ,  $\underline{1} \times \underline{1}$ )
- Brout-Englert-Higgs mechanism of spontaneous EW symmetry breaking  $\rightarrow$  Higgs boson
- CKM and PMNS mixing of flavours
- CP violation via phase factors
- Confinement of quarks and gluons inside hadrons
- Baryon and lepton number conservation
- CPT invariance  $\rightarrow$  existence of antimatter

# THE STANDARD MODEL OF FUNDAMENTAL INTERACTIONS

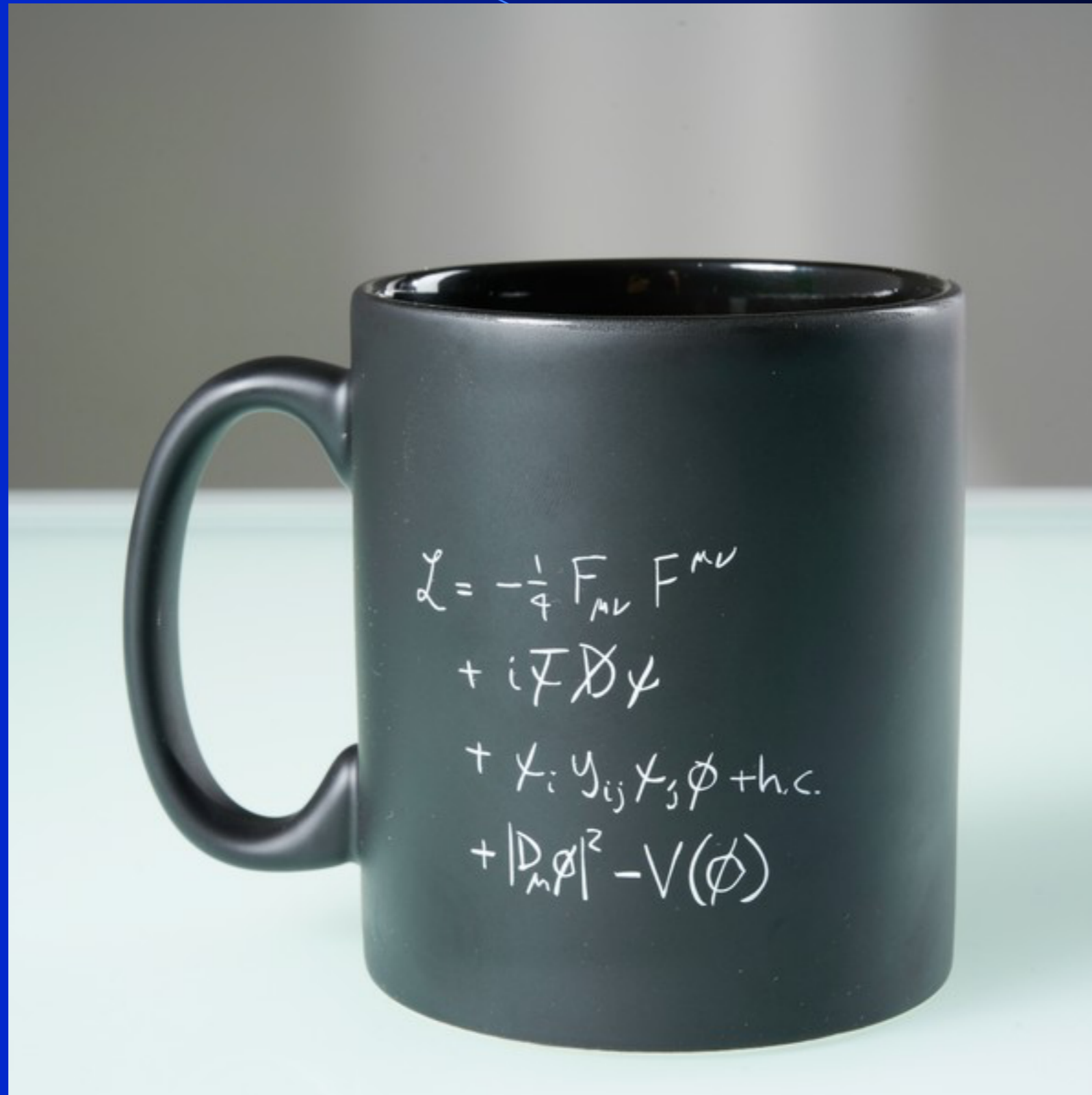
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The ST principles allow:

- Extra families of quarks and leptons
- Presence or absence of right-handed neutrino
- Majorana or Dirac nature of neutrino
- Extra Higgs bosons

# The Standard Model



## THE LAGRANGIAN

$$\mathcal{L} = \mathcal{L}_{gauge} + \mathcal{L}_{Yukawa} + \mathcal{L}_{Higgs},$$



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Two parameters



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All these parameters are not predicted by the SM and determined experimentally

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All these parameters are not predicted

$$\mathcal{L}_{\text{Higgs}} = -V = -\frac{1}{2} M^2 H^2 - \frac{1}{4} \lambda H^4$$

$$\begin{aligned} \mathcal{L}_{SM} = & -\frac{1}{2} \partial_\nu g_\mu^a \partial_\nu g_\mu^a - g_s f^{abc} \partial_\mu g_\nu^a g_\mu^b g_\nu^c - \frac{1}{4} g_s^2 f^{abc} f^{ade} g_\mu^b g_\nu^c g_\mu^d g_\nu^e - \partial_\nu W_\mu^+ \partial_\nu W_\mu^- - \\ & M^2 W_\mu^+ W_\mu^- - \frac{1}{2} \partial_\nu Z_\mu^0 \partial_\nu Z_\mu^0 - \frac{1}{2c_w^2} M^2 Z_\mu^0 Z_\mu^0 - \frac{1}{2} \partial_\mu A_\nu \partial_\mu A_\nu - igc_w (\partial_\nu Z_\mu^0 (W_\mu^+ W_\nu^- - \\ & W_\nu^+ W_\mu^-) - Z_\nu^0 (W_\mu^+ \partial_\nu W_\mu^- - W_\mu^- \partial_\nu W_\mu^+) + Z_\mu^0 (W_\nu^+ \partial_\nu W_\mu^- - W_\nu^- \partial_\nu W_\mu^+)) - \\ & ig s_w (\partial_\nu A_\mu (W_\mu^+ W_\nu^- - W_\nu^+ W_\mu^-) - A_\nu (W_\mu^+ \partial_\nu W_\mu^- - W_\mu^- \partial_\nu W_\mu^+) + A_\mu (W_\nu^+ \partial_\nu W_\mu^- - \\ & W_\nu^- \partial_\nu W_\mu^+)) - \frac{1}{2} g^2 W_\mu^+ W_\mu^- W_\nu^+ W_\nu^- + \frac{1}{2} g^2 W_\mu^+ W_\nu^- W_\mu^+ W_\nu^- + g^2 c_w^2 (Z_\mu^0 W_\mu^+ Z_\nu^0 W_\nu^- - \\ & Z_\mu^0 Z_\nu^0 W_\mu^+ W_\nu^-) + g^2 s_w^2 (A_\mu W_\mu^+ A_\nu W_\nu^- - A_\mu A_\nu W_\mu^+ W_\nu^-) + g^2 s_w c_w (A_\mu Z_\nu^0 (W_\mu^+ W_\nu^- - \\ & W_\nu^+ W_\mu^-) - 2A_\mu Z_\mu^0 W_\nu^+ W_\nu^-) - \frac{1}{2} \partial_\mu H \partial_\mu H - 2M^2 \alpha_h H^2 - \partial_\mu \phi^+ \partial_\mu \phi^- - \frac{1}{2} \partial_\mu \phi^0 \partial_\mu \phi^0 - \\ & \beta_h \left( \frac{2M^2}{g^2} + \frac{2M}{g} H + \frac{1}{2} (H^2 + \phi^0 \phi^0 + 2\phi^+ \phi^-) \right) + \frac{2M^4}{g^2} \alpha_h - \\ & g \alpha_h M (H^3 + H \phi^0 \phi^0 + 2H \phi^+ \phi^-) - \\ & \frac{1}{8} g^2 \alpha_h (H^4 + (\phi^0)^4 + 4(\phi^+ \phi^-)^2 + 4(\phi^0)^2 \phi^+ \phi^- + 4H^2 \phi^+ \phi^- + 2(\phi^0)^2 H^2) - \\ & g M W_\mu^+ W_\mu^- H - \frac{1}{2} g \frac{M}{c_w^2} Z_\mu^0 Z_\mu^0 H - \\ & \frac{1}{2} ig (W_\mu^+ (\phi^0 \partial_\mu \phi^- - \phi^- \partial_\mu \phi^0) - W_\mu^- (\phi^0 \partial_\mu \phi^+ - \phi^+ \partial_\mu \phi^0)) + \\ & \frac{1}{2} g (W_\mu^+ (H \partial_\mu \phi^- - \phi^- \partial_\mu H) + W_\mu^- (H \partial_\mu \phi^+ - \phi^+ \partial_\mu H)) + \frac{1}{2} g \frac{1}{c_w} (Z_\mu^0 (H \partial_\mu \phi^0 - \phi^0 \partial_\mu H) + \\ & M (\frac{1}{c_w} Z_\mu^0 \partial_\mu \phi^0 + W_\mu^+ \partial_\mu \phi^- + W_\mu^- \partial_\mu \phi^+)) - ig \frac{s_w}{c_w} M Z_\mu^0 (W_\mu^+ \phi^- - W_\mu^- \phi^+) + ig s_w M A_\mu (W_\mu^+ \phi^- - \\ & W_\mu^- \phi^+) - ig \frac{1-2c_w^2}{2c_w} Z_\mu^0 (\phi^+ \partial_\mu \phi^- - \phi^- \partial_\mu \phi^+) + ig s_w A_\mu (\phi^+ \partial_\mu \phi^- - \phi^- \partial_\mu \phi^+) - \\ & \frac{1}{4} g^2 W_\mu^+ W_\mu^- (H^2 + (\phi^0)^2 + 2\phi^+ \phi^-) - \frac{1}{8} g^2 \frac{1}{c_w^2} Z_\mu^0 Z_\mu^0 (H^2 + (\phi^0)^2 + 2(2s_w^2 - 1)\phi^+ \phi^-) - \\ & \frac{1}{2} g^2 \frac{s_w^2}{c_w} Z_\mu^0 \phi^0 (W_\mu^+ \phi^- + W_\mu^- \phi^+) - \frac{1}{2} ig^2 \frac{s_w^2}{c_w} Z_\mu^0 H (W_\mu^+ \phi^- - W_\mu^- \phi^+) + \frac{1}{2} g^2 s_w A_\mu \phi^0 (W_\mu^+ \phi^- + \\ & W_\mu^- \phi^+) + \frac{1}{2} ig^2 s_w A_\mu H (W_\mu^+ \phi^- - W_\mu^- \phi^+) - g^2 \frac{s_w}{c_w} (2c_w^2 - 1) Z_\mu^0 A_\mu \phi^+ \phi^- - \\ & g^2 s_w^2 A_\mu A_\mu \phi^+ \phi^- + \frac{1}{2} ig s_w \lambda_{ij}^a (\bar{q}_i^\sigma \gamma^\mu q_j^\sigma) g_\mu^a - \bar{e}^\lambda (\gamma \partial + m_e) e^\lambda - \bar{\nu}^\lambda (\gamma \partial + m_\nu) \nu^\lambda - \bar{u}_j^\lambda (\gamma \partial + \\ & m_u^\lambda) u_j^\lambda - \bar{d}_j^\lambda (\gamma \partial + m_d^\lambda) d_j^\lambda + ig s_w A_\mu (-\bar{e}^\lambda \gamma^\mu e^\lambda + \frac{2}{3} (\bar{u}_j^\lambda \gamma^\mu u_j^\lambda) - \frac{1}{3} (\bar{d}_j^\lambda \gamma^\mu d_j^\lambda)) + \\ & \frac{ig}{4c_w} Z_\mu^0 \{ (\bar{\nu}^\lambda \gamma^\mu (1 + \gamma^5) \nu^\lambda) + (\bar{e}^\lambda \gamma^\mu (4s_w^2 - 1 - \gamma^5) e^\lambda) + (\bar{d}_j^\lambda \gamma^\mu (\frac{4}{3}s_w^2 - 1 - \gamma^5) d_j^\lambda) + \\ & (\bar{u}_j^\lambda \gamma^\mu (1 - \frac{8}{3}s_w^2 + \gamma^5) u_j^\lambda) \} + \frac{ig}{2\sqrt{2}} W_\mu^+ ((\bar{\nu}^\lambda \gamma^\mu (1 + \gamma^5) U^{lep}{}_{\lambda\kappa} e^\kappa) + (\bar{u}_j^\lambda \gamma^\mu (1 + \gamma^5) C_{\lambda\kappa} d_j^\kappa)) + \\ & \frac{ig}{2\sqrt{2}} W_\mu^- ((\bar{e}^\kappa U^{lep}{}_{\kappa\lambda} \gamma^\mu (1 + \gamma^5) \nu^\lambda) + (\bar{d}_j^\kappa C_{\kappa\lambda}^\dagger \gamma^\mu (1 + \gamma^5) u_j^\lambda)) + \\ & \frac{ig}{2M\sqrt{2}} \phi^+ (-m_e^\kappa (\bar{\nu}^\lambda U^{lep}{}_{\lambda\kappa} (1 - \gamma^5) e^\kappa) + m_\nu^\lambda (\bar{\nu}^\lambda U^{lep}{}_{\lambda\kappa} (1 + \gamma^5) e^\kappa) + \\ & \frac{ig}{2M\sqrt{2}} \phi^- (m_e^\lambda (\bar{e}^\lambda U^{lep}{}_{\lambda\kappa} (1 + \gamma^5) \nu^\kappa) - m_\nu^\kappa (\bar{e}^\lambda U^{lep}{}_{\lambda\kappa} (1 - \gamma^5) \nu^\kappa) - \frac{g}{2} \frac{m_\nu^\lambda}{M} H (\bar{\nu}^\lambda \nu^\lambda) - \\ & \frac{g}{2} \frac{m_\nu^\lambda}{M} H (\bar{e}^\lambda e^\lambda) + \frac{ig}{2} \frac{m_\nu^\lambda}{M} \phi^0 (\bar{\nu}^\lambda \gamma^5 \nu^\lambda) - \frac{ig}{2} \frac{m_\nu^\lambda}{M} \phi^0 (\bar{e}^\lambda \gamma^5 e^\lambda) - \frac{1}{4} \bar{\nu}_\lambda M_{\lambda\kappa}^R (1 - \gamma_5) \hat{\nu}_\kappa - \\ & \frac{1}{4} \bar{\nu}_\lambda M_{\lambda\kappa}^R (1 - \gamma_5) \hat{\nu}_\kappa + \frac{ig}{2M\sqrt{2}} \phi^+ (-m_d^\kappa (\bar{u}_j^\lambda C_{\lambda\kappa} (1 - \gamma^5) d_j^\kappa) + m_u^\lambda (\bar{u}_j^\lambda C_{\lambda\kappa} (1 + \gamma^5) d_j^\kappa) + \\ & \frac{ig}{2M\sqrt{2}} \phi^- (m_d^\lambda (\bar{d}_j^\lambda C_{\lambda\kappa}^\dagger (1 + \gamma^5) u_j^\kappa) - m_u^\kappa (\bar{d}_j^\lambda C_{\lambda\kappa}^\dagger (1 - \gamma^5) u_j^\kappa) - \frac{g}{2} \frac{m_u^\lambda}{M} H (\bar{u}_j^\lambda u_j^\lambda) - \\ & \frac{g}{2} \frac{m_d^\lambda}{M} H (\bar{d}_j^\lambda d_j^\lambda) + \frac{ig}{2} \frac{m_d^\lambda}{M} \phi^0 (\bar{u}_j^\lambda \gamma^5 u_j^\lambda) - \frac{ig}{2} \frac{m_d^\lambda}{M} \phi^0 (\bar{d}_j^\lambda \gamma^5 d_j^\lambda) + \bar{G}^a \partial^2 G^a + g_s f^{abc} \partial_\mu \bar{G}^a G^b g_\mu^c + \\ & \bar{X}^+ (\partial^2 - M^2) X^+ + \bar{X}^- (\partial^2 - M^2) X^- + \bar{X}^0 (\partial^2 - \frac{M^2}{c_w^2}) X^0 + \bar{Y} \partial^2 Y + igc_w W_\mu^+ (\partial_\mu \bar{X}^0 X^- - \\ & \partial_\mu \bar{X}^+ X^0) + ig s_w W_\mu^+ (\partial_\mu \bar{Y} X^- - \partial_\mu \bar{X}^+ Y) + igc_w W_\mu^- (\partial_\mu \bar{X}^- X^0 - \\ & \partial_\mu \bar{X}^0 X^+) + ig s_w W_\mu^- (\partial_\mu \bar{X}^- Y - \partial_\mu \bar{Y} X^+) + igc_w Z_\mu^0 (\partial_\mu \bar{X}^+ X^+ - \\ & \partial_\mu \bar{X}^- X^-) + ig s_w A_\mu (\partial_\mu \bar{X}^+ X^+ - \\ & \partial_\mu \bar{X}^- X^-) - \frac{1}{2} g M (\bar{X}^+ X^+ H + \bar{X}^- X^- H + \frac{1}{c_w^2} \bar{X}^0 X^0 H) + \frac{1-2c_w^2}{2c_w} ig M (\bar{X}^+ X^0 \phi^+ - \bar{X}^- X^0 \phi^-) + \\ & \frac{1}{2c_w} ig M (\bar{X}^0 X^- \phi^+ - \bar{X}^0 X^+ \phi^-) + ig M s_w (\bar{X}^0 X^- \phi^+ - \bar{X}^0 X^+ \phi^-) + \\ & \frac{1}{2} ig M (\bar{X}^+ X^+ \phi^0 - \bar{X}^- X^- \phi^0) . \end{aligned}$$

# THE LAGRANGIAN

$$\mathcal{L} = \mathcal{L}_{gauge} + \mathcal{L}_{Yukawa} + \mathcal{L}_{Higgs},$$

$$\mathcal{L}_{gauge} = -\frac{1}{4}G_{\mu\nu}^a G_{\mu\nu}^a - \frac{1}{4}W_{\mu\nu}^i W_{\mu\nu}^i - \frac{1}{4}B_{\mu\nu} B_{\mu\nu} + i\bar{L}_\alpha \gamma^\mu D_\mu L_\alpha + i\bar{Q}_\alpha \gamma^\mu D_\mu Q_\alpha + i\bar{E}_\alpha \gamma^\mu D_\mu E_\alpha + i\bar{U}_\alpha \gamma^\mu D_\mu U_\alpha + i\bar{D}_\alpha \gamma^\mu D_\mu D_\alpha + (D_\mu H)^\dagger (D_\mu H),$$

$$+ i\bar{N}_\alpha \gamma^\mu \partial_\mu N_\alpha$$

possible right handed neutrino ?

$$\mathcal{L}_{Yukawa} = y_{\alpha\beta}^L \bar{L}_\alpha E_\beta H + y_{\alpha\beta}^D \bar{Q}_\alpha D_\beta H + y_{\alpha\beta}^U \bar{Q}_\alpha U_\beta \tilde{H} + h.c.,$$

$$+ y_{\alpha\beta}^N \bar{L}_\alpha N_\beta \tilde{H}$$

$$\mathcal{L}_{Higgs} = -V = m^2 H^\dagger H - \frac{\lambda}{2} (H^\dagger H)^2$$

All these parameters are not predicted by the SM and determined experimentally

Three gauge couplings

Three or four Yukawa matrices

Two parameters

# Quantum Numbers of Matter

## ➤ Quarks

$$Q_L = \begin{pmatrix} up \\ down \end{pmatrix}_L$$

$$U_R = up_R$$

$$D_R = down_R$$

## ➤ Leptons

$$L_L = \begin{pmatrix} \nu \\ e \end{pmatrix}_L$$

$$N_R = \nu_R ?$$

$$E_R = e_R$$

SU(3)<sub>c</sub>      SU(2)<sub>L</sub>      U<sub>Y</sub>(1)

3	2	1/3
3	1	4/3
3	1	-2/3

1	2	-1
1	1	0
1	1	-2

# Quantum Numbers of Matter

## ➤ Quarks

$$Q_L = \begin{pmatrix} up \\ down \end{pmatrix}_L$$

$$U_R = up_R$$

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triplets

	SU(3) <sub>c</sub>	SU(2) <sub>L</sub>	U <sub>Y</sub> (1)
$Q_L$	3	2	1/3
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$$E_R = e_R$$

	SU(3) <sub>c</sub>	SU(2) <sub>L</sub>	U <sub>Y</sub> (1)	
	3	2	1/3	doublets
	3	1	4/3	
	3	1	-2/3	

triplets

doublets

1	2	-1
1	1	0
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# Quantum Numbers of Matter

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triplets

SU(3)<sub>c</sub>

SU(2)<sub>L</sub>

U<sub>Y</sub>(1)

doublets

3	2	1/3
3	1	4/3
3	1	-2/3

singlets

1	2	-1
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# Quantum Numbers of Matter

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$$L_L = \begin{pmatrix} \nu \\ e \end{pmatrix}_L$$

$$N_R = \nu_R ?$$

$$E_R = e_R$$

triplets

V-A currents  
in weak  
interactions

SU(3)<sub>c</sub>

SU(2)<sub>L</sub>

U<sub>Y</sub>(1)

doublets

3	2	1/3
3	1	4/3
3	1	-2/3

singlets

1	2	-1
1	1	0
1	1	-2



# Quantum Numbers of Matter

## ➤ Quarks

$$Q_L = \begin{pmatrix} up \\ down \end{pmatrix}_L$$

$$U_R = up_R$$

$$D_R = down_R$$

## ➤ Leptons

$$L_L = \begin{pmatrix} \nu \\ e \end{pmatrix}_L \quad \begin{matrix} \frac{1}{2} \\ -\frac{1}{2} \end{matrix} \begin{matrix} \nearrow \\ \searrow \end{matrix} T_3$$

$$N_R = \nu_R ?$$

$$E_R = e_R$$

triplets

V-A currents  
in weak  
interactions

	SU(3) <sub>c</sub>	SU(2) <sub>L</sub>	U <sub>Y</sub> (1)
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doublets

singlets

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# Quantum Numbers of Matter

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$$Q_L = \begin{pmatrix} up \\ down \end{pmatrix}_L$$

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triplets

V-A currents  
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	SU(3) <sub>c</sub>	SU(2) <sub>L</sub>	U <sub>Y</sub> (1)	
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## ➤ Leptons

$$L_L = \begin{pmatrix} \nu \\ e \end{pmatrix}_L$$

$$N_R = \nu_R ?$$

$$E_R = e_R$$

$$\begin{matrix} \frac{1}{2} \\ -\frac{1}{2} \\ 0 \\ 0 \end{matrix} \begin{matrix} \nearrow \\ \searrow \\ \nearrow \\ \searrow \end{matrix} T_3$$

$L_L$	1	2	-1
$N_R$	1	1	0
$E_R$	1	1	-2

singlets

Electric charge

$$Q = T_3 + Y/2$$

# Quarks – “the building blocks of the Universe”

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Charm came as surprise but completed the picture



# Quarks – “the building blocks of the Universe”



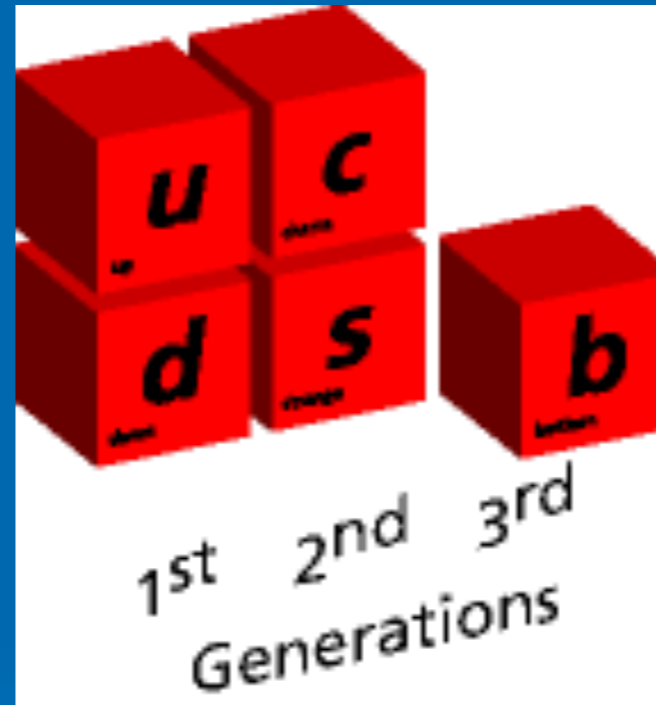
Charm came as surprise but completed the picture



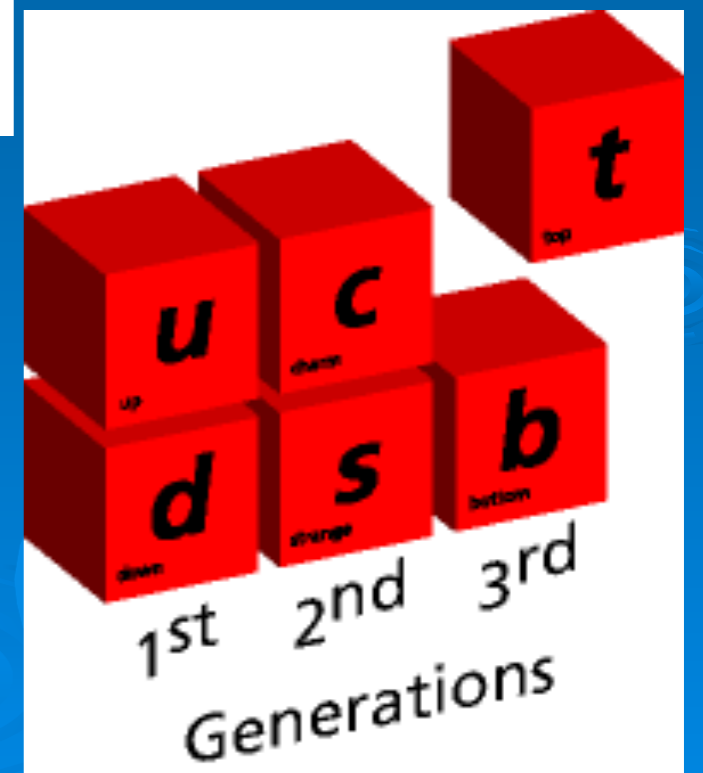
# Quarks – “the building blocks of the Universe”



Charm came as surprise but completed the picture



The number of quarks increased with discoveries of new particles and have reached 6



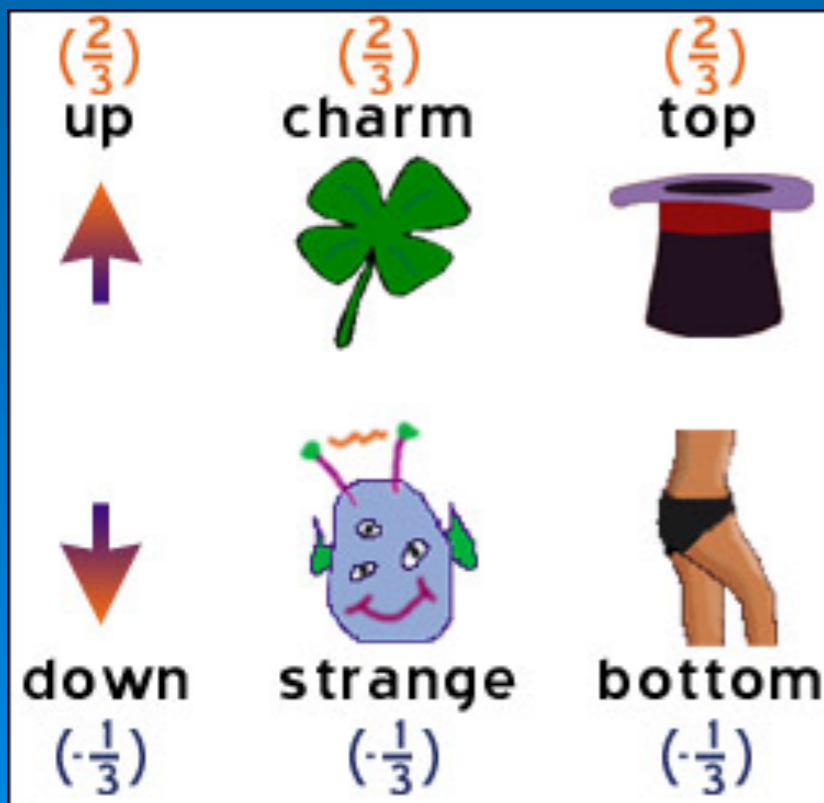
# Quarks – “the building blocks of the Universe”



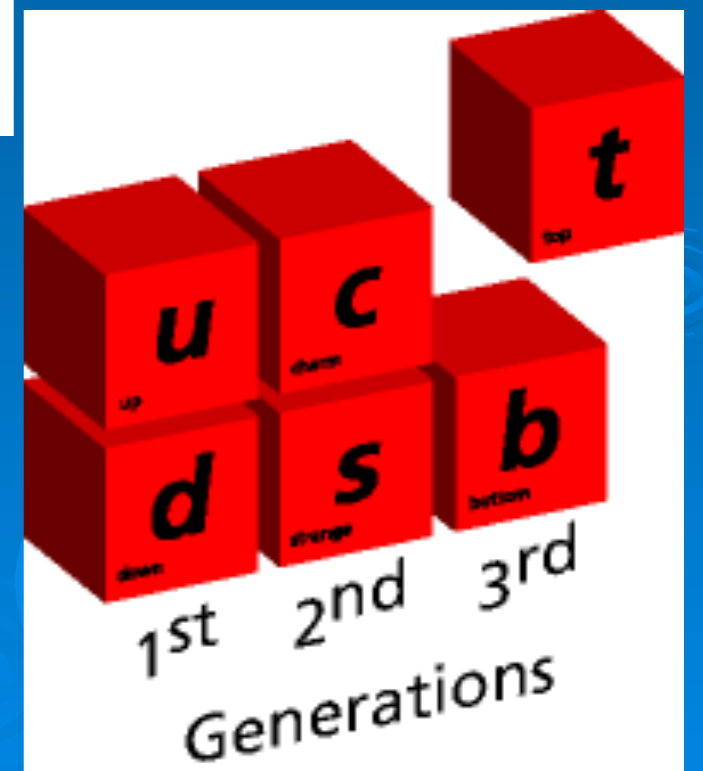
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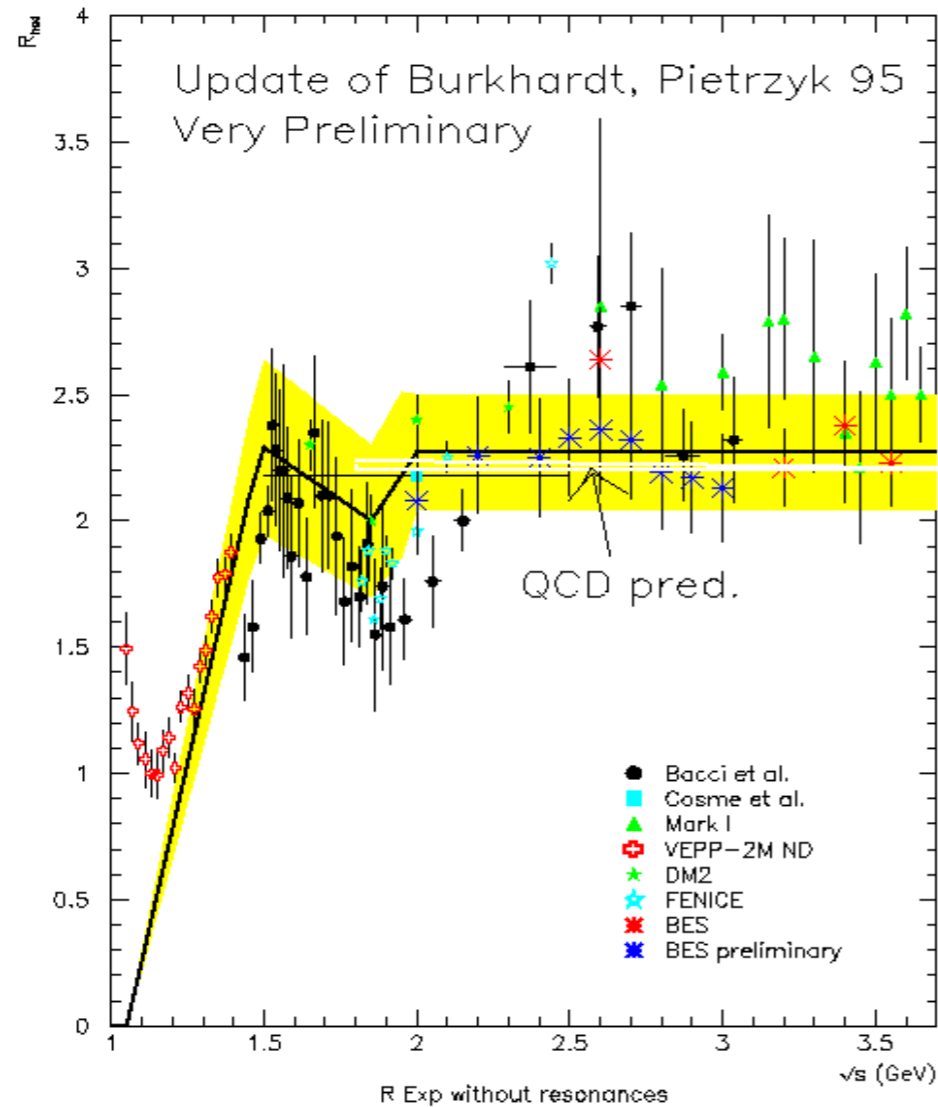


For unknown reasons Nature created 3 copies (generations) of quarks and leptons





# The Number of Colours

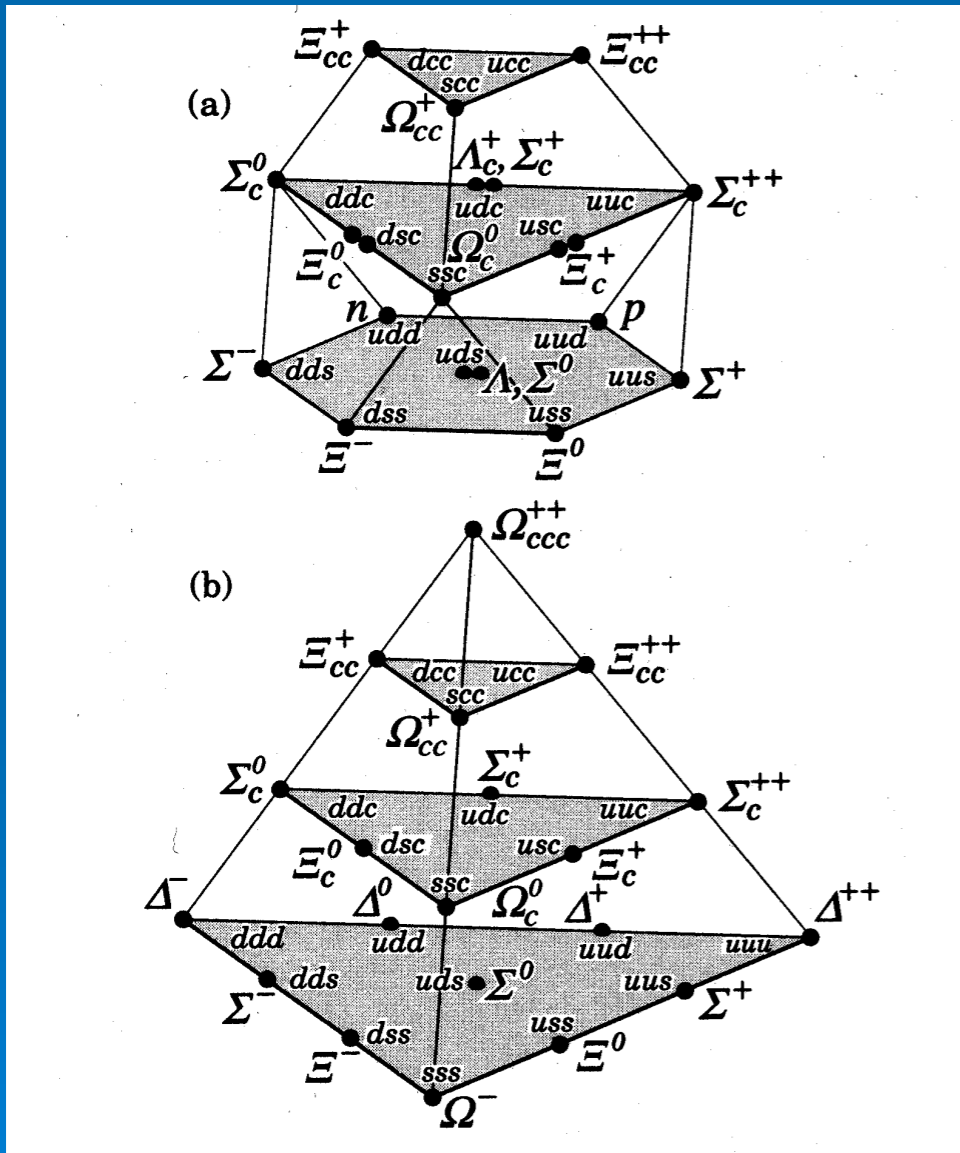


➤ The x-section of electron-positron annihilation into hadrons is proportional to the number of quark colours. The fit to experimental data at various colliders at different energies gives

$$N_c = 3.06 \pm 0.10$$

# Quark's Colour

Baryons are “made” of quarks



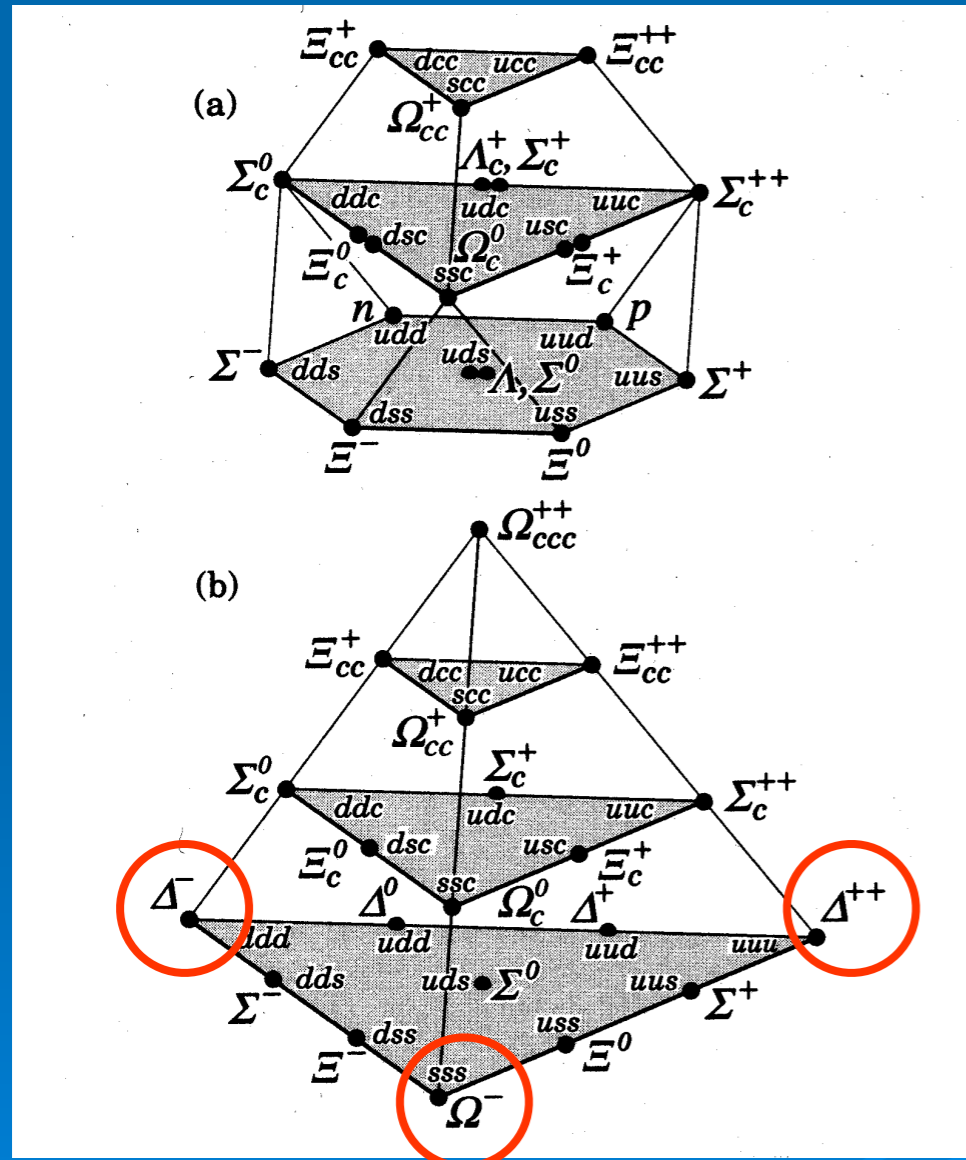
$$\Delta^- (d \uparrow d \uparrow d \uparrow)$$

$$\Omega^- (s \uparrow s \uparrow s \uparrow)$$

$$\Delta^{++} (u \uparrow u \uparrow u \uparrow)$$

# Quark's Colour

Baryons are “made” of quarks



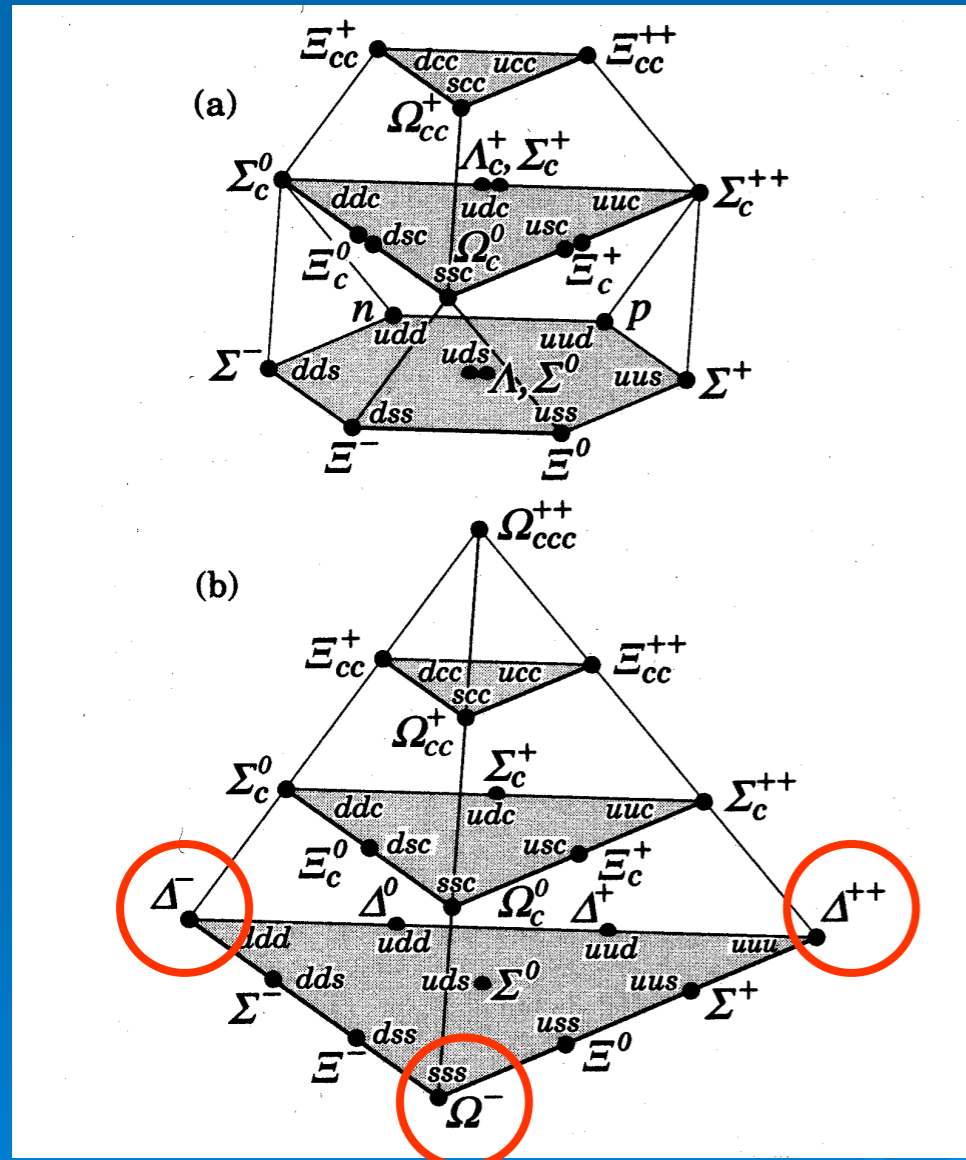
$$\Delta^- (d \uparrow d \uparrow d \uparrow)$$

$$\Omega^- (s \uparrow s \uparrow s \uparrow) \quad ?$$

$$\Delta^{++} (u \uparrow u \uparrow u \uparrow)$$

# Quark's Colour

Baryons are “made” of quarks



$$\Delta^- (d \uparrow d \uparrow d \uparrow)$$

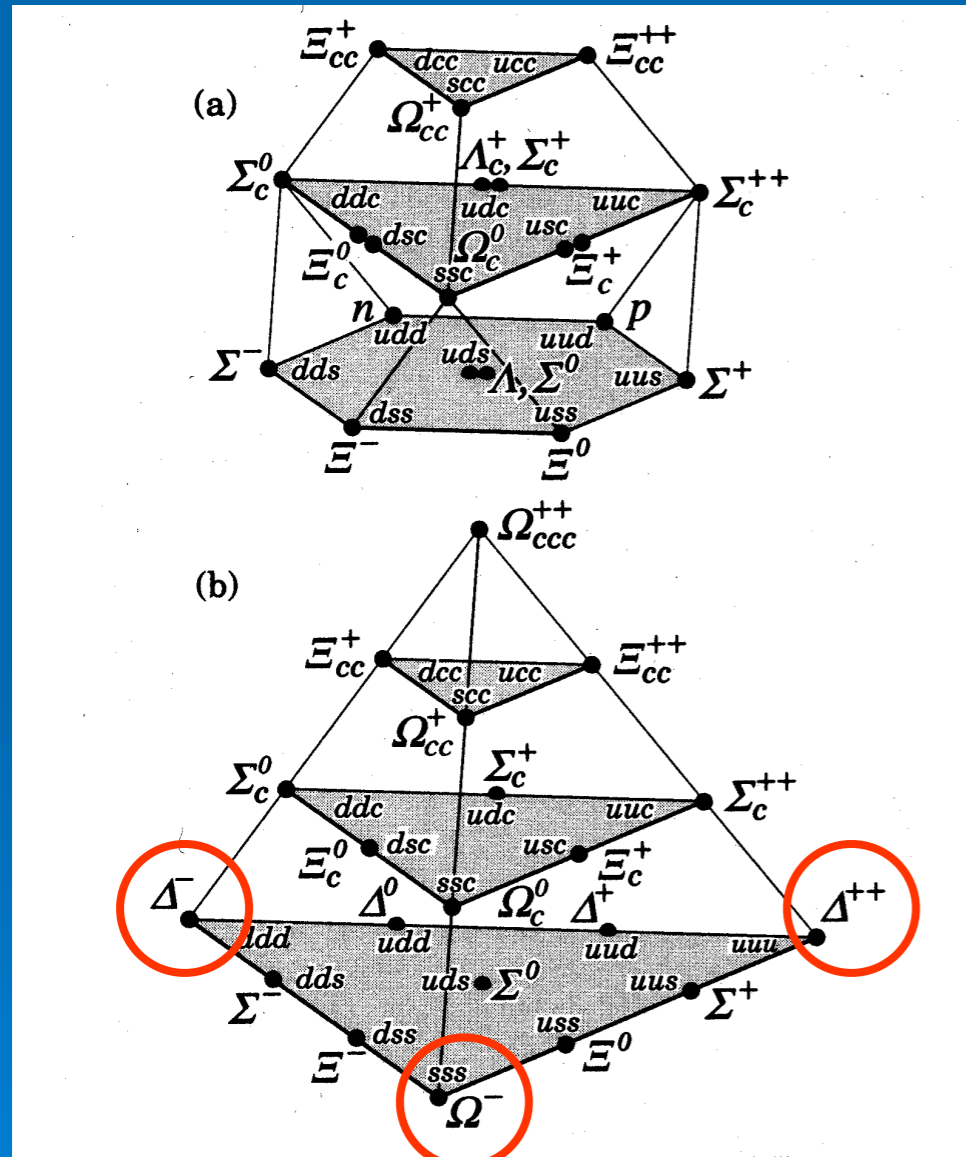
$$\Omega^- (s \uparrow s \uparrow s \uparrow) \quad ?$$

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To avoid Pauli principle veto one can antisymmetrize the wave function introducing a new quantum number - “colour”, so that

# Quark's Colour

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$$\Delta^- (d \uparrow d \uparrow d \uparrow)$$

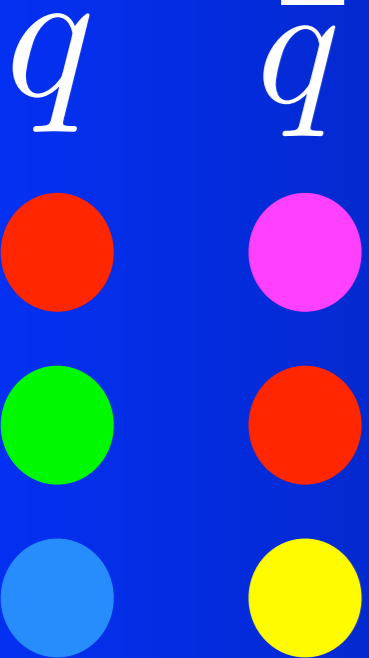
$$\Omega^- (s \uparrow s \uparrow s \uparrow) \quad ?$$

$$\Delta^{++} (u \uparrow u \uparrow u \uparrow)$$

To avoid Pauli principle veto one can antisymmetrize the wave function introducing a new quantum number - “colour”, so that

$$\Delta^- = \epsilon^{ijk} (d_i \uparrow d_j \uparrow d_k \uparrow)$$

# Colored quarks



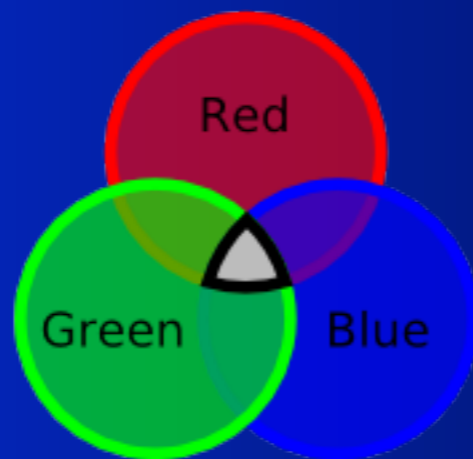
Each flavour of quarks can have three color charges: **red**, **green**, **blue**

Antiquarks have three anticolors: anti**red** - **violet**, anti**green** - **red**, anti**blue** - **yellow**

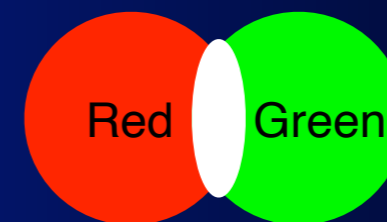
Gluons have eight colors: **red-antiblue**, **green-antired**, ...



All bound states of quarks, baryons and mesons - colorless!



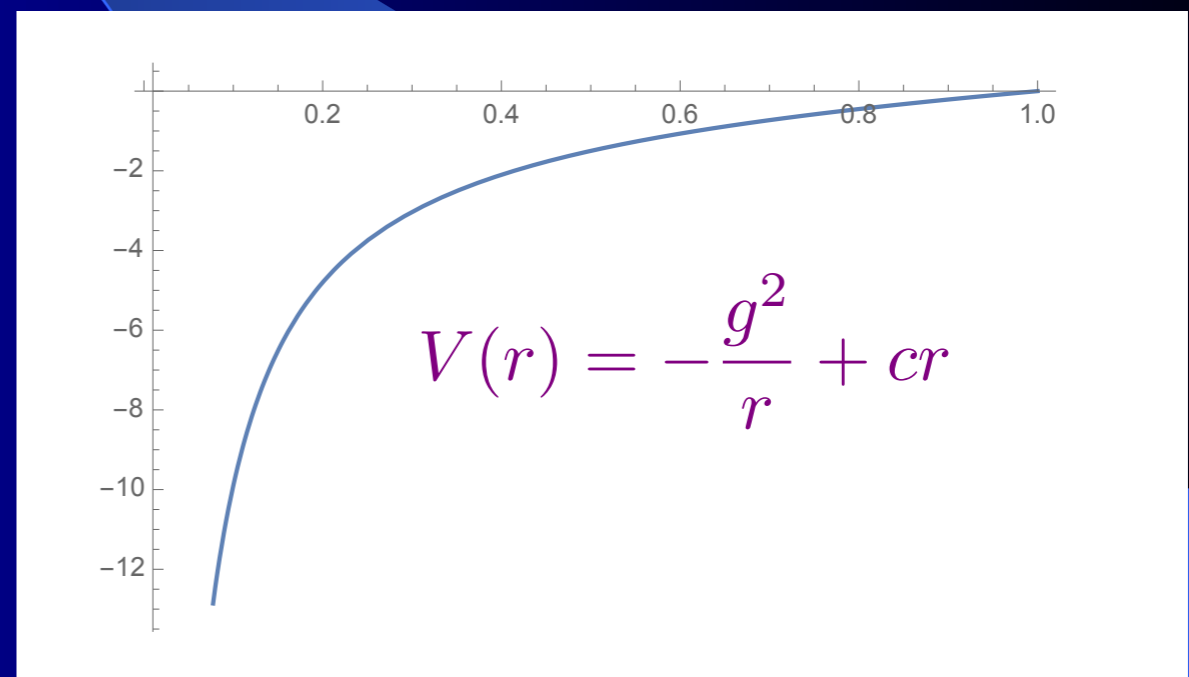
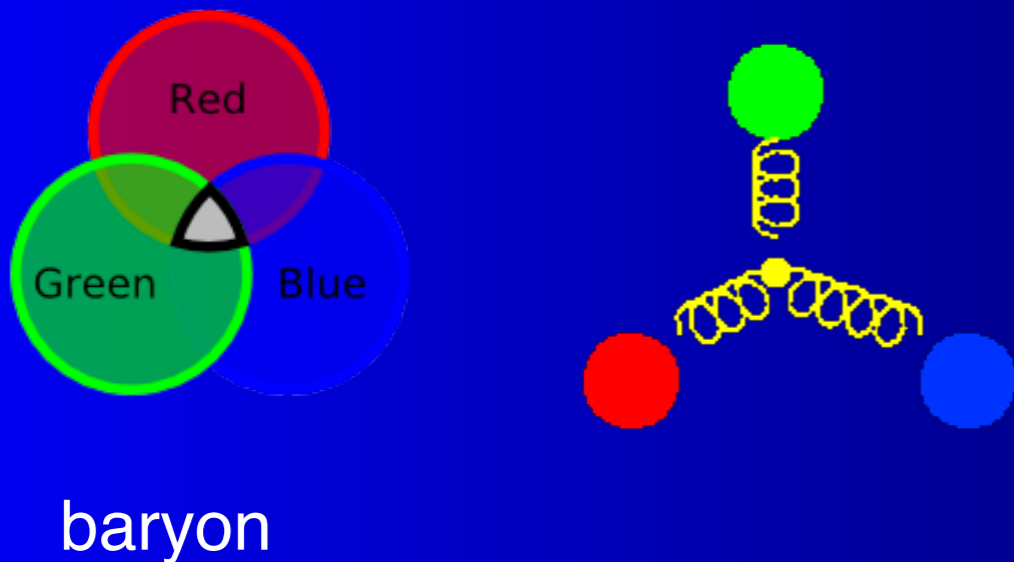
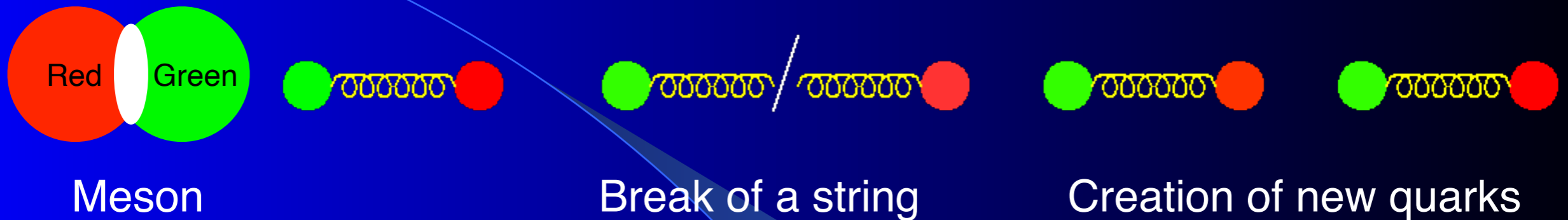
baryon



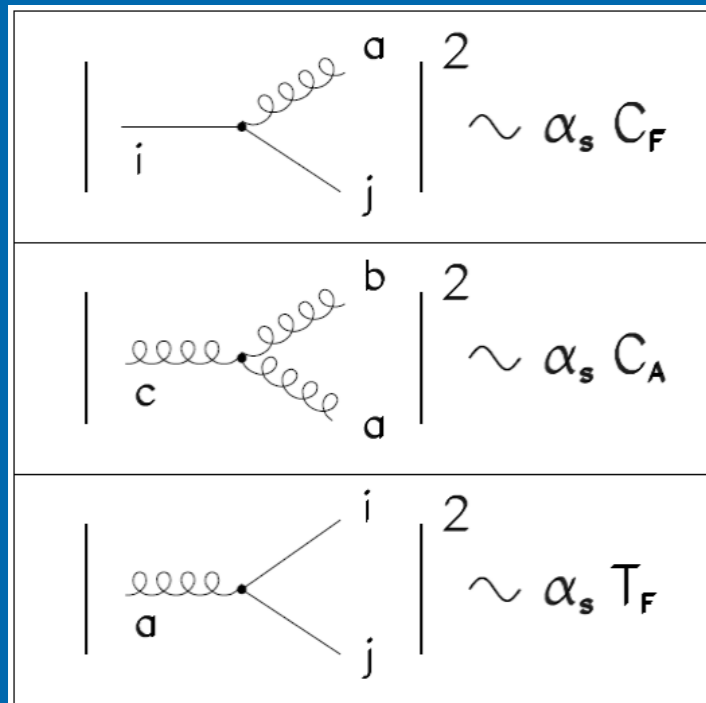
meson

# Hypothesis of quark confinement

Quarks are confined inside hadrons due to interactions with gluons, which form strings stretched between quarks



# The group structure of the SM



$$\sum_{a=1}^{N_A} (T^a T^{\dagger a})_{ij} = \delta_{ij} C_F \quad , \quad \sum_{i,j=1}^{N_F} T_{ij}^a T_{ji}^{\dagger b} = \delta^{ab} T_F \quad , \quad \sum_{a,b=1}^{N_A} f^{abc} f^{*abd} = \delta^{cd} C_A$$

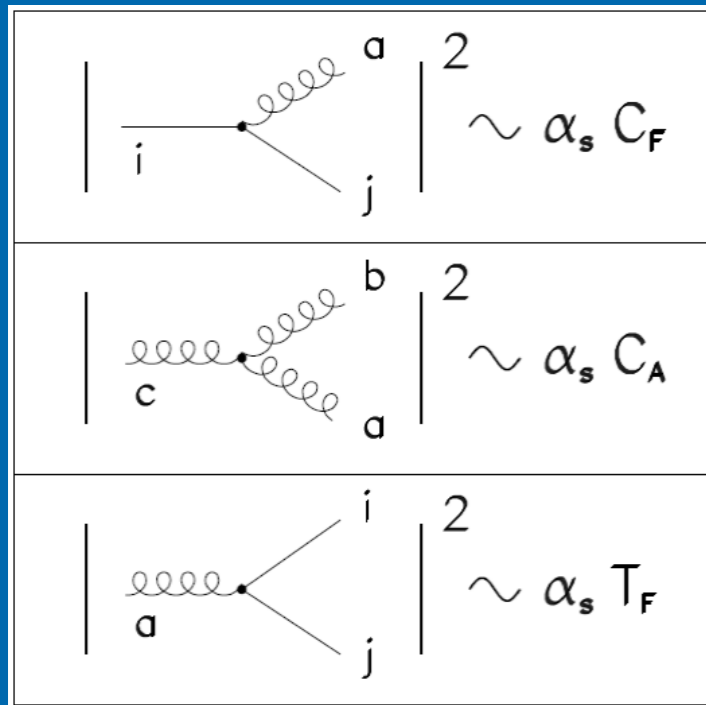
Casimir Operators

For SU(N)

$$C_A = N_C \quad , \quad C_F = \frac{N_C^2 - 1}{2N_C} \quad , \quad T_F = 1/2$$



# The group structure of the SM

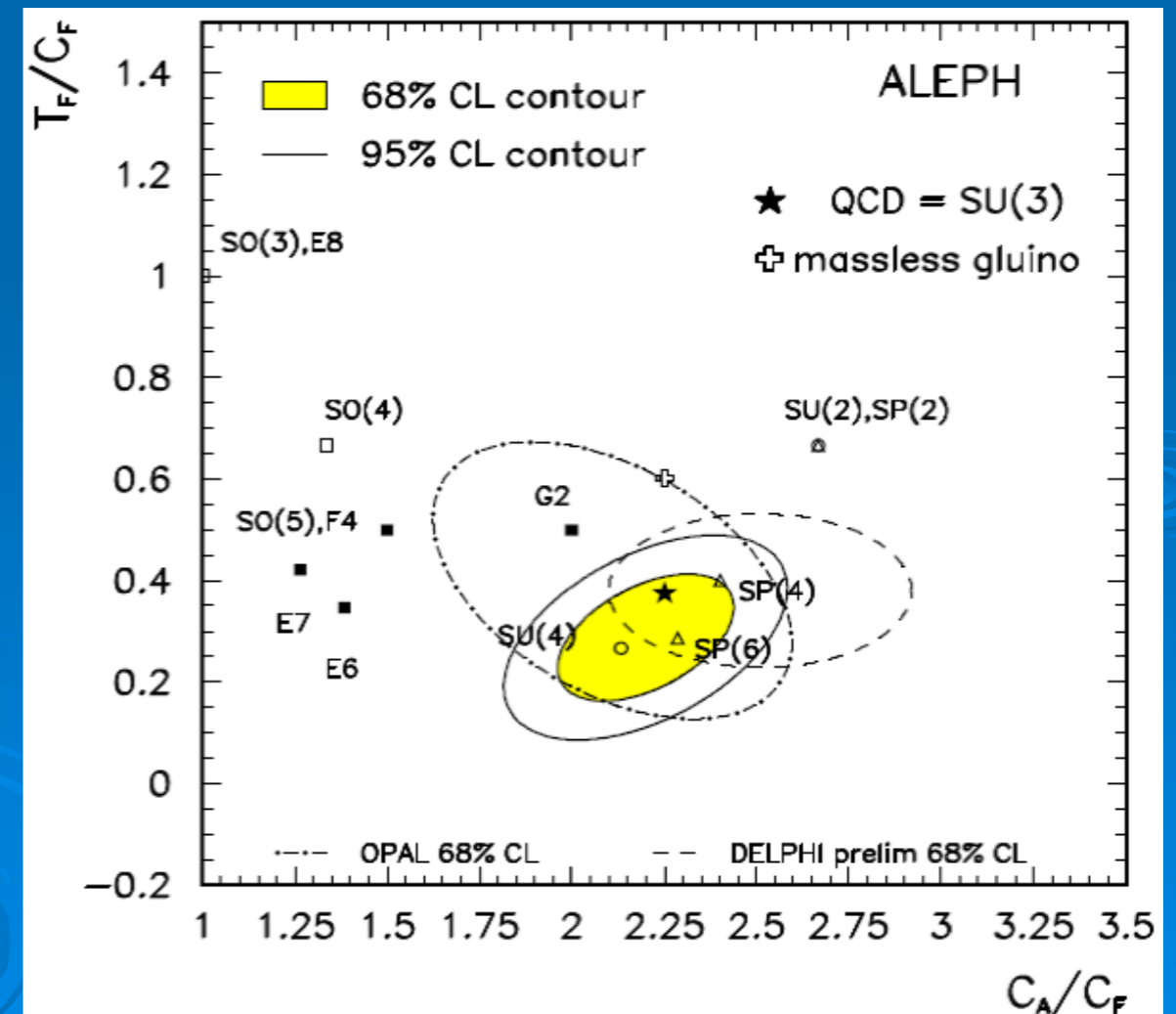


$$\sum_{a=1}^{N_A} (T^a T^{\dagger a})_{ij} = \delta_{ij} C_F \quad , \quad \sum_{i,j=1}^{N_F} T_{ij}^a T_{ji}^{\dagger b} = \delta^{ab} T_F \quad , \quad \sum_{a,b=1}^{N_A} f^{abc} f^{*abd} = \delta^{cd} C_A$$

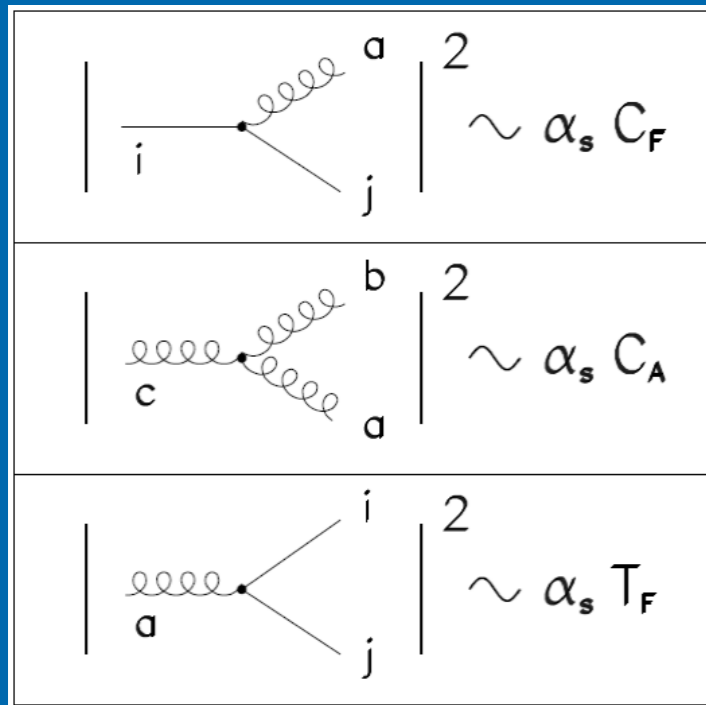
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# The group structure of the SM



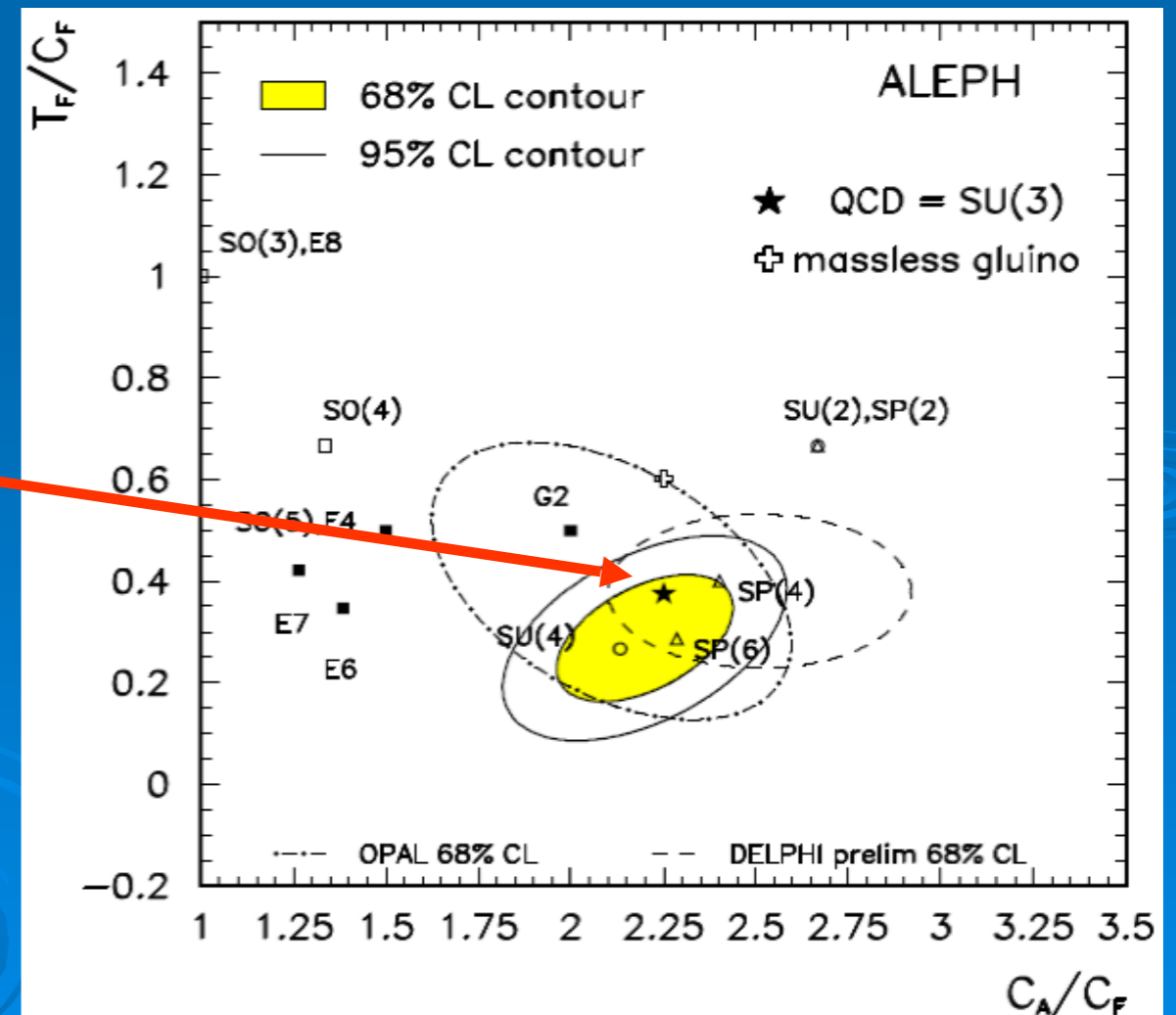
$$\sum_{a=1}^{N_A} (T^a T^{\dagger a})_{ij} = \delta_{ij} C_F, \quad \sum_{i,j=1}^{N_F} T_{ij}^a T_{ji}^{\dagger b} = \delta^{ab} T_F, \quad \sum_{a,b=1}^{N_A} f^{abc} f^{*abd} = \delta^{cd} C_A$$

Casimir Operators

For SU(N)

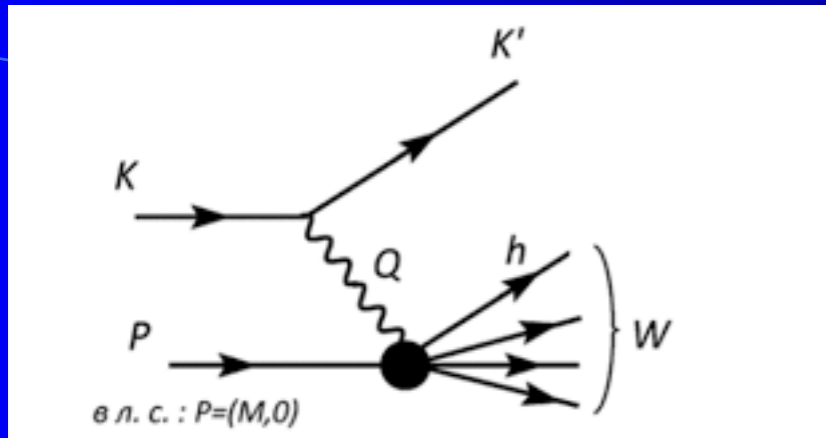
$$C_A = N_C, \quad C_F = \frac{N_C^2 - 1}{2N_C}, \quad T_F = 1/2$$

QCD analysis definitely singles out the SU(3) group as the symmetry group of strong interactions

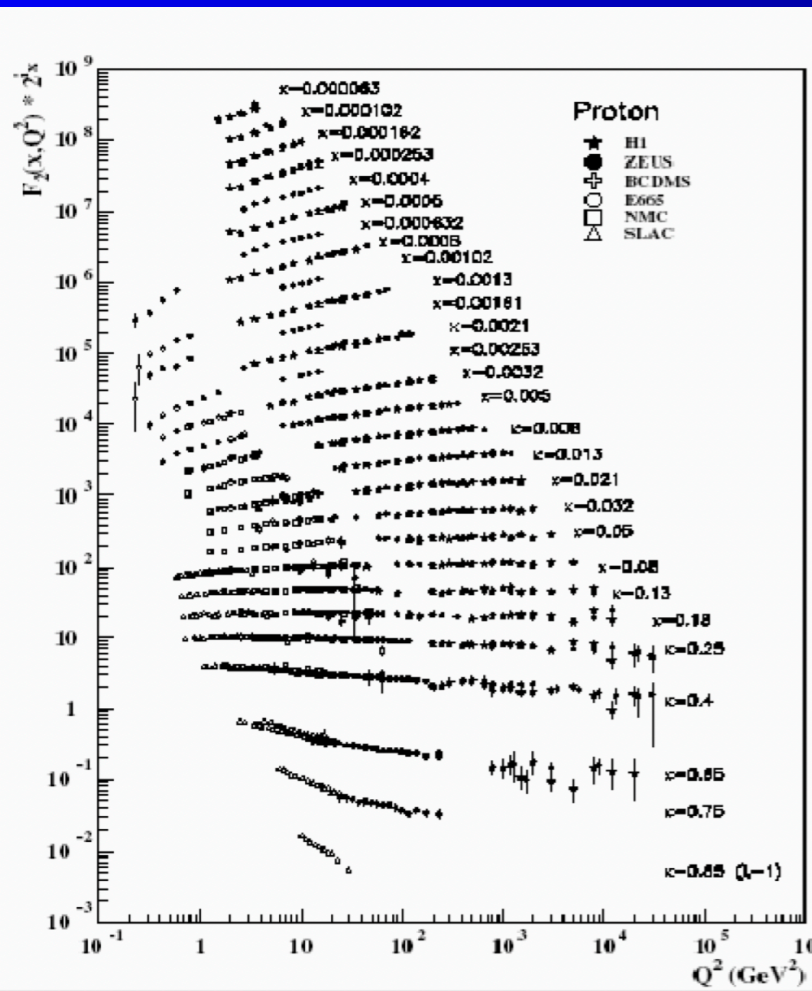
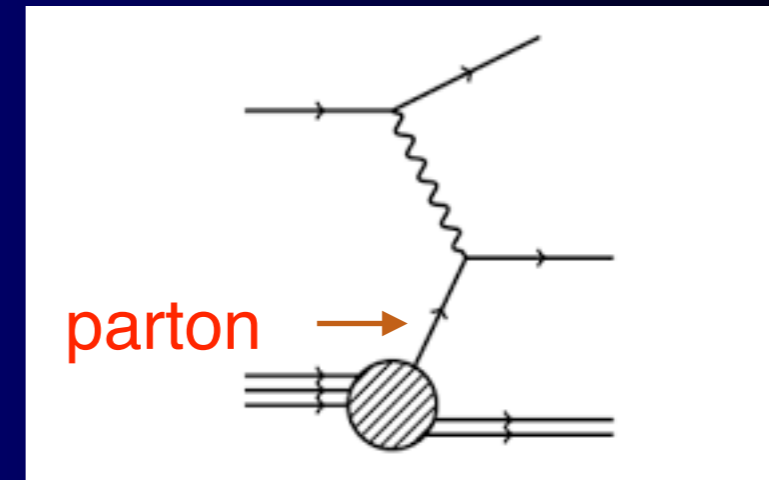


# Scattering of electrons on protons

## Parton Model



Q - transfer momentum from electron to proton

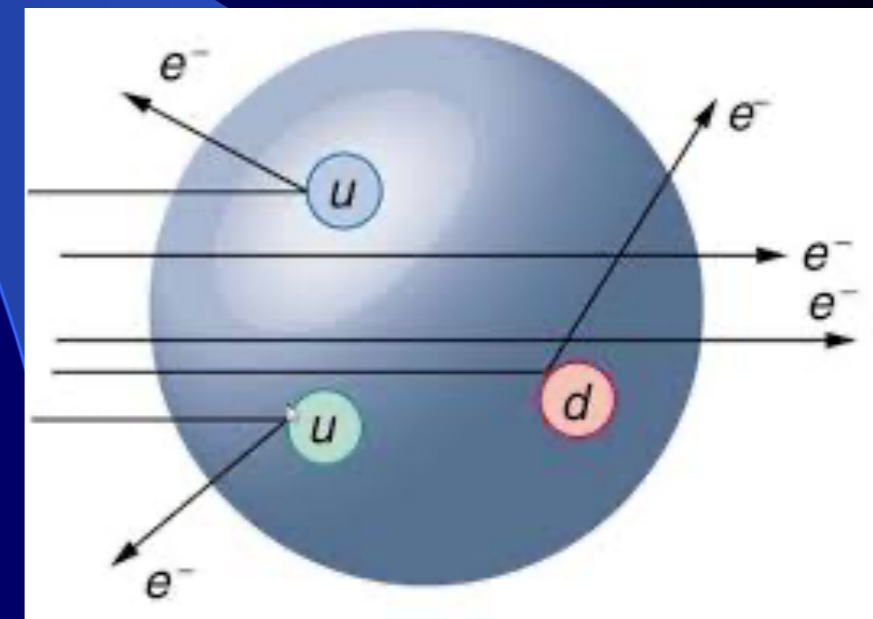


W - total energy of created hadrons

Indetification of partons as quarks

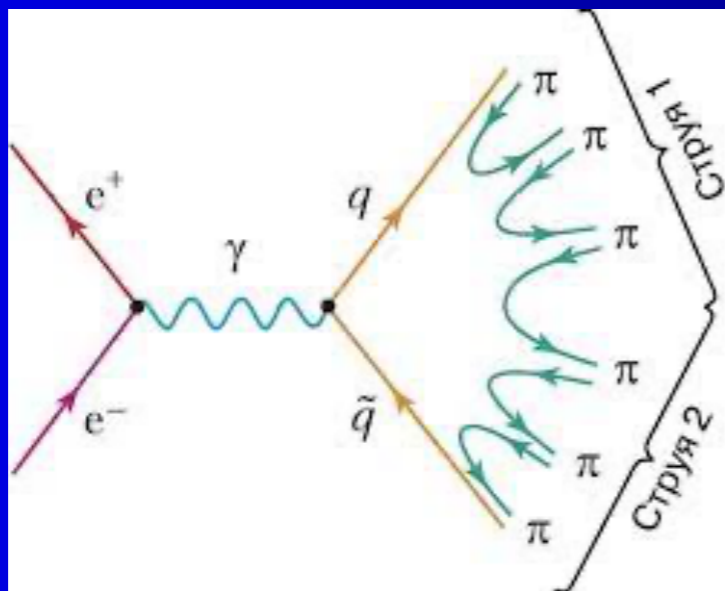
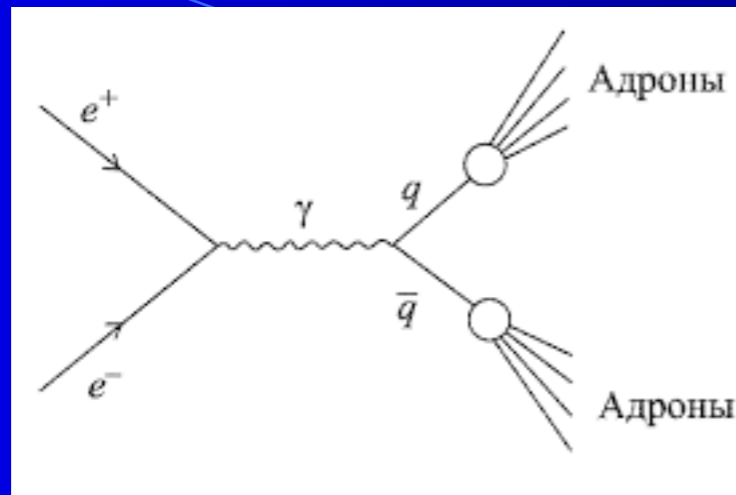
$$x = \frac{Q^2}{W^2}$$

scaling



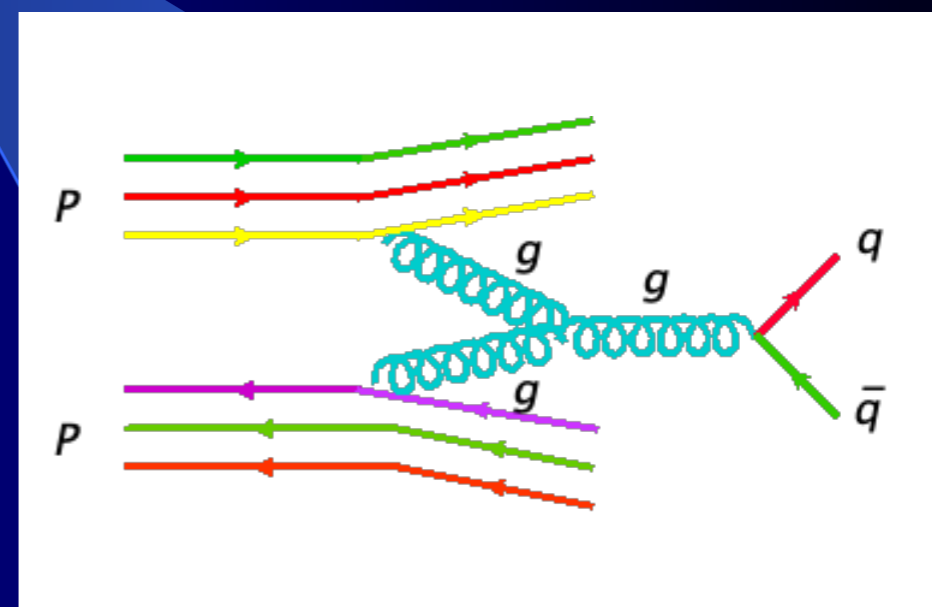
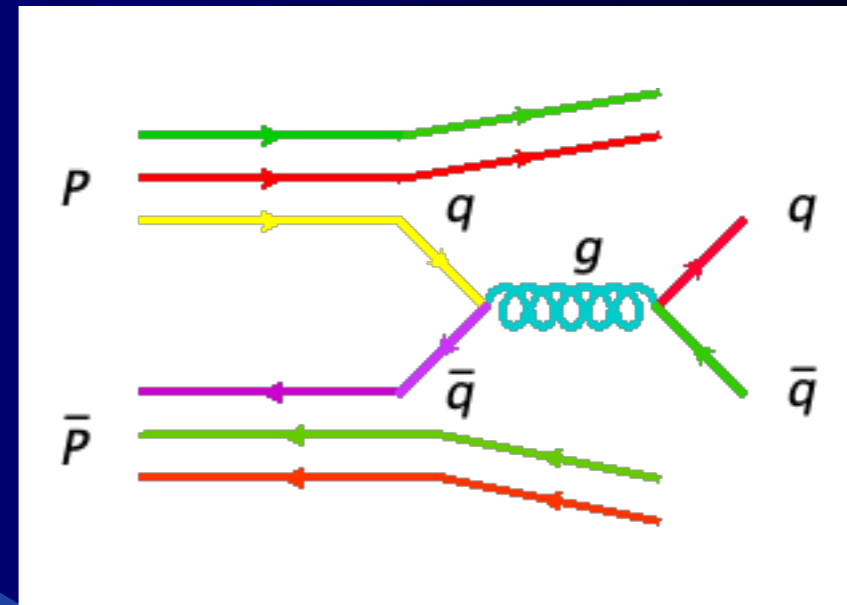
# Creation of hadrons at colliders

Electron-positron collider



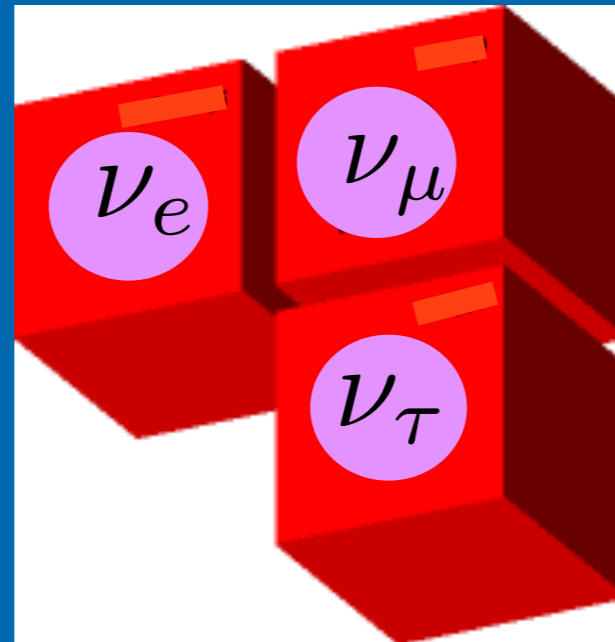
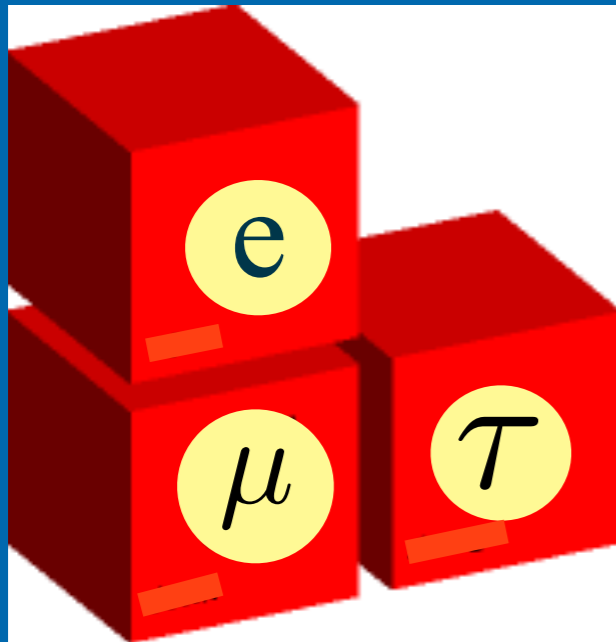
Hadrons form jets along the line of created quarks

Proton collider



Quark subprocesses

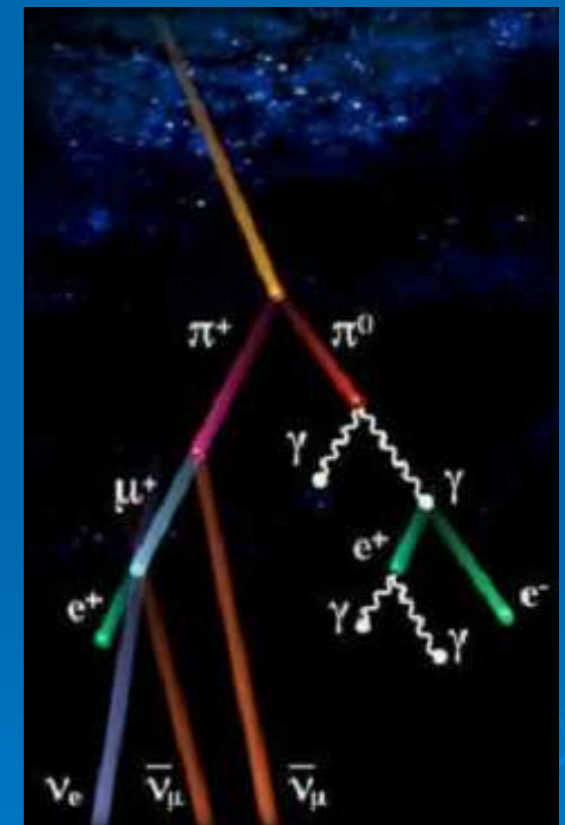
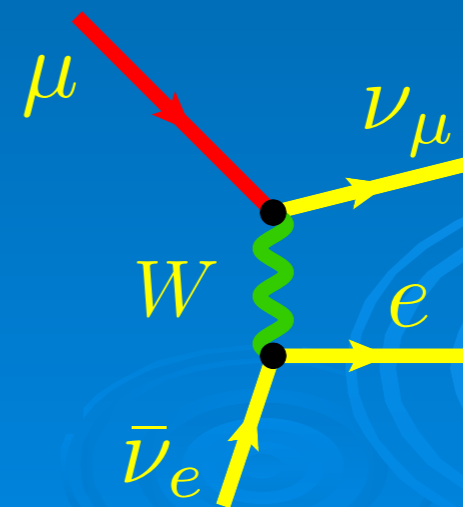
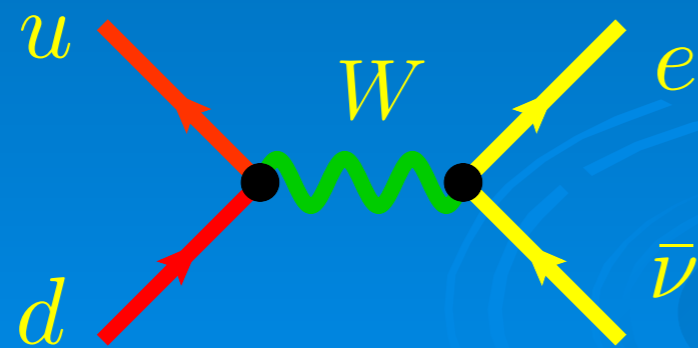
# Leptons are from λεπτός - light



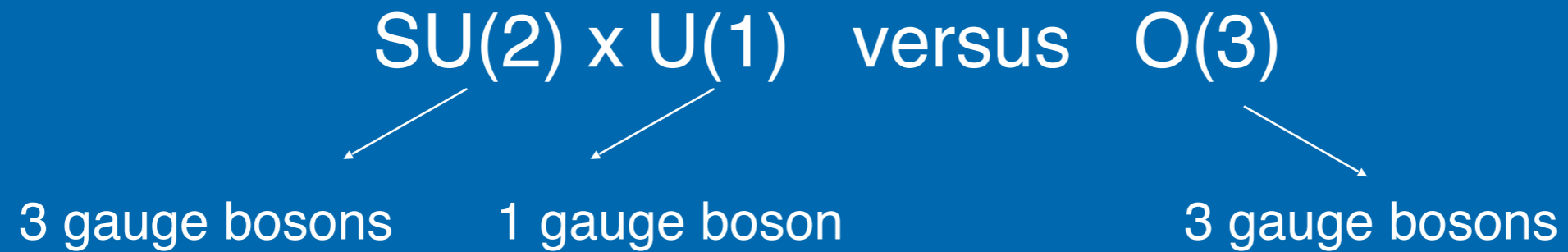
Muons are created from  $\Pi$ -mesons decay in cosmic rays and decay into electrons and two neutrinos

Electrons form atomic shells and define all chemistry of animated and unanimated nature

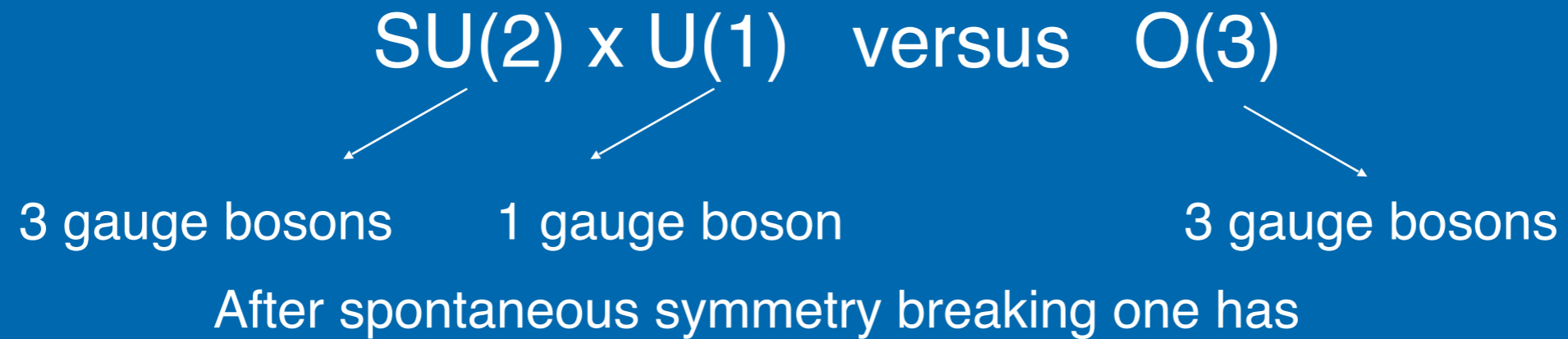
Neutrino are produced in hadron decay



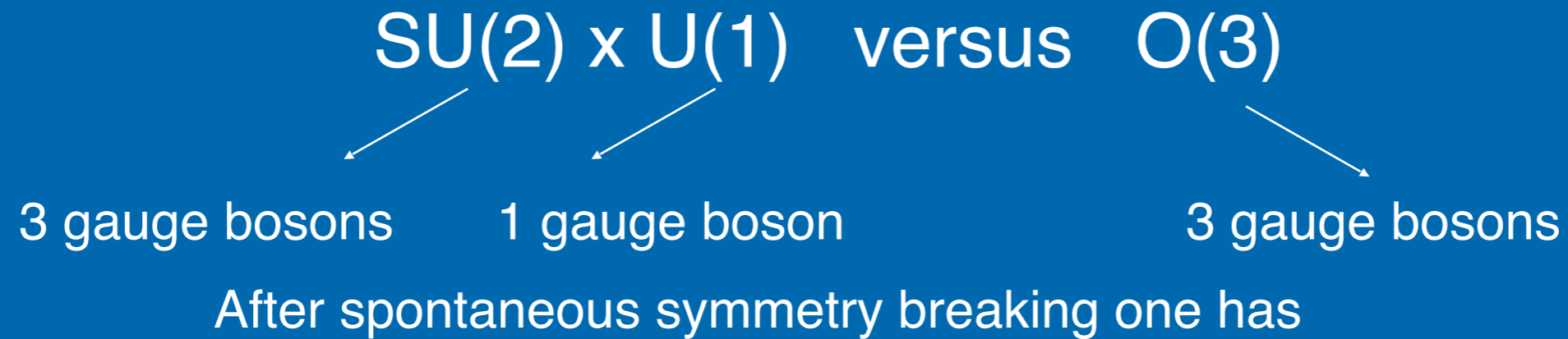
# Electro-weak sector of the SM



# Electro-weak sector of the SM



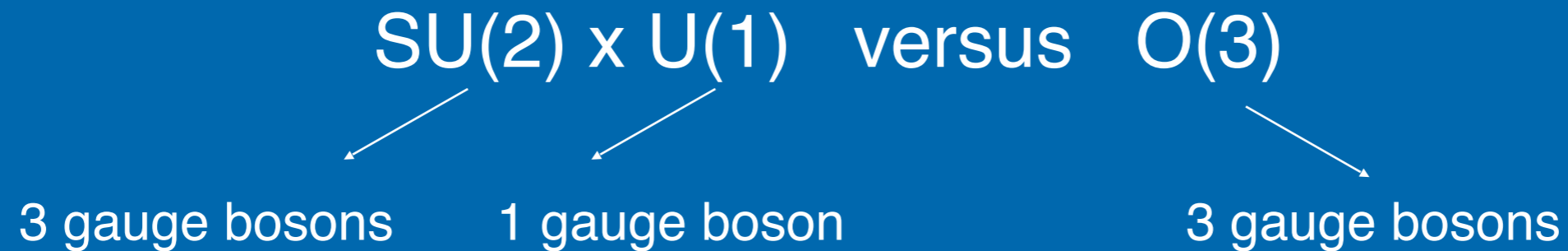
# Electro-weak sector of the SM



3 massive gauge bosons  
( $W^+$ ,  $W^-$ ,  $Z^0$ ) and 1 massless ( $\gamma$ )



# Electro-weak sector of the SM



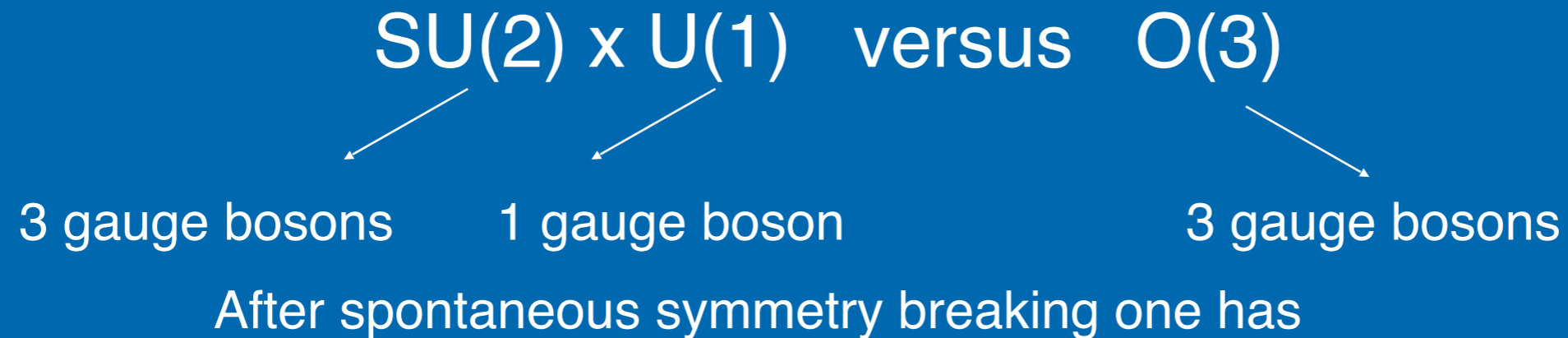
After spontaneous symmetry breaking one has

3 massive gauge bosons  
( $W^+$ ,  $W^-$ ,  $Z^0$ ) and 1 massless ( $\gamma$ )



2 massive gauge bosons  
( $W^+$ ,  $W^-$ ) and 1 massless ( $\gamma$ )

# Electro-weak sector of the SM



3 massive gauge bosons  
( $W^+$ ,  $W^-$ ,  $Z^0$ ) and 1 massless ( $\gamma$ )



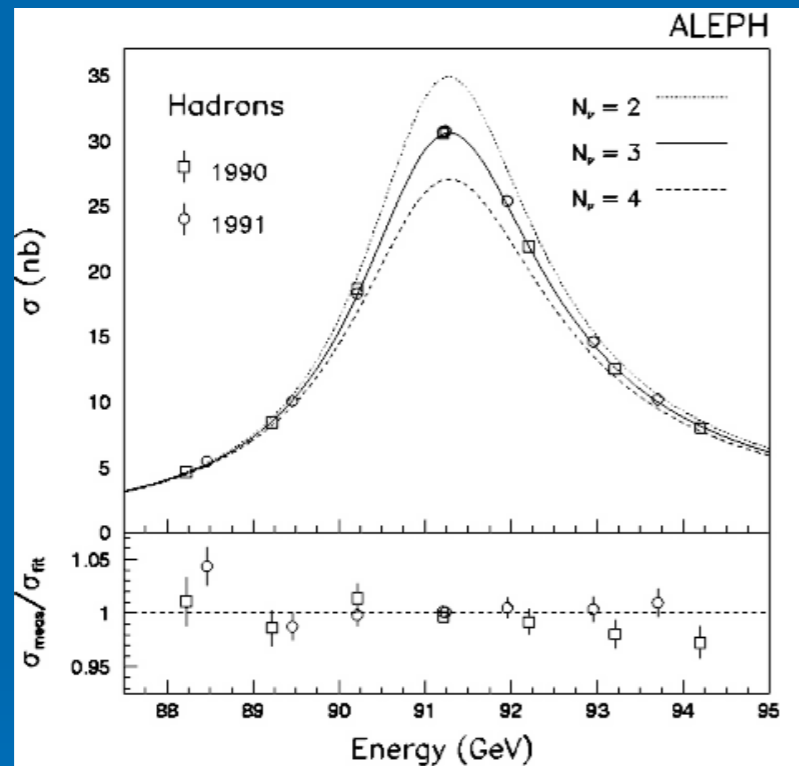
2 massive gauge bosons  
( $W^+$ ,  $W^-$ ) and 1 massless ( $\gamma$ )



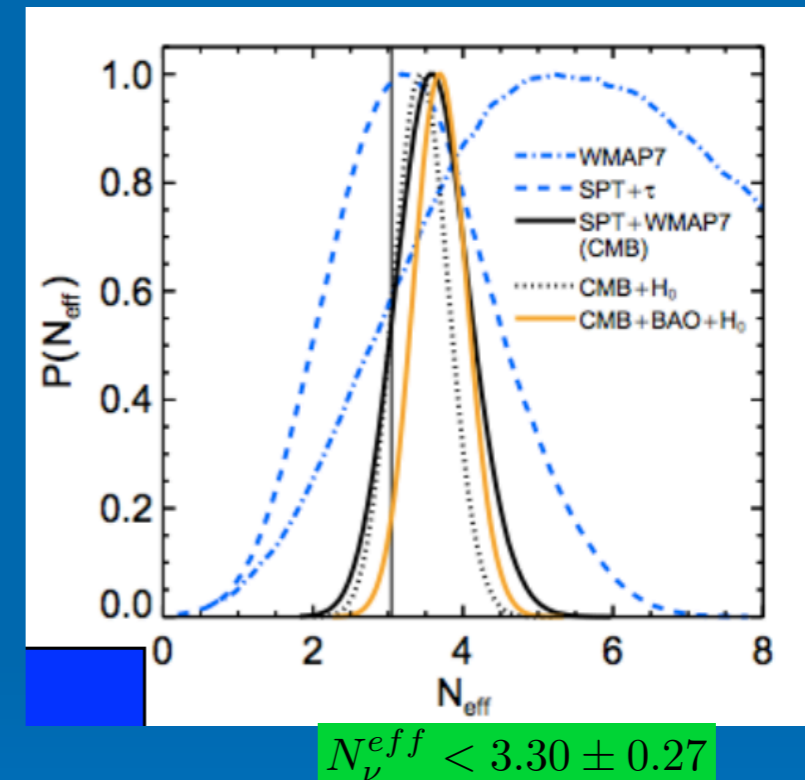
- Discovery of neutral currents was a crucial test of the gauge model of weak interactions at CERN in 1973
- The heavy photon gives the neutral current without flavour violation

# The Number of Generations

- The width of the Z-boson (LEP)



- The CMB spectrum (Planck)



➤ Z-line shape obtained at LEP depends on the number of flavours and gives the number of (light) neutrinos or (generations) of the Standard Model

➤ The shape of the CMB temperature fluctuations give the number of active neutrinos or generations of the Standard Model assuming the quark-lepton symmetry

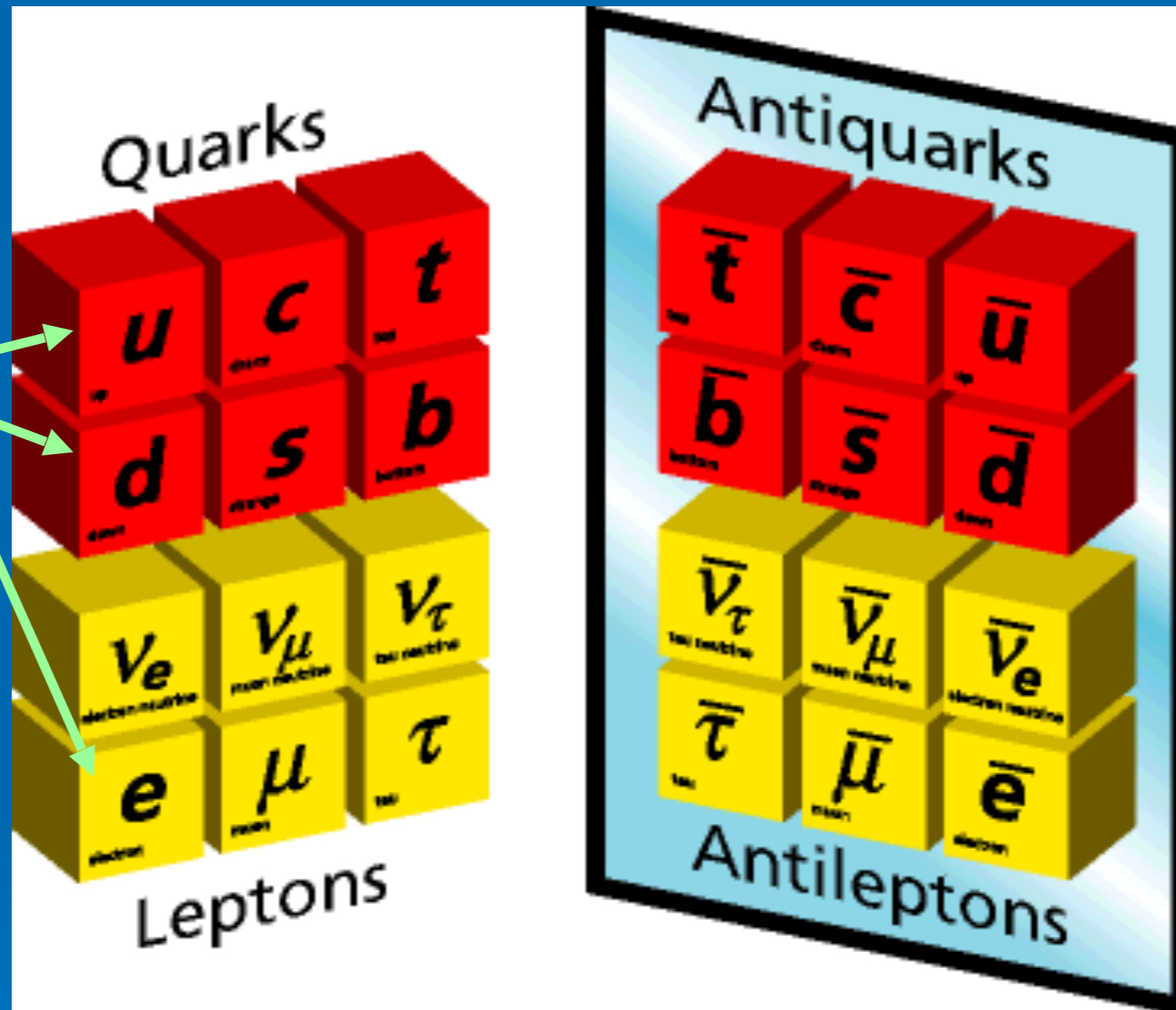
$$N_g = 2.982 \pm 0.013$$

# Flavour Sector



# Matter and Antimatter

The first generation is what we are made of



Antimatter was created together with matter during the “Big bang”

Antiparticles are created at accelerators in ensemble with particles but the visible Universe does not contain antimatter

# Interactions in the SM (Forces)

$SU(3)$

$SU(2)$

$U(1)$

**H**

The Higgs boson

# Interactions in the SM (Forces)



- Strong Interactions between quarks via gluons exchange  
Bound hadrons together, lead to nuclear forces inside the nucleus



- Weak Interactions between quarks and leptons via W and Z exchange  
Responsible for decays of hadrons and leptons



- Electromagnetic Interactions between quarks and leptons via photon exchange  
Responsible for all macro forces in Nature



The Higgs boson

- Yukawa Interactions between quarks and leptons and the Higgs boson  
Responsible for creation of masses of quarks and leptons

# Electromagnetic Interactions

1. Performed via exchange of quanta of electromagnetic field - photon
2. Electromagnetic field is described by Maxwell equations

$$\partial_\mu F_{\mu\nu} + j_\nu = 0$$

$$\partial_\mu \tilde{F}_{\mu\nu} = 0$$

$$F_{\mu\nu} = \partial_\mu A_\nu - \partial_\nu A_\mu$$

$$\partial_t \vec{E} - \vec{\nabla} \times \vec{B} = -\vec{j}$$

$$\vec{\nabla} \cdot \vec{E} = \rho$$

$$\partial_t \vec{B} + \vec{\nabla} \times \vec{E} = 0$$

$$\vec{\nabla} \cdot \vec{B} = 0$$

3. Charged particles (quarks and leptons) obey Dirac equation

$$(\hat{\partial} - m - e\hat{A})\psi = 0$$

$$\hat{\partial} = \gamma^\mu \partial_\mu$$



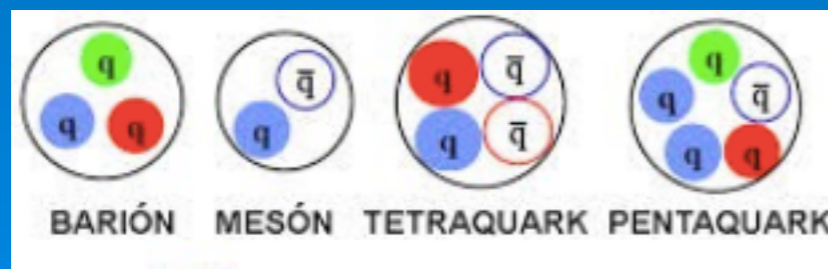
# Strong Interactions

1. Performed via exchange of quanta of gluon (color) field -gluon
2. Gluon field is described by Yang-Mills equations (generalization of Maxwell eqs)

$$D_\mu F_{\mu\nu} + j_\mu = 0$$

$$D_\mu = \partial_\mu + gA_\mu \quad F_{\mu\nu} = \partial_\mu A_\nu - \partial_\nu A_\mu + g[A_\mu, A_\nu]$$

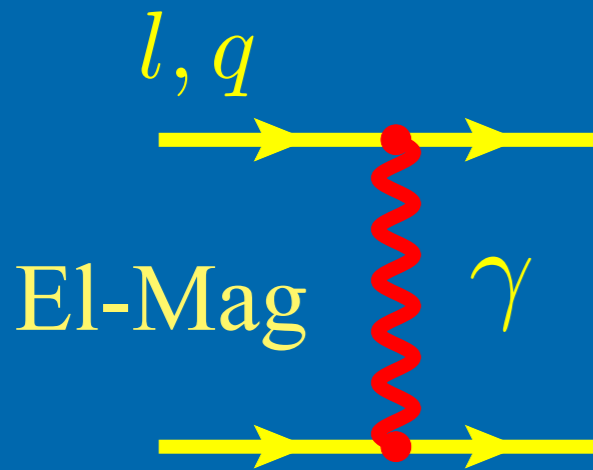
3. The main difference from Electrodynamics is that gluons carry color charge and interact with each other
4. Postulate of confinement: quarks and gluons cannot be observed in free state, only «colorless» objects are observed
5. Colorless objects appear in two combinations:  $M = \bar{q}q$  mesons and baryons  $B = qqq$
6. However, exotic hadrons are proved to exist



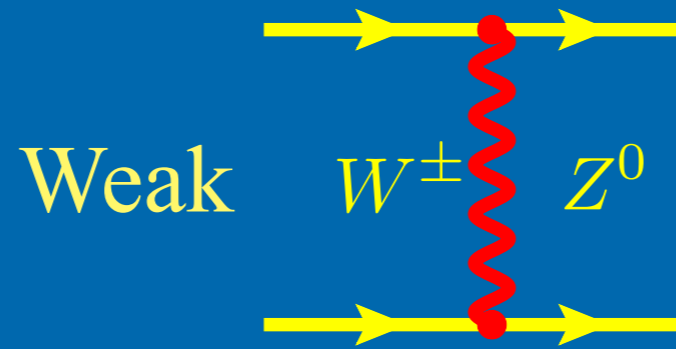
# Weak Interactions

1. Performed via exchange of intermediate weak bosons W, Z
2. The fields W and Z are described by Yang-Mills eqs  
(generalization of Maxwell eqs)
3. The fields W, Z carry weak charge (isospin) and interact with each other
4. W, Z can be observed in free state and are massive
5. Weak interactions involve quarks and leptons
6. Weak interactions are short-range  $R \sim 1/M_W$
7. Weak interactions describe decay of particles

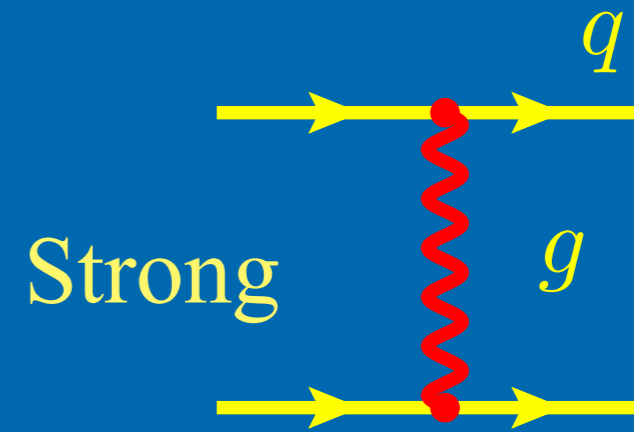
# Five fundamental forces of Nature



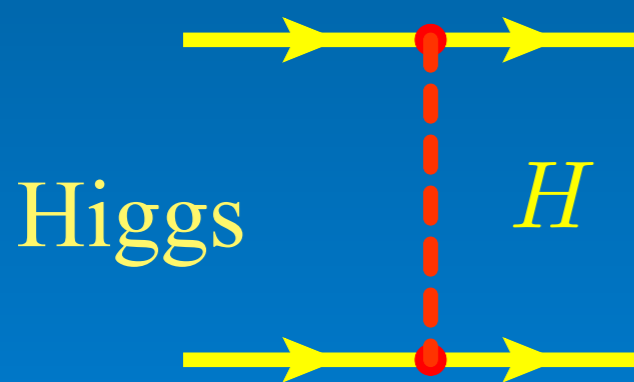
$$V(r) = -\frac{e_1 e_2}{r}$$



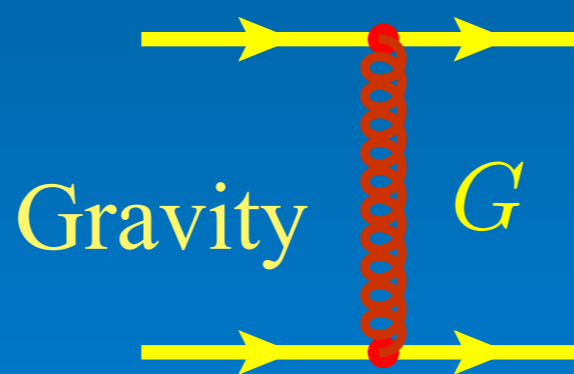
$$V(r) = -\frac{g^2}{r} e^{-M_W r}$$



$$V(r) = -\frac{g_s^2}{r} + br$$



$$V(r) = -\frac{m_1 m_2}{v_H^2 r} e^{-M_H r}$$



$$V(r) = -\frac{m_1 m_2}{M_{PL}^2 r}$$

Spin

$\gamma$	$W^\pm Z^0$	$g$	=1
$H$			=0
$G$			=2

# Gauge Invariance

Gauge transformation  $\psi_i(x) \rightarrow U_{ij}(x)\psi_j(x) = \exp[i\alpha^a(x)T_{ij}^a]\psi_j(x)$

$$\bar{\psi}_i(x) \rightarrow \bar{\psi}_j U_{j1}^\dagger(x)$$

matrix

$$U^\dagger U = 1$$

parameter

matrix

$$a = 1, 2, \dots, N$$

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 $a = 1, 2, \dots, N$

Fermion Kinetic term

$$\begin{aligned} i\bar{\psi}(x)\gamma^\mu\partial_\mu\psi(x) &\rightarrow i\bar{\psi}(x)U^\dagger(x)\gamma^\mu\partial_\mu(U(x)\psi(x)) \\ &= i\bar{\psi}(x)\gamma^\mu\partial_\mu\psi(x) + i\bar{\psi}(x)\gamma^\mu U^\dagger(x)\partial_\mu U(x)\psi(x) \end{aligned}$$

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Covariant derivative  $\partial_\mu \rightarrow D_\mu = \partial_\mu I + gA_\mu^a T^a \equiv \partial_\mu I + gA_\mu$

Gauge field

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Gauge field

Gauge invariant kinetic term

$$i\bar{\psi}(x)\gamma^\mu D_\mu\psi(x)$$



# Gauge Invariance

$$\hat{A}_\mu \rightarrow U^\dagger(x) \hat{A}_\mu U(x) + gU^\dagger(x) \partial_\mu U(x)$$

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$$G_{\mu\nu} \rightarrow U^\dagger(x) G_{\mu\nu} U(x)$$

# Gauge Invariance

Gauge field transformation

$$\hat{A}_\mu \rightarrow U^\dagger(x) \hat{A}_\mu U(x) + gU^\dagger(x) \partial_\mu U(x)$$

Field strength tensor

$$[D_\mu, D_\nu] = G_{\mu\nu} = \partial_\mu A_\nu - \partial_\nu A_\mu + g[A_\mu A_\nu]$$

$$G_{\mu\nu} \rightarrow U^\dagger(x) G_{\mu\nu} U(x)$$

Gauge field kinetic term


$$-\frac{1}{4} \text{Tr} G_{\mu\nu} G^{\mu\nu}$$

Contains self interaction of the gauge fields!

# Fermion Masses in the SM

Direct mass terms are forbidden due to  $SU(2)_L$  invariance !

Dirac Spinors                      left                      right                      Dirac conjugated                      Charge conjugated

$$\psi, \psi_L = \frac{1 - \gamma^5}{2} \psi, \psi_R = \frac{1 + \gamma^5}{2} \psi, \bar{\psi} = \psi^\dagger \gamma^0, \psi^c = C \gamma^0 \psi = i \gamma^2 \psi^*$$


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Lorentz invariant Mass terms

$$\bar{\psi}_L \psi_R + \bar{\psi}_R \psi_L$$

SU(2) doublet      SU(2) singlet

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Lorenz invariant Mass terms

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$SU_L(2)$

$\psi_L$  is an  $SU(2)$  doublet,  $\psi_R$  is an  $SU(2)$  singlet.

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$$\cancel{\bar{\psi}_L \psi_R} + \cancel{\bar{\psi}_R \psi_L} \quad \text{SU}_L(2)$$

$$\bar{\psi}_L \psi_L = \bar{\psi}_R \psi_R = 0$$

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SU(2) singlet

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$$\bar{\psi}_R^c \psi_R + \bar{\psi}_R \psi_R^c$$



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Dirac Spinors
left
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Charge conjugated

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$SU_L(2)$   
SU(2) doublet
SU(2) singlet

$$\cancel{\bar{\psi}_L^c \psi_L + \bar{\psi}_L \psi_L^c} \quad \cancel{\bar{\psi}_R^c \psi_R + \bar{\psi}_R \psi_R^c}$$

$SU_L(2) \ \& \ U_Y(1)$ 
 $U_Y(1)$

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 $SU(2)$  doublet       $SU(2)$  singlet

~~$\bar{\psi}_L^c \psi_L + \bar{\psi}_L \psi_L^c$~~        $SU_L(2) \text{ \& } U_Y(1)$        $U_Y(1)$   
 ~~$\bar{\psi}_R^c \psi_R + \bar{\psi}_R \psi_R^c$~~

Unless  $Q=0, Y=0$   
 $\bar{\nu}_R^c \nu_R$   
 Majorana mass term

# Spontaneous Symmetry Breaking

$$SU_c(3) \otimes SU_L(2) \otimes U_Y(1) \rightarrow SU_c(3) \otimes U_{EM}(1)$$

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Introduce a scalar field with quantum numbers: (1,2,1)  $H = \begin{pmatrix} H^+ \\ H^0 \end{pmatrix}$

With potential  $V = -m^2 H^\dagger H + \frac{\lambda}{2} (H^\dagger H)^2$

# Spontaneous Symmetry Breaking

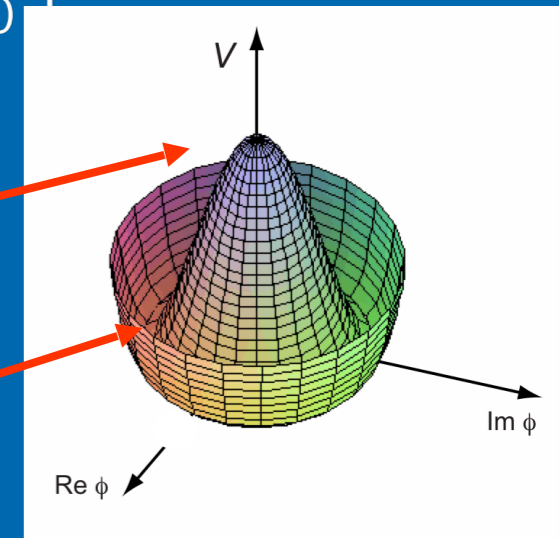
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Unstable maximum

Stable minimum



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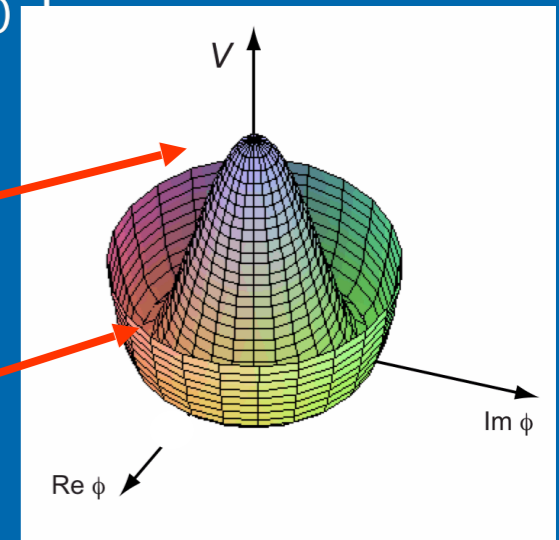
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Unstable maximum

Stable minimum



$$H = \begin{pmatrix} H^+ \\ H^0 \end{pmatrix} = \begin{pmatrix} \overset{\text{v.e.v.}}{\downarrow} H^+ \\ v + \frac{S+iP}{\sqrt{2}} \end{pmatrix} = \exp\left(i \frac{\xi^a \sigma^a}{2}\right) \begin{pmatrix} 0 \\ \frac{S}{\sqrt{2}} \end{pmatrix}$$

scalar
pseudoscalar

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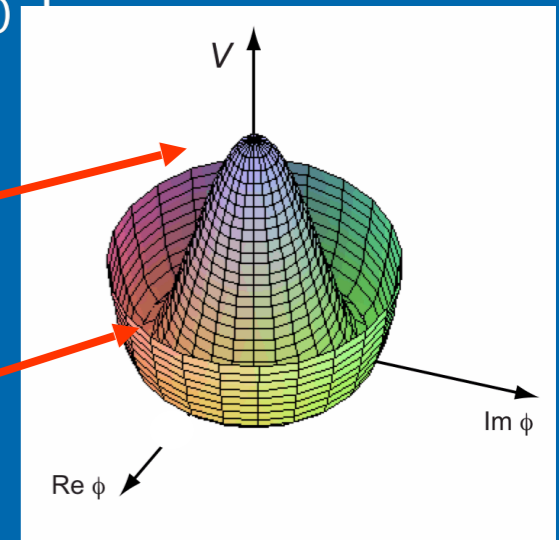
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v.e.v.
scalar
pseudoscalar

Gauge transformation

$$H \rightarrow H' = \exp\left(i \frac{\alpha^a \sigma^a}{2}\right) H \xrightarrow{\alpha^a = -\xi^a} H' = \begin{pmatrix} 0 \\ \frac{h}{\sqrt{2}} \end{pmatrix}$$

Higgs boson

# Mechanism of Spontaneous Symmetry breaking (Brout-Englert-Higgs)

Q: what happens with missing d.o.f (massless Goldstone bosons  $P, H^+$  or  $\vec{\xi}$  )?

A: they become longitudinal d.o.f of the gauge bosons  $W_{\mu}^i, i = 1, 2, 3$



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Gauge transformation

$$\hat{W}_{\mu} \rightarrow e^{i\alpha^a \sigma^a} \hat{W}_{\mu} e^{-i\alpha^a \sigma^a} - \frac{1}{g} \partial_{\mu} (e^{i\alpha^a \sigma^a}) e^{-i\alpha^a \sigma^a}$$

$\alpha^a = -\xi^a$  Longitudinal components

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Higgs field kinetic term

$$|D_{\mu} H|^2 = \left| \partial_{\mu} H - \frac{g}{2} \hat{W}_{\mu} H - \frac{g'}{2} \hat{B}_{\mu} H \right|^2$$

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$$|D_\mu H|^2 = \left| \partial_\mu H - \frac{g}{2} \hat{W}_\mu H - \frac{g'}{2} \hat{B}_\mu H \right|^2 \quad \leftarrow H = \begin{pmatrix} 0 \\ v \end{pmatrix}$$

$$\rightarrow \frac{1}{4} (0v) \begin{pmatrix} gW_\mu^3 + g'B_\mu & \sqrt{2}W_\mu^- \\ \sqrt{2}W_\mu^+ & -gW_\mu^3 + g'B_\mu \end{pmatrix}^2 \begin{pmatrix} 0 \\ v \end{pmatrix}$$

$$\rightarrow \frac{g^2}{2} v^2 W_\mu^+ W_\mu^- + \frac{1}{4} (-gW_\mu^3 + g'B_\mu)^2$$

# Gauge Bosons Masses

$$\Delta L_{mass} \rightarrow \frac{g^2}{2} v^2 W_\mu^+ W_\mu^- + \frac{1}{4} (-gW_\mu^3 + g' B_\mu)^2 + \cancel{\frac{1}{4} (gW_\mu^3 + g' B_\mu)^2}$$

$$W_\mu^\pm = \frac{W_\mu^1 \mp W_\mu^2}{\sqrt{2}}$$

$$Z_\mu = -\sin \theta_W B_\mu + \cos \theta_W W_\mu^3 \quad \tan \theta_W = g'/g$$

$$\gamma_\mu = \cos \theta_W B_\mu + \sin \theta_W W_\mu^3$$

$$M_W^2 = \frac{1}{2} g^2 v^2$$

$$M_Z^2 = \frac{1}{2} (g^2 + g'^2) v^2$$

$$M_\gamma = 0$$

$$M_W^2 = \frac{g^2}{g^2 + g'^2} M_Z^2 = \cos^2 \theta_W M_Z^2$$

# Gauge Bosons Masses

The mass terms

$$\Delta L_{mass} \rightarrow \frac{g^2}{2} v^2 W_\mu^+ W_\mu^- + \frac{1}{4} (-gW_\mu^3 + g' B_\mu)^2 + \frac{1}{4} (gW_\mu^3 + g' B_\mu)^2$$

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$$M_Z^2 = \frac{1}{2} (g^2 + g'^2) v^2$$

$$M_\gamma = 0$$

$$M_W^2 = \frac{g^2}{g^2 + g'^2} M_Z^2 = \cos^2 \theta_W M_Z^2$$

# The Higgs Boson and Fermion Masses

$$H = \begin{pmatrix} 0 \\ v + \frac{h}{\sqrt{2}} \end{pmatrix} \rightarrow V = -m^2 H^\dagger H + \frac{\lambda}{2} (H^\dagger H)^2$$

$$\rightarrow V = -\frac{\lambda v^4}{2} + \lambda v^2 h^2 + \frac{\lambda v}{\sqrt{2}} h^3 + \frac{\lambda}{8} h^4 \quad v^2 = m^2 / \lambda$$

$$m_h = \sqrt{2}m = \sqrt{2\lambda}v$$

$$L_{Yukawa} = y_{\alpha\beta}^E \bar{L}_\alpha E_\beta H + y_{\alpha\beta}^D \bar{Q}_\alpha D_\beta H + y_{\alpha\beta}^U \bar{Q}_\alpha U_\beta \tilde{H}$$

$\alpha, \beta = 1, 2, 3$  - generation index

Dirac fermion mass

$$M_i^u = \text{Diag}(y_{\alpha\beta}^u)v, \quad M_i^d = \text{Diag}(y_{\alpha\beta}^d)v, \quad M_i^l = \text{Diag}(y_{\alpha\beta}^l)v$$

$$y_{\alpha\beta}^N \bar{L}_\alpha N_\beta \tilde{H} \rightarrow M_i^v = \text{Diag}(y_{\alpha\beta}^N)v$$

Dirac neutrino mass

# Quark/Lepton Mixing

- The mass matrix is non-diagonal in generation space
- It can be diagonalized by field rotation  $Q \rightarrow Q' = V Q$

$$\bar{U} M_U U \rightarrow \bar{U}' V_U^+ M_U V_U U' = \bar{U}' M_U^{Diag} U'$$

$$\bar{D} M_D D \rightarrow \bar{D}' V_D^+ M_D V_D D' = \bar{D}' M_D^{Diag} D'$$

- Neutral Current:

$$\bar{U} Z_\mu U \rightarrow \bar{U}' V_U^+ Z_\mu V_U U' = \bar{U}' Z_\mu U' \quad V_U^+ V_U = \bar{U}' Z_\mu U'$$

- Charged Current

$$\bar{U} W_\mu D \rightarrow \bar{U}' V_U^+ W_\mu V_D D = \bar{U}' W_\mu V_U^+ V_D D'$$

Cabibbo-Kobayashi-Maskawa mixing matrix (quarks)

Pontecorvo-Maki-Nakagawa-Sakato mixing matrix (leptons)

The (only) source of flavour mixing in the SM

$$K = V_U^+ V_D$$

$$\text{Unitarity: } K^\dagger K = 1$$

# Mixing Matrix and Unitarity Triangle

Quarks and leptons of different generations can mix interacting with W-boson

Two generations

$$(\bar{u} \ \bar{c}) \begin{pmatrix} \cos \theta & -\sin \theta \\ \sin \theta & \cos \theta \end{pmatrix} W \begin{pmatrix} d \\ s \end{pmatrix}$$

Mixing matrix

Three generations

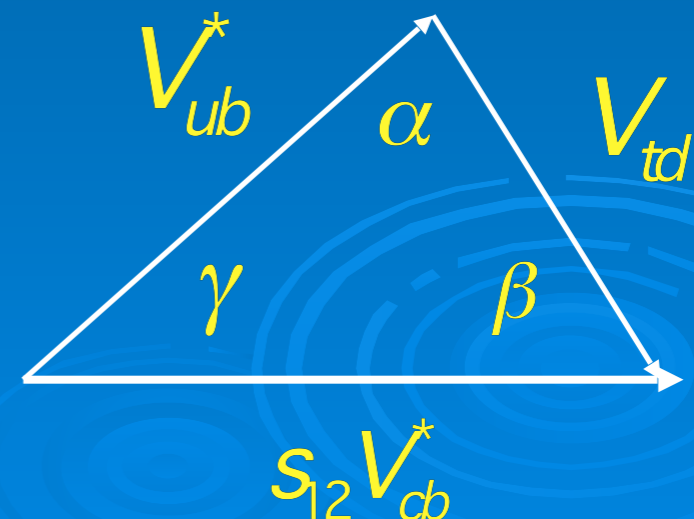
$$K = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} = \begin{pmatrix} c_{12}c_{13} & s_{12}c_{13} & s_{13}e^{-i\delta} \\ -s_{12}c_{23} - c_{12}s_{23}s_{13}e^{i\delta} & c_{12}c_{23} - s_{12}s_{23}s_{13}e^{i\delta} & s_{23}c_{13} \\ s_{12}s_{23} - c_{12}c_{23}s_{13}e^{i\delta} & -c_{12}s_{23} - s_{12}c_{23}s_{13}e^{i\delta} & c_{23}c_{13} \end{pmatrix}$$

Two important properties

1. CP-violation due to a complex phase  $\delta$  !
2. Unitarity triangle

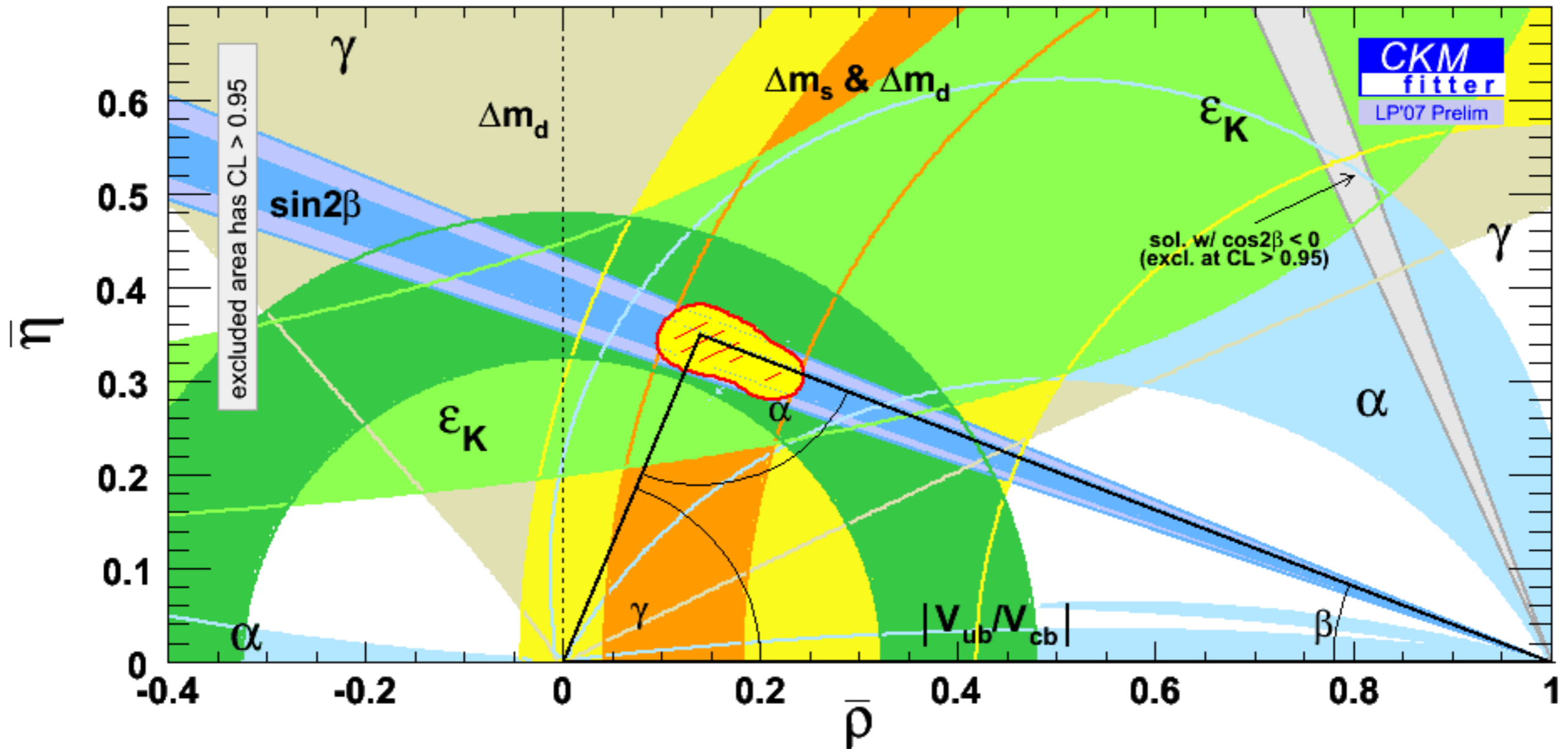
$$V_{ud}V_{ub}^* + V_{cd}V_{cb}^* + V_{td}V_{tb}^* = 0$$

$$\Rightarrow V_{ub}^* + V_{td} = s_{12}V_{cb}^*$$



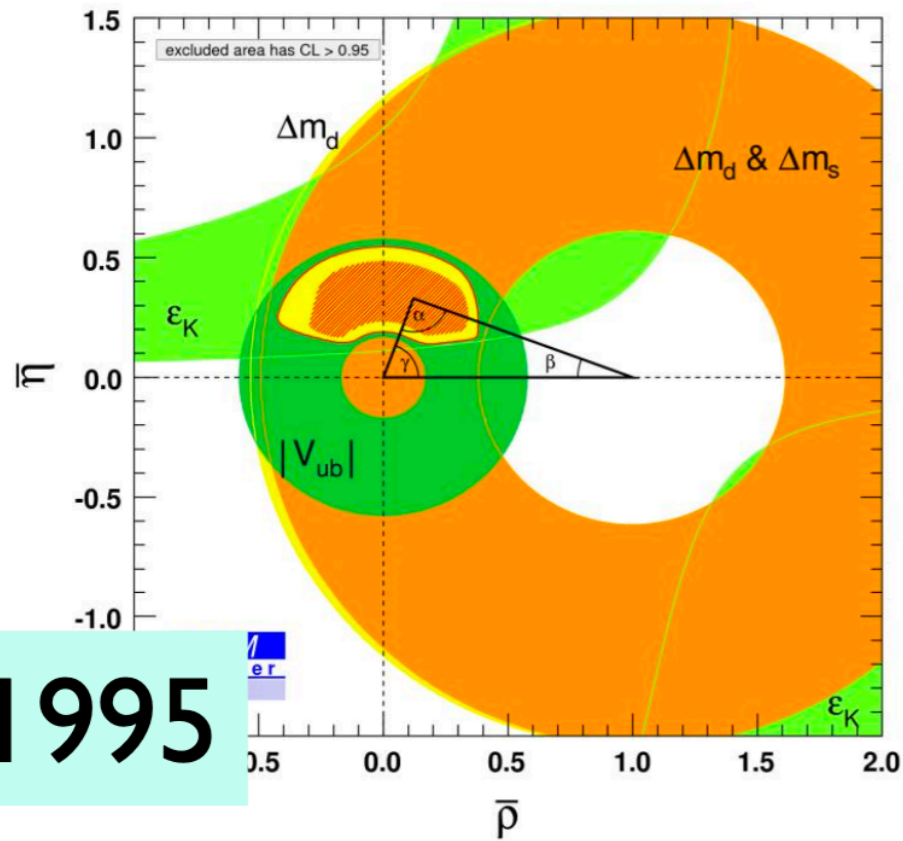


# The Unitarity Triangle: all constraints



A consistent picture across a huge array of measurements

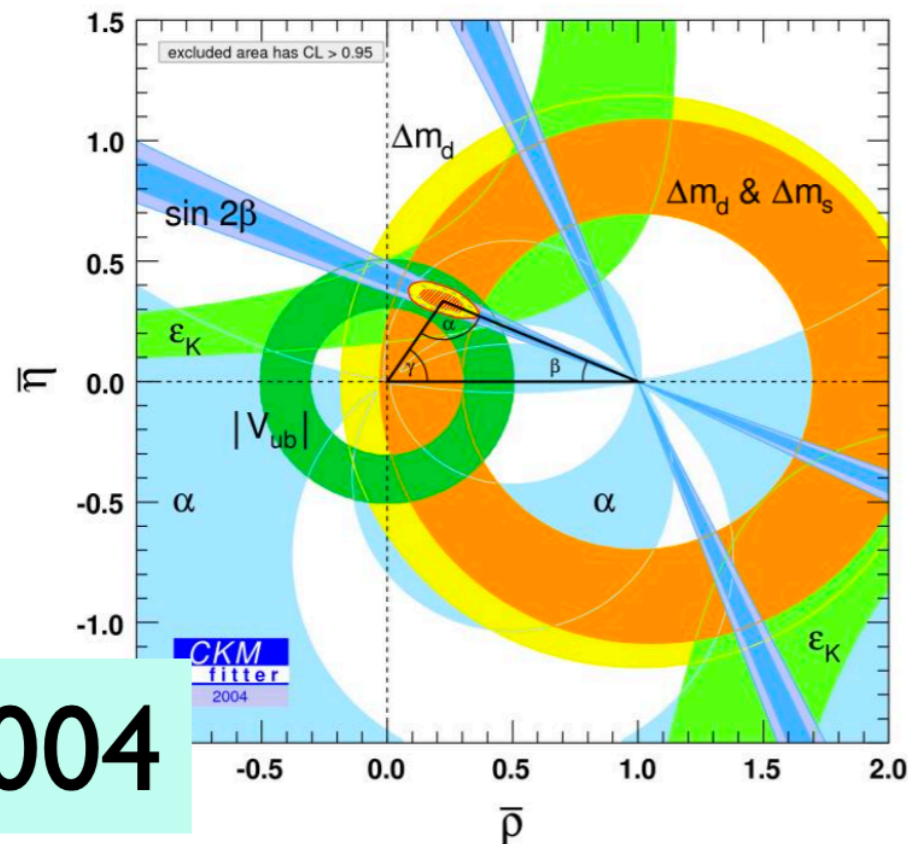
# Unitarity Triangle measurements



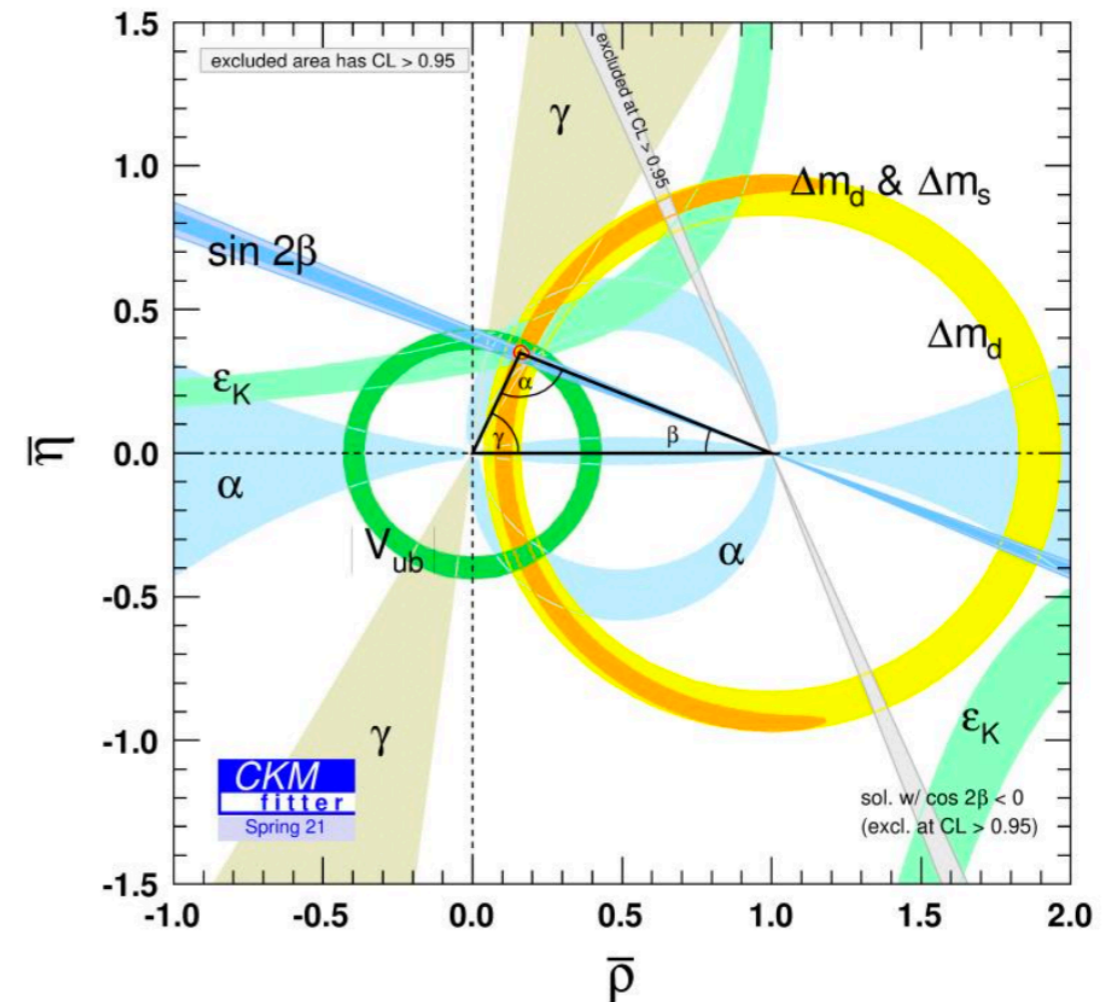
1995

- Amazing progress in the last 27 years; the SM remains intact, but a whole lot still to learn

<http://ckmfitter.in2p3.fr>



2004



Now (dominated by LHCb)

# Mass spectrum and Mixing angles

- Mass spectrum?

$$m_{quark} = y_{quark} \cdot v$$

$$m_{lepton} = y_{lepton} \cdot v$$

$$m_W = g/\sqrt{2} \cdot v$$

$$m_Z = \sqrt{g^2 + g'^2}/\sqrt{2} \cdot v$$

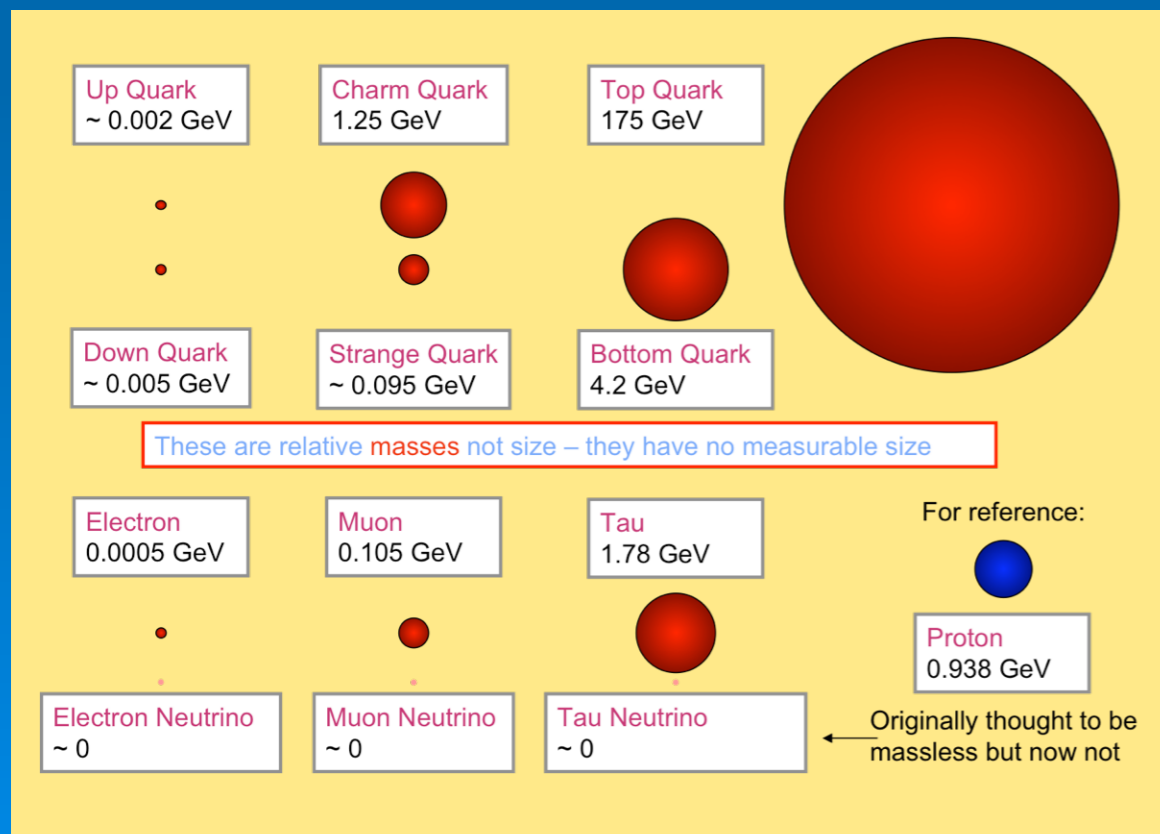
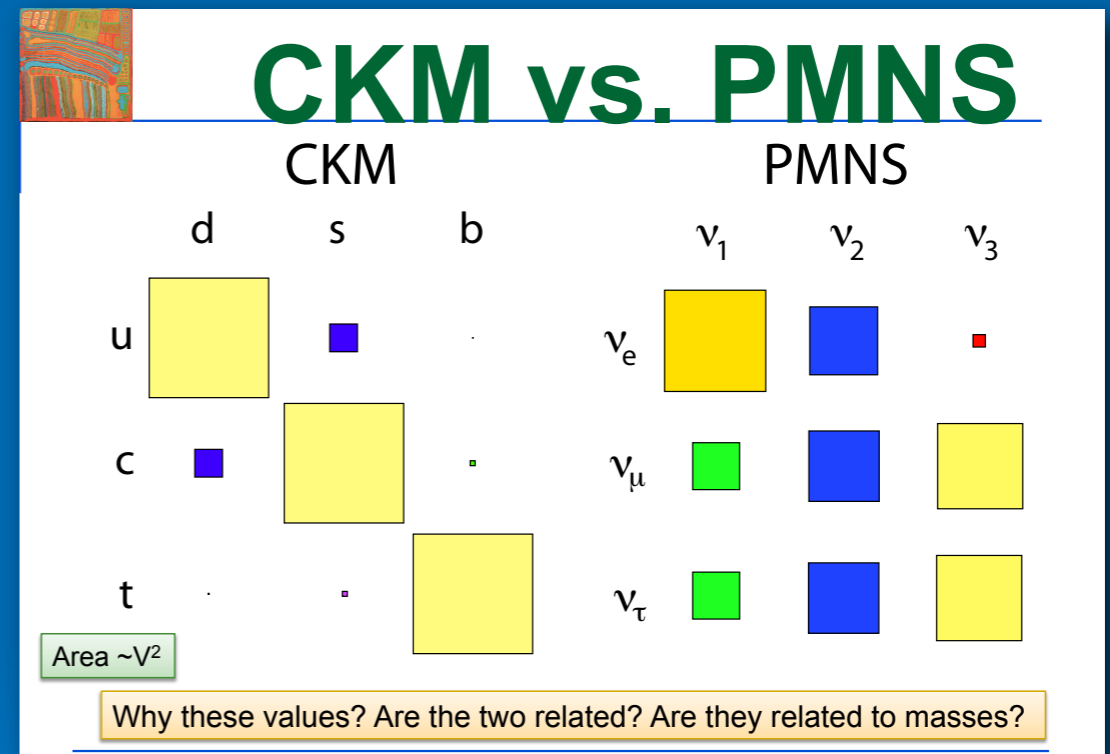
$$m_H = \sqrt{\lambda} \cdot v$$

SM  $m_\gamma = 0$

$$m_{gluon} = 0$$

- Mixing Matrices?

- Quark-Lepton Symmetry
- Strong difference in parameters



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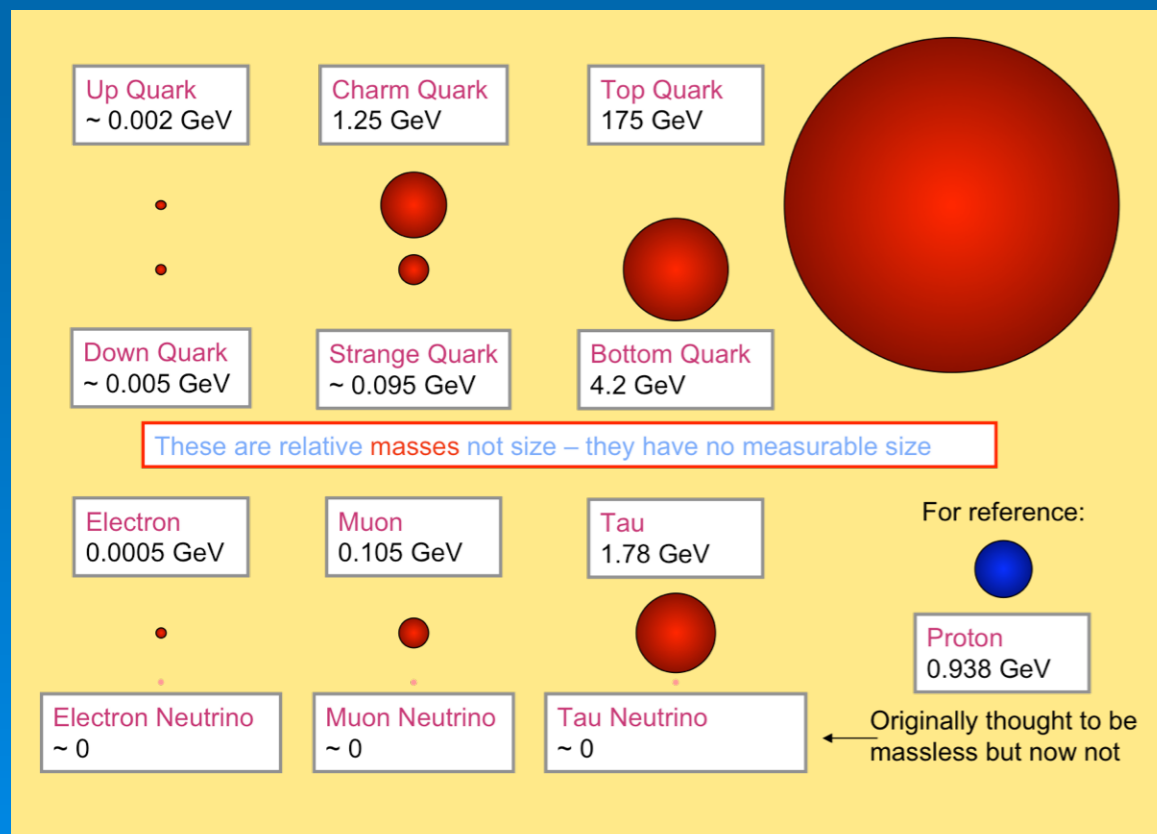
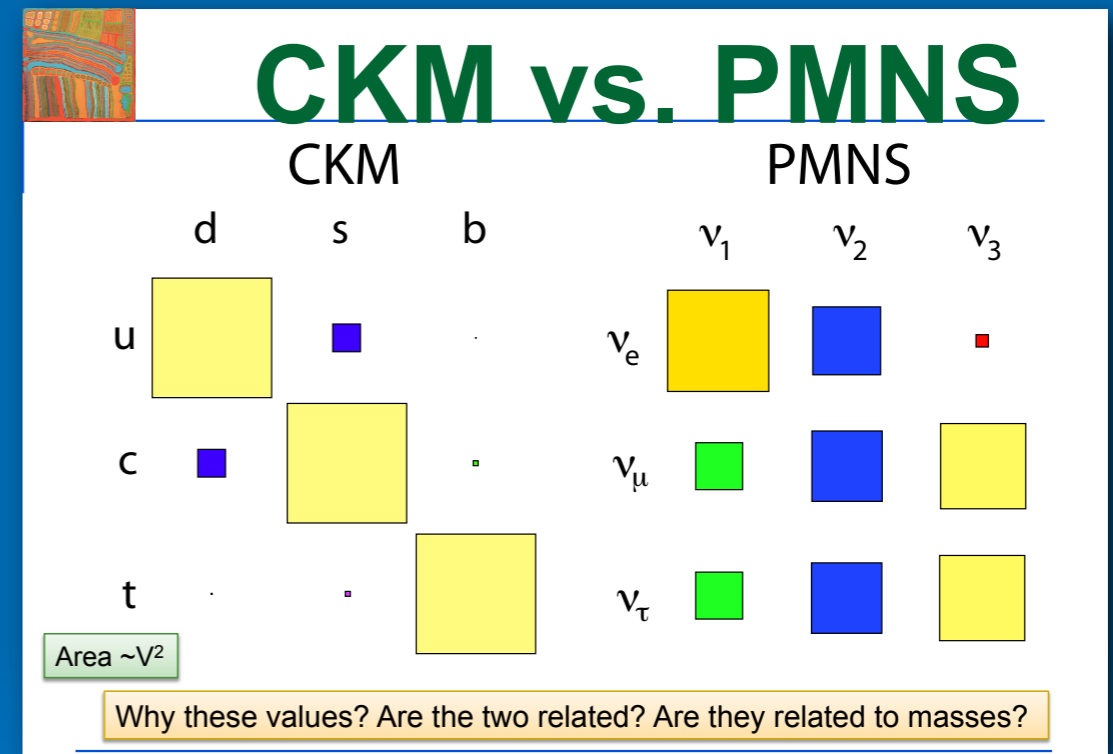
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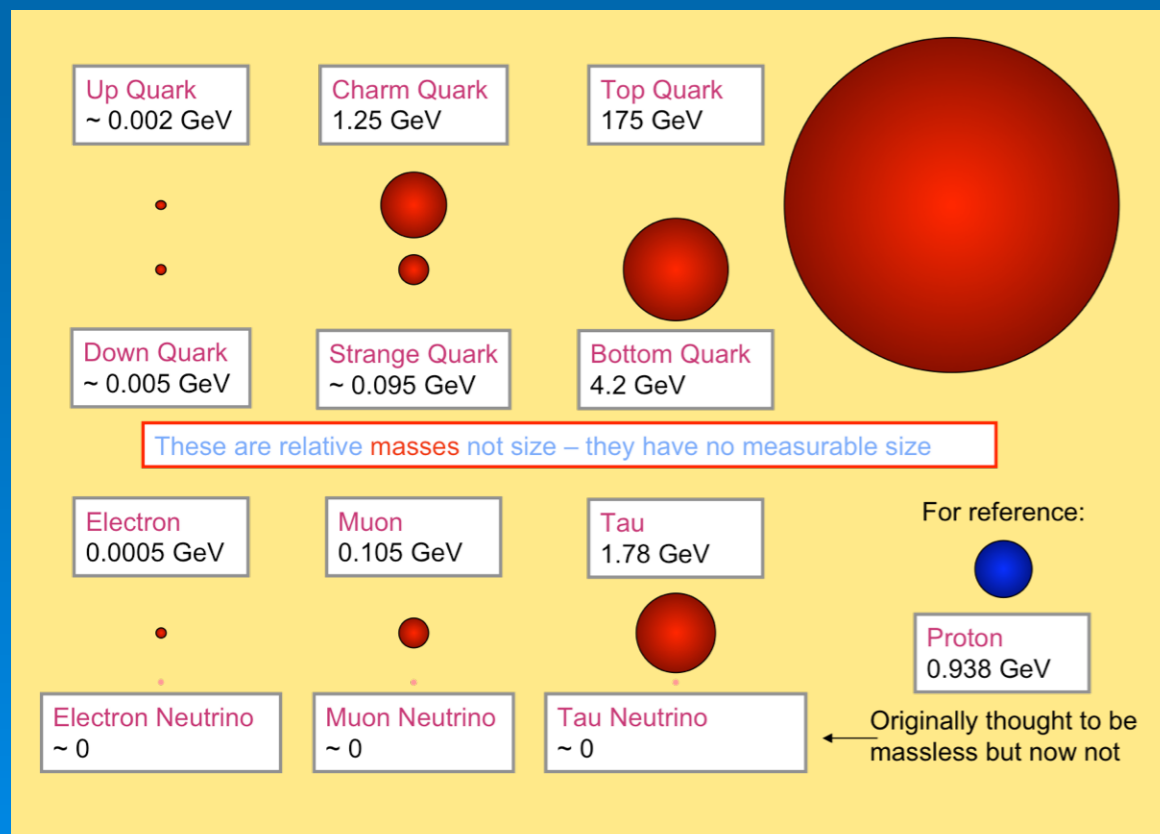
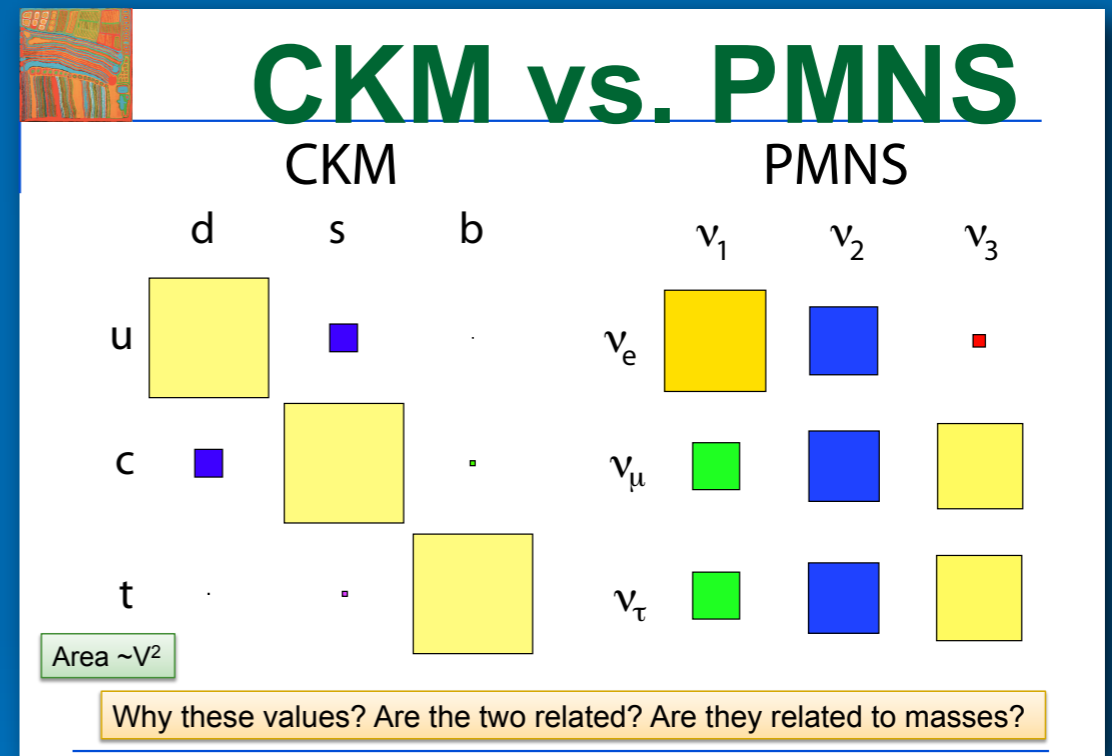
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- What are the CKM and PMNS phases?
- Where lies the source of CP violation: in quark or lepton sector?

$$J_{CP} = \frac{1}{8} \sin 2\theta_{12} \sin 2\theta_{23} \sin 2\theta_{13} \cos \theta_{13} \sin \delta$$

# Calculation of Theoretical Predictions in HEP

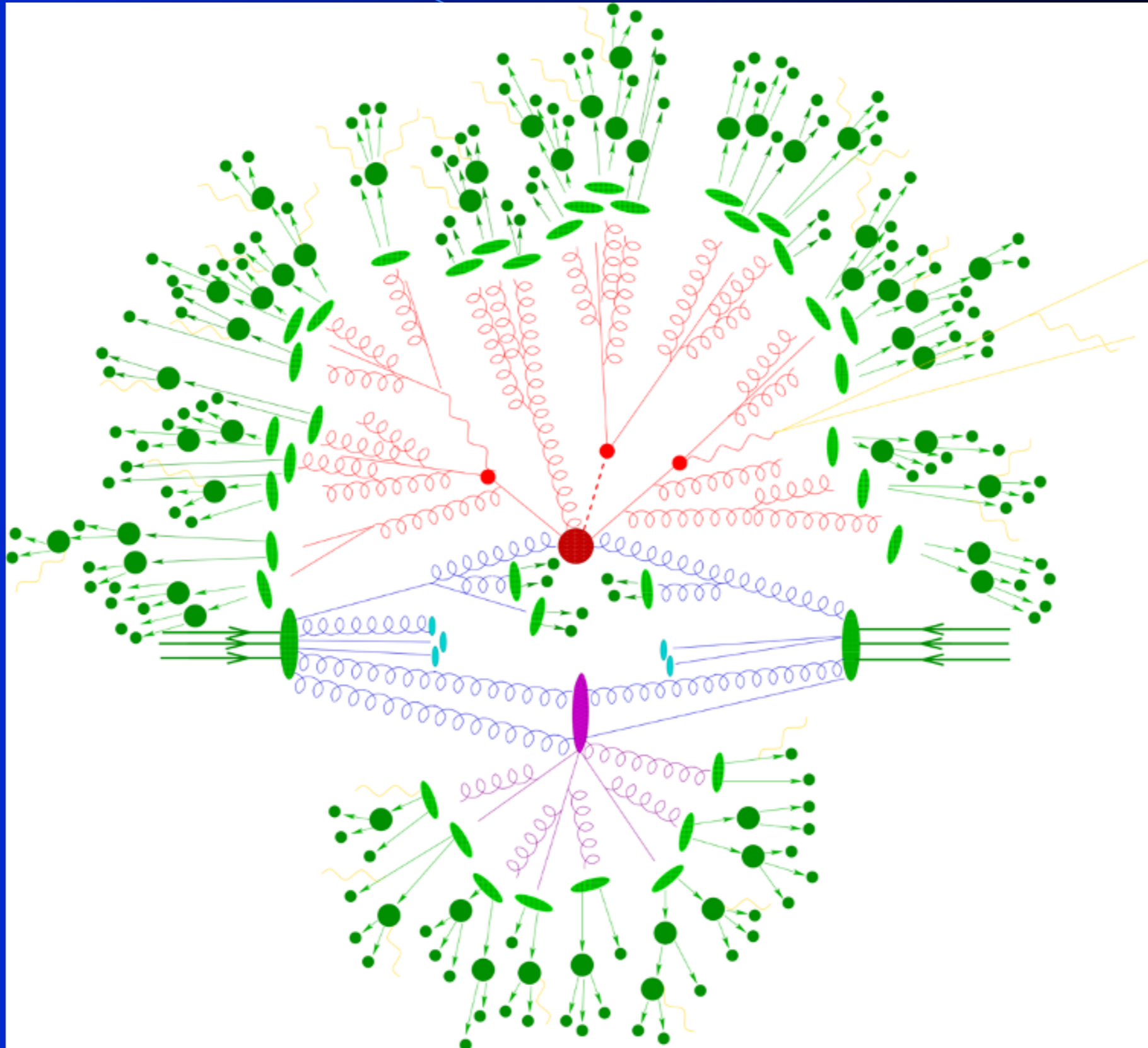
- .Choose a process and estimate the required precision => **number of loops and legs**
- .Generate (or draw) **Feynman diagrams**: from a few to many thousands
- .E.g., Mathematica package **FeynArts** is widely used
- .Perform algebraic evaluation and reduce the problem to calculation of so-called **master integrals**, e.g., by **LiteRed** package.
- .Compute those master integrals either analytically or numerically. There are many advanced methods...
- .Perform **renormalization**, take care on infrared singularities and matching to non-perturbative effects
- .Collect all components and get the analytic result for completely **differential cross section**, e.g., distribution of the reaction products in energy, momenta, and spin.
- .Create a **Monte Carlo event generator** to simulate the distribution. Pass it to the colleagues from an experiment

# Theoretical Codes for HEP Experiments

## Theoretical Codes for HEP experiments

- **General**, e.g., **Pythia**, **HERWIG** and **CompHEP**: many processes and effects but limited precision
- Tree-level calculations + universal non-perturbative effects like hadronic vacuum polarization, PDFs, and parton showers
- **Specific** (dedicated), e.g., **MC@NLO** and **POWHEG**: a few processes but higher precision due inclusion of higher order radiative corrections
- At least 1-loop (NLO, NNLO etc.) calculations + advanced treatment of non-perturbative effects relevant for the given set of processes
- The codes are used for experimental data simulation **in chains**, so their input and output meet certain standards. E.g., events are generated by one Monte Carlo generator and then processed by the **PHOTOS** code to simulate multiple photon radiation

# Progress of Theoretical Calculations





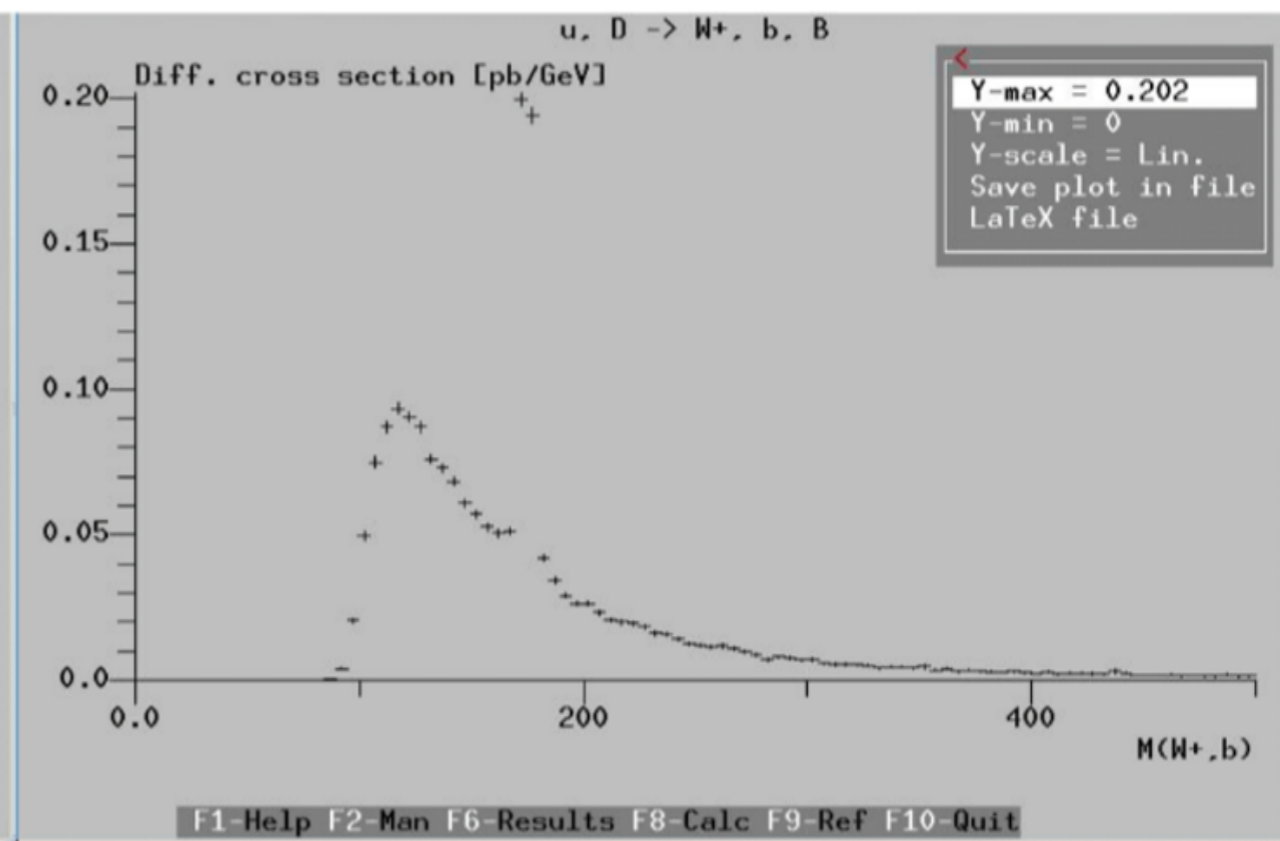
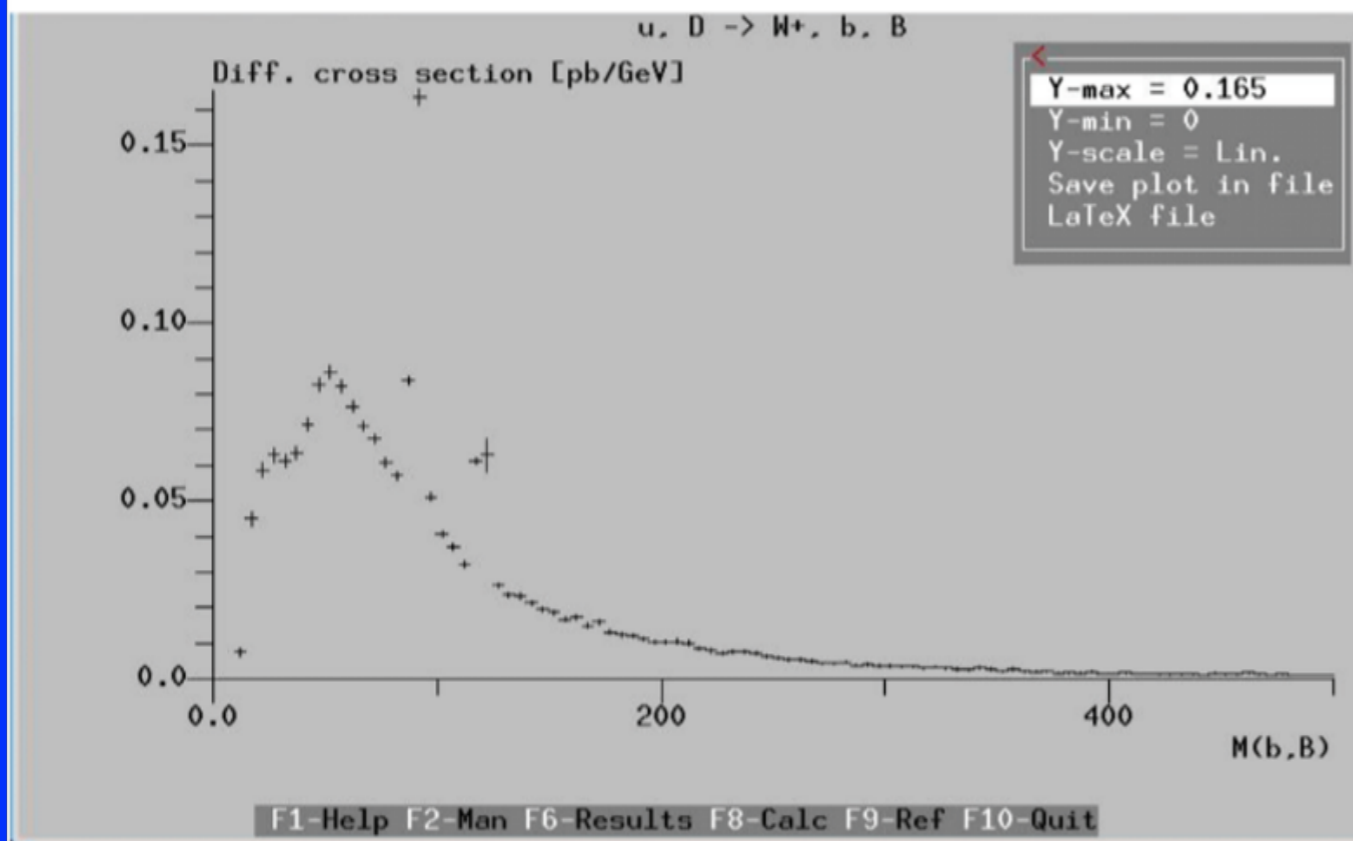
# Example: diagrams generated by CalcHEP

Delete, On/off, Restore, Latex 1/10


F1-Help, F2-Man, PgUp, PgDn, Home, End, #, Esc

# CalcHEP: from Feynman rules to distributions

## Resulting $M_{bb}$ and $M_{Wtb}$ kinematical distributions



# Using a chain of Programs

## Using a chain of programs:

an example on electron loop contributions to  $g-2$  of muon

Step 1. Generate 4-loop QED Feynman diagrams by **QGRAF** code [Nogueira]

Step 2. Read the diagrams: a bridge between **QGRAF** and **exp** [Harlander, Seidensticker, Steinhauser]

Step 3. **exp/asy/in hause**: asymptotic expansion with mass hierarchy  $m_e \ll m_\mu$  [Harlander, Seidensticker, Steinhauser]/ [Pak, Smirnov; Jantzen, Smirnov, Smirnov]

Step 4. **FORM**: calculations of diagrams [Vermaseren]

Step 5. **FIRE/Crusher**: reduction to master integrals [Smirnov]/[Marquard, Seidel]

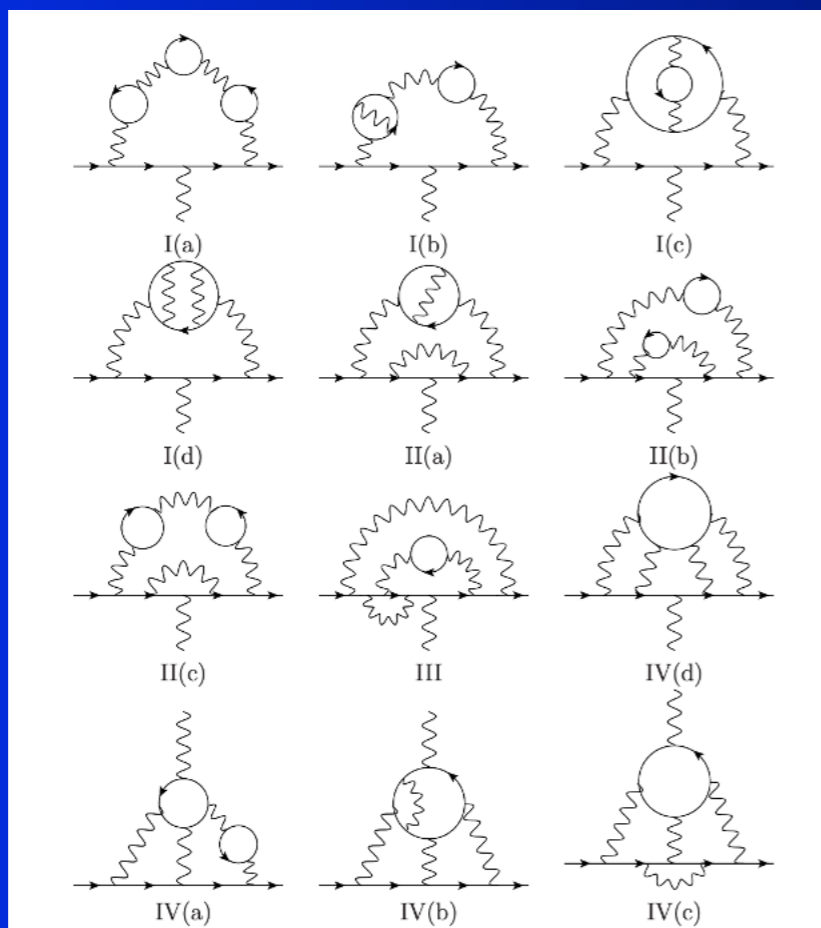
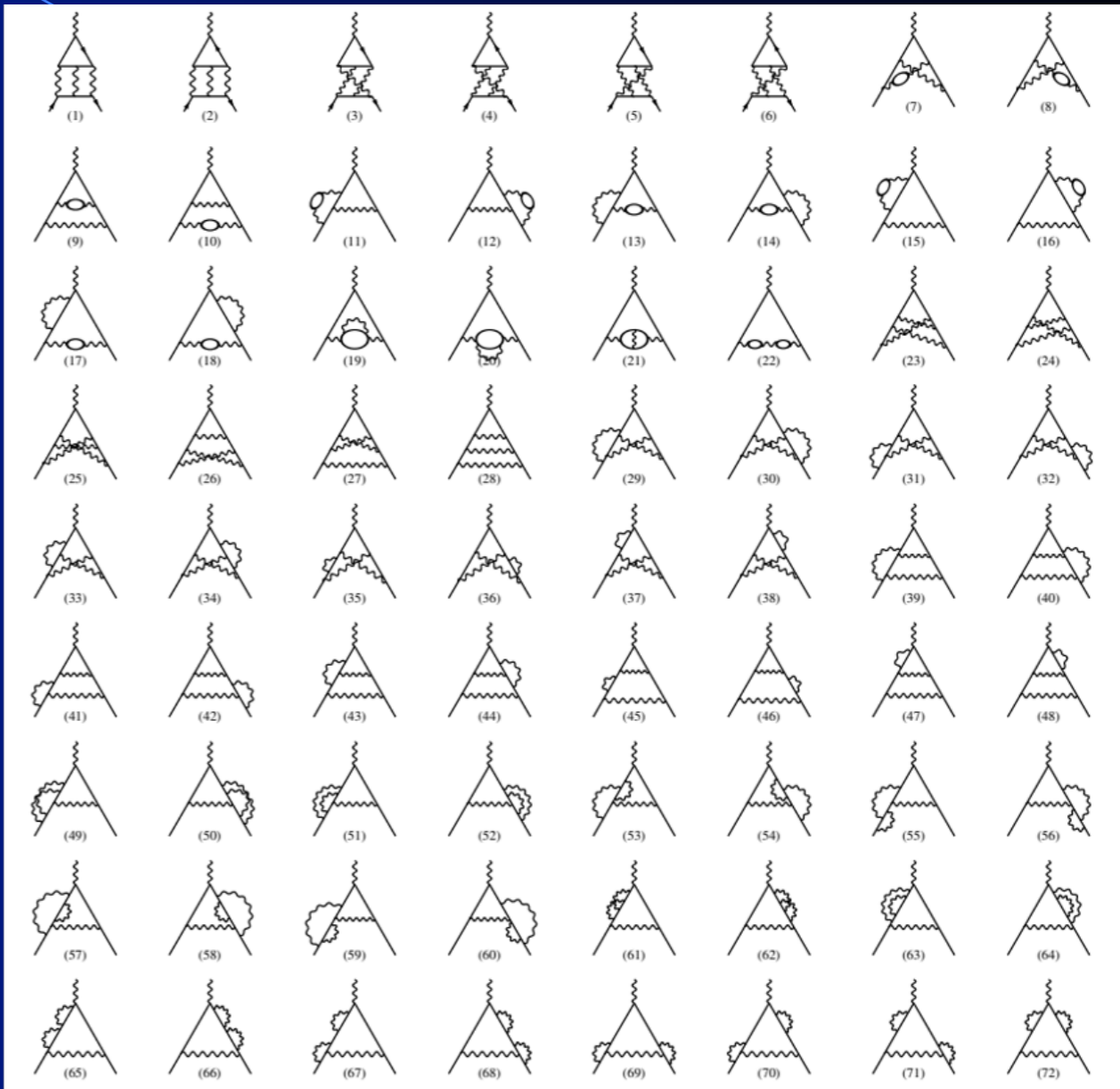
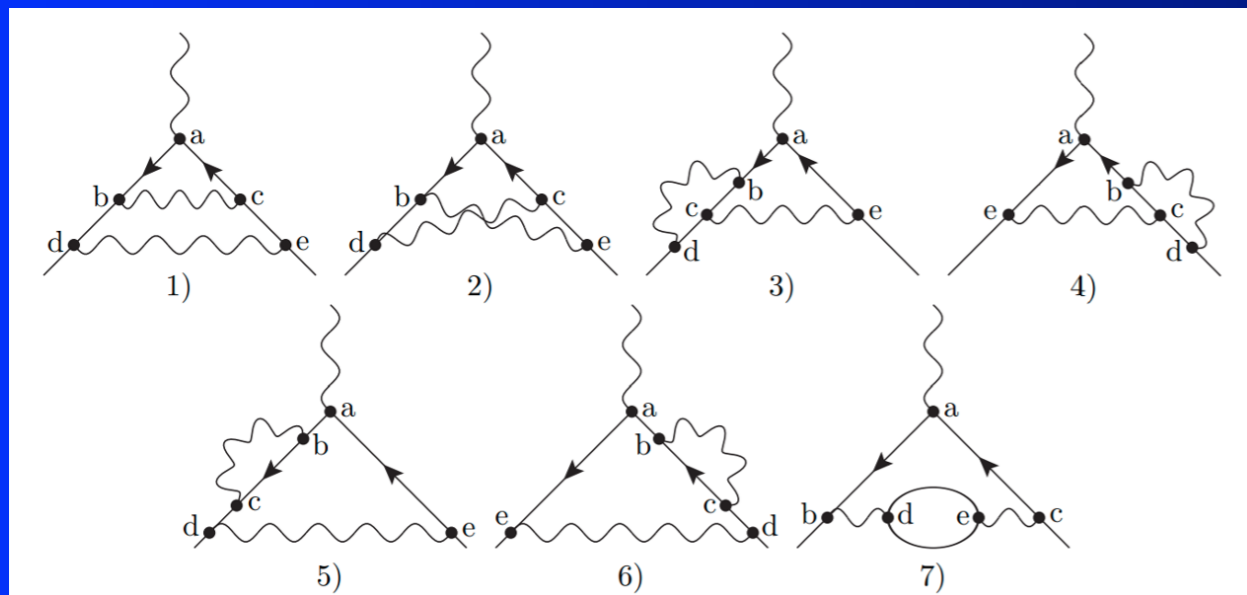
Step 6. **FIESTA**: evaluation of master integrals [Smirnov]

Step 7. See a numerical agreement with Kinoshita's results.

\*The names of computer codes are in blue. Their authors are given in square brackets.

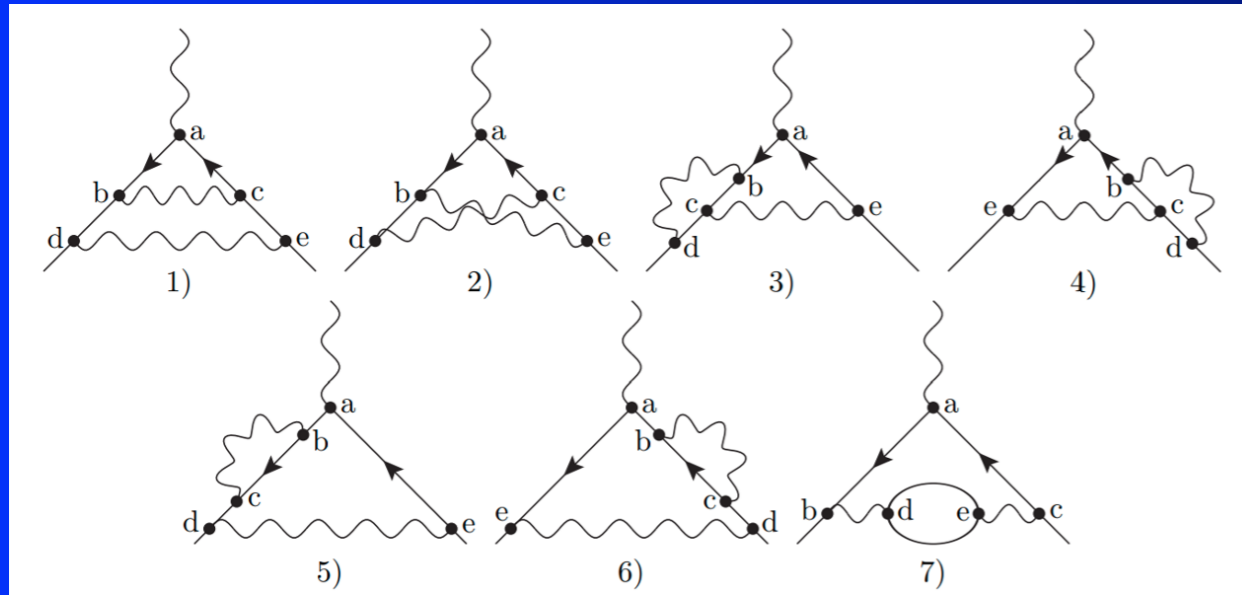
[A. Kurz, P. Marquard, A.V. Smirnov, V.A. Smirnov, M. Steinhauser, *Phys.Rev.D* 93 (2016) 5, 053017]

# QED Diagrams for g-2 of muon

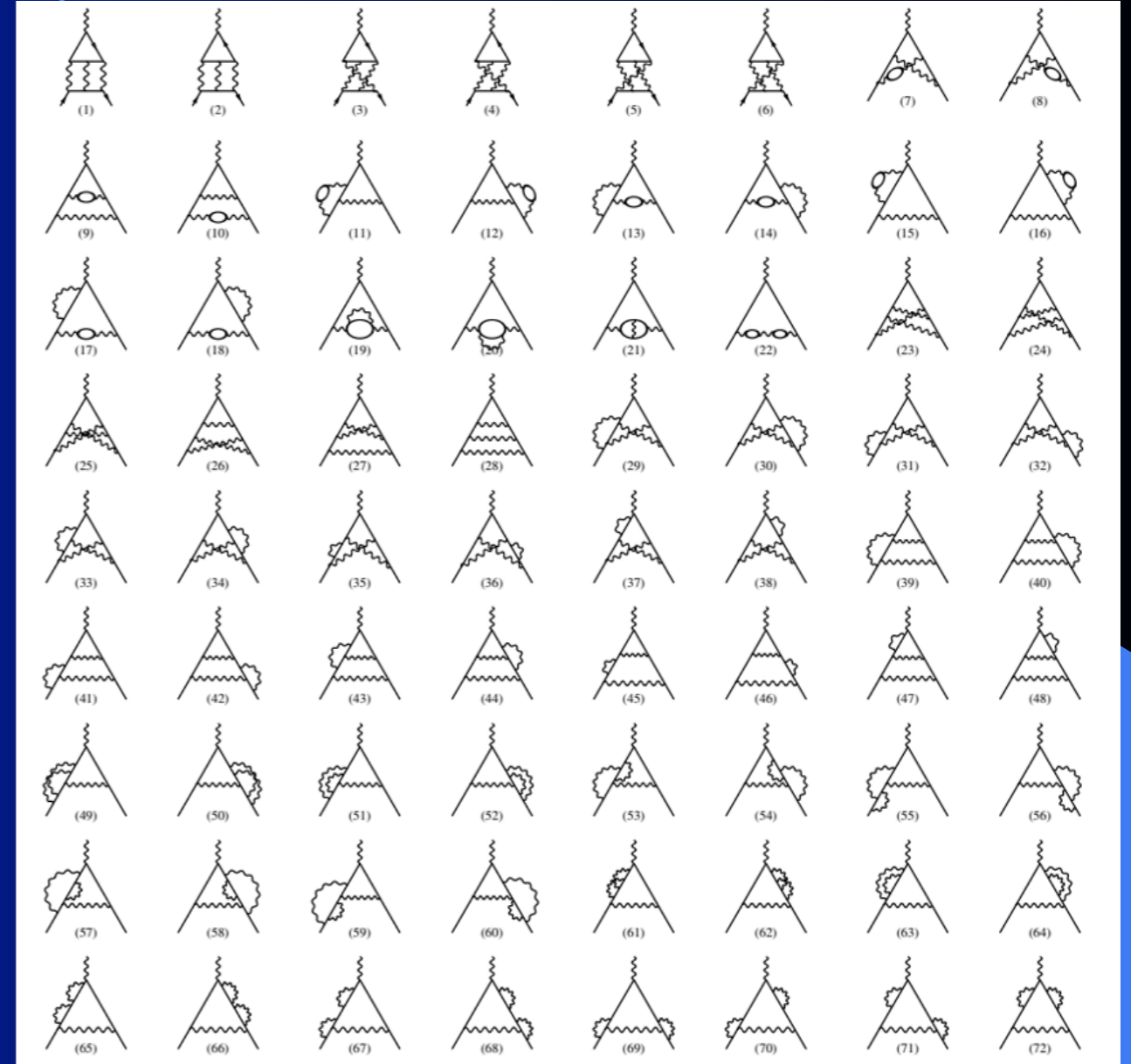


# QED Diagrams for $g-2$ of muon

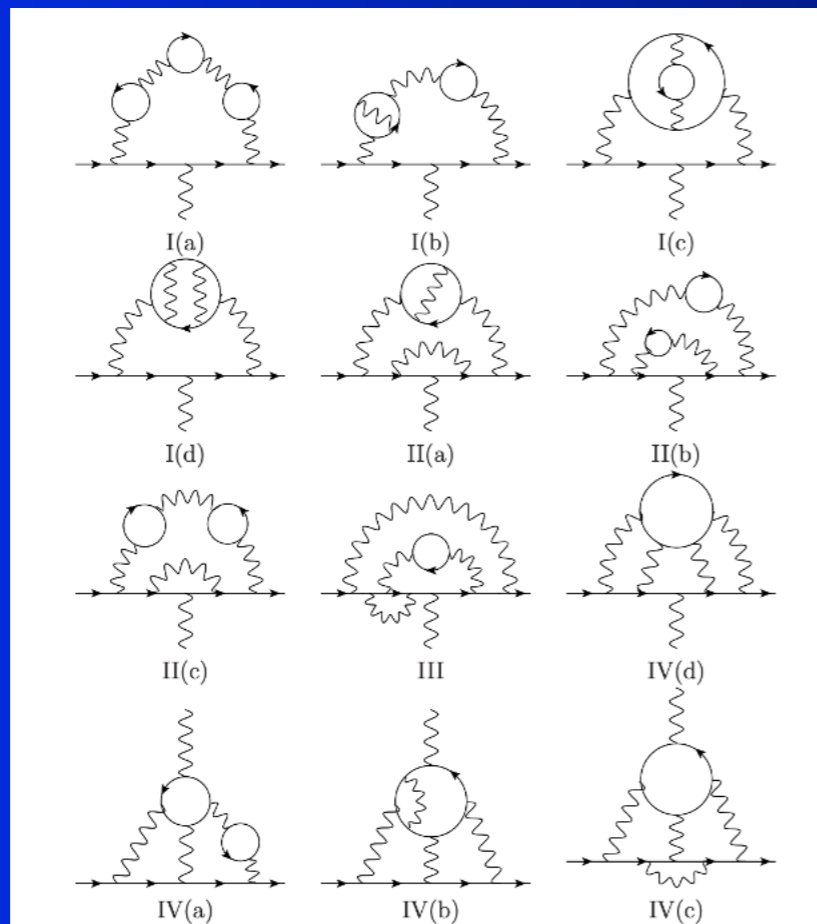
## Two-loop diags



## Three-loop diags

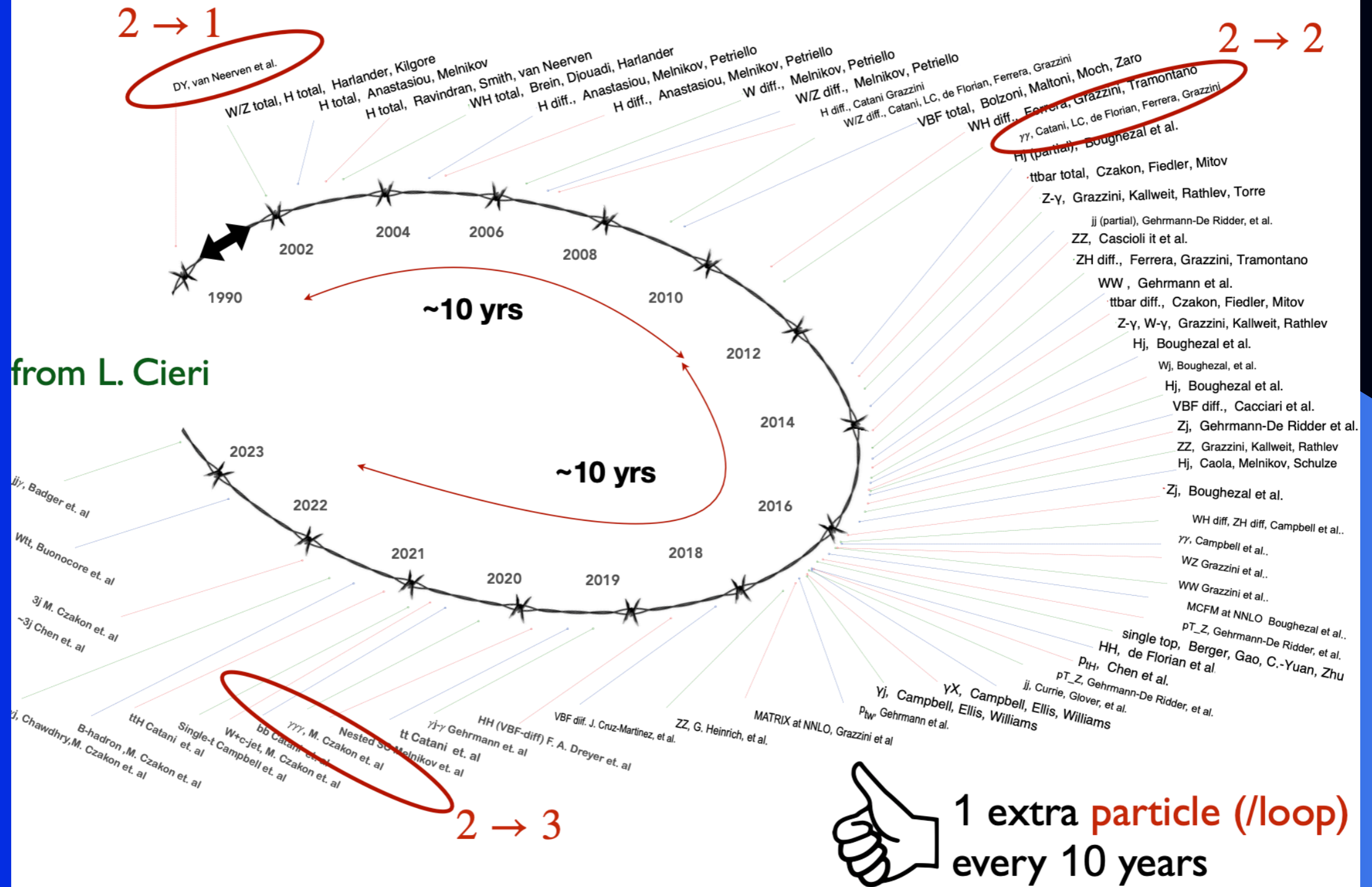


Types of four-loop diags with electron loops

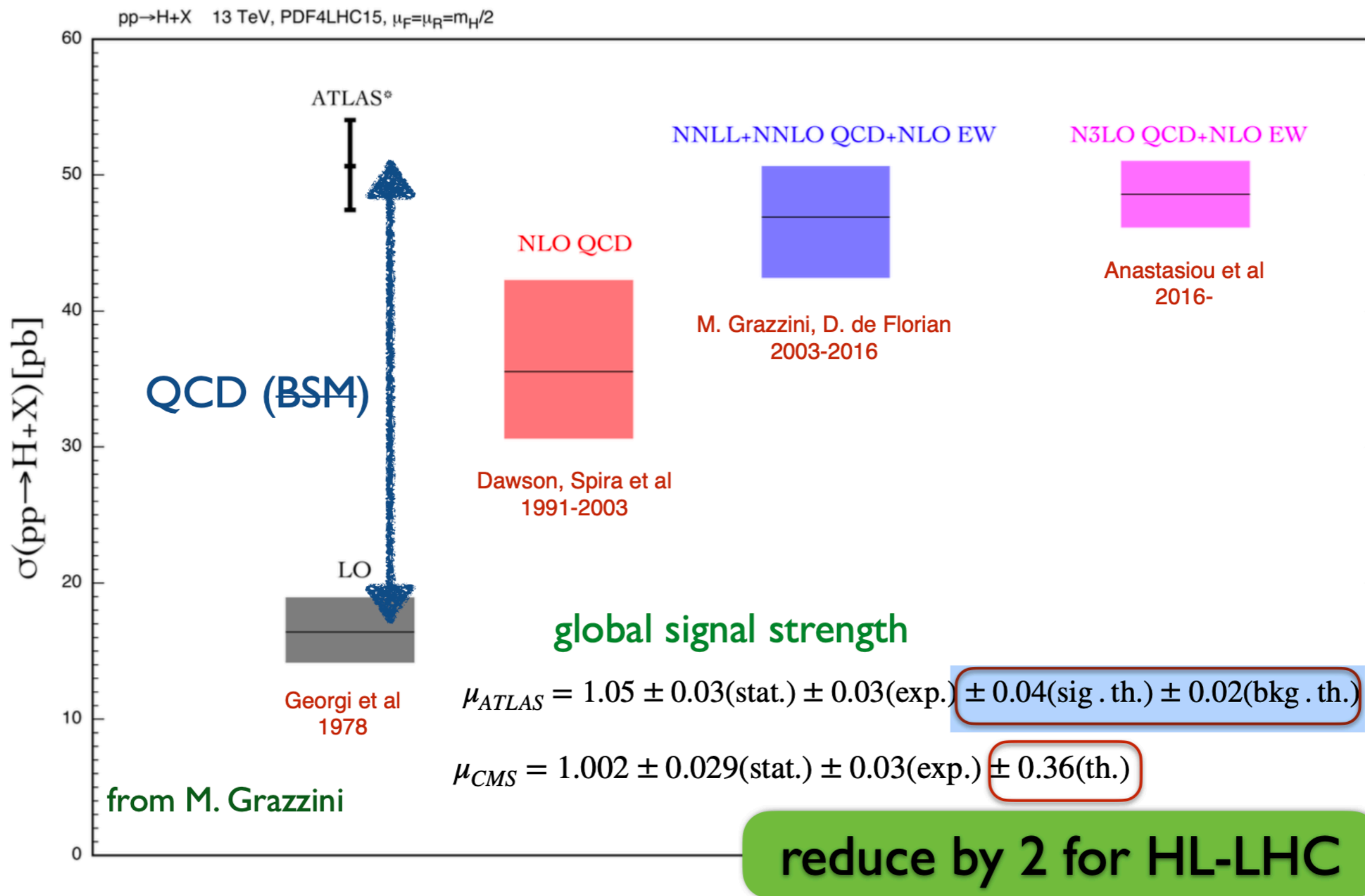


# Progress of Theoretical Calculations

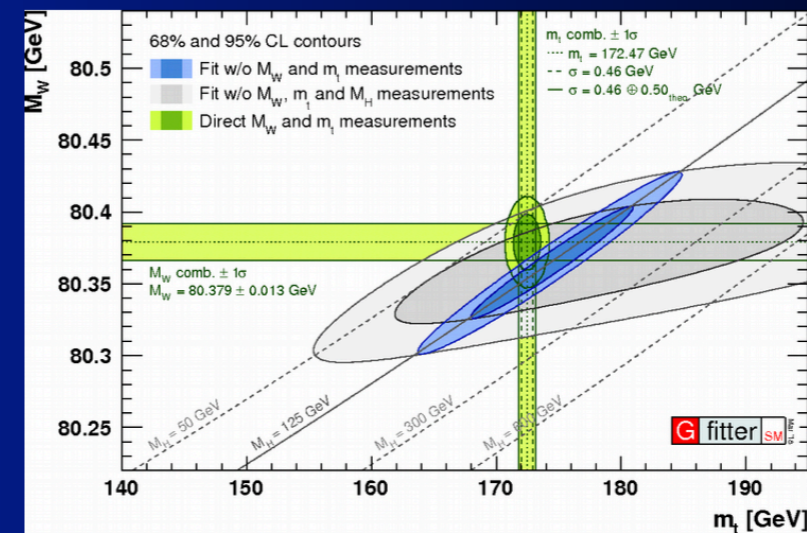
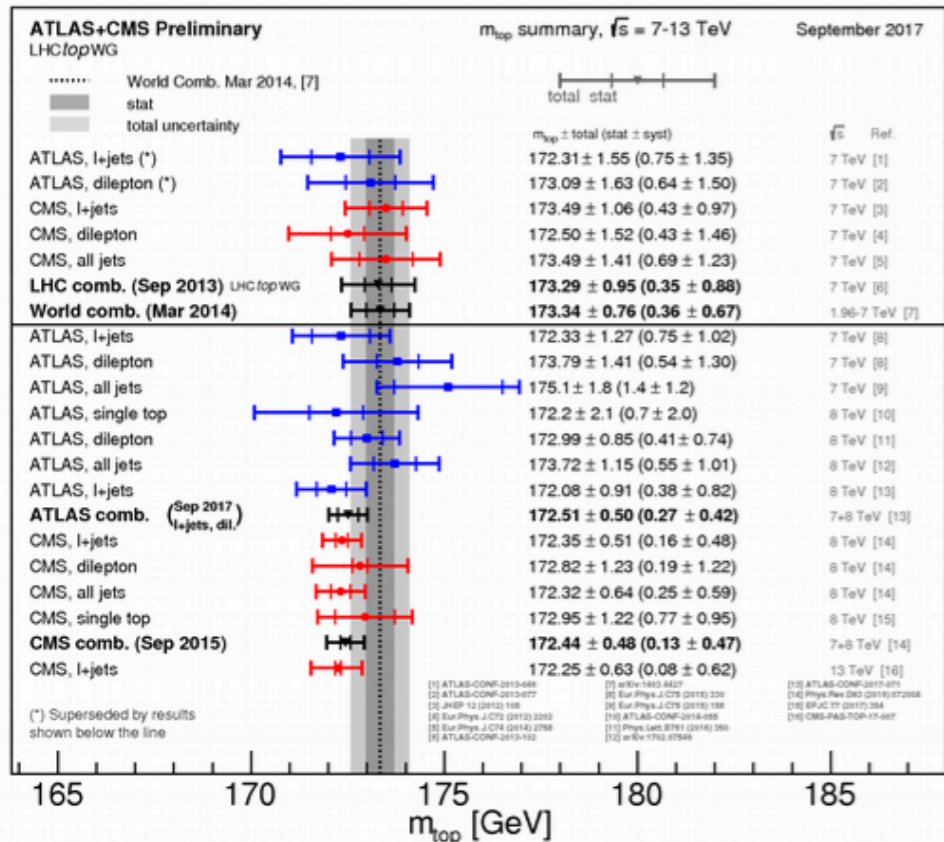
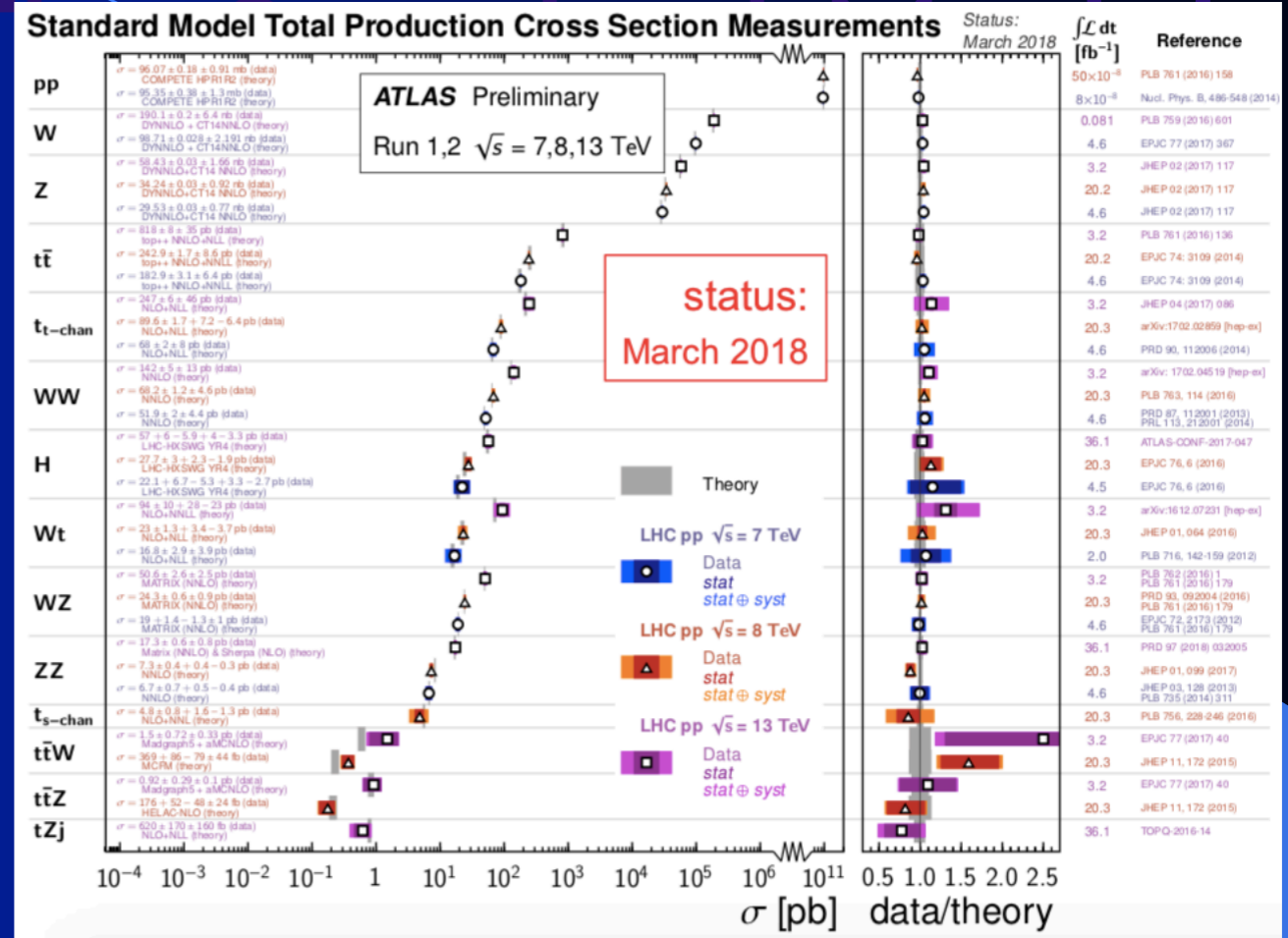
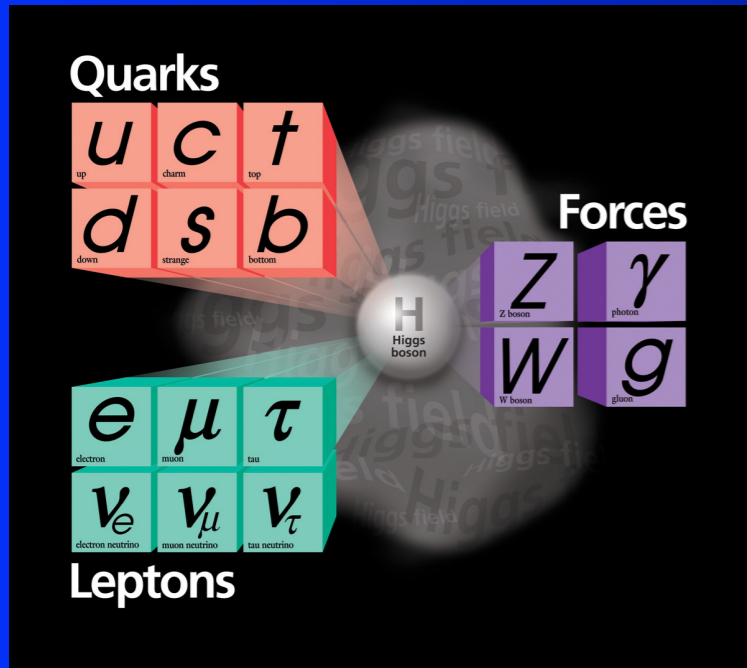
## The NNLO revolution standard



# Inclusive Higgs : an example of precision



# THE STANDARD MODEL: THE STATUS REPORT AND OPEN QUESTIONS



Extraordinary agreement between measurements and SM predictions <sup>47</sup>

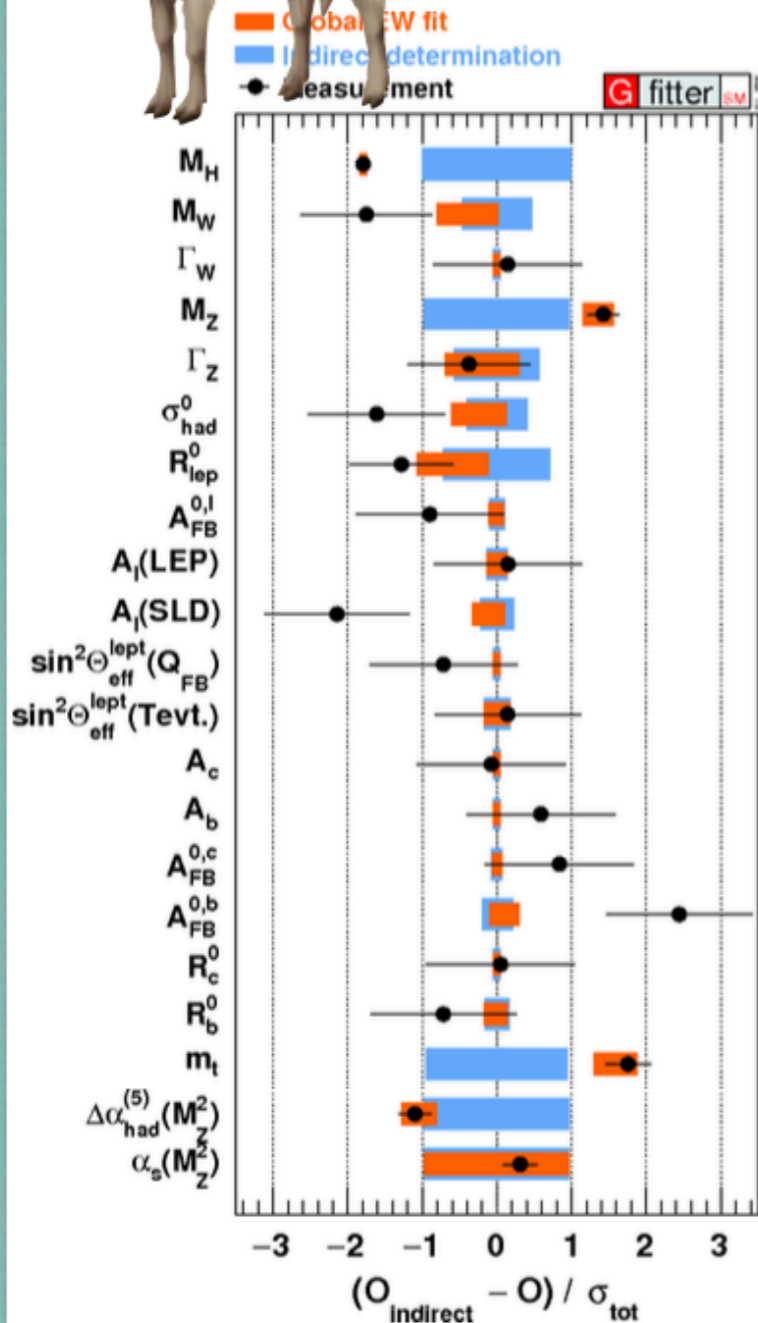


# The Triumph of the Standard Model

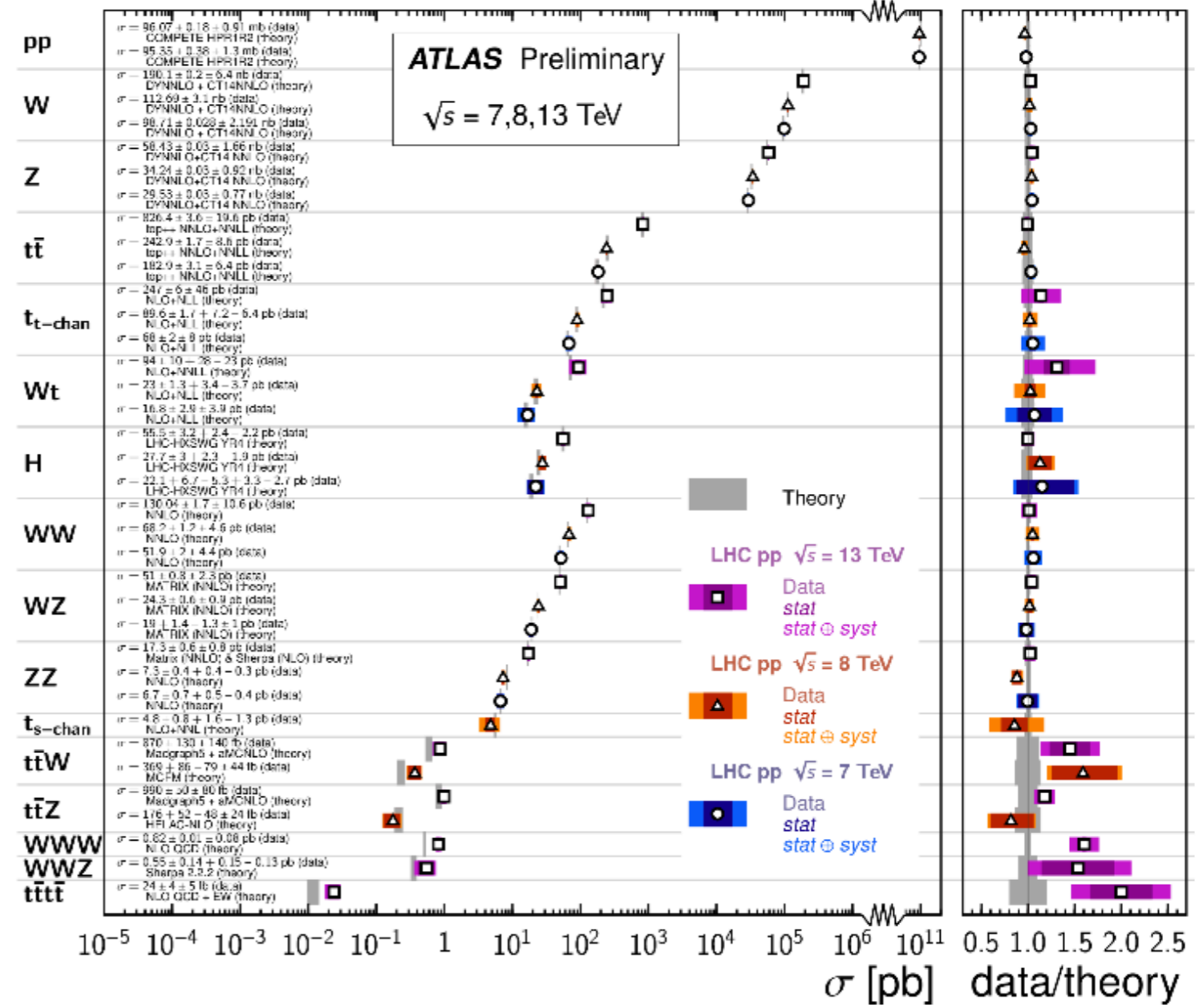


**SM**

**Everything looks SM-like at LHC**  
**Greatest Of All Theories**




## Standard Model Total Production Cross Section Measurements




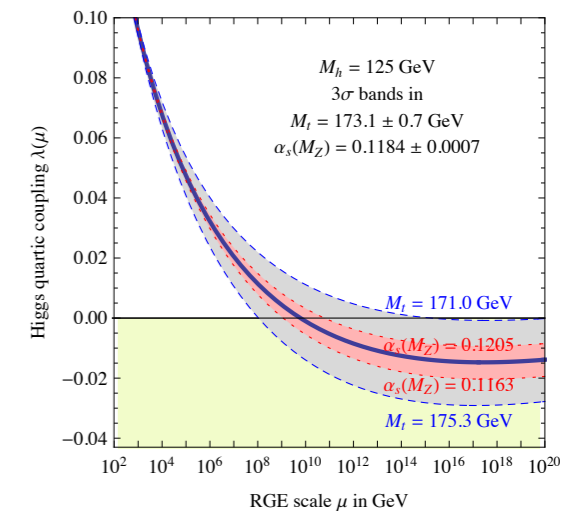
# THE PROBLEMS

 Quantum corrections can make the vacuum unstable



 the whole construction of the SM may be in trouble being metastable or even unstable


 the situation crucially depends on the top and Higgs mass values and requires severe fine-tuning and accuracy




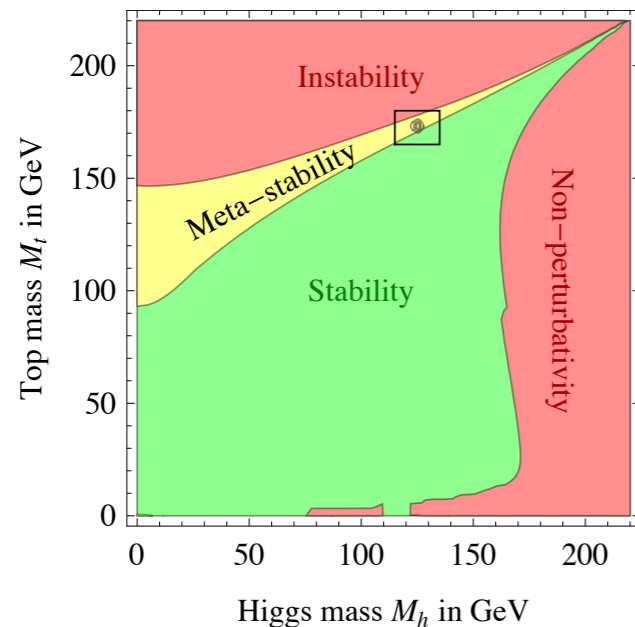
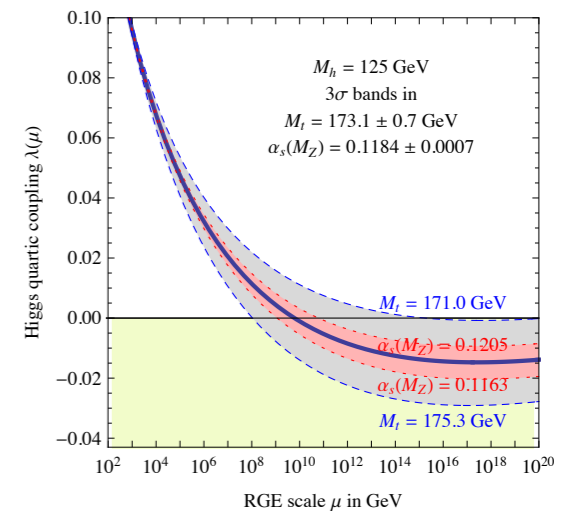
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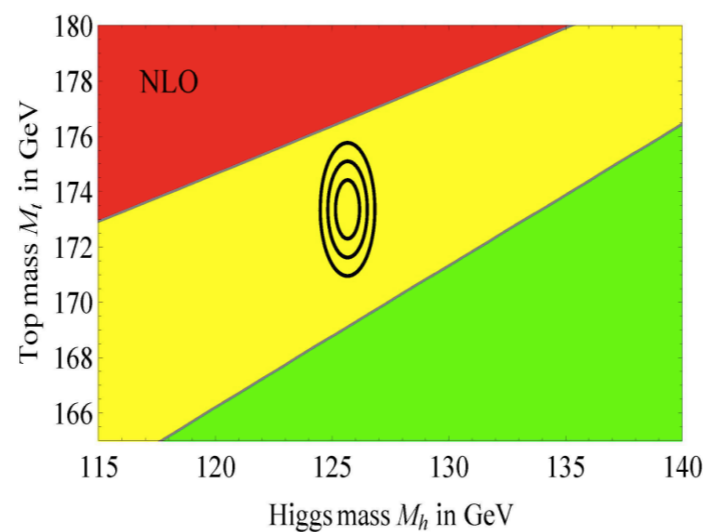
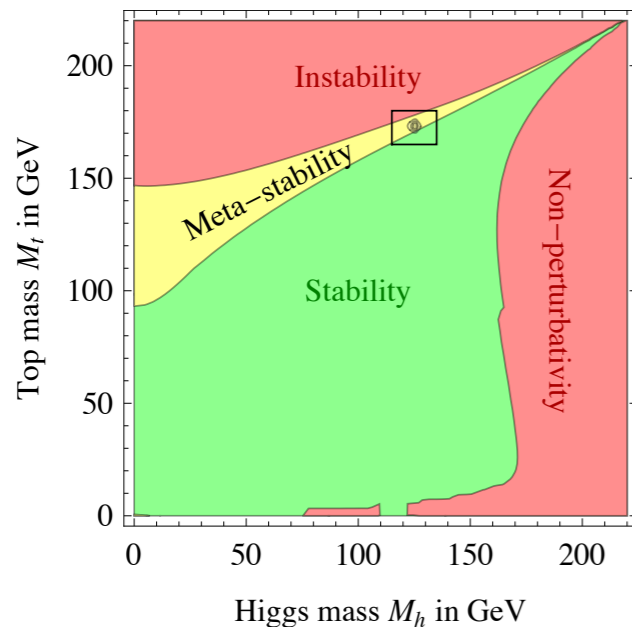
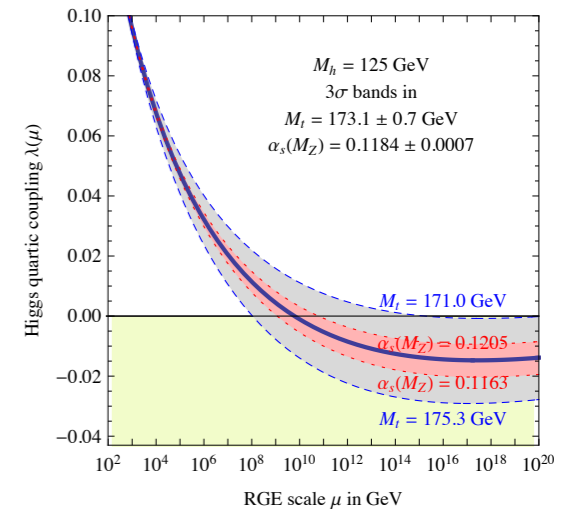
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NLO

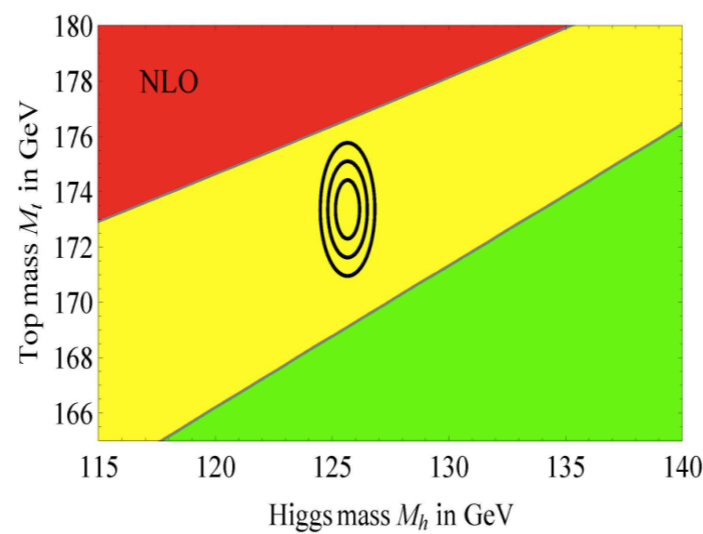
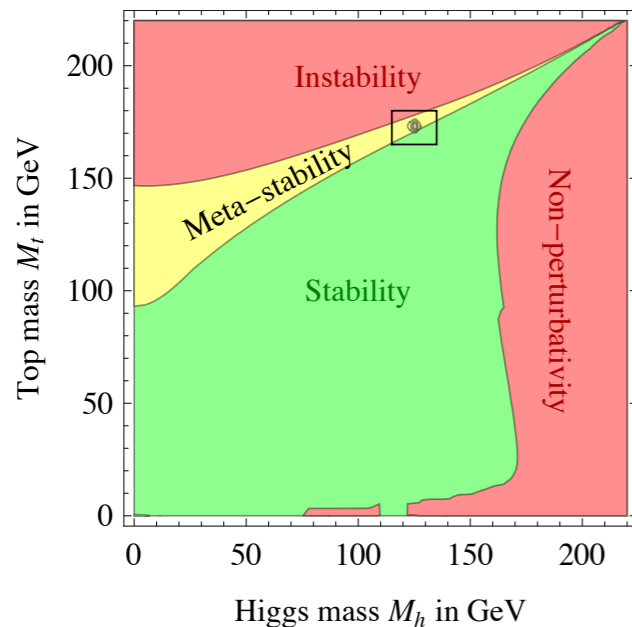
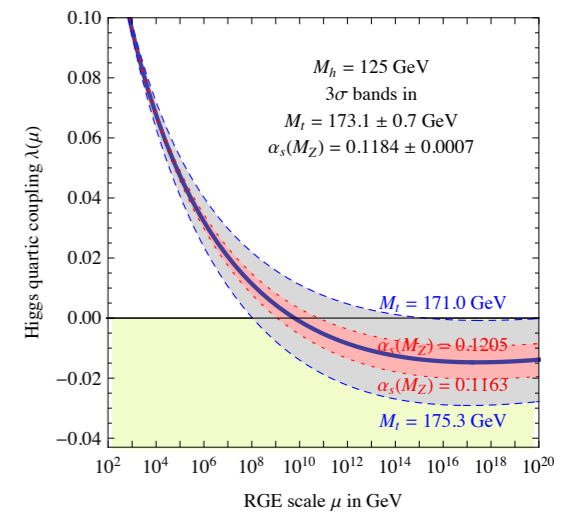
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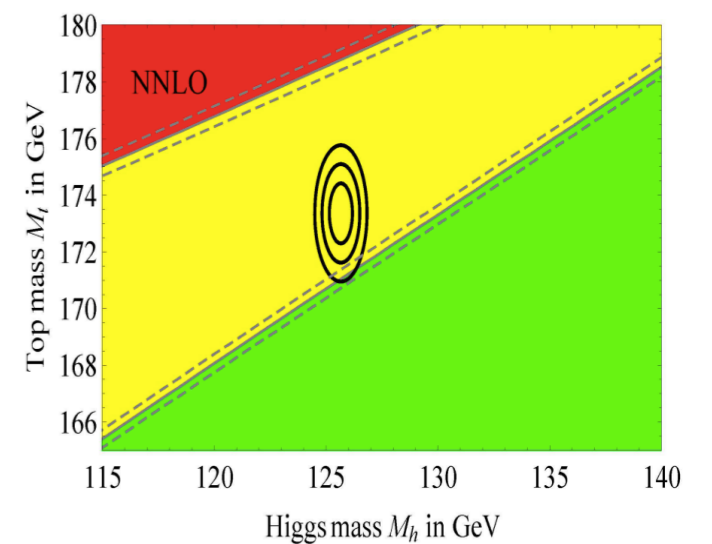


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NLO





NNLO

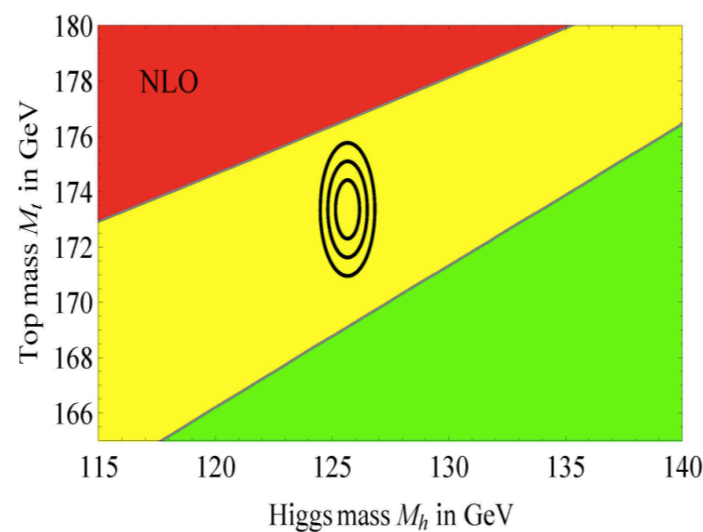
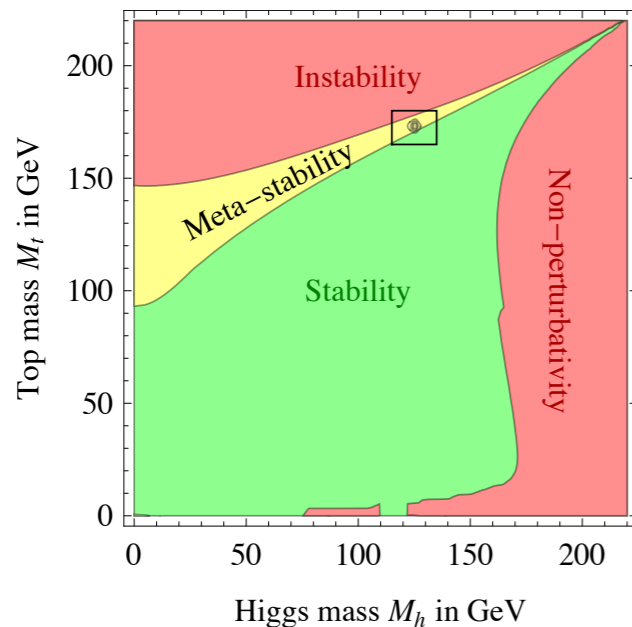
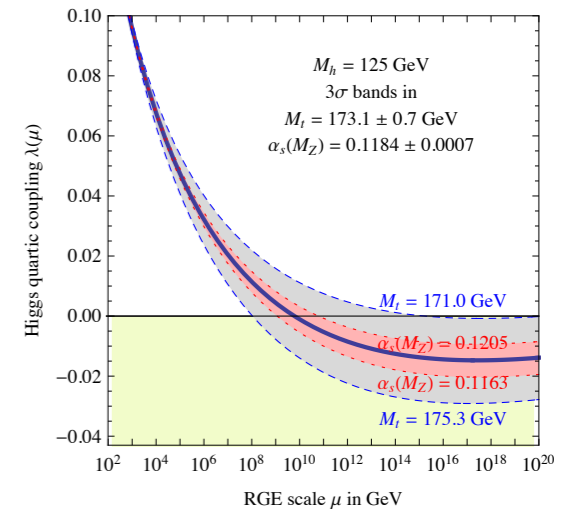
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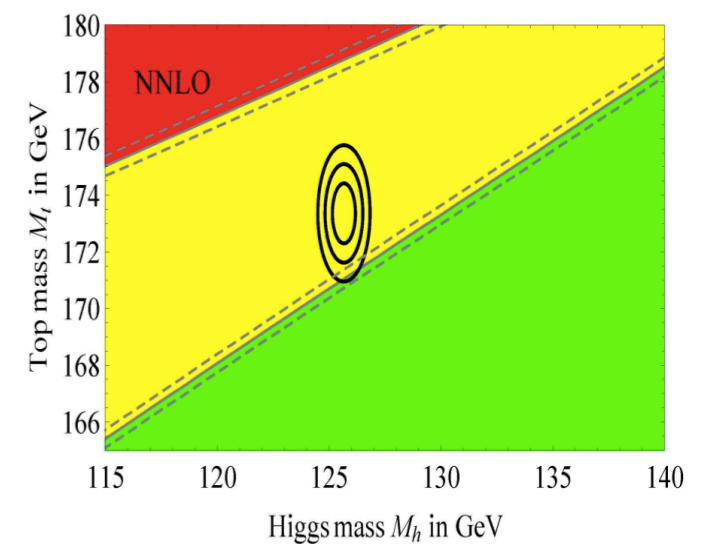


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NLO



NNLO

The way out might be the new physics at higher scale



- With the Higgs Boson discovery the Standard Model is completed !
- Why are we not satisfied and think that new physics exists and new discoveries will come?



- With the Higgs Boson discovery the Standard Model is completed !
- Why are we not satisfied and think that new physics exists and new discoveries will come?



- There are conceptual problems which require a critical view beyond the SM
- There are small discrepancies which might grow up to become a problem for the SM
- It is hard to believe that the quest for the miracle of Nature is over



# The Standard Model of Fundamental Interactions

Higgs Sector

Neutrino Sector

Flavour Sector

Dark Matter

New particles and Interactions

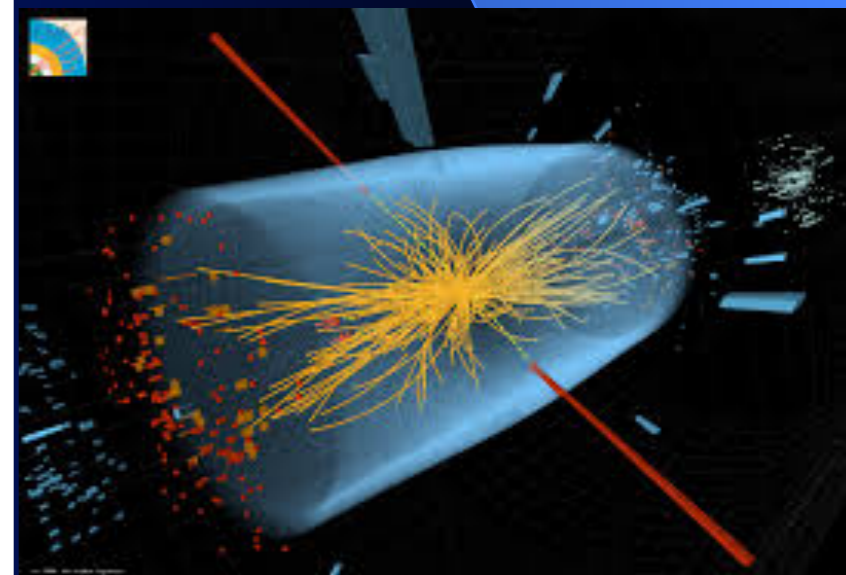
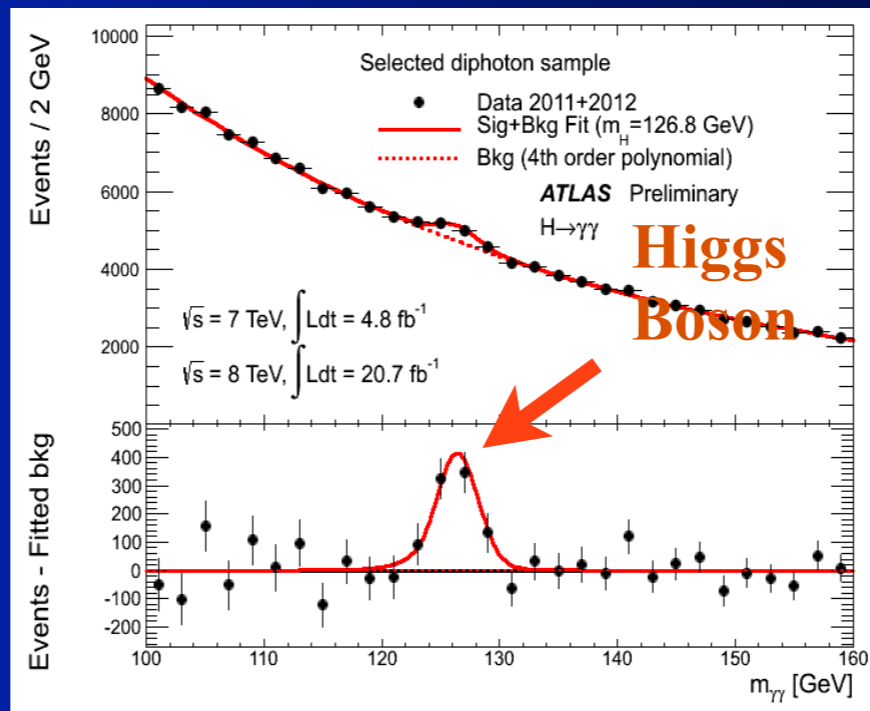
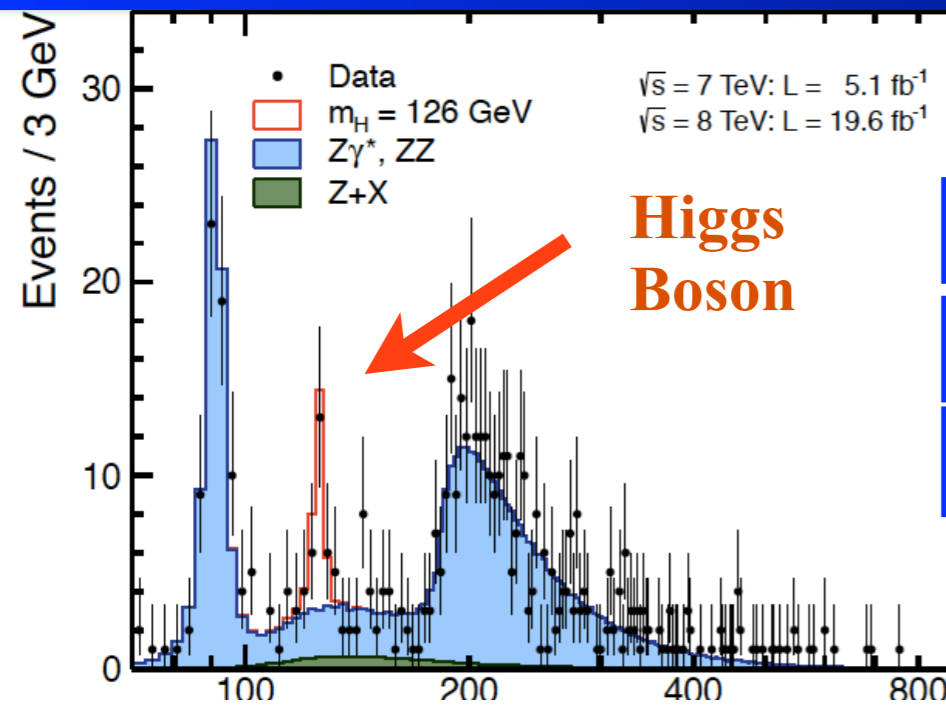
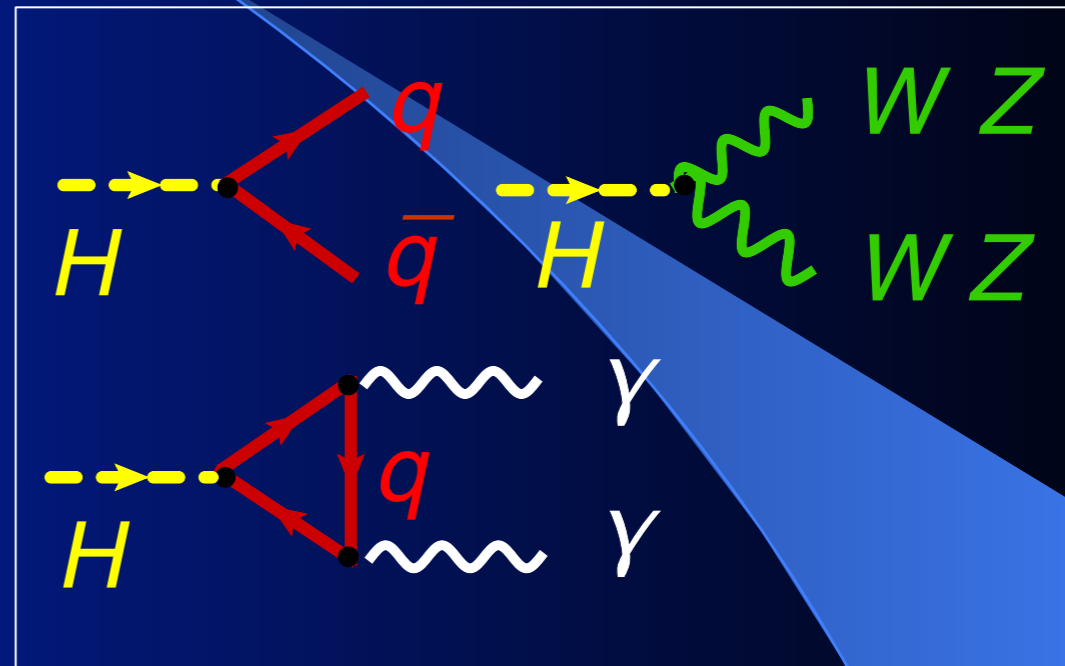
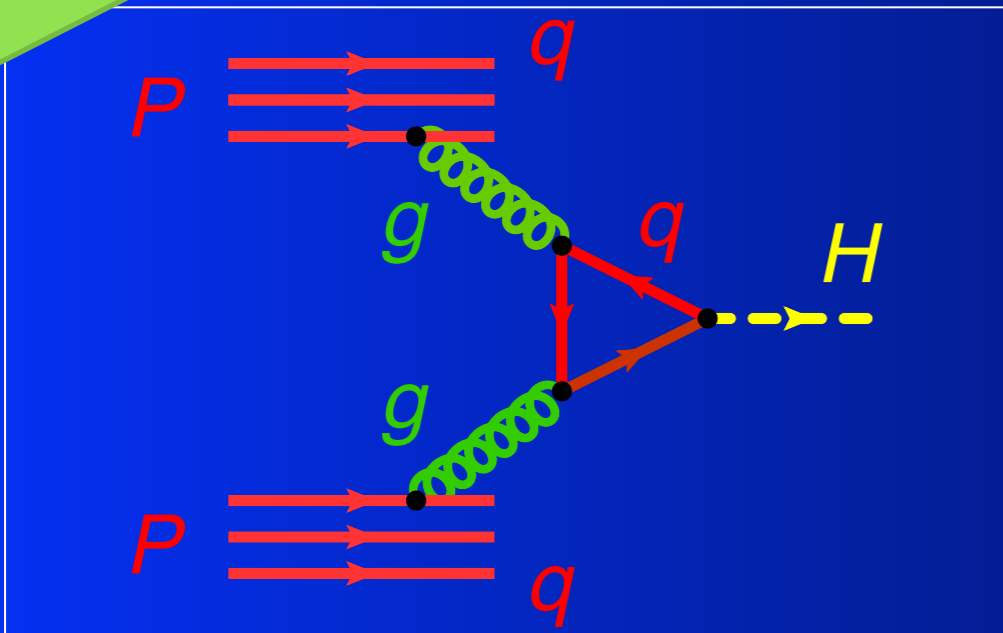
# Discovery of the Higgs Boson

CERN, Large Hadron Collider, 2012

Higgs Sector

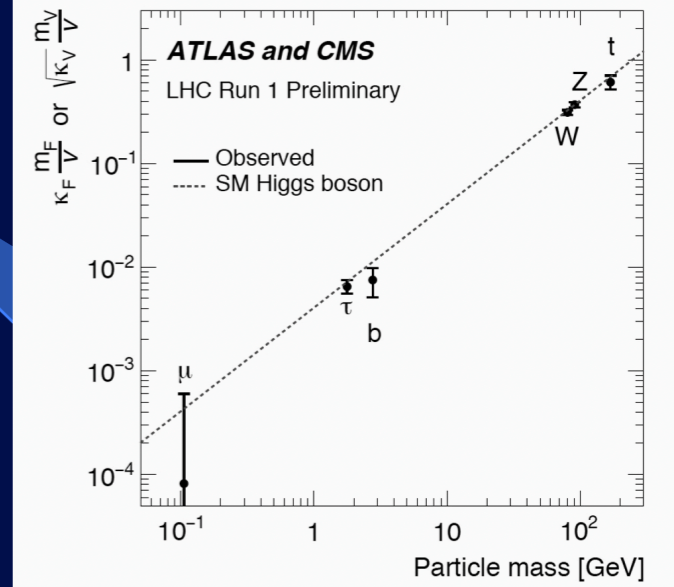
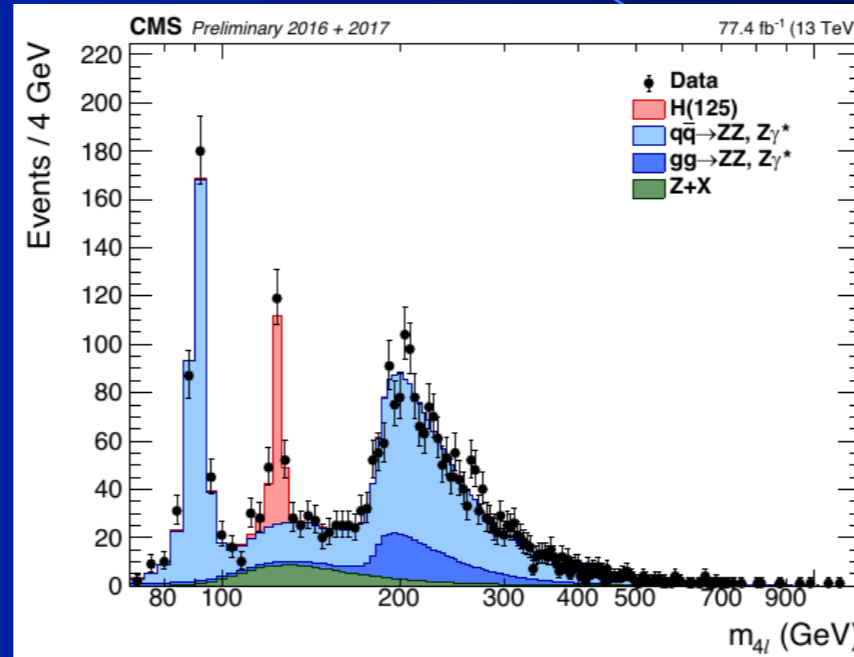
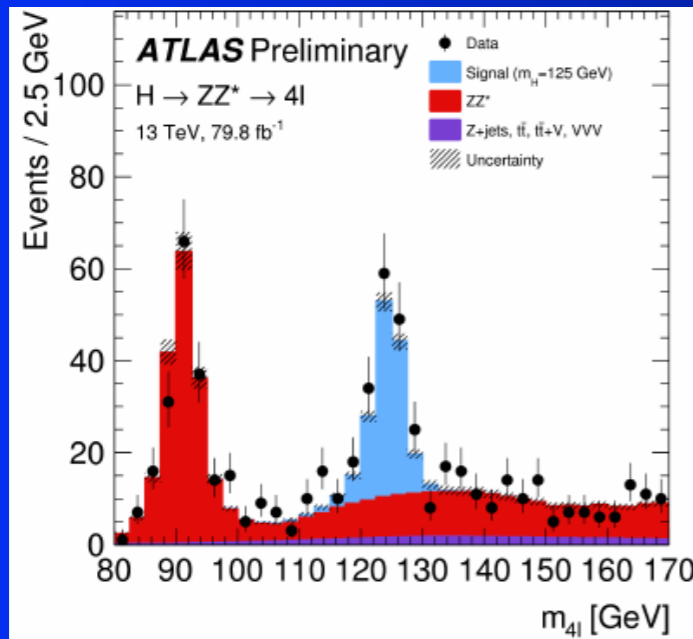
at Hadron Collider

Decay modes

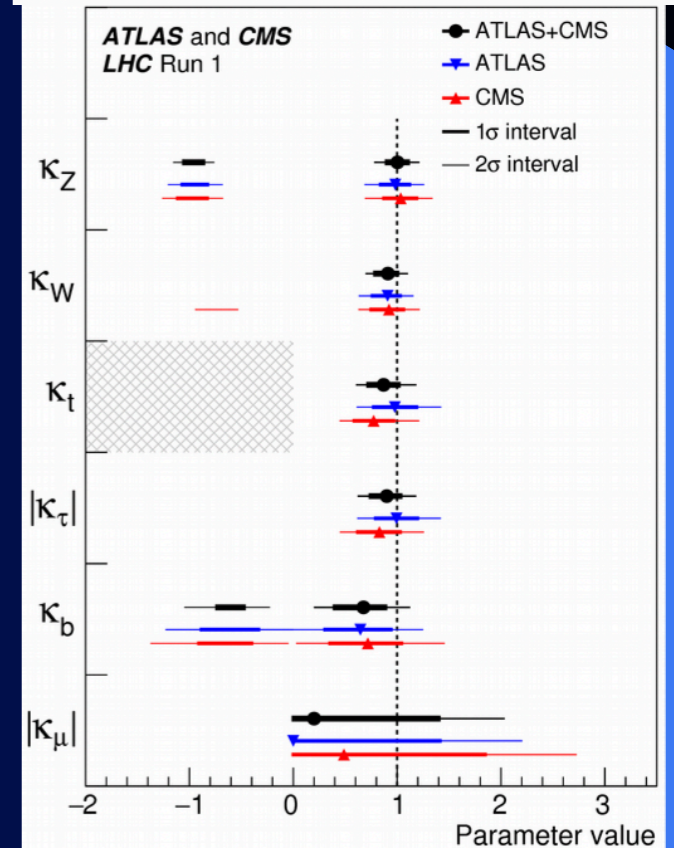
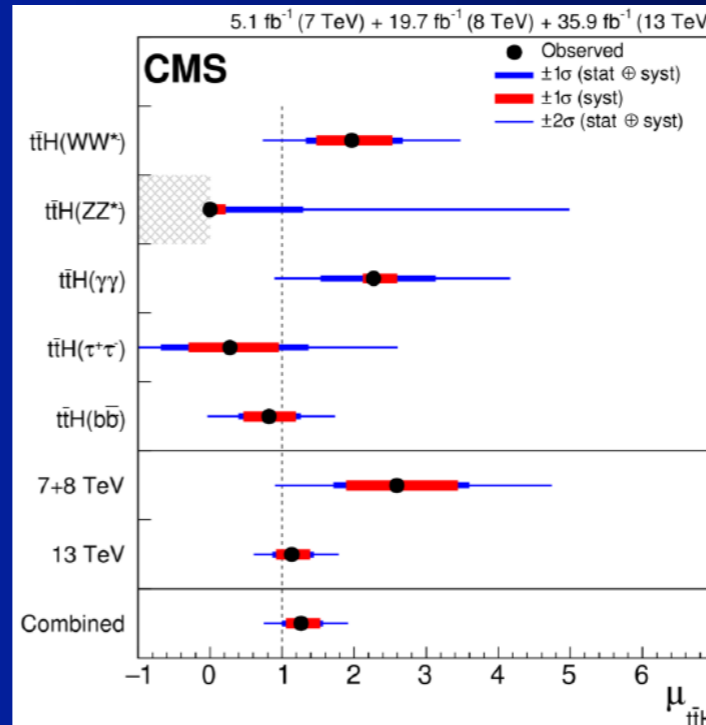
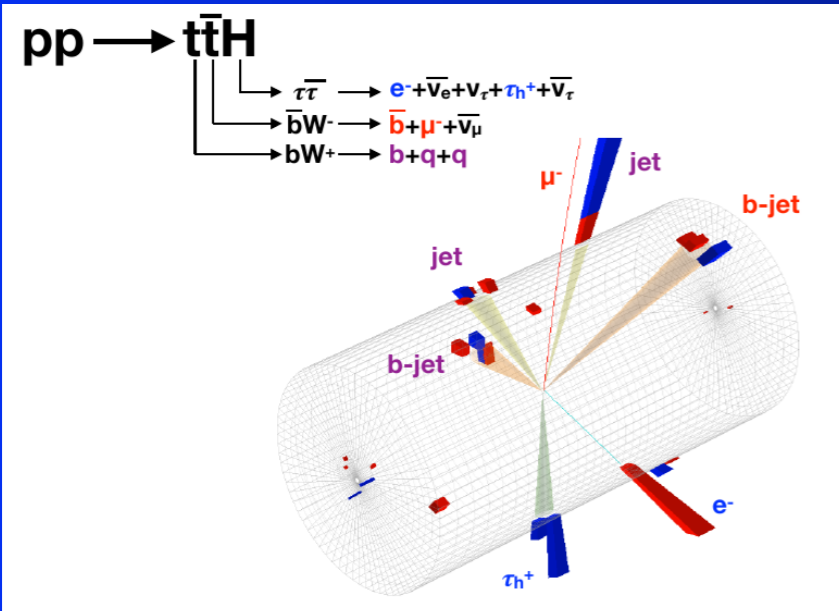


# Higgs bosons - entering precision era

Run-2 analyses with  $80 \text{ fb}^{-1}$  for the first time – higher precision is coming!



## ttH observation



## NEW PARTICLES

## EXTENDED HIGGS SECTOR



## NEW PARTICLES

Is it the SM Higgs boson or not?

What are the alternatives?

## EXTENDED HIGGS SECTOR

- A. Singlet extension
- B. Higgs doublet extension
- C. Higgs triplet extension



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How to probe?

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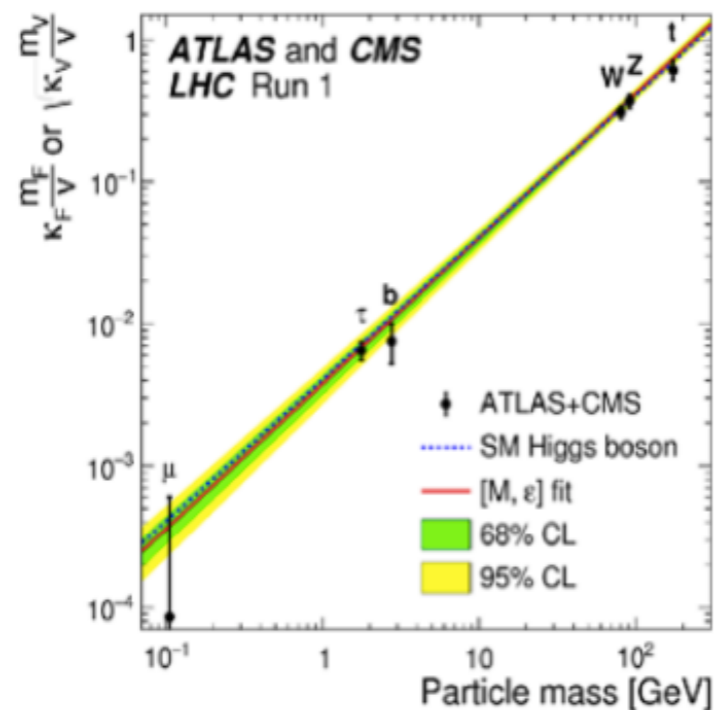
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- Probe deviations from the SM Higgs couplings



## EXTENDED HIGGS SECTOR

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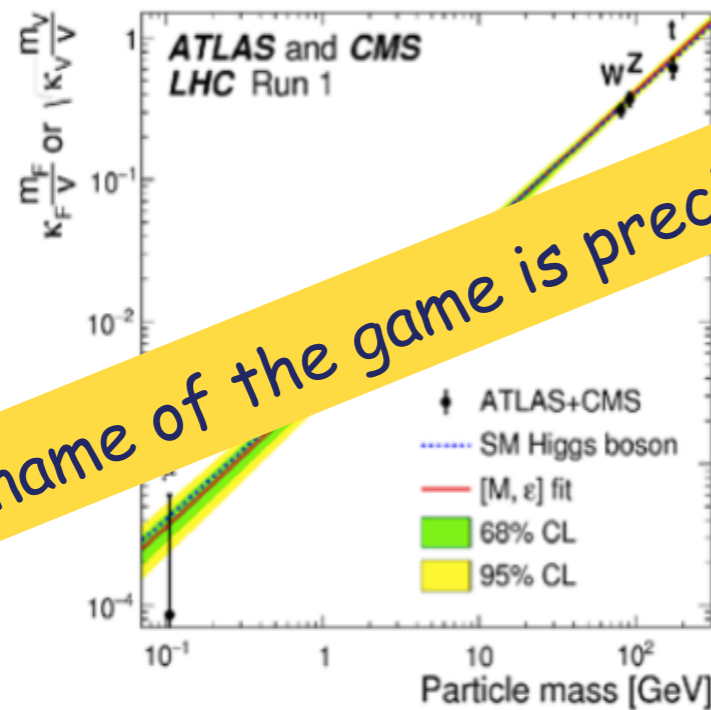
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The name of the game is precision

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What are the alternatives?

How to probe?

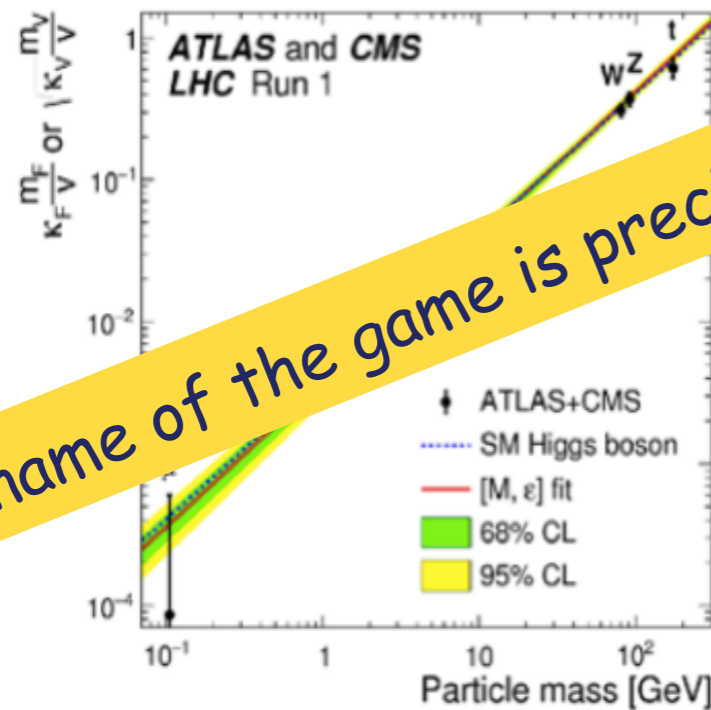
- Probe deviations from the SM Higgs couplings

# EXTENDED HIGGS SECTOR

- A. Singlet extension
- B. Higgs doublet extension
- C. Higgs triplet extension



- Perform direct search for additional scalars



The name of the game is precision

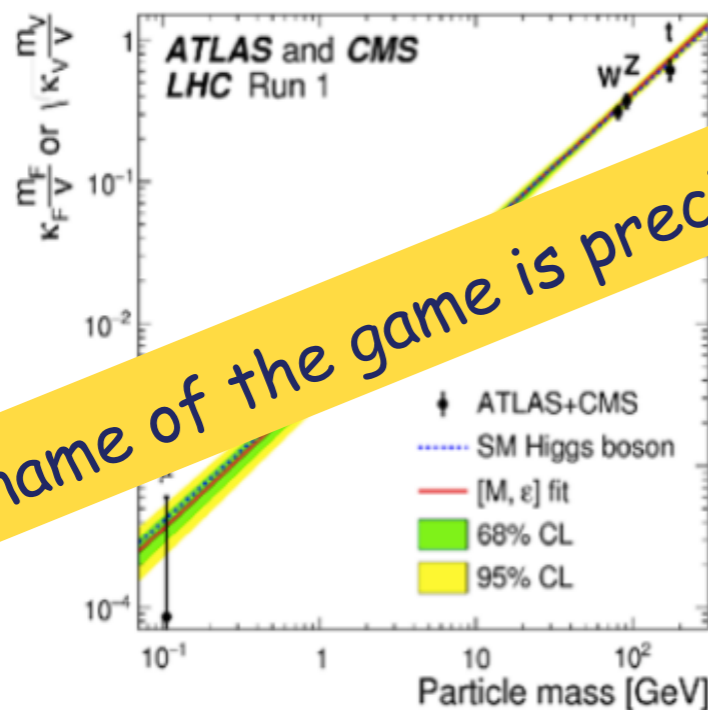
# NEW PARTICLES

Is it the SM Higgs boson or not?

What are the alternatives?

How to probe?

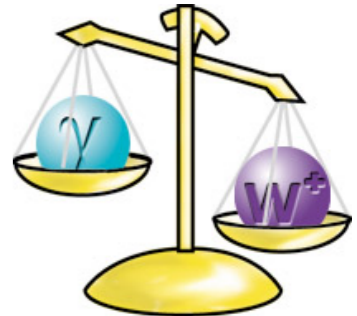
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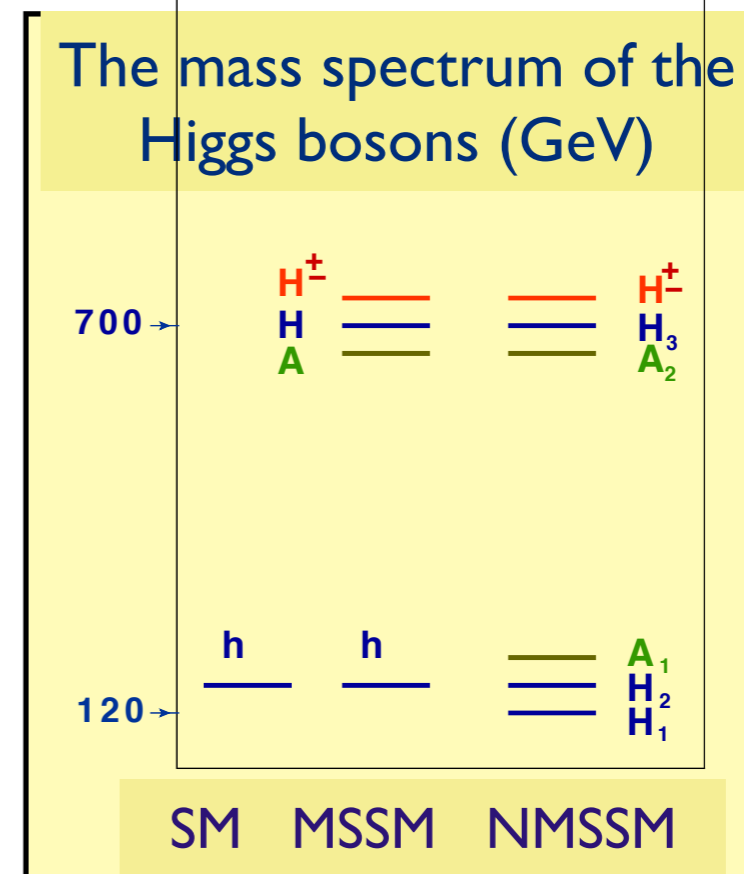
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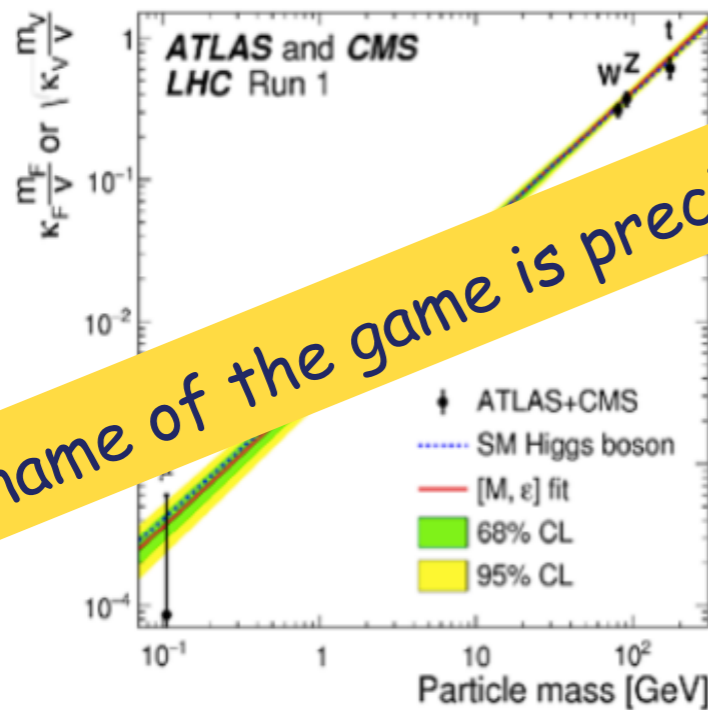
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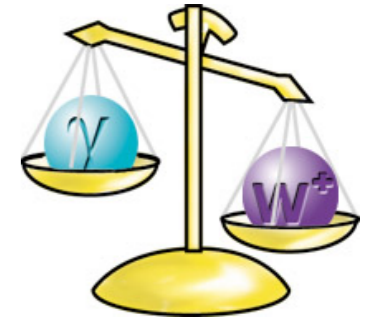
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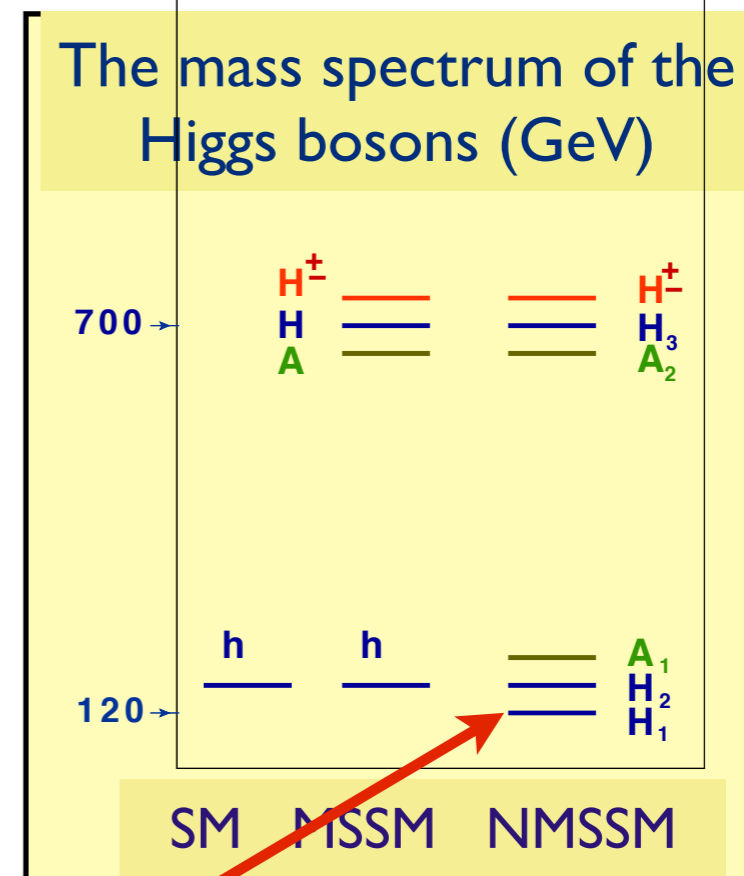
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# EXTENDED HIGGS SECTOR



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- Perform direct search for additional scalars



We may have found one of these states

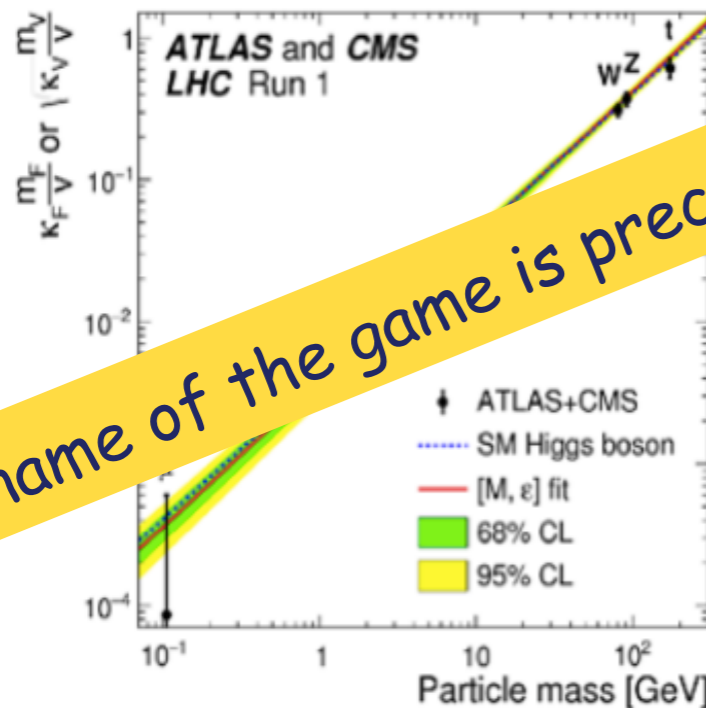
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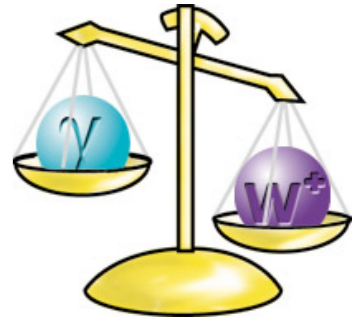
How to probe?

- Probe deviations from the SM Higgs couplings



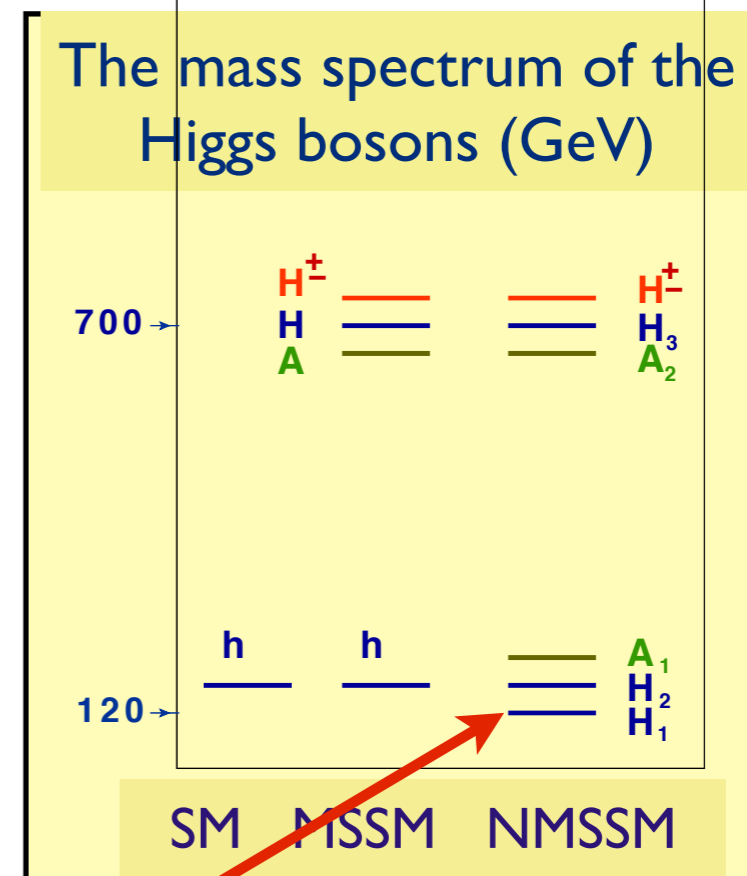
- The Higgs physics has already started
- This is the task of vital importance.
- May require the electron-positron collider

# EXTENDED HIGGS SECTOR



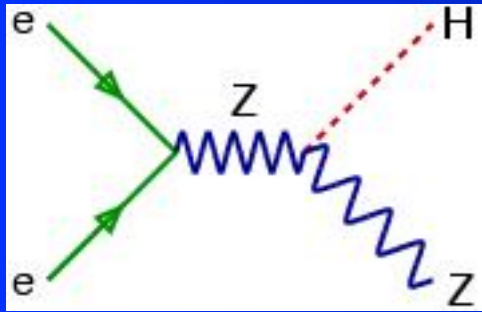
- A. Singlet extension
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# PRECISION PHYSICS OF THE HIGGS BOSONS

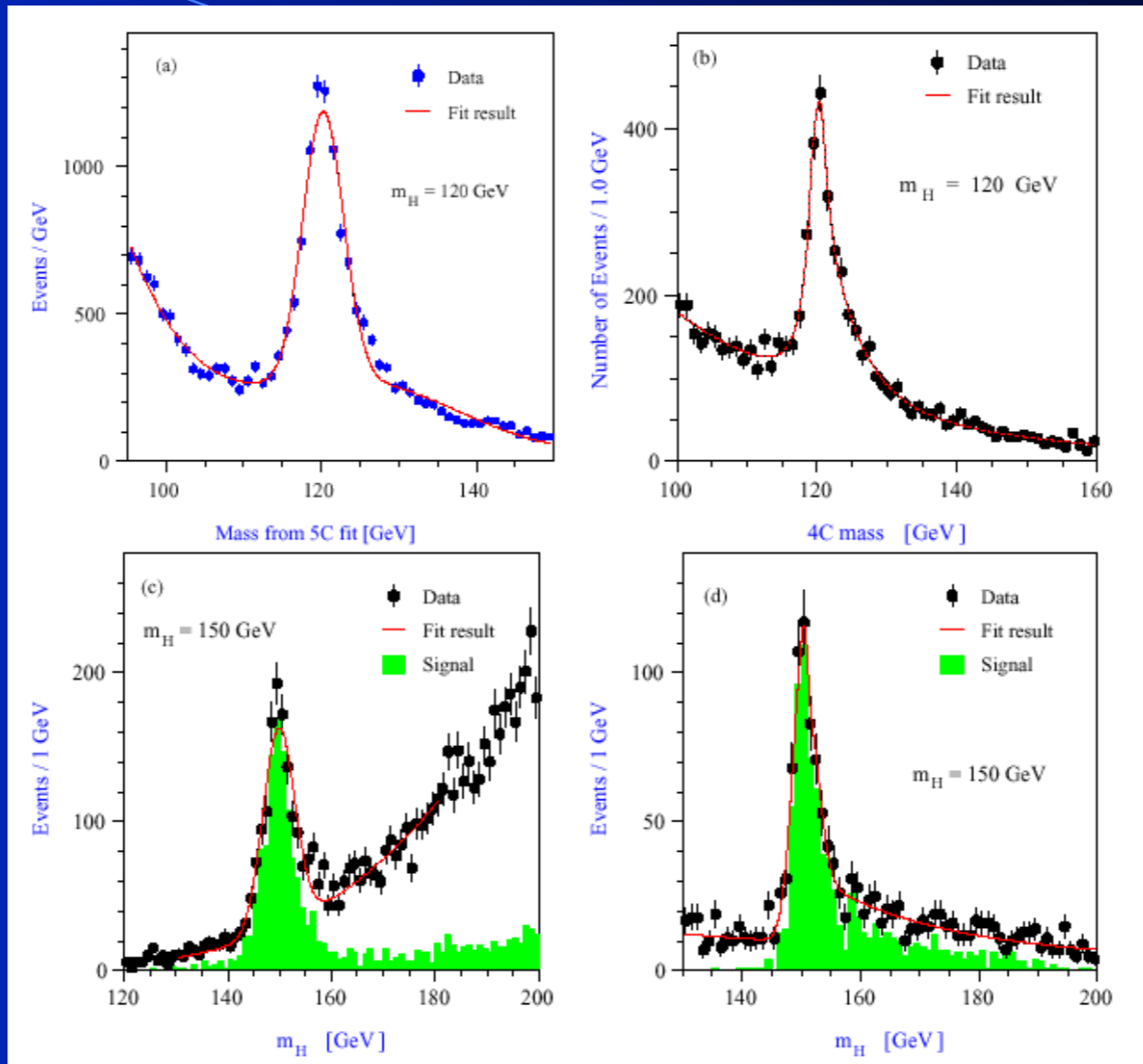


$$\rightarrow b\bar{b}q\bar{q}$$

$ee \rightarrow HZ$  diff. decay channels

Int Linear Collider

$$\rightarrow W^+W^-q\bar{q}$$



$$\rightarrow q\bar{q}l^+l^-$$

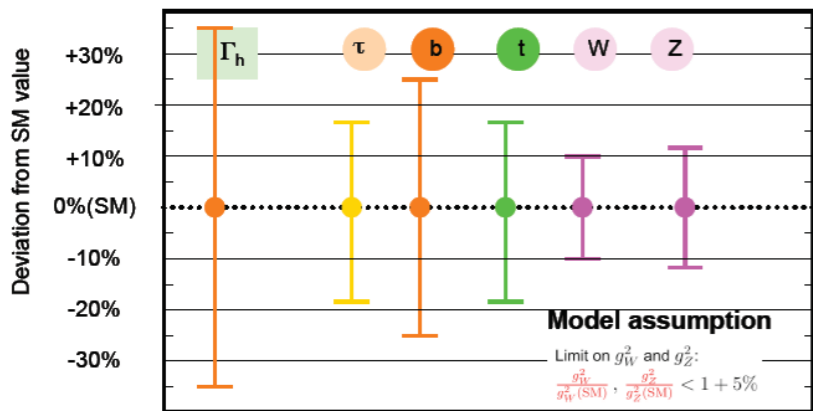
$\Delta m_H = 40 \text{ MeV}$

$$\rightarrow W^+W^-l^+l^-$$

$\Delta m_H = 70 \text{ MeV}$

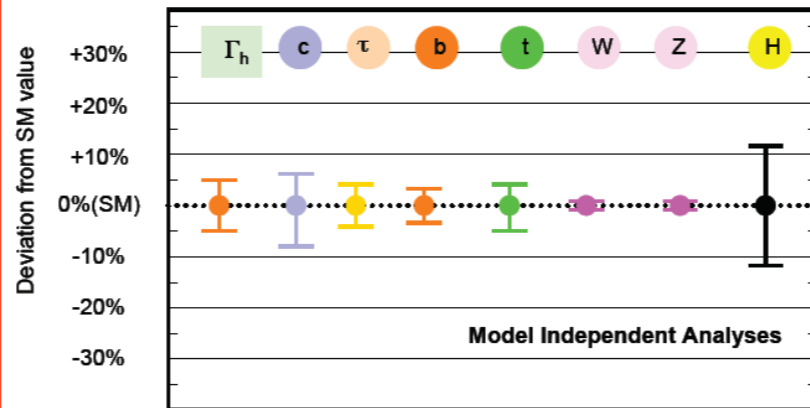
## Coupling Precision

LHC 300 fb<sup>-1</sup> x 2



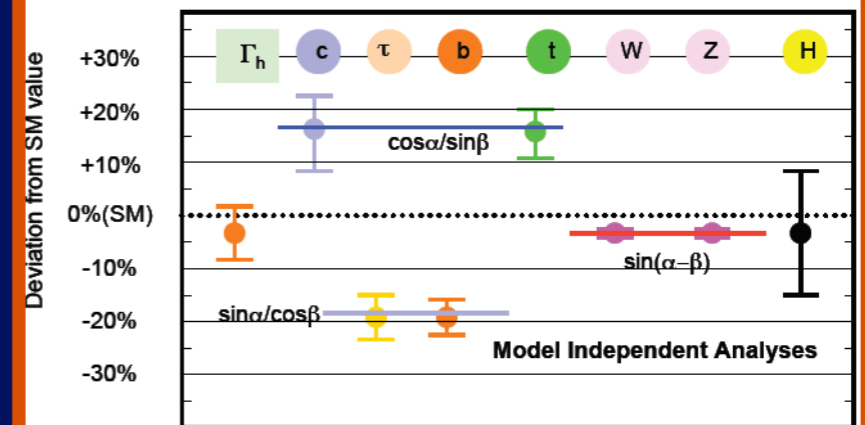
## Coupling Precision

ILC

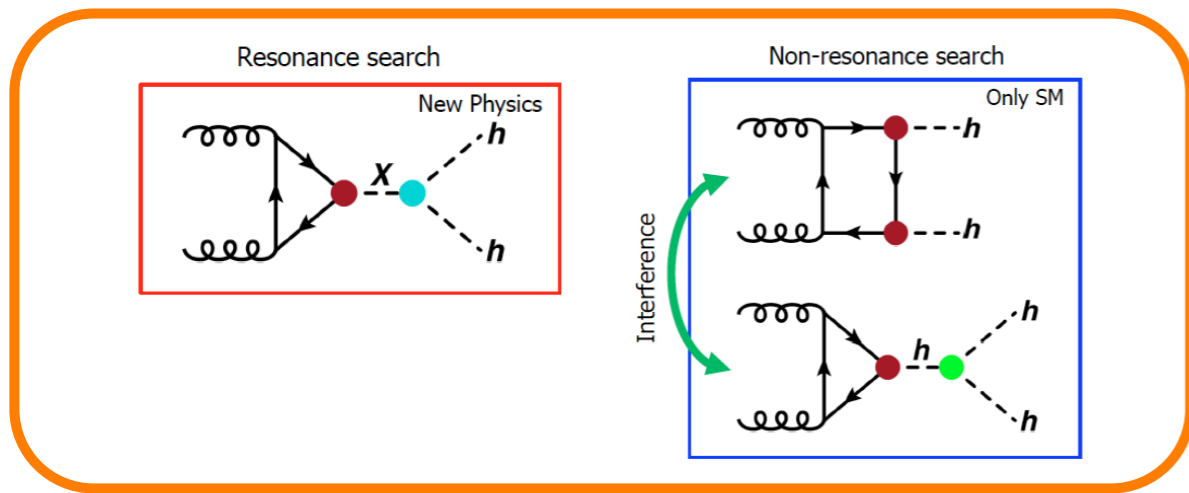


## SUSY or 2HDM

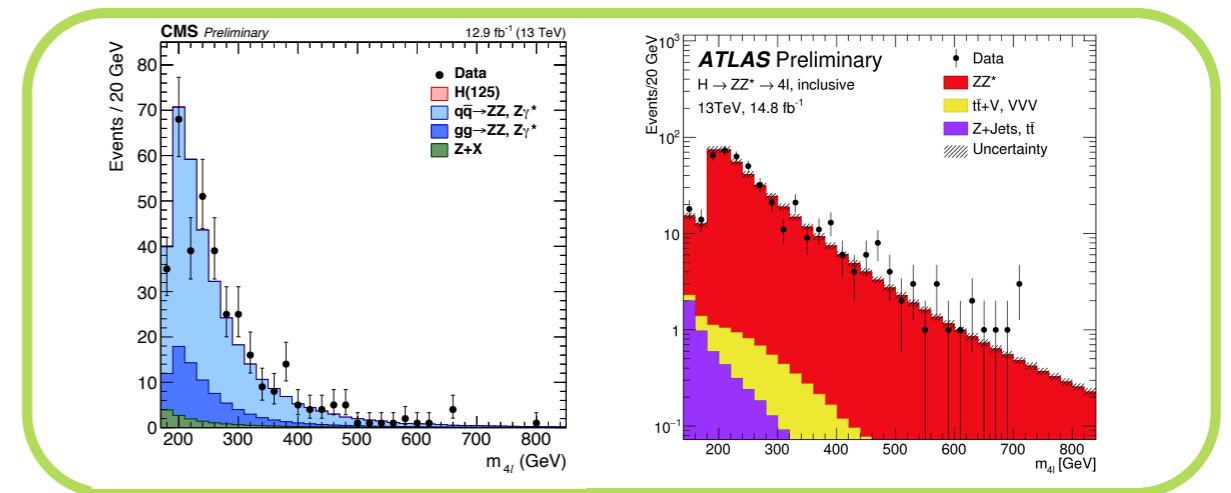
ILC



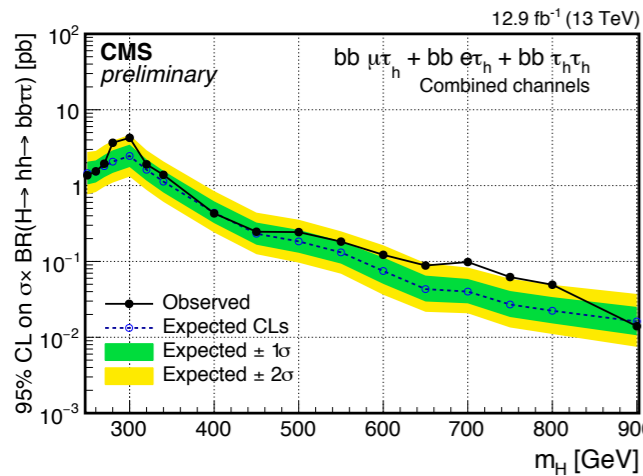
## Higgs $\rightarrow hh \rightarrow bb\tau\tau$



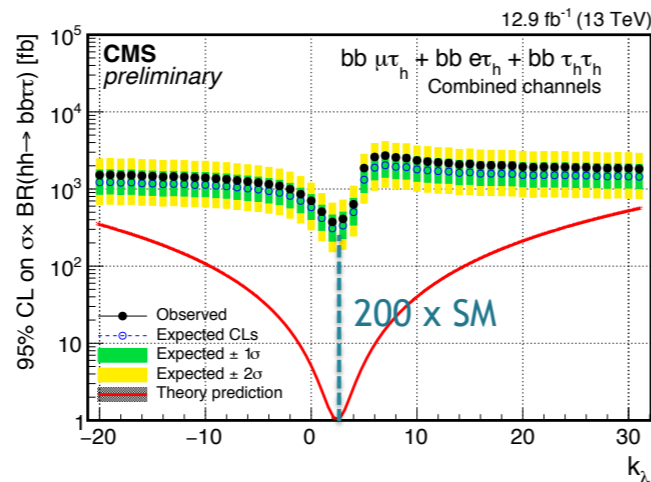
## Heavy Higgs $\rightarrow ZZ \rightarrow 4l$



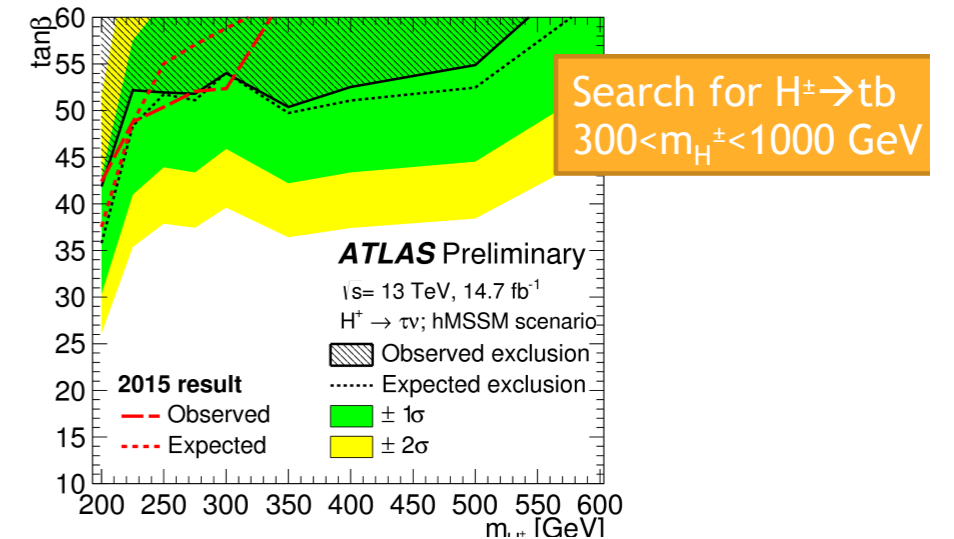
### Resonant



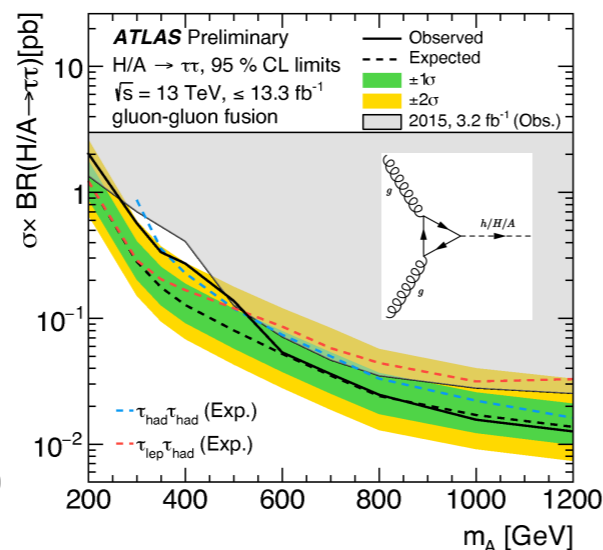
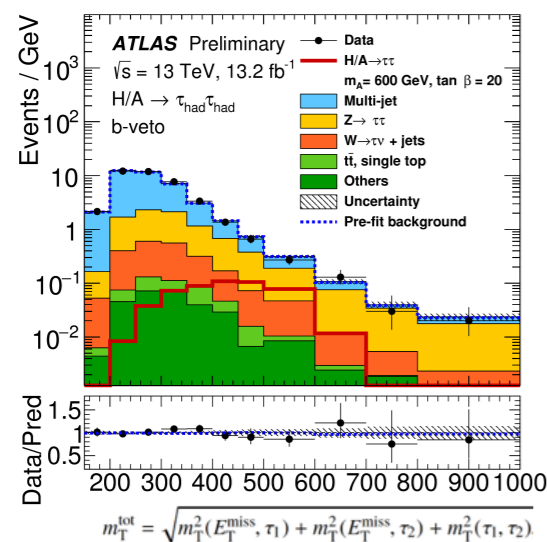
### Non-Resonant



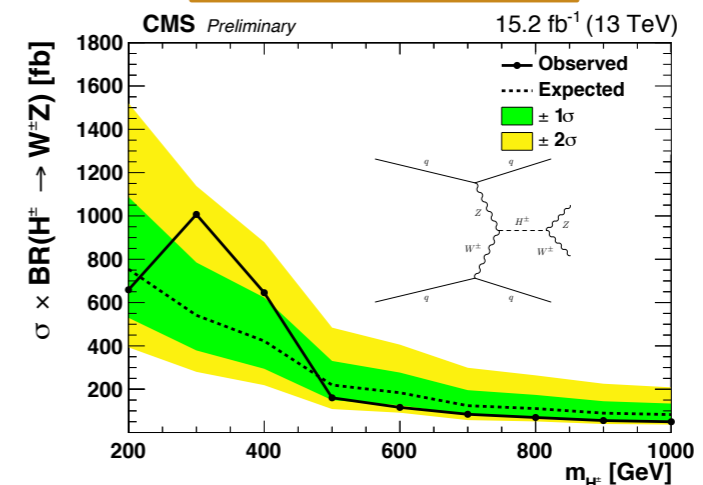
## Charged Higgs



## Heavy Higgs $\rightarrow \tau\tau$



### Search for $H^\pm WZ$



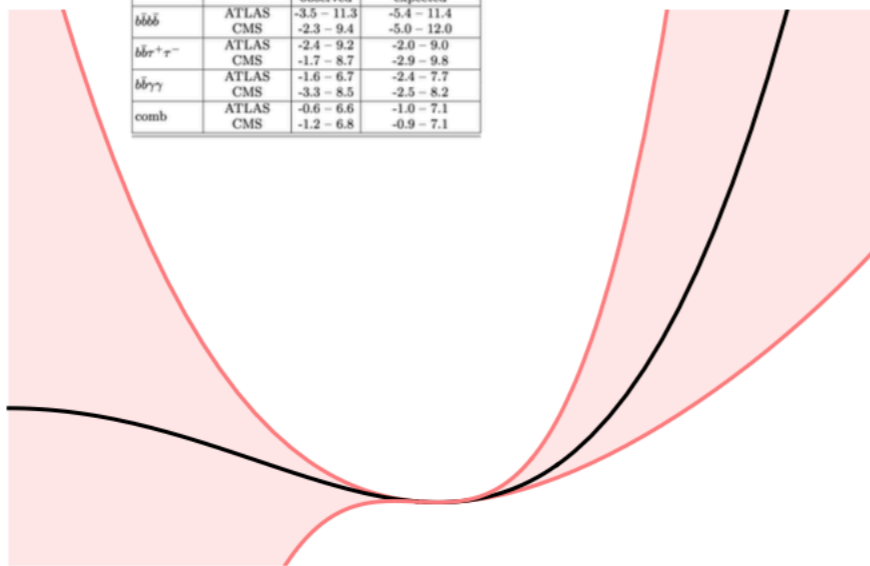
# The Higgs potential - test of the SM

## Higgs self coupling [Meade]

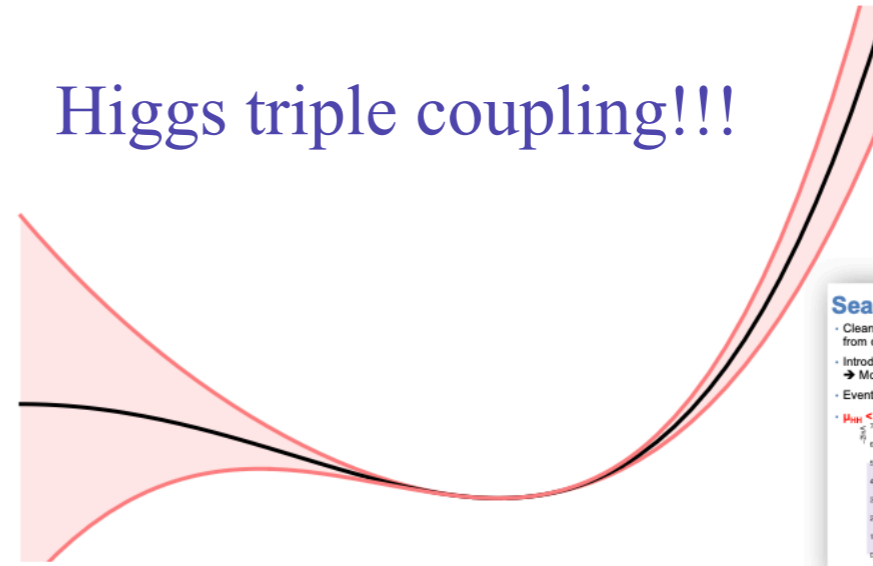
If the questions center on the Higgs, do we need to do more than sit back and wait for more data for more precision (or a Higgs factory)?

Snowmass EF Higgs Topical Report  
2209.07510

Final state	Collaboration	allowed $\kappa_\lambda$ interval at 95% CL observed	expected
$b\bar{b}\delta$	ATLAS	-3.5 - 11.3	-5.4 - 11.4
	CMS	-2.3 - 9.4	-5.0 - 12.0
$b\bar{b}\tau^+\tau^-$	ATLAS	-2.4 - 9.2	-2.0 - 9.0
	CMS	-1.7 - 8.7	-2.9 - 9.8
$b\bar{b}\gamma\gamma$	ATLAS	-1.6 - 6.7	-2.4 - 7.7
	CMS	-3.3 - 8.5	-2.5 - 8.2
comb	ATLAS	-0.6 - 6.6	-1.0 - 7.1
	CMS	-1.2 - 6.8	-0.9 - 7.1



Higgs triple coupling!!!



**Search for DiHiggs in bbyy** ATLAS-CONF-2023-050  
Viviana's talk

- Clean  $H \rightarrow \gamma\gamma$  signature and excellent  $m_{\gamma\gamma}$  resolution to discriminate HH signal from continuum  $\gamma\gamma$  background
- Introduced VBF-jet tagger to improve jet assignment  
→ More sensitive to VBF HH
- Event categorization using BDT scores

**$\mu_{HH} < 4.0$  (6.4 exp.) at 95% CL**

H/T N.Craig, R. Petrossian-Byrne

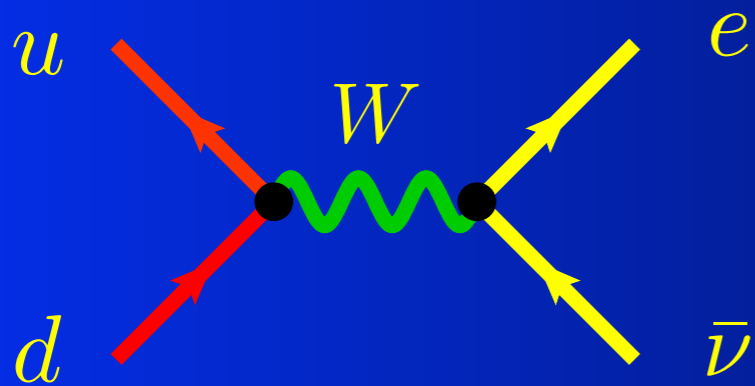
When do we *really* care about non-resonant di-Higgs ( $\lambda_3$ ) for its own sake?

Interesting to think about in more general setups beyond singlet, e.g. composite Higgs

# Neutrino Sector

# Neutrino-mysterious particle

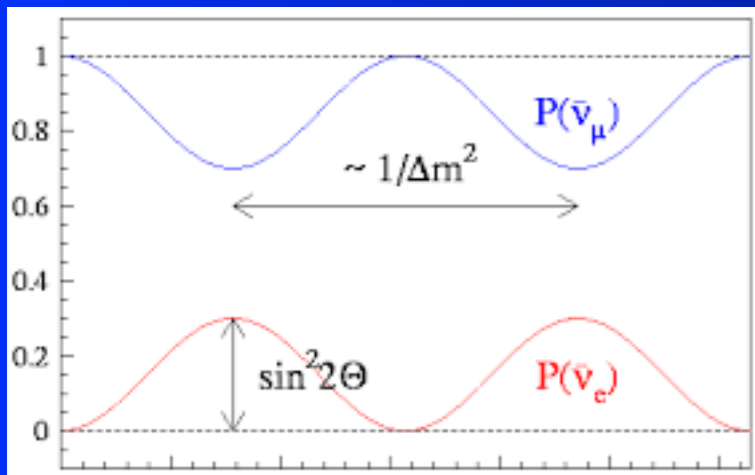
Neutrino is created in the process of weak decays of hadrons



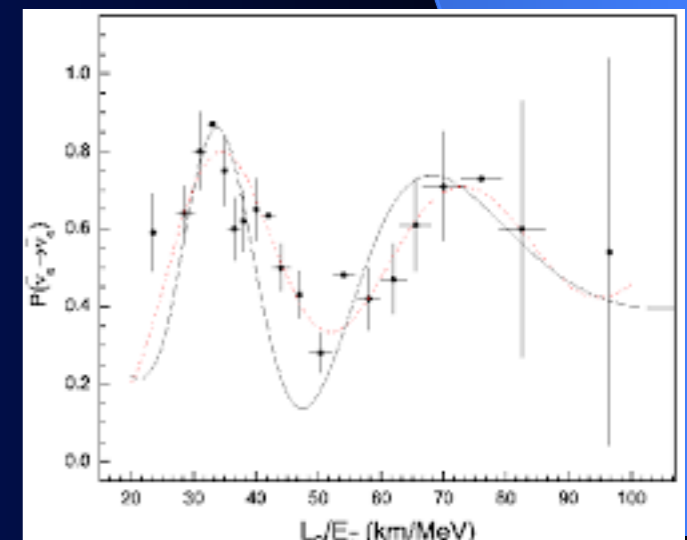
## Neutrino

- Has no electric charge
- Do not participate in electromagnetic interactions
- Do not participate in strong interactions
- Participate in weak interactions
- Interact with the Higgs field
- Has a very small ( $< 1$  eV) mass

Non-zero neutrino mass follows from the observation of neutrino oscillations



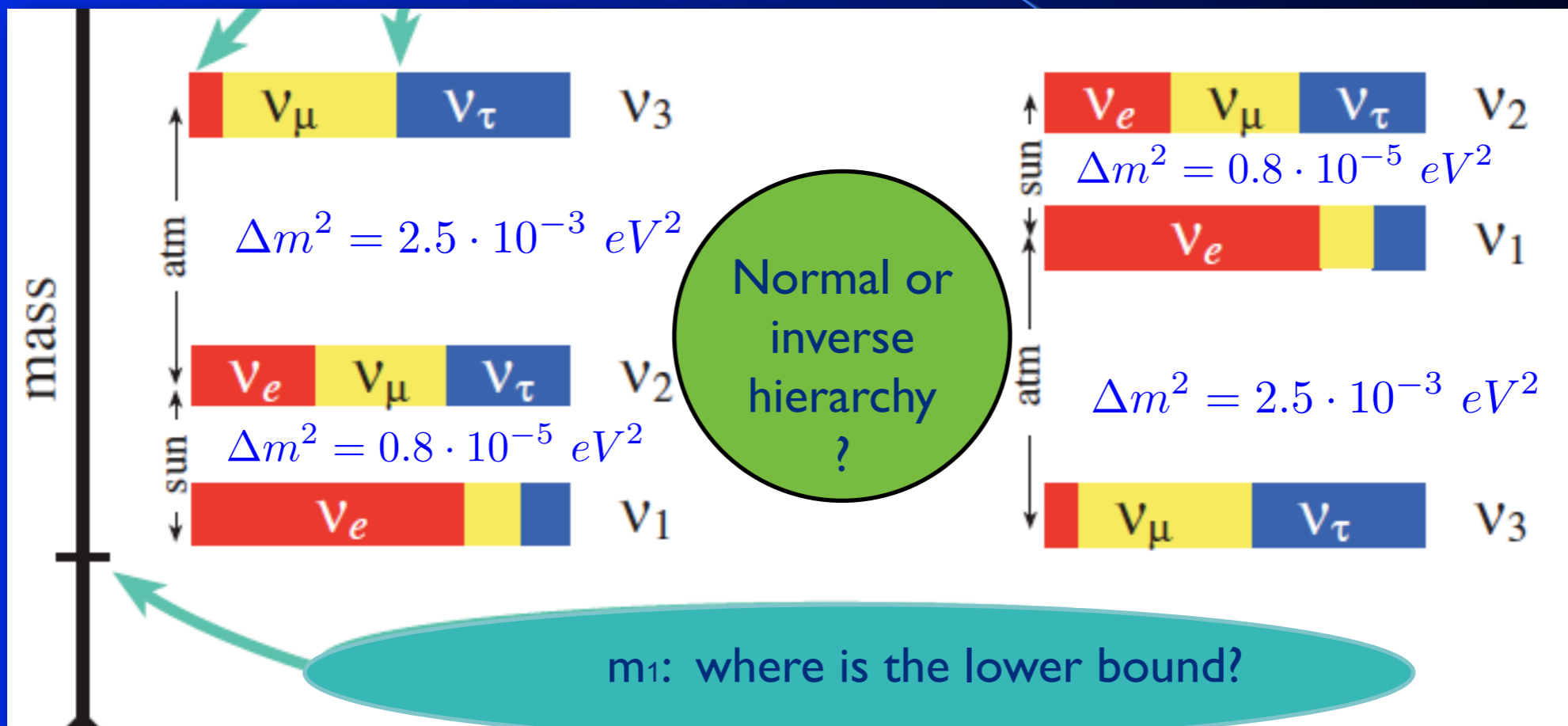
$$P_{\nu_{\alpha} \rightarrow \nu_{\beta}} = \sin^2 2\theta_{\alpha\beta} \sin^2 \left( \frac{\Delta m_{\alpha\beta}^2 L}{4E} \right)$$





# Neutrino-mysterious particle

## Neutrino masses



Planck

$$m_{\nu_e} < 2 eV$$



$$m_{\nu_e} < 0.2 eV$$

$$0.06 eV < \sum m_\nu < 0.12 eV$$

$\beta$ -decay

KATRIN

Neutrino oscillations

Spectrum of cosmic  
59 microwave  
background

Troitsk-Mainz

# Is neutrino an antiparticle to itself ?

$$\nu_D = \begin{pmatrix} \nu_L \\ \nu_R \end{pmatrix} \quad \nu_{M_1} = \begin{pmatrix} \xi_1 \\ \xi_1^* \end{pmatrix}, \quad \nu_{M_2} = \begin{pmatrix} \xi_2 \\ \xi_2^* \end{pmatrix}$$

$$\nu_D \neq \nu_D^*$$

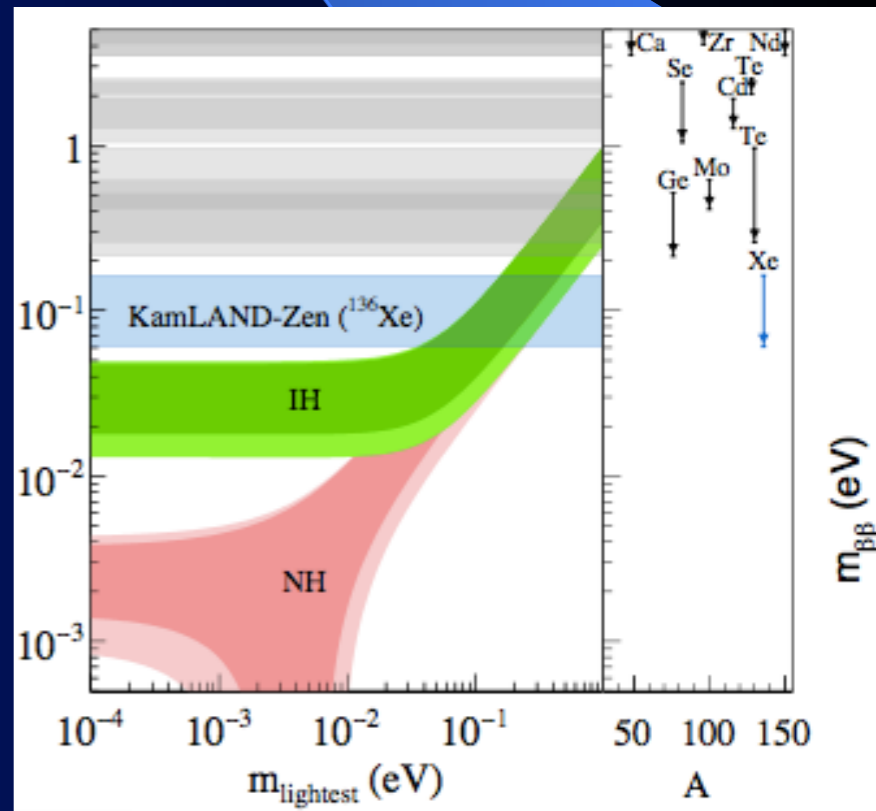
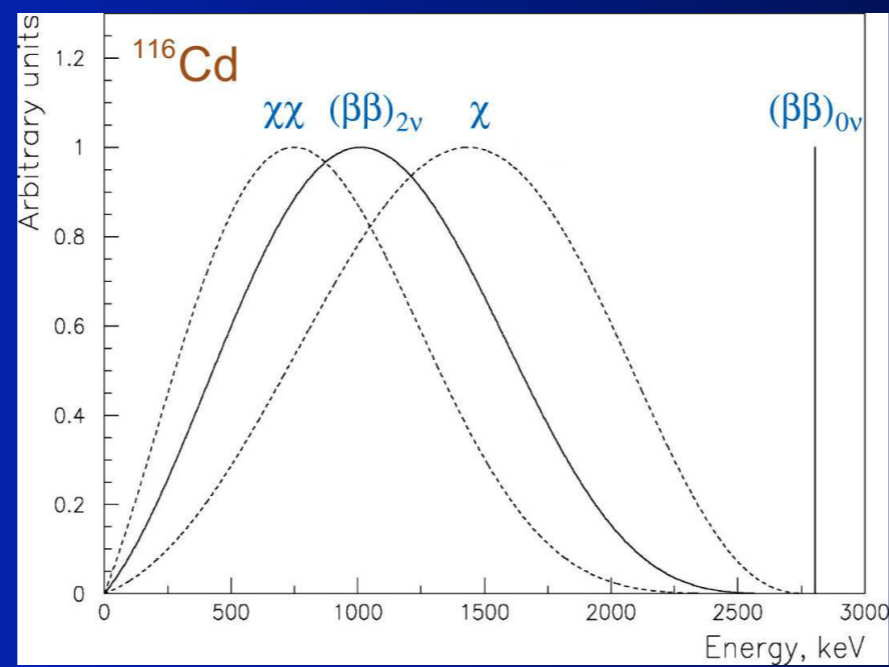
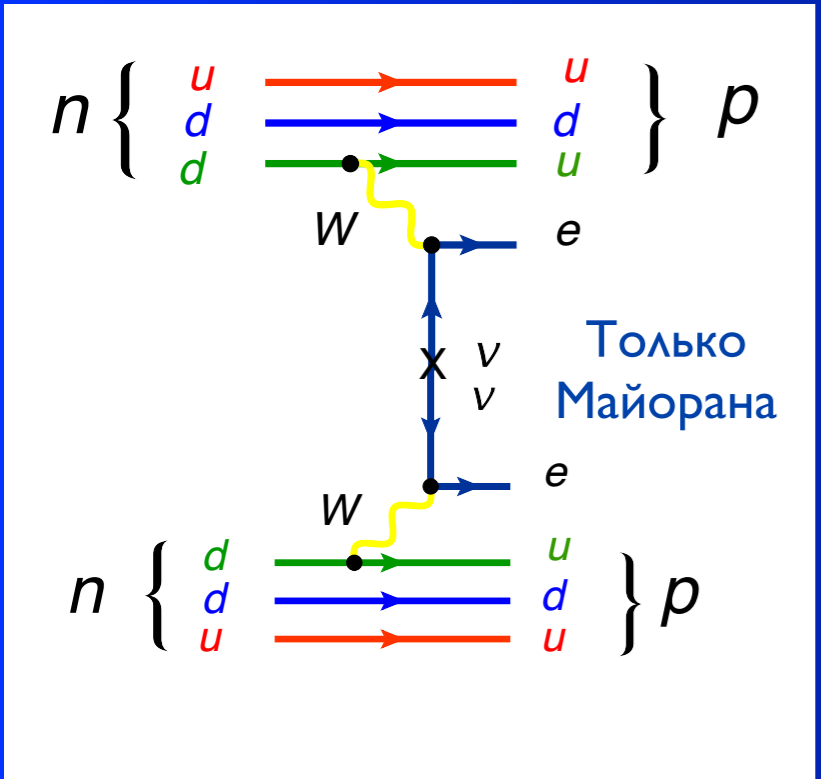
$$m_{\nu_L} = m_{\nu_R}$$



$$\nu_M = \nu_M^*$$

$$m_{\nu_{M_1}} \neq m_{\nu_{M_2}}$$

## $0\nu\beta\beta$ decay



$T_{1/2} 0\nu\beta\beta (^{136}\text{Xe}) \times 10^{25} \text{ yr} > 1.6 \text{ (90\% CL)}$

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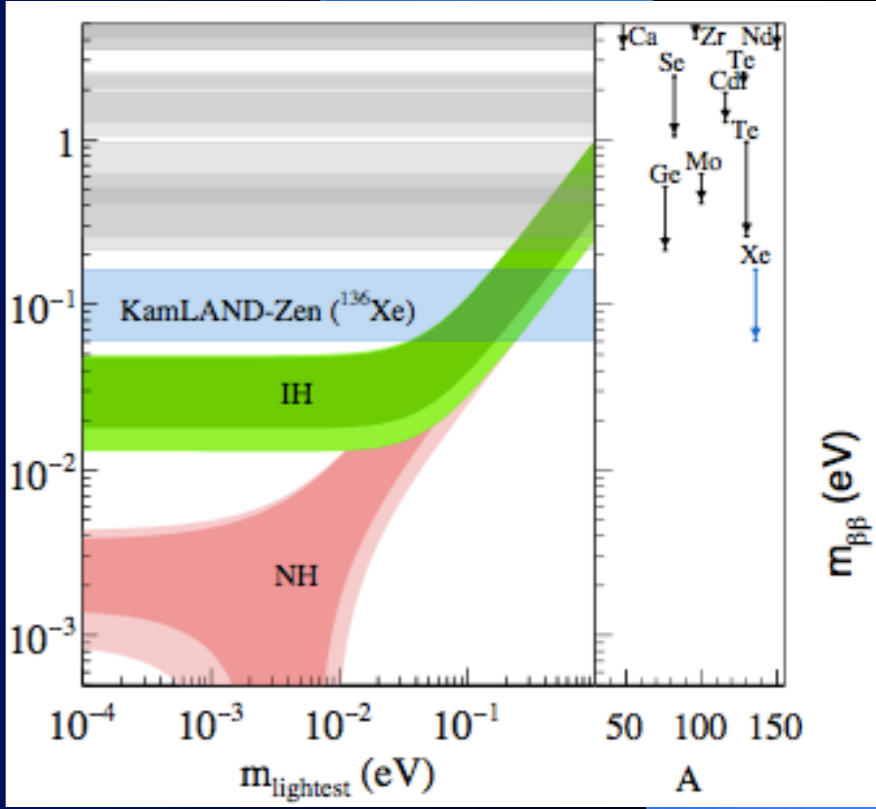
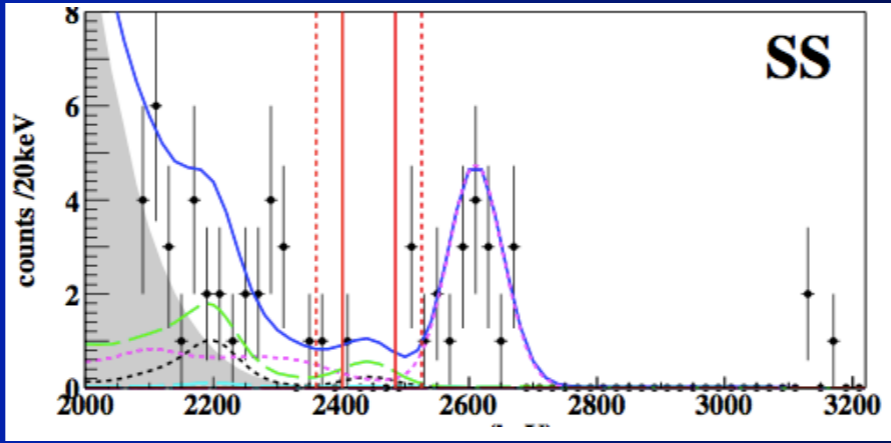
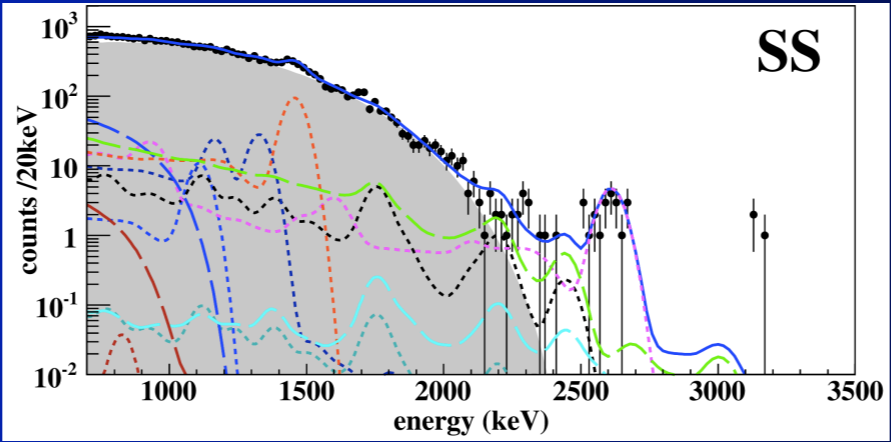
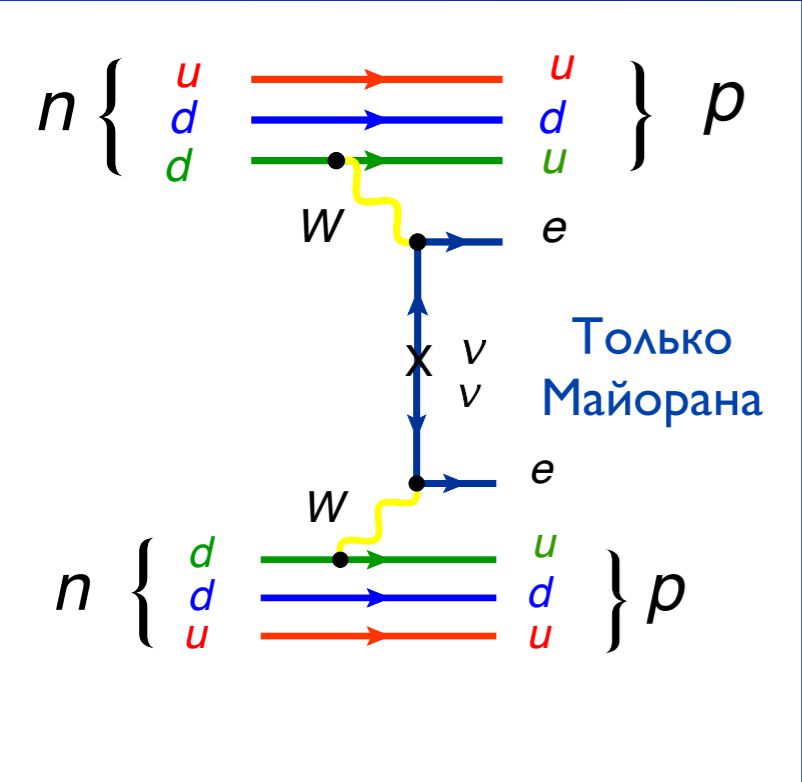
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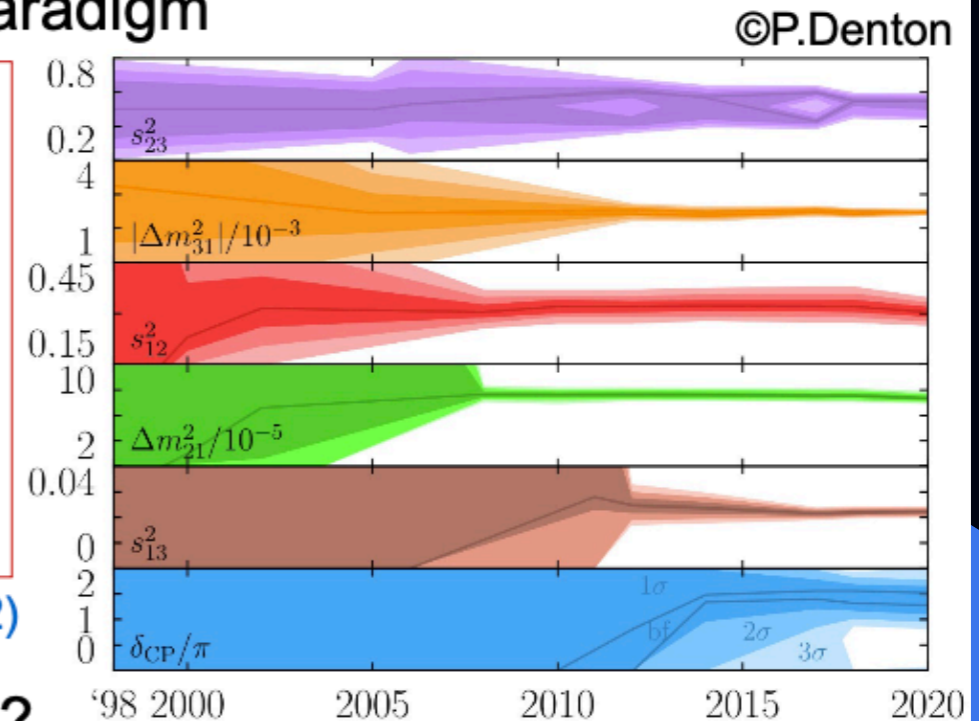
# Precision Neutrino Physics

## Current knowledge and open questions

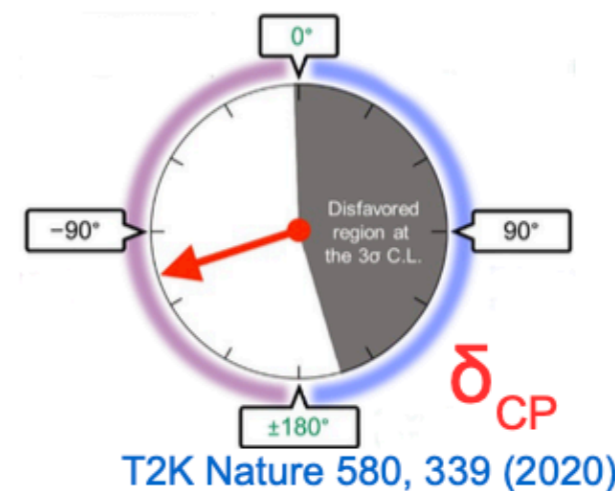
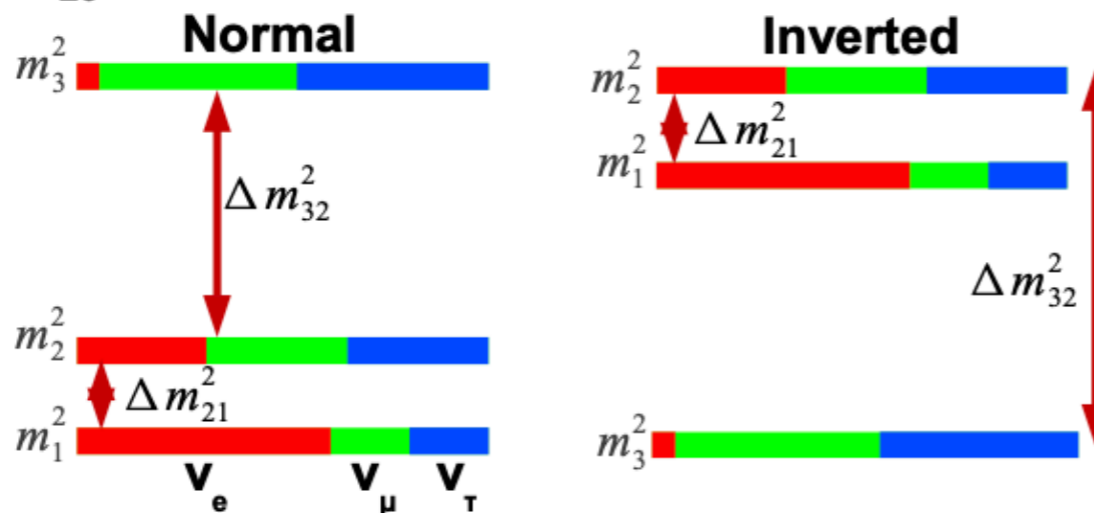
- precise measurements test the 3-flavor paradigm

$$\begin{aligned} \sin^2(\theta_{12}) &= 0.307 \pm 0.013 \\ \Delta m_{21}^2 &= (7.53 \pm 0.18) \times 10^{-5} \text{ eV}^2 \\ \sin^2(\theta_{23}) &= 0.539 \pm 0.022 \quad (S = 1.1) \quad (\text{Inverted order}) \\ \sin^2(\theta_{23}) &= 0.546 \pm 0.021 \quad (\text{Normal order}) \\ \Delta m_{32}^2 &= (-2.536 \pm 0.034) \times 10^{-3} \text{ eV}^2 \quad (\text{Inverted order}) \\ \Delta m_{32}^2 &= (2.453 \pm 0.033) \times 10^{-3} \text{ eV}^2 \quad (\text{Normal order}) \\ \sin^2(\theta_{13}) &= (2.20 \pm 0.07) \times 10^{-2} \\ \delta, \text{ CP violating phase} &= 1.36^{+0.20}_{-0.16} \pi \text{ rad} \end{aligned}$$

PTEP 2022, 083C01 (2022)



- $\theta_{23}$  octant, mass ordering, CP violation ???



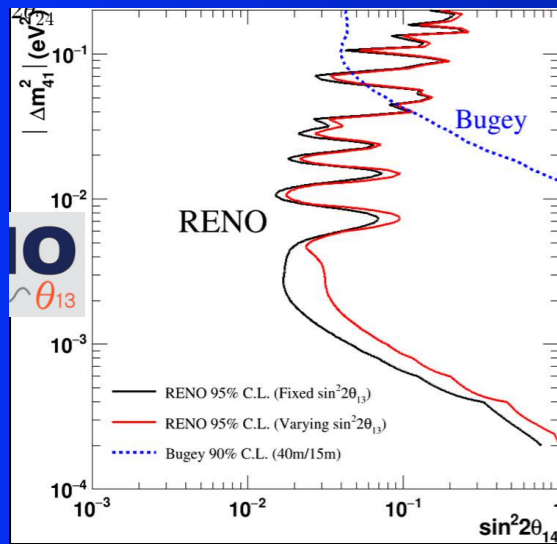
T2K Nature 580, 339 (2020)

Not covered by this talk: direct mass measurements, Dirac/Majorana nature of neutrinos, origin of masses and mixing

# STERILE NEUTRINO

No evidence for sterile neutrinos

Various exps interpreted within 4 neutrino framework



Oscillation channels are related:

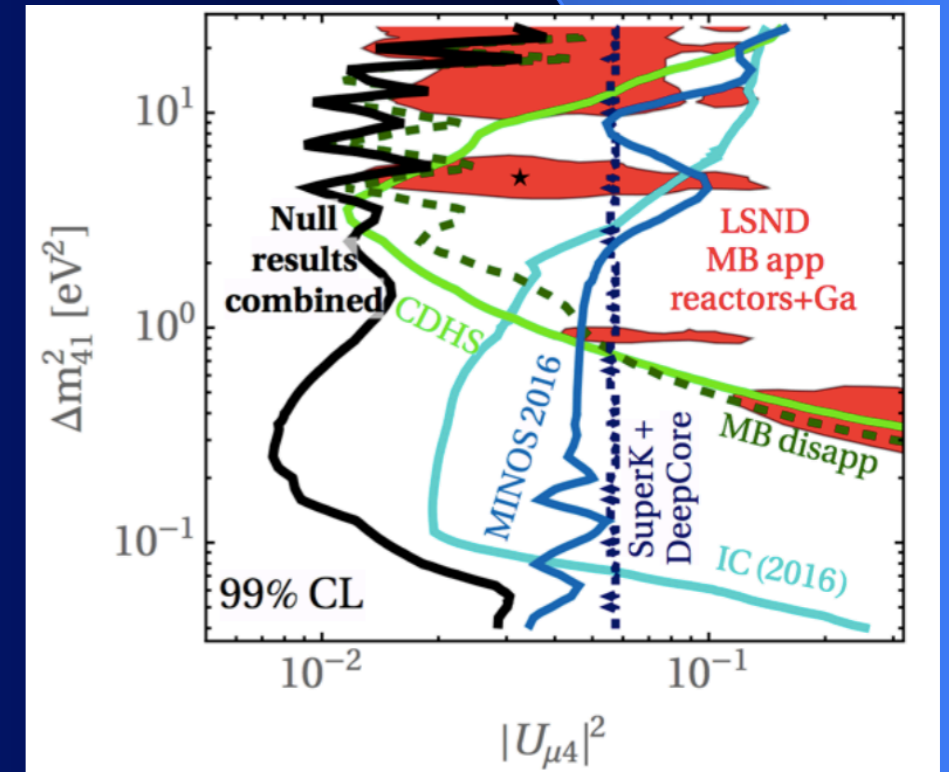
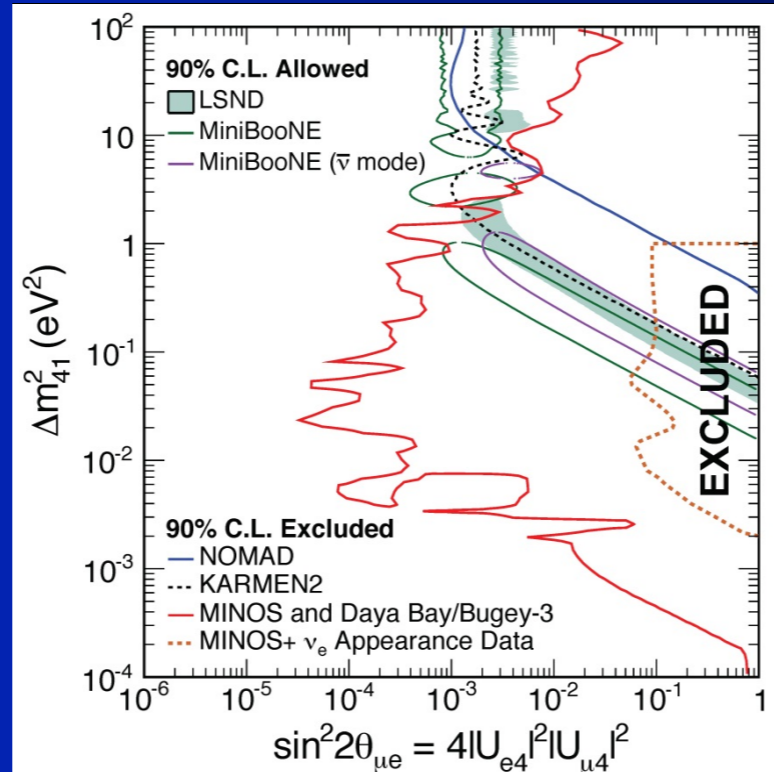
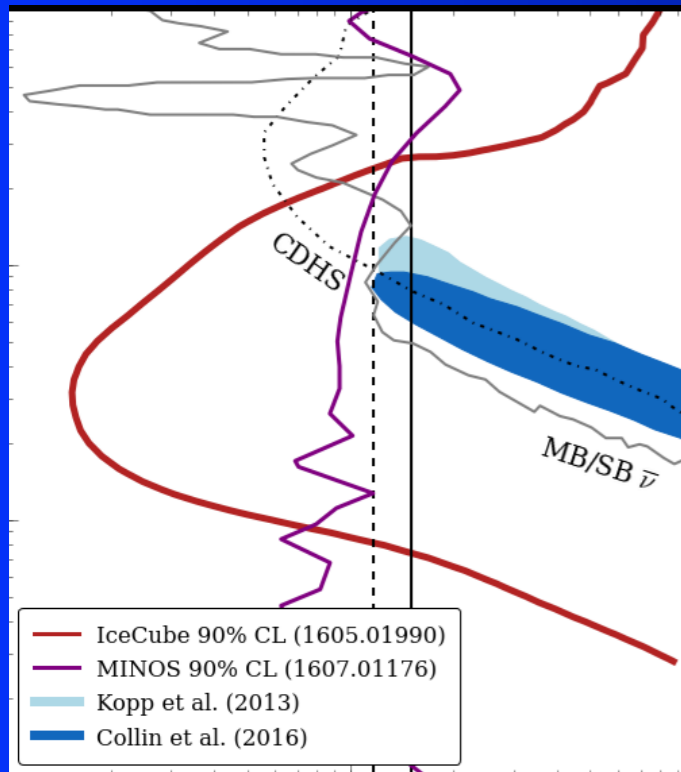
$$P_{\nu_e \rightarrow \nu_e} \approx 1 - 2|U_{e4}|^2(1 - |U_{e4}|^2)$$

$$P_{\nu_\mu \rightarrow \nu_\mu} \approx 1 - 2|U_{\mu4}|^2(1 - |U_{\mu4}|^2)$$

$$P_{\nu_\mu \rightarrow \nu_e} \approx 2|U_{e4}|^2|U_{\mu4}|^2$$

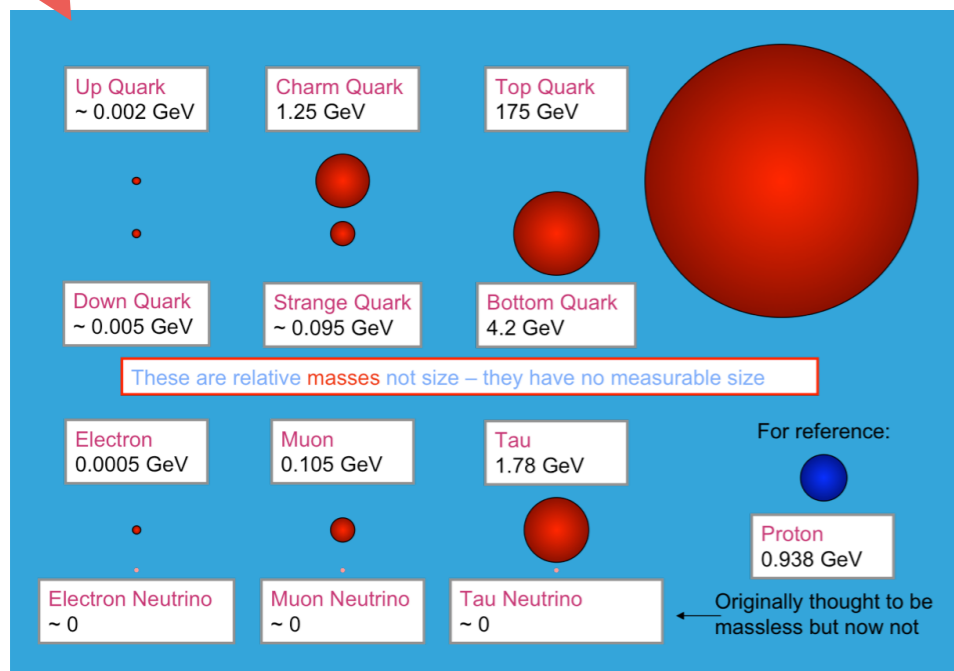
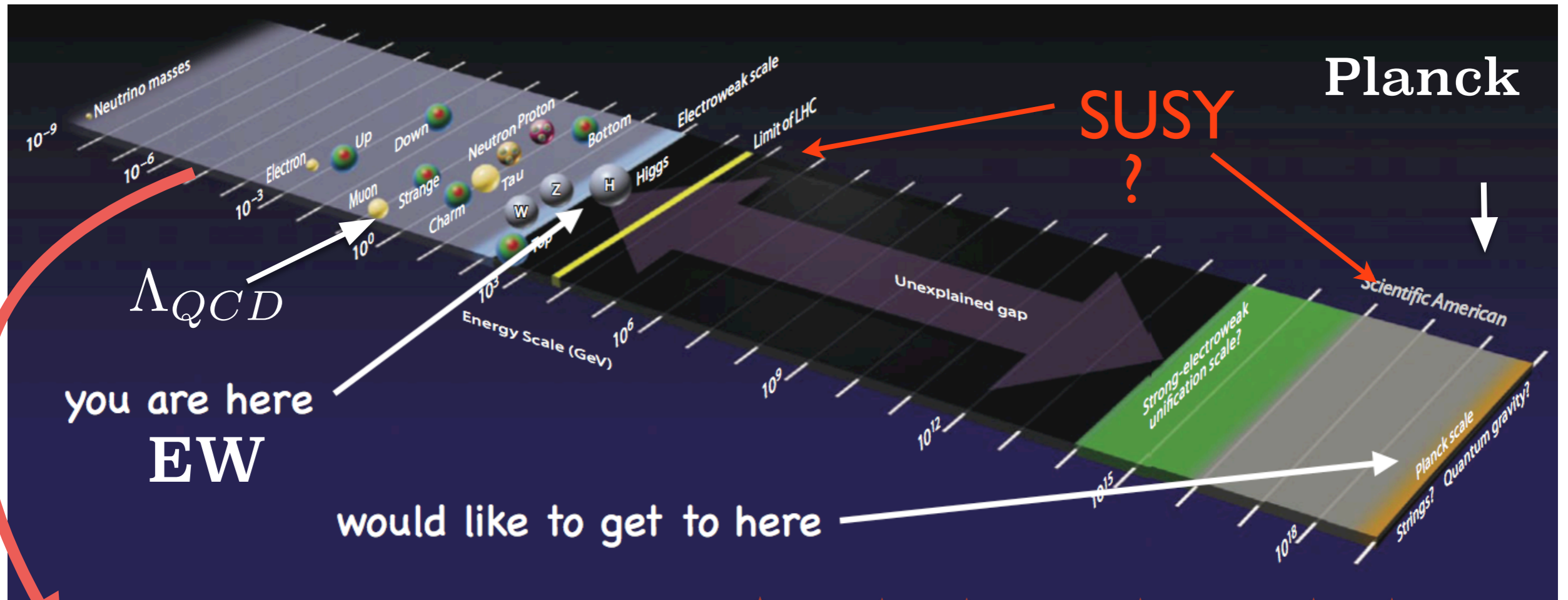
for

$$4\pi E / \Delta m_{41}^2 \ll L \ll 4\pi E / \Delta m_{31}^2$$



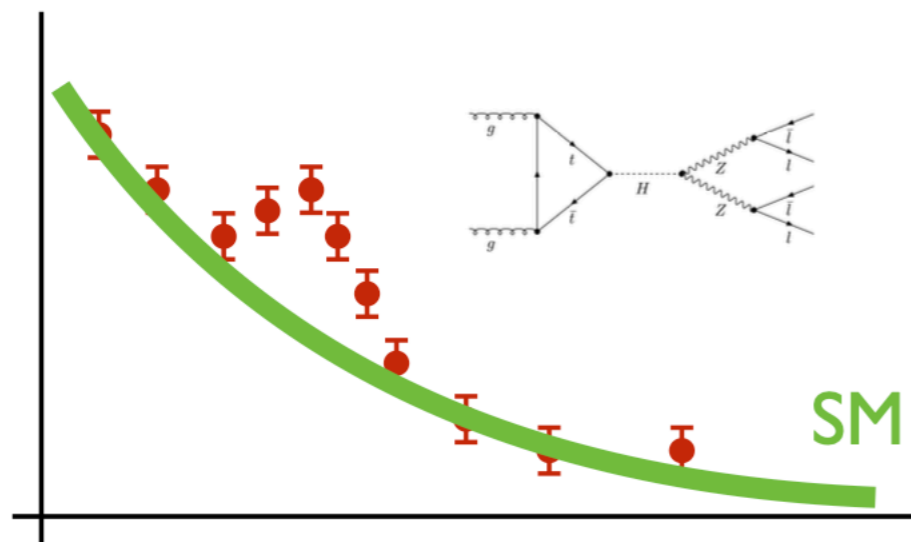
# Beyond the Standard Model

# IS THERE ANOTHER SCALE EXCEPT FOR EW AND PLANK?



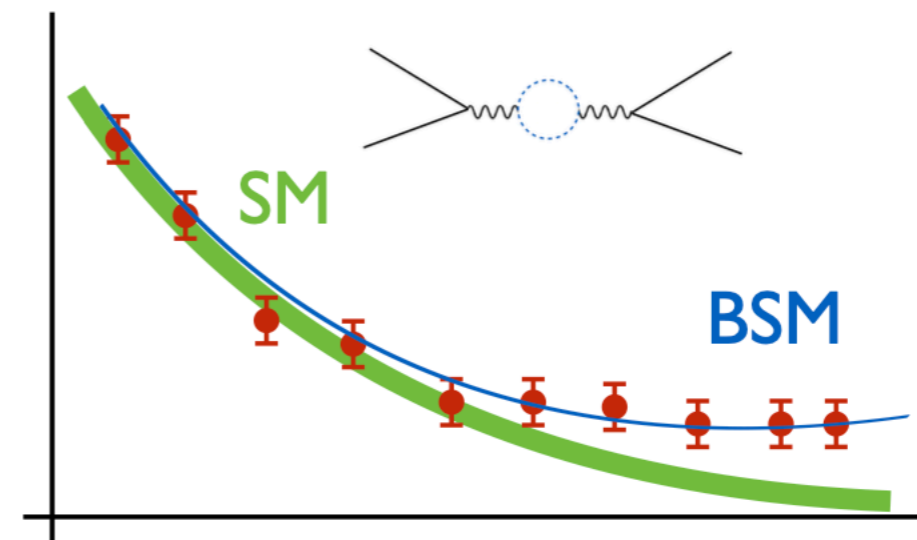
# Search for New Physics

- ▶ Still plenty of room for new discoveries : two main scenarios



- ▶ Search for (and find) new states
- ▶ Resonance needs “descriptive” TH

Most likely look for “new interactions”  
Small deviations from SM : PRECISION  
EFT description / BSM model





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- 📌 New paradigm beyond local QFT: string theory, brane world, etc
  - > main task is unification with gravity and construction of quantum gravity

## NEW SYMMETRIES

## SUPERSYMMETRY

Supersymmetry is an extension of the Poincare symmetry of the SM

## Poincare Algebra

$$\begin{aligned}
 [P_\mu, P_\nu] &= 0, \\
 [P_\mu, M_{\rho\sigma}] &= i(g_{\mu\rho}P_\sigma - g_{\mu\sigma}P_\rho), \\
 [M_{\mu\nu}, M_{\rho\sigma}] &= i(g_{\nu\rho}M_{\mu\sigma} - g_{\nu\sigma}M_{\mu\rho} - g_{\mu\rho}M_{\nu\sigma} + g_{\mu\sigma}M_{\nu\rho})
 \end{aligned}$$

## Super Poincare Algebra

 $Q_i, \bar{Q}_i$ 

$$\begin{aligned}
 [Q_\alpha^i, P_\mu] &= [\bar{Q}_{\dot{\alpha}}^i, P_\mu] = 0, \\
 [Q_\alpha^i, M_{\mu\nu}] &= \frac{1}{2}(\sigma_{\mu\nu})_\alpha^\beta Q_\beta^i, & [\bar{Q}_{\dot{\alpha}}^i, M_{\mu\nu}] &= -\frac{1}{2}\bar{Q}_{\dot{\beta}}^i(\bar{\sigma}_{\mu\nu})^{\dot{\beta}}_{\dot{\alpha}}, \\
 \{Q_\alpha^i, \bar{Q}_{\dot{\beta}}^j\} &= 2\delta^{ij}(\sigma^\mu)_{\alpha\dot{\beta}}P_\mu, \\
 \{Q_\alpha^i, Q_\beta^j\} &= 2\epsilon_{\alpha\beta}Z^{ij}, & Z^{ij} &= Z_{ij}^+, \\
 \{\bar{Q}_{\dot{\alpha}}^i, \bar{Q}_{\dot{\beta}}^j\} &= -2\epsilon_{\dot{\alpha}\dot{\beta}}Z^{ij}, & [Z_{ij}, \text{anything}] &= 0, \\
 \alpha, \dot{\alpha} &= 1, 2 & i, j &= 1, 2, \dots, N.
 \end{aligned}$$

## NEW SYMMETRIES

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 \end{aligned}$$

# SUSY MULTIPLETS

**Chiral multiplet**  $N = 1, \lambda = 0$

helicity	-1/2	0	1/2
# of states	1	2	1

scalar    spinor  
↓        ↙  
 $(\varphi, \psi)$

**Vector multiplet**  $N = 1, \lambda = 1/2$

helicity	-1	-1/2	1/2	1
# of states	1	1	1	1

$(\lambda, A_\mu)$   
↑        ↙  
spinor    vector



# SUSY MULTIPLETS

**Chiral multiplet**  $N = 1, \lambda = 0$

helicity	-1/2	0	1/2
# of states	1	2	1

scalar    spinor  
↓        ↓  
( $\varphi, \psi$ )

**Vector multiplet**  $N = 1, \lambda = 1/2$

helicity	-1	-1/2	1/2	1
# of states	1	1	1	1

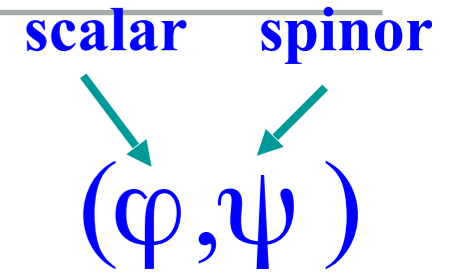
( $\lambda, A_\mu$ )  
↑        ↓  
spinor    vector

**Members of a supermultiplet are called superpartners**

# SUSY MULTIPLETS

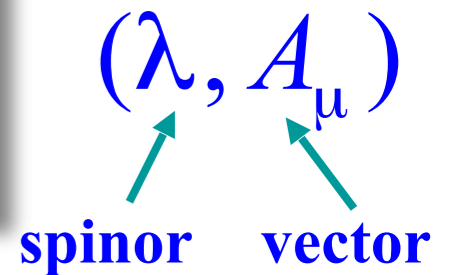
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Members of a supermultiplet are called **superpartners**

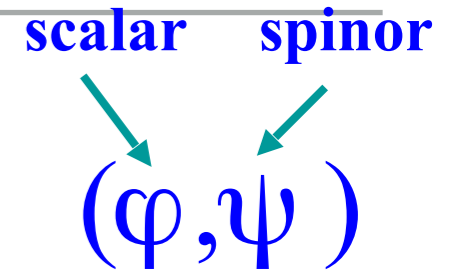
## Extended supersymmetry

N=4	SUSY YM	helicity	-1	-1/2	0	1/2	1				
	$\lambda = -1$	# of states	1	4	6	4	1				
N=8	SUGRA	helicity	-2	-3/2	-1	-1/2	0	1/2	1	3/2	2
	$\lambda = -2$	# of states	1	8	28	56	70	56	28	8	1

# SUSY MULTIPLETS

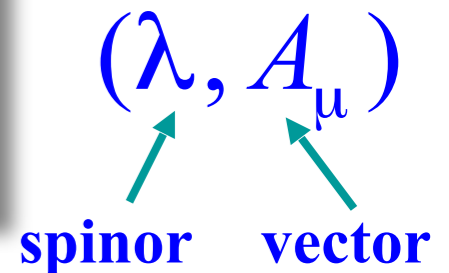
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$N \leq 4S$

← spin

$N \leq 4$

For renormalizable theories (YM)

$N \leq 8$

For (super)gravity

Bosons and Fermions come in pairs

$(\varphi, \psi)$

$(\tilde{\lambda}, A_\mu)$

$(\tilde{g}, g)$

Spin 0

Spin 1/2

Spin 1/2

Spin 1

Spin 3/2

Spin 2

scalar

chiral  
fermion

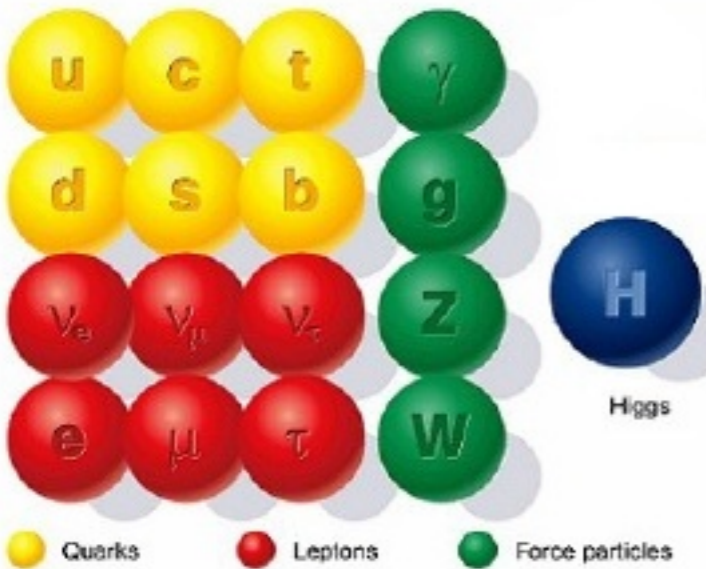
majorana  
fermion

vector

gravitino

graviton

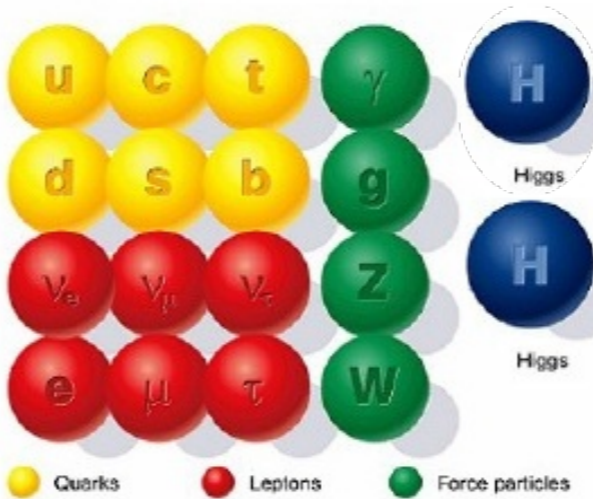
Supersymmetry is a dream of a unified theory of all particles and interactions



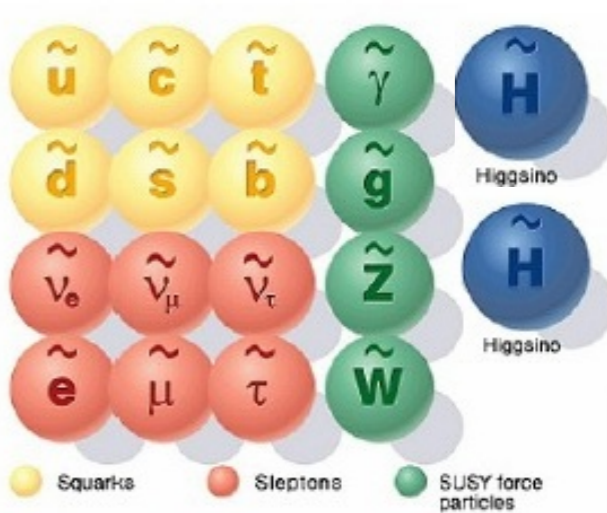
Standard particles



## SUPERSYMMETRY

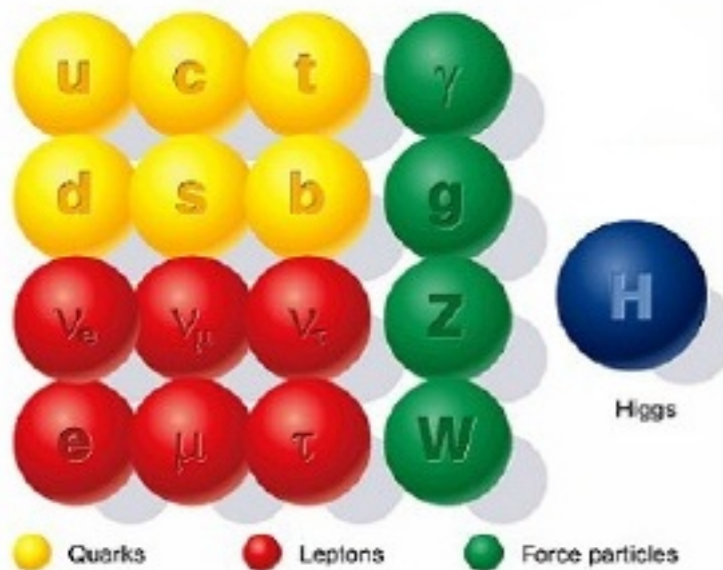


Standard particles



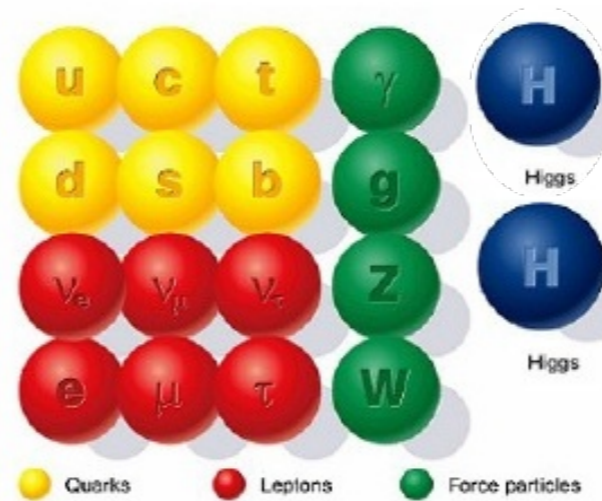
SUSY particles

Supersymmetry is a dream of a unified theory of all particles and interactions

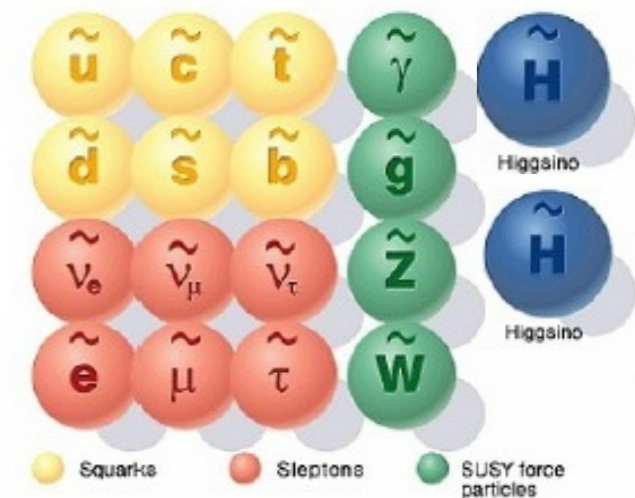


**Standard particles**

## SUPERSYMMETRY



**Standard particles**

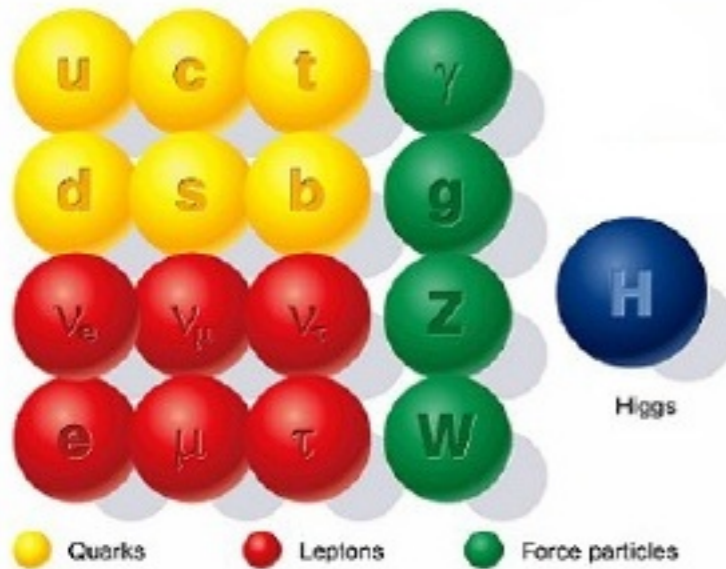


**SUSY particles**

## Why SUSY?

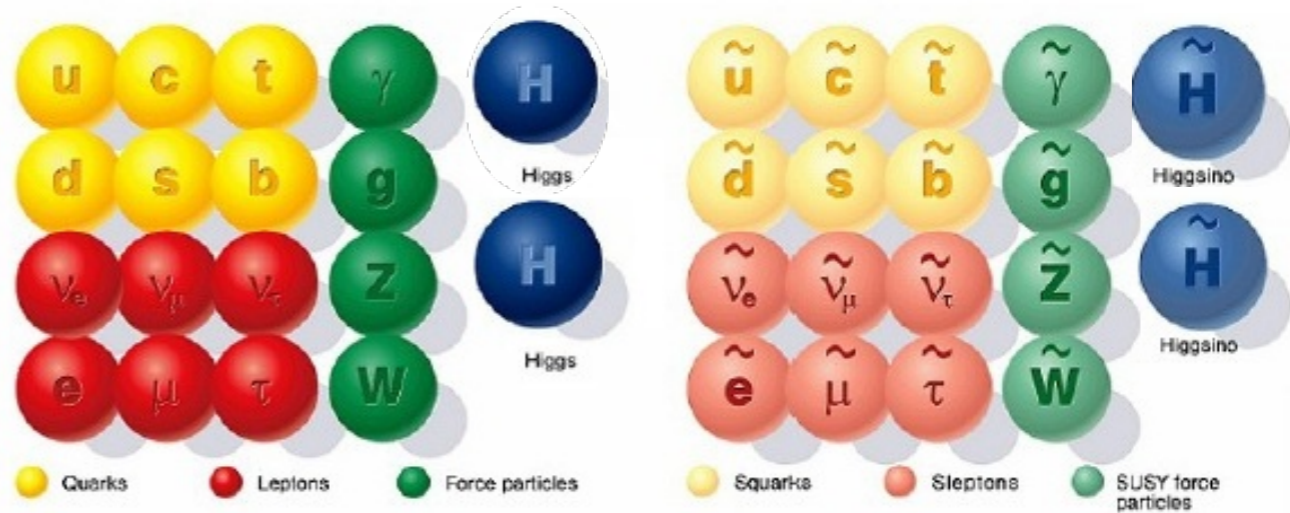
- Unification with gravity!
- Unification of the gauge couplings
- Solution of the hierarchy problem
- Explanation of the EW symmetry violation
- Provided the DM particle

Supersymmetry is a dream of a unified theory of all particles and interactions



Standard particles

## SUPERSYMMETRY



Standard particles

SUSY particles

## Why SUSY?

- Unification with gravity!
- Unification of the gauge couplings
- Solution of the hierarchy problem
- Explanation of the EW symmetry violation
- Provided the DM particle

Unification with gravity!

$$\{Q_\alpha^i, \bar{Q}_\beta^j\} = 2\delta^{ij}(\sigma^\mu)_{\alpha\beta} P_\mu \Rightarrow \{\delta_\varepsilon, \bar{\delta}_{\bar{\varepsilon}}\} = 2(\varepsilon\sigma^\mu\bar{\varepsilon})P_\mu$$

$\varepsilon = \varepsilon(x)$  local coordinate transf.  $\Rightarrow$  (super)gravity

**Local supersymmetry = general relativity !**

Supersymmetry is a dream of a unified theory of all particles and interactions

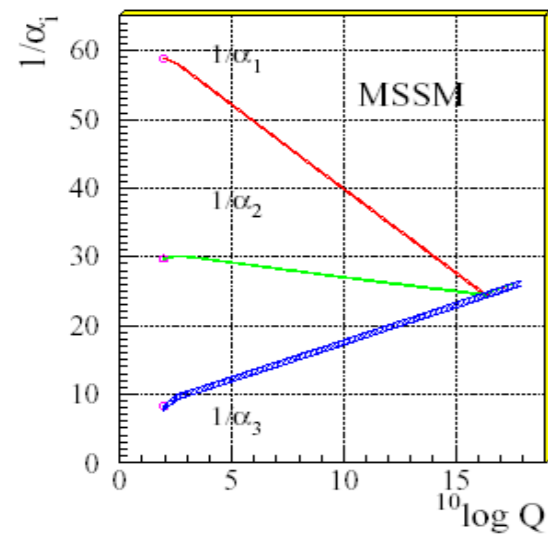
## Why SUSY?



Supersymmetry is a dream of a unified theory of all particles and interactions

## Why SUSY?

Unification of the gauge couplings

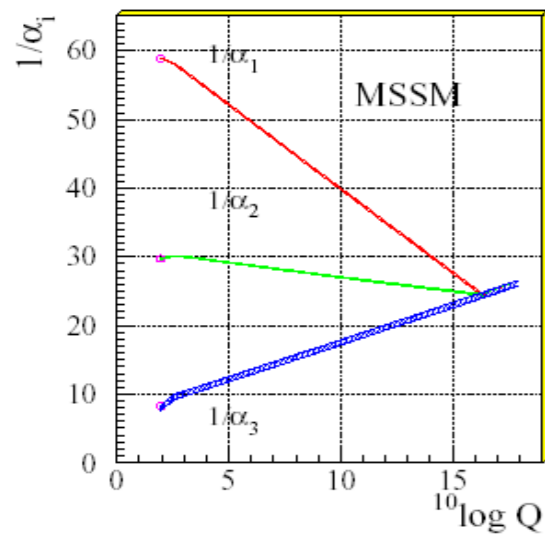


The basis of a grand  
Unified Theory

Supersymmetry is a dream of a unified theory of all particles and interactions

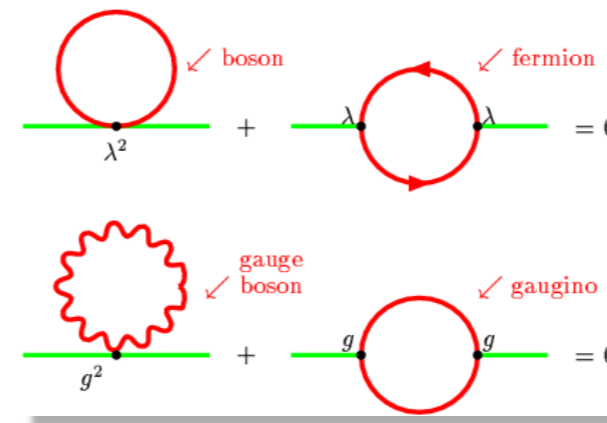
## Why SUSY?

Unification of the gauge couplings



The basis of a grand Unified Theory

Solution of the hierarchy problem

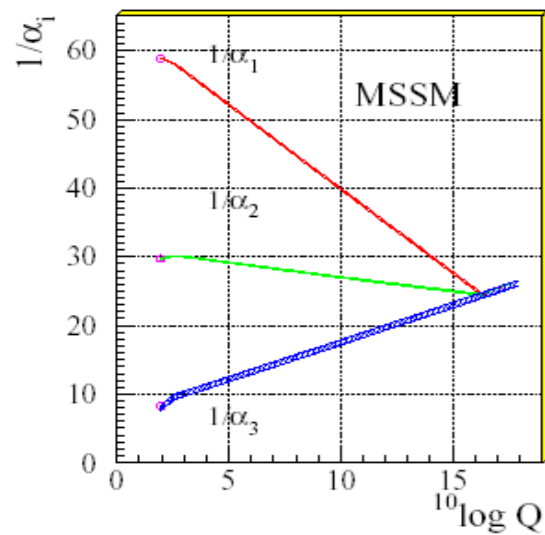


Cancellations of corrections and stabilization of the Higgs potential

Supersymmetry is a dream of a unified theory of all particles and interactions

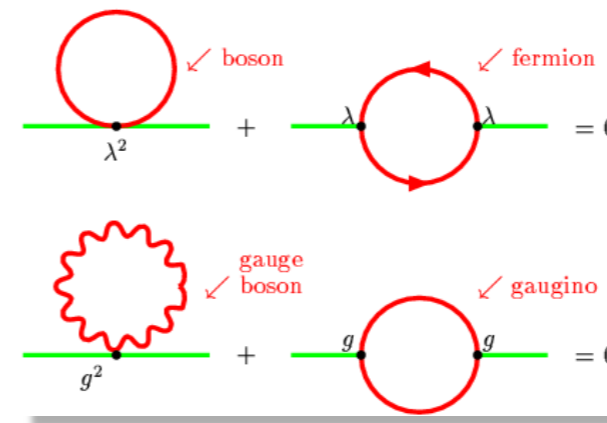
## Why SUSY?

### Unification of the gauge couplings



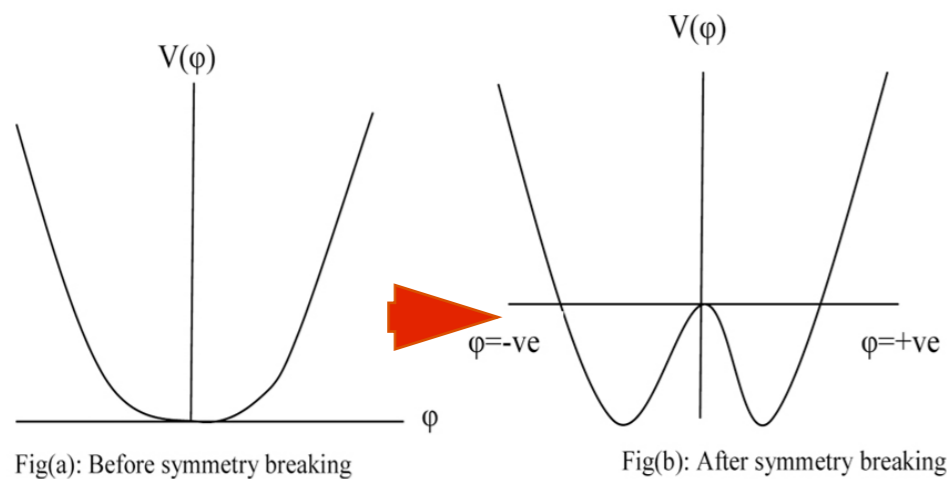
The basis of a grand Unified Theory

### Solution of the hierarchy problem



Cancellations of corrections and stabilization of the Higgs potential

### Explanation of the EW symmetry violation

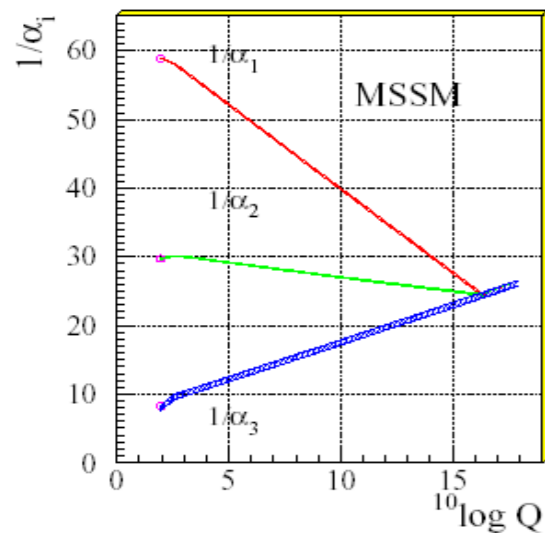


Violation of symmetry comes from radiative corrections

Supersymmetry is a dream of a unified theory of all particles and interactions

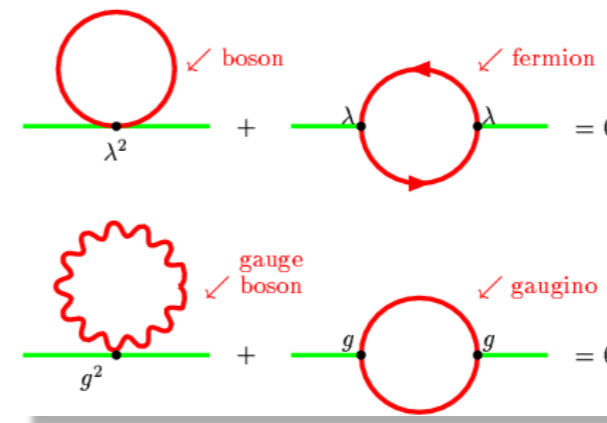
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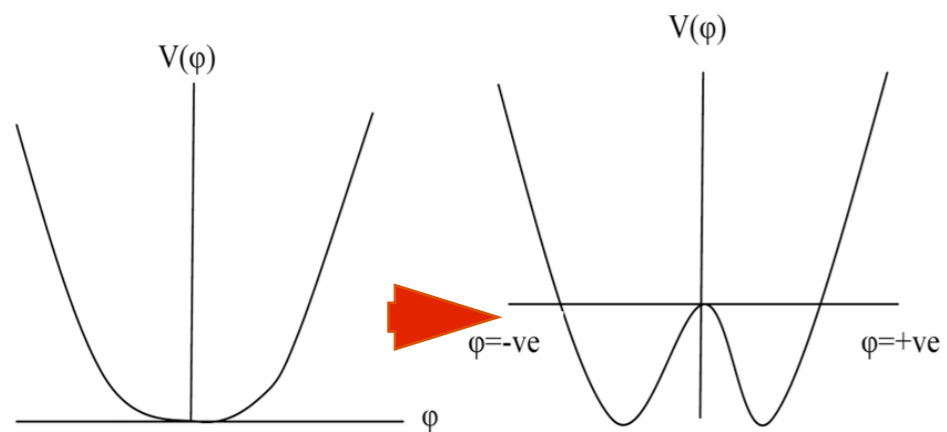
The basis of a grand Unified Theory

### Solution of the hierarchy problem



Cancellations of corrections and stabilization of the Higgs potential

### Explanation of the EW symmetry violation



Fig(a): Before symmetry breaking

Fig(b): After symmetry breaking

### Provided the DM particle

$$\tilde{\chi}^0 = N_1 \tilde{\gamma} + N_2 \tilde{z} + N_3 \tilde{H}_1^0 + N_4 \tilde{H}_2^0$$

Neutralino=DM

Violation of symmetry comes from radiative corrections

Superfield	Bosons		Fermions		$SU_c(3)$	$SU_L(2)$	$U_Y(1)$
<b>Gauge</b>							
$\mathbf{G}^a$	gluon	$g^a$	gluino	$\tilde{g}^a$	8	0	0
$\mathbf{V}^k$	Weak	$W^k (W^\pm, Z)$	wino, zino	$\tilde{w}^k (\tilde{w}^\pm, \tilde{z})$	1	3	0
$\mathbf{V}'$	Hypercharge	$B (\gamma)$	bino	$\tilde{b}(\tilde{\gamma})$	1	1	0
<b>Matter</b>							
$\mathbf{L}_i$	sleptons	$\left\{ \begin{array}{l} \tilde{L}_i = (\tilde{\nu}, \tilde{e})_L \\ \tilde{E}_i = \tilde{e}_R \\ \tilde{N}_i = \tilde{\nu}_R \end{array} \right.$	leptons	$\left\{ \begin{array}{l} L_i = (\nu, e)_L \\ E_i = e_R \\ N_i = \nu_R \end{array} \right.$	1	2	-1
$\mathbf{E}_i$					1	1	2
$\mathbf{N}_i$					1	1	0
$\mathbf{Q}_i$	squarks	$\left\{ \begin{array}{l} \tilde{Q}_i = (\tilde{u}, \tilde{d})_L \\ \tilde{U}_i = \tilde{u}_R \\ \tilde{D}_i = \tilde{d}_R \end{array} \right.$	quarks	$\left\{ \begin{array}{l} Q_i = (u, d)_L \\ U_i = u_R^c \\ D_i = d_R^c \end{array} \right.$	3	2	1/3
$\mathbf{U}_i$					$3^*$	1	-4/3
$\mathbf{D}_i$					$3^*$	1	2/3
<b>Higgs</b>							
$\mathbf{H}_1$	Higgses	$\left\{ \begin{array}{l} H_1 \\ H_2 \end{array} \right.$	higgsinos	$\left\{ \begin{array}{l} \tilde{H}_1 \\ \tilde{H}_2 \end{array} \right.$	1	2	-1
$\mathbf{H}_2$					1	2	1

Superfield	Bosons		Fermions	$SU_c(3)$	$SU_L(2)$	$U_Y(1)$	
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$\mathbf{G}^a$	gluon	$g^a$		8	0	0	
$\mathbf{V}^k$	Weak	$W^k$ ( $W^\pm, Z$ )	<i>wino, zino</i> $\tilde{w}^k$ ( $\tilde{w}^\pm, \tilde{z}$ )	1	3	0	
$\mathbf{V}'$	Hypercharge	$B$ ( $\gamma$ )	<i>binos</i> $\tilde{b}(\tilde{\gamma})$	1	1	0	
Matter							
$\mathbf{L}_i$	sleptons	$\left\{ \begin{array}{l} \tilde{L}_i = (\tilde{\nu}, \tilde{e})_L \\ \tilde{E}_i = \tilde{e}_R \\ \tilde{N}_i = \tilde{\nu}_R \end{array} \right.$	leptons	$\left\{ \begin{array}{l} L_i = (\nu, e)_L \\ E_i = e_R \\ N_i = \nu_R \end{array} \right.$	1	2	-1
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$\mathbf{V}'$	Hypercharge	$B (\gamma)$	<i>binos</i> $\tilde{b}(\tilde{\gamma})$	1	1	0	
Matter							
$\mathbf{L}_i$	sleptons	$\tilde{L}_i = (\tilde{\nu}, \tilde{e})_L$ $\tilde{E}_i = \tilde{e}_R$ $\tilde{N}_i = \tilde{\nu}_R$	leptons	$L_i = (\nu, e)_L$ $E_i = e_R$ $N_i = \nu_R$	1	2	-1
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Higgs							
$\mathbf{H}_1$	Higgses	$H_1$ $H_2$	higgsinos	$\tilde{H}_1$ $\tilde{H}_2$	1	2	-1
$\mathbf{H}_2$					1	2	1



# THE PARTICLE CONTENT OF THE MSSM

Superfield	Bosons		Fermions		$SU_c(3)$	$SU_L(2)$	$U_Y(1)$		
Gauge			<i>gluino</i> $\tilde{g}^a$						
$\mathbf{G}^a$	gluon	$g^a$			8	0	0		
$\mathbf{V}^k$	Weak	$W^k (W^\pm, Z)$	<i>wino, zino</i> $\tilde{w}^k (\tilde{w}^\pm, \tilde{z})$		1	3	0		
$\mathbf{V}'$	Hypercharge	$B (\gamma)$	<i>binos</i> $\tilde{b}(\tilde{\gamma})$		1	1	0		
Matter									
$\mathbf{L}_i$	sleptons	$\tilde{L}_i = (\tilde{\nu}, \tilde{e})_L$	leptons	$L_i = (\nu, e)_L$	1	2	-1		
$\mathbf{E}_i$					$\tilde{E}_i = \tilde{e}_R$	$E_i = e_R$	1	1	2
$\mathbf{N}_i$					$\tilde{N}_i = \tilde{\nu}_R$	$N_i = \nu_R$	1	1	0
$\mathbf{Q}_i$	squarks	$\tilde{Q}_i = (\tilde{u}, \tilde{d})_L$	quarks	$Q_i = (u, d)_L$	3	2	1/3		
$\mathbf{U}_i$					$\tilde{U}_i = \tilde{u}_R$	$U_i = u_R^c$	3*	1	-4/3
$\mathbf{D}_i$					$\tilde{D}_i = \tilde{d}_R$	$D_i = d_R^c$	3*	1	2/3
Higgs									
$\mathbf{H}_1$	Higgses	$H_1$	higgsinos	$\tilde{H}_1$	1	2	-1		
$\mathbf{H}_2$					$H_2$	$\tilde{H}_2$	1	2	1
$\mathbf{S}$	Singlet	$s$	singlino	$s$	1	1	0		

# THE PARTICLE CONTENT OF THE MSSM

Superfield	Bosons		Fermions		$SU_c(3)$	$SU_L(2)$	$U_Y(1)$		
Gauge			<i>gluino</i> $\tilde{g}^a$						
$G^a$	gluon	$g^a$			8	0	0		
$V^k$	Weak	$W^k (W^\pm, Z)$	<i>wino, zino</i> $\tilde{w}^k (\tilde{w}^\pm, \tilde{z})$		1	3	0		
$V'$	Hypercharge	$B (\gamma)$	<i>binos</i> $\tilde{b}(\tilde{\gamma})$		1	1	0		
Matter									
$L_i$	sleptons	$\tilde{L}_i = (\tilde{\nu}, \tilde{e})_L$	leptons	$L_i = (\nu, e)_L$	1	2	-1		
$E_i$					$\tilde{E}_i = \tilde{e}_R$	$E_i = e_R$	1	1	2
$N_i$					$\tilde{N}_i = \tilde{\nu}_R$	$N_i = \nu_R$	1	1	0
$Q_i$	squarks	$\tilde{Q}_i = (\tilde{u}, \tilde{d})_L$	quarks	$Q_i = (u, d)_L$	3	2	1/3		
$U_i$					$\tilde{U}_i = \tilde{u}_R$	$U_i = u_R^c$	3*	1	-4/3
$D_i$					$\tilde{D}_i = \tilde{d}_R$	$D_i = d_R^c$	3*	1	2/3
Higgs									
$H_1$	Higgses	$H_1$	higgsinos	$\tilde{H}_1$	1	2	-1		
$H_2$					$H_2$	$\tilde{H}_2$	1	2	1
$S$	Singlet	$s$	singlino	$s$	1	1	0		

MSSM

$$R = (-)^{3(B-L)+2S}$$

The Usual Particle :  $R = + 1$   
SUSY Particle :  $R = - 1$

B - Baryon Number  
L - Lepton Number  
S - Spin

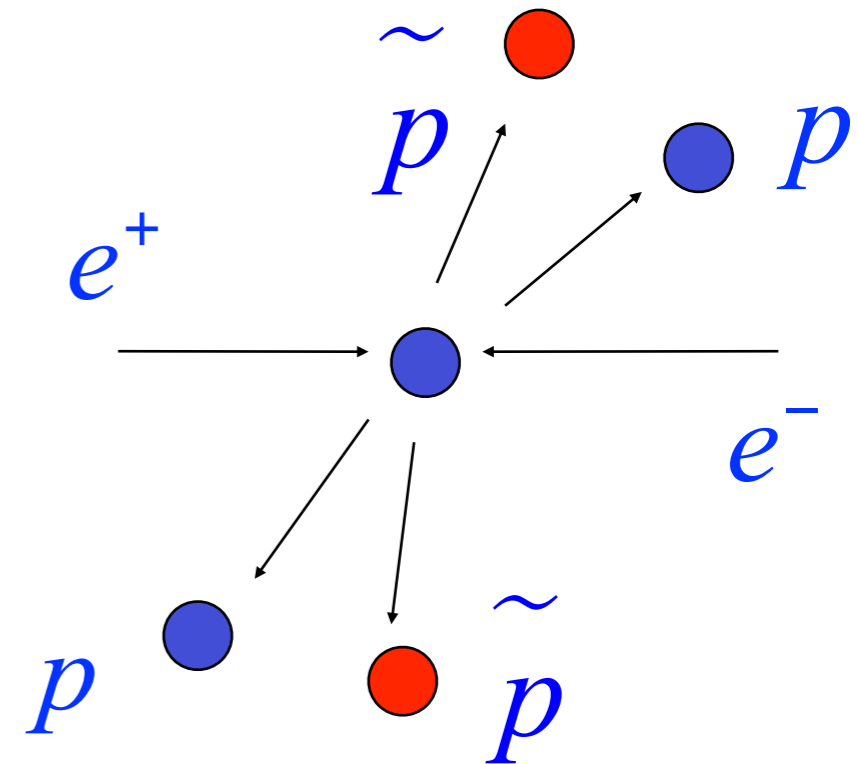
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The Usual Particle :  $R = + 1$   
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B - Baryon Number  
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The consequences:

- The superpartners are created in pairs
- The lightest superparticle is stable



$$R = (-1)^{3(B-L)+2S}$$

The Usual Particle :  $R = + 1$   
 SUSY Particle :  $R = - 1$

B - Baryon Number  
 L - Lepton Number  
 S - Spin

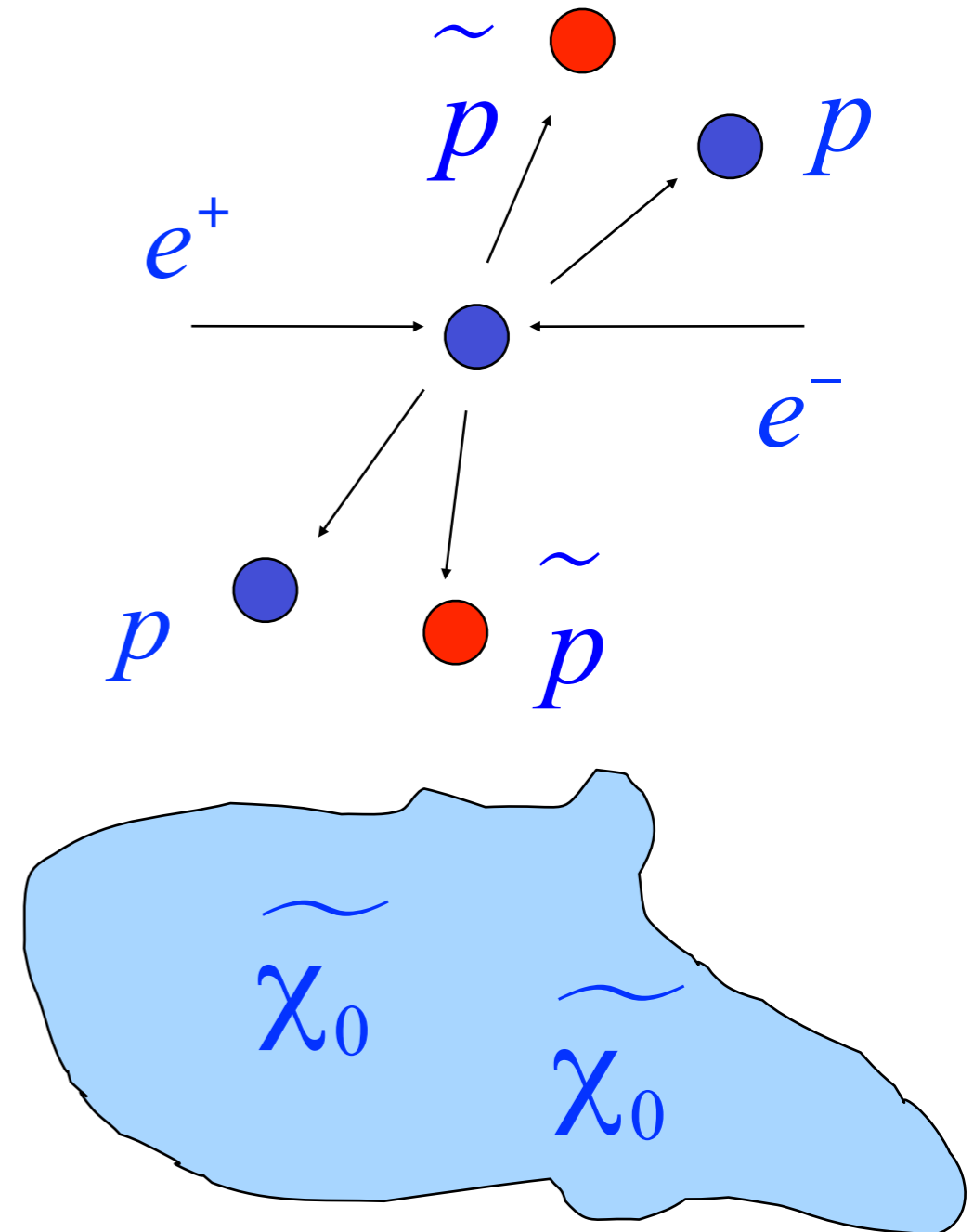
## The consequences:

- The superpartners are created in pairs
- The lightest superparticle is stable



- The lightest superparticle (LSP) should be neutral - the best candidate is neutralino (photino or higgsino)
- It can survive from the Big Bang and form the Dark matter in the Universe

$\tilde{\chi}_0$

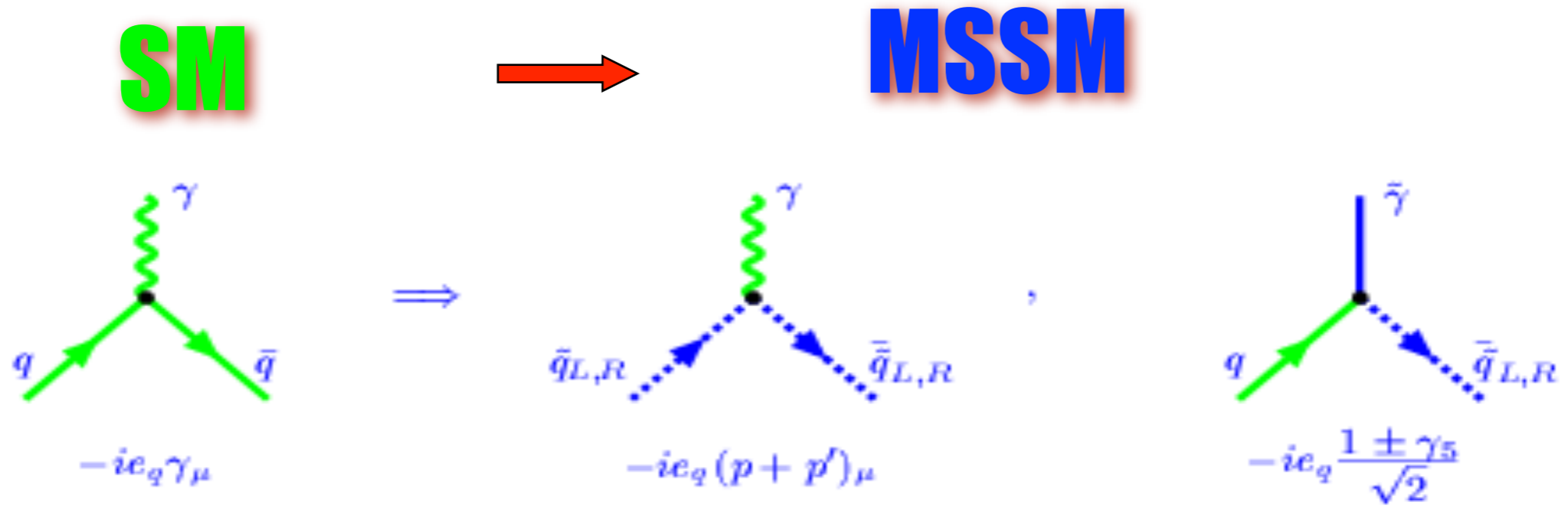


**SM**

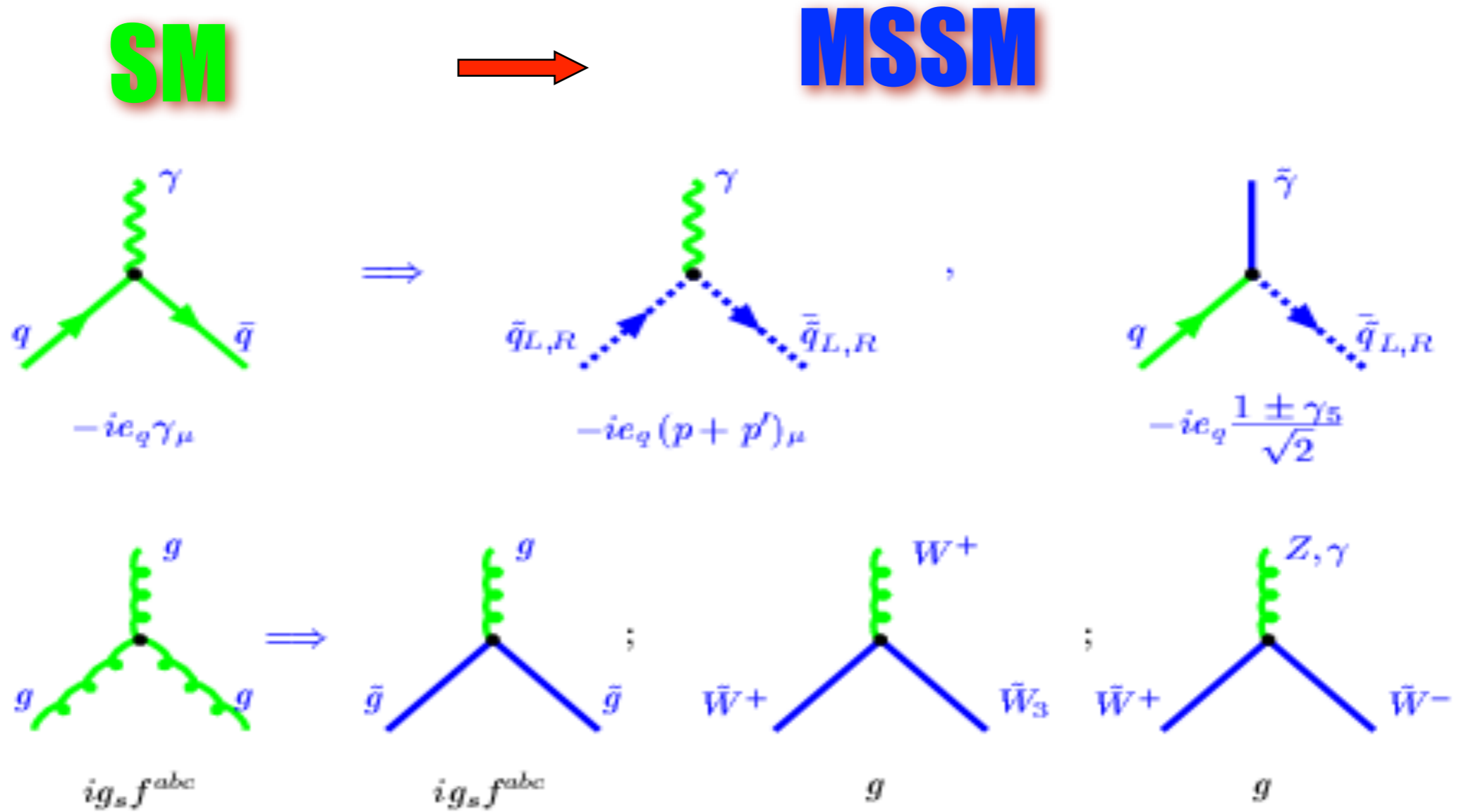


**MSSM**

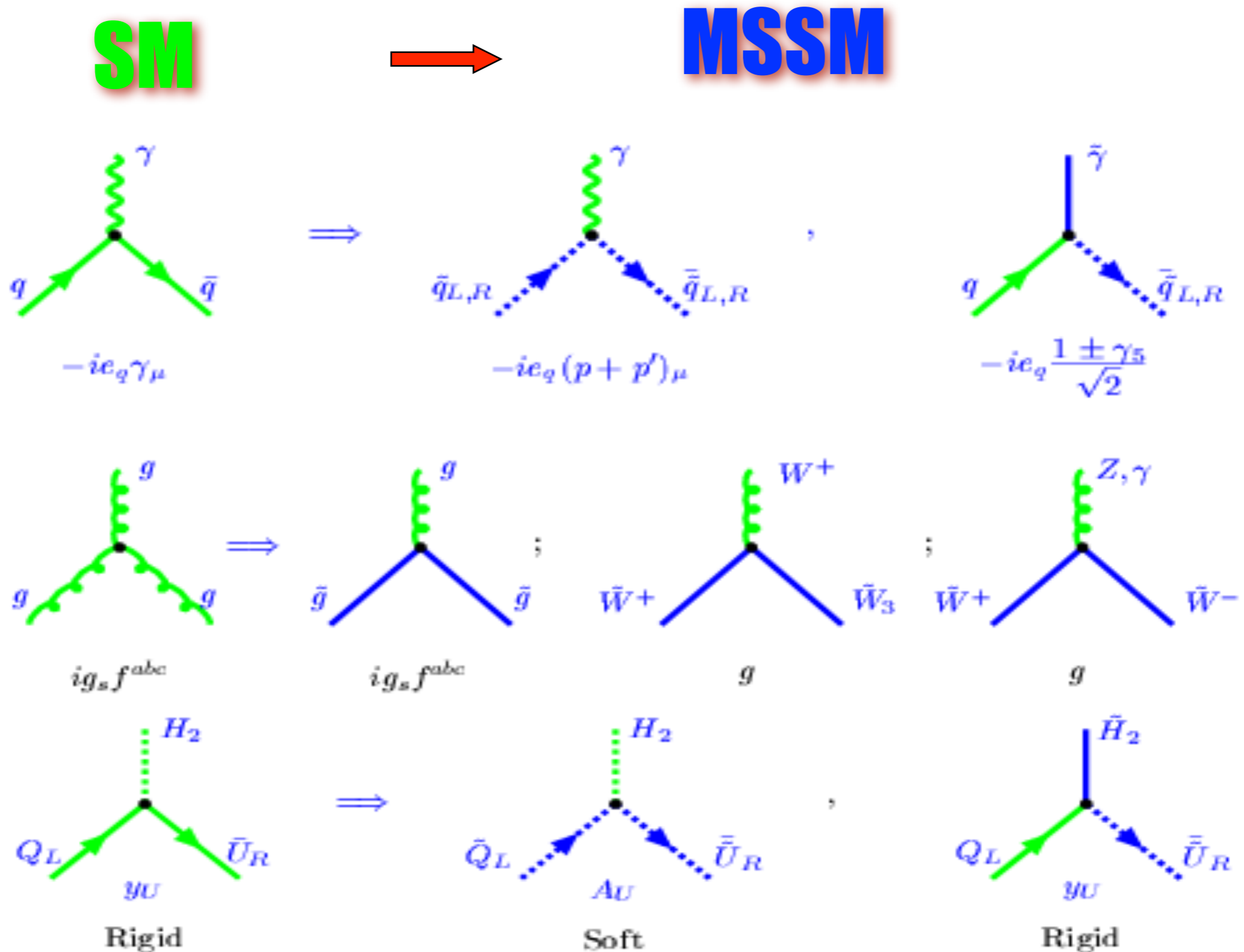
## Vertices



## Vertices

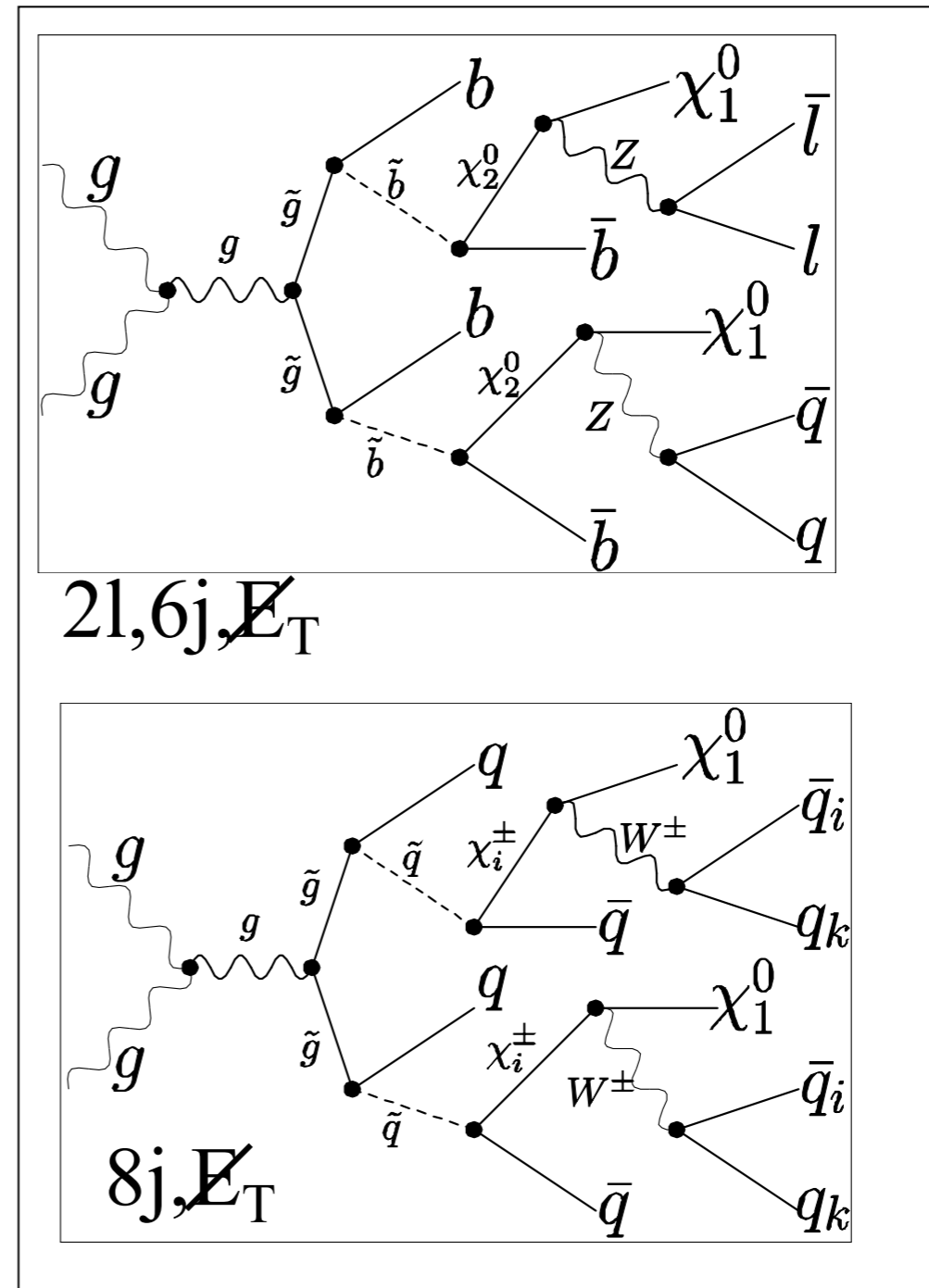
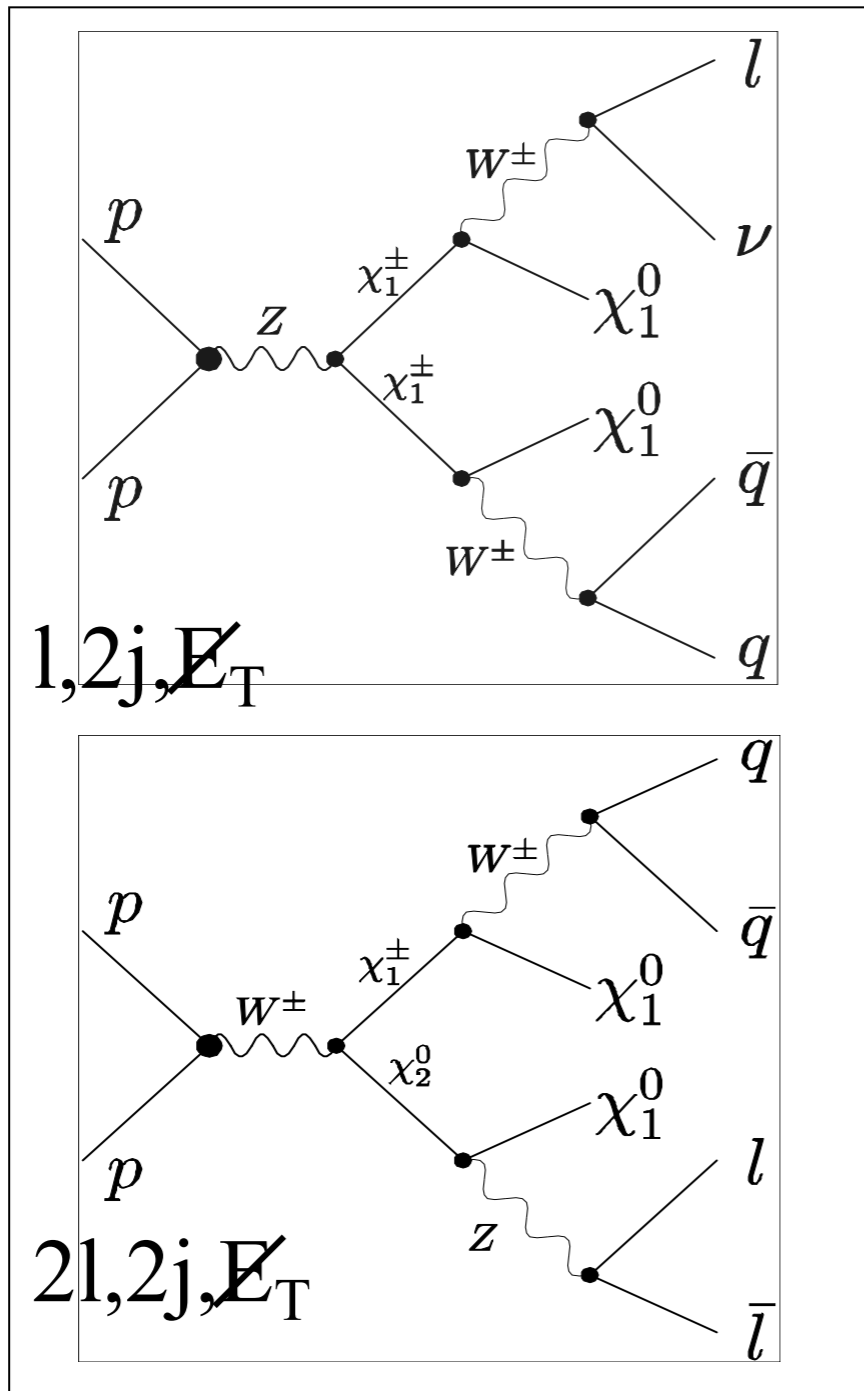






# CREATION AND DECAY OF SUPERPARTNERS IN CASCADE PROCESSES @ LHC

**weak int's**

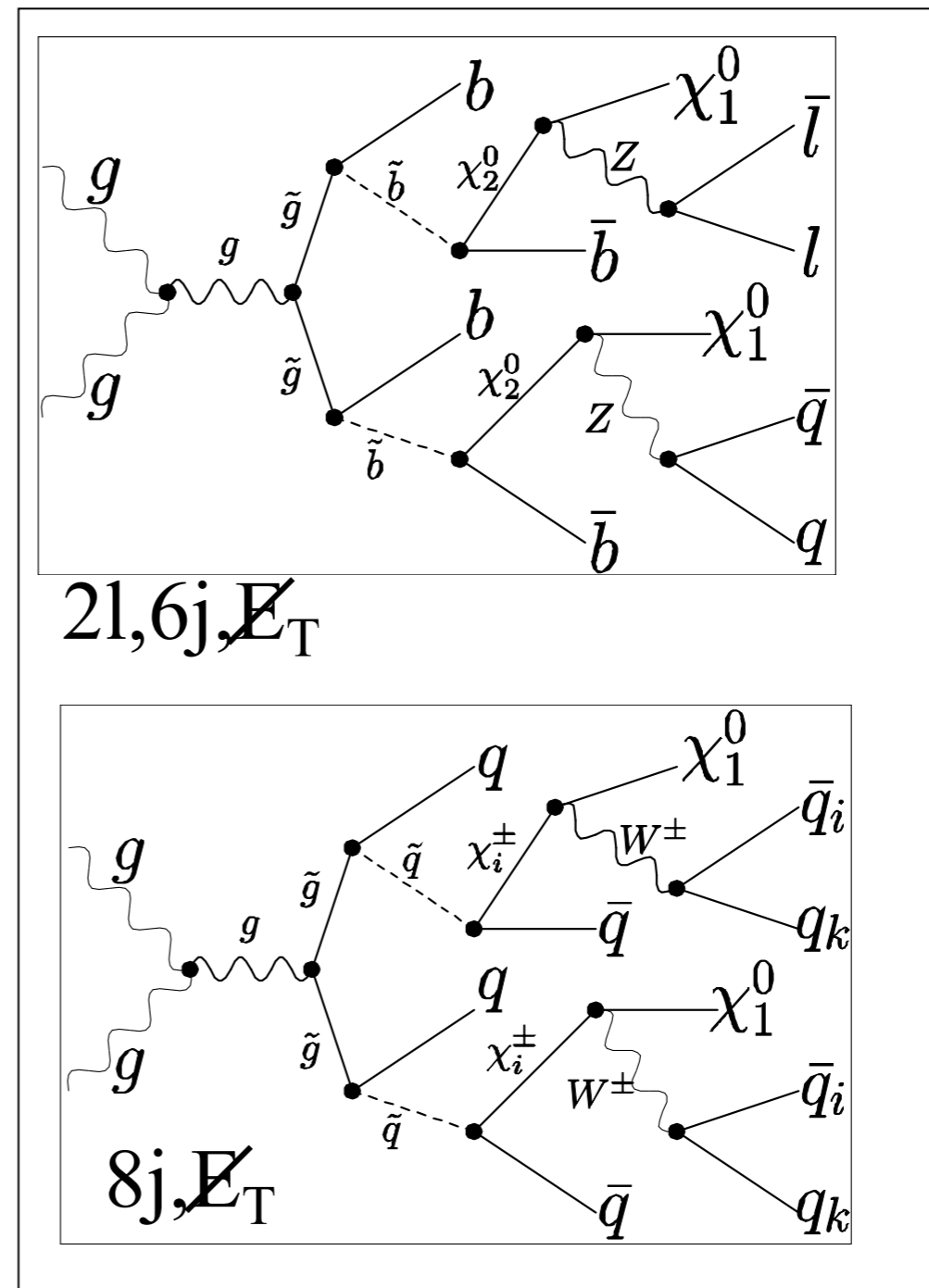
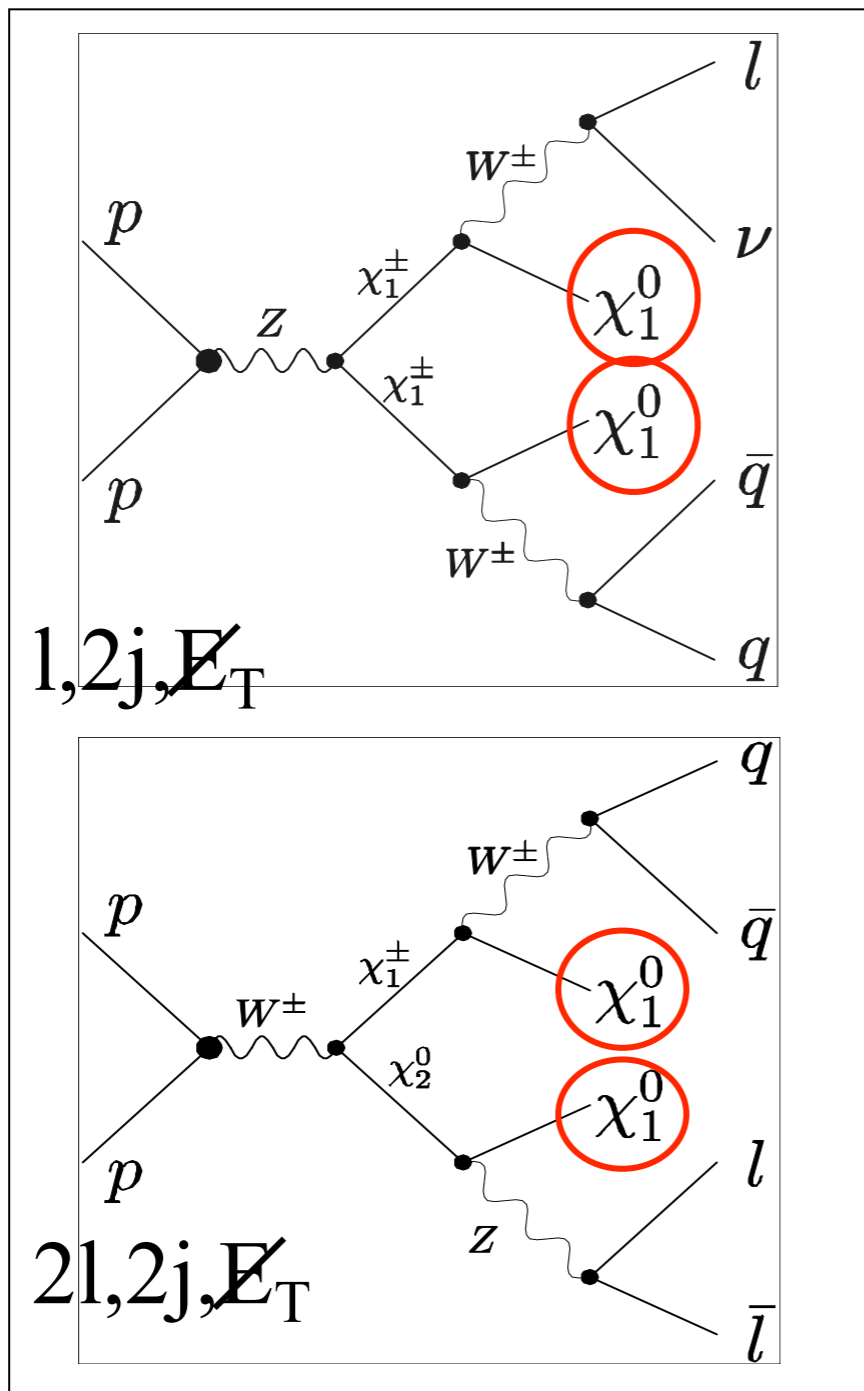


**Strong int's**

Typical SUSY signature: Missing Energy and Transverse Momentum

# CREATION AND DECAY OF SUPERPARTNERS IN CASCADE PROCESSES @ LHC

*weak int's*

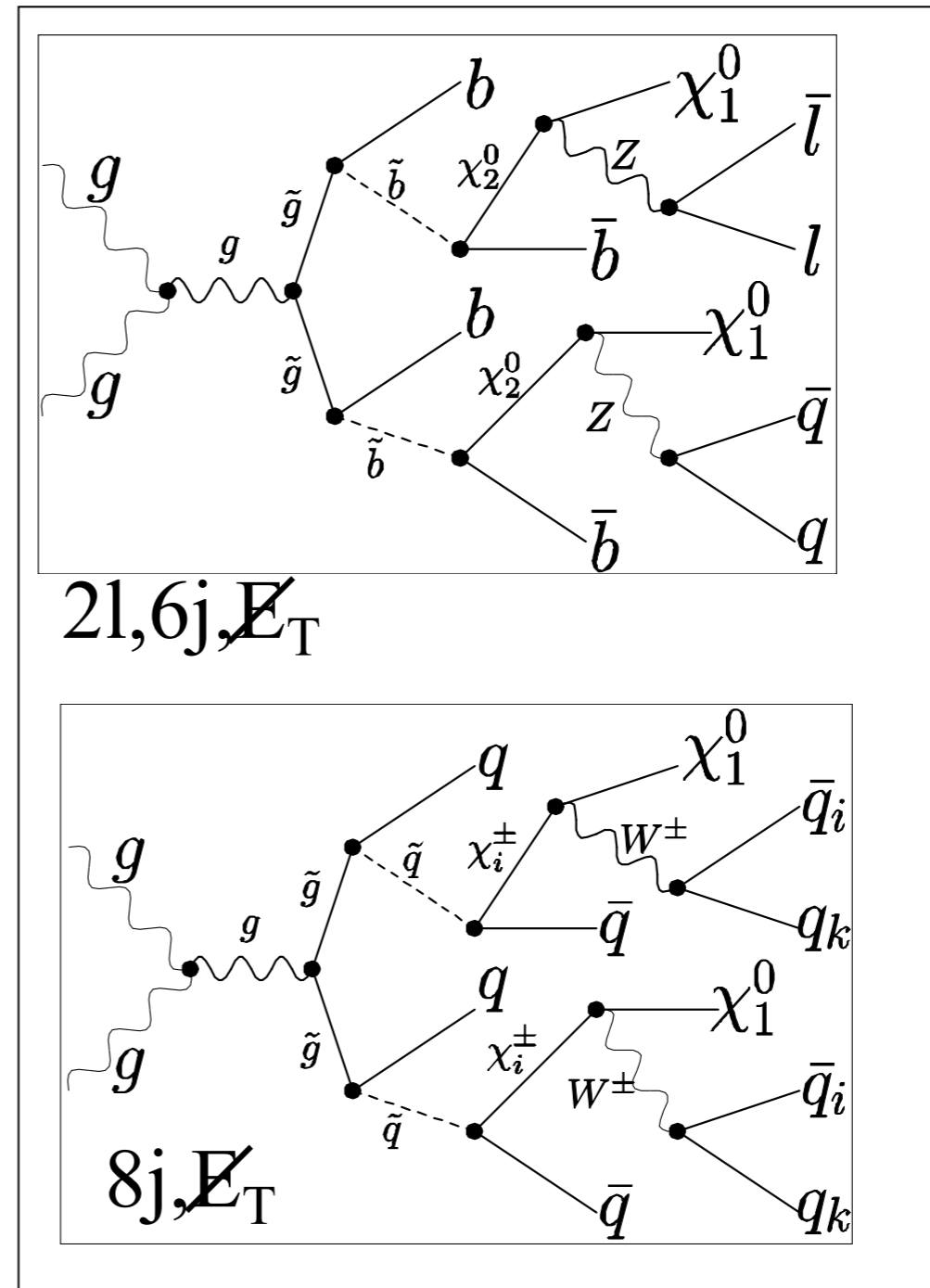
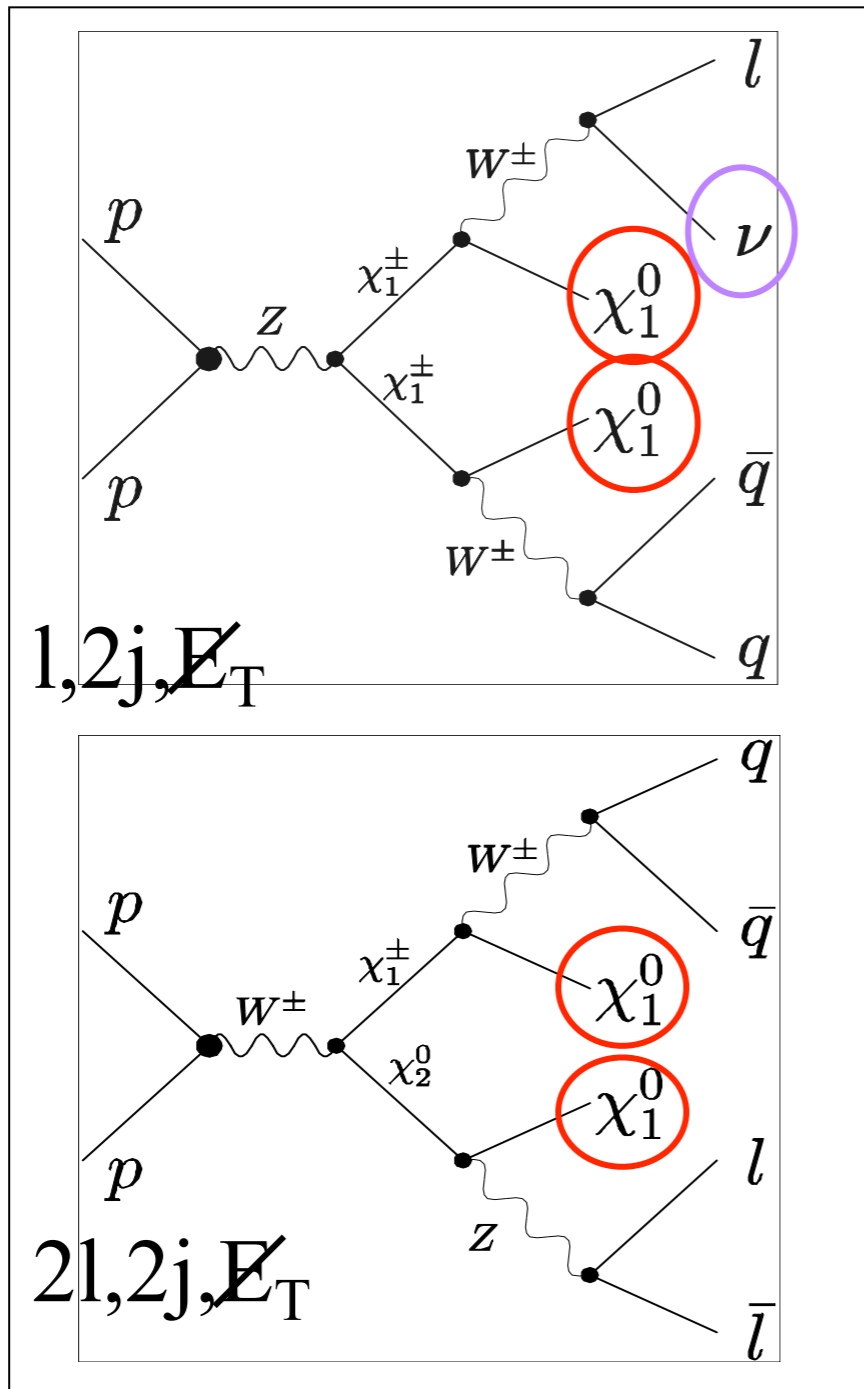


*Strong int's*

Typical SUSY signature: Missing Energy and Transverse Momentum

# CREATION AND DECAY OF SUPERPARTNERS IN CASCADE PROCESSES @ LHC

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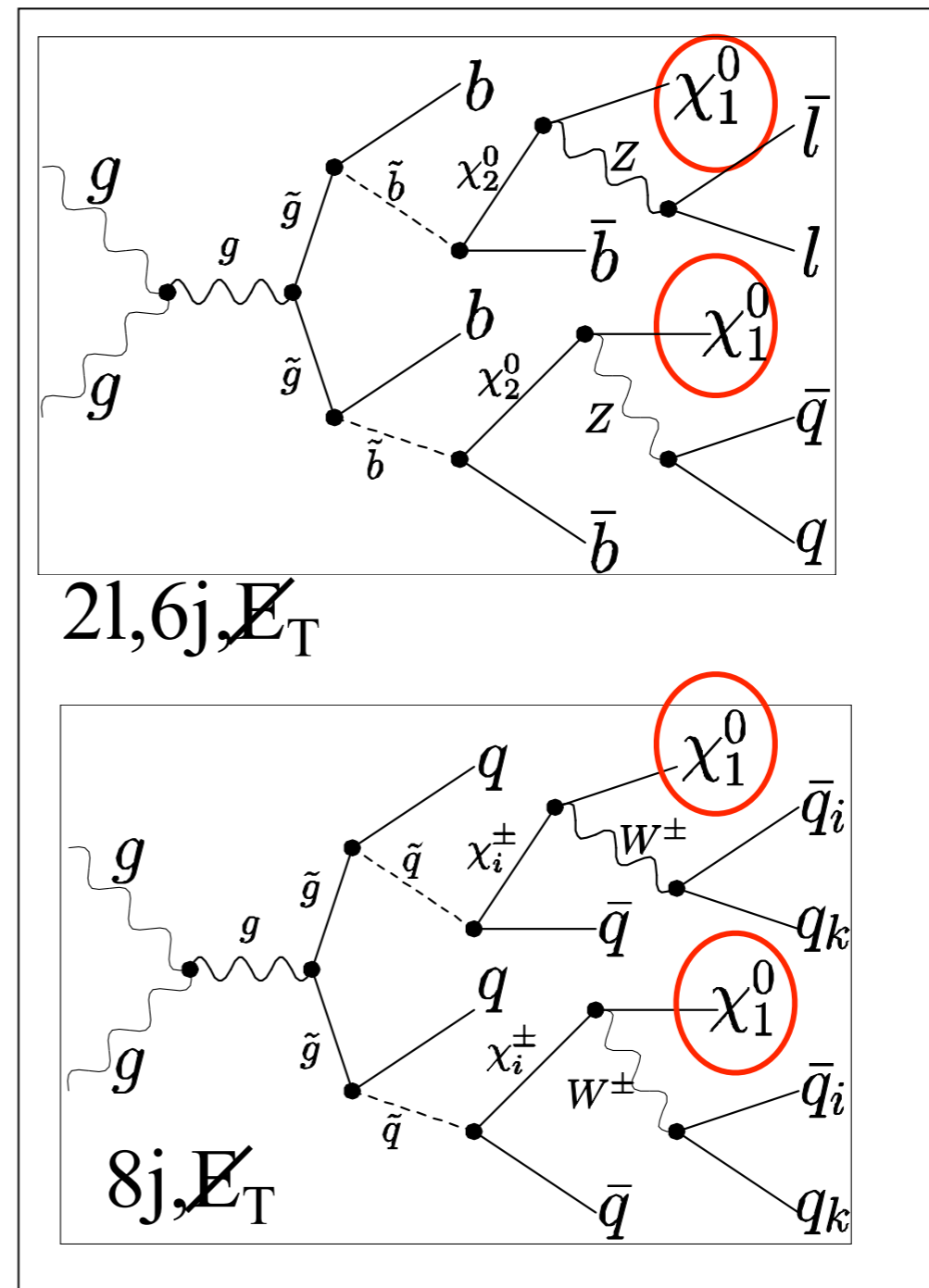
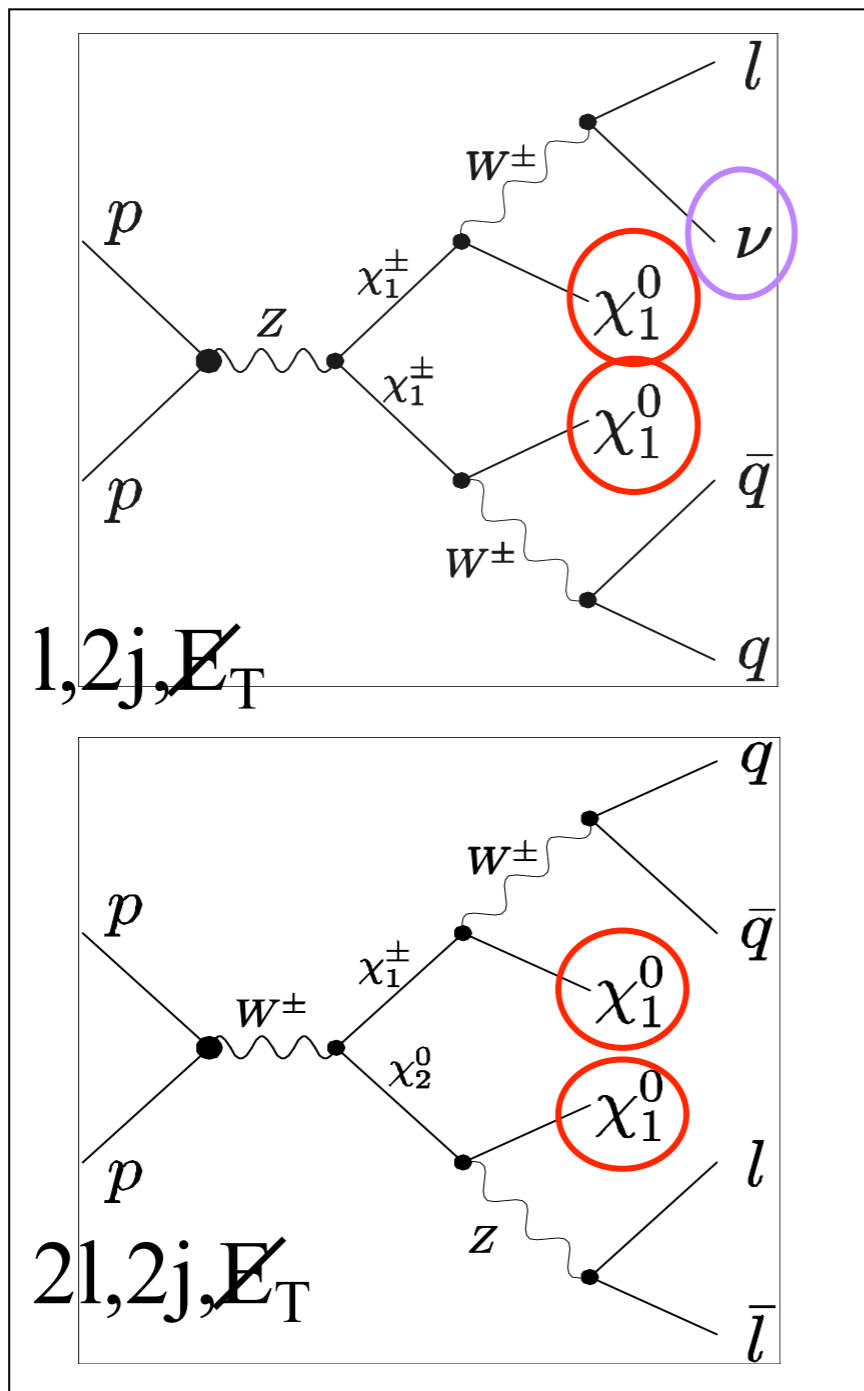


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Typical SUSY signature: Missing Energy and Transverse Momentum

# CREATION AND DECAY OF SUPERPARTNERS IN CASCADE PROCESSES @ LHC

**weak int's**



**Strong int's**

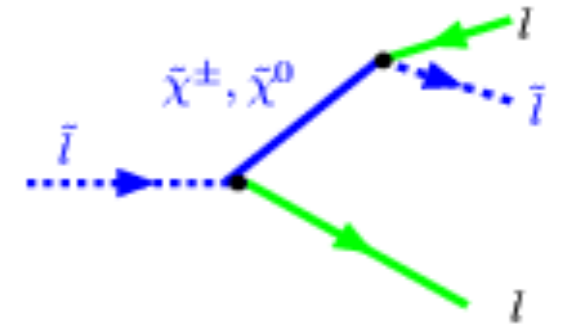
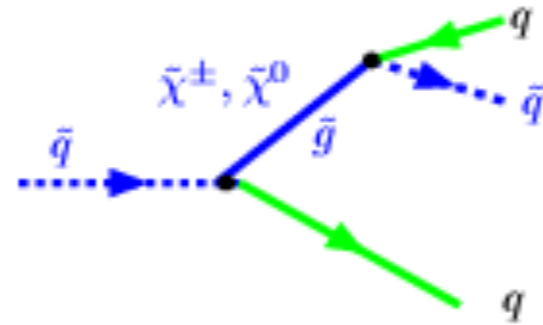
Typical SUSY signature: Missing Energy and Transverse Momentum

squarks

$$\tilde{q}_{L,R} \rightarrow q + \tilde{\chi}_i^0$$

$$\tilde{q}_L \rightarrow q' + \tilde{\chi}_i^\pm$$

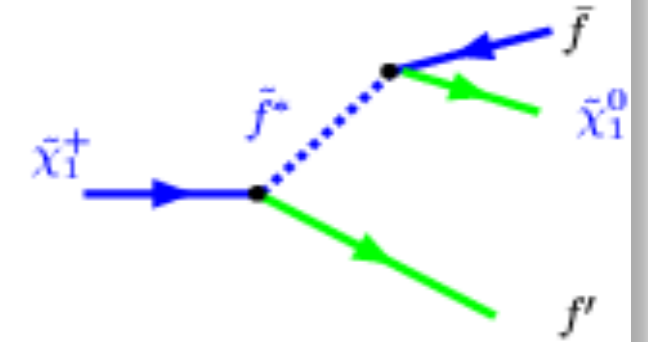
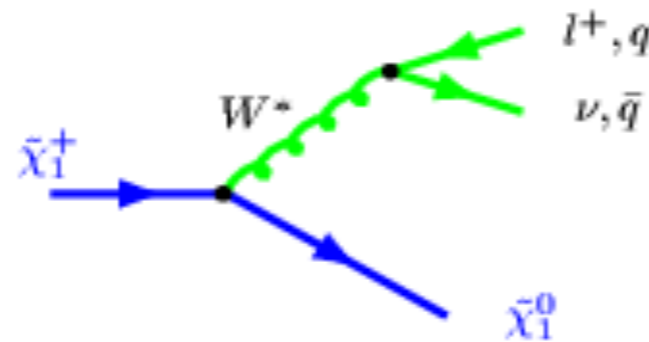
$$\tilde{q}_{L,R} \rightarrow q + g$$



sleptons

$$\tilde{l} \rightarrow l + \tilde{\chi}_i^0$$

$$\tilde{l}_L \rightarrow \nu_l + \tilde{\chi}_i^\pm$$



chargino

$$\tilde{\chi}_i^\pm \rightarrow e + \nu_e + \tilde{\chi}_i^0$$

$$\tilde{\chi}_i^\pm \rightarrow q + \bar{q}' + \tilde{\chi}_i^0$$

neutralino

$$\tilde{\chi}_i^0 \rightarrow \tilde{\chi}_1^0 + l^+ + l^-$$

$$\tilde{\chi}_i^0 \rightarrow \tilde{\chi}_1^0 + q + \bar{q}'$$

$$\tilde{\chi}_i^0 \rightarrow \tilde{\chi}_1^\pm + l^\pm + \nu_l$$

$$\tilde{\chi}_i^0 \rightarrow \tilde{\chi}_1^0 + \nu_l + \bar{\nu}_l$$

Final states

$$l^+ l^- + \cancel{E}_T$$

$$2 \text{ jets} + \cancel{E}_T$$

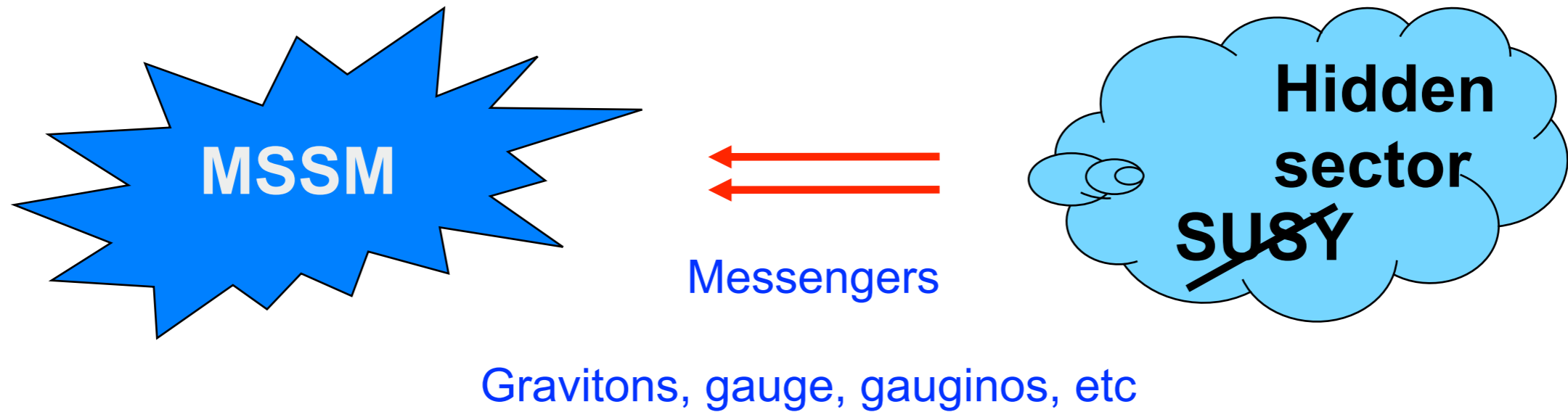
$$\gamma + \cancel{E}_T$$

$$\cancel{E}_T$$

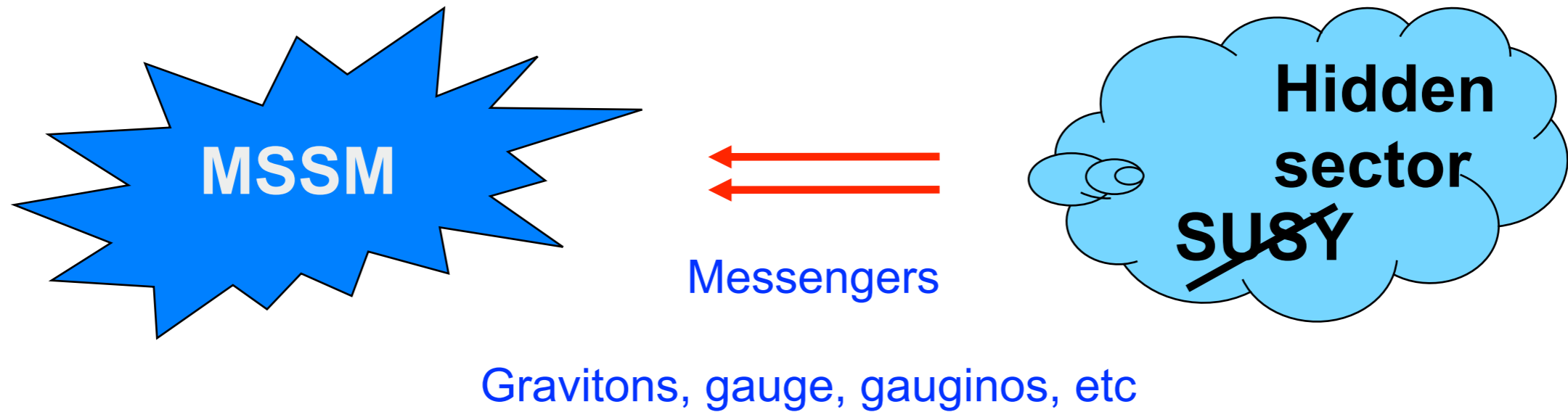
gluino

$$\tilde{g} \rightarrow q + \bar{q} + \tilde{\gamma}$$

$$\tilde{g} \rightarrow g + \tilde{\gamma}$$



Breaking via F and D terms in a hidden sector

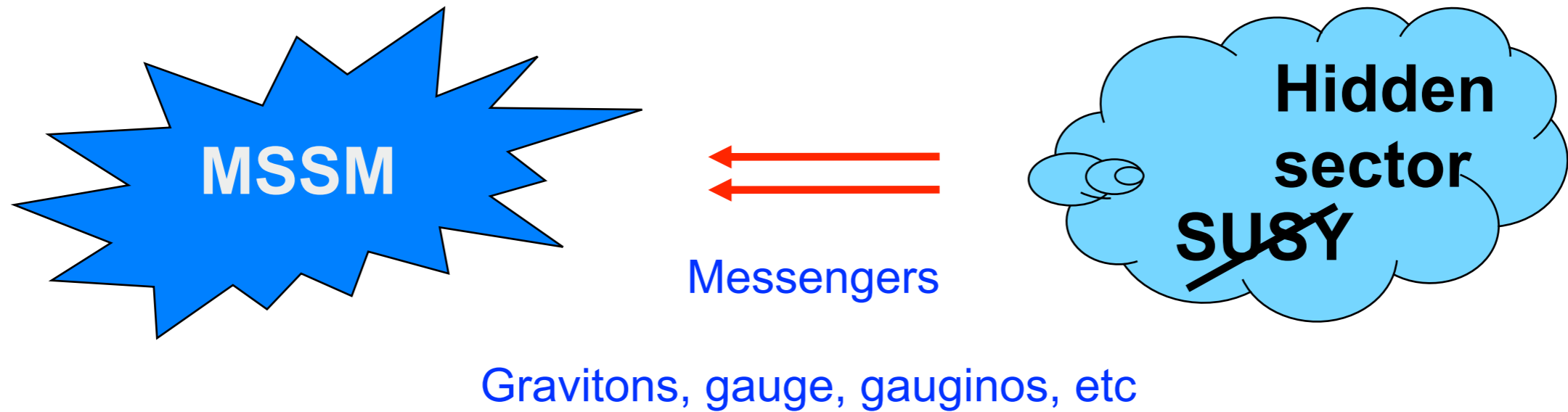


Breaking via F and D terms in a hidden sector

$$-L_{Soft} = \sum_{\alpha} M_{\alpha} \tilde{\lambda}_{\alpha} \tilde{\lambda}_{\alpha} + \sum_i m_{0i}^2 |A_i|^2 + \sum_{ijk} A_{ijk} A_i A_j A_k + \sum_{ij} B_{ij} A_i A_j$$

gauginos
scalar fields





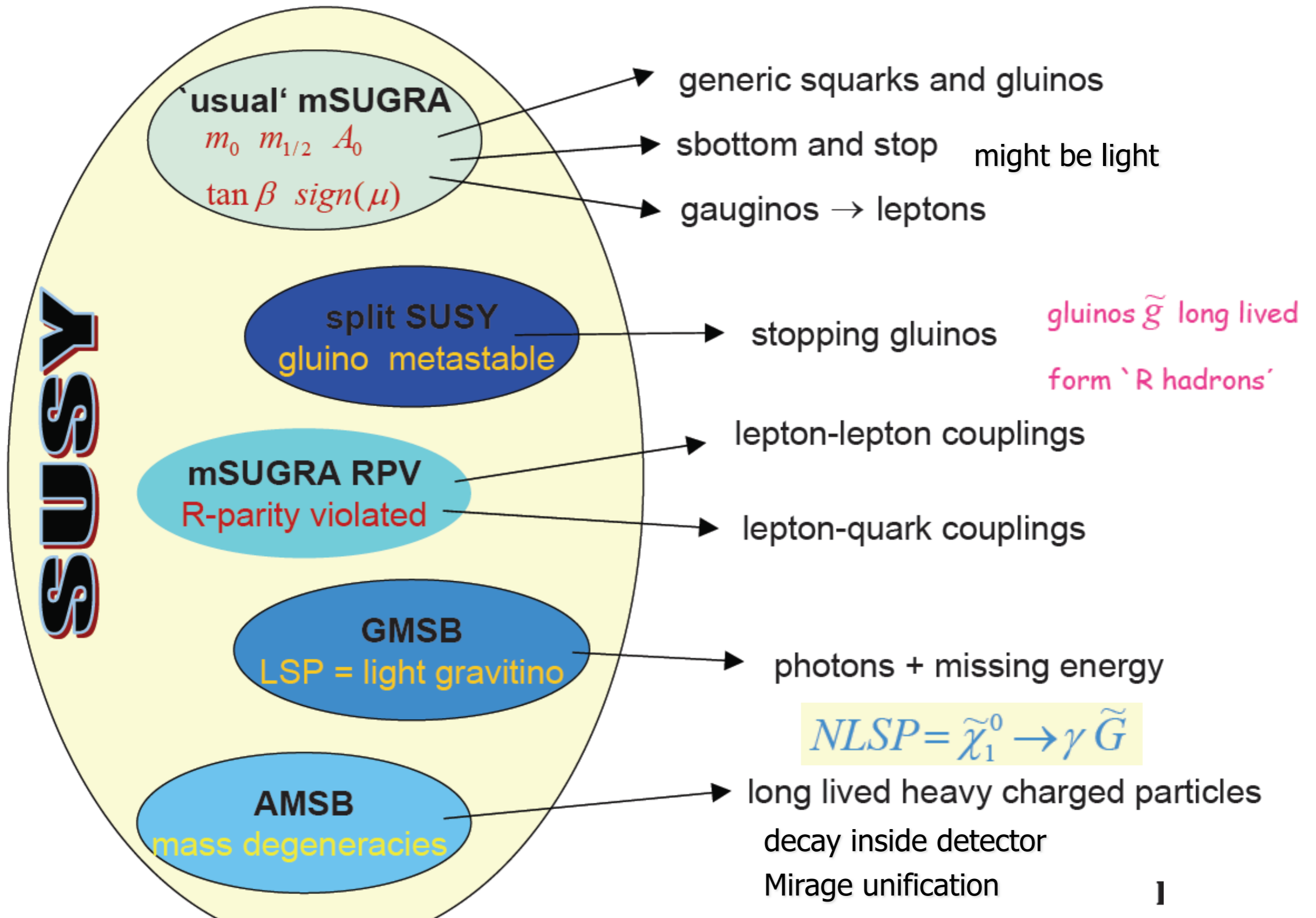
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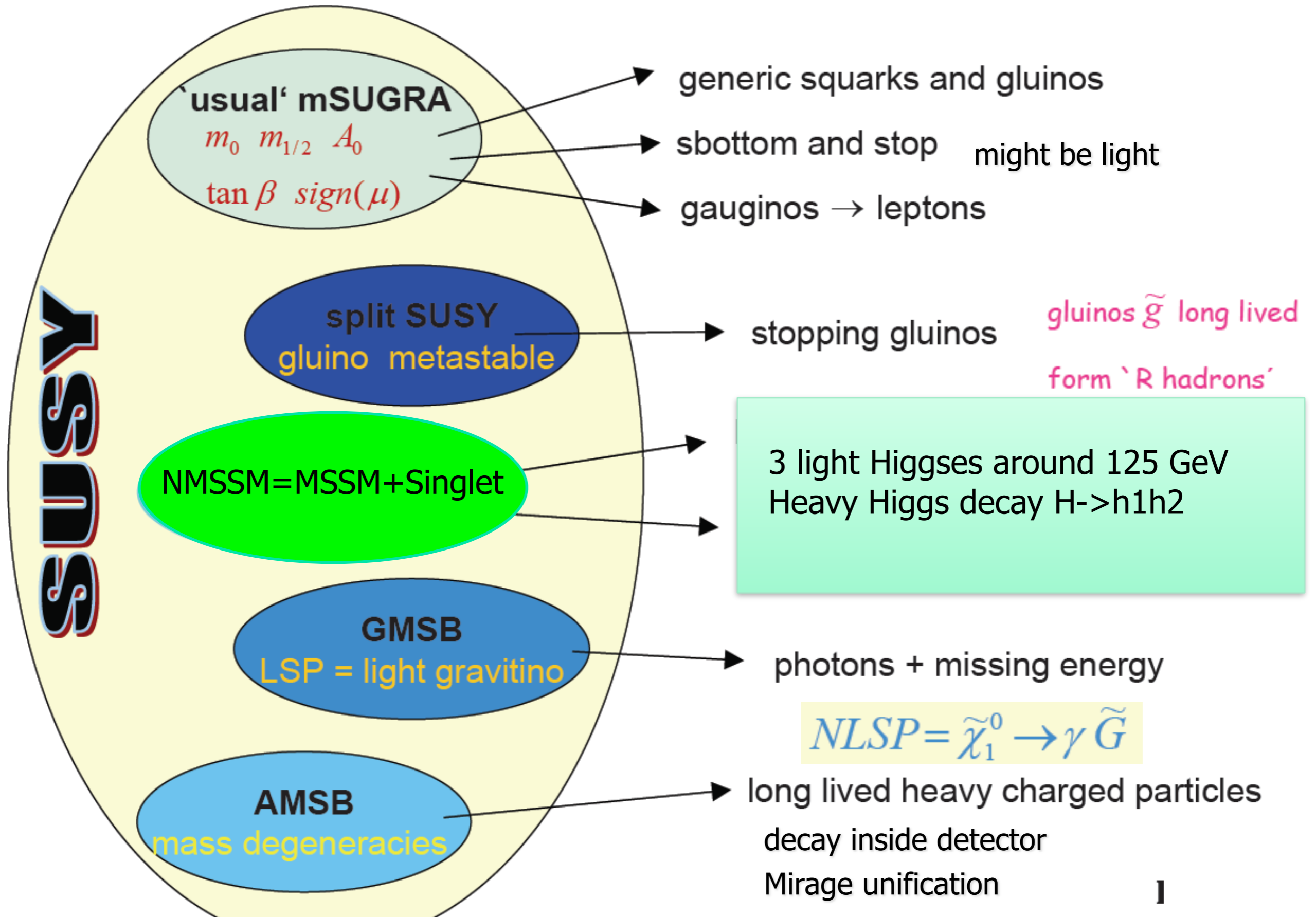
gauginos
scalar fields

Over 100 of free parameters !

# SUSY Models and Signatures



# SUSY Models and Signatures



**Particle Phys**

- Direct production at colliders at high energies
- Indirect manifestation at low energies
  - Rare decays (  $B_s \rightarrow s\gamma, B_s \rightarrow \mu^+\mu^-, B_s \rightarrow \tau\nu$  )
  - g-2 of the muon

- Search for long-lived SUSY particles

**Astro Phys  
(if SUSY DM)**

- Relic abundancy of Dark Matter in the Universe
- DM annihilation signal in cosmic rays
- Direct DM interaction with nucleons

**Particle Phys**

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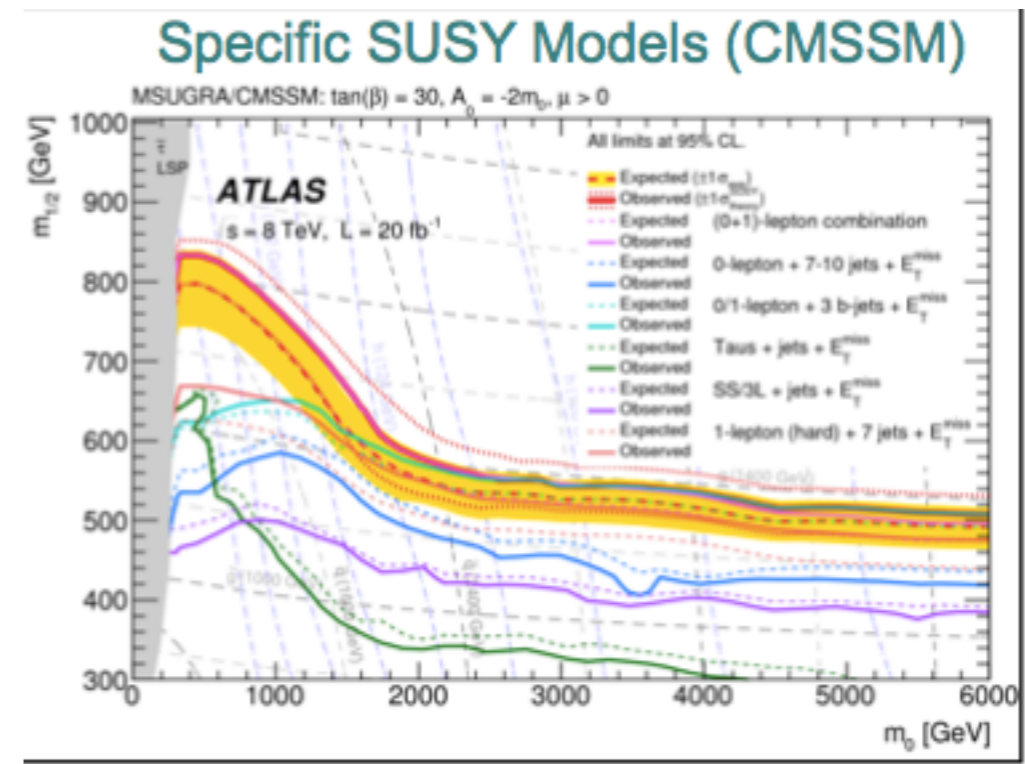
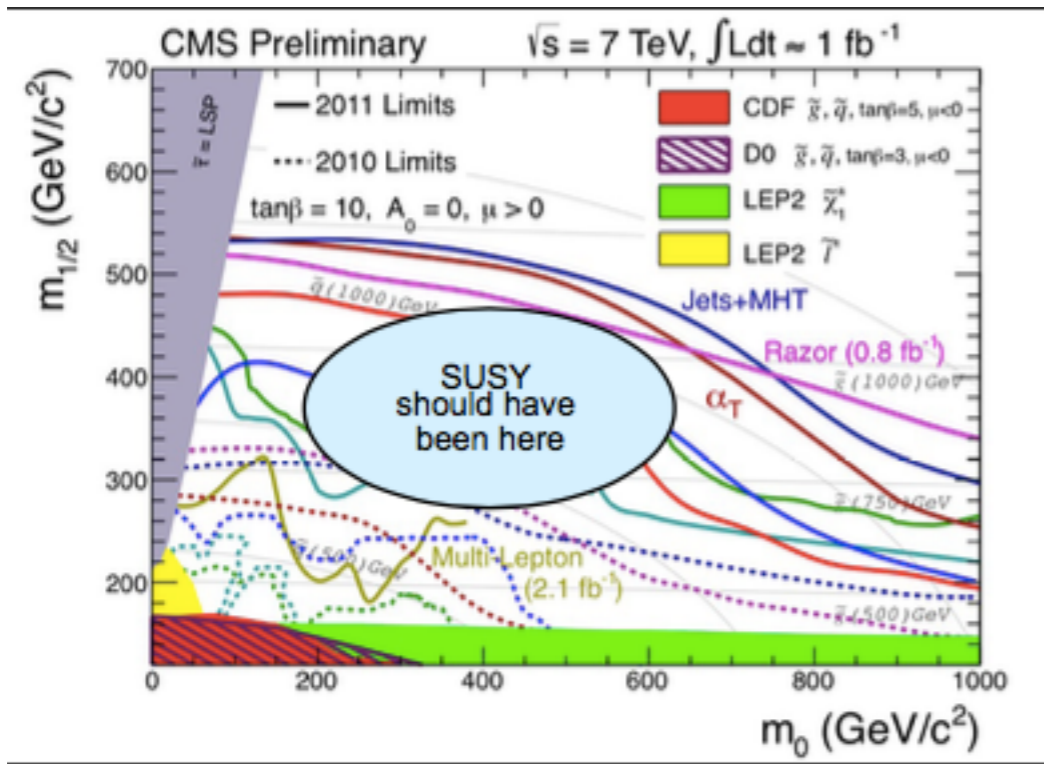
- Direct DM interaction with nucleons

Nothing so far ...

# WHAT IS THE LHC REACH NOW?

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# WHAT IS THE LHC REACH NOW?

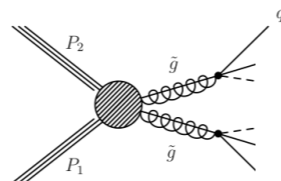


Universal parameters

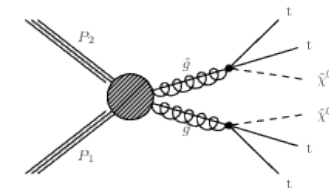




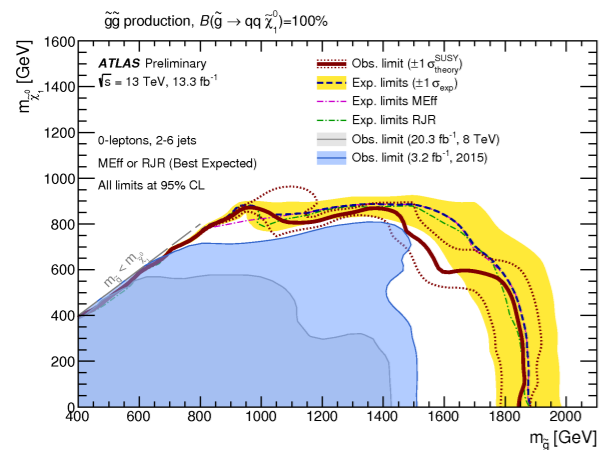
## Glauino decays to qq+LSP



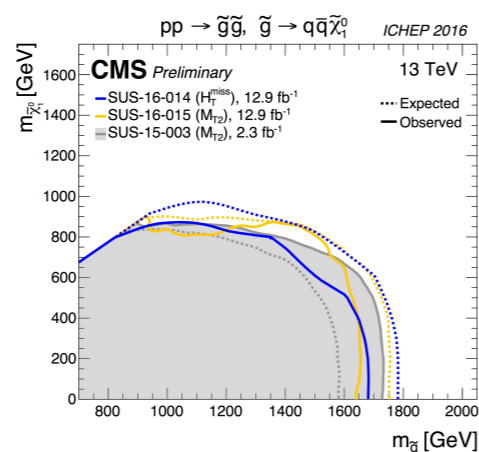
## Glauino decays to tt+LSP



### Summary of decays to light quarks + LSP

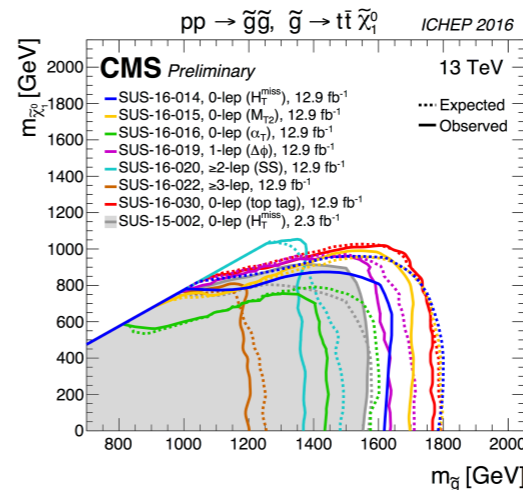


ATLAS-CONF-2016-078



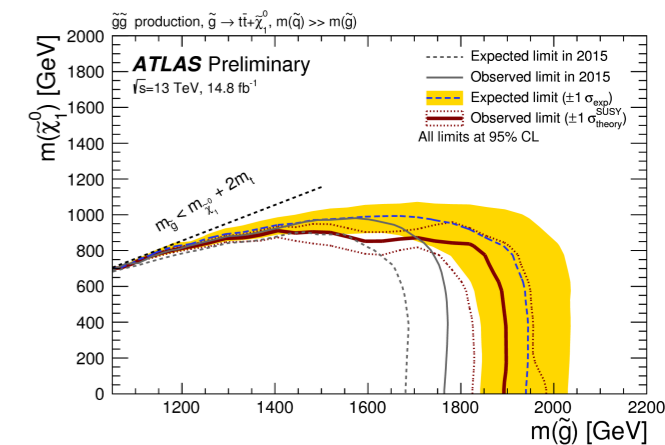
CMS-SUS-16-014  
CMS-SUS-16-015

### CMS summary

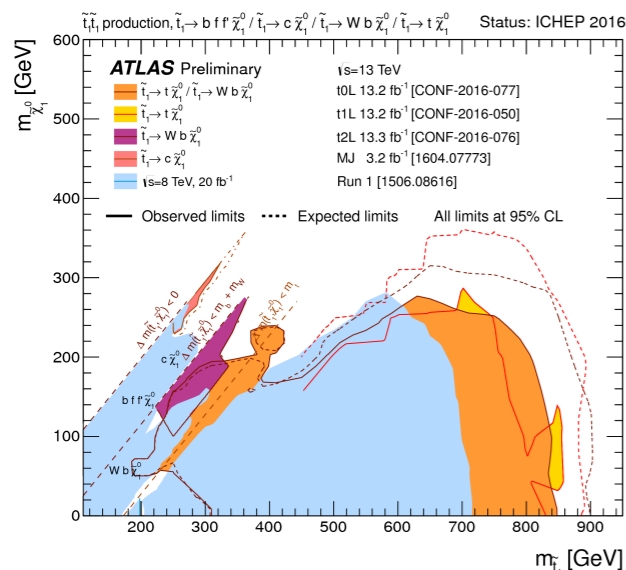


### ATLAS multi-b

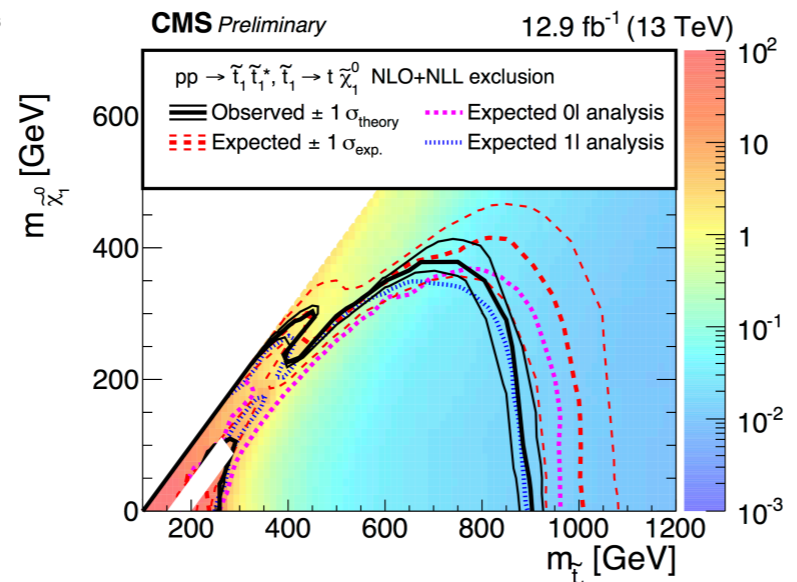
ATLAS-CONF-2016-052



## Top squarks - summaries



ATLAS summary

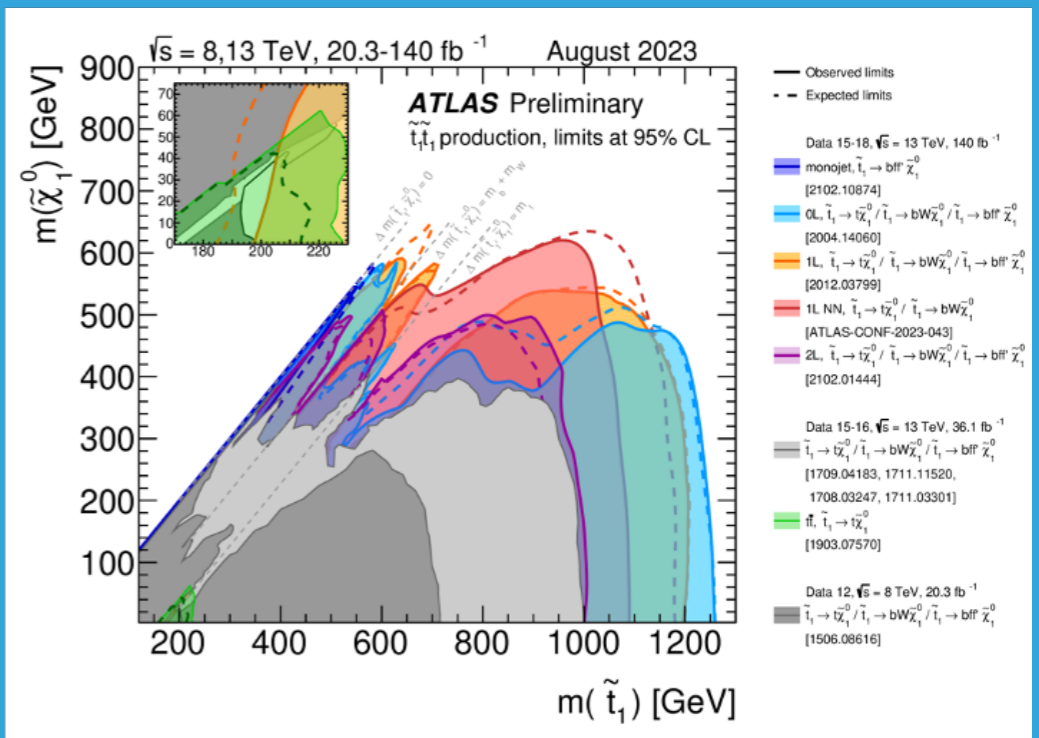
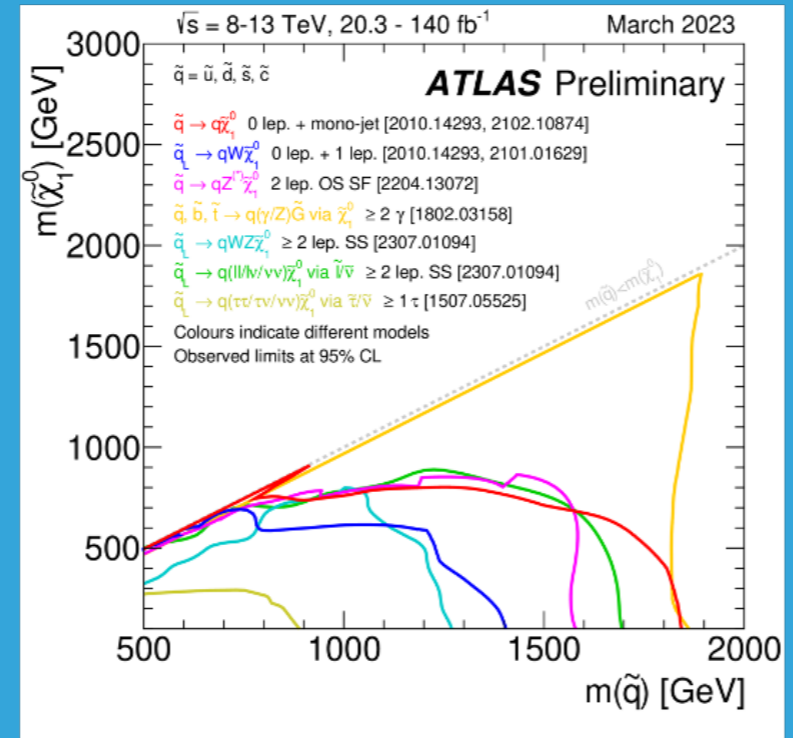
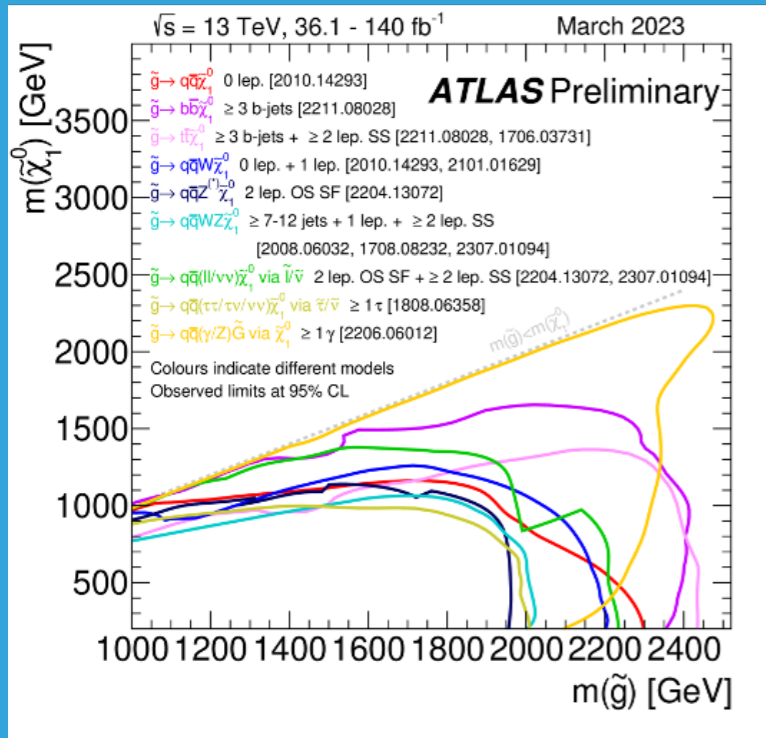
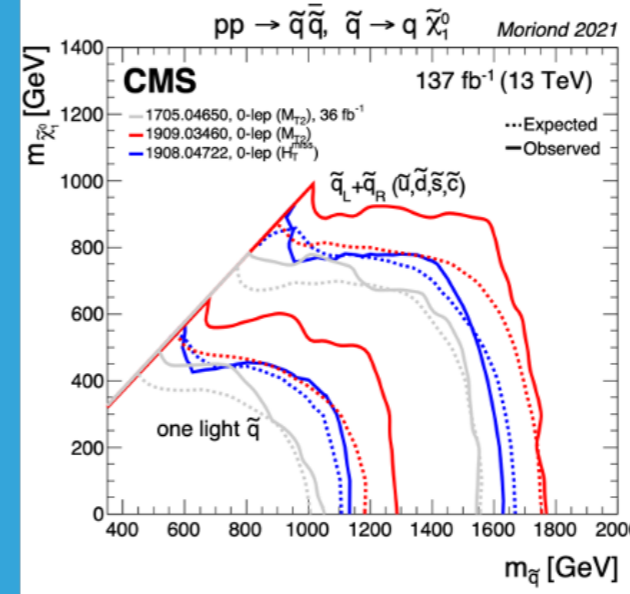
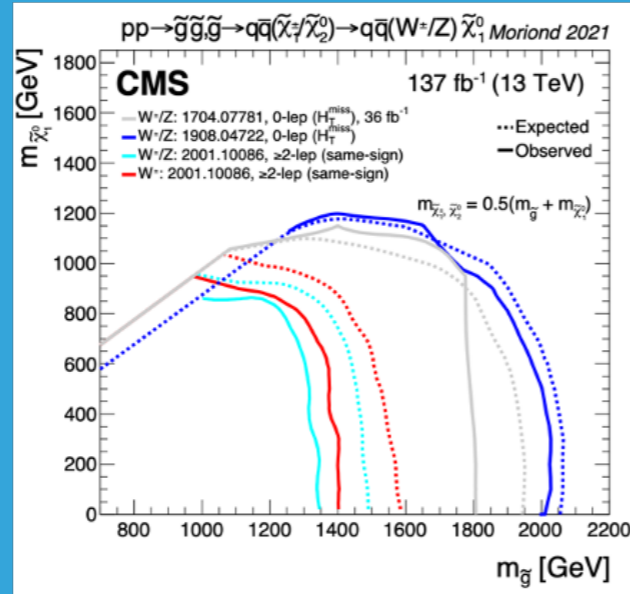
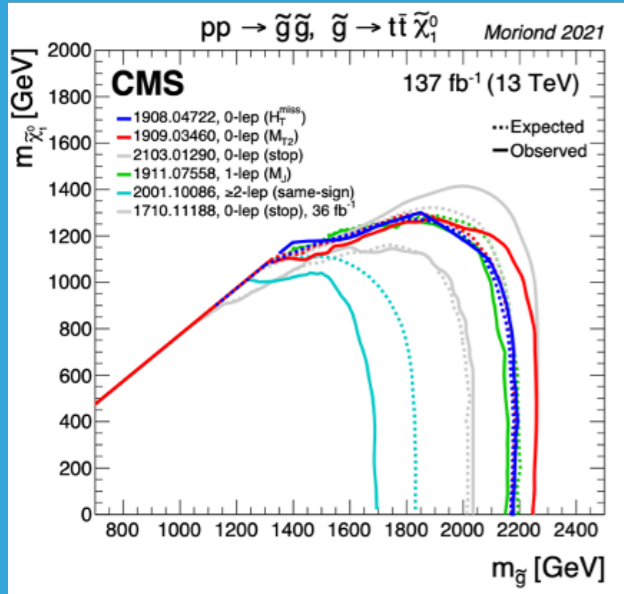


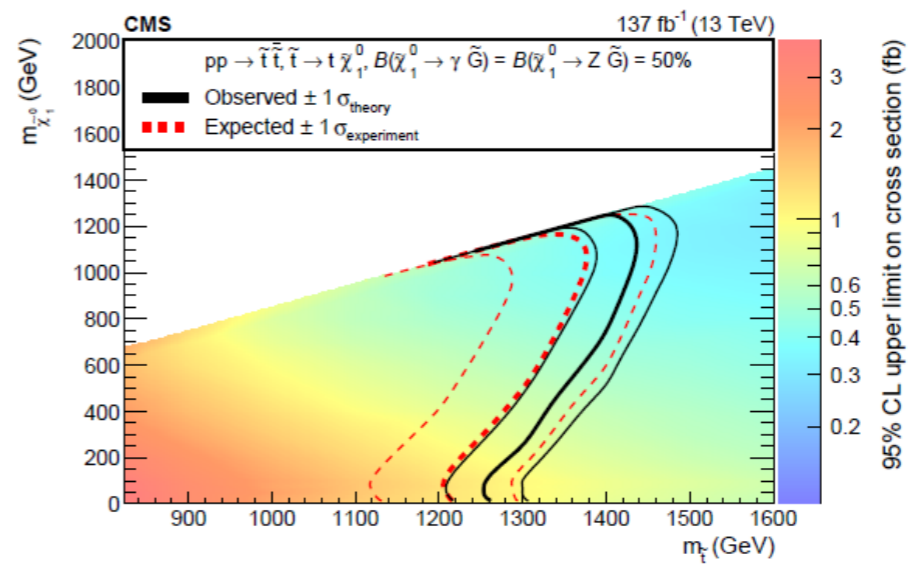
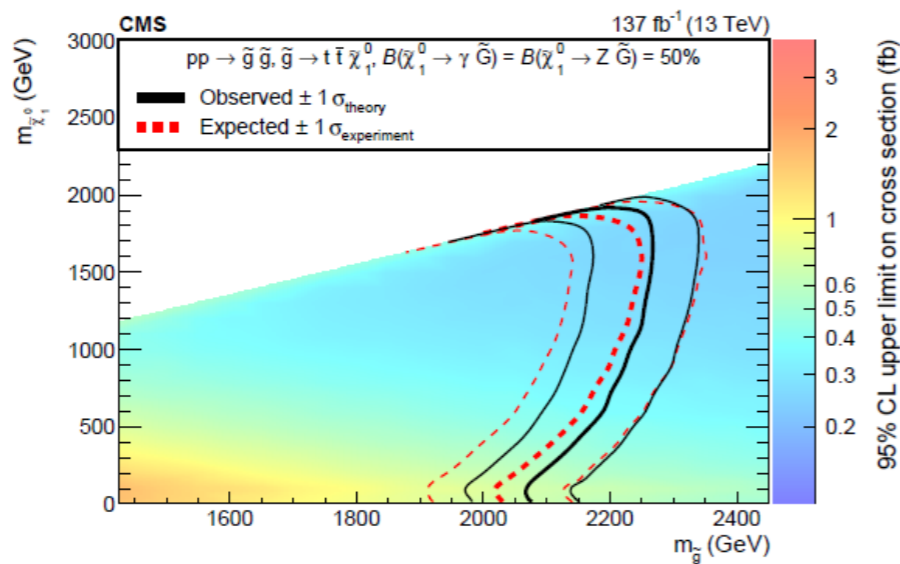
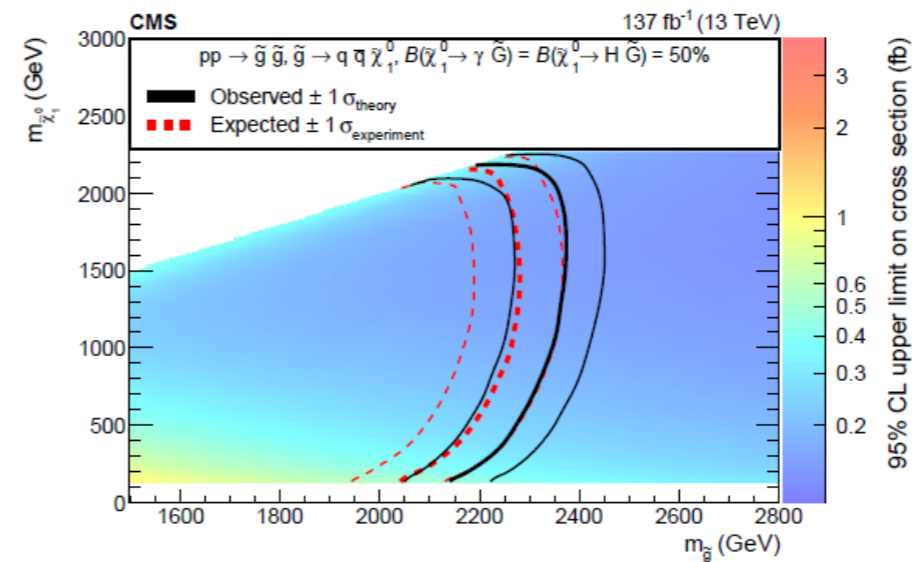
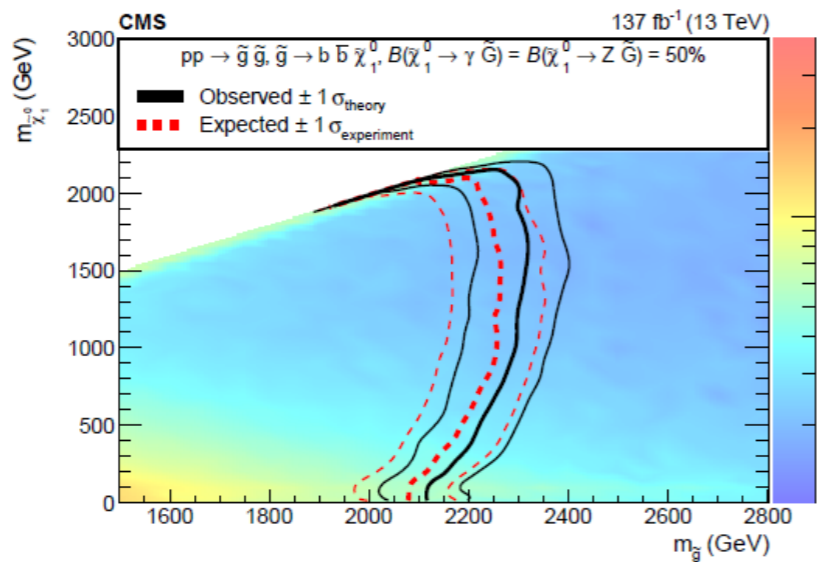
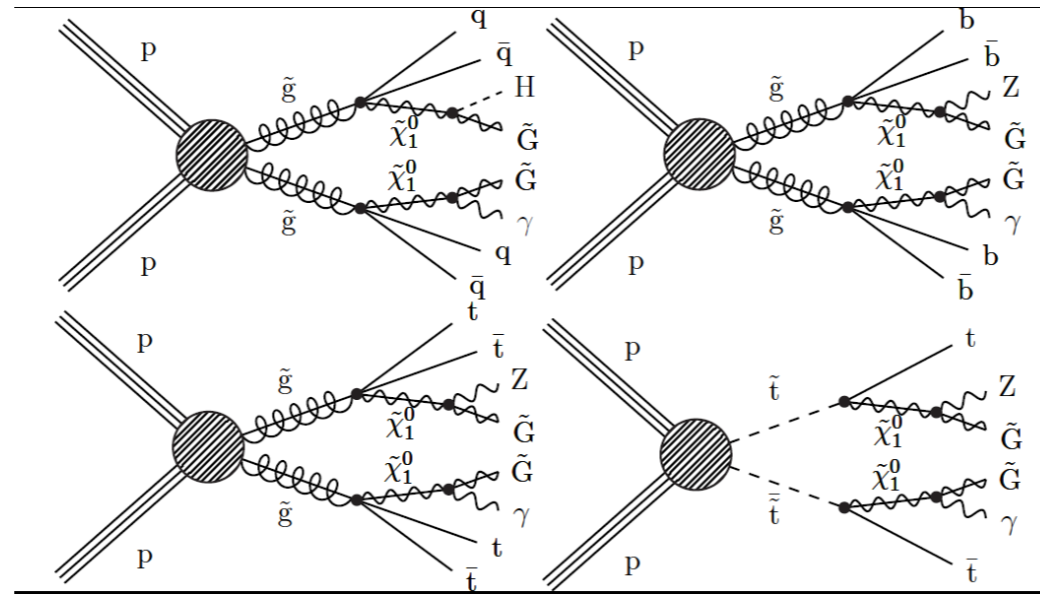
CMS 0l+1l combination  
for 2-/3-body decay

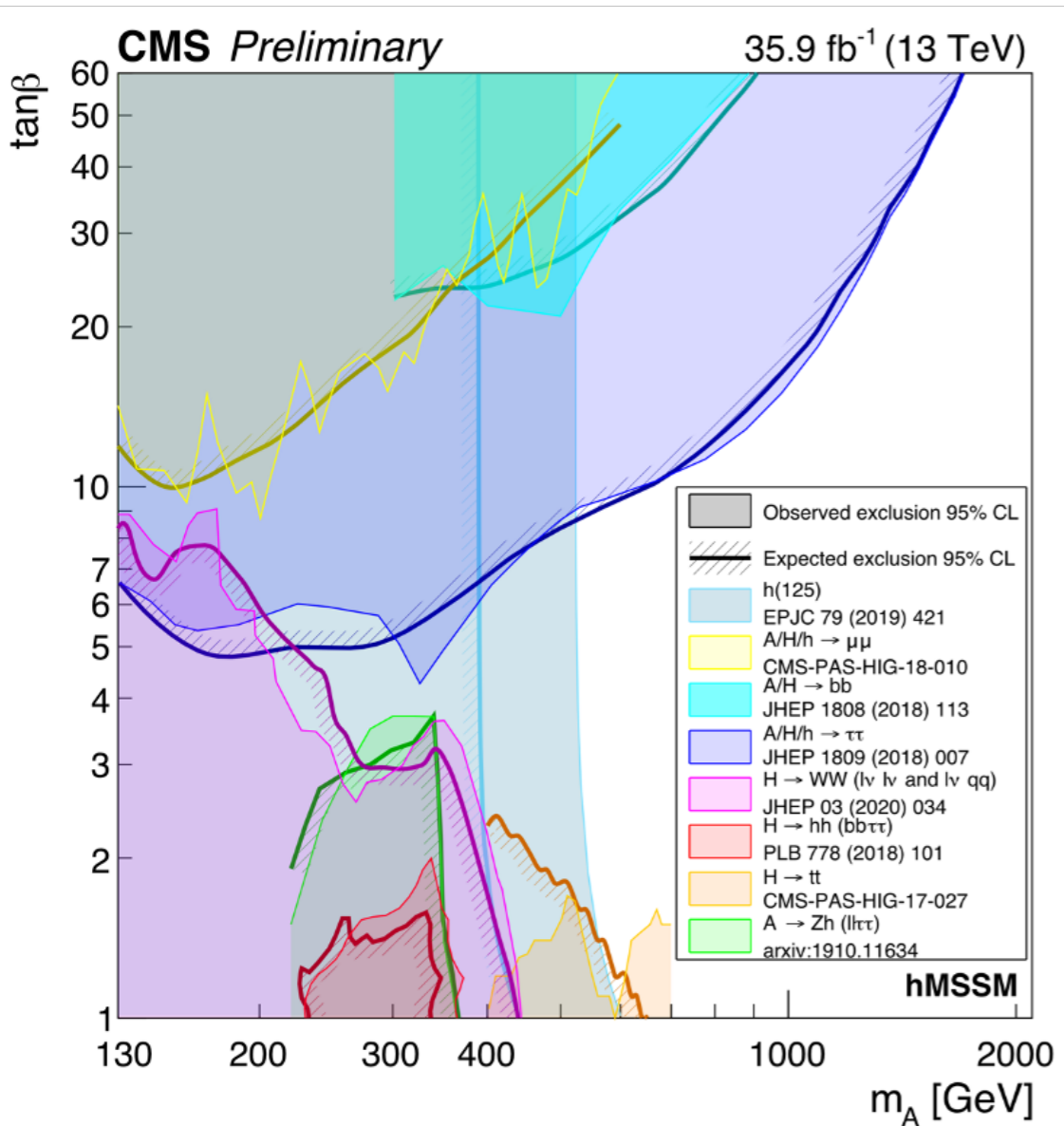
- SUSY limits for strong int's are pushed above 1 TeV
- This already requires fine tuning - little hierarchy prob
- No guiding lines

# RECENT LHC LIMITS ON MSSM '23 82

## RUN2 LHC limits on MSSM, ATLAS&CMS

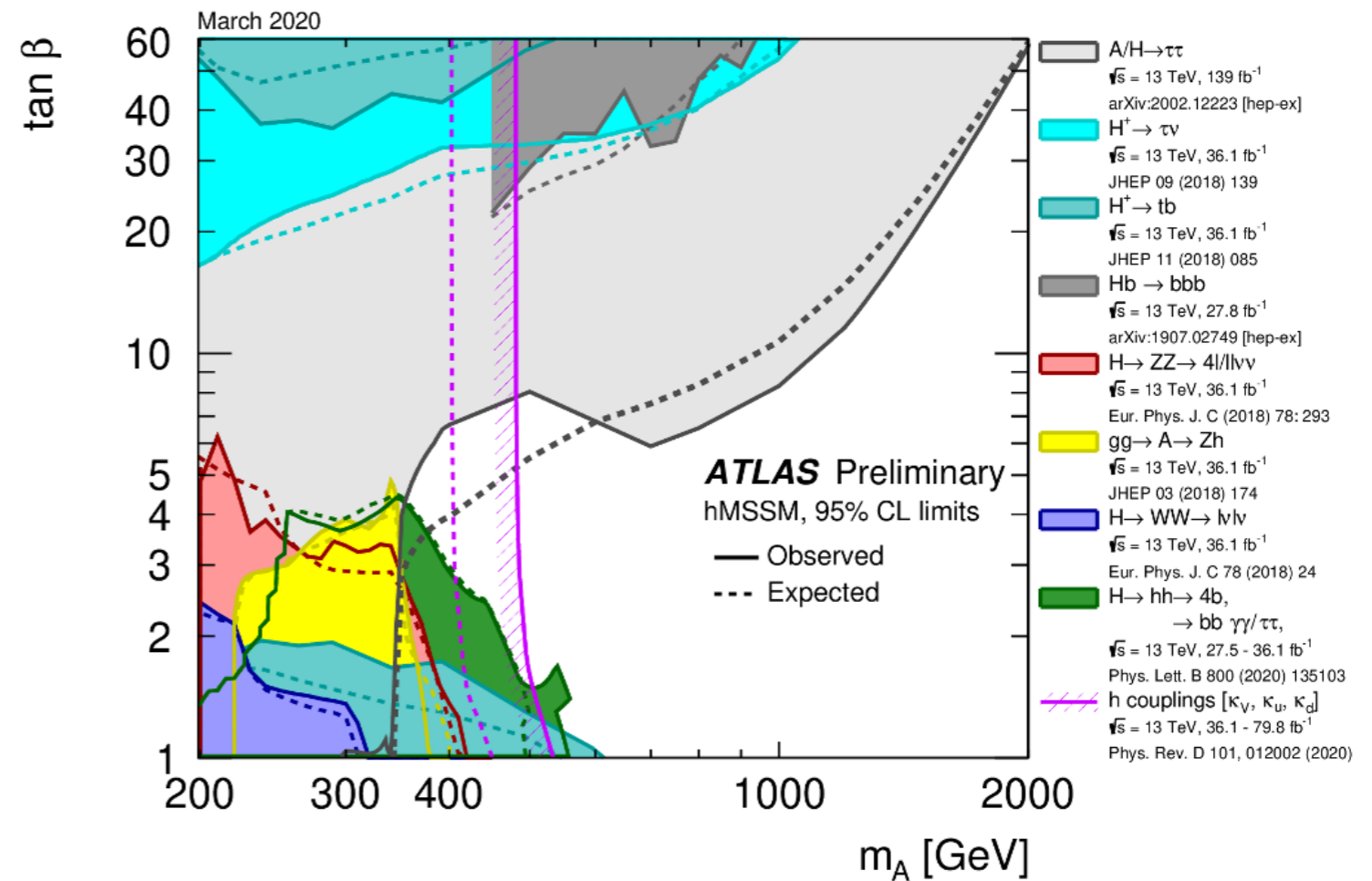




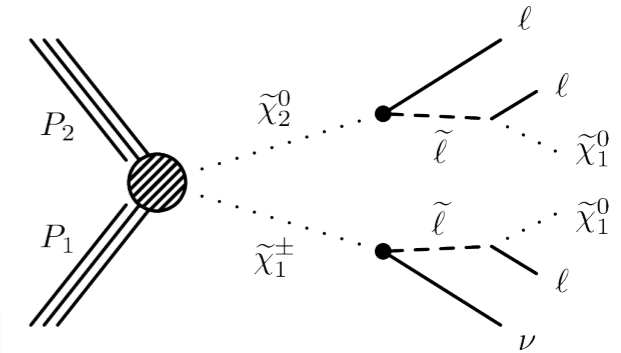


## 2HDM hMSSM combined results, RUN2

Much more details see in a talk by [Adam Bailey](#)  
 (+ comprehensive list of analyses for ATLAS & CMS)



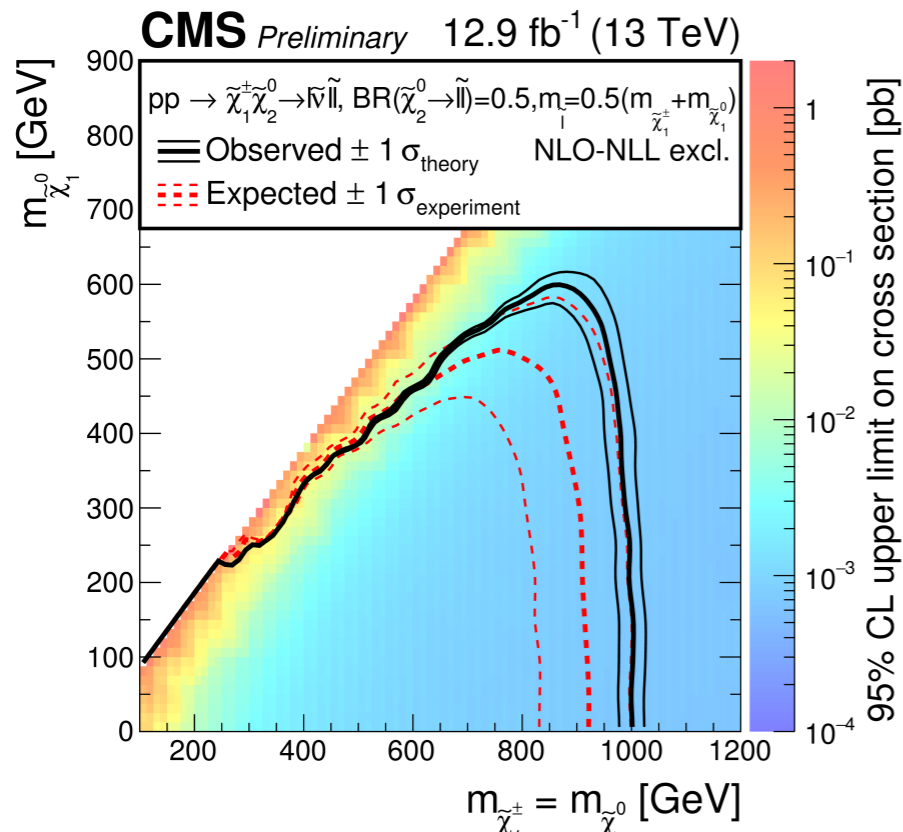
## Chargino / neutralino production



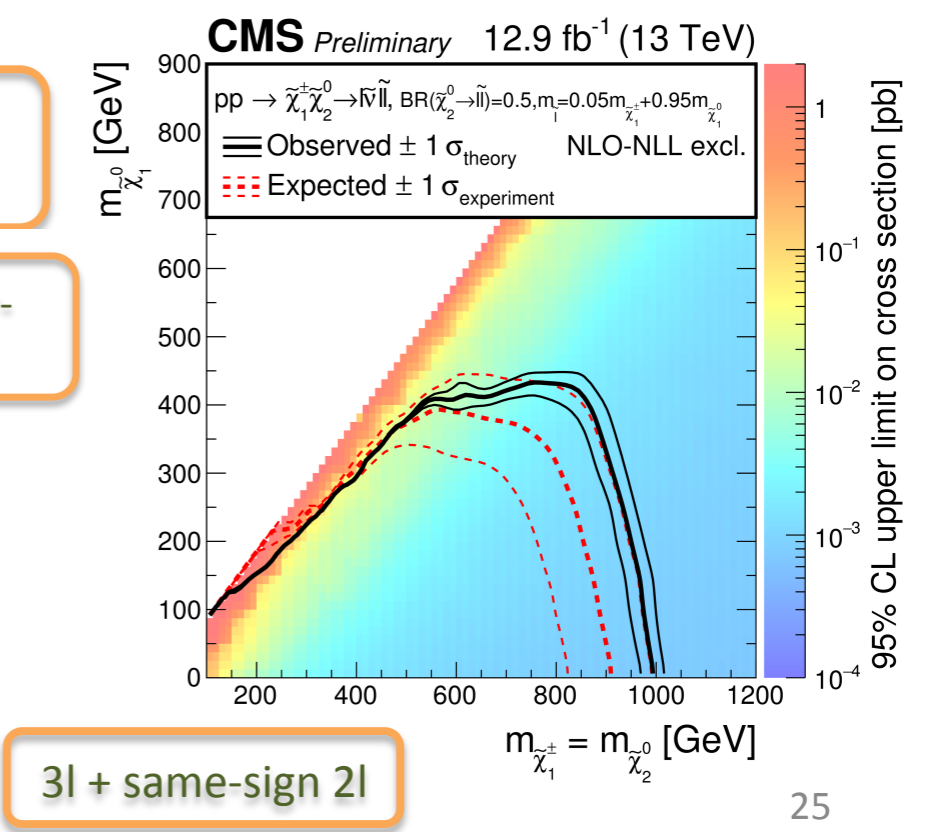
### Direct production of “electroweakino” pairs

- decays via sleptons / sneutrinos
- using benchmarks to illustrate different scenarios (depend on mixings and nature of lightest slepton)

## No light EWkinos

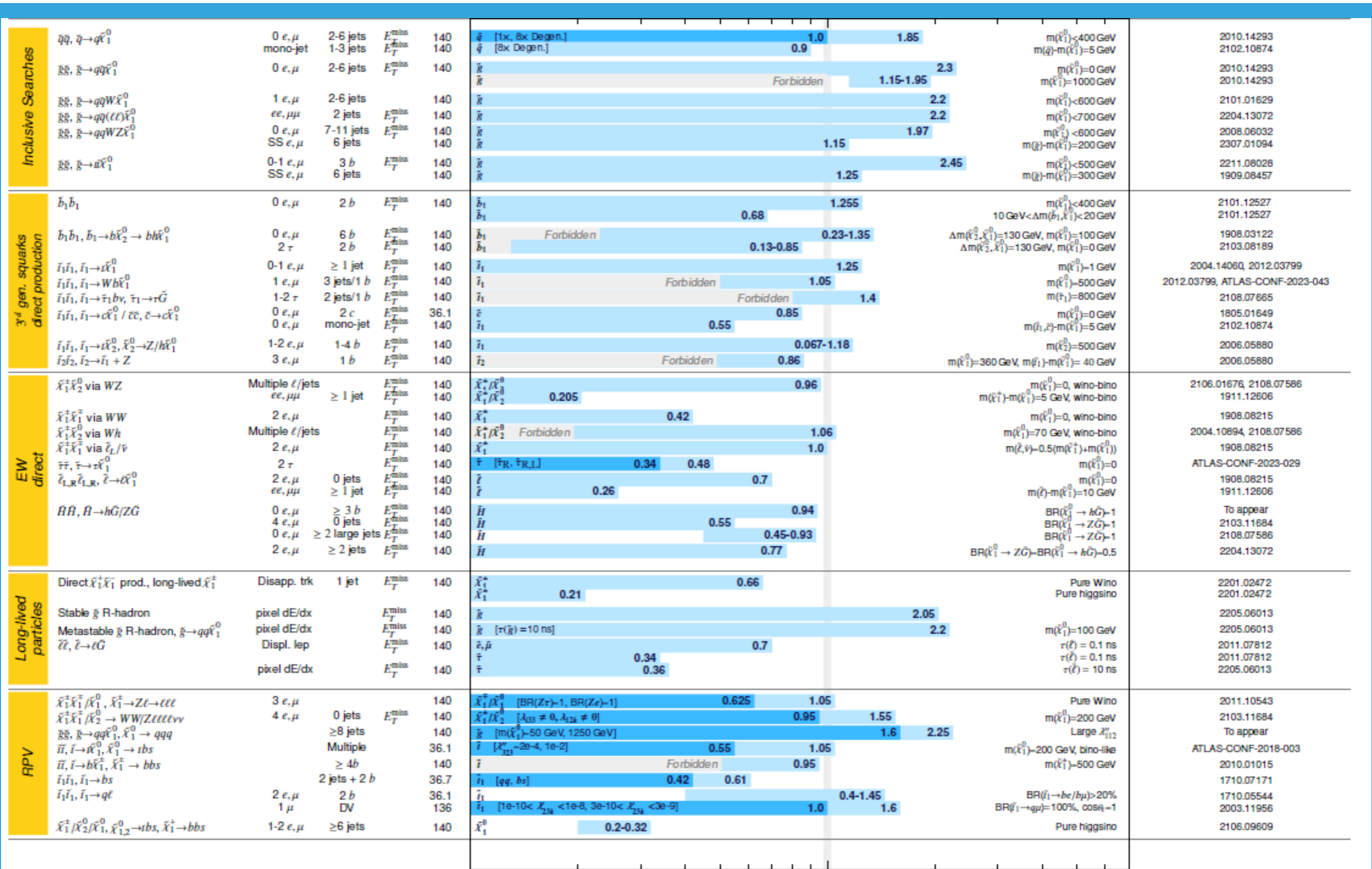


Effect of change in intermediate slepton mass



3l + same-sign 2l

# ATLAS AND CMS LIMITS 2023



\*Only a selection of the available mass limits on new states or phenomena is shown. Many of the limits are based on



## “The non-standard” (Long-Lived Particle) signatures

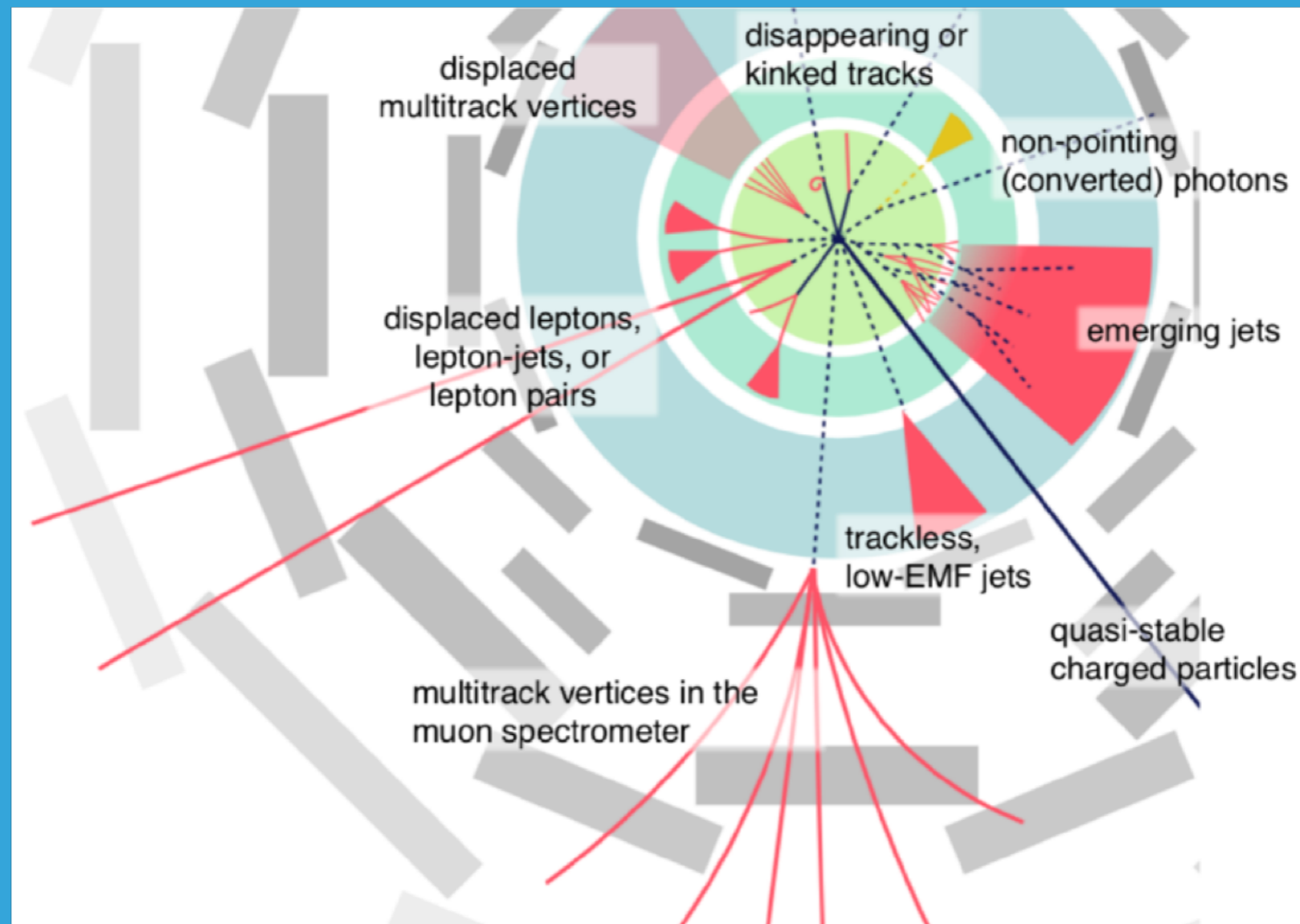
### LLP:

a proper lifetime  $\tau_0$  is greater than or comparable to the characteristic size of the (sub)detectors

✓ small  $\tau_0$  that comparable to the inner tracker size, no displaced tracks → “standard” prompt decay

✓ intermediate  $\tau_0$  → LLP

✓ very large/infinite large  $\tau_0$  → stable particles, “standard” MET signatures

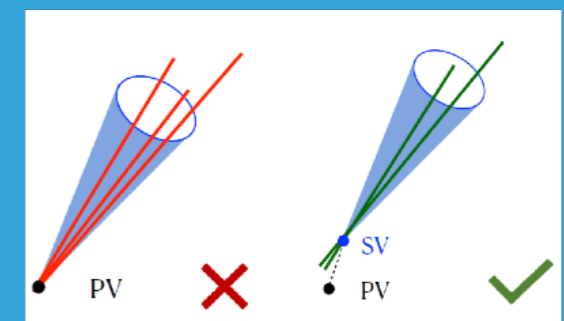
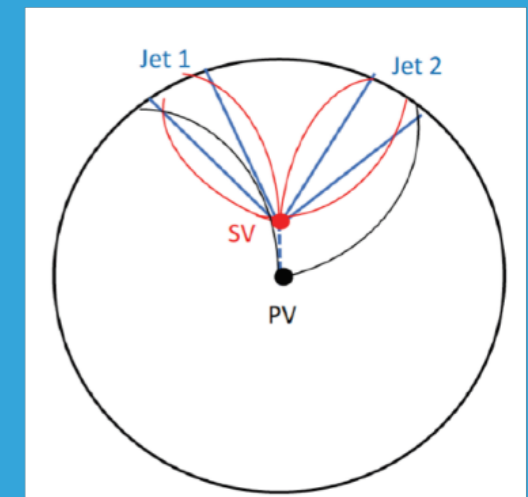


Searching for long-lived particles beyond the Standard Model at the Large Hadron Collider, arXiv:1903.04497

LLP White Paper:  
arXiv:1903.04497

LLP theory motivations:  
arXiv:1806.07396

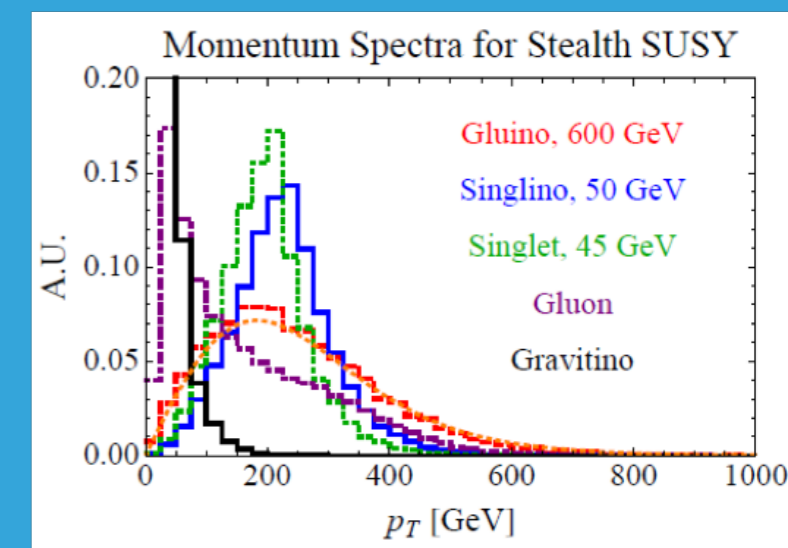
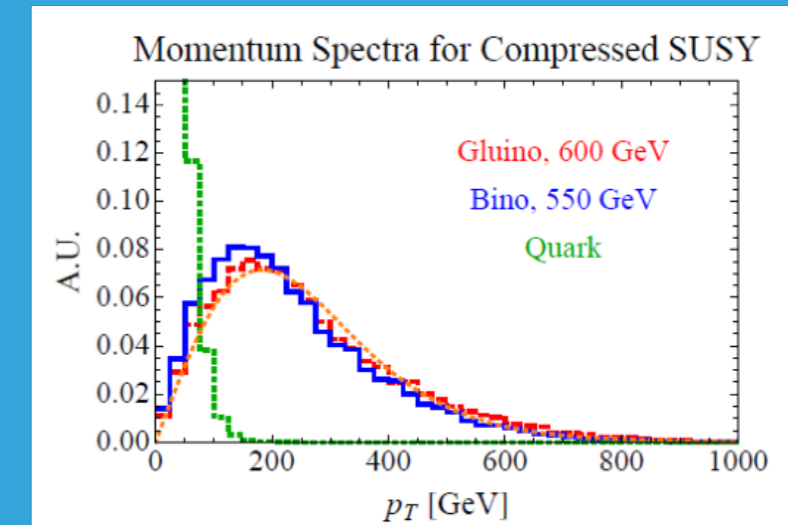
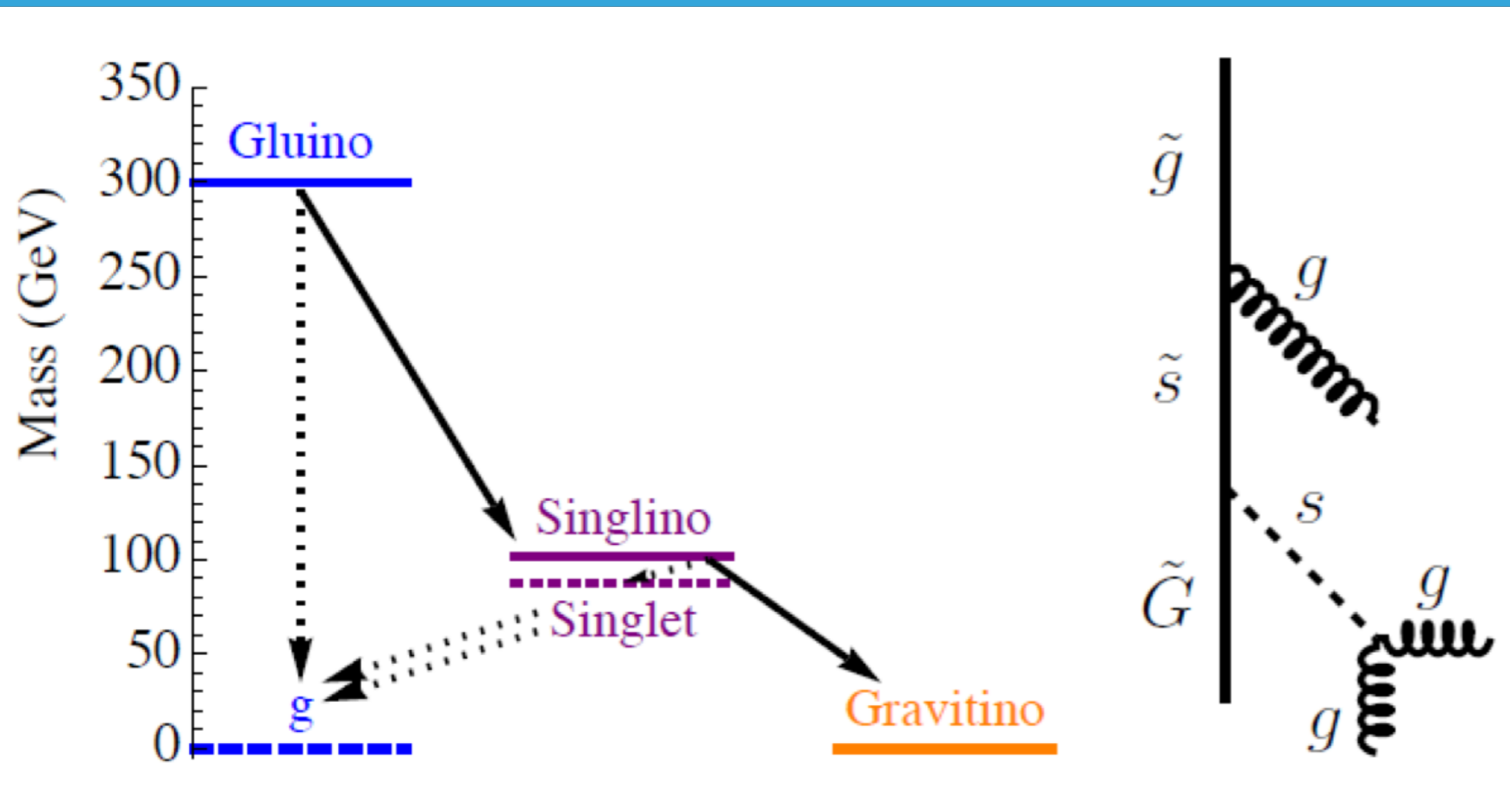
displaced jets/leptons



# Stealth supersymmetry model

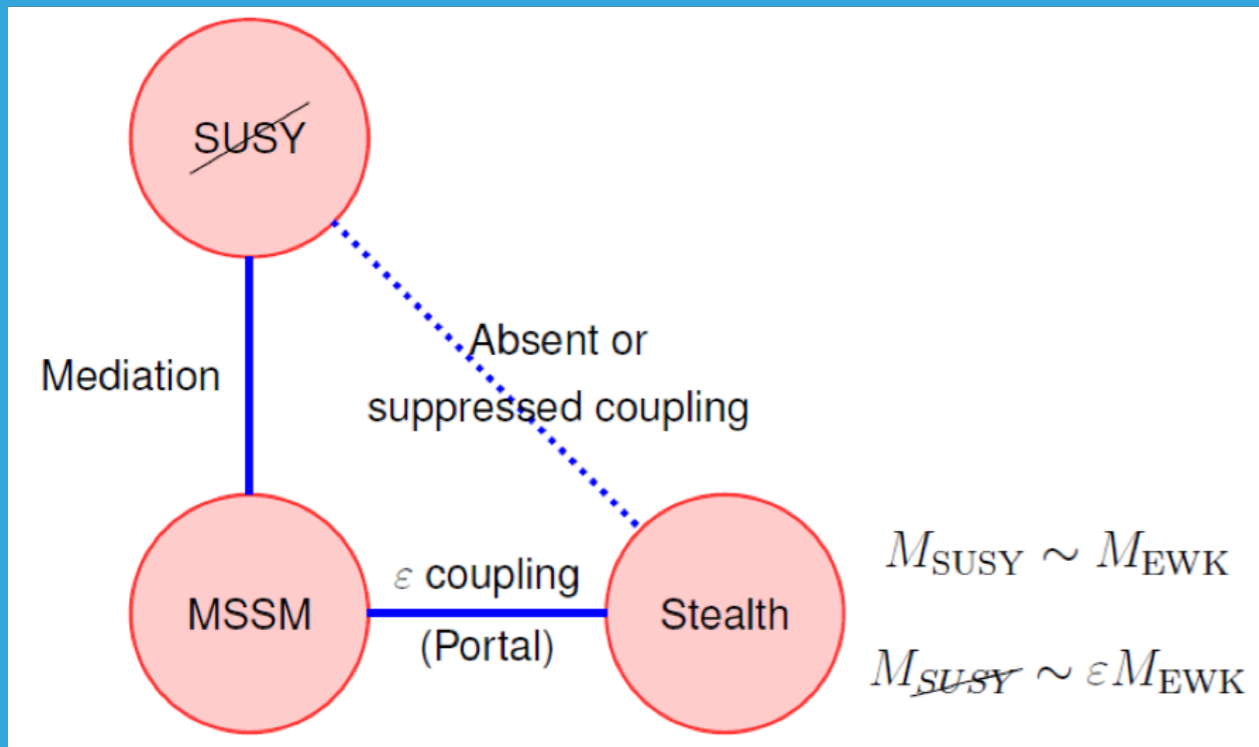
## Stealth supersymmetry idea

SUSY is natural, low-scale SUSY breaking, hidden sector with one chiral singlet superfield (singlino/singlet). The lightest supersymmetric particle – gravitino (GMSB), LOSP decay to gravitino through a hidden sector. R-odd singlino, R-even singlet. Masses in a hidden sector of order the EW scale, states approximately supersymmetric – mass splitting is much smaller than masses, states are **closely degenerated by masses**. Suppression of large missing  $E_T$  (connected with gravitino).





## Stealth supersymmetry idea



SUSY breaking – low-scale vs high-scale (large soft mass contributions to the stealth sector),  $m_{X_1 X_2}$

Soft SUSY\_breaking B-term (or  $M_{Pl}$  suppression in SUGRA)

$$\mathcal{L} \supset \int d^2\theta m (1 + \theta^2 m_{3/2}) X_1 X_2 \supset m_{3/2} m X_1 X_2$$

$$\delta m = m - \sqrt{m^2 - B} \approx \frac{B}{2m}$$

splitting of about 10 GeV,

$$B = m_{3/2} m \quad \longrightarrow \quad m_{3/2} \lesssim 2\delta m \lesssim 20 \text{ GeV}$$

Stealth masses of about the EW scale – accident or common underlying physics? **Small  $B_\mu$ /dynamically generated masses**

GMSB decay width

$$\Gamma(\tilde{g} \rightarrow g\tilde{G}) = \frac{m_{\tilde{g}}^5}{48\pi M^2 m_{\tilde{G}}^2} = 1.1 \times 10^{-9} \text{ GeV} \left( \frac{m_{\tilde{g}}}{250 \text{ GeV}} \right)^5 \left( \frac{m_{\tilde{G}}}{1 \text{ eV}} \right)^{-2}$$

will be modified by new hidden sector

SUSY is certainly a compelling candidates of BSM physics, so we should keep searching for her without leaving any stone unturned.

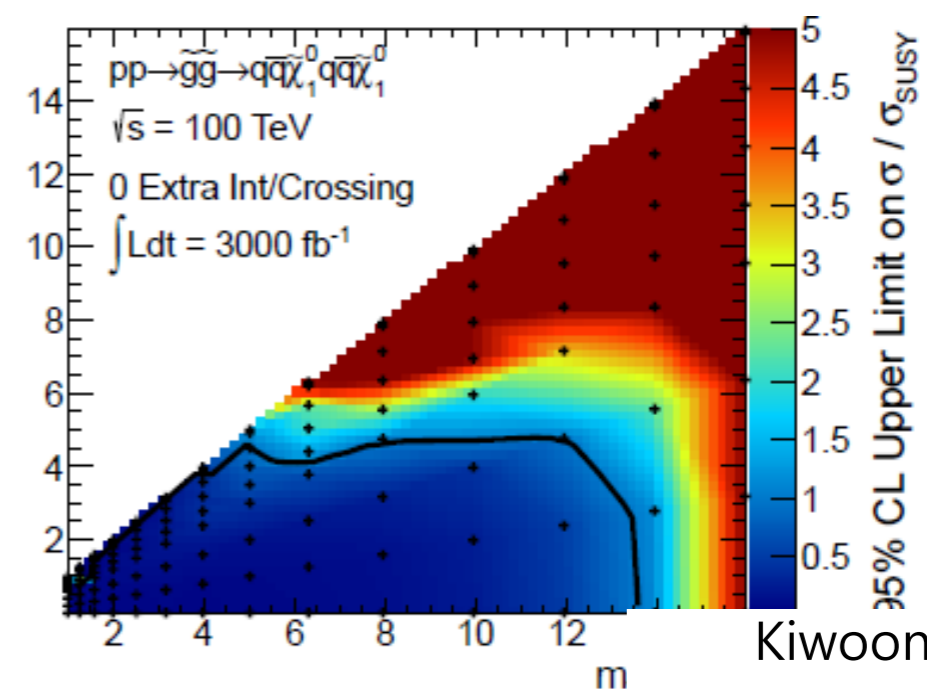
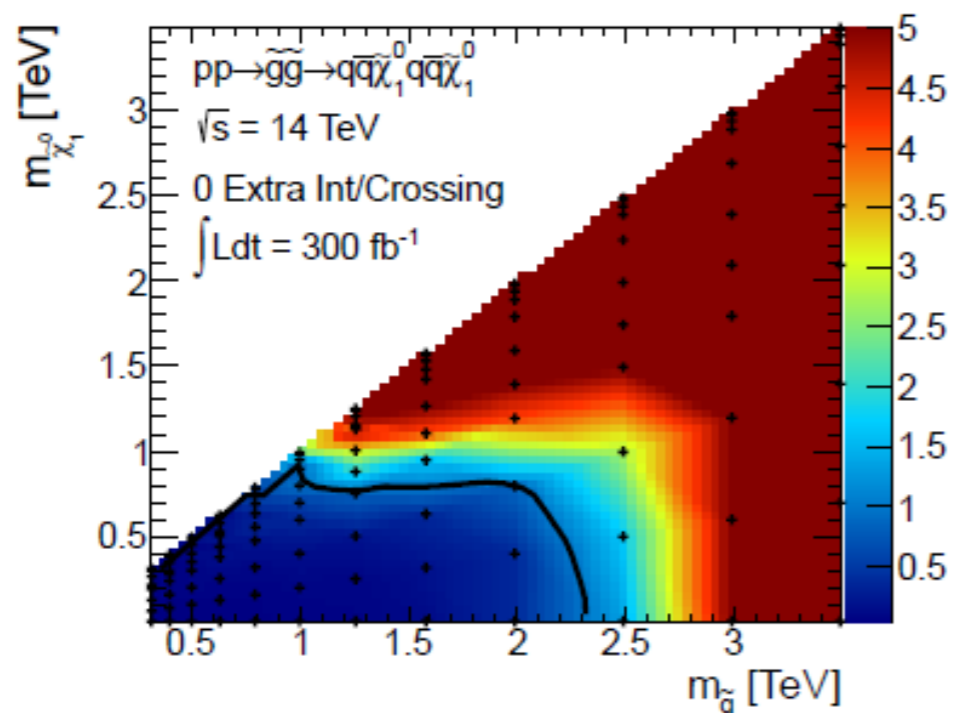


\* Taking the gauge coupling unification seriously, SUSY may have some chance to be seen at LHC, and a good chance at the FCC:

High luminosity LHC

Cohen et al, '13

100 TeV collider

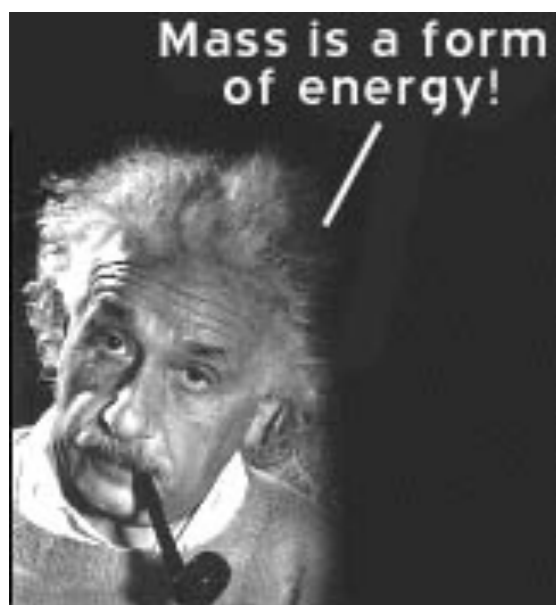
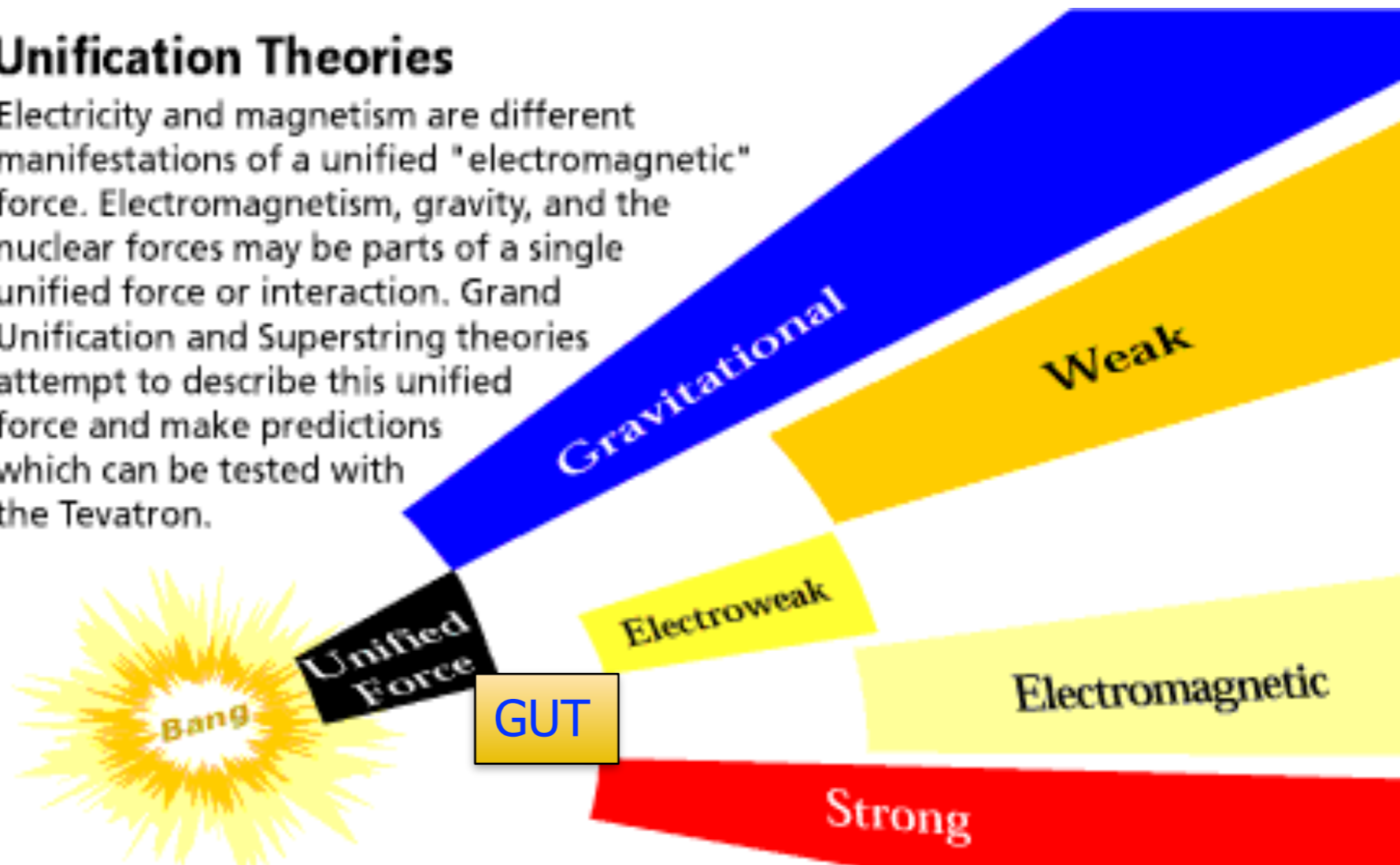


Kiwoon Choi

(ICHEP 2016, Chicago)

## Unification Theories

Electricity and magnetism are different manifestations of a unified "electromagnetic" force. Electromagnetism, gravity, and the nuclear forces may be parts of a single unified force or interaction. Grand Unification and Superstring theories attempt to describe this unified force and make predictions which can be tested with the Tevatron.



$10^{-34}$  cm



D=10

- Unification of strong, weak and electromagnetic interactions within Grand Unified Theories is a new step in unification of all forces of Nature
- Creation of a unified theory of everything based on string paradigm seems to be possible

## NEW SYMMETRIES



## GRAND UNIFICATION

Grand Unification is an extension of the Gauge symmetry of the SM

	Low energy		$\Rightarrow$	High energy
$SU_c(3) \otimes$	$SU_L(2) \otimes$	$U_Y(1)$	$\Rightarrow$	$G_{GUT}$ (or $G^n$ + discrete symmetry)
gluons	$W, Z$	photon	$\Rightarrow$	gauge bosons
quarks	leptons		$\Rightarrow$	fermions
$g_3$	$g_2$	$g_1$	$\Rightarrow$	$g_{GUT}$

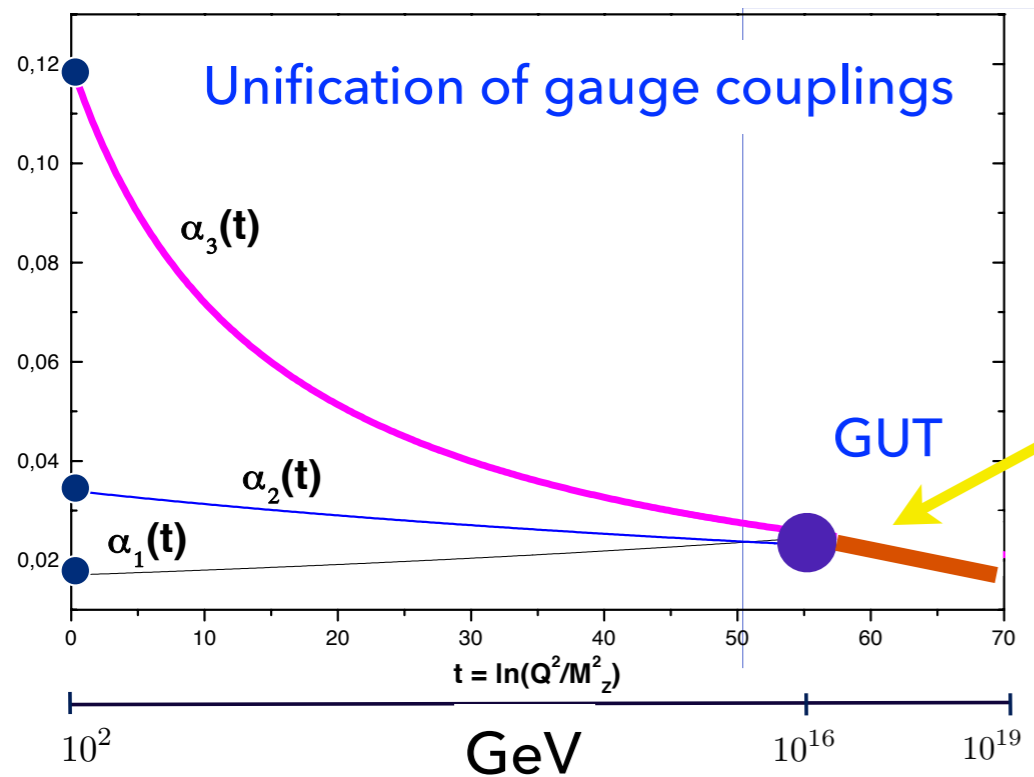
# NEW SYMMETRIES



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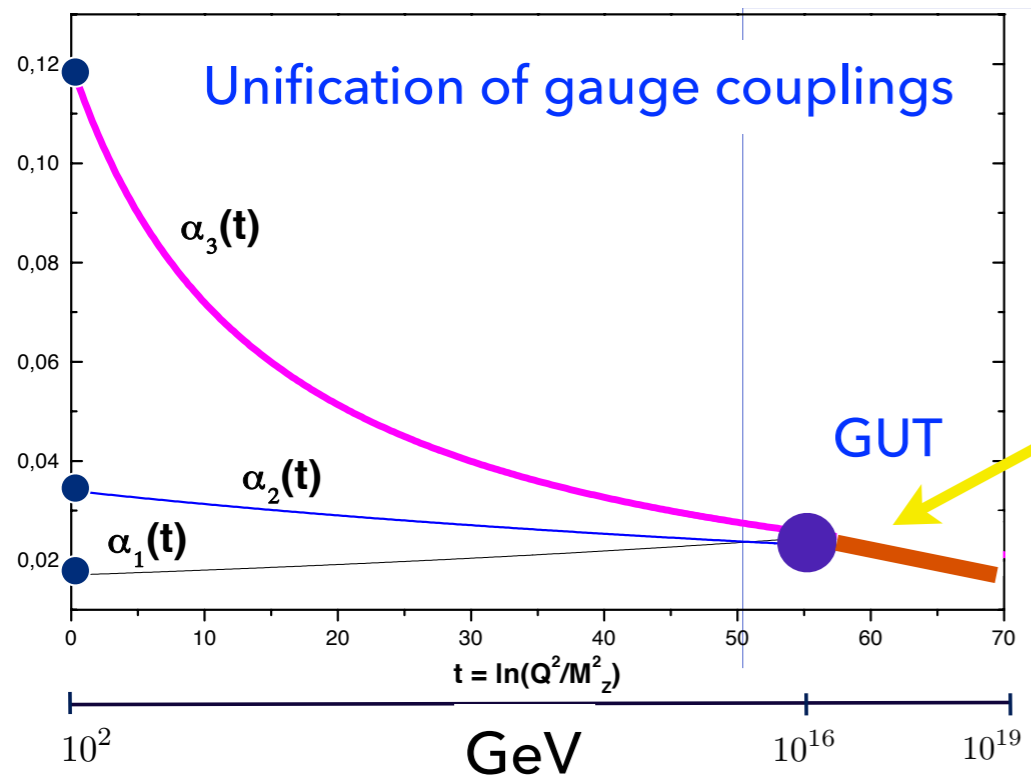
# NEW SYMMETRIES



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$g_3$	$g_2$	$g_1$	$\Rightarrow$	$g_{GUT}$



$$SU(3) \times SU(2) \times U(1) \subset G_{GUT}$$

Ex :  $SU(5), SO(10), E(6), SU(5) \times U(1),$   
 $SU(4) \times SU(2) \times SU(2), SO(10) \times U(1)$

## SU(5) - Minimal GUT

### Gauge fields

$$\underline{24} = (\underline{8}, \underline{1}) + (\underline{1}, \underline{3}) + (\underline{3}, \underline{2}) + (\underline{3}, \underline{2})$$

*gluons      W and Z      leptoquarks*

$$\left( \begin{array}{ccc} & & \vdots \\ & SU_c(3) & \vdots \\ & & \vdots \\ \dots & \dots & \dots \\ X & X & X \\ Y & Y & Y \end{array} \right) \begin{array}{l} X \\ Y \\ X \\ Y \\ \dots \\ SU_L(2) \\ \dots \end{array}$$

$$SU(5) : \bar{5} + 10 + 1$$

$$\underline{5}^* = (d_1^c, d_2^c, d_3^c, e^-, \nu_e)_{Left} \quad \underline{10} = \left( \begin{array}{c} 0 \\ u_3^c \\ 0 \\ u_1^c \\ 0 \\ u_2 \\ u_3 \\ 0 \\ d_1 \\ d_2 \\ d_3 \\ e^+ \\ 0 \end{array} \right)_{Left} \quad 1 = \nu_L^c$$

## SU(5) - Minimal GUT

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$$\underline{24} = (\underline{8}, \underline{1}) + (\underline{1}, \underline{3}) + (\underline{3}, \underline{2}) + (\underline{3}, \underline{2})$$

*gluons      W and Z      leptiquarks*

$$\left( \begin{array}{ccc|cc} & & & \vdots & X & Y \\ & & & \vdots & X & Y \\ & & & \vdots & X & Y \\ \dots & \dots & \dots & \vdots & \dots & \dots \\ X & X & X & \vdots & SU_L(2) & \\ Y & Y & Y & \vdots & & \end{array} \right)$$

$$SU(5) : \bar{5} + 10 + 1$$

$$\underline{5}^* = (d_1^c, d_2^c, d_3^c, e^-, \nu_e)_{Left} \quad \underline{10} = \left( \begin{array}{ccccc} 0 & u_3^c & -u_2^c & u_1 & d_1 \\ & 0 & u_1^c & u_2 & d_2 \\ & & 0 & u_3 & d_3 \\ & & & 0 & e^+ \\ & & & & 0 \end{array} \right)_{Left} \quad 1 = \nu_L^c$$

## SO(10) - Optimal GUT

### Matter fields - just one representation

$$\underline{16} = (u_1 \ u_2 \ u_3 \ d_1 \ d_2 \ d_3 \ \nu_e \ e^- \ u_1^c \ u_2^c \ u_3^c \ d_1^c \ d_2^c \ d_3^c \ \nu_e^c \ e^+)_{Left}$$

### SU(5) decomposition

$$\underline{16} = \underline{5}^* + \underline{10} + \underline{1} \quad \text{fermions,}$$

$$\underline{45} = \underline{24} + \underline{10} + \underline{10}^* + \underline{1} \quad \text{gauge bosons}$$



GUT symmetry is broken spontaneously by Brout-Englert-Higgs Mechanism

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SU(5)

Higgs Multiplets  $SU(5) \xrightarrow{\Sigma} SU(3) \times SU(2) \times U(1) \xrightarrow{H} SU(3) \times U(1)$

$$\langle \Sigma_{24} \rangle = \begin{pmatrix} V & & & & \\ & V & & & \\ & & V & & \\ & & & -3/2 V & \\ & & & & -3/2 V \end{pmatrix}$$

$$V \sim 10^{15} \text{ GeV}$$

$$\langle H_5 \rangle = \begin{pmatrix} 0 \\ 0 \\ 0 \\ 0 \\ v/\sqrt{2} \end{pmatrix}$$

$$v \sim 10^2 \text{ GeV}$$

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## SO(10)

Higgs Multiplets 16 or 126; 45 or 54 or 210

$$SO(10) \begin{array}{l} \nearrow \\ M_1 \\ \searrow \end{array} \begin{array}{l} SU(5) \xrightarrow{M_2} SU(3) \otimes SU(2) \otimes U(1) \xrightarrow{M_W} SU(3) \otimes U(1) \\ SO(6) \otimes SO(4) \sim SU(4) \otimes SU_L(2) \otimes SU_R(2) \end{array}$$

$$M_1 \gg M_2 \gg \dots M_W$$

## Solves many problems of the SM:

- absence of Landau pole
- Decreases the number of parameters
- All particles in a single representation (**16** of SO(10))
- Unifies quarks and leptons -> spectrum and mixings from «textures»
- A way to **B** and **L** violation

## Creates new problems:

- Hierarchy of scales  $M_W/M_G \sim 10^{-14}$
- Large Higgs sector is needed for GUT symmetry breaking

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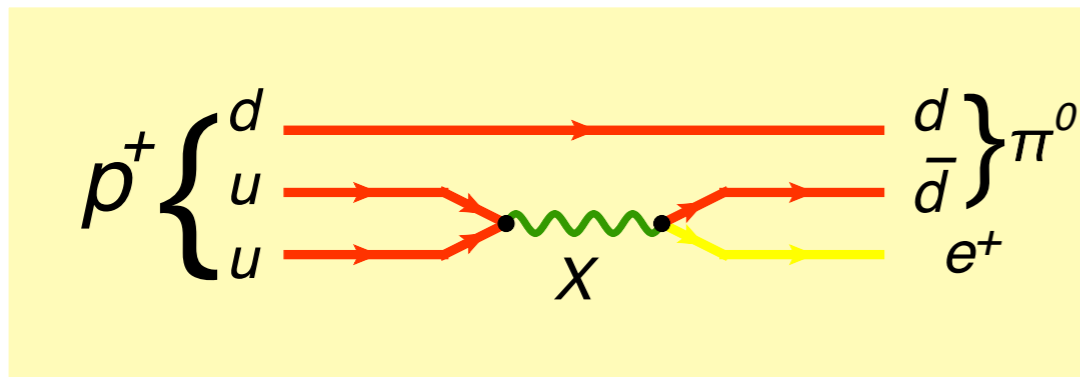
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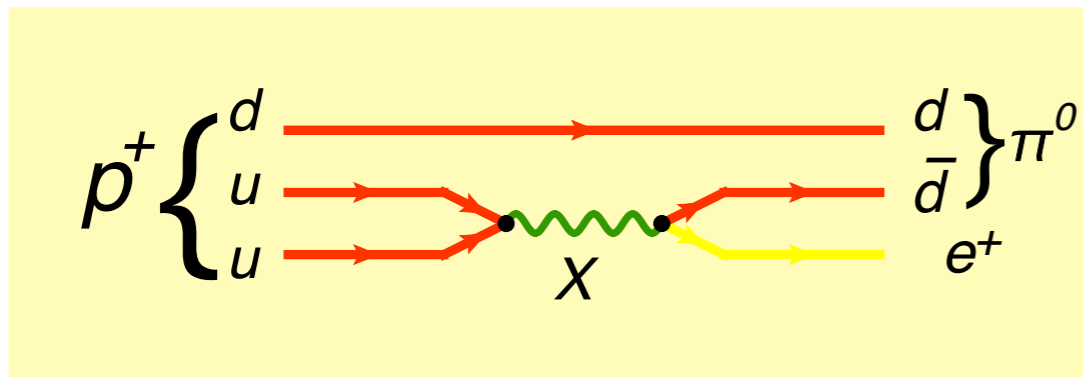
## Crucial predictions:

- Proton decay  $P \rightarrow e^+ \pi, P \rightarrow \bar{\nu} K^+$
- Neutron-antineutron oscillations
- $|\Delta(B - L)| = 1$  ( $|\Delta(B - L)| = 2$ ) processes



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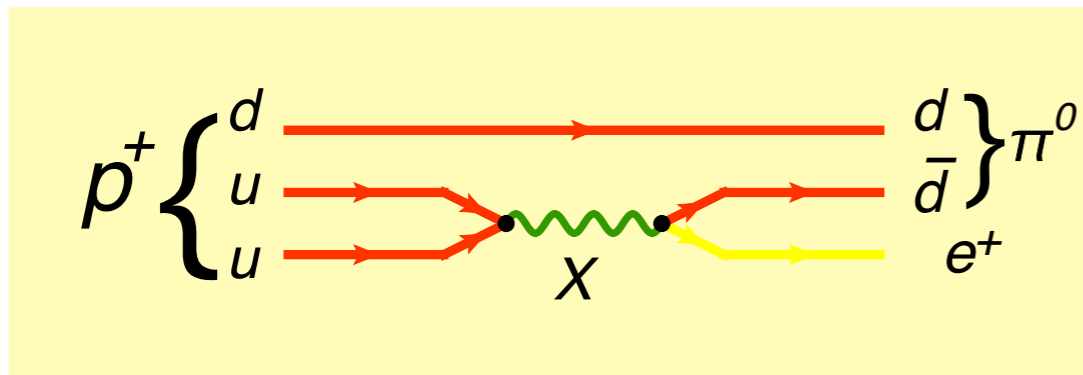
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mean life time  $> 10^{31} - 10^{33}$  years

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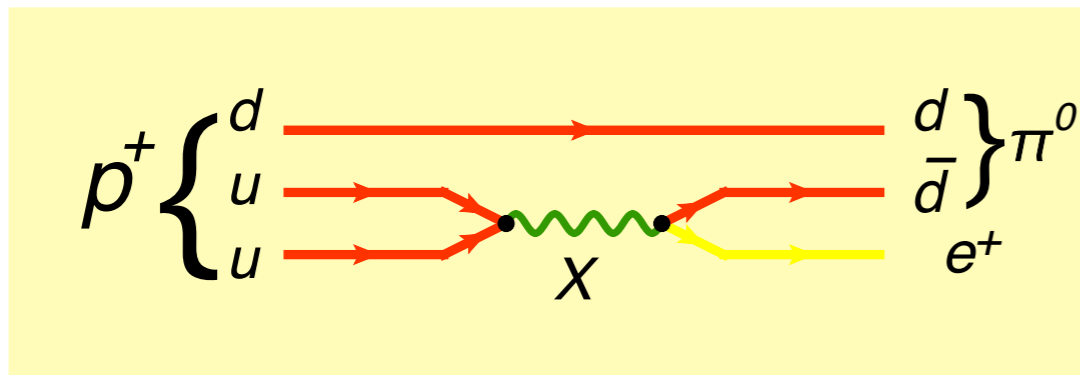
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$$\tau_{Universe} \approx 14 \cdot 10^9 \text{ years}$$

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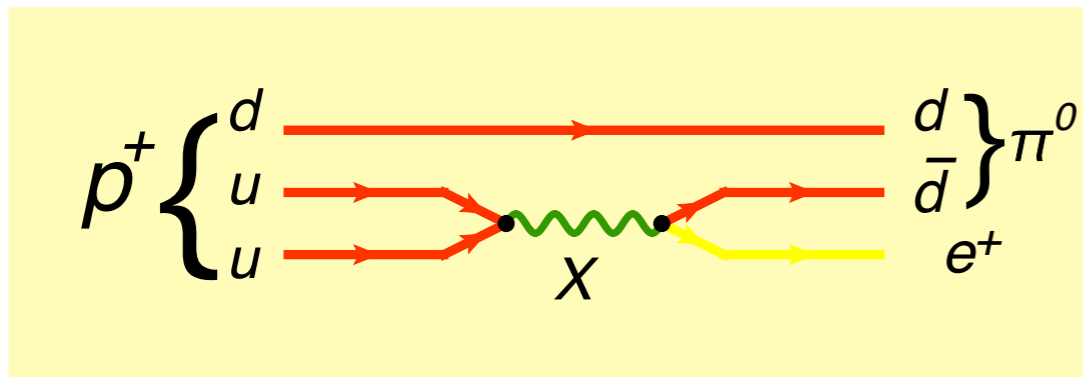
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Low energy SUSY

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- SUSY leads to unification
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## New properties:

- Later unification - higher GUT scale
- Longer proton life-time  $\tau \sim M_{GUT}^4$
- New modes of proton decay

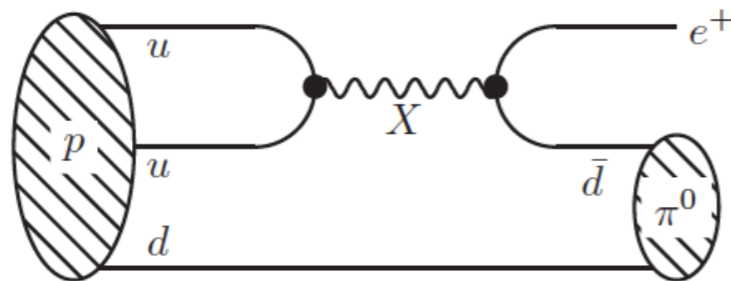
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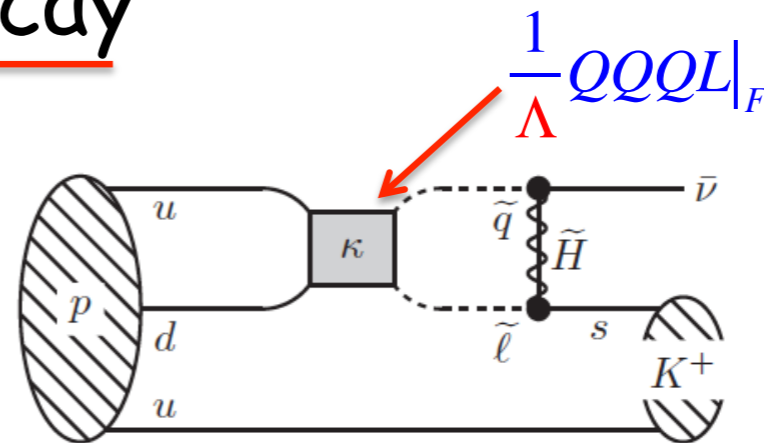
## SUSY GUTS - Nucleon decay



(a) Dimension 6.

$$p \rightarrow \pi^0 + e^+$$

$$\tau_{p \rightarrow e^+ \pi^0} > 1 \times 10^{34} \text{ yrs}, M_X > 10^{16} \text{ GeV}$$



(b) Dimension 5.

$$p \rightarrow K^+ + \bar{\nu}$$

$$\tau_{p \rightarrow K^+ \bar{\nu}} > 3.3 \times 10^{33} \text{ yrs}$$

## NEW SYMMETRIES

- Appear in some GUT models
- Inspired by string models

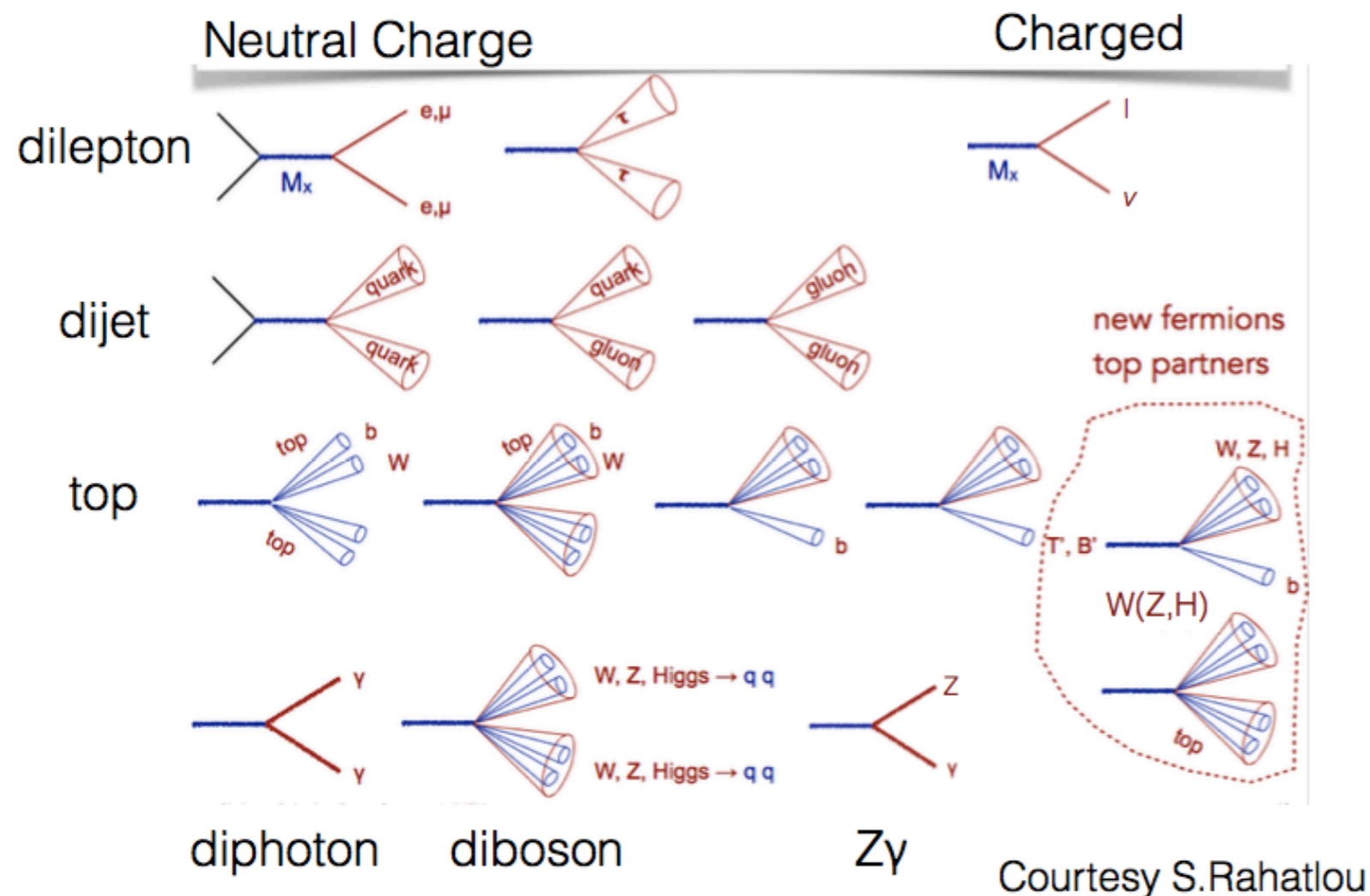
EXTRA  $U(1)'$ ,  $SU(2)'$

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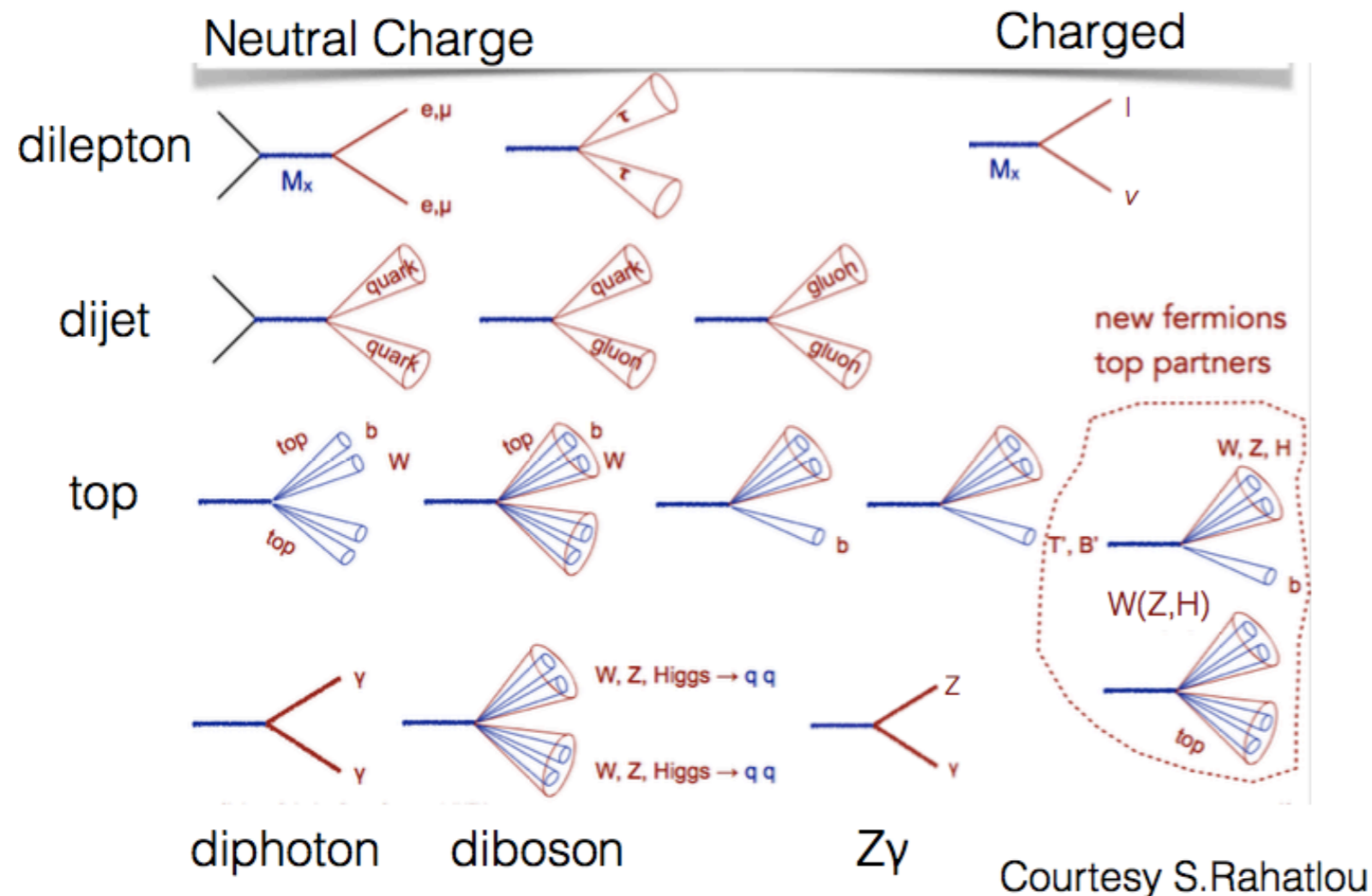
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# EXTRA U(1)', SU(2)'

Used as possible Dark matter candidate - Dark photon



Mixture of a usual EM U(1) photon and a new U(1)' one

$$\mathcal{L} \sim F_{\mu\nu} F'^{\mu\nu}$$

Dedicated experiment to look for conversion of a usual photon into a dark one



# NEW SYMMETRIES

## ADDITIONAL GAUGE BOSONS

### Experiment

- Search for  $Z'$  (Di-muon events)
- Search for  $W'$  (single muon/ jets)
- Search for resonance decaying to  $t$ - $\bar{t}$
- Search for diboson resonances
- Monojets + invisible

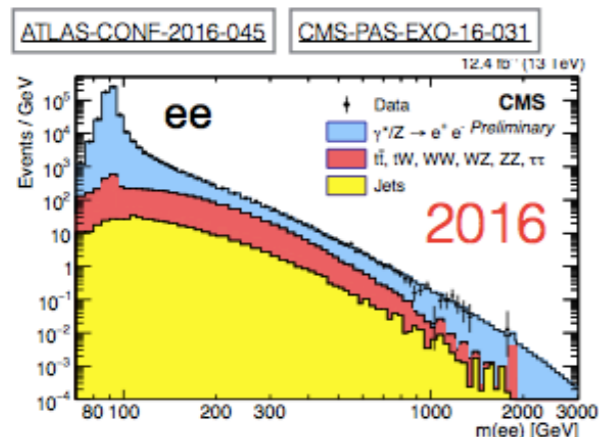
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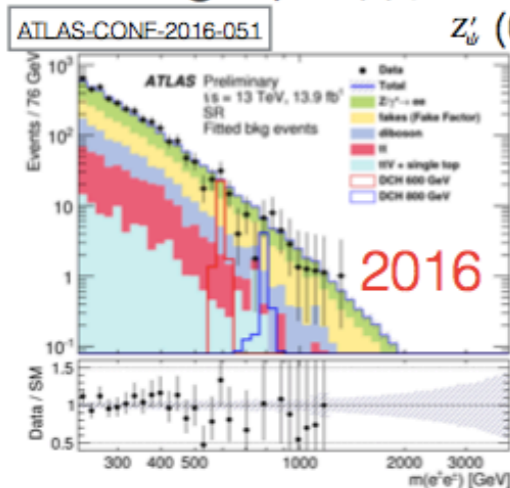
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Same Flavor Opposite Sign ( $ee, \mu\mu, \tau\tau$ )



Same Sign ( $ee, \mu\mu$ )  $Z'_{SSM}(3\% \text{ width}) > 4 \text{ TeV}$

$Z'_\psi (0.5\% \text{ width}) > 3.36 \text{ TeV}$



95% CL  
exclusion limit

$H_R^{\pm\pm} > 420 \text{ GeV}$   
 $H_L^{\pm\pm} > 570 \text{ GeV}$

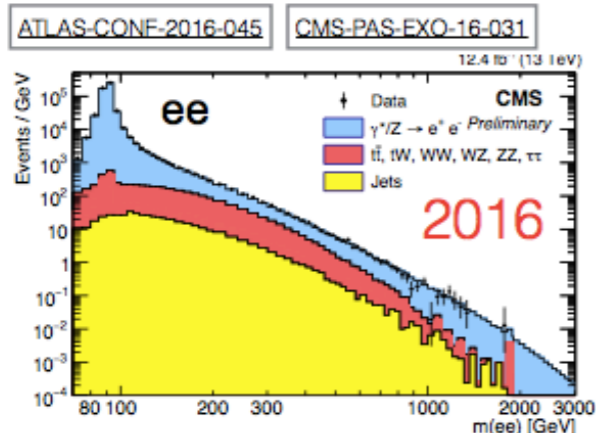
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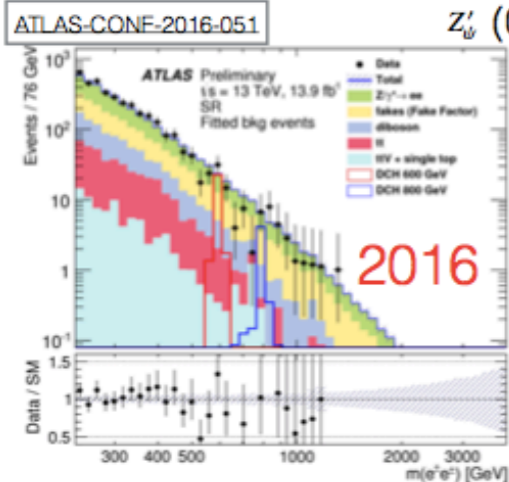
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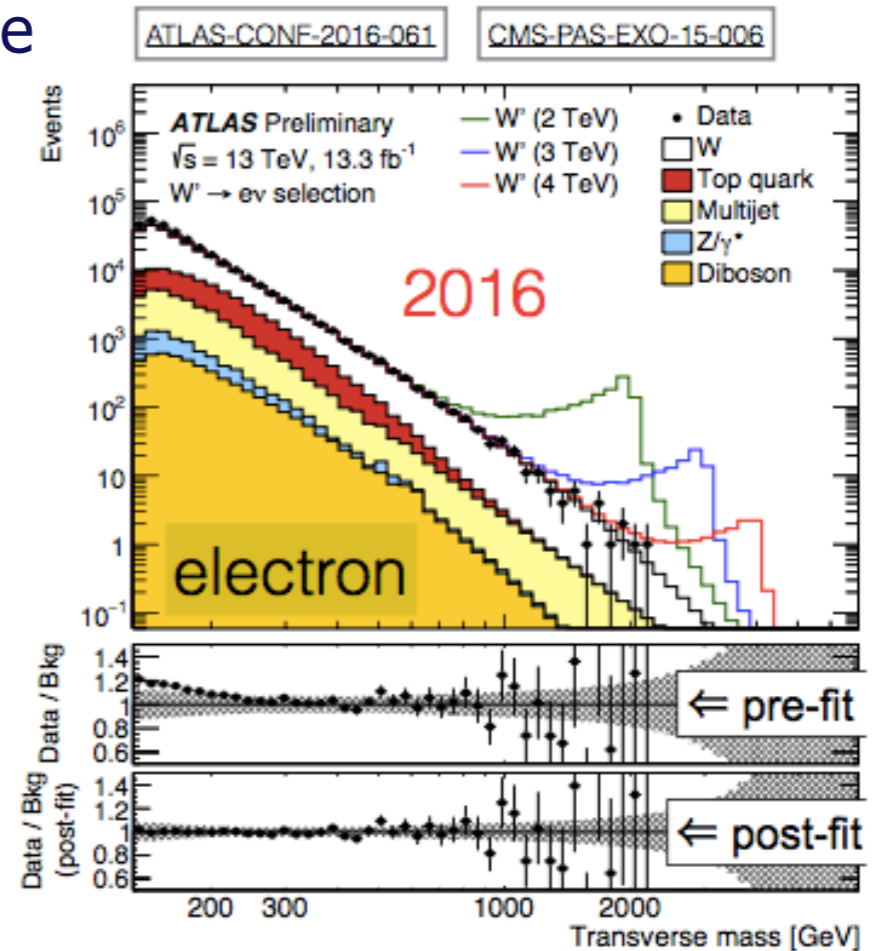


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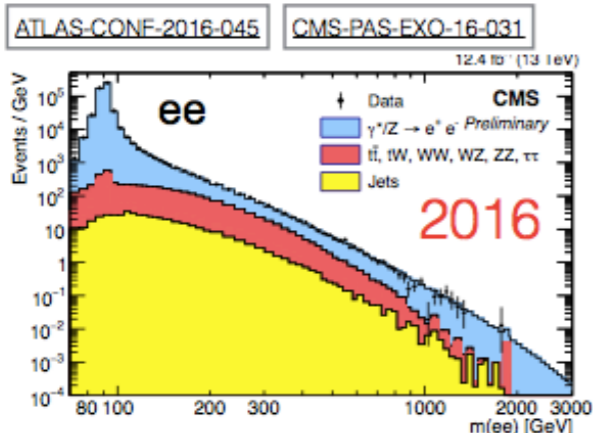
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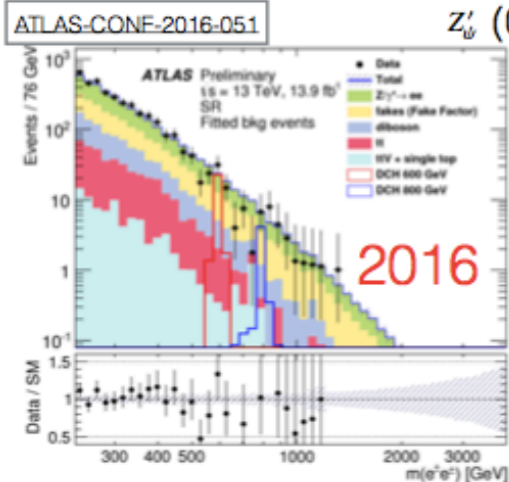
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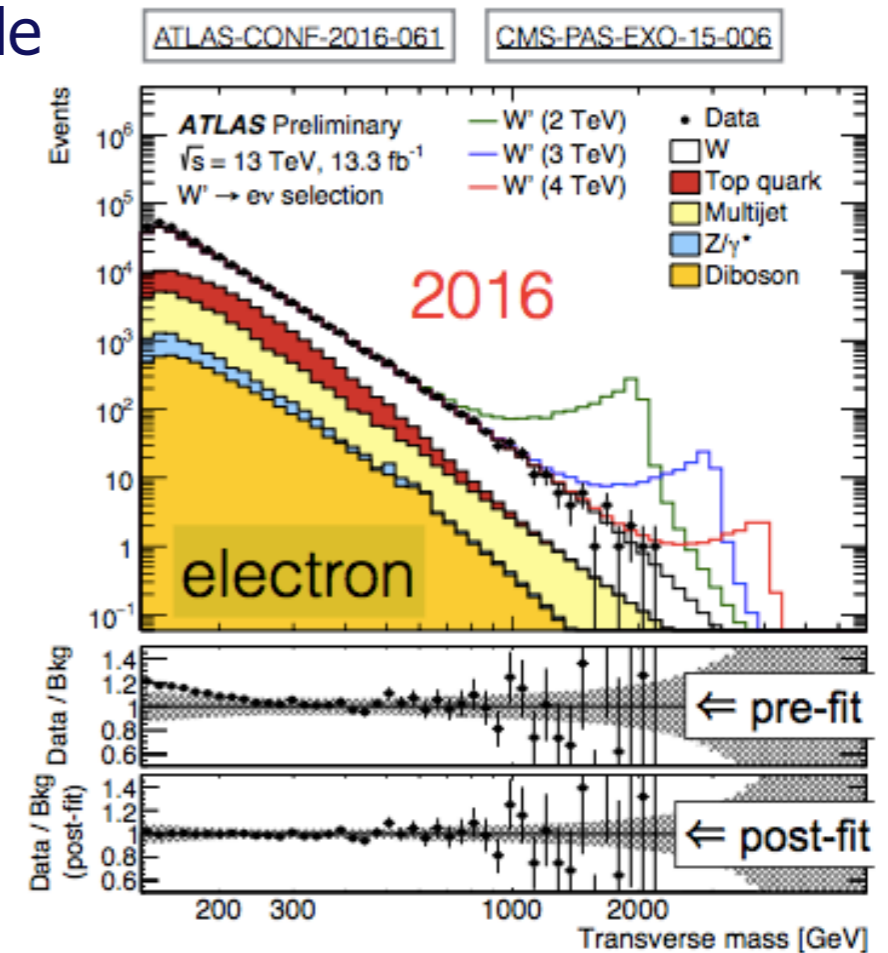


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SSM  $W' > 4.74$  TeV

No indication so far - experimental limits on  $Z'$  and  $W'$  masses around few TeV

## NEW PARTICLES

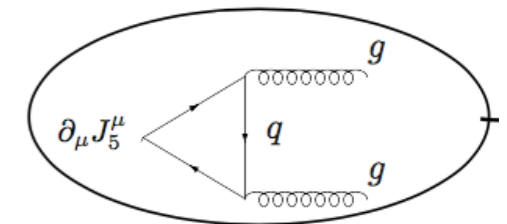
## AXION OR AXION-LIKE PARTICLES

Javier Redondo, EPS HEP 2017

- CP violation in QCD sector: CKM angle  $\delta_{13} = 1.2 \pm 0.1$  rad AND flavour-neutral phase  $\theta = \theta_{\text{QCD}} + N_f \delta$

$$\mathcal{L}_{\text{SM}} \in -\bar{q}_L \begin{pmatrix} m_u e^{i\delta/2} & 0 & \dots \\ 0 & m_d e^{i\delta/2} & \dots \\ 0 & 0 & \dots \end{pmatrix} \begin{pmatrix} u \\ d \\ \dots \end{pmatrix}_R - \frac{\alpha_s}{8\pi} G\tilde{G} \theta_{\text{QCD}}$$

Axial anomaly



# NEW PARTICLES

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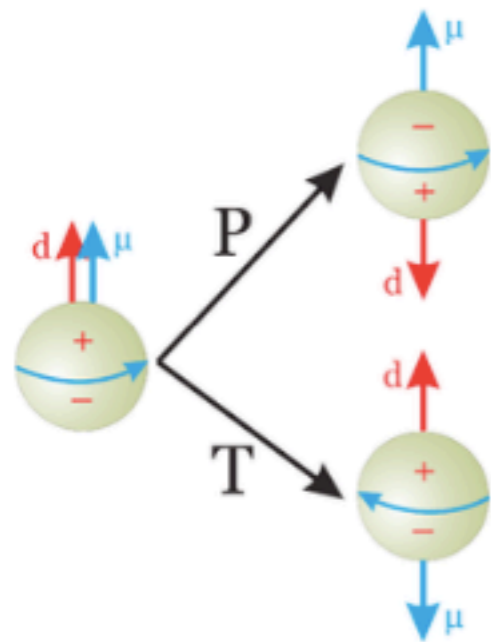
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Axial anomaly

The  $\theta$ -angle produces flavour-neutral CP violation like Electric Dipole Moments



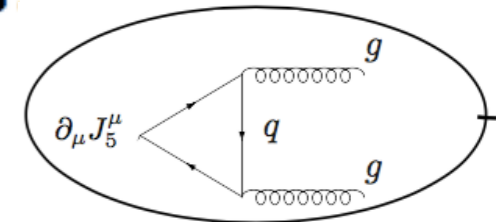
- Neutron EDM (Guo 1502.02295)

$$d_n = -4 \times 10^{-3} \times \theta \text{ [e fm]}$$

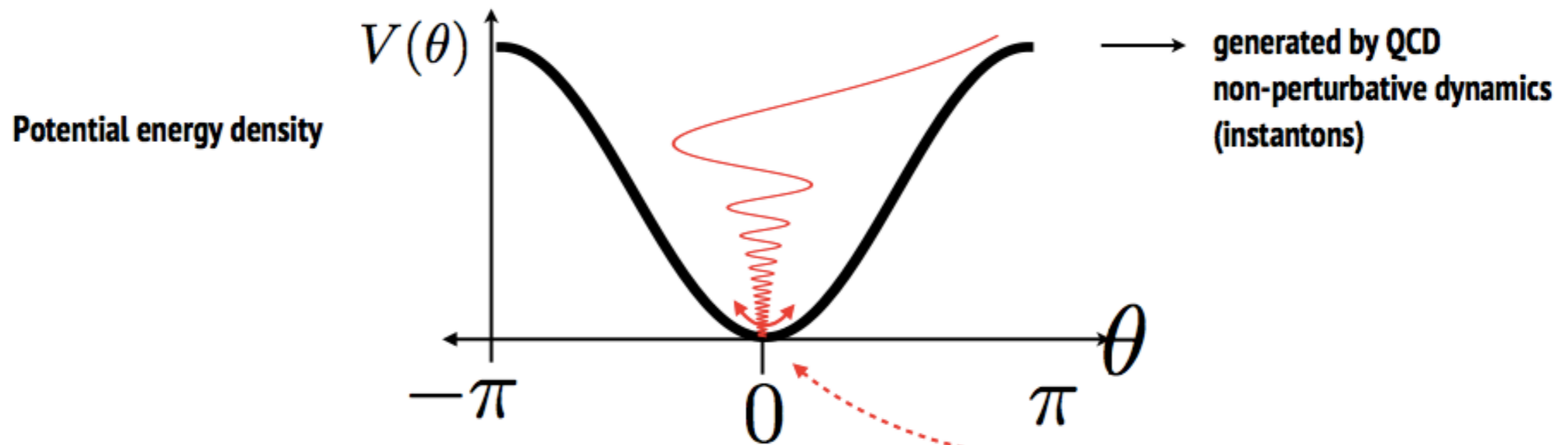
- Experimental upper limit (Grenoble hep-ex/0602020)

$$|d_n| < 3 \times 10^{-13} \text{ [e fm]}$$

- Why is  $\theta < 10^{-10}$ ?



- Any theory promoting  $\theta$  to a dynamical field,  $\theta(t, \mathbf{x})$ , will dynamically set  $\theta \rightarrow 0$  after some time...

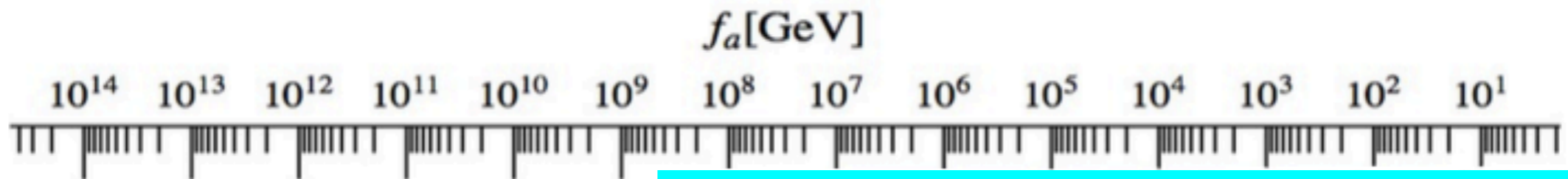


- PQ Mechanism: Global U(1) axial symmetry, spontaneously broken, colour anomalous -> Goldstone boson

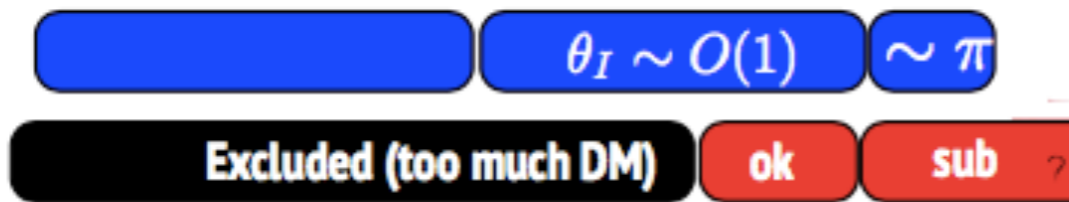
$$\mathcal{L}_\theta = \frac{1}{2}(\partial_\mu\theta)(\partial^\mu\theta)f_a^2 - \frac{\alpha_s}{8\pi}G_{\mu\nu a}\tilde{G}_a^{\mu\nu}\theta$$

New Spontaneous symmetry breaking [energy] scale  $f_a$

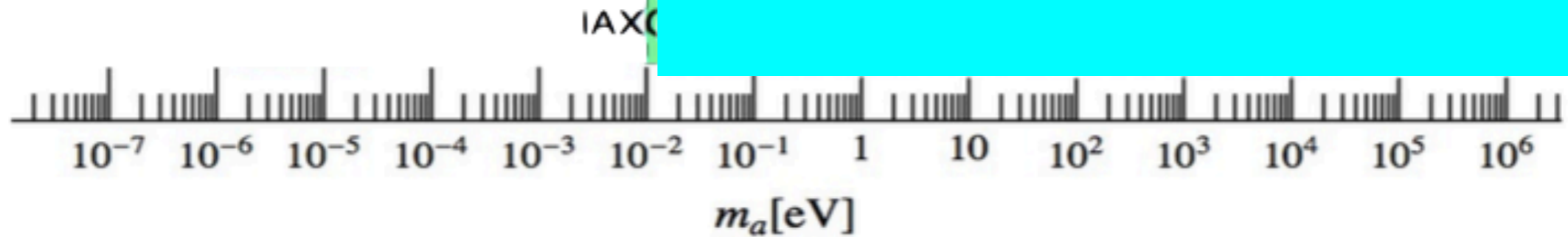
Canonically normalised  $\theta$  field is the QCD AXION!  $a(x) = \theta(x)f_a$



## - Axion DM scenarios



Excluded by Labs+ Astro



- Less minimal axion models have further possibilities ....



# Dark Matter

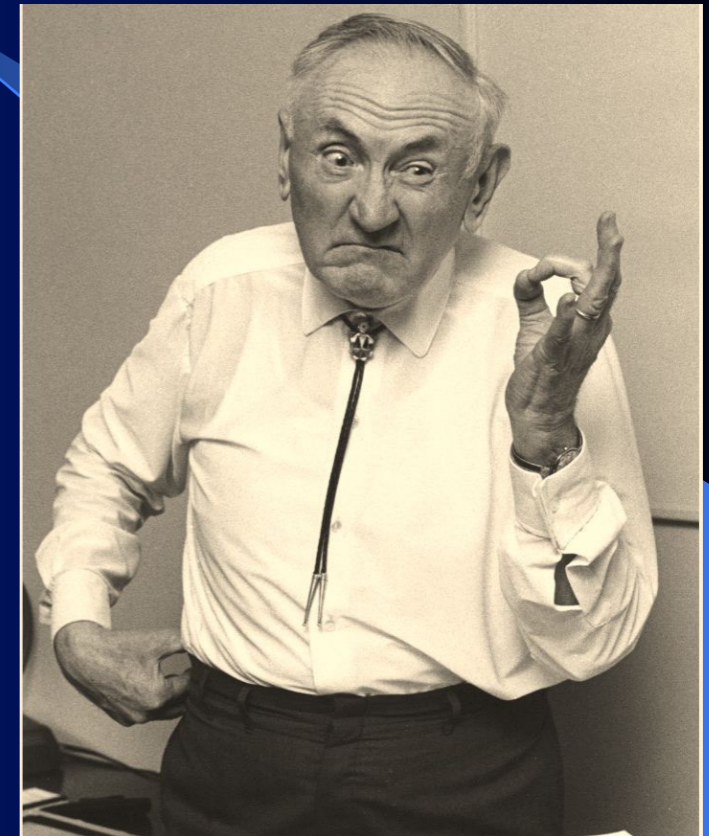
# Three questions

- What is Dark matter and what it is composed of?
- What is the role of Dark matter in the energetic balance of the Universe?
- How to find manifestations of Dark Mater in space, underground and at Large Hadron Collider?

# Gravitational manifestation of existence of Dark matter

## FRITZ ZWICKY

- Swiss Astrophysicist
- Helped to invent Schmidt Telescope
- Helped to discover neutron stars
- Virial theorem of unseen matter: today known as “dark matter”
- Supernovae as yardstick for deep space measurements



Introduced the notions of

- **Supernova and neutron stars**
- **Dark matter (hidden mass)**
- **Gravitational Lensing**

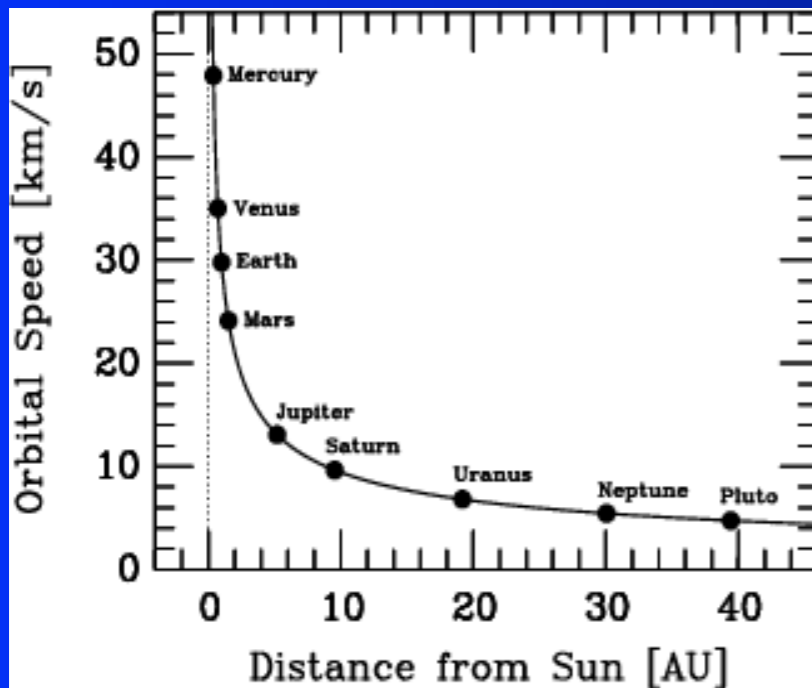
Galactic coaster Coma (1934r.)

# Stars rotation curves

Centrifugal force

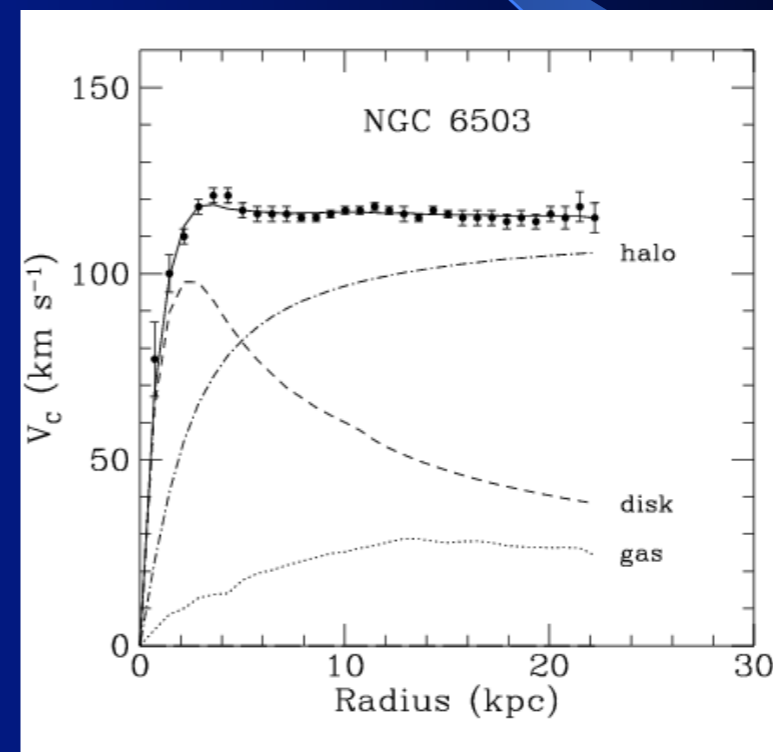
$$\frac{mv^2}{r} = G \frac{mM(r)}{r^2}$$

Gravity



Density of dark matter in Solar system is negligible

Solar system

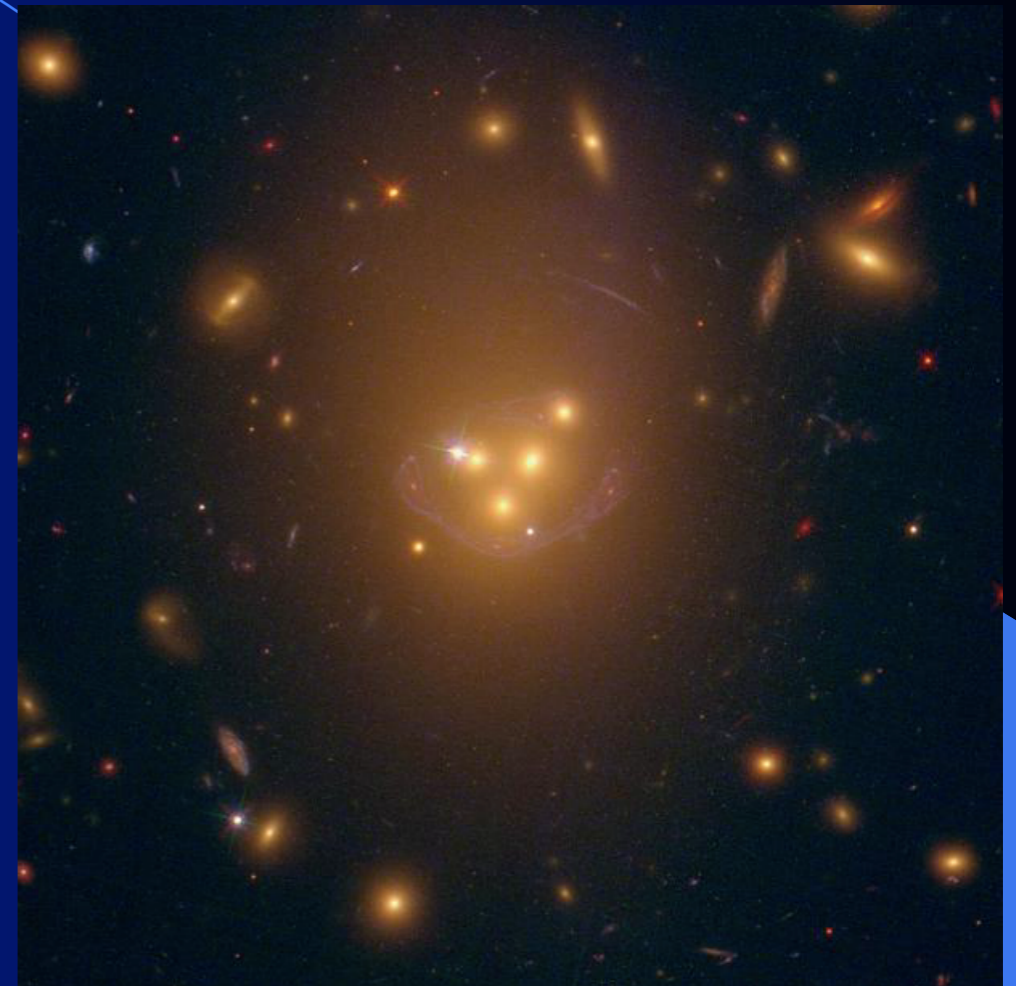
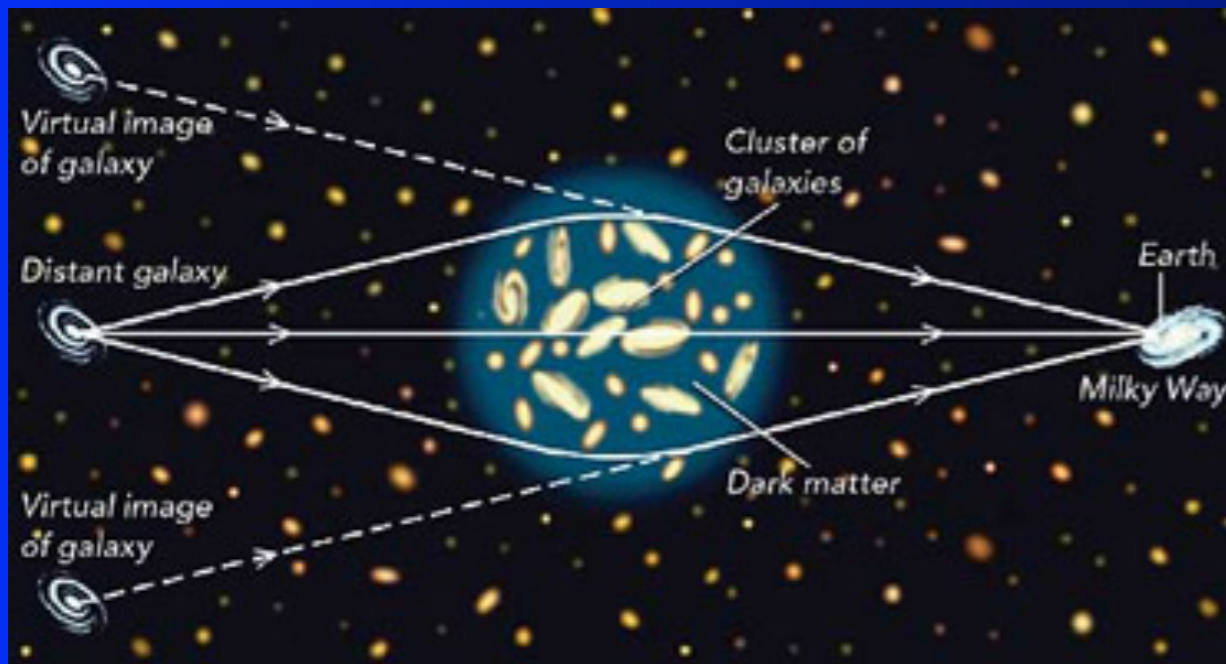


Dark matter is bounded at Galactic scales

Galaxy

- Today we know thousands of rotation curves and all of them indicate in favour of existence of hidden mass in the halo of a Galaxy which is 10 times exceeds the mass of the stars in a disk

# Gravitational Lenses

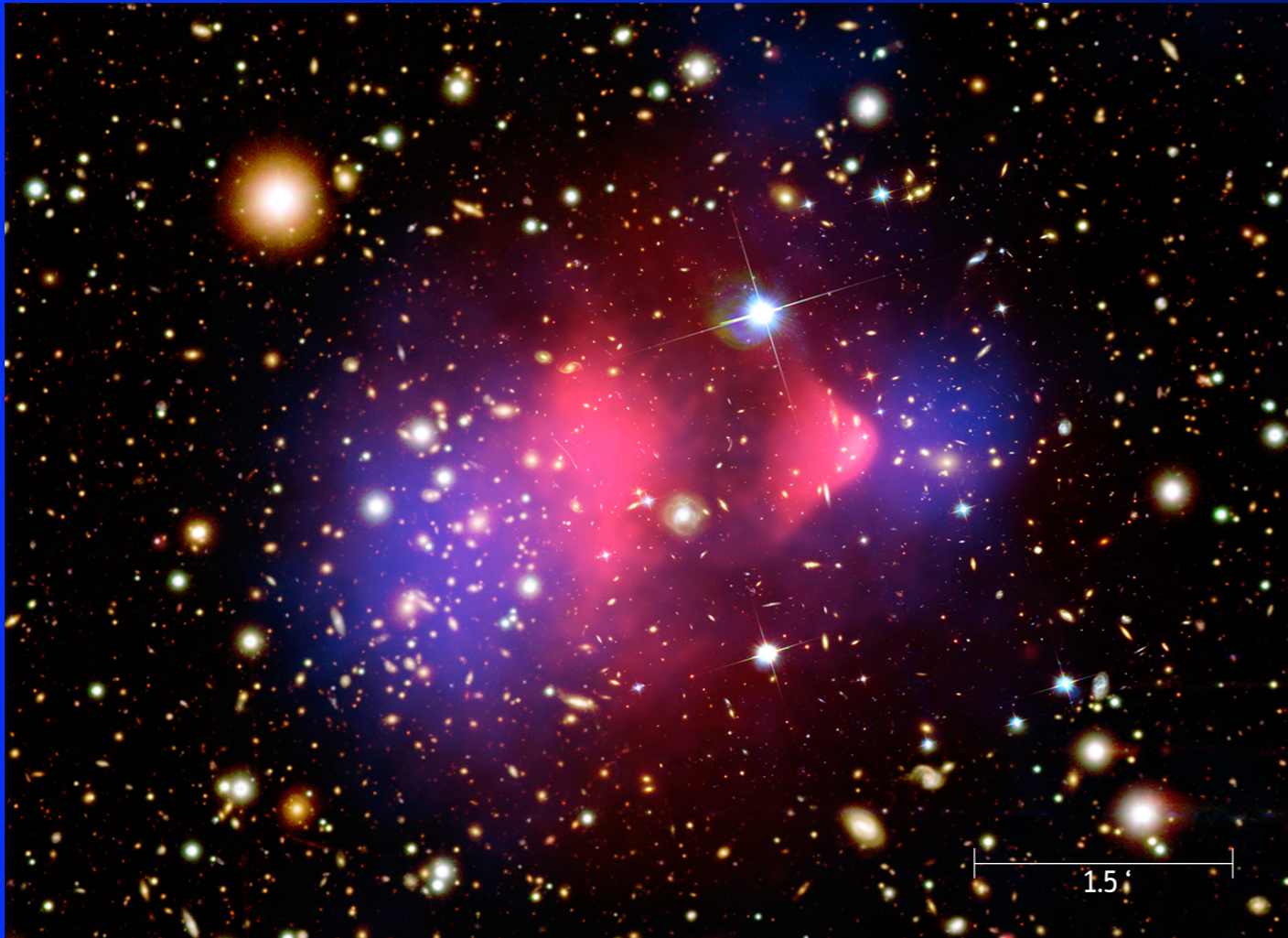


Consequence of GR: deflection of light in gravitational field

The formation of a virtual image of a distant galaxy due to the deflection of light rays by dark matter located between the galaxy and the observer

# Observation of Dark Matter

## Bullet cluster

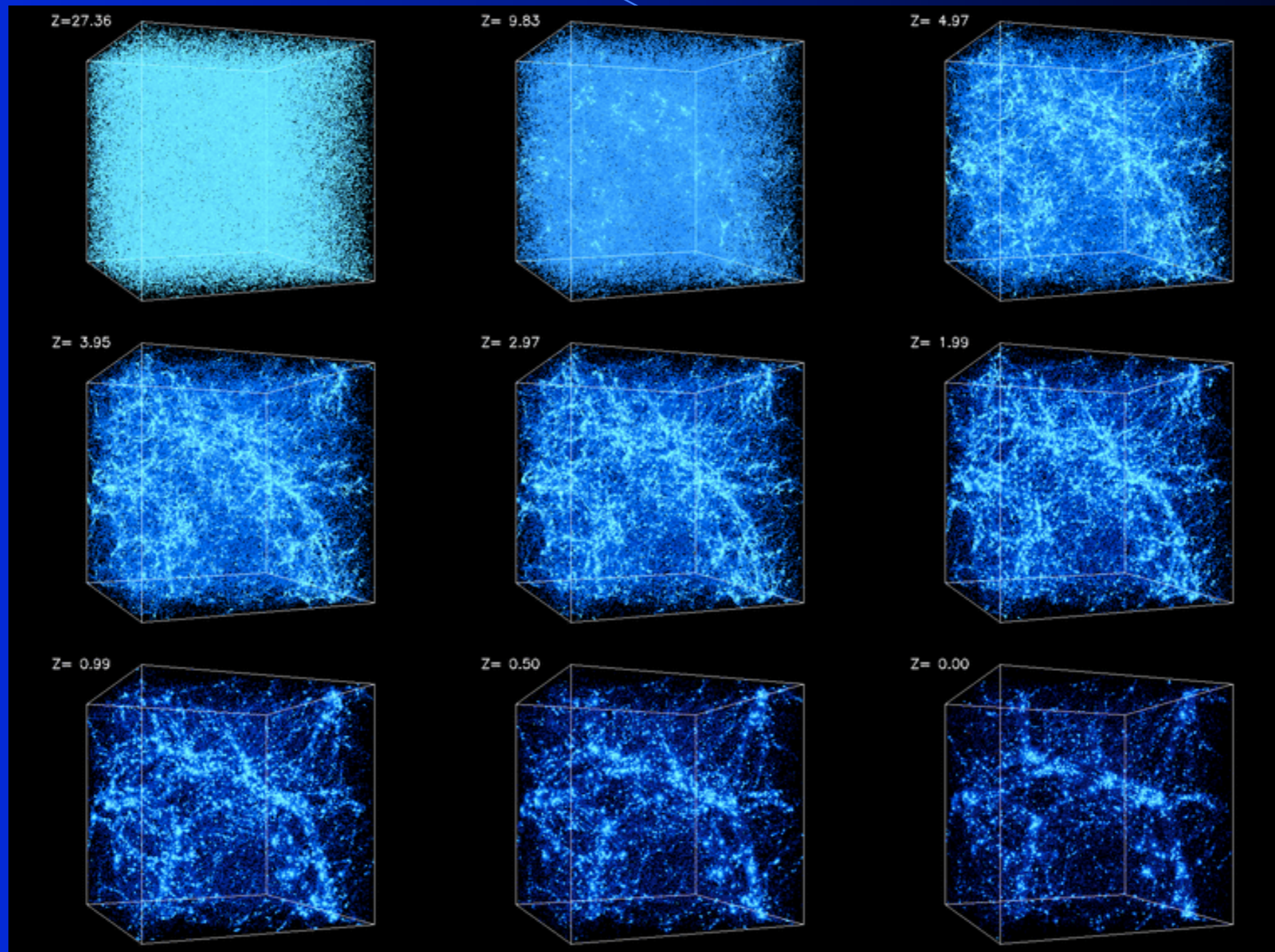


The most direct observational evidence comes from the Bullet cluster. In most regions, dark and visible matter are found together due to their gravitational pull. In the Bullet cluster, they have diverged due to past collisions between two small clusters. Electromagnetic interactions between the gas particles led to a concentration of gas near the impact site.

X-ray observations show that most of the luminous matter is concentrated in the center of the cluster. Gravitational lensing shows that dark matter is located outside the central region. Unlike galactic rotation curves, these proofs are independent of the details of Newtonian gravity, directly supporting the dark matter hypothesis.

The mass distribution reconstructed from strong and weak gravitational lensing is shown in blue, the X-ray emission of hot gas observed by the Chandra telescope is shown in red.

# The formation of large-scale structures in the Universe



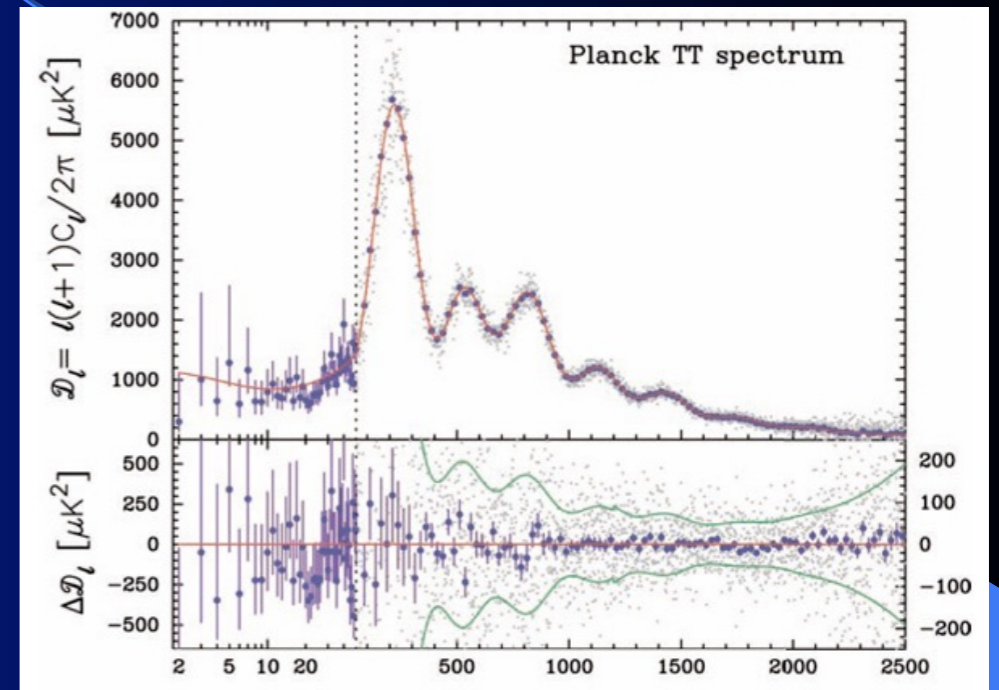
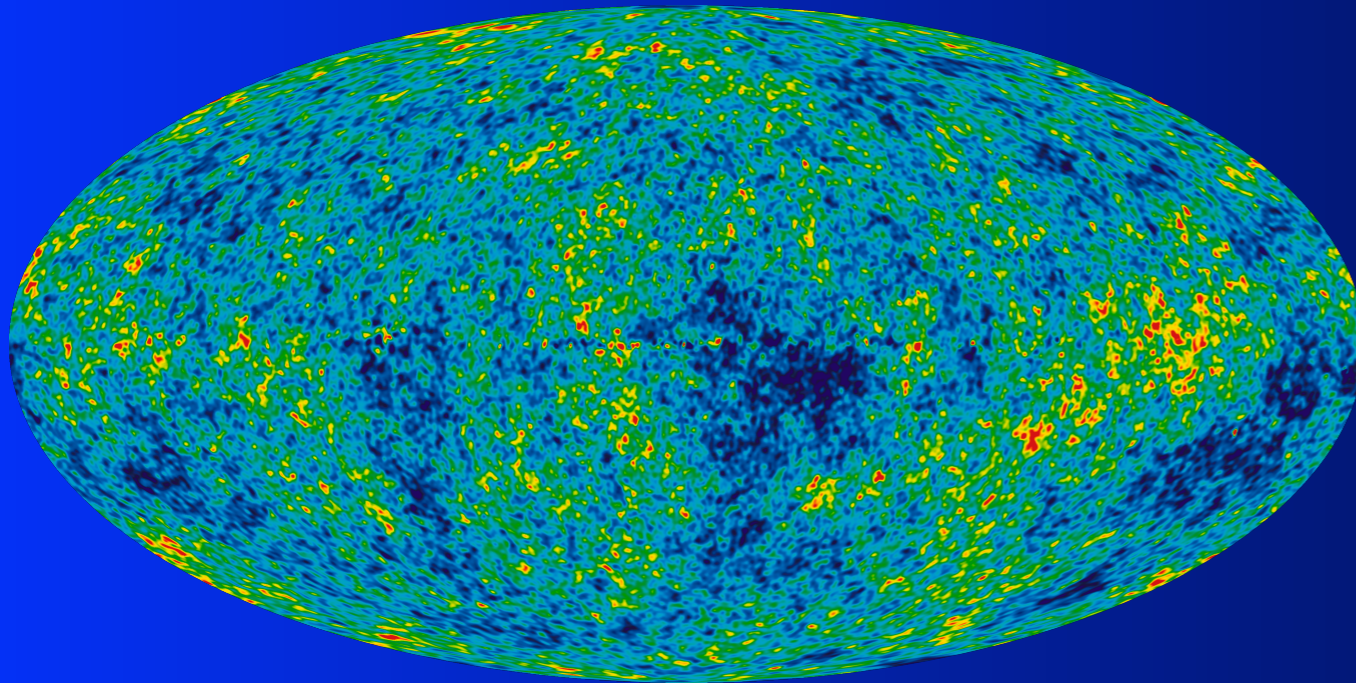
First, the formation of structures from dark matter occurs, and then the concentration of ordinary matter occurs in the gravitational potential formed by dark matter

# Cosmic Microwave Background

Map of CMB

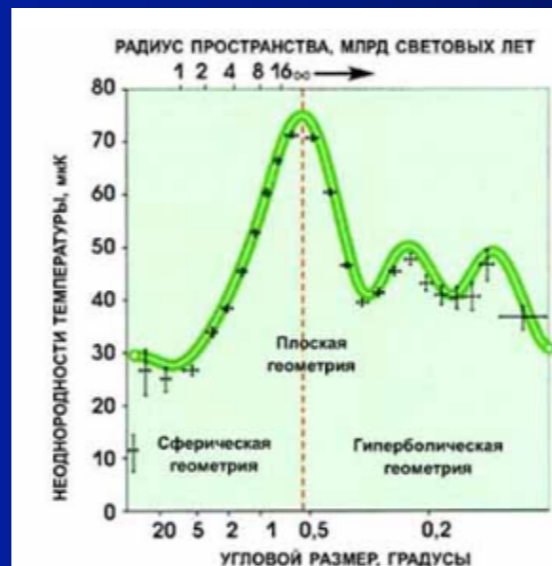
$$T \approx 2.7K^{\circ}$$

Angular harmonics expansion



Temperature fluctuations of CMB

$$\frac{\Delta T}{T} \sim 10^{-5}$$



$$\Omega_{UsualMatter} = 4.9\%$$

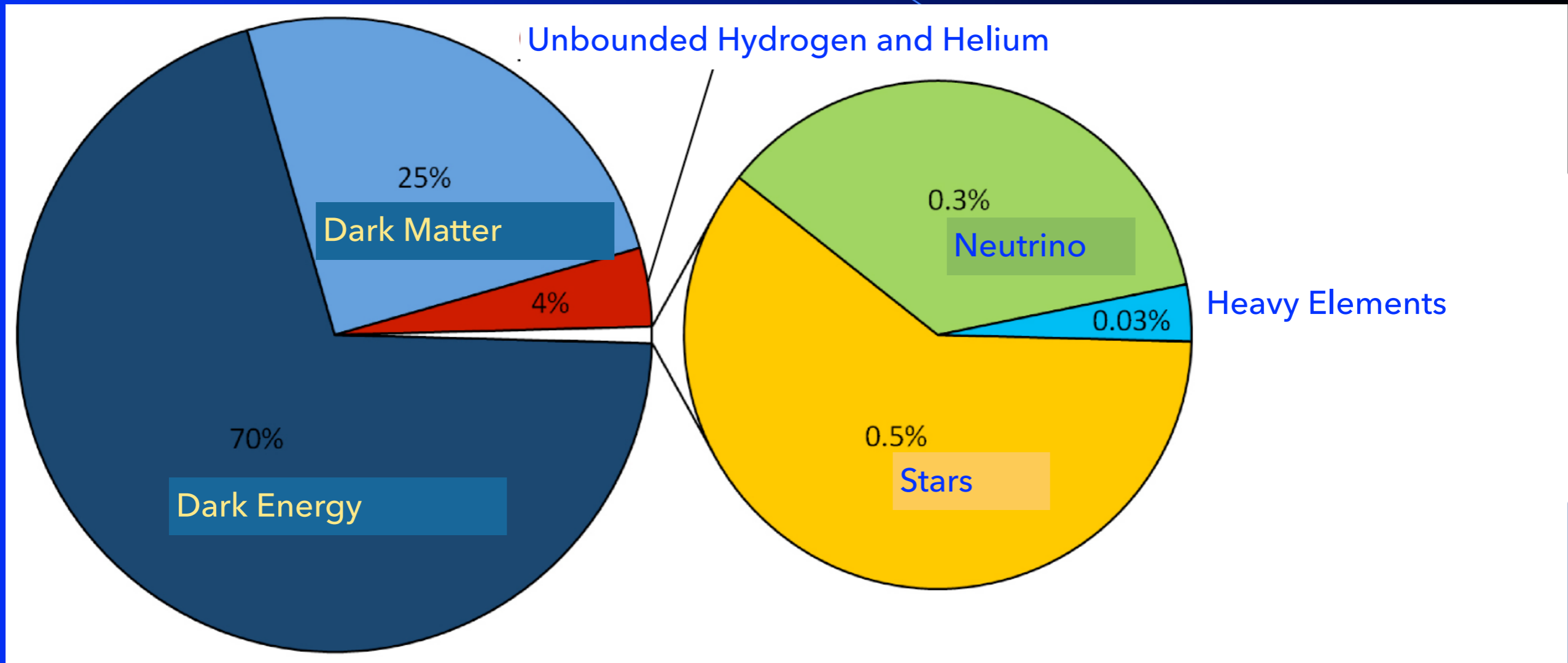
$$\Omega_{DarkMatter} = 26.8\%$$

$$\Omega_{DarkEnergy} = 68.3\%$$

$$\Omega = 1.02 \pm 0.02$$



# The Energy Balance of the Universe



Our knowledge concerns only a small part of the universe, but perhaps we know 90% (50%) of elementary particles

# Dark Matter



What is Dark Matter ?

# Dark Matter



What is Dark Matter ?

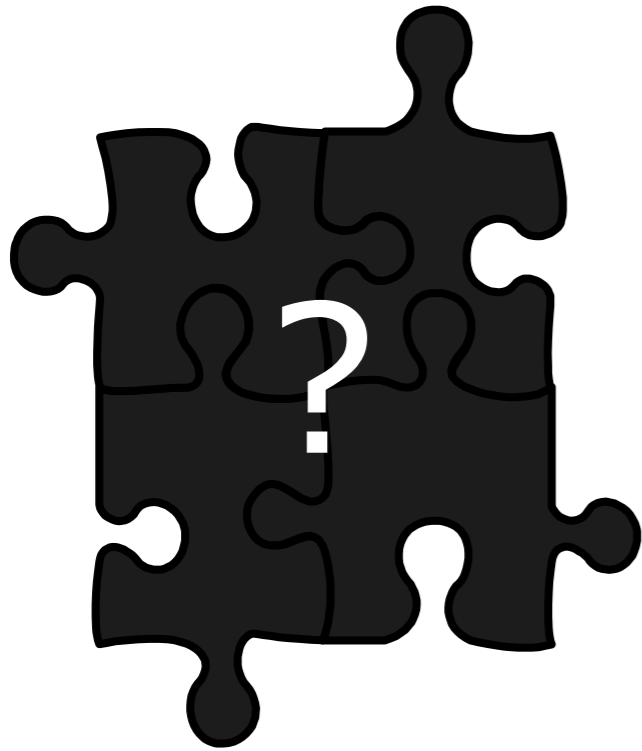


DARK

# Dark Matter

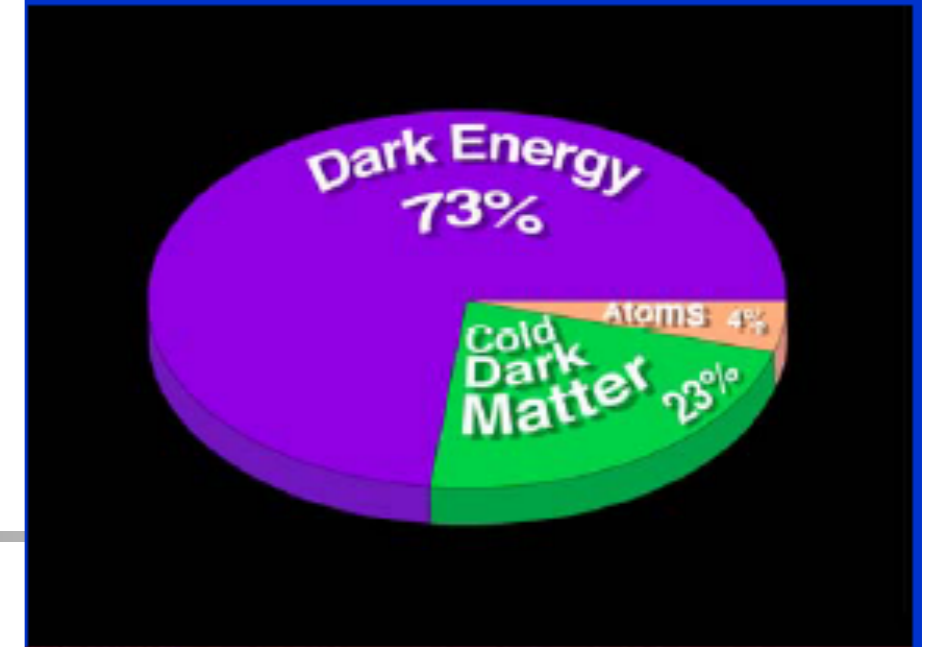


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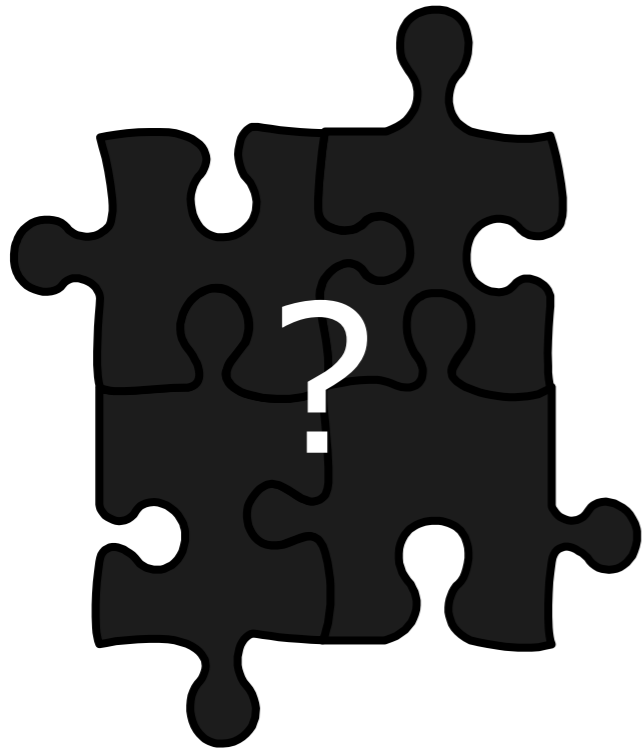


DARK  
WIMP

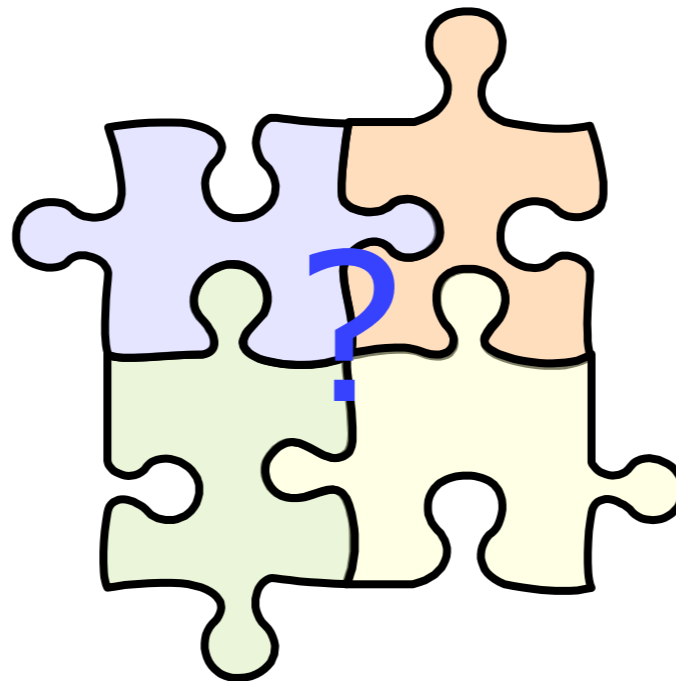
# Dark Matter



## What is Dark Matter ?



DARK  
WIMP

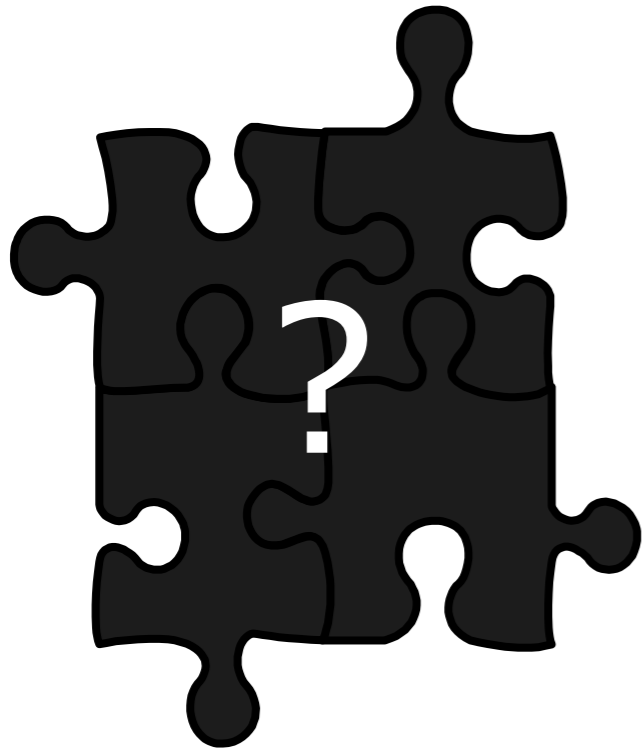


TRANSPARENT

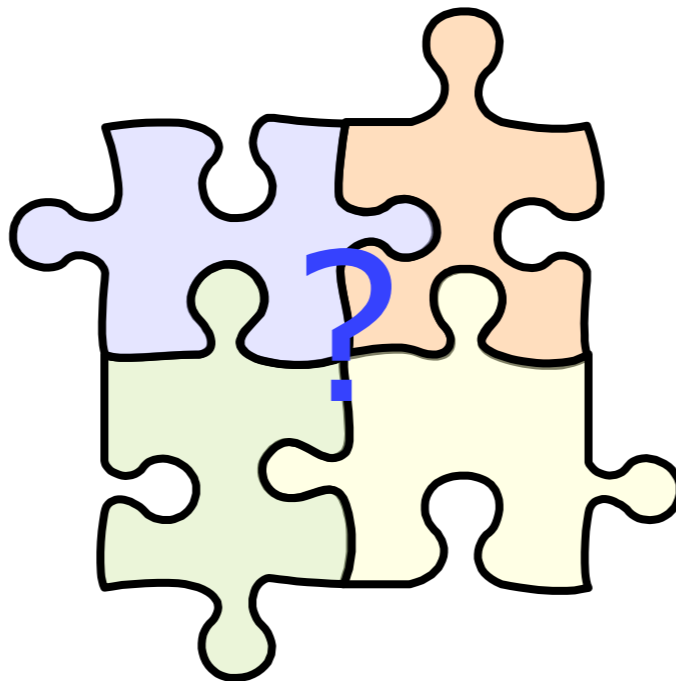
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## What is Dark Matter ?

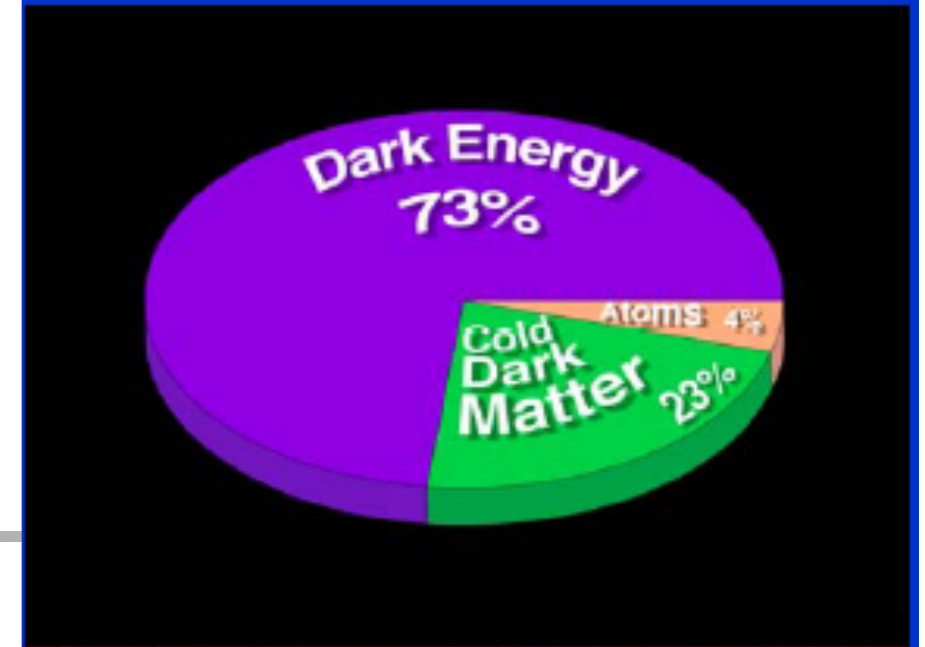


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WIMP

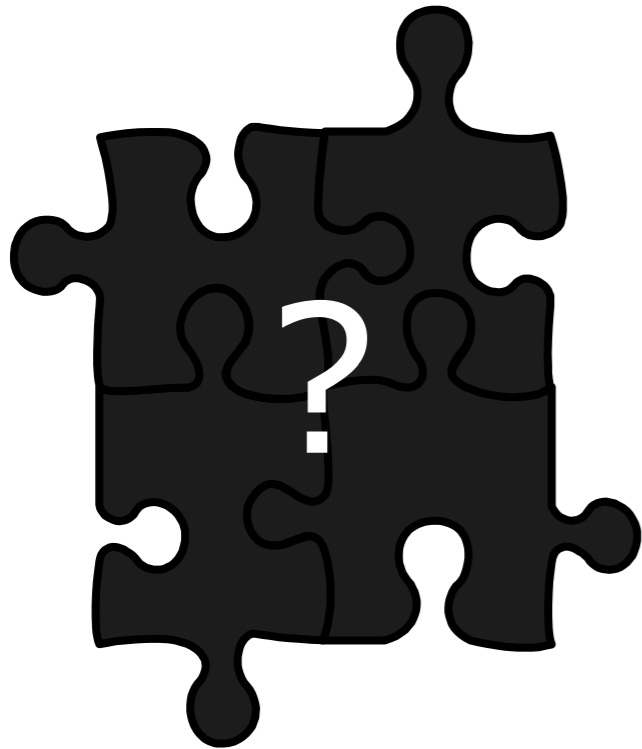


TRANSPARENT  
GRAVITINO

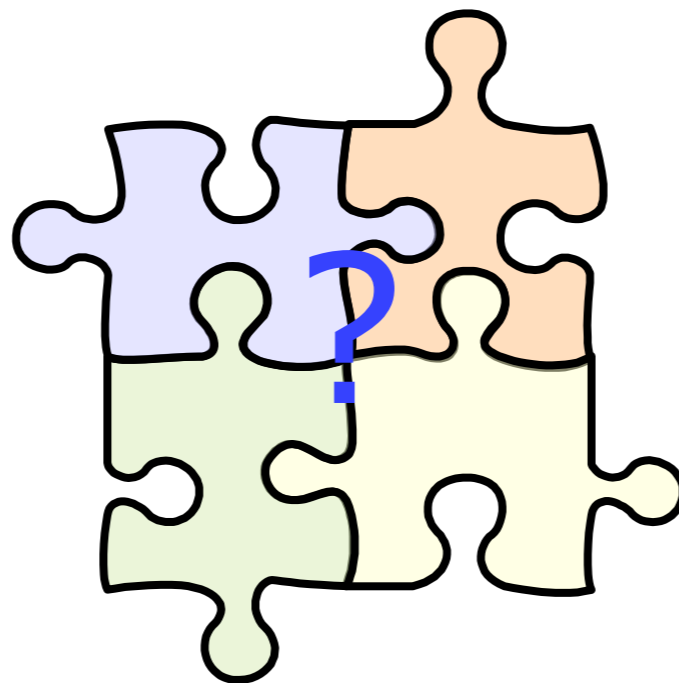
# Dark Matter



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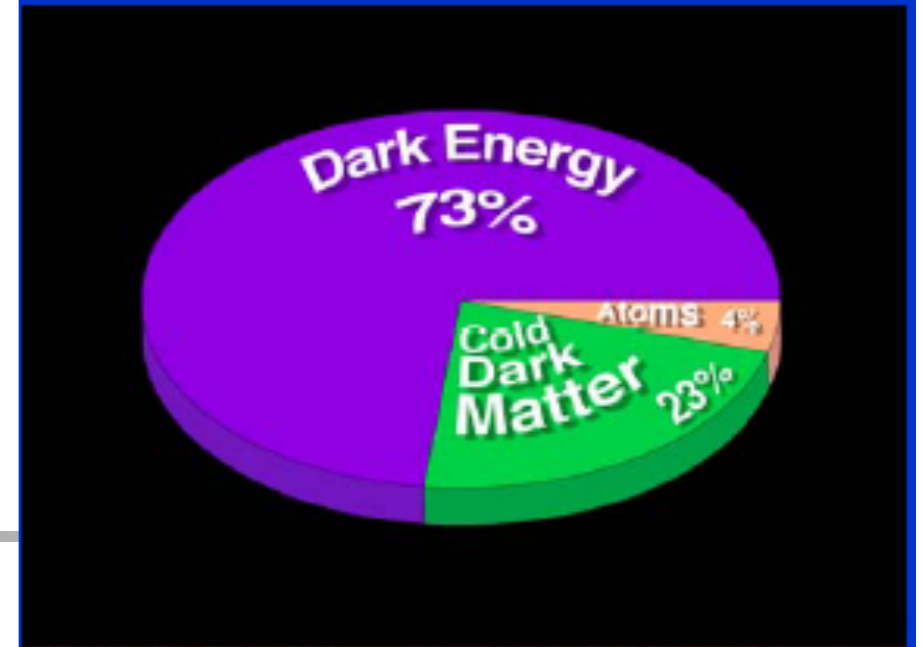


TRANSPARENT  
GRAVITINO

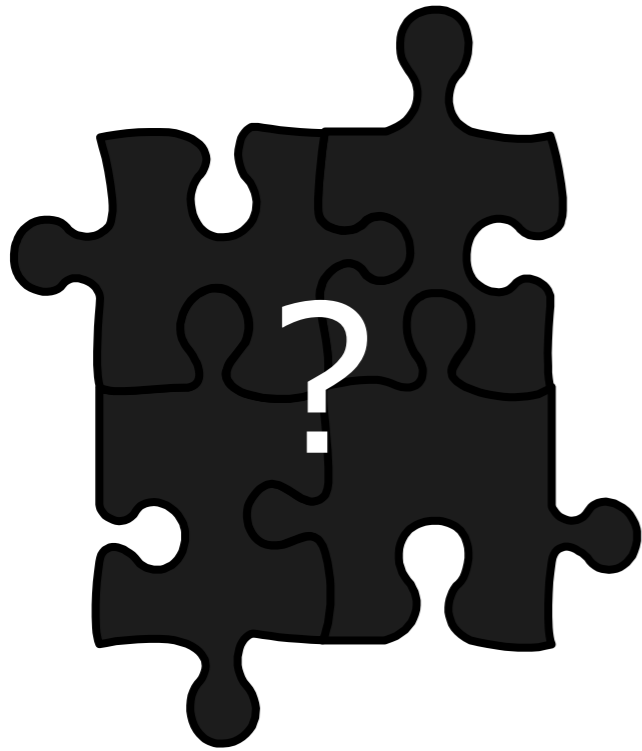


*INVISIBLE*

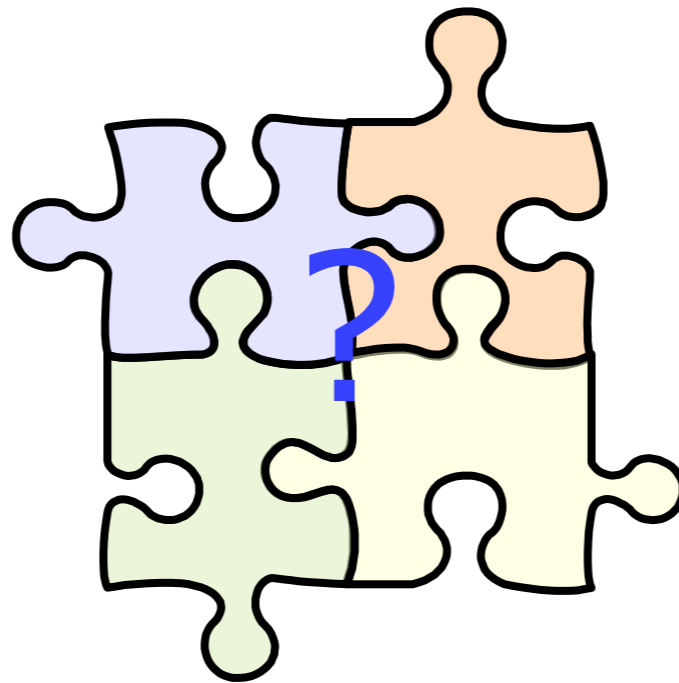
# Dark Matter



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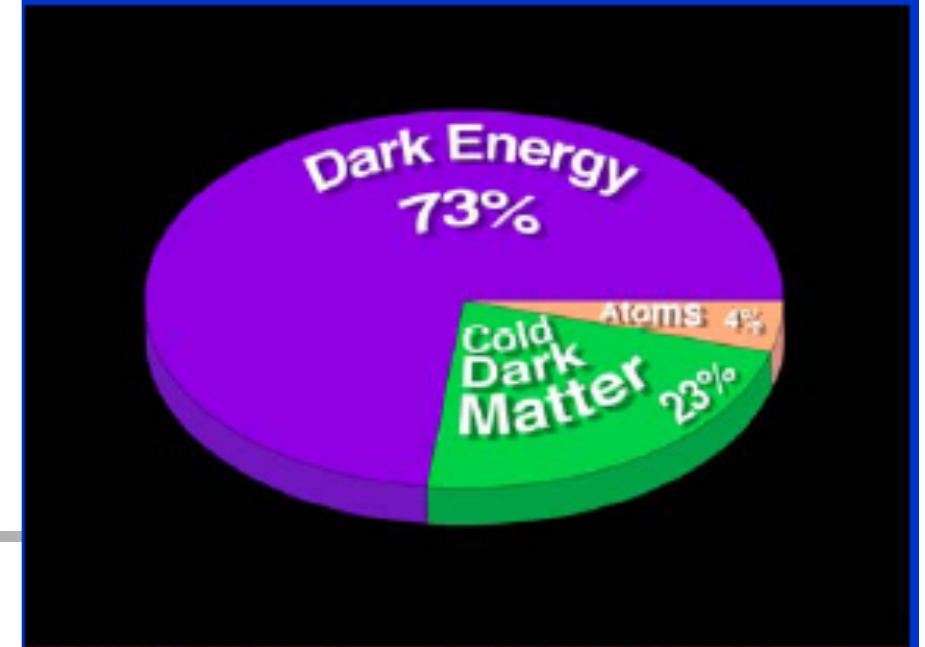
TRANSPARENT  
GRAVITINO



*INVISIBLE*  
*AXION*



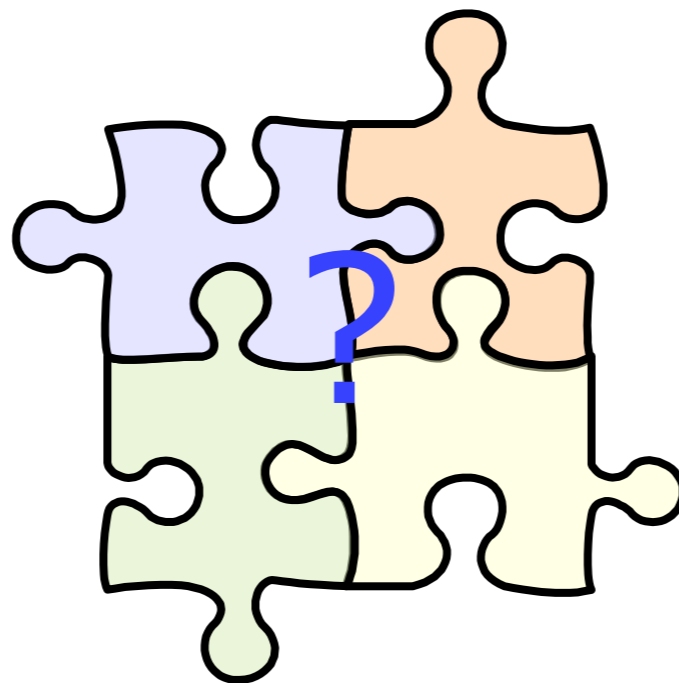
# Dark Matter



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DARK  
WIMP



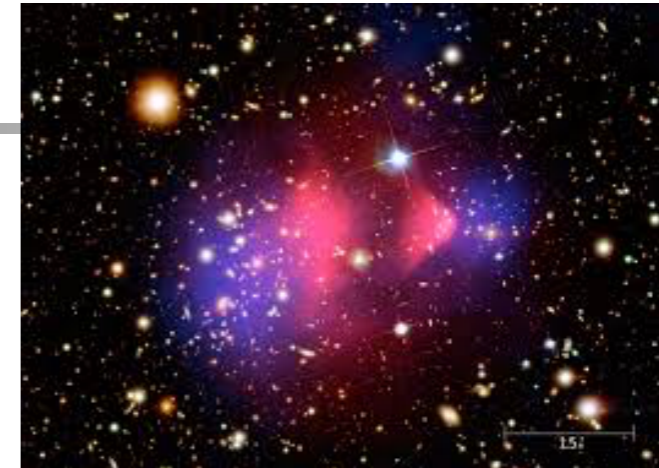
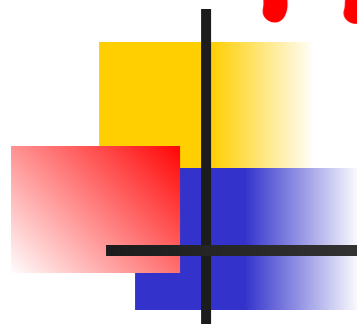
TRANSPARENT  
GRAVITINO



INVISIBLE  
AXION

## What is it made of ?

# The Origin of Dark Matter

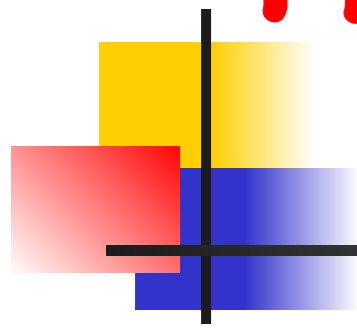


The Dark Matter is made of:

- Macro objects – **Not seen**
- New particles – right neutrino
  - axion (axino)
  - neutralino mSUGRA
  - sneutrino
  - gravitino
  - heavy photon
  - heavy pseudo-goldstone
  - light sterile higgs

Not from the SM

# The Origin of Dark Matter



The Dark Matter is made of:

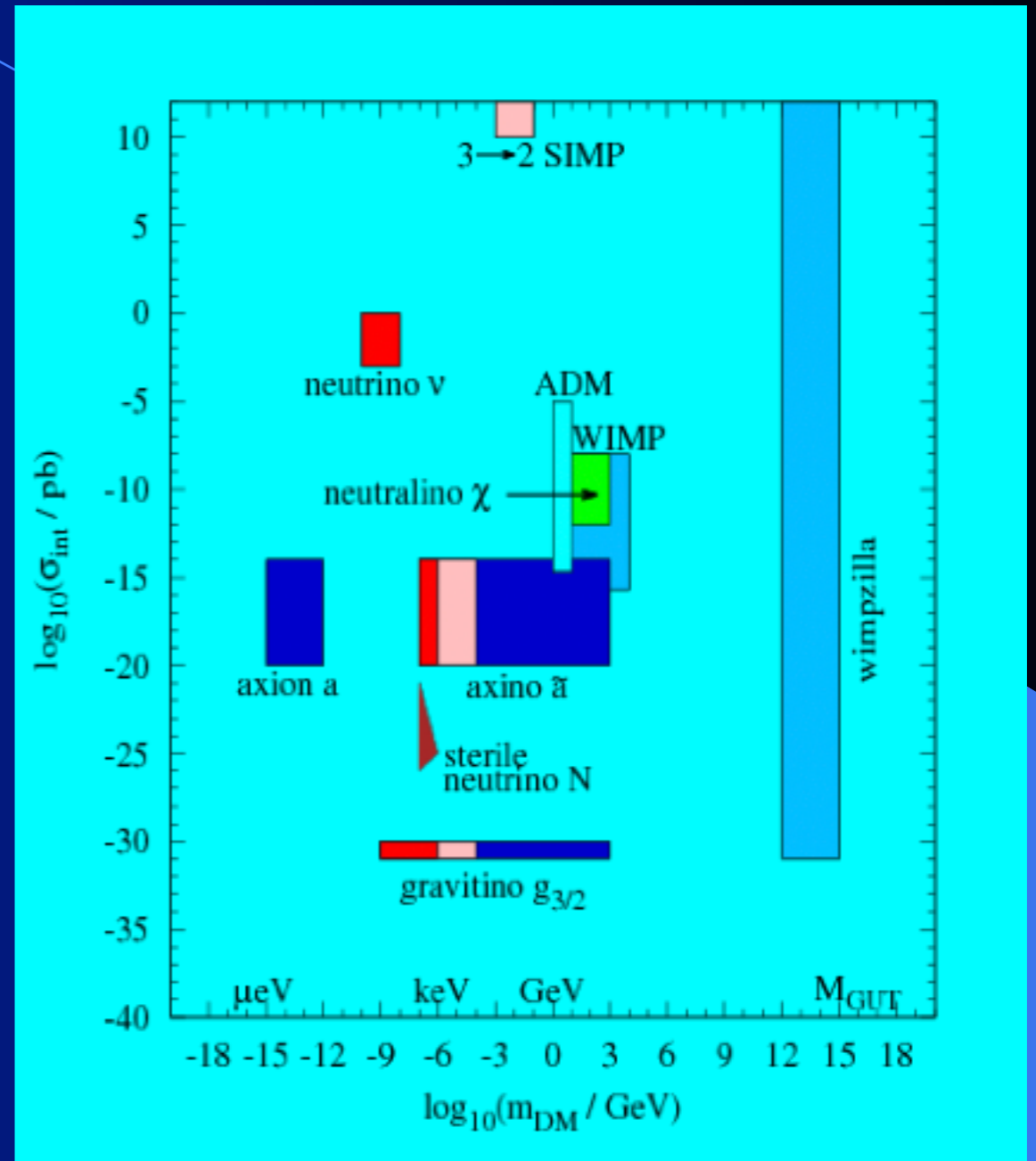
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  - heavy pseudo-goldstone
  - light sterile higgs

not favorable but possible  
might be invisible (?)  
detectable in 3 spheres  
less theory favorable  
might be undetectable (?)  
  
possible, but not  
related to the other  
models

Not from the SM

# Dark Matter candidates

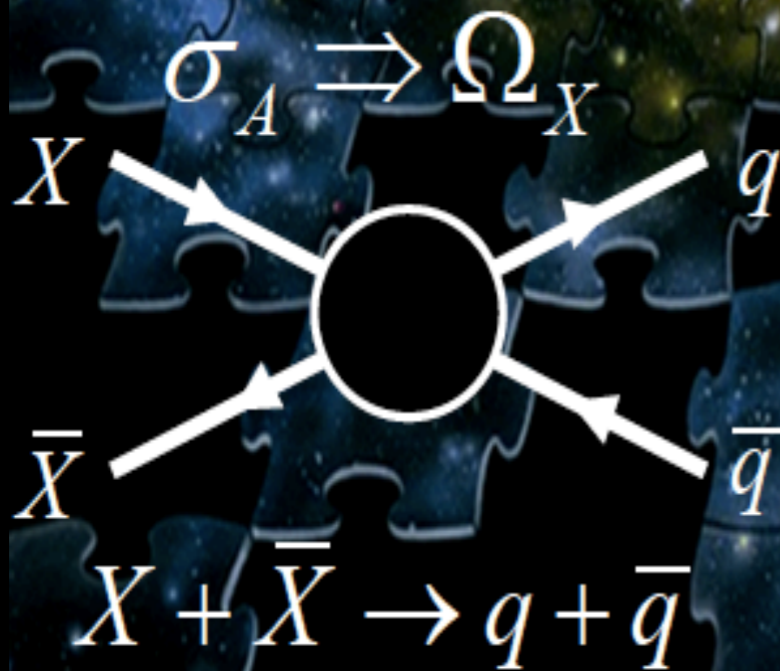
Can one register the Dark matter particle?



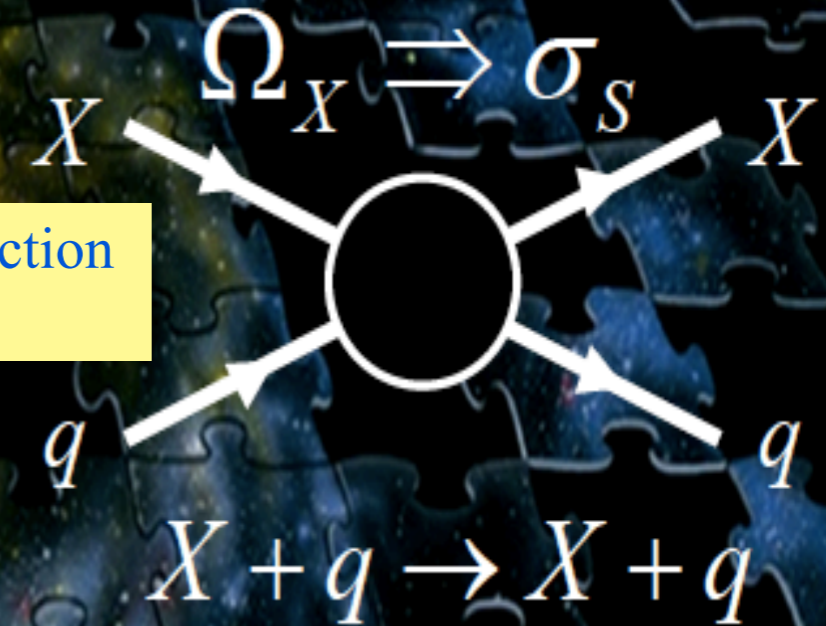
If it is a WIMP, then it can be detected by means of elementary particle physics. If it is only a gravitationally interacting particle, then detection is very difficult.

# Search for Dark Matter Particles

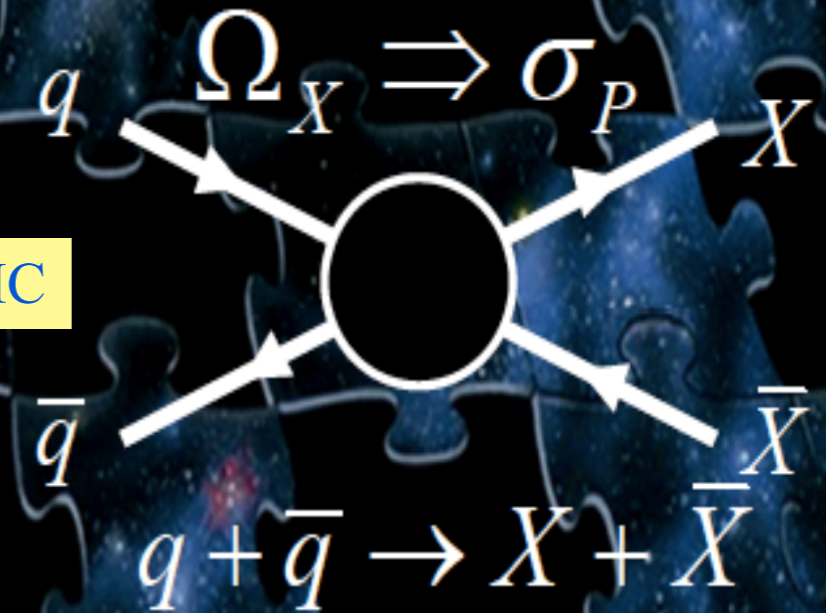
Annihilation  $\rightarrow$  new component in cosmic rays



Direct interaction with matter



Creation at the LHC



R. Kolb

The signal is absent so far

# Search for Dark Matter Particles



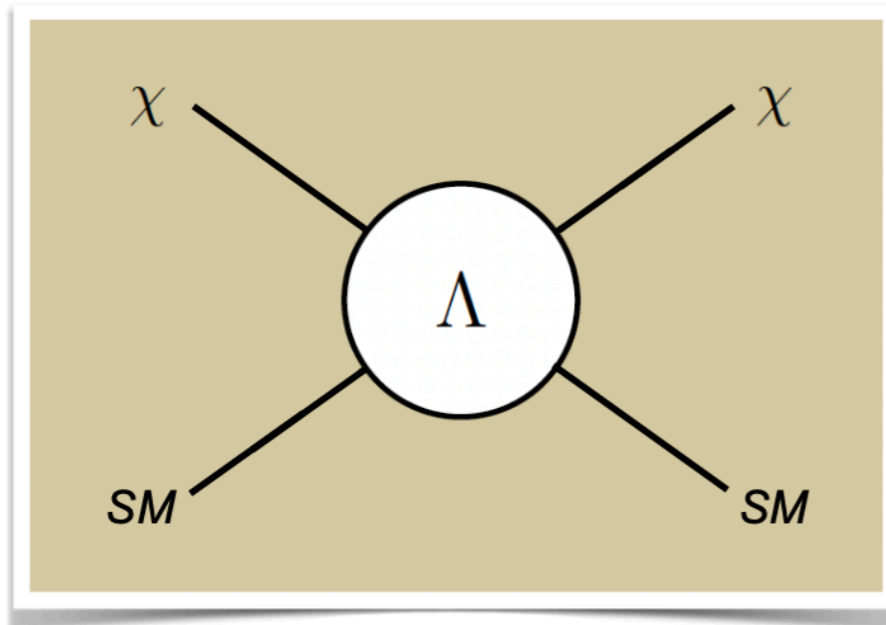
## Ways to search for dark matter and axions / ALPs

ALP: axionlike particle

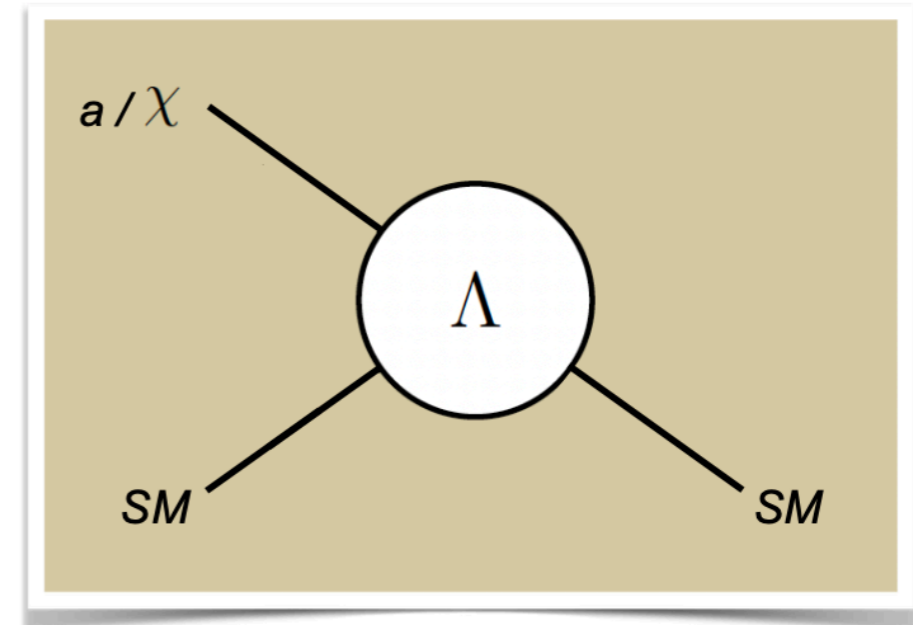
direct detection

axion experiments

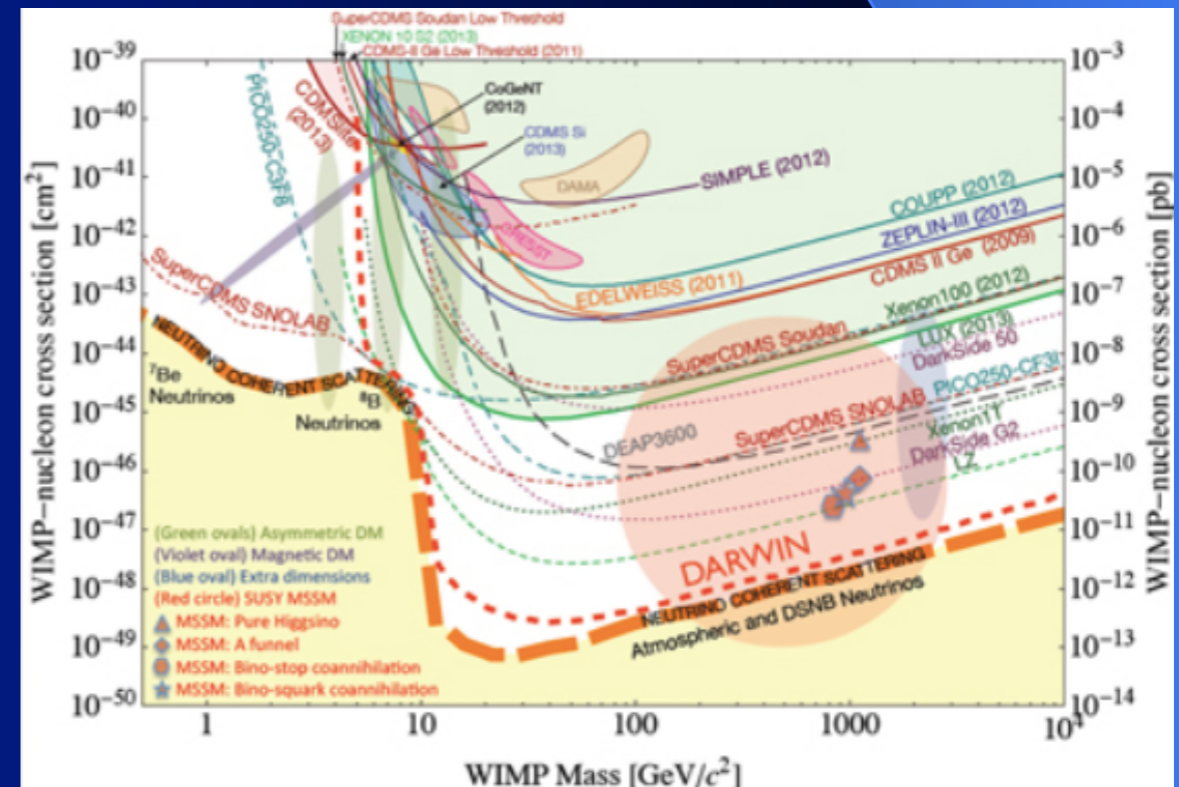
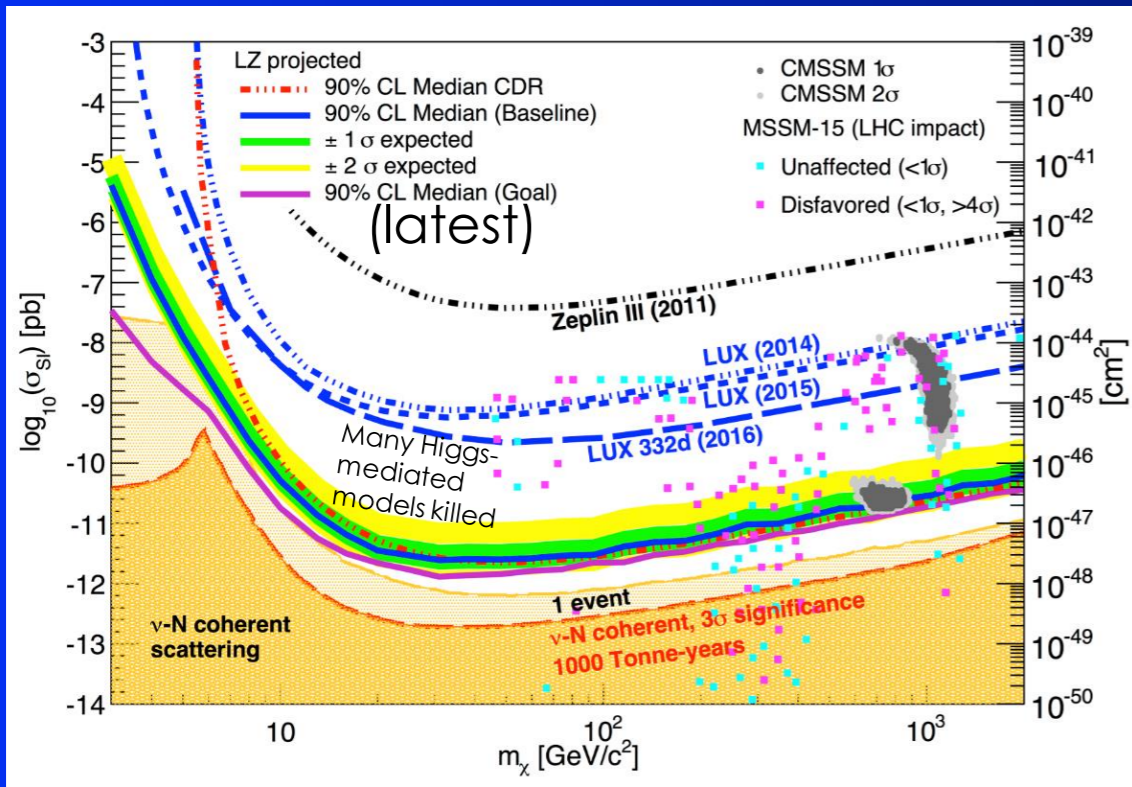
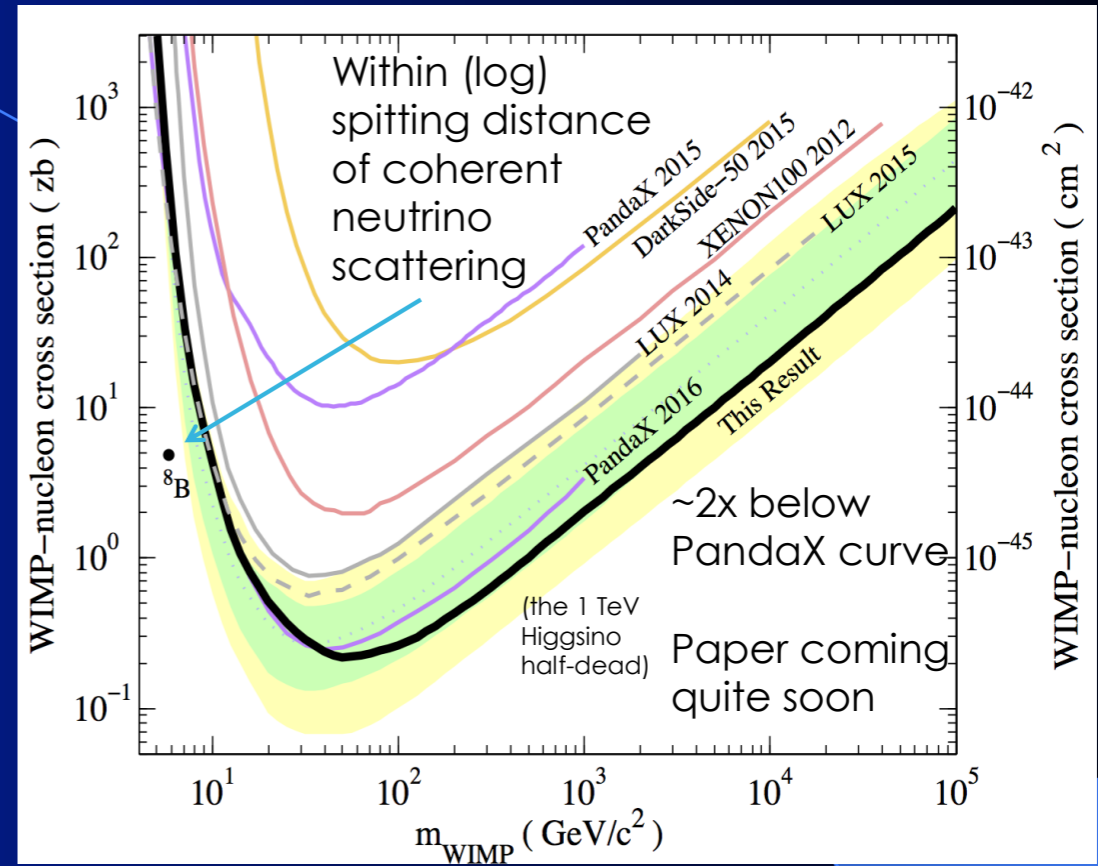
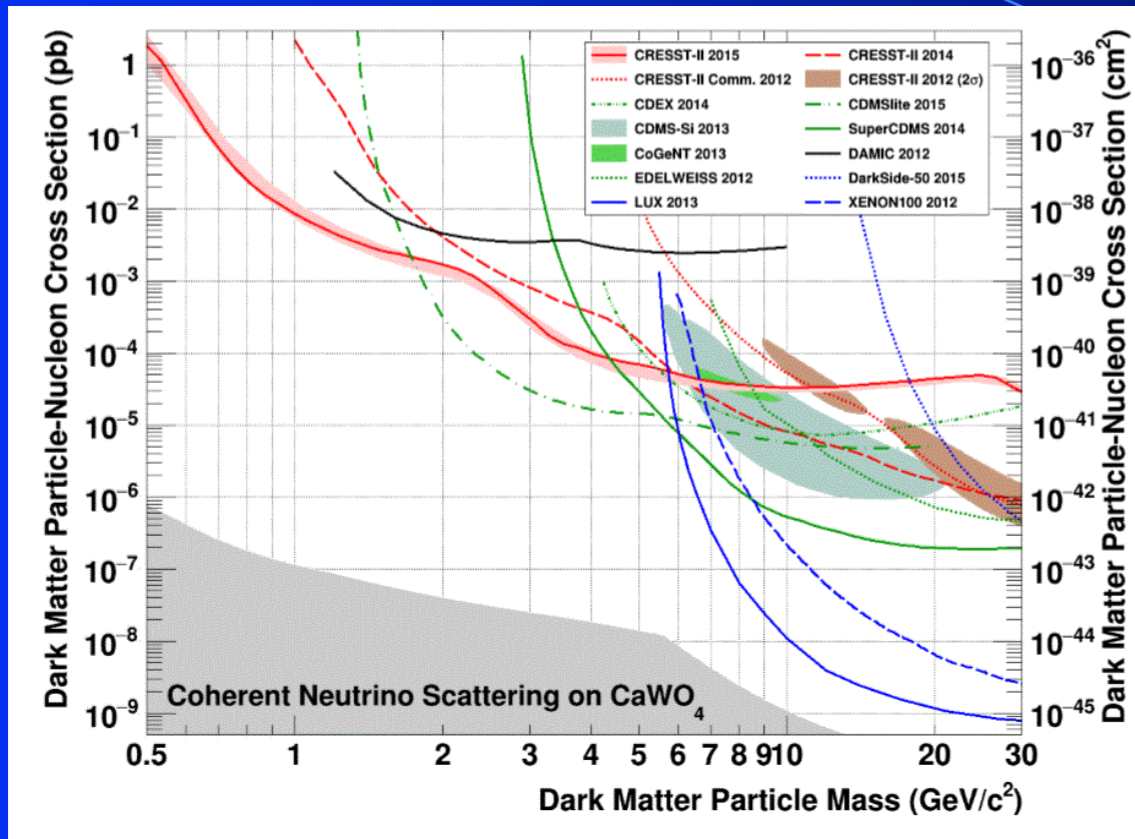
collider experiments



indirect detection

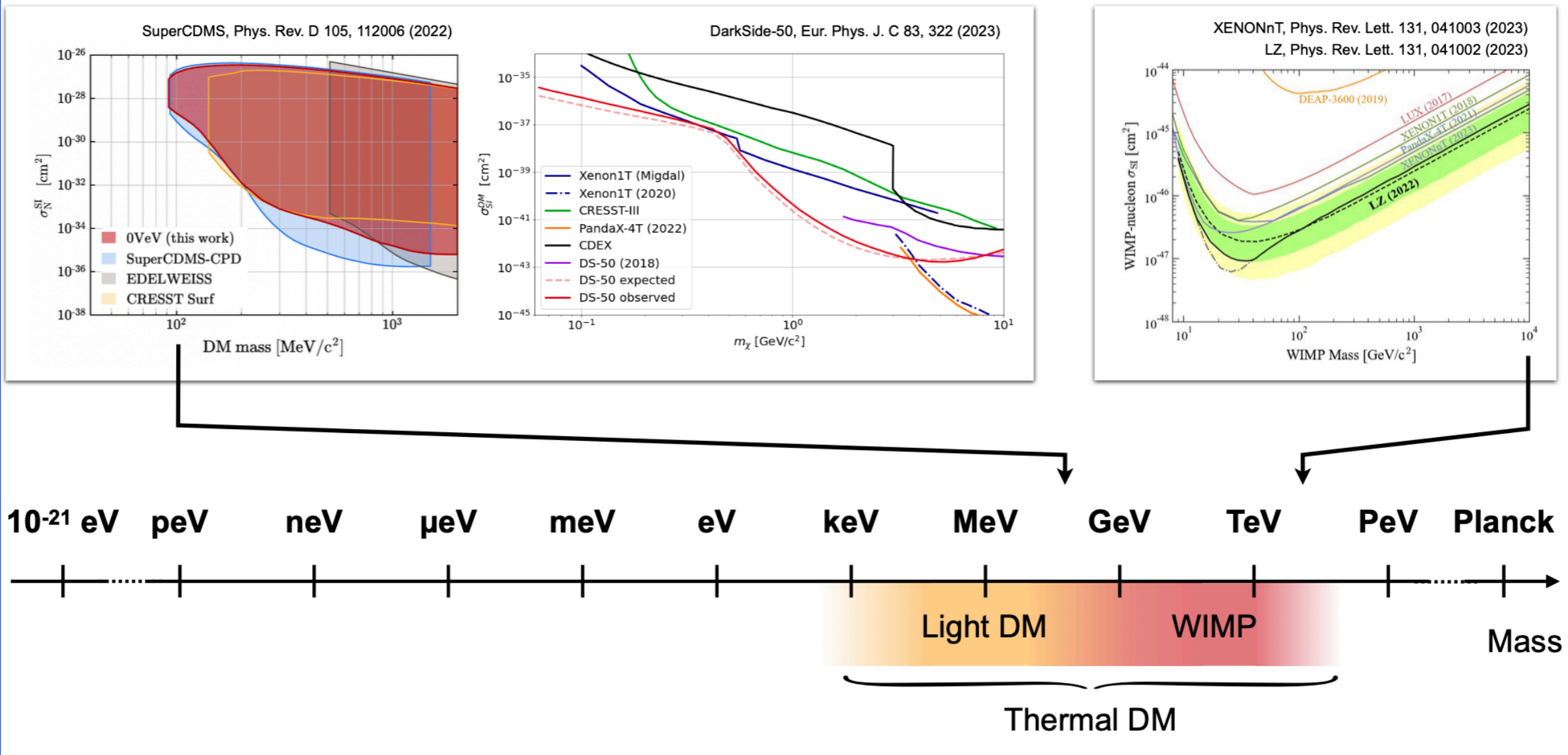


# DARK MATTER: DIRECT DETECTION



# Direct Detection of WIMPs

## Direct detection of WIMP(-like) candidates

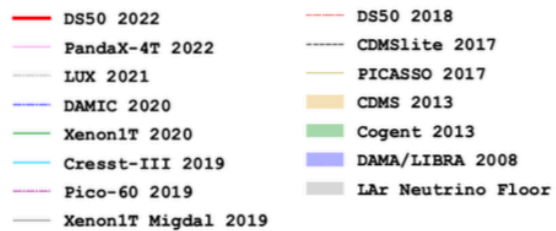
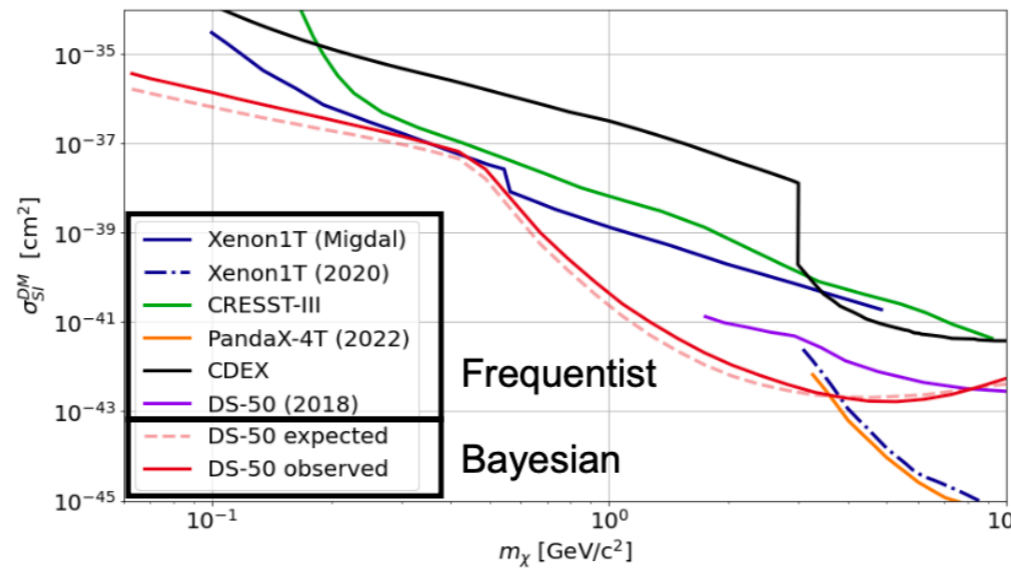
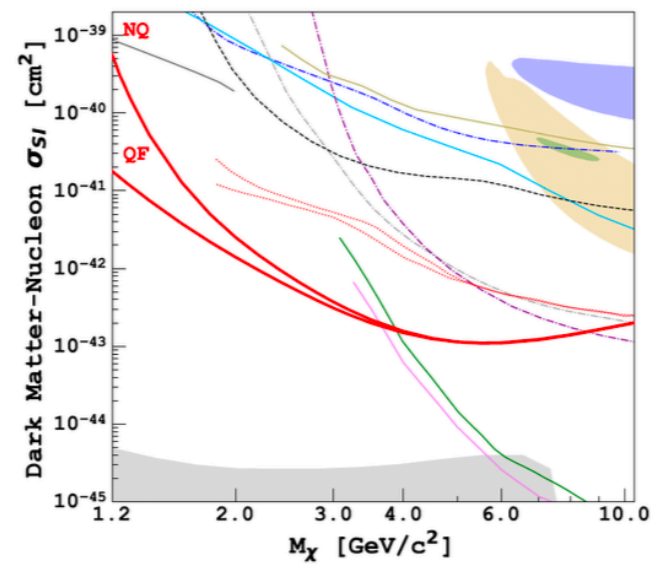




# Detection of light WIMPs

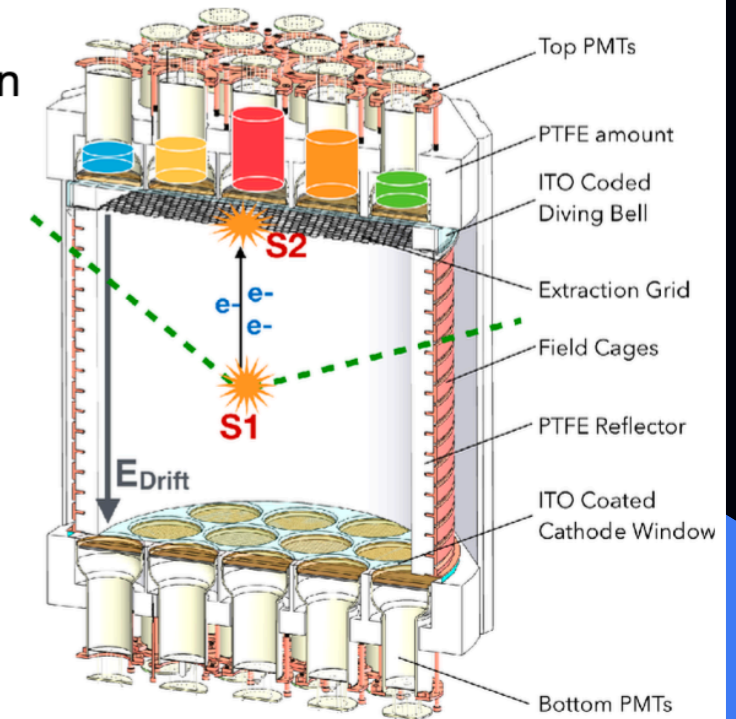
## Most recent results ~1 GeV: **DarkSide-20k**

- Main unknowns: fluctuations in ionization quenching, in energy partitioning between excitons and electrons, and in ion-electron recombinations
- Results (left) confirmed using an alternative Bayesian approach (right), where the analytical calibration responses are made explicit in the likelihood



DarkSide-50, Phys.Rev.D 107 (2023) 6, 063001

DarkSide-50, Eur. Phys. J. C 83, 322 (2023)

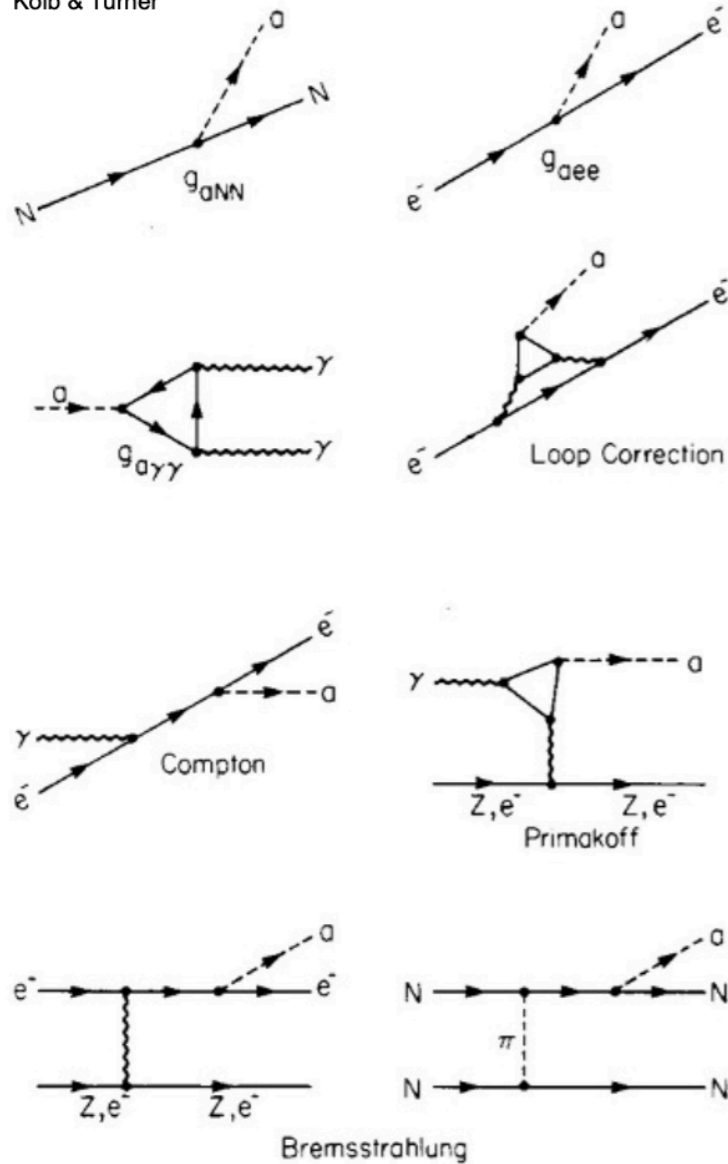


50 kg active mass of LAr

# Search for Axions and Axion-like particles

## Axion couplings

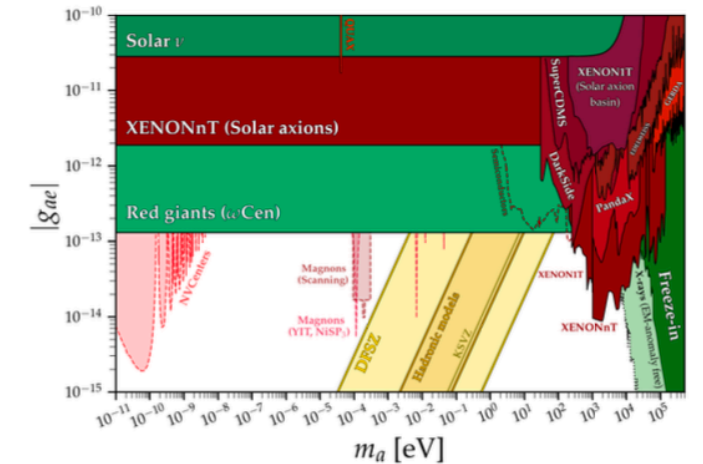
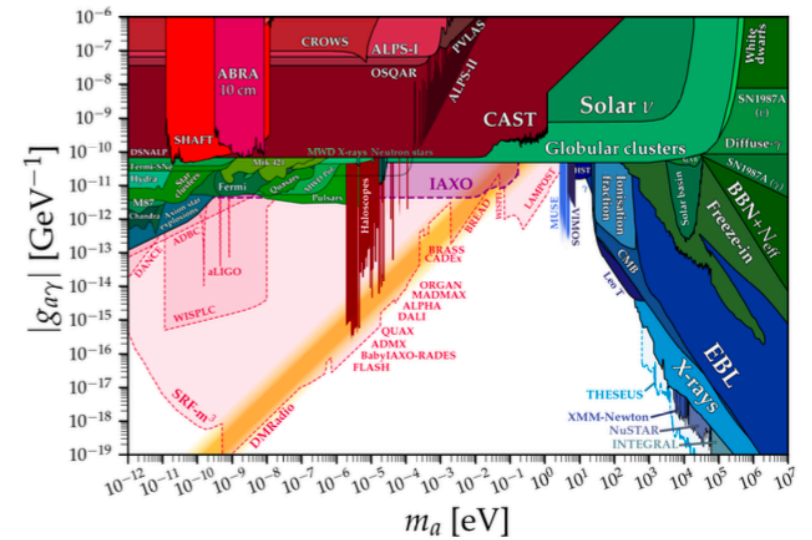
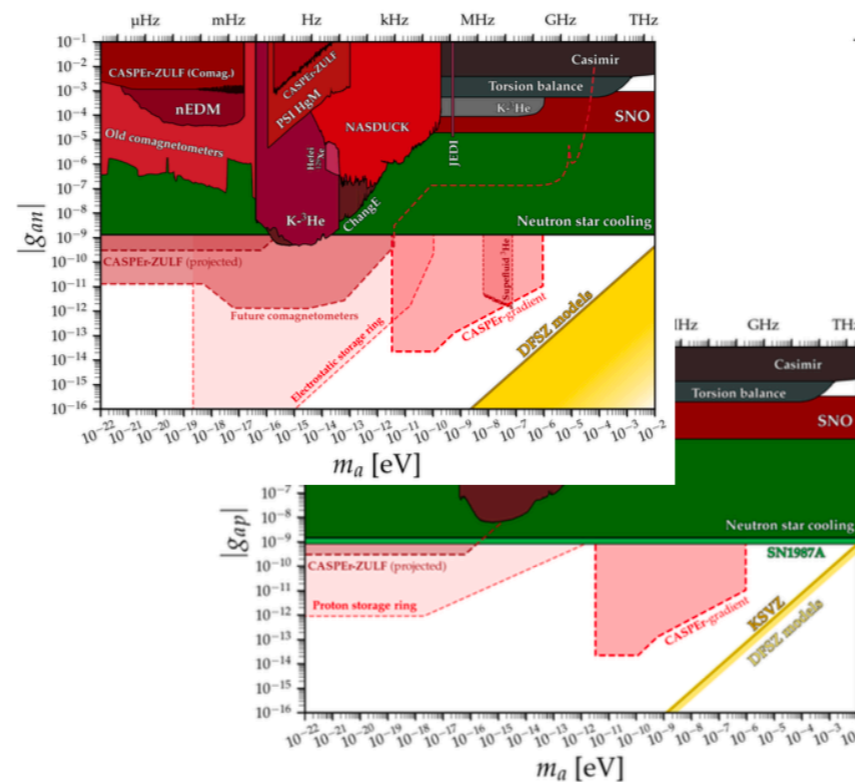
Kolb & Turner



### General classes of couplings

- Axion – Photon
- Axion – Electron
- Axion – Proton / Neutron

C. O'Hare, <https://doi.org/10.5281/zenodo.3932430>

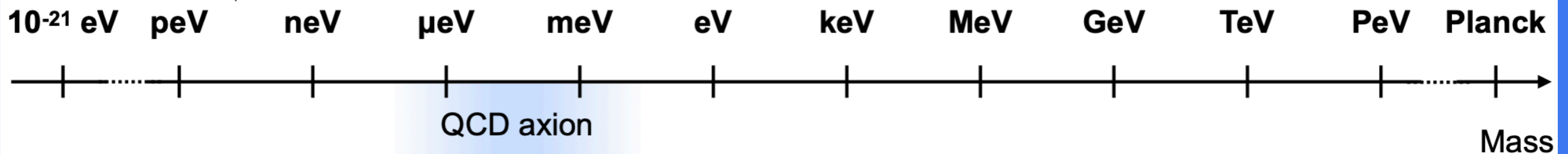
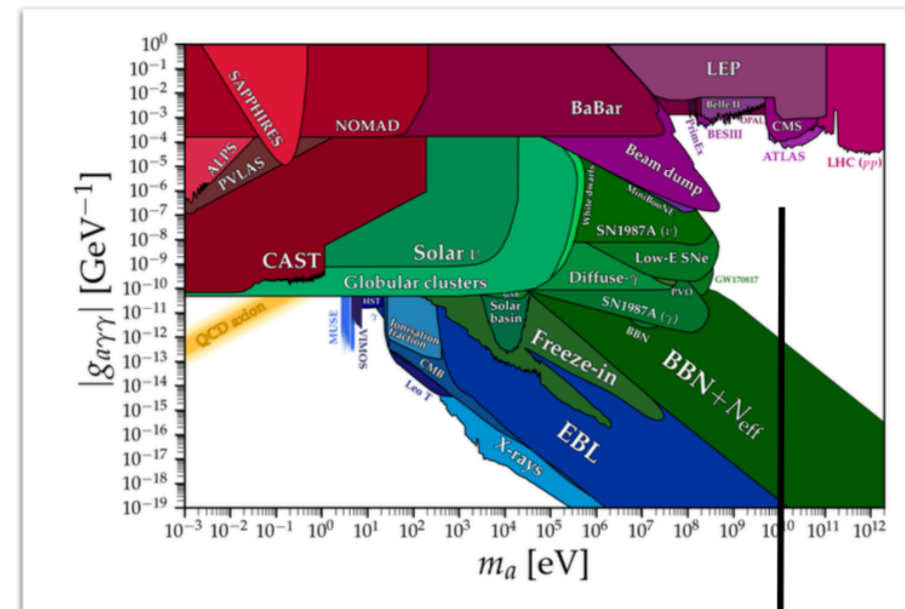
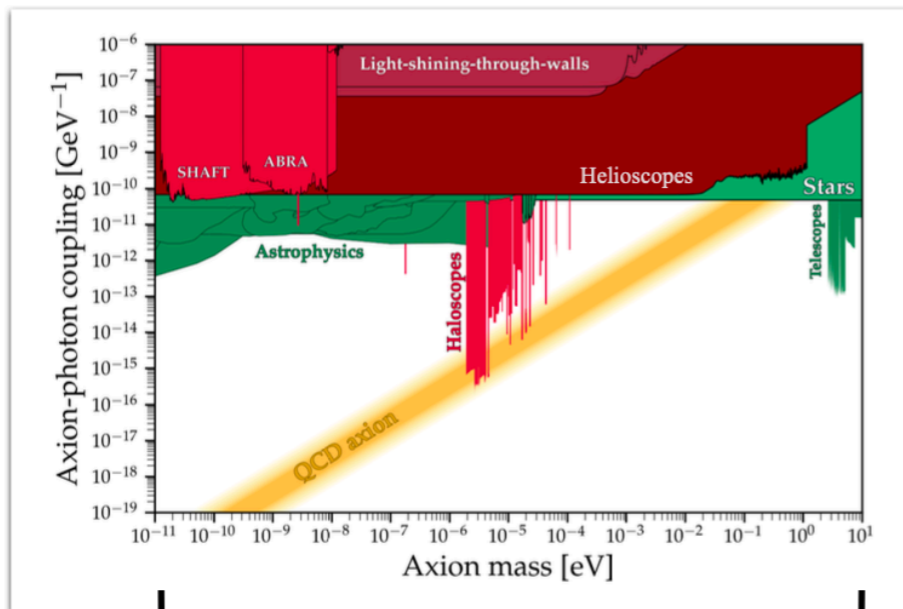


# Detection of ALPs



## Mass ranges of some beyond SM particles

C. O'Hare, <https://doi.org/10.5281/zenodo.3932430>



Bosonic DM (axions, ALPs, dark photons)

# Baryon asymmetry of the Universe

- If there were no baryon asymmetry, there would be no matter in the universe!
- It indicates the existence of a fundamental symmetry breaking between particles and antiparticles



Average number of photons per unit volume

$$n_{\gamma} = 410.4 \pm 0.9 \text{ cm}^{-3}$$

Left after proton-antiproton annihilation

$$\frac{n_B}{n_{\gamma}} = \frac{0.25 \cdot 10^{-6}}{410.4} = 6.1 \cdot 10^{-10}$$

Average number of protons per unit volume

$$n_B = 0.25 \cdot 10^{-6} \text{ cm}^{-3}$$



Three Sakharov's criteria

- Violation of baryon number
- Violation of C and CP invariance
- Violation of thermal equilibrium

- What is the source of baryon asymmetry of the Universe?
- Where the symmetry between particles and antiparticles is violated?

# Baryon asymmetry of the Universe



SM expectation:

$$\frac{n_B - n_{\bar{B}}}{n_\gamma} \sim 10^{-18}$$

vs.

Observed\*:

$$\frac{n_B - n_{\bar{B}}}{n_\gamma} \sim 10^{-10}$$

Sakharov criteria

1. Baryon number violation
2. C and CP violation
3. Thermal non-equilibrium



\*WMAP

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Sakharov criteria

1. Baryon number violation
2. C and CP violation
3. Thermal non-equilibrium



\*WMAP

- Baryon number is conserved in the SM with exponential accuracy
- Violation of baryon number occurs in Grand Unified Theories and in Lepton=fourth color models (Pati-Salam model)

New particles = Leptoquarks, Extended Higgs sector

$$B = \frac{N_q - N_{\bar{q}}}{3}$$



- Violation of CP invariance in the SM achieved via phase factors in the CKM and PMNS mixing matrices



BAU requires larger CP than in the SM

Possible Baryogeneses via Leptogeneses

The presence of new phase factors in extended models (2HDM, SUSY, etc)

## BEYOND THE STANDARD MODEL: CONCLUSIONS

---

**WHAT MAKES US THINK THAT THERE IS PHYSICS BEYOND THE STANDARD MODEL?**

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- Baryon asymmetry of the Universe is a fundamental problem (Baryon and Lepton genesis might require new ingredients)
- Lack of understanding of flavor structure of the SM calls for explanation at higher level
- New era in gravity due to discovery of gravitational waves and black holes might change the landscape

## ***Ideas*** (conventional and not)

- **Symmetries**
  - Supersymmetry, family, ...
- **Compositeness**
  - Higgs, fermions, ...
- **Extra dimensions**
  - large, warped, ...
- **Dark or hidden sectors**
  - Dark, SUSY-breaking, random, ...
- **Unification**
  - GUT, string, ...
- **New dynamical ideas**
  - Relaxion, unnaturalness, clockwork, string instantons, ...
- **Random or environmental**
  - multiverse
- **String remnants**
  - (need not solve SM problem)
  - $Z'$ , vector fermions, extended Higgs, dark, moduli, axions, ...

**Looking for new physics we are looking for new Symmetry of Nature!**



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# BEYOND THE STANDARD MODEL: QUEST FOR SYMMETRY

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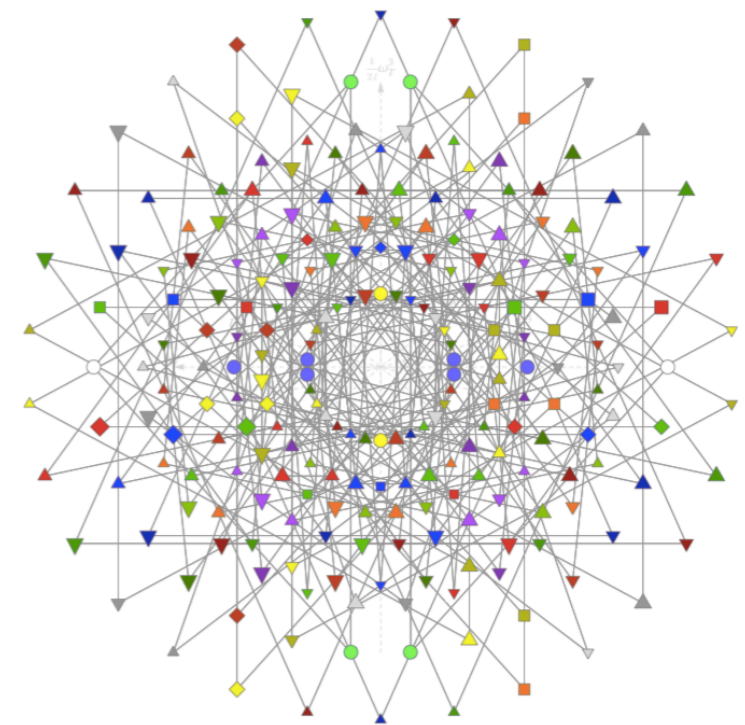
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# BEYOND THE STANDARD MODEL: QUEST FOR SYMMETRY

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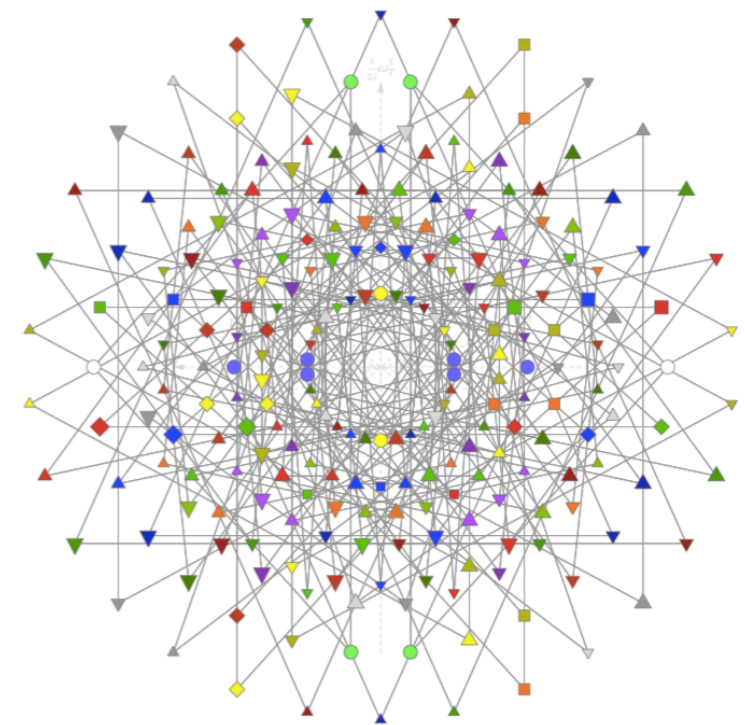
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E8 roots

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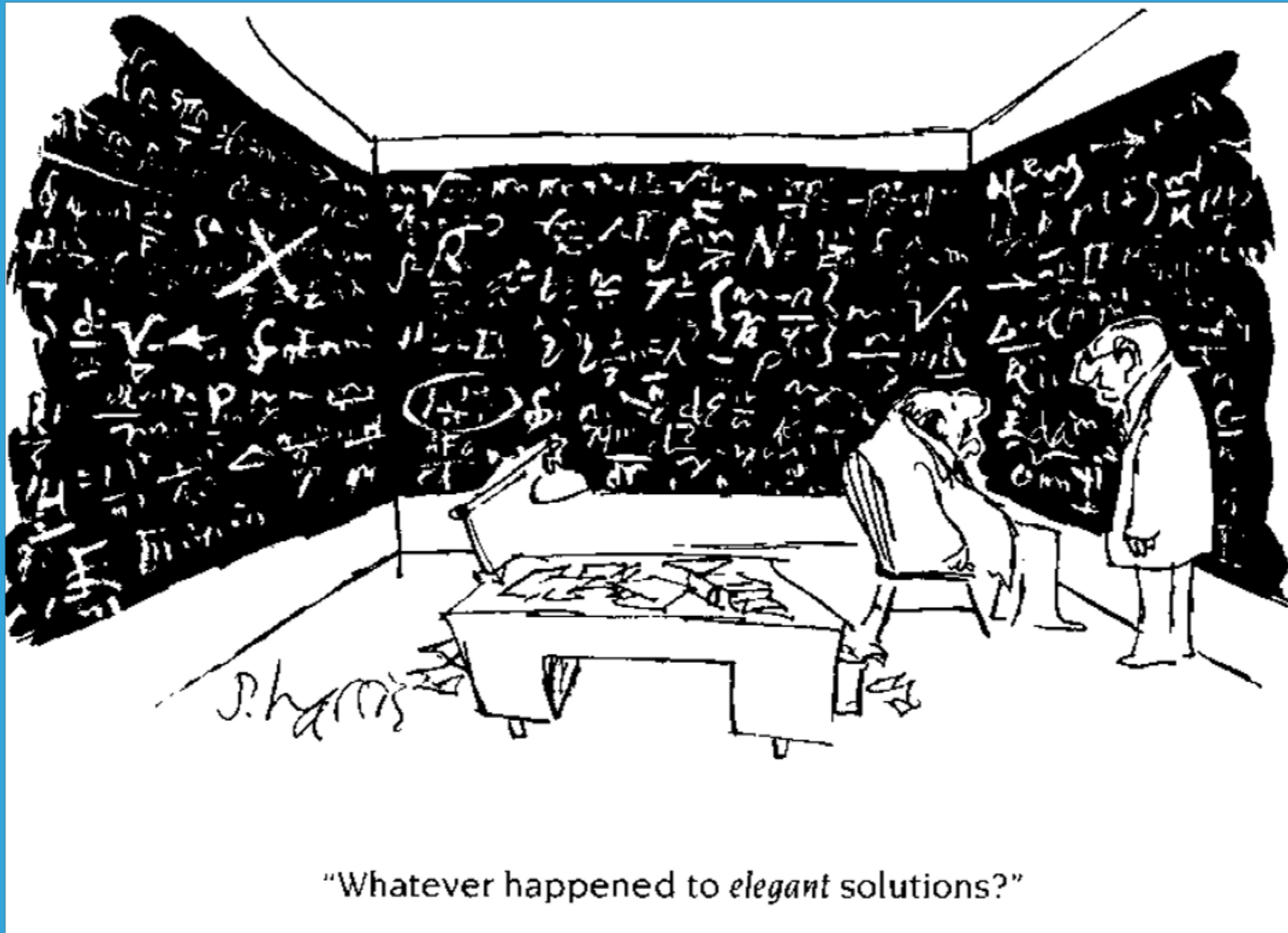
Looking for new physics we are looking for new Symmetry of Nature!



E8 roots

Symmetry might be tricky

# We like elegant solutions





## Future Particle Physics



### Beyond SM

**Energy frontier:** HL LHC, FCC  $e^+e^-$ -mode, CLIC, China colliders

**Intensity Frontier:** SuperBelle, BEPCIII, SHiP, NA62, NA64, VEPP, Super  $c$ - $\tau$ -factory

**Precision Frontier:**  $g-2$ , nEDM

**Under -ground, -water, -ice:** Icecube, Baikal

**Neutrino:** JUNO, HyperK, ..., DUNE

**Cosmic Rays:** Pierre Auger, ..., satellites

### New Dynamics in SM

EIC (electron ion collider) BNL

NICA

FAIR

JLAB

U-76

China electron-ion collider



# Experimental Particle Physics



## Russia & JINR

### Beyond SM

#### Intensity & Precision Frontier:

VEPP, Super  $c$ - $\tau$ -factory, nEDM

#### Under -ground, -water: GVD-Baikal

Neutrino: BEST, NEUTRINO-4, DANSS, ...

Cosmic Rays: Pamir, Tian-Shan, satellites ...

### New Dynamics in SM

**NICA:** MPD heavy-ion collisions

BM@N short-range nucleon correlations

SPD spin structure, partonic 3D-structure

exotic resonances

electron-ion collider option R&D

**U-76** SPASCHARM charm and exotic resonances

**Which way to go ?**



## Which way to go ?



## Which way to go ?



## Which way to go ?



What the future may bring?