



BEYOND THE STANDARD MODEL

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Outline

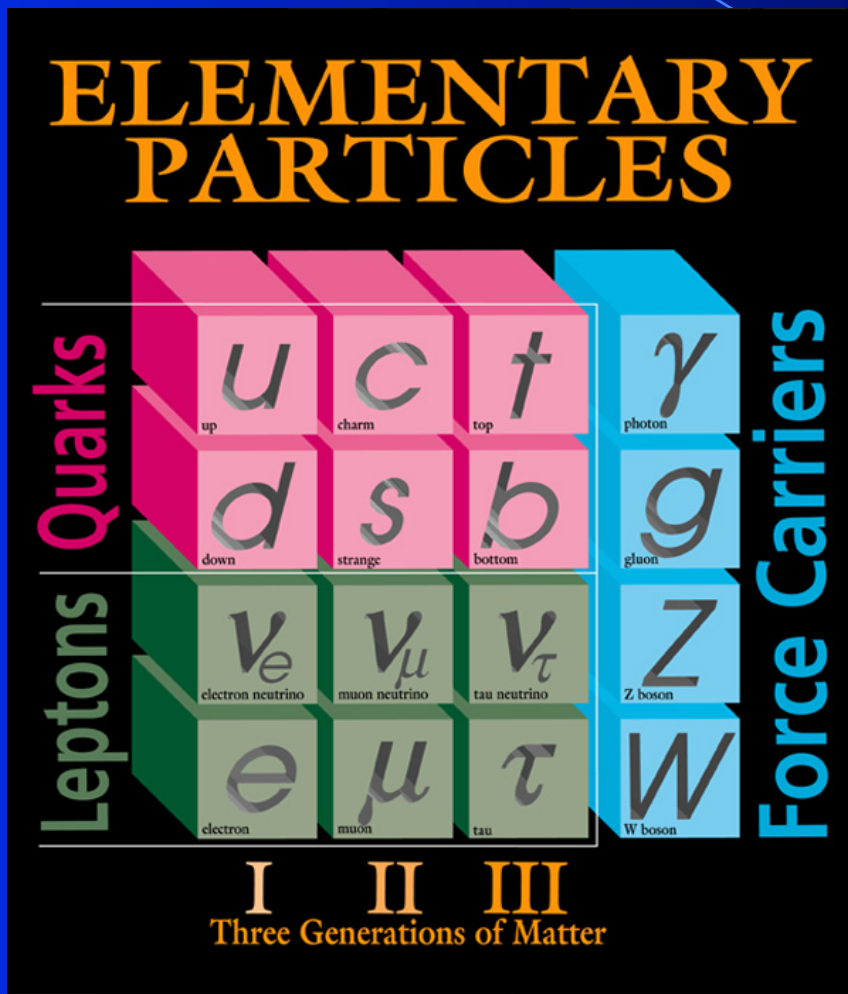
Part I Supersymmetry

1. What is SUSY
2. Basics of SUSY
3. The MSSM
4. Constrained MSSM
5. SUSY searches
6. SUSY DM

Part II Extra Dimensions

1. The main idea
2. Kaluza-Klein Approach
3. Brane-world models
4. Possible experimental signatures of ED

The Standard Model



Forces

Electromagnetic

Strong

Weak

Gravity

Standard Model

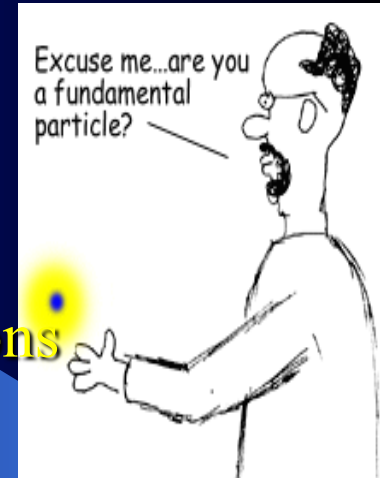
H

The Higgs boson

The SM and Beyond

The problems of the SM:

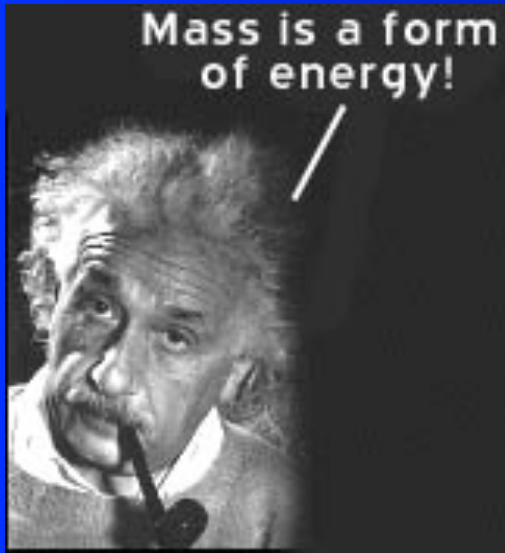
- Inconsistency at high energies due to Landau pole
- Large number of free parameters
- Formal unification of strong and electroweak interactions
- Still unclear mechanism of EW symmetry breaking
- CP-violation is not understood
- Flavour mixing and the number of generations is arbitrary
- The origin of the mass spectrum is unclear



The ways beyond the SM:

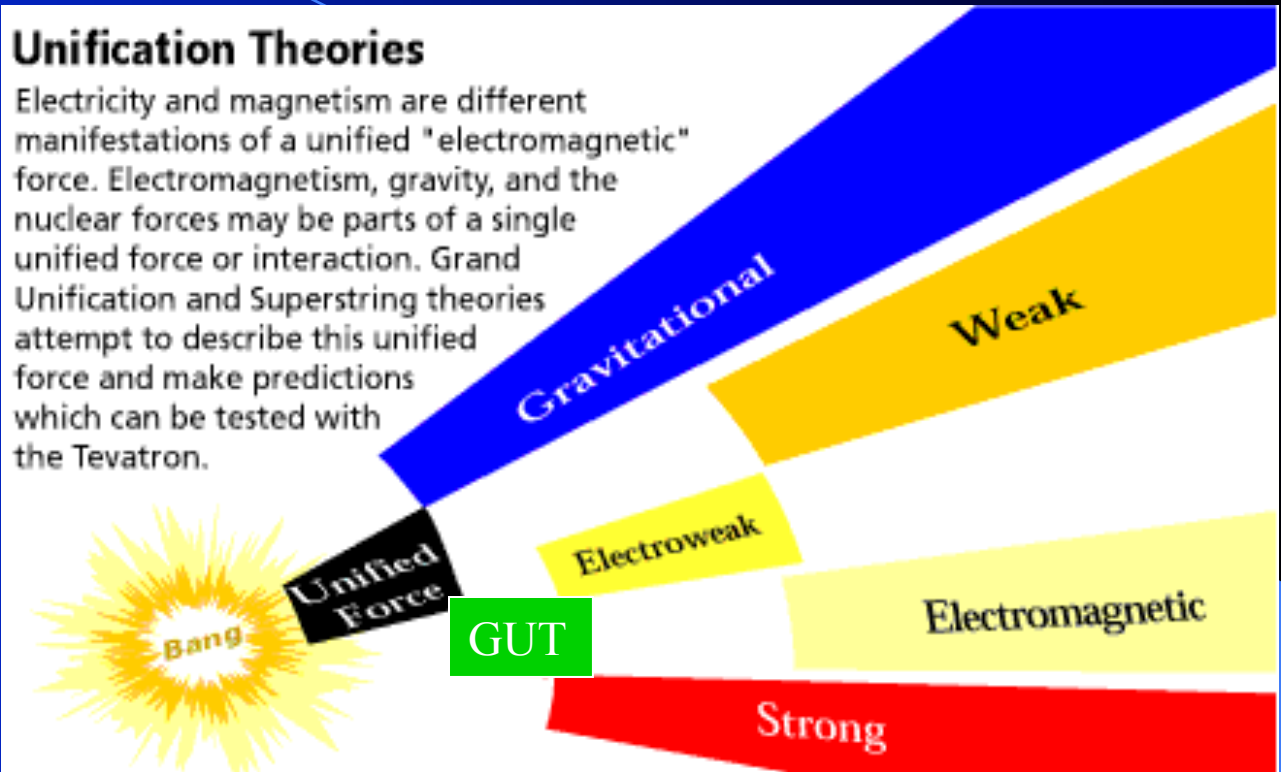
- The SAME fields with NEW interactions → GUT, SUSY, String
- NEW fields with NEW interactions → Compositeness, Technicolour, preons

Grand Unified Theories

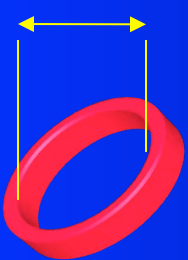


Unification Theories

Electricity and magnetism are different manifestations of a unified "electromagnetic" force. Electromagnetism, gravity, and the nuclear forces may be parts of a single unified force or interaction. Grand Unification and Superstring theories attempt to describe this unified force and make predictions which can be tested with the Tevatron.



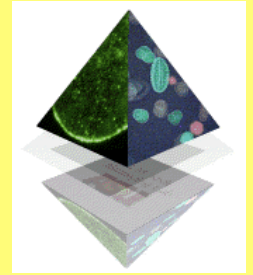
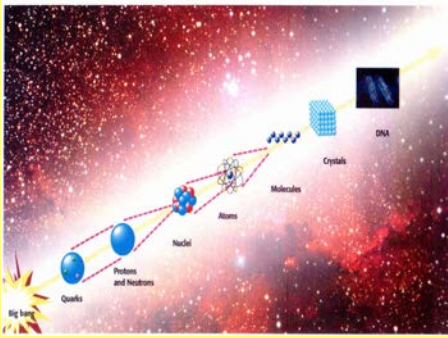
$10^{-34} m$



$D=10$

- Unification of strong, weak and electromagnetic interactions within Grand Unified Theories is the new step in unification of all forces of Nature
- Creation of a unified theory of everything based on string paradigm seems to be possible

What is SUSY?



- **Supersymmetry** is a boson-fermion symmetry that is aimed to unify all forces in Nature including gravity within a single framework

$$Q | boson \rangle = | fermion \rangle$$

$$[b, b] = 0 \quad \{b, b\} = 2\sigma^j \quad (\sigma^\mu)_{\alpha\beta} P_\mu$$

- Modern theories in particle physics are based on GRM, though low energy manifestations of SUSY can be found (?) at modern colliders and in non-accelerator experiments

First papers in 1971-1972
 No evidence in particle physics yet

Motivation of SUSY in Particle Physics

- Unification with Gravity
- Unification of gauge couplings
- Solution of the hierarchy problem
- Dark matter in the Universe
- Superstrings

Superalgebra

(Super) Algebra

Lorentz Algebra

$$[P_\mu, P_\nu] = 0, [P_\mu, M_{\rho\sigma}] = i(g_{\mu\rho} P_\sigma - g_{\mu\sigma} P_\rho),$$

$$[M_{\mu\nu}, M_{\rho\sigma}] = i(g_{\nu\rho} M_{\mu\sigma} - g_{\nu\sigma} M_{\mu\rho} - g_{\mu\rho} M_{\nu\sigma} + g_{\mu\sigma} M_{\nu\rho}),$$

SUSY Algebra

$$[Q_\alpha^i, P_\mu] = [\bar{Q}_{\dot{\alpha}}^i, P_\mu] = 0,$$

$$[Q_\alpha^i, M_{\mu\nu}] = \frac{1}{2}(\sigma_{\mu\nu})_\alpha^\beta Q_\beta^i, [\bar{Q}_{\dot{\alpha}}^i, M_{\mu\nu}] = -\frac{1}{2}\bar{Q}_{\dot{\beta}}^i (\bar{\sigma}_{\mu\nu})_{\dot{\alpha}}^{\dot{\beta}},$$

$$\{Q_\alpha^i, \bar{Q}_{\dot{\beta}}^j\} = 2\delta^{ij} (\sigma^\mu)_{\alpha\dot{\beta}} P_\mu$$

$$\alpha, \dot{\alpha}, \beta, \dot{\beta} = 1, 2; i, j = 1, 2, \dots, N.$$

Superspace

$$x_\mu \rightarrow x_\mu, \theta_\alpha, \bar{\theta}_{\dot{\alpha}}$$

$$\alpha, \dot{\alpha} = 1, 2$$

Grassmannian
parameters

$$\theta_\alpha^2 = 0, \bar{\theta}_{\dot{\alpha}}^2 = 0$$

SUSY Generators

$$Q_\alpha = \frac{\partial}{\partial \theta_\alpha} - i\sigma_{\alpha\dot{\alpha}}^\mu \bar{\theta}^{\dot{\alpha}} \partial_\mu$$

$$\bar{Q}_{\dot{\alpha}} = -\frac{\partial}{\partial \bar{\theta}_{\dot{\alpha}}} + i\theta_\alpha \sigma_{\alpha\dot{\alpha}}^\mu \partial_\mu$$

$$Q_\alpha^2 = 0, \bar{Q}_{\dot{\alpha}}^2 = 0$$

This is the only possible graded Lie algebra that mixes integer and half-integer spins and changes statistics

Quantum States

Quantum states: Vacuum = $|E, \lambda\rangle$ $Q|E, \lambda\rangle = 0$

$[Q_\alpha^i, P_\mu] = [\bar{Q}_\alpha^i, P_\mu] = 0$ Energy helicity

State	Expression	# of states
vacuum	$ E, \lambda\rangle$	1
1-particle	$\bar{Q}_i E, \lambda\rangle = E, \lambda + 1/2\rangle$	$\binom{N}{1} = N$
2-particle	$\bar{Q}_i \bar{Q}_j E, \lambda\rangle = E, \lambda + 1\rangle$	$\binom{N}{2} = \frac{N(N-1)}{2}$
...
N-particle	$\bar{Q}_1 \bar{Q}_2 \dots \bar{Q}_N E, \lambda\rangle = E, \lambda + N/2\rangle$	$\binom{N}{N} = 1$

Total # of states: $\sum_{k=0}^N \binom{N}{k} = 2^N = 2^{N-1} \text{ bosons} + 2^{N-1} \text{ fermions}$

SUSY Multiplets

Chiral multiplet $N = 1, \lambda = 0$

helicity	-1/2	0	1/2
# of states	1	2	1

scalar spinor
 (φ, ψ)

Vector multiplet $N = 1, \lambda = 1/2$

helicity	-1	-1/2	1/2	1
# of states	1	1	1	1

(λ, A_μ)
 spinor vector

Members of a supermultiplet are called **superpartners**

N=4	SUSY YM	helicity	-1	-1/2	0	1/2	1				
	$\lambda = -1$	# of states	1	4	6	4	1				
N=8	SUGRA	helicity	-2	-3/2	-1	-1/2	0	1/2	1	3/2	2
	$\lambda = -2$	# of states	1	8	28	56	70	56	28	8	1

$N \leq 4S$ ← spin

$N \leq 4$ For renormalizable theories (YM)

$N \leq 8$ For (super)gravity

Simplest (N=1) SUSY Multiplets

Bosons and Fermions come in pairs

(φ, ψ)

(λ, A_μ)

(\tilde{g}, g)

Spin 0

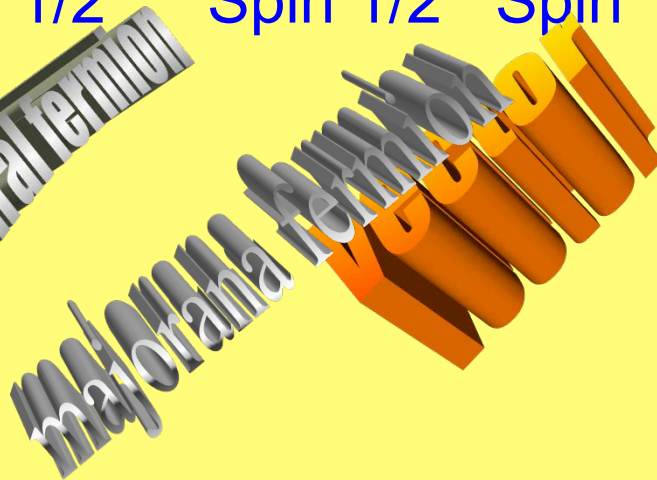
Spin 1/2

Spin 1/2

Spin 1

Spin 3/2

Spin 2



SUSY Transformation

N=1 SUSY Chiral supermultiplet:

spin=0

spin=1/2

$$\begin{aligned} \delta_\epsilon A &= \sqrt{2}\epsilon\psi, \\ \delta_\epsilon \psi &= i\sqrt{2}\sigma^\mu \bar{\epsilon} \partial_\mu A + \sqrt{2}\epsilon F, \\ \delta_\epsilon F &= i\sqrt{2}\bar{\epsilon}\sigma^\mu \partial_\mu \psi \end{aligned}$$

parameter of SUSY transformation
(spinor)

Auxiliary field

(unphysical d.o.f. needed to close SUSY algebra)

SUSY multiplets \rightarrow Superfield in Superspace

$$\begin{aligned} \Phi(y, \theta) &= A(y) + \sqrt{2}\theta\psi(y) + \theta\theta F(y) \\ &= A(x) + i\theta\sigma^\mu \bar{\theta} \partial_\mu A(x) + \frac{1}{4}\theta\theta\bar{\theta}\bar{\theta}W(x) \\ &\quad + \sqrt{2}\theta\psi(x) - i/\sqrt{2}\theta\theta\partial_\mu \psi(x)\sigma^\mu \bar{\theta} + \theta\theta F(x) \end{aligned}$$

$$(y = x + i\theta\sigma\bar{\theta})$$

Expansion over grassmannian parameter

superfield

component fields

$$\theta^2 = \theta_1\theta_2, \quad \theta_1^2 = \theta_2^2 = 0!$$

Gauge superfields

Gauge superfield

$$\begin{aligned}
 V(x, \theta, \bar{\theta}) = & C(x) + i\theta\chi(x) - i\bar{\theta}\bar{\chi}(x) + i\theta\theta M(x) - i\bar{\theta}\bar{\theta}M^+(x) \\
 & -\theta\sigma^\mu\bar{\theta}v_\mu(x) + i\theta\theta\bar{\theta}[\bar{\lambda}(x) + i\bar{\sigma}^\mu\partial_\mu\chi(x)] - i\bar{\theta}\bar{\theta}\theta[\lambda(x) + i\sigma^\mu\partial_\mu\bar{\chi}(x)] \\
 & + \frac{1}{2}\theta\theta\bar{\theta}\bar{\theta}[D(x) + \frac{1}{2}\mathbb{W}C(x)]
 \end{aligned}$$

Field strength tensor

$$W_\alpha = -\frac{1}{4}\bar{D}^2 e^V D_\alpha e^{-V}$$

Gauge transformation

$$V \rightarrow V + \Phi + \bar{\Phi}$$

$$C \rightarrow C + A + A^*$$

$$\chi \rightarrow \chi - i\sqrt{2}\psi$$

$$M \rightarrow M - 2iF$$

$$v_\mu \rightarrow v_\mu - i\partial_\mu(A - A^*)$$

$$\lambda \rightarrow \lambda$$

$$D \rightarrow D$$

Wess-Zumino gauge

$$C = \chi = M = 0$$

physical fields

Covariant derivatives

$$D_\alpha = \frac{\partial}{\partial\vartheta_\alpha} + i\sigma_{\alpha\dot{\alpha}}^\mu \vartheta^{\dot{\alpha}} \partial_\mu$$

$$\bar{D}_{\dot{\alpha}} = -\frac{\partial}{\partial\bar{\theta}_{\dot{\alpha}}} - i\bar{\theta}_{\dot{\alpha}} \sigma_{\alpha\dot{\alpha}}^\mu \partial_\mu$$

$$W_\alpha = -i\lambda_\alpha + \theta_\alpha D - \frac{i}{2}(\sigma^\mu \bar{\sigma}^\nu \theta)_\alpha F_{\mu\nu} + \theta^2 \sigma^\mu D_\mu \bar{\lambda}$$

How to write SUSY Lagrangians

1st step

Take your favorite Lagrangian written in terms of fields

2nd step

Replace *Field* $(\varphi, \psi, A_\mu) \Rightarrow$ *Superfield* (Φ, V)

3rd step

Replace

$$\textit{Action} = \int d^4x L(x) \quad \Rightarrow \quad \int d^4x d^4\theta L(x, \theta, \bar{\theta})$$

Grassmannian integration in superspace

$$\int d\theta_\alpha = 0, \quad \int \theta_\beta d\theta_\alpha = \delta_{\alpha\beta}$$

Minimal Supersymmetric Standard Model (MSSM)

- SUSY: # of fermions = # of bosons N=1 SUSY: (φ, ψ) (λ, A_μ)
- SM: 28 bosonic d.o.f. & 90 (96) fermionic d.o.f.

There are no particles in the SM that can be superpartners

SUSY associates known bosons with new fermions and known fermions with new bosons

- Even number of the Higgs doublets – min = 2
- Cancellation of axial anomalies (in each generation)

$$Tr Y^3 = 3\left(\frac{1}{27} + \frac{1}{27} - \frac{64}{27} + \frac{8}{27}\right) - 1 - 1 + 8 = 0$$

colour
 u_L
 d_L
 u_R
 d_R
 ν_L
 e_L
 e_R

Higgsinos

$$-1+1=0$$

Particle Content of the MSSM

Superfield	Bosons	Fermions	$SU_c(3)$	$SU_L(2)$	$U_Y(1)$			
<i>Gauge</i>								
G^a	gluon g^a	gluino \tilde{g}^a	8	1	0			
V^k	Weak $W^k (W^\pm, Z)$	wino, zino $\tilde{w}^k (\tilde{w}^\pm, \tilde{z})$	1	3	0			
V'	Hypercharge $B(\gamma)$	binos $\tilde{b}(\tilde{\gamma})$	1	1	0			
<i>Matter</i>								
L_i	sleptons	$\tilde{L}_i = (\tilde{\nu}, \tilde{e})_L$	leptons	$L_i = (\nu, e)_L$	1	2	-1	
E_i				$\tilde{E}_i = \tilde{e}_R$	$E_i = e_R$	1	1	2
Q_i	squarks	$\tilde{Q}_i = (\tilde{u}, \tilde{d})_L$	quarks	$Q_i = (u, d)_L$	3	2	1/3	
U_i				$\tilde{U}_i = \tilde{u}_R$	$U_i = u_R^c$	3^*	1	-4/3
D_i				$\tilde{D}_i = \tilde{d}_R$	$D_i = d_R^c$	3^*	1	2/3
<i>Higgs</i>								
H_1	Higgses	H_1	higgsinos	\tilde{H}_1	1	2	-1	
H_2				H_2	\tilde{H}_2	1	2	1

The MSSM Lagrangian

$$L = L_{gauge} + L_{Yukawa} + L_{SoftBreaking}$$

The Yukawa Superpotential

Superfields

$$W_R = y_U Q_L H_2 U_R + y_D Q_L H_1 D_R + y_L L_L H_1 E_R + \mu H_1 H_2$$

Yukawa couplings

Higgs mixing term

$$W_{NR} = \lambda_L L_L L_L E_R + \lambda'_L L_L Q_L D_R + \mu' L_L H_2 + \lambda_B U_R D_R D_R$$

Violate:

Lepton number

Baryon number

$$\lambda_L, \lambda'_L < 10^{-6}, \quad \lambda_B < 10^{-9}$$

These terms are forbidden in the SM

R-parity

$$R = (-)^{3(B-L)+2S}$$

The Usual Particle : $R = +1$
SUSY Particle : $R = -1$

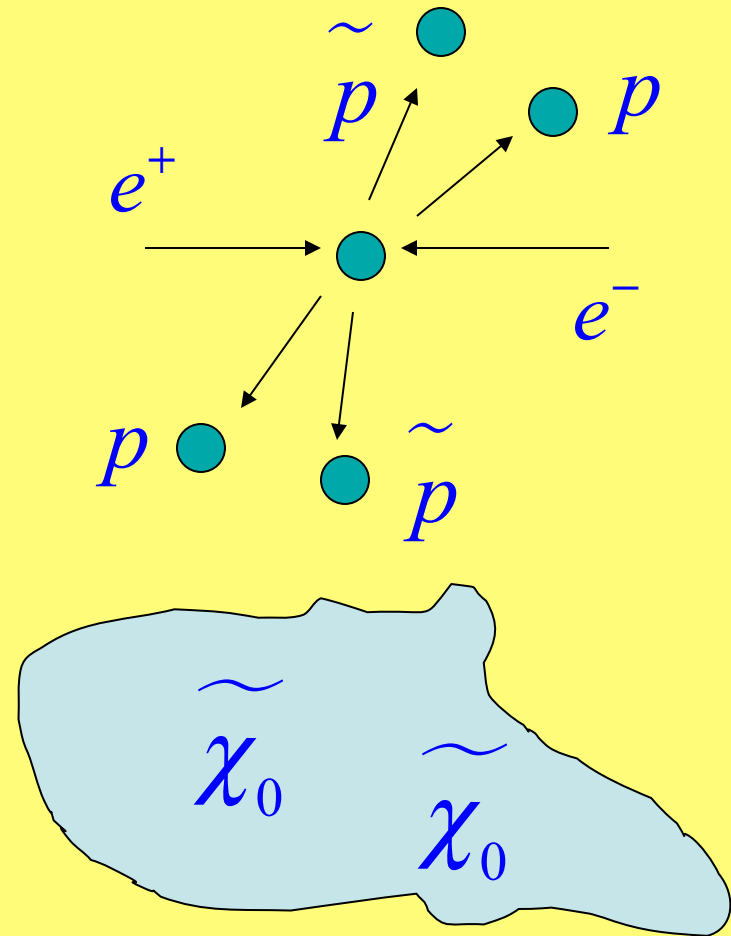
B - Baryon Number
L - Lepton Number
S - Spin

The consequences:

- The superpartners are created in pairs
- The lightest superparticle is stable



- The lightest superparticle (LSP) should be neutral - the best candidate is neutralino (photino or higgsino) $\tilde{\chi}_0$
- It can survive from the Big Bang and form the Dark matter in the Universe

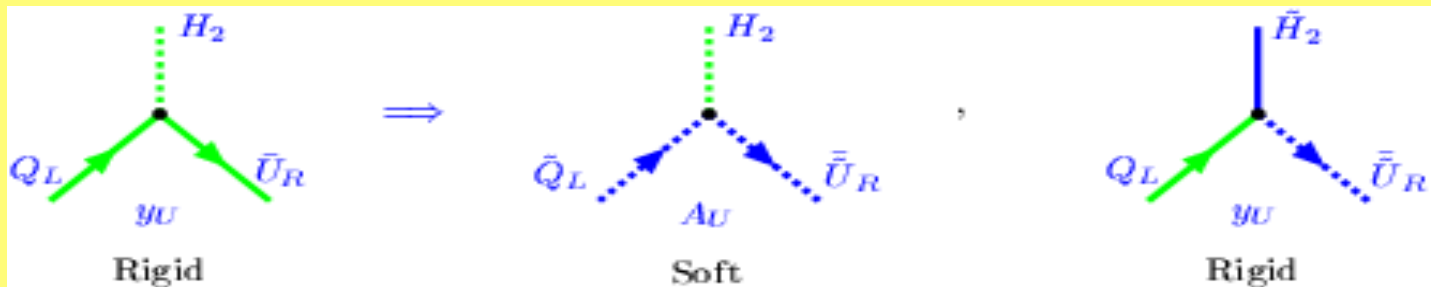
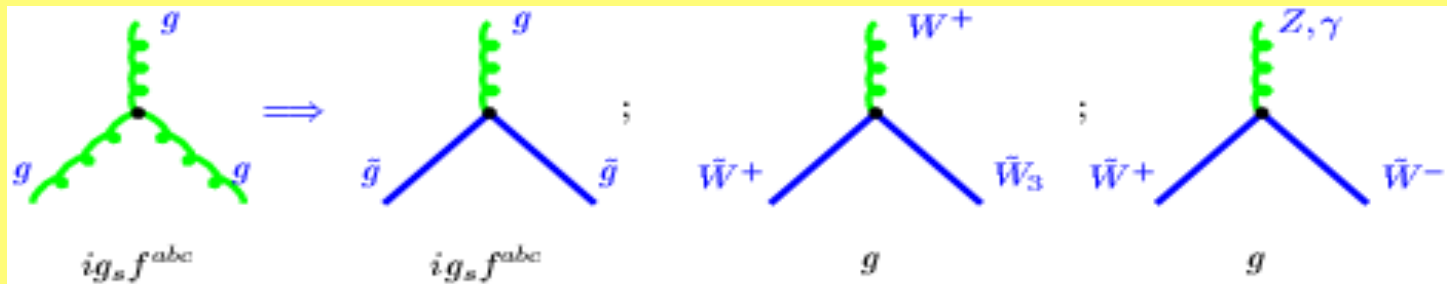
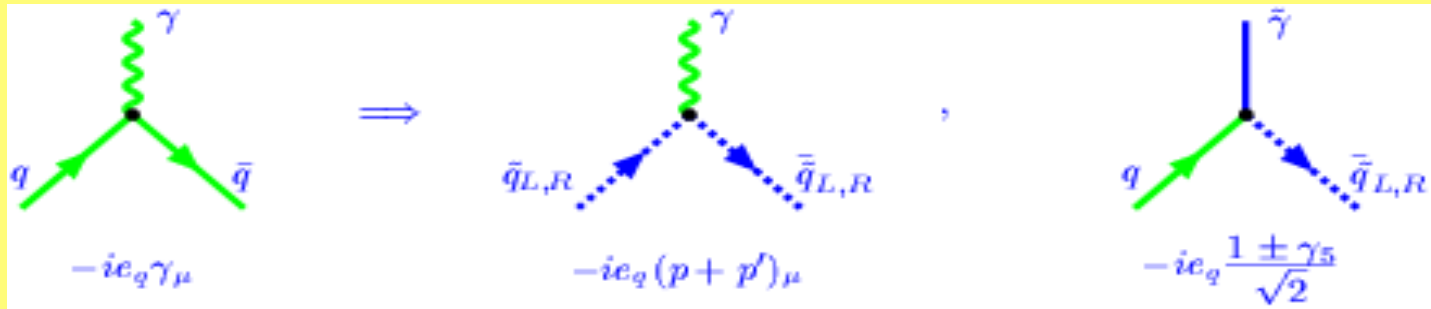


Interactions in the MSSM

SM



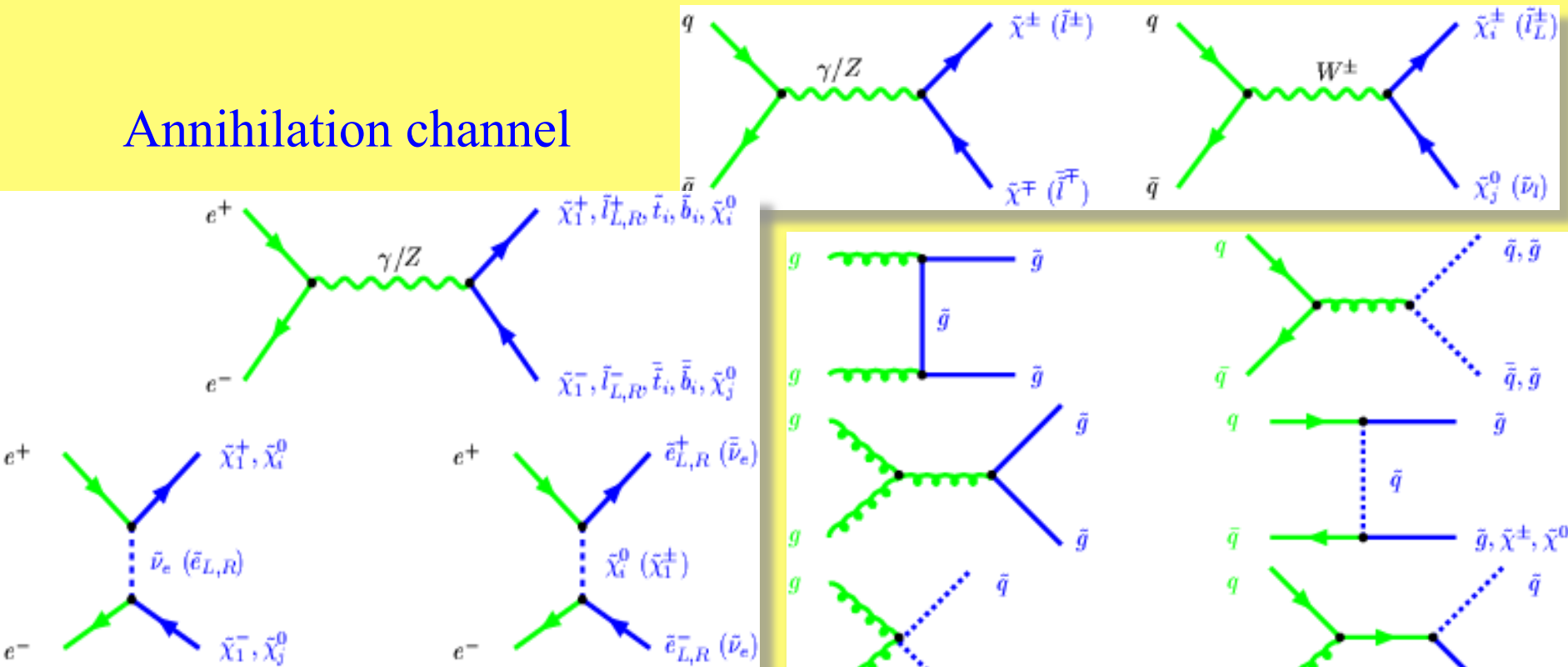
MSSM



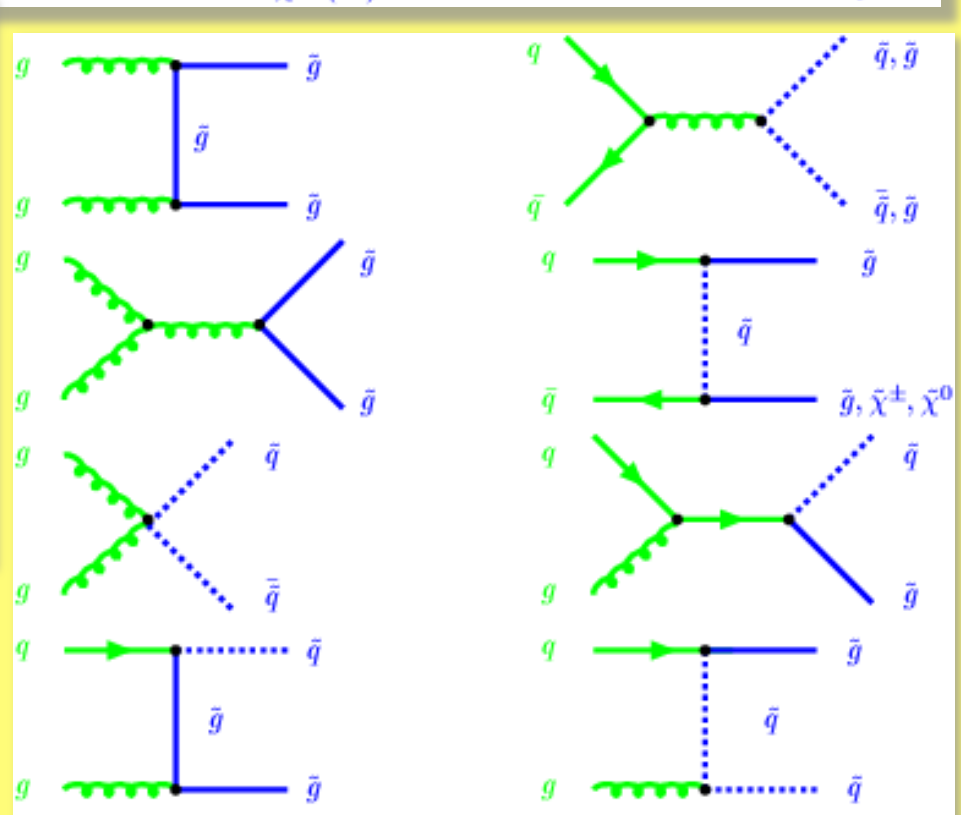
SM → MSSM

Creation of Superpartners at colliders

Annihilation channel



Gluon fusion, ee, qq scattering and qq scattering channels



Decay of Superpartners

squarks

$$\tilde{q}_{L,R} \rightarrow q + \tilde{\chi}_i^0$$

$$\tilde{q}_L \rightarrow q' + \tilde{\chi}_i^\pm$$

$$\tilde{q}_{L,R} \rightarrow q + g$$

sleptons

$$\tilde{l} \rightarrow l + \tilde{\chi}_i^0$$

$$\tilde{l}_L \rightarrow \nu_l + \tilde{\chi}_i^\pm$$

chargino

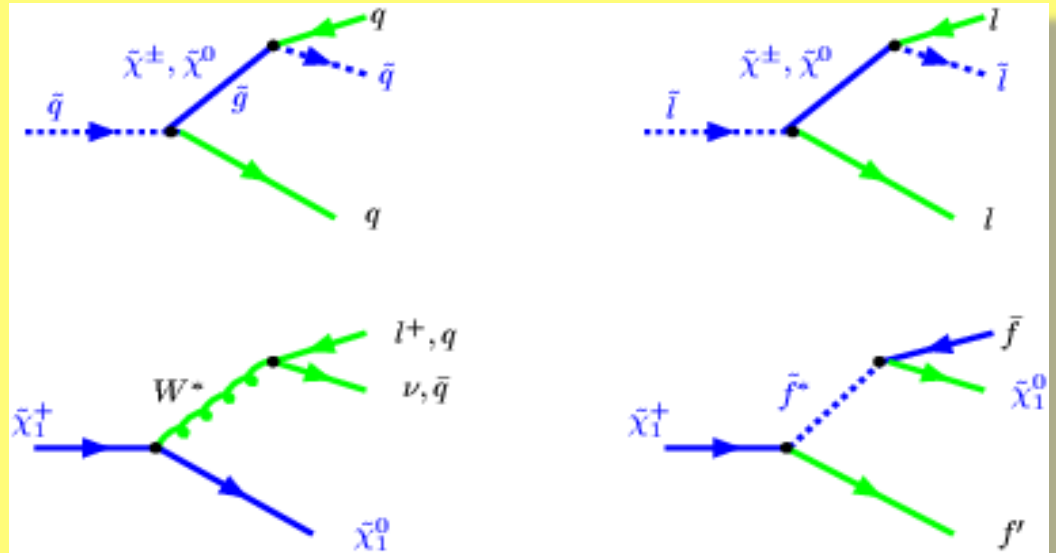
$$\tilde{\chi}_i^\pm \rightarrow e + \nu_e + \tilde{\chi}_i^0$$

$$\tilde{\chi}_i^\pm \rightarrow q + \bar{q}' + \tilde{\chi}_i^0$$

gluino

$$\tilde{g} \rightarrow q + \bar{q} + \tilde{\gamma}$$

$$\tilde{g} \rightarrow g + \tilde{\gamma}$$



neutralino

$$\tilde{\chi}_i^0 \rightarrow \tilde{\chi}_1^0 + l^+ + l^-$$

$$\tilde{\chi}_i^0 \rightarrow \tilde{\chi}_1^0 + q + \bar{q}'$$

$$\tilde{\chi}_i^0 \rightarrow \tilde{\chi}_1^\pm + l^\pm + \nu_l$$

$$\tilde{\chi}_i^0 \rightarrow \tilde{\chi}_1^0 + \nu_l + \bar{\nu}_l$$

Final states

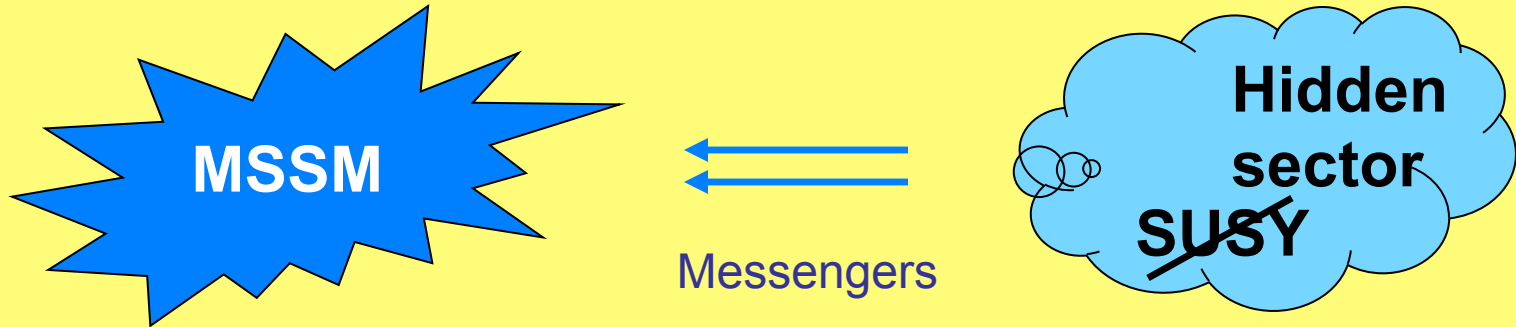
$$l^+ l^- + \cancel{E}_T$$

$$2 \text{ jets} + \cancel{E}_T$$

$$\gamma + \cancel{E}_T$$

$$\cancel{E}_T$$

Soft SUSY Breaking



Gravitons, gauge, gauginos, etc

Breaking via F and D terms in a hidden sector

$$-L_{Soft} = \sum_{\alpha} M_{\alpha} \tilde{\lambda}_{\alpha} \tilde{\lambda}_{\alpha} + \sum_i m_{0i}^2 |A_i|^2 + \sum_{ijk} A_{ijk} A_i A_j A_k + \sum_{ij} B_{ij} A_i A_j$$

↑
↑
↑
↑

gauginos
scalar fields

Over 100 of free parameters !

MSSM Parameter Space

- Three gauge couplings
- Three (four) Yukawa matrices
- The Higgs mixing parameter
- Soft SUSY breaking terms

mSUGRA Universality hypothesis (gravity is colour and flavour blind):
Soft parameters are equal at Planck (GUT) scale

$$-L_{Soft} = A\{y_t Q_L H_2 U_R + y_b Q_L H_1 D_R + y_L L_L H_1 E_R\} + B\mu H_1 H_2 + m_0^2 \sum_i |\varphi_i|^2 + \frac{1}{2} M_{1/2} \sum_\alpha \widetilde{\lambda}_\alpha \widetilde{\lambda}_\alpha$$

Five universal soft parameters:

$$A, m_0, M_{1/2}, B \leftrightarrow \tan\beta = v_2 / v_1 \quad \text{and} \quad \mu$$

versus

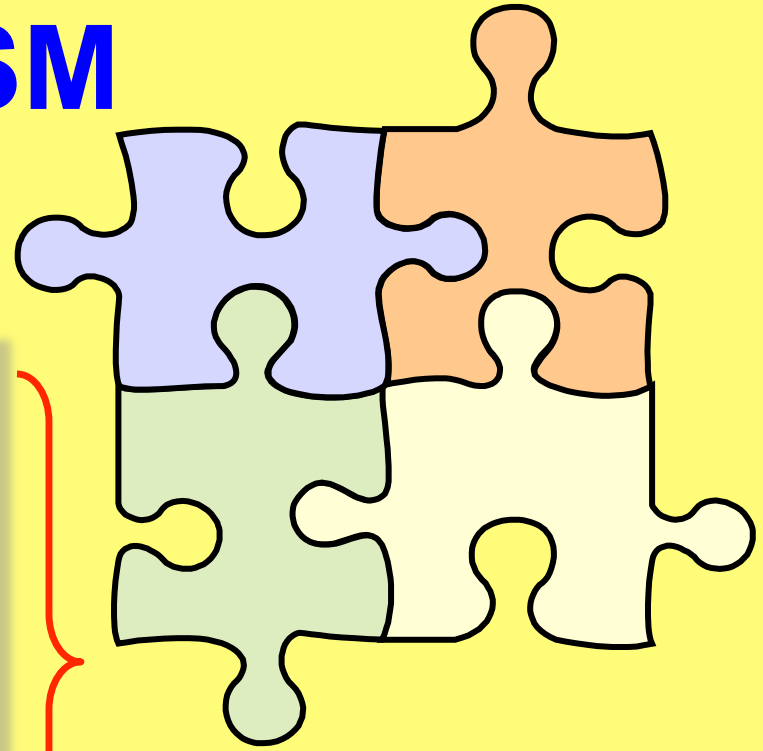
$$m \quad \text{and} \quad \lambda$$

in the SM

Constrained MSSM

Requirements:

- Unification of the gauge couplings
- Radiative EW Symmetry Breaking
- Heavy quark and lepton masses
- Rare decays ($b \rightarrow s\gamma$)
- Anomalous magnetic moment of muon
- LSP is neutral
- Amount of the Dark Matter
- Experimental limits from direct search

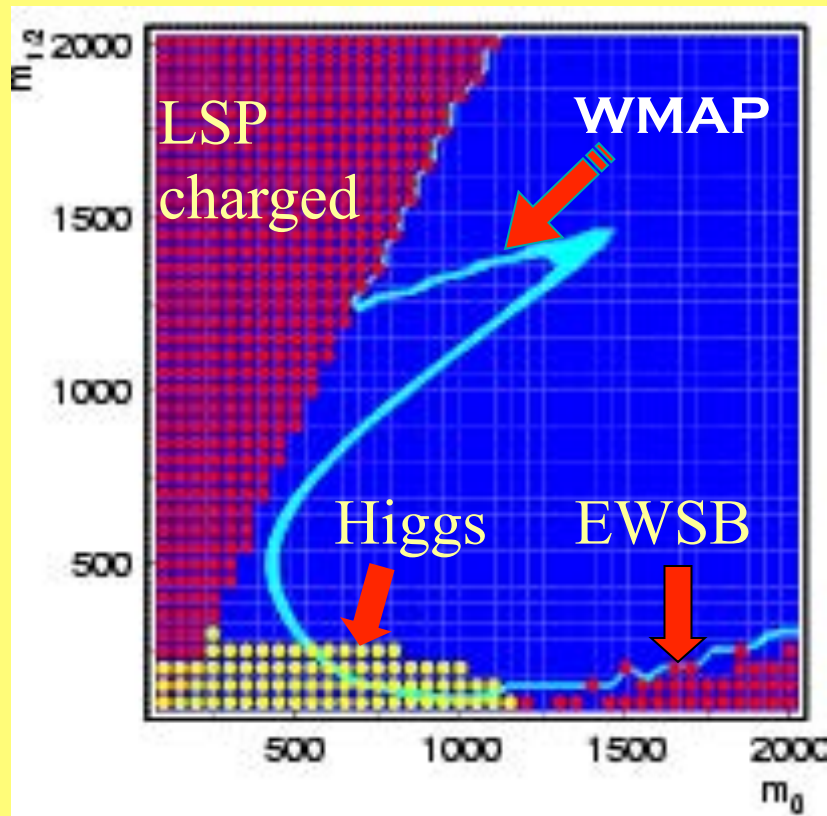


$A_0, m_0, M_{1/2}, \mu, \tan \beta$

Allowed region
in the parameter
space of the MSSM

$$100 \text{ GeV} \leq m_0, M_{1/2}, \mu \leq 2 \text{ TeV}$$
$$-3m_0 \leq A_0 \leq 3m_0, 1 \leq \tan \beta \leq 70$$

Allowed regions after WMAP



$$\tan \beta = 50$$

In allowed region one fulfills all the constraints simultaneously and has the suitable amount of the dark matter

Narrow allowed region enables one to predict the particle spectra and the main decay patterns

Phenomenology essentially depends on the region of parameter space and has direct influence on the strategy of SUSY searches

Mass Spectrum in CMSSM

(Sample)

SUSY Masses in GeV

Fitted SUSY Parameters

Fitted SUSY Parameters			Symbol	Low tan β	High tan β
Symbol	Low tan β	High tan β	$\tilde{\chi}_1^0(\tilde{B}), \tilde{\chi}_2^0(\tilde{W}^3)$	214, 413	170, 322
Tan β	1.71	35.0	$\tilde{\chi}_3^0(\tilde{H}_1), \tilde{\chi}_4^0(\tilde{H}_2)$	1028, 1016	481, 498
m_0	200	600	$\tilde{\chi}_1^\pm(\tilde{W}^\pm), \tilde{\chi}_2^\pm(\tilde{H}^\pm)$	413, 1026	322, 499
$m_{1/2}$	500	400	\tilde{g}	1155	950
$\mu(0)$	1084	-558	\tilde{e}_L, \tilde{e}_R	303, 270	663, 621
A(0)	0	0	$\tilde{\nu}_L$	290	658
$1/\alpha_{\text{GUT}}$	24.8	24.8	\tilde{q}_L, \tilde{q}_R	1028, 936	1040, 1010
M_{GUT}	$1.6 \cdot 10^{16}$	$1.6 \cdot 10^{16}$	$\tilde{\tau}_1, \tilde{\tau}_2$	279, 403	537, 634
			\tilde{b}_1, \tilde{b}_2	953, 1010	835, 915
			\tilde{t}_1, \tilde{t}_2	727, 1017	735, 906
			h, H	95, 1344	119, 565
			A, H $^\pm$	1340, 1344	565, 571