

# SUPERSYMMETRY AS THE NEAREST OPTION BEYOND THE STANDARD MODEL

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## Abstract

The present lectures contain an introduction to possible new physics beyond the Standard Model. Having in mind first of all accelerator experiments of the nearest future we concentrate on supersymmetry, a new symmetry that relates bosons and fermions, as the first target of experimental search. The motivation to introduce supersymmetry is discussed. The main notions of supersymmetry are introduced. The supersymmetric extension of the Standard Model - the Minimal Supersymmetric Standard Model - is considered in more detail. Phenomenological features of the MSSM as well as possible experimental signatures of SUSY at hadron colliders are described.

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## 1 Introduction: What is supersymmetry

*Supersymmetry* is a *boson-fermion* symmetry that is aimed to unify all forces in Nature including gravity within a single framework. Modern views on supersymmetry in particle physics are based on string paradigm, though the low energy manifestations of SUSY can be possibly found at modern colliders and in non-accelerator experiments.

Supersymmetry emerged from the attempts to generalize the Poincaré algebra to mix representations with different spin [1]. It happened to be a problematic task due to the no-go theorems preventing such generalizations [2]. The way out was found by introducing the so-called graded Lie algebras, i.e. adding the anti-commutators to the usual commutators of the Lorentz algebra. Such a generalization, described below, appeared to be the only possible one within relativistic field theory.

If  $Q$  is a generator of SUSY algebra, then acting on a boson state it produces a fermion one and vice versa

$$\bar{Q}|boson\rangle = |fermion\rangle \quad \text{and} \quad Q|fermion\rangle = |boson\rangle.$$

Since bosons commute with each other and fermions anticommute, one immediately finds that SUSY generators should also anticommute, they must be *fermionic*, i.e. they must change the spin by a half-odd amount and change the statistics. Indeed, the key element of SUSY algebra is

$$\{Q_\alpha, \bar{Q}_{\dot{\alpha}}\} = 2\sigma_{\alpha,\dot{\alpha}}^\mu P_\mu, \tag{1.1}$$

where  $Q$  and  $\bar{Q}$  are SUSY generators and  $P_\mu$  is the generator of translation, the four-momentum.

In what follows we describe SUSY algebra in more detail and construct its representations which are needed to build a SUSY generalization of the Standard Model

of fundamental interactions. Such a generalization is based on a softly broken SUSY quantum field theory and contains the SM as a low energy theory.

Supersymmetry promises to solve some problems of the SM and of Grand Unified Theories. In what follows we describe supersymmetry as a nearest option for the new physics on a TeV scale.

## 2 Motivation of SUSY in particle physics

### 2.1 Unification with gravity

The *general idea* is a unification of all forces of Nature including quantum gravity. However, the graviton has spin 2, while the other gauge bosons (photon, gluons,  $W$  and  $Z$  weak bosons) have spin 1. Therefore, they correspond to different representations of the Poincaré algebra. To mix them one can use supersymmetry transformations. Starting with the graviton state of spin 2 and acting by SUSY generators we get the following chain of states:

$$spin\ 2 \rightarrow spin\ 3/2 \rightarrow spin\ 1 \rightarrow spin\ 1/2 \rightarrow spin\ 0.$$

Thus, a partial unification of matter (fermions) with forces (bosons) naturally arises from an attempt to unify gravity with other interactions.

Taking infinitesimal transformations  $\delta_\epsilon = \epsilon^\alpha Q_\alpha$ ,  $\bar{\delta}_{\bar{\epsilon}} = \bar{Q}_{\dot{\alpha}} \bar{\epsilon}^{\dot{\alpha}}$ , and using eq.(1.1) one gets

$$\{\delta_\epsilon, \bar{\delta}_{\bar{\epsilon}}\} = 2(\epsilon\sigma^\mu\bar{\epsilon})P_\mu, \quad (2.1)$$

where  $\epsilon$  is a transformation parameter. Choosing  $\epsilon$  to be local, i.e. a function of a space-time point  $\epsilon = \epsilon(x)$ , one finds from eq.(2.1) that an anticommutator of two SUSY transformations is a local coordinate translation. And a theory which is invariant under local coordinate transformation is General Relativity. Thus, making SUSY local, one naturally obtains General Relativity, or a theory of gravity, or supergravity [3].

### 2.2 Unification of gauge couplings

According to the Grand Unification *hypothesis*, gauge symmetry increases with energy [4]. All known interactions are different branches of a unique interaction associated with a simple gauge group. The unification (or splitting) occurs at high energy. To reach this goal one has to consider how the couplings change with energy. This is described by the renormalization group equations. In the SM the strong and weak couplings associated with non-Abelian gauge groups decrease with energy, while the electromagnetic one associated with the Abelian group on the contrary increases. Thus, it becomes possible that at some energy scale they become equal.

After the precise measurement of the  $SU(3) \times SU(2) \times U(1)$  coupling constants, it has become possible to check the unification numerically. The three coupling

constants to be compared are

$$\begin{aligned}
\alpha_1 &= (5/3)g'^2/(4\pi) = 5\alpha/(3\cos^2\theta_W), \\
\alpha_2 &= g^2/(4\pi) = \alpha/\sin^2\theta_W, \\
\alpha_3 &= g_s^2/(4\pi)
\end{aligned}
\tag{2.2}$$

where  $g'$ ,  $g$  and  $g_s$  are the usual  $U(1)$ ,  $SU(2)$  and  $SU(3)$  coupling constants and  $\alpha$  is the fine structure constant. The factor of  $5/3$  in the definition of  $\alpha_1$  has been included for proper normalization of the generators.

In the modified minimal subtraction ( $\overline{MS}$ ) scheme, the world averaged values of the couplings at the  $Z^0$  energy are obtained from a fit to the LEP and Tevatron data [5]:

$$\begin{aligned}
\alpha^{-1}(M_Z) &= 128.978 \pm 0.027 \\
\sin^2\theta_{\overline{MS}} &= 0.23146 \pm 0.00017 \\
\alpha_s &= 0.1184 \pm 0.0031,
\end{aligned}
\tag{2.3}$$

that gives

$$\alpha_1(M_Z) = 0.017, \quad \alpha_2(M_Z) = 0.034, \quad \alpha_3(M_Z) = 0.118 \pm 0.003.
\tag{2.4}$$

Assuming that the SM is valid up to the unification scale, one can then use the known RG equations for the three couplings. In the leading order they are:

$$\frac{d\tilde{\alpha}_i}{dt} = b_i\tilde{\alpha}_i^2, \quad \tilde{\alpha}_i = \frac{\alpha_i}{4\pi}, \quad t = \log\left(\frac{Q^2}{\mu^2}\right),
\tag{2.5}$$

where for the SM the coefficients are  $b_i = (41/10, -19/6, -7)$ .

The solution to eq.(2.5) is very simple

$$\frac{1}{\tilde{\alpha}_i(Q^2)} = \frac{1}{\tilde{\alpha}_i(\mu^2)} - b_i \log\left(\frac{Q^2}{\mu^2}\right).
\tag{2.6}$$

The result is demonstrated in Fig.1 showing the evolution of the inverse of the couplings as a function of the logarithm of energy. In this presentation, the evolution becomes a straight line in first order. The second order corrections are small and do not cause any visible deviation from a straight line. Fig.1 clearly demonstrates that within the SM the coupling constant unification at a single point is impossible. It is excluded by more than 8 standard deviations. This result means that the unification can only be obtained if new physics enters between the electroweak and the Planck scales.

In the SUSY case, the slopes of the RG evolution curves are modified. The coefficients  $b_i$  in eq.(2.5) now are  $b_i = (33/5, 1, -3)$ . The SUSY particles are assumed to effectively contribute to the running of the coupling constants only for energies above the typical SUSY mass scale. It turns out that within the SUSY model a

## Unification of the Coupling Constants in the SM and the minimal MSSM

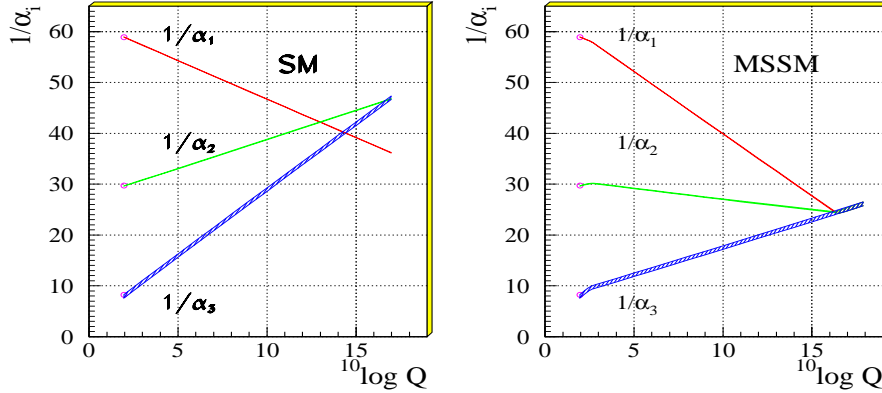


Figure 1: Evolution of the inverse of the three coupling constants in the Standard Model (left) and in the supersymmetric extension of the SM (MSSM) (right). [6]

perfect unification can be obtained as is shown in Fig.1. From the fit requiring unification one finds for the break point  $M_{SUSY}$  and the unification point  $M_{GUT}$  [6]

$$\begin{aligned}
 M_{SUSY} &= 10^{3.4 \pm 0.9 \pm 0.4} \text{ GeV}, \\
 M_{GUT} &= 10^{15.8 \pm 0.3 \pm 0.1} \text{ GeV}, \\
 \alpha_{GUT}^{-1} &= 26.3 \pm 1.9 \pm 1.0,
 \end{aligned}
 \tag{2.7}$$

The first error originates from the uncertainty in the coupling constant, while the second one is due to the uncertainty in the mass splittings between the SUSY particles.

This observation was considered as the first "evidence" for supersymmetry, especially since  $M_{SUSY}$  was found in the range preferred by the fine-tuning arguments.

### 2.3 Solution of the hierarchy problem

The appearance of two different scales  $V \gg v$  in a GUT theory, namely,  $M_W$  and  $M_{GUT}$ , leads to a very serious problem which is called the *hierarchy problem*. There are two aspects of this problem.

The first one is the very existence of the hierarchy. To get the desired spontaneous symmetry breaking pattern, one needs

$$\begin{aligned}
 m_H &\sim v \sim 10^2 \text{ GeV} & \frac{m_H}{m_\Sigma} &\sim 10^{-14} \ll 1, \\
 m_\Sigma &\sim V \sim 10^{16} \text{ GeV} & &
 \end{aligned}
 \tag{2.8}$$

where  $H$  and  $\Sigma$  are the Higgs fields responsible for the spontaneous breaking of the  $SU(2)$  and the GUT groups, respectively. The question arises of how to get so small number in a natural way.

The second aspect of the hierarchy problem is connected with the preservation of a given hierarchy. Even if we choose the hierarchy like eq.(2.8) the radiative corrections will destroy it! To see this, consider the radiative correction to the light Higgs mass given by the Feynman diagram shown in Fig.2. This correction

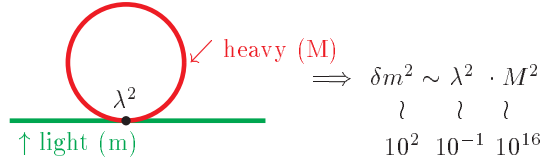


Figure 2: Radiative correction to the light Higgs boson mass

proportional to the mass squared of the heavy particle, obviously, spoils the hierarchy if it is not cancelled. This very accurate cancellation with a precision  $\sim 10^{-14}$  needs a fine tuning of the coupling constants.

The only known way of achieving this kind of cancellation of quadratic terms (also known as the cancellation of the quadratic divergencies) is supersymmetry. Moreover, SUSY automatically cancels quadratic corrections in all orders of PT. This is due to the contributions of superpartners of ordinary particles. The contribution from boson loops cancels those from the fermion ones because of an additional factor (-1) coming from Fermi statistics, as shown in Fig.3. One can see here two types

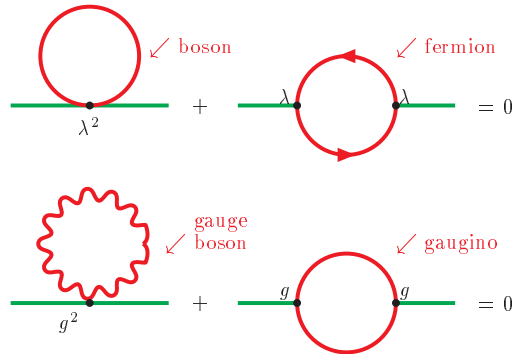


Figure 3: Cancellation of quadratic terms (divergencies)

of contribution. The first line is the contribution of the heavy Higgs boson and its superpartner. The strength of interaction is given by the Yukawa coupling  $\lambda$ . The second line represents the gauge interaction proportional to the gauge coupling constant  $g$  with the contribution from the heavy gauge boson and heavy gaugino.

In both the cases the cancellation of quadratic terms takes place. This cancellation is true up to the SUSY breaking scale,  $M_{SUSY}$ , which should not be very large ( $\leq 1$  TeV) to make the fine-tuning natural. Indeed, let us take the Higgs boson mass. Requiring for consistency of perturbation theory that the radiative corrections to

the Higgs boson mass do not exceed the mass itself gives

$$\delta M_h^2 \sim g^2 M_{SUSY}^2 \sim M_h^2. \quad (2.9)$$

So, if  $M_h \sim 10^2$  GeV and  $g \sim 10^{-1}$ , one needs  $M_{SUSY} \sim 10^3$  GeV in order that the relation (2.9) is valid. Thus, we again get the same rough estimate of  $M_{SUSY} \sim 1$  TeV as from the gauge coupling unification above.

That is why it is usually said that supersymmetry solves the hierarchy problem. We show below how SUSY can also explain the origin of the hierarchy.

## 2.4 Astrophysics and Cosmology

The shining matter is not the only one in the Universe. Considerable amount consists of the so-called dark matter. The direct evidence for the presence of the dark matter are the rotation curves of galaxies (see Fig.4) [7]. What is shown here is the rotation

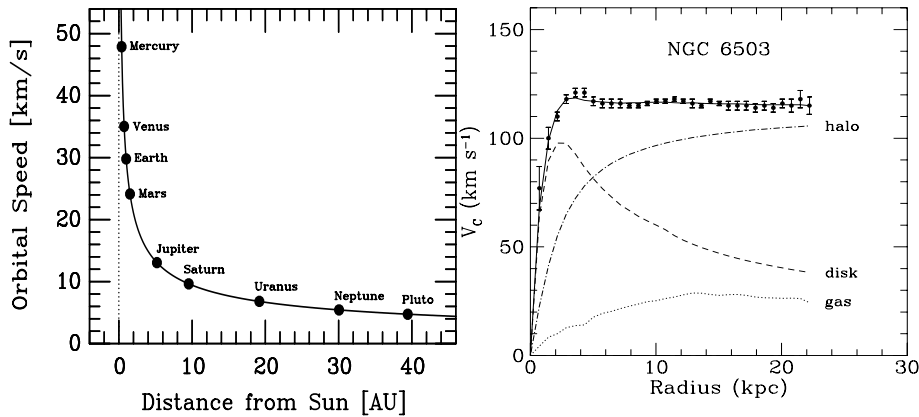


Figure 4: Rotation curves for the solar system and galaxy

speed of the planets of the solar system (left) and the stars in some typical spiral galaxy (right) as a function of a distance from the sun/center of galaxy. One can see that in the solar system all the planets perfectly fit the curve obtained from Newton mechanics: centrifugal force is equal to gravitational force

$$\frac{mv^2}{r} = G \frac{mM}{r^2}, \Rightarrow v = \sqrt{\frac{GM}{r}}.$$

At the same time, if one looks at stars in the galaxy, one finds a completely different picture. To explain these curves, one has to assume the existence of galactic halo made of non shining matter which takes part in gravitational interaction. The flat rotation curves of spiral galaxies provide the most direct evidence for the existence of a large amount of the dark matter. Spiral galaxies consist of a central bulge and

a very thin disc, and are surrounded by an approximately spherical halo of the dark matter.

According to the latest data [8], the matter content of the Universe is the following:

$$\Omega h^2 = 1 \quad \Leftrightarrow \quad \rho = \rho_{crit}$$

$$\Omega_{vacuum} \approx 73\%, \quad \Omega_{DarkMatter} \approx 23\%, \quad \Omega_{Baryon} \approx 4\%$$

Therefore, the amount of the Dark matter is almost 6 times larger than the usual matter in the Universe.

There are two possible types of the dark matter: the hot one, consisting of light relativistic particles and the cold one, consisting of massive weakly interacting particles (WIMPs). The hot dark matter might consist of neutrinos; however, this has problems with galaxy formation. As for the cold dark matter, it has no candidates within the SM. At the same time, SUSY provides an excellent candidate for the cold dark matter, namely neutralino, the lightest superparticle.

### 3 Basics of supersymmetry

Sending off the interested reader to [9] for details we present here the main ideas and building blocks for constructing a supersymmetric quantum field theory.

#### 3.1 Algebra of SUSY

Combined with the usual Poincaré and internal symmetry algebra the Super-Poincaré Lie algebra contains additional SUSY generators  $Q_\alpha^i$  and  $\bar{Q}_{\dot{\alpha}}^i$  [9]

$$\begin{aligned} [P_\mu, P_\nu] &= 0, \\ [P_\mu, M_{\rho\sigma}] &= i(g_{\mu\rho}P_\sigma - g_{\mu\sigma}P_\rho), \\ [M_{\mu\nu}, M_{\rho\sigma}] &= i(g_{\nu\rho}M_{\mu\sigma} - g_{\nu\sigma}M_{\mu\rho} - g_{\mu\rho}M_{\nu\sigma} + g_{\mu\sigma}M_{\nu\rho}), \\ [B_r, B_s] &= iC_{rs}^t B_t, \\ [B_r, P_\mu] &= [B_r, M_{\mu\sigma}] = 0, \\ [Q_\alpha^i, P_\mu] &= [\bar{Q}_{\dot{\alpha}}^i, P_\mu] = 0, \\ [Q_\alpha^i, M_{\mu\nu}] &= \frac{1}{2}(\sigma_{\mu\nu})_\alpha^\beta Q_\beta^i, \quad [\bar{Q}_{\dot{\alpha}}^i, M_{\mu\nu}] = -\frac{1}{2}\bar{Q}_{\dot{\beta}}^i(\bar{\sigma}_{\mu\nu})^{\dot{\beta}}_{\dot{\alpha}}, \\ [Q_\alpha^i, B_r] &= (b_r)_j^i Q_\alpha^j, \quad [\bar{Q}_{\dot{\alpha}}^i, B_r] = -\bar{Q}_{\dot{\alpha}}^j (b_r)_j^i, \\ \{Q_\alpha^i, \bar{Q}_{\dot{\beta}}^j\} &= 2\delta^{ij}(\sigma^\mu)_{\alpha\dot{\beta}} P_\mu, \\ \{Q_\alpha^i, Q_\beta^j\} &= 2\epsilon_{\alpha\beta} Z^{ij}, \quad Z_{ij} = a_{ij}^r b_r, \quad Z^{ij} = Z_{ij}^+, \\ \{\bar{Q}_{\dot{\alpha}}^i, \bar{Q}_{\dot{\beta}}^j\} &= -2\epsilon_{\dot{\alpha}\dot{\beta}} Z^{ij}, \quad [Z_{ij}, \text{anything}] = 0, \\ \alpha, \dot{\alpha} &= 1, 2 \quad i, j = 1, 2, \dots, N. \end{aligned} \tag{3.10}$$

Here  $P_\mu$  and  $M_{\mu\nu}$  are four-momentum and angular momentum operators, respectively,  $B_r$  are the internal symmetry generators,  $Q_\alpha^i$  and  $\bar{Q}_{\dot{\alpha}}^i$  are the spinorial SUSY generators and  $Z_{ij}$  are the so-called central charges;  $\alpha, \dot{\alpha}, \beta, \dot{\beta}$  are the spinorial indices. In the simplest case one has one spinor generator  $Q_\alpha$  (and the conjugated



one  $\bar{Q}_{\dot{\alpha}}$ ) that corresponds to an ordinary or  $N=1$  supersymmetry. When  $N > 1$  one has an extended supersymmetry. In what follows we consider the simplest  $N=1$  case used for phenomenology.

### 3.2 Representations of SUSY algebra

To construct the representations of SUSY algebra (particle states in SUSY model) we start with the some state labeled by energy and helicity, i.e. projection of a spin on the direction of momenta

$$|E, \lambda \rangle$$

and act on it with the SUSY generator  $\bar{Q}$ . Then one obtains the other state with the same energy (because SUSY generator commutes with  $P_{\mu}$ ) but different helicity

$$\bar{Q}|E, \lambda \rangle = |E, \lambda + 1/2 \rangle. \quad (3.11)$$

Due to the nilpotent character of SUSY generators (3.10), the repeated action of the generator  $\bar{Q}$  gives zero. This is common for  $N=1$  SUSY. One has two states, one bosonic and one fermionic. This is a generic property of any supersymmetric theory that the number of bosons equals that of fermions. However, in CPT invariant theories the number of states is doubled, since CPT transformation changes the sign of helicity. Hence, in CPT invariant theories, one has to add the states with opposite helicity to the above mentioned ones.

Consider some examples. Let us take  $\lambda = 0$ . Then one has the following complete multiplet of SUSY:

$$\begin{array}{ccc}
 \text{helicity} & 0 & 1/2 \\
 N = 1 \quad \lambda = 0 & & \xrightarrow{CPT} \\
 \# \text{ of states} & 1 & 1 \\
 \text{helicity} & 0 & -1/2 \\
 & & \xrightarrow{CPT} \\
 \# \text{ of states} & 1 & 1
 \end{array}$$

which contains one complex scalar and one spinor with two helicity states.

The other multiplet can be obtained if one starts with  $\lambda = 1/2$ . Then one has:

$$\begin{array}{ccc}
 \text{helicity} & 1/2 & 1 \\
 N = 1 \quad \lambda = 1/2 & & \xrightarrow{CPT} \\
 \# \text{ of states} & 1 & 1 \\
 \text{helicity} & -1 & 1/2 \\
 & & \xrightarrow{CPT} \\
 \# \text{ of states} & 1 & 1
 \end{array}$$

This multiplet contains one spinor field and one massless vector.

Thus, one has two types of supermultiplets: the so-called chiral multiplet with  $\lambda = 0$ , which contains two physical states  $(\phi, \psi)$  with spin 0 and 1/2, respectively, and the vector multiplet with  $\lambda = 1/2$ , which also contains two physical states  $(\lambda, A_{\mu})$  with spin 1/2 and 1, respectively. These multiplets are used to describe quarks, leptons and vector bosons in SUSY generalization of the SM.

## 4 SUSY generalization of the Standard Model. The MSSM

As has been already mentioned, in SUSY theories the number of bosonic degrees of freedom equals that of fermionic. At the same time, in the SM one has 28 bosonic and 90 (96 with right handed neutrino) fermionic degrees of freedom. So the SM is to a great extent non-supersymmetric. Trying to add some new particles to supersymmetrize the SM, one should take into account the following observations:

- There are no fermions with quantum numbers of the gauge bosons;
- Higgs fields have nonzero v.e.v.s; hence they cannot be superpartners of quarks and leptons since this would induce spontaneous violation of baryon and lepton numbers;
- One needs at least two complex chiral Higgs multiplets to give masses to Up and Down quarks.

The latter is due to the form of a superpotential and chirality of matter superfields. Indeed, the superpotential should be invariant under the  $SU(3) \times SU(2) \times U(1)$  gauge group. If one looks at the Yukawa interaction in the Standard Model, one finds that it is indeed  $U(1)$  invariant since the sum of hypercharges in each vertex equals zero. In the last term this is achieved by taking the conjugated Higgs doublet  $\tilde{H} = i\tau_2 H^\dagger$  instead of  $H$ . However, in SUSY  $H$  is a chiral superfield and hence a superpotential, which is constructed out of chiral fields, can contain only  $H$  but not  $\tilde{H}$  which is an antichiral superfield.

Another reason for the second Higgs doublet is related to chiral anomalies. It is known that chiral anomalies spoil the gauge invariance and, hence, the renormalizability of the theory. They are canceled in the SM between quarks and leptons in each generation. However, if one introduces a chiral Higgs superfield, it contains higgsinos, which are chiral fermions, and contain anomalies. To cancel them one has to add the second Higgs doublet with the opposite hypercharge. Therefore, the Higgs sector in SUSY models is inevitably enlarged, it contains an even number of doublets.

*Conclusion:* In SUSY models supersymmetry associates *known* bosons with *new* fermions and *known* fermions with *new* bosons.

### 4.1 The field content

Consider the particle content of the Minimal Supersymmetric Standard Model [10]. According to the previous discussion, in the minimal version we double the number of particles (introducing a superpartner to each particle) and add another Higgs doublet (with its superpartner). Thus, the characteristic feature of any supersymmetric generalization of the SM is the presence of superpartners (see Fig.5). If supersymmetry is exact, superpartners of ordinary particles should have the same masses and have to be observed. The absence of them at modern energies is believed to be explained by the fact that their masses are very heavy, that means that supersymmetry should be broken.

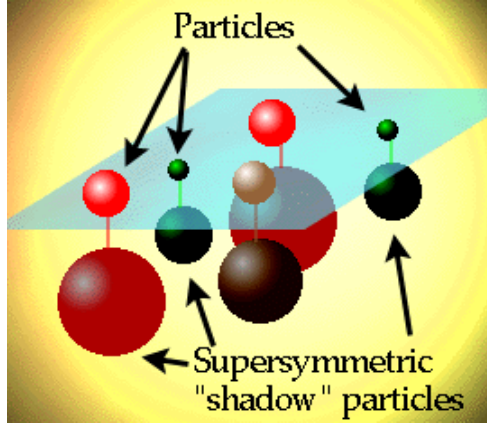


Figure 5: The shadow world of SUSY particles [11]

The particle content of the MSSM then appears as (tilde denotes a superpartner of an ordinary particle).

### Particle Content of the MSSM

Superfield	Bosons		Fermions		$SU_c(3)$	$SU_L(2)$	$U_Y(1)$
<b>Gauge</b>							
$\mathbf{G}^a$	gluon	$g^a$	gluino	$\tilde{g}^a$	8	1	0
$\mathbf{V}^k$	Weak	$W^k$ ( $W^\pm, Z$ )	wino, zino	$\tilde{w}^k$ ( $\tilde{w}^\pm, \tilde{z}$ )	1	3	0
$\mathbf{V}'$	Hypercharge	$B$ ( $\gamma$ )	bino	$\tilde{b}(\tilde{\gamma})$	1	1	0
<b>Matter</b>							
$\mathbf{L}_i$	sleptons	$\left\{ \begin{array}{l} \tilde{L}_i = (\tilde{\nu}, \tilde{e})_L \\ \tilde{E}_i = \tilde{e}_R \end{array} \right.$	leptons	$\left\{ \begin{array}{l} L_i = (\nu, e)_L \\ E_i = e_R \end{array} \right.$	1	2	-1
$\mathbf{E}_i$					1	1	2
$\mathbf{Q}_i$	squarks	$\left\{ \begin{array}{l} \tilde{Q}_i = (\tilde{u}, \tilde{d})_L \\ \tilde{U}_i = \tilde{u}_R \\ \tilde{D}_i = \tilde{d}_R \end{array} \right.$	quarks	$\left\{ \begin{array}{l} Q_i = (u, d)_L \\ U_i = u_R^c \\ D_i = d_R^c \end{array} \right.$	3	2	1/3
$\mathbf{U}_i$					3*	1	-4/3
$\mathbf{D}_i$					3*	1	2/3
<b>Higgs</b>							
$\mathbf{H}_1$	Higgses	$\left\{ \begin{array}{l} H_1 \\ H_2 \end{array} \right.$	higgsinos	$\left\{ \begin{array}{l} \tilde{H}_1 \\ \tilde{H}_2 \end{array} \right.$	1	2	-1
$\mathbf{H}_2$					1	2	1

The labels L or R for squarks or sleptons do not mean that they are left or right handed. Being spin zero particles they have no handedness. This is used to mark that they are superpartners of left or right handed quarks and leptons.

The presence of an extra Higgs doublet in SUSY model is a novel feature of the theory. In the MSSM one has two doublets with the quantum numbers (1,2,-1) and

(1,2,1), respectively:

$$H_1 = \begin{pmatrix} H_1^0 \\ H_1^- \end{pmatrix} = \begin{pmatrix} v_1 + \frac{S_1 + iP_1}{\sqrt{2}} \\ H_1^- \end{pmatrix}, \quad H_2 = \begin{pmatrix} H_2^+ \\ H_2^0 \end{pmatrix} = \begin{pmatrix} H_2^+ \\ v_2 + \frac{S_2 + iP_2}{\sqrt{2}} \end{pmatrix},$$

where  $v_i$  are the vacuum expectation values of the neutral components.

Hence, one has  $8=4+4=5+3$  degrees of freedom. As in the case of the SM, 3 degrees of freedom can be gauged away, and one is left with 5 physical states compared to 1 in the SM. Thus, in the MSSM, as actually in any of two Higgs doublet models, one has five physical Higgs bosons: two CP-even neutral, one CP-odd neutral and two charged. We consider the mass eigenstates below.

## 4.2 Lagrangian of the MSSM

The Lagrangian of the MSSM consists of two parts; the first part is SUSY generalization of the Standard Model, while the second one represents the SUSY breaking as mentioned above.

$$\mathcal{L} = \mathcal{L}_{SUSY} + \mathcal{L}_{Breaking}. \quad (4.12)$$

$\mathcal{L}_{SUSY}$  contains the usual gauge invariant kinetic terms for the matter fields and the gauge bosons as well as for their superpartners and has no free parameters. Everything is fixed by gauge invariance. There is also Yukawa type interaction, like in the SM. However explicit Higgs potential is absent. It is calculated from the superpotential in a straightforward way as will be shown below.

The Yukawa interaction in the MSSM consists of two parts. The first one almost exactly repeats that of the SM except that the fields are now the supermultiplets rather than the ordinary fields of the SM. The only difference is the last term which describes the Higgs mixing. It is absent in the SM since there is only one Higgs field there.

$$W_R = \epsilon_{ij}(y_{ab}^U Q_a^j U_b^c H_2^i + y_{ab}^D Q_a^j D_b^c H_1^i + y_{ab}^L L_a^j E_b^c H_1^i + \mu H_1^i H_2^j), \quad (4.13)$$

where  $i, j = 1, 2, 3$  are the  $SU(2)$  and  $a, b = 1, 2, 3$  are the generation indices; colour indices are suppressed. The index  $R$  in a superpotential refers to the so-called  $R$ -parity [12]. The first part of  $\mathcal{W}$  is  $R$ -symmetric.

The second part is  $R$ -nonsymmetric

$$W_{NR} = \epsilon_{ij}(\lambda_{abd}^L L_a^i L_b^j E_d^c + \lambda_{abd}^{L'} L_a^i Q_b^j D_d^c + \mu'_a L_a^i H_2^j) + \lambda_{abd}^B U_a^c D_b^c D_d^c. \quad (4.14)$$

These terms are absent in the SM. The reason is very simple: one can not replace the superfields in eq.(4.14) by the ordinary fields like in eq.(4.13) because of the Lorentz invariance. These terms have a different property, they violate either lepton (the first 3 terms in eq.(4.14)) or baryon number (the last term). Since both effects are not observed in Nature, these terms must be suppressed or be excluded. One can avoid such terms if one introduces special symmetry called the  $R$ -symmetry. This is the global  $U(1)_R$  invariance

$$U(1)_R: \quad \theta \rightarrow e^{i\alpha}\theta, \quad \Phi \rightarrow e^{i\alpha}\Phi, \quad (4.15)$$

which is reduced to the discrete group  $Z_2$ , called the  $R$ -parity. The  $R$ -parity quantum number is given by  $R = (-1)^{3(B-L)+2S}$  for particles with spin  $S$ . Thus, all the ordinary particles have the  $R$ -parity quantum number equal to  $R = +1$ , while all the superpartners have  $R$ -parity quantum number equal to  $R = -1$ . The  $R$ -parity obviously forbids the  $W_{NR}$  terms. However, it may well be that these terms are present, though experimental limits on the couplings are very severe [13]

$$\lambda_{abc}^L, \lambda_{abc}^{L'} < 10^{-4}, \quad \lambda_{abc}^B < 10^{-9}.$$

The breaking part is the main source of arbitrariness in the MSSM since the mechanism of SUSY breaking is unknown. We consider the breaking terms in more detail below.

### 4.3 Properties of interactions

If one assumes that the  $R$ -parity is preserved, then the interactions of superpartners are essentially the same as in the SM, but two of three particles involved into an interaction at any vertex are replaced by superpartners. The reason for it is the  $R$ -parity. Conservation of the  $R$ -parity has two consequences

- the superpartners are created in pairs;
- the lightest superparticle (LSP) is stable. Usually it is photino  $\tilde{\gamma}$ , the superpartner of a photon with some admixture of neutral higgsino.

Typical vertices are shown in Figs.6. The tilde above a letter denotes the corresponding superpartner. Note that the coupling is the same in all the vertices

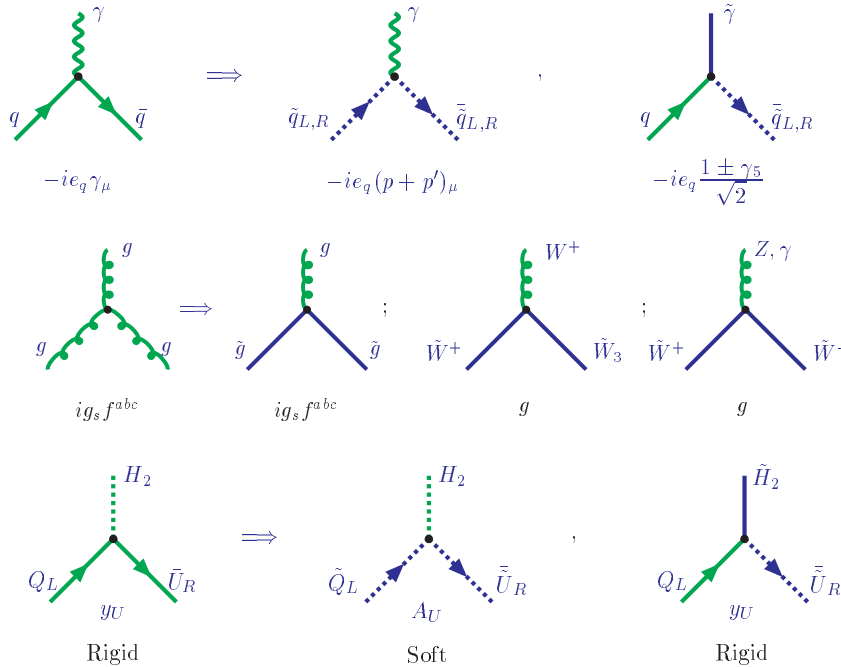


Figure 6: Interaction vertices in the MSSM

#### 4.4 Creation and decay of superpartners

The above-mentioned rule together with the Feynman rules for the SM enables one to draw the diagrams describing creation of superpartners. One of the most promising processes is the  $e^+e^-$  annihilation (see Fig.7).

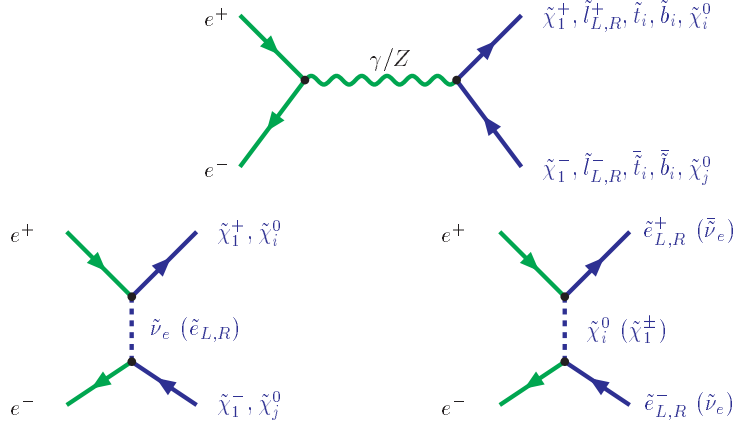


Figure 7: Creation of superpartners

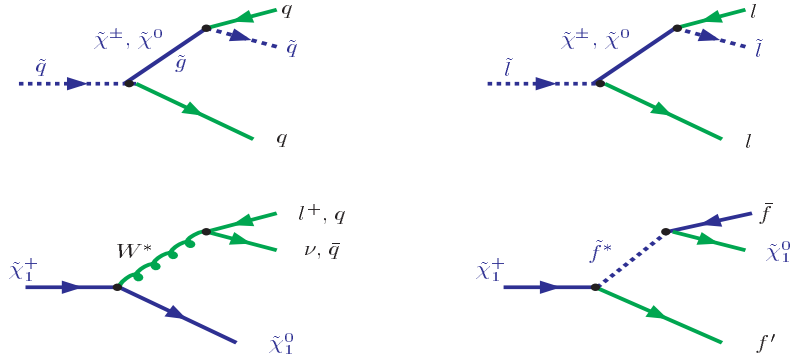


Figure 8: Decay of superpartners

The usual kinematic restriction is given by the c.m. energy  $m_{particle}^{max} \leq \frac{\sqrt{s}}{2}$ . Similar processes take place at hadron colliders with electrons and positrons being replaced by quarks and gluons.

Creation of superpartners can be accompanied by creation of ordinary particles as well. We consider various experimental signatures for  $e^+e^-$  and hadron colliders below. They crucially depend on SUSY breaking pattern and on the mass spectrum of superpartners.

The decay properties of superpartners also depend on their masses. For the quark and lepton superpartners the main processes are shown in Fig.8.

When the  $R$ -parity is conserved, new particles will eventually end up giving neutralinos (the lightest superparticle) whose interactions are comparable to those of neutrinos and they leave undetected. Therefore, their signature would be missing energy and transverse momentum. Thus, if supersymmetry exists in Nature and if it is broken somewhere below 1 TeV, then it will be possible to detect it in the nearest future.

## 5 Breaking of SUSY in the MSSM

### 5.1 The mechanisms of SUSY breaking

Since none of the fields of the MSSM can develop non-zero v.e.v. to break SUSY without spoiling the gauge invariance, it is supposed that spontaneous supersymmetry breaking takes place via some other fields. The most common scenario for producing low-energy supersymmetry breaking is called the *hidden sector* one [14]. According to this scenario, there exist two sectors: the usual matter belongs to the "visible" one, while the second, "hidden" sector, contains fields which lead to breaking of supersymmetry. These two sectors interact with each other by exchange of some fields called *messengers*, which mediate SUSY breaking from the hidden to the visible sector. There might be various types of messenger fields: gravity, gauge, etc. The hidden sector is the weakest part of the MSSM. It contains a lot of ambiguities and leads to uncertainties of the MSSM predictions considered below.

So far there are known four main mechanisms to mediate SUSY breaking from a hidden to a visible sector:

- Gravity mediation (SUGRA) [15];
- Gauge mediation [16];
- Anomaly mediation [17];
- Gaugino mediation [18].

All four mechanisms of soft SUSY breaking are different in details but are common in results. Predictions for the sparticle spectrum depend on the mechanism of SUSY breaking. For comparison of the four above-mentioned mechanisms we show in Fig.9 the sample spectra as the ratio to the gaugino mass  $M_2$  [19].

In what follows, to calculate the mass spectrum of superpartners, we need an explicit form of SUSY breaking terms. For the MSSM and without the  $R$ -parity violation one has

$$\begin{aligned}
 -\mathcal{L}_{Breaking} = & \sum_i m_{0i}^2 |\varphi_i|^2 + \left( \frac{1}{2} \sum_\alpha M_\alpha \tilde{\lambda}_\alpha \tilde{\lambda}_\alpha + B H_1 H_2 \right. \\
 & \left. + A_{ab}^U \tilde{Q}_a \tilde{U}_b^c H_2 + A_{ab}^D \tilde{Q}_a \tilde{D}_b^c H_1 + A_{ab}^L \tilde{L}_a \tilde{E}_b^c H_1 + h.c. \right), \quad (5.16)
 \end{aligned}$$

where we have suppressed the  $SU(2)$  indices. Here  $\varphi_i$  are all scalar fields,  $\tilde{\lambda}_\alpha$  are the gaugino fields,  $\tilde{Q}, \tilde{U}, \tilde{D}$  and  $\tilde{L}, \tilde{E}$  are the squark and slepton fields, respectively, and  $H_{1,2}$  are the  $SU(2)$  doublet Higgs fields.

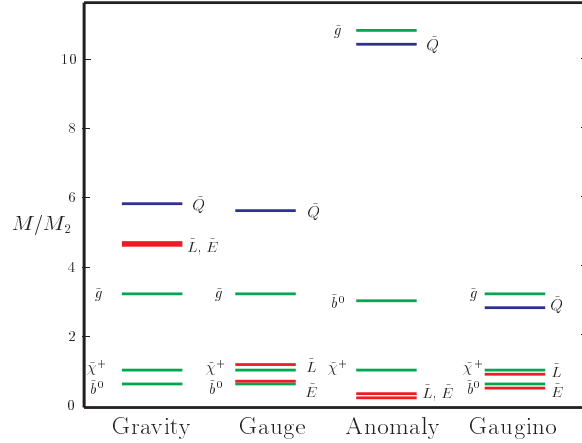


Figure 9: Superparticle spectra for various mediation mechanisms

Eq.(5.16) contains a vast number of free parameters which spoils the prediction power of the model. To reduce their number, we adopt the so-called *universality* hypothesis, i.e., we assume the universality or equality of various soft parameters at a high energy scale. Namely, following the so-called mSUGRA SUSY breaking scenario, we put all the spin 0 particle masses to be equal to the universal value  $m_0$ , all the spin 1/2 particle (gaugino) masses to be equal to  $m_{1/2}$  and all the cubic and quadratic terms, proportional to  $A$  and  $B$ , to repeat the structure of the Yukawa superpotential (4.13). This is an additional requirement motivated by the supergravity mechanism of SUSY breaking. Universality is not a necessary requirement and one may consider nonuniversal soft terms as well. However, it will not change the qualitative picture presented below; so for simplicity, in what follows we consider the universal boundary conditions. In this case, eq.(5.16) takes the form

$$\begin{aligned}
 -\mathcal{L}_{Breaking} = & m_0^2 \sum_i |\varphi_i|^2 + \left( \frac{1}{2} m_{1/2} \sum_\alpha \tilde{\lambda}_\alpha \tilde{\lambda}_\alpha \right. \\
 & \left. + A[y_{ab}^U \tilde{Q}_a \tilde{U}_b^c H_2 + y_{ab}^D \tilde{Q}_a \tilde{D}_b^c H_1 + y_{ab}^L \tilde{L}_a \tilde{E}_b^c H_1] + B[\mu H_1 H_2] + h.c. \right),
 \end{aligned}
 \tag{5.17}$$

The soft terms explicitly break supersymmetry. As will be shown later, they lead to the mass spectrum of superpartners different from that of ordinary particles. Remind that the masses of quarks and leptons remain zero until  $SU(2)$  invariance is spontaneously broken.

## 5.2 The soft terms and the mass formulas

There are two main sources of the mass terms in the Lagrangian: the  $D$  terms and soft ones. With given values of  $m_0, m_{1/2}, \mu, Y_t, Y_b, Y_\tau, A$ , and  $B$  one can construct the mass matrices for all the particles. Knowing them at the GUT scale, one can



solve the corresponding RG equations, thus linking the values at the GUT and electroweak scales. Substituting these parameters into the mass matrices, one can predict the mass spectrum of superpartners [20, 21].

**Gaugino-higgsino mass terms** The mass matrix for gauginos, the superpartners of the gauge bosons, and for higgsinos, the superpartners of the Higgs bosons, is nondiagonal, thus leading to their mixing. The mass terms look like

$$\mathcal{L}_{Gaugino-Higgsino} = -\frac{1}{2}M_3\bar{\lambda}_a\lambda_a - \frac{1}{2}\bar{\chi}M^{(0)}\chi - (\bar{\psi}M^{(c)}\psi + h.c.), \quad (5.18)$$

where  $\lambda_a, a = 1, 2, \dots, 8$ , are the Majorana gluino fields and

$$\chi = \begin{pmatrix} \tilde{B}^0 \\ \tilde{W}^3 \\ \tilde{H}_1^0 \\ \tilde{H}_2^0 \end{pmatrix}, \quad \psi = \begin{pmatrix} \tilde{W}^+ \\ \tilde{H}^+ \end{pmatrix} \quad (5.19)$$

are, respectively, the Majorana neutralino and Dirac chargino fields.

The neutralino mass matrix is

$$M^{(0)} = \begin{pmatrix} M_1 & 0 & -M_Z \cos \beta \sin_W & M_Z \sin \beta \sin_W \\ 0 & M_2 & M_Z \cos \beta \cos_W & -M_Z \sin \beta \cos_W \\ -M_Z \cos \beta \sin_W & M_Z \cos \beta \cos_W & 0 & -\mu \\ M_Z \sin \beta \sin_W & -M_Z \sin \beta \cos_W & -\mu & 0 \end{pmatrix}, \quad (5.20)$$

where  $\tan \beta = v_2/v_1$  is the ratio of two Higgs v.e.v.s and  $\sin_W = \sin \theta_W$  is the usual sinus of the weak mixing angle. The physical neutralino masses  $M_{\tilde{\chi}_i^0}$  are obtained as eigenvalues of this matrix after diagonalization.

For charginos one has

$$M^{(c)} = \begin{pmatrix} M_2 & \sqrt{2}M_W \sin \beta \\ \sqrt{2}M_W \cos \beta & \mu \end{pmatrix}. \quad (5.21)$$

This matrix has two chargino eigenstates  $\tilde{\chi}_{1,2}^\pm$  with mass eigenvalues

$$M_{1,2}^2 = \frac{1}{2} \left[ M_2^2 + \mu^2 + 2M_W^2 \mp \sqrt{(M_2^2 - \mu^2)^2 + 4M_W^4 \cos^2 2\beta + 4M_W^2(M_2^2 + \mu^2 + 2M_2\mu \sin 2\beta)} \right]. \quad (5.22)$$

**Squark and slepton masses** Non-negligible Yukawa couplings cause a mixing between the electroweak eigenstates and the mass eigenstates of the third generation particles. The mixing matrices for  $\tilde{m}_t^2, \tilde{m}_b^2$  and  $\tilde{m}_\tau^2$  are

$$\begin{pmatrix} \tilde{m}_{tL}^2 & m_t(A_t - \mu \cot \beta) \\ m_t(A_t - \mu \cot \beta) & \tilde{m}_{tR}^2 \end{pmatrix}, \quad (5.23)$$

$$\begin{pmatrix} \tilde{m}_{bL}^2 & m_b(A_b - \mu \tan \beta) \\ m_b(A_b - \mu \tan \beta) & \tilde{m}_{bR}^2 \end{pmatrix}, \quad (5.24)$$

$$\begin{pmatrix} \tilde{m}_{\tau L}^2 & m_\tau(A_\tau - \mu \tan \beta) \\ m_\tau(A_\tau - \mu \tan \beta) & \tilde{m}_{\tau R}^2 \end{pmatrix} \quad (5.25)$$

with

$$\tilde{m}_{tL}^2 = \tilde{m}_Q^2 + m_t^2 + \frac{1}{6}(4M_W^2 - M_Z^2) \cos 2\beta,$$

$$\tilde{m}_{tR}^2 = \tilde{m}_U^2 + m_t^2 - \frac{2}{3}(M_W^2 - M_Z^2) \cos 2\beta,$$

$$\tilde{m}_{bL}^2 = \tilde{m}_Q^2 + m_b^2 - \frac{1}{6}(2M_W^2 + M_Z^2) \cos 2\beta,$$

$$\tilde{m}_{bR}^2 = \tilde{m}_D^2 + m_b^2 + \frac{1}{3}(M_W^2 - M_Z^2) \cos 2\beta,$$

$$\tilde{m}_{\tau L}^2 = \tilde{m}_L^2 + m_\tau^2 - \frac{1}{2}(2M_W^2 - M_Z^2) \cos 2\beta,$$

$$\tilde{m}_{\tau R}^2 = \tilde{m}_E^2 + m_\tau^2 + (M_W^2 - M_Z^2) \cos 2\beta$$

and the mass eigenstates are the eigenvalues of these mass matrices. For the light generations the mixing is negligible.

The first terms here ( $\tilde{m}^2$ ) are the soft ones, which are calculated using the RG equations starting from their values at the GUT (Planck) scale. The second ones are the usual masses of quarks and leptons and the last ones are the  $D$ -terms of the potential.

### 5.3 The Higgs potential

As has already been mentioned, the Higgs potential in the MSSM is totally defined by superpotential  $\mathcal{W}$  and the soft terms. Due to the structure of  $\mathcal{W}$  the Higgs self-interaction is given by the  $D$ -terms while the  $F$ -terms contribute only to the mass matrix. The tree level potential is

$$\begin{aligned} V_{tree}(H_1, H_2) &= m_1^2 |H_1|^2 + m_2^2 |H_2|^2 - m_3^2 (H_1 H_2 + h.c.) \\ &+ \frac{g^2 + g'^2}{8} (|H_1|^2 - |H_2|^2)^2 + \frac{g^2}{2} |H_1^+ H_2|^2, \end{aligned} \quad (5.26)$$

where  $m_1^2 = m_{H_1}^2 + \mu^2$ ,  $m_2^2 = m_{H_2}^2 + \mu^2$ . At the GUT scale  $m_1^2 = m_2^2 = m_0^2 + \mu_0^2$ ,  $m_3^2 = -B\mu_0$ . Notice that the Higgs self-interaction coupling in eq.(5.26) is fixed and defined by the gauge interactions as opposed to the SM.

The potential (5.26), in accordance with supersymmetry, is positive definite and stable. It has no nontrivial minimum different from zero. Indeed, let us write the minimization condition for the potential (5.26)

$$\frac{1}{2} \frac{\delta V}{\delta H_1} = m_1^2 v_1 - m_3^2 v_2 + \frac{g^2 + g'^2}{4} (v_1^2 - v_2^2) v_1 = 0, \quad (5.27)$$

$$\frac{1}{2} \frac{\delta V}{\delta H_2} = m_2^2 v_2 - m_3^2 v_1 + \frac{g^2 + g'^2}{4} (v_1^2 - v_2^2) v_2 = 0, \quad (5.28)$$

where we have introduced the notation

$$\langle H_1 \rangle \equiv v_1 = v \cos \beta, \quad \langle H_2 \rangle \equiv v_2 = v \sin \beta, \quad v^2 = v_1^2 + v_2^2, \quad \tan \beta \equiv \frac{v_2}{v_1}.$$

Solution of eqs.(5.27),(5.28) can be expressed in terms of  $v^2$  and  $\sin 2\beta$

$$v^2 = \frac{4(m_1^2 - m_2^2 \tan^2 \beta)}{(g^2 + g'^2)(\tan^2 \beta - 1)}, \quad \sin 2\beta = \frac{2m_3^2}{m_1^2 + m_2^2}. \quad (5.29)$$

One can easily see from eq.(5.29) that if  $m_1^2 = m_2^2 = m_0^2 + \mu_0^2$ ,  $v^2$  happens to be negative, i.e. the minimum does not exist. In fact, real positive solutions to eqs.(5.27),(5.28) exist only if the following conditions are satisfied:

$$m_1^2 + m_2^2 > 2m_3^2, \quad m_1^2 m_2^2 < m_3^4, \quad (5.30)$$

which is not the case at the GUT scale. This means that spontaneous breaking of the  $SU(2)$  gauge invariance, which is needed in the SM to give masses for all the particles, does not take place in the MSSM.

This strong statement is valid, however, only at the GUT scale. Indeed, going down with energy, the parameters of the potential (5.26) are renormalized. They become the "running" parameters with the energy scale dependence given by the RG equations. The running of the parameters leads to a remarkable phenomenon known as *radiative spontaneous symmetry breaking* to be discussed below.

Provided conditions (5.30) are satisfied, the mass matrices at the tree level are CP-odd components  $P_1$  and  $P_2$  :

$$\mathcal{M}^{odd} = \left. \frac{\partial^2 V}{\partial P_i \partial P_j} \right|_{H_i=v_i} = \begin{pmatrix} \tan \beta & 1 \\ 1 & \cot \beta \end{pmatrix} m_3^2, \quad (5.31)$$

CP-even neutral components  $S_1$  and  $S_2$ :

$$\mathcal{M}^{ev} = \left. \frac{\partial^2 V}{\partial S_i \partial S_j} \right| = \begin{pmatrix} \tan \beta & -1 \\ -1 & \cot \beta \end{pmatrix} m_3^2 + \begin{pmatrix} \cot \beta & -1 \\ -1 & \tan \beta \end{pmatrix} M_Z \frac{\sin 2\beta}{2}, \quad (5.32)$$

Charged components  $H^-$  and  $H^+$ :

$$\mathcal{M}^{ch} = \left. \frac{\partial^2 V}{\partial H_i^+ \partial H_j^-} \right|_{H_i=v_i} = \begin{pmatrix} \tan \beta & 1 \\ 1 & \cot \beta \end{pmatrix} (m_3^2 + M_W \cos \beta \sin \beta). \quad (5.33)$$

Diagonalizing the mass matrices, one gets the mass eigenstates:

$$\begin{cases} G^0 & = -\cos \beta P_1 + \sin \beta P_2, & \text{Goldstone boson} \rightarrow Z_0, \\ A & = \sin \beta P_1 + \cos \beta P_2, & \text{Neutral CP} = -1 \text{ Higgs,} \end{cases}$$

$$\begin{cases} G^+ & = -\cos \beta (H_1^-)^* + \sin \beta H_2^+, & \text{Goldstone boson} \rightarrow W^+, \\ H^+ & = \sin \beta (H_1^-)^* + \cos \beta H_2^+, & \text{Charged Higgs,} \end{cases}$$

$$\begin{cases} h & = -\sin \alpha S_1 + \cos \alpha S_2, & \text{SM Higgs boson CP} = 1, \\ H & = \cos \alpha S_1 + \sin \alpha S_2, & \text{Extra heavy Higgs boson,} \end{cases}$$

where the mixing angle  $\alpha$  is given by equation:  $\tan 2\alpha = \tan 2\beta \left( \frac{m_A^2 + M_Z^2}{m_A^2 - M_Z^2} \right)$ .

The physical Higgs bosons acquire the following masses [10]:

$$\begin{aligned} \text{CP-odd neutral Higgs } A : & \quad m_A^2 = m_1^2 + m_2^2, \\ \text{Charge Higgses } H^\pm : & \quad m_{H^\pm}^2 = m_A^2 + M_W^2, \end{aligned} \quad (5.34)$$

CP-even neutral Higgses  $H, h$ :

$$m_{H,h}^2 = \frac{1}{2} \left[ m_A^2 + M_Z^2 \pm \sqrt{(m_A^2 + M_Z^2)^2 - 4m_A^2 M_Z^2 \cos^2 2\beta} \right], \quad (5.35)$$

where, as usual,

$$M_W^2 = \frac{g^2}{2} v^2, \quad M_Z^2 = \frac{g^2 + g'^2}{2} v^2.$$

This leads to the once celebrated SUSY mass relations

$$\begin{aligned} m_{H^\pm} &\geq M_W, \quad m_h \leq m_A \leq M_H, \\ m_h &\leq M_Z |\cos 2\beta| \leq M_Z, \quad m_h^2 + m_{H^\pm}^2 = m_A^2 + M_Z^2. \end{aligned} \quad (5.36)$$

Thus, the lightest neutral Higgs boson happens to be lighter than the  $Z$  boson, which clearly distinguishes it from the SM one. Though we do not know the mass of the Higgs boson in the SM, there are several indirect constraints leading to the lower boundary of  $m_h^{SM} \geq 135$  GeV [22]. After including the radiative corrections, the mass of the lightest Higgs boson in the MSSM,  $m_h$ , however, increases. We consider it in more detail below.

## 5.4 Renormalization group analysis

To calculate the low energy values of the soft terms, we use the corresponding RG equations. The one-loop RG equations for the rigid MSSM couplings are [23]

$$\begin{aligned} \frac{d\tilde{\alpha}_i}{dt} &= b_i \tilde{\alpha}_i^2, \quad t \equiv \log Q^2 / M_{GUT}^2 \\ \frac{dY_U}{dt} &= -Y_L \left( \frac{16}{3} \tilde{\alpha}_3 + 3\tilde{\alpha}_2 + \frac{13}{15} \tilde{\alpha}_1 - 6Y_U - Y_D \right), \\ \frac{dY_D}{dt} &= -Y_D \left( \frac{16}{3} \tilde{\alpha}_3 + 3\tilde{\alpha}_2 + \frac{7}{15} \tilde{\alpha}_1 - Y_U - 6Y_D - Y_L \right), \\ \frac{dY_L}{dt} &= -Y_L \left( 3\tilde{\alpha}_2 + \frac{9}{5} \tilde{\alpha}_1 - 3Y_D - 4Y_L \right), \end{aligned} \quad (5.37)$$

where we use the notation  $\tilde{\alpha} = \alpha/4\pi = g^2/16\pi^2$ ,  $Y = y^2/16\pi^2$ .

For the soft terms one finds

$$\begin{aligned} \frac{dM_i}{dt} &= b_i \tilde{\alpha}_i M_i. \\ \frac{dA_U}{dt} &= \frac{16}{3} \tilde{\alpha}_3 M_3 + 3\tilde{\alpha}_2 M_2 + \frac{13}{15} \tilde{\alpha}_1 M_1 + 6Y_U A_U + Y_D A_D, \end{aligned}$$

$$\begin{aligned}
\frac{dA_D}{dt} &= \frac{16}{3}\tilde{\alpha}_3 M_3 + 3\tilde{\alpha}_2 M_2 + \frac{7}{15}\tilde{\alpha}_1 M_1 + 6Y_D A_D + Y_U A_U + Y_L A_L, \\
\frac{dA_L}{dt} &= 3\tilde{\alpha}_2 M_2 + \frac{9}{5}\tilde{\alpha}_1 M_1 + 3Y_D A_D + 4Y_L A_L, \\
\frac{dB}{dt} &= 3\tilde{\alpha}_2 M_2 + \frac{3}{5}\tilde{\alpha}_1 M_1 + 3Y_U A_U + 3Y_D A_D + Y_L A_L. \\
\frac{d\tilde{m}_Q^2}{dt} &= - \left[ \left( \frac{16}{3}\tilde{\alpha}_3 M_3^2 + 3\tilde{\alpha}_2 M_2^2 + \frac{1}{15}\tilde{\alpha}_1 M_1^2 \right) \right. \\
&\quad \left. - Y_U(\tilde{m}_Q^2 + \tilde{m}_U^2 + m_{H_2}^2 + A_U^2) - Y_D(\tilde{m}_Q^2 + \tilde{m}_D^2 + m_{H_1}^2 + A_D^2) \right], \\
\frac{d\tilde{m}_U^2}{dt} &= - \left[ \left( \frac{16}{3}\tilde{\alpha}_3 M_3^2 + \frac{16}{15}\tilde{\alpha}_1 M_1^2 \right) - 2Y_U(\tilde{m}_Q^2 + \tilde{m}_U^2 + m_{H_2}^2 + A_U^2) \right], \\
\frac{d\tilde{m}_D^2}{dt} &= - \left[ \left( \frac{16}{3}\tilde{\alpha}_3 M_3^2 + \frac{4}{15}\tilde{\alpha}_1 M_1^2 \right) - 2Y_D(\tilde{m}_Q^2 + \tilde{m}_D^2 + m_{H_1}^2 + A_D^2) \right], \\
\frac{d\tilde{m}_L^2}{dt} &= - \left[ 3(\tilde{\alpha}_2 M_2^2 + \frac{1}{5}\tilde{\alpha}_1 M_1^2) - Y_L(\tilde{m}_L^2 + \tilde{m}_E^2 + m_{H_1}^2 + A_L^2) \right], \\
\frac{d\tilde{m}_E^2}{dt} &= - \left[ \left( \frac{12}{5}\tilde{\alpha}_1 M_1^2 \right) - 2Y_L(\tilde{m}_L^2 + \tilde{m}_E^2 + m_{H_1}^2 + A_L^2) \right], \\
\frac{d\mu^2}{dt} &= -\mu^2 \left[ 3(\tilde{\alpha}_2 + \frac{1}{5}\tilde{\alpha}_1) - (3Y_U + 3Y_D + Y_L) \right], \tag{5.38} \\
\frac{dm_{H_1}^2}{dt} &= - \left[ 3(\tilde{\alpha}_2 M_2^2 + \frac{1}{5}\tilde{\alpha}_1 M_1^2) - 3Y_D(\tilde{m}_Q^2 + \tilde{m}_D^2 + m_{H_1}^2 + A_D^2) \right. \\
&\quad \left. - Y_L(\tilde{m}_L^2 + \tilde{m}_E^2 + m_{H_1}^2 + A_L^2) \right], \\
\frac{dm_{H_2}^2}{dt} &= - \left[ 3(\tilde{\alpha}_2 M_2^2 + \frac{1}{5}\tilde{\alpha}_1 M_1^2) - 3Y_U(\tilde{m}_Q^2 + \tilde{m}_U^2 + m_{H_2}^2 + A_U^2) \right].
\end{aligned}$$

Having all the RG equations, one can now find the RG flow for the soft terms. Taking the initial values of the soft masses at the GUT scale in the interval between  $10^2 \div 10^3$  GeV consistent with the SUSY scale suggested by unification of the gauge couplings [6] leads to the RG flow of the soft terms shown in Fig.10. [20, 21]

One should mention the following general features common to any choice of initial conditions:

i) The gaugino masses follow the running of the gauge couplings and split at low energies. The gluino mass is running faster than the others and is usually the heaviest due to the strong interaction.

ii) The squark and slepton masses also split at low energies, the stops (and sbottoms) being the lightest due to relatively big Yukawa couplings of the third generation.

iii) The Higgs masses (or at least one of them) are running down very quickly and may even become negative.

Typical dependence of the mass spectra on the initial conditions ( $m_0$ ) is also shown in Fig.11 [24]. For a given value of  $m_{1/2}$  the masses of the lightest particles are practically independent of  $m_0$ , while the heavier ones increase with it monotonically.

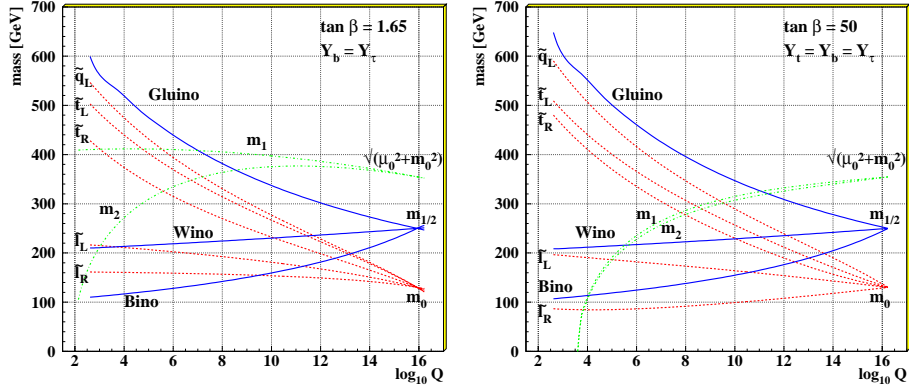


Figure 10: An example of evolution of particle masses and soft supersymmetry breaking parameters  $m_1^2 = m_{H_1}^2 + \mu^2$  and  $m_2^2 = m_{H_2}^2 + \mu^2$  for low (left) and high (right) values of  $\tan \beta$

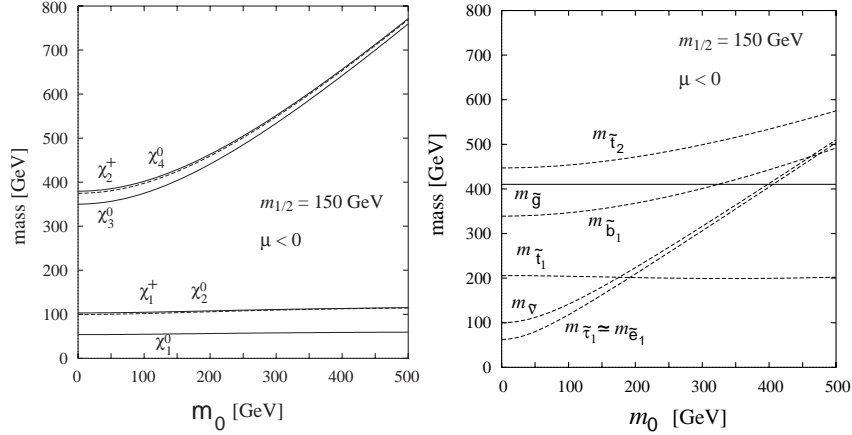


Figure 11: The masses of particles as functions of the initial value  $m_0$

One can see that the lightest neutralinos and charginos as well as the stop squark may be rather light.

## 5.5 Radiative electroweak symmetry breaking

The running of the Higgs masses leads to the phenomenon known as *radiative electroweak symmetry breaking*. Indeed, one can see in Fig.10 that  $m_2^2$  (or both  $m_1^2$  and  $m_2^2$ ) decreases when going down from the GUT scale to the  $M_Z$  scale and can even become negative. As a result, at some value of  $Q^2$  the conditions (5.30) are satisfied, so that the nontrivial minimum appears. This triggers spontaneous breaking of the  $SU(2)$  gauge invariance. The vacuum expectations of the Higgs fields acquire nonzero values and provide masses to quarks, leptons and  $SU(2)$  gauge bosons, and

additional masses to their superpartners.

In this way one also obtains the explanation of why the two scales are so much different. Due to the logarithmic running of the parameters, one needs a long "running time" to get  $m_2^2$  (or both  $m_1^2$  and  $m_2^2$ ) to be negative when starting from a positive value of the order of  $M_{SUSY} \sim 10^2 \div 10^3$  GeV at the GUT scale.

## 6 Constrained MSSM

### 6.1 Parameter space of the MSSM

The Minimal Supersymmetric Standard Model has the following free parameters:

- i) three gauge couplings  $\alpha_i$ ;
- ii) three matrices of the Yukawa couplings  $y_{ab}^i$ , where  $i = L, U, D$ ;
- iii) the Higgs field mixing parameter  $\mu$ ;
- iv) the soft supersymmetry breaking parameters.

Compared to the SM there is an additional Higgs mixing parameter, but the Higgs self-coupling, which is arbitrary in the SM, is fixed by supersymmetry. The main uncertainty comes from the unknown soft terms.

With the universality hypothesis one is left with the following set of 5 free parameters defining the mass scales

$$\mu, m_0, m_{1/2}, A \text{ and } B \leftrightarrow \tan \beta = \frac{v_2}{v_1}.$$

While choosing parameters and making predictions, one has two possible ways to proceed:

i) take the low-energy parameters like superparticle masses  $\tilde{m}_{t1}, \tilde{m}_{t2}, m_A, \tan \beta$ , mixings  $X_{stop}, \mu$ , etc. as input and calculate cross-sections as functions of these parameters.

ii) take the high-energy parameters like the above mentioned 5 soft parameters as input, run the RG equations and find the low-energy values. Now the calculations can be carried out in terms of the initial parameters. The experimental constraints are sufficient to determine these parameters, albeit with large uncertainties.

Both the ways are used in a phenomenological analysis. We show below how it works in practice.

### 6.2 The choice of constraints

When subjecting constraints on the MSSM, perhaps, the most remarkable fact is that all of them can be fulfilled simultaneously. In our analysis we impose the following constraints on the parameter space of the MSSM:

- Gauge coupling constant unification;

This is one of the most restrictive constraints. It fixes the scale of SUSY breaking of an order of 1 TeV.

- $M_Z$  from electroweak symmetry breaking;

Radiative EW symmetry breaking (see eq.(5.29)) defines the mass of the Z-boson

$$M_Z^2 = 2 \frac{m_1^2 - m_2^2 \tan^2 \beta}{\tan^2 \beta - 1}. \quad (6.39)$$

This condition determines the value of  $\mu^2$  for given values of  $m_0$  and  $m_{1/2}$ .

- Yukawa coupling constant unification;

The masses of top, bottom and  $\tau$  can be obtained from the low energy values of the running Yukawa couplings via

$$m_t = y_t v \sin \beta, \quad m_b = y_b v \cos \beta, \quad m_\tau = y_\tau v \cos \beta. \quad (6.40)$$

They can be translated to the pole masses with account taken of the radiative corrections. The requirement of bottom-tau Yukawa coupling unification, i.e. equality of  $b$ -quark and  $\tau$ -lepton masses at the GUT scale, strongly restricts the possible solutions in  $m_t$  versus  $\tan \beta$  plane [25] as it can be seen from Fig.12. Releasing this constraint one may use intermediate values of  $\tan \beta$ .

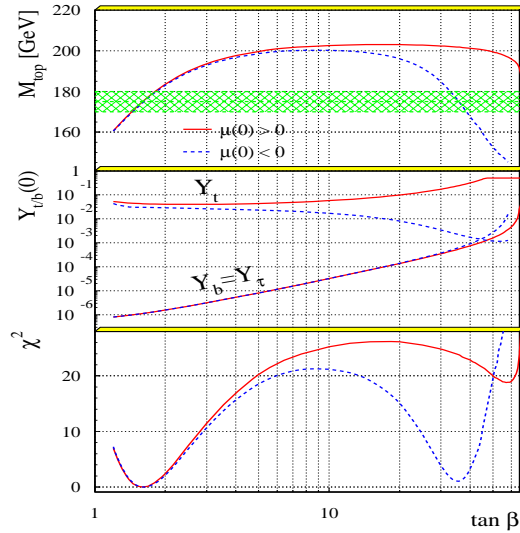


Figure 12: The upper part shows the top quark mass as a function of  $\tan \beta$  for  $m_0 = 600$  GeV,  $m_{1/2} = 400$  GeV. The middle part shows the corresponding values of the Yukawa couplings at the GUT scale and the lower part of the  $\chi^2$  values.

- Precision measurement of decay rates;

We take the branching ratio  $BR(b \rightarrow s\gamma)$  which has been measured by the CLEO [26] collaboration and later by ALEPH [27] and yields the world average of  $BR(b \rightarrow s\gamma) = (3.14 \pm 0.48) \cdot 10^{-4}$ . The Standard Model contribution to this process gives slightly lower result, thus leaving window for SUSY. This requirement imposes severe restrictions on the parameter space, especially for the case of large  $\tan \beta$ .

- Anomalous magnetic moment of muon.

Recent measurement of the anomalous magnetic moment indicates small deviation



from the SM of the order of  $2 \sigma$ . The deficiency may be easily filled with SUSY contribution, which is proportional to  $\mu$ . This requires positive sign of  $\mu$  that kills a half of the parameter space of the MSSM [28].

- Experimental lower limits on SUSY masses;

SUSY particles have not been found so far and from the searches at LEP one knows the lower limit on the charged lepton and chargino masses of about half of the centre of mass energy [29]. The lower limit on the neutralino masses is smaller. There exist also limits on squark and gluino masses from the hadron colliders [30]. These limits restrict the minimal values for the SUSY mass parameters.

- Dark Matter constraint;

In the early Universe all particles were produced abundantly and were in thermal equilibrium through annihilation and production processes. the present, the mass density in units of the critical density is given by [32]

$$\Omega_\chi h^2 = \frac{m_\chi n_\chi}{\rho_c} \approx \left( \frac{2 \cdot 10^{-27} \text{ cm}^3 \text{ s}^{-1}}{\langle \sigma v \rangle} \right). \quad (6.41)$$

The amount of neutralinos should not be too big to overclose the Universe and, at the same time, it should be enough to produce the right amount of the Dark matter. Conservative bounds are  $\Omega_\chi h_0^2 \sim 0.1 \div 0.3$ . and serve as a very severe bound on SUSY parameters [33]. We show below that recent very precise data from WMAP collaboration, which measured thermal fluctuations of Cosmic Microwave Background radiation and restricted the amount of the Dark matter in the Universe up to  $23 \pm 4\%$ , leave a very narrow band of allowed region in parameter space.

Having in mind the above mentioned constraints one can find the most probable region of the parameter space by minimizing the  $\chi^2$  function [21]. One finds two possible solutions: low  $\tan \beta$  solution corresponding to  $\tan \beta \approx 1.7$  and high  $\tan \beta$  solution corresponding to  $\tan \beta \approx 30 \div 60$ .

The low  $\tan \beta$  solution which predicts light particles was very popular at the time of LEP. Unfortunately, LEP found neither superpartners nor the light Higgs boson. A modern limit on the value of  $\tan \beta$  comes from non-observation of the Higgs boson up to 114 GeV and restricts  $\tan \beta \geq 3 \div 4$ .

In what follows, we consider the plane  $m_0, m_{1/2}$  and find the allowed region in this plane. Each point at this plane corresponds to a fixed set of parameters and allows one to calculate the spectrum, the cross-sections, etc.

We present the allowed regions of the parameter space for two typical values of  $\tan \beta$  in Fig.13. This plot demonstrates the role of various constraints in the  $\chi^2$  function. The contours enclose domains by the particular constraints used in the analysis [34]. Fig.14 shows the role of the Dark Matter constraint (before WMAP).

Taking into account the WMAP data puts even more severe constrains due to very high precision of measurement. This constraint is shown in Fig.15 as a narrow light blue band [35, 36]. We have taken here a twice wider region in the  $m_0, m_{1/2}$  plane, thus allowing higher masses of superpartners.

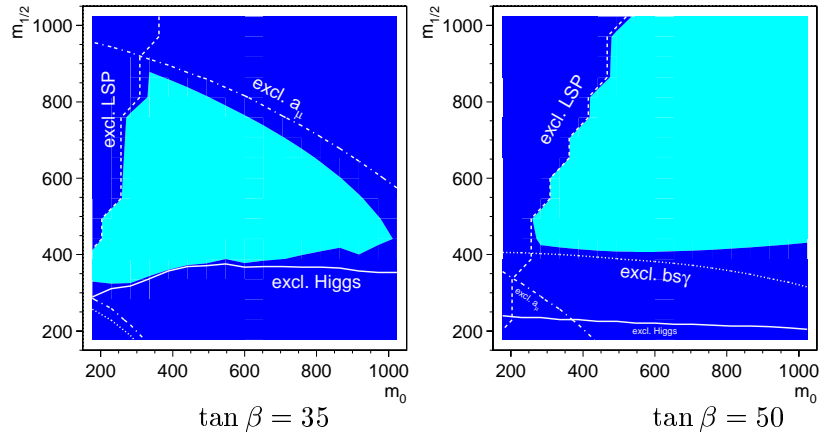


Figure 13: Allowed regions of parameter space for high  $\tan \beta$  scenario.

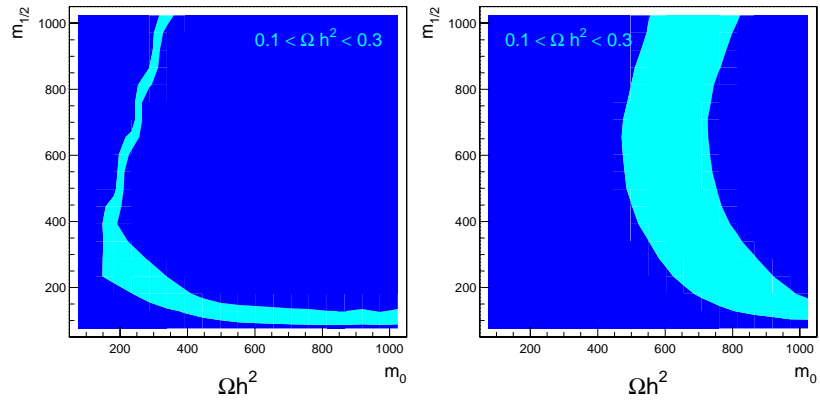


Figure 14: Restrictions on parameter space from the Dark matter constraint.

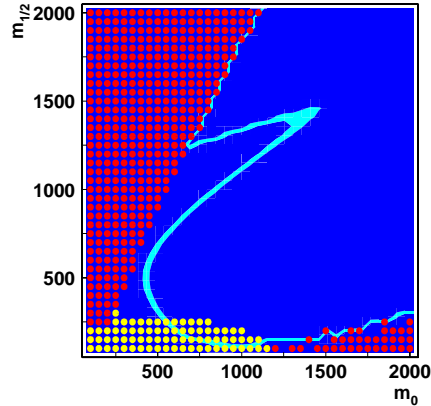


Figure 15: The light shaded (blue) line is the region allowed by WMAP for  $\tan \beta = 51$ ,  $\mu > 0$  and  $A_0 = 0.5m_0$ . The excluded regions where the stau would be the LSP (red, left upper corner) or EWSB fails (red, right corner) or the Higgs boson is too light (yellow, left low corner) are indicated by the dots.

### 6.3 The mass spectrum of superpartners

When the parameter set is fixed, one can calculate the mass spectrum of superpartners. Below we show the typical mass spectrum [35] for large  $\tan\beta$  solution. At the top we show the fitted values of the soft SUSY breaking parameters and at the bottom of the table one can see also the values of some observables used as constraints and fitted by the choice of parameters.

Parameter	Value	Value
$m_0$	500 GeV	500 GeV
$m_{1/2}$	350 GeV	550 GeV
$\tan\beta$	50	52
$A_0$	$0 \cdot m_0$	$0 \cdot m_0$
sign $\mu$	+	+
Particle	Mass [GeV]	Mass [GeV]
$\tilde{\chi}_{1,2,3,4}^0$	144, 259, 447, 462	230, 420, 665, 676
$\tilde{\chi}_{1,2}^\pm$	259, 463	420, 677
$\tilde{g}$	803	1231
$\tilde{t}_{1,2}$	618, 769	899, 1066
$\tilde{b}_{1,2}$	679, 758	960, 1052
$\tilde{u}_{1,2}$	864, 889	1185, 1230
$\tilde{d}_{1,2}$	862, 892	1180, 1233
$\tilde{\tau}_{1,2}$	318, 496	289, 565
$\tilde{l}_{1,2}$	519, 556	544, 626
$\tilde{\nu}_\tau$	475	538
$\tilde{\nu}$	550	621
$h$	115.0	118.0
$H$	375.4	493.6
$A$	375.7	496.0
$H^\pm$	386.7	505.0
Observable	Value	Value
$Br(b \rightarrow X_s \gamma)$	$1.63 \cdot 10^{-4}$	$2.68 \cdot 10^{-4}$
$Br(B_s \rightarrow \mu^+ \mu^-)$	$\sim 5 \cdot 10^{-8}$	$\sim 2 \cdot 10^{-8}$
$a_\mu$	$363 \cdot 10^{-11}$	$224 \cdot 10^{-11}$
$\Omega h^2$	0.117	0.113

Table 1: mSUGRA parameters and the corresponding mass spectrum of superpartners.

Notice the low values of the masses of the lightest Higgs boson and of the lightest neutralino which is the LSP. They happen to be very sensitive to the value of  $\tan\beta$  and increase with increase of the latter.

#### 6.4 Experimental signatures at $e^+e^-$ colliders

Experiments are finally beginning to push into a significant region of supersymmetry parameter space. We know the sparticles and their couplings, but we do not know their masses and mixings. Given the mass spectrum one can calculate the cross-sections and consider the possibilities of observing new particles at modern accelerators. Otherwise, one can get restrictions on unknown parameters.

We start with  $e^+e^-$  colliders. In the leading order creation of superpartners is given by the diagrams shown in Fig.7 above. For a given center of mass energy the cross-sections depend on the mass of created particles and vanish at the kinematic boundary. Experimental signatures are defined by the decay modes which vary with the mass spectrum. The main ones are summarized below. A characteristic feature of all possible signatures is the missing energy and transverse momenta, which is a trade mark of a new physics.

<u>Production</u>	<u>Key Decay Modes</u>	<u>Signatures</u>
• $\tilde{l}_{L,R}\tilde{l}_{L,R}$	$\tilde{l}_R^\pm \rightarrow l^\pm \tilde{\chi}_i^0 \searrow$ cascade $\tilde{l}_L^\pm \rightarrow l^\pm \tilde{\chi}_i^0 \nearrow$ decays	acomplanar pair of charged leptons + $\cancel{E}_T$
• $\tilde{\nu}\tilde{\nu}$	$\tilde{\nu} \rightarrow l^\pm \tilde{\chi}_1^0$	$\cancel{E}_T$
• $\tilde{\chi}_1^\pm \tilde{\chi}_1^\pm$	$\tilde{\chi}_1^\pm \rightarrow \tilde{\chi}_1^0 l^\pm \nu$ , $\tilde{\chi}_1^0 q \bar{q}'$ $\tilde{\chi}_1^\pm \rightarrow \tilde{\chi}_2^0 f \bar{f}'$ $\tilde{\chi}_1^\pm \rightarrow l \tilde{\nu}_l \rightarrow l \nu_l \tilde{\chi}_1^0$ $\tilde{\chi}_1^\pm \rightarrow \nu_l \tilde{l} \rightarrow \nu_l l \tilde{\chi}_1^0$	isol lept + 2 jets + $\cancel{E}_T$ pair of acomplanar leptons + $\cancel{E}_T$
• $\tilde{\chi}_i^0 \tilde{\chi}_j^0$	$\tilde{\chi}_i^0 \rightarrow \tilde{\chi}_1^0 X$ , $\tilde{\chi}_j^0 \rightarrow \tilde{\chi}_1^0 X'$	4 jets + $\cancel{E}_T$ $X = \nu_l \tilde{\nu}_l$ invisible = $\gamma, 2l, 2$ jets $2l + \cancel{E}_T, l + 2j + \cancel{E}_T$
• $\tilde{t}_i \tilde{t}_j$	$\tilde{t}_1 \rightarrow c \tilde{\chi}_1^0$ $\tilde{t}_1 \rightarrow b \tilde{\chi}_1^\pm \rightarrow b f \bar{f}' \tilde{\chi}_1^0$	2 jets + $\cancel{E}_T$ 2 b jets + 2 leptons + $\cancel{E}_T$
• $\tilde{b}_i \tilde{b}_j$	$\tilde{b}_i \rightarrow b \tilde{\chi}_1^0$ $\tilde{b}_i \rightarrow b \tilde{\chi}_2^0 \rightarrow b f \bar{f}' \tilde{\chi}_1^0$	2 b jets + lepton + $\cancel{E}_T$ 2 b jets + $\cancel{E}_T$ 2 b jets + 2 leptons + $\cancel{E}_T$ 2 b jets + 2 jets + $\cancel{E}_T$

Numerous attempts to find superpartners at LEP II gave no positive result thus imposing the lower bounds on their masses [29]. They are shown on the parameter plane in Fig.16.

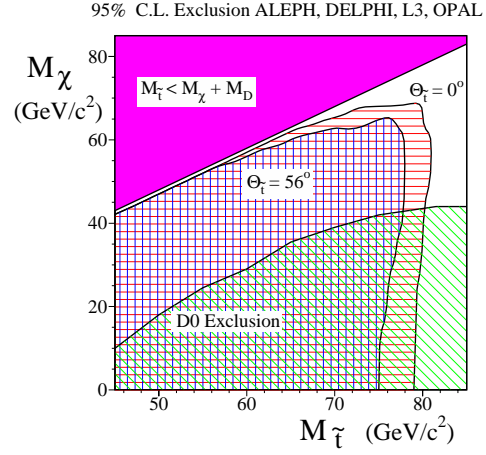
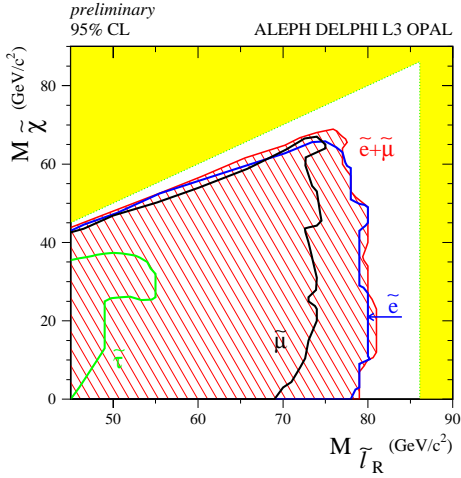


Figure 16: The excluded region in chargino-slepton and chargino-stop mass plane

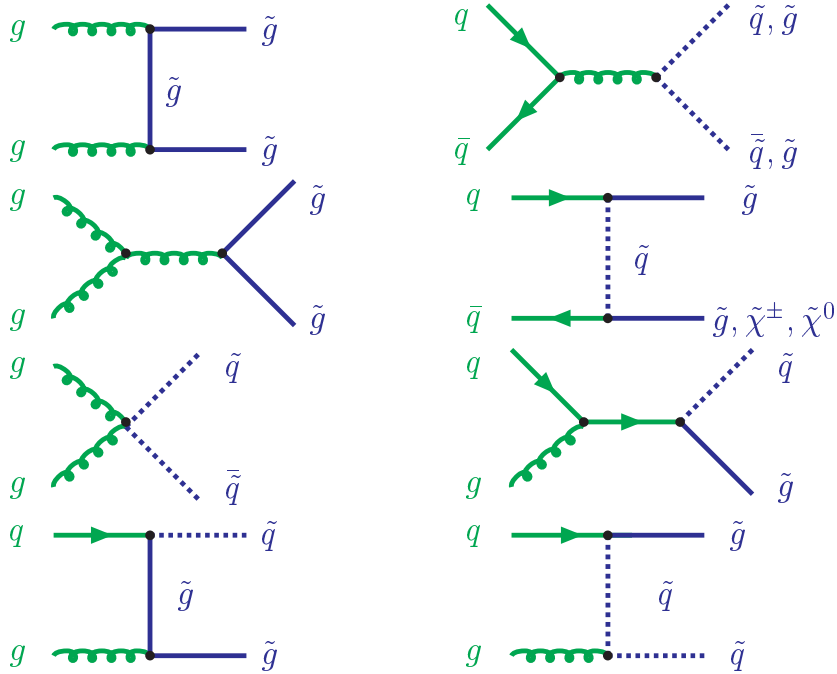


Figure 17: Gluon fusion,  $q\bar{q}$  scattering, quark-gluon scattering

Typical LEP II limits on the masses of superpartners are

$$\begin{aligned}
 m_{\chi_1^0} &> 40 \text{ GeV} & m_{\tilde{e}_{L,R}} &> 105 \text{ GeV} & m_{\tilde{t}} &> 90 \text{ GeV} \\
 m_{\chi_1^\pm} &> 100 \text{ GeV} & m_{\tilde{\mu}_{L,R}} &> 100 \text{ GeV} & m_{\tilde{b}} &> 80 \text{ GeV} \\
 & & m_{\tilde{\tau}_{L,R}} &> 80 \text{ GeV} & &
 \end{aligned}
 \tag{6.42}$$

## 6.5 Experimental signatures at hadron colliders

Experimental signatures at hadron colliders are similar to those at  $e^+e^-$  machines; however, here one has much wider possibilities. Besides the usual annihilation channel identical to  $e^+e^-$  one with the obvious replacement of electrons by quarks (see Fig.7), one has numerous processes of gluon fusion, quark-antiquark and quark-gluon scattering (see Fig.17).

Experimental SUSY signatures at the Tevatron (and LHC) are

<u>Production</u>	<u>Key Decay Modes</u>	<u>Signatures</u>
• $\tilde{g}\tilde{g}, \tilde{q}\tilde{q}, \tilde{g}\tilde{q}$	$\left. \begin{array}{l} \tilde{g} \rightarrow q\bar{q}\tilde{\chi}_1^0 \\ q\bar{q}'\tilde{\chi}_1^\pm \\ g\tilde{\chi}_1^0 \end{array} \right\} m_{\tilde{q}} > m_{\tilde{g}}$	$\cancel{E}_T$ + multijets (+leptons)
	$\left. \begin{array}{l} \tilde{q} \rightarrow q\tilde{\chi}_i^0 \\ \tilde{q} \rightarrow q'\tilde{\chi}_i^\pm \end{array} \right\} m_{\tilde{g}} > m_{\tilde{q}}$	
• $\tilde{\chi}_1^\pm \tilde{\chi}_2^0$	$\tilde{\chi}_1^\pm \rightarrow \tilde{\chi}_1^0 l^\pm \nu, \tilde{\chi}_2^0 \rightarrow \tilde{\chi}_1^0 ll$	Trilepton + $\cancel{E}_T$
	$\tilde{\chi}_1^\pm \rightarrow \tilde{\chi}_1^0 q\bar{q}', \tilde{\chi}_2^0 \rightarrow \tilde{\chi}_1^0 ll$	Dilepton + jet + $\cancel{E}_T$
• $\tilde{\chi}_1^+ \tilde{\chi}_1^-$	$\tilde{\chi}_1^+ \rightarrow l\tilde{\chi}_1^0 l^\pm \nu$	Dilepton + $\cancel{E}_T$
• $\tilde{\chi}_i^0 \tilde{\chi}_i^0$	$\tilde{\chi}_i^0 \rightarrow \tilde{\chi}_1^0 X, \tilde{\chi}_i^0 \rightarrow \tilde{\chi}_1^0 X'$	$\cancel{E}_T$ + Dilept+(jets)+lept
• $\tilde{t}_1 \tilde{t}_1$	$\tilde{t}_1 \rightarrow c\tilde{\chi}_1^0$	2 acollinear jets + $\cancel{E}_T$
	$\tilde{t}_1 \rightarrow b\tilde{\chi}_1^\pm, \tilde{\chi}_1^\pm \rightarrow \tilde{\chi}_1^0 q\bar{q}'$	single lepton + $\cancel{E}_T$ + $b's$
	$\tilde{t}_1 \rightarrow b\tilde{\chi}_1^\pm, \tilde{\chi}_1^\pm \rightarrow \tilde{\chi}_1^0 l^\pm \nu$	Dilepton + $\cancel{E}_T$ + $b's$
• $\tilde{l}\tilde{l}, \tilde{l}\tilde{\nu}, \tilde{\nu}\tilde{\nu}$	$\tilde{l}^\pm \rightarrow l \pm \tilde{\chi}_i^0, \tilde{l}^\pm \rightarrow \nu_l \tilde{\chi}_i^\pm$	Dilepton + $\cancel{E}_T$
	$\tilde{\nu} \rightarrow \nu \tilde{\chi}_1^0$	Single lept + $\cancel{E}_T$ + jets $\cancel{E}_T$

Note again the characteristic missing energy and transverse momenta events. Contrary to  $e^+e^-$  colliders, at hadron machines the background is extremely rich and essential.

## 6.6 The lightest superparticle

One of the crucial questions is the properties of the lightest superparticle. Different SUSY breaking scenarios lead to different experimental signatures and different LSP.

- Gravity mediation

In this case, the LSP is the lightest neutralino  $\tilde{\chi}_1^0$ , which is almost 90% photino for a low  $\tan\beta$  solution and contains more higgsino admixture for high  $\tan\beta$ . The usual signature for LSP is missing energy;  $\tilde{\chi}_1^0$  is stable and is the best candidate for the cold dark matter in the Universe. Typical processes, where the LSP is created, end up with jets +  $\cancel{E}_T$ , or leptons +  $\cancel{E}_T$ , or both jest + leptons +  $\cancel{E}_T$ .

- Gauge mediation

In this case the LSP is the gravitino  $\tilde{G}$  which also leads to missing energy. The actual question here is what the NLSP, the next-to-lightest particle, is. There are two possibilities:

i)  $\tilde{\chi}_1^0$  is the NLSP. Then the decay modes are:  $\tilde{\chi}_1^0 \rightarrow \gamma\tilde{G}, h\tilde{G}, Z\tilde{G}$ . As a result, one has two hard photons +  $\cancel{E}_T$ , or jets +  $\cancel{E}_T$ .

ii)  $\tilde{l}_R$  is the NLSP. Then the decay mode is  $\tilde{l}_R \rightarrow \tau\tilde{G}$  and the signature is a charged lepton and the missing energy.

- Anomaly mediation

In this case, one also has two possibilities:

i)  $\tilde{\chi}_1^0$  is the LSP and wino-like. It is almost degenerate with the NLSP.

ii)  $\tilde{\nu}_L$  is the LSP. Then it appears in the decay of chargino  $\tilde{\chi}^+ \rightarrow \tilde{\nu}l$  and the signature is the charged lepton and the missing energy.

- R-parity violation

In this case, the LSP is no longer stable and decays into the SM particles. It may be charged (or even colored) and may lead to rare decays like neutrinoless double  $\beta$ -decay, etc.

Experimental limits on the LSP mass follow from non-observation of the corresponding events. Modern lower limit from LEP is around 40 GeV (see Fig.18).

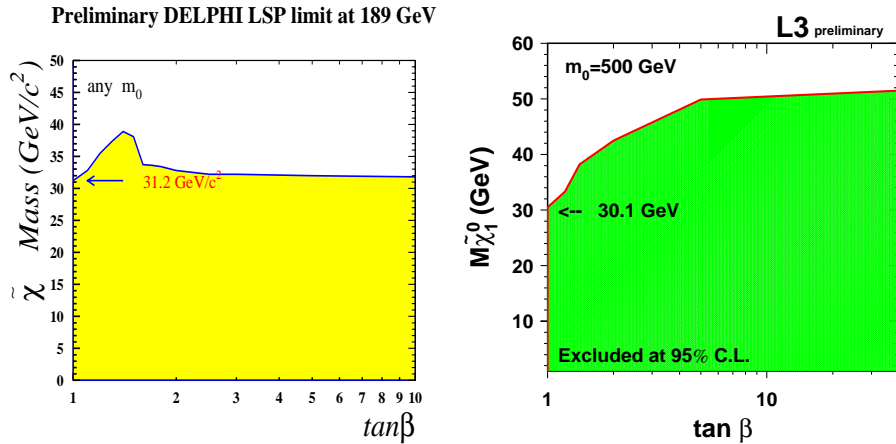


Figure 18: The LSP mass limits within the MSSM [29]

## 7 The Higgs boson mass in the MSSM

One of the hottest topics in the SM now is the search for the Higgs boson. It is also a window to a new physics. Below we consider properties of the Higgs boson in the MSSM.

It has already been mentioned that in the MSSM the mass of the lightest Higgs boson is predicted to be less than the  $Z$ -boson mass. This is, however, the tree level result and the masses acquire the radiative corrections. With account taken of the one-loop radiative corrections the lightest Higgs mass is

$$m_h^2 \approx M_Z^2 \cos^2 2\beta + \frac{3g^2 m_t^4}{16\pi^2 M_W^2} \log \frac{\tilde{m}_{t_1}^2 \tilde{m}_{t_2}^2}{m_t^4}. \quad (7.43)$$

One finds that the one-loop correction is positive and increases the mass value. Two loop corrections have the opposite effect but are smaller [37].

The Higgs mass depends mainly on the following parameters: the top mass, the squark masses, the mixing in the stop sector and  $\tan \beta$ . The maximum Higgs mass is obtained for large  $\tan \beta$ , for a maximum value of the top and squark masses and a minimum value of the stop mixing.

The lightest Higgs boson mass  $m_h$  is shown as a function of  $\tan \beta$  in Fig. 19 [38]. The shaded band corresponds to the uncertainty from the stop mass and stop mixing for  $m_t = 175$  GeV. The upper and lower lines correspond to  $m_t=170$  and 180 GeV, respectively.

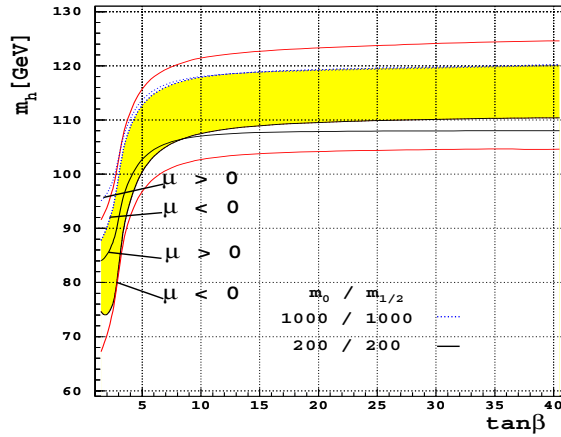


Figure 19: The mass of the lightest Higgs boson in the MSSM as a function of  $\tan \beta$

Combining all the uncertainties the results for the Higgs mass in the CMSSM can be summarized as follows:

- The low  $\tan \beta$  scenario ( $\tan \beta < 3.3$ ) of the CMSSM is excluded by the lower limit on the Higgs mass of 113.3 GeV [5].
- For the high  $\tan \beta$  scenario the Higgs mass is found to be [38]:

$$m_h = 115 \pm 3 \text{ (stopm)} \pm 1.5 \text{ (stopmix)} \pm 2 \text{ (theory)} \pm 5 \text{ (topm)} \text{ GeV,}$$

where the errors are the estimated standard deviations around the central value.

One can see that the LEP came very close to SUSY prediction for the Higgs mass and already ruled out low  $\tan \beta$  scenario. The next step is to be made by



Tevatron. Unfortunately, the luminosity of Tevatron at the moment is not enough to distinguish the Higgs boson from the background. One has to wait till LHC starts operation.

However, these SUSY limits on the Higgs mass may not be so restricting if non-minimal SUSY models are considered. Already in the Next-to-Minimal model [39] the Higgs mass at low  $\tan\beta$  may be lifted by 20-30 GeV. However, more sophisticated models do not change the generic feature of SUSY theories, the presence of the light Higgs boson.

## 8 Perspectives of SUSY observation

With the LEP shut down, further attempts to discover supersymmetry are connected with the Tevatron and LHC hadron colliders.

### 8.1 Tevatron

The Fermilab Tevatron collider will define the high energy frontier of particle physics while CERN's Large Hadron Collider is being built. At the first stage (Run IIa), it has  $2 \text{ fb}^{-1}$  of integrated luminosity per experiment at  $\sqrt{s} = 2 \text{ TeV}$ . At the second stage (Run IIb), the luminosity is expected to reach  $15 \text{ fb}^{-1}$  per experiment. However, since it is a hadron collider, not the full energy goes into collision taken away by those quarks in a proton that do not take part in the interaction. Any direct search is kinematically limited to below 450 GeV.

There exist numerous papers on SUSY searches at the Tevatron [40]-[43]. Modern exclusion areas are shown in plots in Fig.20 [40] for squarks, sneutrinos, and gluino.

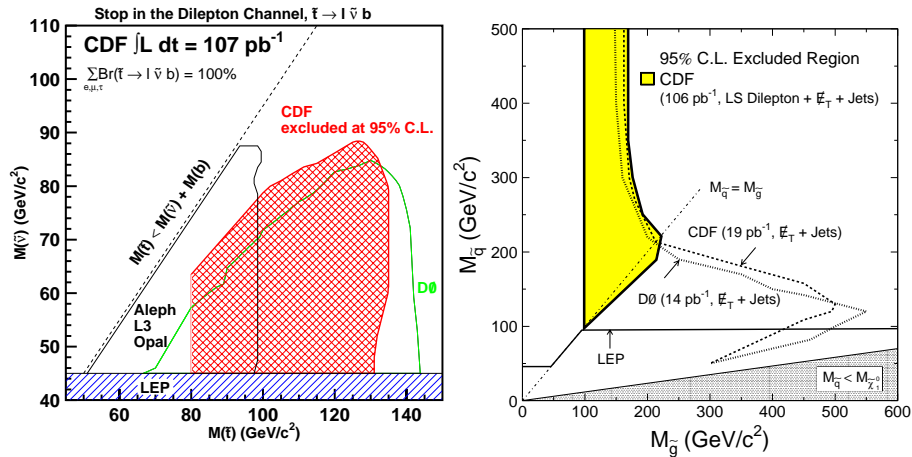


Figure 20: Exclusion plots for squarks and sneutrinos (left) and squarks and gluino (right) at Tevatron

They impose the limits on the squark and gluino masses:  $m_{\tilde{q}} \geq 300 \text{ GeV}$ ,  $m_{\tilde{g}} \geq 195 \text{ GeV}$ .

We show in Table 2 [41] the discovery reach of the Tevatron for squarks of the third generation for  $20 \text{ fb}^{-1}$  of integrated luminosity. They are still far from the expected masses of superpartners predicted by the MSSM (see Table 1).

Decay ( $Br = 100\%$ )	Subsequent Decay	Final State of $\tilde{b}_1\tilde{b}_1$ or $\tilde{t}_1\tilde{t}_1$	Discovery Reach @20 $\text{fb}^{-1}$	Run I
$\tilde{b}_1 \rightarrow b\tilde{\chi}_1^0$		$b\cancel{b}\cancel{E}_T$	260 $\text{GeV}/c^2$	146 $\text{GeV}/c^2$
$\tilde{t}_1 \rightarrow c\tilde{\chi}_1^0$		$c\cancel{c}\cancel{E}_T$	220 $\text{GeV}/c^2$	116 $\text{GeV}/c^2$
$\tilde{t}_1 \rightarrow b\tilde{\nu}$	$\tilde{\nu} \rightarrow \nu\tilde{\chi}_1^0$	$l^+l^-b\cancel{E}_T$	240 $\text{GeV}/c^2$	140 $\text{GeV}/c^2$
$\tilde{t}_1 \rightarrow b\tilde{\nu}\tilde{\chi}_1^0$		$l^+l^-b\cancel{E}_T$	-	129 $\text{GeV}/c^2$
$\tilde{t}_1 \rightarrow b\tilde{\chi}_1^\pm$	$\tilde{\chi}_1^\pm \rightarrow W^{(*)}\tilde{\chi}_1^0$	$l^+l^-b\cancel{E}_T$ ;	210 $\text{GeV}/c^2$	(-)
$\tilde{t}_1 \rightarrow bW\tilde{\chi}_1^0$		$l^+l^-bj\cancel{E}_T$	190 $\text{GeV}/c^2$	(-)

Table 2: Discovery reaches on  $M_{\tilde{b}}$  and  $M_{\tilde{t}}$  expected in Run II.

Gluinos and squarks are pair-produced at the Tevatron. One may have  $\tilde{g}\tilde{g}$ ,  $\tilde{g}\tilde{q}$ , and  $\tilde{q}\tilde{q}$  pairs. In most of the parameter space accessible at the Tevatron, the left-chiral squark dominantly decays into a quark and either a  $\tilde{\chi}_1^\pm$  or a  $\tilde{\chi}_2^0$ . Pair-produced squarks and gluinos have at least two large- $E_T$  jets associated with large missing energy. The final state with lepton(s) is possible due to leptonic decays of the  $\tilde{\chi}_1^\pm$  and/or  $\tilde{\chi}_2^0$ .

We show also the discovery reach of the Tevatron in the  $m_0, m_{1/2}$  parameter plane of the MSSM in the trilepton channel [41] for two values of  $\tan\beta$  (see Fig.21). The trilepton signal arises when both the lightest chargino ( $\tilde{\chi}_1^\pm$ ) and the next-to-lightest neutralino ( $\tilde{\chi}_2^0$ ) decay leptonically in  $p\bar{p} \rightarrow \tilde{\chi}_1^\pm\tilde{\chi}_2^0 + X$ . In the trilepton channel the Tevatron will be sensitive up to  $m_{1/2} \leq 250 \text{ GeV}$  if  $m_0 \leq 200 \text{ GeV}$  and up to  $m_{1/2} \leq 200 \text{ GeV}$  if  $m_0 \geq 500 \text{ GeV}$ .

## 8.2 LHC

The LHC hadron collider is the ultimate machine for new physics at the TeV scale. Its c.m. energy is planned to be 14 TeV with very high luminosity up to a few hundred  $\text{fb}^{-1}$ . The LHC is supposed to cover a wide range of parameters of the MSSM (see Figs. below) and discover the superpartners with the masses below 2 TeV [44]. This will be a crucial test for the MSSM and the low energy supersymmetry. The LHC potential to discover supersymmetry is widely discussed in the literature [44]-[46].

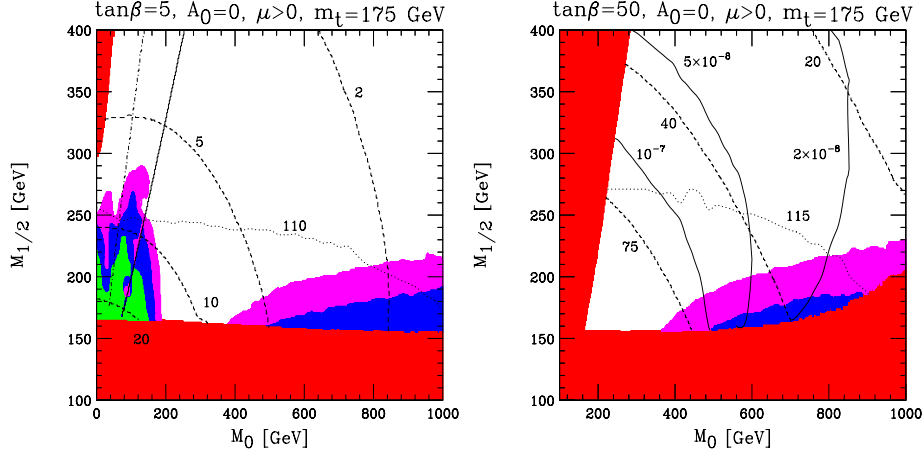


Figure 21: Regions of the  $m_0, m_{1/2}$  plane where the trilepton events should be detectable at the level of  $5\sigma$  significance for  $\tan\beta = 5$  (left) and  $\tan\beta = 50$  (right) [42]. Three areas are shown for the integrated luminosity of  $30 \text{ fb}^{-1}$  (magenta),  $10 \text{ fb}^{-1}$  (blue) and  $2 \text{ fb}^{-1}$  (green). The red regions are excluded. Dashed lines represent the SUSY contribution to the muon anomalous magnetic moment (in units of  $10^{-10}$ ) and the dotted lines are iso-mass contours of the lightest neutral Higgs boson.

The gluino and squark production cross sections at LHC can reach 1 pb for masses around 1 TeV. Their decays produce missing transverse momentum from the LSP escape plus multiple jets and a varying number of leptons from the intermediate gauginos. The main decay mode is quarks and gluons plus the LSP. Cascade decays and as a consequence of multilepton events are almost negligible. A typical event with the cascade squark decay is shown in Fig.22.

The LHC will be able to discover SUSY with squark and gluino masses up to  $2 \div 2.5 \text{ TeV}$  for the luminosity  $L_{tot} = 100 \text{ fb}^{-1}$ . The expected discovery reach for various channels is shown in Figs.23, 24. The most powerful signature for squark and gluino detection are multijet events; however, the discovery potential depends on relation between the LSP, squark, and gluino masses, and decreases with the increase of the LSP mass.

Slepton pairs produced through the Drell-Yan mechanism  $pp \rightarrow \gamma^*/Z^* \rightarrow \tilde{l}^+\tilde{l}^-$  can be detected through their leptonic decays  $\tilde{l} \rightarrow l + \tilde{\chi}_1^0$ . The typical signature used for sleptons detection is the dilepton pair with missing energy and no hadronic jets. For the luminosity  $L_{tot} = 100 \text{ fb}^{-1}$  LHC will be able to discover sleptons with the masses up to 400 GeV [44]. The discovery reach for sleptons in various channels is shown in Fig.25.

Chargino and neutralino pairs are also produced via the Drell-Yan mechanism  $pp \rightarrow \tilde{\chi}_1^\pm \tilde{\chi}_2^0$  and may be detected through their leptonic decays  $\tilde{\chi}_1^\pm \tilde{\chi}_2^0 \rightarrow lll + E_T^{miss}$ . So their main signature is the isolated leptons with missing energy. The

## Gluino/squark production event topology allowing sparticle mass reconstruction

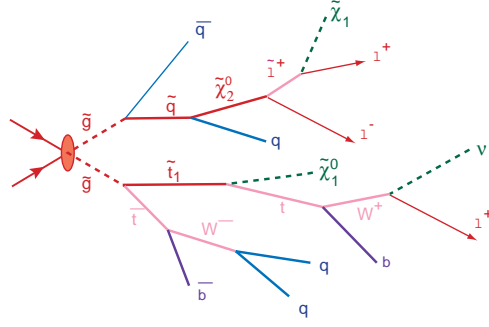


Figure 22: The cascade decay of squarks into jets and neutralino with possible addition of multileptons

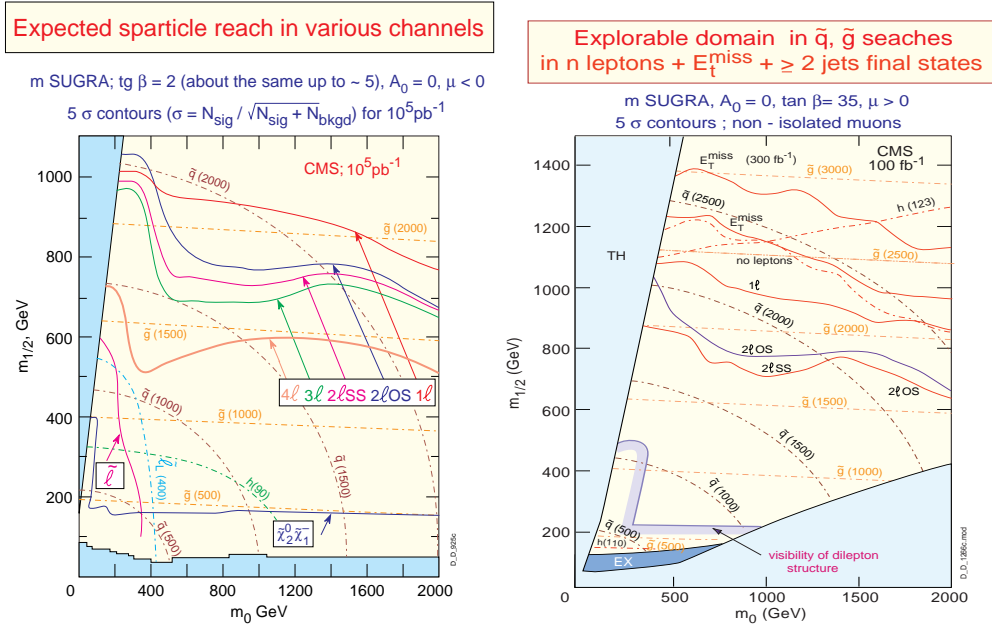


Figure 23: Expected sparticle reach in various channels at LHC [45]

main background to the three lepton channel comes from  $WZ/ZZ, t\bar{t}, Zb\bar{b}$  and  $b\bar{b}$  production. There could also be SUSY background arising from squarks and gluino cascade decays into multileptonic modes. In the case of light gauginos and heavy squarks and sleptons, which can be realized in some regions of parameter space of the MSSM, the cross sections for gaugino production may reach few pb. Neutralinos

and charginos could be detected provided their masses are lighter than 350 GeV [44].

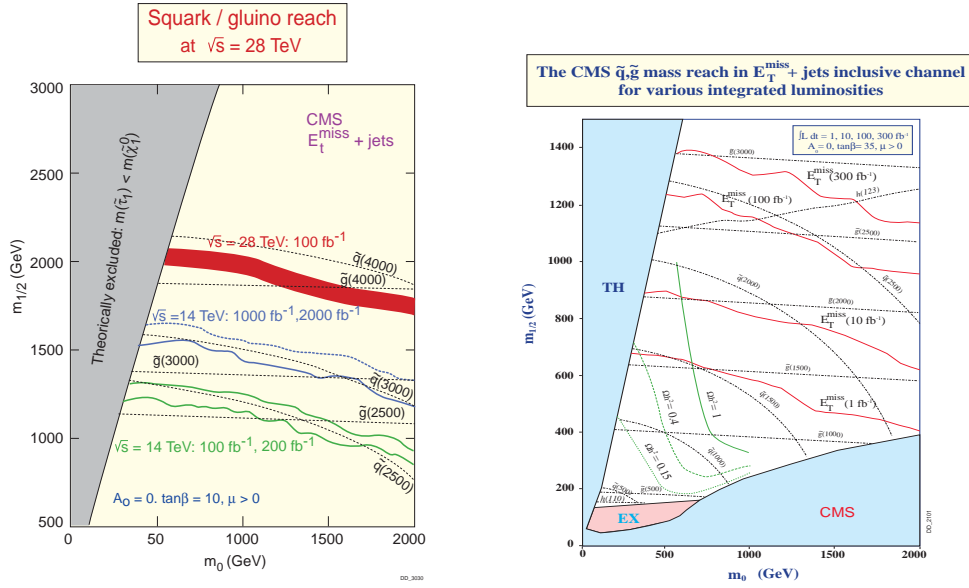


Figure 24: Expected squarks and gluino reach at LHC for various luminosities [45]

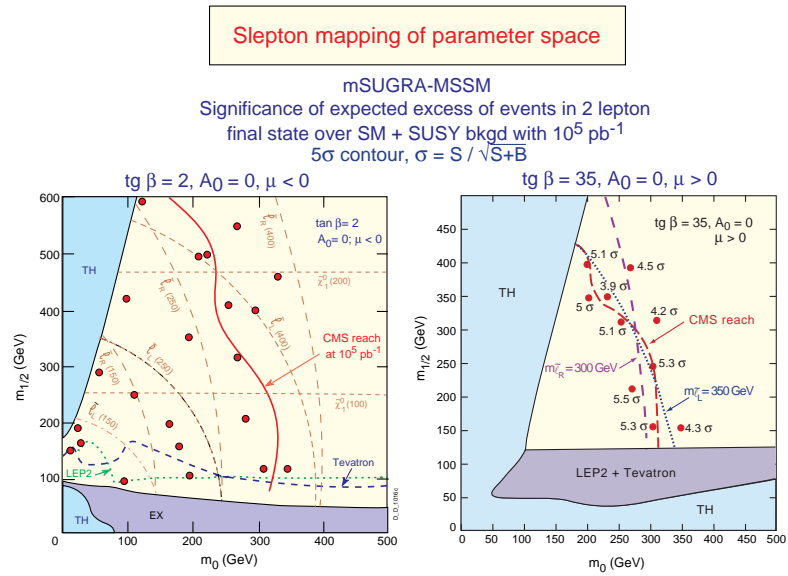


Figure 25: Expected slepton reach at LHC [45]

## 9 Conclusion

Supersymmetry is now the most popular extension of the Standard Model. It promises us that new physics is round the corner at a TeV scale to be exploited at new machines of this decade. If our expectations are correct, very soon we will face new discoveries, the whole world of supersymmetric particles will show up and the table of fundamental particles will be enlarged in increasing rate. This would be a great step in understanding the microworld.

### Acknowledgements

I am grateful to the organizers of the School at Zvenigorod for providing very nice atmosphere during the school and to the students for their interest and attention. Financial support from RFBR grant # 02-02-16889, the grant of THE Russian Ministry of Industry, Science and Technologies # 2339.2003.2 is kindly acknowledged.

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