

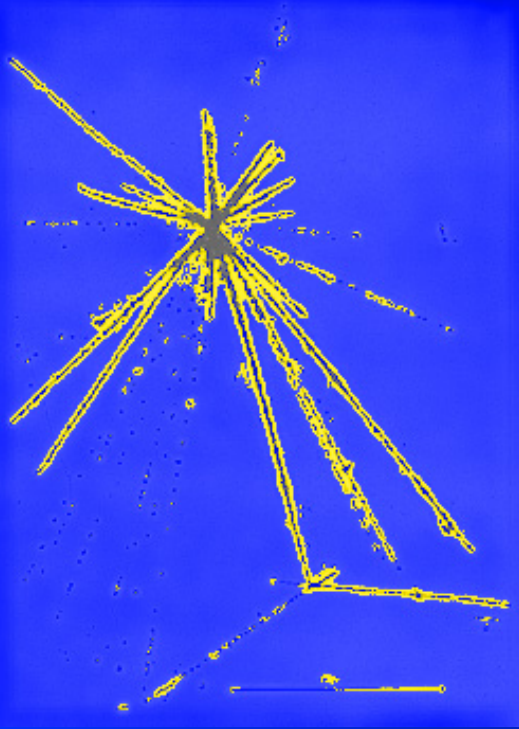
# BEYOND THE STANDARD MODEL

Dmitri Kazakov

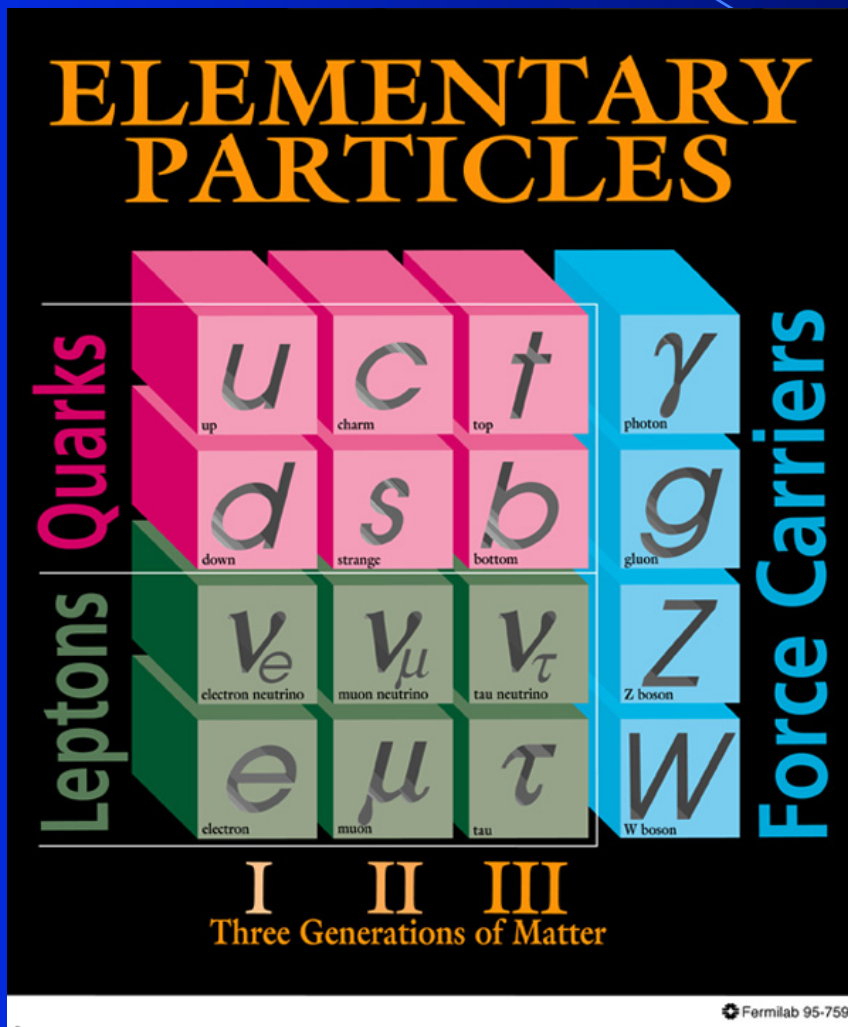
JINR/ITEP

## Outline

1. What is SUSY
2. Motivation of SUSY
3. Basics of SUSY
4. The MSSM
5. Constrained MSSM
6. SUSY searches



# The Standard Model



Forces

Electromagnetic

Strong

Weak

Gravity

Standard Model

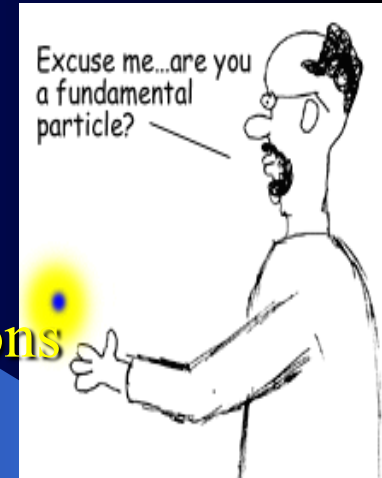
H

The Higgs boson

# The SM and Beyond

## The problems of the SM:

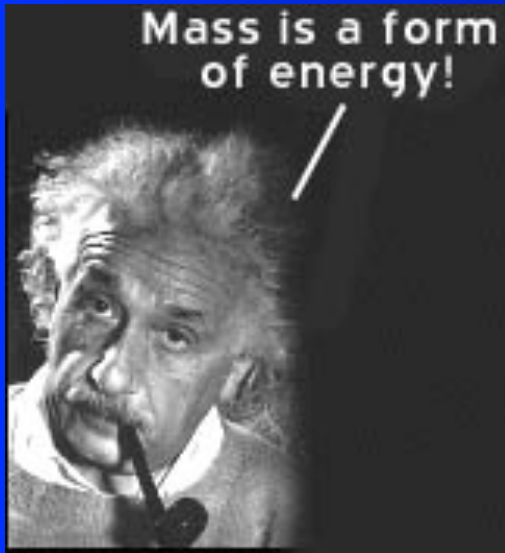
- Inconsistency at high energies due to Landau pole
- Large number of free parameters
- Formal unification of strong and electroweak interactions
- Still unclear mechanism of EW symmetry breaking
- CP-violation is not understood
- Flavour mixing and the number of generations is arbitrary
- The origin of the mass spectrum is unclear



## The ways beyond the SM:

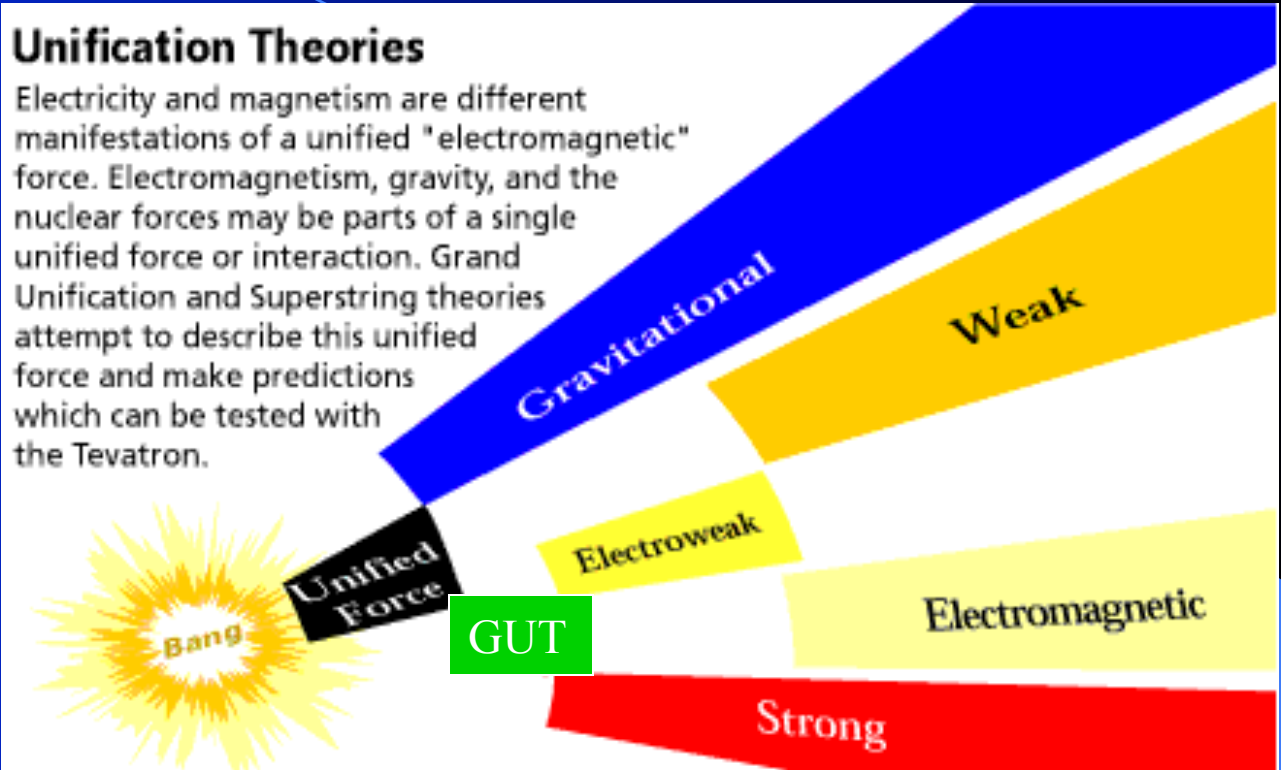
- The SAME fields with NEW interactions → GUT, SUSY, String
- NEW fields with NEW interactions → Compositeness, Technicolour, preons

# Grand Unified Theories

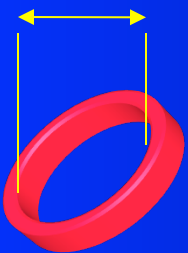


## Unification Theories

Electricity and magnetism are different manifestations of a unified "electromagnetic" force. Electromagnetism, gravity, and the nuclear forces may be parts of a single unified force or interaction. Grand Unification and Superstring theories attempt to describe this unified force and make predictions which can be tested with the Tevatron.



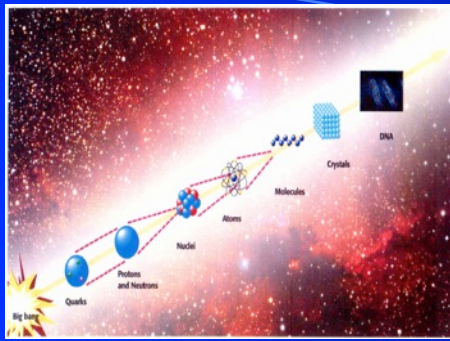
$10^{-34} m$



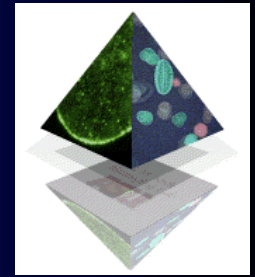
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- Unification of strong, weak and electromagnetic interactions within Grand Unified Theories is the new step in unification of all forces of Nature
- Creation of a unified theory of everything based on string paradigm seems to be possible





# What is SUSY



- **Supersymmetry** is a boson-fermion symmetry that is aimed to unify all forces in Nature including gravity within a single framework

$$Q | \text{boson} \rangle = | \text{fermion} \rangle \quad Q | \text{fermion} \rangle = | \text{boson} \rangle$$

$$[b, b] = 0, \quad \{f, f\} = 0 \Rightarrow$$

$$\{Q_{\alpha}^i, \bar{Q}_{\dot{\beta}}^j\} = 2\delta^{ij} (\sigma^{\mu})_{\alpha\dot{\beta}} P_{\mu}$$

- Modern views on supersymmetry in particle physics are based on string paradigm, though low energy manifestations of SUSY can be found (?) at modern colliders and in non-accelerator experiments

# Motivation of SUSY in Particle Physics

- Unification with Gravity
- Unification of gauge couplings
- Solution of the hierarchy problem
- Dark matter in the Universe  
*spin 2*  $\rightarrow$  *spin 3/2*  $\rightarrow$  *spin 1*  $\rightarrow$  *spin 1/2*  $\rightarrow$  *spin 0*
- Superstrings

Unification of matter (fermions) with forces (bosons) naturally arises

from an attempt to unify gravity with the other interactions

$$\{Q_\alpha^i, \bar{Q}_{\dot{\beta}}^j\} = 2\delta^{ij}(\sigma^\mu)_{\alpha\dot{\beta}} P_\mu \implies \{\delta_\varepsilon, \bar{\delta}_{\bar{\varepsilon}}\} = 2(\varepsilon\sigma^\mu\bar{\varepsilon})P_\mu$$

$\varepsilon = \varepsilon(x)$  local coordinate transformation.

Local translation =  
general relativity !

*Supertranslation*

$$x_\mu \rightarrow x_\mu + i\theta\sigma_\mu\xi - i\xi\sigma_\mu\bar{\theta},$$

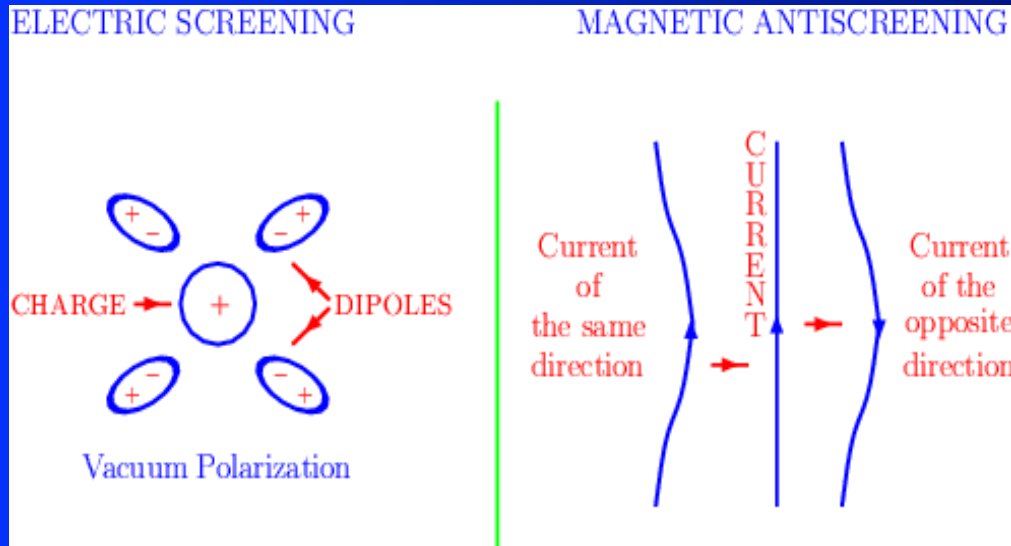
$$\theta \rightarrow \theta + \xi,$$

$$\bar{\theta} \rightarrow \bar{\theta} + \bar{\xi}$$

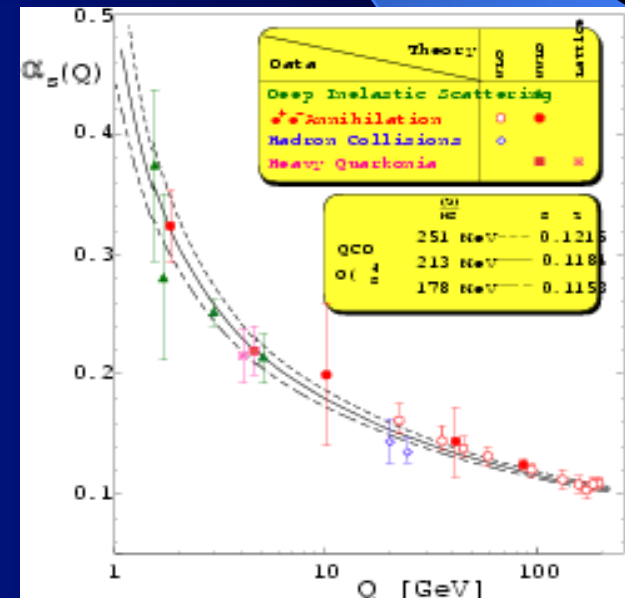
# Motivation of SUSY in Particle Physics

- Unification of gauge couplings

| Low Energy    |                | ⇒ High Energy |                                       |
|---------------|----------------|---------------|---------------------------------------|
| $SU_c(3)$     | $SU_L(2)$      | $U_Y(1)$      | ⇒ $G_{GUT}$ (or $G^n + \text{symm}$ ) |
| <i>gluons</i> | <i>W, Z</i>    | <i>photon</i> | ⇒ <i>gauge bosons</i>                 |
| <i>quarks</i> | <i>leptons</i> |               | ⇒ <i>fermions</i>                     |
| $g_3$         | $g_2$          | $g_1$         | ⇒ $g_{GUT}$                           |



$$\alpha_i = \alpha_i \left( \frac{Q^2}{\Lambda^2} \right) = \alpha_i(\text{distance})$$



Running of the strong coupling 7

# Motivation of SUSY

RG Equations  $\frac{d\tilde{\alpha}_i}{dt} = b_i \tilde{\alpha}_i^2$ ,  $\tilde{\alpha}_i = \alpha_i / 4\pi = g_i^2 / 16\pi^2$ ,  $t = \log(Q^2 / \mu^2)$

$$SM: \quad b_i = \begin{pmatrix} b_1 \\ b_2 \\ b_3 \end{pmatrix} = \begin{pmatrix} 0 \\ -22/3 \\ -11 \end{pmatrix} + N_{Fam} \begin{pmatrix} 4/3 \\ 4/3 \\ 4/3 \end{pmatrix} + N_{Higgs} \begin{pmatrix} 1/10 \\ 1/6 \\ 0 \end{pmatrix}$$

$$MSSM: \quad b_i = \begin{pmatrix} b_1 \\ b_2 \\ b_3 \end{pmatrix} = \begin{pmatrix} 0 \\ -6 \\ -9 \end{pmatrix} + N_{Fam} \begin{pmatrix} 2 \\ 2 \\ 2 \end{pmatrix} + N_{Higgs} \begin{pmatrix} 3/10 \\ 1/2 \\ 0 \end{pmatrix}$$

Unification of the Coupling Constants  
in the SM and in the MSSM

Input

$$\alpha^{-1}(M_Z) = 128.978 \pm 0.027$$

$$\sin^2 \theta_{MS} = 0.23146 \pm 0.00017$$

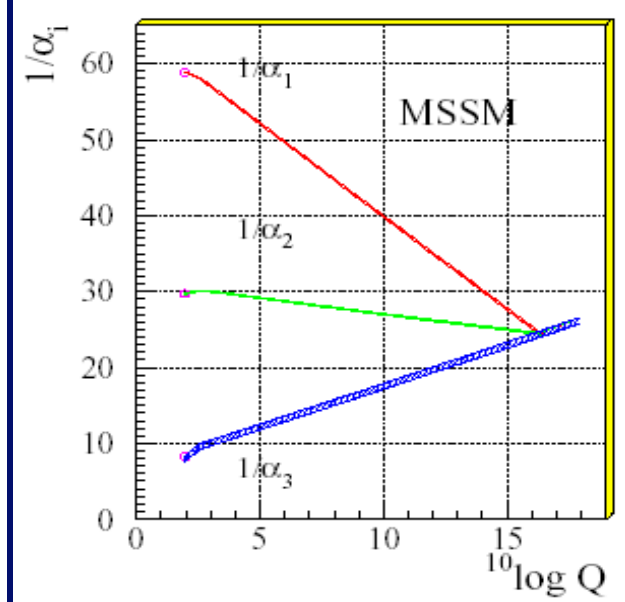
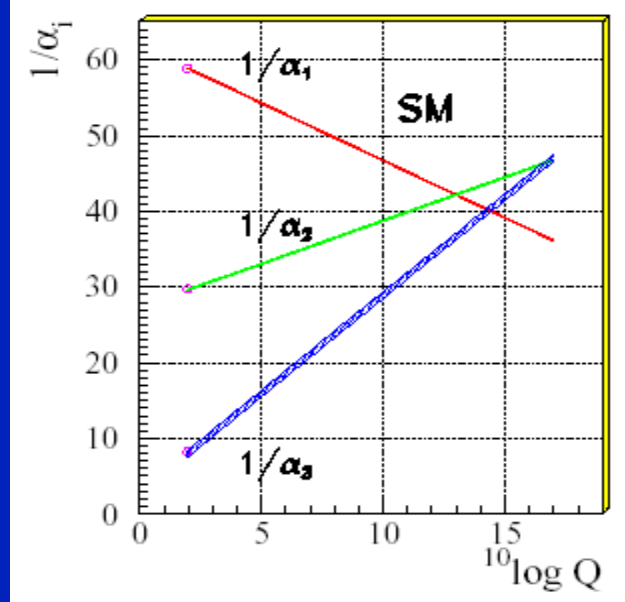
$$\alpha_s(M_Z) = 0.1184 \pm 0.0031$$

Output

$$M_{SUSY} = 10^{3.4 \pm 0.9 \pm 0.4} \text{ GeV}$$

$$M_{GUT} = 10^{15.8 \pm 0.3 \pm 0.1} \text{ GeV}$$

$$\alpha_{GUT}^{-1} = 26.3 \pm 1.9 \pm 1.0$$



SUSY yields unification!



# Motivation of SUSY

- Solution of the Hierarchy Problem

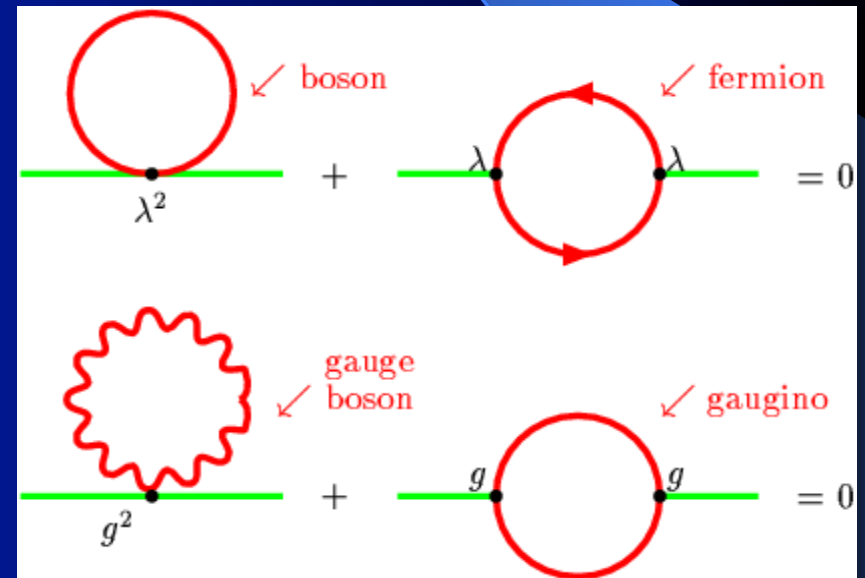
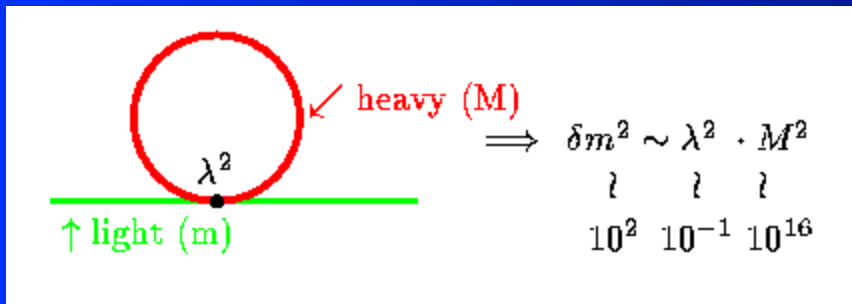
$$m_H \sim v \sim 10^2 \text{ GeV}$$

$$m_\Sigma \sim V \sim 10^{16} \text{ GeV}$$

$$\frac{m_H}{m_\Sigma} \sim 10^{-14} \ll 1$$

Cancellation of quadratic terms

Destruction of the hierarchy by radiative corrections

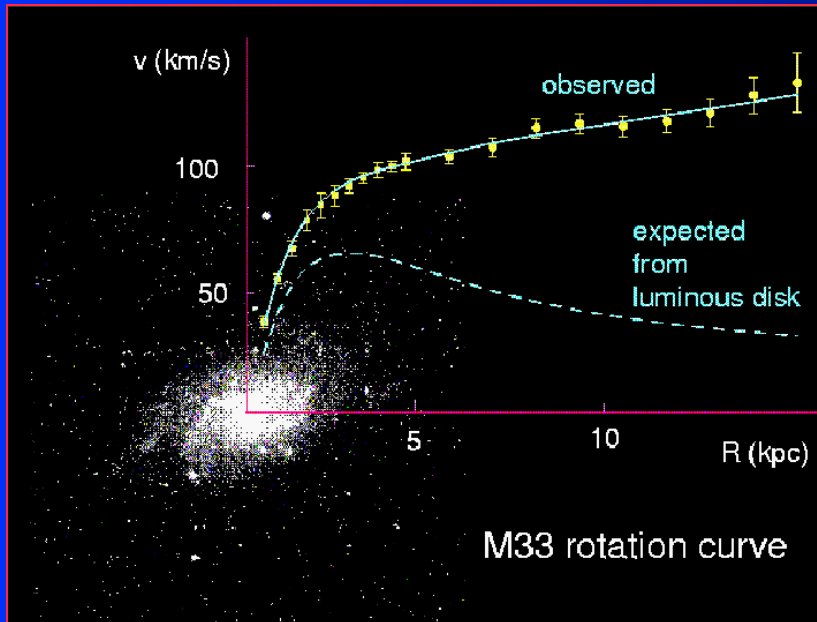


SUSY may also explain the origin of the hierarchy due to radiative mechanism

$$\sum_{\text{bosons}} m^2 = \sum_{\text{fermions}} m^2$$

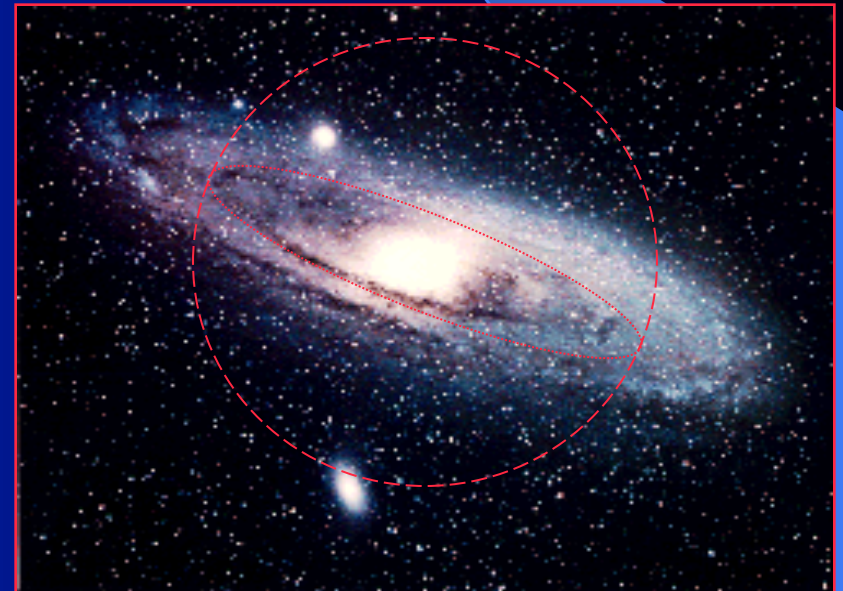
# Motivation of SUSY

- Dark Matter in the Universe



Spiral galaxies consist of a central bulge and a very thin disc, and surrounded by an approximately spherical halo of dark matter

The flat rotation curves of spiral galaxies provide the most direct evidence for the existence of large amount of the dark matter.



SUSY provides a candidate for the Dark matter – a stable neutral particle<sup>10</sup>

# Cosmological Constraints

## New precise cosmological data

$$\Omega h^2 = 1 \quad \longleftrightarrow \quad \rho = \rho_{crit}$$

$$\Omega_{vacuum} \approx 73\%$$

$$\Omega_{DarkMatter} \approx 23 \pm 4\%$$

$$\Omega_{Baryon} \approx 4\%$$

Dark Matter in the Universe:



- Supernova Ia explosion
- CMBR thermal fluctuations  
(news from WMAP)



Hot DM  
(not favoured by  
galaxy formation)

Cold DM  
(rotation curves  
of Galaxies)

SUSY

# Supersymmetry

(Super) Algebra

$$[P_\mu, P_\nu] = 0, [P_\mu, M_{\rho\sigma}] = i(g_{\mu\rho} P_\sigma - g_{\mu\sigma} P_\rho),$$

$$[M_{\mu\nu}, M_{\rho\sigma}] = i(g_{\nu\rho} M_{\mu\sigma} - g_{\nu\sigma} M_{\mu\rho} - g_{\mu\rho} M_{\nu\sigma} + g_{\mu\sigma} M_{\nu\rho}),$$

$$[B_r, B_s] = iC_{rs}^t B_t, [B_r, P_\mu] = [B_r, M_{\mu\sigma}] = 0,$$

$$[Q_\alpha^i, P_\mu] = [\bar{Q}_{\dot{\alpha}}^i, P_\mu] = 0,$$

$$[Q_\alpha^i, M_{\mu\nu}] = \frac{1}{2}(\sigma_{\mu\nu})_\alpha^\beta Q_\beta^i, [\bar{Q}_{\dot{\alpha}}^i, M_{\mu\nu}] = -\frac{1}{2}\bar{Q}_{\dot{\beta}}^i (\bar{\sigma}_{\mu\nu})^{\dot{\alpha}\dot{\beta}},$$

$$[O^i, B] = (b)^i O^j, [\bar{O}^i, B] = -\bar{O}^j (b)^j,$$

$$\{Q_\alpha^i, \bar{Q}_{\dot{\beta}}^j\} = 2\delta^{ij} (\sigma^\mu)_{\alpha\dot{\beta}} P_\mu$$

$$\{Q_\alpha^i, Q_\beta^j\} = 2\varepsilon_{\alpha\beta} Z^{ij}, Z^{ij} = Z_{ij}^\dagger, Z_{ij} = a_{ij}^r b_r,$$

$$\{\bar{Q}_{\dot{\alpha}}^i, \bar{Q}_{\dot{\beta}}^j\} = -2\varepsilon_{\dot{\alpha}\dot{\beta}} Z^{ij}, [Z_{ij}, \text{anything}] = 0,$$

$$\alpha, \dot{\alpha}, \beta, \dot{\beta} = 1, 2; i, j = 1, 2, \dots, N.$$

Superspace

$$x_\mu \rightarrow x_\mu, \theta_\alpha, \bar{\theta}_{\dot{\alpha}}$$

$\alpha, \dot{\alpha} = 1, 2$

Grassmannian

parameters  $\theta_\alpha^2 = 0, \bar{\theta}_{\dot{\alpha}}^2 = 0$

SUSY Generators

$$Q_\alpha = \frac{\partial}{\partial \theta_\alpha} - i\sigma_{\alpha\dot{\alpha}}^\mu \bar{\theta}^{\dot{\alpha}} \partial_\mu$$

$$\bar{Q}_{\dot{\alpha}} = -\frac{\partial}{\partial \bar{\theta}_{\dot{\alpha}}} + i\theta_\alpha \sigma_{\alpha\dot{\alpha}}^\mu \partial_\mu$$

$$Q_\alpha^2 = 0, \bar{Q}_{\dot{\alpha}}^2 = 0$$

This is the only possible graded Lie algebra that mixes integer and half-integer spins and changes statistics



# Basics of SUSY

Quantum states: Vacuum =  $|E, \lambda\rangle$   $Q|E, \lambda\rangle = 0$

$$[Q_\alpha^i, P_\mu] = [\bar{Q}_\alpha^i, P_\mu] = 0$$

↑ Energy
 ↑ helicity

| State      | Expression  | # of states                       |
|------------|---|-----------------------------------|
| vacuum     | $ E, \lambda\rangle$  | 1                                 |
| 1-particle | $\bar{Q}_i  E, \lambda\rangle =  E, \lambda + 1/2\rangle$                           | $\binom{N}{1} = N$                |
| 2-particle | $\bar{Q}_i \bar{Q}_j  E, \lambda\rangle =  E, \lambda + 1\rangle$                   | $\binom{N}{2} = \frac{N(N-1)}{2}$ |
| ...        | ...   | ...                               |
| N-particle | $\bar{Q}_1 \bar{Q}_2 \dots \bar{Q}_N  E, \lambda\rangle =  E, \lambda + N/2\rangle$ | $\binom{N}{N} = 1$                |

Total # of states  $\sum_{k=0}^N \binom{N}{k} = 2^N = 2^{N-1} \text{ bosons} + 2^{N-1} \text{ fermions}$

# SUSY Multiplets

Chiral multiplet  $N = 1, \lambda = 0$

|             |      |   |     |
|-------------|------|---|-----|
| helicity    | -1/2 | 0 | 1/2 |
| # of states | 1    | 2 | 1   |

scalar spinor  
 $(\varphi, \psi)$

Vector multiplet  $N = 1, \lambda = 1/2$

|             |    |      |     |   |
|-------------|----|------|-----|---|
| helicity    | -1 | -1/2 | 1/2 | 1 |
| # of states | 1  | 1    | 1   | 1 |

spinor vector  
 $(\lambda, A_\mu)$

Members of a supermultiplet are called **superpartners**

Extended SUSY multiplets

|     |         |             |    |      |    |      |    |     |    |     |   |
|-----|---------|-------------|----|------|----|------|----|-----|----|-----|---|
| N=4 | SUSY YM | helicity    | -1 | -1/2 | 0  | 1/2  | 1  |     |    |     |   |
|     |         | # of states | 1  | 4    | 6  | 4    | 1  |     |    |     |   |
| N=8 | SUGRA   | helicity    | -2 | -3/2 | -1 | -1/2 | 0  | 1/2 | 1  | 3/2 | 2 |
|     |         | # of states | 1  | 8    | 28 | 56   | 70 | 56  | 28 | 8   | 1 |

$N \leq 4S$  ← spin

$N \leq 4$

For renormalizable theories (YM)

$N \leq 8$

For (super)gravity

# Minimal Supersymmetric Standard Model (MSSM)

- SUSY: # of fermions = # of bosons    N=1 SUSY:  $(\varphi, \psi)$   $(\lambda, A_\mu)$
- SM: 28 bosonic d.o.f. & 90 (96) fermionic d.o.f.

There are no particles in the SM that can be superpartners

SUSY associates known bosons with new fermions and known fermions with new bosons

- Even number of the Higgs doublets – min = 2

Cancellation of axial anomalies (in each generation)

$$\text{Tr } Y^3 = 3\left(\frac{1}{27} + \frac{1}{27} - \frac{64}{27} + \frac{8}{27}\right) - 1 - 1 + 8 = 0$$

↑ ↑ ↑ ↑ ↑ ↑ ↑ ↑

colour  $u_L$   $d_L$   $u_R$   $d_R$   $\nu_L$   $e_L$   $e_R$

Higgsinos

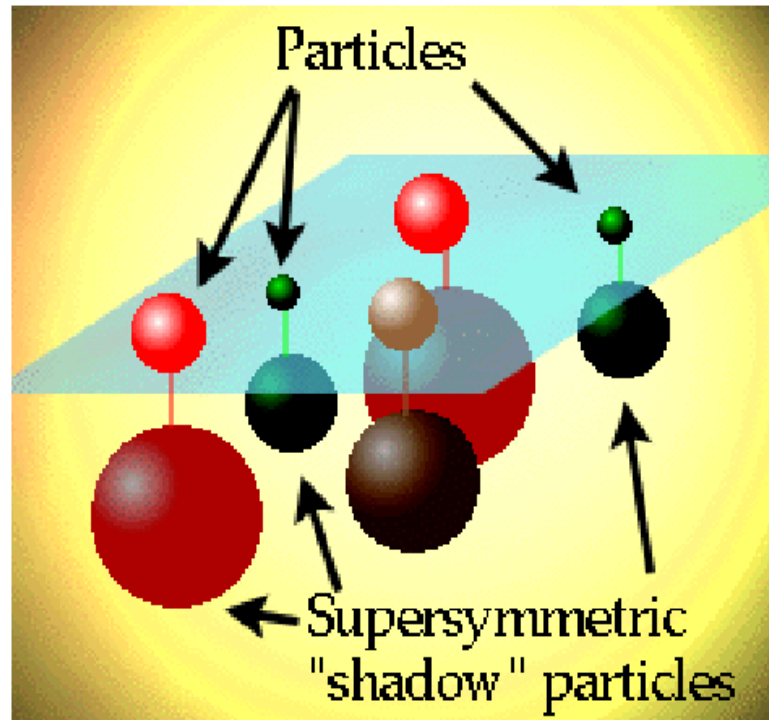
$$-1 + 1 = 0$$

# Particle Content of the MSSM

| Superfield    | Bosons                  | Fermions   | $SU_c(3)$ | $SU_L(2)$          | $U_Y(1)$ |   |      |
|---------------|-------------------------|--|-----------|--------------------|----------|---|------|
| <i>Gauge</i>  |                         |  |           |                    |          |   |      |
| $G^a$         | gluon $g^a$             | gluino $\tilde{g}^a$   | 8         | 1                  | 0        |   |      |
| $V^k$         | Weak $W^k (W^\pm, Z)$   | wino, zino $\tilde{w}^k (\tilde{w}^\pm, \tilde{z})$  | 1         | 3                  | 0        |   |      |
| $V'$          | Hypercharge $B(\gamma)$ | bino $\tilde{b}(\tilde{\gamma})$   | 1         | 1                  | 0        |   |      |
| <i>Matter</i> |                         |  |           |                    |          |   |      |
| $L_i$         | sleptons                | $\tilde{L}_i = (\tilde{\nu}, \tilde{e})_L$<br>$\tilde{E}_i = \tilde{e}_R$                              | leptons   | $L_i = (\nu, e)_L$ | 1        | 2 | -1   |
| $E_i$         |                         |  |           | $E_i = e_R$        | 1        | 1 | 2    |
| $Q_i$         | squarks                 | $\tilde{Q}_i = (\tilde{u}, \tilde{d})_L$<br>$\tilde{U}_i = \tilde{u}_R$<br>$\tilde{D}_i = \tilde{d}_R$ | quarks    | $Q_i = (u, d)_L$   | 3        | 2 | 1/3  |
| $U_i$         |                         |  |           | $U_i = u_R^c$      | 3*       | 1 | -4/3 |
| $D_i$         |                         |  |           | $D_i = d_R^c$      | 3*       | 1 | 2/3  |
| <i>Higgs</i>  |                         |  |           |                    |          |   |      |
| $H_1$         | Higgses                 | $H_1$<br>$H_2$   | higgsinos | $\tilde{H}_1$      | 1        | 2 | -1   |
| $H_2$         |                         |  |           | $\tilde{H}_2$      | 1        | 2 | 1    |



# SUSY Shadow World



One half is observed!

One half is NOT observed!

# The MSSM Lagrangian

$$L = L_{gauge} + L_{Yukawa} + L_{SoftBreaking}$$

The Yukawa Superpotential

superfields

$$W_R = y_U Q_L H_2 U_R + y_D Q_L H_1 D_R + y_L L_L H_1 E_R + \mu H_1 H_2$$

Yukawa couplings

Higgs mixing term

$$W_{NR} = \lambda_L L_L L_L E_R + \lambda'_L L_L Q_L D_R + \mu' L_L H_2 + \lambda_B U_R D_R D_R$$

R-parity  $R = (-)^{3(B-L)+2S}$

The Usual Particle :  $R = + 1$

SUSY Particle :  $R = - 1$

B - Baryon Number

L - Lepton Number

S - Spin

These terms are forbidden in the SM

# R-parity Conservation

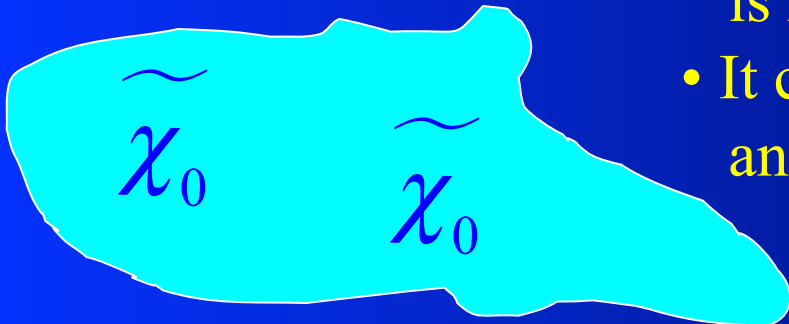
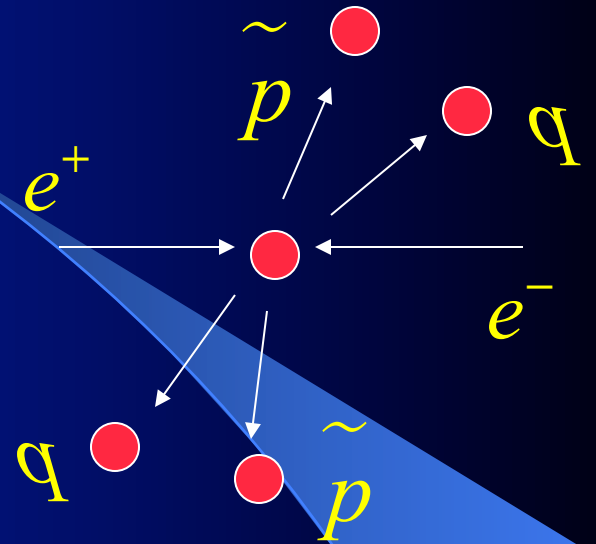
The consequences:

- The superpartners are created in pairs
- The lightest superparticle is stable



Physical output:

- The lightest superparticle (LSP) should be neutral - the best candidate is neutralino (photino or higgsino)
- It can survive from the Big Bang and form the Dark matter in the Universe



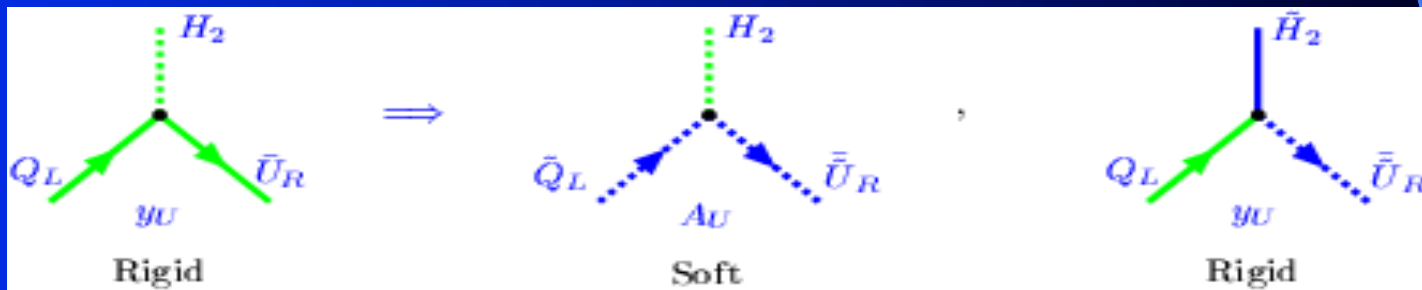
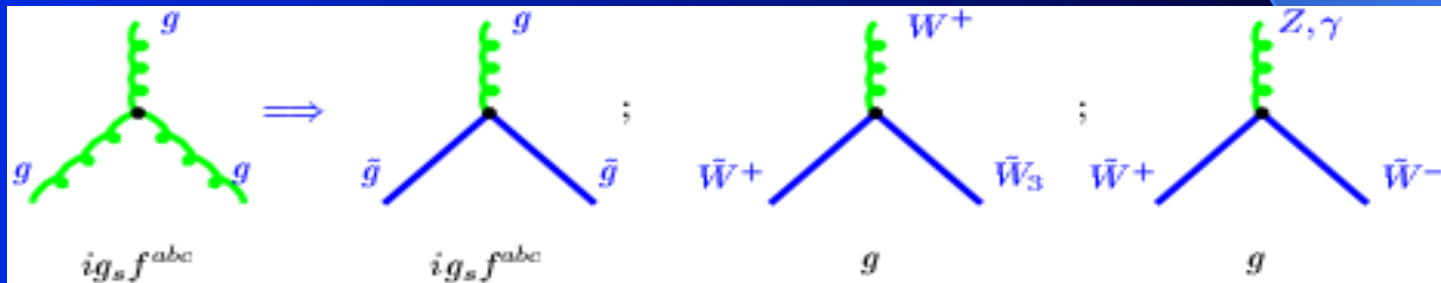
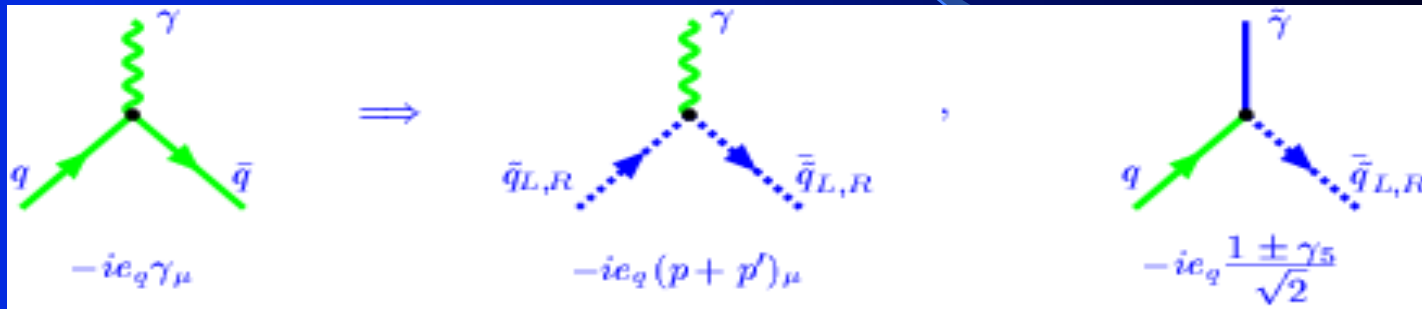
# Interactions in the MSSM

SM



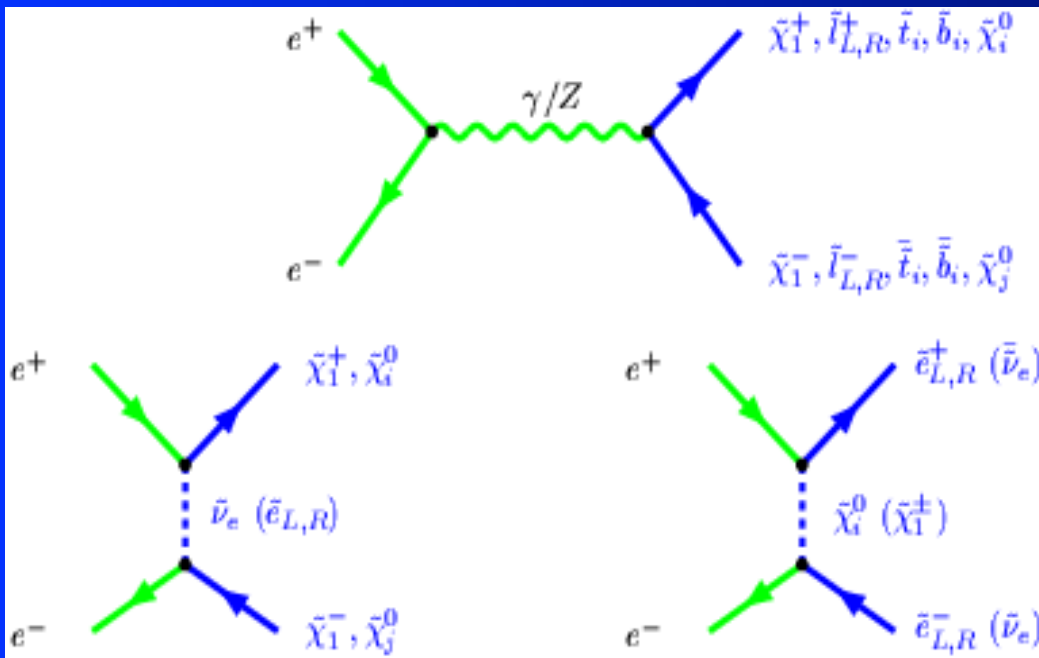
MSSM

SUSY QCD



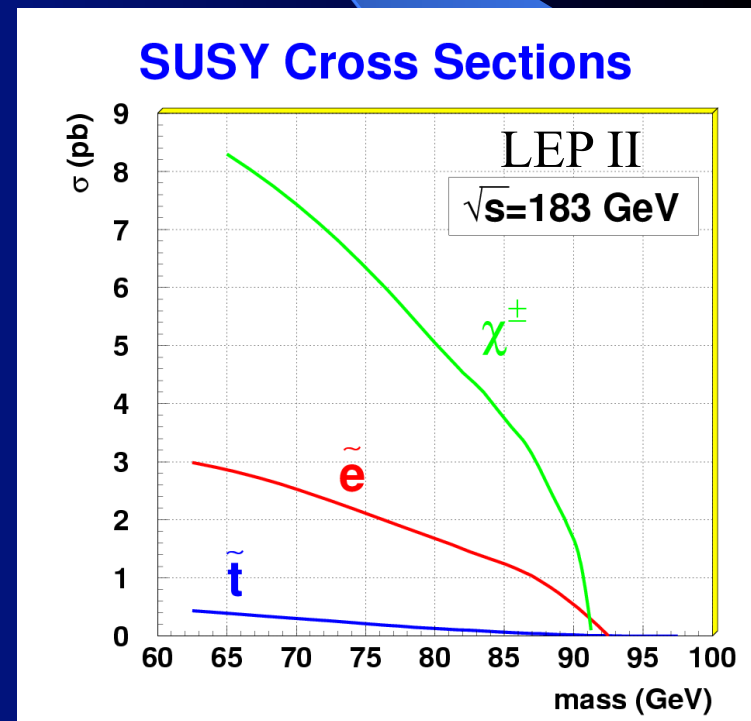


# Creation of Superpartners at $e^+e^-$ colliders



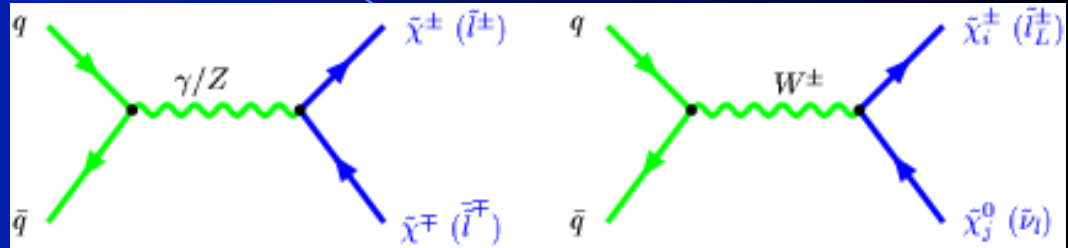
$$m_{\text{sparticle}}^{\text{max}} \leq \frac{\sqrt{s}}{2}$$

Experimental signature:  
missing energy and transverse momentum



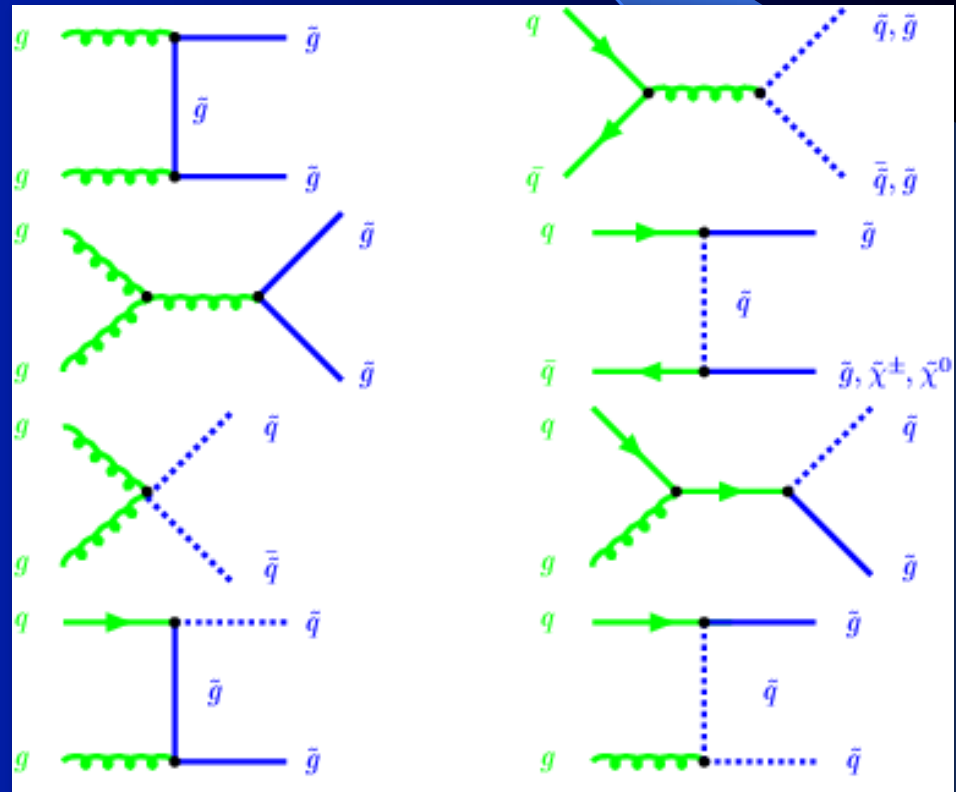
# SUSY Production at Hadron Colliders

Annihilation channel



Gluon fusion, qq scattering and qg scattering channels

No new data so far due to insufficient luminosity at the Tevatron



# Decay of Superpartners

squarks

$$\tilde{q}_{L,R} \rightarrow q + \tilde{\chi}_i^0$$

$$\tilde{q}_L \rightarrow q' + \tilde{\chi}_i^\pm$$

$$\tilde{q}_{L,R} \rightarrow q + g$$

sleptons

$$\tilde{l} \rightarrow l + \tilde{\chi}_i^0$$

$$\tilde{l}_L \rightarrow \nu_l + \tilde{\chi}_i^\pm$$

chargino

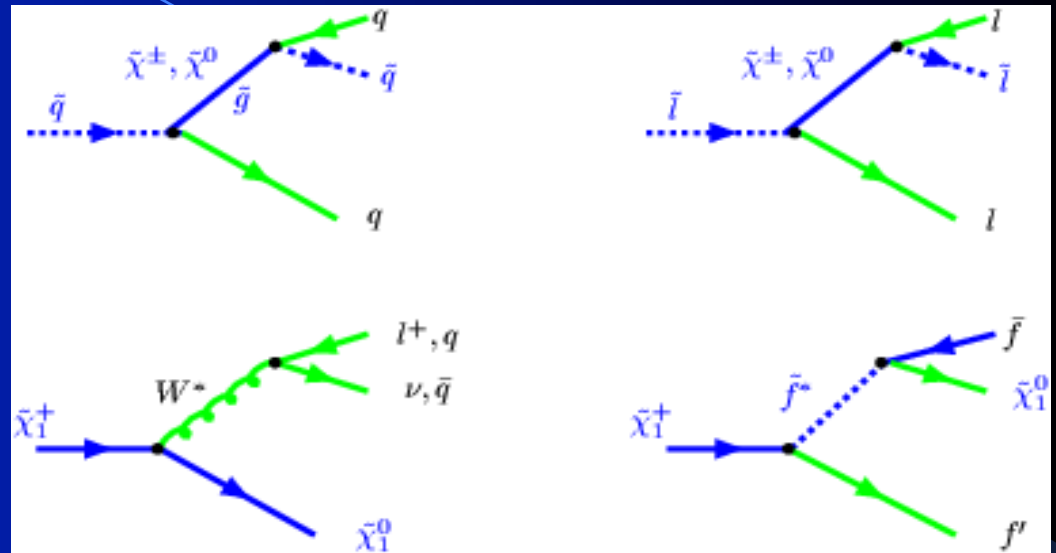
$$\tilde{\chi}_i^\pm \rightarrow e + \nu_e + \tilde{\chi}_i^0$$

$$\tilde{\chi}_i^\pm \rightarrow q + \bar{q}' + \tilde{\chi}_i^0$$

gluino

$$\tilde{g} \rightarrow q + \bar{q} + \tilde{\gamma}$$

$$\tilde{g} \rightarrow g + \tilde{\gamma}$$



neutralino

$$\tilde{\chi}_i^0 \rightarrow \tilde{\chi}_1^0 + l^+ + l^-$$

$$\tilde{\chi}_i^0 \rightarrow \tilde{\chi}_1^0 + q + \bar{q}'$$

$$\tilde{\chi}_i^0 \rightarrow \tilde{\chi}_1^\pm + l^\pm + \nu_l$$

$$\tilde{\chi}_i^0 \rightarrow \tilde{\chi}_1^0 + \nu_l + \bar{\nu}_l$$

Final states

$$l^+ l^- + \cancel{E}_T$$

$$2 \text{ jets} + \cancel{E}_T$$

$$\gamma + \cancel{E}_T$$

$$\cancel{E}_T$$

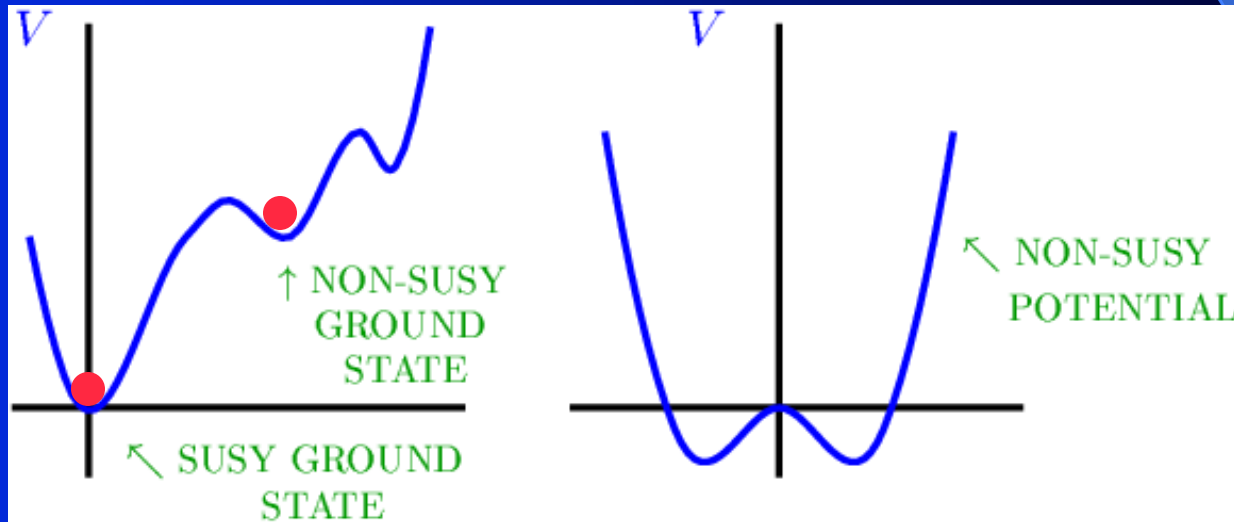
# Spontaneous Breaking of SUSY

Energy  $E = \langle 0 | H | 0 \rangle$

$$\{Q_\alpha^i, \bar{Q}_\beta^j\} = 2\delta^{ij} (\sigma^\mu)_{\alpha\beta} P_\mu$$

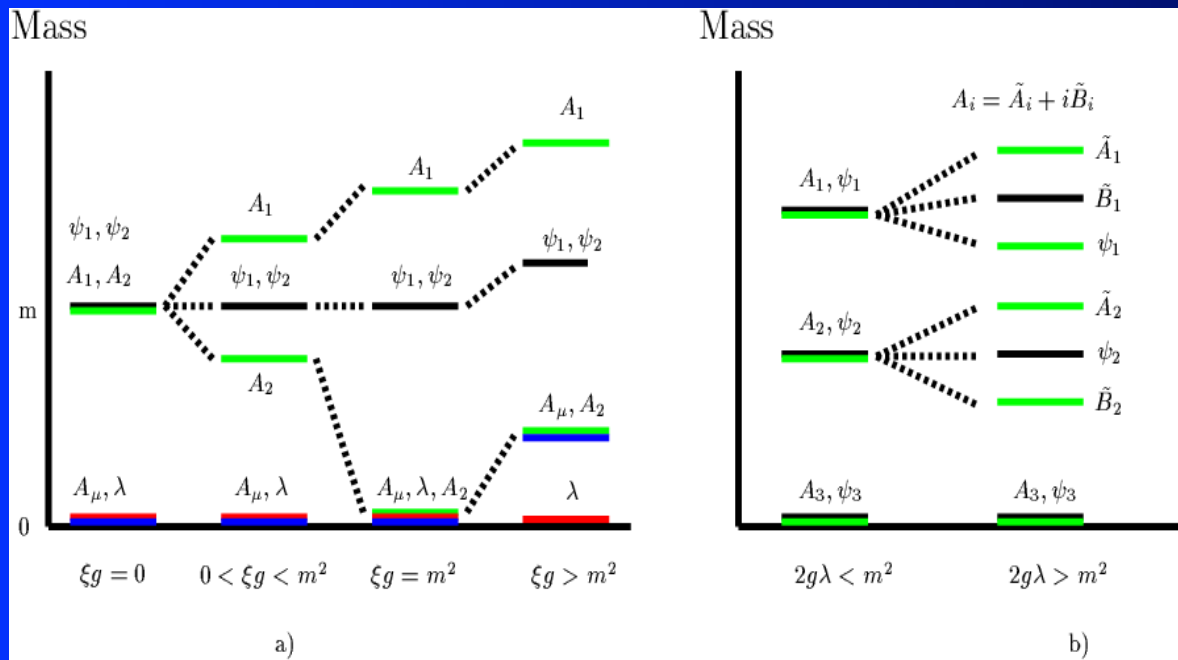
$$E = \frac{1}{4} \sum_{\alpha=1,2} \langle 0 | \{Q_\alpha^i, \bar{Q}_\alpha^j\} | 0 \rangle = \frac{1}{4} \sum_{\alpha} |Q_\alpha | 0 \rangle|^2 \geq 0$$

$$E = \langle 0 | H | 0 \rangle \neq 0 \quad \text{if and only if} \quad Q_\alpha | 0 \rangle \neq 0$$



# Mechanism of SUSY Breaking

- Fayet-Iliopoulos (D-term) mechanism (in Abelian theory)  $\Delta L = \xi V |_{\theta\theta\bar{\theta}\bar{\theta}} = \xi \int d^4\theta V = \xi D \neq 0$
- O'Raifeartaigh (F-term) mechanism  $W(\Phi) = \lambda\Phi_3 + m\Phi_1\Phi_2 + g\Phi_3\Phi_1^2$



D-term

F-term

$$F_1^* = mA_2 + 2gA_1A_2$$

$$F_2^* = mA_1$$

$$F_3^* = \lambda + gA_1^2$$

$$\Rightarrow \langle F_i \rangle \neq 0$$

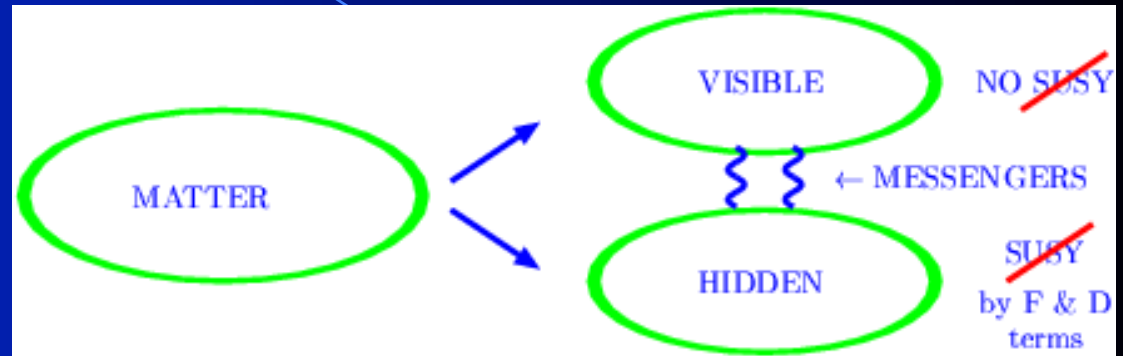
$$\sum_{\text{bosons}} m_i^2 = \sum_{\text{fermions}} m_i^2$$

# Soft SUSY Breaking

Hidden sector scenario:

four scenarios:

1. Gravity mediation
2. Gauge mediation
3. Anomaly mediation
4. Gaugino mediation



SUGRA S-dilaton, T-moduli  $\langle F_T \rangle \neq 0, \langle F_S \rangle \neq 0$

$$M_{SUSY} \sim \frac{\langle F_T \rangle}{M_{PL}} + \frac{\langle F_S \rangle}{M_{PL}} \sim m_{3/2} \leftarrow \text{gravitino mass} \sim 1 \text{ TeV}$$

$$L_{soft} = -\sum_i m_i^2 |A_i|^2 - \sum_i M_i (\lambda_i \lambda_i + \bar{\lambda}_i \bar{\lambda}_i) - BW^{(2)}(A) - AW^{(3)}(A)$$

$$m_i^2 \sim B \sim m_{3/2}^2, M_i \sim A \sim m_{3/2}$$



# Soft SUSY Breaking Cont'd

## Gauge mediation

Scalar singlet S

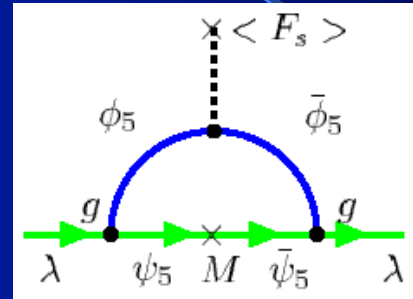
$$\langle S \rangle = M \quad \langle F_S \rangle \neq 0$$

Messenger  $\Phi \quad W \sim S\Phi^+\Phi$

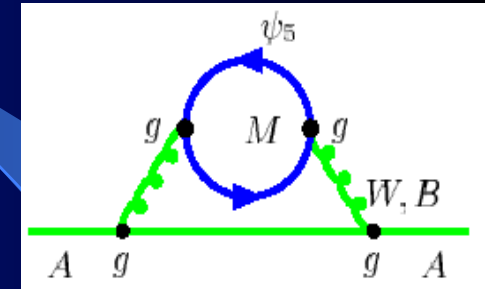
$$m_{\tilde{G}} \sim \frac{\langle F_S \rangle}{M_{PL}} \frac{M}{M_{PL}} \sim 10^{-14} \frac{M}{[GeV]}$$

gravitino mass

- LSP=gravitino



gaugino



squark

$$M_i \sim c_i N \frac{\alpha_i \langle F_S \rangle}{4\pi M} \quad m_i^2 \sim \left( \frac{\langle F_S \rangle}{M_{PL}} \right)^2 N \left( \frac{\alpha_i}{4\pi} \right)^2$$

## Anomaly mediation

Results from conformal anomaly =  $\beta$  function

$$M_i \sim b_i \frac{\alpha_i(\Lambda)}{4\pi} \frac{\langle F_{T,S} \rangle}{M_{PL}} \sim b_i \alpha_i m_{3/2}$$

$$m_i^2 \sim b_i^2 \alpha_i^2 m_{3/2}^2$$

- $M_1 : M_2 : M_3 = b_1 : b_2 : b_3$

- LSP=slepton

# Soft SUSY Breaking Cont'd

## Gaugino mediation

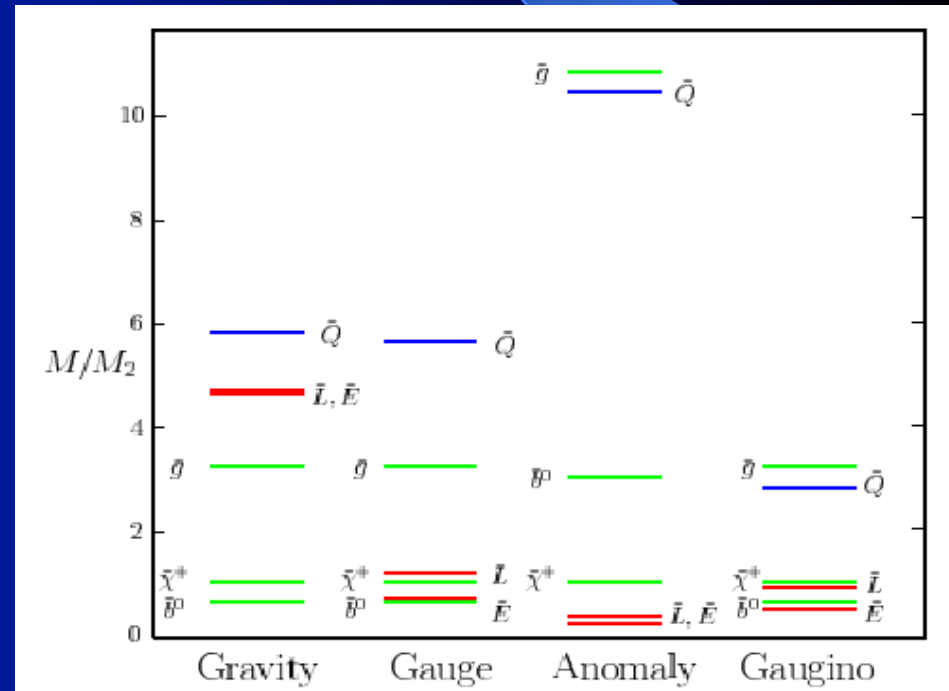
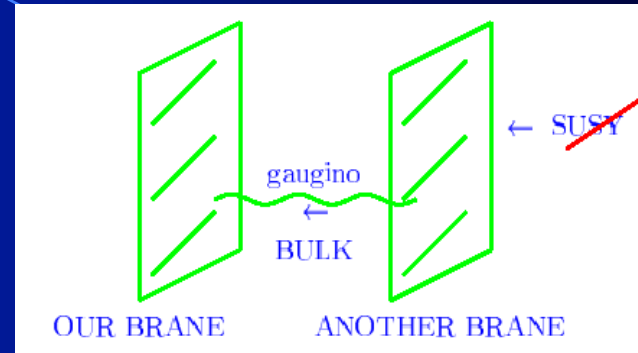
All scenarios produce soft SUSY breaking terms

Soft = operators of dimension  $\leq 4$

## Net result of SUSY breaking

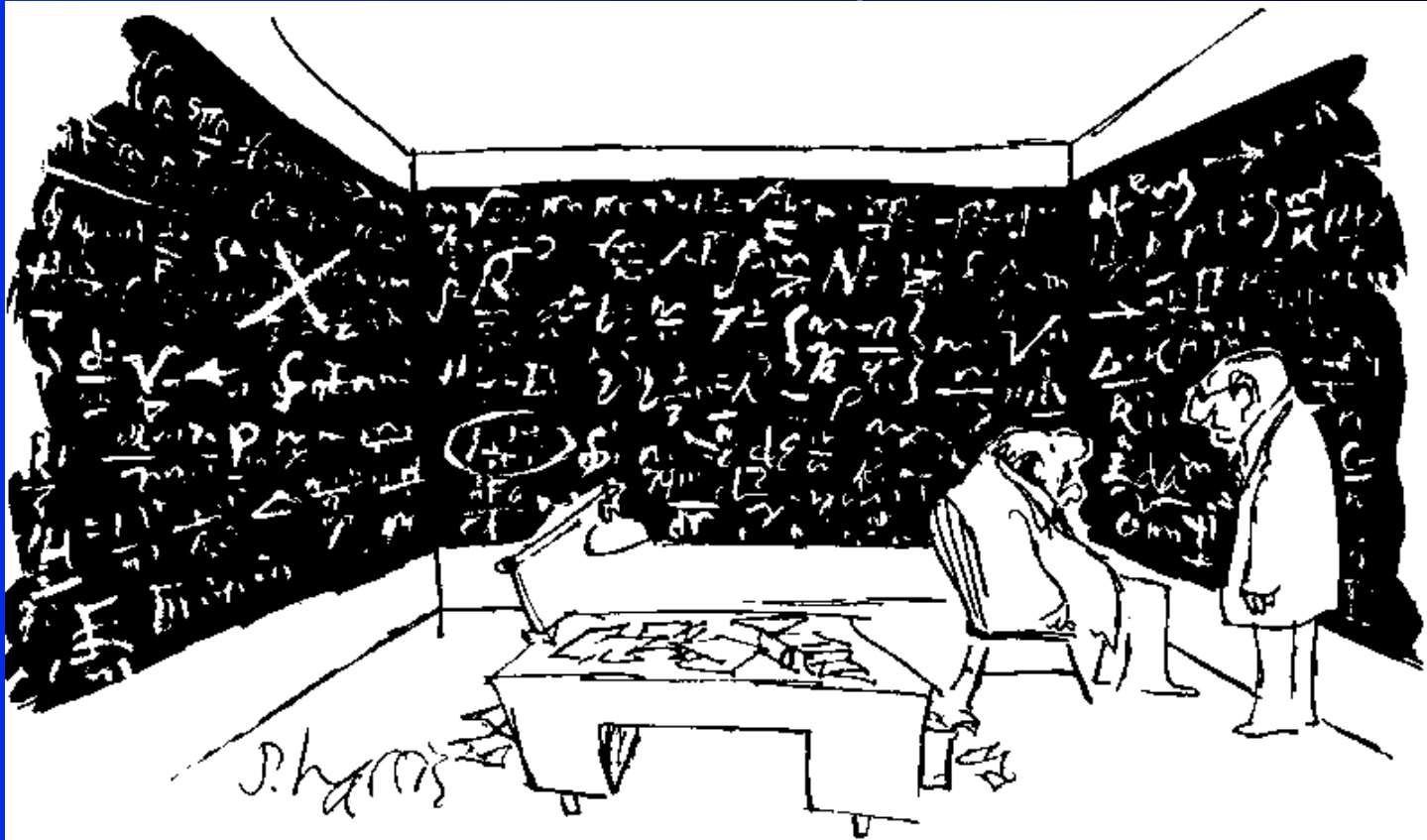
$$\begin{aligned}
 -L_{Soft} = & \sum_i m_{0i}^2 |A_i|^2 + \sum_\alpha M_\alpha \tilde{\lambda}_\alpha \tilde{\lambda}_\alpha \\
 & + \sum_{ijk} A_{ijk} A_i A_j A_k + \sum_{ij} B_{ij} A_i A_j
 \end{aligned}$$

↑ scalar fields
↑ gauginos



SUSY spectra for various mediation mechanisms

# We like elegant solutions



"Whatever happened to *elegant* solutions?"

# Parameter Space of the MSSM

- Three gauge couplings  $\alpha_i, i=1,2,3$
- Three (four) Yukawa matrices  $y_{ab}^k, k = U, D, L, (E)$
- The Higgs mixing parameter  $\mu$
- Soft SUSY breaking terms

SUGRA Universality hypothesis: soft terms are universal and repeat the Yukawa potential

$$-L_{Soft} = A\{y_t Q_L H_2 U_R + y_b Q_L H_1 D_R + y_L L_L H_1 E_R\} + B\mu H_1 H_2 + m_0^2 \sum_i |\varphi_i|^2 + \frac{1}{2} M_{1/2} \sum_\alpha \widetilde{\lambda}_\alpha \widetilde{\lambda}_\alpha$$

Five universal soft parameters:

$$A, m_0, M_{1/2}, B \leftrightarrow \tan\beta \quad \text{and} \quad \mu$$

versus

$$m \quad \text{and} \quad \lambda$$

in the SM

# Mass Spectrum

$$L_{\text{gaugino-Higgsino}} = -\frac{1}{2} M_3 \bar{\lambda}_a \lambda_a - \frac{1}{2} \bar{\chi} M^{(0)} \chi - (\bar{\psi} M^{(c)} \psi + h.c.)$$

$$\psi = \begin{pmatrix} \tilde{W}^+ \\ \tilde{H}^+ \end{pmatrix}$$

$$M^{(c)} = \begin{pmatrix} M_2 & \sqrt{2} M_W \sin \beta \\ \sqrt{2} M_W \cos \beta & \mu \end{pmatrix}$$



$$\begin{pmatrix} \chi_1^+ \\ \chi_2^+ \end{pmatrix}$$

$$\chi_1^0, \chi_2^0, \chi_3^0, \chi_4^0$$

$$\chi = \begin{pmatrix} \tilde{B}^0 \\ \tilde{W}^3 \\ \tilde{H}_1^0 \\ \tilde{H}_2^0 \end{pmatrix} M^{(0)} = \begin{pmatrix} M_1 & 0 & -M_Z \cos \beta \sin W & M_Z \sin \beta \sin W \\ 0 & M_2 & M_Z \cos \beta \cos W & -M_Z \sin \beta \cos W \\ -M_Z \cos \beta \sin W & M_Z \cos \beta \cos W & 0 & -\mu \\ M_Z \sin \beta \sin W & -M_Z \sin \beta \cos W & -\mu & 0 \end{pmatrix}$$

# Mass Spectrum

$$\tilde{m}_t^2 = \begin{pmatrix} \tilde{m}_{tL}^2 & m_t(A_t - \mu \cot \beta) \\ m_t(A_t - \mu \cot \beta) & \tilde{m}_{tR}^2 \end{pmatrix}$$

$$\tilde{m}_b^2 = \begin{pmatrix} \tilde{m}_{bL}^2 & m_b(A_b - \mu \tan \beta) \\ m_b(A_b - \mu \tan \beta) & \tilde{m}_{bR}^2 \end{pmatrix}$$



$$\begin{pmatrix} \tilde{t}_1 \\ \tilde{t}_2 \end{pmatrix}$$



$$\begin{pmatrix} \tilde{b}_1 \\ \tilde{b}_2 \end{pmatrix}$$

$$\tilde{m}_{tL}^2 = \tilde{m}_Q^2 + m_t^2 + \frac{1}{6}(4M_W^2 - M_Z^2)\cos 2\beta,$$

$$\tilde{m}_{tR}^2 = \tilde{m}_U^2 + m_t^2 - \frac{2}{3}(M_W^2 - M_Z^2)\cos 2\beta,$$

$$\tilde{m}_{bL}^2 = \tilde{m}_Q^2 + m_b^2 - \frac{1}{6}(2M_W^2 + M_Z^2)\cos 2\beta,$$

$$\tilde{m}_{bR}^2 = \tilde{m}_D^2 + m_b^2 + \frac{1}{3}(M_W^2 - M_Z^2)\cos 2\beta,$$

$$\tilde{m}_{\tau L}^2 = \tilde{m}_L^2 + m_\tau^2 - \frac{1}{2}(2M_W^2 - M_Z^2)\cos 2\beta,$$

$$\tilde{m}_{\tau R}^2 = \tilde{m}_E^2 + m_\tau^2 + (M_W^2 - M_Z^2)\cos 2\beta.$$

$$\tilde{m}_\tau^2 = \begin{pmatrix} \tilde{m}_{\tau L}^2 & m_\tau(A_\tau - \mu \tan \beta) \\ m_\tau(A_\tau - \mu \tan \beta) & \tilde{m}_{\tau R}^2 \end{pmatrix}$$



$$\begin{pmatrix} \tilde{\tau}_1 \\ \tilde{\tau}_2 \end{pmatrix}$$



# SUSY Higgs Bosons

SM

$$4=2+2=3+1$$

$$H = \begin{pmatrix} H^0 \\ H^- \end{pmatrix} = \begin{pmatrix} v + \frac{S + iP}{\sqrt{2}} \\ H^- \end{pmatrix} = \exp\left(i\frac{\vec{\xi}\vec{\sigma}}{2}\right) \begin{pmatrix} v + \frac{S}{\sqrt{2}} \\ 0 \end{pmatrix}$$

$$H \rightarrow H' = \exp\left(i\frac{\vec{\alpha}\vec{\sigma}}{2}\right)H \xrightarrow{(\vec{\alpha}=-\vec{\xi})} H' = \begin{pmatrix} v + \frac{S}{\sqrt{2}} \\ 0 \end{pmatrix}$$

MSSM

$$8=4+4=3+5$$

$$H_1 = \begin{pmatrix} H_1^0 \\ H_1^- \end{pmatrix} = \begin{pmatrix} v_1 + \frac{S_1 + iP_1}{\sqrt{2}} \\ H_1^- \end{pmatrix}, \quad H_2 = \begin{pmatrix} H_2^+ \\ H_2^0 \end{pmatrix} = \begin{pmatrix} H_2^+ \\ v_2 + \frac{S_2 + iP_2}{\sqrt{2}} \end{pmatrix}$$

$$v_1^2 + v_2^2 = v^2, \quad v_2/v_1 \equiv \tan\beta$$

$$G^0 = -\cos\beta P_1 + \sin\beta P_2$$

Goldstone boson  $\rightarrow Z_0$

$$A = \sin\beta P_1 + \cos\beta P_2$$

Neutral CP = -1 Higgs  $\leftarrow$

$$G^+ = -\cos\beta (H_1^-)^* + \sin\beta H_2^+$$

Goldstone boson  $\rightarrow W^+$

$$H^+ = \sin\beta (H_1^-)^* + \cos\beta H_2^+$$

Charged Higgs  $\leftarrow$

$$h = -\sin\alpha S_1 + \cos\alpha S_2$$

SM Higgs boson CP = 1  $\leftarrow$

$$H = \cos\alpha S_1 + \sin\alpha S_2$$

Extra heavy Higgs boson  $\leftarrow$

$$\tan 2\alpha = \tan 2\beta \frac{m_A^2 + m_Z^2}{m_A^2 - m_Z^2}$$

# The Higgs Potential

$$V_{tree}(H_1, H_2) = m_1^2 |H_1|^2 + m_2^2 |H_2|^2 - m_3^2 (H_1 H_2 + h.c.) \\ + \frac{g^2 + g'^2}{8} (|H_1|^2 - |H_2|^2)^2 + \frac{g^2}{2} |H_1^+ H_2|^2$$

At the GUT scale:  $m_1^2 = m_2^2 = \mu_0^2 + m_0^2$ ,  $m_3^2 = -B\mu_0$

Minimization

$$\frac{1}{2} \frac{\delta V}{\delta H_1} = m_1^2 v_1 - m_3^2 v_2 + \frac{g^2 + g'^2}{4} (v_1^2 - v_2^2) v_1 = 0,$$

$$\frac{1}{2} \frac{\delta V}{\delta H_2} = m_2^2 v_2 - m_3^2 v_1 - \frac{g^2 + g'^2}{4} (v_1^2 - v_2^2) v_2 = 0.$$

$$\langle H_1 \rangle \equiv v_1 = v \cos \beta, \quad \langle H_2 \rangle \equiv v_2 = v \sin \beta,$$

Solution

$$v^2 = \frac{4(m_1^2 - m_2^2 \tan^2 \beta)}{(g^2 + g'^2)(\tan^2 \beta - 1)},$$

$$\sin 2\beta = \frac{2m_3^2}{m_1^2 + m_2^2}$$

At the GUT scale

$$v^2 = -\frac{4}{g^2 + g'^2} m^2 < 0$$

No SSB in SUSY theory !

# Renormalization Group Eqns

$$\tilde{\alpha}_i \equiv \frac{g_i^2}{16\pi^2} = \frac{\alpha_i}{4\pi}, \quad Y_k \equiv \frac{y_k^2}{16\pi^2}, \quad t = \log(M_{GUT}^2 / Q^2)$$

$$i = 1, 2, 3 \quad k = U, D, L$$

*The couplings*

$$\dot{\tilde{\alpha}}_i = -b_i \tilde{\alpha}_i^2, \quad b_i^{MSSM} = \left(\frac{33}{5}, 1, -3\right)$$

$$\dot{Y}_U = Y_U \left(\frac{16}{3} \tilde{\alpha}_3 + 3\tilde{\alpha}_2 + \frac{13}{15} \tilde{\alpha}_1 - 6Y_U - Y_D\right),$$

$$\dot{Y}_D = Y_D \left(\frac{16}{3} \tilde{\alpha}_3 + 3\tilde{\alpha}_2 + \frac{7}{15} \tilde{\alpha}_1 - Y_U - 6Y_D - Y_L\right),$$

$$\dot{Y}_L = Y_L \left(3\tilde{\alpha}_2 + \frac{9}{5} \tilde{\alpha}_1 - 3Y_D - 4Y_L\right),$$

$$\dot{M}_i = b_i \tilde{\alpha}_i M_i,$$

$$\dot{A}_U = -\left(\frac{16}{3} \tilde{\alpha}_3 M_3 + 3\tilde{\alpha}_2 M_2 + \frac{13}{15} \tilde{\alpha}_1 M_1\right) - 6Y_U A_U - Y_D A_D,$$

$$\dot{A}_D = -\left(\frac{16}{3} \tilde{\alpha}_3 M_3 + 3\tilde{\alpha}_2 M_2 + \frac{7}{15} \tilde{\alpha}_1 M_1\right) - Y_U A_U - 6Y_D A_D - Y_L A_L,$$

$$\dot{A}_L = -\left(3\tilde{\alpha}_2 M_2 + \frac{9}{5} \tilde{\alpha}_1 M_1\right) - 3Y_D A_D - 4Y_L A_L,$$

$$\dot{B} = -3\left(\tilde{\alpha}_2 M_2 + \frac{1}{5} \tilde{\alpha}_1 M_1\right) - 3Y_U A_U - 3Y_D A_D - Y_L A_L,$$

$$\dot{\mu} = -\mu^2 \left(3\tilde{\alpha}_2 + \frac{3}{5} \tilde{\alpha}_1 - 3Y_U - 3Y_D - Y_L\right)$$

*Soft Terms*

# RG Eqns for the Soft Masses

$$\dot{\tilde{m}}_Q^2 = -\left[\frac{16}{3}\tilde{\alpha}_3 M_3^2 + 3\tilde{\alpha}_2 M_2^2 + \frac{1}{15}\tilde{\alpha}_1 M_1^2 - Y_t(\Sigma_t + A_t^2) - Y_b(\Sigma_b + A_b^2)\right]$$

$$\dot{\tilde{m}}_U^2 = -\left[\frac{16}{3}\tilde{\alpha}_3 M_3^2 + \frac{16}{15}\tilde{\alpha}_1 M_1^2 - 2Y_t(\Sigma_t + A_t^2)\right]$$

$$\dot{\tilde{m}}_D^2 = -\left[\frac{16}{3}\tilde{\alpha}_3 M_3^2 + \frac{4}{15}\tilde{\alpha}_1 M_1^2 - 2Y_b(\Sigma_b + A_b^2)\right]$$

$$\dot{\tilde{m}}_L^2 = -\left[3\tilde{\alpha}_2 M_2^2 + \frac{3}{5}\tilde{\alpha}_1 M_1^2 - Y_\tau(\Sigma_\tau + A_\tau^2)\right]$$

$$\dot{\tilde{m}}_E^2 = -\left[\frac{12}{5}\tilde{\alpha}_1 M_1^2 - 2Y_\tau(\Sigma_\tau + A_\tau^2)\right]$$

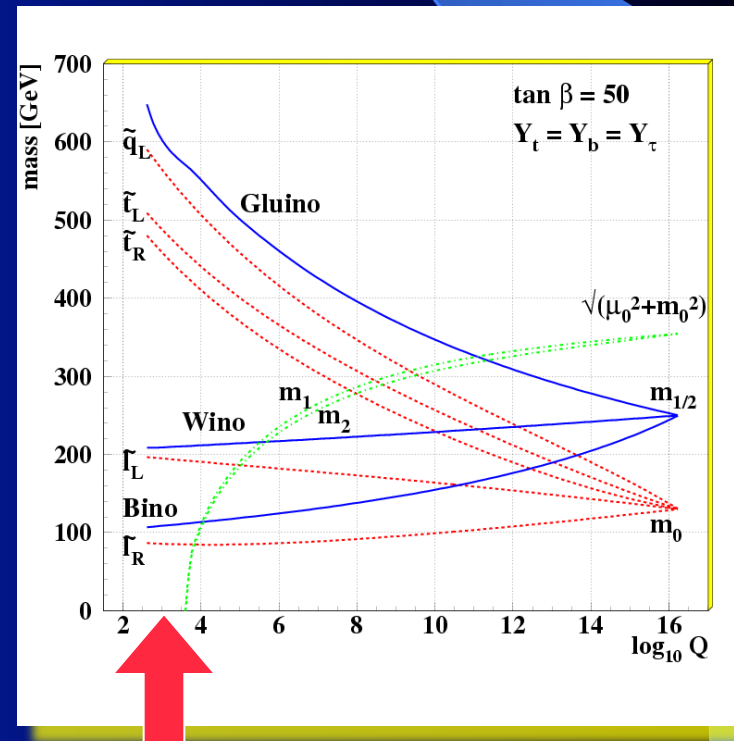
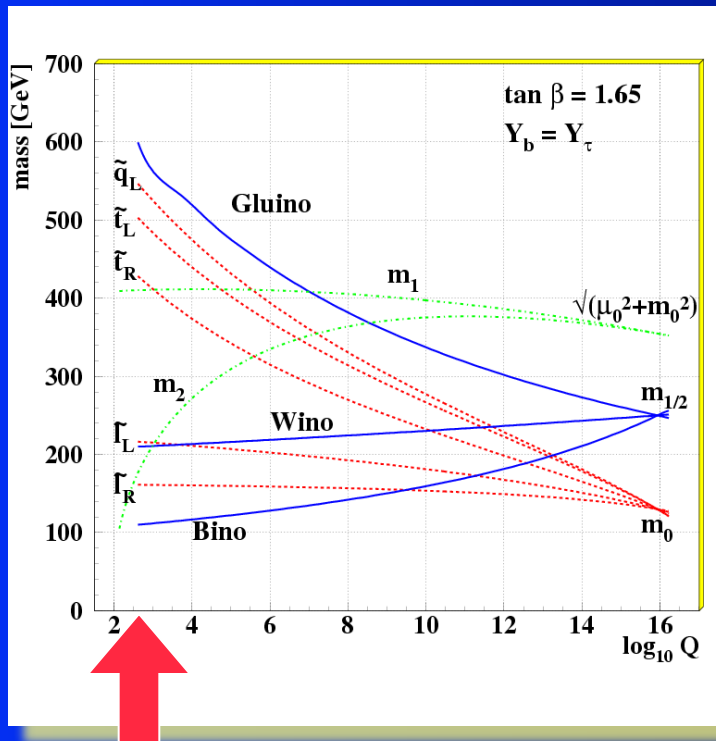
$$\dot{\tilde{m}}_{H_1}^2 = -\left[3\tilde{\alpha}_2 M_2^2 + \frac{3}{5}\tilde{\alpha}_1 M_1^2 - 3Y_b(\Sigma_b + A_b^2) - Y_\tau(\Sigma_\tau + A_\tau^2)\right]$$

$$\dot{\tilde{m}}_{H_2}^2 = -\left[3\tilde{\alpha}_2 M_2^2 + \frac{3}{5}\tilde{\alpha}_1 M_1^2 - 3Y_t(\Sigma_t + A_t^2)\right]$$

$$\Sigma_t = m_Q^2 + m_U^2 + m_{H_2}^2, \Sigma_b = m_Q^2 + m_D^2 + m_{H_1}^2, \Sigma_\tau = m_L^2 + m_E^2 + m_{H_1}^2$$

# Radiative EW Symmetry Breaking

Due to RG controlled running of the mass terms from the Higgs potential they may change sign and trigger the appearance of non-trivial minimum leading to spontaneous breaking of EW symmetry - this is called Radiative EWSB



# The Higgs Bosons Masses

CP-odd neutral Higgs A  $m_A^2 = m_1^2 + m_2^2$   $M_W^2 = \frac{g^2}{2} v^2$

CP-even charged Higgses  $H_{\pm}$   $m_{H^{\pm}}^2 = m_A^2 + M_W^2$   $M_Z^2 = \frac{g^2 + g'^2}{2} v^2$

CP-even neutral Higgses h,H

$$m_{h,H}^2 = \frac{1}{2} [m_A^2 + M_Z^2 \pm \sqrt{(m_A^2 + M_Z^2)^2 - 4m_A^2 M_Z^2 \cos^2 2\beta}]$$

$m_h \approx M_Z |\cos 2\beta| < M_Z ! \Rightarrow$  Radiative corrections

$$m_h^2 \approx M_Z^2 \cos^2 2\beta + \frac{3g^2 m_t^4}{16\pi^2 M_W^2} \log \frac{m_{t_1} m_{t_2}}{m_t^4} + 2 \text{ loops}$$

$\sim 2 \sim 2$



# The Lightest Superparticle

property

signature

- Gravity mediation LSP =  $\tilde{\chi}_1^0$  stable jets/leptons +  $\cancel{E}_T$
- Gauge mediation LSP =  $\tilde{G}$  stable  $\cancel{E}_T$
- NLSP =  $\begin{cases} \tilde{\chi}_1^0 & \tilde{\chi}_1^0 \rightarrow \gamma \tilde{G}, h \tilde{G}, Z \tilde{G} & \text{photons/jets} + \cancel{E}_T \\ \tilde{l}_R & \tilde{l}_R \rightarrow \tau \tilde{G} & \text{lepton} + \cancel{E}_T \end{cases}$
- Anomaly mediation LSP =  $\begin{cases} \tilde{\chi}_1^0 & \text{stable} \\ \tilde{\nu}_L & \text{stable} \end{cases}$  lepton +  $\cancel{E}_T$
- R-parity violation LSP is unstable  $\rightarrow$  SM particles

$M_{LSP} \geq 40 \text{ GeV}$

Rare decays  
Neutrinoless double  $\beta$  decay



# Constrained MSSM

## Requirements:

- Unification of the gauge couplings
- Radiative EW Symmetry Breaking
- Heavy quark and lepton masses
- Rare decays ( $b \rightarrow s\gamma$ )
- Anomalous magnetic moment of muon
- LSP is neutral
- Amount of the Dark Matter
- Experimental limits from direct search

Allowed region  
in the parameter  
space of the MSSM

$$A_0, m_0, M_{1/2}, \mu, \tan \beta$$

Parameter space:

$$100 \text{ GeV} < m_0, M_{1/2}, \mu < 2 \text{ TeV} \\ -3m_0 < A_0 < 3m_0, 1 < \tan \beta < 70$$

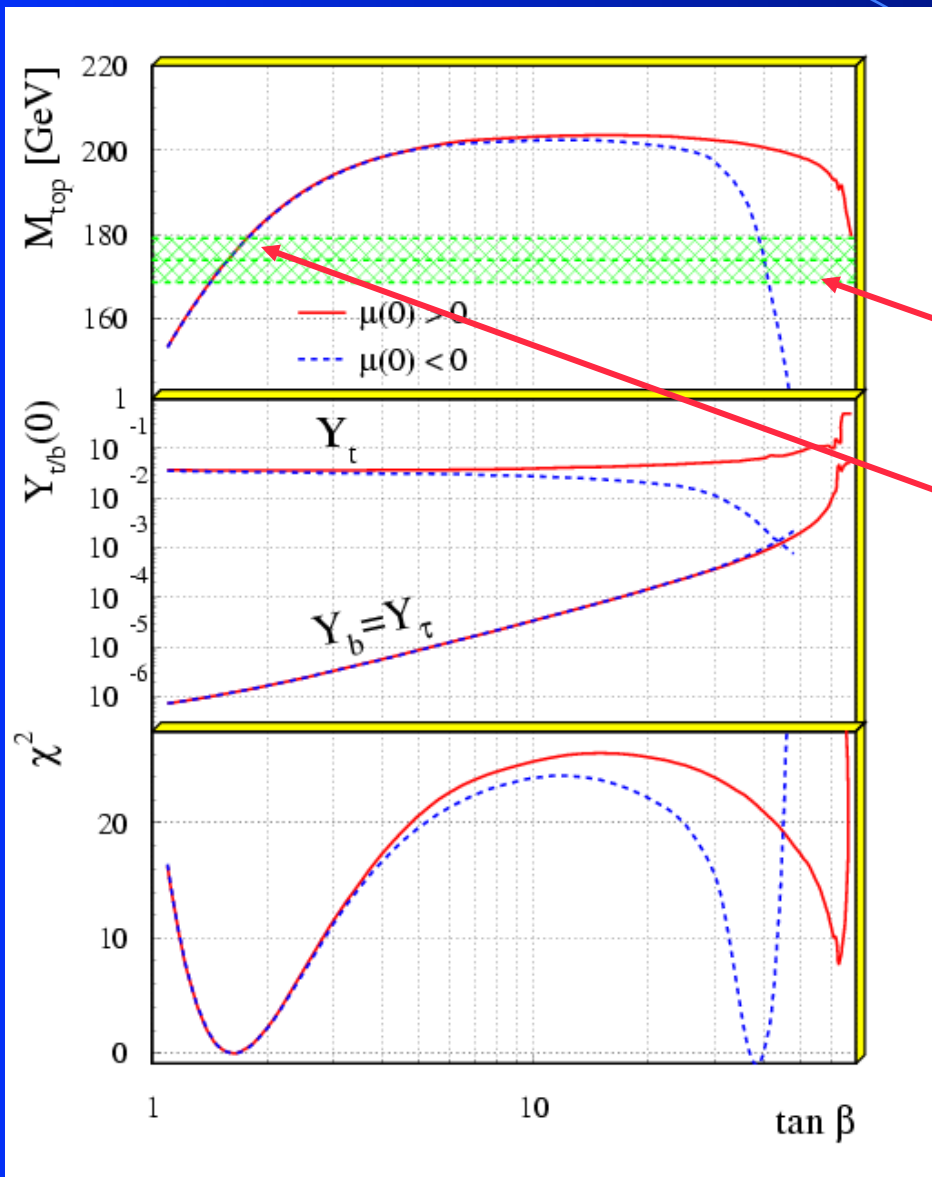
# SUSY Fits

$$\begin{aligned}
 \chi^2 = & \sum_{i=1}^3 \frac{(\alpha_i^{-1}(M_Z) - \alpha_{MSSMi}^{-1}(M_Z))^2}{\sigma_i^2} \\
 & + \frac{(M_Z - 91.18)^2}{\sigma_Z^2} + \frac{(M_t - 174)^2}{\sigma_t^2} \\
 & + \frac{(M_b - 4.94)^2}{\sigma_b^2} + \frac{(M_\tau - 1.7771)^2}{\sigma_\tau^2} \\
 & + \frac{(\text{Br}(b \rightarrow s\gamma) - 3.14 \times 10^{-4})^2}{\sigma^2(b \rightarrow s\gamma)} \\
 & + \frac{(\Omega h^2 - 1)^2}{\sigma_\Omega^2} \quad (\text{for } \Omega h^2 > 1) \\
 & + \frac{(\tilde{M} - \tilde{M}_{\text{exp}})^2}{\sigma_{\tilde{M}}^2} \quad (\text{for } \tilde{M} < \tilde{M}_{\text{exp}}) \\
 & + \frac{(\tilde{m}_{\text{LSP}} - \tilde{m}_\chi)^2}{\sigma_{\text{LSP}}^2} \quad (\text{for } \tilde{m}_{\text{LSP}} \text{ charged})
 \end{aligned}$$

Minimize  $\chi^2$

| Exp. input data                | Fit                       | Parameters                 |
|--------------------------------|---------------------------|----------------------------|
|                                | low $\tan\beta$           | high $\tan\beta$           |
| $\alpha_1, \alpha_2, \alpha_3$ | $M_{GUT}, \alpha_{GUT}$   | $M_{GUT}, \alpha_{GUT}$    |
| $m_t$                          | $Y_t^0, Y_b^0 = Y_\tau^0$ | $Y_t^0 = Y_b^0 = Y_\tau^0$ |
| $m_b$                          | $m_0, m_{1/2}$            | $m_0, m_{1/2}$             |
| $m_\tau$                       | $\tan\beta$               | $\tan\beta$                |
| $M_Z$                          | $\mu$                     | $\mu$                      |
| $b \rightarrow s\gamma$        | $(A_0)$                   | $A_0$                      |
| $\tau_{\text{Universe}}$       |                           |                            |

# Low and High $\tan\beta$ Solutions



Requirements:

- EWSB
- $b\tau$  unification

Low  $\tan\beta$   
solution

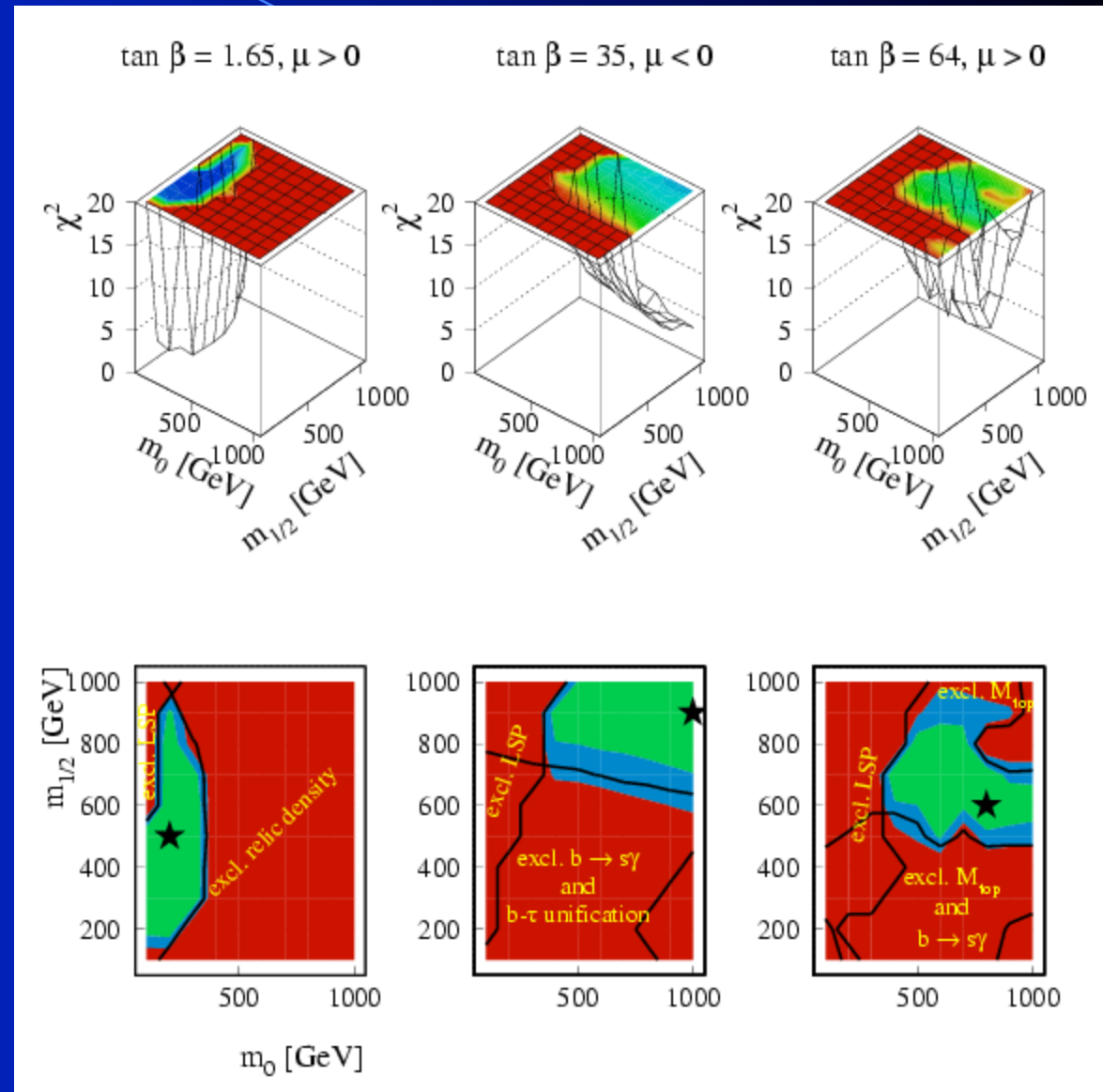
High  $\tan\beta$   
solution

- $b\tau$  unification is the consequence of GUT
- Non working for the light generations

# Allowed Regions in Parameter Space

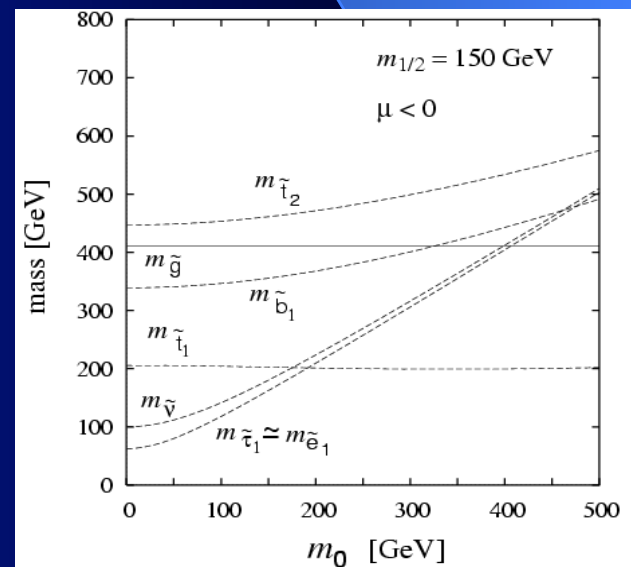
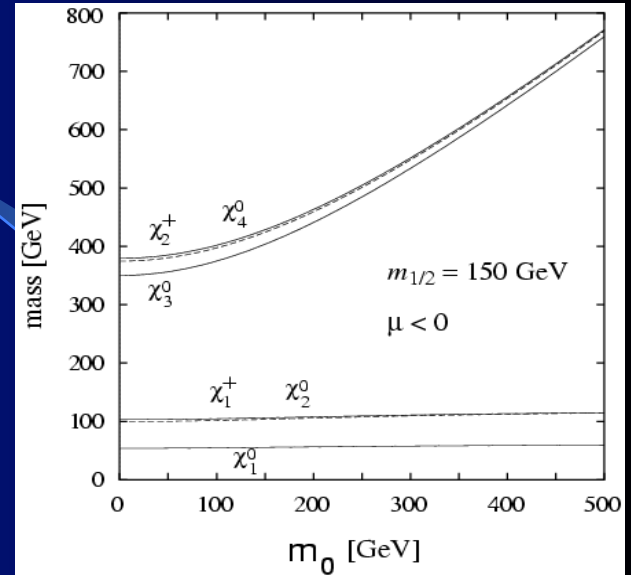
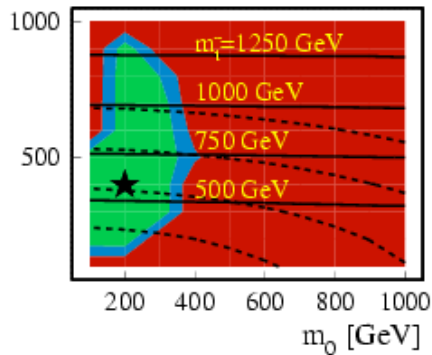
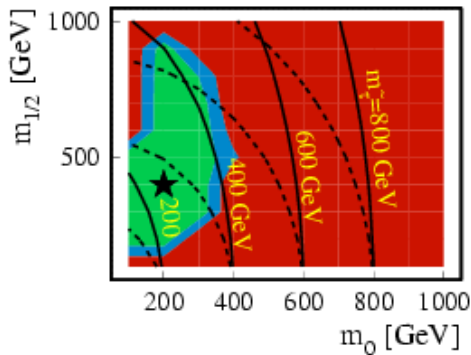
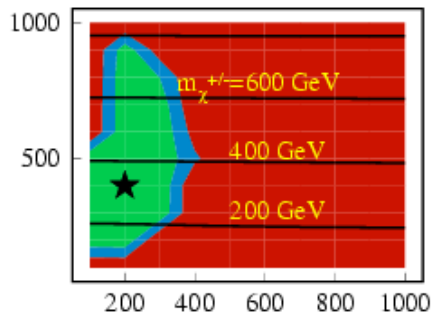
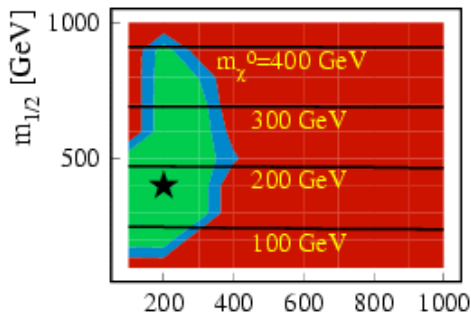
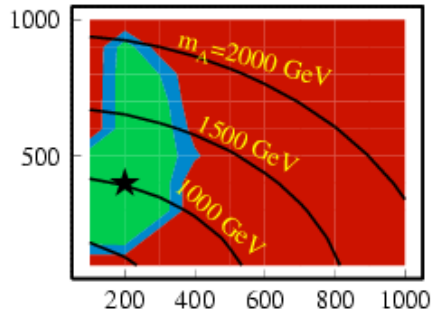
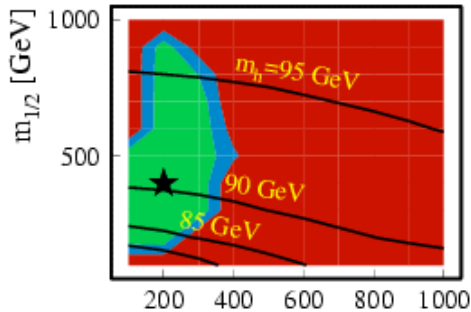
All the requirements are fulfilled simultaneously !

- $\mu$  is defined from the EWSB
  - $A_0 = 0$
- ★ - is the best fit value



# Masses of Superpartners

$\tan \beta = 1.65, \mu > 0$





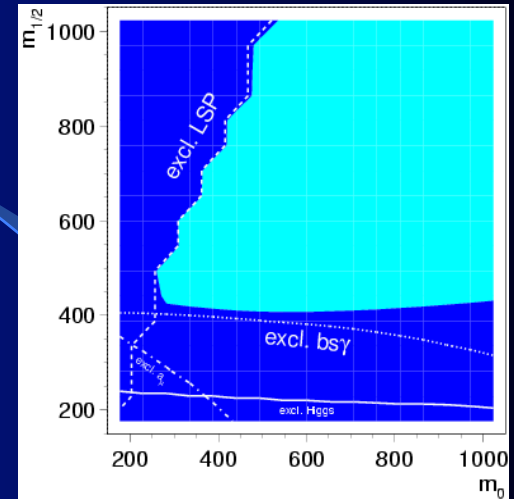
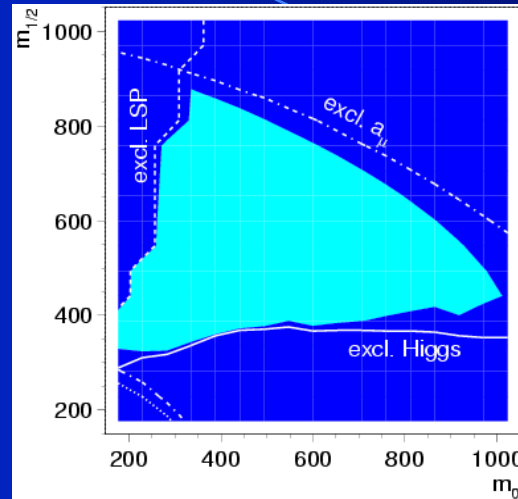
# Allowed regions of parameter space

- $\tan \beta > 4$

From the Higgs searches

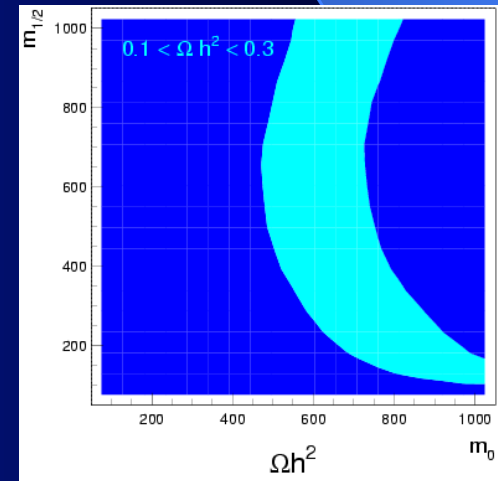
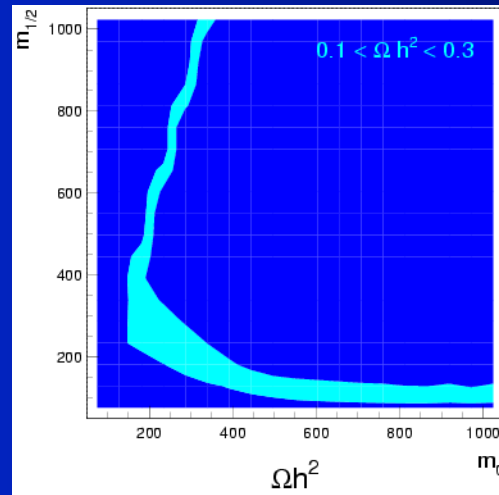
- $\mu > 0$

From  $a_\mu$  measurement



Fit to all constraints

In allowed region one fulfills all the constraints simultaneously and has the suitable amount of the dark matter



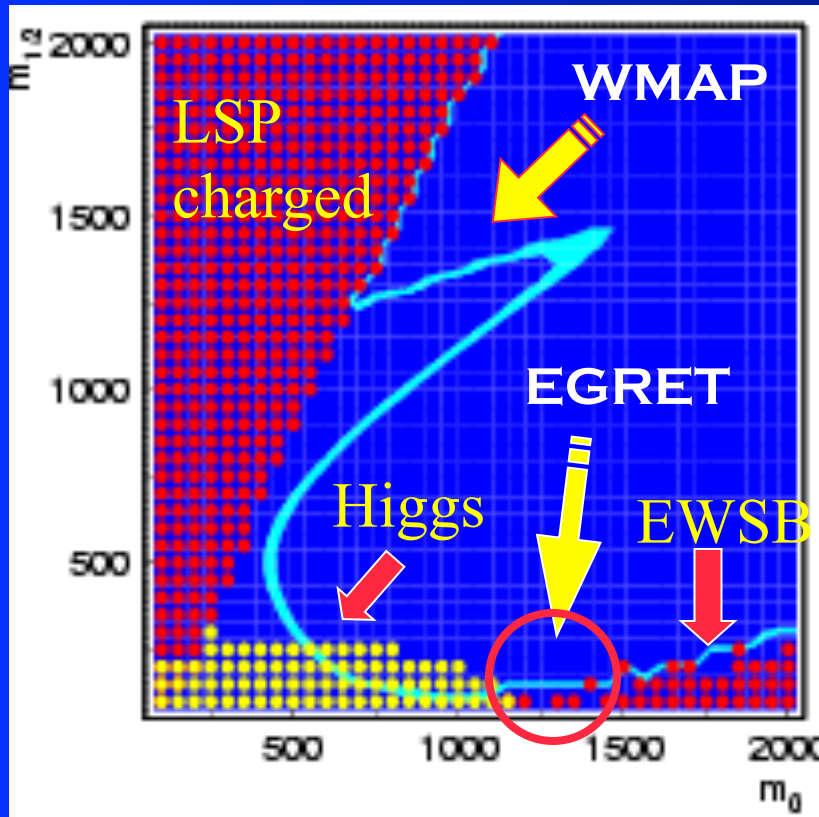
$\tan \beta = 35$

Fit to Dark Matter constraint  $\tan \beta = 50$

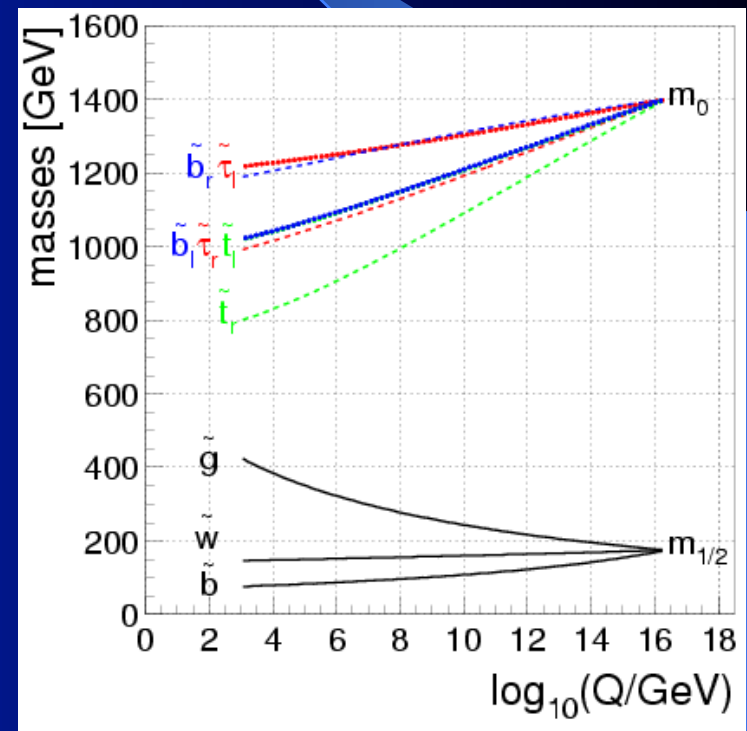
45 50

# Allowed regions after WMAP

Fit to Dark Matter constraint



In allowed region one fulfills all the constraints simultaneously and has the suitable amount of the dark matter



Narrow allowed region enables one to predict the particle spectra and has direct influence on phenomenology and SUSY searches

$$m_\chi : 50 \div 100 \text{ GeV}$$

# Mass Spectrum in CMSSM

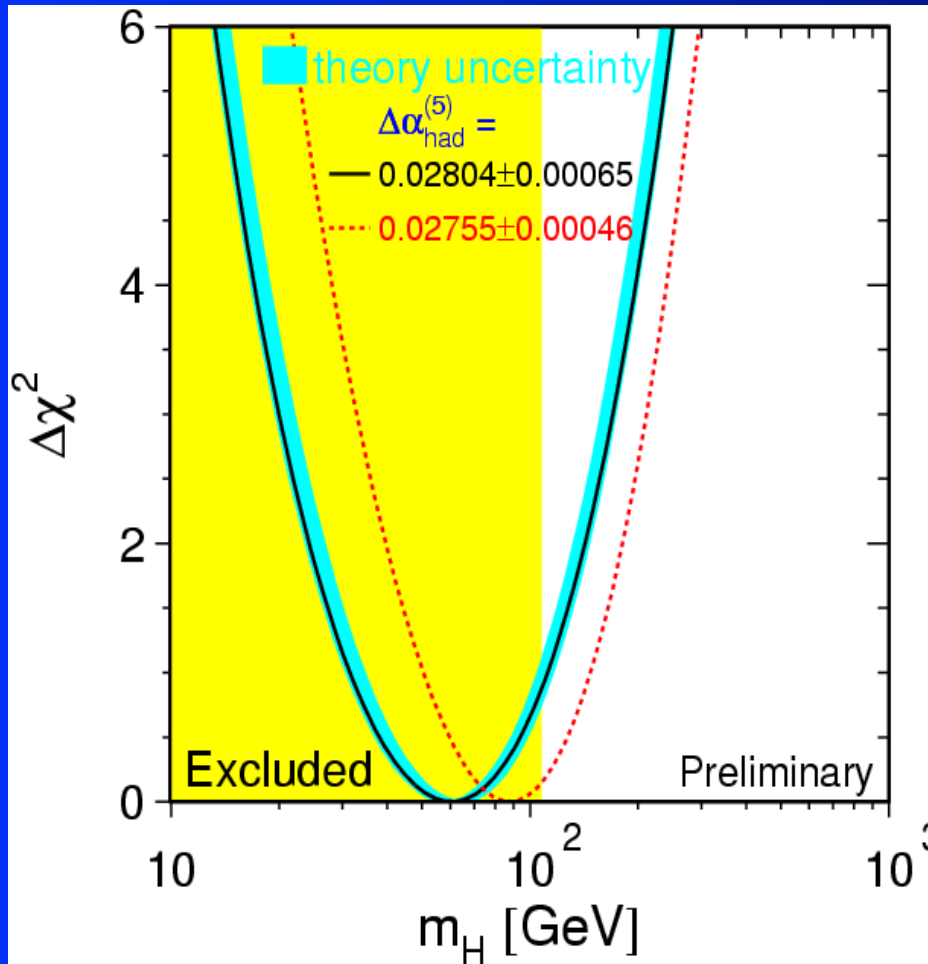
## SUSY Masses in GeV

### Fitted SUSY Parameters

| Symbol                  | Low tan $\beta$     | High tan $\beta$    |
|-------------------------|---------------------|---------------------|
| Tan $\beta$             | 1.71                | 35.0                |
| $m_0$                   | 200                 | 600                 |
| $m_{1/2}$               | 500                 | 400                 |
| $\mu(0)$                | 1084                | -558                |
| $A(0)$                  | 0                   | 0                   |
| $1/\alpha_{\text{GUT}}$ | 24.8                | 24.8                |
| $M_{\text{GUT}}$        | $1.6 \cdot 10^{16}$ | $1.6 \cdot 10^{16}$ |

| Symbol   | Low tan $\beta$ | High tan $\beta$       |
|--|-----------------|------------------------|
| $\tilde{\chi}_1^0(\tilde{B}), \tilde{\chi}_2^0(\tilde{W}^3)$           | 214, 413        | 170, 322               |
| $\tilde{\chi}_3^0(\tilde{H}_1), \tilde{\chi}_4^0(\tilde{H}_2)$         | 1028, 1016      | 481, 498               |
| $\tilde{\chi}_1^\pm(\tilde{W}^\pm), \tilde{\chi}_2^\pm(\tilde{H}^\pm)$ | 413, 1026       | 322, 499               |
| $\tilde{g}$  | 1155            | 950                    |
| $\tilde{e}_L, \tilde{e}_R$   | 303, 270        | 663, 621               |
| $\tilde{\nu}_L$  | 290             | 658                    |
| $\tilde{q}_L, \tilde{q}_R$   | 1028, 936       | 1040, 1010             |
| $\tilde{\tau}_1, \tilde{\tau}_2$                                       | 279, 403        | 537, 634               |
| $\tilde{b}_1, \tilde{b}_2$   | 953, 1010       | 835, 915               |
| $\tilde{t}_1, \tilde{t}_2$   | 727, 1017       | 735, 906               |
| h, H   | 95, 1344        | 119, 565               |
| A, H $^\pm$  | 1340, 1344      | 565, 571 <sup>47</sup> |

# The Higgs Mass Limit

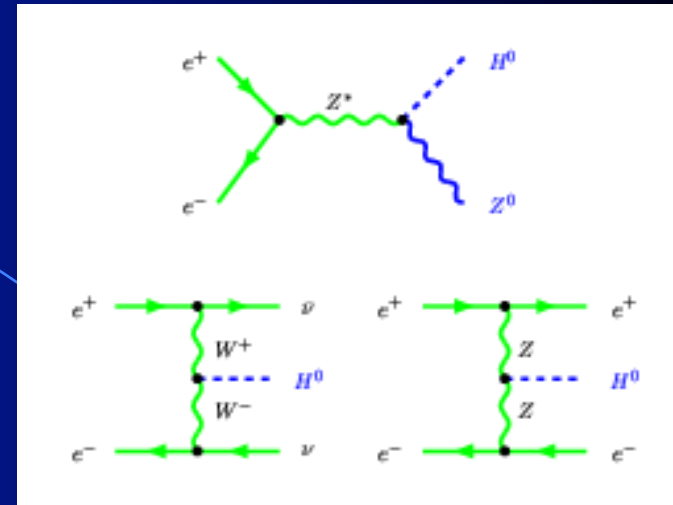
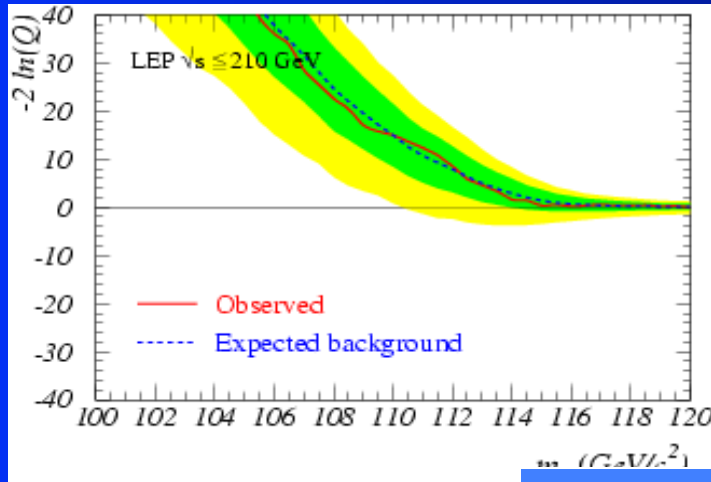


- Indirect limit from radiative corrections
- Direct limit from Higgs non-observation at LEP II (CERN)

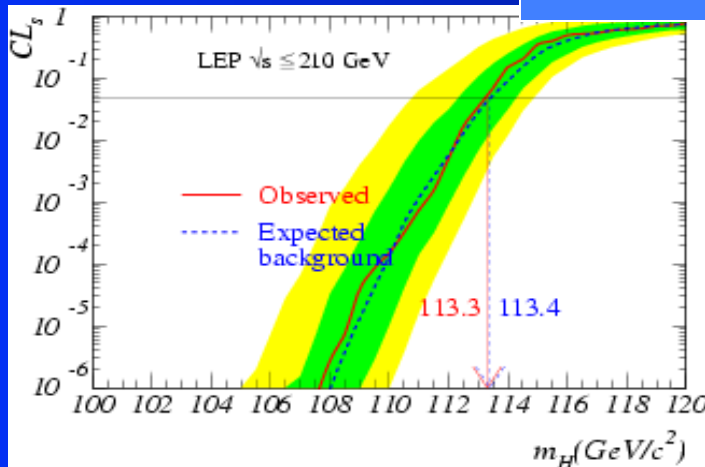
$$113 < m_H < 200 \text{ GeV}$$

At 95 % C.L.

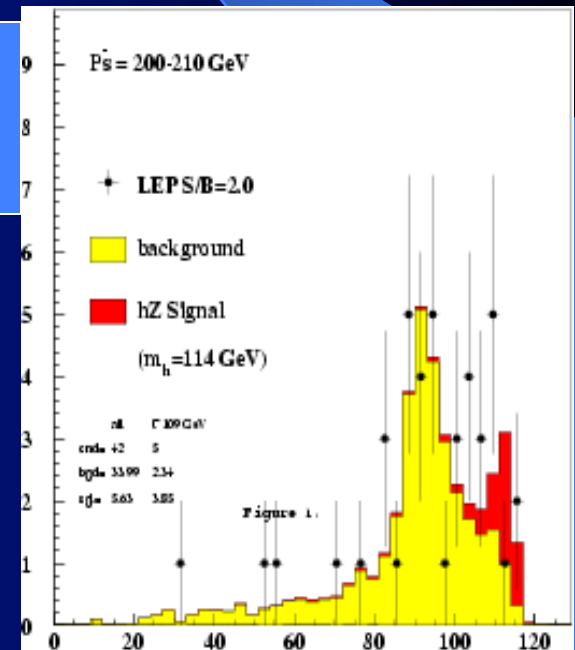
# Higgs Searches



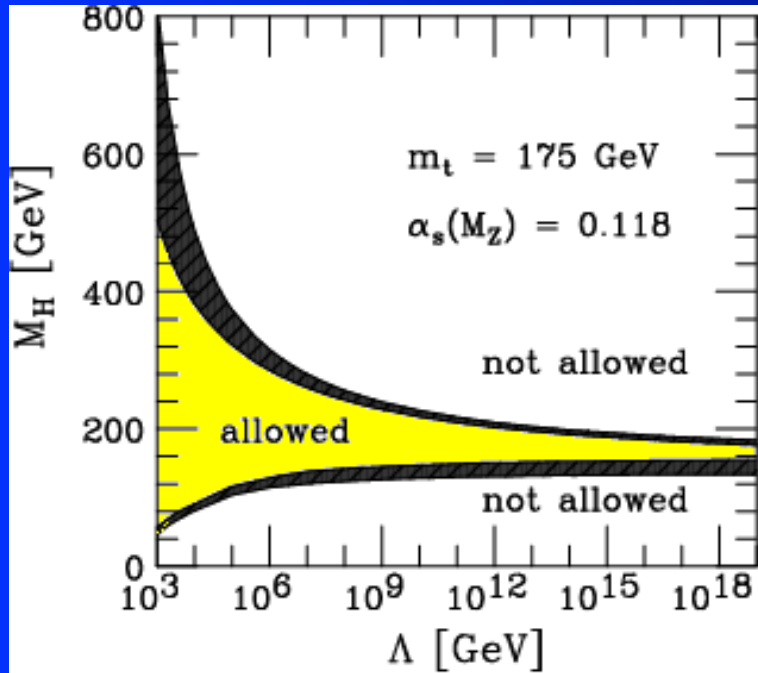
$m_H \geq 113.4$  GeV at  
95 % C.L.



114 -115 GeV  
Event

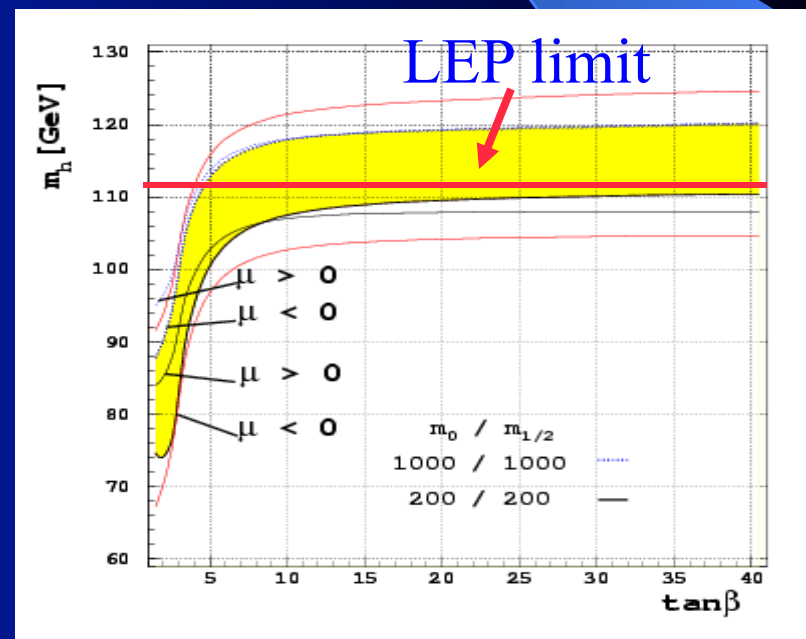


# The Higgs Mass Limit (Theory)

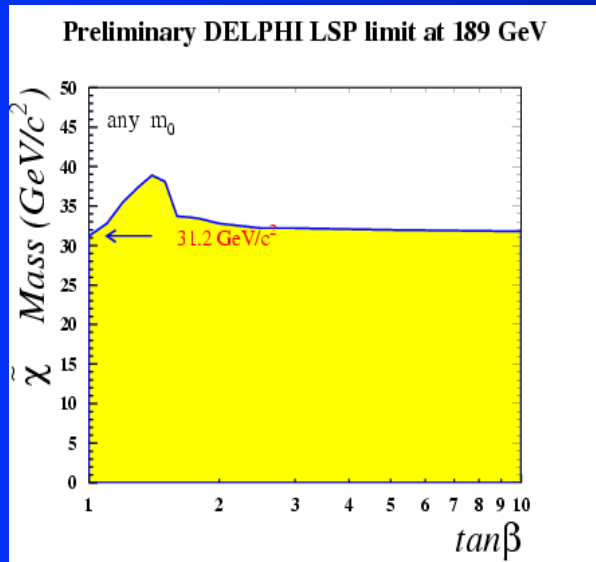


• The SM Higgs  
 $m_H \geq 134$  GeV

SUSY Higgs  
 $m_H \leq 130$  GeV



# SUSY Searches at LEP



neutralinos

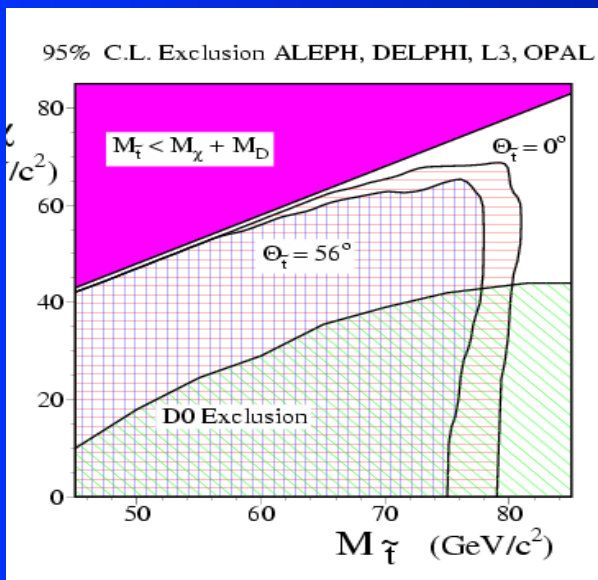
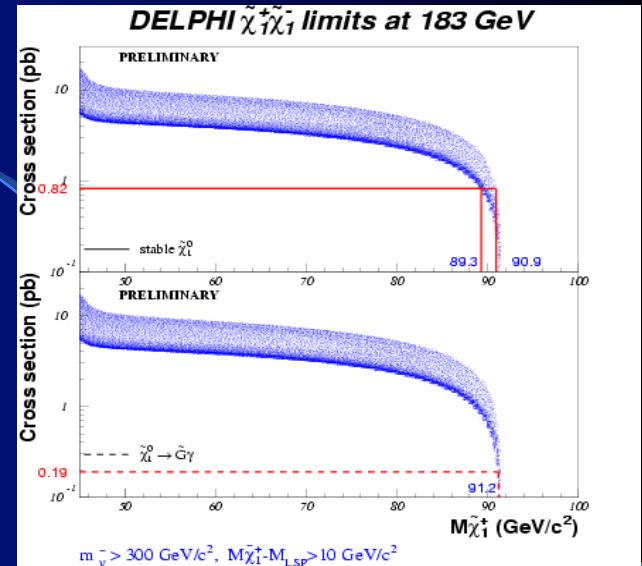


$$\tilde{M}_{\tilde{\chi}_0} \geq 45 \text{ GeV}$$

charginos



$$\tilde{m}_{\tilde{\chi}^+} \geq 104 \text{ GeV}$$



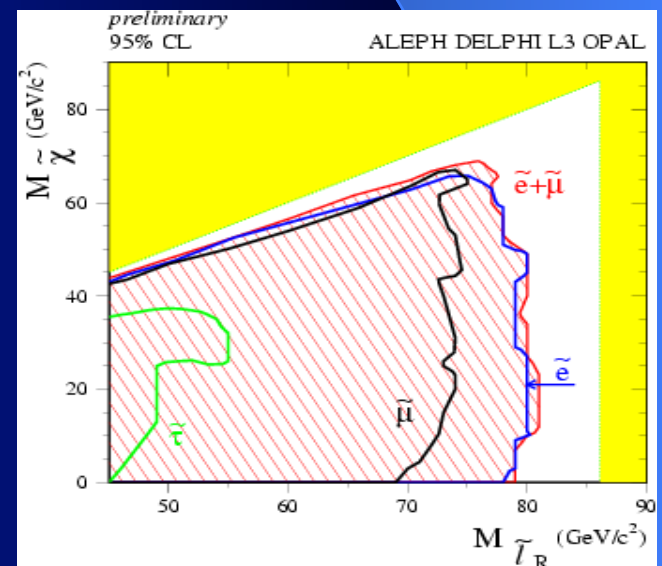
squarks



sleptons



$$\tilde{m}_{\tilde{l}} \geq 104 \text{ GeV}$$

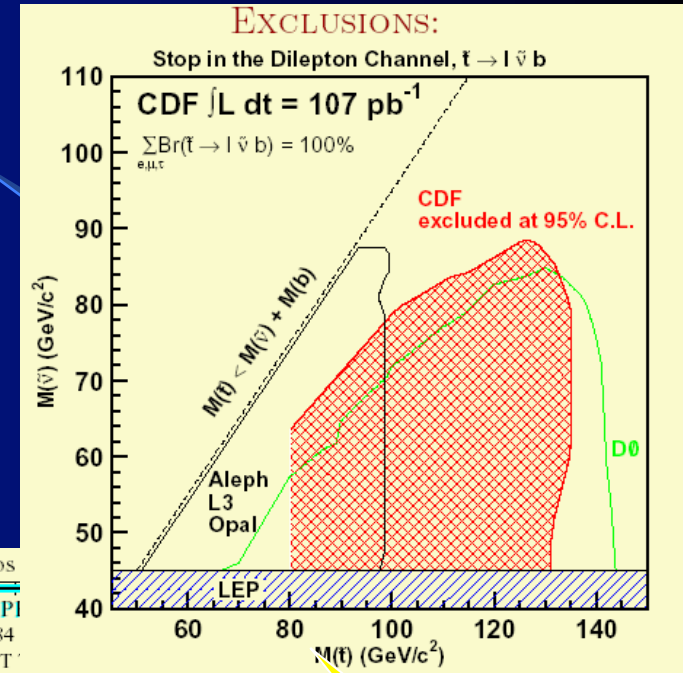
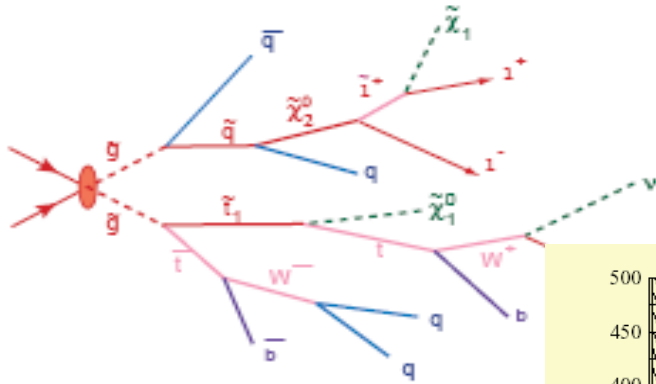




# SUSY Searches at Tevatron

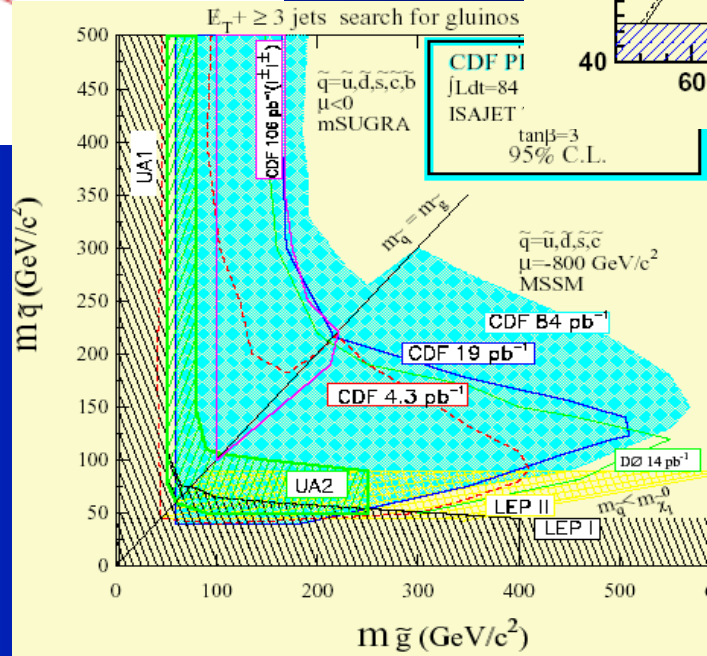
Cascade production of superpartners in hadron collisions

Glauino/squark production event topology allowing sparticle mass reconstruction



Exclusion:  
World's Best Limits

$M_{\tilde{q}} \geq 300 \text{ GeV}$   
 $m_{\tilde{g}} \geq 195 \text{ GeV}$



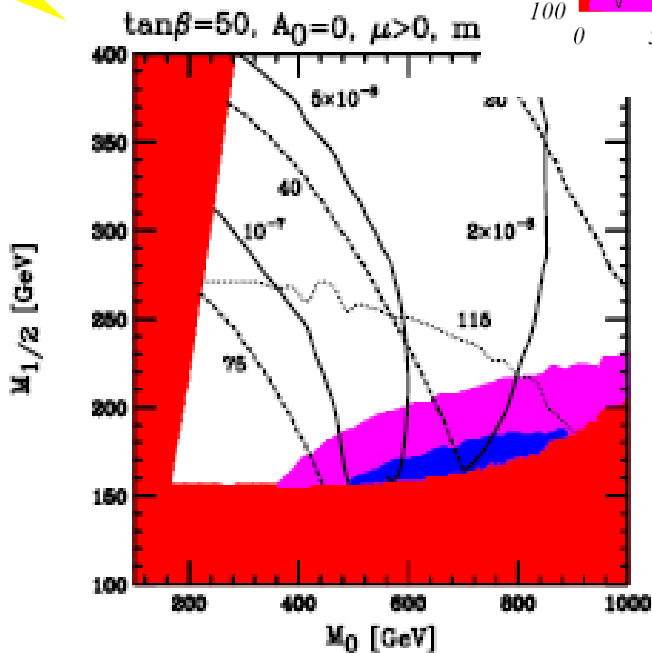
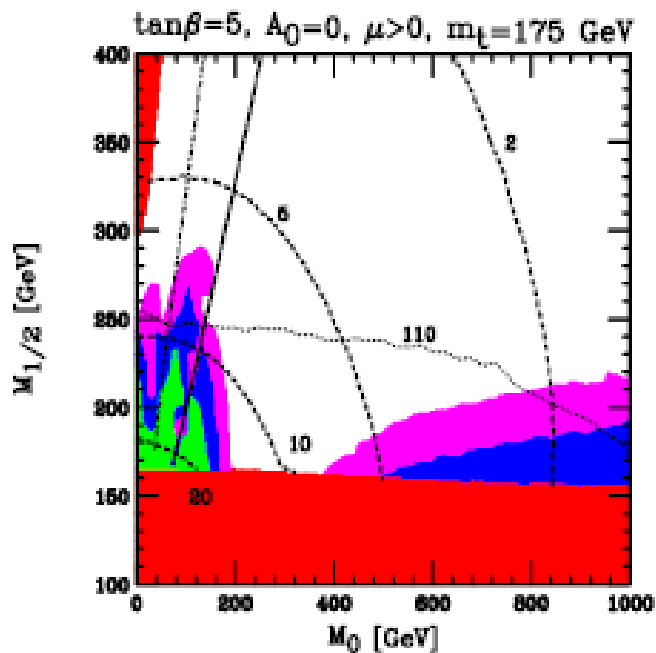
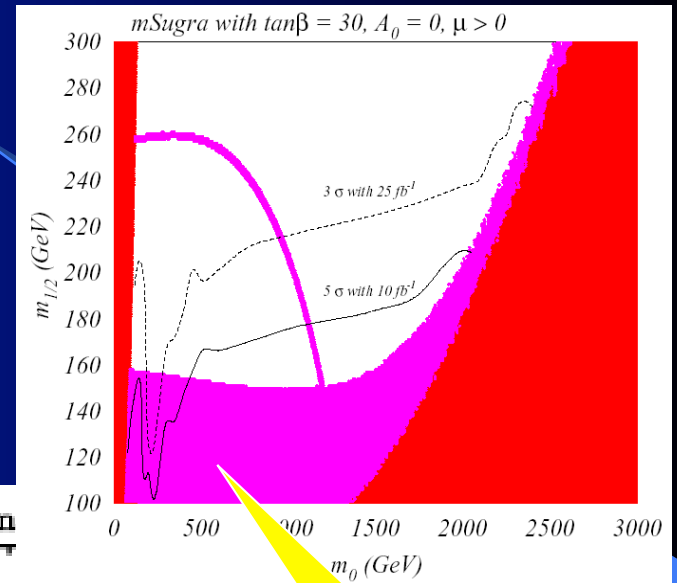
Dilepton Channel

3 jet channel

# SUSY Searches at Tevatron

The reach of Tevatron in lepton channels in  $m_0/m_{1/2}$  plane

Trilepton events reach at  $2 \text{ fb}^{-1}$ ,  $10 \text{ fb}^{-1}$ ,  $30 \text{ fb}^{-1}$

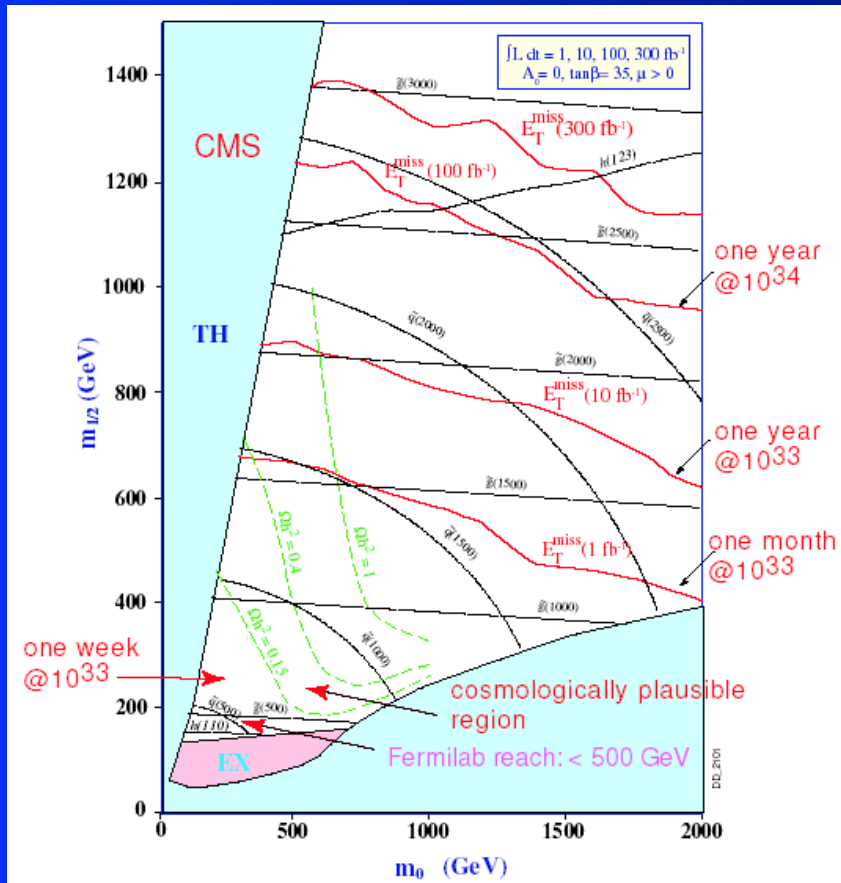


Dimuon Channel at  $10 \text{ fb}^{-1}$ ,  $25 \text{ fb}^{-1}$

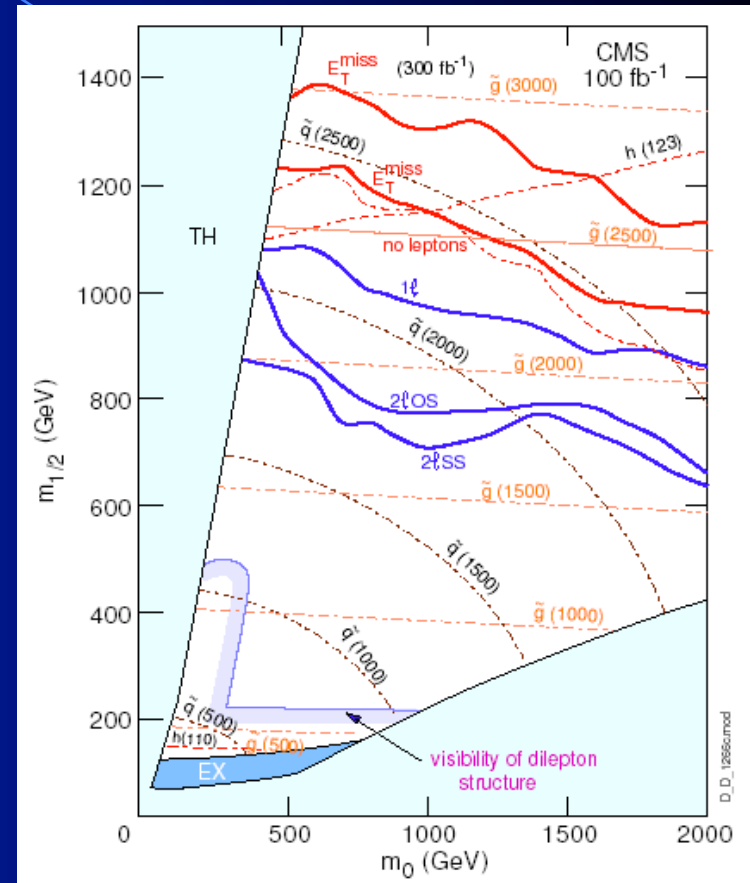
# Tevatron Discovery Reach

| Decay<br>( $Br = 100\%$ )                       | Subsequent Decay   | Final State of<br>$\tilde{b}_1\tilde{\bar{b}}_1$ or $\tilde{t}_1\tilde{\bar{t}}_1$ | Discovery Reach in $M_{\tilde{t}_1}$ or $M_{\tilde{b}_1}$<br>@20 fb $^{-1}$ (Run I) |   |   |
|---|--|--|---|---|---|
| $\tilde{b}_1 \rightarrow b\tilde{\chi}_1^0$     |  | $bb\cancel{E}_T$   | 260 GeV/ $c^2$  | (146 GeV/ $c^2$ [26])   |   |
| $\tilde{t}_1 \rightarrow c\tilde{\chi}_1^0$     |  | $cc\cancel{E}_T$   | 220 GeV/ $c^2$  | (116 GeV/ $c^2$ [26])   |   |
| $\tilde{t}_1 \rightarrow bl\tilde{\nu}$         | $\tilde{\nu} \rightarrow \nu\tilde{\chi}_1^0$            | $\ell^+\ell^-b\cancel{E}_T$  | 240 GeV/ $c^2$  | (140 GeV/ $c^2$ [28])   |   |
| $\tilde{t}_1 \rightarrow bl\nu\tilde{\chi}_1^0$ |  | $\ell^+\ell^-b\cancel{E}_T$  | -   | (129 GeV/ $c^2$ [28])   |   |
| $\tilde{t}_1 \rightarrow b\tilde{\chi}_1^\pm$   | $\tilde{\chi}_1^\pm \rightarrow W^{(*)}\tilde{\chi}_1^0$ | $\ell bj\cancel{E}_T$ and $\ell^+\ell^-j\cancel{E}_T$                              | 210 GeV/ $c^2$  | (-)   |   |
| $\tilde{t}_1 \rightarrow bW\tilde{\chi}_1^0$    |  | $\ell bj\cancel{E}_T$  | 190 GeV/ $c^2$  | (-)   |   |
| NLSP  | Decay Mode   | $c\tau$  | Prod.   | Key Final State(s)  | Discovery Reach<br>@30 fb $^{-1}$       |
| Bino $\tilde{\chi}_1^0$                         | $\gamma + \tilde{G}$                                     | p  | all   | $\gamma\gamma\cancel{E}_T + X$  | 340 GeV/ $c^2$ ( $\tilde{\chi}_1^\pm$ ) |
|   |  | d  | all   | $\gamma dj\cancel{E}_T$ or $\gamma\gamma\cancel{E}_T + X$                               | 300 GeV/ $c^2$ ( $\tilde{\chi}_1^\pm$ ) |
|   |  |  |   |   | ( $c\tau = 50$ cm)                      |
| Higgsino $\tilde{\chi}_1^0$                     | $(h, Z, \gamma) + \tilde{G}$                             | p  | all   | $(hh, h\gamma, hZ, Z\gamma, ZZ, \gamma\gamma)\cancel{E}_T + X$                          | 220 GeV/ $c^2$ ( $\tilde{\chi}_1^\pm$ ) |
|   |  | d  | all   | $\delta_{ip} < 0$ for $h \rightarrow bb, Z \rightarrow \ell^+\ell^-$                    | -                                       |
|   |  | d  | all   | $\gamma_d + X$  | -                                       |
| $\tilde{\tau}$                                  | $\tau + \tilde{G}$                                       | p  | all   | $\ell\ell\ell j\cancel{E}_T, \ell^\pm\ell^\pm jj\cancel{E}_T, \tau_h\tau_h\cancel{E}_T$ | 230 GeV/ $c^2$ ( $\tilde{\chi}_1^\pm$ ) |
|   |  |  |   |   | 120 GeV/ $c^2$ ( $\tilde{\tau}_1$ )     |
|   |  | ll   | all   | $\mu(dE/dx) + \ell\ell(M_{\ell\ell} > 150 \text{ GeV}/c^2)$                             | 420 GeV/ $c^2$ ( $\tilde{\chi}_1^\pm$ ) |
|   |  |  |   |   | 210 GeV/ $c^2$ ( $\tilde{\tau}$ )       |
|   |  | ll   | all   | $\mu(dE/dx) + X$  | 180 GeV/ $c^2$ ( $\tilde{\tau}$ )       |
|   |  | ll   | all   | $\mu(dE/dx + \text{TOF}) + X$   | 210 GeV/ $c^2$ ( $\tilde{\tau}$ )       |
| $\tilde{t}_1$                                   | $(c, bW) + \tilde{G}$                                    | p  | $\tilde{t}_1\tilde{\bar{t}}_1$  | $cc\cancel{E}_T$ or $\ell + jets + \cancel{E}_T$  | 175 GeV/ $c^2$ ( $\tilde{t}_1$ )        |

# SUSY Searches at LHC

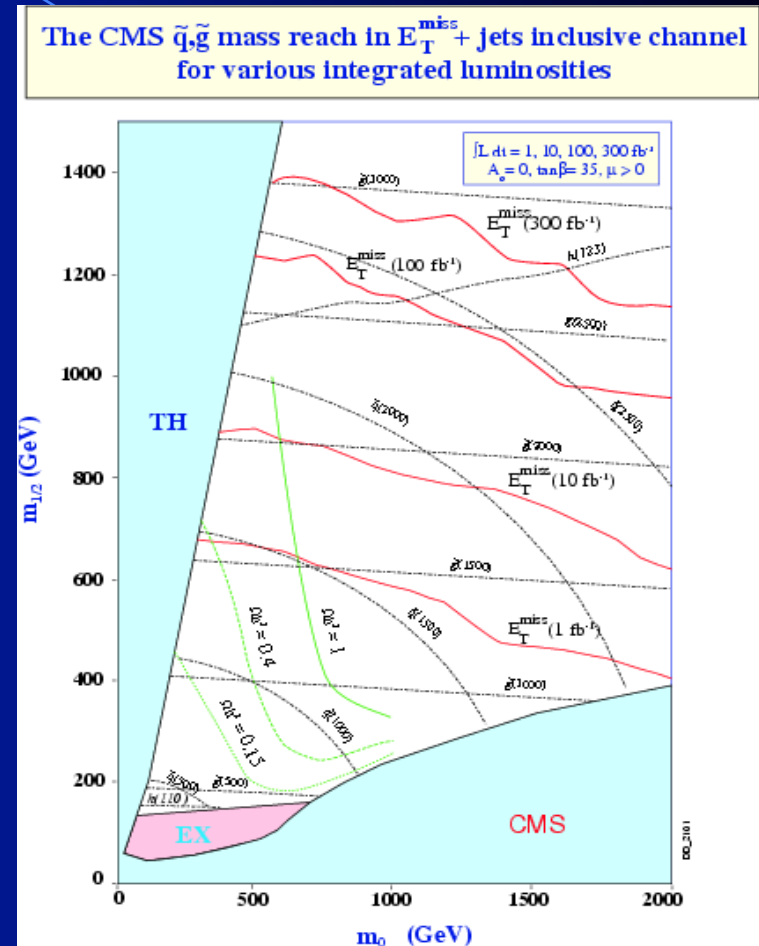
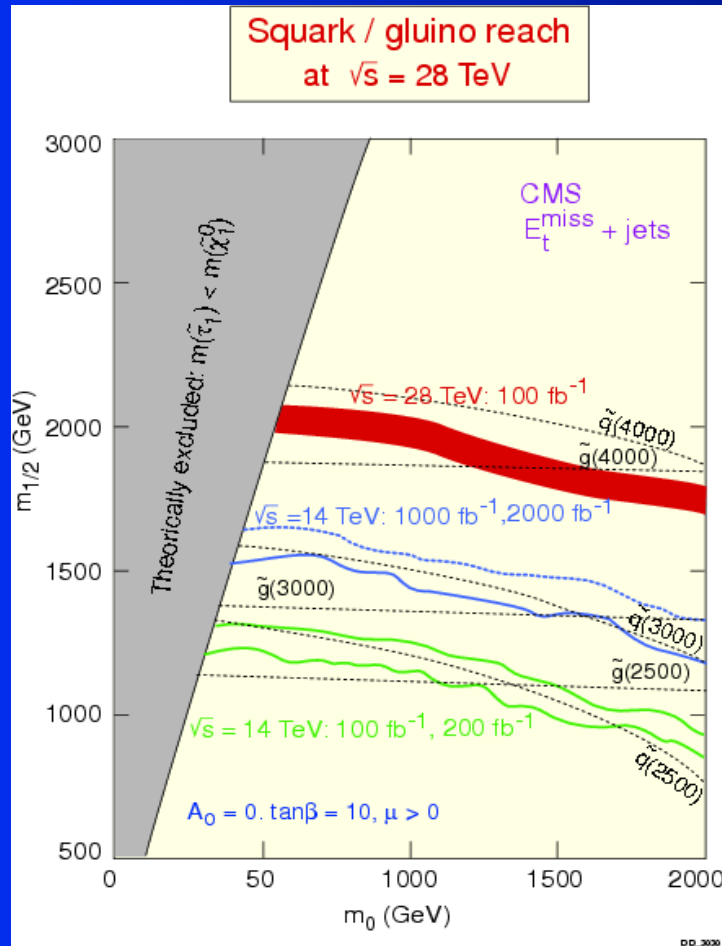


5  $\sigma$  reach in jets +  $\cancel{E}_T$  channel



Reach limits for various channels at  $100 \text{ fb}^{-1}$

# SUSY Searches at LHC



Squark and gluino reaches at various luminosities

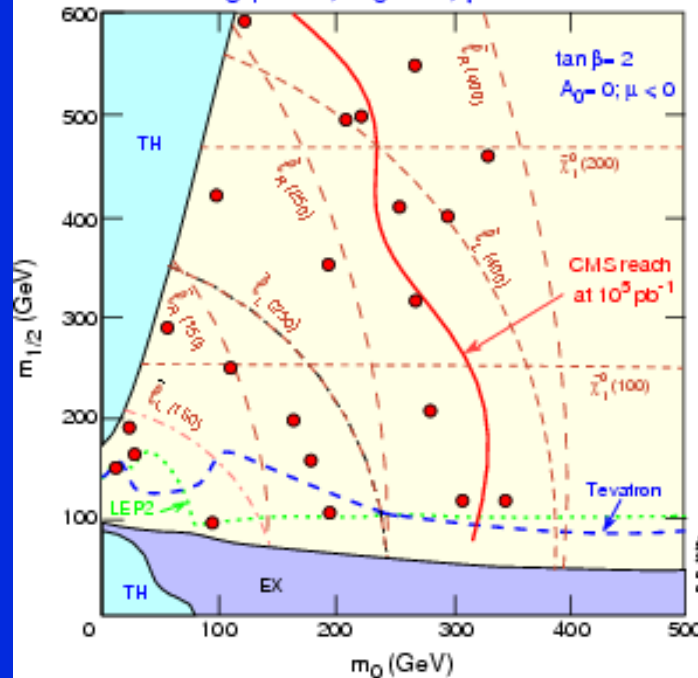
# SUSY Searches at LHC

Slepton mapping of parameter space

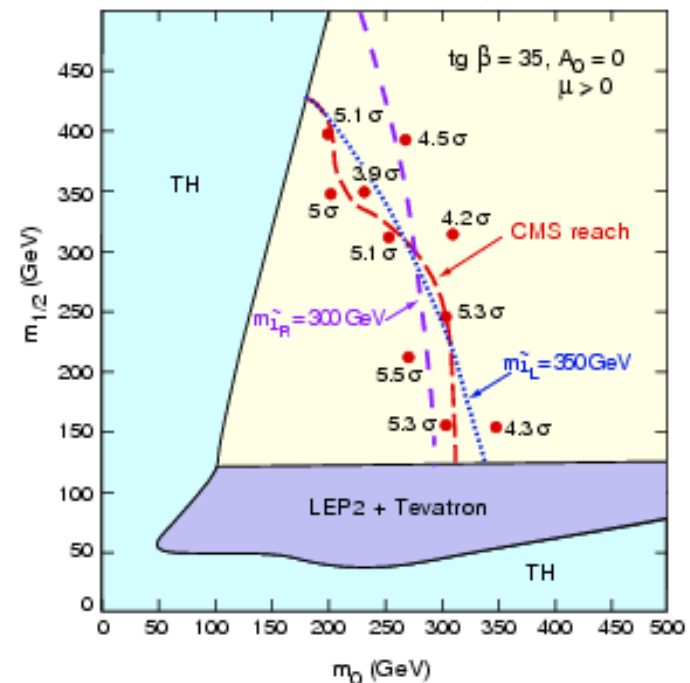
mSUGRA-MSSM

Significance of expected excess of events in 2 lepton final state over SM + SUSY bkgd with  $10^5 \text{ pb}^{-1}$   
 $5\sigma$  contour,  $\sigma = S / \sqrt{S+B}$

$\tan \beta = 2, A_0 = 0, \mu < 0$



$\tan \beta = 35, A_0 = 0, \mu > 0$





# Superparticles



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[C. Caso et al.](#), The European Physical Journal **C103** (2018) 1 (2018 Authors)

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- **2019** [2019 Web update of Sparticle Listings](#) [New July 6, 2019](#)
- **2018** [2018 Summary Tables and Conservation Laws](#)
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Discovery of  
the new world  
of SUSY

Back to 60's

New  
discoveries  
every year





What comes beyond  
the Standard Model ?

**SM**