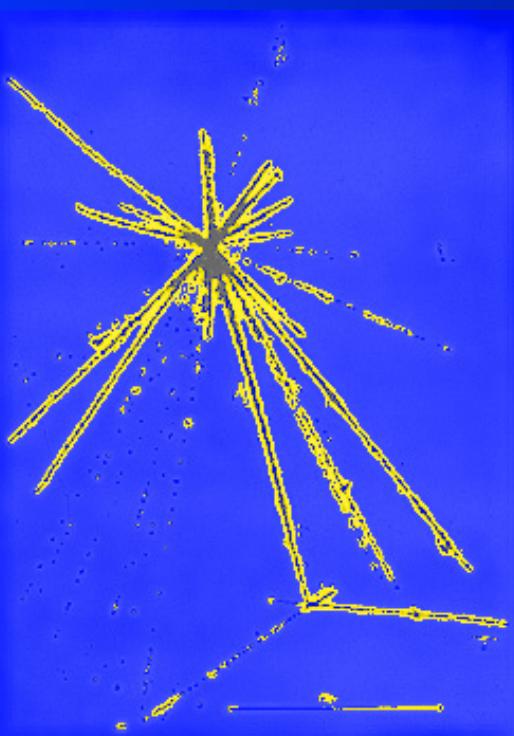


# SUPERSYMMETRIC EXTENSION OF THE STANDARD MODEL

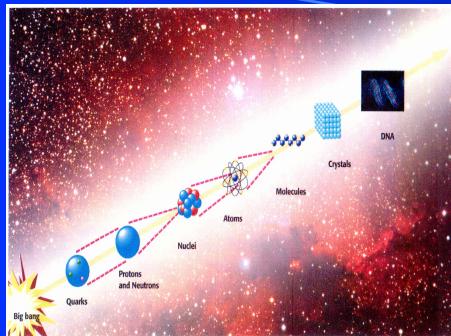


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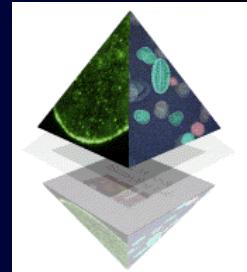
JINR / ITEP

## Outline

1. What is SUSY
2. Motivation of SUSY
3. The MSSM
4. SUSY Searches
5. SUSY in Astrophysics



# What is SUSY



- **Supersymmetry** is a boson-fermion symmetry that is aimed to unify all forces in Nature including gravity within a single framework
- Modern views on supersymmetry in particle physics are based on string paradigm, though low energy manifestations of SUSY can be found (?) at modern colliders and in non-accelerator experiments
- The concepts of Quantum Field Theory allow SUSY without any restrictions
- There is no direct confirmation of SUSY but this does not stop theorists due to extreme beauty of SUSY models

# Supersymmetry

(*Super*) Algebra

$$[P_\mu, P_\nu] = 0, [P_\mu, M_{\rho\sigma}] = i(g_{\mu\rho}P_\sigma - g_{\mu\sigma}P_\rho),$$

$$[M_{\mu\nu}, M_{\rho\sigma}] = i(g_{\nu\rho}M_{\mu\sigma} - g_{\nu\sigma}M_{\mu\rho} - g_{\mu\rho}M_{\nu\sigma} + g_{\mu\sigma}M_{\nu\rho}),$$

$$[B_r, B_s] = iC_{rs}^t B_t, \quad [B_r, P_\mu] = [B_r, M_{\mu\sigma}] = 0,$$

$$[Q_\alpha^i, P_\mu] = [\bar{Q}_{\dot{\alpha}}^i, P_\mu] = 0,$$

$$[Q_\alpha^i, M_{\mu\nu}] = \frac{1}{2}(\sigma_{\mu\nu})_\alpha^\beta Q_\beta^i, \quad [\bar{Q}_{\dot{\alpha}}^i, M_{\mu\nu}] = -\frac{1}{2}\bar{Q}_{\dot{\beta}}^i(\bar{\sigma}_{\mu\nu})_{\dot{\beta}}^{\dot{\alpha}},$$

$$[Q_\alpha^i, B_r] = (b_r)_j^i Q_\alpha^j, \quad [\bar{Q}_{\dot{\alpha}}^i, B_r] = -\bar{Q}_{\dot{\alpha}}^j (b_r)_j^i,$$

$$\{Q_\alpha^i, \bar{Q}_{\dot{\beta}}^j\} = 2\delta^{ij}(\sigma^\mu)_{\alpha\dot{\beta}} P_\mu$$

$$\{Q_\alpha^i, Q_\beta^j\} = 2\varepsilon_{\alpha\beta} Z^{ij}, \quad Z^{ij} = Z_{ij}^\dagger, \quad Z_{ij} = a_{ij}^r b_r,$$

$$\{\bar{Q}_{\dot{\alpha}}^i, \bar{Q}_{\dot{\beta}}^j\} = -2\varepsilon_{\dot{\alpha}\dot{\beta}} Z^{ij}, \quad [Z_{ij}, \text{anything}] = 0,$$

$$\alpha, \dot{\alpha}, \beta, \dot{\beta} = 1, 2; \quad i, j = 1, 2, \dots, N.$$

*Superspace*

$$x_\mu \rightarrow x_\mu, \vartheta, \bar{\vartheta}$$

*Group Element*

$$G(x, \vartheta, \bar{\vartheta}) = e^{i(-x^\mu P_\mu + \vartheta Q + \bar{\vartheta} \bar{Q})}$$

*Supertranslation*

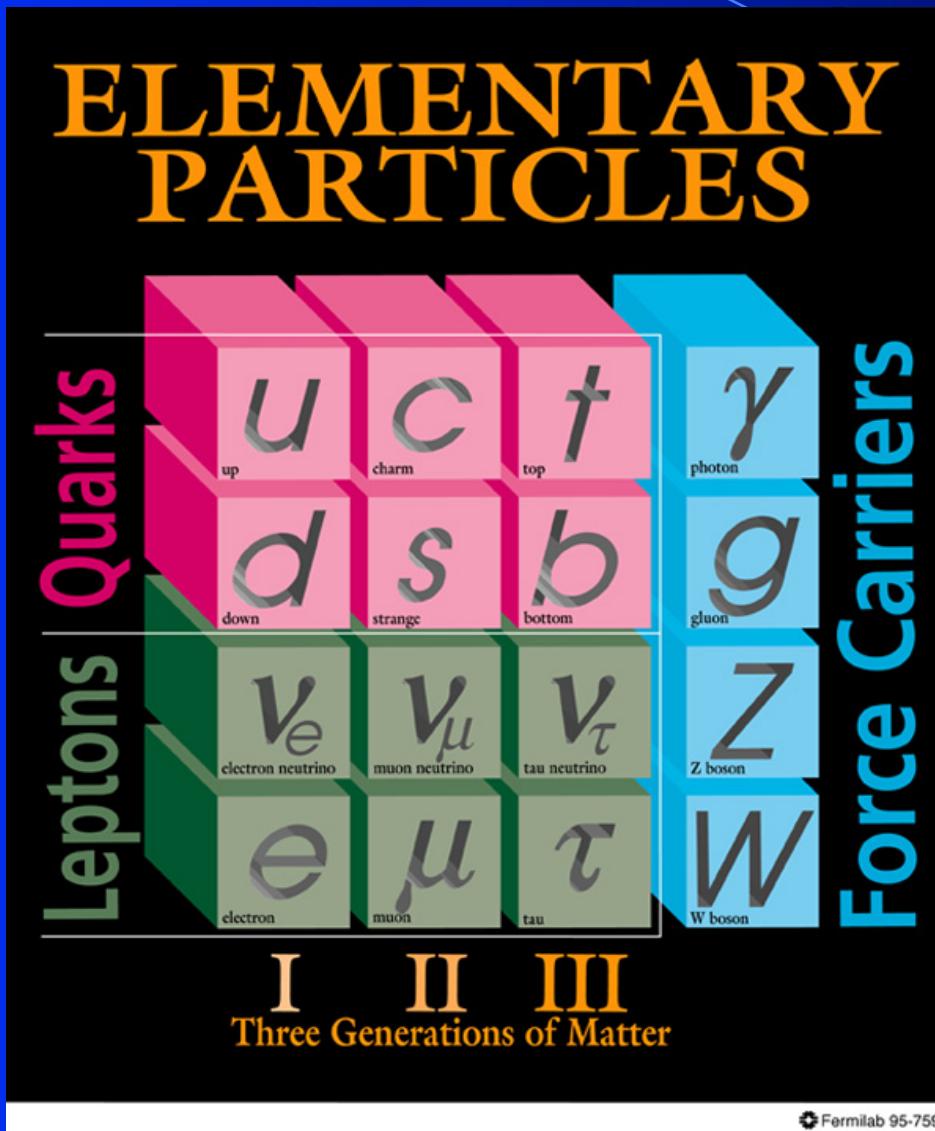
$$x_\mu \rightarrow x_\mu, \vartheta, \bar{\vartheta}$$

$$\vartheta \rightarrow \vartheta + \xi,$$

$$\bar{\vartheta} \rightarrow \bar{\vartheta} + \bar{\xi}$$

Local translation =  
general relativity !

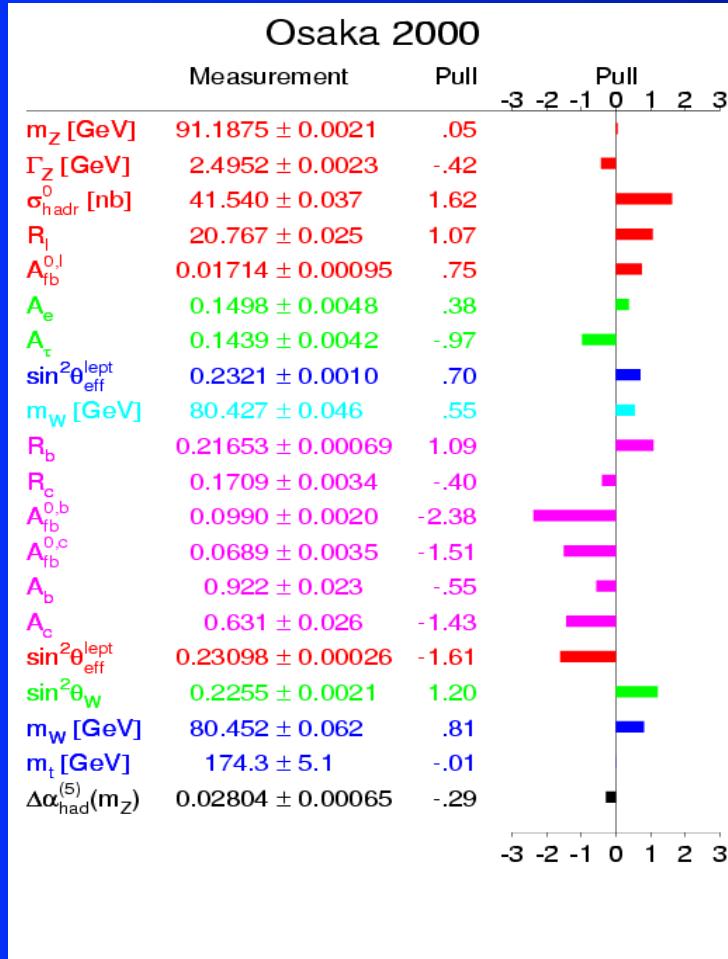
# The Standard Model



- Fits the experimental data very well
- Has too many free parameters and unexplained features
- The Higgs boson is still missing

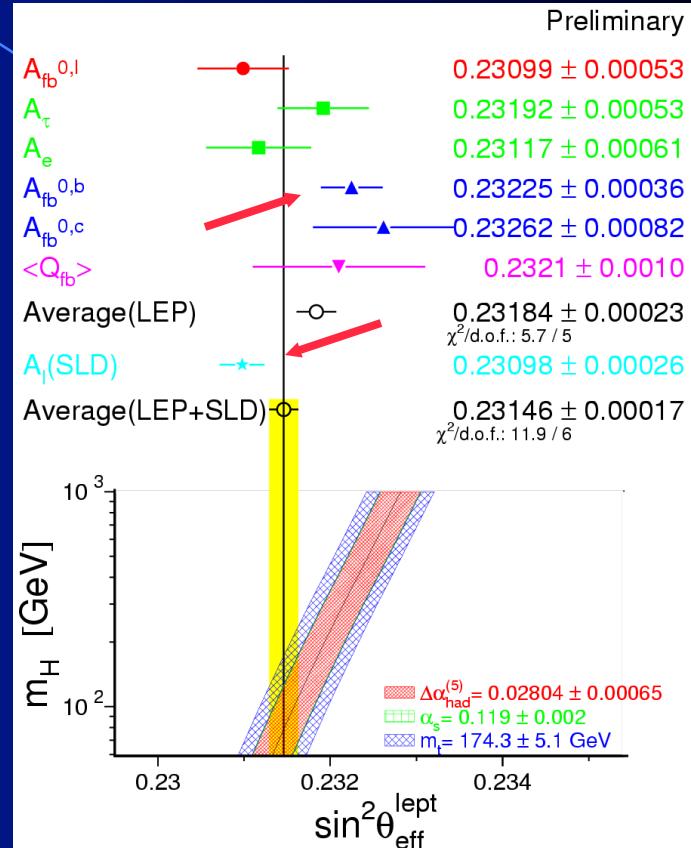
# Comparison with Experiment

## Global Fit to Data



Remarkable agreement of ALL the data with the SM predictions - precision tests of radiative corrections and the SM

## Higgs Mass Constraint



Though the values of  $\sin \theta_W$  extracted from different experiments are in good agreement, two most precise measurements from hadron and lepton asymmetries disagree by  $3\sigma$

# The SM and Beyond

## The problems of the SM:

- Inconsistency at high energies due to Landau pole
- Large number of free parameters
- Formal unification of strong and electroweak interactions
- Still unclear mechanism of EW symmetry breaking
- CP-violation is not understood
- Flavour mixing and the number of generations is arbitrary
- The origin of the mass spectrum in unclear

## The way beyond the SM:

- The SAME fields with NEW interactions

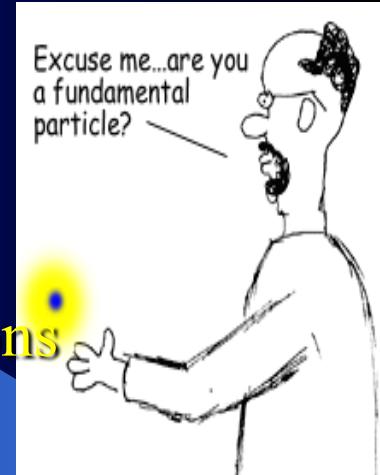


GUT, SUSY, String

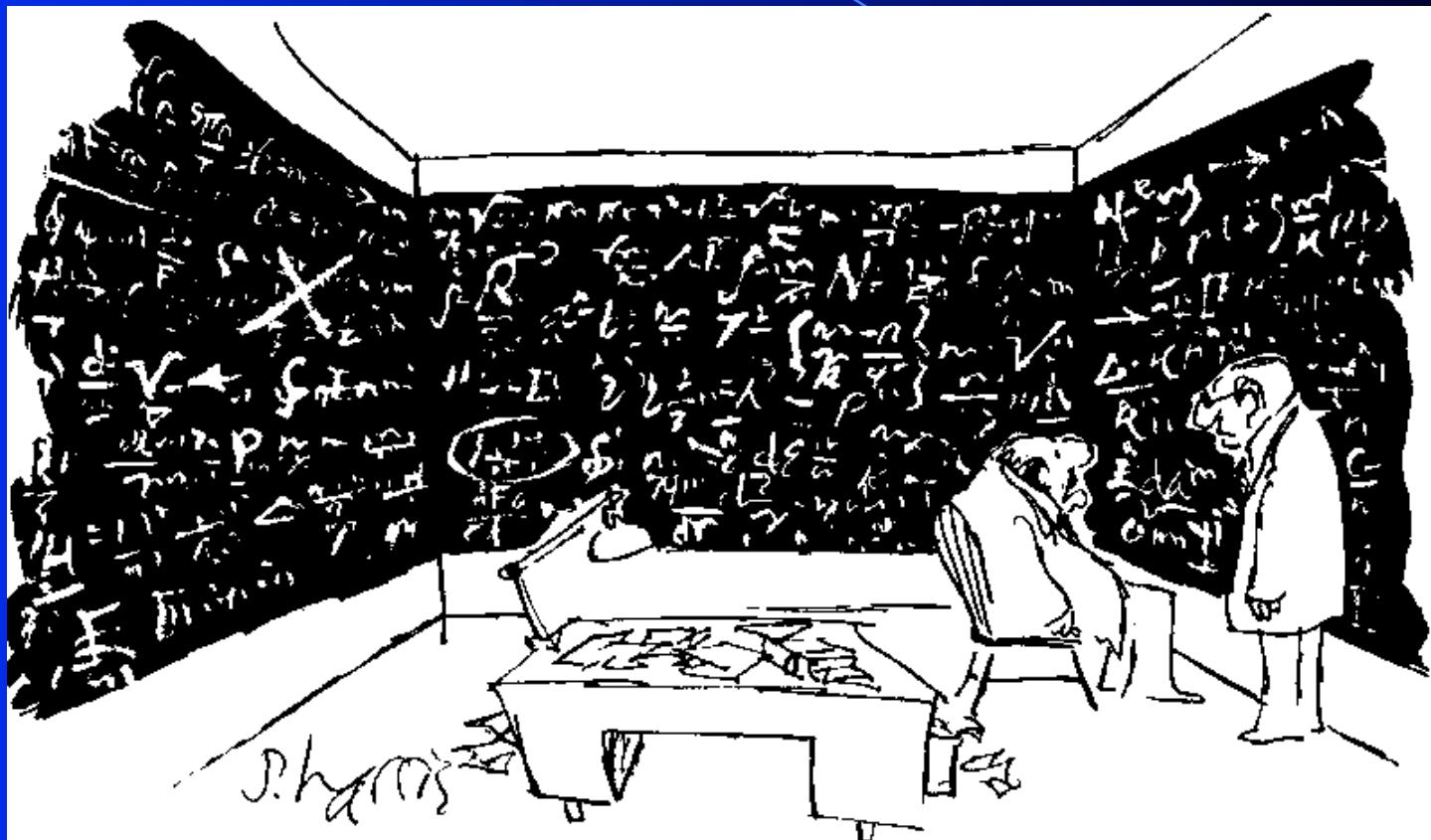
- NEW fields with NEW interactions



Compositeness, Technicolour,  
preons



# We like elegant solutions



"Whatever happened to *elegant* solutions?"

# Motivation of SUSY in Particle Physics

- Unification with Gravity
- Unification of gauge couplings
- Solving the fermion problem
- Dark matter in the Universe
- Superstrings  
 $spin\ 2 \rightarrow spin\ 3/2 \rightarrow spin\ 1 \rightarrow spin\ 1/2 \rightarrow spin\ 0$

Unification of matter (fermions) with forces (bosons) naturally arises

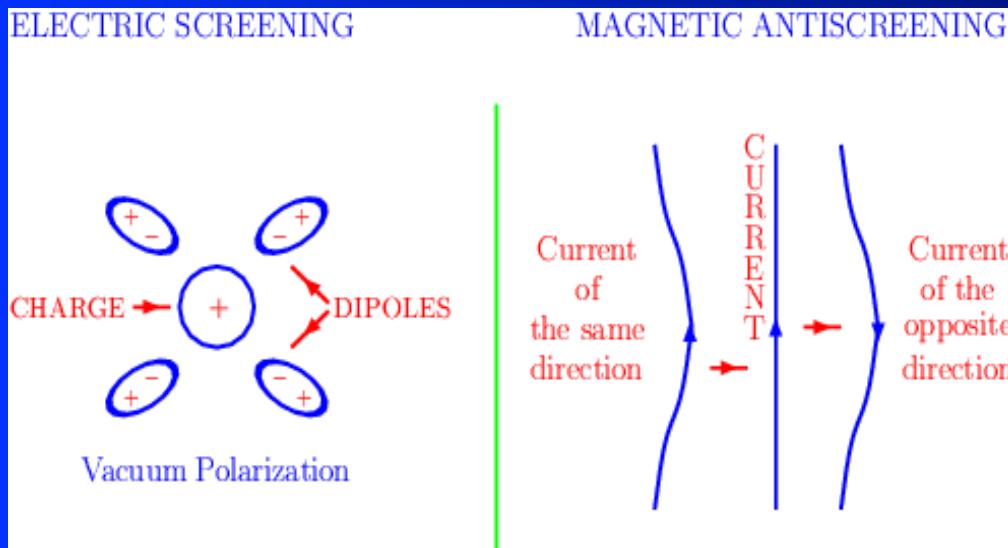
from an attempt to unify gravity with the other interactions

$$\{Q_\alpha^i, \bar{Q}_{\dot{\beta}}^j\} = 2\delta^{ij}(\sigma^\mu)_{\alpha\dot{\beta}} P_\mu \Rightarrow \{\delta_\varepsilon, \bar{\delta}_{\bar{\varepsilon}}\} = 2(\varepsilon\sigma^\mu\bar{\varepsilon})P_\mu$$
$$\varepsilon = \varepsilon(x) \text{ local coordinate transf.} \Rightarrow \text{(super)gravity}$$

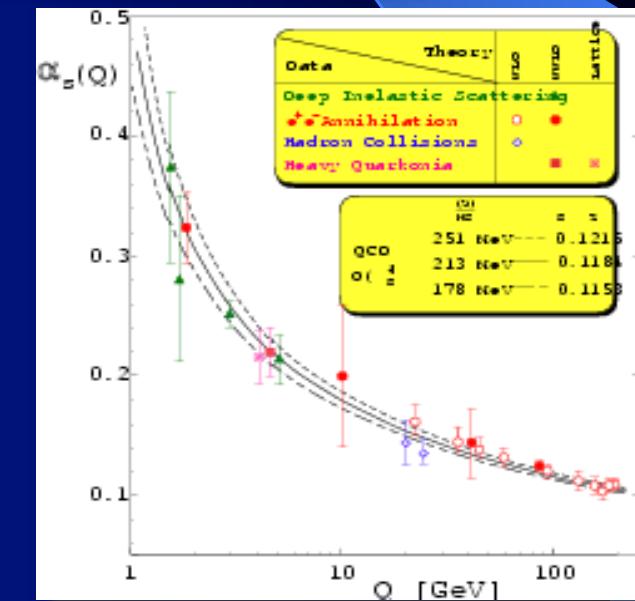
# Motivation of SUSY in Particle Physics

- Unification of gauge couplings

<i>Low Energy</i>			$\Rightarrow$	<i>High Energy</i>
SU <sub>c</sub> (3)	SU <sub>L</sub> (2)	U <sub>Y</sub> (1)	$\Rightarrow$	$G_{GUT}$ (or $G^n + \text{symm}$ )
<i>gluons</i>	$W, Z$	<i>photon</i>	$\Rightarrow$	<i>gauge bosons</i>
<i>quarks</i>	<i>leptons</i>		$\Rightarrow$	<i>fermions</i>
$g_3$	$g_2$	$g_1$	$\Rightarrow$	$g_{GUT}$



$$\alpha_i = \alpha_i(\frac{Q^2}{\Lambda^2}) = \alpha_i(\text{distance})$$



Running of the strong coupling

# Motivation of SUSY

RG Equations

$$\frac{d\tilde{\alpha}_i}{dt} = b_i \tilde{\alpha}_i^2, \quad \tilde{\alpha}_i = \alpha_i / 4\pi = g_i^2 / 16\pi^2, \quad t = \log(Q^2 / \mu^2)$$

$$SM: \quad b_i = \begin{pmatrix} b_1 \\ b_2 \\ b_3 \end{pmatrix} = \begin{pmatrix} 0 \\ -22/3 \\ -11 \end{pmatrix} + N_{Fam} \begin{pmatrix} 4/3 \\ 4/3 \\ 4/3 \end{pmatrix} + N_{Higgs} \begin{pmatrix} 1/10 \\ 1/6 \\ 0 \end{pmatrix}$$

$$MSSM: \quad b_i = \begin{pmatrix} b_1 \\ b_2 \\ b_3 \end{pmatrix} = \begin{pmatrix} 0 \\ -6 \\ -9 \end{pmatrix} + N_{Fam} \begin{pmatrix} 2 \\ 2 \\ 2 \end{pmatrix} + N_{Higgs} \begin{pmatrix} 3/10 \\ 1/2 \\ 0 \end{pmatrix}$$

Input

$$\alpha^{-1}(M_Z) = 128.978 \pm 0.027$$

$$\sin^2 \theta_{MS} = 0.23146 \pm 0.00017$$

$$\alpha_s(M_Z) = 0.1184 \pm 0.0031$$

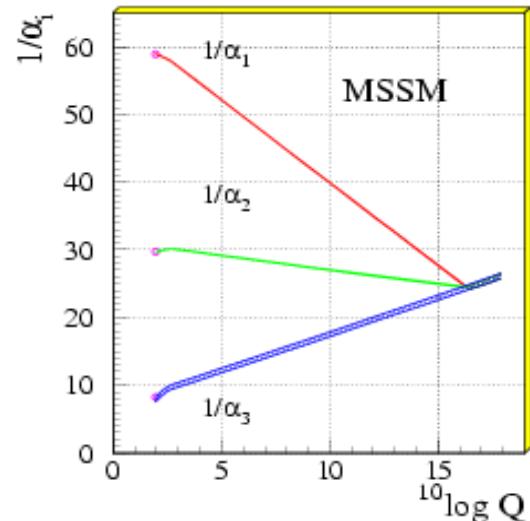
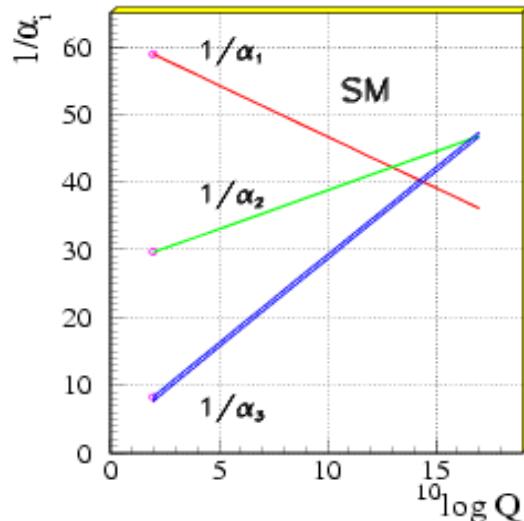
Output

$$M_{SUSY} = 10^{3.4 \pm 0.9 \pm 0.4} \text{ GeV}$$

$$M_{GUT} = 10^{15.8 \pm 0.3 \pm 0.1} \text{ GeV}$$

$$\alpha_{GUT}^{-1} = 26.3 \pm 1.9 \pm 1.0$$

Unification of the Coupling Constants  
in the SM and the minimal MSSM



SUSY yields unification!

# Motivation of SUSY

- Solution of the Hierarchy Problem

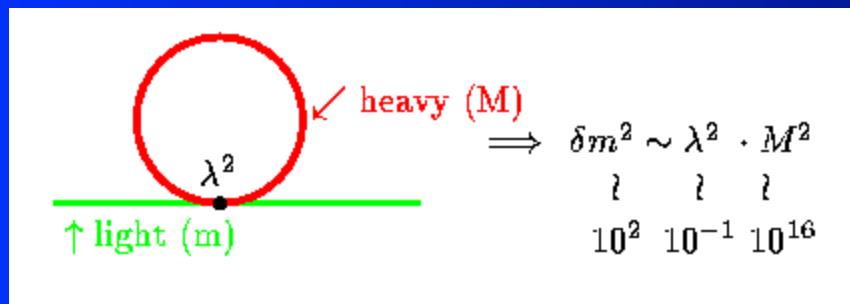
$$m_H \sim v \sim 10^2 \text{ GeV}$$

$$m_\Sigma \sim V \sim 10^{16} \text{ GeV}$$

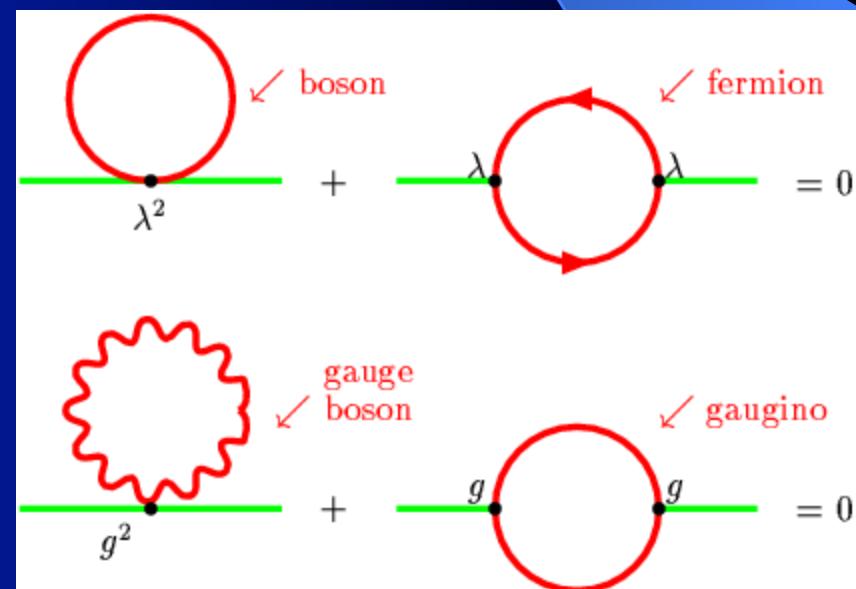
$$\frac{m_H}{m_\Sigma} \sim 10^{-14} \ll 1$$

Cancellation of quadratic terms

Destruction of the hierarchy by  
Radiative corrections

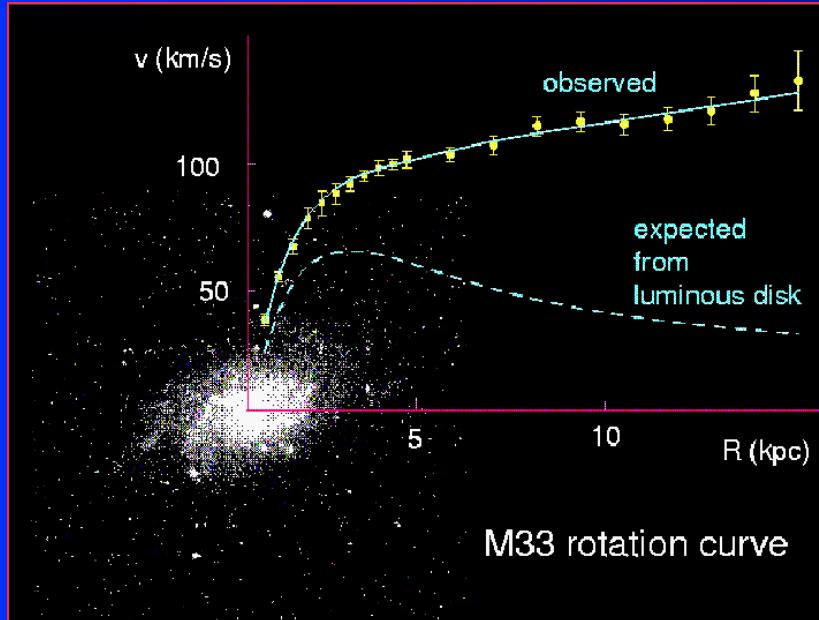


$$\sum_{bosons} m^2 = \sum_{fermions} m^2$$



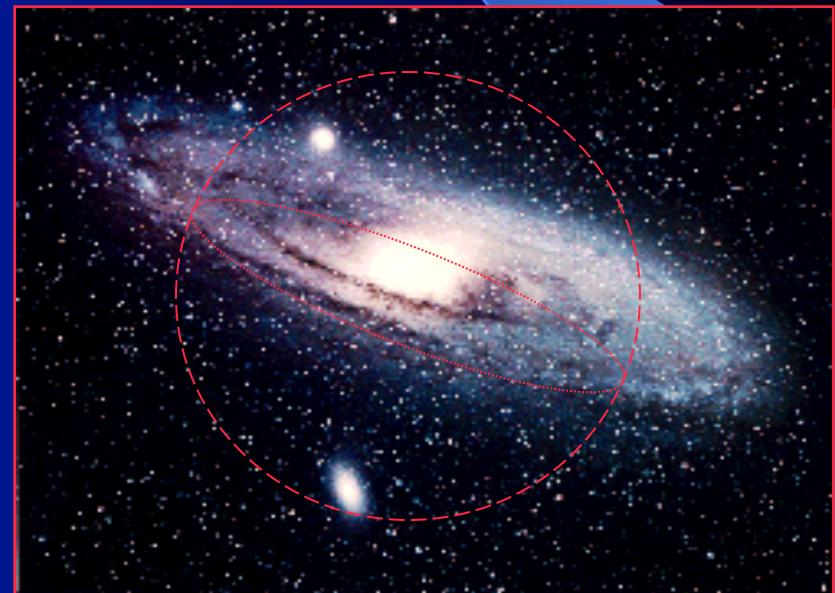
# Motivation of SUSY

- Dark Matter in the Universe



Spiral galaxies consist of a central bulge and a very thin disc, and surrounded by an approximately spherical halo of dark matter

The flat rotation curves of spiral galaxies provide the most direct evidence for the existence of large amount of the dark matter.

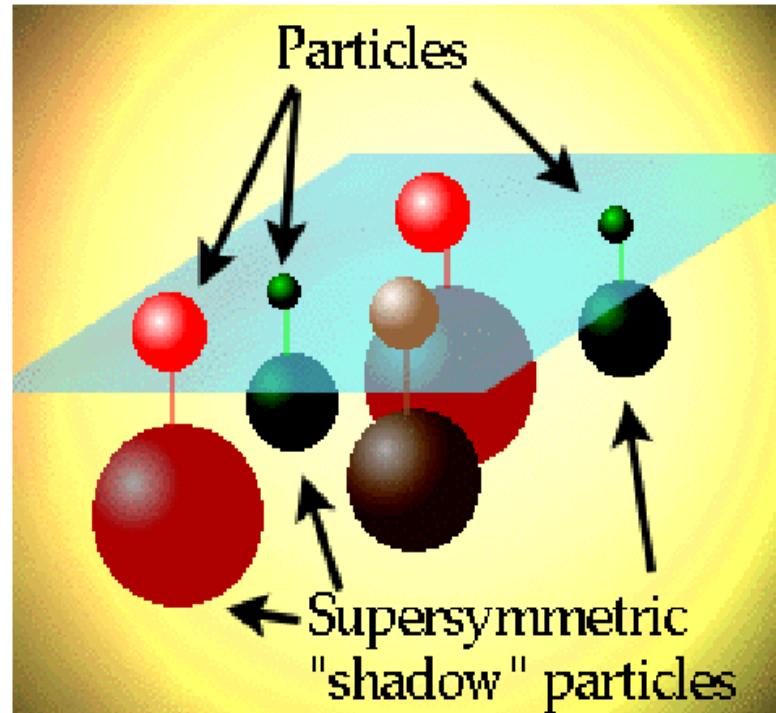


SUSY provides a candidate for the Dark matter – a stable neutral particle

# Particle Content of the MSSM

<i>Superfield</i>	<i>Bosons</i>	<i>Fermions</i>	$SU_c(3)$	$SU_L(2)$	$U_Y(1)$		
<i>Gauge</i>							
$G^a$	gluon	$g^a$	gluino	$\tilde{g}^a$	8	0	0
$V^k$	Weak	$W^k(W^\pm, Z)$	wino, zino	$\tilde{w}^k(\tilde{w}^\pm, \tilde{z})$	1	3	0
$V'$	Hypercharge	$B(\gamma)$	bino	$\tilde{b}(\tilde{\gamma})$	1	1	0
<i>Matter</i>							
$L_i$	sleptons	$\begin{cases} \tilde{L}_i = (\tilde{\nu}, \tilde{e})_L \\ \tilde{E}_i = \tilde{e}_R \end{cases}$	leptons	$\begin{cases} L_i = (v, e)_L \\ E_i = e_R \end{cases}$	1	2	-1
$E_i$					1	1	2
$Q_i$		$\begin{cases} \tilde{Q}_i = (\tilde{u}, \tilde{d})_L \\ \tilde{U}_i = \tilde{u}_R \\ \tilde{D}_i = \tilde{d}_R \end{cases}$	quarks	$\begin{cases} Q_i = (u, d)_L \\ U_i = u_R \\ D_i = d_R \end{cases}$	3	2	1/3
$U_i$	squarks				3*	1	-4/3
$D_i$					3*	1	2/3
<i>Higgs</i>							
$H_1$	Higgses	$\begin{cases} H_1 \\ H_2 \end{cases}$	higgsinos	$\begin{cases} \tilde{H}_1 \\ \tilde{H}_2 \end{cases}$	1	2	-1
$H_2$					1	2	1

# SUSY Shadow World



One half is observed!



One half is NOT observed!

# SUSY Lagrangians

*Superfields*

$$L_{SUSY \ YM} = \frac{1}{4} \int d^2\theta \text{ Tr}(W^\alpha W_\alpha) + \frac{1}{4} \int d^2\bar{\theta} \text{ Tr}(\bar{W}^\alpha \bar{W}_\alpha) \\ + \int d^2\theta d^2\bar{\theta} \Phi_{ia} (e^{gV})_b^a \Phi_i^b + \int d^2\theta W(\Phi_i) + \int d^2\bar{\theta} \bar{W}(\bar{\Phi}_i)$$

*Components*

$$L_{SUSY \ YM} = -\frac{1}{4} F_{\mu\nu}^a F^{a\mu\nu} - i\lambda^a \sigma^\mu D_\mu \bar{\lambda}^a + \frac{1}{2} D^a D^a \\ + (\partial_\mu A_i - igv_\mu^a T^a A_i)^\dagger (\partial_\mu A_i - igv_\mu^a T^a A_i) - i\bar{\psi}_i \bar{\sigma}^\mu (\partial_\mu \psi_i - igv_\mu^a T^a \psi_i) \\ - D^a g A_i^\dagger T^a A_i - i\sqrt{2} g A_i^\dagger T^a \lambda^a A + i\sqrt{2} g \bar{\psi}_i T^a \bar{\lambda}^a A_i + F_i^\dagger F_i \\ + \frac{\partial W}{\partial A_i} F_i + \frac{\partial \bar{W}}{\partial A_i^\dagger} F_i^\dagger - \frac{1}{2} \frac{\partial^2 W}{\partial A_i \partial A_j} \psi_i \psi_j - \frac{1}{2} \frac{\partial^2 \bar{W}}{\partial A_i^\dagger \partial A_j^\dagger} \bar{\psi}_i \bar{\psi}_j$$

*Potential*

$$D^a = -g A_i^\dagger T^a A_i, \quad F_i = -\frac{\partial W}{\partial A_i} \quad \rightarrow \quad V = \frac{1}{2} D^a D^a + F_i^\dagger F_i$$

# The MSSM Lagrangian

$$L = L_{gauge} + L_{Yukawa} + L_{SoftBreaking}$$

The Yukawa Superpotential

$$W_R = y_U Q_L H_2 U_R + y_D Q_L H_1 D_R + y_L L_L H_1 E_R + \mu H_1 H_2$$

Yukawa couplings

superfields

Higgs mixing term

$$W_{NR} = \lambda_L L_L L_L E_R + \lambda'_L L_L Q_L D_R + \mu' L_L H_2 + \lambda_B U_R D_R D_R$$

R-parity

$$R = (-)^{3(B-L)+2S}$$

B-Bartion Number

The Usual Particle : R= + 1

L-Lepton Number

SUSY Particle : R= - 1

S-Spin

# R-parity Conservation

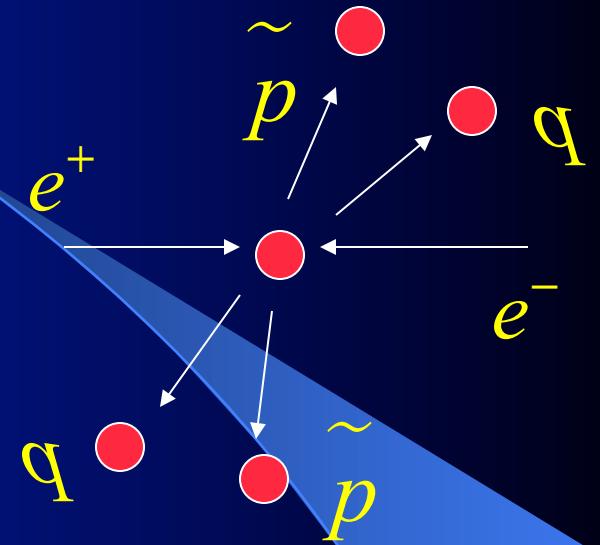
The consequences:

- The superpartners are created in pairs
- The lightest superparticle is stable



Physical output:

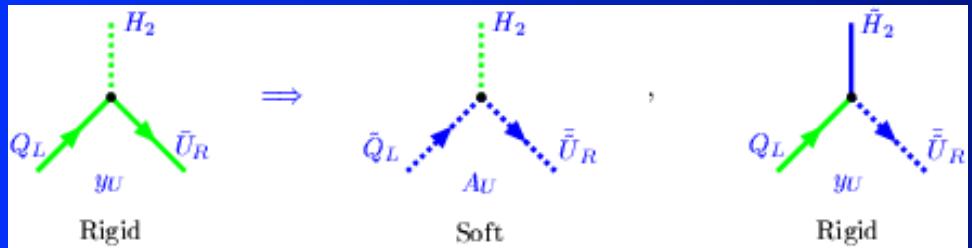
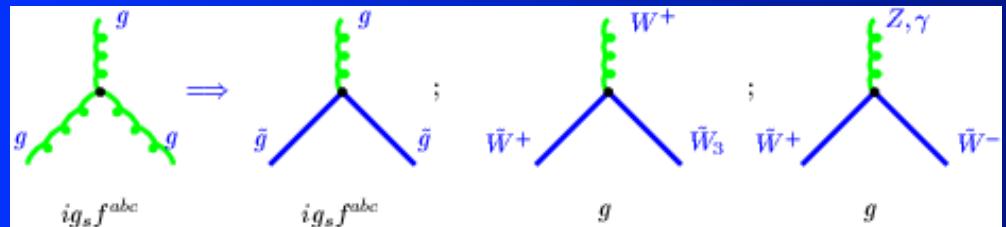
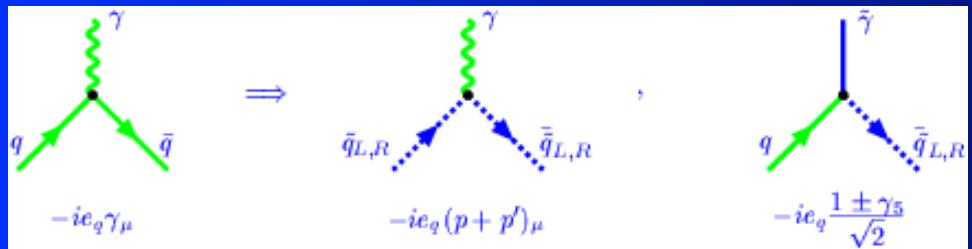
- The lightest superparticle (LSP)  $\tilde{\chi}_0$  should be neutral - the best candidate is neutralino (photino or higgsino)
- It can survive from the Big Bang and form the Dark matter in the Universe



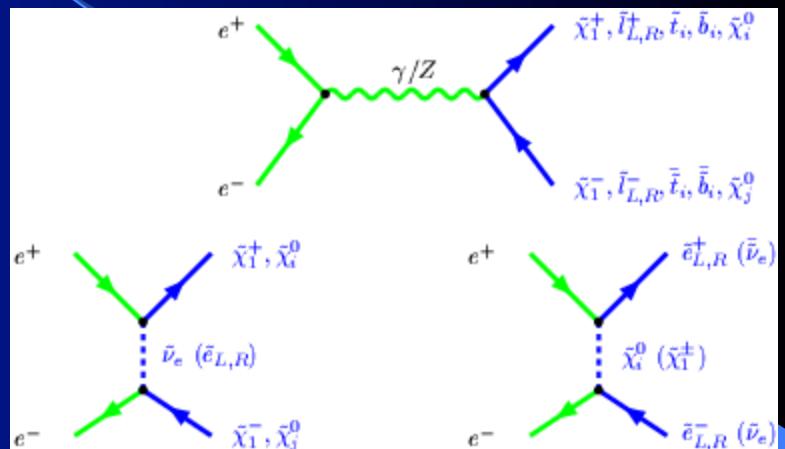
$\tilde{\chi}_0$   $\tilde{\chi}_0$

# Interactions in the MSSM

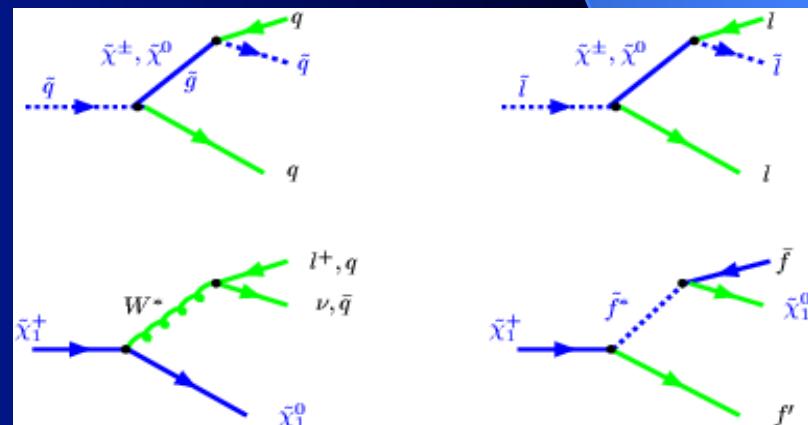
## Interaction Vertices



## Creation of superpartners

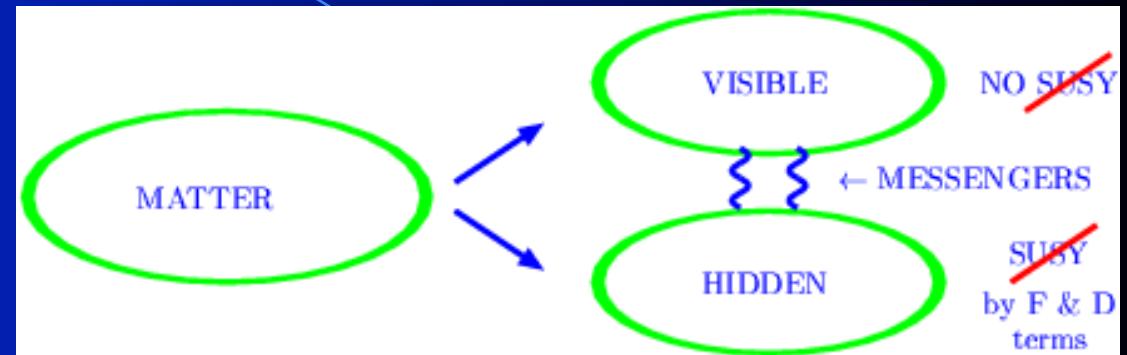


## Decay of superpartners



# Soft SUSY Breaking

Hidden Sector Scenario:



SUGRA

$$\begin{aligned} -L_{Soft} = & A \{ y_t Q_L H_2 U_R + y_b Q_L H_1 D_R + y_L L_L H_1 E_R \} + B \mu H_1 H_2 \\ & + m_0^2 \sum_i |\varphi_i|^2 + \frac{1}{2} M_{1/2} \sum_\alpha \tilde{\lambda}_\alpha \tilde{\lambda}_\alpha \end{aligned}$$

The Universal  
Soft Parameters:

Versus

$A, B, m_0, M_{1/2}$  and  $\mu$   
 $m$  and  $\lambda$  in the SM

# Mass Spectrum

$$L_{gaugino-Higgsino} = -\frac{1}{2} M_3 \bar{\lambda}_a \lambda_a - \frac{1}{2} \bar{\chi} M^{(0)} \chi - (\bar{\psi} M^{(c)} \psi + h.c.)$$

$$M^{(0)} = \begin{pmatrix} M_1 & 0 & -M_Z \cos \beta \sin W & M_Z \sin \beta \sin W \\ 0 & M_2 & M_Z \cos \beta \cos W & -M_Z \sin \beta \cos W \\ -M_Z \cos \beta \sin W & M_Z \cos \beta \cos W & 0 & -\mu \\ M_Z \sin \beta \sin W & -M_Z \sin \beta \cos W & -\mu & 0 \end{pmatrix}$$

$$\chi = \begin{pmatrix} \tilde{B}^0 \\ \tilde{W}^3 \\ \tilde{H}_1^0 \\ \tilde{H}_2^0 \end{pmatrix}$$

$$M^{(c)} = \begin{pmatrix} M_2 & \sqrt{2} M_W \sin \beta \\ \sqrt{2} M_W \cos \beta & \mu \end{pmatrix}$$

$$\psi = \begin{pmatrix} \tilde{W}^+ \\ \tilde{H}^+ \end{pmatrix}$$

Neutralino

Chargino

Squarks & Sleptons

$$\tilde{m}_t^2 = \begin{pmatrix} \tilde{m}_{tL}^2 & m_t(A_t - \mu \cot \beta) \\ m_t(A_t - \mu \cot \beta) & \tilde{m}_{tR}^2 \end{pmatrix}$$

$$\tilde{m}_b^2 = \begin{pmatrix} \tilde{m}_{bL}^2 & m_b(A_b - \mu \tan \beta) \\ m_b(A_b - \mu \tan \beta) & \tilde{m}_{bR}^2 \end{pmatrix}$$

$$\tilde{m}_\tau^2 = \begin{pmatrix} \tilde{m}_{\tau L}^2 & m_\tau(A_\tau - \mu \tan \beta) \\ m_\tau(A_\tau - \mu \tan \beta) & \tilde{m}_{\tau R}^2 \end{pmatrix}$$

$$\tilde{m}_{tL}^2 = \tilde{m}_Q^2 + m_t^2 + \frac{1}{6}(4M_W^2 - M_Z^2)\cos 2\beta,$$

$$\tilde{m}_{tR}^2 = \tilde{m}_U^2 + m_t^2 - \frac{2}{3}(M_W^2 - M_Z^2)\cos 2\beta,$$

$$\tilde{m}_{bL}^2 = \tilde{m}_Q^2 + m_b^2 - \frac{1}{6}(2M_W^2 + M_Z^2)\cos 2\beta,$$

$$\tilde{m}_{bR}^2 = \tilde{m}_D^2 + m_b^2 + \frac{1}{3}(M_W^2 - M_Z^2)\cos 2\beta,$$

$$\tilde{m}_{\tau L}^2 = \tilde{m}_L^2 + m_\tau^2 - \frac{1}{2}(2M_W^2 - M_Z^2)\cos 2\beta,$$

$$\tilde{m}_{\tau R}^2 = \tilde{m}_E^2 + m_\tau^2 + (M_W^2 - M_Z^2)\cos 2\beta.$$

# SUSY Higgs Bosons

SM

$$H = \begin{pmatrix} H^0 \\ H^- \end{pmatrix} = \begin{pmatrix} v + \frac{S + iP}{\sqrt{2}} \\ H^- \end{pmatrix} = \exp(i \frac{\vec{\xi} \vec{\sigma}}{2}) \begin{pmatrix} v + \frac{S}{\sqrt{2}} \\ 0 \end{pmatrix}$$

$$H \rightarrow H' = \exp(i \frac{\vec{\alpha} \vec{\sigma}}{2}) H \xrightarrow{(\vec{\alpha} = -\vec{\xi})} H' = \begin{pmatrix} v + \frac{S}{\sqrt{2}} \\ 0 \end{pmatrix}$$

$$H_1 = \begin{pmatrix} H_1^0 \\ H_1^- \end{pmatrix} = \begin{pmatrix} v_1 + \frac{S_1 + iP_1}{\sqrt{2}} \\ H_1^- \end{pmatrix}, \quad H_2 = \begin{pmatrix} H_2^+ \\ H_2^0 \end{pmatrix} = \begin{pmatrix} H_2^+ \\ v_2 + \frac{S_2 + iP_2}{\sqrt{2}} \end{pmatrix},$$

$$v_1^2 + v_2^2 = v^2, \quad v_2/v_1 \equiv \tan\beta$$

MSSM

$$G^0 = -\cos\beta P_1 + \sin\beta P_2$$

*Goldstone boson  $\rightarrow Z_0$*

$$A = \sin\beta P_1 + \cos\beta P_2$$

*Neutral CP = -1 Higgs*

$$G^+ = -\cos\beta (H_1^-)^* + \sin\beta H_2^+$$

*Goldstone boson  $\rightarrow W^+$*

$$H^+ = \sin\beta (H_1^-)^* + \cos\beta H_2^+$$

*Charged Higgs*

$$h = -\sin\alpha S_1 + \cos\alpha S_2$$

*SM Higgs boson CP = 1*

$$H = \cos\alpha S_1 + \sin\alpha S_2$$

*Extra heavy Higgs boson*

$$\tan 2\alpha = \tan 2\beta \frac{m_A^2 + m_Z^2}{m_A^2 - m_Z^2}$$

# The Higgs Potential

$$V_{tree}(H_1, H_2) = m_1^2 |H_1|^2 + m_2^2 |H_2|^2 - m_3^2 (H_1 H_2 + h.c.) \\ + \frac{g^2 + g'^2}{8} (|H_1|^2 - |H_2|^2)^2 + \frac{g^2}{2} |H_1^+ H_2^-|^2$$

At the GUT scale:  $m_1^2 = m_2^2 = \mu_0^2 + m_0^2$ ,  $m_3^2 = -B\mu_0$

Minimization

$$\frac{1}{2} \frac{\delta V}{\delta H_1} = m_1^2 v_1 - m_3^2 v_2 + \frac{g^2 + g'^2}{4} (v_1^2 - v_2^2) v_1 = 0,$$

$$\frac{1}{2} \frac{\delta V}{\delta H_2} = m_2^2 v_2 - m_3^2 v_1 - \frac{g^2 + g'^2}{4} (v_1^2 - v_2^2) v_2 = 0.$$

$$\langle H_1 \rangle \equiv v_1 = v \cos \beta, \quad \langle H_2 \rangle \equiv v_2 = v \sin \beta,$$

Solution

$$v^2 = \frac{4(m_1^2 - m_2^2 \tan^2 \beta)}{(g^2 + g'^2)(\tan^2 \beta - 1)}, \quad \sin 2\beta = \frac{2m_3^2}{m_1^2 + m_2^2}$$

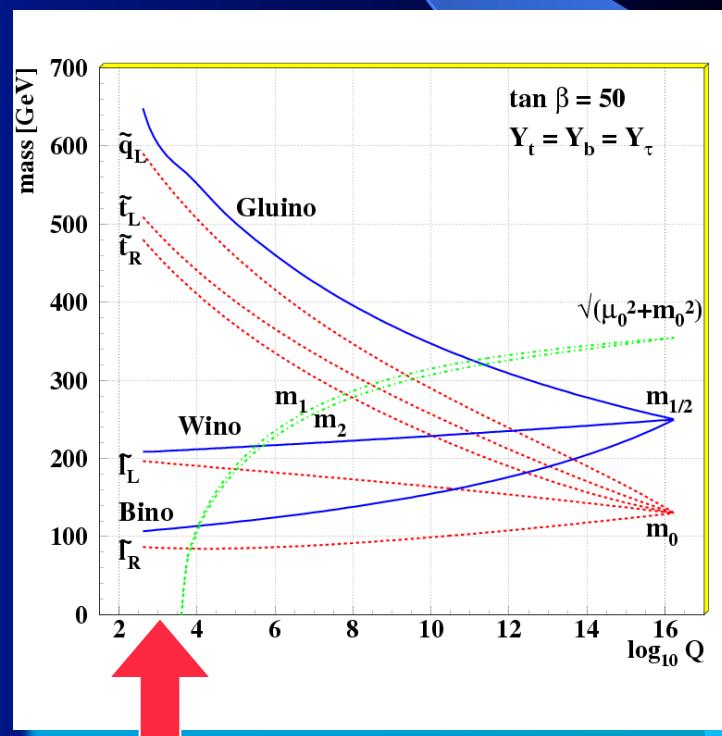
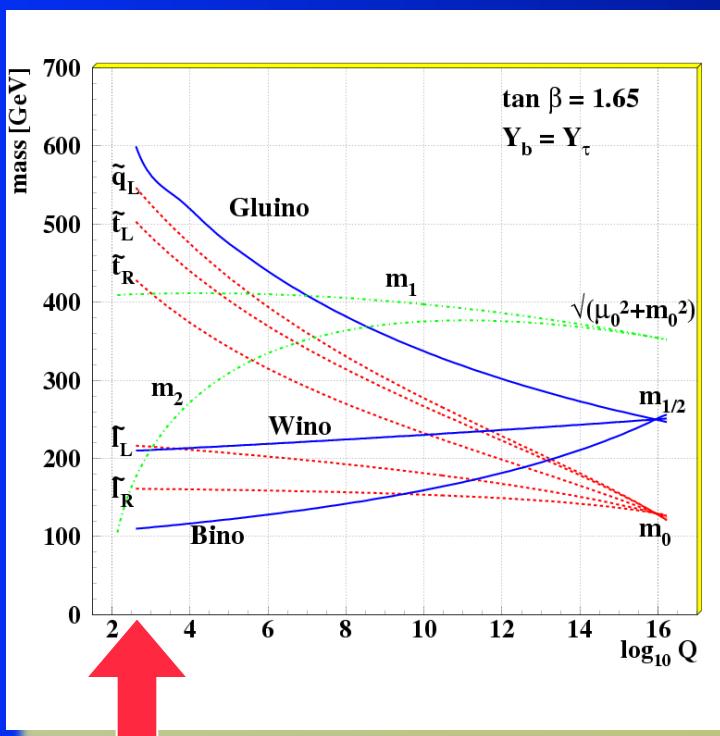
At the GUT scale

$$v^2 = -\frac{4}{g^2 + g'^2} m^2 < 0$$

No SSB in SUSY theory !

# Radiative EW Symmetry Breaking

Due to RG controlled running of the mass terms from the Higgs potential they may change sign and trigger the appearance of non-trivial minimum leading to spontaneous breaking of EW symmetry - this is called Radiative EWSB



# Constrained MSSM

Requirements:

- Unification of the gauge couplings
- Radiative EW Symmetry Breaking
- Heavy quark and lepton masses
- Rare decays ( $b \rightarrow s\gamma$ )
- Anomalous magnetic moment of muon
- LSP is neutral
- Amount of the Dark Matter
- Experimental limits from direct search



Allowed region  
in the parameter  
space of the MSSM

$$A_0, m_0, M_{1/2}, \mu, \tan \beta$$

$$100 \text{ Gev} < m_0, M_{1/2}, \mu < 2 \text{ Tev}$$

Parameter space:

$$-3m_0 < A_0 < 3m_0, 1 < \tan \beta < 70$$

# SUSY Fits

$$\chi^2 = \sum_{i=1}^3 \frac{(\alpha_i^{-1}(M_Z) - \alpha_{MSSMi}^{-1}(M_Z))^2}{\sigma_i^2}$$

$$+ \frac{(M_Z - 91.18)^2}{\sigma_Z^2} + \frac{(M_t - 174)^2}{\sigma_t^2}$$

$$+ \frac{(M_b - 4.94)^2}{\sigma_b^2} + \frac{(M_\tau - 1.7771)^2}{\sigma_\tau^2}$$

$$+ \frac{(\text{Br}(b \rightarrow s\gamma) - 3.14 \times 10^{-4})^2}{\sigma^2(b \rightarrow s\gamma)}$$

$$+ \frac{(\Omega h^2 - 1)^2}{\sigma_\Omega^2} \quad (\text{for } \Omega h^2 > 1)$$

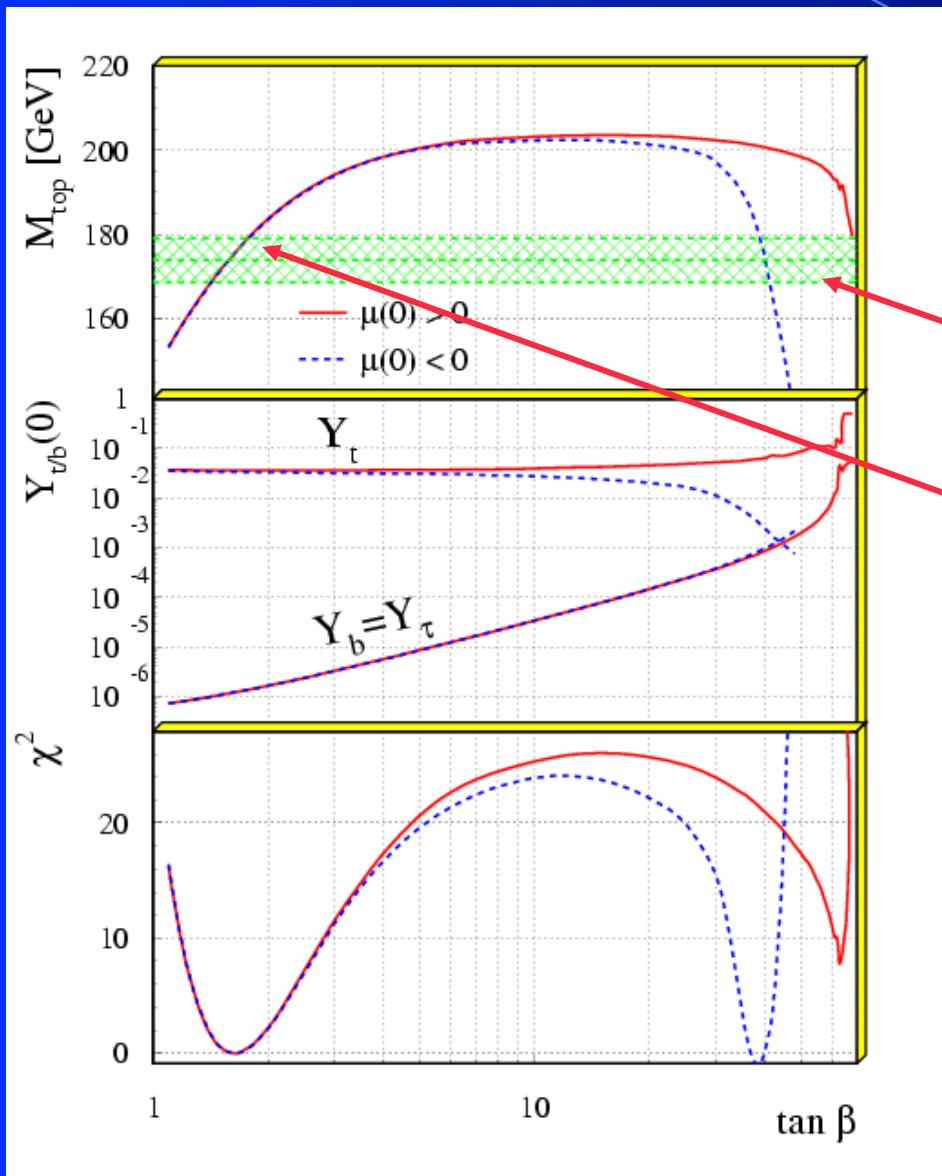
$$+ \frac{(\tilde{M} - \tilde{M}_{\text{exp}})^2}{\sigma_{\tilde{M}}^2} \quad (\text{for } \tilde{M} < \tilde{M}_{\text{exp}})$$

$$+ \frac{(\tilde{m}_{\text{LSP}} - \tilde{m}_\chi)^2}{\sigma_{\text{LSP}}^2} \quad (\text{for } \tilde{m}_{\text{LSP}} \text{ charged})$$

Minimize  $\chi^2$

Exp.input data	Fit low $\tan \tilde{\chi}$	Parameters high $\tan \tilde{\chi}$
$\alpha_1, \alpha_2, \alpha_3$	$M_{GUT}, \alpha_{GUT}$	$M_{GUT}, \alpha_{GUT}$
$m_t$	$Y_t^0, Y_b^0 = Y_\tau^0$	$Y_t^0 = Y_b^0 = Y_\tau^0$
$m_b$	$m_0, m_{1/2}$	$m_0, m_{1/2}$
$m_\tau$	$\tan \beta$	$\tan \beta$
$M_Z$	$\mu$	$\mu$
$b \rightarrow s\gamma$	$(A_0)$	$A_0$
$\tau_{\text{Universe}}$		

# Low and High $\tan\beta$ Solutions



Requirements:

- EWSB
- $b\tau$  unification

Low  $\tan\beta$   
solution

High  $\tan\beta$   
solution

- $b\tau$  unification is the consequence of GUT
- Non working for the light generations

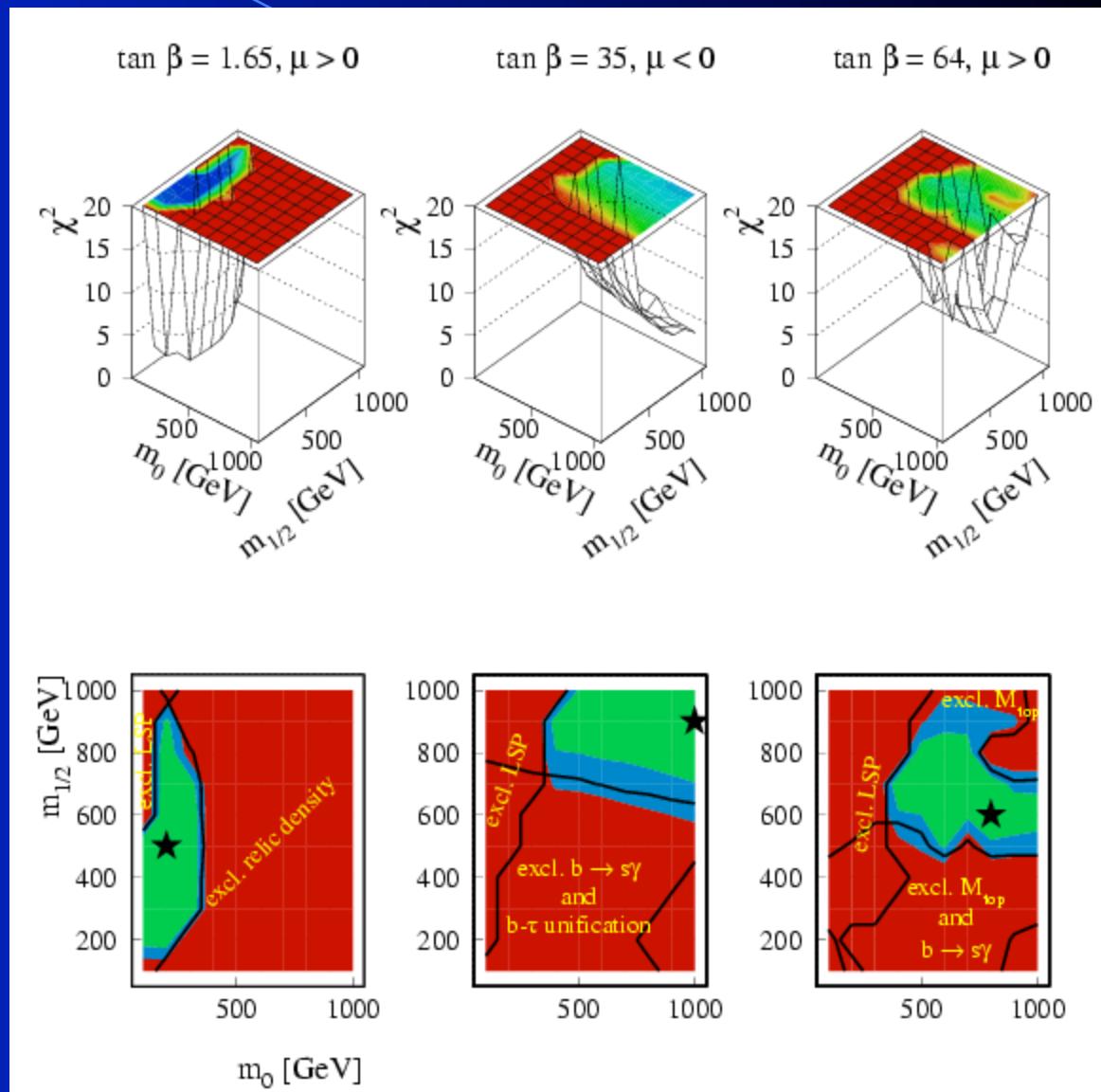
# Allowed Regions in Parameter Space

All the requirements  
are fulfilled  
simultaneously !

- $\mu$  is defined from the EWSB

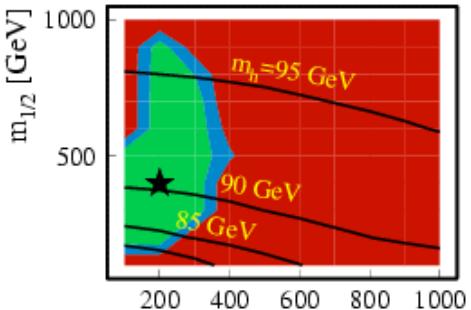
- $A_0 = 0$

\* - is the best fit value

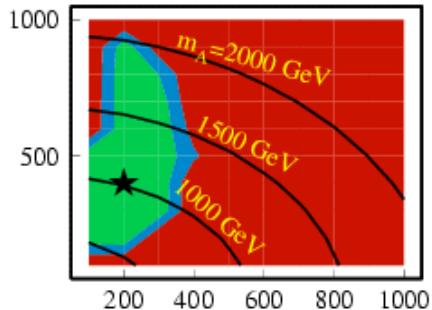


# Masses of Superpartners

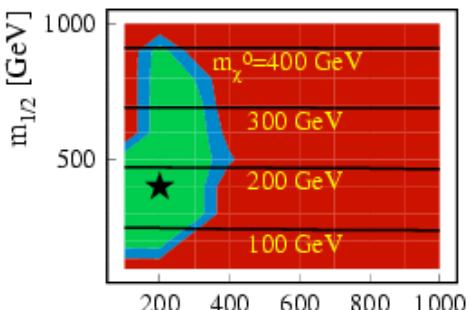
$\tan \beta = 1.65, \mu > 0$



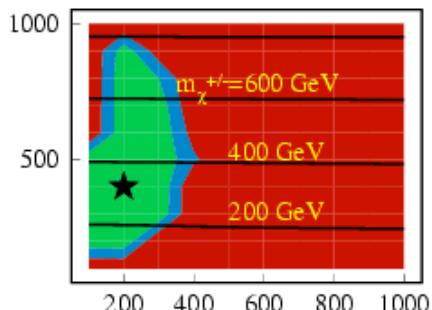
$h$



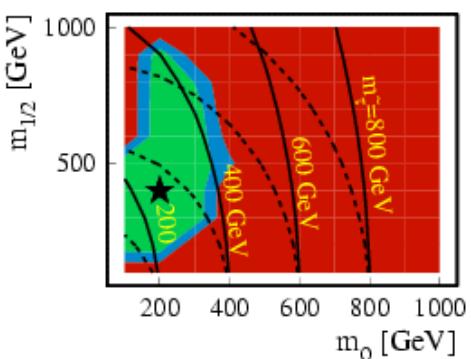
$A, H$



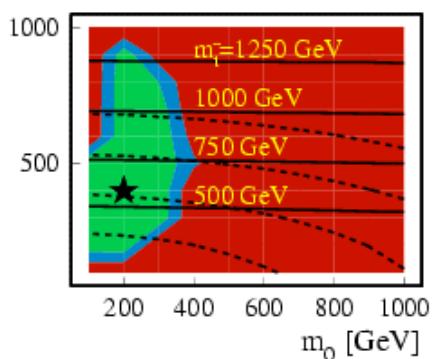
$\chi_0^0$  LSP



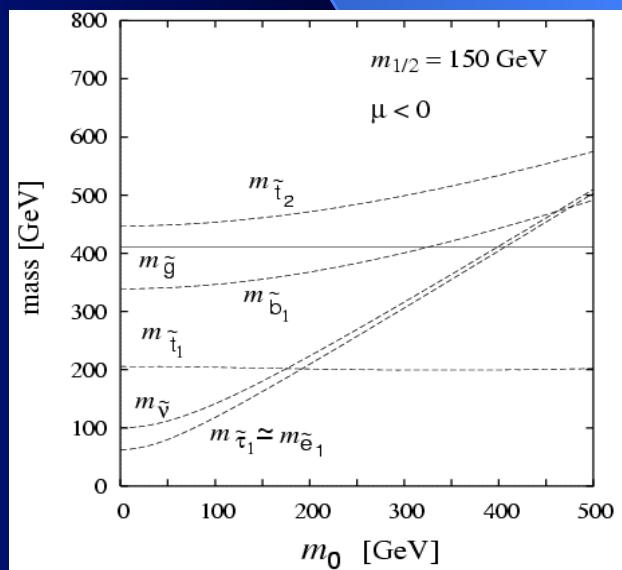
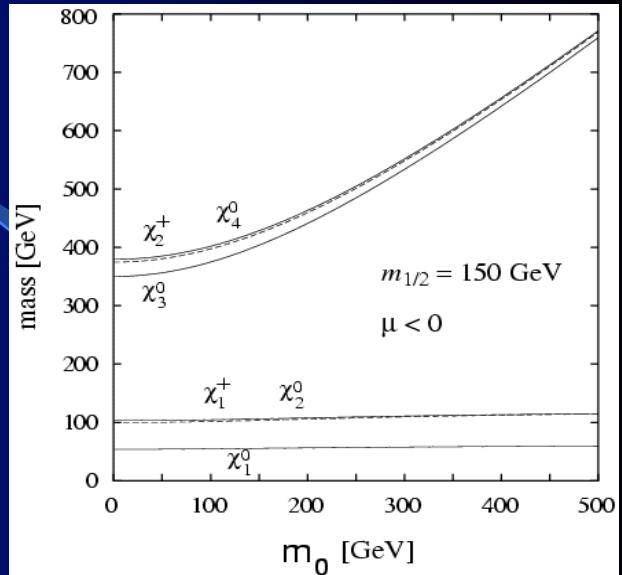
$\chi^{+/-}$



$\tilde{\tau}$



$\tilde{t}$



# Mass Spectrum in CMSSM

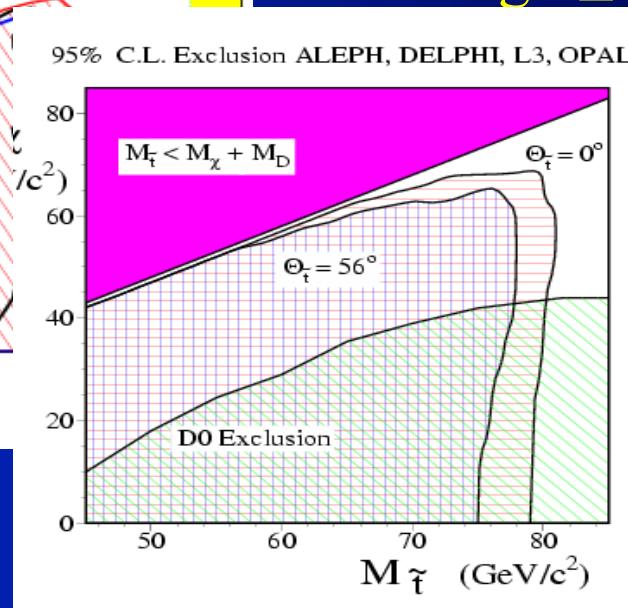
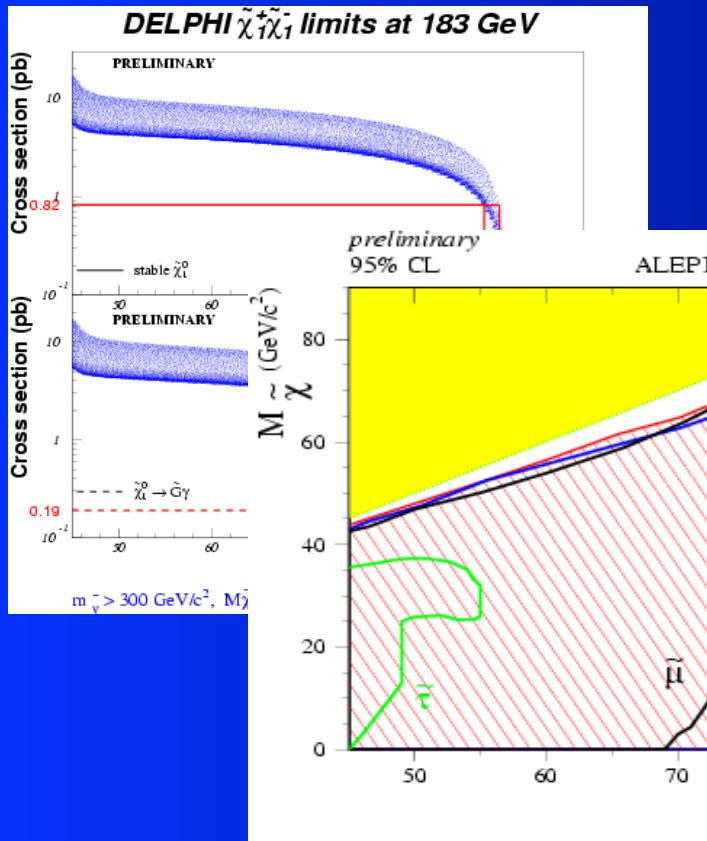
## Fitted SUSY Parameters

Symbol	Low tan $\beta$	High tan $\beta$
Tan $\beta$	1.71	35.0
$m_0$	200	600
$m_{1/2}$	500	400
$\mu(0)$	1084	-558
$A(0)$	0	0
$1/\alpha_{\text{GUT}}$	24.8	24.8
$M_{\text{GUT}}$	$1.6 \cdot 10^{16}$	$1.6 \cdot 10^{16}$

## SUSY Masses in GeV

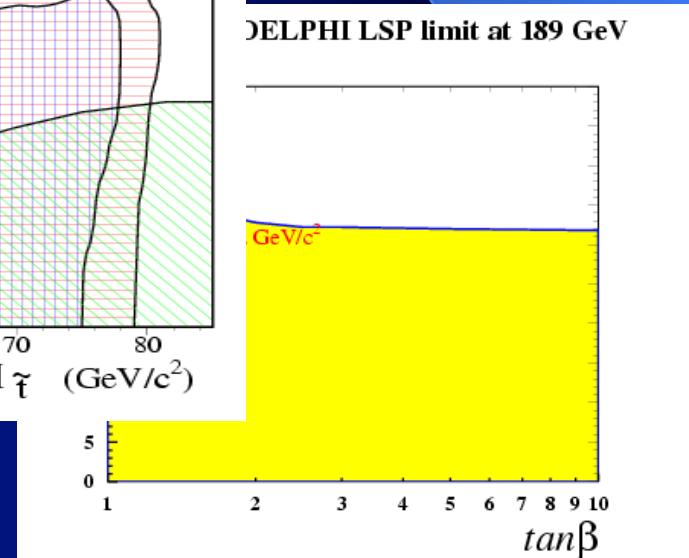
Symbol	Low tan $\beta$	High tan $\beta$
$\tilde{\chi}_1^0(\tilde{B}), \tilde{\chi}_2^0(\tilde{W}^3)$	214, 413	170, 322
$\tilde{\chi}_3^0(\tilde{H}_1), \tilde{\chi}_4^0(\tilde{H}_2)$	1028, 1016	481, 498
$\tilde{\chi}_1^\pm(\tilde{W}^\pm), \tilde{\chi}_2^\pm(\tilde{H}^\pm)$	413, 1026	322, 499
$\tilde{g}$	1155	950
$\tilde{e}_L, \tilde{e}_R$	303, 270	663, 621
$\tilde{\nu}_L$	290	658
$\tilde{q}_L, \tilde{q}_R$	1028, 936	1040, 1010
$\tilde{\tau}_1, \tilde{\tau}_2$	279, 403	537, 634
$\tilde{b}_1, \tilde{b}_2$	953, 1010	835, 915
$\tilde{t}_1, \tilde{t}_2$	727, 1017	735, 906
$h, H$	95, 1344	119, 565
$A, H^\pm$	1340, 1344	565, 571

# SUSY Searches



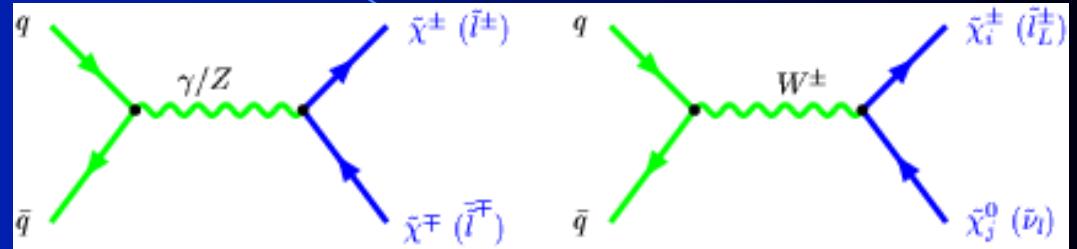
$M_{\tilde{q}} \geq 300 \text{ GeV}$   
 $m_{\tilde{l}} \geq 100 \text{ GeV}$

$m\tilde{\chi}^+ \geq 100 \text{ GeV}$   
 $m\tilde{\chi}^0 \geq 40 \text{ GeV}$   
 $m\tilde{g} \geq 300 \text{ GeV}$



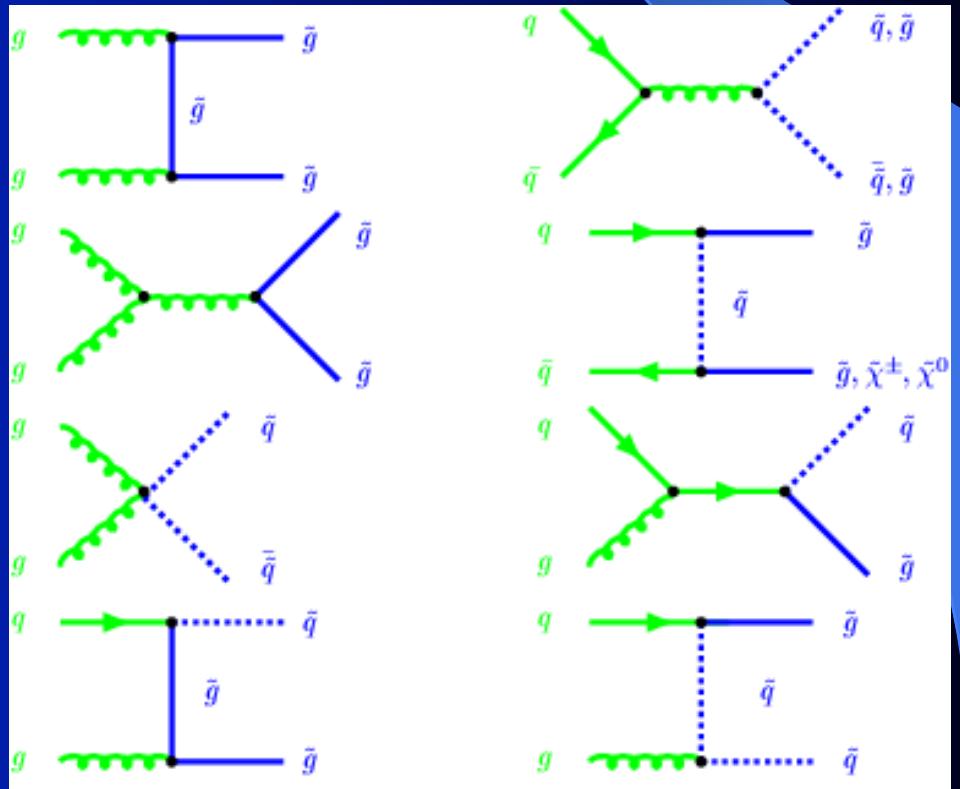
# SUSY Production at Hadron Colliders

Annihilation channel

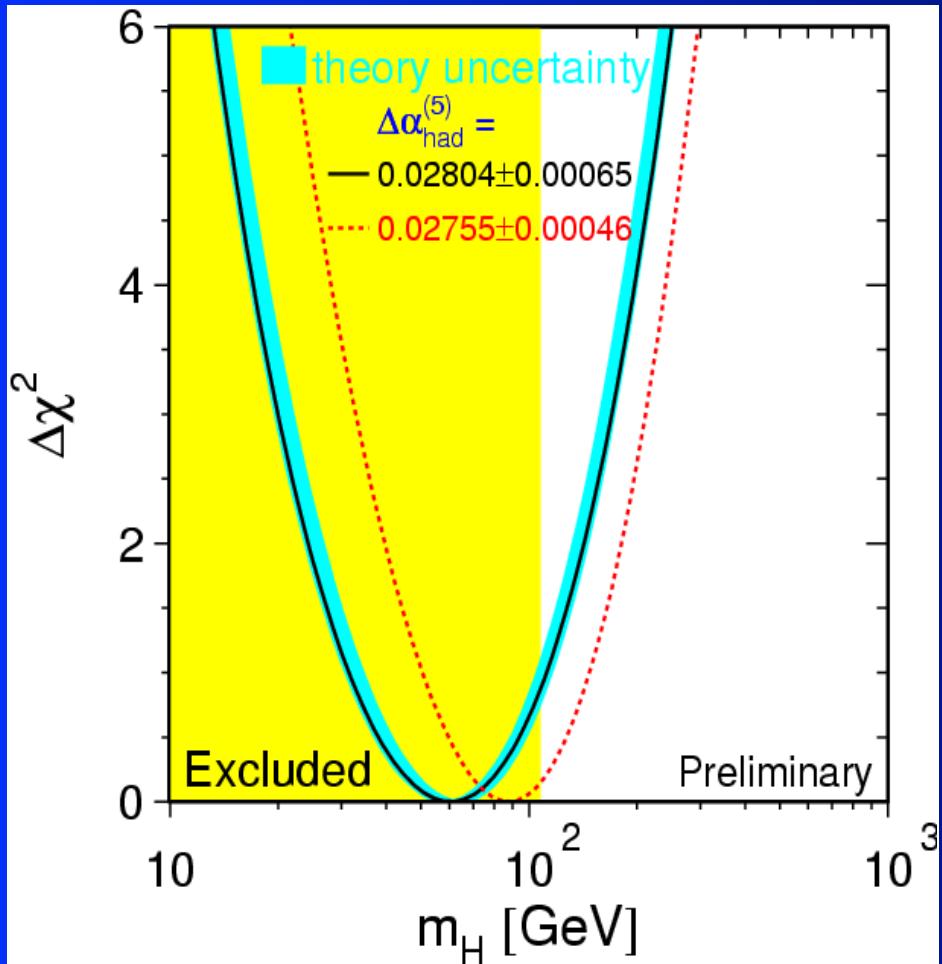


Gluon fusion, qq scattering  
and qg scattering channels

No new data so far due to  
insufficient luminosity  
at the Tevatron



# The Higgs Mass Limit

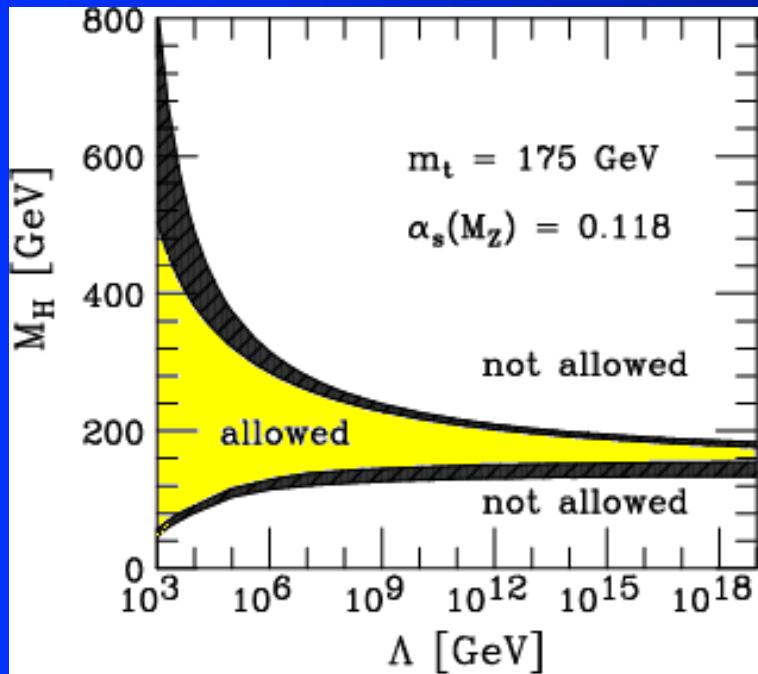


- Indirect limit from radiative corrections
- Direct limit from Higgs non-observation at LEP II (CERN)

$113 < m_H < 200$  GeV

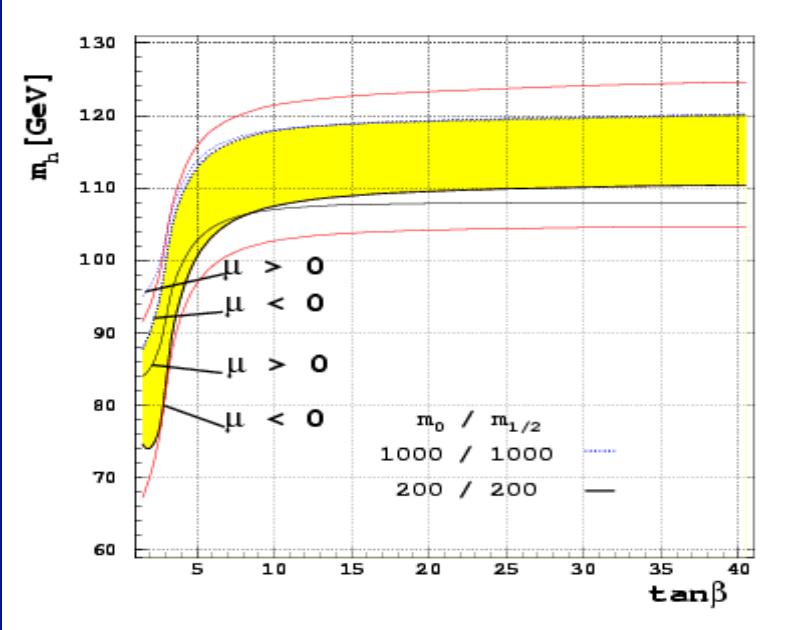
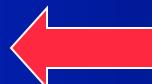
At 95 % C.L.

# The Higgs Mass Limit (Theory)

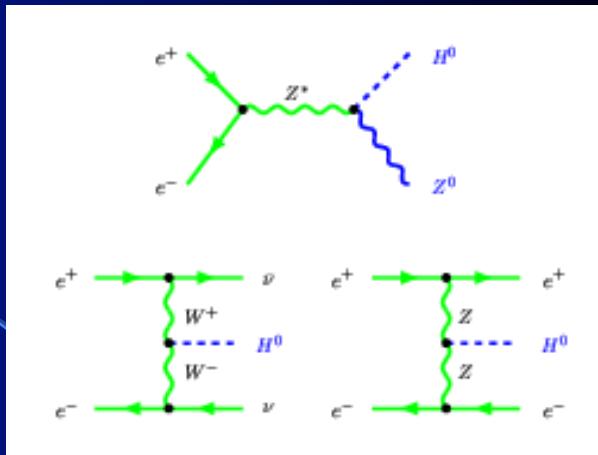
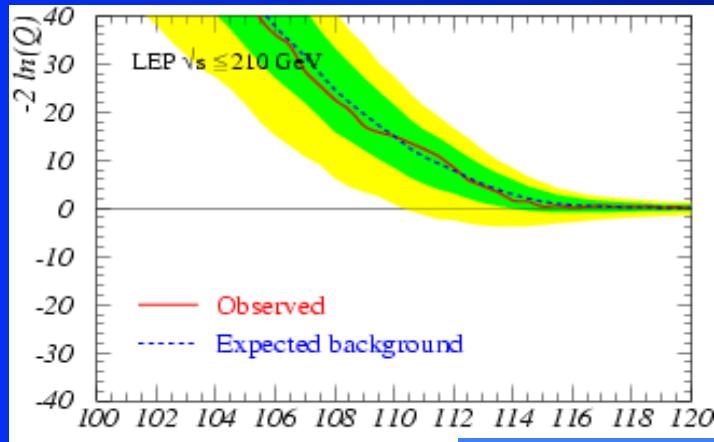


- The SM Higgs  
 $m_H \geq 134$  GeV

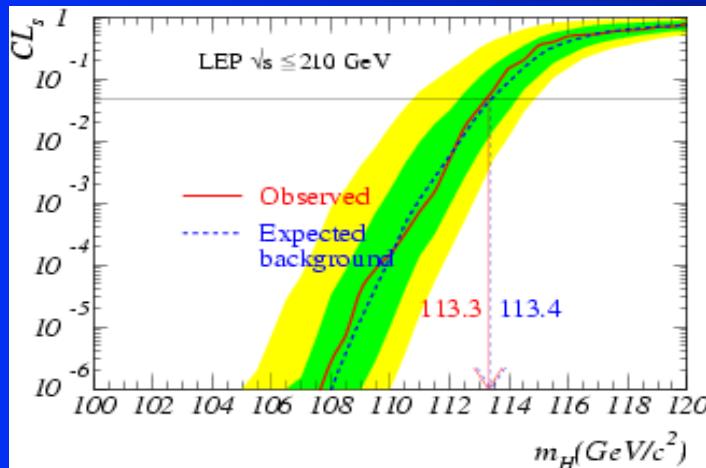
SUSY Higgs  
 $m_H \leq 130$  GeV



# Higgs Searches

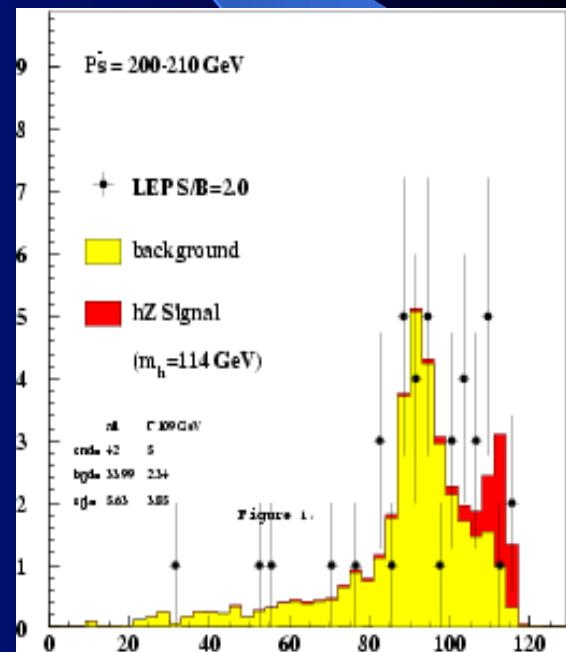


$m_H \geq 113.4$  GeV at  
95 % C.L.



114 -115 GeV  
Event

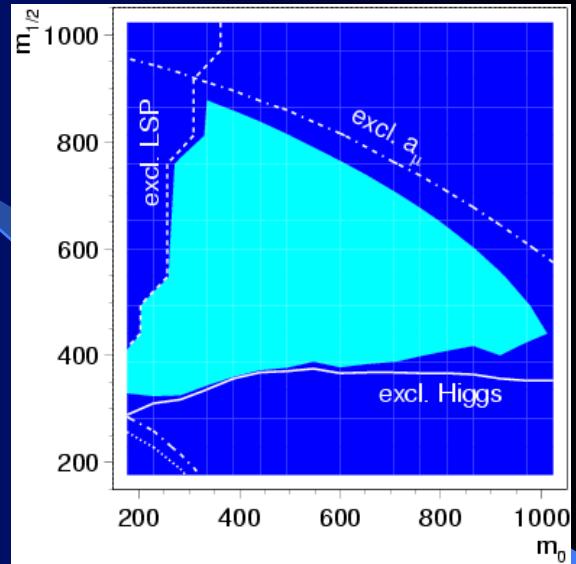
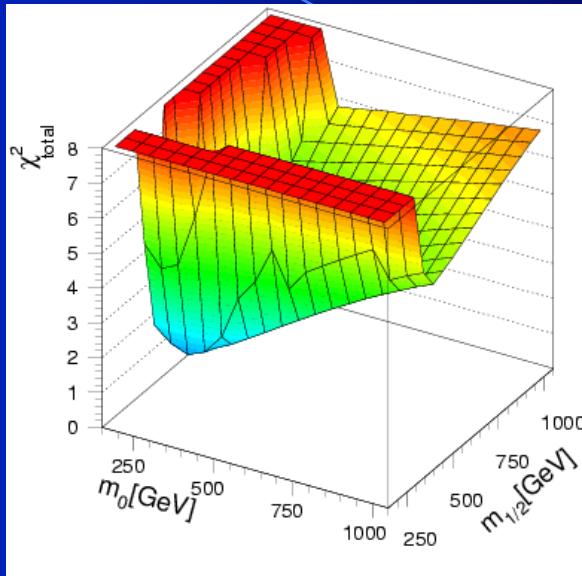
← →



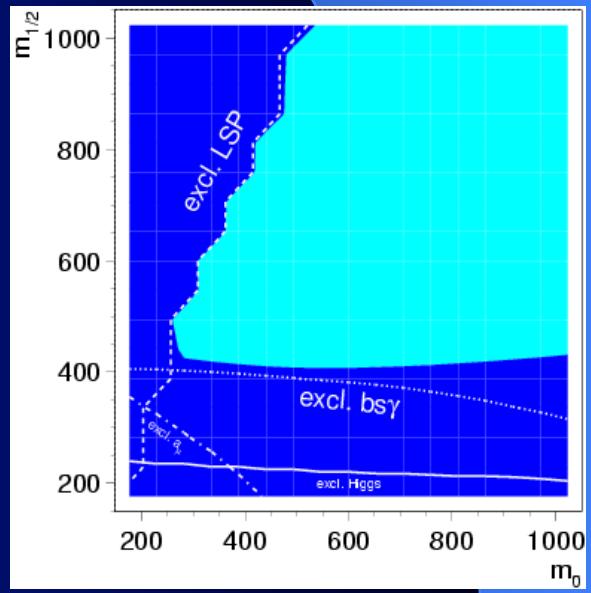
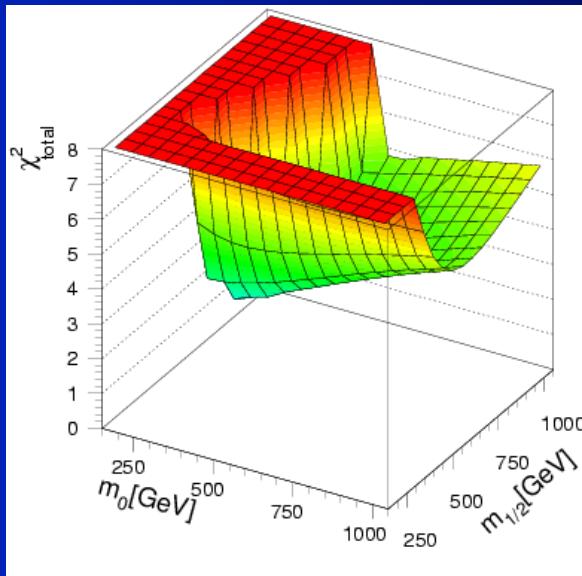
# Allowed Regions Renewed

- $\tan \beta > 4$  from the Higgs limit at LEP
- $\mu > 0$  from  $a_\mu$

$\tan \beta = 35$



$\tan \beta = 50$



# Cosmological Constraints

New precise cosmological data

$$\Omega h^2 = 1 \longleftrightarrow \rho = \rho_{crit}$$

$$\Omega_{vacuum} \approx 73\%$$

$$\Omega_{DarkMatter} \approx 23 \pm 4\%$$

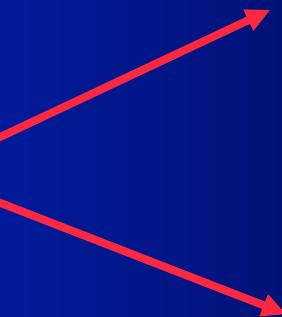
$$\Omega_{Baryon} \approx 4\%$$

Dark Matter in the Universe:



- Supernova Ia explosion
- CMBR thermal fluctuations  
(recent news from WMAP )

Hot DM  
(not favoured by  
galaxy formation)

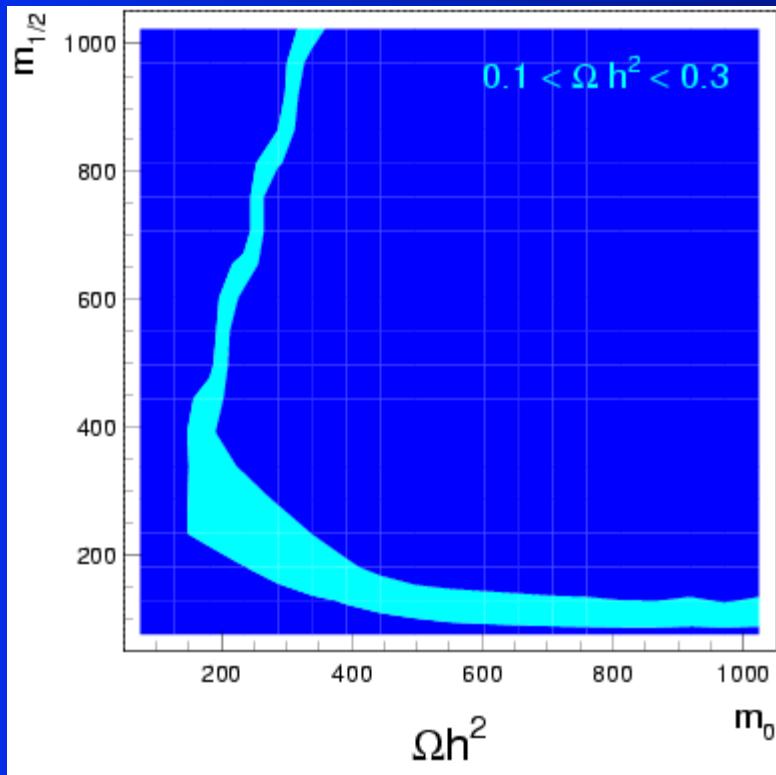


Cold DM  
(rotation curves  
of Galaxies)

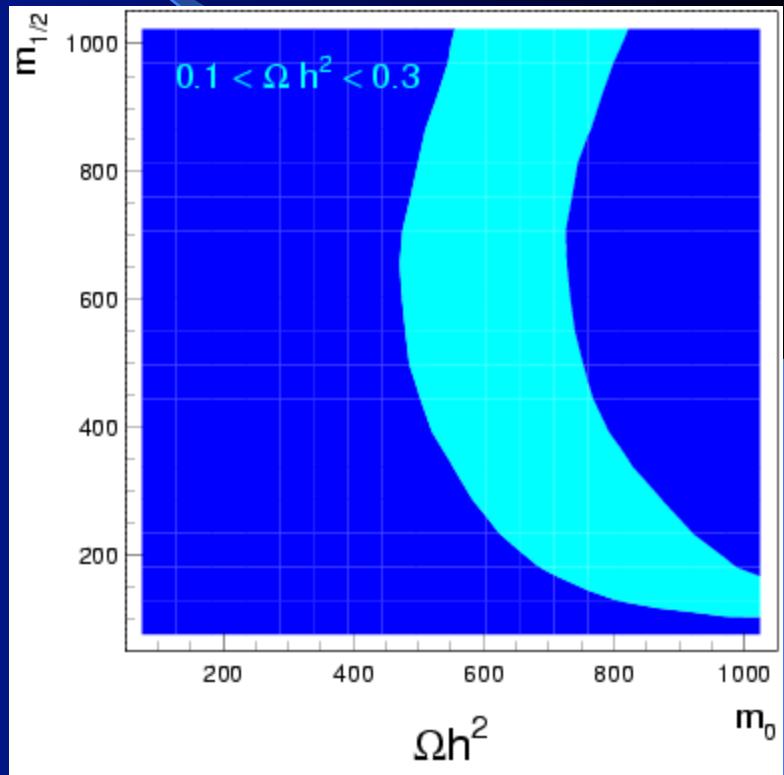


# SUSY Fits to Dark Matter

Results in severe constraints on parameter space



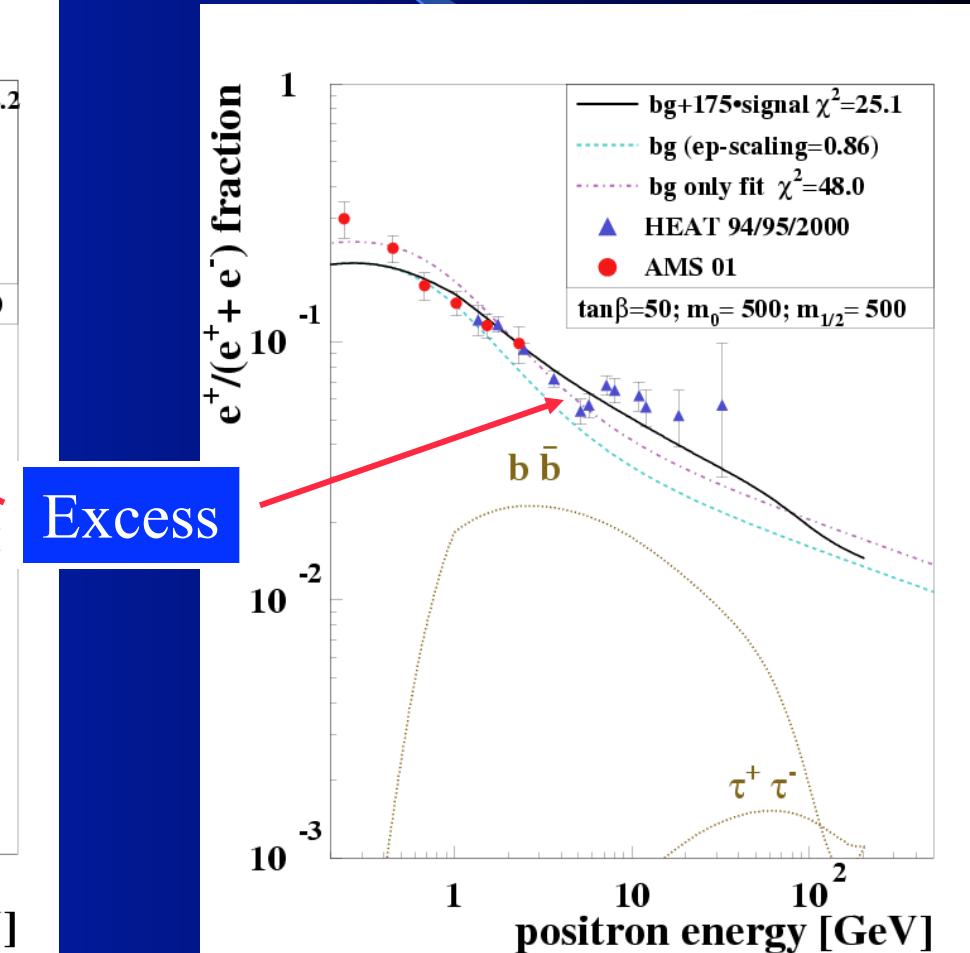
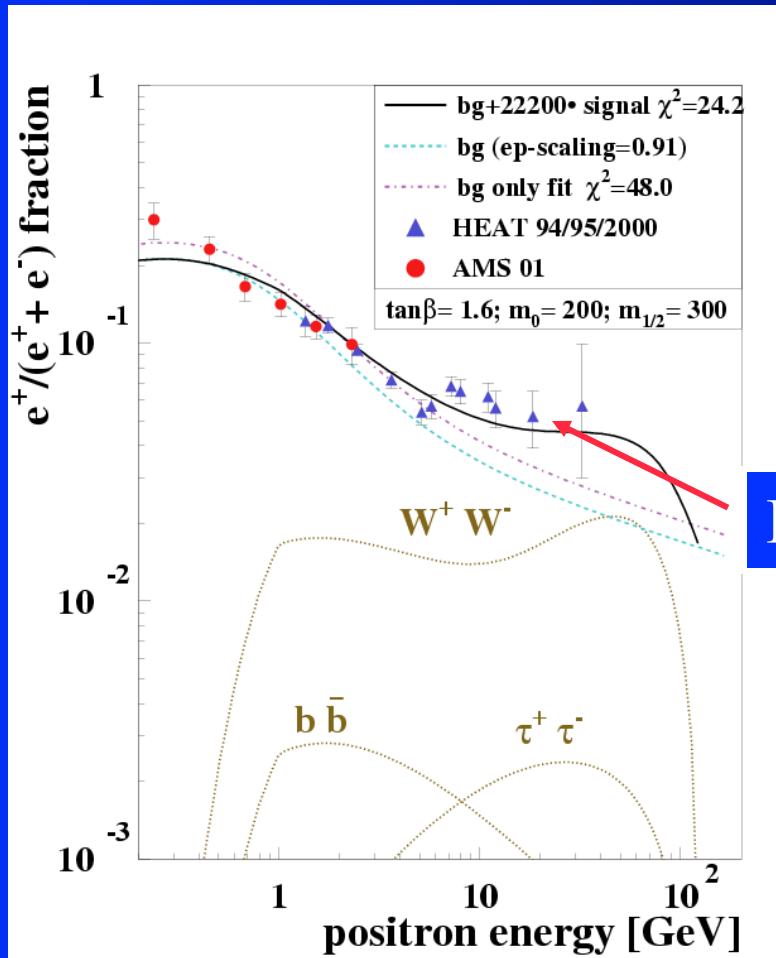
$\tan \beta = 35$



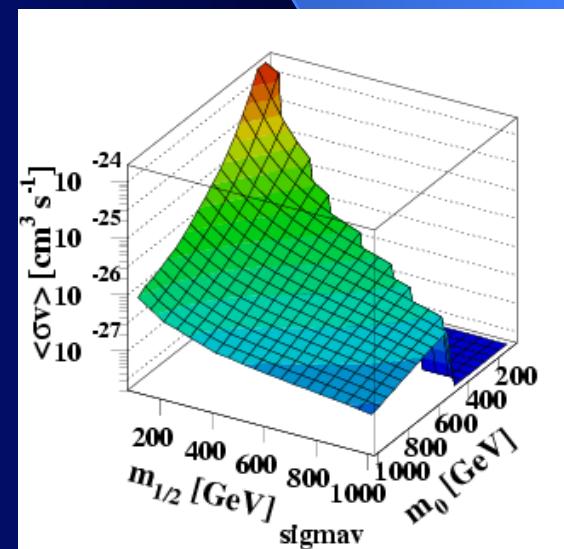
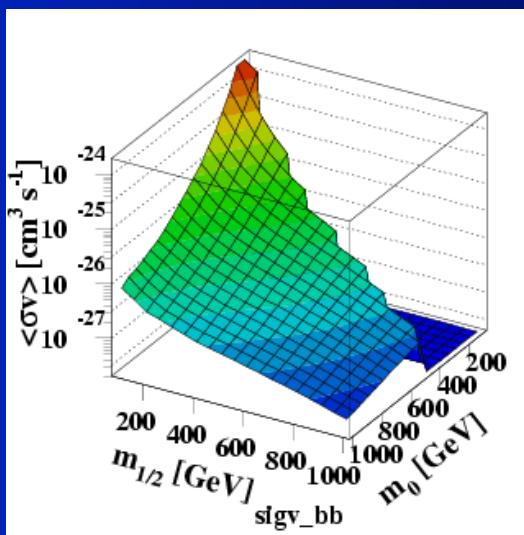
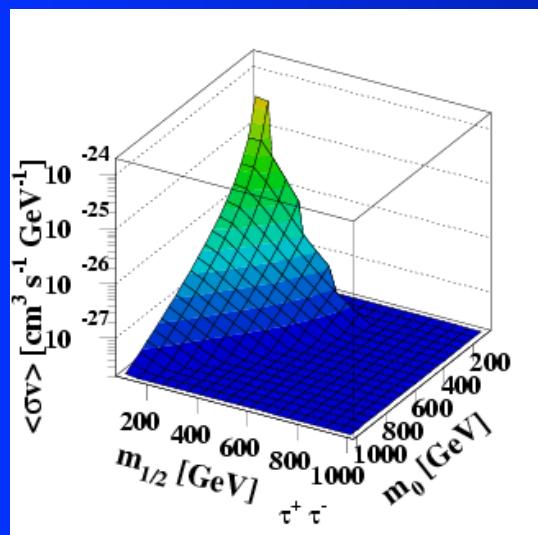
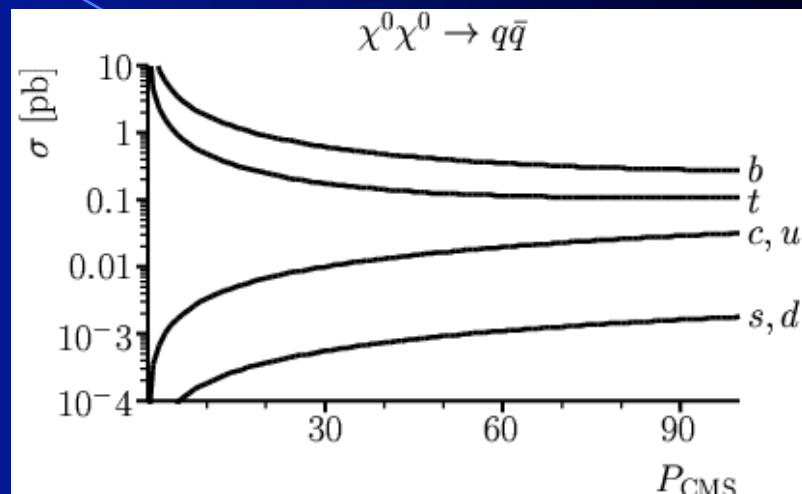
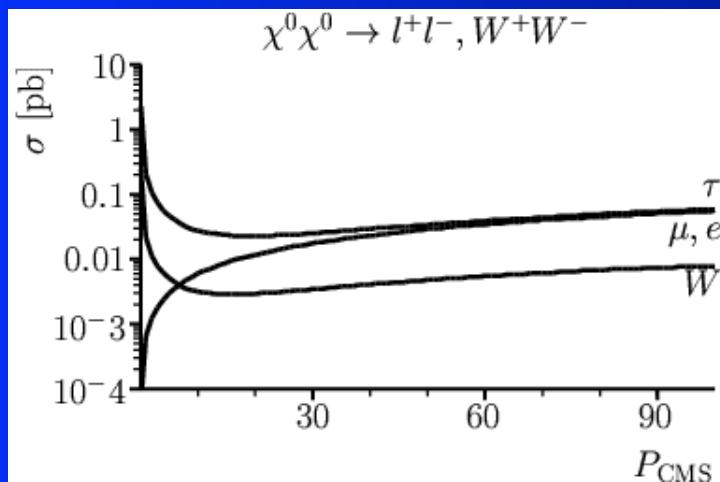
$\tan \beta = 50$

# SUSY Search in Space

Cosmic ray spectrum at high energies



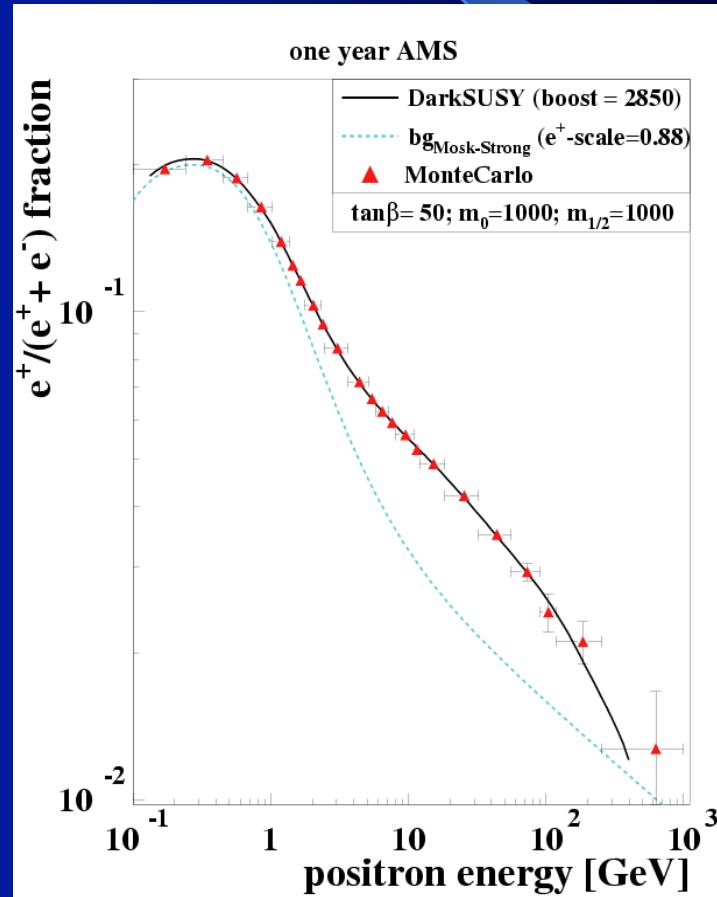
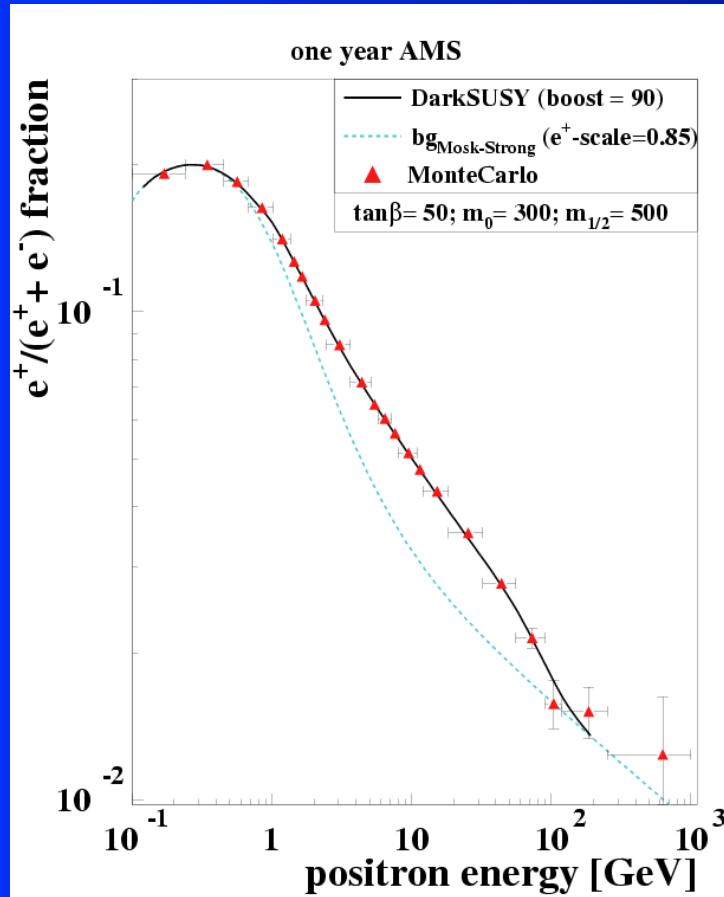
# Positrons from Neutralinos of the Dark Matter



# AMS – Antimatter Search in Space at ISS



Will be able to check SUSY Dark matter predictions



# Superparticles



The **SPDG** is an international collaboration that reviews Sparticle Physics and related areas of Astrophysics, and compiles/analyzes data on particle properties. SPDG products are distributed to 130,000 physicists, teachers, and other interested people. The Review of Sparticle Physics is the most cited publication in particle physics during the last twenty years. Plots of [SPDG statistics](#) are available.

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[Review of Sparticle Physics](#) [Charts, Educational materials, Sparticle Adventure](#) [Information and Databases](#)  
[US-HIPFCOLK](#) [Particle Physics: Twenty Years of Discoveries](#) [Home Pages of major HEP labs](#)

## The Review of Sparticle Physics

[C. Caso \*et al.\*, The European Physical Journal C103 \(2018\) 1 \(2018 Authors\)](#)

●	2019	<a href="#">2019 Web update of Reviews, Tables, Plots</a>	New November 2, 2019
●	2019	<a href="#">2019 Web update of Sparticle Listings</a>	New July 6, 2019
●	2018	<a href="#">2018 Summary Tables and Conservation Laws</a> <a href="#">2018 Reviews, Tables, Plots (incl. Intro. Text)</a> <a href="#">2018 Sparticle Listings (published version)</a>	Superseded by <a href="#">2019 Web Version</a> Superseded by <a href="#">2019 Web Version</a>
●		<a href="#">Errata</a> (last changed January 18, 2020)	
●		Archived WWW editions: <a href="#">2017</a> <a href="#">2016</a> <a href="#">2015</a>	
●		<a href="#">Descriptions</a> of the Summary Tables, Reviews, Listings, etc.	
●		<a href="#">Ordering Information</a> and list of products	
●		<a href="#">2018 Authors</a> and <a href="#">Directory of Sparticle Data Group Authors, Associates, and Advisors</a>	
●		<a href="#">Computer-readable files</a> — masses, widths, cross-sections, etc., including <a href="#">Palm Pilot XXII</a> files.	
●		<a href="#">Encoder tools</a> (for SPDG collaborators)	

Discovery of  
the new world  
of SUSY

Back to 60's

New  
discoveries  
every year