

News from the proton

Lamb shift and hyperfine splitting in muonic hydrogen

Randolf Pohl
for the CREMA collaboration



- The problem:

Proton rms charge radius r_p from muonic hydrogen μp is 4 % smaller than the values from elastic electron-proton scattering and hydrogen spectroscopy.

That's 5σ ... 9.4σ .

But the μp result is 10 times more accurate than any other measurement.

- Introduction:

How large is the proton?

- Muonic hydrogen:

Size does matter!

- Experiment:

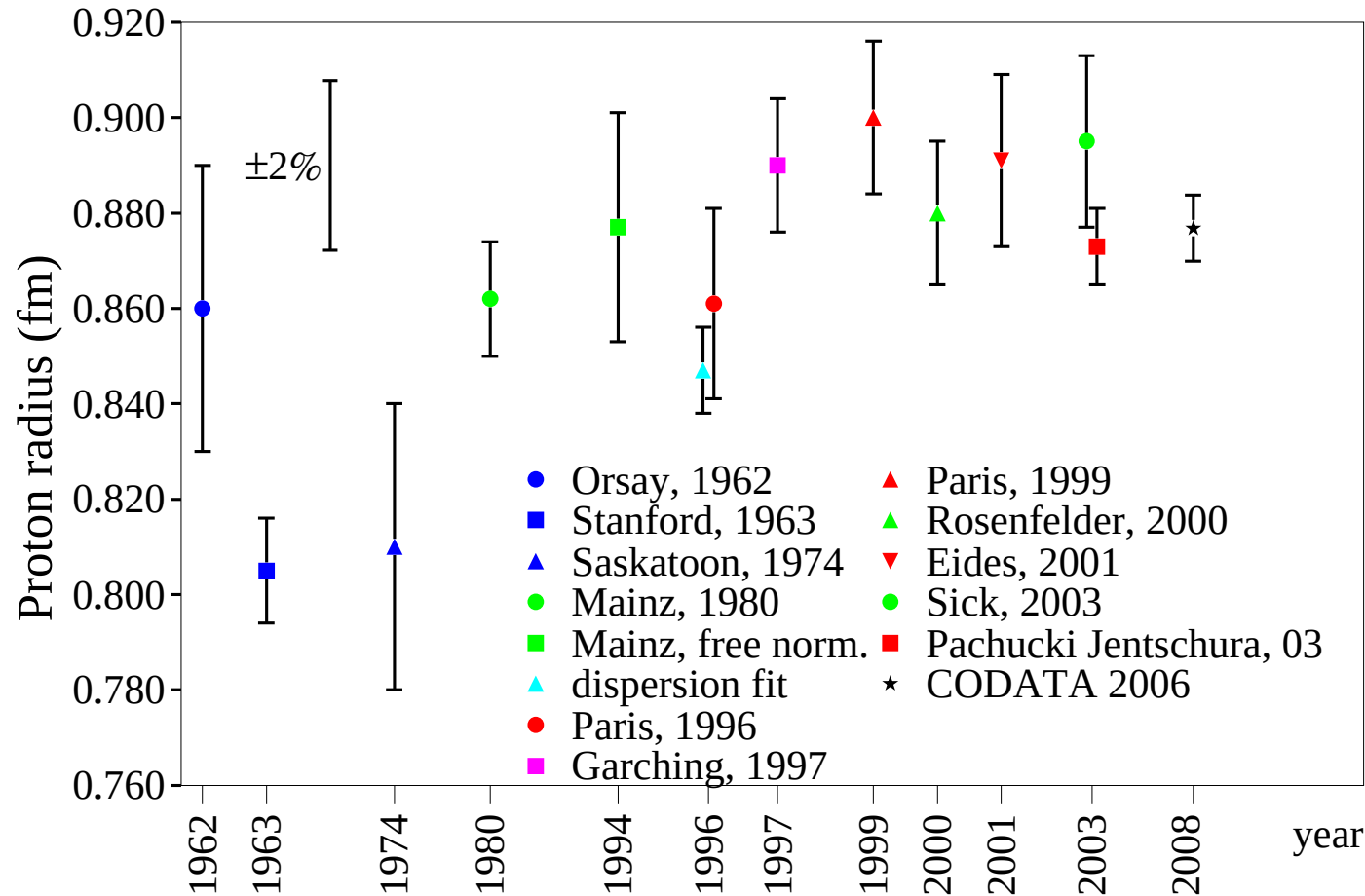
- Principle
- Muon beam
- Laser system
- NEW ANALYSIS
- NEW DATA

- Towards a solution of the “proton radius puzzle”

Proton radius vs. time



The **proton rms charge radius** is not the most accurate quantity in the universe.



● electron scattering
 ● slope of G_E at $Q^2 = 0$

● hydrogen spectr.
 ● Lamb shift (S-states)

e-p scattering: $r_p = 0.895(18) \text{ fm}$ ($u_r = 2\%$)

CODATA: $r_p = 0.8768(69) \text{ fm}$ ($u_r = 0.8\%$)

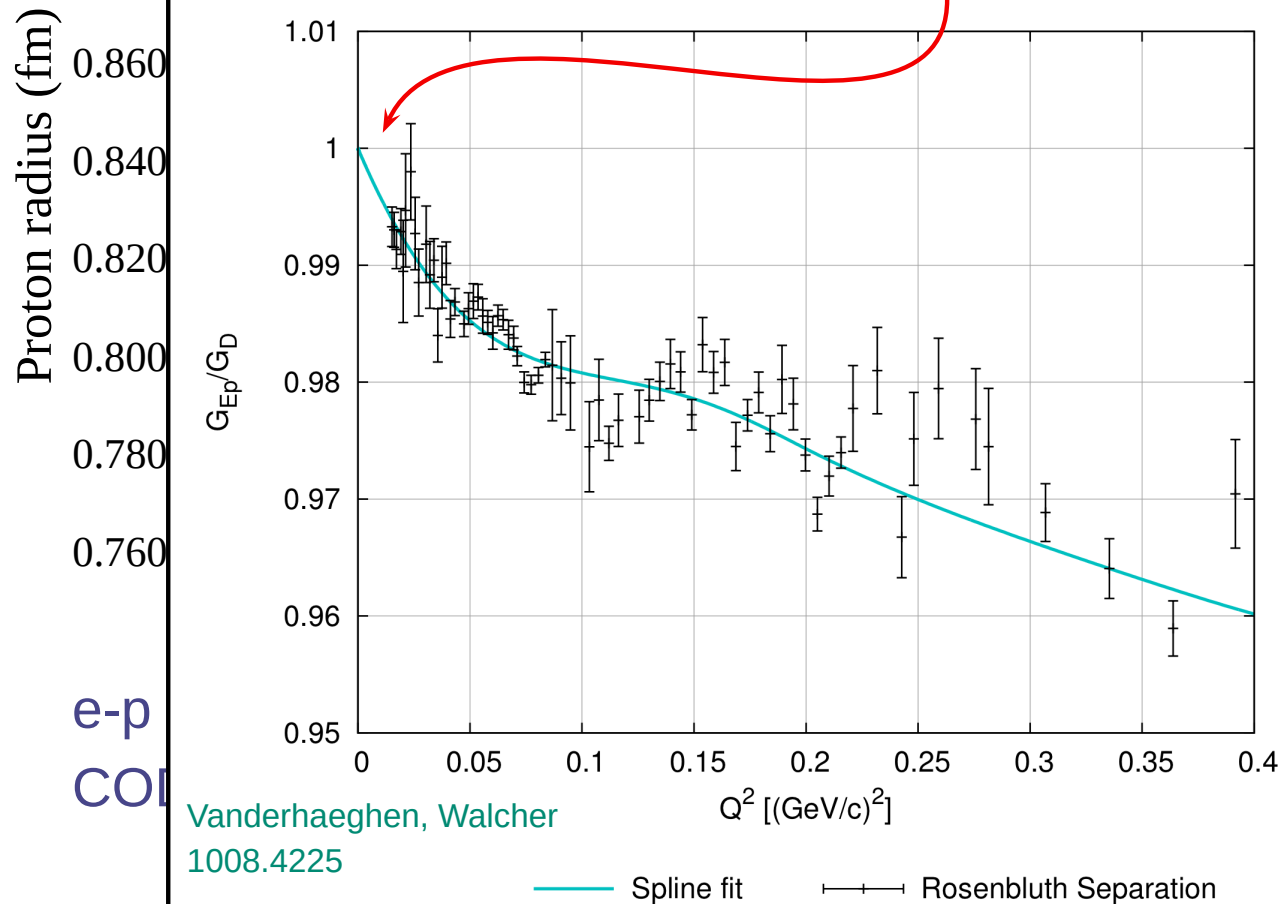
Proton radius vs. time



The **proton rms charge radius** is not the most accurate quantity in the universe.

Electron scattering:

$$\langle r_p^2 \rangle = -6\hbar^2 \left. \frac{dG_E(Q^2)}{dQ^2} \right|_{Q^2=0} \Rightarrow \text{slope of } G_E \text{ at } Q^2 = 0$$



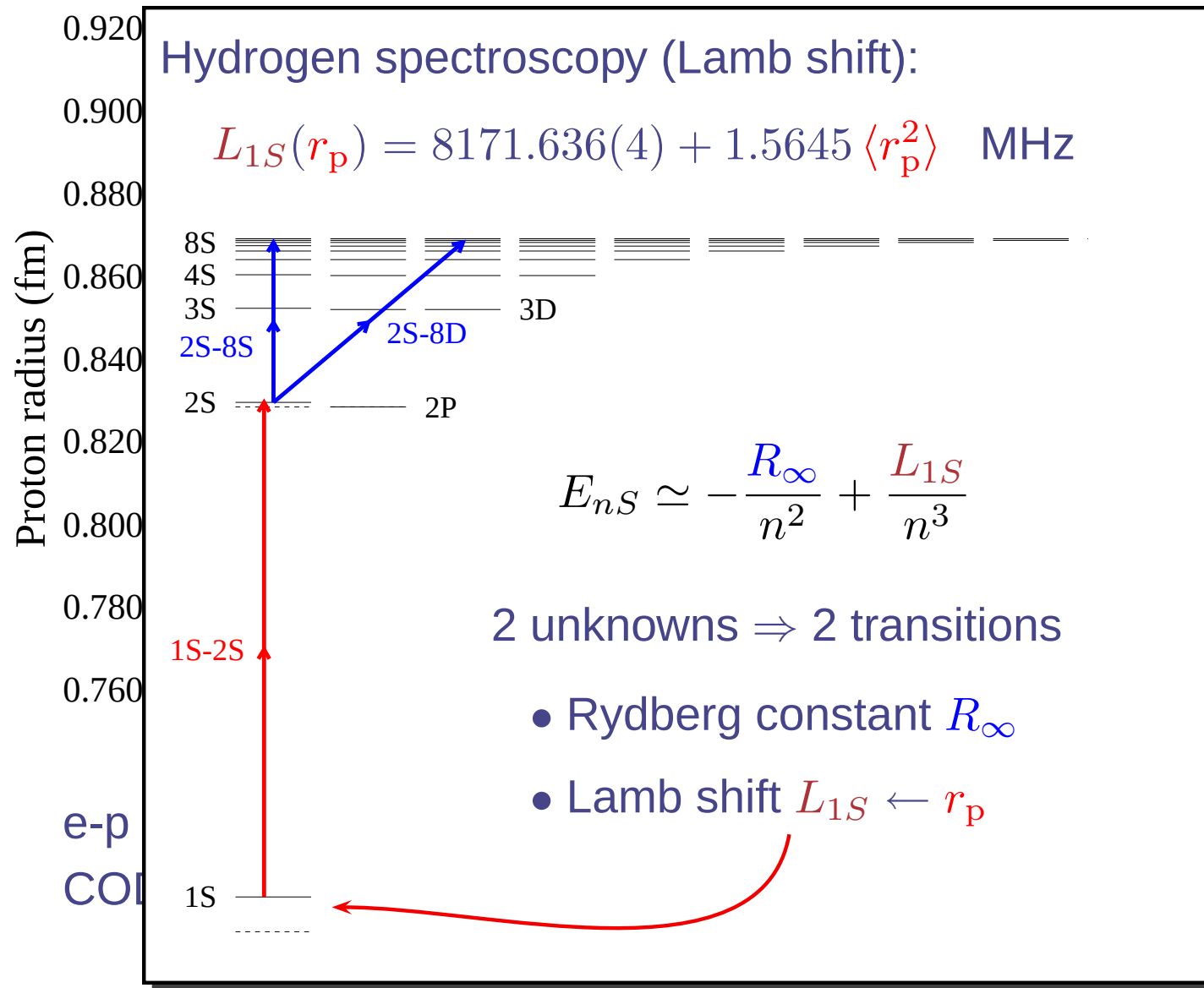
- electron scattering
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- Lamb shift (S-states)

e-p
COL

Proton radius vs. time



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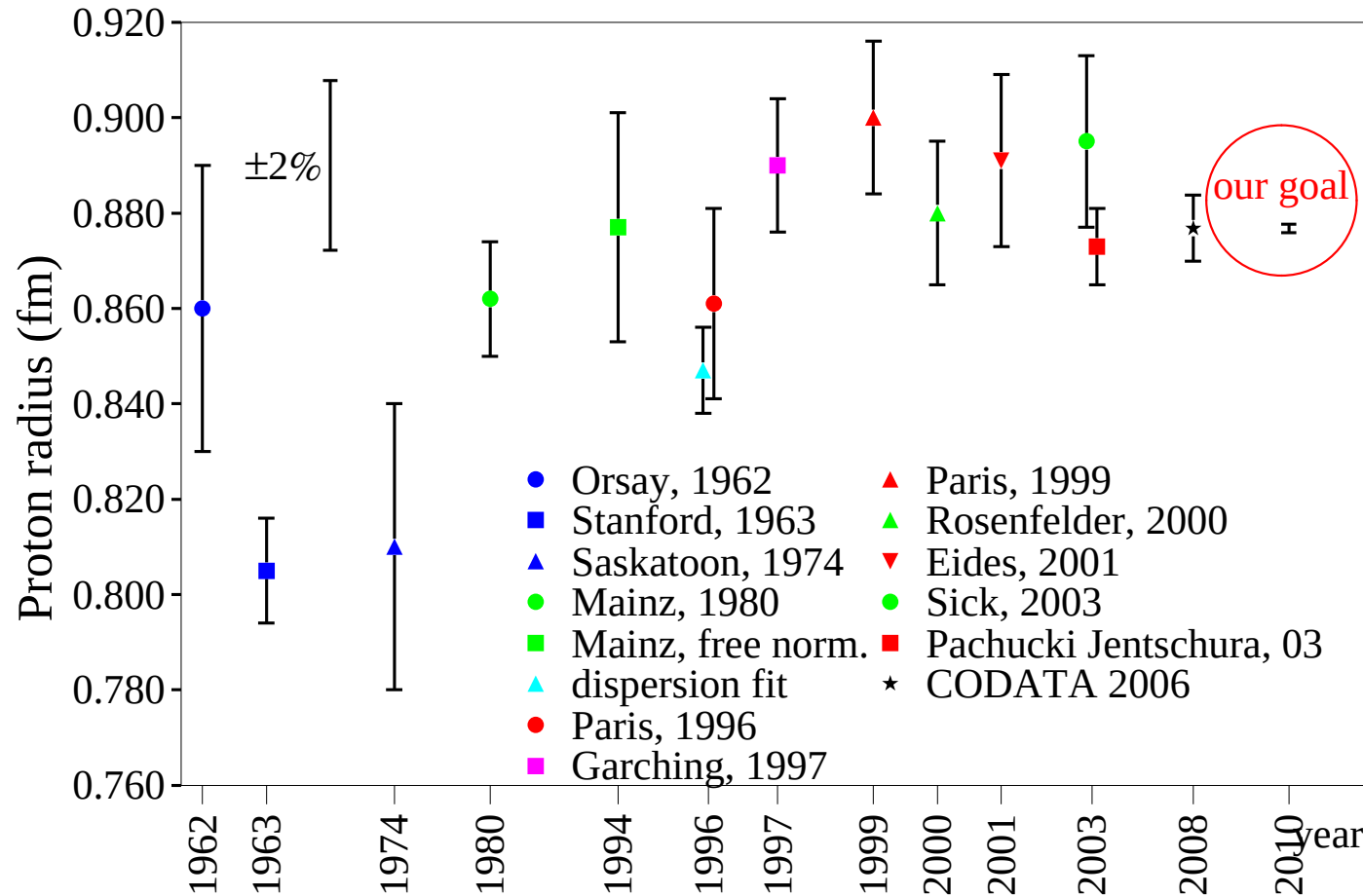


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muonic hydrogen goal (1998): $u_r = 0.1\%$

20x improvement

(aim: 10x better QED test in H)

Proton charge radius and muonic hydrogen



muonic hydrogen = $\mu^- p$ mass $m_\mu = 207 m_e$

$$\Rightarrow \text{Bohr: } \langle r^{\text{orbit}} \rangle \sim \frac{\hbar}{Z\alpha m_r c} n^2$$

$$\Delta E_{\text{finite size}}(nl) \sim r_p^2 |\Psi(r=0)|^2$$

$$\Rightarrow \Delta E_{\text{finite size}}(nl) = \frac{2(Z\alpha)^4 c^4}{3\hbar^2 n^3} m_r^3 r_p^2 \delta_{l0}$$

Lamb shift in μp : $\Delta E(2P_{3/2}^{F=2} - 2S_{1/2}^{F=1}) =$

$$209.9779(49) - 5.2262 r_p^2 + 0.0347 r_p^3 \text{ [meV]}$$

finite size contribution is 2% of the μp Lamb shift

measure $\Delta E(2S-2P)$ to 30 ppm = 1.5 GHz

$$\Rightarrow r_p \text{ to } 10^{-3}$$

$$\Gamma_{2P} = 18.6 \text{ GHz} \quad (\Gamma_{\text{rad.}})$$

$\mu p(n=2)$ levels:

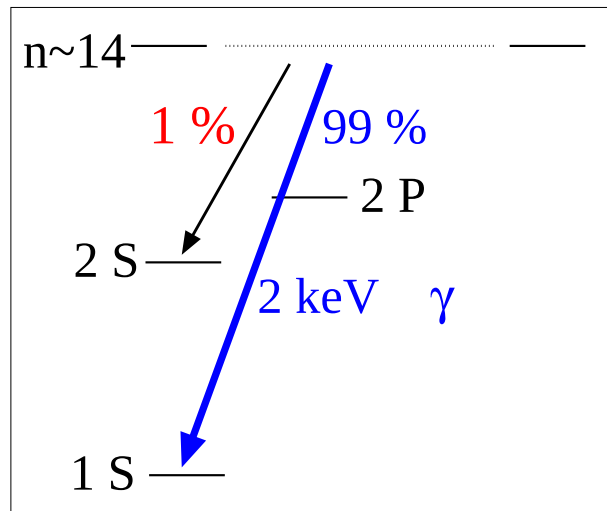
206 meV
50 THz
6 μm

fin. size:
3.8 meV

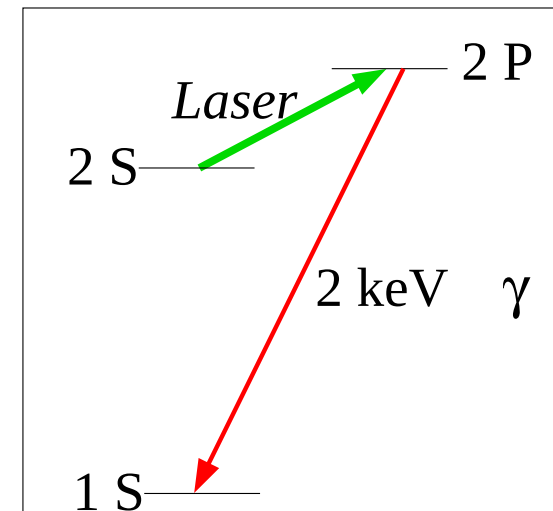
μ p Lamb shift experiment: Principle



“prompt” ($t \sim 0$)



“delayed” ($t \sim 1 \mu\text{s}$)



μ^- stop in H_2 gas
 $\Rightarrow \mu\text{p}^*$ atoms formed ($n \sim 14$)

99%: cascade to $\mu\text{p}(1\text{S})$,
emitting prompt K_α , K_β ...

1%: long-lived $\mu\text{p}(2\text{S})$ atoms

lifetime $\tau_{2\text{S}} \approx 1 \mu\text{s}$ at 1 mbar H_2

R. Pohl *et. al.*, Phys. Rev. Lett. 97, 193402 (2006).

fire laser ($\lambda \approx 6 \mu\text{m}$, $\Delta E \approx 0.2 \text{ eV}$)

$\Rightarrow$ induce $\mu\text{p}(2\text{S}) \rightarrow \mu\text{p}(2\text{P})$

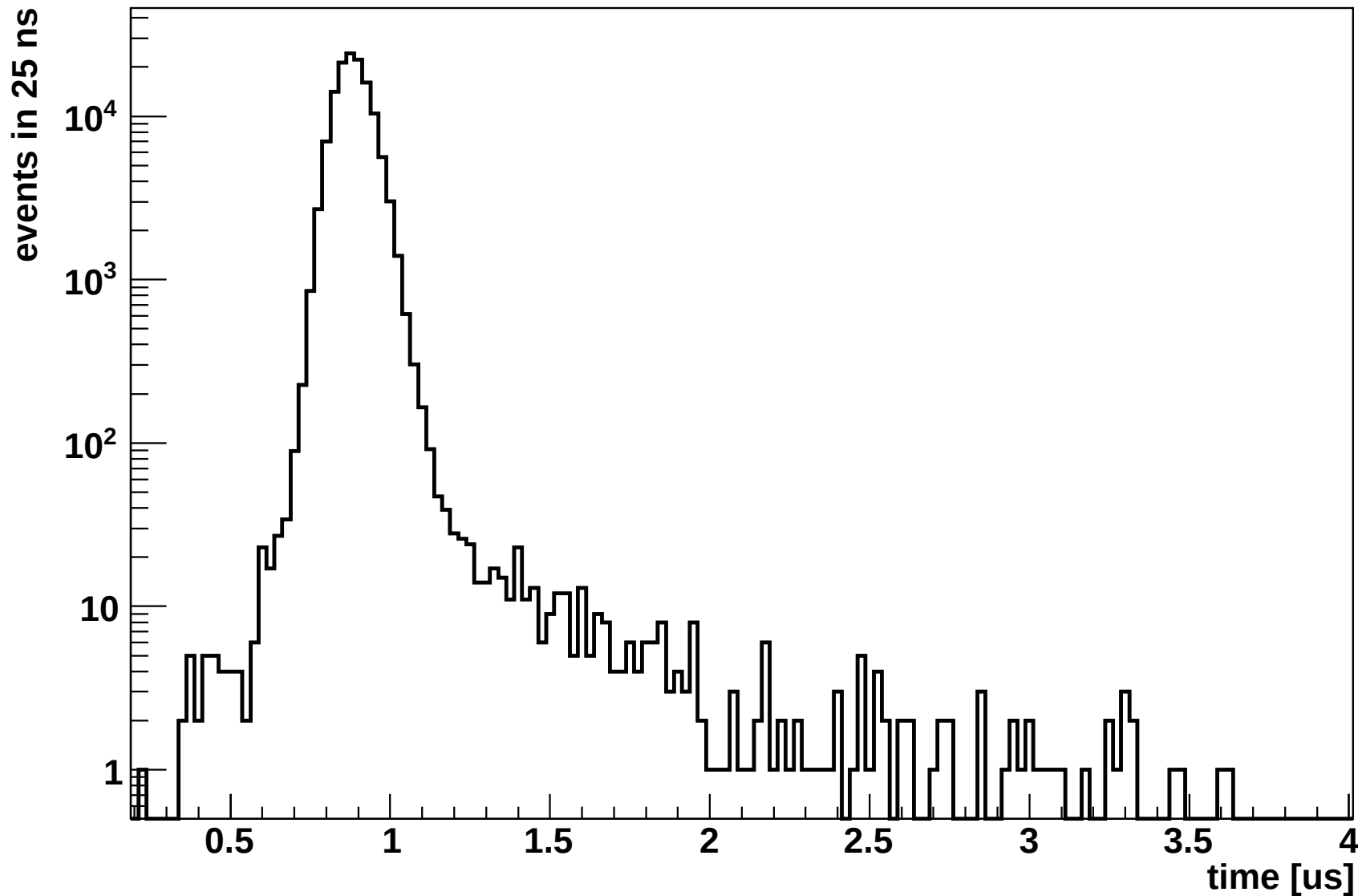
$\Rightarrow$ observe **delayed** K_α x-rays

$\Rightarrow$ normalize $\frac{\text{delayed } \text{K}_\alpha}{\text{prompt } \text{K}_\alpha}$ x-rays

μ p Lamb shift experiment: Principle



time spectrum of 2 keV x-rays (~ 13 hours of data)

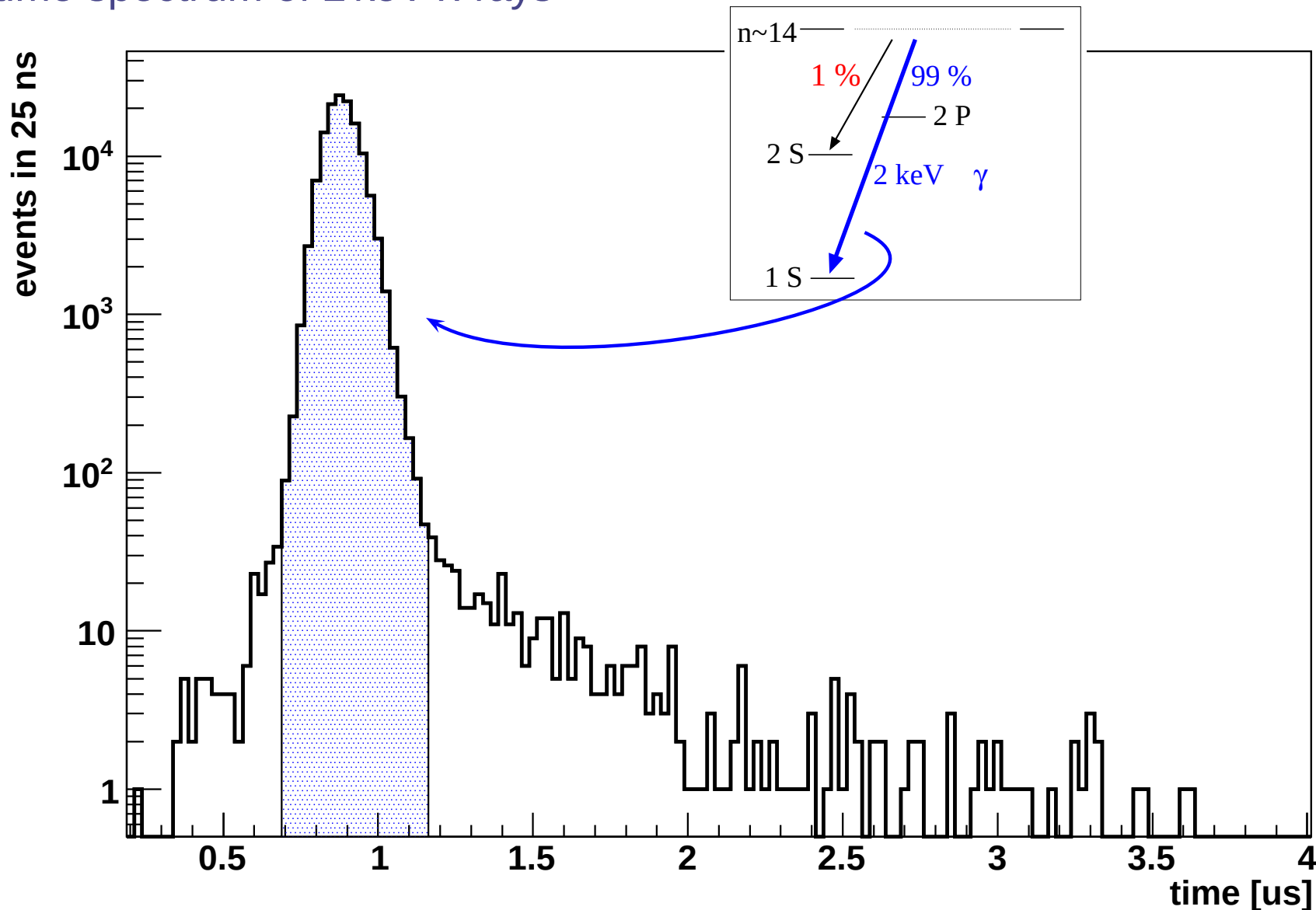


μ p Lamb shift experiment: Principle



time spectrum of 2 keV x-rays

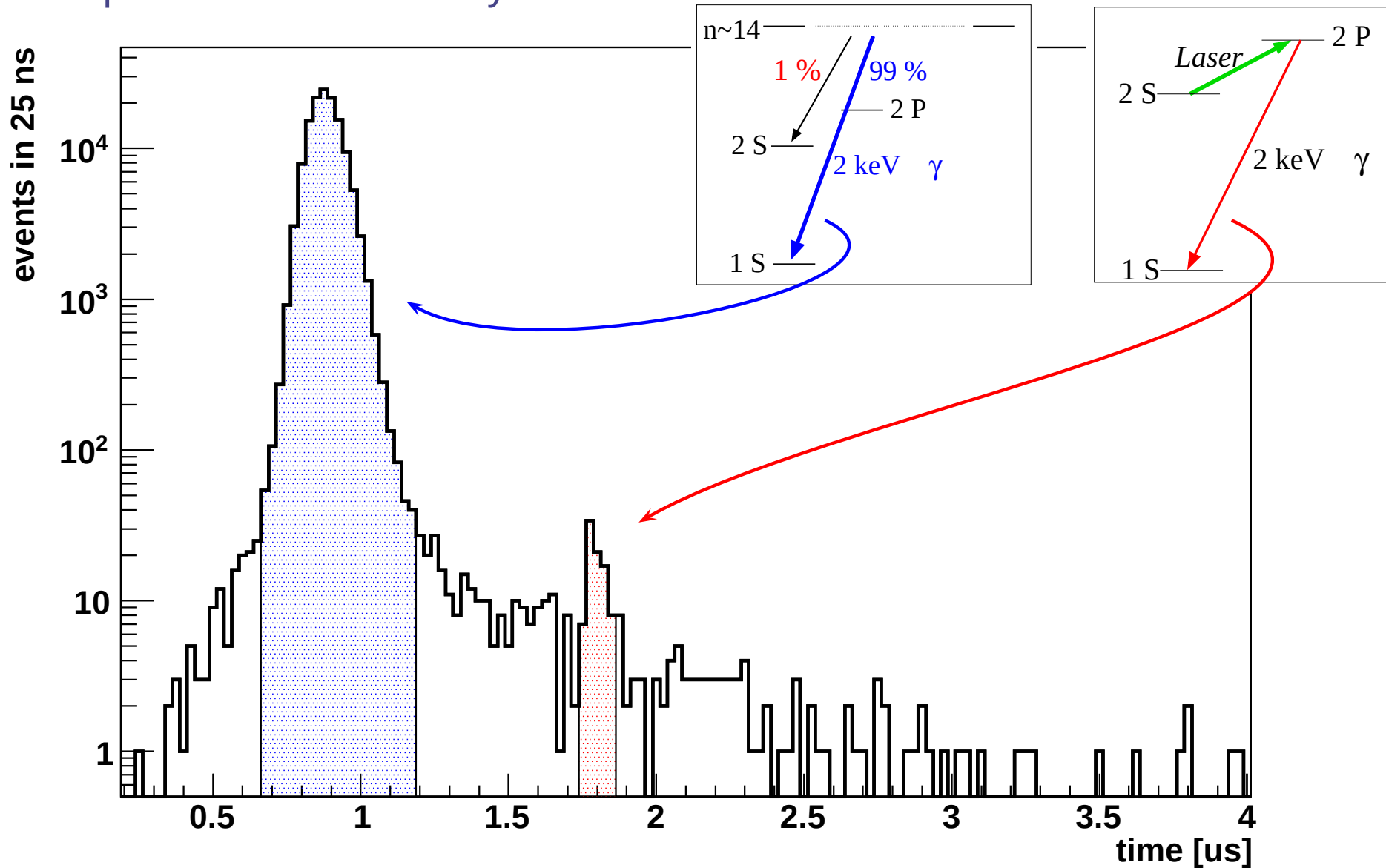
“prompt” ($t \sim 0$)



μ p Lamb shift experiment: Principle



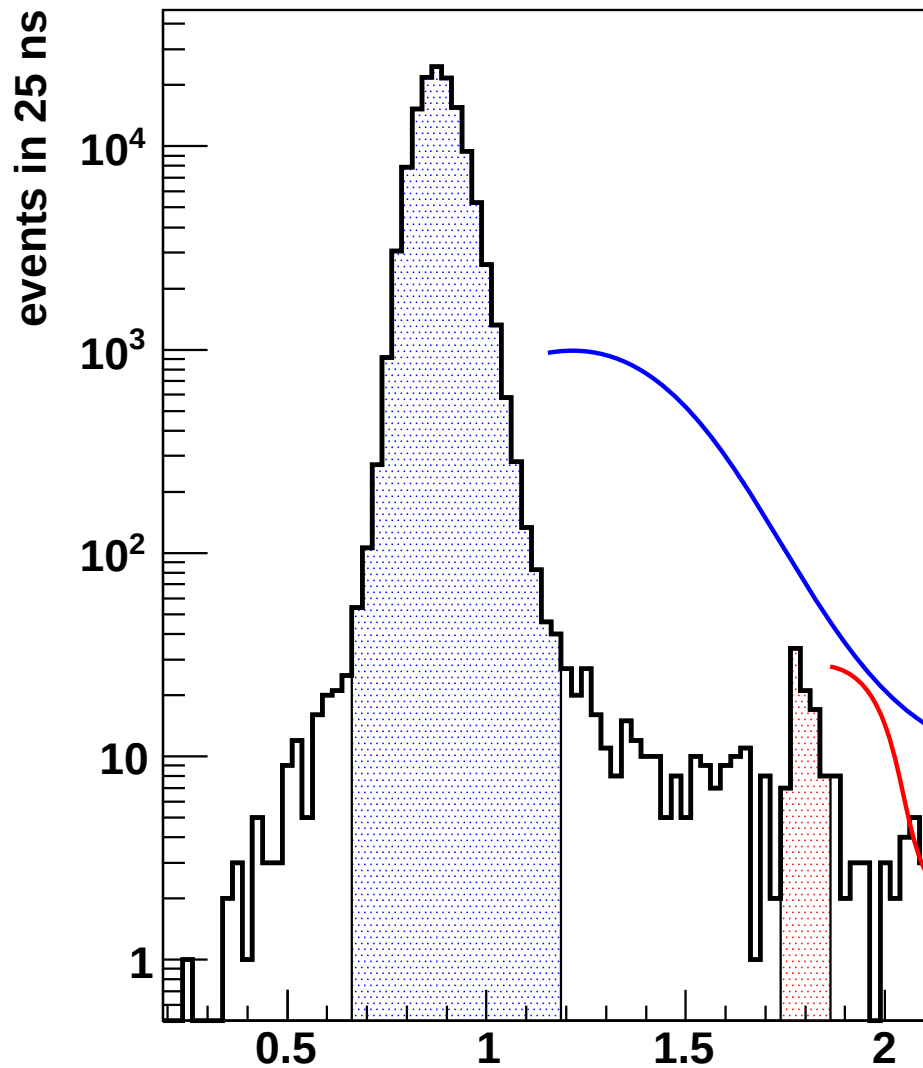
time spectrum of 2 keV x-rays



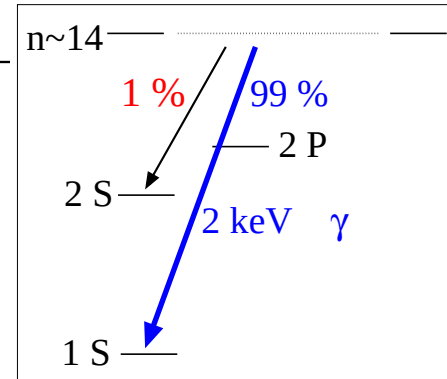
μp Lamb shift experiment: Principle



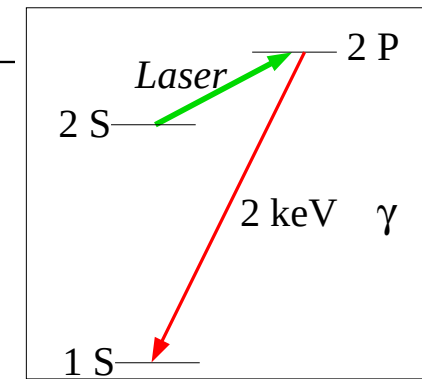
time spectrum of 2 keV x-rays



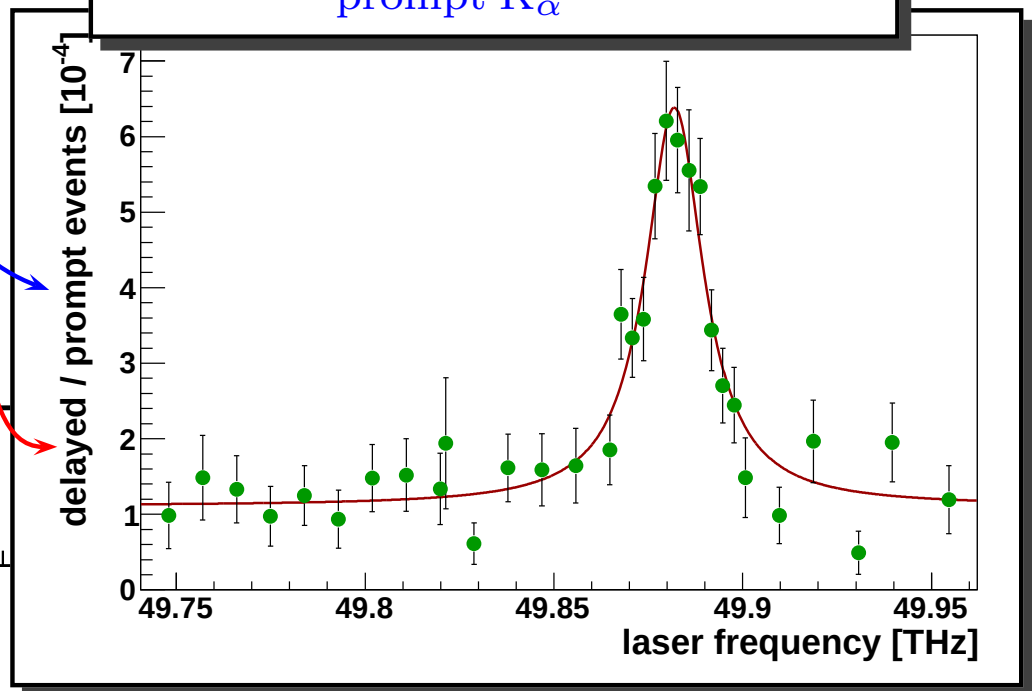
“prompt” ($t \sim 0$)



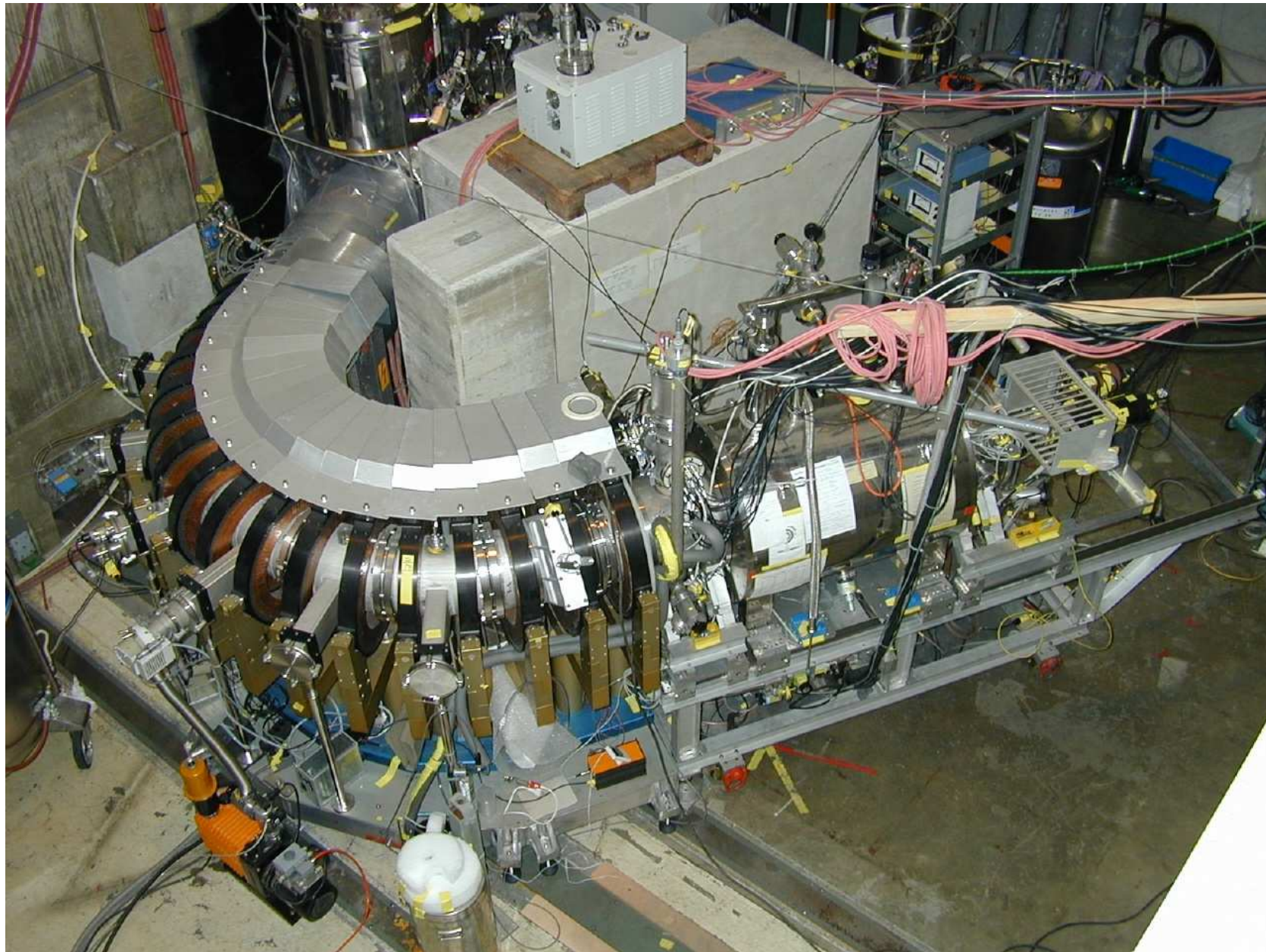
“delayed” ($t \sim 1 \mu\text{s}$)



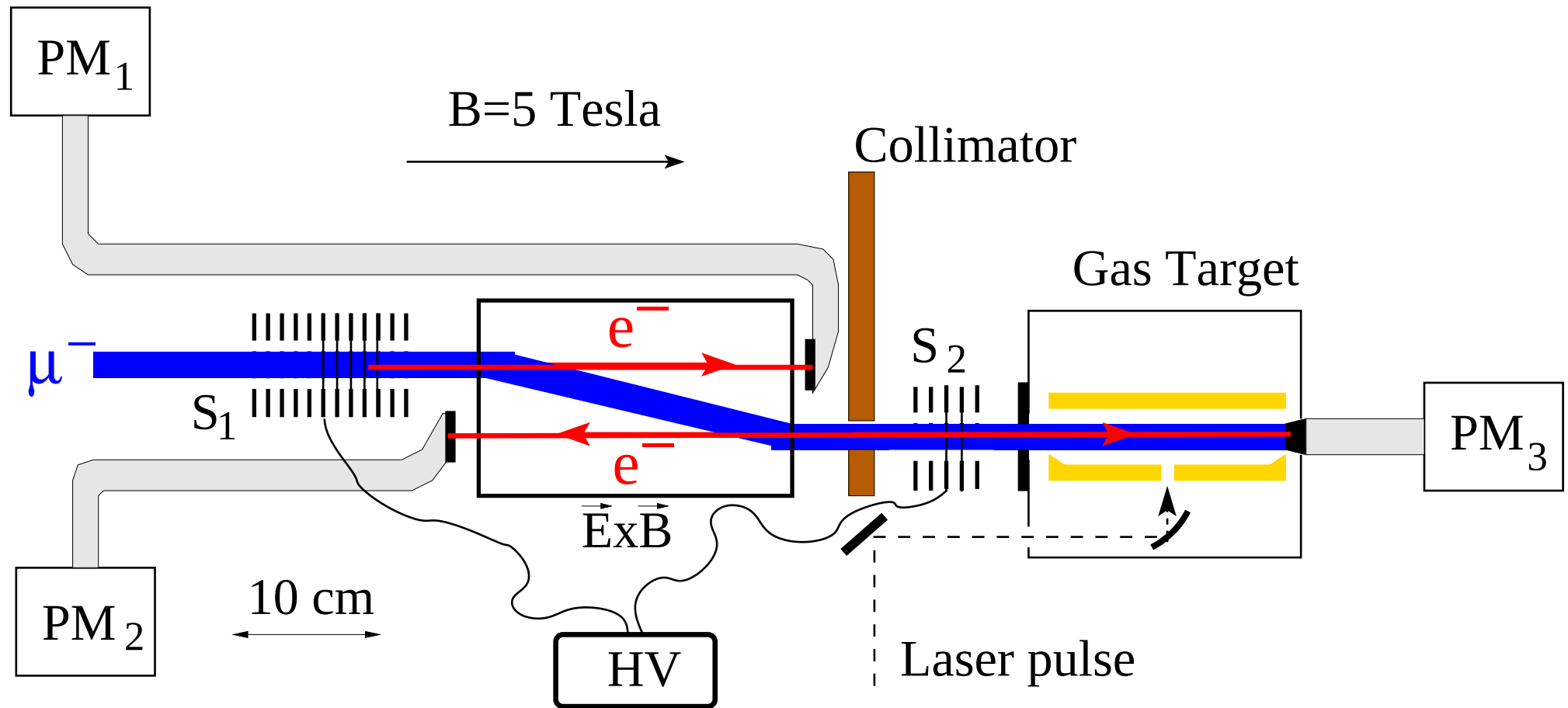
normalize $\frac{\text{delayed } K_{\alpha}}{\text{prompt } K_{\alpha}} \Rightarrow \text{Resonance}$



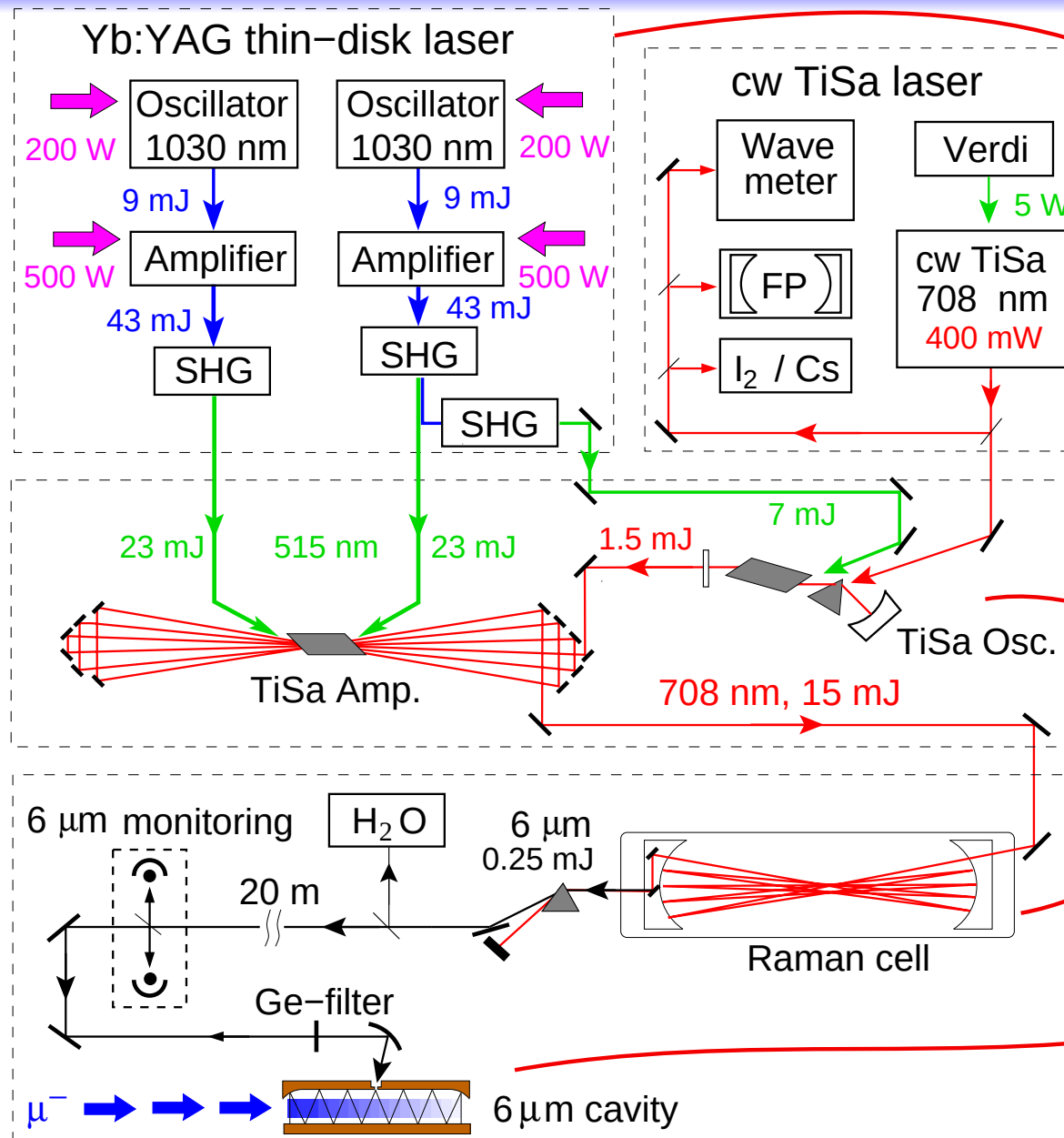
Muon beam line



Muon beam: inside 5 T solenoid



The laser system

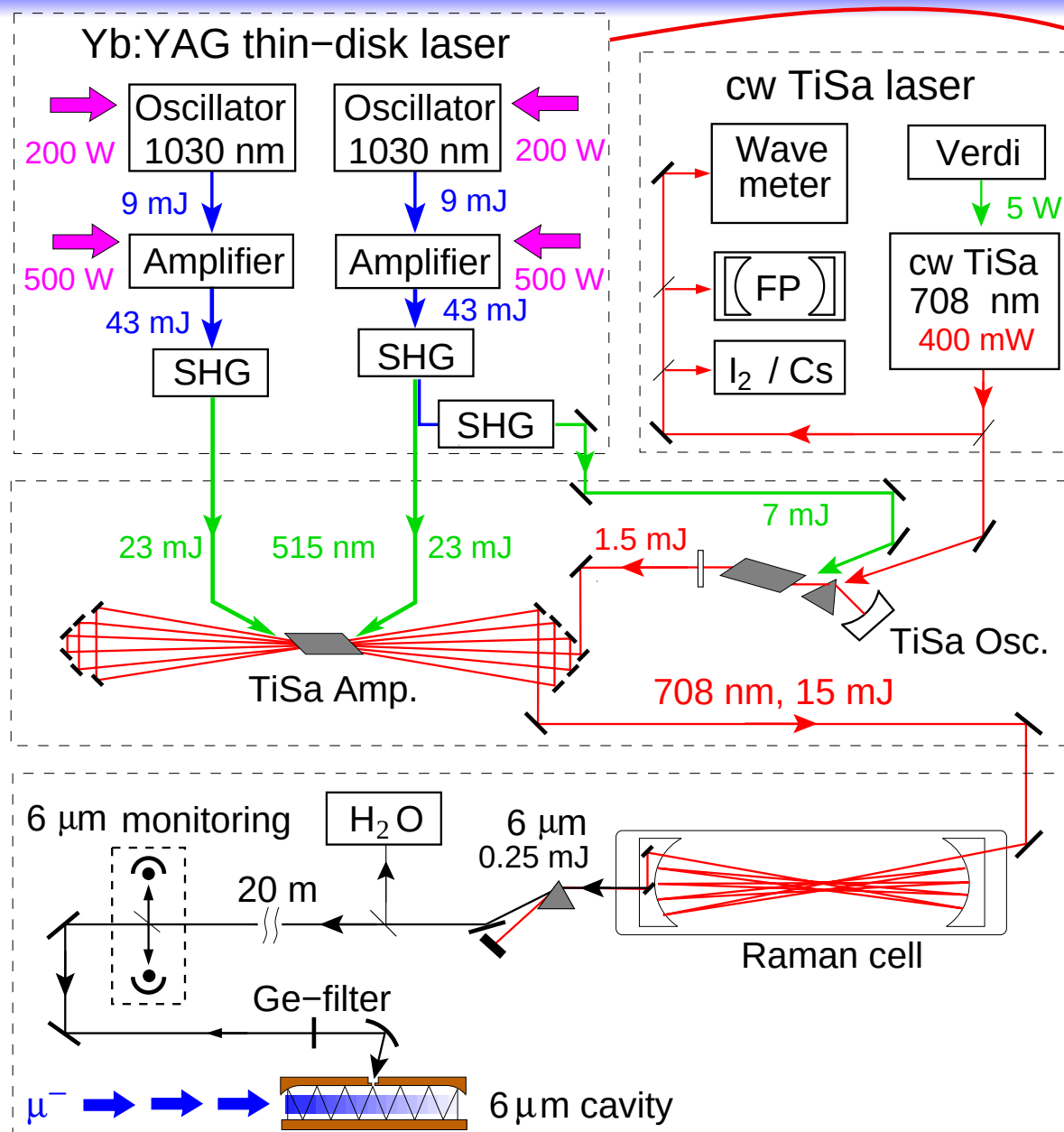


Main components:

- Thin-disk laser
fast response to detected μ^-
- Frequency doubling
- TiSa laser:
frequency stabilized cw laser
injection seeded oscillator
multipass amplifier
- Raman cell
3 Stokes: 708 nm $\rightarrow$ 6 μ m
 λ calibration @ 6 μ m
- Target cavity

A. Antognini *et. al.*, Opt. Comm. 253, 362 (2005).

The laser system

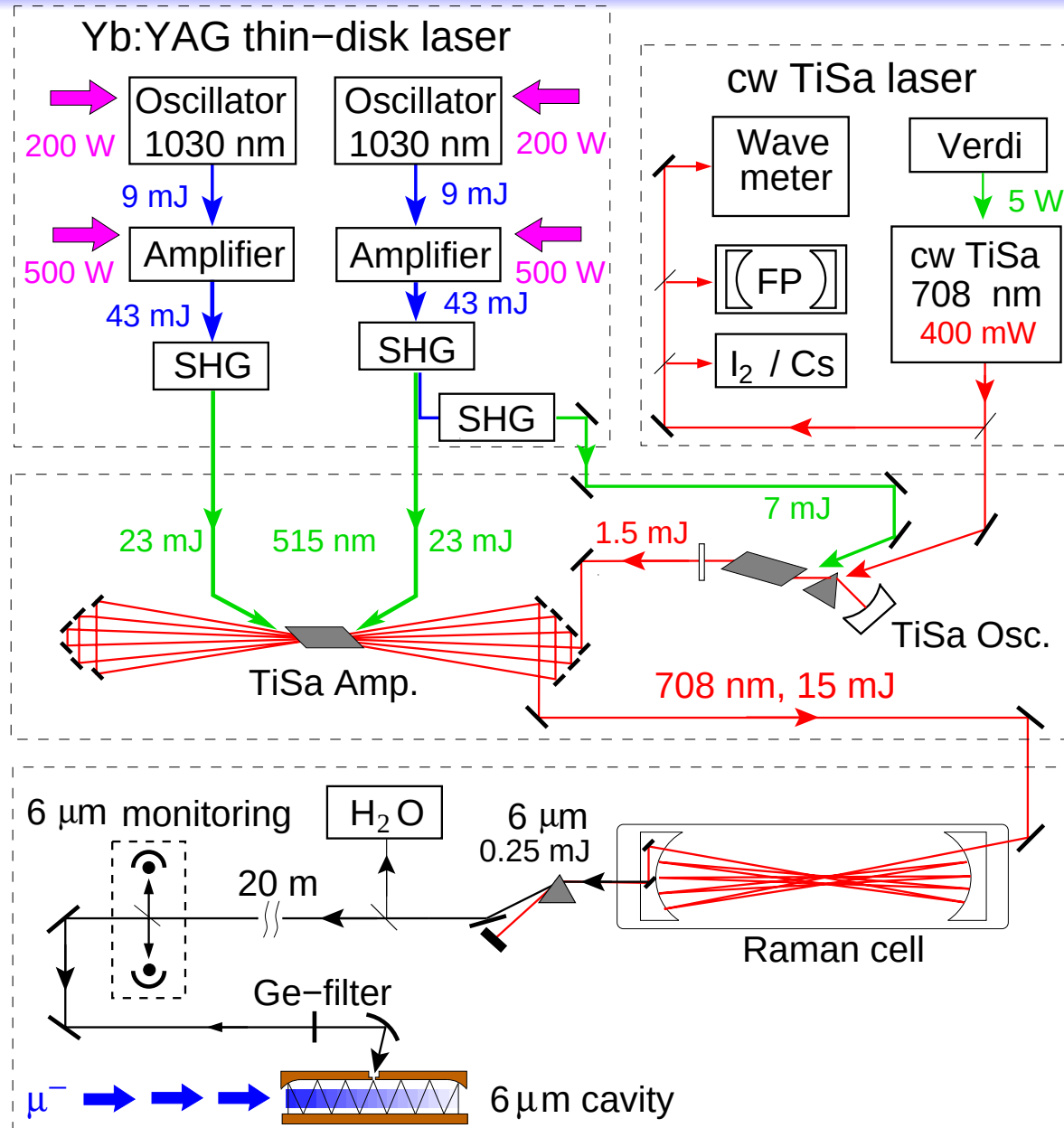


Thin-disk laser

- Large pulse energy: 85 (160) mJ
 - Short trigger-to-pulse delay: $\lesssim 400$ ns
 - Random trigger
 - Pulse-to-pulse delays down to 2 ms (rep. rate $\gtrsim 500$ Hz)
- Each single μ^- triggers the laser system
 - $2S$ lifetime $\approx 1 \mu\text{s} \rightarrow$ short laser delay

A. Antognini *et. al.*,
IEEE J. Quant. Electr. 45, 993 (2009).

The laser system



MOPA TiSa laser:

Cw frequency stabilized laser

- referenced to a stable FP cavity
- FP cavity calibrated with I_2 , Rb, Cs lines

$$\nu_{\text{FP}} = N \cdot \text{FSR}$$

$$\text{FSR} = 1497.344(6) \text{ MHz}$$

$$\nu_{\text{TiSa}}^{\text{cw}} \text{ absolutely known to } 30 \text{ MHz}$$

$$\Gamma_{2\text{P}-2\text{S}} = 18.6 \text{ GHz}$$

Seeded oscillator

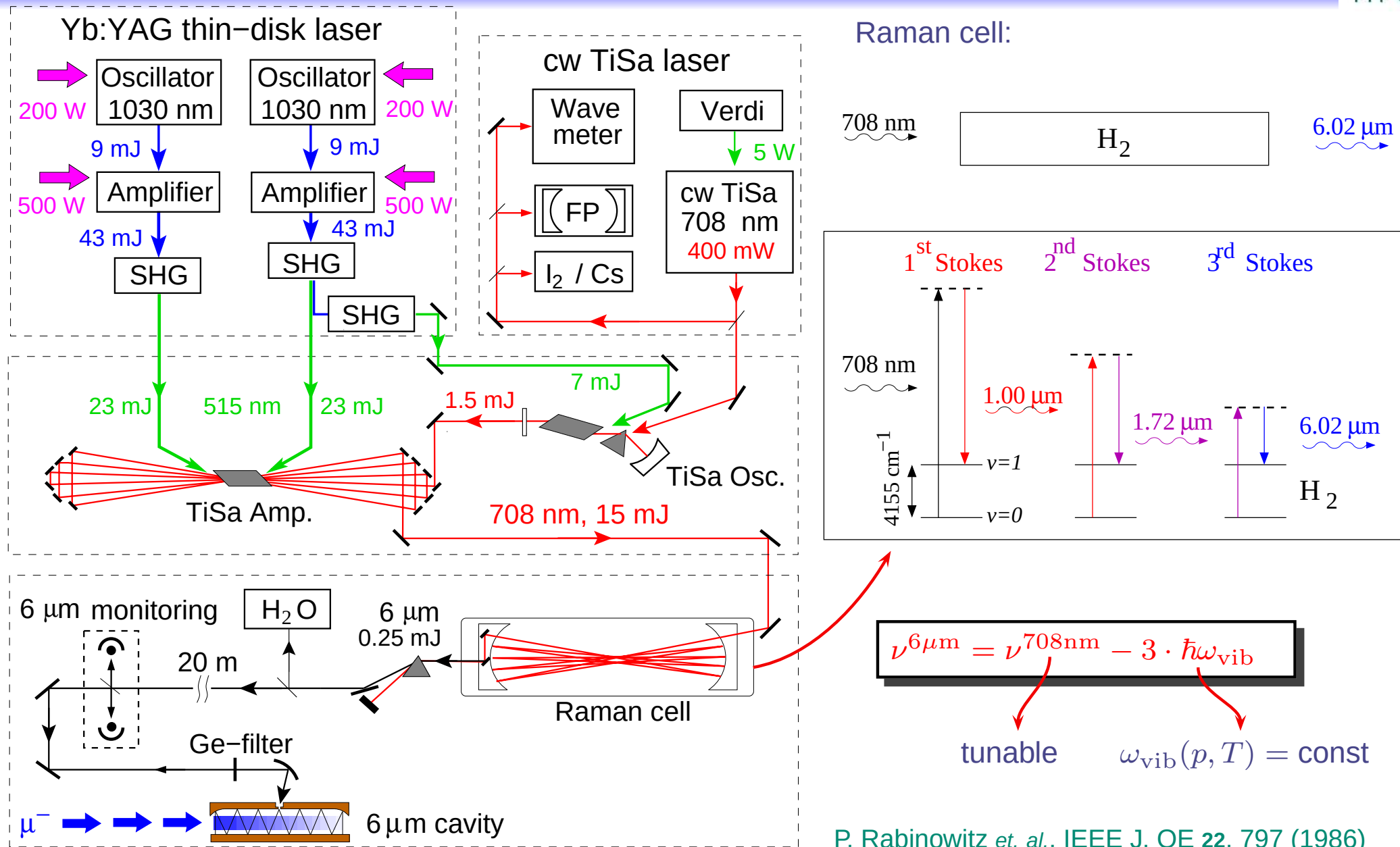
$$\rightarrow \nu_{\text{TiSa}}^{\text{pulsed}} = \nu_{\text{TiSa}}^{\text{cw}}$$

(frequency chirp $\leq 100 \text{ MHz}$)

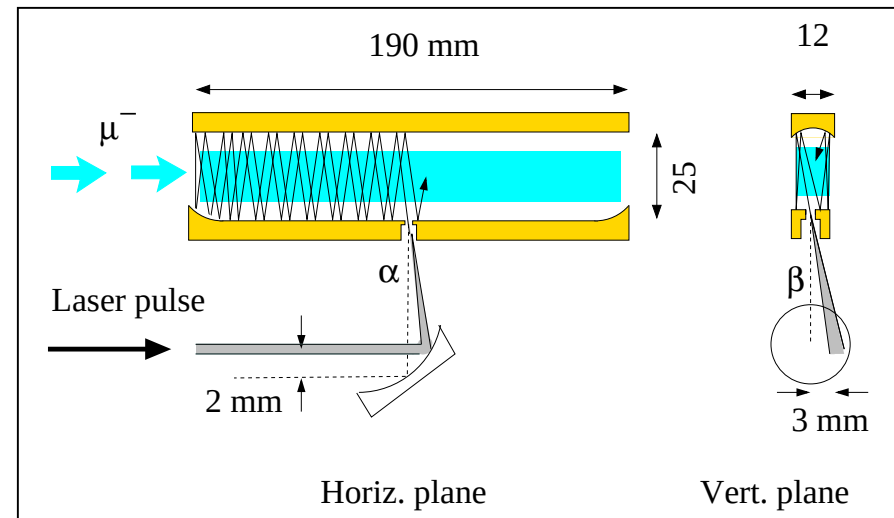
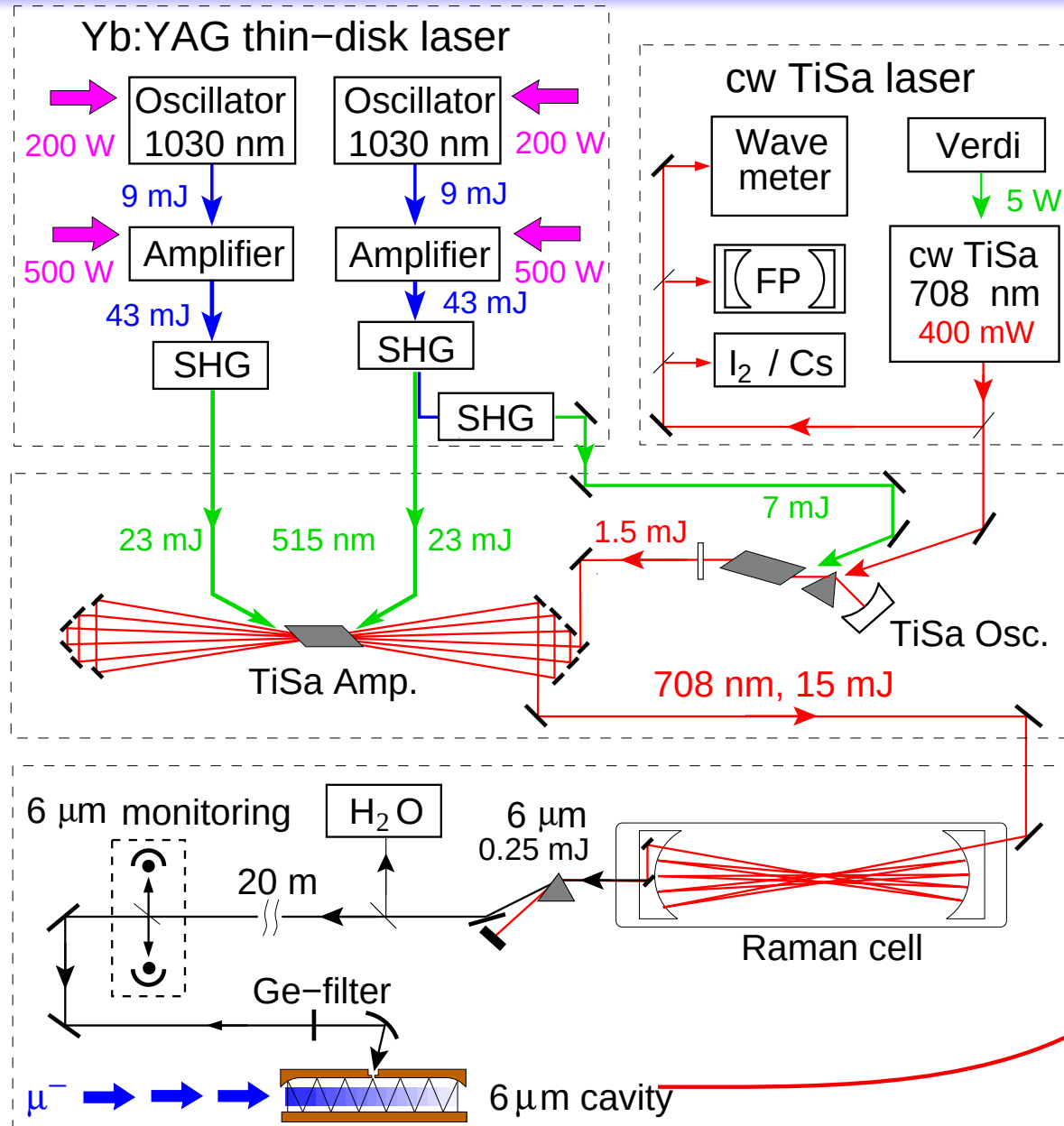
Multipass amplifier (2f- configuration)

gain=10

The laser system



The laser system



Design: insensitive to misalignment

Transverse illumination

Large volume

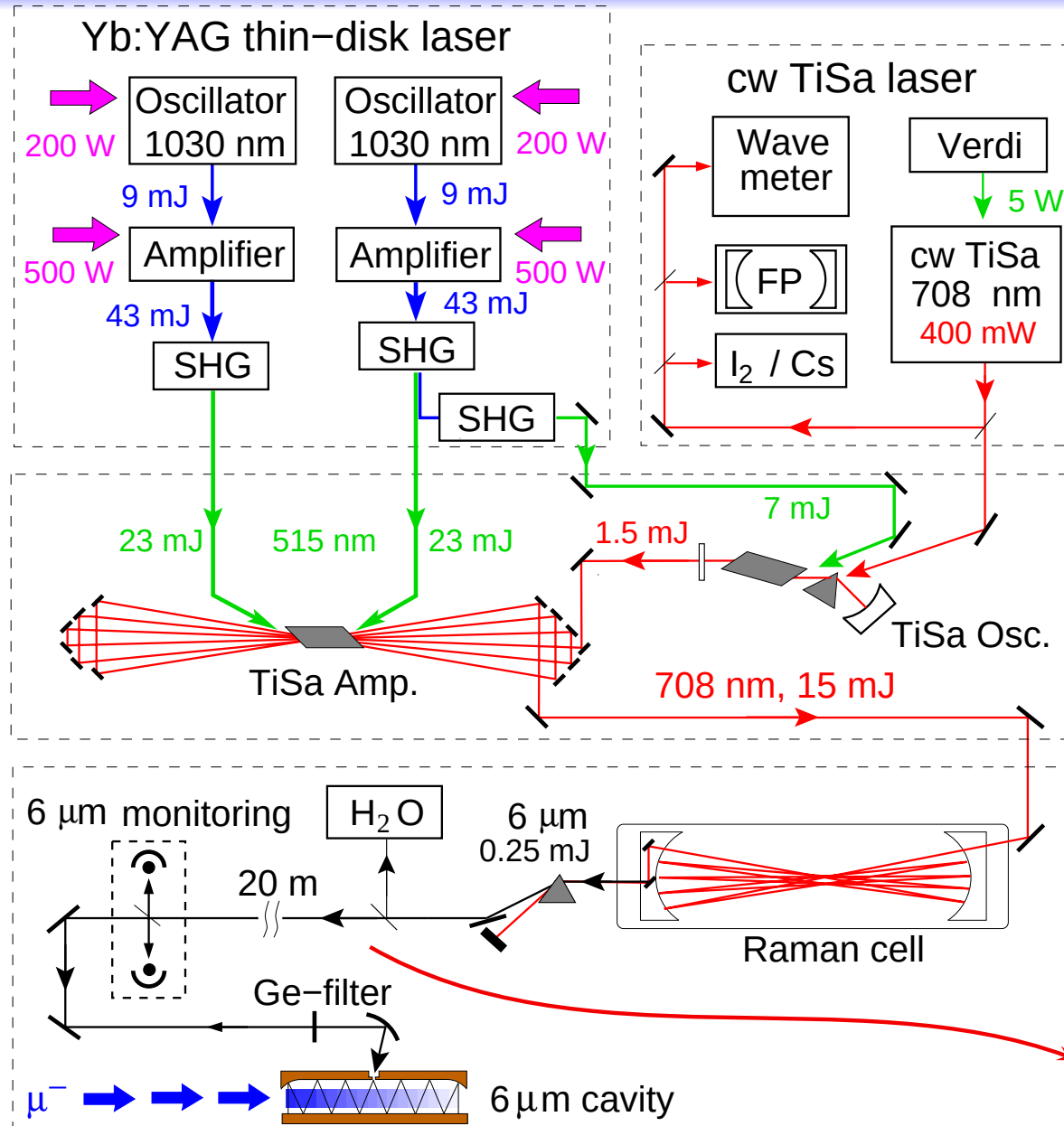
Dielectric coating with $R \geq 99.9\%$ (at 6 μm)

→ Light makes 1000 reflections

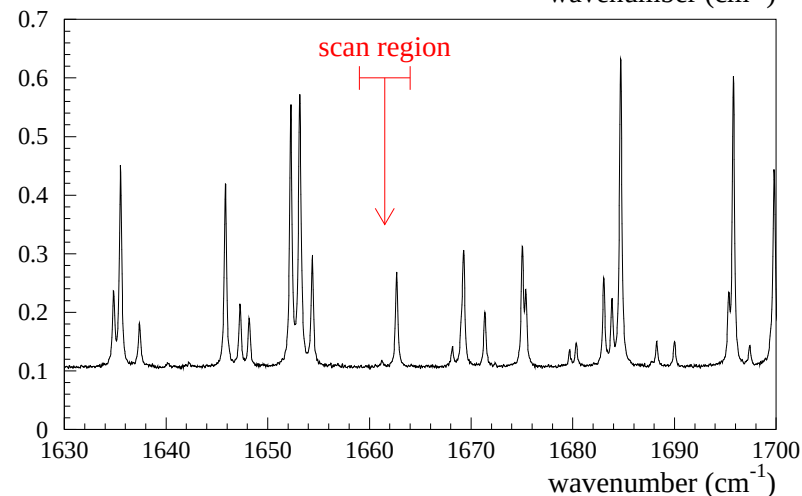
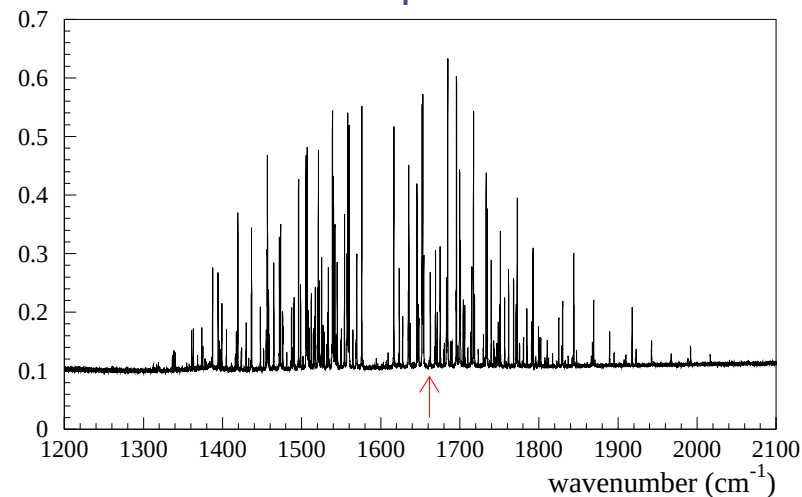
→ Light is confined for $\tau=50$ ns

→ 0.15 mJ saturates the $2S - 2P$ transition

The laser system



Water absorption

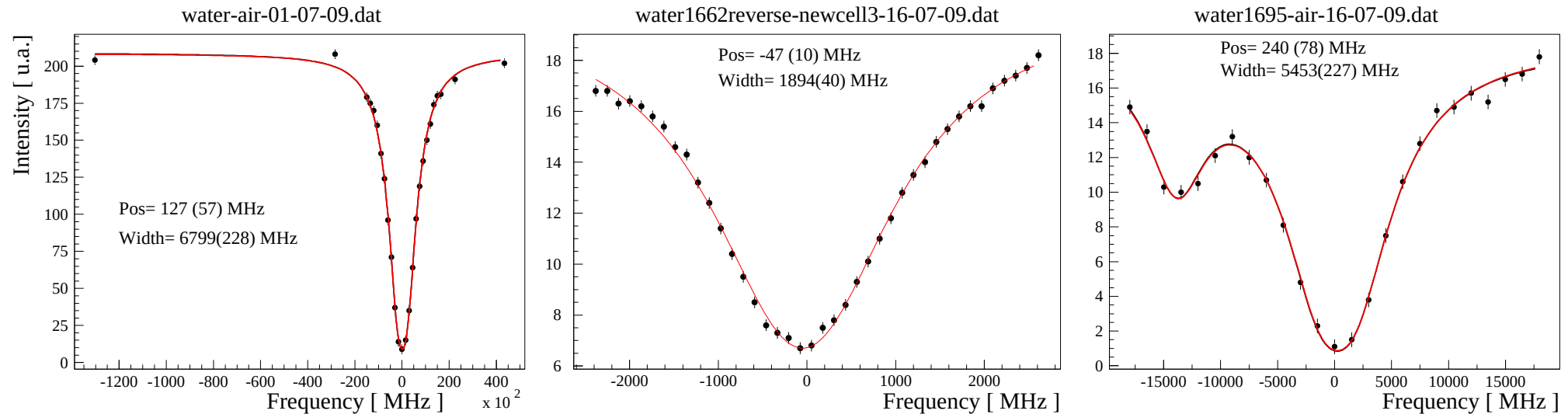


- Vacuum tube for 6 μm beam transport.
- Direct frequency calibration at 6 μm .

6 μm wavelength calibration



MPQ



- 6 μm light calibration: H_2O vapor absorption measurement in air / cell

H_2O absorption lines known to a few MHz (HITRAN)

$\Rightarrow$ $\delta\nu \approx 300$ MHz uncertainty (6 ppm of ΔE_{2S-2P}) due to our calibration accuracy

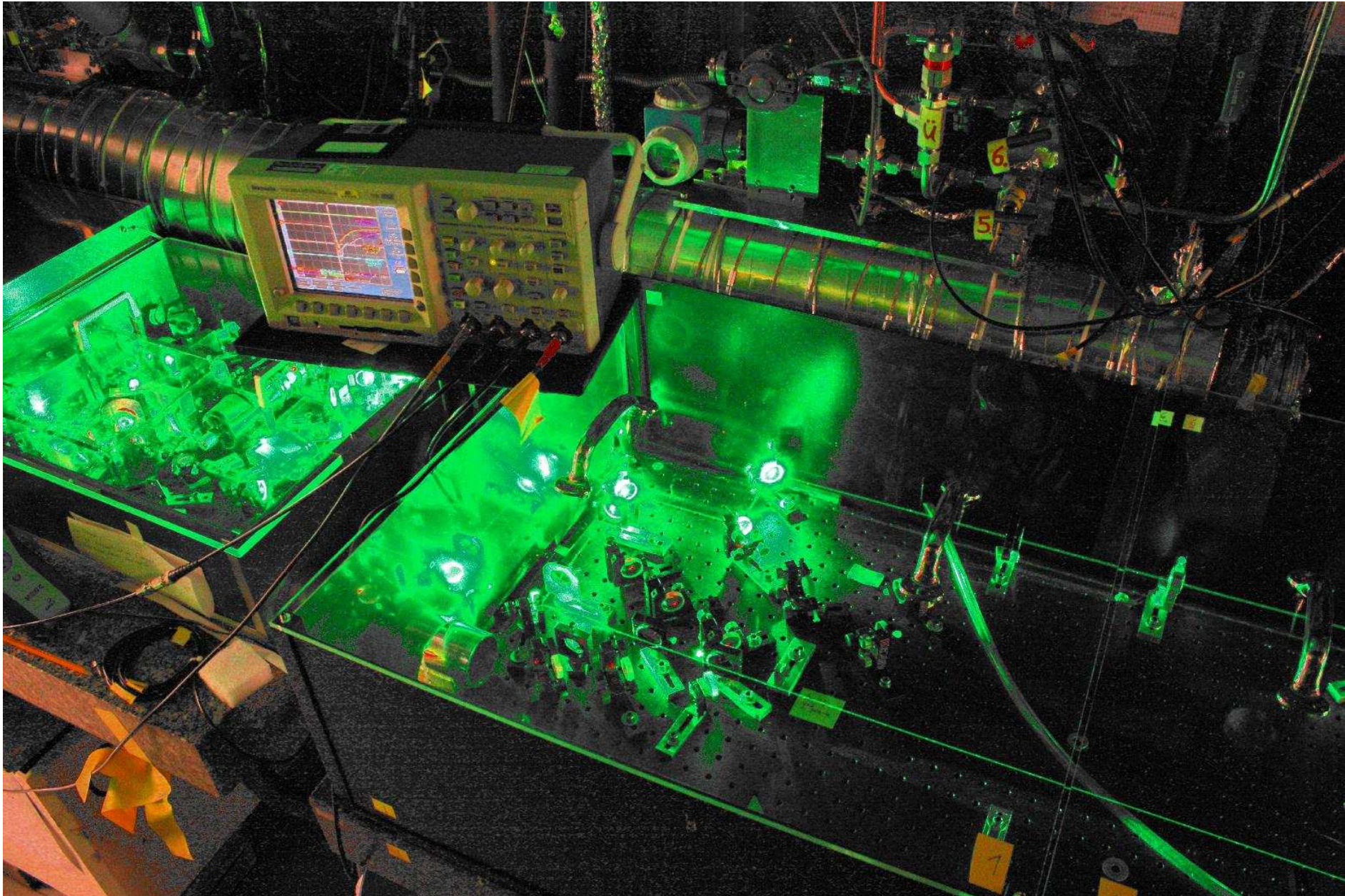
over the whole wavelength range $\lambda = 5.5 \dots 6.1 \mu\text{m}$

- Laser frequency detuning is measured in number of Fabry-Perot cavity fringes
 - grid spacing of our measurement: $\text{FSR}(\text{FP}) = 1497.344(6)$ MHz
 - all measured resonances are within ± 70 FP fringes of a H_2O line

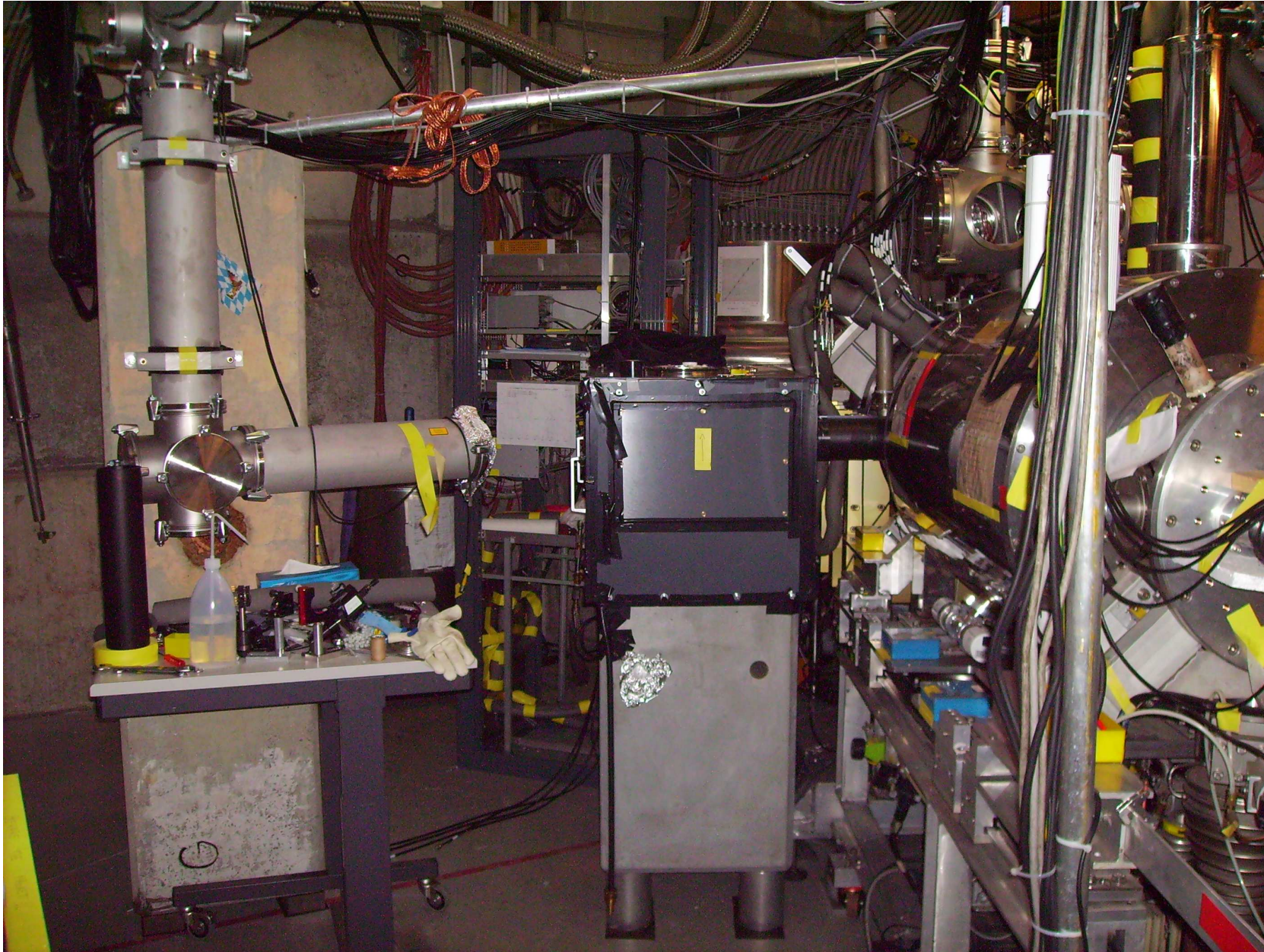
Laser hut



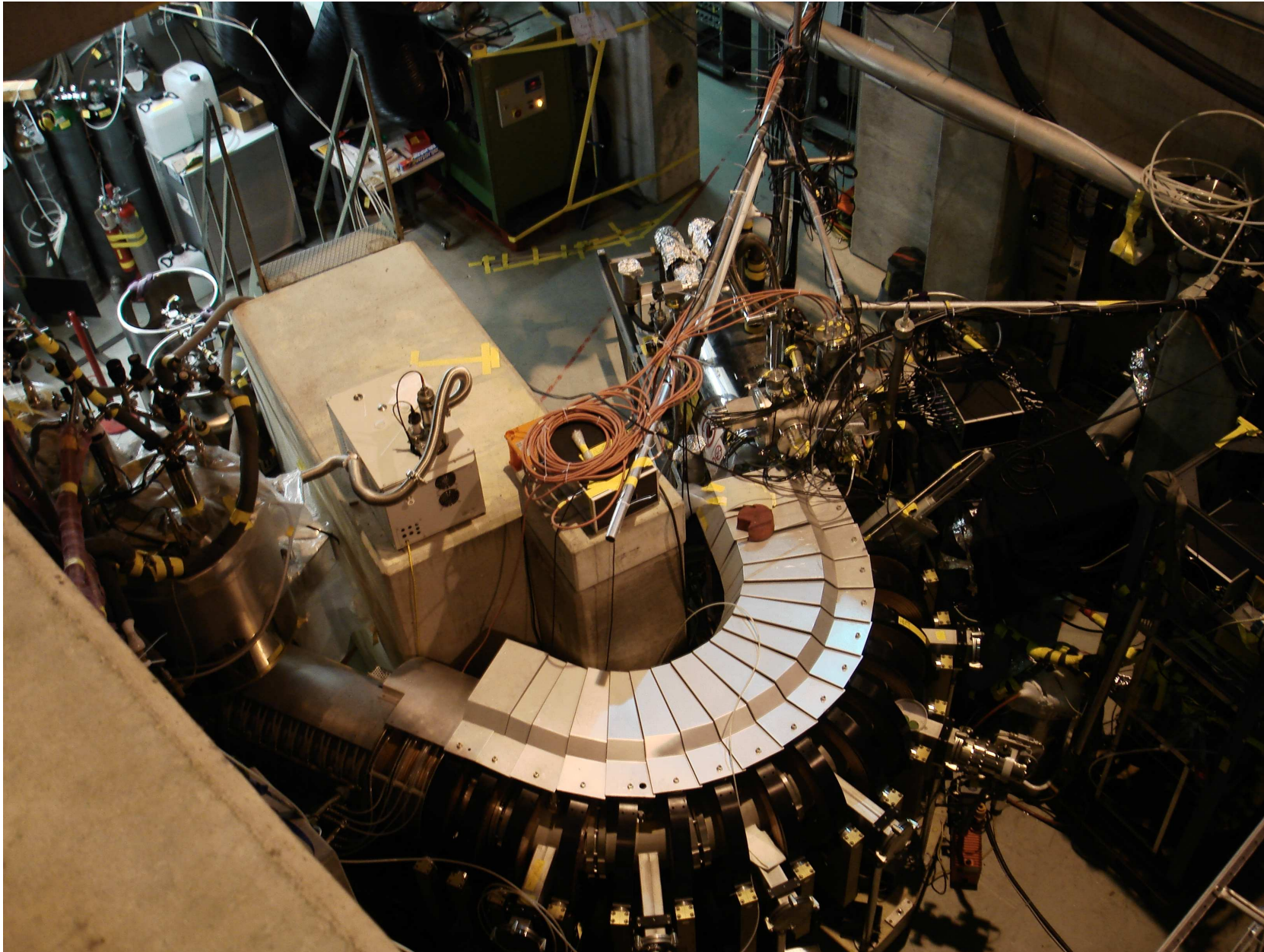
TiSa lasers



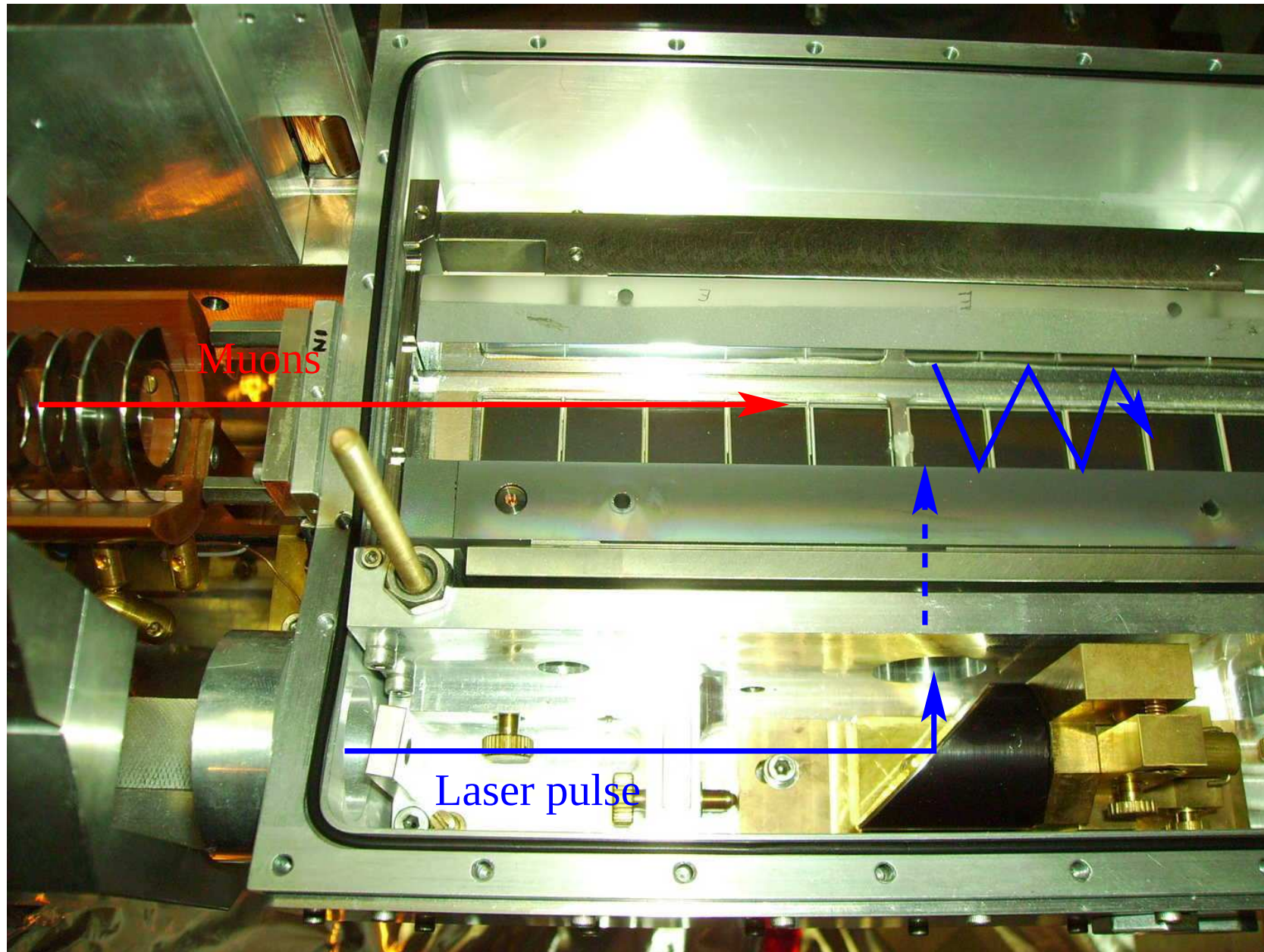
Laser beam tube



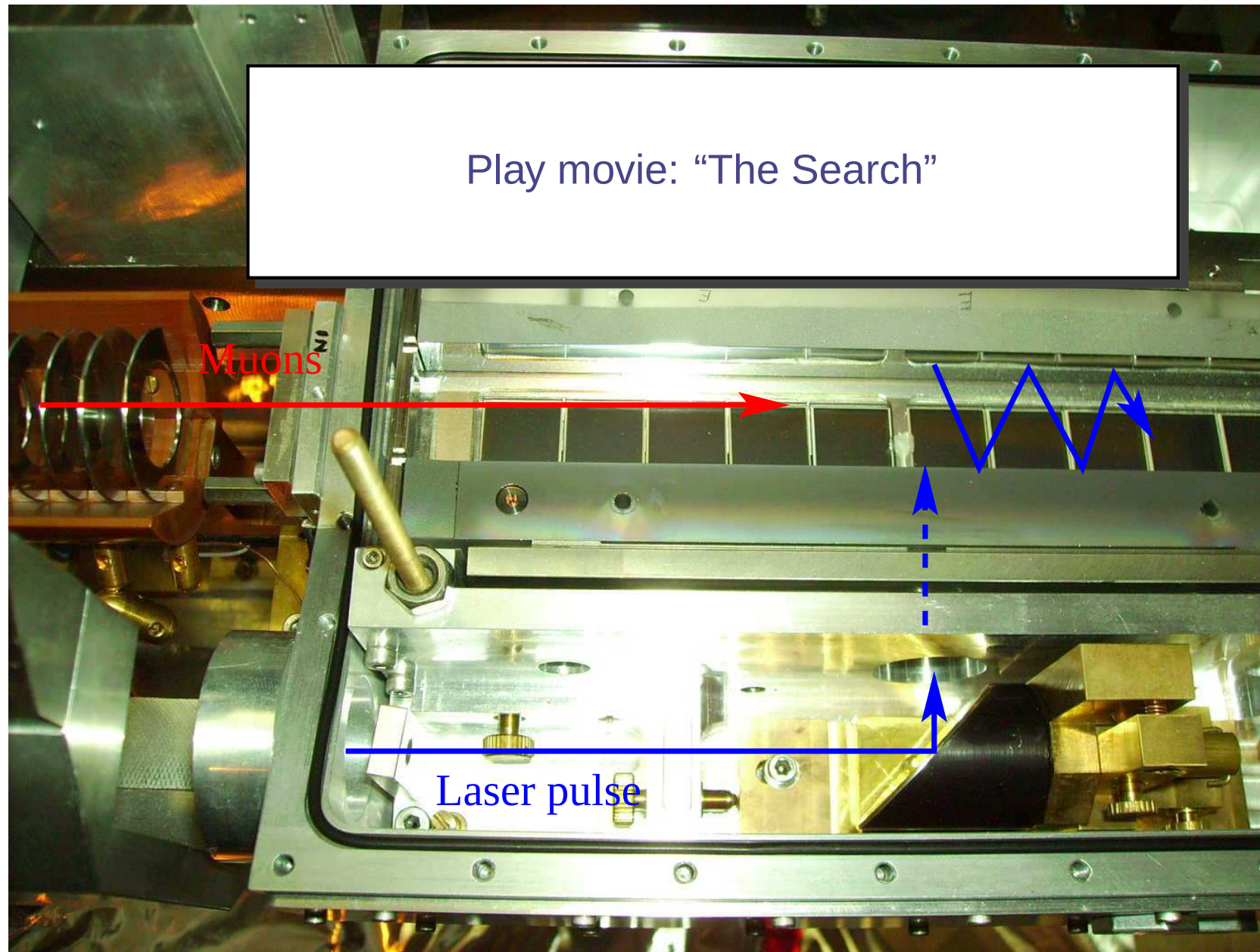
Muon beam line



Target, cavity and detectors



Target, cavity and detectors



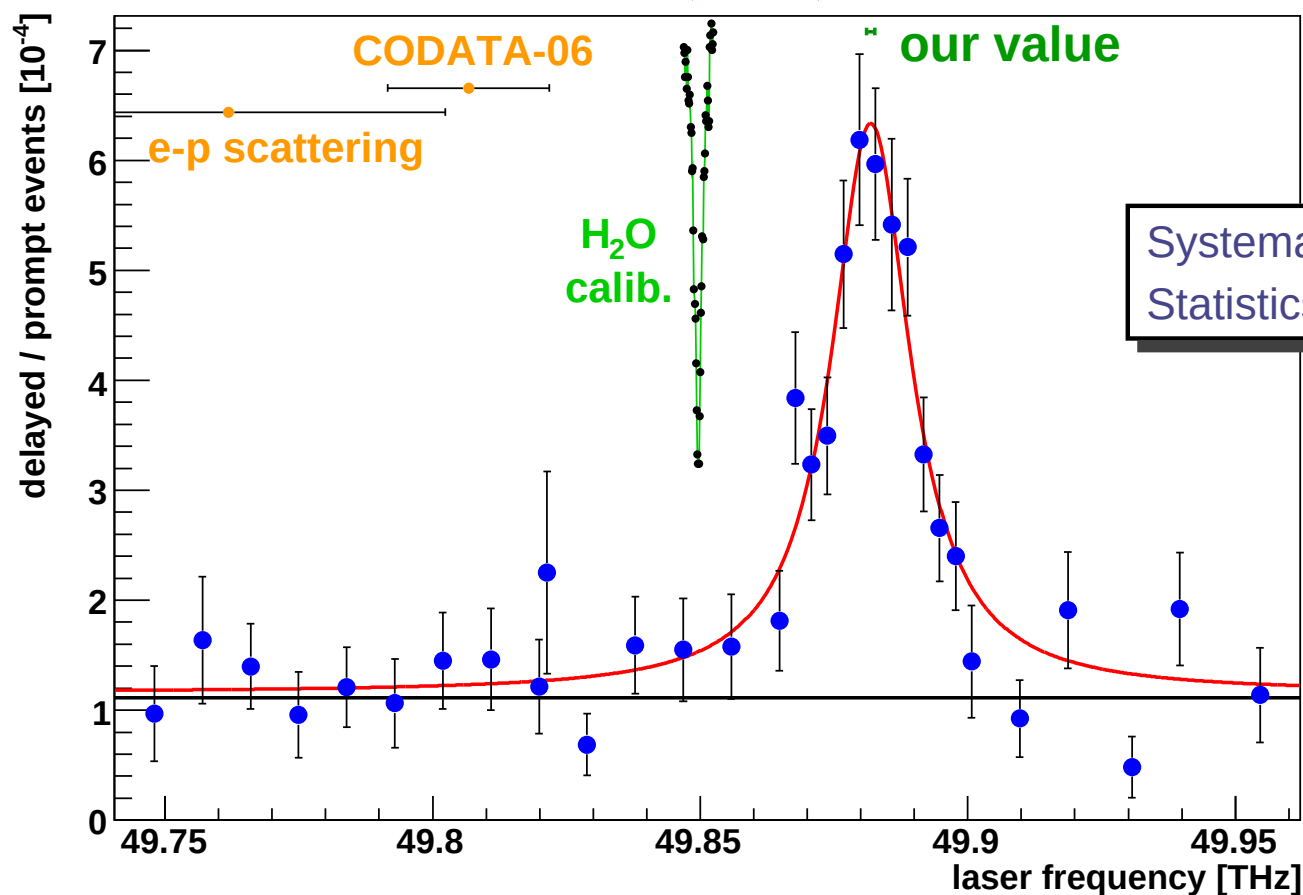
There are still surprises in physics.

The resonance: discrepancy, sys., stat.



Water-line/laser wavelength:
300 MHz uncertainty

$\Delta\nu$ water-line to resonance:
200 kHz uncertainty



Discrepancy:

$$5.0\sigma \leftrightarrow 75 \text{ GHz} \leftrightarrow \delta\nu/\nu = 1.5 \times 10^{-3}$$

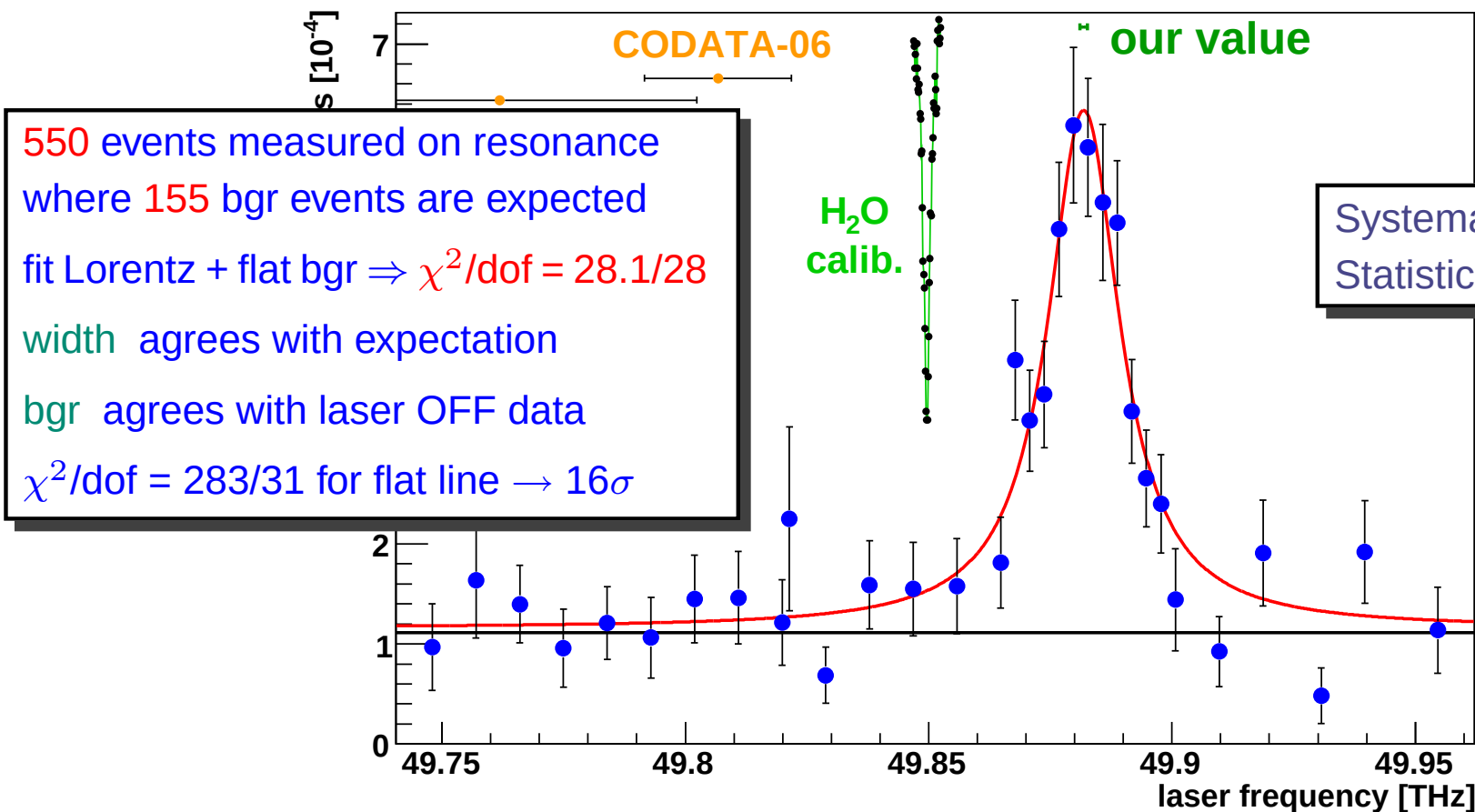
R. Pohl *et al.*, Nature 466, 213 (2010).

The resonance: discrepancy, sys., stat.



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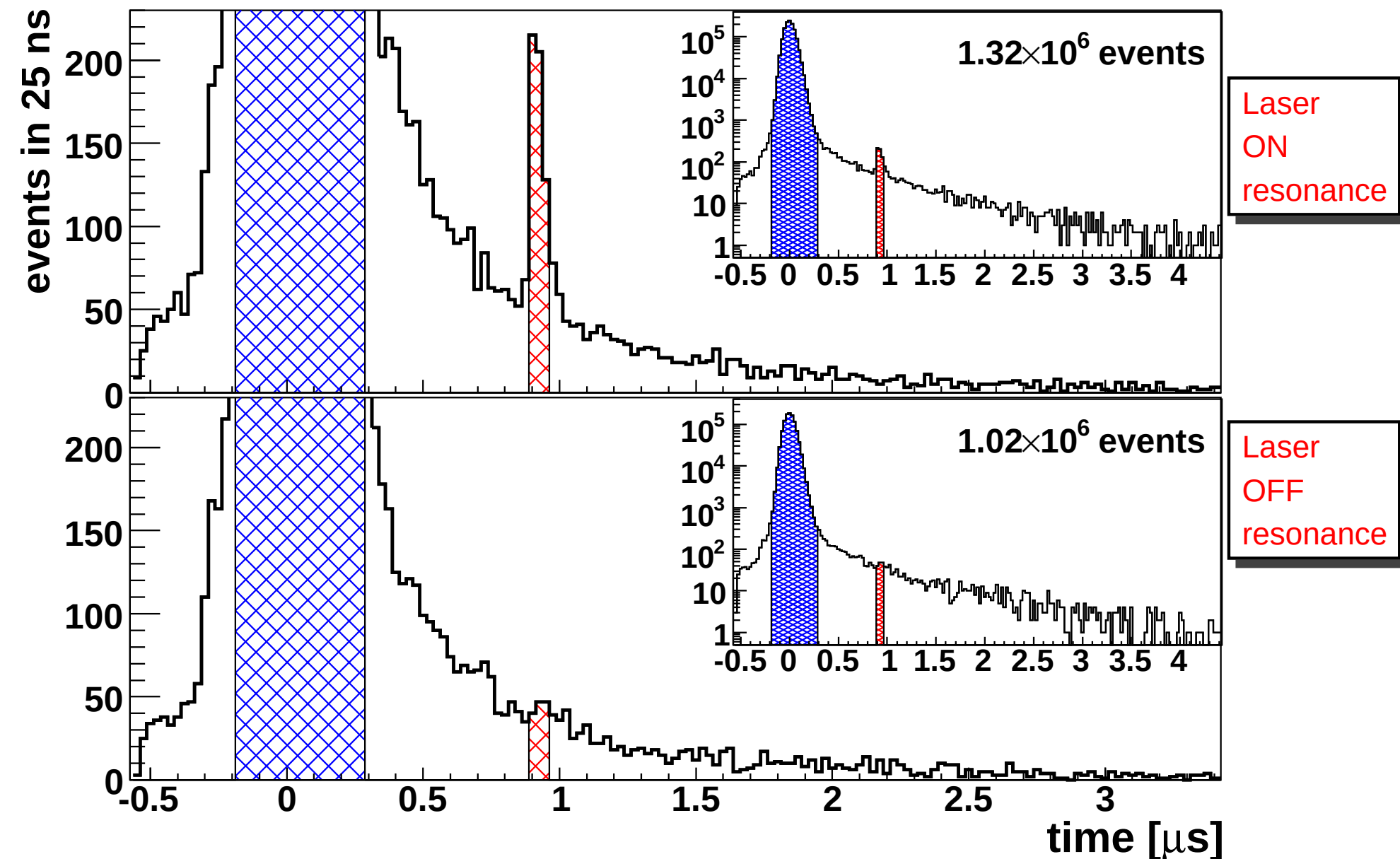


Discrepancy:

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R. Pohl *et al.*, Nature 466, 213 (2010).

The time spectra



Uncertainty budget and sensitivity



- Statistics

Center position uncertainty ($\sim 4\%$ of Γ) 700 MHz

- Systematics

Laser frequency (H_2O calibration) 300 MHz

AC and DC stark shift < 1 MHz

Zeeman shift (5 Tesla) < 30 MHz

Doppler shift < 1 MHz

Collisional shift 2 MHz

• Total uncertainty of the line determination 760 MHz

• Theory: proton polarizability 1200 MHz

• Discrepancy with CODATA prediction 75 300 MHz

Systematic effects are small since they scale like $1/m$

Finite size effect scales like m^3

Uncertainty budget and sensitivity



- Statistics

Center position uncertainty ($\sim 4\%$ of Γ) ~~700 MHz~~ 540 MHz

- Systematics

Laser frequency (H_2O calibration) 300 MHz

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Zeeman shift (5 Tesla) < 30 MHz

Doppler shift < 1 MHz

Collisional shift 2 MHz

• Total uncertainty of the line determination ~~760 MHz~~ 620 MHz

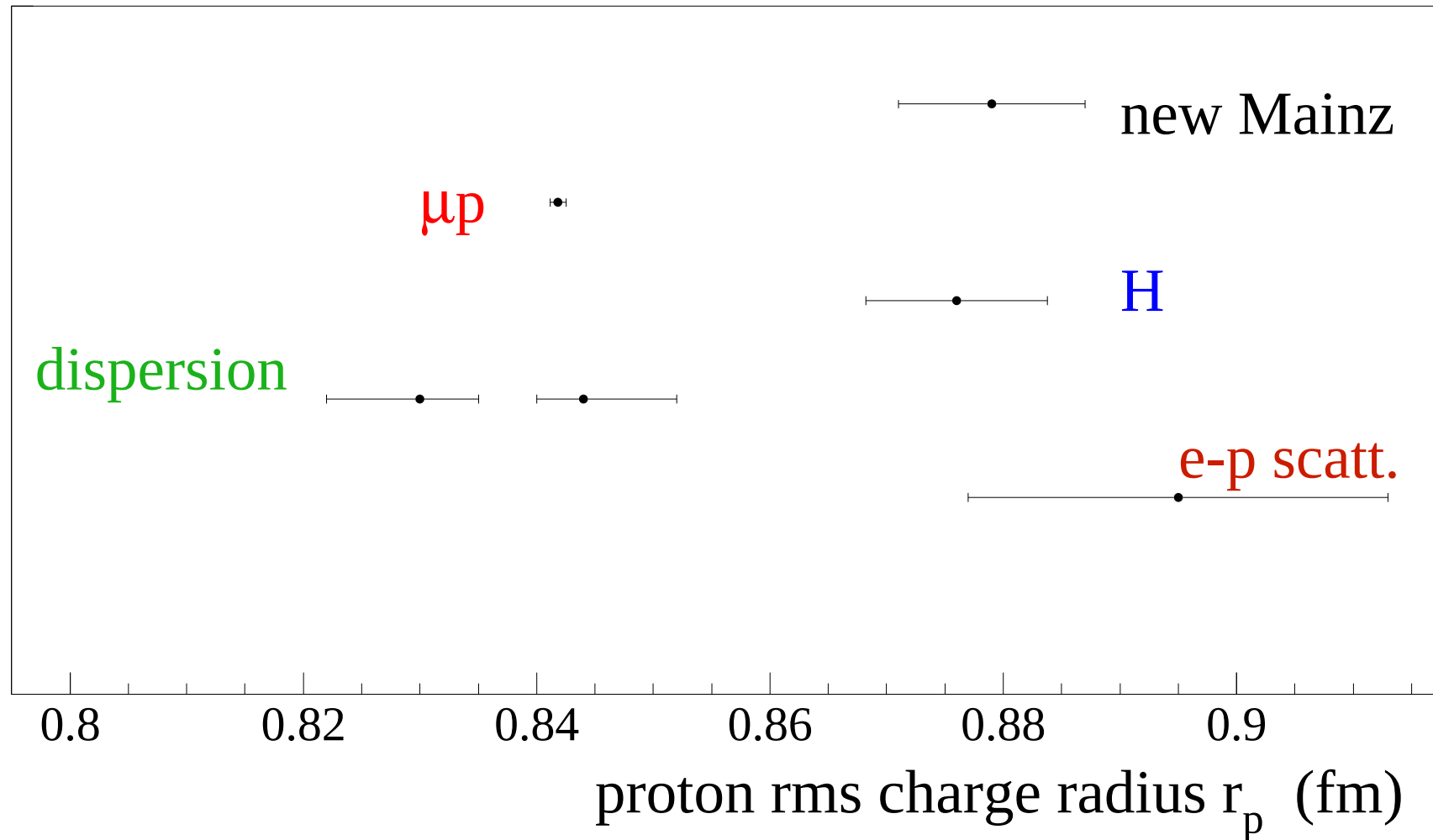
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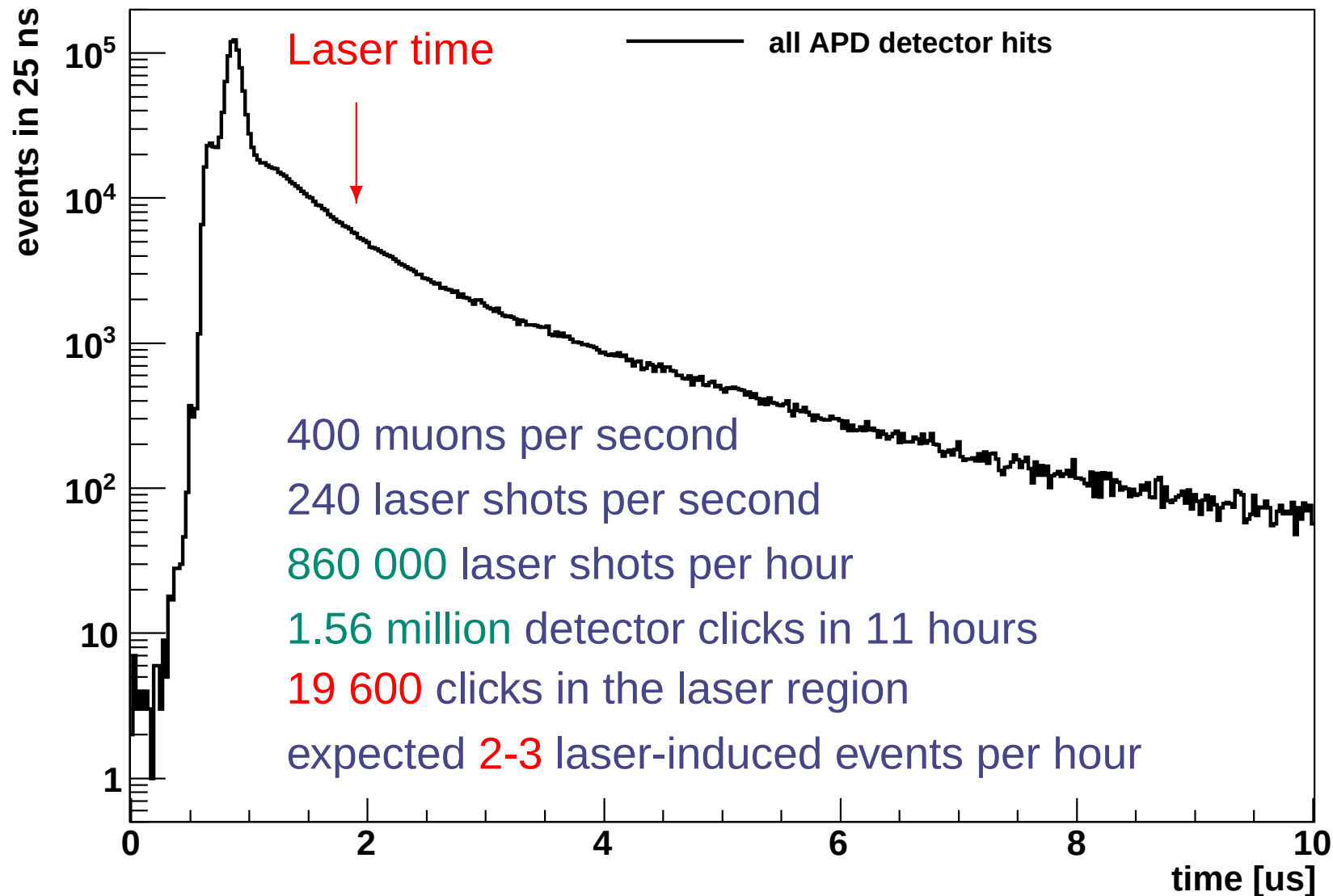
Finite size effect scales like m^3

$$r_p = 0.84184 (36)_{\text{exp}} (56)_{\text{theo}} \text{ fm}$$

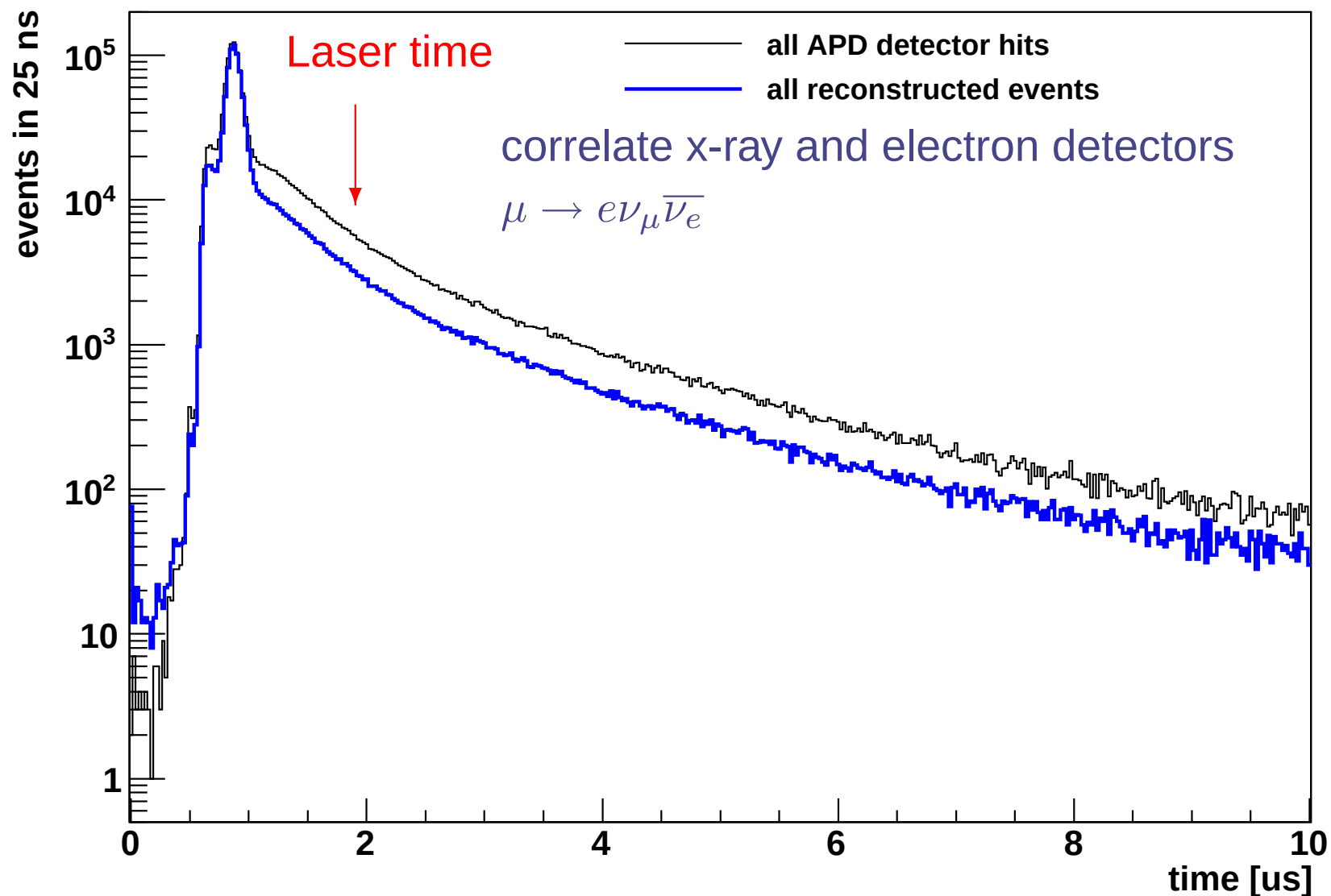


R. Pohl *et al.*, Nature 466, 213 (2010).

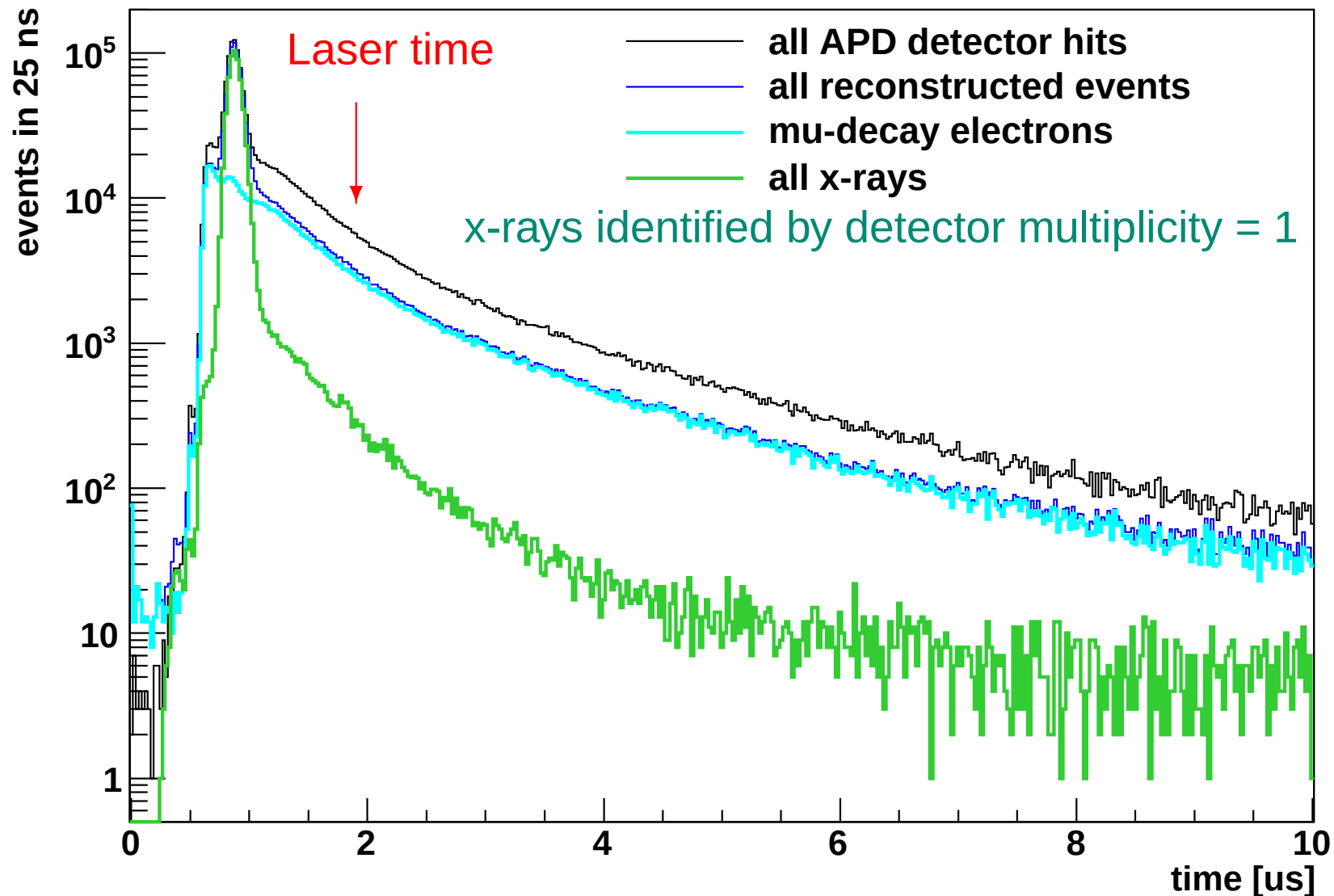
FP 900, 11 hours measurement



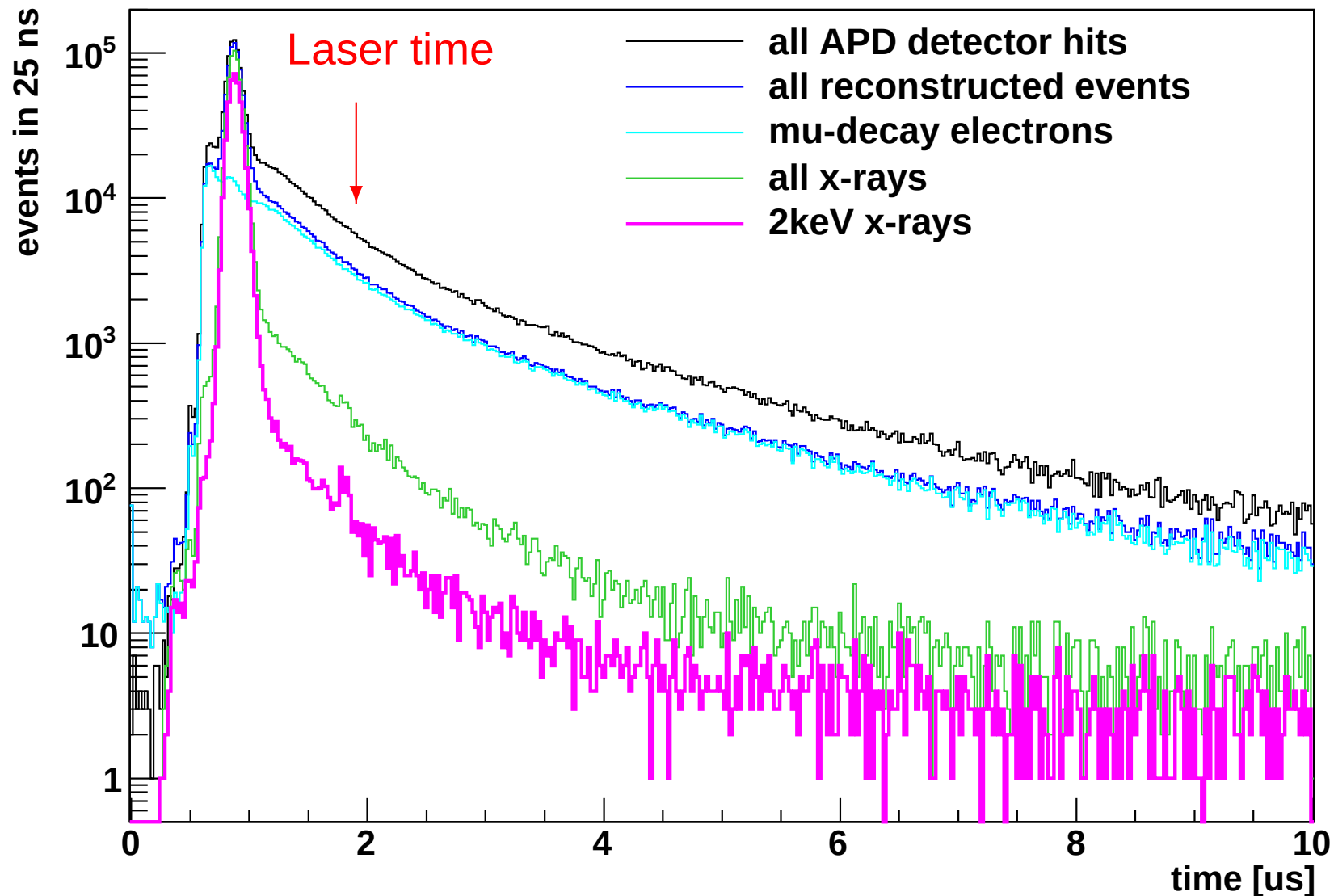
FP 900, 11 hours measurement



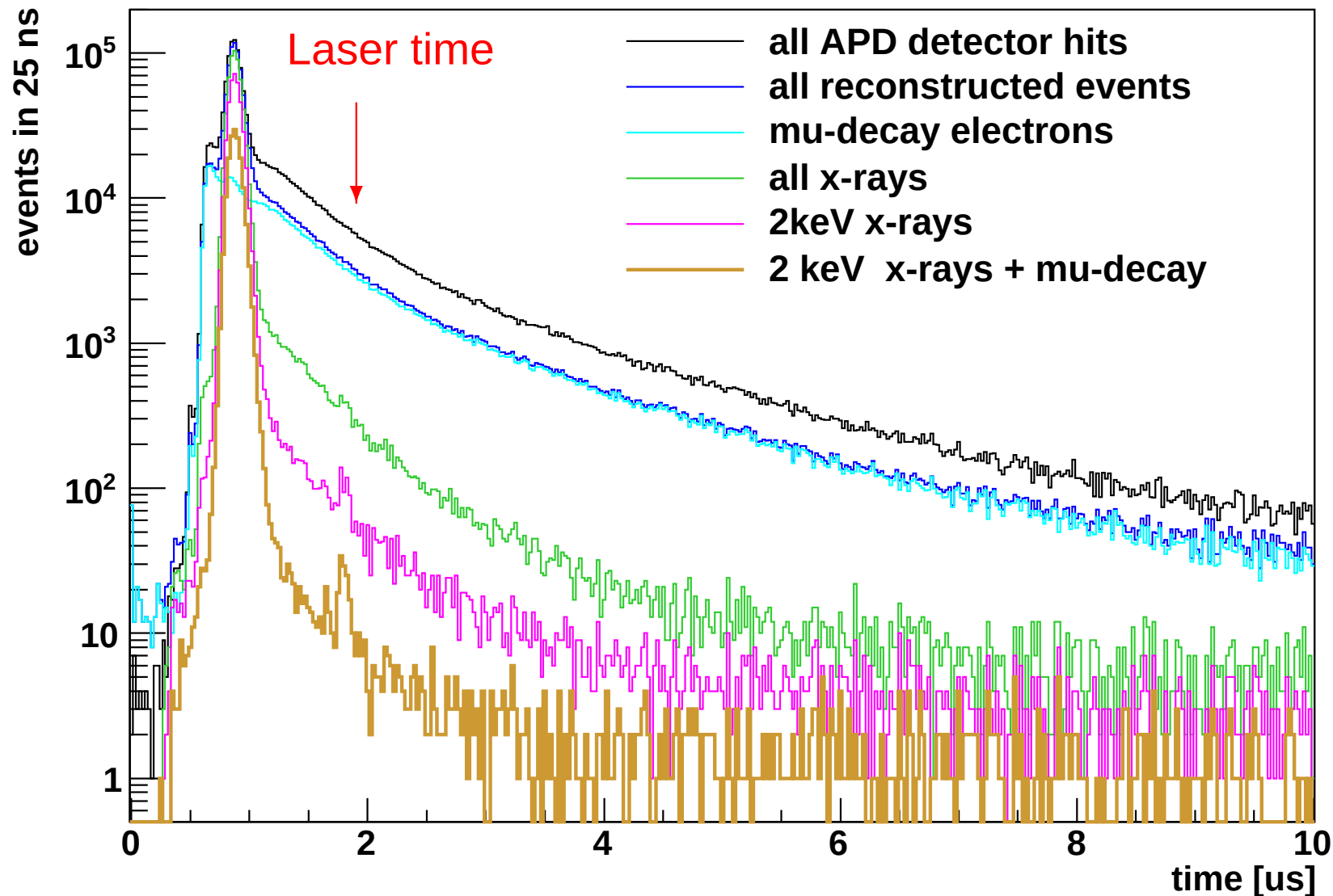
FP 900, 11 hours measurement



FP 900, 11 hours measurement



FP 900, 11 hours measurement

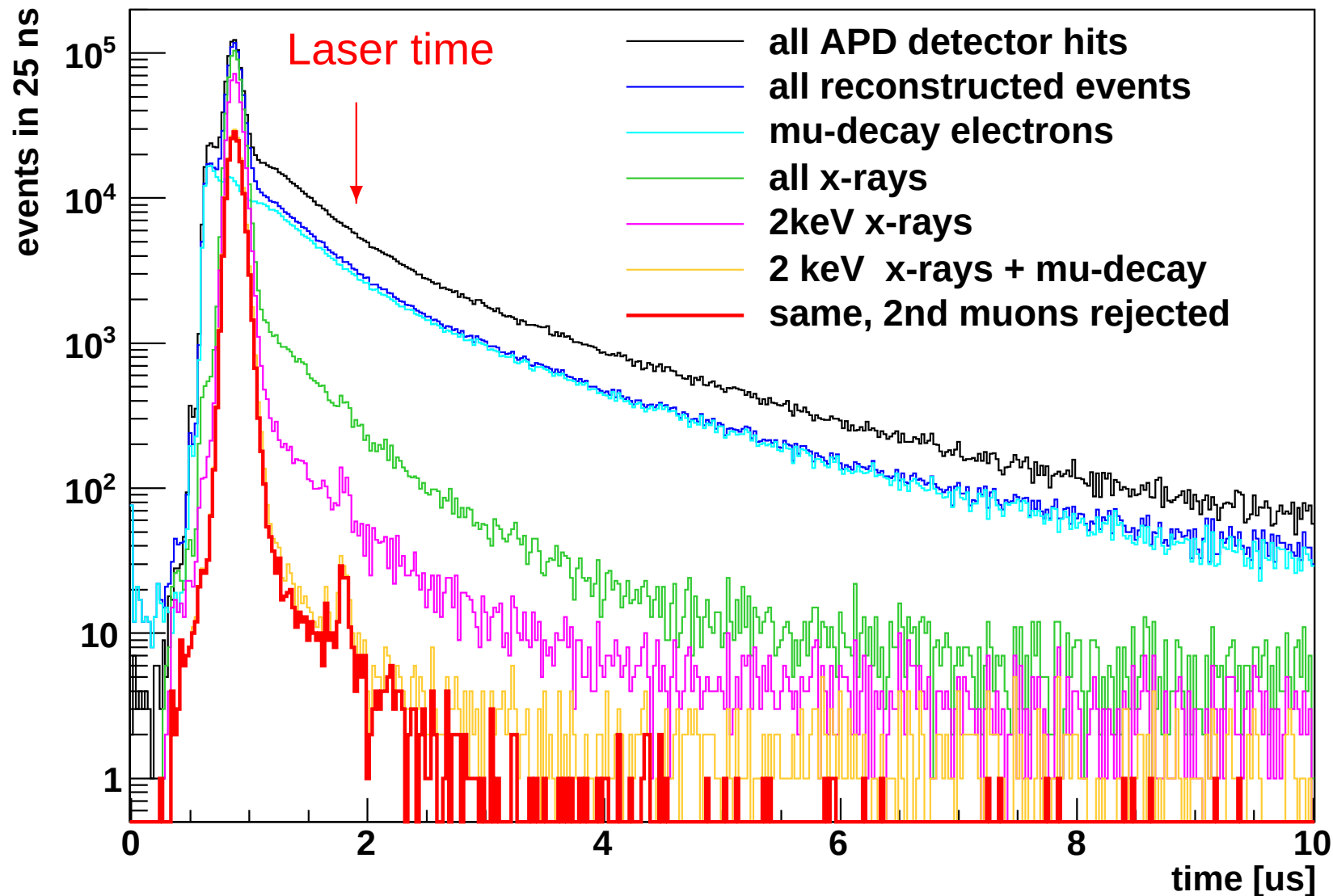


Data analysis

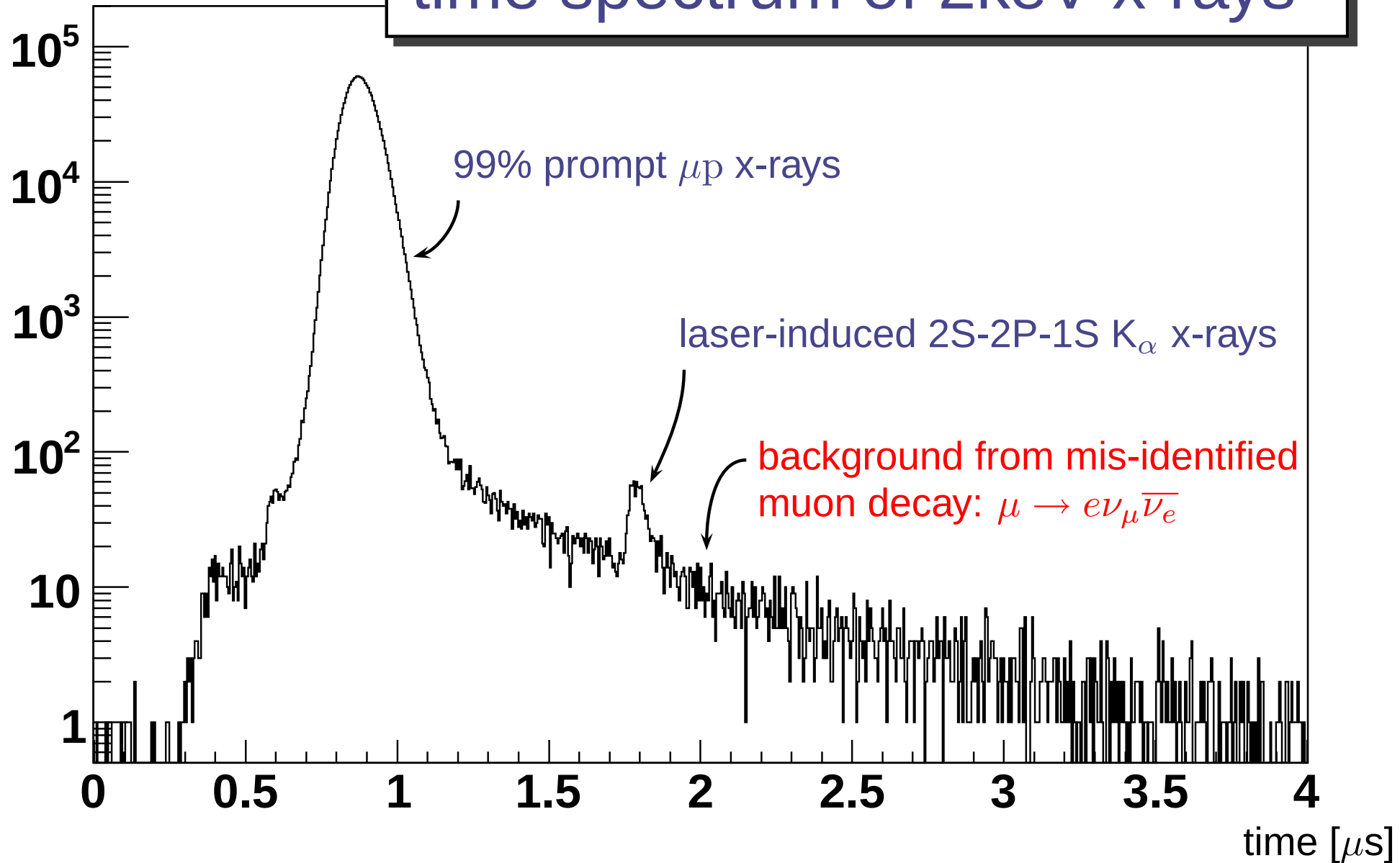


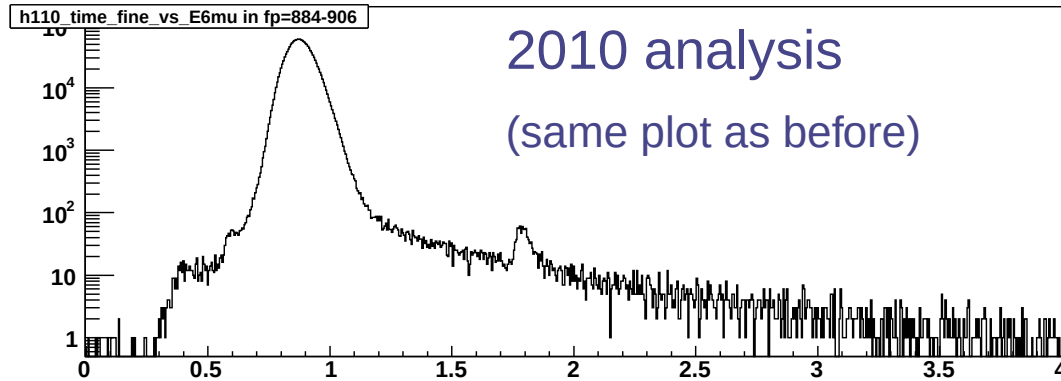
FP 900, 11 hours measurement

6 signal events per hour on resonance!
1 bgr. event/hour



time spectrum of 2keV x-rays





golden event class:

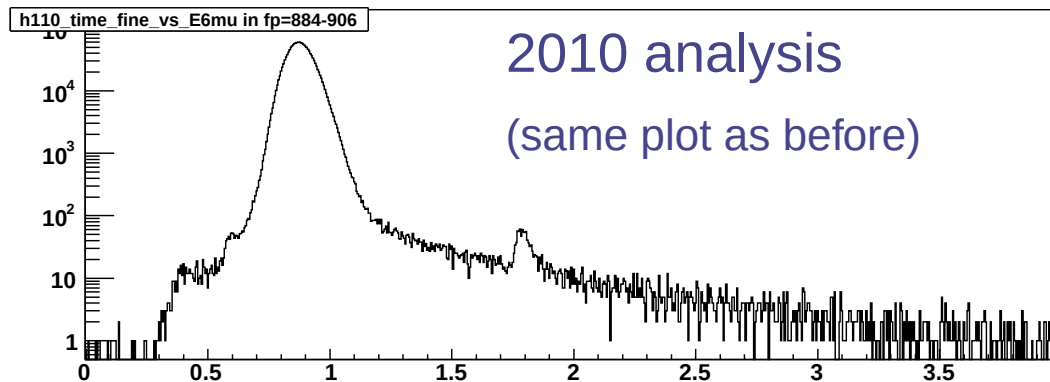
2 keV x-ray , followed by a μ -decay electron

e.g. $[0.2 \dots 5.2] \mu\text{s}$ after the x-ray

several ways to detect μ decay electrons

statistics vs. quality

Divide above data into....



golden event class:

2 keV x-ray , followed by a μ -decay ele

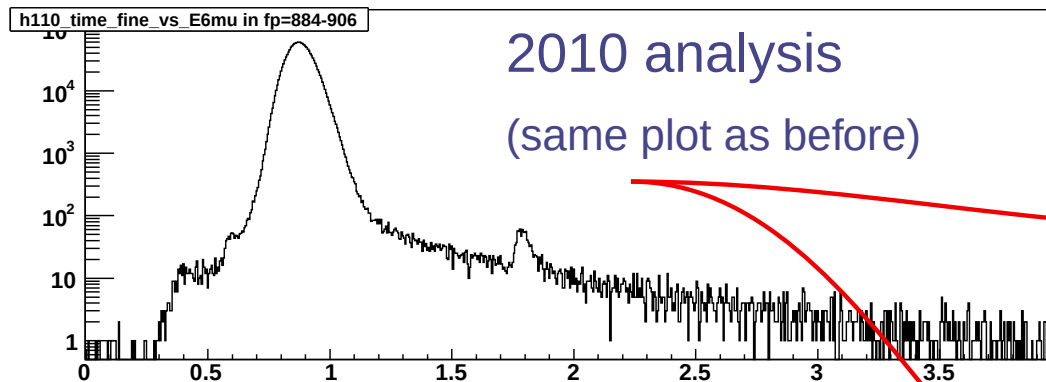
e.g. $[0.2 \dots 5.2] \mu\text{s}$ after the x-ray

several ways to detect μ decay electron
statistics vs. quality

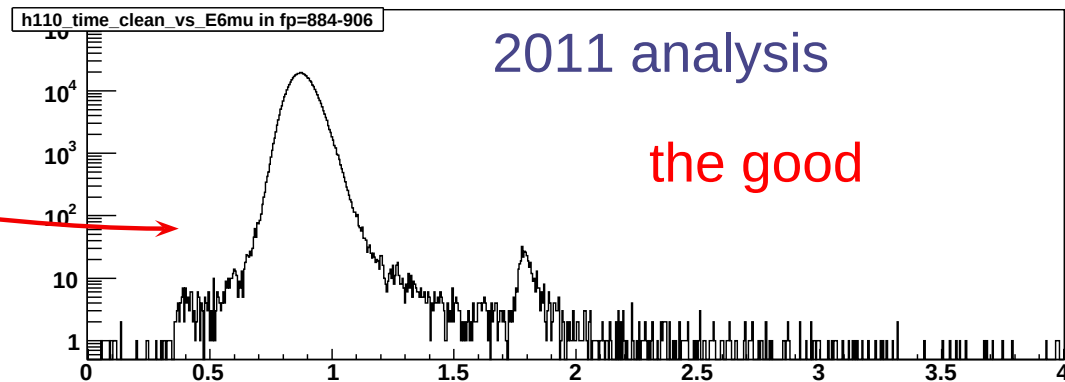
Divide above data into



Data analysis 2011



2010 analysis
(same plot as before)

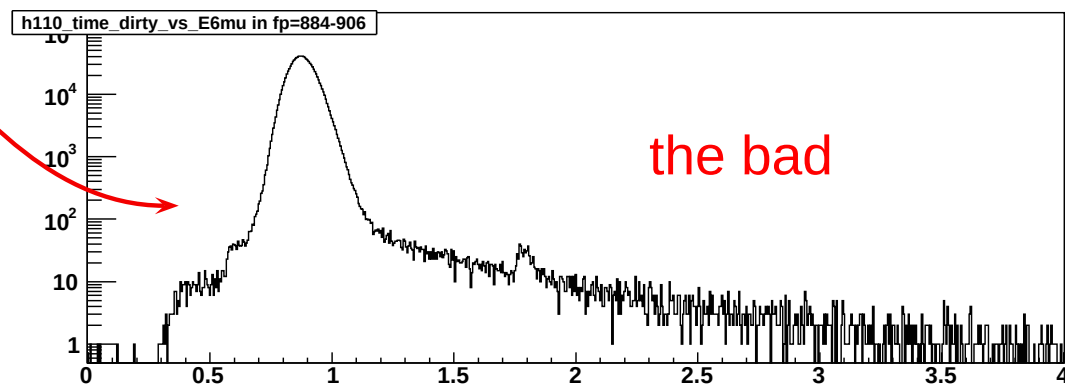


2011 analysis
the good

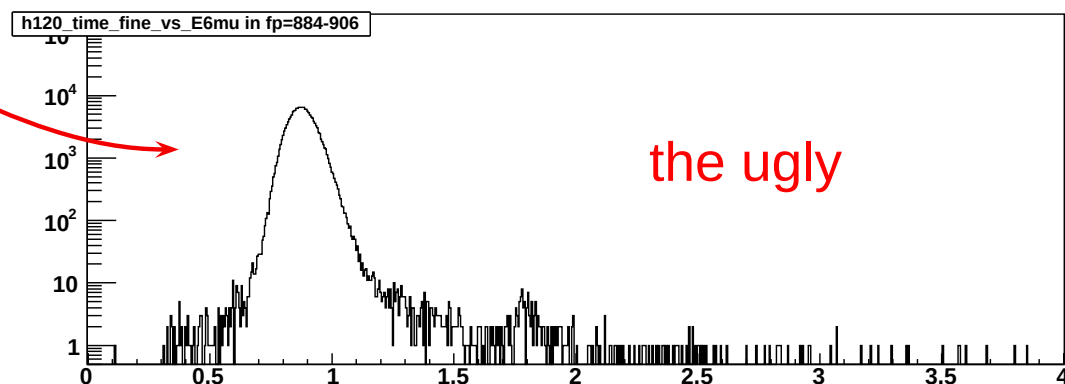
split "2010 data" (Nature)

add previously discarded data

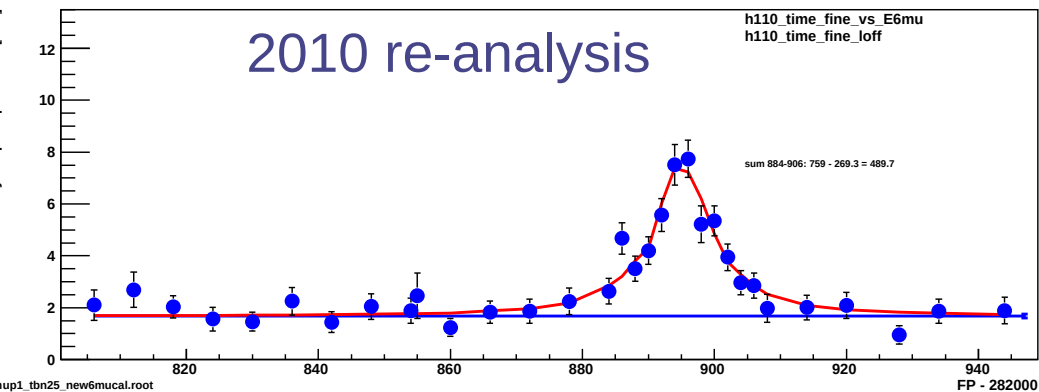
fit 3 resonances simultaneously
common position and width



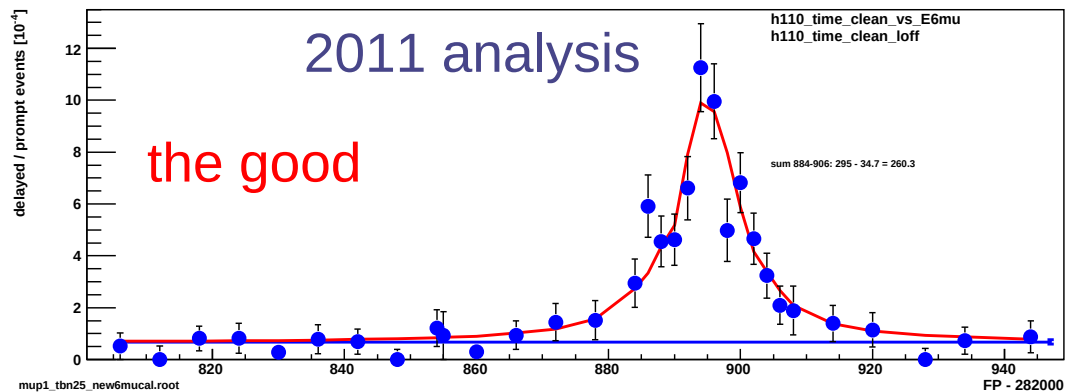
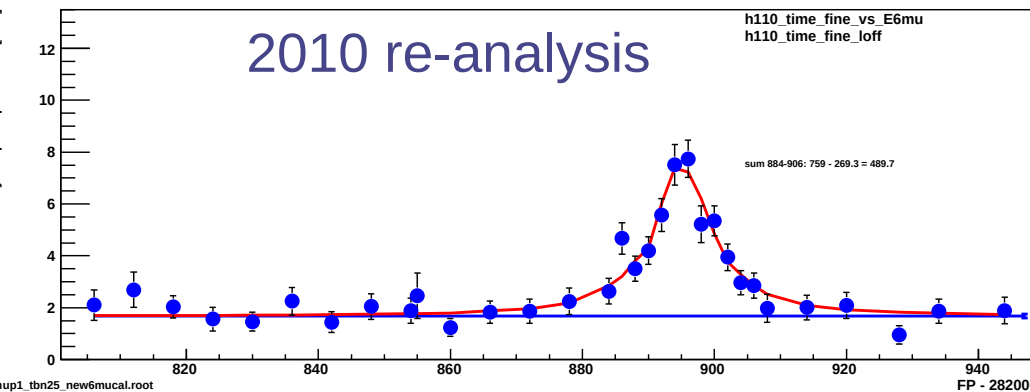
the bad



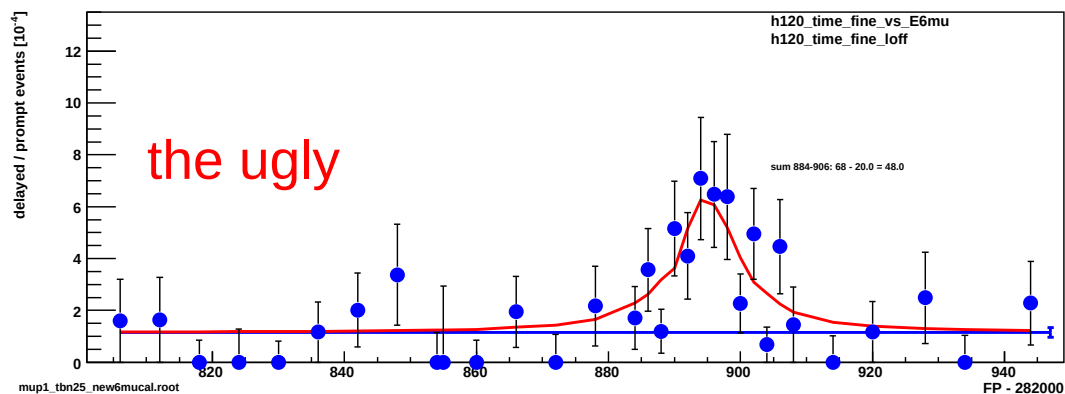
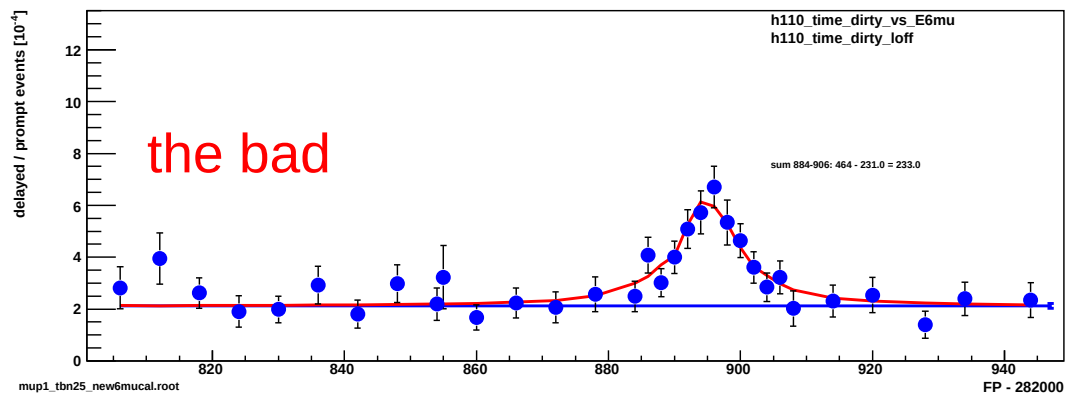
the ugly



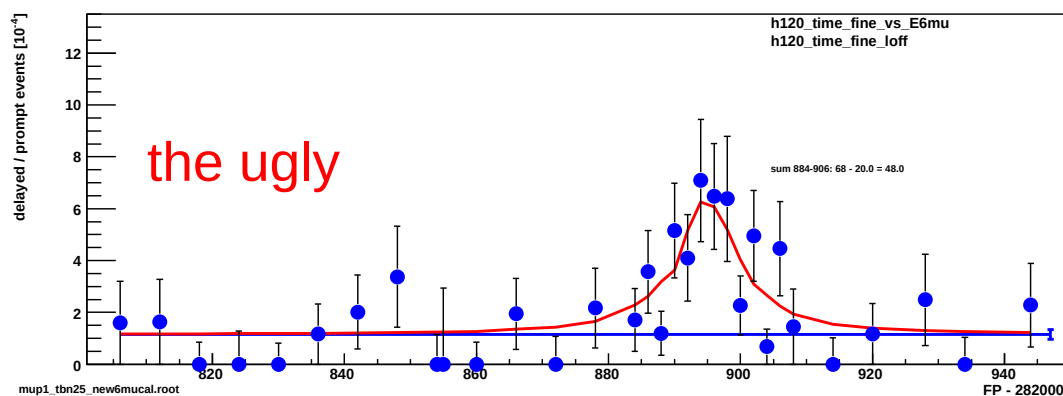
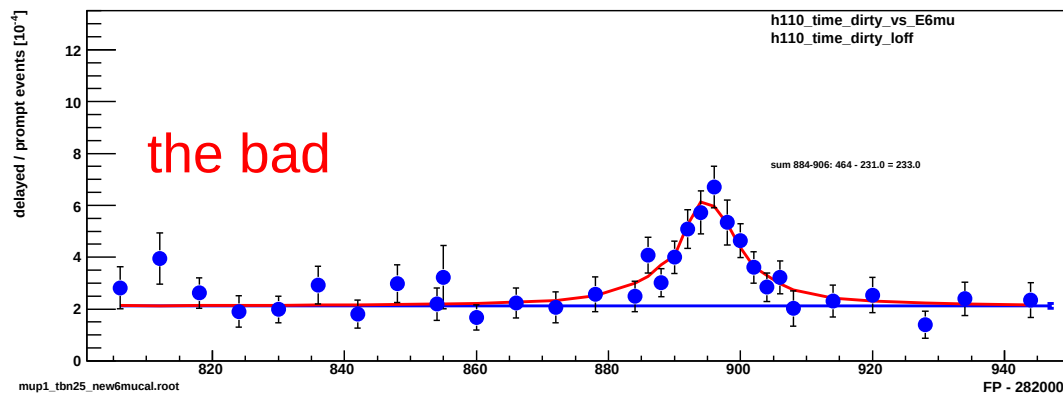
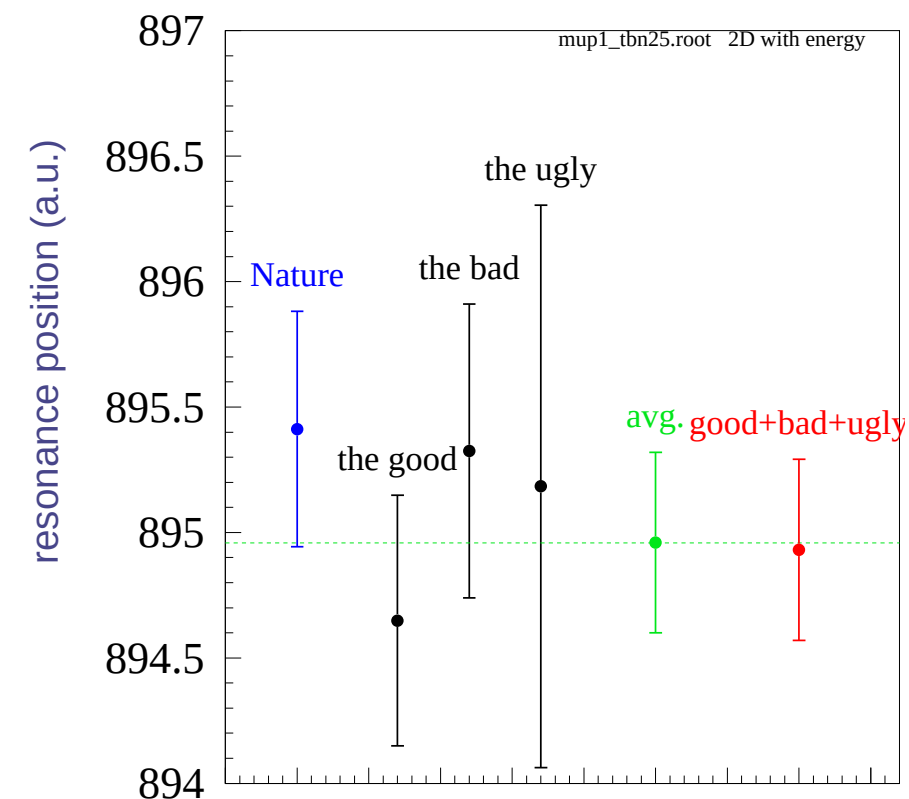
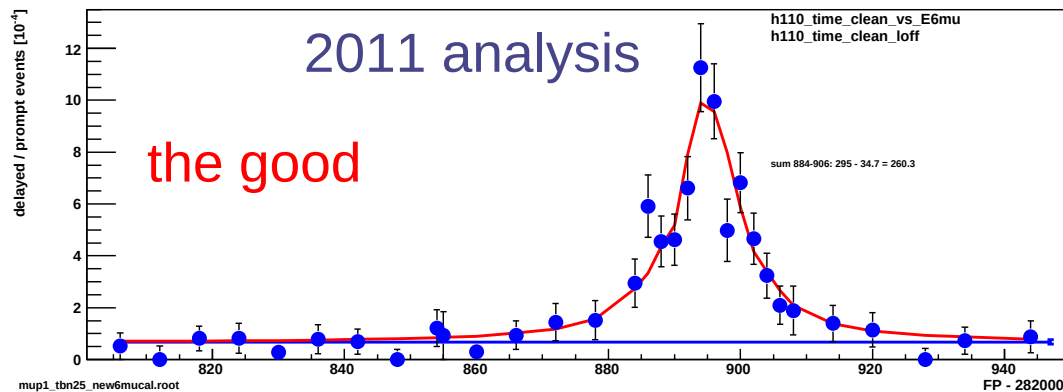
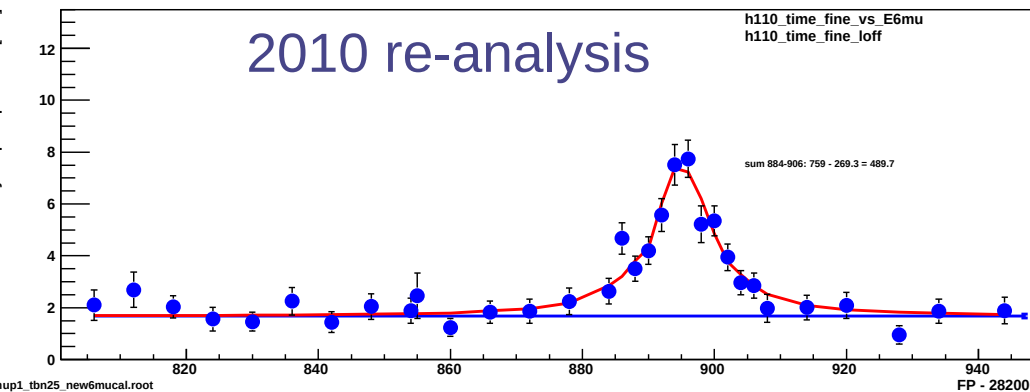
resonance plots



resonance plots



Data analysis 2011



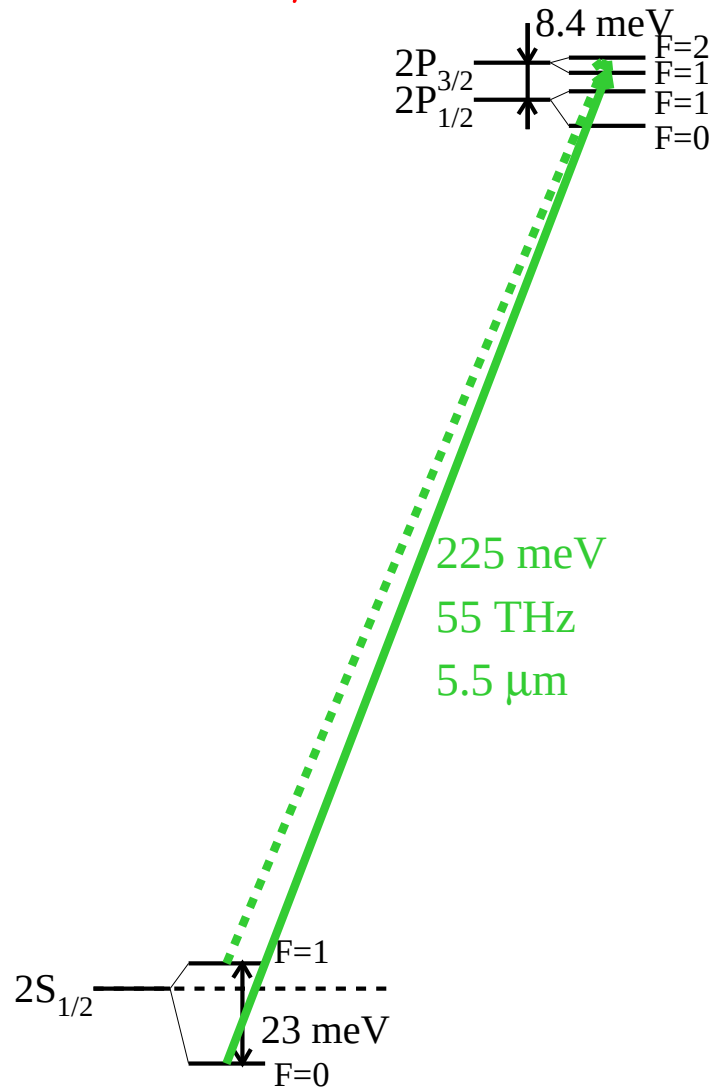
New data

2nd line in muonic hydrogen



$\mu p (2S_{1/2}(F=0) \rightarrow 2P_{3/2}(F=1))$

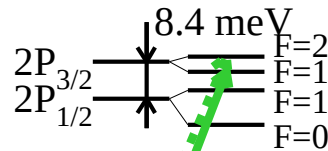
at $\lambda = 5.5 \mu\text{m}$



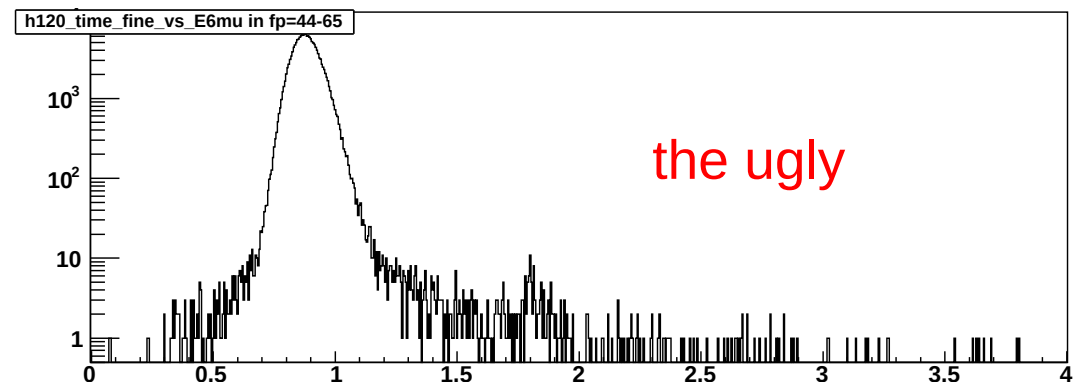
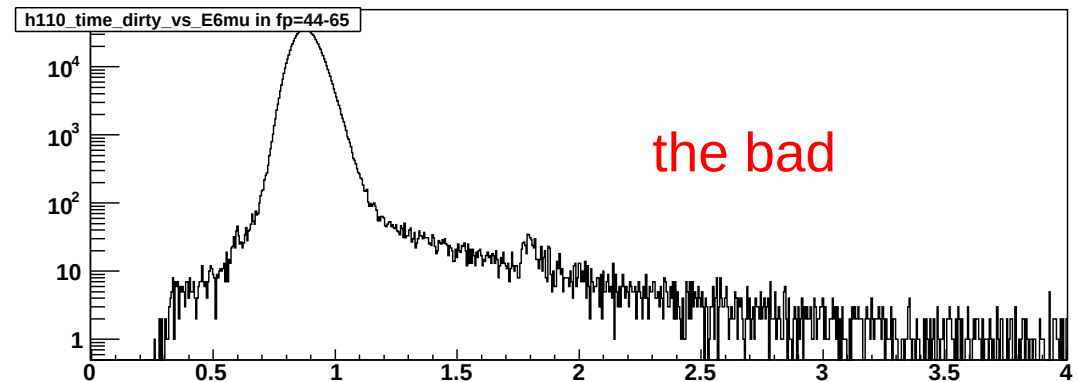
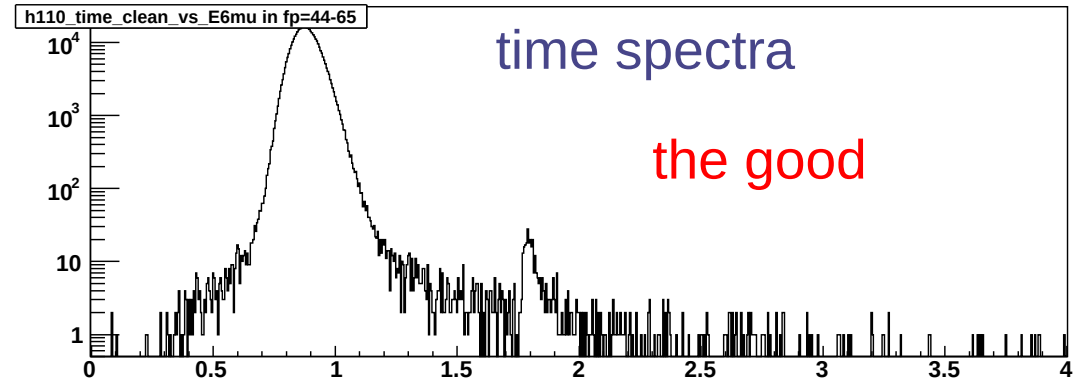
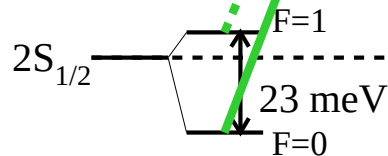
2nd line in muonic hydrogen

$$\mu p (2S_{1/2}(F=0) \rightarrow 2P_{3/2}(F=1))$$

at $\lambda = 5.5 \mu\text{m}$



225 meV
55 THz
5.5 μm

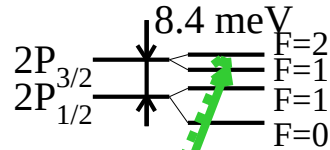


2nd line in muonic hydrogen

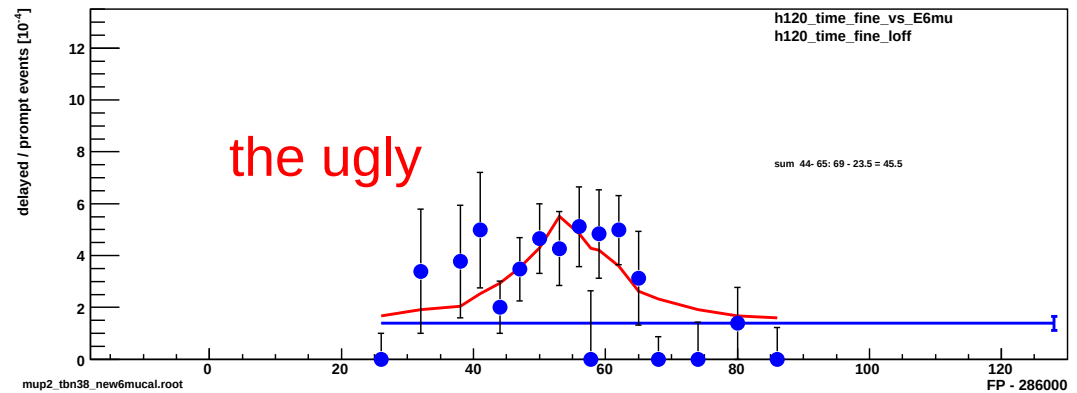
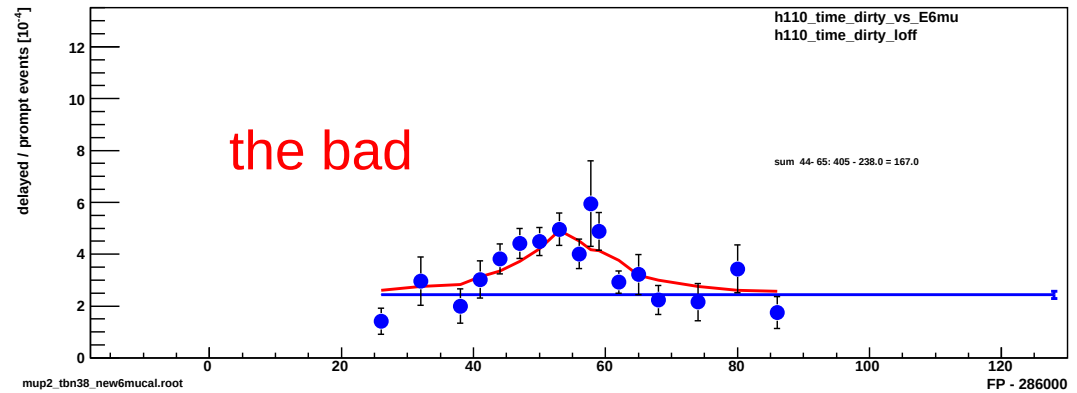
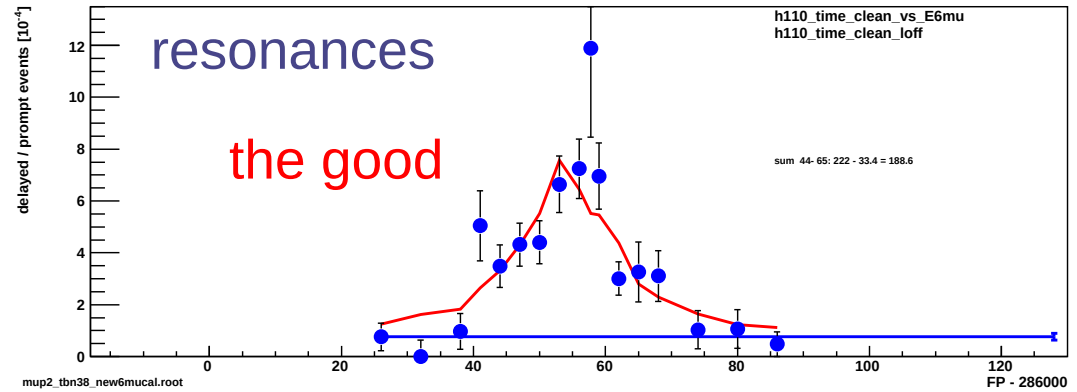
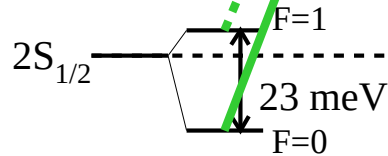


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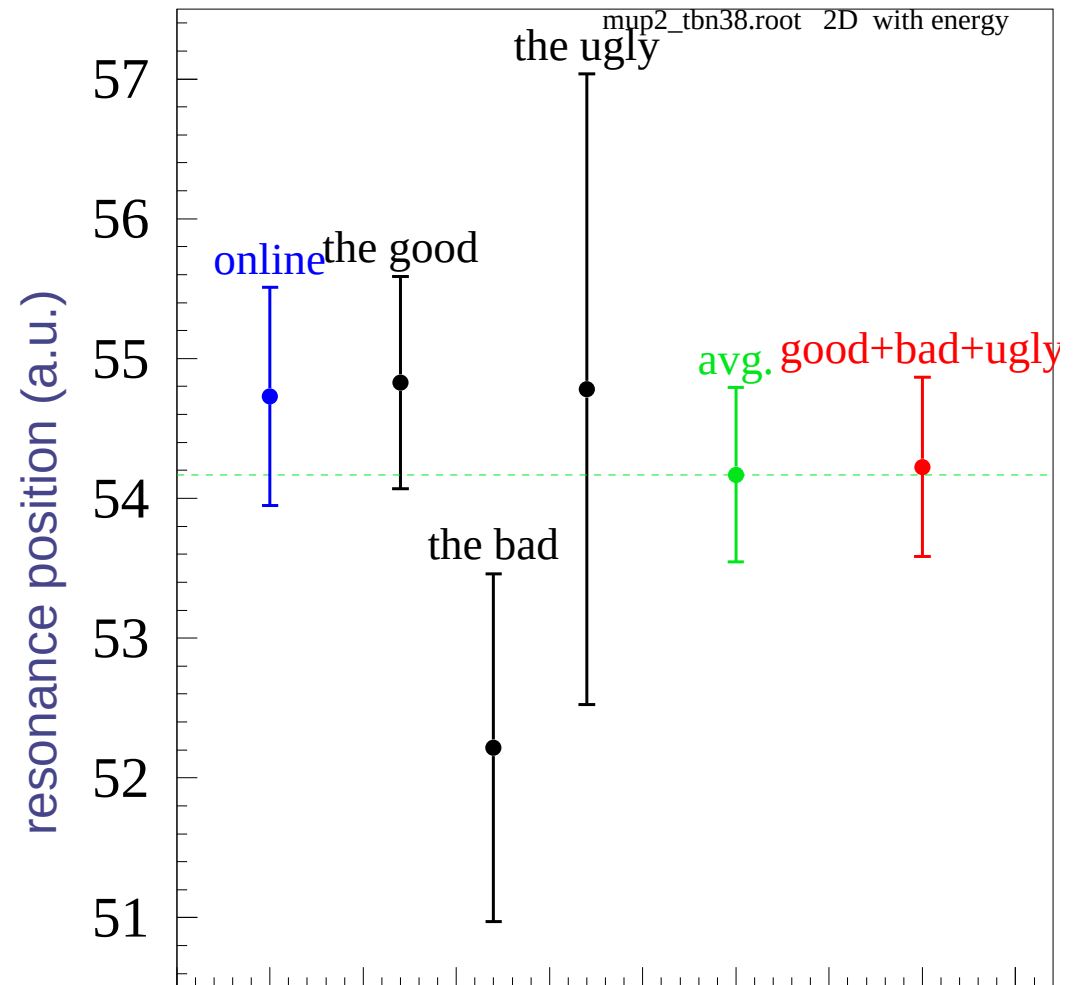
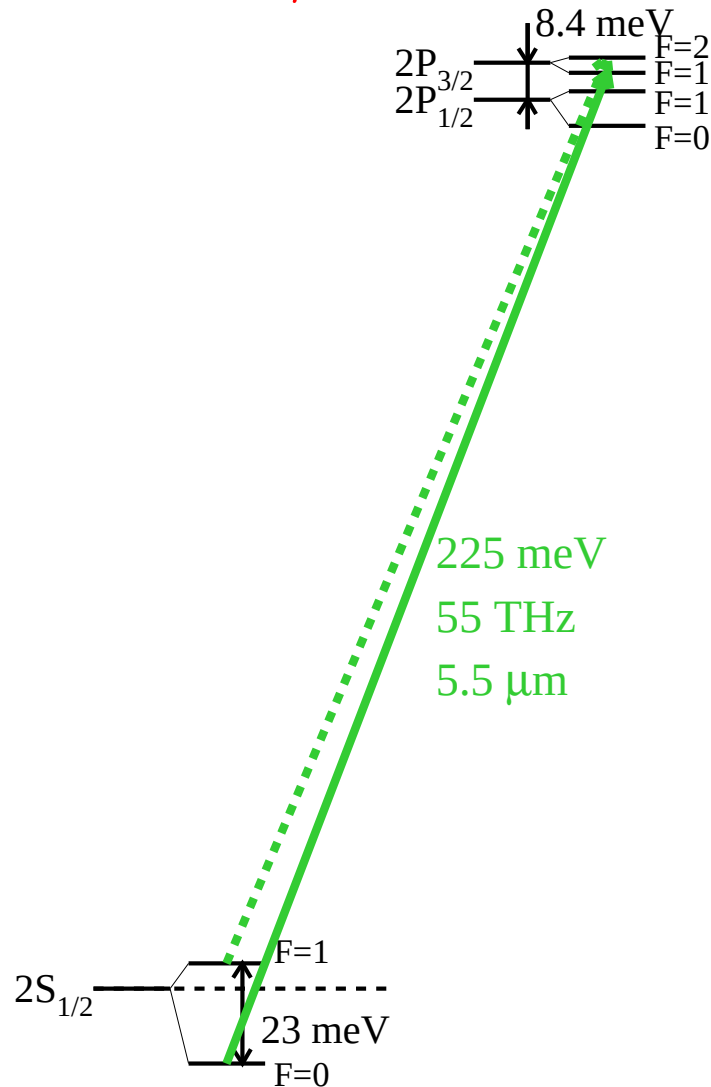


2nd line in muonic hydrogen



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Results on muonic hydrogen



Transition frequencies:

$$\nu(2S_{1/2}^{F=1} \rightarrow 2P_{3/2}^{F=2}) = 49881.88(76) \text{ GHz} \quad \text{R. Pohl et al., Nature 466, 213 (2010)}$$

$$49881.16(62) \text{ GHz} \quad \text{PRELIMINARY 2011}$$

$$\nu(2S_{1/2}^{F=0} \rightarrow 2P_{3/2}^{F=1}) = 54611.87(1.01) \text{ GHz} \quad \text{PRELIMINARY 2011}$$

Proton radius **using 2010 theory**

$$\nu(2S_{1/2}^{F=1} \rightarrow 2P_{3/2}^{F=2}) : 0.84184(36)(56) \text{ fm} \quad \text{R. Pohl et al., Nature 466, 213 (2010)}$$

$$0.84218(29)(56) \text{ fm} \quad \text{PRELIMINARY 2011}$$

$$\nu(2S_{1/2}^{F=0} \rightarrow 2P_{3/2}^{F=1}) : 0.84252(48)(85) \text{ fm} \quad \text{PRELIMINARY 2011}$$

Results on muonic hydrogen

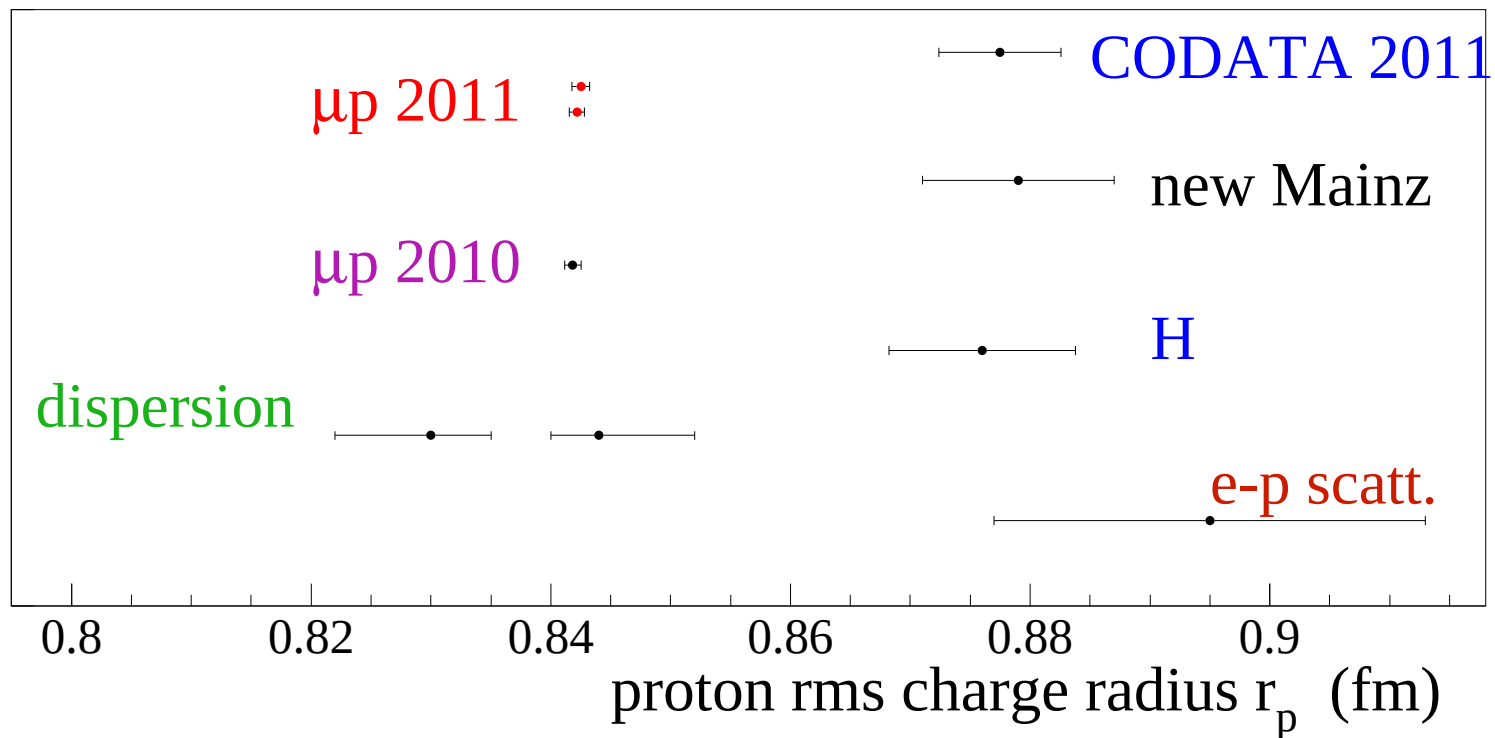


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Proton radius puzzle



From the **two transitions** in muonic hydrogen we extract a **PRELIMINARY** value of the proton rms charge radius of

$$r_p = 0.84284(58) \text{ fm} \quad (u_r = 6.8 \times 10^{-4})$$

$$u_{\text{exp}} = 3.0 \times 10^{-4}$$

$$u_{\text{theo}} = 6.2 \times 10^{-4}$$

BUT:

CODATA 2006: $r_p = (0.8768 \pm 0.0069) \text{ fm}$

Hydrogen: $r_p = (0.876 \pm 0.008) \text{ fm}$

e-p scattering: $r_p = (0.895 \pm 0.018) \text{ fm}$ (Sick 2005)

r_p is 4% smaller

5.0σ from CODATA-2006

4.3σ from H

3.1σ from e-p scatt.

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$r_p = (0.879 \pm 0.008) \text{ fm}$ (Mainz 2010)

$r_p = (0.875 \pm 0.010) \text{ fm}$ (JLab Hall A 2011)

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BUT:

CODATA 2010: $r_p = (0.8775 \pm 0.0051) \text{ fm}$

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6.8 σ from CODATA-2010

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4.3 σ from H

8.4 σ from scatt.

What's wrong ??

What's wrong ??



- PRA **81**, 060501 (2010) Karshenboim et al.: “Nonrelativistic contributions of order $\alpha^5 m_\mu c^2$ to the Lamb shift in muonic ...” (1005.4879)
- JETP Lett. **92**, 8 (2010) Karshenboim et al.: “Contribution of light-by-light scattering to energy levels of light muonic atoms” (1005.4880)
- PRL **105**, 242001 (2010) Bernauer et al.: “High-precision determination of the electric and magnetic form factors of the proton” (1007.5076)
- PRD **82**, 125020 (2010) Jaeckel, Roy: “Spectroscopy as a test of Coulomb’s law” (1008.3536)
- PLB **693**, 555 (2010) De Rujula: “QED is not endangered by the proton’s size” (1008.3861)
- Nucl.Phys.News **21**, 14 (2011) Vanderhaeghen, Walcher: “Long range structure of the nucleon” (1008.4225)
- Can. J. Phys. **89**, 109 (2011) Jentschura: “From first principles of QED to an application: hyperfine structure of P states of muonic hydrogen”
- PRC **83**, 012201(R) (2011) Cloet, Miller: “Third Zemach moment of the proton” (1008.4345)
- PRD **82**, 113005 (2010) Hill, Paz: “Model-independent extraction of the proton charge radius from electron scattering” (1008.4619)
- PLB **697**, 26 (2011) De Rujula: “QED confronts the proton’s radius” (1010.3421)
- PLB **696**, 343 (2011) Distler et al.: “The RMS radius of the proton and Zemach moments” (1011.1861)
- EPJD **61**, 7 (2011) Jentschura: “Proton radius, Darwin-Foldy term and radiative corrections” (1012.4029)
- PRL **106**, 153001 (2011) Barger, Chiang, Keung, Marfatia: “Proton size anomaly” (1011.3519)
- PRA **83**, 012507 (2011) Yerokhin: “Nuclear-size corrections to the Lamb shift of one-electron atoms” (1011.4272)
- PRD **83**, 101702(R) (2011) Tucker-Smith, Yavin: “Muonic hydrogen and MeV forces” (1011.4922)
- Ann. Phys. **326**, 500 (2011) Jentschura: “Lamb shift in muonic hydrogen I: Verification and update of theoretical predictions” (1011.5275)
- Ann. Phys. **326**, 516 (2011) Jentschura: “Lamb shift in muonic hydrogen II: Analysis of the discrepancy of theory and experiment” (1011.5453)
- Few-Body Syst. **50**, 367 (2011) Sick: “Troubles with the proton rms radius”
- PRD **83**, 035020 (2011) Brax, Burrage: “Atomic precision tests and light scalar couplings” (1010.5108)
- PRA **83**, 042509 (2011) Carlson et al.: “Proton-structure corrections to hyperfine splitting in muonic hydrogen” (1101.3239)
- PRL **106**, 193007 (2011) Pachucki: “Nuclear structure corrections in muonic deuterium” (1102.3296)
- PRL **107**, 011803 (2011) Batell, McKeen, Pospelov: “New parity-violating muonic forces and the proton charge radius” (1102.3296)
- PRA **84**, 012506 (2011) Carroll et al.: “Nonperturbative relativistic calculation of the muonic hydrogen spectrum” (1104.2971)
- PRA **84**, 012505 (2011) Jentschura: “Relativistic reduced-mass and recoil corrections to vacuum polarization in muonic hydrogen, ...” (1107.1737)
- PRA **84**, 020101(R) (2011) Miller, Thomas, Carroll, Rafelski: “Toward a resolution of the proton size puzzle” (1101.4073)
- PRA **84**, 020102(R) (2011) Carlson, Vanderhaeghen: “Higher-order proton structure corrections to the Lamb shift in muonic hydrogen” (1101.5965)
- PRL **107**, 160402 (2011) Hill, Paz: “Model independent analysis of proton structure for hydrogenic bound states” (1103.4617)
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Summary

- μp laser experiment is correct
- theory in muonic hydrogen:
 - FS, HFS correct
 - QED correct on the level of the discrepancy
 - proton polarizability under discussion
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- no New Physics :-)

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Summary

- μp laser experiment is correct

except: U.D. Jentschura, Ann. Phys. 326, 516:

e^- bound to $\mu p(2S)$ with $r = a_0$ shifts resonance by 0.4 meV

- How should this bound state form?

- "No" free electrons.

- Why should this bound state be stable?

- Stark mixing !?!
- Auger effect !!
- Collisions: every 100 ns.

- Only 1 line observed: >80% formation rate in 1 state.

- no peak at expected position
- observed peak has expected width

What's wrong ??



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$\Rightarrow$ J.-Ph. Karr, L. Hilico

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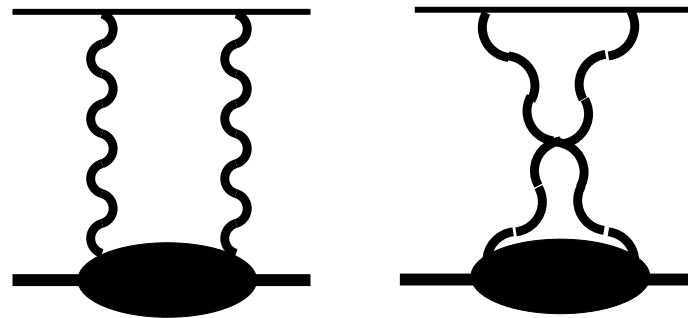
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PRA **84**, 052514 (2011) Krutov, Martynenko, "Lamb shift in the muonic deuterium atom" (1107.3080)

Discussions: Proton polarizability

proton polarizability aka. two-photon exchange



Seems to be the only contribution which *might* be able to solve the proton size puzzle by changing theory in μp .

Keep in mind:

Discrepancy: 0.31 meV

Polarizability: 0.015(4) meV 20 times smaller!

Discussions: Proton polarizability



- PRA 83, 042509 (2011) C.E. Carlson, V. Nazaryan, K. Griffioen:
“Proton-structure corrections to hyperfine splitting in muonic hydrogen” (1101.3239)
 - The 2S HFS is **confirmed** with smaller uncertainty:
22.8146(49) meV instead of the
22.8148(78) meV we used.

Discussions: Proton polarizability



- PRA 84, 020101(R) (2011) G.A. Miller *et al.*:
“Toward a resolution of the proton size puzzle” (1101.4073)
 - New off-mass-shell effect $\sim \alpha \frac{m^4}{M^3}$ solves puzzle.
 - Others say: This is already included in standard treatment.
 - C.E. Carlson: calculation gives 50 times smaller value.
- PRA 84, 020102(R) (2011) C.E. Carlson, M. Vanderhaeghen:
“Higher-order proton structure corrections to the Lamb shift in muonic hydrogen” (1101.5965)
 - All off-shell effects are automatically included in standard treatment.
- PRL, 107, 160402 (2011) R.J. Hill, G. Paz:
“Model independent analysis of proton structure for hydrogenic bound states” (1103.4617)
 - forward Compton amplitude's $W_1(0, Q^2)$ is now well known
 - “Crazy” functional behaviour can give any correction.
 - No numbers given.

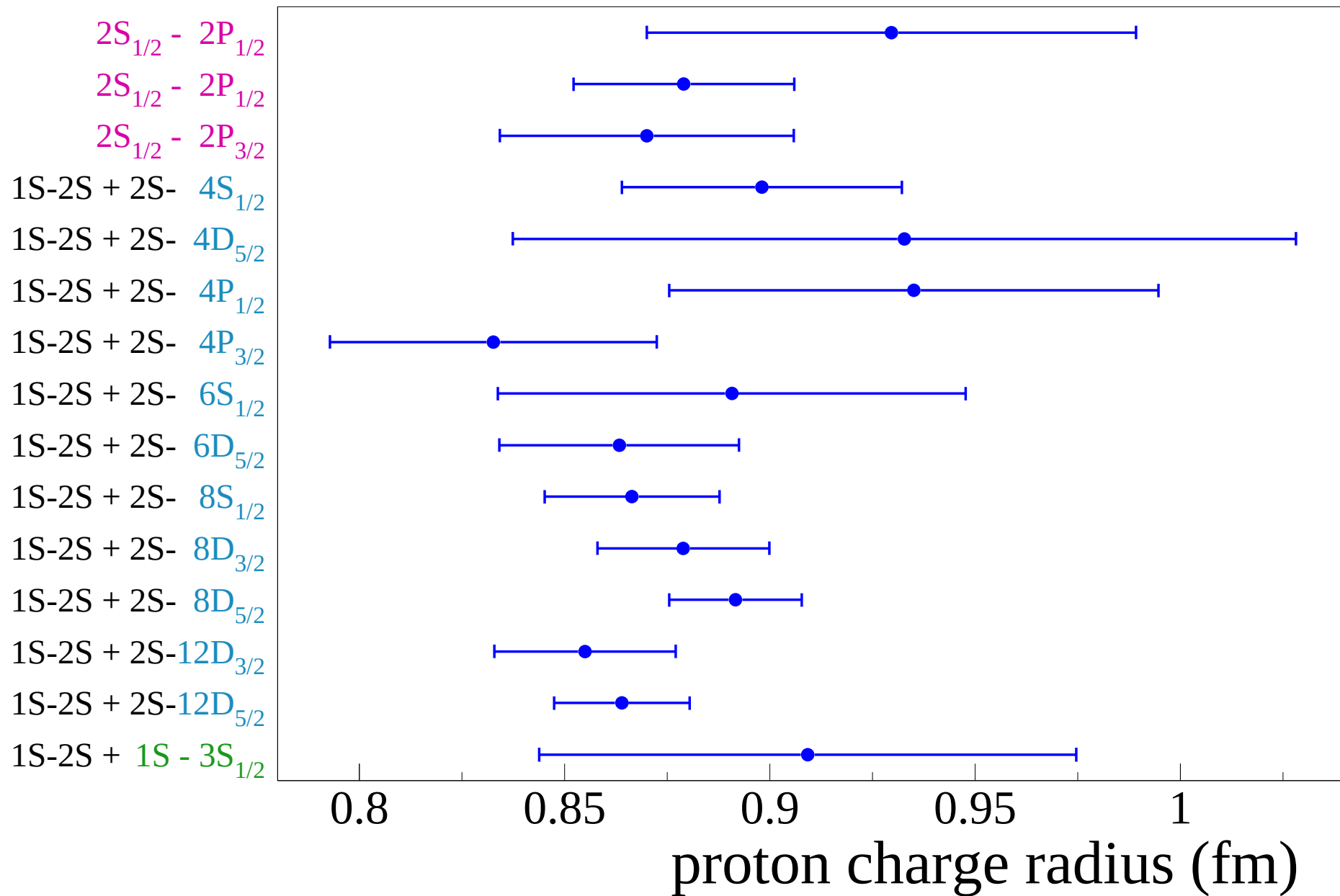
- Our value is based on 3 calculations
 - 0.017(4) meV: Rosenfelder, Phys. Lett. B 463, 317 (1999)
 - 0.012(2) meV: Pachucki, PRA 60, 3593 (1999)
 - 0.018 meV: Martynenko, Faustov, Phys. At. Nucl. 63, 845 (2000)
 - 0.015(4) meV: Borie, PRA 71, 032508 (2005)
- (0.31 meV is our discrepancy)
- No consensus about **validity** of the new claims
- Independent calculation of new effects give **50 times smaller** value.
- Lack of **numbers**

Don't know if this can solve the proton size puzzle.

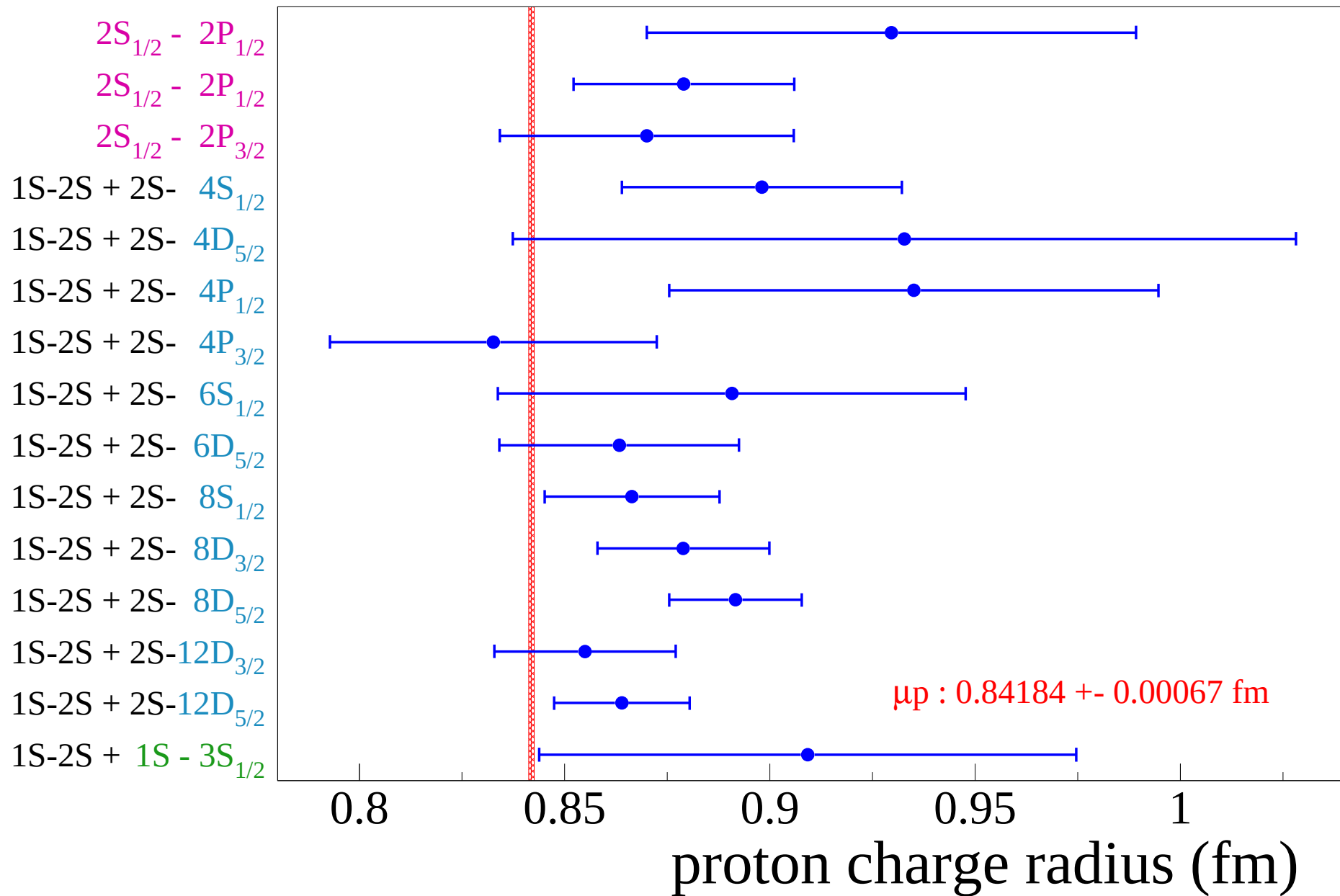
Numbers are needed which can be tested in experiments.

Are H spectroscopy and e-p scattering really
“obviously correct”?

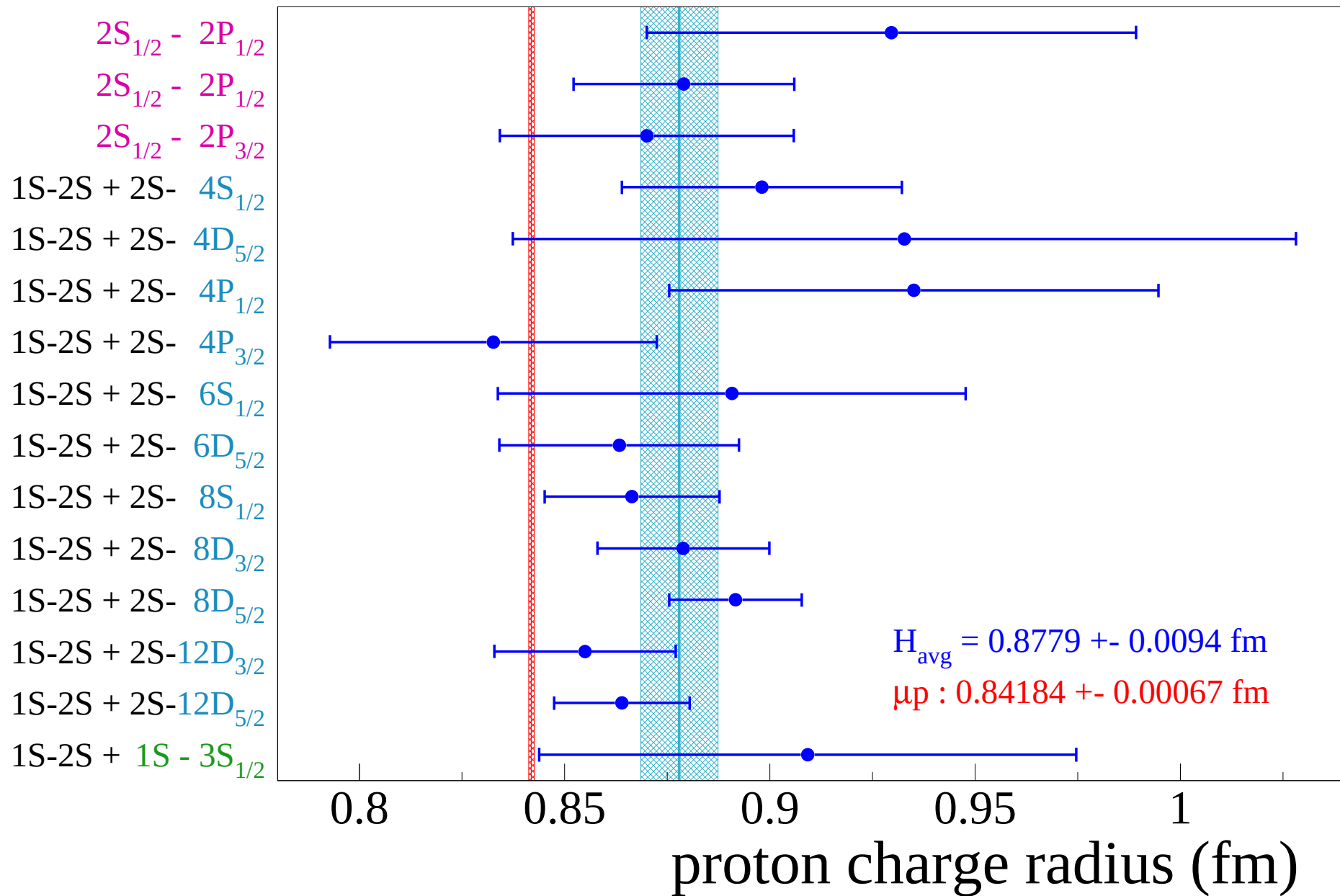
Hydrogen spectroscopy



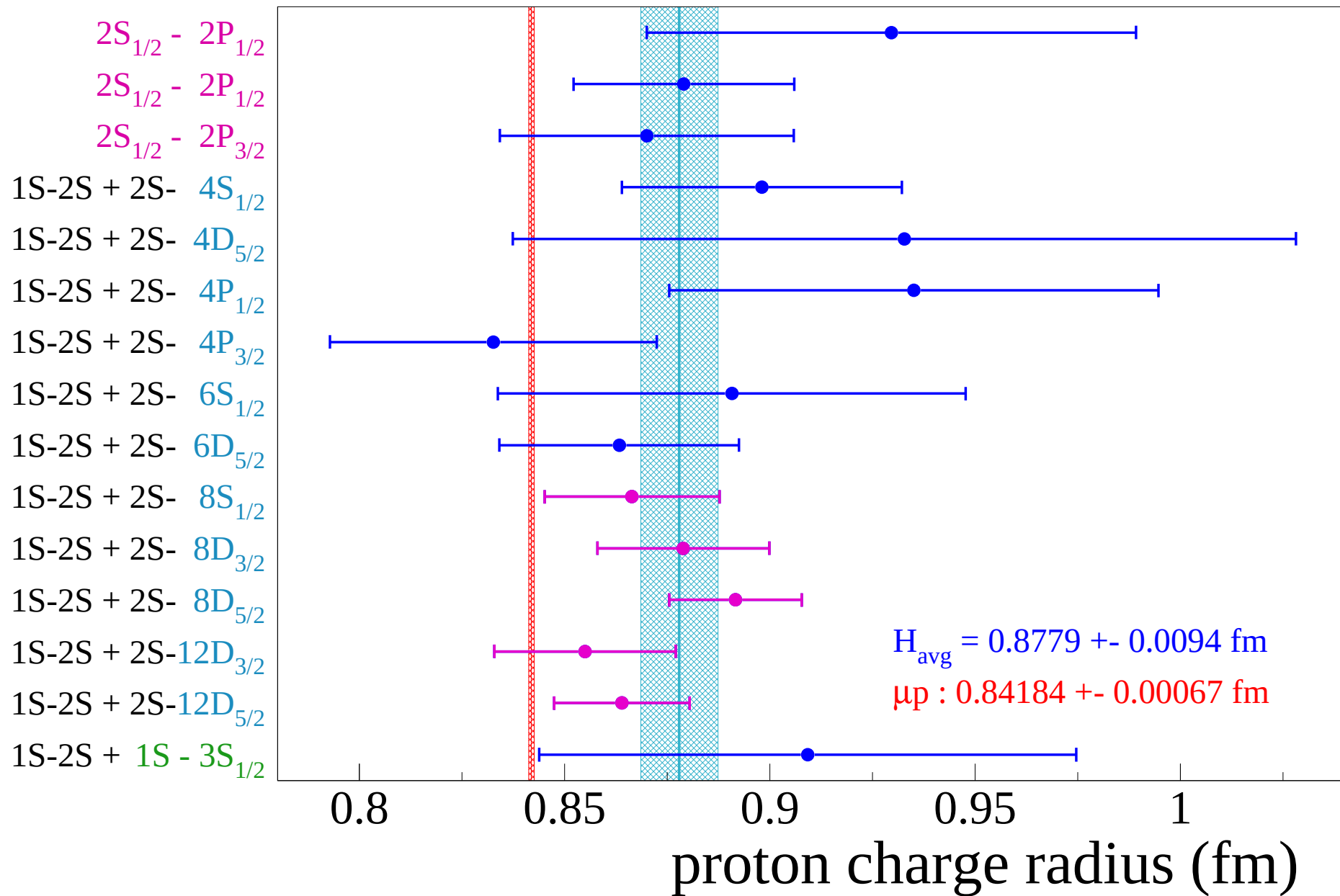
Hydrogen spectroscopy



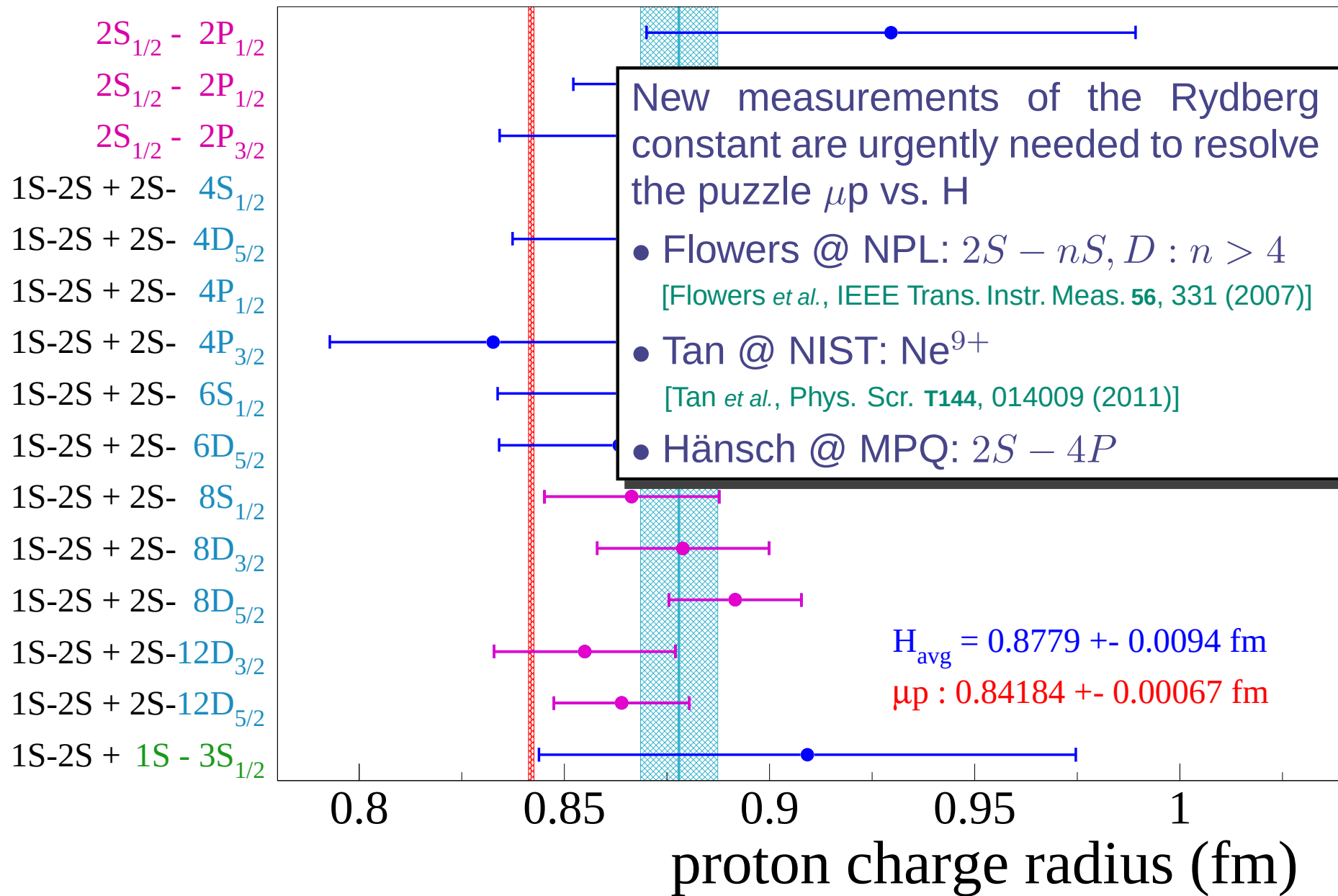
Hydrogen spectroscopy



Hydrogen spectroscopy



Hydrogen spectroscopy



- Rosenbluth cross section $\rightarrow$ Sachs form factor $\rightarrow r_p$

$$\left(\frac{d\sigma}{d\Omega}\right)_{\text{Ros.}} = \left(\frac{d\sigma}{d\Omega}\right)_{\text{Mott}} \frac{\varepsilon G_E^2 + \tau G_M^2}{\varepsilon(1 + \tau)} \quad \varepsilon = \left(1 + 2(1 + \tau) \tan^2 \frac{\theta}{2}\right)^{-1} \quad ; \quad \tau = \frac{Q^2}{4m_p^2}$$

G_E and G_M are the Fourier transforms of the charge and magnetization distributions

$G_E(0) = 1$ (charge), and $G_M(0) = \mu_p$ (magnetic moment)

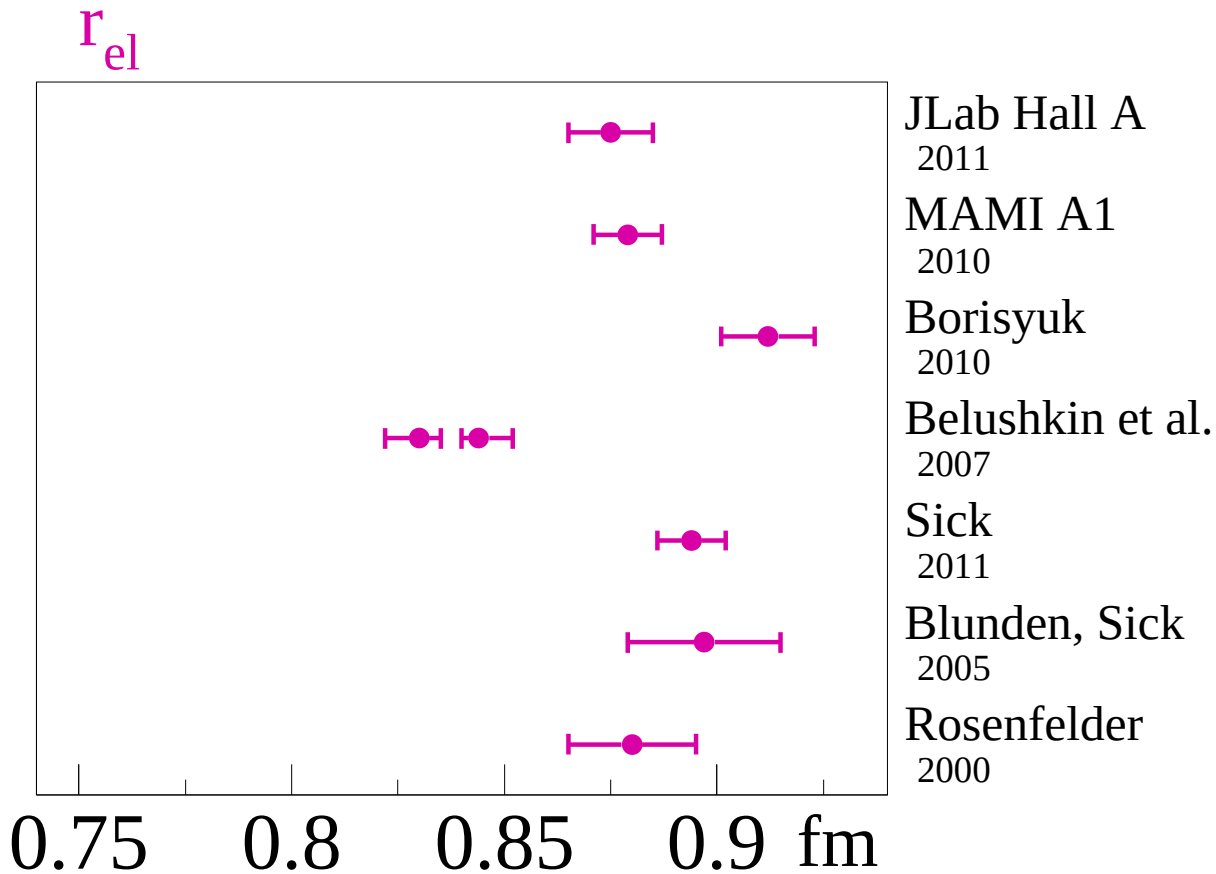
$$\langle r_p^2 \rangle = -6\hbar^2 \frac{dG_E(Q^2)}{dQ^2} \Big|_{Q^2=0} \Rightarrow \text{rms charge radius} = \boxed{\text{slope of } G_E \text{ at } Q^2 = 0}$$

extrapolation to $Q^2 \rightarrow 0$ required

$$Q^2 [(\text{GeV}/c)^2] = \begin{cases} 6 \cdot 10^{-7} & (\mu p) \\ > 2 \cdot 10^{-2} & (\text{e-p scatt.}) \end{cases}$$

Note: You get **charge** and **magnetic radius** *simultaneously*.

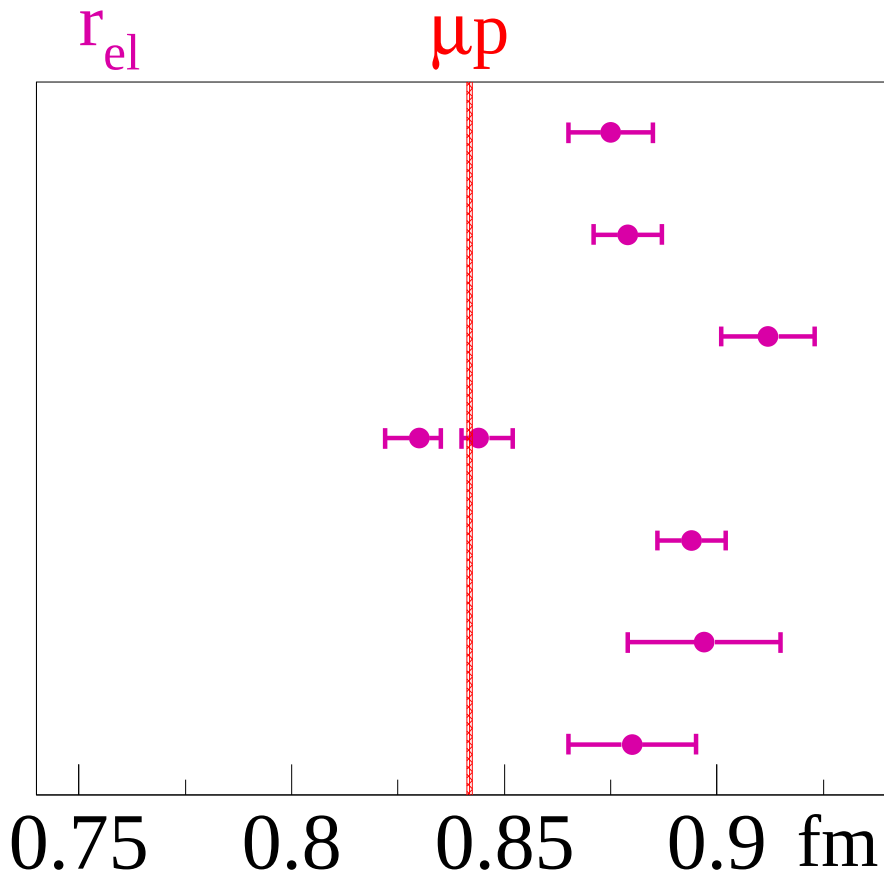
Electron scattering



Rosenfelder , Phys Lett B 479, 381 (2000)
Blunden, Sick , PRC 72, 057601 (2005)
Sick , Few Body Syst. (2011)
Belushkin et al. , PRC 75, 035202 (2007)

Borisyyuk , Nucl Phys A 843, 59 (2010)
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Electron scattering



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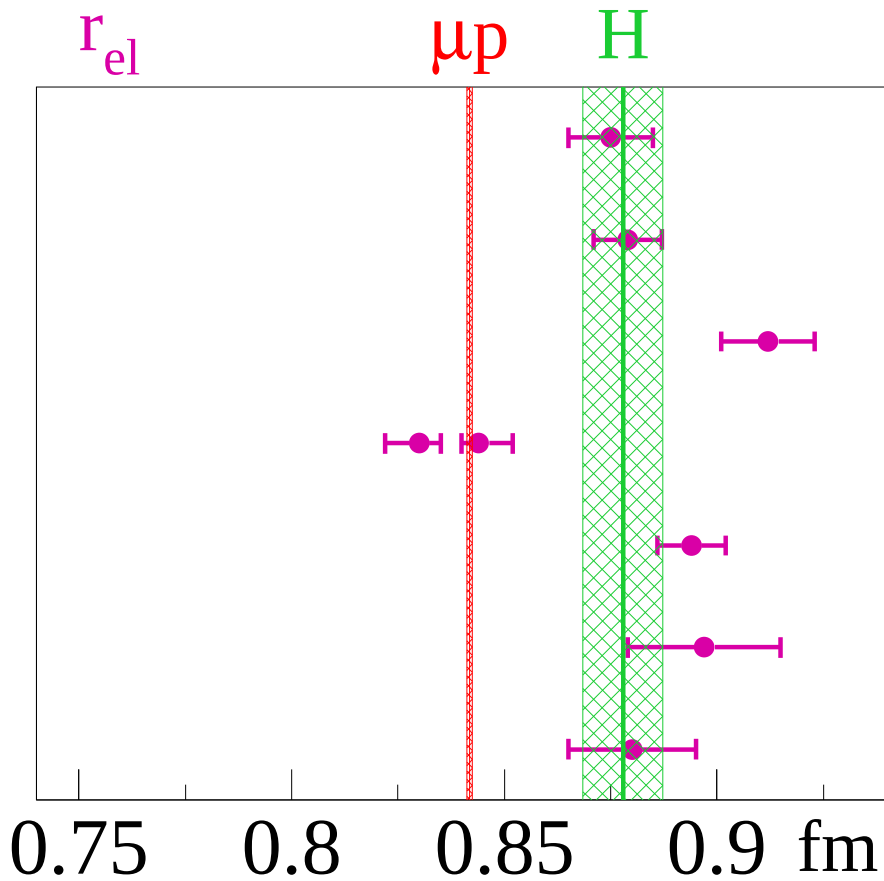
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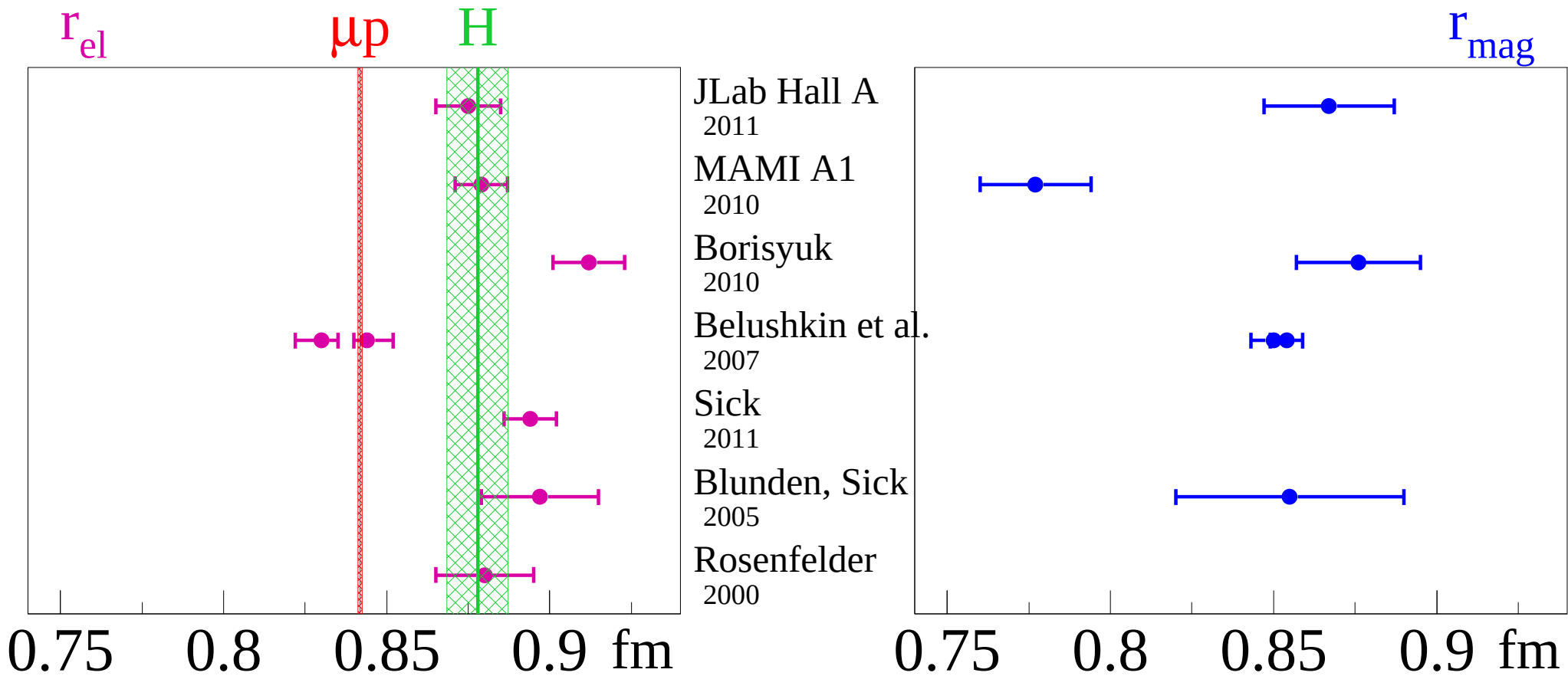
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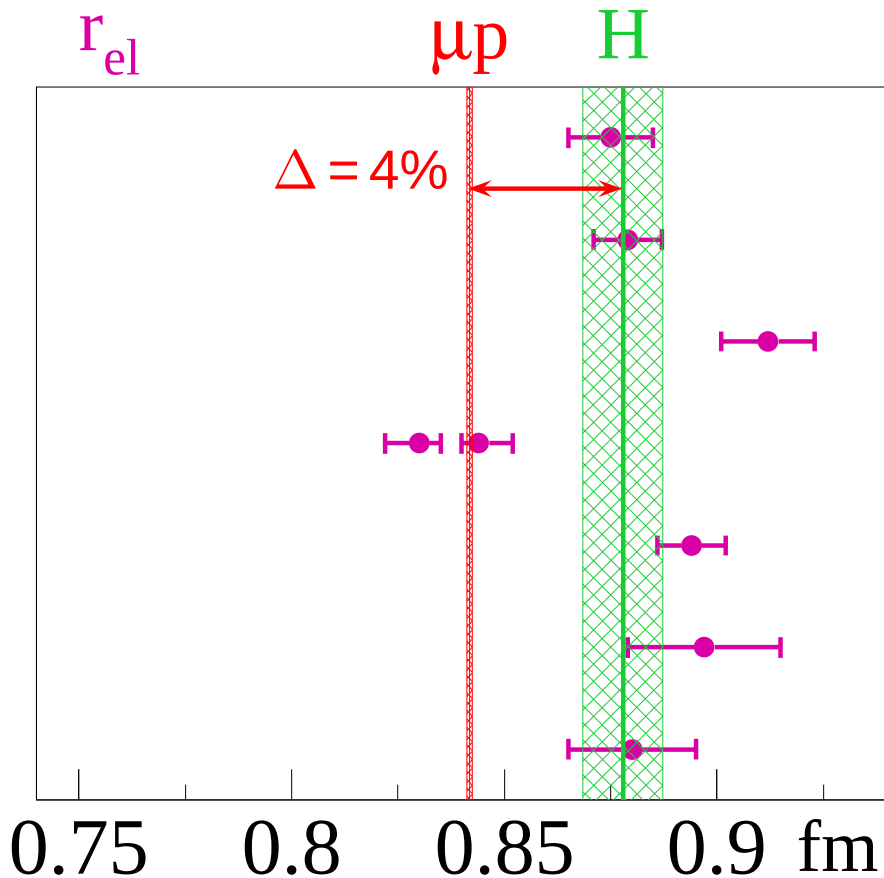
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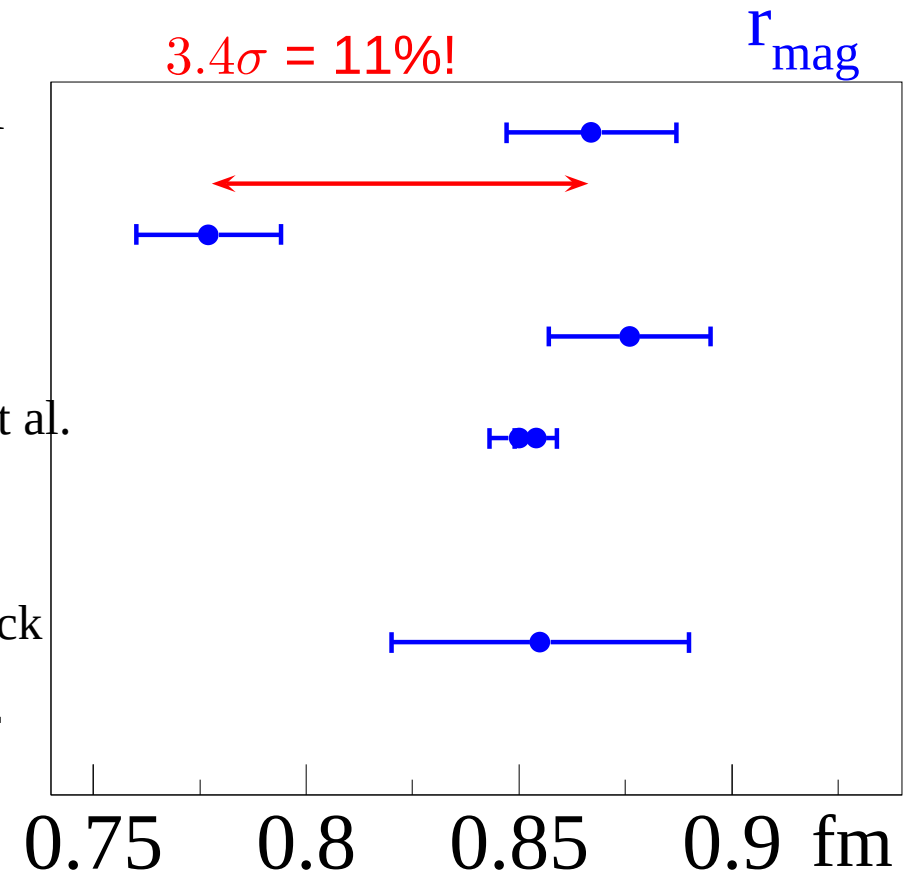
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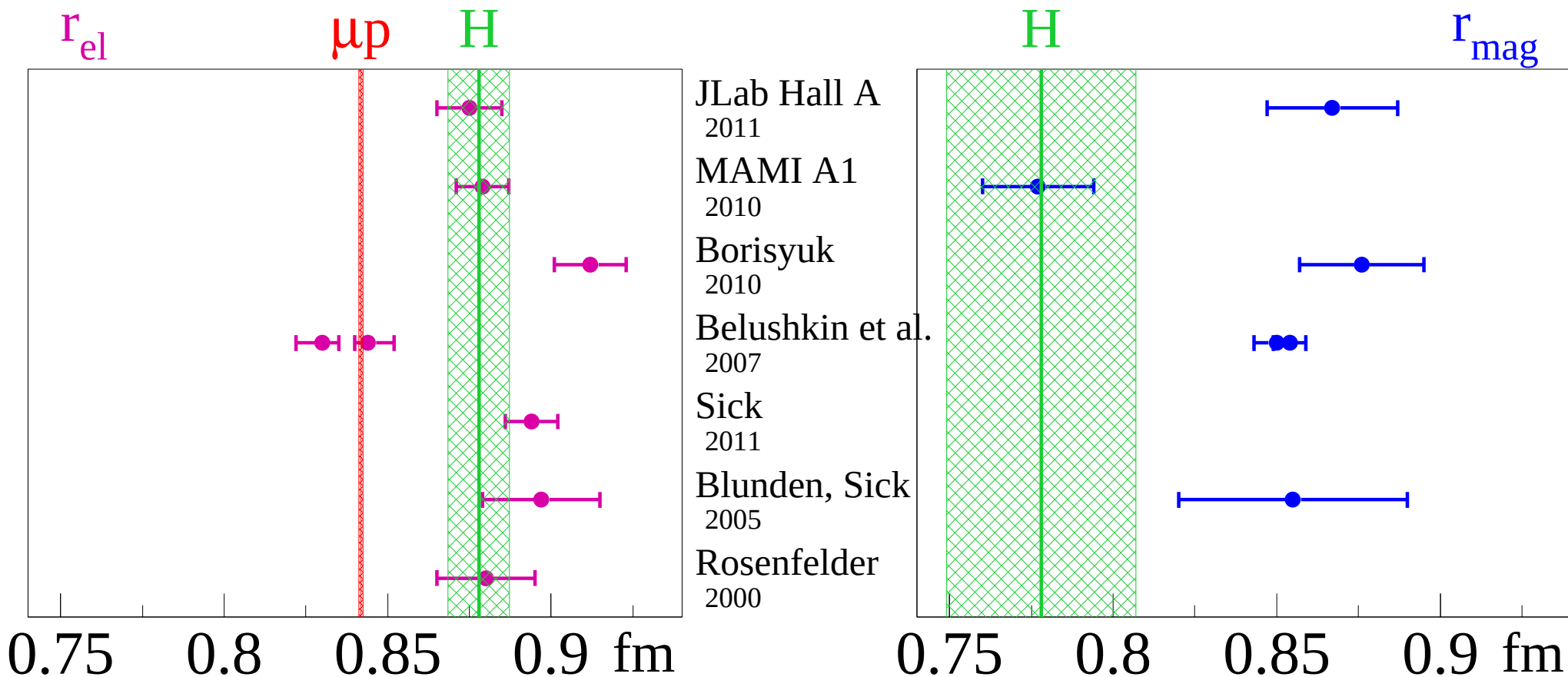
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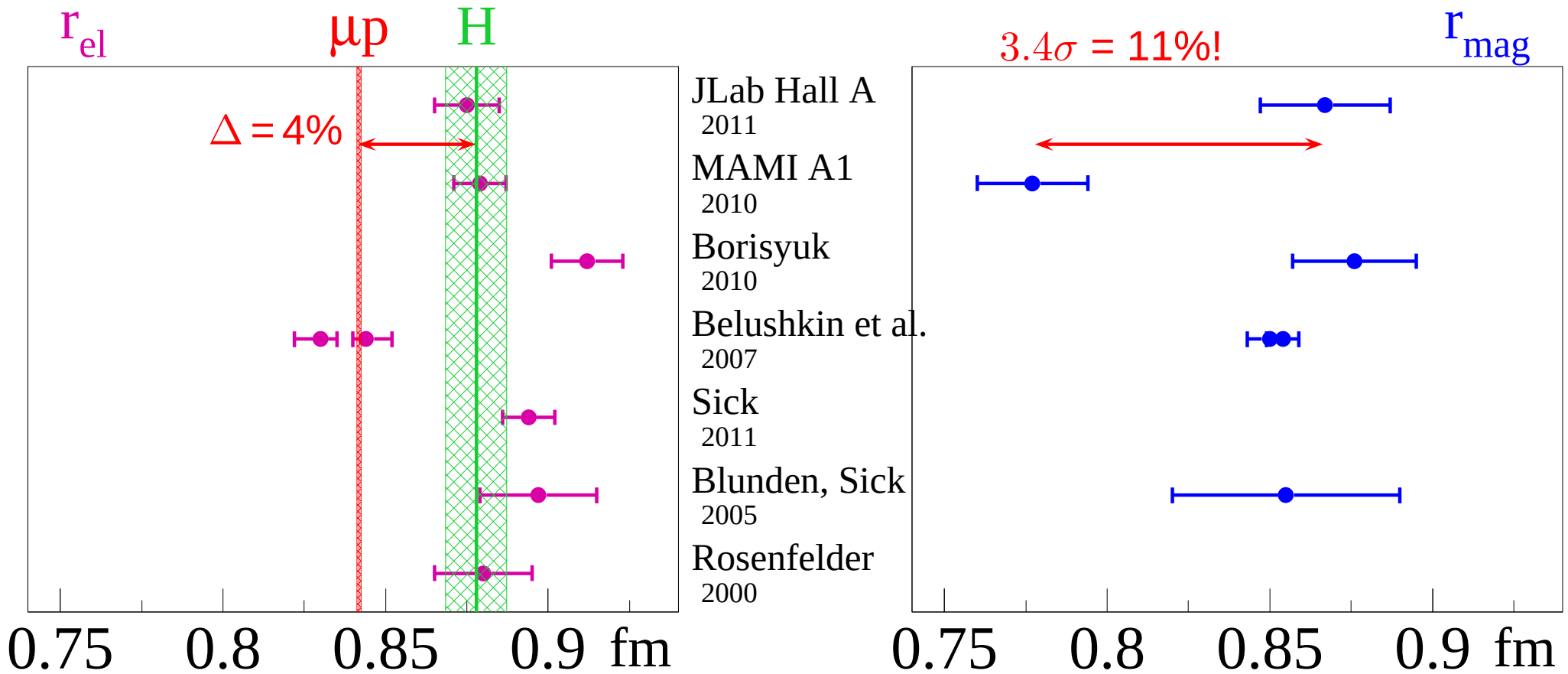
Electron scattering



Rosenfelder , Phys Lett B 479, 381 (2000)
 Blunden, Sick , PRC 72, 057601 (2005)
 Sick , Few Body Syst. (2011)
 Belushkin et al. , PRC 75, 035202 (2007)

Borisjuk , Nucl Phys A 843, 59 (2010)
 MAMI A1 Bernauer et al., PRL 105, 242001 (2010)
 JLab Hall A Zhan et al., 1102.0318 (nucl-ex) (2011)
 $r_{mag}(H)$ Volotka et al., Eur Phys J D33, 23 (2005)

Electron scattering



Ros
Blu
Sick
Belu

e-p scattering claims 1% error bars for 40 years now $\Rightarrow$ limit reached?

Scatter of results suggests larger uncertainty.

- Rosenbluth cross section $\rightarrow$ Sachs form factor $\rightarrow r_p$

$$\left(\frac{d\sigma}{d\Omega}\right)_{\text{Ros.}} = \left(\frac{d\sigma}{d\Omega}\right)_{\text{Mott}} \frac{\varepsilon G_E^2 + \tau G_M^2}{\varepsilon(1 + \tau)} \quad \varepsilon = \left(1 + 2(1 + \tau) \tan^2 \frac{\theta}{2}\right)^{-1} \quad ; \quad \tau = \frac{Q^2}{4m_p^2}$$

G_E and G_M are the Fourier transforms of the charge and magnetization distributions

$G_E(0) = 1$ (charge), and $G_M(0) = \mu_p$ (magnetic moment)

$$\langle r_p^2 \rangle = -6\hbar^2 \frac{dG_E(Q^2)}{dQ^2} \Big|_{Q^2=0} \Rightarrow \text{rms charge radius} = \boxed{\text{slope of } G_E \text{ at } Q^2 = 0}$$

extrapolation to $Q^2 \rightarrow 0$ required

$$Q^2 [(\text{GeV}/c)^2] = \begin{cases} 6 \cdot 10^{-7} & (\mu\text{p}) \\ > 2 \cdot 10^{-2} & (\text{e-p scatt.}) \end{cases}$$

- Extrapolation non-trivial

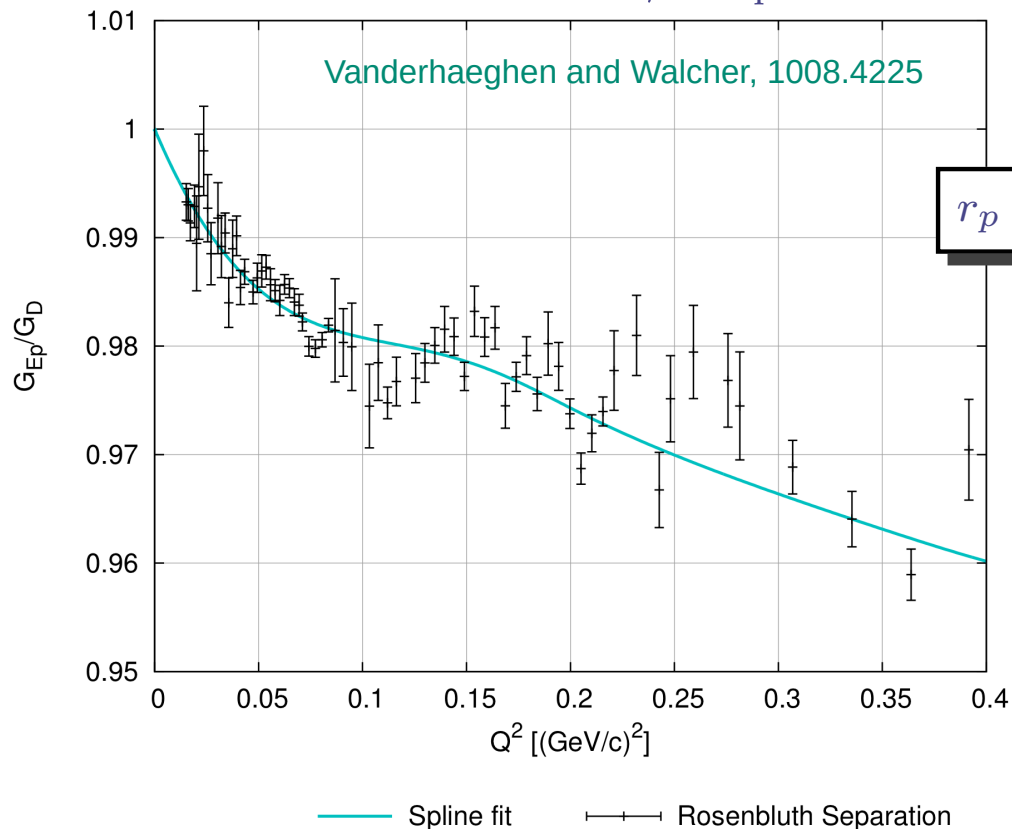
- Presence of “bump/dip” structure at lower Q^2 ?
- Model assumption of the functional behavior of the form factor?
- Normalization problems. Fitting with $G_E(Q^2 = 0) = 1 \rightarrow$ uncertainty underestimated.

r_p from new scattering data with 1% accuracy. Is that realistic?

- Extrapolation non-trivial

- Presence of “bump/dip” structure at lower Q^2 ?
- Model assumption of the functional behavior of the form factor?
- Normalization problems. Fitting with $G_E(Q^2 = 0) = 1 \rightarrow$ uncertainty underestimated.

New Mainz data: G_E/G_{dipole} vs. $Q^2 \Leftarrow$ world's most accurate data at low Q^2



$$r_p = (0.879 \pm 0.005_{\text{stat}} \pm 0.004_{\text{syst}} \pm 0.005_{\text{model}}) \text{ fm}$$

Bernauer *et al.*, PRL **105**, 242001 (2010)

r_p from electron scattering

- Bernauer *et al.*, PRL **105**, 242001 (2010)

$$r_p = (0.879 \pm 0.005_{\text{stat}} \pm 0.004_{\text{syst}} \pm 0.005_{\text{model}}) \text{ fm}$$

- Bernauer, PhD thesis (2010)

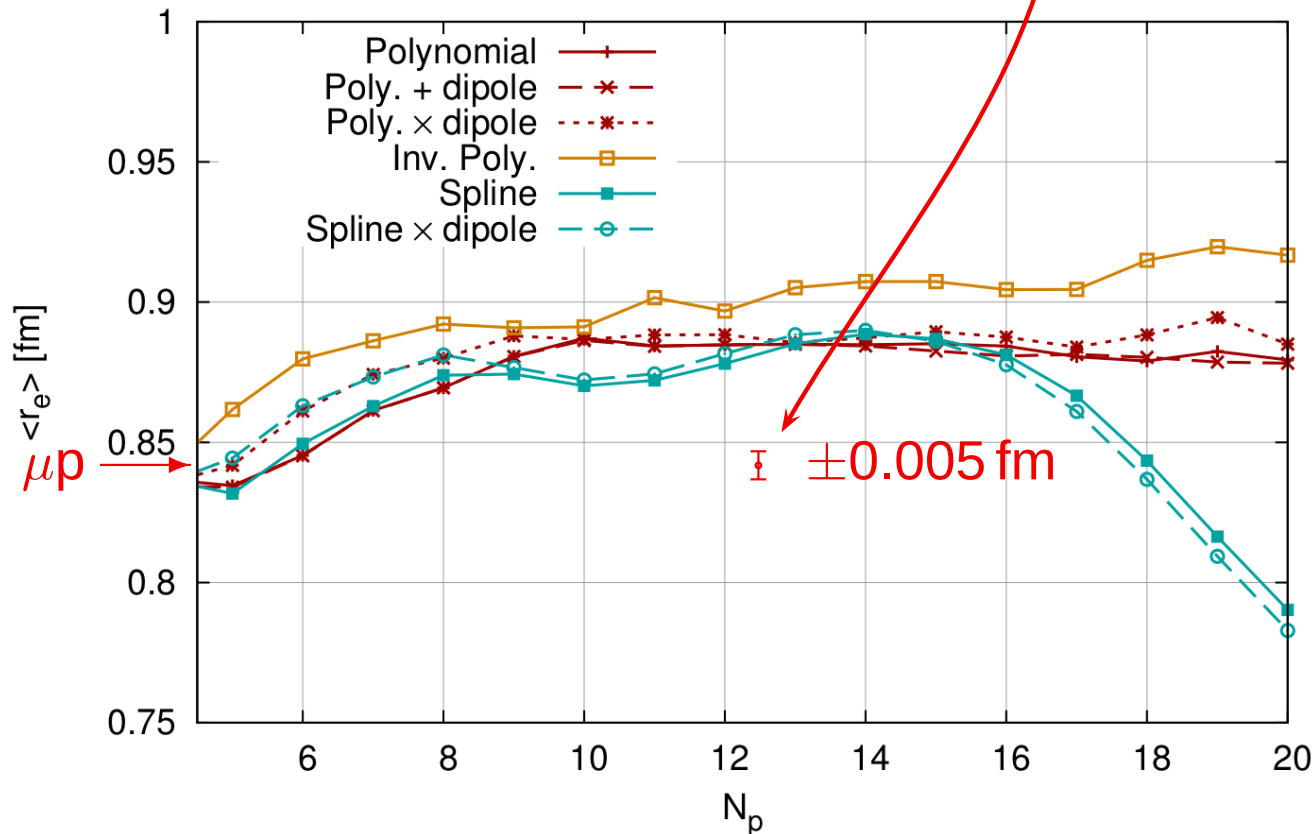


Fig. 9.21 (top):

The dependence of the extracted electric radius of the different flexible models on the number of parameters.

r_p from electron scattering



- Bernauer *et al.*, PRL **105**, 242001 (2010)

$$r_p = (0.879 \pm 0.005_{\text{stat}} \pm 0.004_{\text{syst}} \pm 0.002_{\text{th}}) \text{ fm}$$

- Bernauer, PhD thesis (2010)

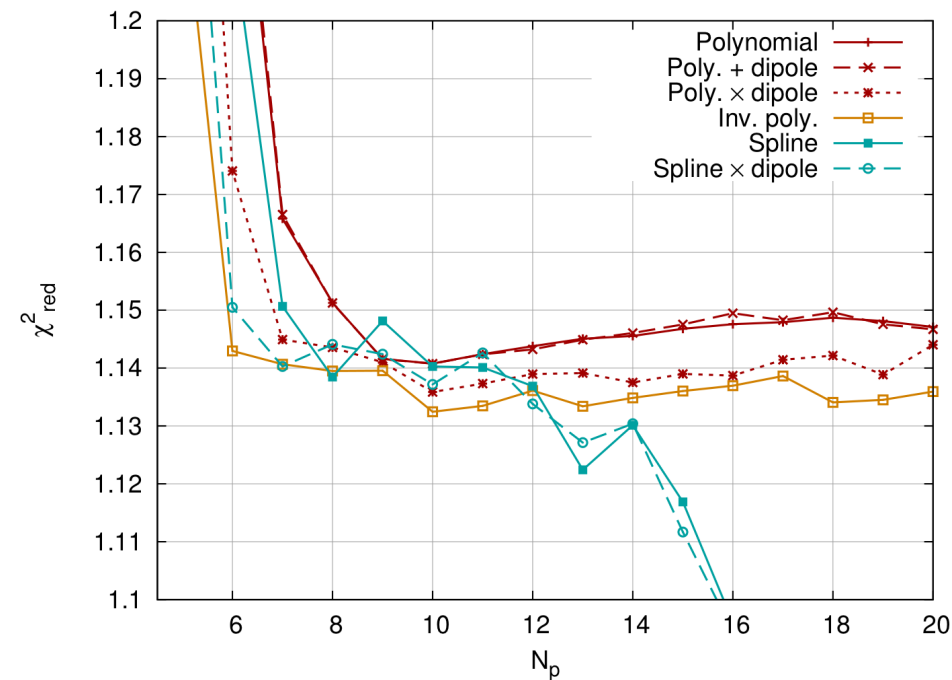
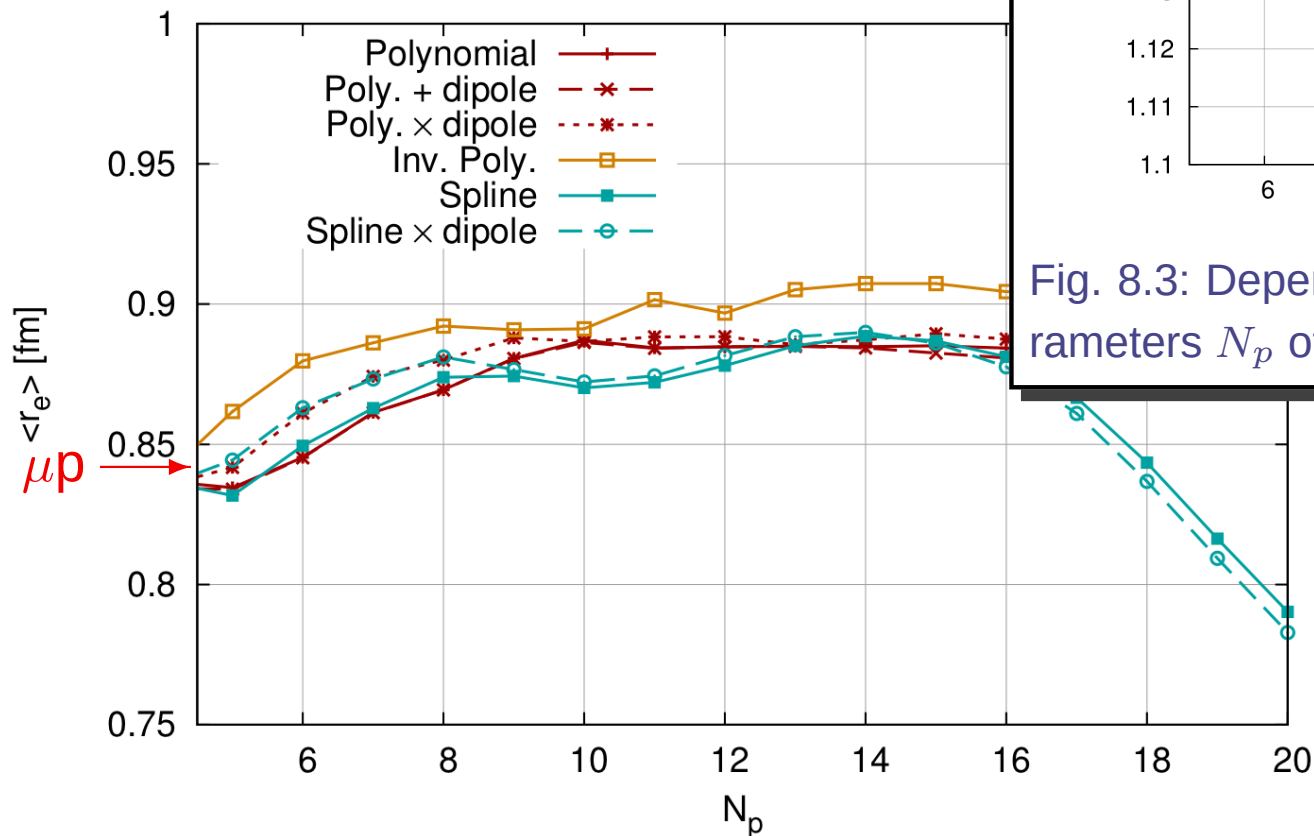


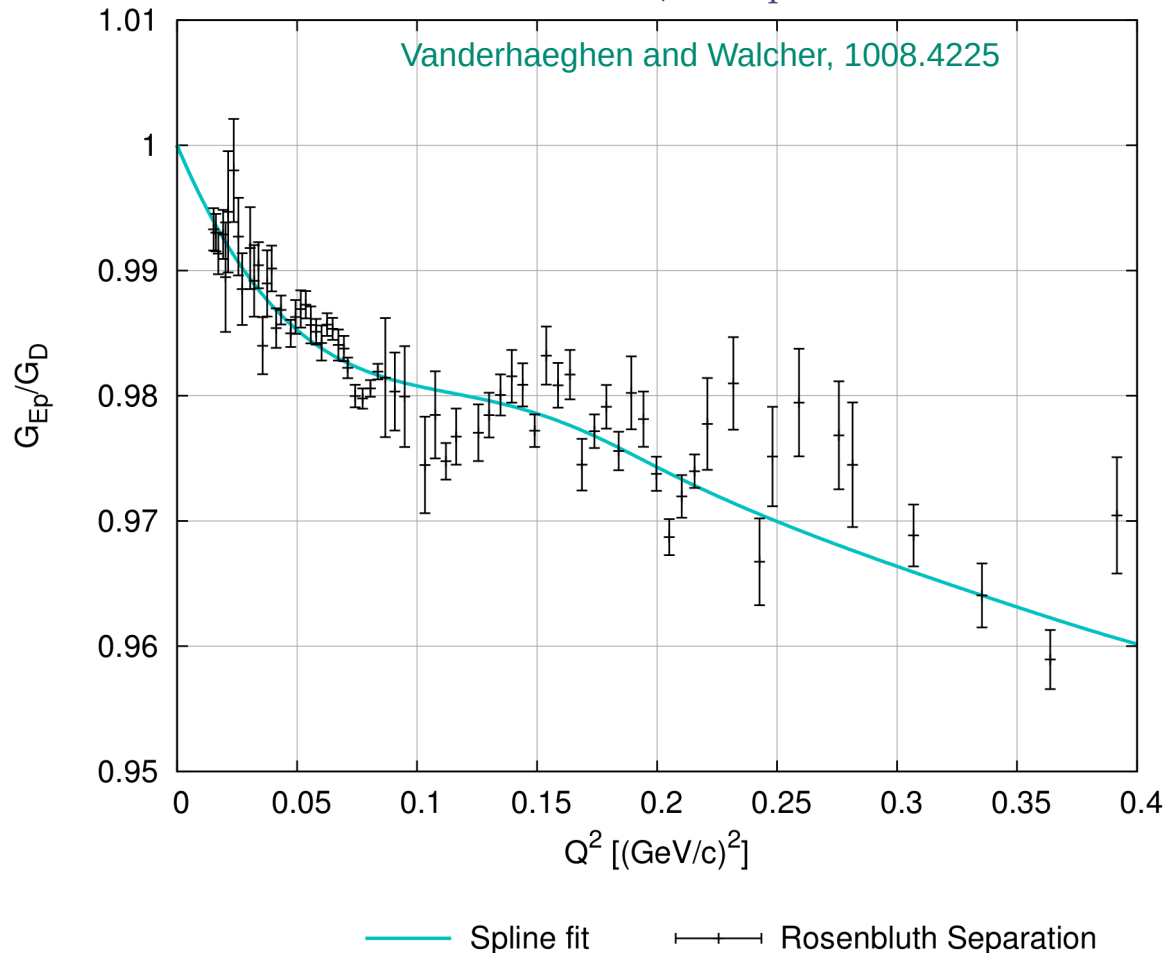
Fig. 8.3: Dependence of χ^2_{red} on the number of parameters N_p of the form factor parametrizations...

Mainz scattering data at lowest Q^2



$$\langle r_p^2 \rangle = -6\hbar^2 \left. \frac{dG_E(Q^2)}{dQ^2} \right|_{Q^2=0} \Rightarrow \text{rms charge radius} = \text{slope of } G_E \text{ at } Q^2 = 0$$

New Mainz data: G_E/G_{dipole} vs. Q^2



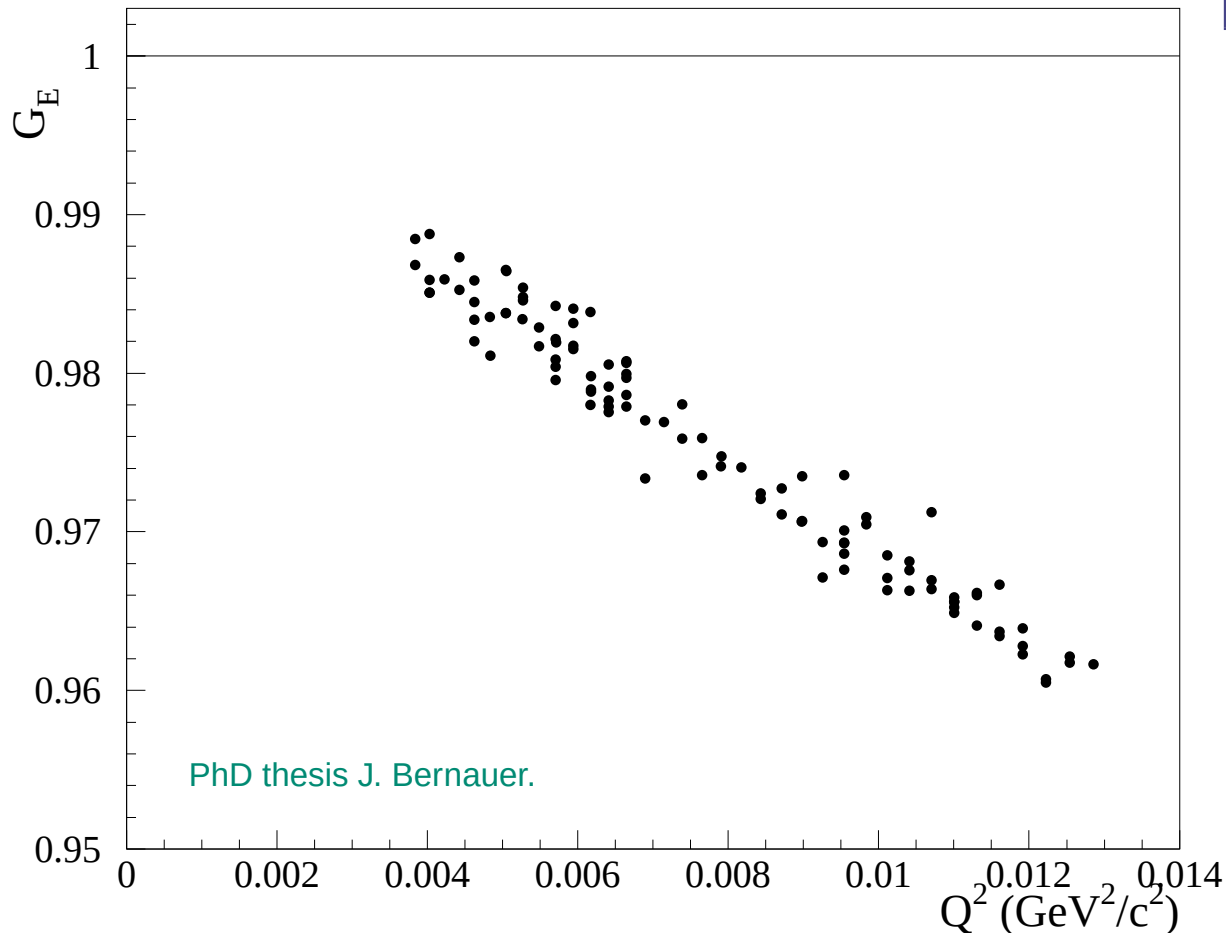
extrapolation to $Q^2 \rightarrow 0$ required

Mainz scattering data at lowest Q^2

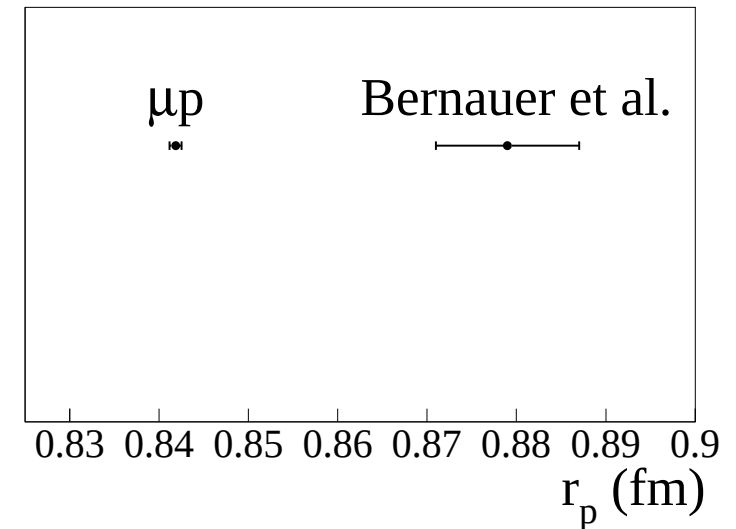


$$\langle r_p^2 \rangle = -6\hbar^2 \left. \frac{dG_E(Q^2)}{dQ^2} \right|_{Q^2=0} \Rightarrow \text{rms charge radius} = \boxed{\text{slope of } G_E \text{ at } Q^2 = 0}$$

Lower half of 180MeV data



extrapolation to $Q^2 \rightarrow 0$ required

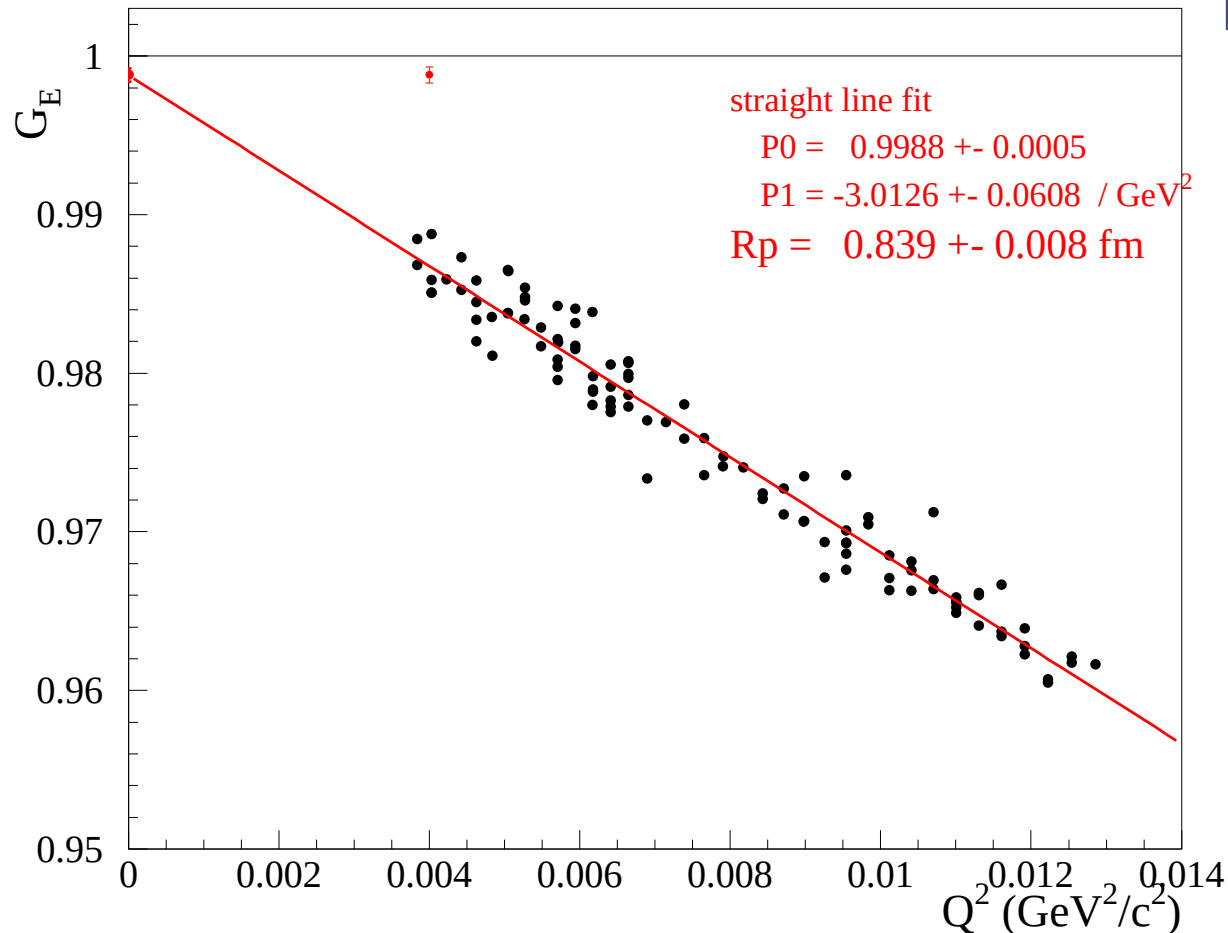


Mainz scattering data at lowest Q^2

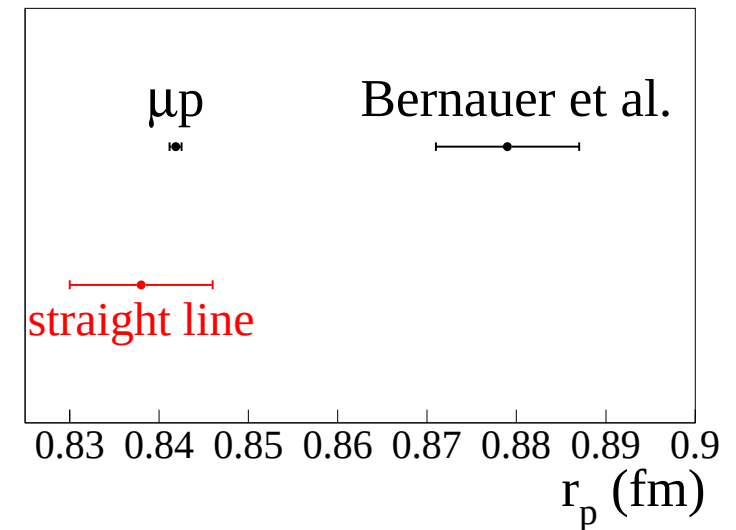


$$\langle r_p^2 \rangle = -6\hbar^2 \left. \frac{dG_E(Q^2)}{dQ^2} \right|_{Q^2=0} \Rightarrow \text{rms charge radius} = \text{slope of } G_E \text{ at } Q^2 = 0$$

Fitting a straight line



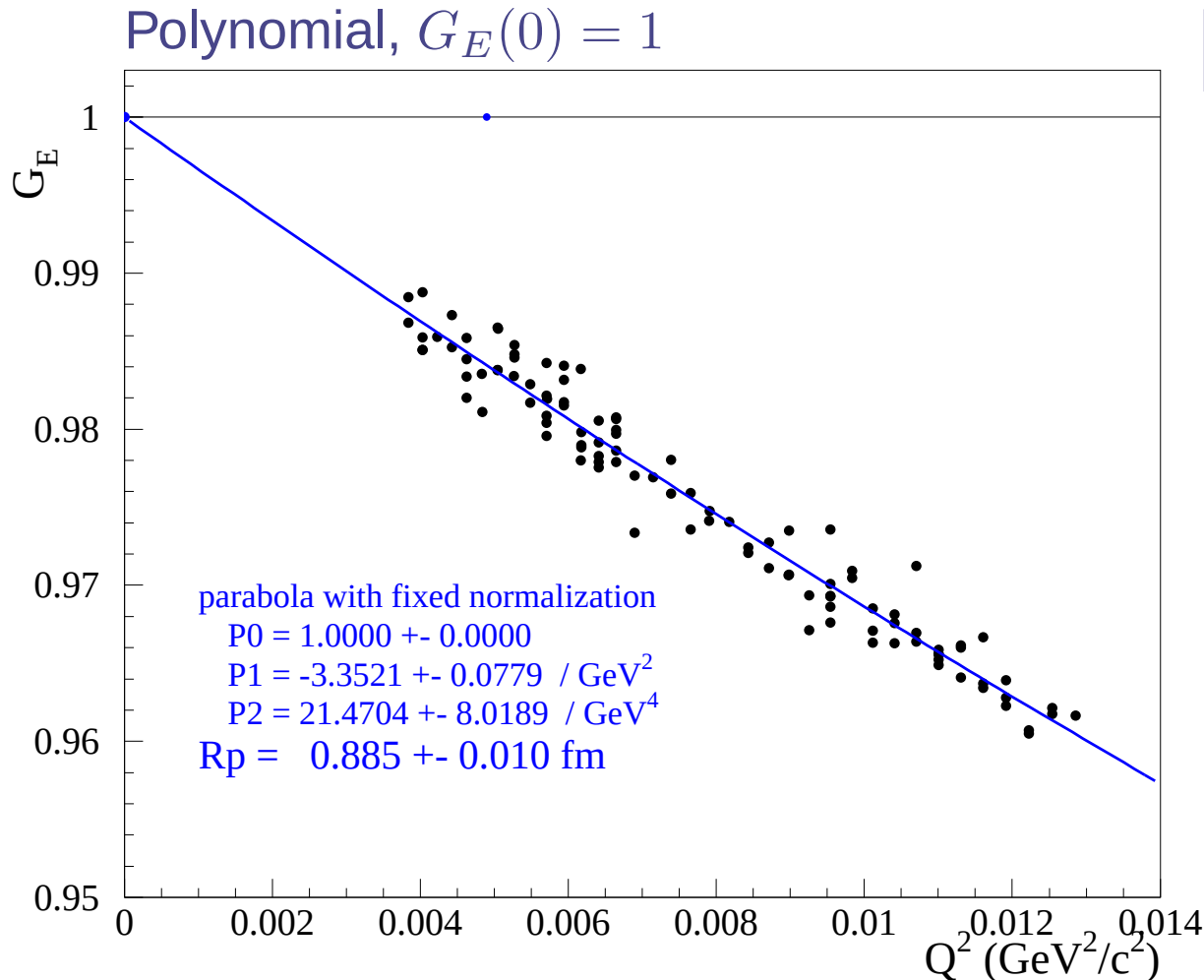
extrapolation to $Q^2 \rightarrow 0$ required



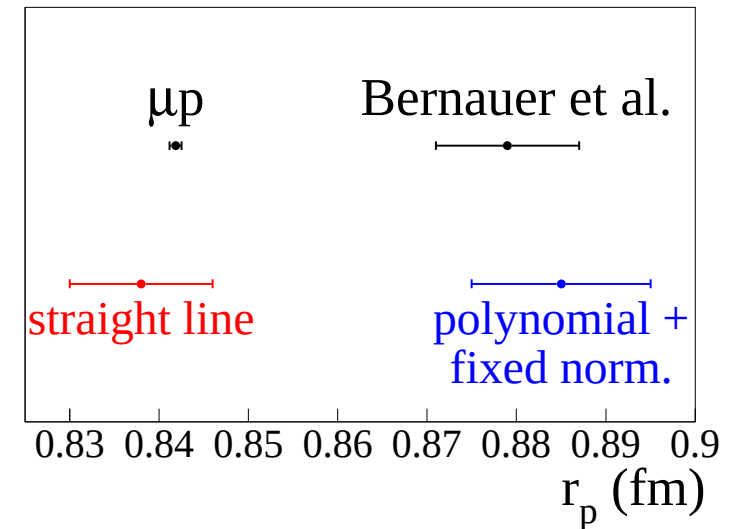
Mainz scattering data at lowest Q^2



$$\langle r_p^2 \rangle = -6\hbar^2 \left. \frac{dG_E(Q^2)}{dQ^2} \right|_{Q^2=0} \Rightarrow \text{rms charge radius} = \text{slope of } G_E \text{ at } Q^2 = 0$$



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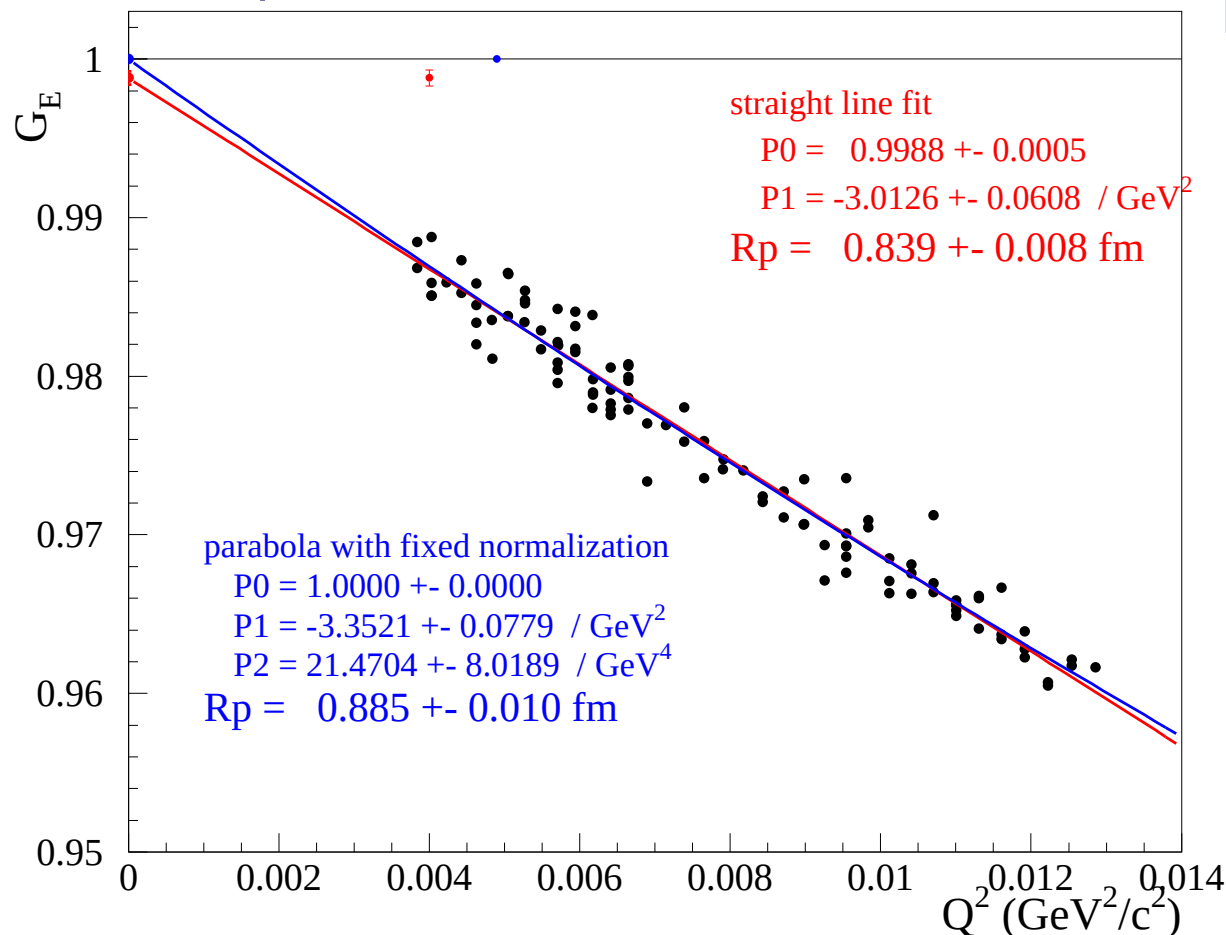


Mainz scattering data at lowest Q^2

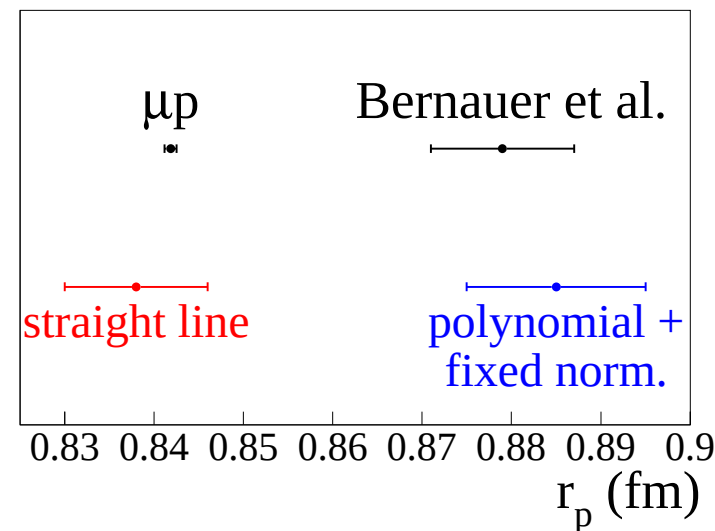


$$\langle r_p^2 \rangle = -6\hbar^2 \left. \frac{dG_E(Q^2)}{dQ^2} \right|_{Q^2=0} \Rightarrow \text{rms charge radius} = \text{slope of } G_E \text{ at } Q^2 = 0$$

Extrapolation is subtle

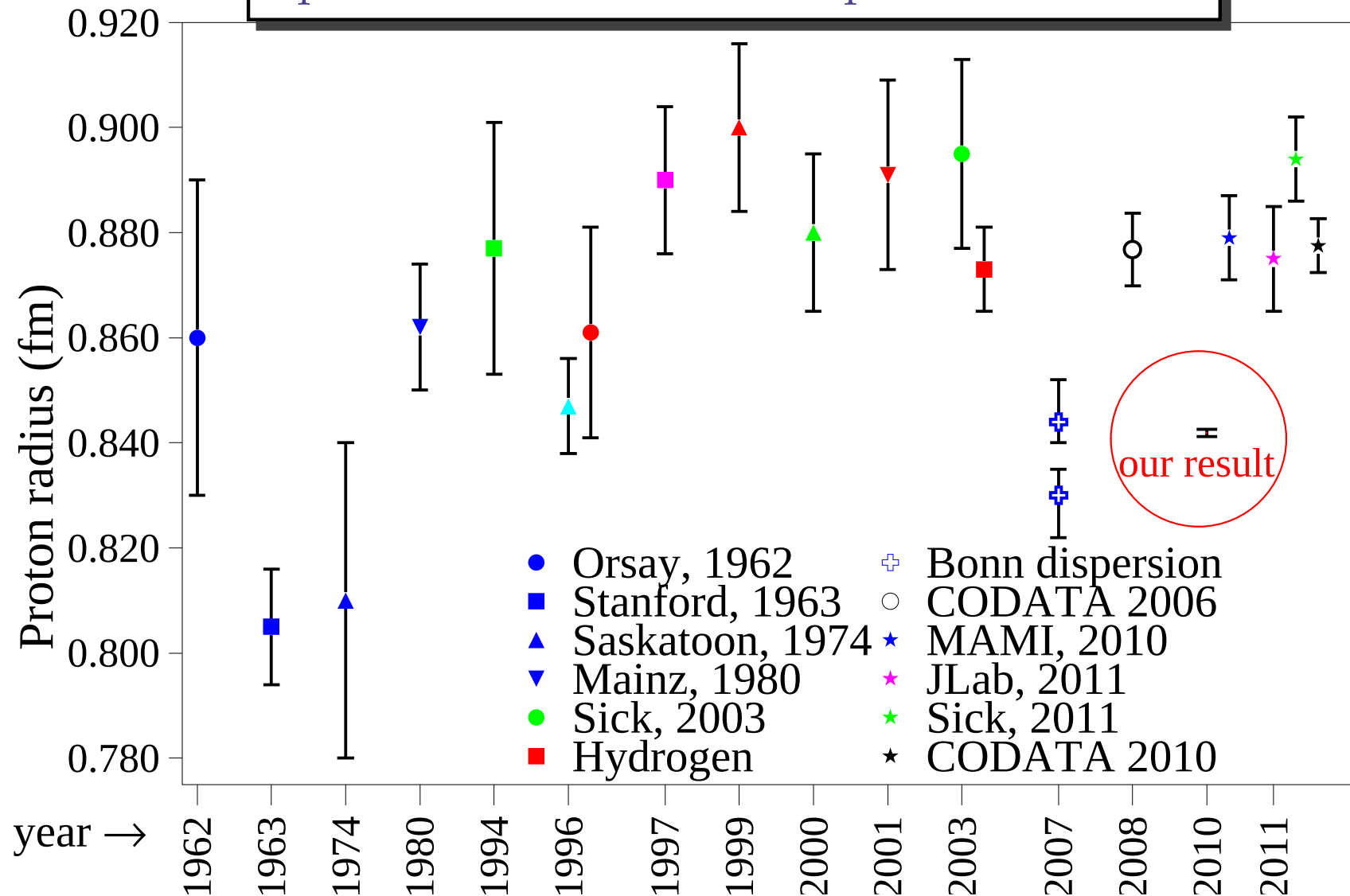


extrapolation to $Q^2 \rightarrow 0$ required



Proton radius 2011

$$r_p = 0.84184 (36)_{\text{exp}} (56)_{\text{theo}} \text{ fm}$$

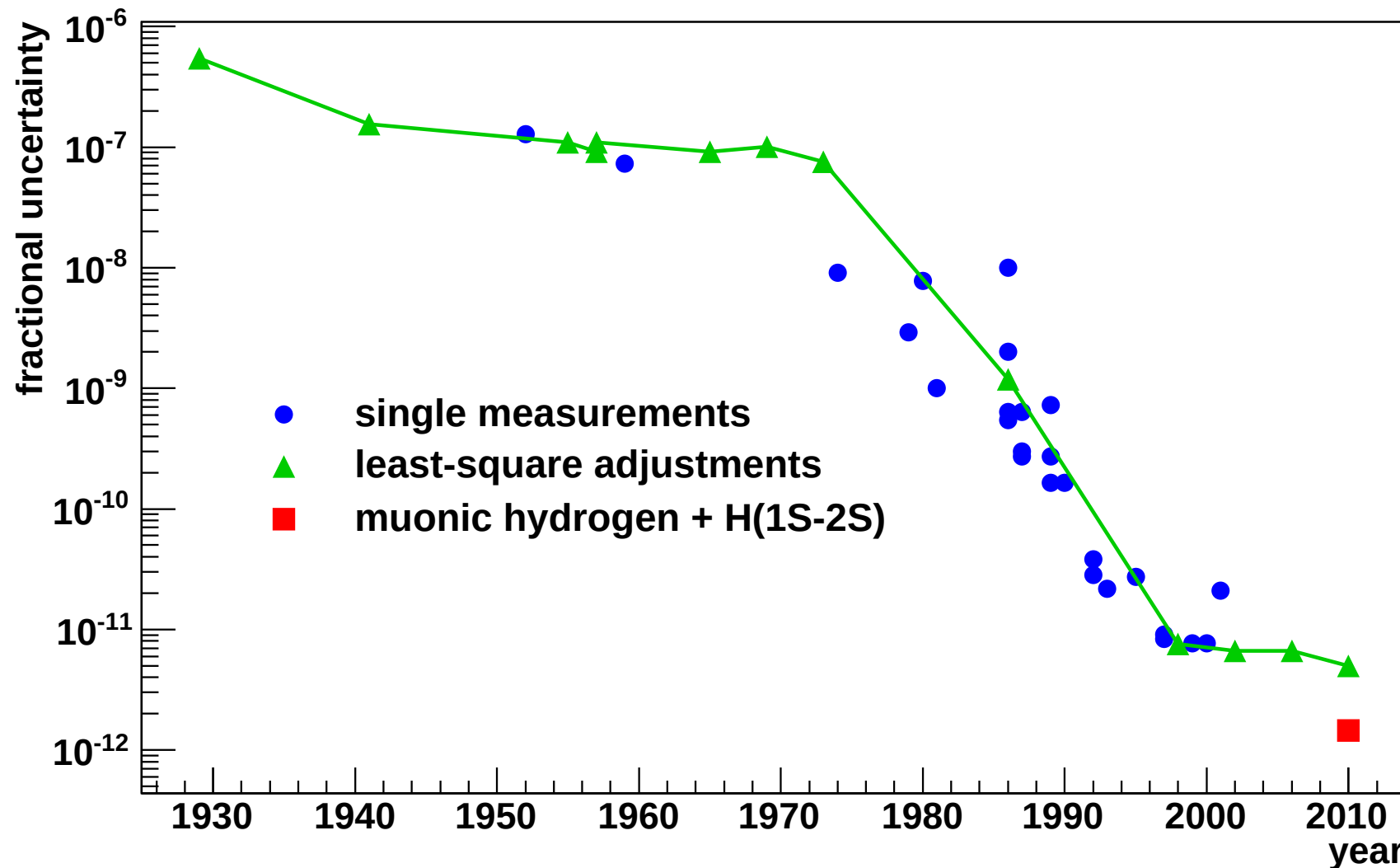


R. Pohl *et al.*, Nature 466, 213 (2010).

Rydberg constant 2011



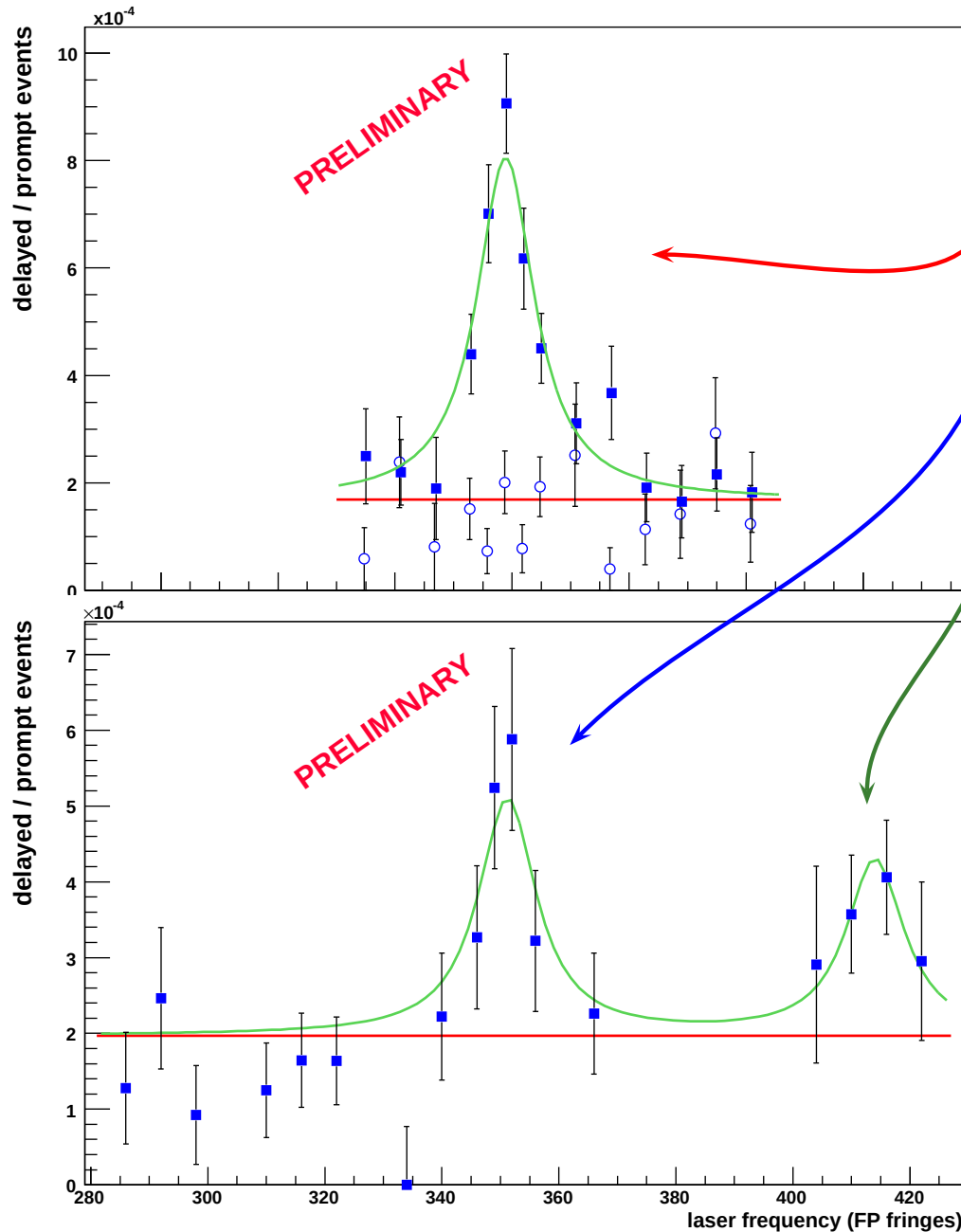
$$R_{\infty} = 10973731.568160(16) \text{ m}^{-1} \quad [1.5 \text{ parts in } 10^{12}]$$



R. Pohl *et al.*, Nature 466, 213 (2010).

muonic deuterium

Muonic DEUTERIUM

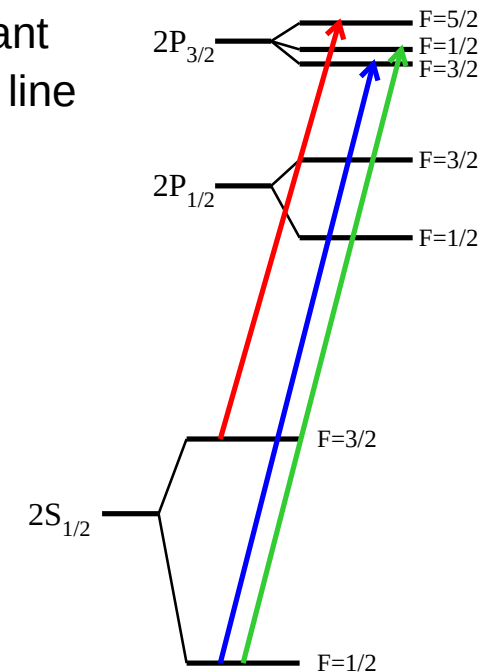


2.5 resonances in muonic deuterium

● $\mu d [2S_{1/2}(F=3/2) \rightarrow 2P_{3/2}(F=5/2)]$
20 ppm (stat., online)

● $\mu d [2S_{1/2}(F=1/2) \rightarrow 2P_{3/2}(F=3/2)]$
45 ppm (stat., online)

● $\mu d [2S_{1/2}(F=1/2) \rightarrow 2P_{3/2}(F=1/2)]$
70 ppm (stat., online)
only 5 σ significant
identifies F=3/2 line



- muonic **hydrogen** $2S_{1/2}(F=1) \rightarrow 2P_{3/2}(F=2)$ to 15 ppm (stat.+syst.)
→ r_p to 8×10^{-4} (experimental precision 4×10^{-4})

$r_p = 0.84284 \pm 0.00058 \text{ fm}$ is ~~5 σ~~ ¹⁰ away from CODATA-2006
~~6.8 σ~~

The proton is 4% smaller, and the Rydberg constant R_∞ is ~~4.9~~^{6.6} sigma off

- muonic **hydrogen** $2S_{1/2}(F=0) \rightarrow 2P_{3/2}(F=1)$ to 18 ppm (to be published)
exactly at the position deduced with our new r_p
→ **2S hyperfine splitting** to 220 ppm
→ **Zemach radius** to a few % (radius of the magnetic moment distribution)
- muonic **deuterium** $2S_{1/2}(F=3/2) \rightarrow 2P_{3/2}(F=5/2)$ to 20 ppm (stat., online)
Theory: missing QED and nuclear structure corrections
→ **deuteron charge radius** and **polarizability**
- muonic **deuterium** $2S_{1/2}(F=1/2) \rightarrow 2P_{3/2}(F=3/2)$ and $F=1/2$
→ **HFS**, check calculations in μd

<http://muhy.web.psi.ch>

μ p Lamb shift collaboration in 2009



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F. MULHAUSER, L. SCHALLER

former members, spent holidays at run 2009



University of Stuttgart
Germany

Outlook: Lamb shift in muonic helium

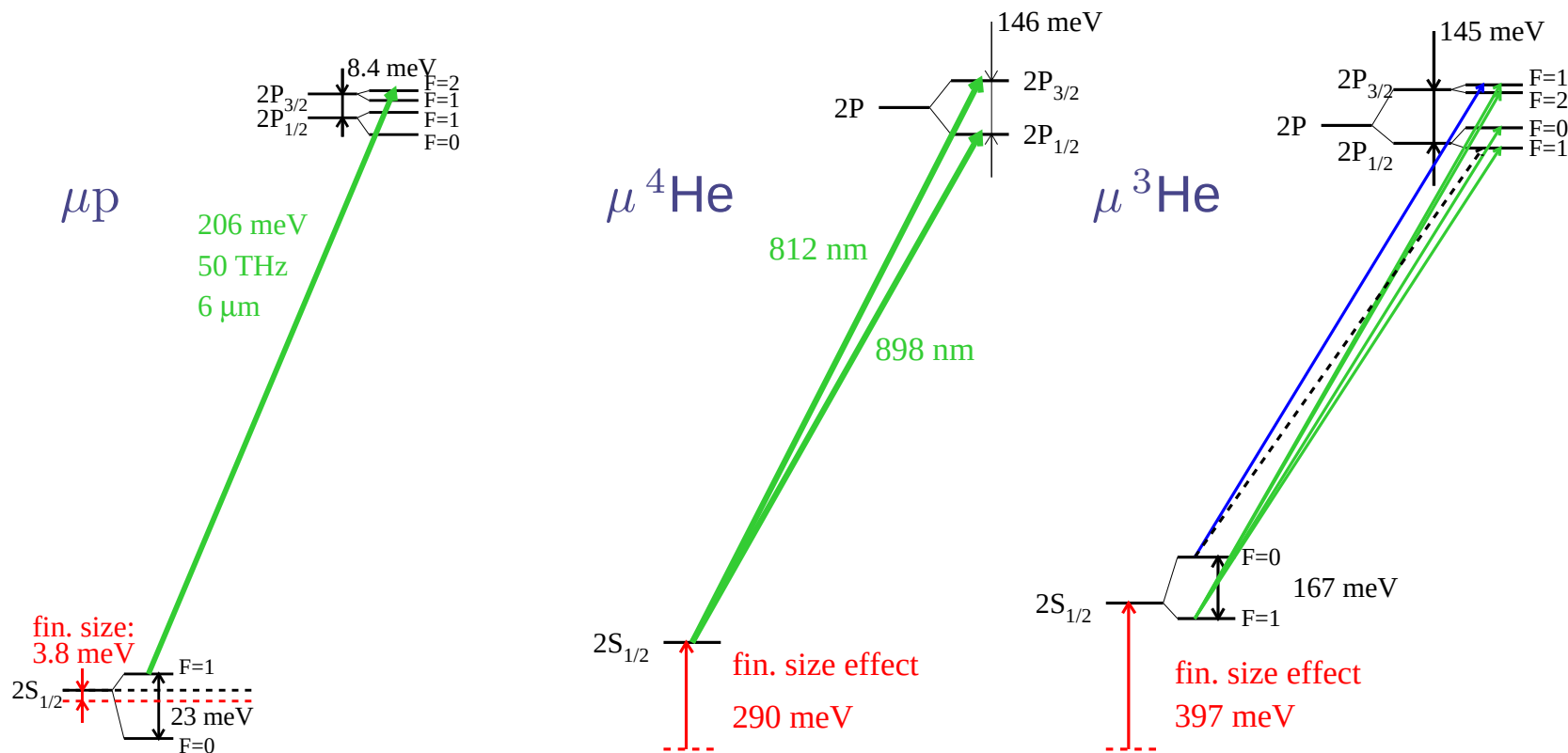


- CREMA collaboration: Charge Radius Experiment with Muonic Atoms
- Exp. R10-01 approved at PSI in Feb. 2010
- Goal: Measure $\Delta E(2S-2P)$ in $\mu^4\text{He}$, $\mu^3\text{He}$
- $\Rightarrow$ alpha particle and helion charge radius to 3×10^{-4} (0.0005 fm)

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 - help to solve the proton size puzzle
 - absolute charge radii of helion, alpha
 - low-energy effective nuclear models: ^1H , ^2D , ^3He , ^4He
 - QED test with $\text{He}^+(1S-2S)$ [Udem @ MPQ, Eikema @ Amsterdam]

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- identical muon beam
- similar laser, no Raman cell ($\rightarrow$ more pulse energy)
- similar, maybe better x-ray detectors (8.2 keV)
- event rate: 16-48 events per hour (not 6 per hour, μp)
- line with 300 GHz (1 nm!)

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 - abso
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ERC Starting Grant for RP, 2011

1st beam time expected for 2013.

, ^4He

na @ Amsterdam]



Proton Size Investigators thank you for your attention



The r_p^3 coefficient



$$\Delta E(2P_{3/2}^{F=2} - 2S_{1/2}^{F=1}) = 209.9779(49) - 5.2262 r_p^2 + 0.0347 r_p^3 \text{ [meV]}$$

We've used the coefficient for a Dipole form factor given by Borie.

[PRA 71, 032508 (2005)]

Dipole	0.0347 r_p^3	0.0207 meV
Gaussian	0.0317 r_p^3	0.0189 meV
difference		0.0018 meV
published uncertainty		0.0058 meV
discrepancy		0.31 meV

The r_p^3 coefficient

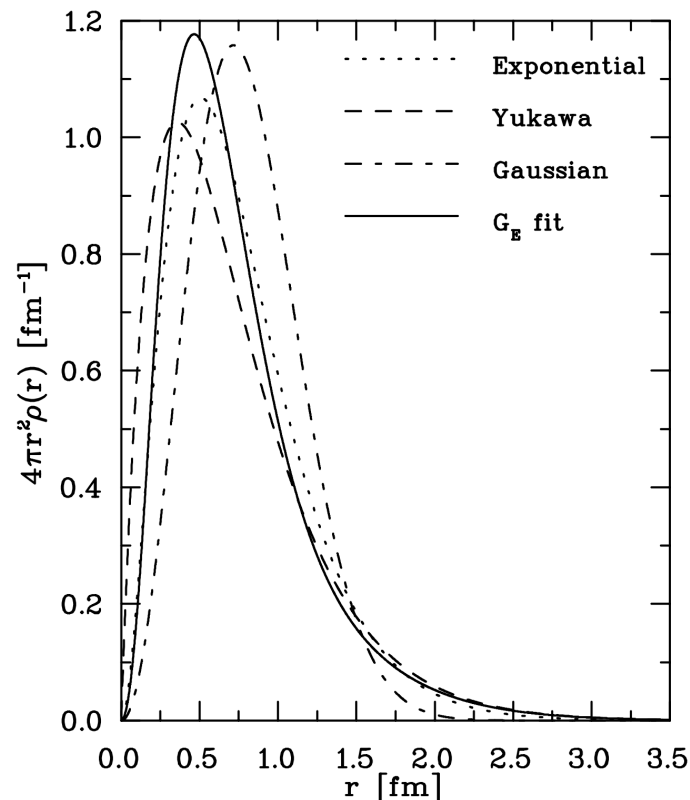
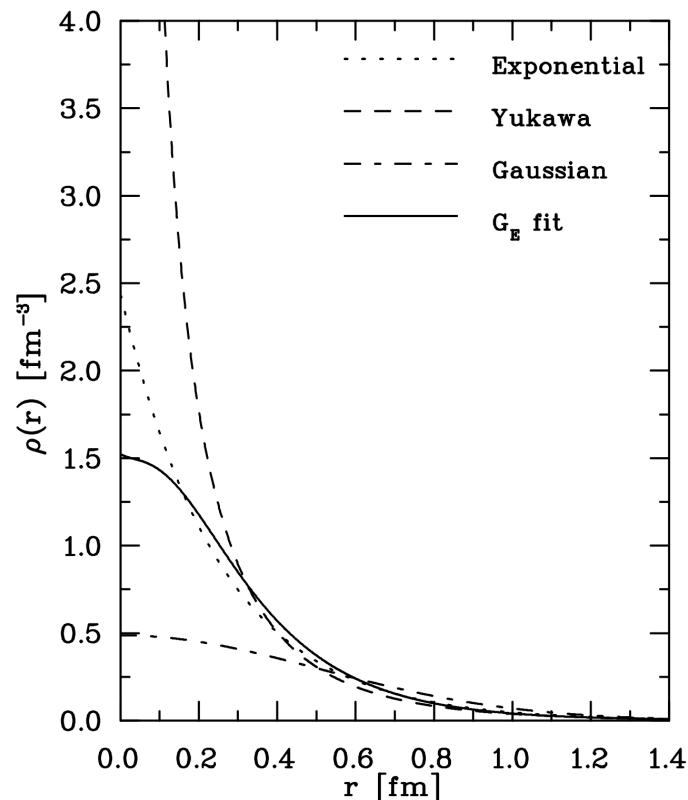


$$\Delta E(2P_{3/2}^{F=2} - 2S_{1/2}^{F=1}) = 209.9779(49) - 5.2262 r_p^2 + 0.0347 r_p^3 \text{ [meV]}$$

more recently: Carroll, Thomas, Rafelski, Miller (1108.2541):

“Proton form-factor dependence of the finite-size correction to the Lamb shift in muonic hydrogen”

Various charge distributions: Exponential, Yukawa, Gaussian, G_E fit



The r_p^3 coefficient



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more recently: Carroll, Thomas, Rafelski, Miller (1108.2541):

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resulting r_p^2 and r_p^3 coefficients:

Name	$\rho(r)$	$a [\propto \langle r^2 \rangle]$	$b [\propto \langle r^2 \rangle^{3/2}]$
exponential	Ae^{-Br}	-5.2276	0.0351
Yukawa	Ae^{-Br}/r	-5.2275	0.0378
Gaussian	Ae^{-Br^2}	-5.2276	0.0323
Ref. [1]		-5.22495	0.0347
Ref. [3]		-5.22456	0.0346
Ref. [13]		-5.2249	0.0363

The r_p^3 coefficient

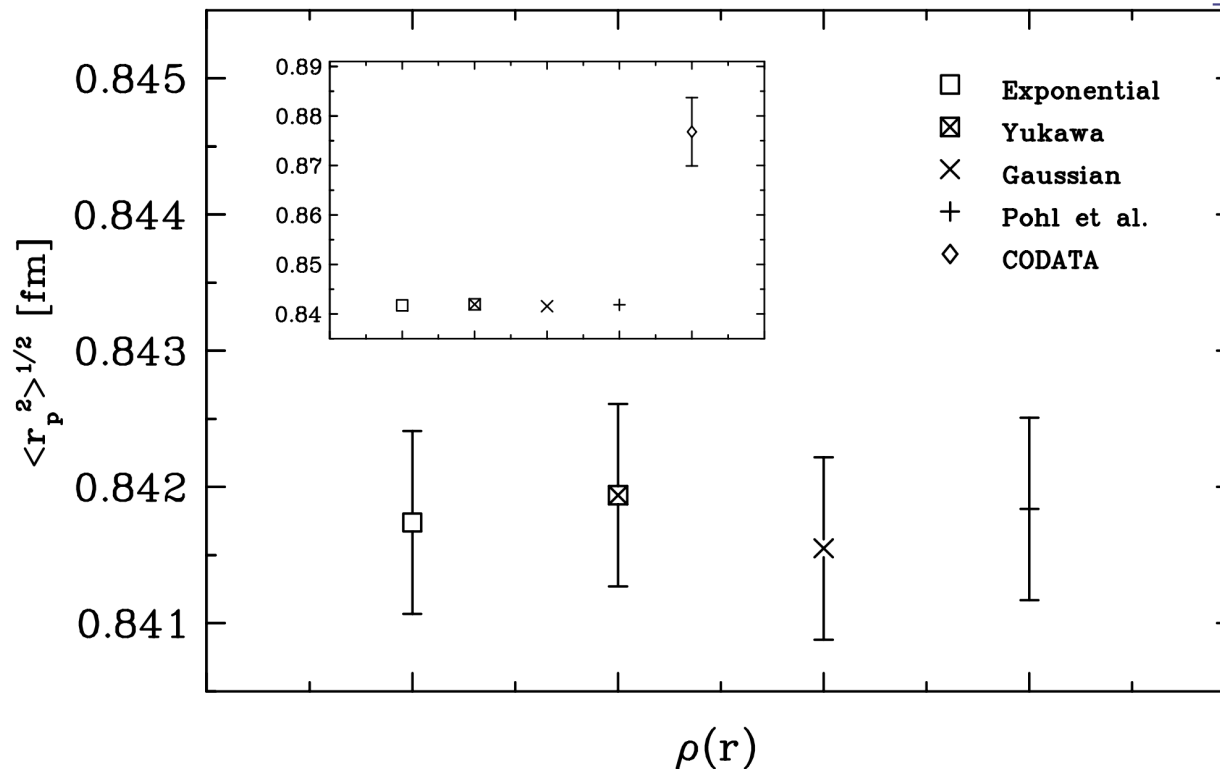


$$\Delta E(2P_{3/2}^{F=2} - 2S_{1/2}^{F=1}) = 209.9779(49) - 5.2262 r_p^2 + 0.0347 r_p^3 \text{ [meV]}$$

more recently: Carroll, Thomas, Rafelski, Miller (1108.2541):

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and the corresponding r_p values they extract



Name	$\rho(r)$	$\sqrt{\langle r_p^2 \rangle}$ [fm]
exponential	Ae^{-Br}	0.84174(67)
Yukawa	Ae^{-Br}/r	0.84194(67)
Gaussian	Ae^{-Br^2}	0.84155(67)
ours		0.84184(67)

r_p^3 coefficient increases
our uncertainty by 11.6%
to ± 0.00078 fm

The r_p^3 coefficient

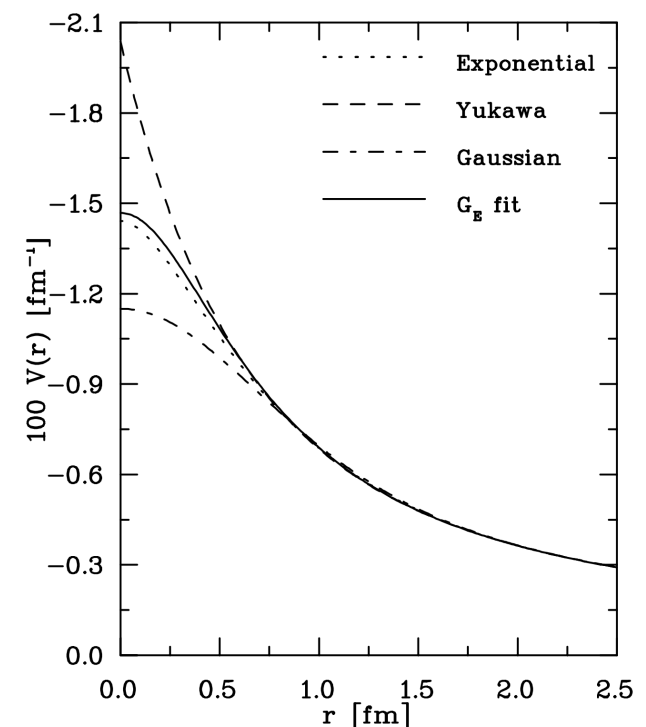
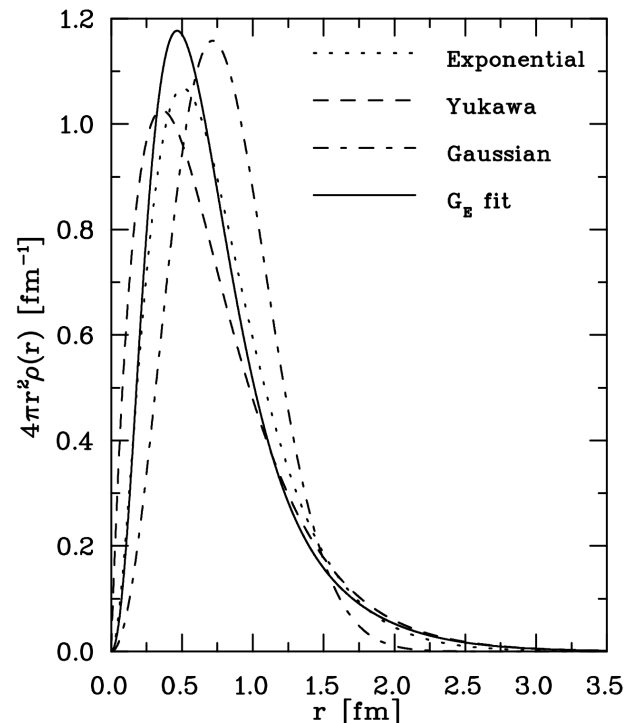
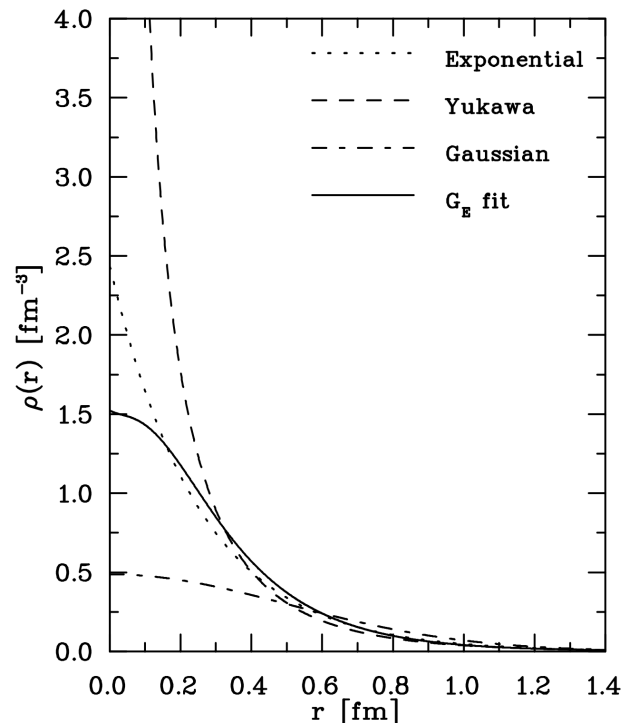


$$\Delta E(2P_{3/2}^{F=2} - 2S_{1/2}^{F=1}) = 209.9779(49) - 5.2262 r_p^2 + 0.0347 r_p^3 \text{ [meV]}$$

more recently: Carroll, Thomas, Rafelski, Miller (1108.2541):

“Proton form-factor dependence of the finite-size correction to the Lamb shift in muonic hydrogen”

Very different charge distributions give quite **similar Coulomb potentials**:



Contributions to the μp Lamb shift



#	Contribution	Value	Unc.
3	Relativistic one loop VP	205.0282	
4	NR two-loop electron VP	1.5081	
5	Polarization insertion in two Coulomb lines	0.1509	
6	NR three-loop electron VP	0.00529	
7	Polarisation insertion in two and three Coulomb lines (corrected)	0.00223	
8	Three-loop VP (total, uncorrected)		
9	Wichmann-Kroll	-0.00103	
10	Light by light electron loop ((Virtual Delbrück)	0.00135	0.00135
11	Radiative photon and electron polarization in the Coulomb line $\alpha^2 (Z\alpha)^4$	-0.00500	0.0010
12	Electron loop in the radiative photon of order $\alpha^2 (Z\alpha)^4$	-0.00150	
13	Mixed electron and muon loops	0.00007	
14	Hadronic polarization $\alpha (Z\alpha)^4 m_r$	0.01077	0.00038
15	Hadronic polarization $\alpha (Z\alpha)^5 m_r$	0.000047	
16	Hadronic polarization in the radiative photon $\alpha^2 (Z\alpha)^4 m_r$	-0.000015	
17	Recoil contribution	0.05750	
18	Recoil finite size	0.01300	0.001
19	Recoil correction to VP	-0.00410	
20	Radiative corrections of order $\alpha^n (Z\alpha)^k m_r$	-0.66770	
21	Muon Lamb shift 4th order	-0.00169	
22	Recoil corrections of order $\alpha (Z\alpha)^5 \frac{m}{M} m_r$	-0.04497	
23	Recoil of order α^6	0.00030	
24	Radiative recoil corrections of order $\alpha (Z\alpha)^n \frac{m}{M} m_r$	-0.00960	
25	Nuclear structure correction of order $(Z\alpha)^5$ (Proton polarizability)	0.015	0.004
26	Polarization operator induced correction to nuclear polarizability $\alpha (Z\alpha)^5 m_r$	0.00019	
27	Radiative photon induced correction to nuclear polarizability $\alpha (Z\alpha)^5 m_r$	-0.00001	
	Sum	206.0573	0.0045

Contributions to the μp Lamb shift



Contribution	our selection		Pachucki	Borie
Leading nuclear size contribution	-5.19745	$\langle r_p^2 \rangle$	-5.1974	-5.1971
Radiative corrections to nuclear finite size effect	-0.0275	$\langle r_p^2 \rangle$	-0.0282	-0.0273
Nuclear size correction of order $(Z\alpha)^6 \langle r_p^2 \rangle$	-0.001243	$\langle r_p^2 \rangle$		
Total $\langle r_p^2 \rangle$ contribution	-5.22619	$\langle r_p^2 \rangle$	-5.2256	-5.2244
Nuclear size correction of order $(Z\alpha)^5$	0.0347	$\langle r_p^3 \rangle$	0.0363	0.0347
Nuclear size correction of order $(Z\alpha)^6 \langle r_p^4 \rangle$	-0.000043	$\langle r_p^2 \rangle^2$		

Contributions to the μ p Lamb shift



Lamb shift: $\Delta E_{LS} = 206.0573(45) - 5.2262 r_p^2 + 0.0347 r_p^3$ meV

$u = 0.0045$ meV dominated by proton polarizability

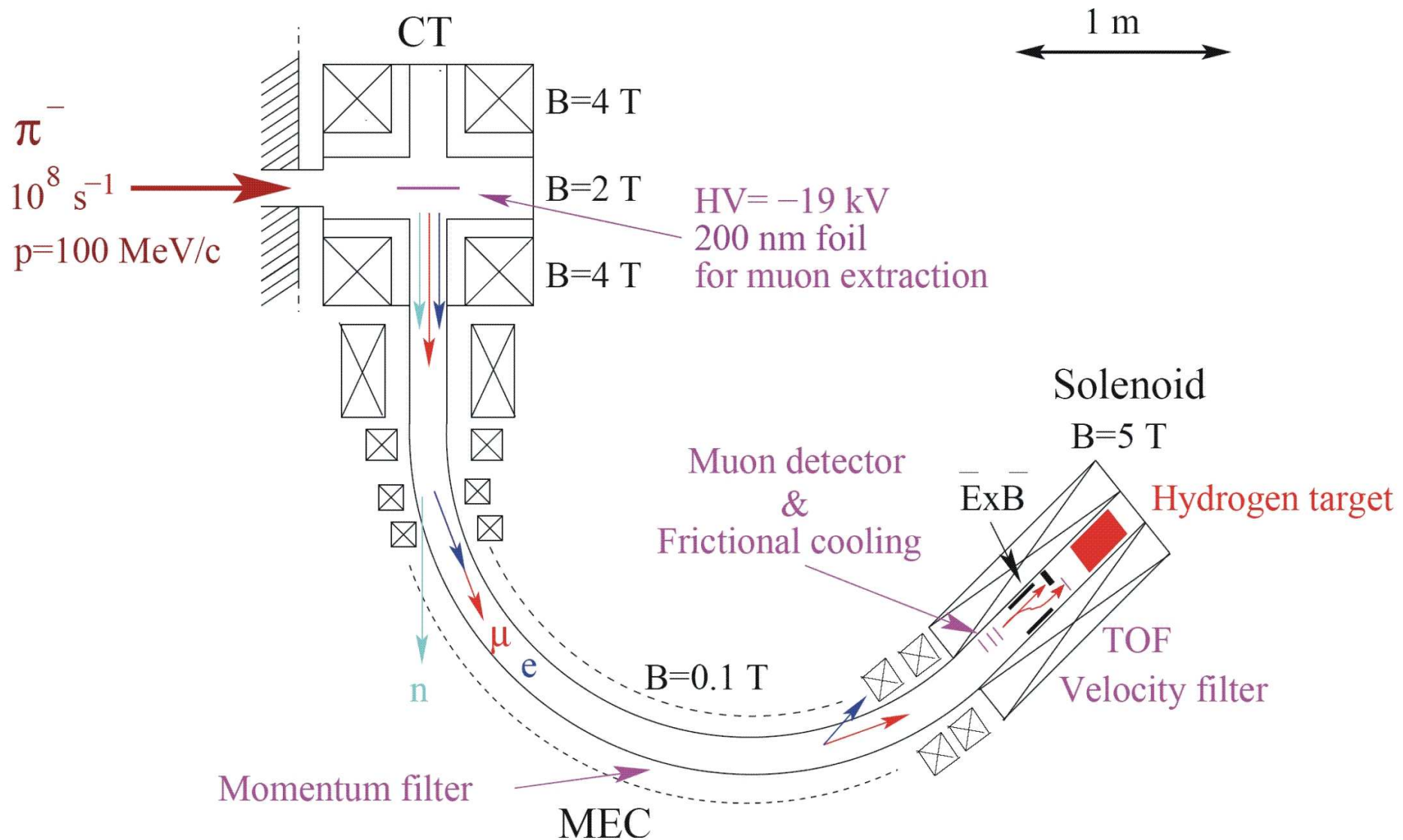
$2S$ Hyperfine structure: $\Delta E_{HFS}^{2S} = 22.8148(78)$ meV

using $R_Z = 1.022$ fm and scatter.

Fine structure: $\Delta E_{FS} = 8.352082$ meV

$2P_{3/2}$ Hyperfine structure: $\Delta E_{HFS}^{2P_{3/2}} = 3.392588$ meV

Muon beam line



What's wrong ??



- PRA **81**, 060501 (2010) Karshenboim et al.: "Nonrelativistic contributions of order $\alpha^5 m_\mu c^2$ to the Lamb shift in muonic ..." (1005.4879)
- JETP Lett. **92**, 8 (2010) Karshenboim et al.: "Contribution of light-by-light scattering to energy levels of light muonic atoms" (1005.4880)
- PRL **105**, 242001 (2010) Bernauer et al.: "High-precision determination of the electric and magnetic form factors of the proton" (1007.5076)
- PRD **82**, 125020 (2010) Jaeckel, Roy: "Spectroscopy as a test of Coulomb's law" (1008.3536)
- PLB **693**, 555 (2010) De Rujula: "QED is not endangered by the proton's size" (1008.3861)
- Nucl.Phys.News **21**, 14 (2011) Vanderhaeghen, Walcher: "Long range structure of the nucleon" (1008.4225)
- Can. J. Phys. **89**, 109 (2011) Jentschura: "From first principles of QED to an application: hyperfine structure of P states of muonic hydrogen"
- PRC **83**, 012201(R) (2011) Cloet, Miller: "Third Zemach moment of the proton" (1008.4345)
- PRD **82**, 113005 (2010) Hill, Paz: "Model-independent extraction of the proton charge radius from electron scattering" (1008.4619)
- PLB **697**, 26 (2011) De Rujula: "QED confronts the proton's radius" (1010.3421)
- PLB **696**, 343 (2011) Distler et al.: "The RMS radius of the proton and Zemach moments" (1011.1861)
- EPJD **61**, 7 (2011) Jentschura: "Proton radius, Darwin-Foldy term and radiative corrections" (1012.4029)
- PRL **106**, 153001 (2011) Barger, Chiang, Keung, Marfatia: "Proton size anomaly" (1011.3519)
- PRA **83**, 012507 (2011) Yerokhin: "Nuclear-size corrections to the Lamb shift of one-electron atoms" (1011.4272)
- PRD **83**, 101702(R) (2011) Tucker-Smith, Yavin: "Muonic hydrogen and MeV forces" (1011.4922)
- Ann. Phys. **326**, 500 (2011) Jentschura: "Lamb shift in muonic hydrogen I: Verification and update of theoretical predictions" (1011.5275)
- Ann. Phys. **326**, 516 (2011) Jentschura: "Lamb shift in muonic hydrogen II: Analysis of the discrepancy of theory and experiment" (1011.5453)
- Few-Body Syst. **50**, 367 (2011) Sick: "Troubles with the proton rms radius"
- PRD **83**, 035020 (2011) Brax, Burrage: "Atomic precision tests and light scalar couplings" (1010.5108)
- PRA **83**, 042509 (2011) Carlson et al.: "Proton-structure corrections to hyperfine splitting in muonic hydrogen" (1101.3239)
- PRL **106**, 193007 (2011) Pachucki: "Nuclear structure corrections in muonic deuterium" (1102.3296)
- PRL **107**, 011803 (2011) Batell, McKeen, Pospelov: "New parity-violating muonic forces and the proton charge radius" (1102.3296)
- PRA **84**, 012506 (2011) Carroll et al.: "Nonperturbative relativistic calculation of the muonic hydrogen spectrum" (1104.2971)
- PRA **84**, 012505 (2011) Jentschura: "Relativistic reduced-mass and recoil corrections to vacuum polarization in muonic hydrogen, ..." (1107.1737)
- PRA **84**, 020101(R) (2011) Miller, Thomas, Carroll, Rafelski: "Toward a resolution of the proton size puzzle" (1101.4073)
- PRA **84**, 020102(R) (2011) Carlson, Vanderhaeghen: "Higher-order proton structure corrections to the Lamb shift in muonic hydrogen" (1101.5965)

- PLB 693, 555 De Rujula: “QED is not endangered by the proton’s size” (1008.3861)

A large **third Zemach moment** $\langle r_p^3 \rangle_{(2)} = \int d^3r_1 d^3r_2 \rho(r_1) \rho(r_2) |\mathbf{r}_1 - \mathbf{r}_2|^3$

of the proton **can explain all three measurements**: μ_p , H, e-p

$\rho(r)$ is not a simple Dipole, but has “core” and “tail”

- PRC 83, 012201 Cloet, Miller: “Third Zemach moment of the proton” (1008.4345)

Such a large third Zemach moment is **impossible**.

$$\langle r_p^3 \rangle_{(2)} \text{ (De Rujula)} = 36.6 \pm 6.9 \text{ fm}^3$$

$$\langle r_p^3 \rangle_{(2)} \text{ (Sick)} = 2.71 \pm 0.13 \text{ fm}^3$$

- PLB 696, 343 Distler *et al*: “The RMS radius of the proton and Zemach moments” (1011.1861)

$$\langle r_p^3 \rangle_{(2)} \text{ (Mainz 2010)} = 2.85 \pm 0.08 \text{ fm}^3$$

Discussions: New Physics



- PRD 82, 125020 Jaeckel, Roy: “Spectroscopy as a test of Coulomb’s law” (1008.3536)
hidden photons, minicharged particles → deviations from Coulomb’s law.
 μp transition can NOT be explained this. (contradicts Lamb shift in H)
- PRL 106, 153001 Barger et al.: “Proton size anomaly” (1011.3519)
decay of Υ , J/ψ , π^0 , η , neutron scattering, muon g-2, $\mu^{24}\text{Mg}$, $\mu^{28}\text{Si}$
⇒ It’s NOT a new flavor-conserving spin-0, 1 or 2 particle
- PRD 83, 101702 Tucker-Smith, Yavin: “Muonic hydrogen and MeV forces” (1011.4922)
MeV force carrier can explain discrepancies for r_p and $(g-2)_\mu$
IF coupling to e , n is suppressed relative to coupling to μ , p
prediction for μHe^+ , $\mu^+\mu^-$
- PRL 107, 011803 Batell et al.: “New Parity-violating muonic forces” (1103.0721)
10...100 MeV heavy photon (“light Higgs”) can explain r_p and $(g-2)_\mu$
prediction for μHe^+ , enhanced PNC in muonic systems
- 1109.6652, Barger et al.: “Constraint on parity-violating muonic forces”
No missing mass events observed in leptonic Kaon decay.
⇒ no light Higgs.

- EPJD **61**, 7 Jentschura: “Proton radius, Darwin-Foldy term and radiative corrections”
 - Darwin-Foldy term: Zitterbewegung of spin-1/2 nucleus
 - Atomic physics: Nuclear size is *without* DF term (point-like $\rightarrow r=0$)
 - Nuclear physics: DF term sometimes pushed into nuclear size
 - CODATA: $\rightarrow$ consistent treatment $\Rightarrow$ proton charge radius = slope of electric Sachs G_E FF, w/o DF term
 - Radiative corrections are treated consistently.
- PRA **83**, 012507 Yerokhin: “Nucl. size corr. to the Lamb shift of 1-e atoms” (1011.4272)
 - Higher-order NS corr. to SE, VP increase LO result by 4.4%
 - shifts H(1S) state by ~ 800 Hz $\Leftrightarrow$ 110'000 Hz discrepancy
- Ann. Phys. **326**, 500 Jentschura: “LS in μp 1: Theory verification + update” (1011.5275)
 - μp theory ok, minor corrections $\rightarrow r_p = 0.84169(66)$ fm
- Ann. Phys. **326**, 516 Jentschura: “LS in μp 2: Analysis of discrepancy” (1011.5453)
 - no millicharged particles, no unstable neutral vector boson
 - e^- bound to $\mu p(2S)$!?!?!
NO!!!

- EPJD 61, 7 Jentschura: “Proton radius, Darwin-Foldy term and radiative corrections”

e^- bound to $\mu p(2S)$ not likely:

- How should this bound state form?

- “No” free electrons.

- Why should this bound state be stable?

- Stark mixing !?!

- Auger effect !!

- Collisions: every 100 ns.

- Only 1 line observed: >80% formation rate in 1 state.

- no peak at expected position

- observed peak has expected width

- no milli-charged particles, no unstable neutral vector boson

- e^- bound to $\mu p(2S)$!? !? !?

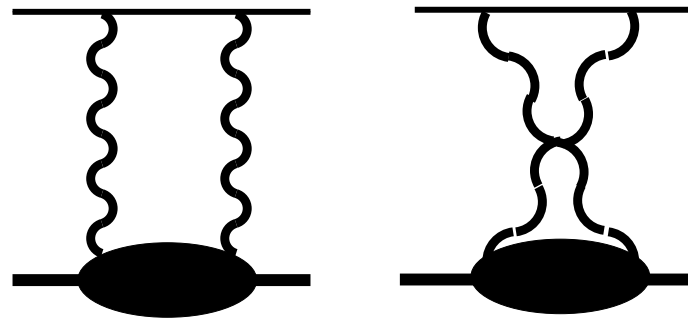
NO!!!

- PRA 84, 012506 J.D. Carroll, A.W. Thomas, J. Rafelski, and G.A. Miller:
“Nonperturbative relativistic calculation of the muonic hydrogen spectrum”, (1104.2971)
 - Theory in muonic hydrogen **confirmed** by fully numerical calculations.
 - Creative treatment of the 2S HFS
won't fit with our measured 2nd transition in μp
 - Other than that: **Our r_p confirmed.** ✓
- 1103.1772 Borie: *“Lamb shift in light muonic atoms - revisited”*
 - Recalculation of all 2S–2P energy differences for
 - muonic **hydrogen**
 - muonic **deuterium** (measured 2009)
 - muonic **helium-3** (CREMA 2014)
 - muonic **helium-4** (CREMA 2013)
 - **Our r_p confirmed.** ✓

Discussions: Proton polarizability



proton polarizability aka. two-photon exchange



Seems to be the only contribution which *might* be able to solve the proton size puzzle by changing theory in μp .

Keep in mind:

Discrepancy: 0.31 meV

Polarizability: 0.015(4) meV **20 times smaller!**

Discussions: Proton polarizability



- PRA 83, 042509 (2011) C.E. Carlson, V. Nazaryan, K. Griffioen:
“Proton-structure corrections to hyperfine splitting in muonic hydrogen” (1101.3239)
 - The 2S HFS is **confirmed** with smaller uncertainty:
22.8146(49) meV instead of the
22.8148(78) meV we used.

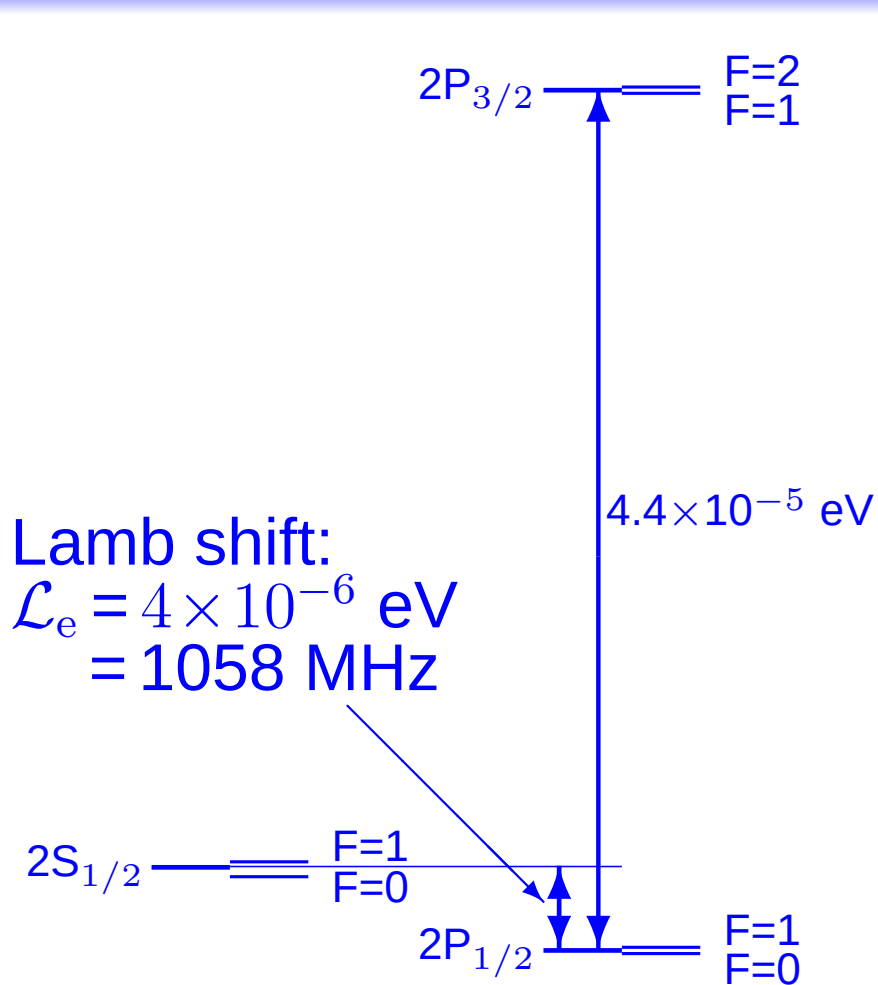
- PRA 84, 020101(R) (2011) G.A. Miller *et al.*:
“Toward a resolution of the proton size puzzle” (1101.4073)
 - New off-mass-shell effect $\sim \alpha \frac{m^4}{M^3}$ solves puzzle.
 - Others say: This is already included in standard treatment.
 - C.E. Carlson: calculation gives 50 times smaller value.
- PRA 84, 020102(R) (2011) C.E. Carlson, M. Vanderhaeghen:
“Higher-order proton structure corrections to the Lamb shift in muonic hydrogen” (1101.5965)
 - All off-shell effects are automatically included in standard treatment.
- PRL, 107, 160402 (2011) R.J. Hill, G. Paz:
“Model independent analysis of proton structure for hydrogenic bound states” (1103.4617)
 - forward Compton amplitude's $W_1(0, Q^2)$ is now well known
 - “Crazy” functional behaviour can give any correction.
 - No numbers given.

- Our value is based on 3 calculations
 - 0.017(4) meV: Rosenfelder, Phys. Lett. B 463, 317 (1999)
 - 0.012(2) meV: Pachucki, PRA 60, 3593 (1999)
 - 0.018 meV: Martynenko, Faustov, Phys. At. Nucl. 63, 845 (2000)
 - 0.015(4) meV: Borie, PRA 71, 032508 (2005)
- (0.31 meV is our discrepancy)
- No consensus about **validity** of the new claims
- Independent calculation of new effects give **50 times smaller** value.
- Lack of **numbers**

Don't know if this can solve the proton size puzzle.

Numbers are needed which can be tested in experiments.

(n=2) - states of $e p$ and μp

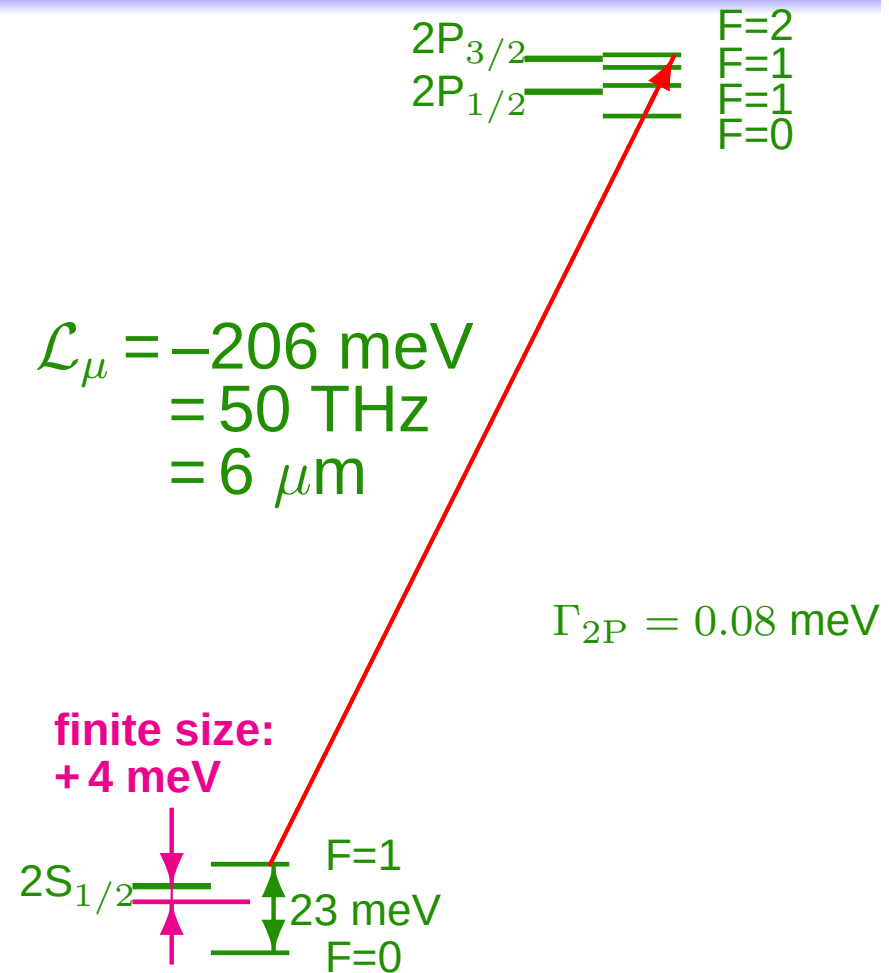


$$a_o = 5 \times 10^{-11} \text{ m}$$

$$\Delta E_{2P-1S} = 10 \text{ eV}$$

$$\text{self energy} = +1086 \text{ MHz}$$

$$\text{vac. pol.} = -27 \text{ MHz}$$



$$a_o^\mu = 3 \times 10^{-13} \text{ m}$$

$$\Delta E_{2P-1S} = 1900 \text{ eV}$$

$$\text{self energy} = +0.6 \text{ meV}$$

$$\text{vac. pol.} = -206 \text{ meV}$$

Contributions to the $\mu^4\text{He}^+$ Lamb shift



Contributions	ΔE (meV)
One-photon VP contribution, $\alpha(Z\alpha)^2$	1665.782
Two-loop VP contributions in first and second order PT, $\alpha^2(Z\alpha)^2$	15.188
Wichmann-Kroll correction	0.135
Three-loop VP in first and second order PT $\alpha^3(Z\alpha)^2$	0.138
Relativistic VP effects	-0.203
Hadronic VP	0.223
μ self-energy, μ VP, μ form factor corrections ($F_1'(0)$, $F_2(0)$)	-11.243
Recoil corrections $(Z\alpha)^4$, $(Z\alpha)^5$, $(Z\alpha)^6$	-0.355
Radiative-recoil corrections	-0.040
Nuclear structure contribution of order $(Z\alpha)^4$: $-105.322 r_{\text{He}}^2$	-297.615 (1.420)
Nuclear structure contribution of order $(Z\alpha)^5$: $1.529 r_{\text{He}}^3$	7.261 (0.035)
Nuclear structure and one- two-loop VP+ higher order nucl. structure	-2.357
Nuclear polarizability contribution	3.100 (0.600)
Total splitting	1380.020 meV

$$\begin{aligned}\Delta E(2P_{1/2} - 2S_{1/2}) &= 1670.370(10)(600) - 105.322 r_{\text{He}}^2 + 1.529 r_{\text{He}}^3 \text{ meV} \\ &= 1380.020(10)^{\text{th}}(600)^{\text{pol}}(1420)^{\text{fin. size}} \text{ meV}\end{aligned}$$

for $r_{\text{He}} = 1.681(4) \text{ fm}$ (Sick, 2008)

- Measure the transition frequency to 50 ppm ($\Leftrightarrow \Gamma/20 \Leftrightarrow 20 \text{ GHz}$)
 - Determine r_{He} with $u_r = 1 \times 10^{-3}$ accuracy
 - Limited by nuclear polarizability
 - Polarizability was calculated in 1978 with $u_r = 20\%$
- Once He nuclear polarizability is calculated with $u_r = 5\%$
 - Determine r_{He} with $u_r = 3 \times 10^{-4}$ accuracy (10 times better than now)

Transitions in $\mu^3\text{He}^+$ and $\mu^4\text{He}^+$



Isotope	Transition	ΔE [meV]	λ [nm]	Pop.(η)	Mat. el. [a_μ]	$f_{a,b}$	F_{sat} [J/cm ²]	event rate [h ⁻¹]
$\mu^4\text{He}^+$	$2S_{1/2} - 2P_{3/2}$	1526	812	1	6	8/12	1.1	48
$\mu^4\text{He}^+$	$2S_{1/2} - 2P_{1/2}$	1380	898	1	3	4/12	2.2	48
$\mu^3\text{He}^+$	$2S_{1/2}^{F=0} - 2P_{1/2}^{F=1}$	1119	1108	1/4	3	1/12	2.1	—
$\mu^3\text{He}^+$	$2S_{1/2}^{F=0} - 2P_{3/2}^{F=1}$	1294	958	1/4	6	2/12	1.1	12
$\mu^3\text{He}^+$	$2S_{1/2}^{F=1} - 2P_{1/2}^{F=1}$	1286	964	3/4	2	2/12	3.2	22
$\mu^3\text{He}^+$	$2S_{1/2}^{F=1} - 2P_{1/2}^{F=0}$	1344	923	3/4	1	1/12	6.4	13
$\mu^3\text{He}^+$	$2S_{1/2}^{F=1} - 2P_{3/2}^{F=2}$	1436	863	3/4	5	5/12	1.3	36
$\mu^3\text{He}^+$	$2S_{1/2}^{F=1} - 2P_{3/2}^{F=1}$	1461	849	3/4	1	1/12	6.4	16

adapted from A.P. Martynenko, PRA **76**, 0125505 (2007), with

$r_{4\text{He}} = 1.681(4)$ fm from I. Sick, PRC **77**, 041302, (2008).

$r_{3\text{He}} = 1.971(4)$ fm using ^3He - ^4He isotope shift from P. Mueller et al., PRL **99**, 252501 (2007).

μHe^+ Signal rates



Effect	μp 1 mbar	$\mu^4\text{He}^+$ 4 mbar	$\mu^4\text{He}^+ / \mu\text{p}$
Long lived $2S$ -population	1.1%	2.2% *	2
$2S$ sub-level population	75%	100%	1.33
$2S$ -lifetime (survival probability = $e^{-t_{\text{Laser}}/\tau_{2S}}$)	1 μs	1.7 μs *	1.65
Muon stop in gas (trigger quality Q)	40%	60%	1.5
Muonic $2S$ atoms not drifting out of laser volume	80%	100%	1.25
Laser transition probability (only 20% for some weak transitions in $\mu^3\text{He}^+$)	30%	30%	1
Laser repetition rate	500 s^{-1}	500 s^{-1}	1
Detection of Lyman alpha X-ray	70%	70%	1
Total event rate increase: for $\mu^4\text{He}^+$			8
Total event rate increase: for $\mu^3\text{He}^+$ strong transition and triplet population			6
Total event rate increase: for $\mu^3\text{He}^+$ singlet population			2

* v. Arb *et al.*, Phys. Lett. B **136**, 232 (1984)

μp rate = 6 events/h $\longrightarrow$ $\mu^4\text{He}^+$ rate = 48 events/h

	$\mu^4\text{He}^+$	$\mu^3\text{He}^+$ (max)	$\mu^3\text{He}^+$ (min)	μp (max)
Event rate on resonance:	48 ev/h	36 ev/h	12 ev/h	6 ev/h
Background rate:	2.5 ev/h for all μHe^+			1 ev/h

- We want to measure the transition with **50 ppm** accuracy.

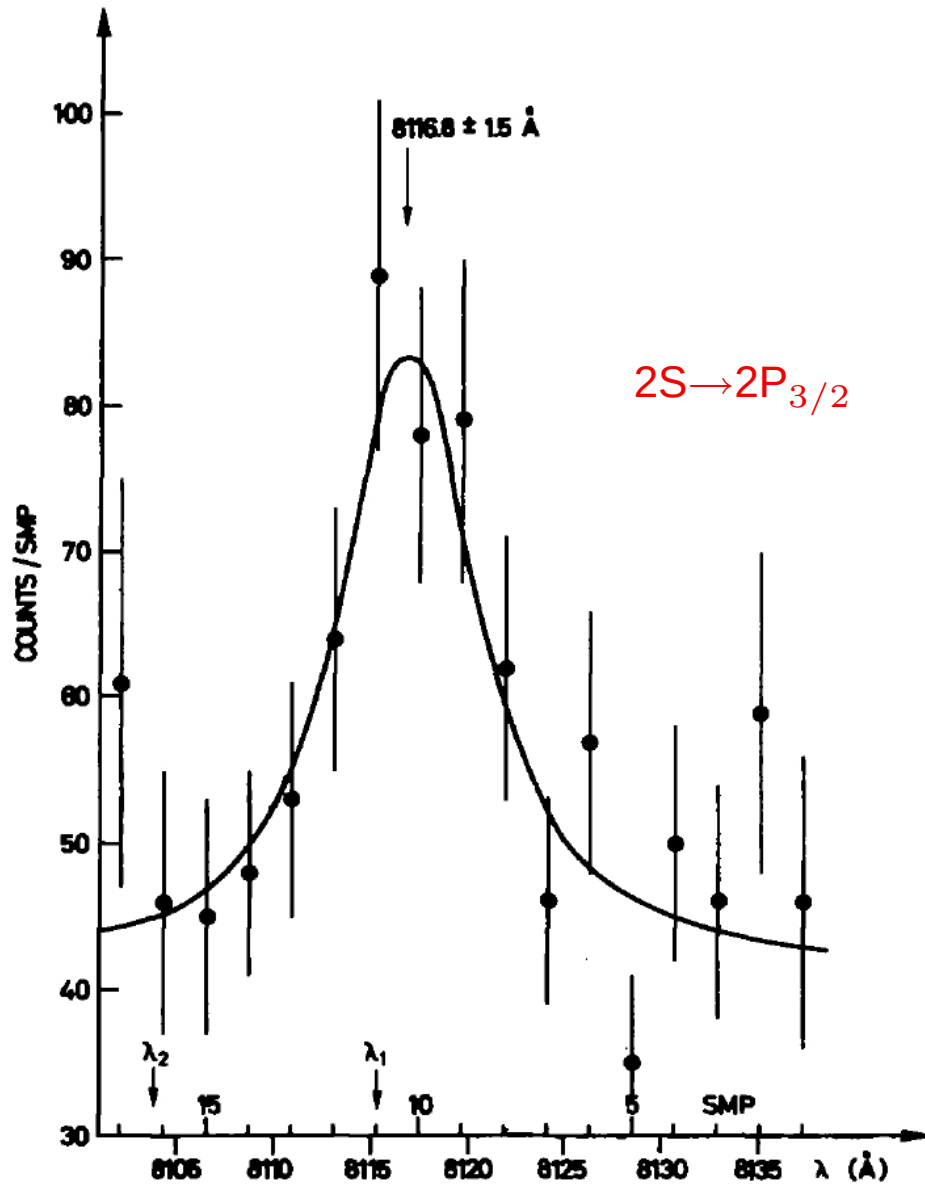
This corresponds to $\Gamma/20 = 20 \text{ GHz}$.

- 500 events are sufficient $\iff$ **1500 events** on resonance
- **laser wavelength calibration**: uncritical
(we have determined the μp transition freq. to $< 1 \text{ GHz}$)

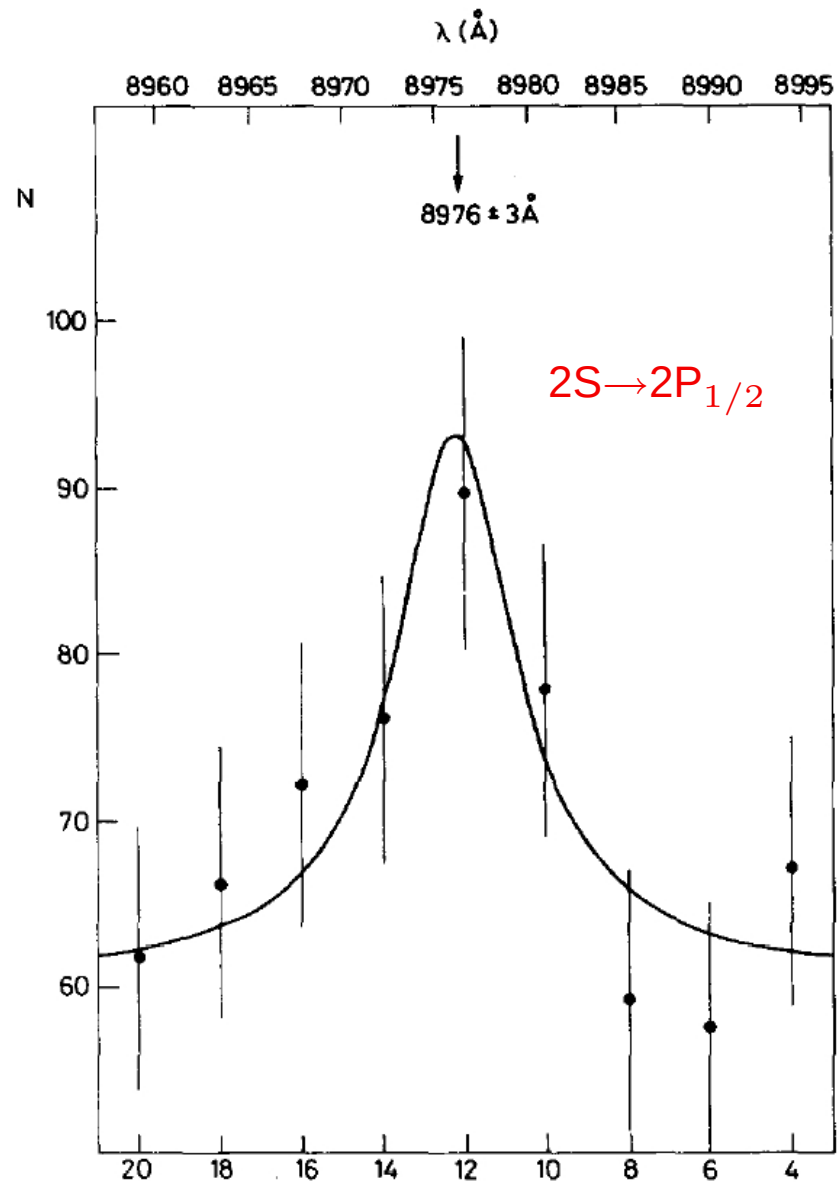
- Systematics: will be **$< 5 \text{ GHz}$**

- AC/DC-Stark shift, Zeeman shift are **all uncritical**
- Pressure shift, Doppler shift **$< 50 \text{ MHz}$** .
- Laser energy asymmetry left/right of centroid:
→ Need to measure the **average laser energy with 3% accuracy**

Old μHe^+ resonances



Carboni et al, Nucl. Phys. A273, 381 (1977)



Carboni et al, Phys. Lett. 73B, 229 (1978)