NICA project at JINR



G.Trubnikov JINR Dubna, on behalf of the team

> BLTP, Dubna, 26 August 2014



Evolution of collision region in Nucleus-Nucleus Interaction



1 fm/c = $1 \cdot 10^{-13}$ / $3 \cdot 10^{10}$ = $3 \cdot 33 \cdot 10^{-23}$ sec

"Chemical freeze-out" – finish of inelastic interactions; "Kinetic freeze-out" – finish of elastic interactions.

*) freeze-out – here means "to get rid" (phys. slang)





2nd generation HI experiments

STAR/PHENIX @ BNL/RHIC.

designed for high energy researches ($\sqrt{s_{NN}} > 20$ GeV), low luminosity for LES program L<10²⁶ cm⁻²s⁻¹ for Au⁷⁹⁺



NA61 @ CERN/SPS.

Fixed target, non-uniform acceptance, few energies (10,20,30,40,80,160A GeV), poor nomenclature of beam species

3nd generation HI experiments



CBM @ FAIR/SIS-100/300 Fixed target, E/A=10-40 GeV, high luminosity



MPD & SPD @ JINR/NICA.

Collider, small enough energy steps in the range $\sqrt{s_{NN}} = 4-11$ GeV, a variety of colliding systems, L~10²⁷ cm⁻²s⁻¹ for Au⁷⁹⁺

Baryon density in Au + Au collisions at $\sqrt{S_{NN}} = 4 - 11 \text{ GeV/u}$



u - "unit" => from "amu" -

An example:

- atomic mass unit

Fixed target, ions, $E_1 = 100 \text{ GeV/u}$

$$E_1^{total} = 100 + 0.938 \ GeV/u, \quad E_2^{total} = 0.938 \ MeV/u,$$

 $\sqrt{s} \approx 13.76 \ GeV/u, \quad E_1^{total} >> m_u c^2$

<u>Colliding beams</u>: the same √s at (E₁)_{kin} = (E_{kin})₂ ≈ 6 GeV/u

What is a problem? Luminosity!



Luminosity

Luminosity is a parameter of an experiment with particle beams equal to event number per time unit (rate) if the process under study has cross section of $\sigma = 1$. Luminosity is measured in cm⁻²·s⁻¹.

$$L = \begin{cases} \frac{N_1 N_2}{S} \cdot f & \text{for colliding beams} \\ \left(n_0 l \right)_{t \, arg \, et} \cdot \frac{dN}{dt} & \text{for fixed target experiment} \end{cases}$$

 N_1 , N_2 - particle number in colliding beams, 5 - maximal crosssection of two beams, f - frequency of collisions (for collider particle rvolution frequency in the ring); n_0 - target density (cm⁻³), l - target thickness, dN/dt - particle flux bombarding the target.

NĬCA

Fixed target experiment: a particle beam extracted from an accelerator bombards an immovable ("fixed") target

$$\sqrt{s} \approx E_{total}^{cms} \approx \begin{cases} \sqrt{2Mc^2 E_{ion_total}^{lab}}, E_{ion_total}^{lab} >> Mc^2 \\ (m+M)c^2 + \frac{M}{m+M} \cdot E_{ion_kin}^{Lab}, E_{ion_kin}^{Lab} << mc^2, Mc^2 \end{cases}$$

Both primary particles and generated in collision with fixed target move with <u>the speed of the center of the mass</u> in direction of primary (bombarding) particle!

Colliding beams

$$s = E_{total}^{cms} = E_{1total} + E_{2total}, \quad p_1 = p_2 (!)$$

History of colliding beams

1956, D.W.Kerst et al., – First proposal, pp collider

1958 - 1965 VEP, INP at Novosibirsk



<u>G.Budker</u>, A.Naumov, <u>A.Skrinsky</u>, S.Popov, V.Sidorov, G.Tumaikin et al.

> $e^{-}e^{-}$, 2 x 160 MeV, L = 3.10²⁷ cm⁻².s⁻¹





1958 - 1965 SLAC

Princeton-Stanford group: G. K. O'Neill, B.Richter et al.

e⁻e⁻ collider 2 x 500 MeV



Wolfgang ("Pief") Panofsky





Motivation:

"Experiments with spin have killed more theories than any other single physical parameter." (J.D.Bjorken) [Cited by Elliot Leader, "Spin in Particle Physics", Cambridge Univ. Press, 2001]





Future Machines with Polarized Beams





NICA White Paper - International Effort



Draft v 10.01 January 24, 2014

> SEARCHING for a QCD MIXED PHASE at the NUCLOTRON-BASED ION COLLIDER FACILITY (NICA White Paper)

Statistics of White Paper Contributions

111 contributions: **188** authors from **70** centers in **24** countries

Indicates the activity of scientific community









Unique Dubna technologies of fast-cycling superconducting magnets tested during several tens of Nuclotron runs and chosen as basic for accelerator complexes NICA and FAIR

Common European Research infrastructure for Heavy Ion High Energy Physics: NICA + FAIR





Superconducting accelerator complex NICA (Nuclotron based Ion Collider fAcility)



NICA goals

1a) Heavy ion colliding beams 197Au79+ x 197Au79+ at $\sqrt{s_{NN}} = 4 \div 11 \text{ GeV} (1 \div 4.5 \text{ GeV/u} \text{ ion kinetic energy})$ at L_{average}= 1x10²⁷ cm⁻²·s⁻¹ (at $\sqrt{s_{NN}} = 9 \text{ GeV}$)

1b) Light-Heavy ion colliding beams of the same energy range and L

2) Polarized beams of protons and deuterons in collider mode:

 $p\uparrow p\uparrow \sqrt{s_{pp}} = 12 \div 27 \text{ GeV} (5 \div 12.6 \text{ GeV kinetic energy})$

 $d\uparrow d\uparrow \sqrt{s_{NN}} = 4 \div 13.8 \text{ GeV} (2 \div 5.9 \text{ GeV/u ion kinetic energy})$

 $L_{average} \ge 1x10^{31} \text{ cm}^{-2} \cdot \text{s}^{-1}$ (at $\sqrt{s_{pp}} = 27 \text{ GeV}$)

3) The beams of light ions and polarized protons and deuterons for fixed

target experiments:

Li \div Au = 1 \div 4.5 GeV /u ion kinetic energy p, p[↑] = 5 \div 12.6 GeV kinetic energy d, d[↑] = 2 \div 5.9 GeV/u ion kinetic energy

4) Applied research on ion beams at kinetic energy

from 0.5 GeV/u up to 12.6 GeV (p) and 4.5 GeV /u (Au)

Here must be Movie...

NICA: <u>Nuclotron based</u> <u>Ion</u> <u>Collider</u> f<u>A</u>cility



B = 2T 42+Xe124

Status of the Nuclotron

Perfect test-bench for NICA booster/collider modes

Energy:

5.15 GeV/u (~ 1.8 T) – routine operation (At higher field the routine operation after 2015)

Intensity:

Deuterons - 3e10 (maximum achieved 5e10) Light ions – 5e9 ppp (new Laser Source for ions) Heavy ions – 1e6, after the Booster commissioning – 1e9 (2016) Polarized deuterons – 1e10 starting from 2015

Slow extraction:

Duty factor:

 $K_dc = 0.8 - 0.9$

50% (the beam lines in bld. #205 have to be tested and recertified)

- Stochastic cooling of coasting and bunched carbon (C6+) beam
- Beam acceleration up to maximum design field 2 T
- Coasting beam at two plateau
- Demonstration of slow extraction at spill duration of 20 s

Two (three) plateaus

Adiabatic debunching and recapture at efficiency of about 95% was demonstrated



Technical limit of the intermediate plateau duration is about 0.5 s now.

During 2013 (it is a question to the RF station control system) iwill be realized possibility to operate with 3 flattops: 1st-on the arising front, 2nd-main plateau, 3rd-on the back front (useful for polarimetry).

Veksler & Baldin Laboratory of High Energy Physics, JINR



Source of polarized ions (p, d, H) JINR+INR RAS



the intensity of the accelerated polarized beams (D+,H+) at the JINR Accelerator Complex up to **10¹⁰ p/pulse**

Results of the test to the end of 2013: polarized protons and deutrons up to 10¹¹ ppp.

HV power supplies rack

We plan to assemble and TEST SPI at Nuclotron with [↑]d in 2015 year After commissioning of the new RFQ foreinjector for LU-20

Progress in ion sources development and commissioning

Source for polarized particles (SPP)



Source is assembled in 2013 and works on its commissioning had been started in June 2013. The goal is to get 10¹⁰ deuterons per pulse.

Heavy ion source: Krion-6T ESIS



B= 5.4 Tesla magnetic field reached in a robust regime. Full-scale tests of new ESIS in reflex mode of operation was started in spring 2013.
Test gold ion beams have been produced:
Au³⁰⁺ ÷ Au32³²⁺, 6·10^8 ppp, T_{ioniz} = 20 ms for
Au³²⁺ -> repetition rate 50 Hz.
ion beams Au⁵¹⁺ ÷ Au⁵⁴⁺ are produced.

Now the goal is: production of Au⁶⁵⁺ ÷ Au⁶⁹⁺

ion beams for their possible injection into LU-20 -> Nuclotron in spring 2014. 22

Injection complex

New laser source for ions

New Nd-YAG laser,

 $E \ge 2 J$, $\tau \approx 7-8 \text{ ns}$, $\sim 5 \cdot 10^{12} \text{ W/cm}^2$



LU-20



New foreinjector for LU-20

sia

		Production in Russ
	Z/A	1.0- 0.3
	Max current, [mA]	≤20
	Output energy [MeV/u]	0.156
	RFQ lengh, [m]	≤ 3
		•



Injection complex. Development

New Heavy Ion Linac (HILac) – under completion









2013 October (70% readiness)













Magnets for the Booster



Booster dipole at cryo-test (9690A) and magnetic measurements



Cryogenic test-bench @ LHEP



Quadrupole lense at assembly for test



Sextupole corrector prototype (for SIS100 and NICA booster) at assembly

Nuclotron – Collider beam line

Goals of the beam line

- The beam transport with minimal ion losses.
- The beam matching with lattice functions of Collider rings*.
- * except vertical dispersion which suppression is required.



Beam Farameters				
Sort of ions	Au ⁷⁹⁺			
Energy of ions, GeV/u	1÷4.5			
Magnetic rigidity of ions, T m	14 ÷ 45			
lon number	1·10 ⁹			

Ream Parameters

Nuclotron – Collider beam line

Parameters of magnetic elements

Magnetic element	Number	Effective length, m	Max. magnetic field (gradient), T (T/m)
Horizontal bending magnet	19	2	1.5
Vertical bending magnet	6	2	1.5
Switch bending magnet	1	2	1.5
Quadrupole	45 ÷ 50	0.5	20





Designed by BINP team







Collider parameters

Parameter	Value
Circumference, m	503.04
Max. magnetic rigidity, T.m	45.0
Max. magnetic field, T	1.8
Acceptance, π ·mm·mrad	40.0
Longitudinal acceptance (<i>Ap/p</i>)	± 0.01
Number of dipole magnets	80

Collider

FODO, 12 cells x 90° each arc,

 $\gamma_{\rm tr}$ = 7.091 , β^* = 0.35 m (variable)



Collider parameters



Maximal achievable luminosity, average

$$L = \frac{dN}{dt}_{reaction} / \sigma_{reaction} \le \frac{dN}{dt}_{production} / \sigma_{loss}$$

Examples:

NICA: Ion generation rate: 10⁹ per 4 seconds, reaction cross-section = 7 barn $L \le \frac{10^9}{4c \cdot 7 \cdot 10^{-24} cm^2} = 3.6 \cdot 10^{31} cm^{-2} c^{-1}$

RHIC (100 GeV/u), cross-section ~ 219 barn L_{max} ~ 5.10²⁹ cm⁻² s⁻¹

CBM (FAIR) Acceleration at SIS300 up to 10^{10} U ions, extraction during 10 sec $L_{max} \sim 10^{32} \text{ cm}^{-2} \text{ s}^{-1}$

PANDA (FAIR) Antiproton production rate 10^7 / sec, cross-section 0.05 barn $L_{max} = 10^7/5 \cdot 10^{-26} = 2 \cdot 10^{32} \text{ cm}^{-2} \text{ s}^{-1}$

Cycle parameters limitations

RHIC: Filling of both rings and acceleration up to E_exp ~ 15 min Experiment duration (L_lifetime) ~ 4 hours

 $L_{max} \sim 1.2 \cdot 10^{30} \text{ cm}^{-2} \text{ c}^{-1} * 1/4 /4 \sim 8 \cdot 10^{28} \text{ cm}^{-2} \text{ s}^{-1}$

Average luminosity RHIC 10²⁸ cm⁻² s⁻¹ – During experiment decreases by 20-30% **This will require more intensive collider filling (more often)**

NICA It is planned to fill both rings during 200 sec, "Luminosity lifetime ~ 2000 sec $L_{max} \sim 3.6 \cdot 10^{31} \text{ cm}^{-2} \text{ s}^{-1} * 2/20 \sim 3.6 \cdot 10^{30} \text{ cm}^{-2} \text{ s}^{-1}$

At designed luminosity 10²⁷ cm⁻² s⁻¹ and stabilization of beam emittances due to beam cooling, the luminosity of experiment is practically constant (if main loss mechanism is defined by interaction at Collision Point). Limitation to the experiment characteristical time is connected to losses due to interaction with residual gas

NICA Injection chain is designed with reserve of k~ 50
Limitations caused by Detector possibilities (event count)

Each detector sub-system has technical limitations on event count and registration

$$L_{\max,\det\,ector} = \frac{dN}{dt}_{count} / \sigma_{reaction}$$

Rate of MPD is 7 kHz

$$L \le \frac{7 \cdot 10^3 Hz}{7 \cdot 10^{-24} cm^2} = 10^{27} cm^{-2} s^{-1}$$

In the fixed target experiment we can control optimal detector load by varying width of the target. But during energy scan the geometry of the reaction products changes

Collider luminosity

$$L = n_b f_{rev} \iint_{V_t} \sqrt{(\vec{v}_1 - \vec{v}_2)^2 - \frac{[\vec{v}_1 \times \vec{v}_2]^2}{c^2}} \rho_1 \rho_2 dV dt$$



For similar round-shape bunches colliding at zero angle:

$$L = \frac{n_b N_b^2}{4\pi\varepsilon\beta^*} f_{rev} f\left(\frac{\sigma_s}{\beta^*}\right)$$

$$f\left(\frac{\sigma_s}{\beta^*}\right) = \frac{1}{\sqrt{\pi}} \int_{-\infty}^{\infty} \frac{\exp(-u^2) du}{\left[1 + \left(\frac{u\sigma_s}{\beta^*}\right)^2\right]}$$

- to increase number of bunches -> parasitic collisions;
- to increase bunch current -> coherent instability;
- to decrease emittance (bunch size) -> incoherent tune shift -> resonanses;
- to decrease IP beta-function -> severe demands to FF QL, chromaticity;
- to increase rev. frequency -> to decrease circumference (no space for equipment)
- to have optimal bunch length ("hour-glass" effect).

Example of the optic structure in the IP region



vacuum chambers walls

Bunch length







β* **= 0.5** m

	RHIC	NICA
Circumference, m	3800	503
Bunch spacing, m	3800/120 = 32 (electron clouds, injection, parasitic collisions)	15 (distance between dipoles)
Beta-function at IP	5	0.35
Distance from IP to FFL	50	5

$$\frac{L_{NICA}}{L_{RHIC}} = \frac{3800}{500} \frac{32}{15} \frac{5}{0.35} \approx 230$$

$$3.5 \text{ GeV/u}$$

RHIC < $10^{25} \text{ cm}^{-2}\text{s}^{-1}$
NICA $\ge 10^{27} \text{ cm}^{-2}\text{s}^{-1}$

Luminosity life-time



Without beam cooling - beam emittance grows due to intra-beam scattering

Characteristic time of the luminosity decrease rate ~ several minutes (at RHIC operating with 100 GeV/u ~ 4 hours)

RHIC:

Construction of the Electron cooling system at low energy ions (< 5 GeV/u), Stochastic cooling is used at maximal energy.

NICA:

Electron + stochastic cooling during beam stacking,

Electron + stochastic cooling during the experiment (collision mode)

IntraBeam scattering (IBS)

Single scattering on large angles – Touschek effect

IBS leads to 3 independent effects:

-"Maxwellisation" of the distribution fuction;

- Equal energy swaping between all 3 degrees of freedom
- Increasing of the 6D phase volume

Why IBS differs from situation when molecules interact? -

Cyclic accelerators because of curvature sections (arcs, etc) have Dispersion. Due to Dispersion the variation of the longitudinal coordinate leads to The variation of transverse oscillation amplitude.

By other words transverse and longitudinal motion are coupled.

There is no way to keep Luminosity without beam cooling !!!

Electron Cooling



superposition of a cold intense electron beam with the same velocity momentum transfer by Coulomb collisions cooling force results from energy loss in the co-moving gas of free electrons

Courtesy to M.Steck

Stochastic Cooling

First cooling method which was successfully used for beam preparation



S. van der Meer, D. Möhl, L. Thorndahl et al.

Conditions: Betatron phase advance (pick-up to kicker): $(n + \frac{1}{2}) \pi$

Signal travel time = time of flight of particle (between pick-up and kicker)

Sampling of sub-ensemble of total beam

Principle of transverse cooling: measurement of deviation from ideal orbit is used for correction kick (feedback)

Two regimes and cooling methods: injection & storage

Questions:

- 1. What kind of storage method?
- ✓ Barrier Bucket method with electron cooling application!
- 2. What about storage with stochastic cooling application?
- ✓ Problems below 2.5 GeV/u \Rightarrow studies in progress...
- 3. What kind of acceleration system is proposed?
 - ✓ Barrier Bucket system.



Barrier Bucket Method



In reality RF voltage pulses can be (and are actually) of nonrectangular shape

The first proposal: Fermilab, J. Griffin et.al., IEEE Trans. on Nuclear Science, v.NS30 No.4, 3502 (1983) The particle storage with barrier buckets method was tested at ESR (GSI) with electron cooling (2008).

NICA: T_{revolution} = 0.85 ÷ 0.96 $\mu s, V_{BB} \leq 5 \ kV$

The problems we have met and the solutions





Strategy of the cooling at experiment



IBS is calculated for equal rates in 3 degrees of freedom, $I_e = 0.5 A$



Proposed Scheme of Ion Stacking and Bunch Formation in The Collider

Barrier RF system (1-st RF)



Stochastic Cooling System

Stochastic Cooling System installed at Nuclotron - is a prototype for the NICA Collider: W=2-4 HGz, P = up to 60 W Collaboration: JINR-IKP FZJ-CERN



Ring slot-coupler RF structure (design FZJ)



Pick-Up station

Spectrum analyzer $\sigma_{init} = 0.15 \times 10^{-3}$ 15 pVe $\sigma_{final} = 0.07 \times 10^{-3}$ 12 pW- $\tau \approx 27s$ CF 2.07 $\sigma_{init} = 0.2 \times 10^{-3}$ 6 pW- $\sigma_{final} = 0.13 \times 10^{-3}$ 5 pW- $\tau \approx 64s$

Experimental results (2013): stochastic cooling of the carbon (C6+) beam, E = 2.5 GeV/u

Kicker station

Bunched beam

CF 2.385415164 GH

Span 200.0 kHz

Collider Electron cooling



1. Facility structure and operation regimes





Full-scale Nuclotron-type superconducting model dipole and quadrupole magnets for the NICA booster and collider were manufactured at Laboratory of High Energy Physics JINR. First dipole and quadrupole magnets for the NICA booster have successfully passed the cryogenic test on the bench. 3 pre-serial dipole magnets for the NICA booster will be manufactured and tested this year. Serial production of the magnets for the booster is scheduled for 2014. Cryogenic tests of the model twin aperture dipole and quadrupole magnets for the NICA collider are scheduled for the first half of this year.



Booster dipole at cryo-test (9690A) and magnetic measurements









Twin aperture dipole magnet for Collider was tested June 2013 up to 11 kA

Sextupole corrector prototype (for SIS100 and NICA booster) at assembly





Collider magnets construction



Test on vacuum tightness of the tubes for cooling the yoke





High-temperature current leads (LN temp.)



The first of four pair of HTS current leads on 18 kA before acceptance test in Dubna Collaboration with China (ASIPP): Power (high-current) HTSC current-leads up to 17 kA for NICA. Liquid N2 temperature



<u>Strategy</u>: to exchange all LHe powerful current leads at Nuclotron to HTSC and to use such HTSC in booster and Collider in order to minimize operational costs (~several times). China – is our excellent partner.

SC magnets assembly and test area (b.217): cooperation with German centers



Satellite helium refrigerators



Satellite helium refrigerator during assembly on-site in October 2013.



Satellite helium refrigerator in b.217.59

Cryogenic system for the NICA complex



New units for the NICA accelerators:

1 – 6600 Nm³/h screw compressors Kaskad-110/30; 2 – 1300 kg/h nitrogen liquefier OA-1.3: 3 – nitrogen turbo compressors Samsung Techwin SM - 5000; 4 – liquid helium tank; 5-500 kg/h nitrogen recondenser RA-0,5 of the booster: 6 – satellite refrigerator of the booster: 7 – draining and oil-purification units; 8 – 1000 l/h helium liquefier OG-1000; 9 – satellite refrigerator of the collider; 10 – 500 kg/h nitrogen recondenser RA-0,5 of the 60 collider.

Already signed agreements in cooperation with:

- CERN
- 🗖 GSI
- State committee in science
 & technology of Belarus
- Kurchatov Federal Center
- Institute for Nuclear Research RAS
- Moscow State University
- Budker Institute of Nuclear Physics RAN
- Tsinghua University, China
- Institute of Plasma Physics CAS, China
- University of Science and
 - Technology of China
- and others







1111



On-line web-camera http://betacool.jinr.ru/b/

11 11



Innovations based on Accelerator technologies

Results of a radiation damage test for PAMELA

> M. Boscherini S. Straulino December 20, 2001

Transmutaion of nuclear fuel waste



Radiobiology and medicine



Study of molecular mechanisms of genetic influence on human & mammal

Irradiation treatment of space craft elements and electronics

> logic signal. T device which or limited, so per be recovered in To ensure it it must undergo parameter for *LKT* (Linner pass of the test Under Test) ar

Obtaining the basic data for design of set-ups for nuclear waste processing

Ion tracking technologies:



Safety systems



Design and Development of accelerator and detector

technologies for medicine





...What NEXT ?...





Heaviest atoms in QED





Yu. Oganessian 113-th Session of the Scientific Council of JINR, Feb.21, 2013, Dubna





Cos-φ Dipoles



Block number	5
Turn number/quadrant	34 (17+9+4+2+2)
Operating current	8924 A
Yoke inner radius	98 mm
Peak field on conductor (with self field)	4.90 T
Bpeak / Bo	1.09
Working point on load line	69%
Current sharing temperature	5.69 K
Inductance/length	2.9 mH/m
Stored energy/length	116.8 kJ/m

Discorap-Project by INFN Magnet finished in 2010

UNK project





Goal: MW proton beam to the target




Thank you for your attention !









Extraction.

stripping to

197Au79+

600

100

1(3) inj.

cycles.

e-cooling

E-cooling

(optional)

Sort of ions:	
before stripping station	Au ³¹⁺ , Au ⁵²⁺ , Au ⁶⁵⁺
after stripping station	Au ⁷⁹⁺
Maximum energy of ions,	
MeV/u	685
Maximum magnetic rigidity of	
ions, T m:	
before stripping station	25
after stripping station	11
lon number	2·10 ⁹

Startup version of the collider

Energy range from 3 to 4.5 GeV/u (optimum ~ 3.5 GeV/u)

Operation scenario:

- Stacking with BB + Stoch. longitudinal cooling
- Bunching at h = 22 and Stoch. longitudinal cooling
 Parameters

Bunch length is about 1.2 m (instead of 0.6 m)

Momentum spread of $4.2 \cdot 10^{-4}$ (instead of $1 \cdot 10^{-3}$)

Bunch intensity $5 \cdot 10^8$ (instead of $2 \cdot 10^9$)

Luminosity (1+7) \cdot 10²⁵ cm⁻²s⁻¹

Startup version of the collider: goals

- -Test of the beam stacking procedure:
- stacking efficiency, evolution of transverse emittance
- Test and optimization of Stoch. cooling system
- -Test of the beam bunching with cooling -Investigation of IBS, ring tune ability, beam life-time...

-Test of MPD systems at L ~ $5 \cdot 10^{25}$ cm⁻²s⁻¹



Big Bang & Hot Universe

The Planck Era:

Newton potential + dimension consideration

$$U = \frac{Gm^{2}}{l}$$

$$l = ct$$

$$mc^{2} = \frac{\hbar}{t}$$

$$H_{Planck} = \sqrt{\frac{\hbar c}{G}} \approx 2.2 \cdot 10^{-5} g = 10^{19} GeV / c^{2}$$

$$t_{Planck} = \sqrt{\frac{G\hbar}{c^{5}}} = 5.4 \cdot 10^{-44} s$$

$$l_{Planck} = ct_{Planck} = \sqrt{\frac{G\hbar}{c^{3}}} = 10^{-33} cm = 10^{-20} fm$$



Introduction

Big Bang and Hot Universe

$$\frac{\text{The Planck Era:}}{X \ge X_{\text{Planck}}} \qquad T_{Planck} = \frac{m_{Planck}c^2}{k} = 1.41679 \cdot 10^{32} \text{ K} \approx 1.5 \cdot 10^{19} \text{ GeV}$$

$$\frac{X \ge X_{\text{Planck}}}{\text{The Planck}} = \frac{m_{Planck}}{l_{Planck}^3} = \frac{c^5}{G^2 \hbar} \sim 10^{94} \text{ g/cm}^3$$

$$1 \text{ fm} = 10^{-13} \text{ cm} \quad n_{Planck} = l_{Planck}^{-3} \sim 10^{60} \text{ fm}^{-3},$$

$$n_{proton} \sim \left[\frac{4\pi (0.876 \text{ fm})^3}{3}\right]^{-1} = 0.354 \text{ fm}^{-3}, \quad n_{nucl} = 0.16 \text{ fm}^{-3}$$

Planck Parameters are criteria for beginning of The Modern Era: $\rho < \rho_{\text{Planck}}$, $T < T_{\text{Planck}}$

