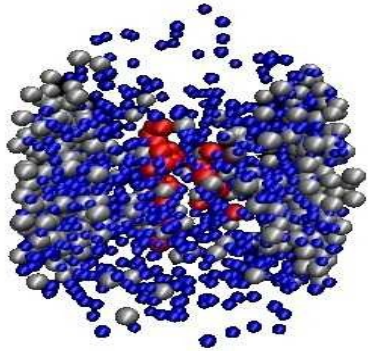


Institut für
Theoretische Physik

HIC
for FAIR
Helmholtz International Center



Directed flow in heavy-ion collisions from PHSD transport approach



Alessia Palmese

Wolfgang Cassing



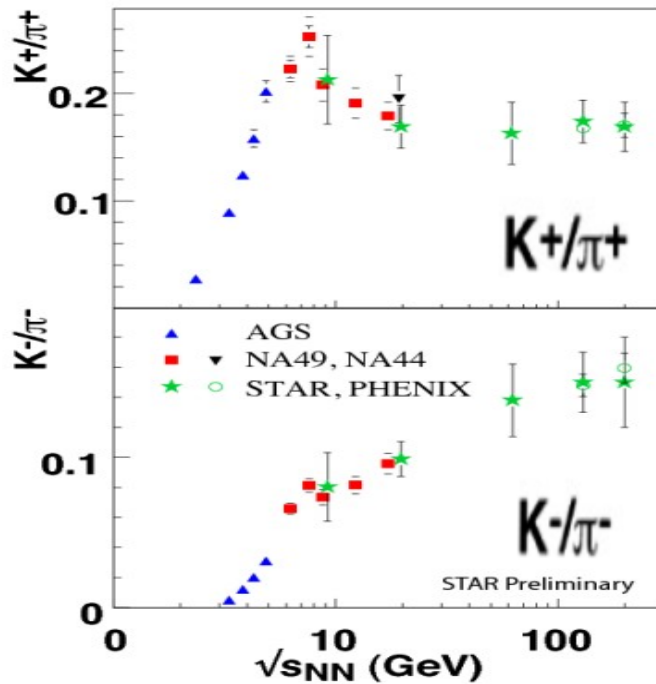
Dubna, 10.07.2015

Strangeness in Quark Matter 2015

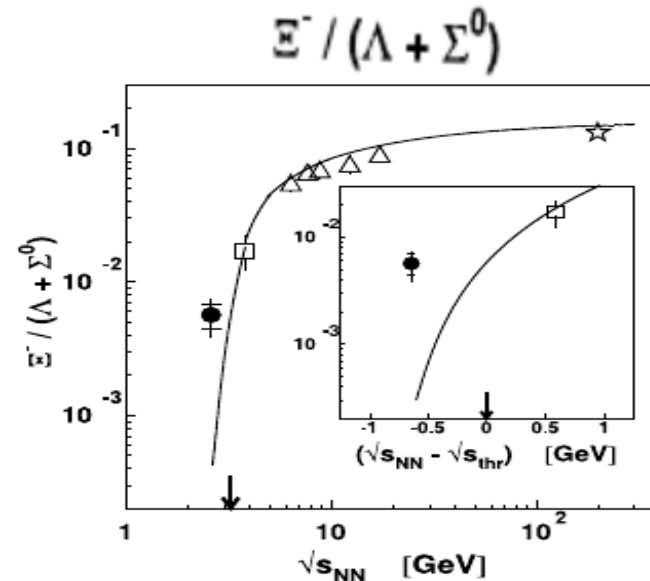


Motivation

Strangeness observables are still not well understood!



M.M. Aggarwal et al. [STAR Collaboration],
arXiv:1007.2613 (2010).



G.Agakishiev et al. [HADES Collaboration],
Phys. Rev. Lett. 103, 132301 (2009).

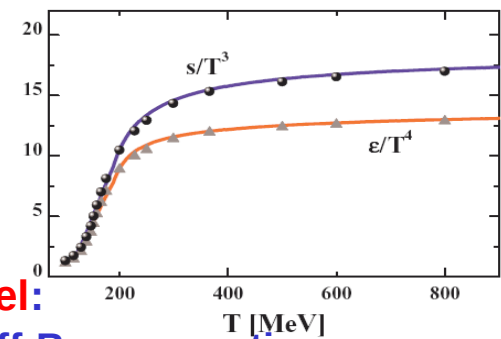
Low energy scan (NICA, FAIR, RHIC) is going to provide us new information!

Which is the role played by the Kaon potential?

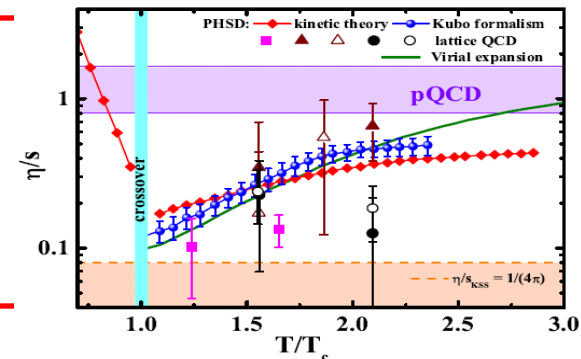


Parton Hadron String Dynamics

- Microscopic description of the heavy-ion collision with full time evolution: transition from hadrons to partons; lattice QCD EoS; dynamical hadronization and hadronic rescattering.
- Non-equilibrium relativistic off-shell transport model: based on the 1st order gradient expansion of Kadanoff-Baym equations



Applicable to describe strongly-interacting liquids as well as gases!



- Off-shell hadronic collision dynamics and mean fields

High energy inelastic hadron-hadron collisions are described by the FRITIOF string model (including PYTHIA) whereas low energy hadron-hadron collisions are modelled based on experimental cross sections.

- QGP phase by the Dynamical Quasi-Particle Model which matches lattice QCD.

Strongly interacting quasi-particles massive quarks and gluons (g, q, q_{bar}) with sizeable collisional widths in self-generated mean-field potential.

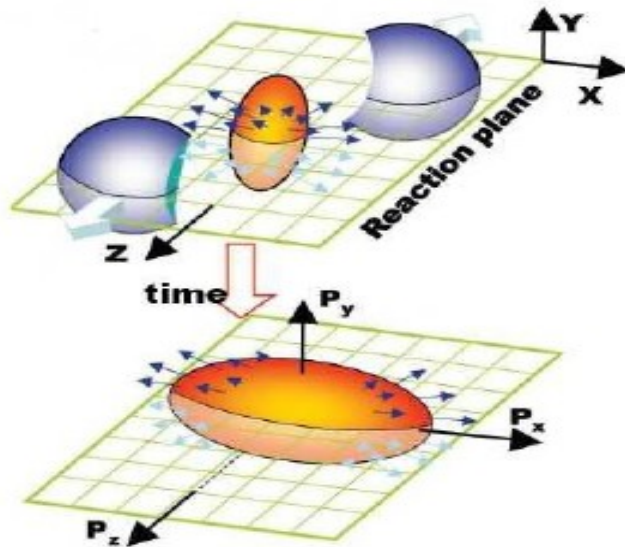
Talks by Elena Bratkovskaya and Pierre Moreau

Directed Flow: $\langle p_x \rangle$ and v_1

First type of collective motion to be identified among fragments of HIC.
It represents the deflection of the produced particles in the reaction plane.

$$\frac{dN}{d\varphi} \propto \left(1 + 2 \sum_{n=1}^{+\infty} v_n \cos[n(\varphi - \psi_n)] \right)$$
$$v_n = \langle \cos n(\varphi - \psi_n) \rangle, \quad n = 1, 2, 3, \dots$$

$$v_1 = \left\langle \frac{p_x}{p_T} \right\rangle$$



Non central collisions!

Interaction between constituents



Pressure gradient



Spatial asymmetry



Asymmetry in momentum space



Collective transverse motion

Time Evolution of the Directed Flow



Protons:

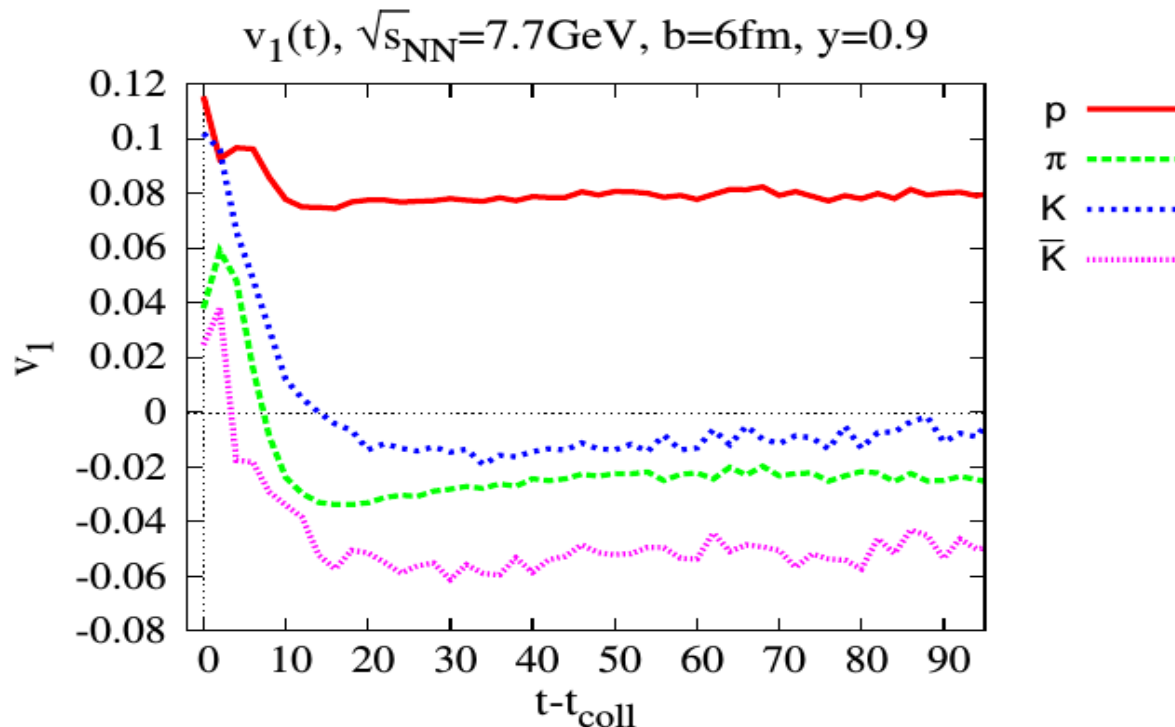
Normal flow

is established in the **early stage** of the collision and marginally distorted during the evolution.

Mesons:

Antiflow

is sensitive to **rescattering** of hadrons.



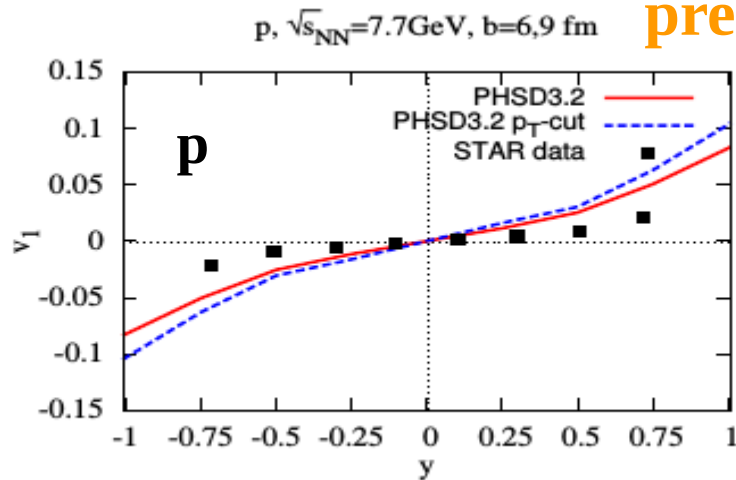
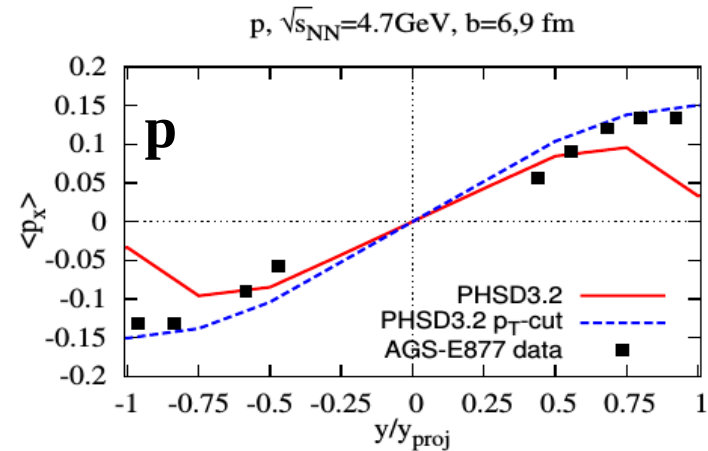
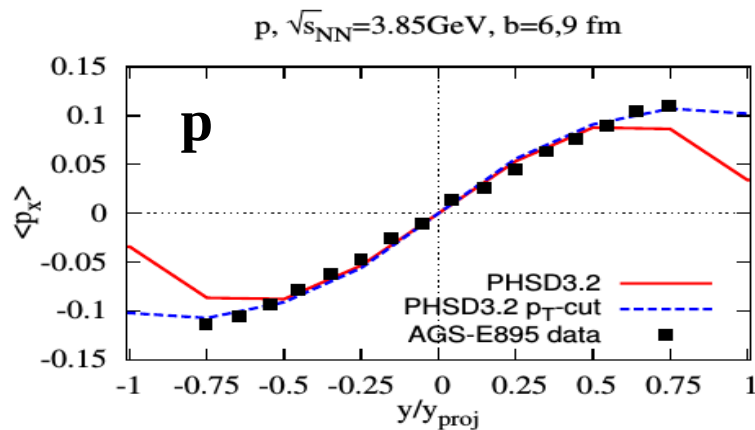
N.B.: PHSD as transport approach includes intrinsically a screening of long range interactions. **4**

Proton flow in Au+Au collisions

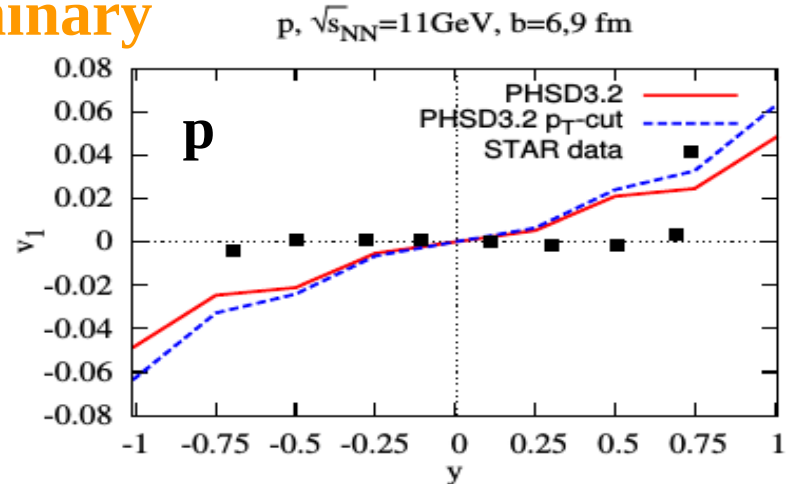


The proton flow has an S-shape, but is approximately linear at midrapidity.

The P_T cut deflects the tails of the flow.



preliminary



AGS data: $P_y > 0.3\text{GeV}$

STAR data: $0.4\text{GeV} < P_T < 2\text{GeV}$

Data E895: H. Liu et al. (E895 Collab.), Phys. Rev. Lett. 84, 5488 (2000).

Data E877: J. Barrette et al. (E877 Collab.), Phys. Rev. C 55, 1420 (1997); 56, 3254 (1997).

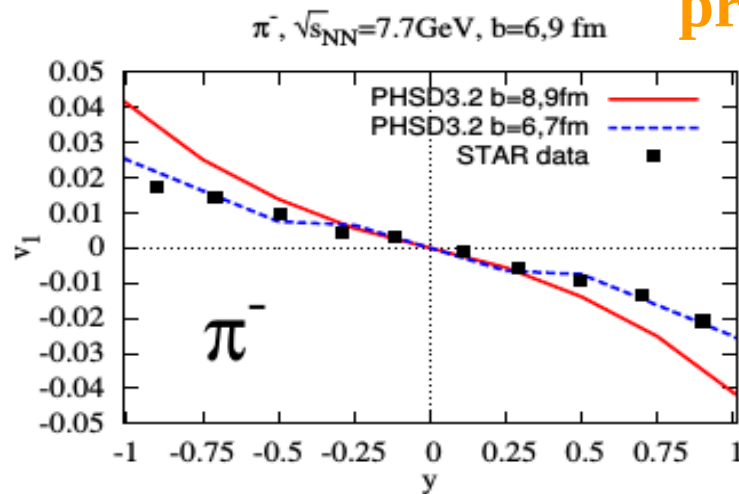
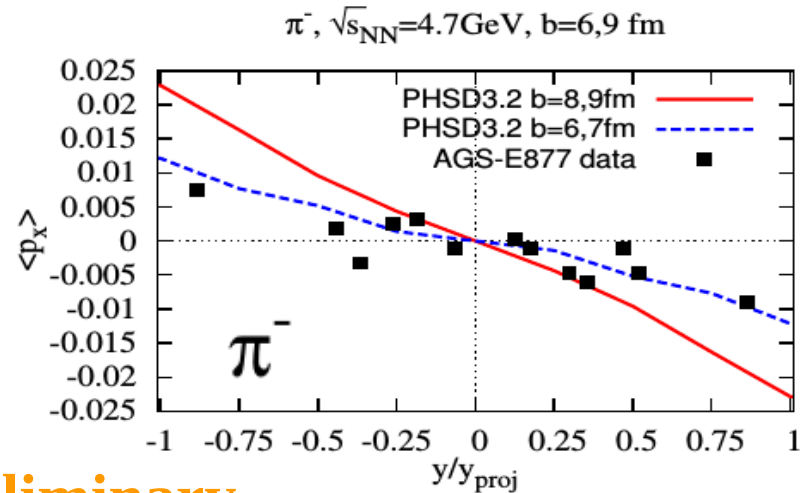
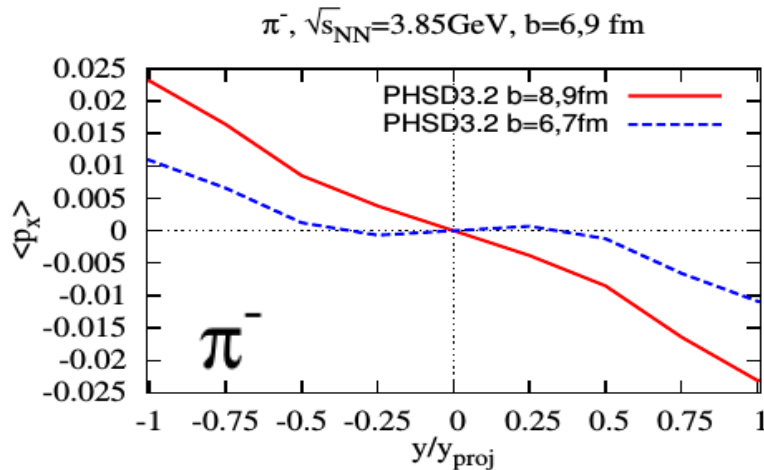
Data STAR: L. Adamczyk et al. (STAR Collab.), Phys. Rev. Lett. 112, 162301 (2014).

Pion antiflow in Au+Au collisions

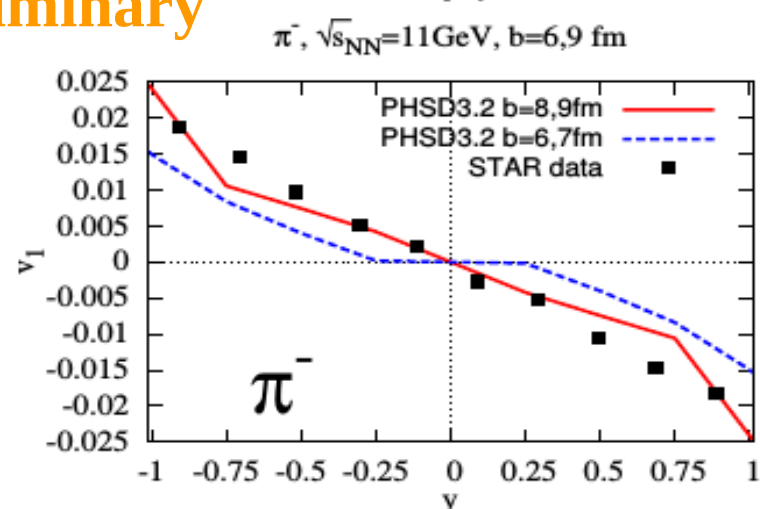


The **antiflow of pions** presents a **flattening** at midrapidity.

This flattening disappears with increasing **impact parameter**.



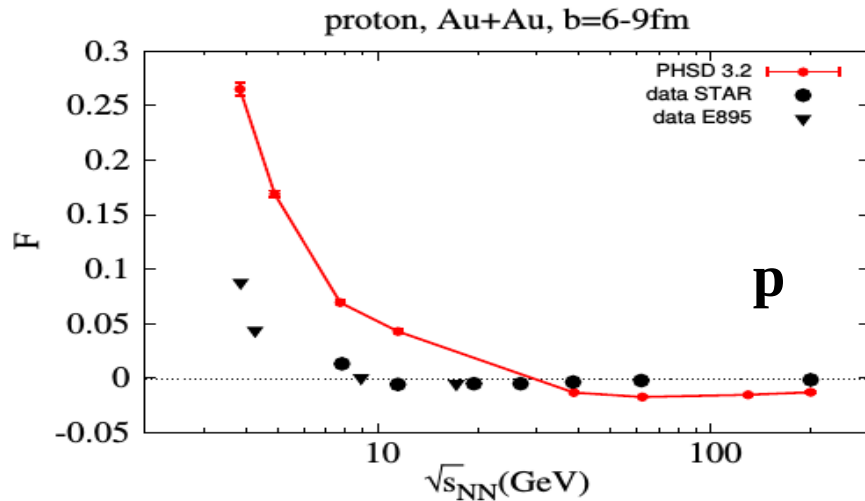
preliminary



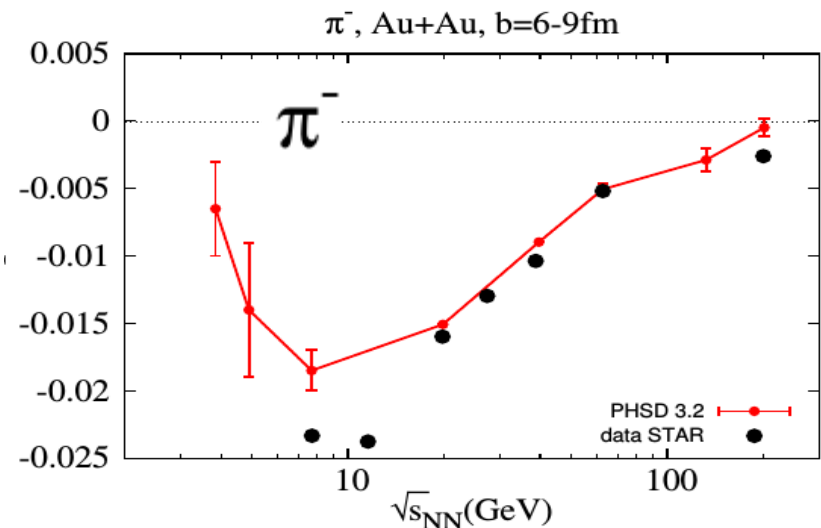
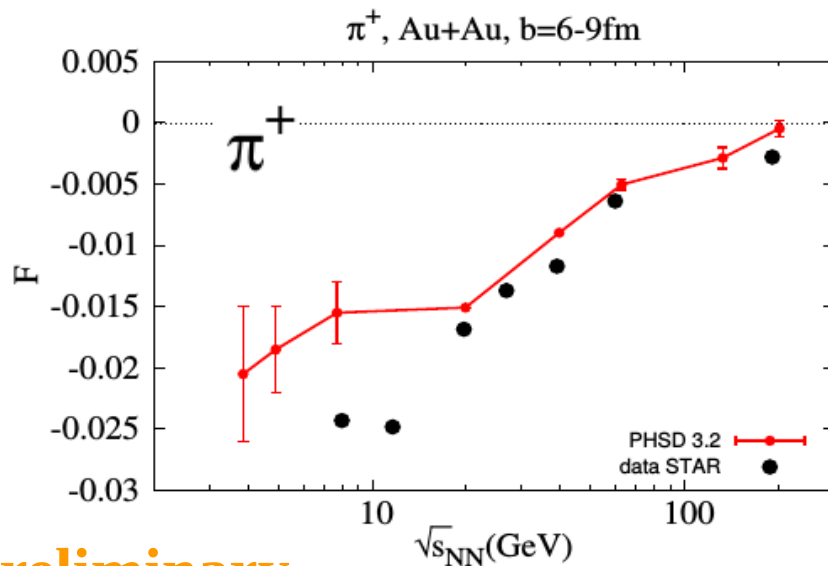
STAR data: $P_T > 0.2\text{GeV}$, $P < 1.6\text{GeV}$
midcentral centrality class: 10-40%

Data E877: J. Barrette et al. (E877 Collab.), Phys. Rev. C 55, 1420 (1997); 56, 3254 (1997).
Data STAR: L. Adamczyk et al. (STAR Collab.), Phys. Rev. Lett. 112, 162301 (2014).

Directed Flow: Slope F



Fitting procedure:
 $v_1(Y)=F Y$ at midrapidity
and $v_1(Y)=F Y + C Y^3$ for $|Y|<1$.



preliminary

Kaon Potentials



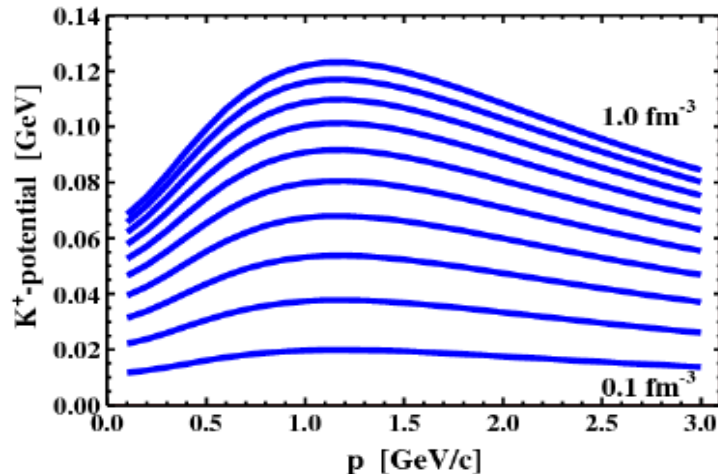
G-Matrix theory

L.Tolos, A.Ramos, A.Polls, PRC65 (2002) 054907;
 W.Cassing, L.Tolos, E.L.Bratkovskaya, A.Ramos, NPA727 (2003) 59;
 W.Cassing, V. Konchakovski, A. P., V.D. Toneev, E.L. Bratkovskaya [1408.4313]

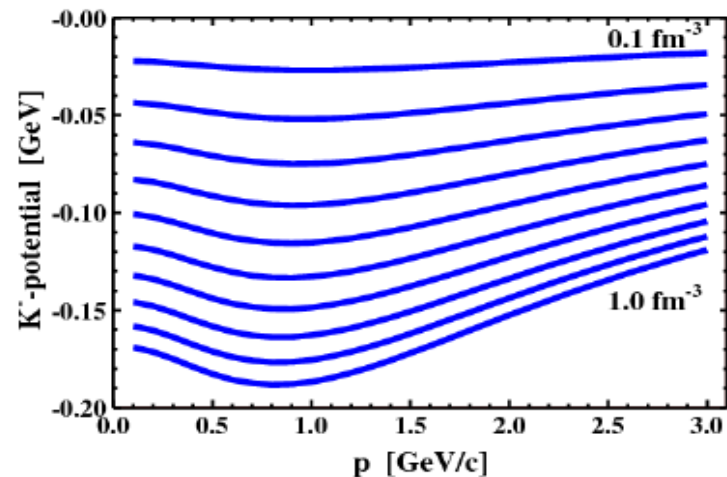
Dispersion relation
$$\omega_K^2(\vec{p}, \rho) = \pm \frac{3}{4} \frac{\omega}{f_K^2} \rho_N + p^2 + m_K^2 - \frac{\Sigma_{KN}}{f_K^2} \rho_s$$

Kaon potential
$$U_K(\vec{p}, \rho) = \omega_K(\vec{p}, \rho) - \sqrt{p^2 + m_K^2}$$

K Repulsive

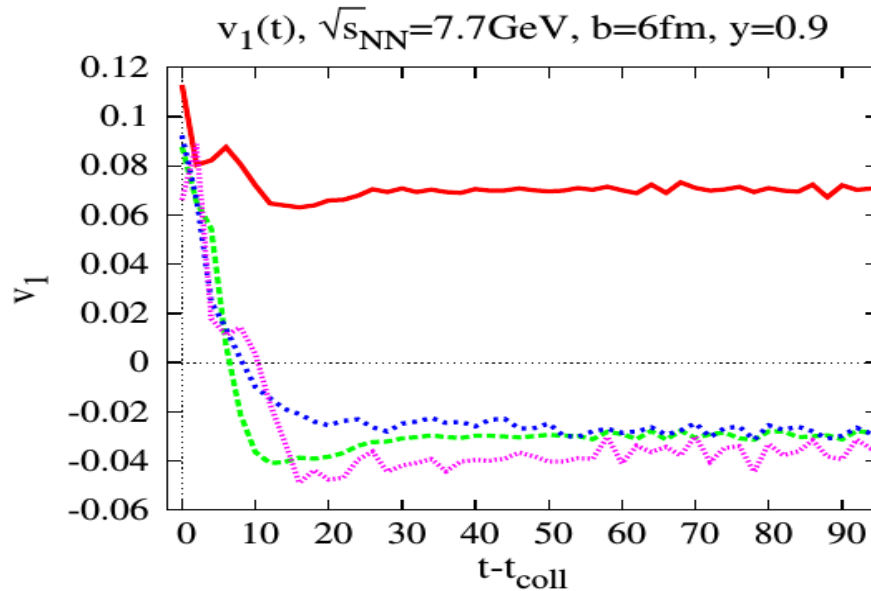


\bar{K} attractive



Potentials are density- and momentum-dependent.
 PHSD explores these potentials in collisions up to $3\rho_0$.

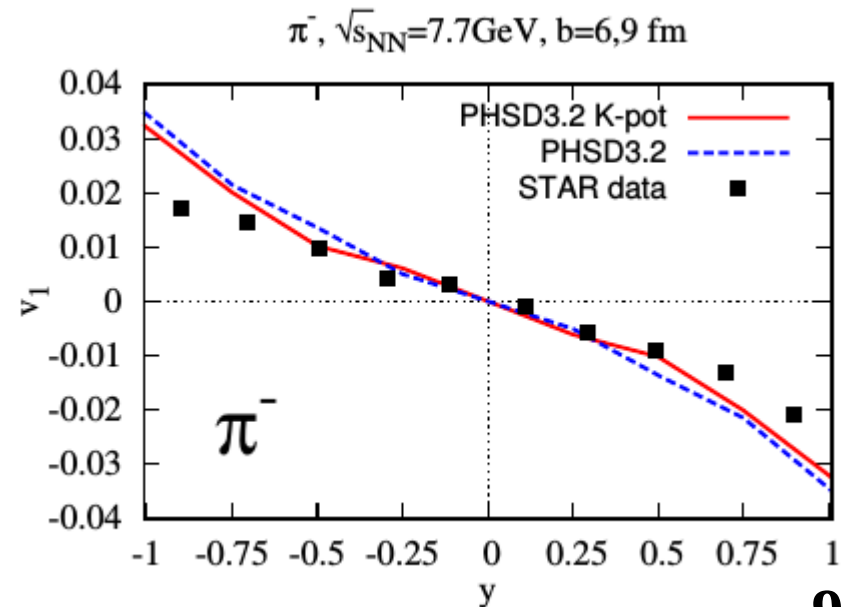
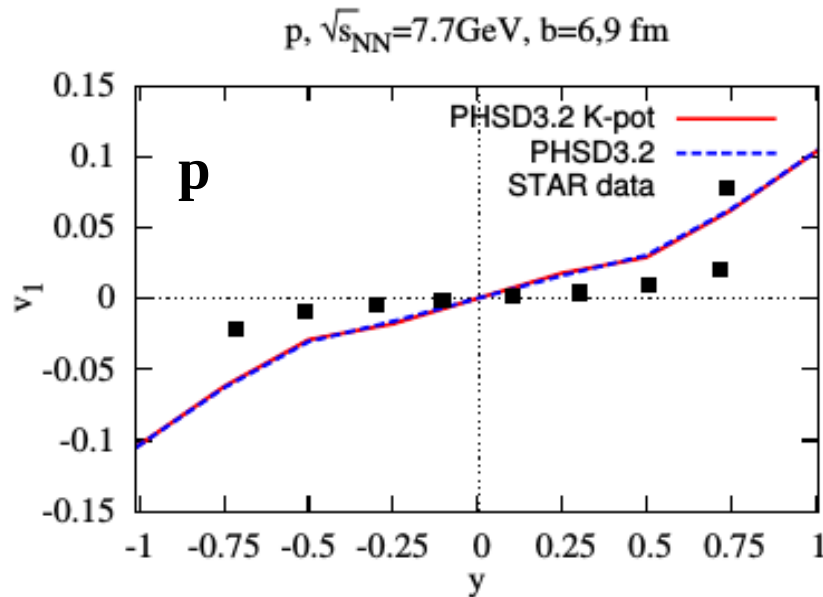
Directed flow with Kaon Potential



p ———
 π - - - -
 K ·····
 \bar{K} ·····

The time evolution of the flow does not change with the inclusion of the potentials.

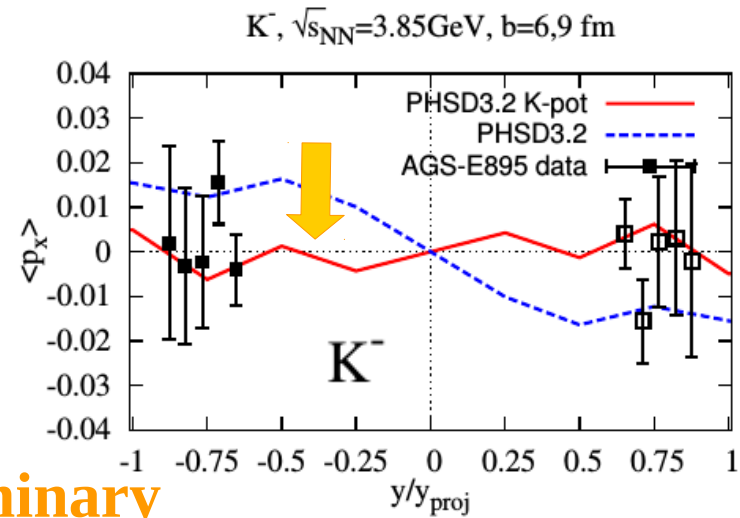
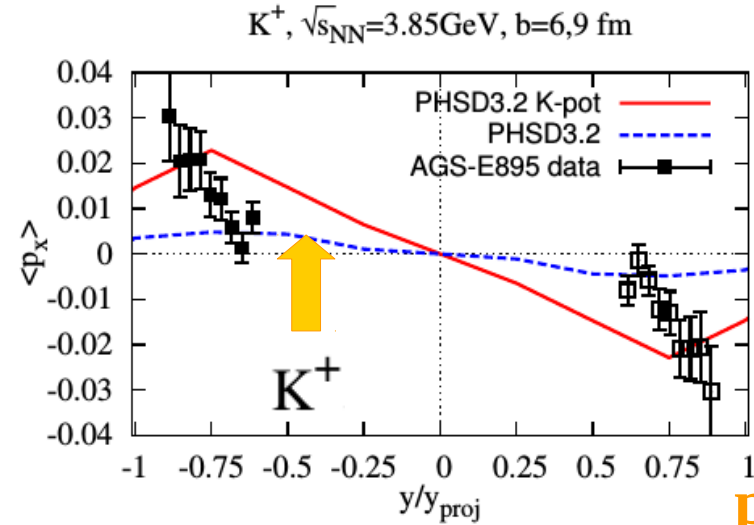
The **non-strange particles flow** is not deflected introducing the Kaon potential.



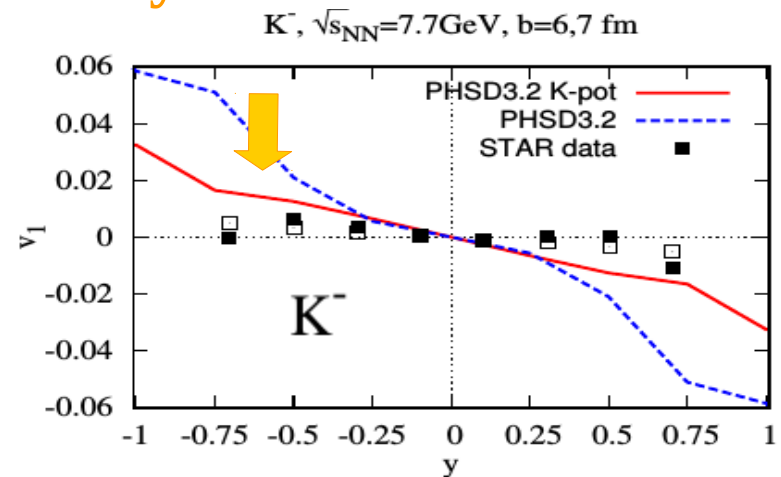
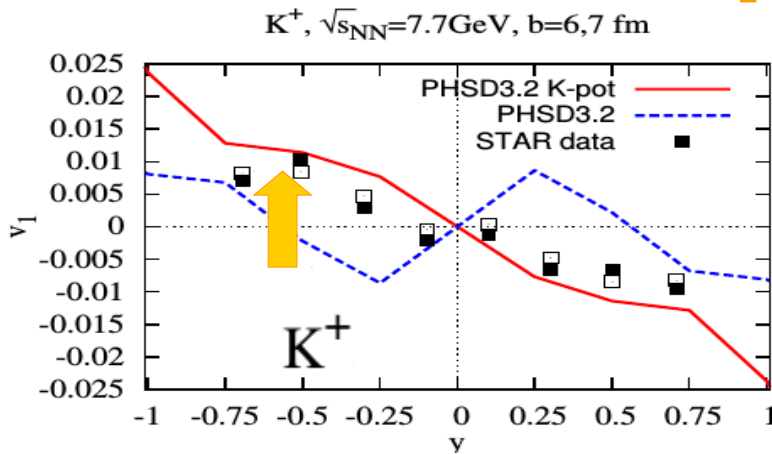
Kaon antiflow in Au+Au collisions



The **antiflow of Kaons** is sensitive to the potential!



preliminary



AGS data: $P_T < 0.3\text{GeV}$

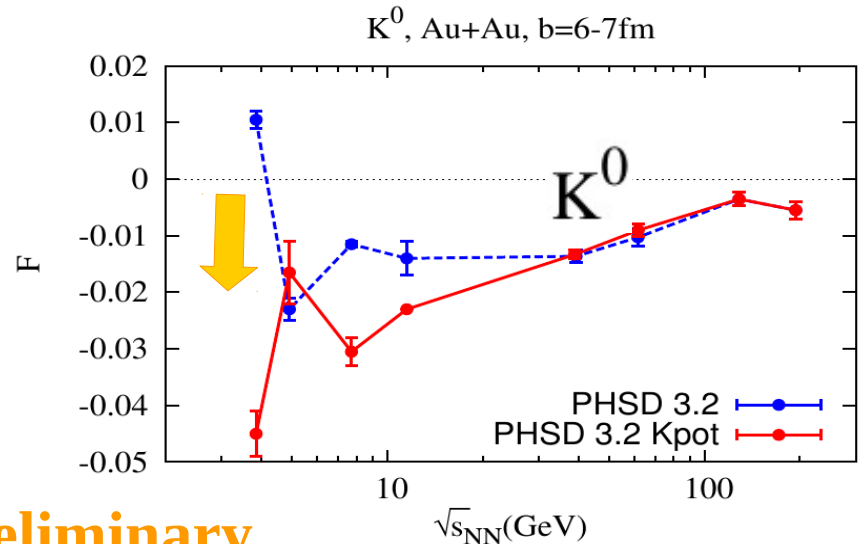
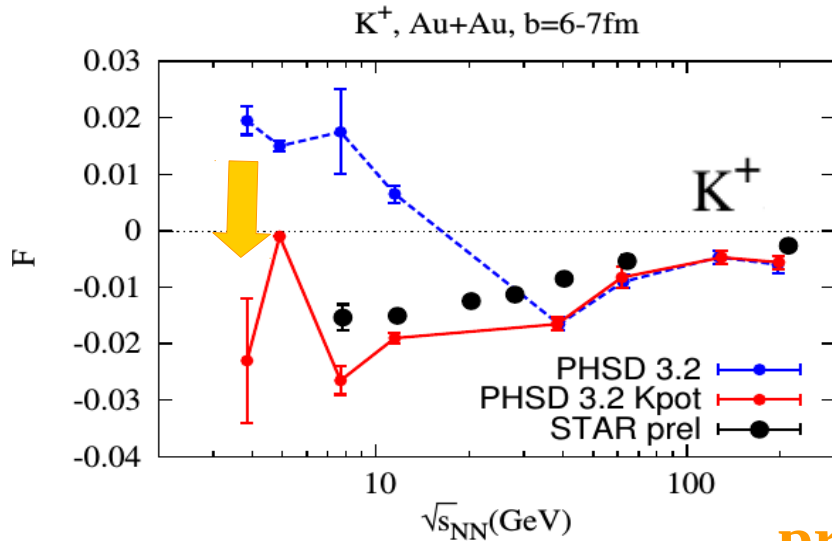
STAR data: $P_T > 0.2\text{GeV}$, $P < 1.6\text{GeV}$

Data E895: C. Pinkenburg et al. (E895 Collab.), arXiv: nucl-ex/0104025(2001).
Data STAR: Y. Pandit et al. (STAR Collab.), arXiv:1505.03933 (2015).

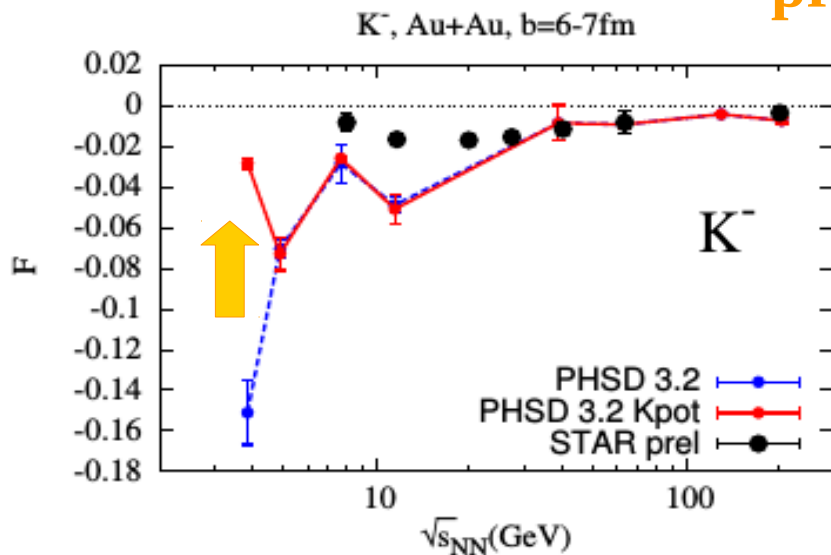
Kaon Directed Flow slope F



Fitting procedure: $v_1(Y)=F Y$ at midrapidity and $v_1(Y)=F Y + C Y^3$ for $|Y|<1$.



preliminary



Kaon potential \rightarrow **Change of the sign of the flow**

AntiKaon potential \rightarrow **Flatter Antiflow**

With increasing energy the flow vanishes and there is no more relevant role of the potentials.

Summary

- Directed Flow is established at the **early stage** of the collisions but the mesons flows are sensitive to **rescattering** of hadrons.
- Directed Flow is sensitive to **P_T cuts** and value of the **impact parameter**.
- **Directed Flow is a probe to study the Kaon Potentials in the medium!**

We look forward for low energy-scan!



Thanks for your attention!



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Mark I. Gorenstein
Vadym Voronyuk
Laura Tolos
Angel Ramos



FIAS Frankfurt Institute
for Advanced Studies



Back up slides

Directed Flow: $\langle p_x \rangle$ and v_1

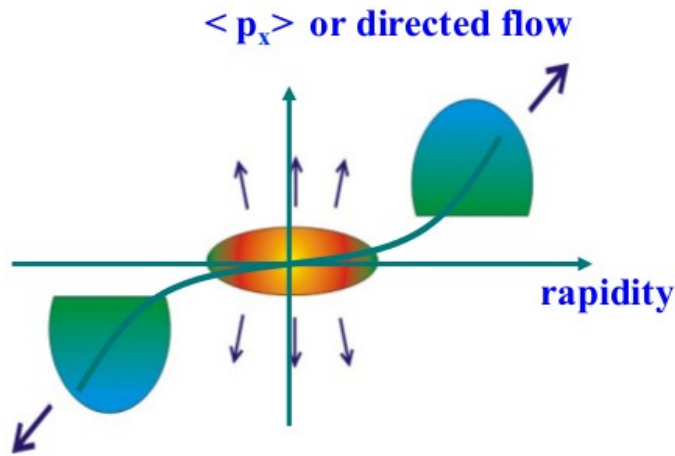
Spatial asymmetry and asymmetry in momentum space

- v_1 : directed flow
- v_2 : elliptic flow
- v_3 : triangular flow.....

$$\frac{dN}{d\varphi} \propto \left(1 + 2 \sum_{n=1}^{+\infty} v_n \cos[n(\varphi - \psi_n)] \right)$$

$$v_n = \langle \cos n(\varphi - \psi_n) \rangle, \quad n = 1, 2, 3, \dots$$

$$v_1 = \left\langle \frac{p_x}{p_T} \right\rangle, \quad v_2 = \left\langle \frac{p_x^2 - p_y^2}{p_x^2 + p_y^2} \right\rangle$$

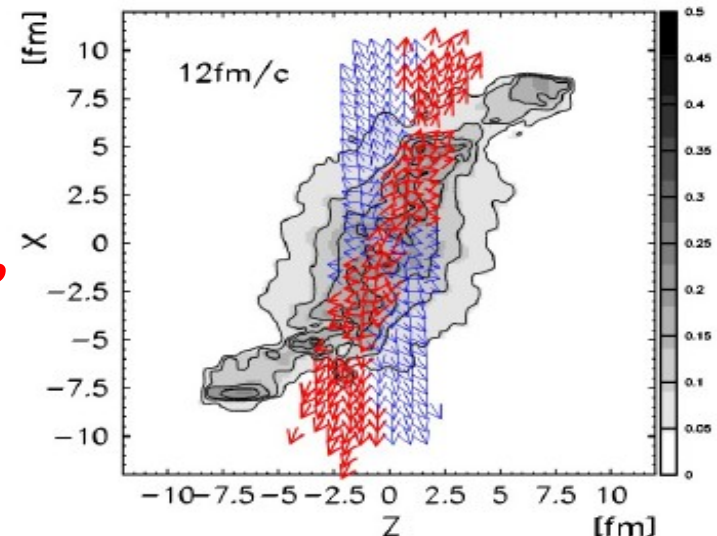


Collective transverse motion:

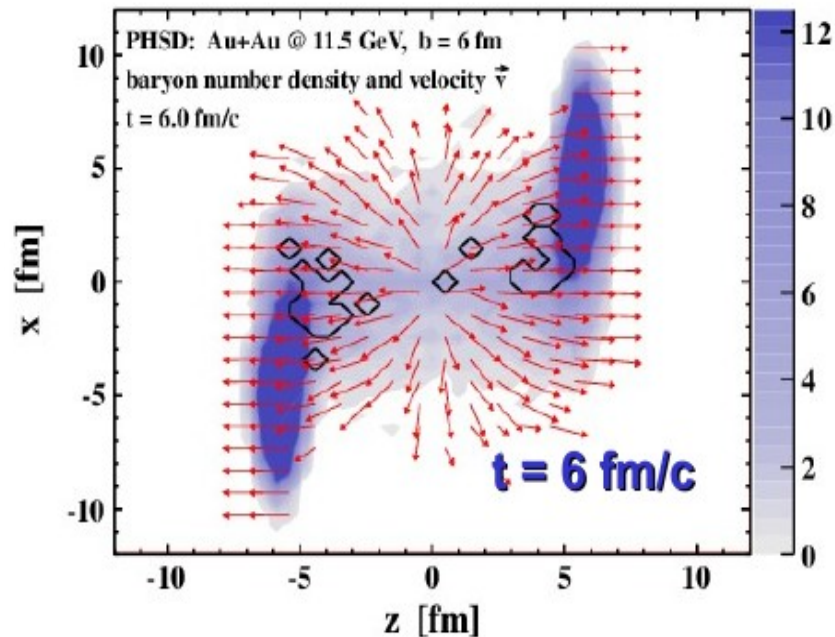
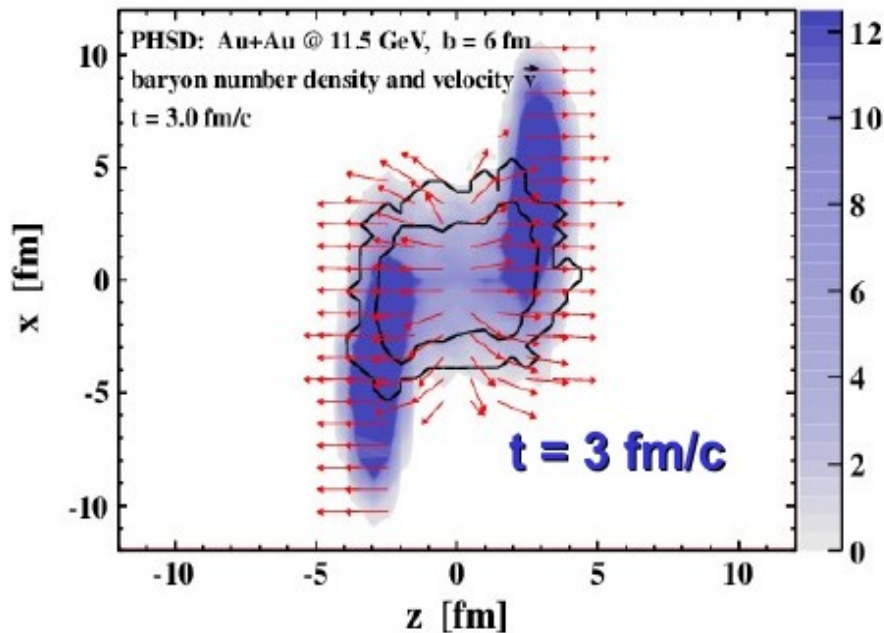
$\langle p_x \rangle$ and v_1

$\frac{d\langle p_x \rangle}{dY}, \frac{dV_1}{dY} > 0$ “normal flow”

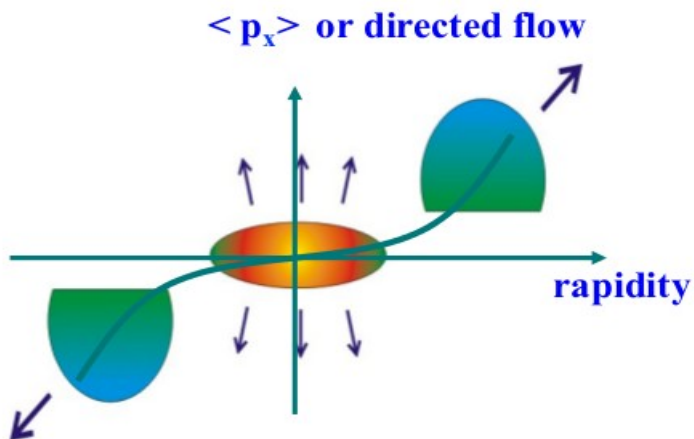
$\frac{d\langle p_x \rangle}{dY}, \frac{dV_1}{dY} < 0$ “antiflow”



Snapshot of the reaction plane



V. Konchakovski, W. Cassing, Yu. Ivanov, V. Toneev, PRC90 (2014) 014903.



$d\langle p_x \rangle/dY, dV_1/dY > 0$ “normal flow”

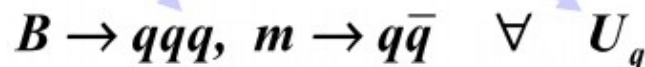
$d\langle p_x \rangle/dY, dV_1/dY < 0$ “antiflow”

I. From hadrons to QGP:

- **Initial A+A collisions** – as in HSD:
 - **string** formation in primary NN collisions
 - string decay to **pre-hadrons** (B - baryons, m - mesons)
- **Formation of QGP stage** by dissolution of pre-hadrons (all new produced secondary hadrons) into **massive colored quarks + mean-field energy**



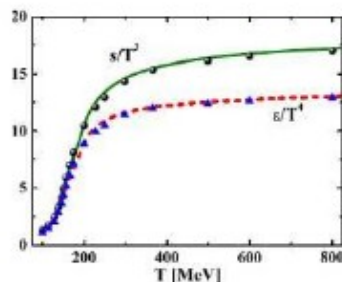
QGP phase:
 $\epsilon > \epsilon_{\text{critical}}$



based on the **Dynamical Quasi-Particle Model (DQPM)** which defines **quark spectral functions**, i.e. masses $M_q(\epsilon)$ and widths $\Gamma_q(\epsilon)$

+ **mean-field potential** U_q at given ϵ – local energy density

(ϵ related by IQCD EoS to T - temperature in the local cell)



W. Cassing, E. Bratkovskaya, PRC 78 (2008) 034919;
 NPA831 (2009) 215; EPJ ST 168 (2009) 3; NPA856 (2011) 162.

II. Partonic phase - QGP:

quarks and gluons (= ,dynamical quasiparticles‘)

with off-shell spectral functions (width, mass) defined by the DQPM

- in **self-generated mean-field potential** for quarks and gluons U_q, U_g from the DQPM
- **EoS of partonic phase: ,crossover‘ from lattice QCD** (fitted by DQPM)
- **(quasi-) elastic and inelastic** parton-parton interactions: using the effective cross sections from the DQPM

- **(quasi-) elastic collisions:**

$$q + q \rightarrow q + q \quad g + q \rightarrow g + q$$

$$q + \bar{q} \rightarrow q + \bar{q} \quad g + \bar{q} \rightarrow g + \bar{q}$$

$$\bar{q} + \bar{q} \rightarrow \bar{q} + \bar{q} \quad g + g \rightarrow g + g$$

- **inelastic collisions:**

(Breit-Wigner cross sections)

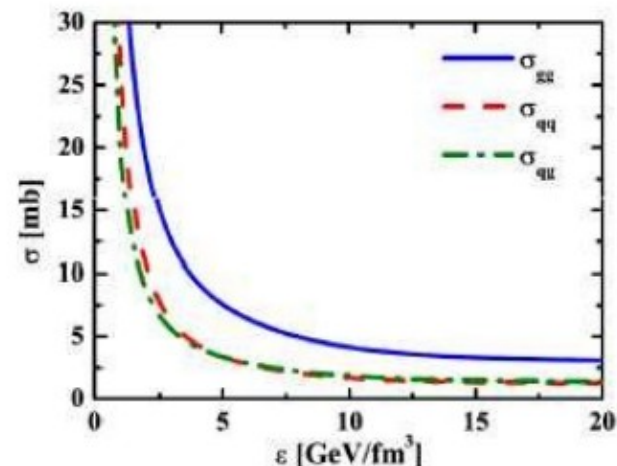
$$q + \bar{q} \rightarrow g$$

$$g \rightarrow q + \bar{q}$$

~~$$q + \bar{q} \rightarrow g + g$$~~

~~$$g \rightarrow g + g$$~~

} suppressed (<1%)
due to the large
mass of gluons





III. Hadronization:

□ **Hadronization:** based on DQPM

- **massive, off-shell (anti-)quarks** with broad spectral functions hadronize to **off-shell mesons and baryons or color neutral excited states - ,strings‘** (strings act as ,doorway states‘ for hadrons)

$$g \rightarrow q + \bar{q}, \quad q + \bar{q} \leftrightarrow \text{meson ('string')} \\ q + q + q \leftrightarrow \text{baryon ('string')}$$

- Local covariant off-shell **transition rate** for $q+q\bar{q}$ fusion

→ **meson formation:**

$$\frac{dN^{q+\bar{q} \rightarrow m}}{d^4x d^4p} = \text{Tr}_q \text{Tr}_{\bar{q}} \delta^4(p - p_q - p_{\bar{q}}) \delta^4\left(\frac{x_q + x_{\bar{q}}}{2} - x\right) \delta(\text{flavor, color}) \\ \cdot N_q(x_q, p_q) N_{\bar{q}}(x_{\bar{q}}, p_{\bar{q}}) \cdot \omega_q \rho_q(p_q) \cdot \omega_{\bar{q}} \rho_{\bar{q}}(p_{\bar{q}}) \cdot |M_{q\bar{q}}|^2 W_m(x_q - x_{\bar{q}}, p_q - p_{\bar{q}})$$

- $N_j(x, p)$ is the phase-space density of parton j at space-time position x and 4-momentum p
- W_m is the phase-space distribution of the formed ,pre-hadrons‘ (Gaussian in phase space)
- $|M_{qq}|^2$ is the effective quark-antiquark interaction from the DQPM

IV. Hadronic phase: hadron-string interactions – off-shell HSD

Boltzmann equation -> off-shell transport

$$\left(\frac{\partial}{\partial t} + \vec{v}_1 \cdot \nabla_{\vec{r}} + \frac{\vec{K}}{m} \cdot \nabla_{\vec{v}_1} \right) f_1 = \int d\Omega \int d\vec{v}_2 \sigma(\Omega) |\vec{v}_1 - \vec{v}_2| \left(f'_1 f'_2 - f_1 f_2 \right)$$



GENERALIZATION

(First order gradient expansion of the Wigner-transformed Kadanoff-Baym equations)

drift term

Vlasov term

backflow term

collision term = „loss“ term - „gain“ term

$$\underbrace{\diamond \{ P^2 - M_0^2 - Re\Sigma_{XP}^{ret} \}}_{\text{drift term}} \underbrace{\{ S_{XP}^< \}}_{\text{Vlasov term}} - \underbrace{\diamond \{ \Sigma_{XP}^< \}}_{\text{backflow term}} \underbrace{\{ ReS_{XP}^{ret} \}}_{\text{collision term}} = \frac{i}{2} \left[\underbrace{\Sigma_{XP}^>}_{\text{„loss“ term}} \underbrace{S_{XP}^<}_{\text{„gain“ term}} - \Sigma_{XP}^< S_{XP}^> \right]$$

Backflow term incorporates the **off-shell** behavior in the particle propagation

! vanishes in the quasiparticle limit $A_{XP} = 2\pi \delta(p^2 - M^2)$
Propagation of the Green's function $iS_{XP}^< = A_{XP} f_{XP}$, which carries information not only on the number of particles, but also on their properties, interactions and correlations

$$A_{XP} = \frac{\Gamma_{XP}}{(P^2 - M_0^2 - Re\Sigma_{XP}^{ret})^2 + \Gamma_{XP}^2/4}$$

$$\diamond \{ F_1 \} \{ F_2 \} := \frac{1}{2} \left(\frac{\partial F_1}{\partial X_\mu} \frac{\partial F_2}{\partial P^\mu} - \frac{\partial F_1}{\partial P_\mu} \frac{\partial F_2}{\partial X^\mu} \right)$$

Γ_{XP} - **width of spectral function** = **reaction rate** of a particle (at phase-space position XP)