



## Baryon Stopping in Heavy-Ion Collisions from AGS to SPS Energies

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Int. Workshop "Critical point and onset of deconfinement"  
Dubna, JINR, August 23 - 28, 2010



# 3-Fluid Dynamics

Baryon Stopping

JINR,  
24.08.10

Model

Rapidity  
Density

Fit

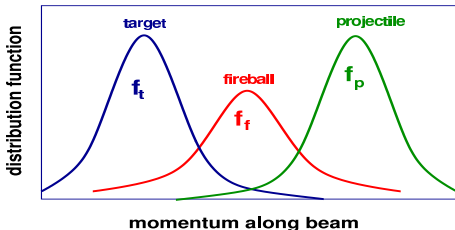
Reduced  
curvature

Trajectories

Crossover

Summary

Produced particles  
populate mid-rapidity  
⇒ **fireball** fluid



**Target-like fluid:**

$$\partial_\mu J_t^\mu = 0$$

Leading particles carry bar. charge

$$\partial_\mu T_t^{\mu\nu} = -F_{tp}^\nu + F_{ft}^\nu$$

exchange/emission

**Projectile-like fluid:**

$$\partial_\mu J_p^\mu = 0,$$

$$\partial_\mu T_p^{\mu\nu} = -F_{pt}^\nu + F_{fp}^\nu$$

**Fireball fluid:**

$$J_f^\mu = 0,$$

Baryon-free fluid

$$\partial_\mu T_f^{\mu\nu} = F_{pt}^\nu + F_{tp}^\nu - F_{fp}^\nu - F_{ft}^\nu$$

Source term      Exchange

The **source term** is delayed due to a formation time  $\tau \sim 1 \text{ fm}/c$

**Total energy-momentum conservation:**

$$\partial_\mu (T_p^{\mu\nu} + T_t^{\mu\nu} + T_f^{\mu\nu}) = 0$$



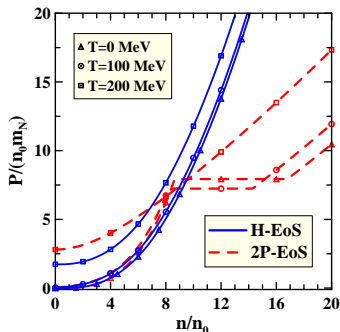
- Equation of State (EoS)

## Hadronic EoS (H-EoS)

[Galitsky and Mishustin, Sov. J. Nucl. Phys. **29**, 181 (1979)]

## 1st-order transition to QGP (2P-EoS)

[Khvorostukhin, Skokov, Redlich, Toneev, EPJ **C48**, 531 (2006)]



**Phase transition  $\implies$  EoS softening** (in dense baryon matter)

- Freeze-out energy-density:  $\varepsilon_{frz} = 0.4 \text{ GeV/fm}^3$
- Friction: *estimated and tuned*
- Formation Time:  $\tau = 2 \text{ fm/c}$  for H-EoS and  $\tau = 0.33 \text{ fm/c}$  for 2P-EoS
- Coalescence coefficients for fragments



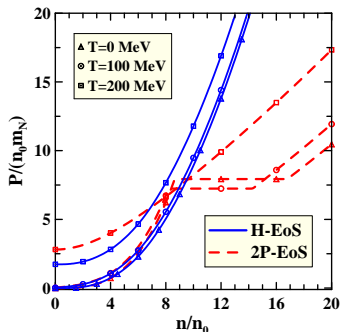
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**Net-baryon rapidity distribution  
is a direct measure of the baryon stopping.**

However, we have to rely on net-proton data.

We consider only central collisions:  
Au+Au at AGS and Pb+Pb at SPS.



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# Representation of Rapidity Distributions

Baryon Stopping

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Rapidity Density

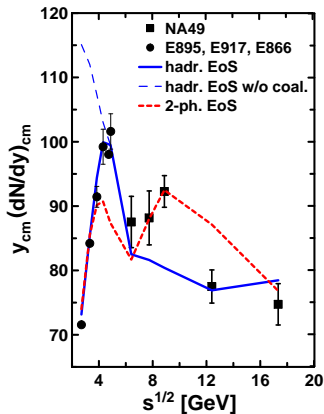
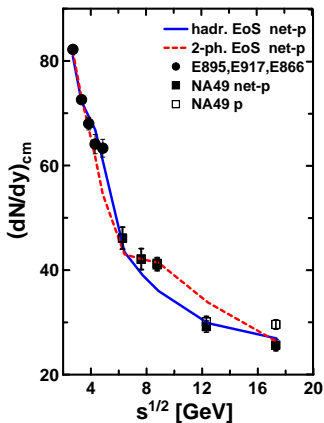
Fit

Reduced curvature

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**Scaled  $y_{cm} dN/dy$  acts as a zoom.**



# 3FD calculations versus exp. data

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Model

Rapidity Density

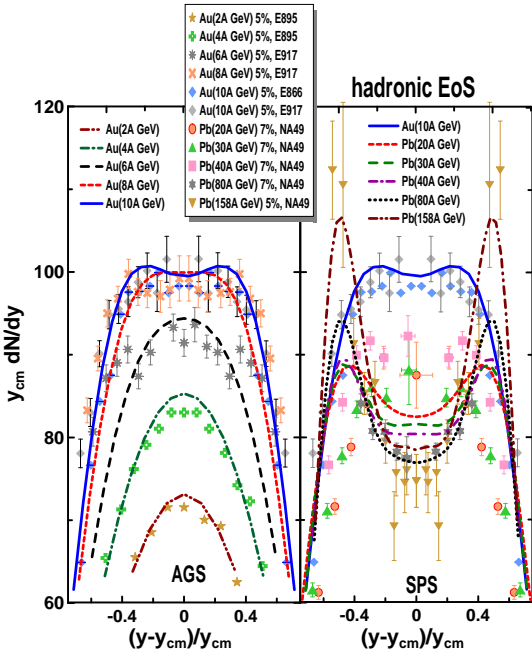
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How to quantify agreement or disagreement with  $y_{cm} dN/dy$ ?

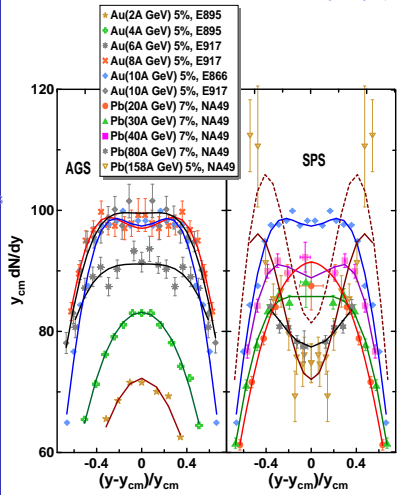




# Two-Thermal-Sources Fit

- Baryon Stopping
- JINR, 24.08.10
- Model
- Rapidity Density
- Fit
- Reduced curvature
- Trajectories
- Crossover
- Summary

$$\frac{dN}{dy} = a (\exp \{ -(1/w_s) \cosh(y - y_{cm} - y_s) \} + \exp \{ -(1/w_s) \cosh(y - y_{cm} + y_s) \})$$



Two thermal sources shifted by  $\pm y_s$  from the midrapidity.

$w_s$  = width of the sources



# Parameters of the fit

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Model

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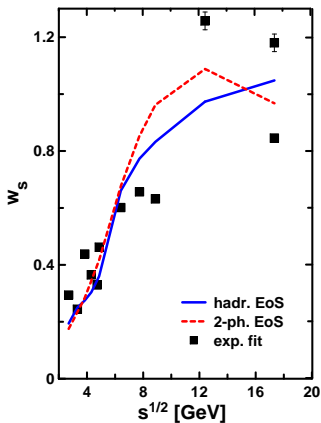
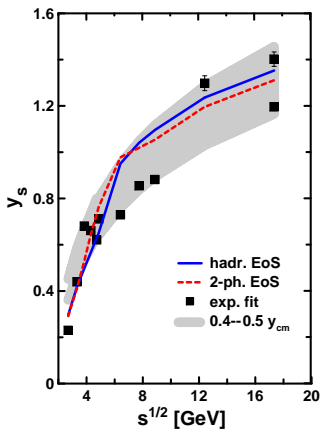
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Not very spectacular. Is there something better?



# Reduced curvature in the midrapidity

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$$\begin{aligned} C_y &\equiv \left( y_{cm}^3 \frac{d^3 N}{dy^3} \right)_{y=y_{cm}} / \left( y_{cm} \frac{dN}{dy} \right)_{y=y_{cm}} \\ &= (y_{cm}/w_s)^2 \left( \sinh^2 y_s - w_s \cosh y_s \right) \end{aligned}$$

with respect to the “dimensionless” rapidity  $(y - y_{cm})/y_{cm}$ .

$C_y$  is independent of the overall normalization

$C_y =$  **shape (concave or convex) at midrapidity**  
and

$(y_{cm} dN/dy)_{y=y_{cm}} =$  **magnitude at midrapidity**

**two independent characteristics of a spectrum**



# “zig-zag” irregularity

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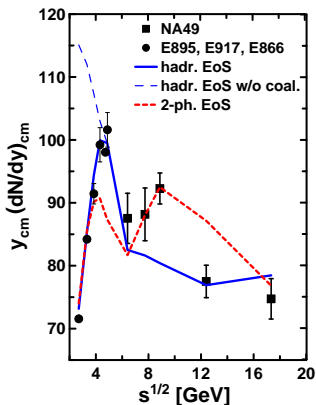
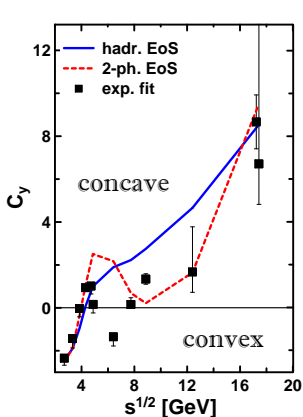
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$C_y$  in 2P-EoS scenario  $\Rightarrow$  zig-zag irregularity  
[qualitatively similar to that in the data]

Hadronic scenario  $\Rightarrow$  monotonous behaviour



# Why “zig-zag”?

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Model

Rapidity  
Density

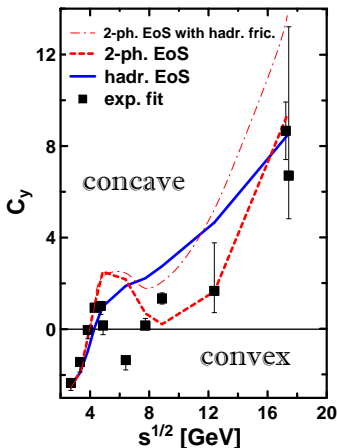
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**Phase transition results in:**

change of content of constituents



**change of stopping power**

the softer EoS



**the higher stopping power**



# Trajectories of matter evolution in the center box

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Model

Rapidity Density

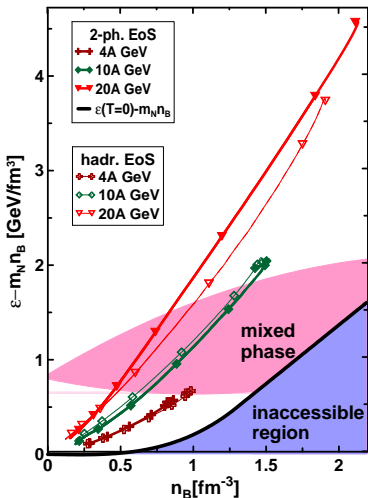
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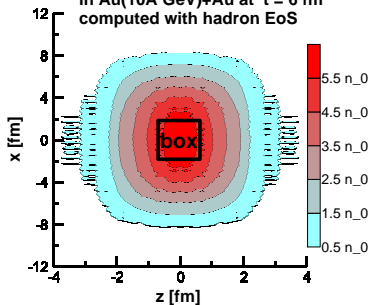
Summary



## Densities in the center box

$$4 \times 4 \times 4 \gamma_{cm}$$

Baryon density (in local rest frame)  
in Au(10A GeV)+Au at  $t = 6$  fm  
computed with hadron EoS



**System gets into phase-transition region  $\Rightarrow$  Zig-zag starts**



# Crossover EoS (preliminary)

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Reduced curvature

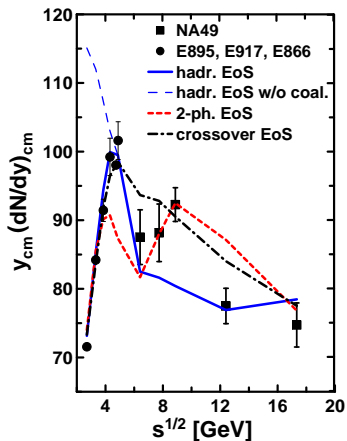
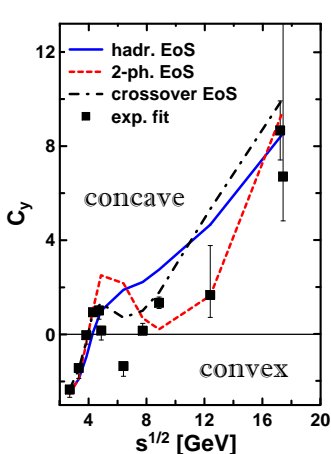
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Summary

## Crossover transition to QGP

[Khvorostukhin, Skokov, Redlich, Toneev, Eur. Phys. J. **C48**, 531 (2006)]



Phase transition is smoother  $\Rightarrow$  wiggle instead of zig-zag



# Summary

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- Baryon stopping is sensitive to phase transition into QGP

- **Data qualitatively favor onset of a phase transition between 10 and 20 GeV/nucl.**

- **Why there is no quantitative agreement?**

neither with the 1st-order transition scenario nor with the crossover one

- **Probable answers:**

**(i) Real EoS at high baryon densities ( $n_B$ ) is very different from those fitted to lattice data near  $n_B = 0$  and then extrapolated to high  $n_B$ .**

**(ii) We have to consider a Van-der-Waals EoS**

[i.e. supercooled QGP, superheated hadronic matter, etc.]

**instead of the Gibbs construction.**