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# *SUSY Physics and (Composite) Higgs at the LHC*

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(Karlsruhe Institute of Technology)

CALC 2012, Dubna, July/August 2012



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# *CALC 2012 - Outline*

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## *I SUSY at the LHC*

- Motivation for beyond the SM (BSM) physics
- Introduction Supersymmetry
- MSSM
- SUSY GUT
- SUSY Breaking
- SUSY Particle Production
- SUSY Searches

## *II SM Higgs Physics and Beyond*

- Introduction Higgs mechanism
- SM Higgs Sector
- Experimental Searches
- MSSM Higgs Sector (Brief)
- Composite Higgs Sector

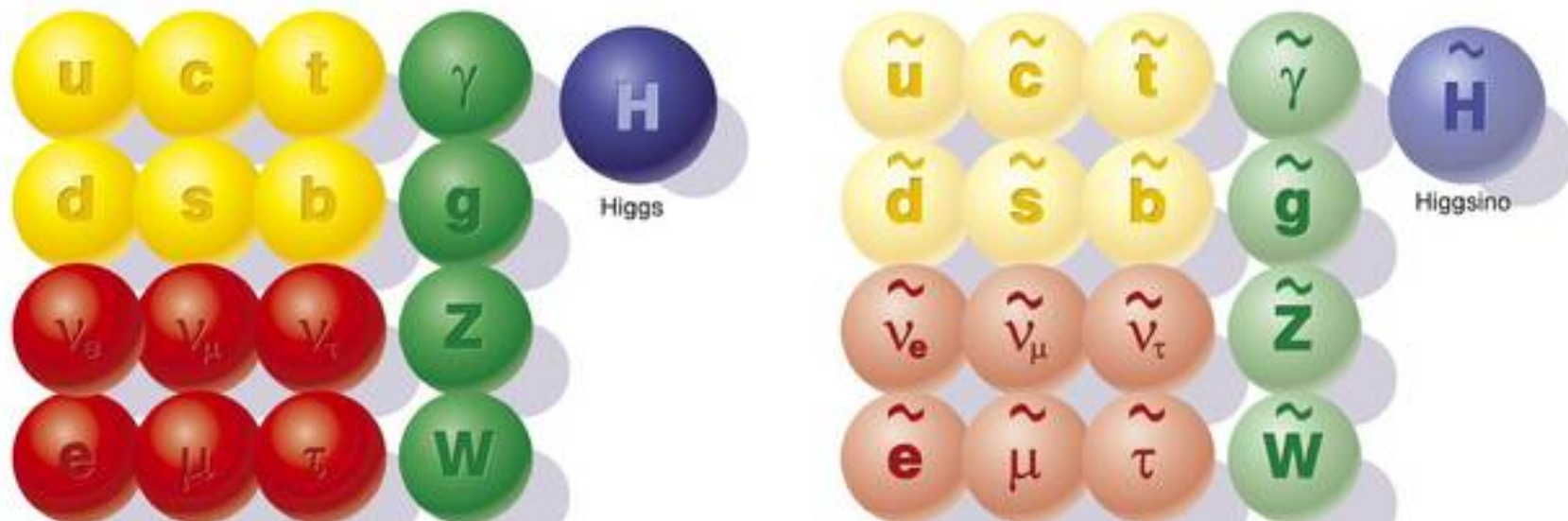
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# SUSY Physics at the LHC

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Margarete Mühlleitner  
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## Literature

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- ☞ H. Kalka und G. Soff, *Supersymmetrie*, Teubner Studienbücher 1997.  
(For notation, SUSY algebra etc.)
- ☞ ATLAS, CMS Webpages

# (I) Motivation

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# Why *Beyond Standard Model (BSM)* Physics?

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## Standard Model: incomplete picture of the universe

- Standard Model (SM) has 19 free parameters:
  - 3 gauge couplings:  $g_1, g_2, g_3$
  - 6 quark and 3 lepton masses
  - Higgs mass  $M_H$ , the vacuum expectation value (VEV)
  - 3 mixing angles and 1 phase in the CKM matrix
  - the  $\theta$  parameter of QCD
- What are the values of these parameters?
  - Why is the top quark so heavy compared to the other fermions?
  - Why is the  $\theta$  parameter so small?
  - Enough CP violation to explain matter-antimatter asymmetry?



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# Why *Beyond Standard Model (BSM) Physics?*

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## Standard Model: incomplete picture of the universe

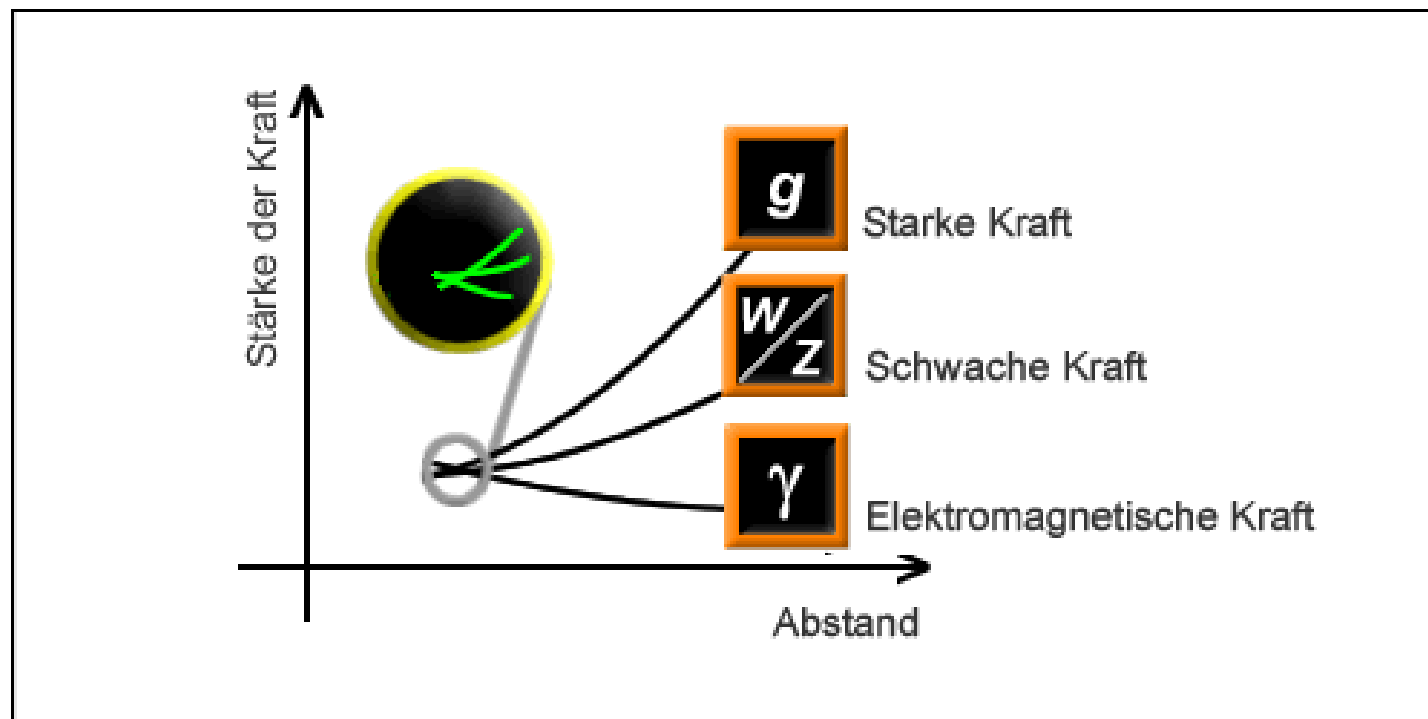
- Standard Model (SM) has 19 free parameters:
- What are the values of these parameters?
- Common origin of all three forces of the SM?
- How to incorporate gravity?
- Candidate for Dark Matter (DM)? ...



# Why *Beyond Standard Model (BSM)* Physics?

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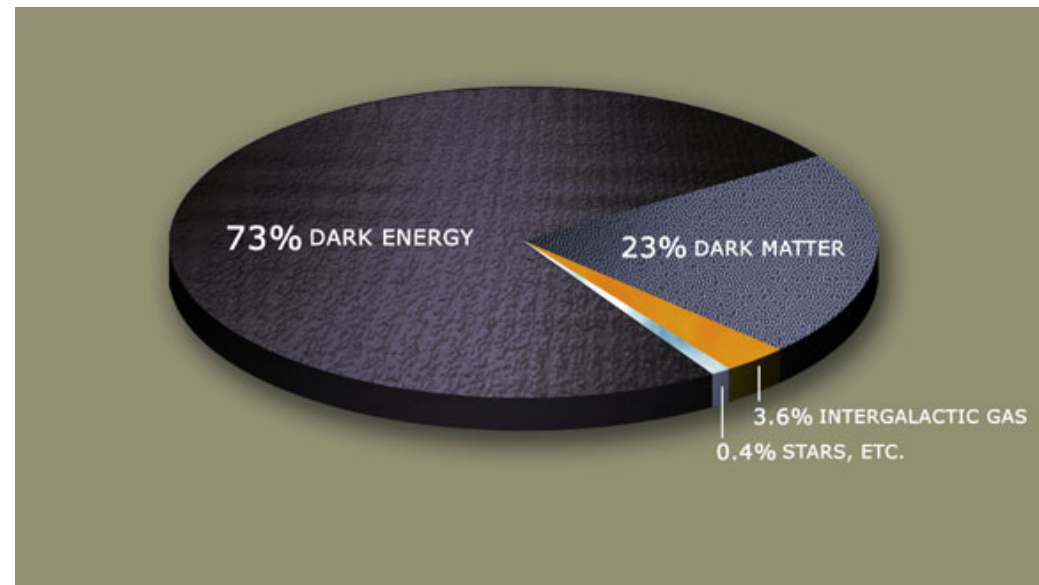
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# Why *Beyond Standard Model (BSM)* Physics?

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## Standard Model: incomplete picture of the universe

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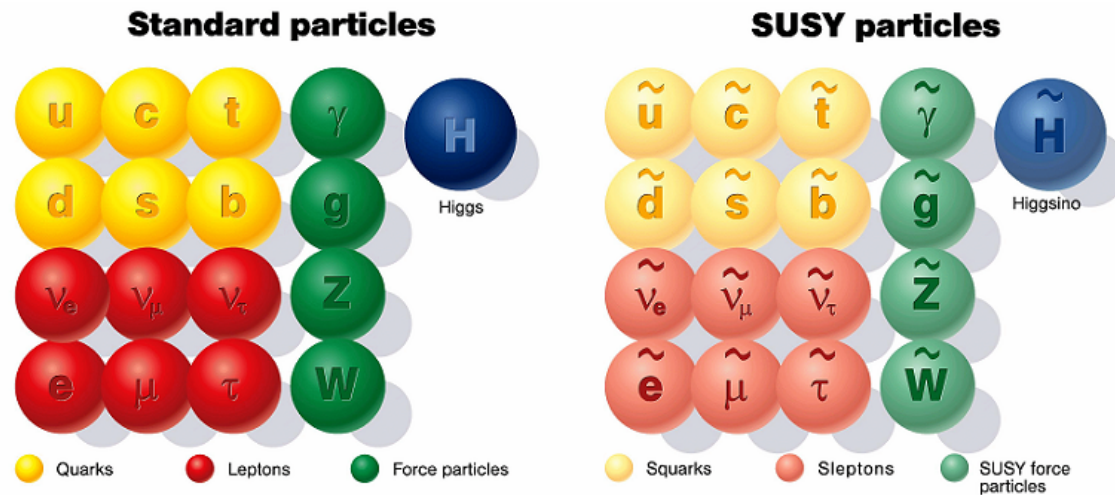
# Supersymmetry

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## Possible answers from: Supersymmetry

Fermions  $\leftrightarrow$  Bosons

Price: doubling of the particle spectrum



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## Supersymmetry - Motivation

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(i) Relates bosons  $\leftrightarrow$  fermions:

$$\left. \begin{array}{l} Q|F\rangle = |B\rangle \\ Q|B\rangle = |F\rangle \end{array} \right\} 1 \text{ multiplet}$$

(ii) Maximal symmetry of the  $\mathcal{S}$ -matrix:

Coleman-Mandula theorem: Bosonic operators cannot extend the Poincaré algebra.

Fermionic operators:  $Q \sim \text{spin } \frac{1}{2} \Rightarrow$  graded Lie-algebra

(iii) Hierarchy problem:

Standard Model:

Relevant low-energy scale: electroweak scale  $v \sim 10^2$  GeV ( $\rightarrow$  Higgs mass  $M_H$ )

Up to which scale is the SM valid? E.g. the GUT scale  $M_{GUT} \sim 10^{16}$  GeV

Hierarchy problem:  $M_H$  unstable w.r.t. the quantum corrections:  $\delta M_H^2 \sim \Lambda^2$

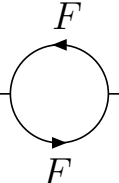
# Hierarchy Problem

Boson masses unstable w.r.t. quantum corrections:

$$\mathcal{L}_1 = \bar{\psi}(i\not{\partial} - m_F)\psi + \frac{1}{2}(\partial_\mu S)^2 - \frac{1}{2}m_S^2 S^2 - \frac{\lambda_F}{2}\bar{\psi}\psi S$$

Free propagator:  $S \text{ --- } S$       inverse propagator:  $i(p^2 - m_S^2)$

Loop corrections:  $S \text{ --- } \text{---} S$       inverse propagator:  $i(p^2 - m_S^2 + \underbrace{\Sigma_S^F}_{\Delta m_S^2})$



We find for the integration over all possible loop momenta  $k$  by dimensional analysis

$$\Delta m_S^2 \sim \lambda_F^2 \int d^4 k \left( \frac{1}{k^2 - m_F^2} + \frac{2m_F^2}{(k^2 - m_F^2)^2} \right)$$

$$\Lambda \rightarrow \infty : \quad \Delta m_S^2 \sim \lambda_F^2 \left( \underbrace{\int \frac{d^4 k}{k^2}}_{\sim \Lambda^2} + 2m_f^2 \underbrace{\int \frac{dk}{k}}_{\sim \ln \Lambda} \right) \Rightarrow \text{quadratically divergent}$$

## Hierarchy Problem

- For  $\Lambda = M_{GUT} = 10^{16}$  GeV:

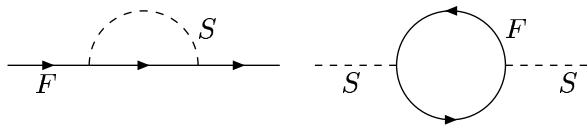
$$\Delta m_S^2 \sim M_{GUT}^2 \Rightarrow \Delta m_S^2 \approx 10^{28} m_S^2$$

for  $m_S \sim \mathcal{O}(10^2 \text{ GeV})$ . Hence

$$m_{S_R}^2 = m_S^2 + \Delta m_S^2 + \text{counterterm} = (1 + 10^{28})m_S^2 + \text{counterterm} \stackrel{!}{=} (10^2 \text{ GeV})^2$$

$\Rightarrow$  Counterterm must be extremely finetuned

- Comparison of corrections to fermion masses and scalar masses:



$$\delta m_F = -\frac{3\lambda_F^2 m_F}{64\pi^2} \log \frac{\Lambda^2}{m_F^2} + \dots$$

$$\delta m_S^2 = -\frac{\lambda_F^2}{8\pi^2} \left[ \Lambda^2 - m_F^2 \log \frac{\Lambda^2}{m_F^2} \right] + \dots$$

$F$ : mild log. divergence  $\sim m_F \log \Lambda \rightarrow 0$  for  $m_F \rightarrow 0$  ( $m_F \rightarrow 0 \rightarrow \gamma_5$ -symmetry)

$B$ : quadratic divergence  $\sim \Lambda^2 \rightarrow$  cancelled only by **fine-tuning** of the bare mass term.

Bosonic masses cannot be kept small in a natural way within the presence of high-energy scales

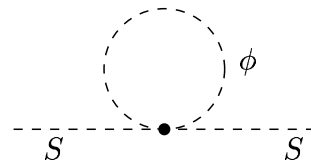
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## Hierarchy Problem

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- **Solution:** Bosonic masses can be kept small in a natural way if bosons are related to fermions.

$$\mathcal{L}_2 = |\partial_\mu \phi_1|^2 + |\partial_\mu \phi_2|^2 + \frac{\lambda_S}{2} S^2 (|\phi_1|^2 + |\phi_2|^2) - m_\phi^2 (|\phi_1|^2 + |\phi_2|^2) \quad [\psi \leftrightarrow \phi_1, \phi_2]$$



$$\delta m_S'^2 = + \frac{\lambda_S^2}{8\pi^2} \left[ \Lambda^2 - m_\phi^2 \log \frac{\Lambda^2}{m_\phi^2} \right] + \dots \quad (\pm \text{Pauli principle})$$

$$\delta m_S^2 = - \frac{\lambda_F^2}{8\pi^2} \left[ \Lambda^2 - m_F^2 \log \frac{\Lambda^2}{m_F^2} \right] + \dots$$

$$\text{SUSY: } \left. \begin{array}{l} \text{degree of freedoms : 4 fermionic} \leftrightarrow 4 \text{ bosonic} \\ \lambda_F = \lambda_S \end{array} \right\} \delta m_S^2 \sim \frac{\lambda^2}{8\pi^2} (m_F^2 - m_\phi^2) \log \Lambda^2$$

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## Hierarchy Problem

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$$\text{SUSY: } \left. \begin{array}{l} \text{degree of freedoms : 4 fermionic} \leftrightarrow 4 \text{ bosonic} \\ \lambda_F = \lambda_S \end{array} \right\} \delta m_S^2 \sim \frac{\lambda^2}{8\pi^2} (m_F^2 - m_\phi^2) \log \Lambda^2$$

- Exact cancellation for  $m_F = m_\phi \Rightarrow$   
exact supersymmetry between bosonic and fermionic degrees of freedom
- No SUSY particles discovered yet  $\Rightarrow$  **SUSY must be broken**
- Soft SUSY breaking:  $m_{SUSY} \neq m_{SM}$ , but  $\lambda_{SUSY} = \lambda_{SM}$
- Corrections remain small enough not to reintroduce finetuning if  $m_{SUSY} \lesssim 1 \text{ TeV}$

TeV scale Supersymmetry:  
solution to hierarchy problem

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## Supersymmetry - Motivation

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(iv) Higgs mechanism generated via radiative corrections (for  $m_t \sim 100\dots 200$  GeV)  $\rightarrow$  T

(v) Unification of ELM + weak + strong couplings  $\rightarrow$  T

$$\frac{1}{\alpha_i(Q^2)} = \frac{1}{\alpha_i} - \frac{b_i}{2\pi} \log Q^2 \quad \text{for } i = U(1), SU(2), SU(3)$$

SM: No single crossing point: order of magnitude deficit.

SUSY: Unification of couplings  $\delta\alpha/\alpha \approx 1.5\%$ . Depends solely on quantum numbers, independent of mass spectrum beyond  $\sim 1$  TeV.

(vi) Cold Dark Matter (CDM) If SUSY particles assigned conserved multiplicative quantum number,

R-parity = +1 SM, = -1 SUSY, then

SUSY particles prod. pairwise in SM collisions    lightest SUSY particle stable: CDM candidate

(vii) Local SUSY: enforces gravity



# Supersymmetry - Motivation

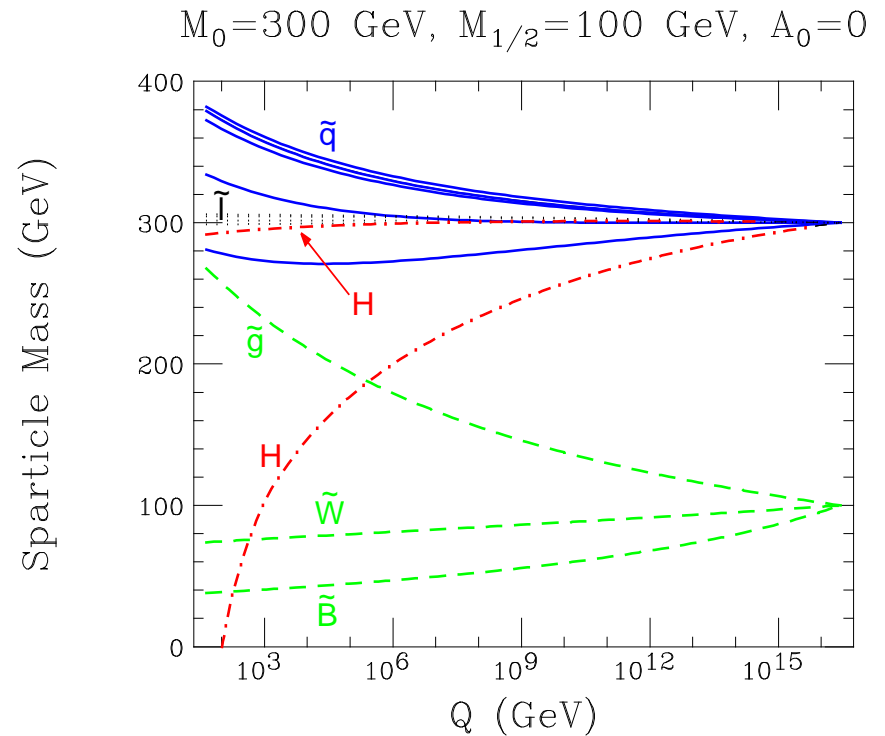
Evolution:  $M_{H_2}^2(Q^2) \approx M_0^2 + \mu^2 - \frac{3g_t^2}{8\pi^2}(3M_0^2 + \mu^2) \log \frac{M_{GUT}}{Q}$

Bagger

$M_{H_2}^2(M_Z^2) < 0$  possible for  $m_t \sim 100 - 200$  GeV

→ radiative symmetry breaking

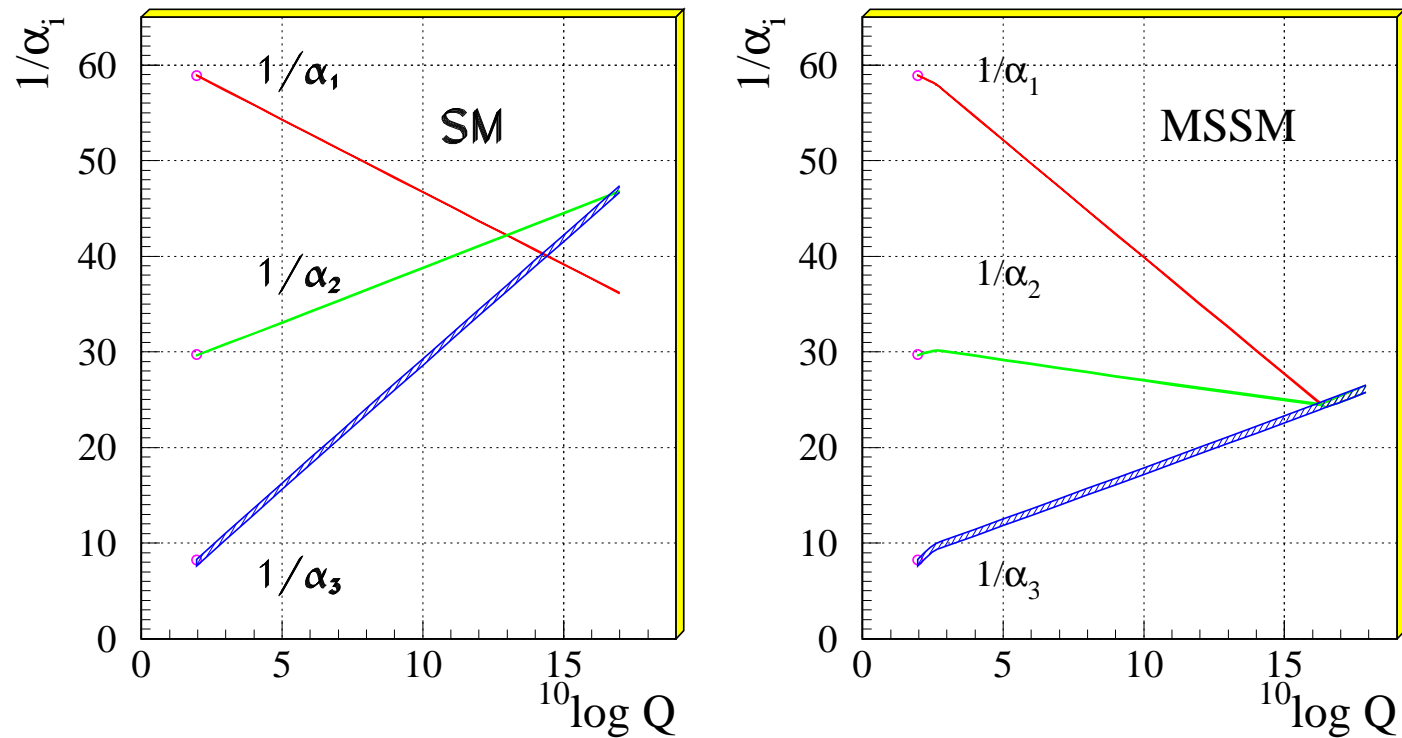
$SU_3 \times SU_2 \times U_1 \rightarrow SU_3 \times U_1^{em}$



# Supersymmetry - Motivation

Amaldi, de Boer, Fürstenau

## Unification of the Coupling Constants in the SM and the minimal MSSM



## (II) Supersymmetry Introduction

## (II) Supersymmetry Introduction

### a) Symmetries

Lagrangian called symmetric if invariant under a certain group of transformations.

Generators of the group fulfill an algebra.

Continuous symmetry of the Lagrangian related to existence of a conserved quantity  $Q \rightarrow$  Noethertheorem.

### Examples

(i) **Invariance under 3-dim rotations** ( $\leftarrow$  isotropy of space):  $\psi \rightarrow \psi e^{i\theta^a L_a}$

generators: angular momenta  $L_a$ ; algebra  $[L_a, L_b] = i\epsilon_{abc} L_c$

quantum numbers: angular momentum (also spin)  $|\vec{L}|^2, L_3$

(ii) **Internal symmetries**, e.g. Standard Model invariant under  $SU(2)_L \times U(1)_Y \times SU(3)_C$

gauge symmetries of the electroweak and strong forces

e.g.  $SU(3)_C$  generators  $T_a$  with the algebra  $[T_a, T_b] = if_{abc} T_c$

quantum numbers: weak isospin, hypercharge, colour

(iii) **Poincaré symmetry** - describes structure of our space-time:

Lorentz transformations  $\Lambda_{\nu}^{\mu}$  (rotations & boosts) and translations  $P^{\mu}$

quantum numbers: mass, spin of particles

**Weyl spinors:** Two-component spinors; all other spinors are built from Weyl spinors

\* Left- and right-handed Weyl spinors  $\Psi_L$  and  $\Psi_R$  transform under the left and right fundamental representation of the special Lorentz group

$$A_L := \Lambda^{(\frac{1}{2}, 0)} = \exp \left\{ -\frac{i}{2} (\vec{\varphi} - i\vec{\nu}) \cdot \vec{\sigma} \right\}$$

$$A_R := \Lambda^{(0, \frac{1}{2})} = \exp \left\{ -\frac{i}{2} (\vec{\varphi} + i\vec{\nu}) \cdot \vec{\sigma} \right\}$$

(rapidity  $\vec{\nu}$ , Pauli matrices  $\sigma_i$ ,  $i=1,2,3$ ) as

$$\psi'_L = A_L \psi_L \quad \text{and} \quad \psi'_R = A_R \psi_R$$

\* Complex  $2 \times 2$  matrix  $A \in SL(2, \mathbb{C})$ : 4 representations

|                                 |                        |                |
|---------------------------------|------------------------|----------------|
| selbst representation:          | $D(A) = A$             |                |
| duale self representation:      | $D(A) = A^{-1T}$       | } equivalent   |
| conjugate representation:       | $D(A) = A^{-1\dagger}$ |                |
| duale conjugate representation: | $D(A) = A^*$           | } equivalent . |

\*  $\Psi_L$  transforms under the  $(\frac{1}{2}, 0)$  fundamental representation

$\Psi_R$  transforms under the  $(0, \frac{1}{2})$  fundamental (conjugate) representation

- \* Notation: fundamental and dual representation: lower  $\leftrightarrow$  higher indices (co- and contravariant)  
conjugate representation: dotted indices

$$\Psi_L = \begin{pmatrix} \psi_1 \\ \psi_2 \end{pmatrix} \quad \text{and} \quad \Psi_R^\dagger = (\psi^1, \psi^2),$$

$$\Psi_R = \begin{pmatrix} \bar{\psi}^1 \\ \bar{\psi}^2 \end{pmatrix} \quad \text{and} \quad \Psi_L^\dagger = (\bar{\psi}_1, \bar{\psi}_2).$$

- \* **Bispinor**: Direct sum of the fundamental reprs.  $(\frac{1}{2}, 0) \oplus (0, \frac{1}{2}) \rightsquigarrow$  bispinor with 4 spinor comps.
- \* **Dirac spinor (chiral representation)**

$$\text{Dirac spinor: } \Psi = \begin{pmatrix} \psi_L \\ \phi_R \end{pmatrix}$$

transforms according to

$$\Psi \rightarrow \Psi' = S\Psi \quad \text{with} \quad S := \Lambda^{(\frac{1}{2}, 0) \oplus (0, \frac{1}{2})} = \begin{pmatrix} A_L & 0 \\ 0 & A_R \end{pmatrix}$$

- \* **Majorana spinor**: half degrees of freedom of Dirac spinor

$$\text{Majorana spinor: } \Psi = \begin{pmatrix} \psi_L \\ \psi_R \end{pmatrix}$$

- **Standard Model** described by

- ▷ internal symmetry:  $T^a$

- ▷ Poincaré symmetry:  $\Lambda^{\mu\nu}, P^\rho$

Internal symmetry is a **trivial** extension of the Poincaré symmetry:

$$[\Lambda^{\mu\nu}, T^a] = 0, \quad [P^\rho, T^a] = 0$$

⇒ direct product: (Poincaré group)  $\otimes$  (internal symmetry)

Particles characterized by maximal set of commuting observables:

$$\underbrace{m, s; \vec{p}, s_3}_{\text{space-time}}; \underbrace{Q, I, I_3, Y, \dots}_{\text{internal}} \\ \text{quantum numbers}$$

- **Question: Can we extend the Standard Model (SM)?**

### c) The Coleman Mandula Theorem (1967) - No go theorem

Every quantum field theory satisfying certain assumptions about its  $S$  matrix and which has non-trivial interactions can only have:

a symmetry Lie algebra which is always

a direct product of the Poincaré group and an internal group

beyond  $P_\mu, M_{\mu\nu}$  (generators of the Lorentz rotations) no more conserved bosonic observables

- New group  $G$  with generators  $R^\alpha$  and

$$[\Lambda^{\mu\nu}, R^\alpha] \neq 0, \quad [P^\alpha, R^\alpha] \neq 0$$

impossible

- New symmetry must predict new particles with the same mass and spin as in the SM

Experimentally excluded



### c) Way out: SUSY algebra

Uniqueness of SUSY extension: beyond  $P_\mu, M_{\mu\nu}$  no more conserved bosonic observables.

HOWEVER: fermionic transformations are not forbidden  $\Rightarrow$

( $Q_\alpha$  = left-handed Weyl spinor:  $\gamma_5 Q = -Q$ ;  $[A, B] \equiv AB - BA$ ;  $\{A, B\} \equiv AB + BA$ )

|                               |                                       |   |
|-------------------------------|---------------------------------------|---|
| <u>Poincaré algebra:</u>      | $[P_\mu, P_\nu]$                      | $= 0$   |
|                               | $[P_\mu, M_{\rho\sigma}]$             | $= i(g_{\mu\rho}P_\sigma - g_{\mu\sigma}P_\rho)$  |
|                               | $[M_{\mu\nu}, M_{\rho\sigma}]$        | $= i(-g_{\mu\rho}M_{\nu\sigma} + g_{\mu\sigma}M_{\nu\rho} + g_{\nu\rho}M_{\mu\sigma} - g_{\nu\sigma}M_{\mu\rho})$ |
| $\oplus$ <u>SUSY algebra:</u> | $\{Q_\alpha, Q_\beta\}$               | $= \{\bar{Q}_{\dot{\alpha}}, \bar{Q}_{\dot{\beta}}\} = 0$   |
| of fermionic $Q$ 's           | $\{Q_\alpha, \bar{Q}_{\dot{\beta}}\}$ | $= 2\sigma_{\alpha\dot{\beta}}^\mu P_\mu$   |
|                               | $[Q_\alpha, P_\mu]$                   | $= [\bar{Q}_{\dot{\alpha}}, P_\mu] = 0$   |
|                               | $[Q_\alpha, M_{\mu\nu}]$              | $= \frac{1}{2}(\sigma_{\mu\nu})_{\alpha\beta} Q_\beta$  |

**SUSY multiplets combine fermions with bosons** spectrum:  $M_{12} = J_3, \sigma_{12} = \sigma_3$

$J_3 \bar{Q}_{1,2} = \bar{Q}_{1,2} (J_3 \pm \frac{1}{2}) \Rightarrow \bar{Q}_{1(2)}$  generates (destroys),  $Q_{1(2)}$  destroys (generates) spin  $\frac{1}{2}$

multiplet structure: particle multiplet  $|\lambda\rangle, |\lambda + \frac{1}{2}\rangle$   
 antiparticle multiplet  $|\lambda\rangle, |\lambda - \frac{1}{2}\rangle$

**Generalization:**  $Q_{\alpha=1,2}^{i=1,2,\dots,N} : \{Q_{\alpha}^i, Q_{\beta}^j\} = \{\bar{Q}_{\dot{\alpha}}^i, \bar{Q}_{\dot{\beta}}^j\} = 0, \quad \{Q_{\alpha}^i, \bar{Q}_{\dot{\beta}}^j\} = 2\delta_{ij}\sigma_{\alpha\dot{\beta}}^{\mu}P_{\mu}$

Maximum:  $|- \lambda_{max} > \dots | - \lambda_{max} + \frac{N}{2} > = |\lambda_{max} >$  consistent field theory:  $\lambda_{max} = 2 \Rightarrow \boxed{N \leq 8}$

## d) Implications

### Same number of fermions and bosons in one multiplet

Witten Index:  $\Delta = \text{Tr}(-1)^{N_F}$  , with  $N_F$  the particle number operator for fermions

$$\Delta|B \rangle = |B \rangle \quad \text{and} \quad \Delta|F \rangle = -|F \rangle$$

We have  $\{Q, \bar{Q}\} = 2\sigma_{\mu}P^{\mu} \Rightarrow$

$$\begin{aligned} \Delta\{Q, \bar{Q}\} = \Delta 2\sigma_{\mu}P^{\mu} \quad \text{LHS:} \quad & \text{Tr} \langle (-1)^{N_F} Q \bar{Q} \rangle + \text{Tr} \langle (-1)^{N_F} \bar{Q} Q \rangle \\ & = \quad \sim \quad + \text{Tr} \langle Q (-1)^{N_F} \bar{Q} \rangle \\ & = \quad \sim \quad - \text{Tr} \langle (-1)^{N_F} Q \bar{Q} \rangle = 0 \\ \text{RHS:} \quad & 2\sigma^{\mu} \text{Tr} [(-1)^{N_F} P_{\mu}] = 0 \quad \Rightarrow \Delta = \text{Tr}(-1)^{N_F} = 0 \end{aligned}$$

Witten index = difference in number of bosonic and fermionic states:  $\Delta = 0 \Rightarrow$

number of bosons = number of fermions

## Masses of fermions and bosons are equal

We have  $[P_\mu, Q] = [P_\mu, \bar{Q}] = 0$ . Hence for  $P_0 = H$ :

$$\begin{aligned} [P_0, Q] = [P_0, \bar{Q}] = 0 \quad H|B\rangle &= m_B|B\rangle \\ QH|B\rangle &= HQ|B\rangle = H|F\rangle \Rightarrow \\ m_B|F\rangle &= m_F|F\rangle \end{aligned}$$

$$m_B = m_F$$

**Experimentally:** no SUSY partners to SM particles with identical mass observed  $\Rightarrow$

If SUSY is realized in nature, it must be broken.

## e) Superfields

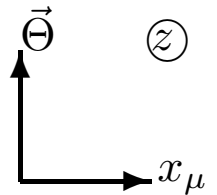
Superfield: combination of fields belonging to the same multiplet into one single field.

|                   |                 |        |                      |                                |
|-------------------|-----------------|--------|----------------------|--------------------------------|
| <u>pairings</u> : | fermion $f$     | $\sim$ | sfermion $\tilde{f}$ | [spin $\frac{1}{2}$ - spin 0]  |
|                   | gauge field $W$ | $\sim$ | gaugino $\tilde{W}$  | [spin 1 - spin $\frac{1}{2}$ ] |
|                   | Higgs $H$       | $\sim$ | Higgsino $\tilde{H}$ | [spin 0 - spin $\frac{1}{2}$ ] |

combined to superfields defined in superspace.

## Superspace:

- Translation transformation  $P_\mu$ ; parameter:  $x_\mu$
- SUSY transformation:  $Q_\alpha, \bar{Q}_{\dot{\alpha}}$ ; parameter:  $\theta, \bar{\theta}$



The diagram shows a coordinate system with a horizontal axis labeled  $x_\mu$  and a vertical axis labeled  $\vec{\theta}$ . A circled  $z$  is positioned in the upper right quadrant. To the right of the diagram, the text reads:  $z = [x_\mu; \theta, \bar{\theta}]$   $x_\mu =$  space-time,  $\theta_{1,2}, \bar{\theta}_{1,2}$  fermionic coordinates

## Reminder Grassmann numbers:

▷ Without spinor index  $\{\theta, \theta\} = 0 \quad \Rightarrow \quad \theta\theta = 0$

▷ With two-component spinor index:

Metric:  $\theta_\alpha, \bar{\theta}_{\dot{\alpha}}$  ( $\alpha = 1, 2$ ) ( $\epsilon^{12} = -\epsilon^{21} = 1$ )

$$\begin{aligned}\theta^2 &= \theta_\alpha \theta^\alpha = \epsilon^{\alpha\beta} \theta_\alpha \theta_\beta = 2\theta_1 \theta_2 \\ &= -\theta^1 \theta_1 - \theta^2 \theta_2 = \theta_1 \theta^1 + \theta_2 \theta^2\end{aligned}$$

$\theta^2 \neq 0$ , but  $\theta^\alpha \theta^\beta \theta^\gamma = 0$  ( $\alpha, \beta, \gamma = 1, 2$ )

Taylor expansion ends after  $\theta\theta$ :  $\phi(\theta) = a + \theta\psi + \theta\theta f$

Integration:  $\int d\theta = 0$ ,  $\int d\theta\theta = 1$  and  $d^2\theta = \frac{1}{2}d\theta_1 d\theta_2$

$$\Rightarrow \int d^2\theta \phi(\theta) = \int d^2\theta (a + \theta\psi + \theta\theta f) = f$$

## e) Translations in superspace

- ◇ 14 generators  $\{P^\mu, M^{\mu\nu}, Q, \bar{Q}\} \Rightarrow$  group of symmetry transformations

$$\text{Translation:} \quad \exp\{-iy^\mu P_\mu\}$$

$$\text{SUSY-Translation:} \quad \exp\{i(\xi Q + \bar{\xi}\bar{Q})\}$$

SUSY generators lead to translations in super-space by the spinorial parameters  $\xi, \bar{\xi}$

- ◇ Element of the Poincaré supergroup

$$S(y, \xi, \bar{\xi}) = \exp\{i(\xi Q + \bar{\xi}\bar{Q} - y^\mu P_\mu - \frac{1}{2}\omega^{\mu\nu} M_{\mu\nu})\}$$

In the following only SUSY translations (w/o rotations)

- ◇ SUSY translations form a group;  $\xi, \bar{\xi}$  independent of  $y^\mu$ : global SUSY transformation

- ◇ Transformation of a superfield,  $S(y, \xi, \bar{\xi})\phi(x, \theta, \bar{\theta})$ :

$$S(y, \xi, \bar{\xi})\phi(x, \theta, \bar{\theta}) = \phi(x^\mu + y^\mu - i\xi\sigma^\mu\bar{\theta} + i\theta\sigma^\mu\bar{\xi}, \xi + \theta, \bar{\xi} + \bar{\theta})$$

- ◇ Representations of the generators ( $\partial_\alpha = \partial/\partial\theta^\alpha, \bar{\partial}_{\dot{\alpha}} = \partial/\partial\bar{\theta}^{\dot{\alpha}}, \overset{(\sim)}{\sigma}_\mu = (1, \pm\vec{\sigma}), \sigma_i$  Pauli Matrices)

$$P_\mu = -i\partial_\mu, \quad Q_\alpha = -i\partial_\alpha - (\sigma^\mu\bar{\theta})_\alpha\partial_\mu, \quad \bar{Q}_{\dot{\alpha}} = -i\bar{\partial}_{\dot{\alpha}} - (\tilde{\sigma}^\mu\theta)_{\dot{\alpha}}\partial_\mu$$

- ◇ Definition of covariant derivatives

$$D_\alpha = \partial_\alpha + i(\sigma^\mu\bar{\theta})_\alpha\partial_\mu, \quad \bar{D}_{\dot{\alpha}} = -\bar{\partial}_{\dot{\alpha}} + i(\tilde{\sigma}^\mu\theta)_{\dot{\alpha}}\partial_\mu$$

## f) General superfield in component form

\* Most general superfield  $\mathcal{F}(x, \theta, \bar{\theta})$  dependent on  $x, \theta, \bar{\theta}$

$$\begin{aligned}\mathcal{F}(x, \theta, \bar{\theta}) &= f(x) + \theta\phi(x) + \bar{\theta}\bar{\chi}(x) + (\theta\theta)M(x) + (\bar{\theta}\bar{\theta})N(x) + \theta\sigma^\mu\bar{\theta}A_\mu(x) \\ &+ (\theta\theta)\bar{\theta}\bar{\lambda}(x) + (\bar{\theta}\bar{\theta})\theta\alpha(x) + (\theta\theta)(\bar{\theta}\bar{\theta})d(x)\end{aligned}$$

\* Component fields (16 real bosonic and 16 real fermionic, boson-fermion rule  $\checkmark$ )

|                                    |                                   |
|------------------------------------|-----------------------------------|
| 4 complex scalar fields:           | $f(x), M(x), N(x), d(x)$          |
| 2 left-handed Weyl spinor fields:  | $\phi(x), \alpha(x)$              |
| 2 right-handed Weyl spinor fields: | $\bar{\chi}(x), \bar{\lambda}(x)$ |
| 1 complex vector fields:           | $A_\mu(x)$                        |

\* Superfields: linear but reducible representation of the SUSY algebra  $\Rightarrow$

## g) Constraint superfields

\* SUSY-invariant conditions on superfield  $\rightsquigarrow$  constraint superfield

$$\begin{aligned}\bar{D}_{\dot{A}}\mathcal{F} = 0 &\Rightarrow \text{chiral (scalar) superfield } \Phi(x, \theta, \bar{\theta}) \\ D_A\mathcal{F} = 0 &\Rightarrow \text{antichiral (scalar) superfield } \Phi^\dagger(x, \theta, \bar{\theta}) \\ \mathcal{F} = \mathcal{F}^\dagger &\Rightarrow \text{vector superfield } V(x, \theta, \bar{\theta})\end{aligned}$$

Chiral Superfield Defined by covariant condition

$$\text{Chiral Superfield: } \bar{D}\Phi_- = 0$$

with  $\bar{D} = \frac{\partial}{\partial\theta} + i\theta\sigma\partial$ : SUSY-invariant  $[\bar{D}, Q] = \dots = 0$

antichiral superfield:  $D\Phi_+ = 0$   $D = \frac{\partial}{\partial\bar{\theta}} + i\sigma\bar{\theta}\partial$

Solution:  $\Phi_- = \Phi_-(x + i\theta\sigma\bar{\theta}; \theta, 0) \equiv \Phi_-(y; \theta)$  is general chiral superfield

$$\bar{D}\Phi_- = -i\theta\sigma\partial\Phi + i\theta\sigma\partial\Phi = 0$$

$$* \Phi(y, \theta) = \varphi(y) + \sqrt{2}\theta\psi(y) + (\theta\theta)F(y)$$

Taylor expansion  $[y = x + i\theta\sigma\bar{\theta}] \rightsquigarrow$  chiral superfield in component fields

$$\begin{aligned} \Phi(x, \theta, \bar{\theta}) = & \varphi + \sqrt{2}\theta\psi + (\theta\theta)F + i(\theta\sigma^\mu\bar{\theta})\partial_\mu\varphi \\ & - \frac{i}{\sqrt{2}}(\theta\theta)\partial_\mu(\psi\sigma^\mu\bar{\theta}) - \frac{1}{4}(\theta\theta)(\bar{\theta}\bar{\theta})\square\varphi \end{aligned}$$

$\varphi$  = 1 complex scalar field for the description of sleptons and squarks

$\Phi$ :  $\psi$  = 1 left-handed Weyl spinor field for the description of leptons and quarks

$F$  = 1 non-propagating auxiliary field

Gauge Superfield Defined by:

$$V = V^\dagger \text{ hermitesch}$$

\* gauge trafo:  $V \rightarrow V + \chi + \chi^\dagger \rightarrow$  minimal field content: Wess-Zumino gauge

$$V = -\theta\sigma_\mu\bar{\theta}A^\mu(x) + i\theta^2\bar{\theta}\bar{\lambda}(x) - i\bar{\theta}^2\theta\lambda(x) + \theta^2\bar{\theta}^2d(x)$$

$A_\mu$  = real vector field

$\hat{V} : \lambda$  = spin  $\frac{1}{2}$  vectorino field

$d$  = non-propagating auxiliary field

\* Supersymmetric field strength  $W_\alpha$

$$W_\alpha = -\frac{1}{4}(\bar{D}\bar{D})D_\alpha V(x, \theta, \bar{\theta})$$

\* Components of  $W_\alpha$

$$W_\alpha = i\lambda_\alpha - 2d\theta_\alpha - (\sigma^{\mu\nu}\theta)_\alpha F_{\mu\nu} - (\theta\theta)(\sigma^\mu\partial_\mu\bar{\lambda})_\alpha$$

Fields  $\lambda, d, F_{\mu\nu}, = \partial_\mu A_\nu - \partial_\nu A_\mu$  are gauge invariant



## h) Behaviour under SUSY transformations

\* Highest components of superfields transform as total derivative:

$$\text{Chiral superfield: } \delta F = i\sqrt{2}\partial_\mu(\bar{\xi}\tilde{\sigma}^\mu\psi)$$

$$\text{Vector superfield: } \delta d = \frac{i}{2}\partial_\mu(\xi\sigma^\mu\bar{\lambda})$$

## i) Construction of SUSY Lagrangians

\* Action must be invariant under SUSY transformations:

$$\delta S = \delta \int d^4x \mathcal{L} = 0$$

Satisfied if  $\mathcal{L} \rightarrow \mathcal{L} + \text{total derivative}$

\*  $d(\theta\theta\bar{\theta}\bar{\theta})$  component) and  $F(\theta\theta)$  component) terms transform as total derivative

\* SUSY Lagrangian given by highest component of products of superfields

$$\mathcal{L} = (\text{superfields})|_{\theta\theta\bar{\theta}\bar{\theta}} + (\text{chiral superfields})|_{\theta\theta y \rightarrow x} + h.c.$$

\* Superfield products:

Products of chiral superfields are chiral superfields

## j) Lagrangian of chiral superfields consists of kinetic, mass and interaction term

$$\mathcal{L} = \mathcal{L}_{kin} + \mathcal{L}_m + \mathcal{L}_{int}$$

with ( $m$  - mass,  $g$  - coupling constant)

$$\begin{aligned}\mathcal{L}_{kin} &= \Phi^\dagger(x, \theta, \bar{\theta})\Phi(x, \theta, \bar{\theta})|_{\theta\theta\bar{\theta}\bar{\theta}} \\ \mathcal{L}_m &= -\frac{m}{2}\Phi^2(y, \theta)|_{\theta\theta}{}_{y\rightarrow x} + h.c. \\ \mathcal{L}_{int} &= -\frac{g}{3}\Phi^3(y, \theta)|_{\theta\theta}{}_{y\rightarrow x} + h.c.\end{aligned}$$

leads to

$$\mathcal{L}_{kin} = (\partial_\mu\varphi^*)(\partial^\mu\varphi) - \frac{i}{2}(\bar{\psi}\tilde{\sigma}^\mu\partial_\mu\psi + \psi\sigma^\mu\partial_\mu\bar{\psi}) + F^*F$$

### • In terms of the superpotential

$$\mathcal{L} = \mathcal{L}_{kin} - [U(\Phi)|_{\theta\theta}{}_{y\rightarrow x} + h.c.]$$

with the potential

$$U(\Phi) = \frac{m}{2}\Phi^2 + \frac{g}{3}\Phi^3$$

Potential is a super function with the Taylor expansion ( $\Phi_S = \sqrt{2}\theta\psi + (\theta\theta)F$ )

$$U(\Phi) = U(\varphi + \Phi_S) = U(\varphi) + \frac{dU(\varphi)}{d\varphi}\Phi_S + \frac{1}{2}\frac{d^2U(\varphi)}{d\varphi^2}\Phi_S^2$$

### • Lagrangian without auxiliary fields

Use Euler-Lagrange equation to eliminate the auxiliary field  $F \rightsquigarrow F = m\varphi^* + g\varphi^{*2} \Rightarrow$

$$\begin{aligned} \mathcal{L} = & (\partial_\mu\varphi^*)(\partial^\mu\varphi) - m^2|\varphi|^2 \\ & - \frac{i}{2}(\bar{\psi}\tilde{\sigma}^\mu\partial_\mu\psi + \psi\sigma^\mu\partial_\mu\bar{\psi}) + \frac{m}{2}(\psi\psi + \bar{\psi}\bar{\psi}) \\ & + g(\varphi\psi\psi + \varphi^*\bar{\psi}\bar{\psi}) - mg|\varphi|^2(\varphi + \varphi^*) - g^2|\varphi|^4 \end{aligned}$$

- ◇ First line: free equation of motion of the bosonic field  $\varphi(x)$  with mass  $m$
- ◇ Middle line: free motion of fermionic field  $\psi(x)$  with **the same mass  $m$**
- ◇ The particles described by  $\varphi, \psi$  are the superpartners of the chiral supermultiplet:
  - $\psi(x)$  : lepton, quark
  - $\varphi(x)$  : slepton, squark or Higgs boson
- ◇ Last line: interaction terms Yukawa term:  $g(\varphi\psi\psi + \varphi^*\bar{\psi}\bar{\psi})$   
 Last two terms: self-interaction of the bosonic field  
**Strength of interaction given by  $g$**

## k) Lagrangian for vector superfields

Use field strength tensor  $W_\alpha \rightsquigarrow$

$$\mathcal{L} = \frac{1}{4} W^\alpha W_\alpha |_{\theta\theta} \rightsquigarrow_x + h.c.$$

The Lagrangian of the vector superfield finally reads (fields  $\lambda, F^{\mu\nu}, d$  are gauge invariant)

$$\mathcal{L} = -\frac{i}{2} (\lambda \sigma^\mu \partial_\mu \bar{\lambda} + \bar{\lambda} \tilde{\sigma}^\mu \partial_\mu \lambda) - \frac{1}{4} F_{\mu\nu} F^{\mu\nu} + 2d^2$$

## l) Supersymmetric gauge theory

With the gauge transformation ( $q$  charge,  $\Lambda$  chiral superfield)

$$\Phi' = e^{-iq\Lambda(x)} \Phi$$

the gauge invariant kinetic part of the chiral Lagrangian reads ( $V' = V + i[\Lambda - \Lambda^\dagger]$ )

$$\bar{\mathcal{L}}_{kin} = \Phi^\dagger e^{qV} \Phi |_{\theta\theta\bar{\theta}\bar{\theta}}$$

In terms of the component fields we find

$$\begin{aligned} \bar{\mathcal{L}}_{kin} = & (D_\mu \varphi)^* (D^\mu \varphi) - \frac{i}{2} (\bar{\psi} \tilde{\sigma}^\mu D_\mu \psi + \psi \sigma^\mu D_\mu^* \bar{\psi}) \\ & + |F|^2 + \frac{i}{\sqrt{2}} q [\varphi^* (\psi \lambda) - \varphi (\bar{\psi} \bar{\lambda})] + qd|\varphi|^2 \end{aligned}$$

$$D_\mu = \partial_\mu - \frac{i}{2}qA_\mu$$

$$\begin{aligned} \bar{\mathcal{L}}_{kin} = & (D_\mu\varphi)^*(D^\mu\varphi) - \frac{i}{2}(\bar{\psi}\tilde{\sigma}^\mu D_\mu\psi + \psi\sigma^\mu D_\mu^*\bar{\psi}) \\ & + |F|^2 + \frac{i}{\sqrt{2}}q[\varphi^*(\psi\lambda) - \varphi(\bar{\psi}\bar{\lambda})] + qd|\varphi|^2 \end{aligned}$$

- \* Contains photon - 2 sfermions interaction

$$\frac{i}{2}qA^\mu\varphi^*\partial_\mu\varphi + h.c.$$

- \* The 2 photons - 2 sfermions interaction

$$\frac{q^2}{4}A_\mu A^\mu|\varphi|^2$$

- \* The photon - 2 fermions interaction

$$qA_\mu(\psi\sigma^\mu\bar{\psi})$$

- \* The gaugino - fermion - sfermion interaction

$$\frac{iq}{\sqrt{2}}\varphi^*(\psi\lambda) + h.c.$$

Supersymmetry  $\rightsquigarrow$  all interaction terms are described by the same coupling strength  $q$

- Minimal coupling in the Lagrangian of the vector superfields

\* Non-Abelian gauge theory

$$i\partial_\mu \rightarrow iD_\mu = i\partial_\mu - g_S G_\mu^a \frac{\lambda^a}{2} - g W_\mu^b \frac{\sigma^b}{2} - g' B_\mu \frac{Y}{2}$$

### m) Complete Lagrangian

Built up by kinetic Lagrangian

$$\begin{aligned} \bar{\mathcal{L}}_{kin} = & (D_\mu \varphi)^* (D^\mu \varphi) - \frac{i}{2} (\bar{\psi} \tilde{\sigma}^\mu D_\mu \psi + \psi \sigma^\mu D_\mu^* \bar{\psi}) \\ & + |F|^2 + \frac{i}{\sqrt{2}} q [\varphi^* (\psi \lambda) - \varphi (\bar{\psi} \bar{\lambda})] + q d |\varphi|^2 \end{aligned}$$

the part  $\mathcal{L}_U$  coming from the superpotential

$$U(\Phi)|_{\theta\theta} + h.c. = (m\varphi + g\varphi^2)F - \frac{1}{2}(m + 2g\varphi)(\psi\psi)$$

hence

$$\begin{aligned} \mathcal{L}_U = & \frac{m}{2} (\psi\psi + \bar{\psi}\bar{\psi}) + g(\varphi\psi\psi + \varphi^* \bar{\psi}\bar{\psi}) \\ & - (m\varphi + g\varphi^2)F - (m\varphi^* + g\varphi^{*2})F^* \end{aligned}$$

and the vector superfield Lagrangian with minimal coupling

$$\mathcal{L}_V = -\frac{i}{2} (\lambda \sigma^\mu D_\mu \bar{\lambda} + \bar{\lambda} \tilde{\sigma}^\mu D_\mu \lambda) - \frac{1}{4} F_{\mu\nu} F^{\mu\nu} + 2d^2$$

- ★ Exploiting the Euler Lagrange equation the parts of the Lagrangian containing the auxiliary fields  $F, d$  can be replaced by the potential  $V$

$$V = 2d^2 + |F|^2$$

where for non-Abelian gauge theories

( $t^a$  generators of the respective gauge group with the coupling constants  $q_a$ )

$$|F|^2 = \left| \frac{dU}{d\varphi} \right|^2$$

$$d^2 = \frac{1}{16} \sum_a |q_a \varphi t^a \varphi|^2$$

Note: scalar quartic coupling generated by SUSY gauge interactions  
 $\Rightarrow$  Higgs mass small [quartic Higgs coupling  $\sim g^2$ ]

- ★ Definition of the superpotential depending on several chiral superfields

$$W(\varphi, \varphi^*) := \sum_{i=1}^n |F_i|^2 = \sum_{i=1}^n \left| \frac{\partial U}{\partial \varphi_i} \right|^2$$

and analogously (with the redefinition  $D \equiv 2d$ )

$$V_D = \frac{1}{2} \sum_A D^A D^A$$

$$D^A = -g_A \sum_i \varphi_i T_{ij}^A \varphi_j$$

## n) Supersymmetry Breaking

General supersymmetric system:

same number of fermions and bosons in one multiplet

masses of fermions and bosons are equal

**Supersymmetric ground state has vanishing energy** Algebra:  $\{Q_\alpha, \bar{Q}_\beta\} = 2\sigma_{\alpha\beta}^\mu P_\mu \Rightarrow$

$$H = \frac{1}{4} \sum_\alpha [Q_\alpha Q_\alpha^\dagger + Q_\alpha^\dagger Q_\alpha] \rightsquigarrow \langle 0|H|0 \rangle = \frac{1}{4} \sum_\alpha [\|Q_\alpha^\dagger|0\rangle\|^2 + \|Q_\alpha|0\rangle\|^2] \Rightarrow$$

$$\langle H \rangle \geq 0$$

SUSY ground state  $\langle 0|H|0 \rangle = 0 \Leftrightarrow Q_\alpha|0\rangle = 0, Q_\alpha^\dagger|0\rangle = 0$  for all  $Q_\alpha, Q_\alpha^\dagger$

$\langle H \rangle \neq 0$ : SUSY spontaneously broken, i.e.  $Q_\alpha|0\rangle \neq 0 \Rightarrow \langle H \rangle = E_{\text{vac}} \neq 0$

SUSY broken:  $V = \frac{1}{2}D^2 + |F|^2$ :  $D \neq 0$   $D$  breaking: Fayet-Iliopoulos

$F \neq 0$   $F$  breaking: O'Raifeartaigh

$\rightarrow$  Ferrara-Girardello-Palumbo mass sum rule

$\langle H \rangle = 0$  in SUSY:  $\Lambda_{\text{cosmo}} = 0$

**Scheme cannot be realized by spontaneous symmetry breaking in visible eigenworld:**

Ferrara-Girardello-Palumbo sum rule:

$$\sum (-1)^{2J} (2J + 1) m_J^2 = 0$$

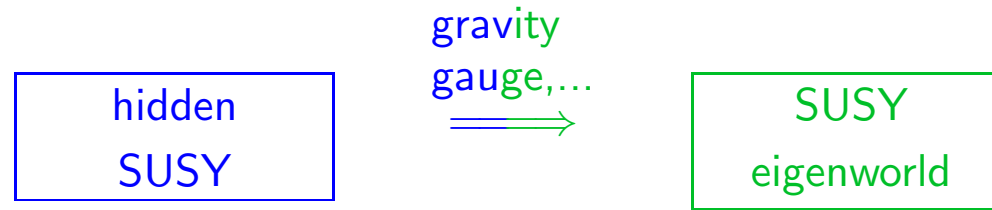
supermultiplet

Example:  $m_{\tilde{e}_L}^2 + m_{\tilde{e}_R}^2 - 2m_e^2 = 0$  not compatible with observation  $\Rightarrow$

Possible solution: RHS  $\neq 0$  through supergravitation sector  $\sim m_{3/2}^2 \rightarrow$  soft, i.e. renormalizable  
SUSY breaking in Standard sector (through explicit mass terms)



Breaking in hidden sector communicated by gravity/gauge/messengers to eigenworld



**Soft SUSY breaking** Define SUSY breaking operators such that no new quadratic divergences are generated

Realisation:

- spontaneous SUSY breaking in “hidden sector”
- mediated in eigen-world through gravitation etc.
- apparent explicit SUSY breaking in eigen-world
- identity between Yukawa/gauge couplings preserved
- SUSY masses  $\neq$  SM masses

**SUSY breaking Lagrangian** [Grisaru, Girardello]

$$\begin{aligned}\mathcal{L}_{break} &= -\frac{1}{2}M_i\bar{\lambda}_i\lambda_i && \text{for gauginos} \\ &- m_f^2|\tilde{f}|^2 + \dots && \text{for sfermions, Higgs} \\ &- W_2(\phi) - W_3(\phi) && \text{superpotential}\end{aligned}$$

## (III) The Minimal Supersymmetry Model

# (III) Minimal Supersymmetry Model - *MSSM*

The SM alone cannot be formulated as SUSY theory ( $N \leq 8$ )  $\Rightarrow$

$$\text{SUSY-Standard Model} = SM \otimes SUSY(N = 1)$$

minimal particle content

$\rightarrow$  Doubling of the particle spectrum: SM+SUSY partner

## Minimal Supersymmetric Standard Model (MSSM)

benchmark model, compatible with experiment, for exploiting phenomenology of SUSY models

### Vector multiplets

| $J = 1$      | $J = \frac{1}{2}$                 |
|--------------|-----------------------------------|
| Gluon $g$    | Gluino $\tilde{g}$                |
| $W^\pm, W^3$ | Wino $\tilde{W}^\pm, \tilde{W}^3$ |
| $B$          | Bino $\tilde{B}$                  |

### Chiral multiplets

| $J = \frac{1}{2}$                    | $J = 0$                             |
|--------------------------------------|-------------------------------------|
| Quarks $q_L, q_R$                    | Squarks $\tilde{q}_L, \tilde{q}_R$  |
| Leptons $l_L, l_R$                   | Sleptons $\tilde{l}_L, \tilde{l}_R$ |
| Higgsinos $\tilde{H}_1, \tilde{H}_2$ | Higgs $H_1, H_2$                    |

## Interactions

Gauge field and matter Lagrangians adapted to  $SU(3) \times SU(2) \times U(1)$  from previous basis

## The Lagrangian

$$\mathcal{L} = \mathcal{L}_{gauge} + \mathcal{L}_{matter} + \mathcal{L}_D + \mathcal{L}_W + \mathcal{L}_{soft}$$

### \* Lagrangian for the gauge fields

$$\mathcal{L}_{gauge} = -\frac{1}{4}G^{a\mu\nu}G_{\mu\nu}^a - \frac{1}{4}W^{a\mu\nu}W_{\mu\nu}^a - \frac{1}{4}B^{\mu\nu}B_{\mu\nu} + Tr[\tilde{g}i\mathcal{D}\tilde{g}] + Tr[\tilde{W}i\mathcal{D}\tilde{W}] + \frac{1}{2}\tilde{B}i\mathcal{D}\tilde{B}$$

covariant derivative  $iD_\mu = i\partial_\mu - gV_\mu$  (minimal subtraction)

field strength tensor  $V_{\mu\nu} = \partial_\nu V_\mu - \partial_\mu V_\nu - ig[V_\mu, V_\nu]$  and the vector potential  $V_\mu = V_\mu^a T^a$

$T^a$  group generators,  $[T^a, T^b] = if_{abc}T^c$

$SU(2) : T^a = \frac{\sigma^a}{2}$  Pauli matrices,  $SU(3) : T^a = \frac{\lambda^a}{2}$  Gell-Mann matrices

### \* Lagrangian for the matter fields

$$\mathcal{L}_{matter} = \sum_{\psi=f, \tilde{H}_i} \bar{\psi}i\mathcal{D}\psi + \sum_{\tilde{f}, H_i} |D_\mu\phi|^2 + i \sum_{\psi, \phi, V} \frac{g_V}{\sqrt{2}} [\bar{\psi}_L T^a \tilde{V}^a \phi - \tilde{V}^a T^a \psi_L \phi^*]$$

### \* Lagrangian of the help fields

$$\mathcal{L}_D = -\frac{1}{2} \sum_{a,V} |D_a^V|^2$$

with  $D_a^V = -g_V \phi_i^* T_{ij}^a \phi_j$

$$\mathcal{L}_W = -\sum_i \left| \frac{\partial W}{\partial \phi_i} \right|^2 - \frac{1}{2} \sum_{ij} \overline{\psi_{iL}^c} \frac{\partial^2 W}{\partial \phi_i \partial \phi_j} \psi_{jL} + h.c.$$

with

$$W = W_R + W_{\mathcal{R}}$$

$$W_R = -\epsilon_{ij} \mu H_1^i H_2^j + \epsilon_{ij} [\lambda_L H_1^i \tilde{L}_j \tilde{E}^c + \lambda_D H_1^i \tilde{Q}_j \tilde{D}^c + \lambda_U H_2^i \tilde{Q}_j \tilde{U}^c]$$

$$W_{\mathcal{R}} = \epsilon_{ij} [\lambda \tilde{L}_i \tilde{L}_j \tilde{E}^c + \lambda' \tilde{L}_i \tilde{Q}_j \tilde{D}^c] + \lambda'' \tilde{U}^c \tilde{D}^c \tilde{D}^c \quad R - \text{parity violating}$$

$$\text{with } \epsilon_{12} = -\epsilon_{21} = 1, \epsilon_{11} = \epsilon_{22} = 0$$

\* **Remark: Multiplicative quantum number  $R$ -parity**

|   |                            |                                     |
|---|----------------------------|-------------------------------------|
| $R - \text{parity} = +1$ for SM particles | if conserved $\Rightarrow$ | • SUSY particle production in pairs |
| $= -1$ for SUSY partners                  |                            | • lightest SUSY particle LSP stable |

\*  **$R$ -parity violating superpotential**  $\sim \epsilon_{ij} [\lambda \tilde{L}_i \tilde{L}_j \tilde{E}^c + \lambda' \tilde{L}_i \tilde{Q}_j \tilde{D}^c] + \lambda'' \tilde{U}^c \tilde{D}^c \tilde{D}^c$

potentially leading to proton decay:

$$\lambda'' \lambda' \sim \begin{matrix} ud \\ u \end{matrix} \rightarrow d^c \rightarrow \begin{matrix} u^c e^+ \\ u \end{matrix}$$

$$P \rightarrow \pi^0 e^+$$

$\lambda'' \lambda' \sim 0$  necessarily, MSSM:  $\lambda = \lambda' = \lambda'' = 0$

## \* The soft SUSY breaking Lagrangian

$$\begin{aligned}
 \mathcal{L}_{soft} = & -\frac{1}{2} \sum_{i=1}^3 M_i \bar{\lambda}_i^a \lambda_i^a - m_1^2 |H_1|^2 - m_2^2 |H_2|^2 + B\mu \epsilon_{ij} (H_1^i H_2^j + h.c.) \\
 & - M_{\tilde{Q}}^2 (\tilde{u}_L^\dagger \tilde{u}_L + \tilde{d}_L^\dagger \tilde{d}_L) - M_{\tilde{U}}^2 \tilde{u}_R^\dagger \tilde{u}_R - M_{\tilde{D}}^2 \tilde{d}_R^\dagger \tilde{d}_R + (\tilde{l}) \\
 & + \frac{g}{\sqrt{2}M_W} \epsilon_{ij} \left[ \frac{M_d}{\cos \beta} A_d H_1^i \tilde{Q}^j \tilde{d}_R^\dagger + (\tilde{u}) + (\tilde{l}) \right]
 \end{aligned}$$

### a) Higgs sector

(i) mass generation of SM particles via Higgs mechanism

(ii) two independent Higgs fields  $H_1, H_2$  to provide mass to down- and up-type particles in holomorphic superpotential of SUSY theories

$$\underline{\text{SM}}: \quad \mathcal{L}_d \sim \bar{Q}_L \phi d_R \quad \phi_0 = \left[0, \frac{v}{\sqrt{2}}\right] \quad \Rightarrow \quad m_d \bar{d}_L d_R + h.c.$$

$$\mathcal{L}_u \sim \bar{Q}_L \phi^c u_R \quad \phi^c = i\tau_2 \phi^*, \quad \phi_0^c = \left[\frac{v}{\sqrt{2}}, 0\right] \quad \Rightarrow \quad m_u \bar{u}_L u_R + h.c.$$

$$\underline{\text{SUSY}}: \quad \phi^c \sim \phi^* \quad \text{not allowed in} \quad \text{holomorphic function next to } \phi$$

(iii) Higgs potential:

$$V_{Higgs} = V_F + V_D + V_{soft}$$

$$V_F = |F|^2 = \sum_{i=1,2} \left| \frac{\partial W}{\partial H_i} \right|^2 = \mu^2 (|H_1|^2 + |H_2|^2)$$

$$V_D = \frac{1}{2} D^2 = \frac{1}{2} \sum_{a,V} | -g_V H_i^* T_{ij}^a H_j |^2 = \frac{g^2 + g'^2}{8} [ |H_1|^2 - |H_2|^2 ]^2 + \frac{g^2}{2} |H_1^\dagger H_2|^2$$

$$V_{soft} = m_1^2 |H_1|^2 + m_2^2 |H_2|^2 - B\mu \epsilon_{ij} (H_1^i H_2^j + h.c.)$$

$$V_{Higgs} = (m_1^2 + \mu^2) |H_1|^2 + (m_2^2 + \mu^2) |H_2|^2 - B\mu \epsilon_{ij} (H_1^i H_2^j + h.c.) \\ + \frac{g^2 + g'^2}{8} [ |H_1|^2 - |H_2|^2 ]^2 + \frac{g^2}{2} |H_1^\dagger H_2|^2$$

$$\text{with } H_1 = \begin{pmatrix} H_1^1 \\ H_1^2 \end{pmatrix} = \begin{pmatrix} \phi_1^{0*} \\ -\phi_1^- \end{pmatrix} \quad H_2 = \begin{pmatrix} H_2^1 \\ H_2^2 \end{pmatrix} = \begin{pmatrix} \phi_2^+ \\ \phi_2^0 \end{pmatrix}$$

quartic couplings  $\sim$  gauge couplings

spontaneous symmetry breaking:  $\min V_{Higgs}$  for  $\langle H_{1,2} \rangle_0 \neq 0$ :

$$H_1 = \begin{pmatrix} \phi_1^{0*} + \frac{v_1}{\sqrt{2}} \\ -\phi_1^- \end{pmatrix} \quad H_2 = \begin{pmatrix} \phi_2^+ \\ \phi_2^0 + \frac{v_2}{\sqrt{2}} \end{pmatrix}$$

8 degrees of freedom: 3 zero-mass states: Goldstone bosons absorbed by elw gauge bosons

5 physical states:

diagonalisation:

$$H_1^1 = \frac{1}{\sqrt{2}}(v_1 + H^0 \cos \alpha - h^0 \sin \alpha + iA^0 \sin \beta - iG^0 \cos \beta)$$

$$H_1^2 = H^- \sin \beta - G^- \cos \beta$$

$$H_2^1 = H^+ \cos \beta + G^+ \sin \beta$$

$$H_2^2 = \frac{1}{\sqrt{2}}(v_2 + H^0 \sin \alpha + h^0 \cos \alpha + iA^0 \cos \beta + iG^0 \sin \beta)$$

$G^\pm, G^0 \Rightarrow$  Goldstone bosons

parameters:

$$M_Z^2 = \frac{g^2 + g'^2}{4}(v_1^2 + v_2^2)$$

$$M_A^2 = B\mu \frac{v_1^2 + v_2^2}{v_1 v_2}$$

$$\tan \beta = \frac{v_2}{v_1}$$

$$m_1^2 + \mu^2 = M_A^2 \sin^2 \beta - \frac{M_Z^2}{2} \cos 2\beta$$

$$m_2^2 + \mu^2 = M_A^2 \cos^2 \beta + \frac{M_Z^2}{2} \cos 2\beta$$

5 physical states:

- charged:  $M_{H^\pm}^2 = M_A^2 + M_W^2$

- pseudoscalar:  $M_A^2$   $\mathcal{CP}_o$

- scalar:  $M_{h,H}^2 = \frac{1}{2}\{M_A^2 + M_Z^2 \mp \sqrt{(M_A^2 + M_Z^2)^2 - 4M_A^2 M_Z^2 \cos^2 2\beta}\}$   $\mathcal{CP}_e$

$$\tan 2\alpha = \tan 2\beta \frac{M_A^2 + M_Z^2}{M_A^2 - M_Z^2} \quad -\frac{\pi}{2} < \alpha < 0$$



Higgs system parameterized by (at LO):  $M_A$  and  $\tan \beta$

$M_A \sim M_H \sim M_{H^\pm} \gg v$  decoupling limit:  $h \rightarrow$  SM-like

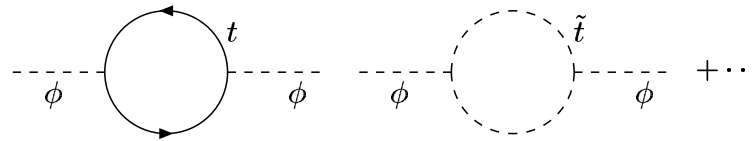
Inequalities:

$$M_h < M_Z, M_A$$

$$M_H > M_Z, M_A$$

$$M_{H^\pm} > M_A, M_W$$

modified through radiative corrections



$$\epsilon = \frac{3G_F m_t^4}{\sqrt{2}\pi^2 \sin^2 \beta} \log \frac{m_{\tilde{t}_1} m_{\tilde{t}_2}}{m_t^2} + \text{stop mixing } [\mu, A_t] \Rightarrow$$

$$M_h \lesssim 140 \text{ GeV}$$

$$M_{H,A,H^\pm} = \mathcal{O}(v) \dots 1 \text{ TeV}$$

## b) Gluino, Charginos/Neutralinos

- Glauino mass:  $M_3 \leftarrow$  soft mass term
- Chargino masses: Charginos are mixings of charged Winos  $\tilde{W}^\pm$  and Higgsinos  $\tilde{H}^\pm \Rightarrow$   
2 charginos  $\tilde{\chi}_1^\pm, \tilde{\chi}_2^\pm$

$$\mathcal{L}_C = -\frac{1}{2}\psi_\pm^T \mathcal{M}_C \psi_\pm + h.c. \quad \text{with} \quad \psi_\pm = \begin{pmatrix} \tilde{W}^+ \\ \tilde{H}_u^+ \\ \tilde{W}^- \\ \tilde{H}_d^- \end{pmatrix} \quad \text{and} \quad \mathcal{M}_C = \begin{pmatrix} 0 & X^T \\ X & 0 \end{pmatrix}$$

where

$$X = \begin{pmatrix} M_2 & \sqrt{2}M_W \sin \beta \\ \sqrt{2}M_W \cos \beta & \mu \end{pmatrix}$$

$M_2$  : from  $\mathcal{L}_{soft}$

$\mu$  : from  $W(\Phi) \rightarrow -\frac{1}{2} \sum_{ij} \overline{\psi_{iL}^c} \frac{\partial^2 W}{\partial \phi_i \partial \phi_j} \psi_{jL} \rightarrow$  higgsino term  $\mu$

non-diag: from  $\mathcal{L}_{matter}^{\lambda H \psi} \rightarrow$  mixing term  $\sim \tilde{W} \tilde{H} \rightarrow M_W \sqrt{2} \cos \beta (\sin \beta)$

diagonalisation  $\rightarrow$  mass eigenstates  $\tilde{\chi}_{1,2}^\pm$  with

$$m_{\tilde{\chi}_{1,2}^\pm}^2 = \frac{1}{2} \{ M_2^2 + \mu^2 + 2M_W^2 \mp \sqrt{(M_2^2 - \mu^2)^2 + 4M_W^2 (M_2^2 + \mu^2 + 2M_2 \mu \sin 2\beta + M_W^2 \cos^2 2\beta)} \}$$

Limits:  $\mu, M_2 \gg M_W$

$$m_{\tilde{\chi}_{1,2}^\pm} = M_2 - \frac{M_W^2 (M_2 + \mu \sin 2\beta)}{\mu^2 - M_2^2}$$

$$m_{\tilde{\chi}_{2,1}^\pm} = |\mu| + \frac{M_W^2 (|\mu| + \epsilon M_2 \sin 2\beta)}{\mu^2 - M_2^2} \quad \epsilon = \text{sign}(\mu)$$

- $|\mu| \gg M_2$  :  $\tilde{\chi}_1^\pm$  gaugino-like,  $\tilde{\chi}_2^\pm$  Higgsino-like
- $|\mu| \ll M_2$  :  $\tilde{\chi}_1^\pm$  Higgsino-like,  $\tilde{\chi}_2^\pm$  gaugino-like
- $\mu \sim -M_2, \tan \beta \sim 1$  :  $m_{\tilde{\chi}_{1,2}^\pm} \sim \sqrt{M_2^2 + M_W^2}$  degenerate
- Neutralino masses: Neutralinos are mixings of  $\tilde{B}, \tilde{W}^3, \tilde{H}_u^0, \tilde{H}_d^0 \Rightarrow$   
4 neutralinos  $\tilde{\chi}_{1,2,3,4}^0$

$$\mathcal{L}_0 = -\frac{1}{2} \psi_0^T \mathcal{M}_0 \psi_0 + h.c. \quad \text{with} \quad \psi_0 = \begin{pmatrix} \tilde{B} \\ \tilde{W}^3 \\ \tilde{H}_d^0 \\ \tilde{H}_u^0 \end{pmatrix}$$

where

$$\mathcal{M}_0 = \begin{pmatrix} M_1 & 0 & -M_Z \sin \theta_W \cos \beta & M_Z \sin \theta_W \sin \beta \\ 0 & M_2 & M_Z \cos \theta_W \cos \beta & -M_Z \cos \theta_W \sin \beta \\ -M_Z \sin \theta_W \cos \beta & M_Z \cos \theta_W \cos \beta & 0 & -\mu \\ M_Z \sin \theta_W \sin \beta & -M_Z \cos \theta_W \sin \beta & -\mu & 0 \end{pmatrix}$$

Diagonalisation  $\rightarrow$  mass eigenstates  $\tilde{\chi}_{1,2,3,4}^0$

Limits:  $\mu, M_1, M_2 \gg M_Z$

$$\begin{aligned}
 m_{\tilde{\chi}_1^0} &= M_1 - \frac{M_Z^2 s_W^2 (M_1 + \mu s_\beta)}{\mu^2 - M_1^2} \\
 m_{\tilde{\chi}_2^0} &= M_2 - \frac{M_Z^2 c_W^2 (M_1 + \mu s_\beta)}{\mu^2 - M_2^2} \\
 m_{\tilde{\chi}_3^0} &= |\mu| + \frac{M_Z^2 (1 - \epsilon s_{2\beta}) (|\mu| + M_1 c_W^2 + M_2 s_W^2)}{2(|\mu| + M_1)(|\mu| + M_2)} \\
 m_{\tilde{\chi}_4^0} &= |\mu| + \frac{M_Z^2 (1 + \epsilon s_{2\beta}) (|\mu| - M_1 c_W^2 - M_2 s_W^2)}{2(|\mu| - M_1)(|\mu| - M_2)}
 \end{aligned}$$

$$\Rightarrow \tilde{\chi}_1^0 \sim \tilde{B}^0, \tilde{\chi}_2^0 \sim \tilde{W}^3, \tilde{\chi}_{3,4}^0 \sim \frac{\tilde{H}_d^0 \pm \tilde{H}_u^0}{\sqrt{2}}, m_{\tilde{\chi}_2^0} \sim m_{\tilde{\chi}_1^\pm}$$

- $|\mu| \gg M_1, M_2$  : LSP gaugino-like
- $|\mu| \ll M_1, M_2$  : LSP Higgsino-like;  $m_{\tilde{\chi}_1^0} \sim m_{\tilde{\chi}_2^0} \sim m_{\tilde{\chi}_1^\pm}$

### c) Slepton/Squark masses

L and R states for fermions and sfermions independent degrees of freedom

LR mass matrix:

$$\mathcal{L}_{\tilde{f}} = -\tilde{f}^\dagger \mathcal{M}_{\tilde{f}}^2 \tilde{f} \quad \text{with } \tilde{f} = \begin{pmatrix} \tilde{f}_L \\ \tilde{f}_R \end{pmatrix} \quad \text{and}$$

$$\mathcal{M}_f^2 = \begin{pmatrix} M_{\tilde{f}_L}^2 + m_f^2 + \overbrace{M_Z^2(I_{3L} - e_f \sin^2 \theta_W) \cos 2\beta}^{D\text{-term}} & m_f(A_f - \mu r_f) \\ m_f(A_f - \mu r_f) & M_{\tilde{f}_R}^2 + m_f^2 - M_Z^2(I_{3R} - e_f \sin^2 \theta_W) \cos 2\beta \end{pmatrix}$$

$$r_f = \begin{cases} \cot \beta & \text{for } f = \text{up-type} \\ \tan \beta & \text{for } f = \text{down-type} \end{cases}$$

$M_{\tilde{f}_{L/R}}^2$  : from  $\mathcal{L}_{soft}$

$m_f^2$  : from  $\mathcal{L}_W \sim \left| \frac{\partial W}{\partial \phi} \right|^2$

$D - term$  : from  $\mathcal{L}_D$

mixing  $m_f \mu r_f$  : from  $\mathcal{L}_W \sim \left| \frac{\partial W}{\partial \phi} \right|^2$

Mixing large only for 3rd generation:  $L, R \rightarrow 1, 2$

$$m_{\tilde{f}_{1,2}}^2 = m_f^2 + \frac{1}{2} \left\{ M_{\tilde{f}_L}^2 + M_{\tilde{f}_R}^2 \mp \sqrt{(M_{\tilde{f}_L}^2 - M_{\tilde{f}_R}^2)^2 + 4m_f^2(A_f - \mu r_f)^2} \right\} \quad (\text{without } D - term)$$

Diagonalisation:

$$\begin{pmatrix} \tilde{f}_1 \\ \tilde{f}_2 \end{pmatrix} = \begin{pmatrix} \cos \theta_f & \sin \theta_f \\ -\sin \theta_f & \cos \theta_f \end{pmatrix} \begin{pmatrix} \tilde{f}_L \\ \tilde{f}_R \end{pmatrix}$$

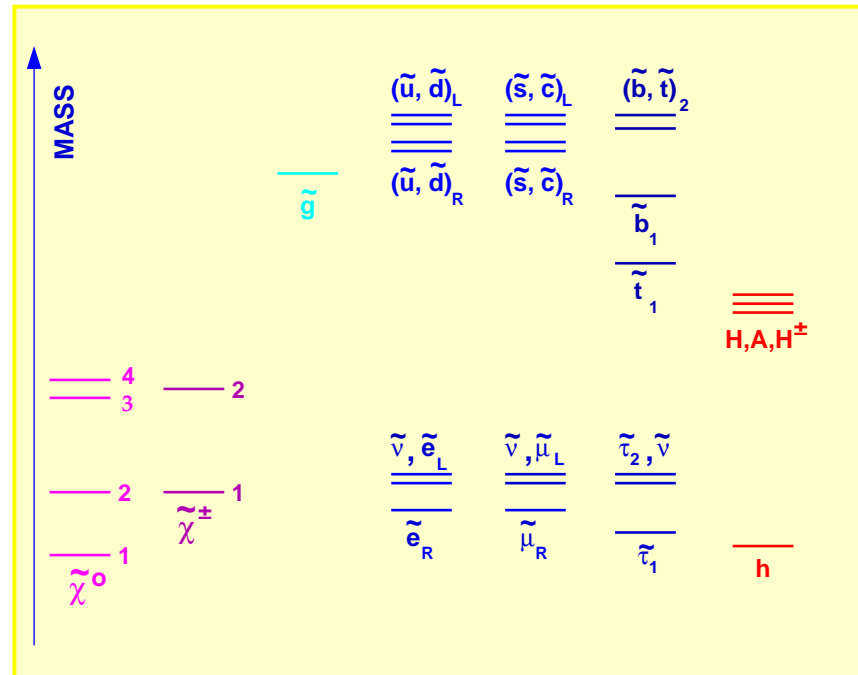
$$\sin 2\theta_f = \frac{2m_f(A_f - \mu r_f)}{m_{\tilde{f}_1}^2 - m_{\tilde{f}_2}^2}$$

$$\cos 2\theta_f = \frac{M_{\tilde{f}_L}^2 - M_{\tilde{f}_R}^2}{m_{\tilde{f}_1}^2 - m_{\tilde{f}_2}^2}$$

- Splitting is largest for the heaviest fermions  $\Rightarrow \tilde{t}_1$  can be the lightest squark  
 $\tilde{\tau}_1$  can be the lightest slepton
- large  $\tan \beta$ : splitting  $\tilde{b}_1 \leftrightarrow \tilde{b}_2$  large  $\Rightarrow$  there are regions where  $\tilde{b}_1$  is the lightest squark

# Example of SUSY Spectrum

## Schematic Sparticle Spectrum in MSSM



## (IV) SUSY-GUT



# (IV) SUSY-GUT

SUSY physically motivated by GUT: stability of the radiative corrections to  $W, Z, H$  masses.

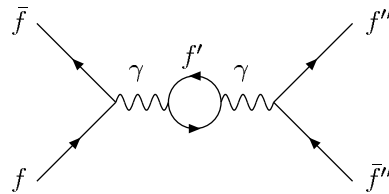
Aim: reconstruction of the fundamental SUSY theory at the GUT/PLANCK scale.

MSSM: 124 free parameters  $\rightsquigarrow$  constrained by unification at the GUT scale

## (a) Unification of the gauge couplings

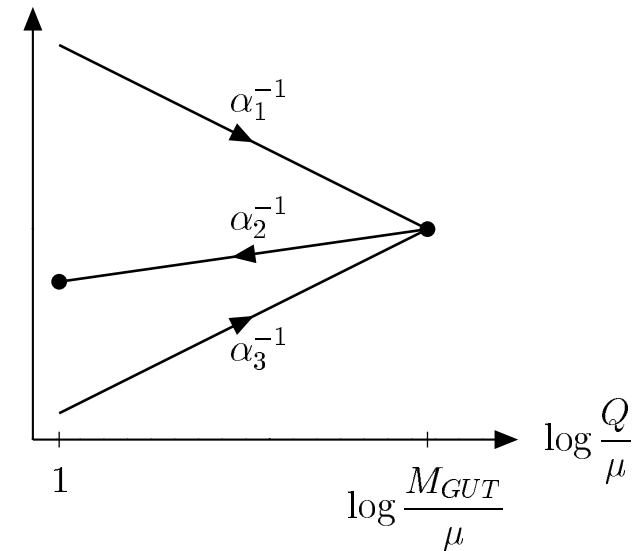
SM:  $SU_3 \times SU_2 \times U_1 \xrightarrow{GUT} SU_5$   $g_3 \ g_2 \ g_1 \rightarrow g_5 : \sin^2 \theta_W = \frac{3}{8}$  at GUT

Running couplings:



$$\frac{\partial \alpha_i}{\partial \log \mu^2} = -\frac{b_i}{4\pi} \alpha_i^2 + \mathcal{O}(\alpha_i^3)$$

|     |         |                |               |               |                |                |
|-----|---------|----------------|---------------|---------------|----------------|----------------|
| SM: | $b_i =$ | 0              | $-N_G$        | $\frac{4}{3}$ | $-N_H$         | $\frac{1}{10}$ |
|     |         | $\frac{22}{3}$ | $\frac{4}{3}$ | $\frac{4}{3}$ | $\frac{1}{6}$  | 0              |
|     |         | 11             | $\frac{4}{3}$ | 0             | $\frac{3}{10}$ | 0              |
|     |         | 0              | $\frac{4}{3}$ | 2             | $\frac{1}{2}$  | 0              |
|     |         | 6              | $-N_G$        | 2             | $-N_H$         | 0              |
|     |         | 9              | 2             | 2             | 0              | 0              |



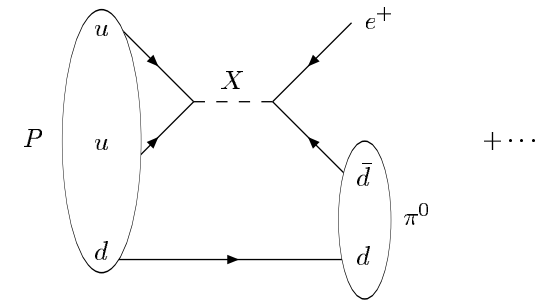
$$\begin{aligned} \sin^2 \theta_W(M_Z^2): \quad & \text{SM:} \quad 0.2100 \pm 0.0026 \\ & \text{MSSM:} \quad 0.2335 \pm 0.0017 \\ & \text{exp:} \quad 0.2316 \pm 0.0002 \end{aligned}$$

- SM couplings cannot be unified. SUSY couplings can
- SUSY predictions of  $\sin^2 \theta_W$  within 2 permille. Independent of details of the  $\tilde{M} \sim 1$  TeV spectrum, only sensitive to particle spectrum.

(b) Proton decay:

SM-SU(5): gauge interactions between leptons and quarks:

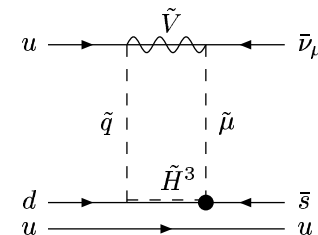
$$\tau(P \rightarrow \pi^0 + e^+) \sim \frac{M_X^4}{\alpha_5^2 M_P^5}$$



SM:  $M_X \sim 10^{15}$  GeV:  $\sim 10^{30}$  a    SUSY:  $M_X > 10^{16}$  GeV:  $\gtrsim 10^{35}$  a (exp:  $> 10^{33}$  a)

However: additional dim 5 contribution

$$\tau(P \rightarrow K^+ \bar{\nu}_\mu) \sim \left( \frac{16\pi^2}{\lambda^2 g^2} \right)^2 \frac{m_{\tilde{H}^3}^2 \tilde{m}^2}{M_P^5} \text{ near experimental limit}$$



(c) Radiative symmetry breaking:

universal sGUT masses (mSUGRA):  
 Gauginos:  $M_1, M_2, M_3 = M_{1/2}$   
 Scalars:  $M_H^2 - \mu^2 = m_{\tilde{l}}^2 = m_{\tilde{q}}^2 = M_0^2$

RGE: GUT  $\rightarrow$  ELW

$$\frac{\partial}{\partial \log Q} \begin{pmatrix} M_{H_2}^2 \\ m_{\tilde{t}_R}^2 \\ m_{\tilde{t}_L}^2 \end{pmatrix} = \frac{g_t^2}{8\pi^2} \begin{pmatrix} 3 & 3 & 3 \\ 2 & 2 & 2 \\ 1 & 1 & 1 \end{pmatrix} \begin{pmatrix} M_{H_2}^2 \\ m_{\tilde{t}_R}^2 \\ m_{\tilde{t}_L}^2 \end{pmatrix} + \frac{g_t^2 A_t^2}{8\pi^2} \begin{pmatrix} 3 \\ 2 \\ 1 \end{pmatrix}$$

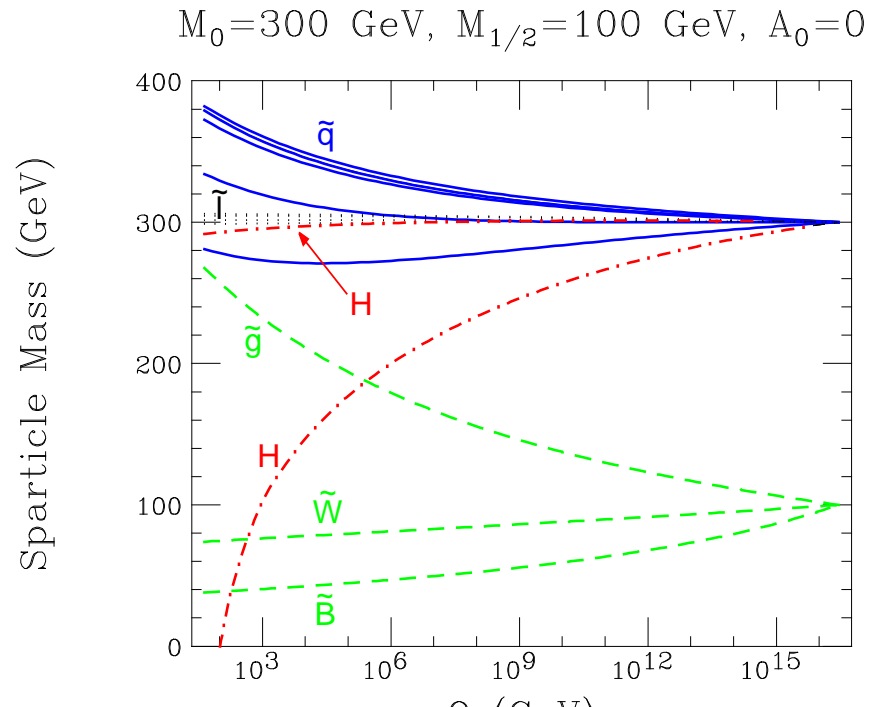
Evolution:  $M_{H_2}^2(Q^2) \approx M_0^2 + \mu^2 - \frac{3g_t^2}{8\pi^2} (3M_0^2 + \mu^2) \log \frac{M_{GUT}}{Q}$

Bagger

$M_{H_2}^2(M_Z^2) < 0$  possible for  $m_t \sim 100 - 200$  GeV

$\rightarrow$  radiative symmetry breaking

$SU_3 \times SU_2 \times U_1 \rightarrow SU_3 \times U_1^{em}$



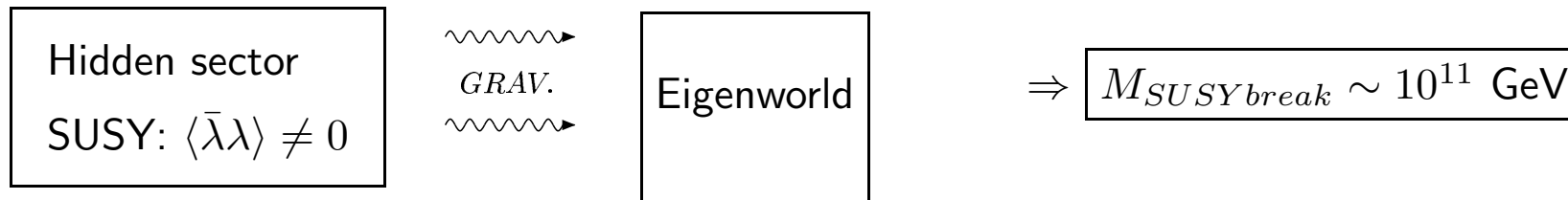
# (V) SUSY Breaking

# (V) SUSY Breaking Mechanisms

Ferrara sum rule: no spontaneous symmetry breaking in eigenworld:  $\sum (-1)^{2J} (2J + 1) M_J^2 \neq 0$ .

|                    |                                |          |
|--------------------|--------------------------------|----------|
| <u>Mechanisms:</u> | Supergravitation               | mSUGRA   |
|                    | Gauge-mediated SUSY breaking   | GMSB     |
|                    | Anomaly-mediated SUSY breaking | AMSB     |
|                    | Scherk-Schwarz SUSY breaking   | SSSB ... |

## Minimal SUPERGRAVITATION:



Soft parameters “universal”: 5 parameters:  $M_0, M_{1/2}, A_0, \tan \beta, \text{sgn}\mu$

Evolution: GUT  $\rightarrow$  ELW:

$$\begin{aligned} \frac{\partial M_i}{\partial \log \mu^2} &= -\frac{b_i}{4\pi} \alpha_i M_i \\ \frac{\partial \alpha_i}{\partial \log \mu^2} &= -\frac{b_i}{4\pi} \alpha_i^2 \\ \Rightarrow \frac{M_i}{\alpha_i} &= \text{const} \end{aligned}$$

Gauginos masses run like gauge couplings  $\Rightarrow M_1 = M_2 \frac{5}{3} \cdot \tan^2 \theta_W \sim \frac{1}{2} M_2 \quad (M_i(M_{GUT}) = M_{1/2})$

$$\frac{M_3}{M_2} = \frac{\alpha_3}{\alpha_2} \gg 1 \Rightarrow m_{\tilde{g}} \gg m_{\tilde{\chi}}$$

## Reconstruction of the fundamental theory at GUT/Planck scale:

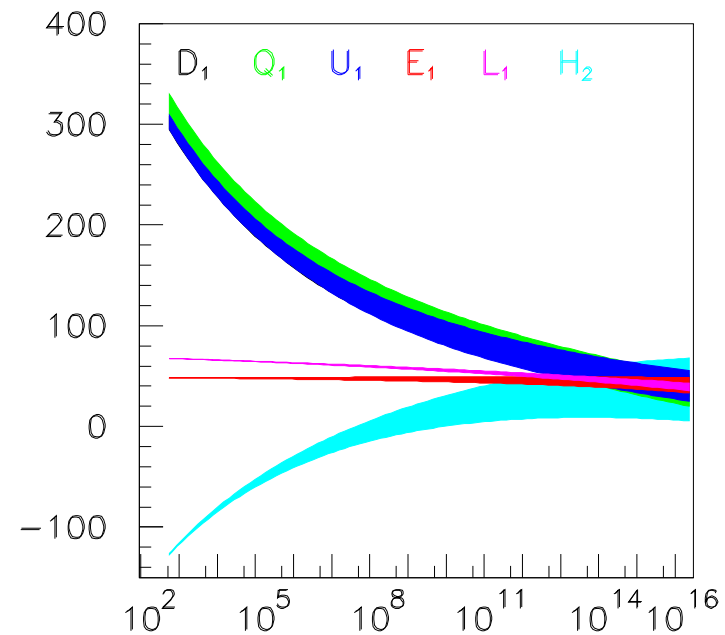
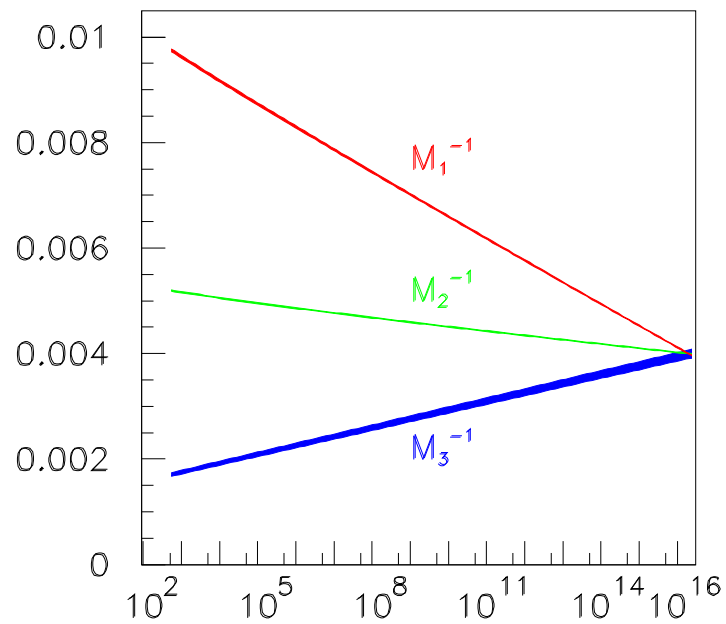
high-precision measurements of low-energy Lagrangian parameters (LHC+ILC)

⇒ extrapolate to high scale: - symmetries/universal behaviour?  
- impact of high-scale physics?

Evolution: RG equations

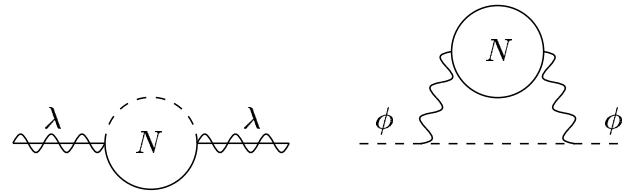
Evolution: gaugino and scalar mass parameters

Blair, Porod, Zerwas



## Gauge-mediated SUSY breaking (GMSB):

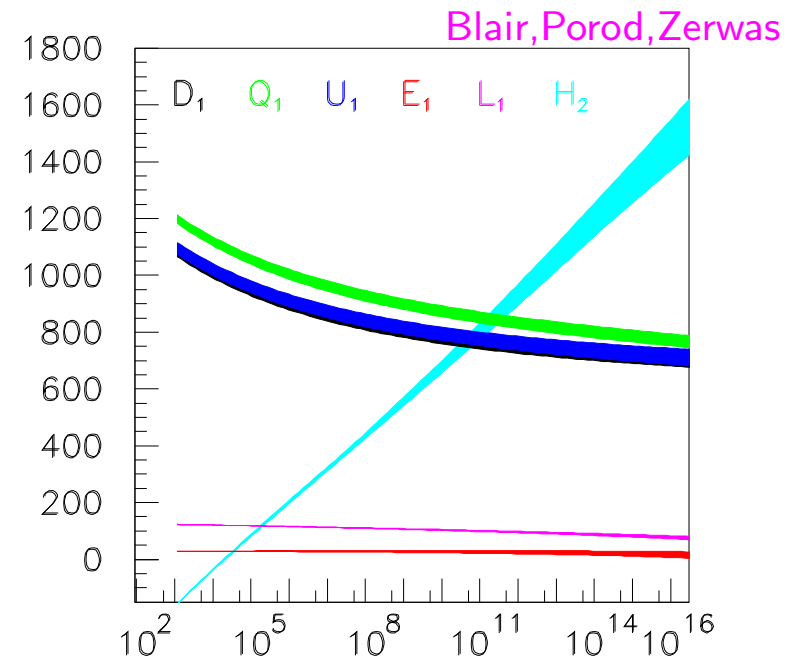
- flavor-blind SUSY-breaking mediating interactions are ordinary EW and QCD gauge interactions
- MSSM soft terms come from loop diagrams involving messenger particles
- messengers are new chiral supermultiplets coupling to a SUSY breaking VEV ( $F$ ) and also have  $SU(3)_C \times SU(2)_L \times U(1)_Y$  interactions providing the necessary connection to the MSSM



- gaugino masses evolve like in mSUGRA but without unification
- scalar masses significantly different, determined by  $F$ , the messenger mass  $M_{mess}$  and the number  $N$  of messenger fields

• **5 parameters:**  $F, M_{mess}, N, \tan \beta, \text{sgn} \mu$

- $m_{\tilde{e}_L} = M_{H_u}$  at  $\mu = \sqrt{F} \rightarrow$  exp. reconstr. of  $\sqrt{F} = M_{SUSY\text{break}}$
- lower limit to  $M_{mess}$ , SUSY masses  $\Rightarrow \sqrt{F} \gtrsim 10^5$  GeV
- Gravitino is LSP,  $m_{\tilde{G}} \sim \frac{\langle F \rangle}{M_{Planck}} \ll M_{weak}$
- NLSP: (i)  $N$  small  $\rightarrow$  neutralino  
(ii)  $N$  large  $\rightarrow$  slepton



## (VI) SUSY Particle Production



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## Scattering processes at hadron colliders

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- Connect incoming quarks, gluons with colliding protons  
outgoing particles with observed hadronic jets
- Scattering processes at high-energy hadron colliders:  $\rightarrow$  hard  $\leftarrow$  QCD  
 $\rightarrow$  soft
- Hard processes (e.g. Higgs boson or high- $p_T$  jet production): perturbation theory
- Soft processes (e.g. total cross section, underlying event etc.)  
non-perturbative QCD effects

### Factorisation theorem of the QCD

Partonic cross sections have collinear divergences in the hadronic initial state, which factorise universally (i.e. independent of the process) from the hard scattering process and can be absorbed in the renormalized parton densities of the initial state. These renormalized parton densities are solutions of the Altarelli-Parisi equations.

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# Master Formula

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- Master Formula  $pp \rightarrow X$ : QCD factorization

$$\sigma_{AB} = \sum_{ab} \int dx_1 dx_2 f_{a/A}(x_1, \mu_F^2) f_{b/B}(x_2, \mu_F^2) \hat{\sigma}_{ab \rightarrow X}$$

$$A = B = p \text{ und } a = b = q/g$$

- Partonic cross section  $\hat{\sigma}$ :

▷ Partons of the incoming hadrons interact at short distance

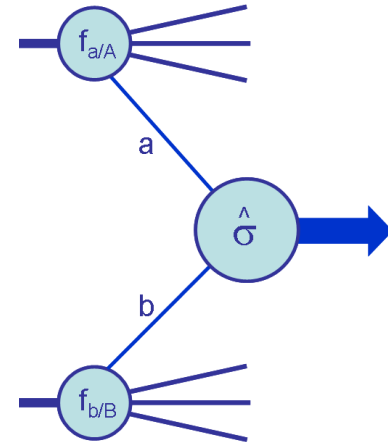
Example Drell-Yan process:  $\hat{\sigma}(q\bar{q} \rightarrow l^+l^-)$

- Parton distribution functions (pdf)  $f_{a/A}(x_1, \mu_F^2), f_{b/B}(x_2, \mu_F^2)$

▷  $x_1 = 2E_a/\sqrt{S}, x_2 = 2E_b/\sqrt{S}$  momentum fraction carried by the incoming quarks, gluons

▷  $\mu_F^2$  factorization scale (separates short- and long-distance physics)

pdf's extracted from deep-inelastic scattering



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# Scattering processes at hadron colliders

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- **General process**  $\sigma(pp \rightarrow X)$

$$\sigma_{pp \rightarrow X} = \sum_{a,b,k} f_{a/p}(\mu_F^2) \otimes f_{b/p}(\mu_F^2) \otimes \hat{\sigma}_{ab \rightarrow k}(\alpha_s(\mu_R^2), \mu_R^2) \otimes D_{k \rightarrow X}(\mu_F^2)$$

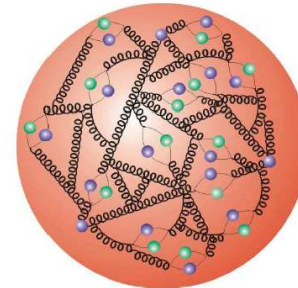
- **Partonic cross section**  $\hat{\sigma}_{ab \rightarrow k}$

calculable with perturbation theory in powers of  $\alpha_s$

$$\hat{\sigma}_{ab \rightarrow k} = [\hat{\sigma}_0 + \alpha_s(\mu_R^2)\hat{\sigma}_1 + \alpha_s^2(\mu_R^2)\hat{\sigma}_2 + \dots]_{ab \rightarrow k}$$

- **Parton luminosity**  $f_{a/p}(\mu_F^2) \otimes f_{b/p}(\mu_F^2)$

proton: very complicated multi-particle bound state



- **Final state**  $X$ : hadrons, mesons, jets, ...

▷ fragmentation function  $D_{k \rightarrow X}(\mu_F^2)$  or jet algorithm

▷ interface with showering-algorithms (Monte Carlo)

---

## *SUSY Particle Production*

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R-Parity: multiplicative quantum numbers (prevents proton decay)

$$R = (-1)^{3B+L+2S} = \begin{cases} +1 & \text{SM particle} \\ -1 & \text{SUSY partner} \end{cases}$$

$R$  – parity = +1 for SM particles  $\Rightarrow$  • SUSY particle production in pairs  
= -1 for SUSY partners • lightest SUSY particle LSP stable

Assume  $R$ -parity conservation in the following

# SUSY Particle Production

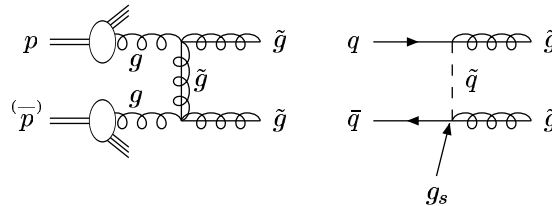
## Hadron Collider

Large production cross sections for moderate squark/gluino masses through strong interactions in  $pp/p\bar{p}$  collisions

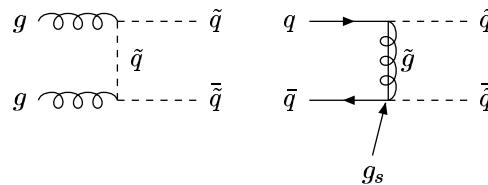
Through cascade decays + 3 classes of SUSY pair production processes:

(i) Strongly interacting particle pairs

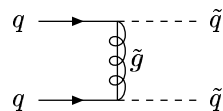
$$p\bar{p}^{(-)} \rightarrow \tilde{g}\tilde{g}$$



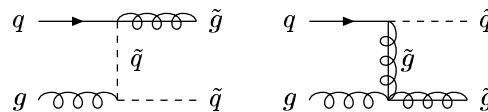
$$p\bar{p}^{(-)} \rightarrow \tilde{q}\tilde{q}$$



$$p\bar{p}^{(-)} \rightarrow \tilde{q}\tilde{q}$$



$$p\bar{p}^{(-)} \rightarrow \tilde{q}\tilde{g}$$



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## *SUSY Particle Production*

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$$\sigma_{gg} = \int_{\tau_0}^1 dx_1 \int_{\tau_0/x_1}^1 dx_2 g(x_1, \mu_F^2) g(x_2, \mu_F^2) \hat{\sigma}_{gg}(\hat{s} = x_1 x_2 s)$$

with  $\tau_0 = 4m^2/s$  [ $m = (m_1 + m_2)/2$ ] and

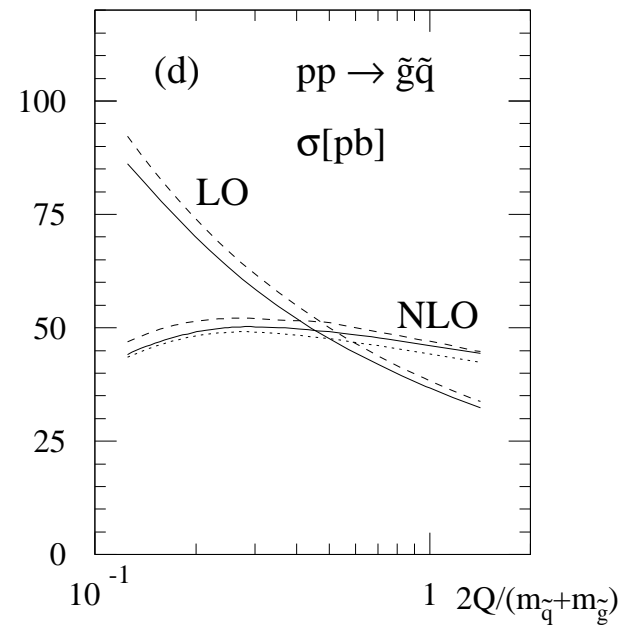
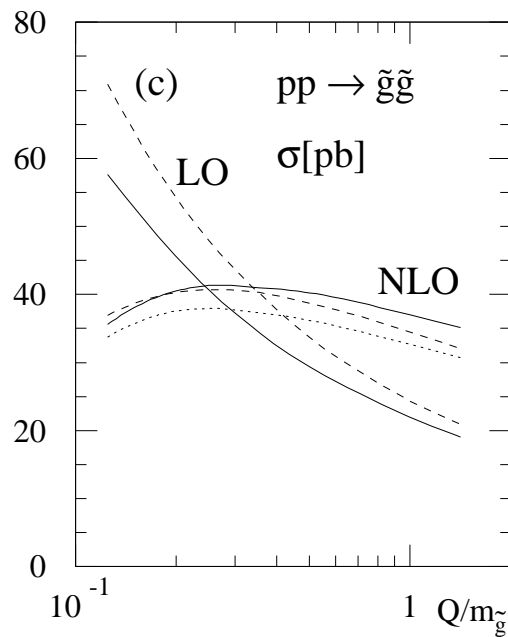
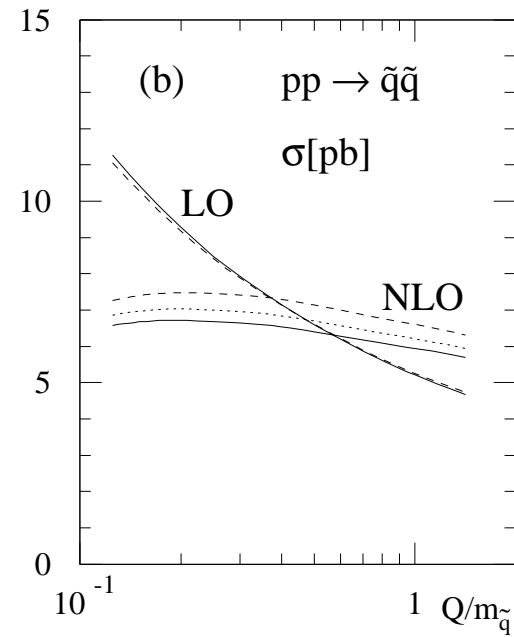
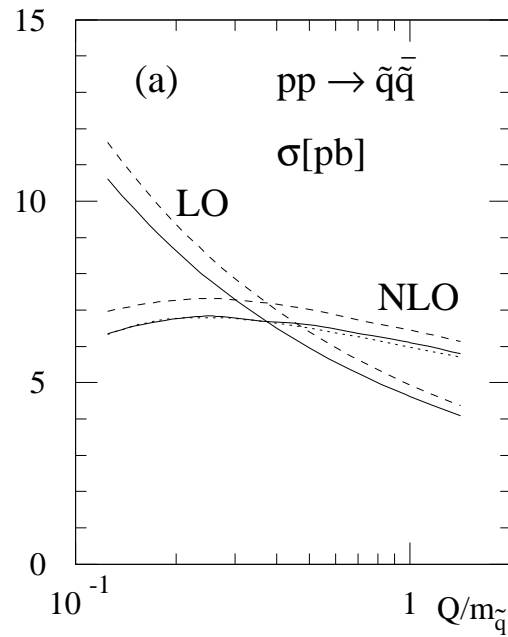
$$\hat{\sigma}_{gg}(\hat{s} = x_1 x_2 s) = \alpha_s^2(\mu_R) f_0(\hat{s} = x_1 x_2 s)$$

- **leading order: large theoretical uncertainties** (due to undefined renormalization scale  $\mu_R$ , factorisation scale  $\mu_F$ )
- natural scale:  $\mu_R = \mu_F = m$ ; scale variation  $\rightarrow$  estimate of theoretical uncertainties with respect to scale choice (large logarithms in higher order):

$$\begin{aligned} \alpha_s(Q^2) &= \frac{\alpha_s(\mu^2)}{1 + \frac{33-2N_F}{12} \frac{\alpha_s(\mu^2)}{\pi} \log \frac{Q^2}{\mu^2}} \\ &= \alpha_s(\mu^2) \left[ 1 - \frac{33-2N_F}{12} \frac{\alpha_s}{\pi} \log \frac{Q^2}{\mu^2} + \mathcal{O}(\alpha_s^2) \right] \end{aligned}$$

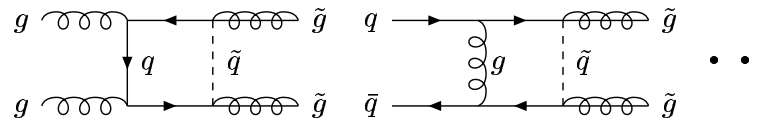
[parton densities in analogy]

$$\frac{1}{2}m < \mu_R = \mu_F < 2m : \delta\sigma \sim \pm 50 \%$$

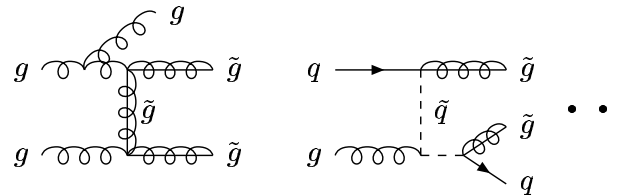


## Effect reduced through SUSY QCD corrections:

- virtual 1-loop contributions



- real contributions through gluon radiation/crossing



$$\begin{aligned}\hat{\sigma}_{gg} &= \alpha_s^2(\mu_R) \left\{ f_0 + f_0 \frac{33-3N_F}{6} \frac{\alpha_s}{\pi} \log \frac{\mu_R^2}{m^2} + \frac{\alpha_s}{\pi} f_1 \right\} \\ &= \alpha_s^2(m^2) \left\{ f_0 + \frac{\alpha_s}{\pi} f_1 + \mathcal{O}(\alpha_s^2) \right\}\end{aligned}$$

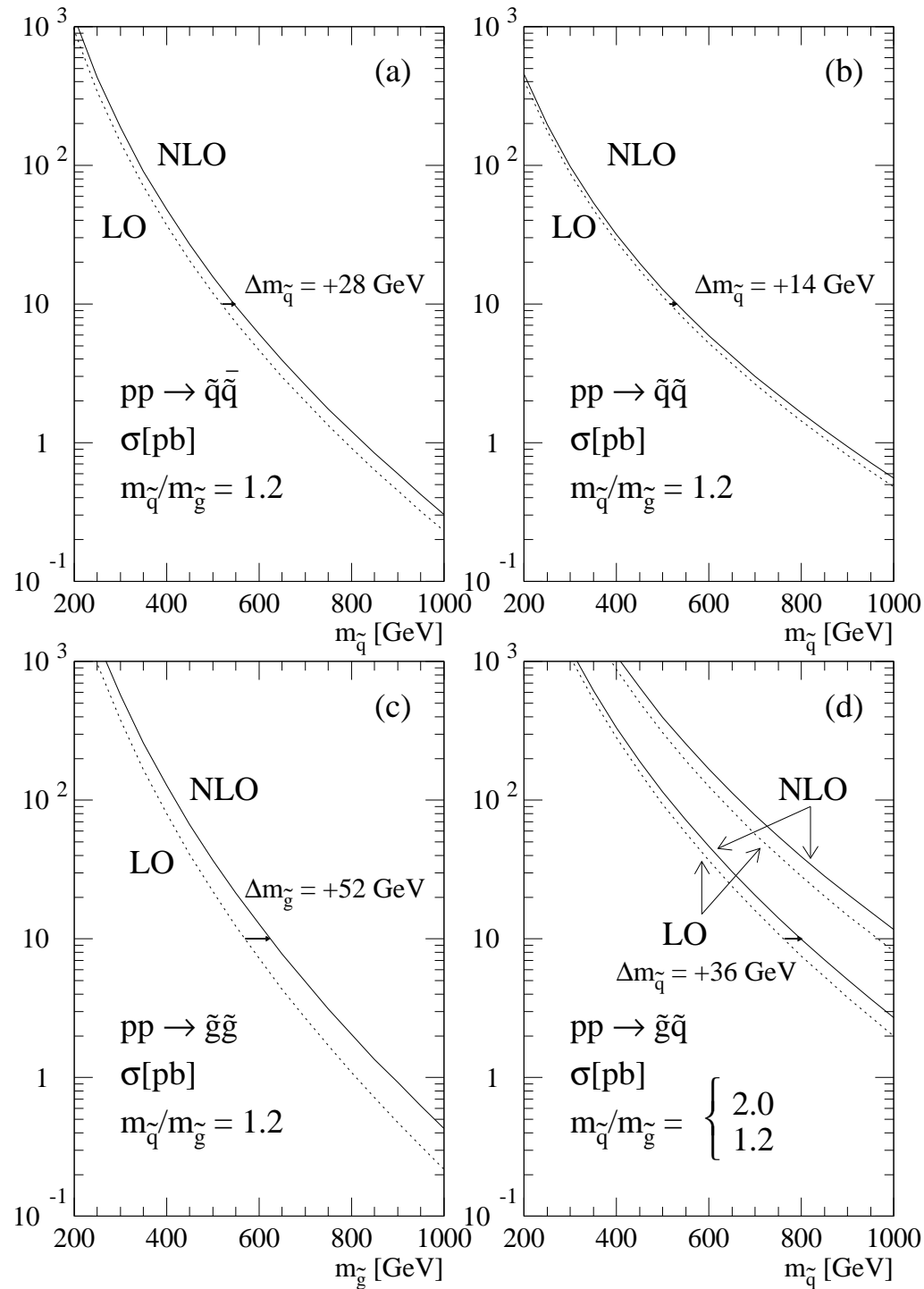
[parton densities in analogy]

$$\frac{1}{2}m < \mu_R = \mu_F < 2m : \delta\sigma \sim \pm 10 \%$$

⇒ NLO corrections provide reliable predictions of cross sections at hadron colliders

$$\text{central scale: } K = \frac{\sigma_{NLO}}{\sigma_{LO}} \sim 1.1 - 2.0$$





## Implications for exp. searches:

- (i) Renorm./factor. scale dep.  
reduced by  $\sim 2.5 - 4 \rightsquigarrow$  stable  
theor. predictions for  $\sigma$
- (ii) NLO corr. large & positive  
 $\rightsquigarrow$  to be included in analyses  
( $\rightarrow$  masses)
- (iii)  $p_T$  and  $y$  distributions hardly  
affected by NLO
- (iv) NLO  $\rightsquigarrow$  raise of TeV lower  $\tilde{q}$ ,  
 $\tilde{g}$  mass bounds by  
 $+10-30$  GeV

---

# Signatures

---

## Classical signatures (R-parity conserving SUSY, i.e. pair production/LSP stable):

- gluino  $>$  squark:  
 $\tilde{q} \rightarrow q\tilde{\chi}_1^0 = q + E_T^{miss}$   
 $\tilde{g} \rightarrow q\tilde{q} \rightarrow qq\tilde{\chi}_1^0 = qq + E_T^{miss}$
- squark  $>$  gluino:  
 $\tilde{g} \rightarrow q\tilde{q}_{virt} \rightarrow qq\tilde{\chi}_1^0 = qqE_T^{miss}$   
 $\tilde{q} \rightarrow q\tilde{g} \rightarrow qq\tilde{\chi}_1^0 = qq + E_T^{miss}$

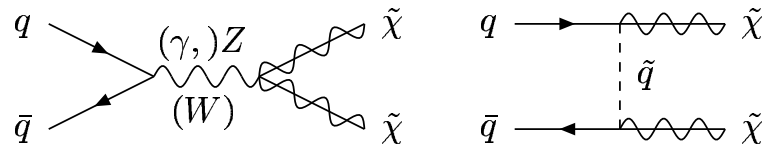
$$pp \rightarrow n \text{ jets} + E_T^{miss}$$

## Discovery range:

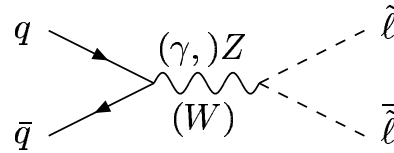
|          |            |             |
|----------|------------|-------------|
| Tevatron | $\lesssim$ | 500 GeV     |
| LHC      | $\lesssim$ | 2.5...3 TeV |

(ii) Weakly interacting particle pairs

$$p \begin{pmatrix} - \\ p \end{pmatrix} \rightarrow \tilde{\chi} \tilde{\chi}$$



$$p \begin{pmatrix} - \\ p \end{pmatrix} \rightarrow \tilde{l} \tilde{l}$$



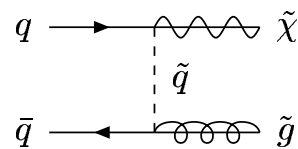
Signatures

$$\tilde{l} \rightarrow l \tilde{\chi}_1^0 : pp \rightarrow l^+ l^- + E_T^{miss}$$

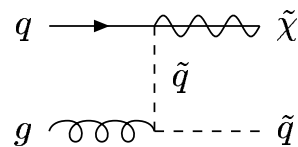
$$\tilde{\chi}_2^0 \rightarrow l^+ l^- \tilde{\chi}_1^0 \text{ etc.} : pp \rightarrow l^+ l^+ l^- l^- + E_T^{miss} \text{ etc.}$$

(iii) Associated production

$$p \begin{pmatrix} - \\ p \end{pmatrix} \rightarrow \tilde{g} \tilde{\chi}$$



$$p \begin{pmatrix} - \\ p \end{pmatrix} \rightarrow \tilde{q} \tilde{\chi}$$

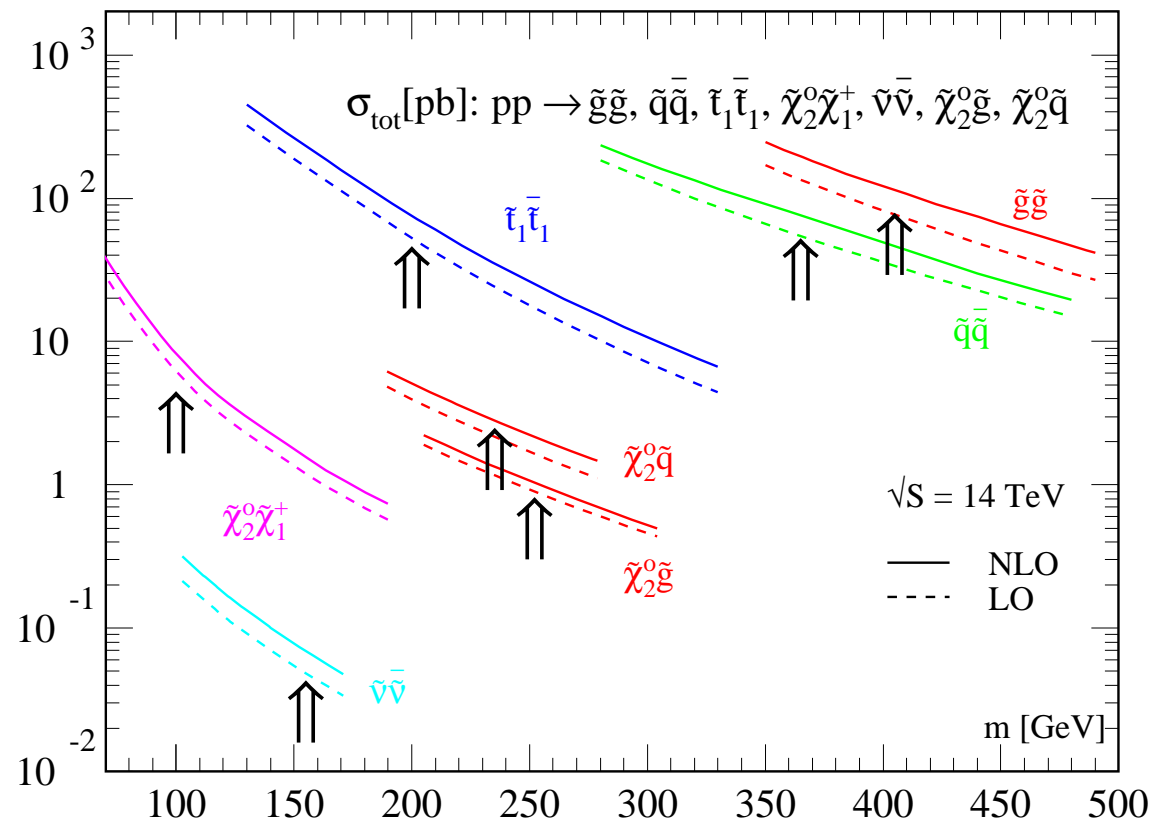


# SUSY Particle Production at the LHC

NLO SUSY-QCD corrections for SUSY particle production at hadron colliders

Public code [PROSPINO](#)

Beenakker, Höpker, Krämer, Plehn, Spira, Zerwas



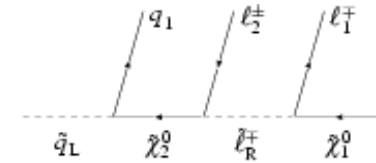
## Cascade decays

gluino/squark decays = rich source for non-colored (supersymmetric) particles

### Mass determination: kinematic endpoint technique

Construct lepton/quark upper/lower endpoints and relate them to the masses in the decay chain

E.g.:  $\tilde{q} \rightarrow \tilde{\chi}_2^0 q \rightarrow \tilde{l}^\pm l^\mp q \rightarrow \tilde{\chi}_1^0 l^+ l^- q = j + l^+ + l^- + E_T^{miss}$



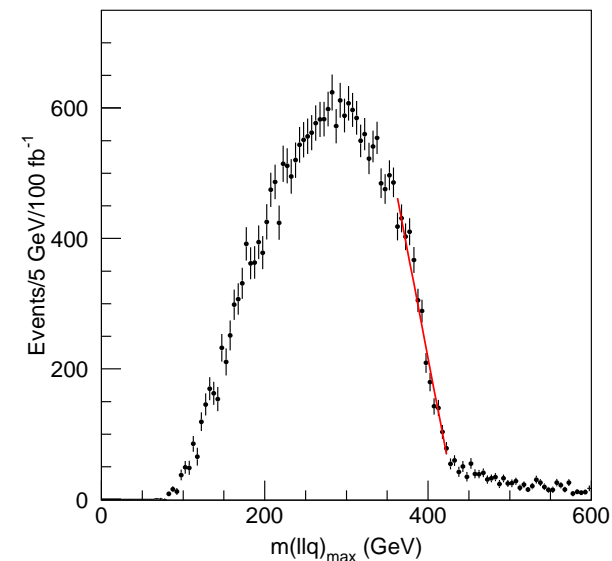
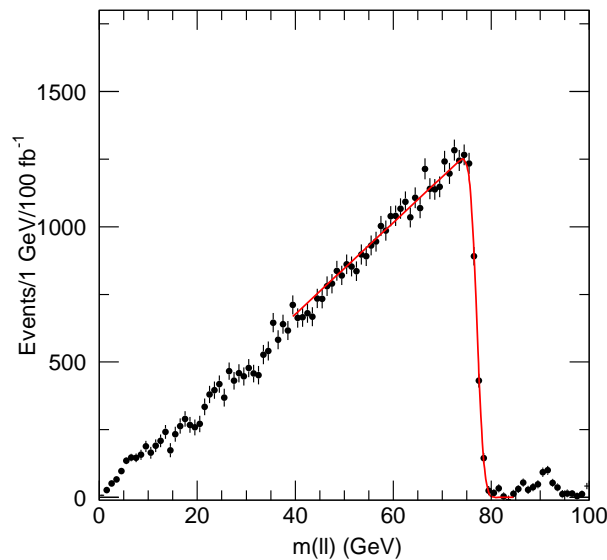
4 unknown masses:  $M_{\tilde{q}}, M_{\tilde{\chi}_2^0}, M_{\tilde{l}}, M_{\tilde{\chi}_1^0}$

4 endpoints:  $M(ll)^{max}, M(l_1q)^{max}, M(l_2q)^{max}, M(llq)^{max}$

⇒ all masses can be determined

$$\max M^2(ll) = M_{\tilde{\chi}_2^0}^2 \left[ 1 - \frac{M_{\tilde{l}}^2}{M_{\tilde{\chi}_2^0}^2} \right] \left[ 1 - \frac{M_{\tilde{\chi}_1^0}^2}{M_{\tilde{l}}^2} \right]$$

$$\max M^2(llq) = M_{\tilde{q}}^2 \left[ 1 - \frac{M_{\tilde{\chi}_2^0}^2}{M_{\tilde{q}}^2} \right] \left[ 1 - \frac{M_{\tilde{\chi}_1^0}^2}{M_{\tilde{\chi}_2^0}^2} \right]$$



## Spin:

particle chain in SUSY equivalent to UED

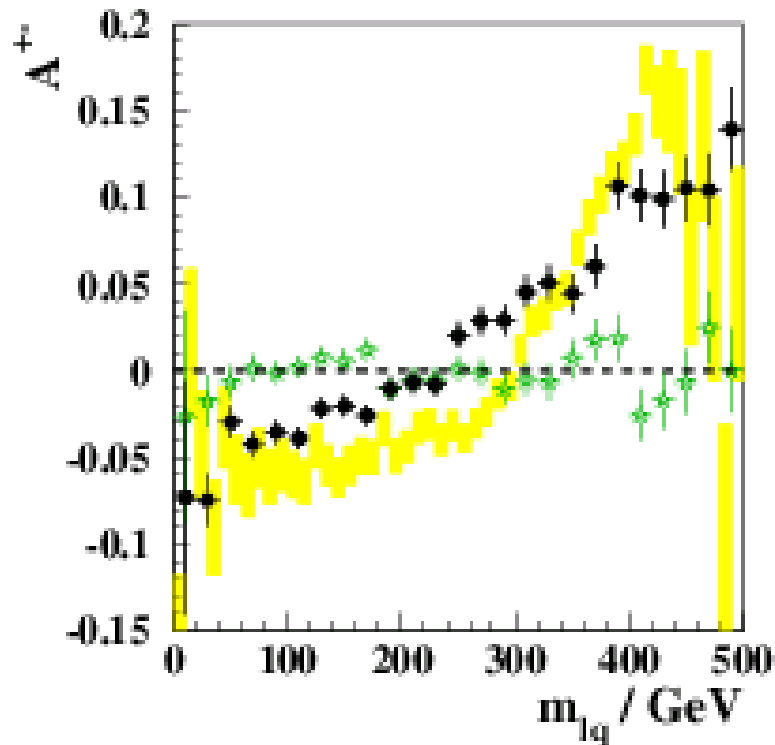
$$\text{SUSY: } \tilde{q}_L \rightarrow q + \tilde{\chi}_2^0 \rightarrow q + (\tilde{l}) \rightarrow q + ll + \tilde{\chi}_1^0$$

$$\text{UED: } q_1 \rightarrow q + Z_1 \rightarrow q + (l_1 l) \rightarrow q + ll + \gamma_1$$

distinction by spin:  $\sim$  angular distributions / invariant masses

charge asymmetry in  $[ql^+]$  vs  $[ql^-]$ :

difficult analysis  $\rightarrow$  A.J.Barr, hep-ph/0405052.

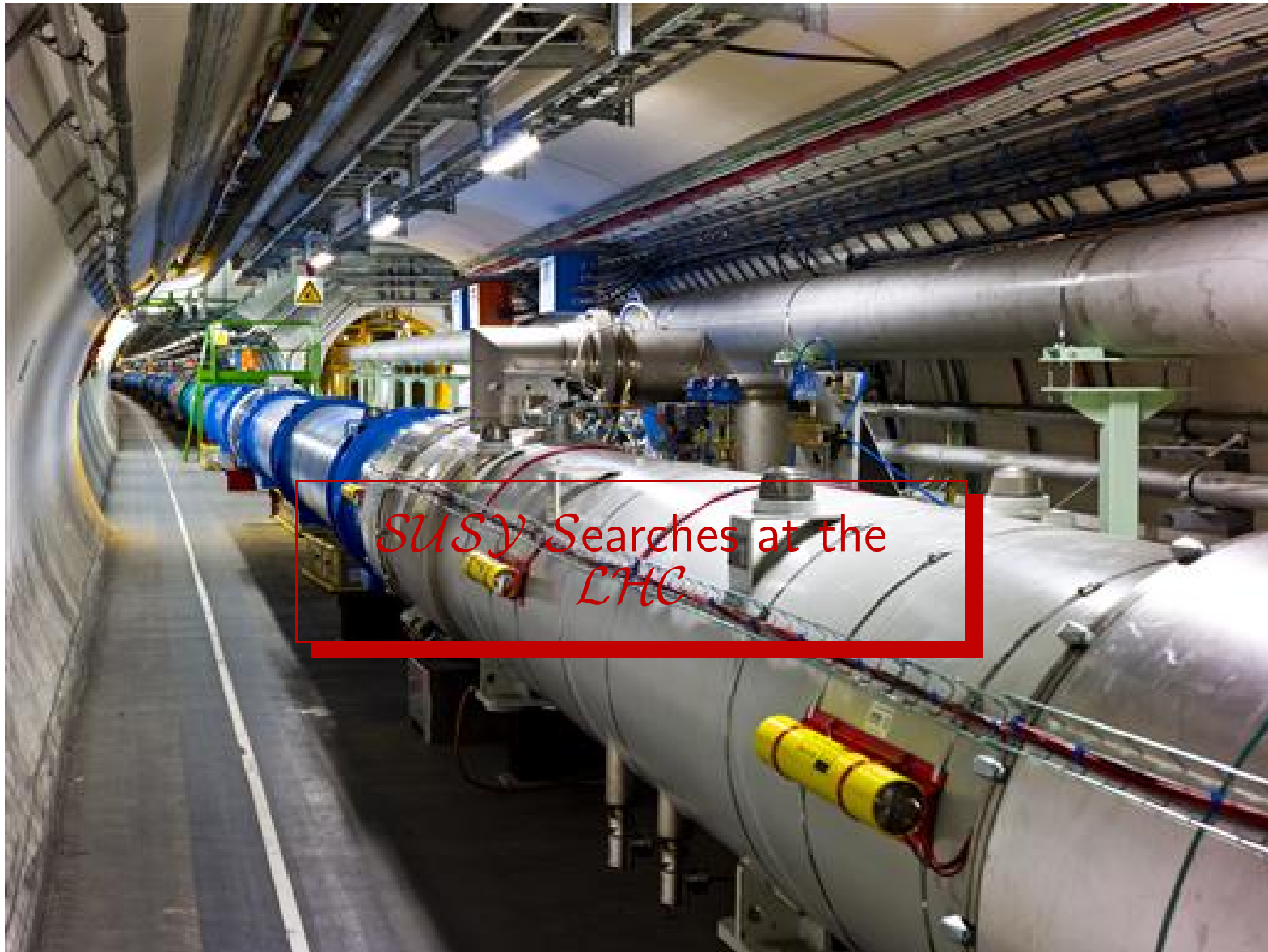


## (VII) LHC Search for SUSY Particles

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# Supersymmetry

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# Large Hadron Collider LHC

Circular collider for hadrons at CERN, LHC is a discovery machine

## Most important parameters

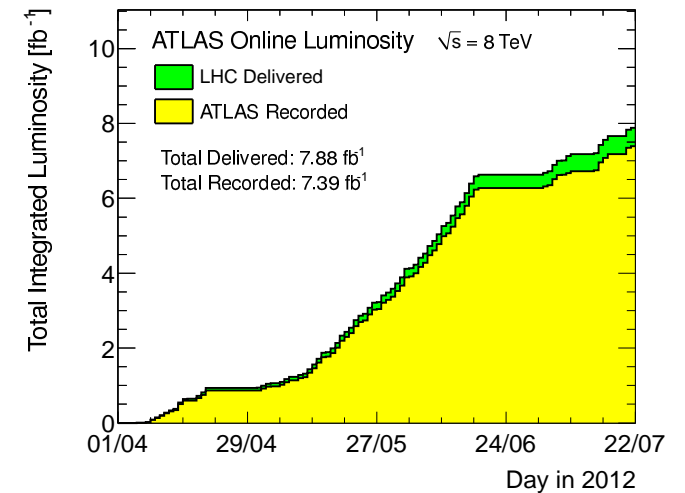
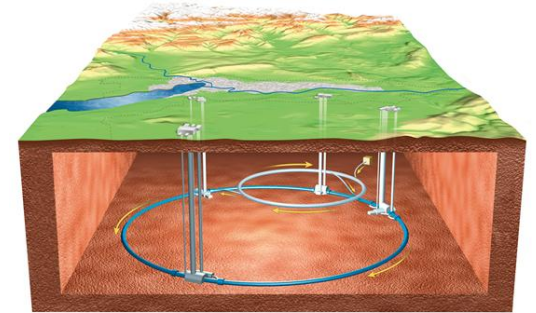
|                     |                        |
|---------------------|------------------------|
| Circumference       | 26,659 km              |
| Colliding particles | Protons and heavy ions |
| Design $\sqrt{s}$   | 14 TeV/Protons         |

4 biggest experiments

- \* ALICE gen. purpose detector: heavy ion collisions
- \* ATLAS general purpose detector: pp collisions
- \* CMS general purpose detector: pp collisions
- \* LHCb pp collisions:  $B$ -physics

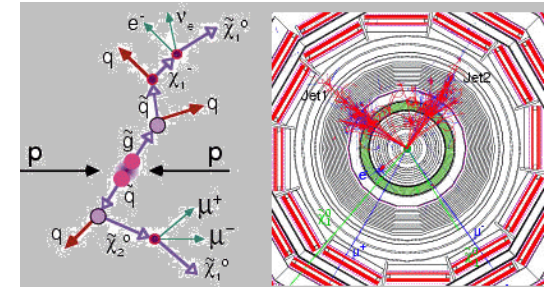
**Outstanding performance 2011/12:**  $\sqrt{s} = 7\text{TeV}$ ,  $\int \mathcal{L} = 5.6 \text{ fb}^{-1}$

**Run 2012:**  $\sqrt{s} = 8 \text{ TeV}$ , by end of 2012:  $\int \mathcal{L} = 15 \text{ fb}^{-1}$



# SUSY Search at the LHC

- **SUSY particle production:** assume R-parity conservation  $\rightsquigarrow$ 
  - ◇ SUSY particles are pair-produced
  - ◇ dominantly coloured particles  $\tilde{q}, \tilde{g}$  due to strong interactions
  - ◇ sparticles cascade decay into stable LSP ( $\tilde{\chi}_1^0$  or  $\tilde{G}$ ): escapes detection



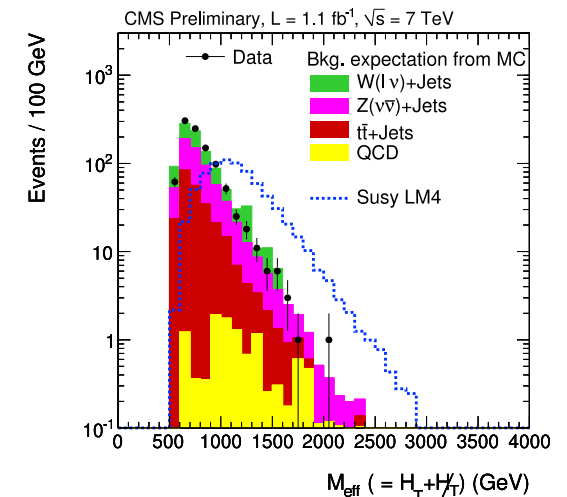
- **Signatures**

- ▷ events with  $E_T^{miss}$  and multiple high- $p_T$  jets (and leptons)
- ▷ final states distinguished through additional particles (0,1,2... leptons, 2  $\gamma$ 's,...,b-jets)

- **Signal & background**

- \* LSP escapes detection  $\rightsquigarrow$  no mass peak, smooth excess at large energies  $\Rightarrow$
- \* background control is crucial:
  - SM background extracted from control region
  - irreducible background from Monte Carlo simulations

CMS PAS-SUS-11-004



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## Interpretation of the Results

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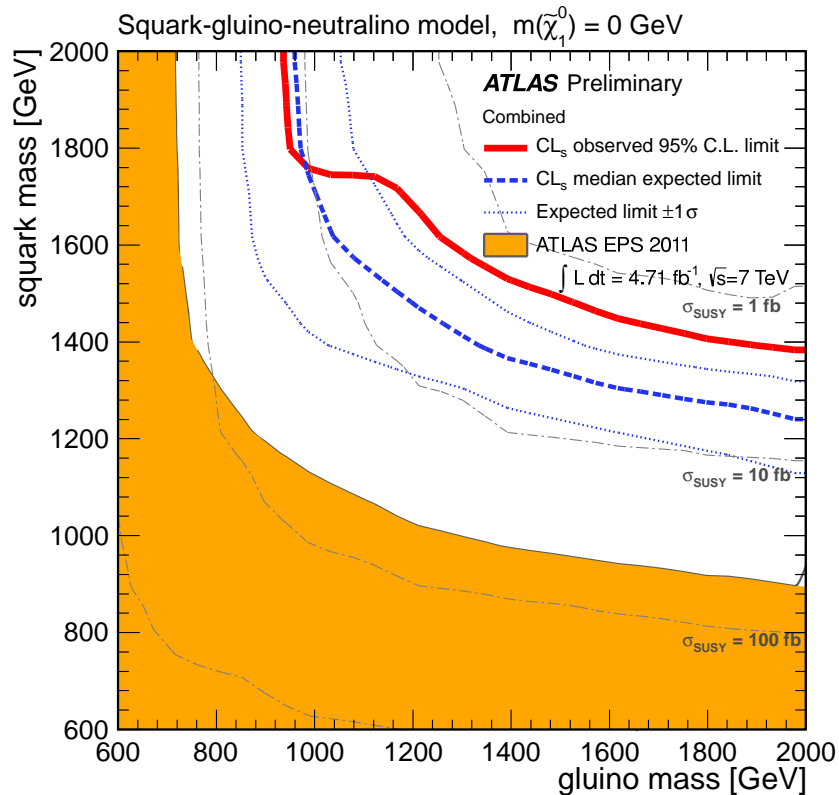
- **If no excess in signal regions**  $\rightsquigarrow$  derive exclusion limits
  - experiment: limits on number of signal events, limits on visible cross section
- **Interpretation**
  - \* Plethora of models, large number of parameters  $\Rightarrow$
  - \* Impossible to test **all models** and the **full parameter space**
  - \* **Interpretation in the framework of specific models**
    - reduce number of parameters, predict mass spectrum
    - models e.g. mSUGRA, CMSSM
  - \* **Benchmark scenarios: capture different and characteristic features of a specific model**
  - \* Compute model-independent cross section limits, translate these to model-dependent results.  $\rightsquigarrow$
  - \* **Simplified models**
    - reduce particle content and number of couplings
    - reproduce a given topological signature
    - test different mass combinations, give limit on  $\sigma_{prod}$

# Exclusion Limits in Missing $p_T$ and Jets

## Simplified Model

- limits on  $\tilde{g}$  and  $\tilde{q}$  of 1st and 2nd generation
- massless  $m_{\tilde{\chi}_1^0}$
- all other SUSY particles assumed to be very heavy

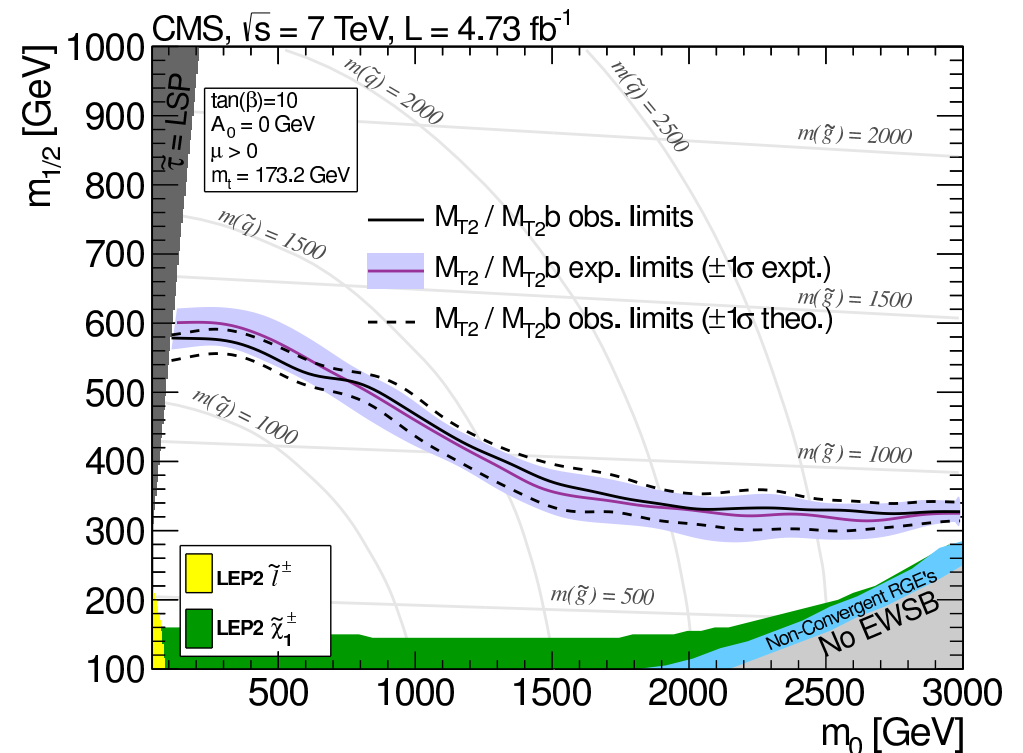
ATLAS-CONF-2012-033



## mSUGRA/CMSSM

assume mSUGRA SUSY breaking mechanism  
 few parameters:  $M_0, M_{1/2}, A_0, \tan \beta, \text{sgn} \mu$

CMS PAS-SUS-12-002



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## Beyond Squark/Gluino Searches

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- **First searches: squark-gluino mediated SUSY production**

- ▷ large  $\sigma_{prod}$
- ▷ rich final state phenomenology

- **More  $\int \mathcal{L} \rightsquigarrow$  sensitivity to more exclusive production modes**

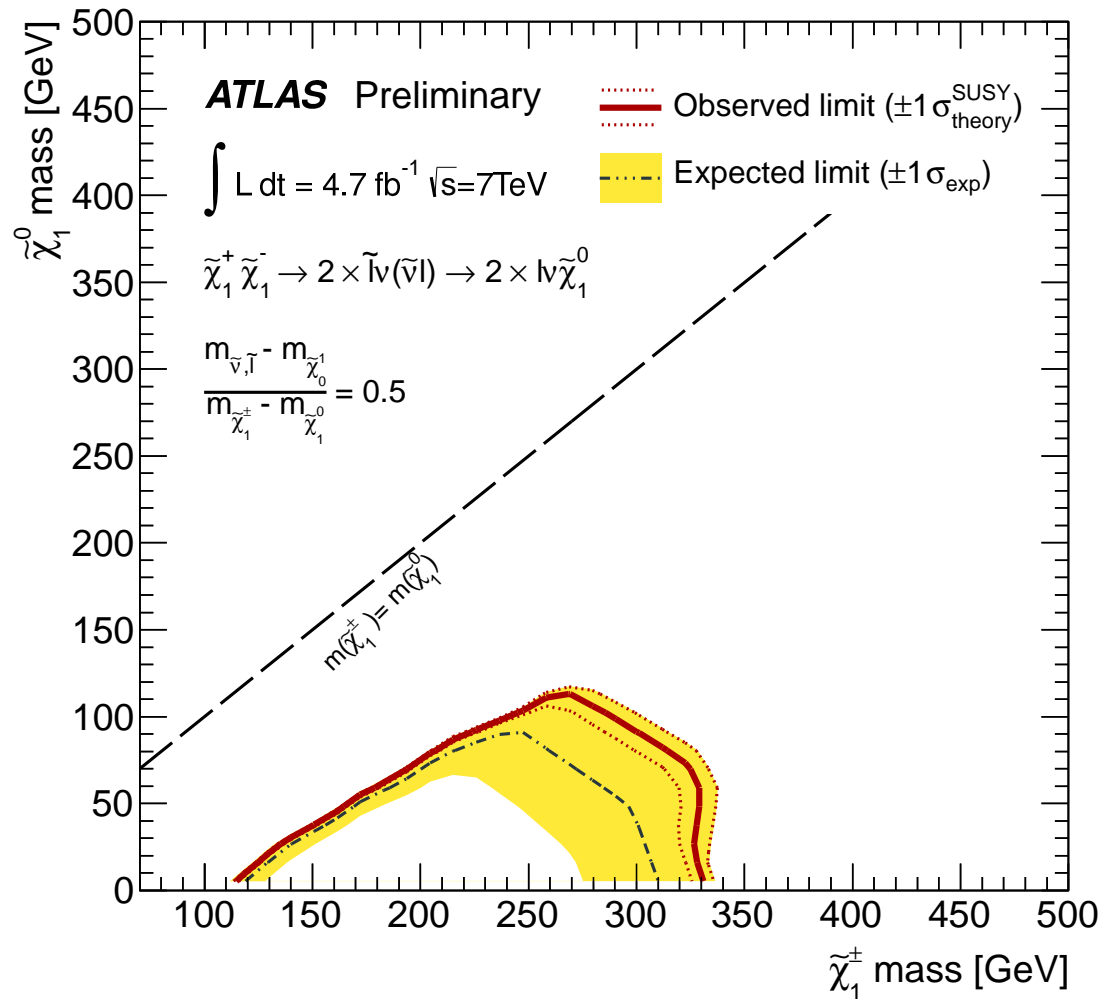
- ▷ electroweak chargino/neutralino production
- ▷ direct sbottom and stop production

# Electroweak Multilepton Production

Slepton or chargino pair production

Example chargino pair production:  $pp \rightarrow \tilde{\chi}^\mp \tilde{\chi}^\pm \rightarrow 2 \times \tilde{l}\nu(\tilde{\nu}l) \rightarrow 2 \times l\nu\tilde{\chi}_1^0$

ATLAS CONF-2012-076



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## Squarks of Third Generation - $\mathcal{S}$ bottom

---

- Squarks of third generation are special:

- ▷ should be light for SUSY naturalness
- ▷ mixing can make stops, sbottoms, staus much lighter than squarks of 1st, 2nd generation  
→ dedicated experimental searches for third generation squarks

- Example: sbottom production

- from gluino decays:  $pp \rightarrow \tilde{g}\tilde{g} \rightarrow (b\tilde{b}_1)(b\tilde{b}_1) \rightarrow (bb\tilde{\chi}_1^0)(bb\tilde{\chi}_1^0)$
- direct production:  $pp \rightarrow \tilde{b}_1^*\tilde{b}_1 \rightarrow (\tilde{\chi}_1^0 b)(\tilde{\chi}_1^0 \bar{b})$

- Simplified 'gluino-sbottom' model (0-lepton)

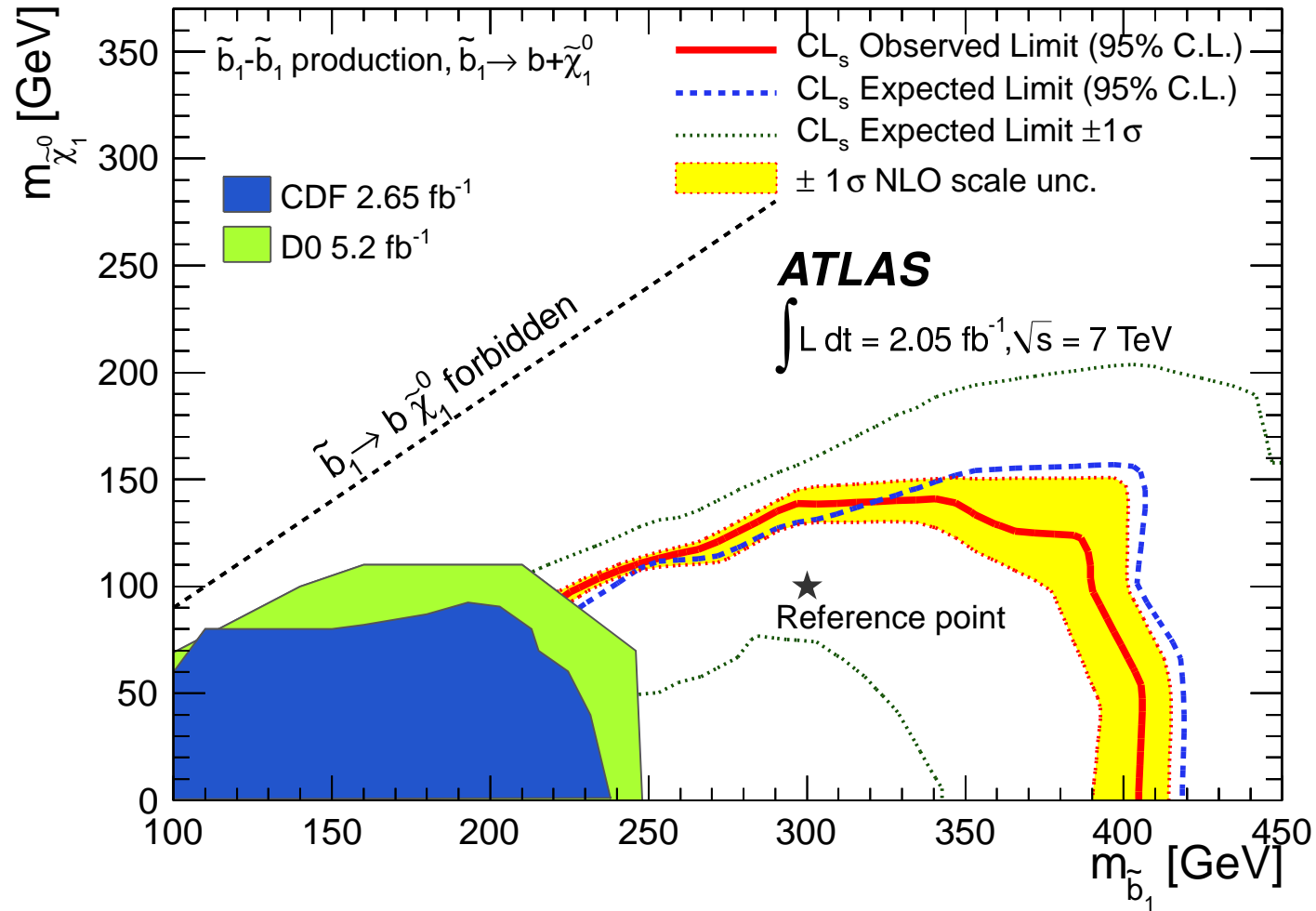
→ T

- $\tilde{b}_1$  lightest squark, all other squarks heavier than  $\tilde{g}$
- $m_{\tilde{g}} > m_{\tilde{b}_1} > m_{\tilde{\chi}_1^0} \rightsquigarrow BR(\tilde{g} \rightarrow \tilde{b}_1 b) = 1$
- sbottom production via  $\tilde{g}\tilde{g}$  and  $\tilde{b}_1\tilde{b}_1$  and  $BR(\tilde{b}_1 \rightarrow b\tilde{\chi}_1^0) = 1$

# Squarks of Third Generation - $\tilde{S}$ bottom

Simplified 'gluino-sbottom model'

ATLAS arXiv:1112.3832





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## Squarks of *Third Generation* - *Stop*

---

- **Exclusion limits on Squarks of 3rd generation are much weaker**

- **Light Stop  $\tilde{t}_1$**

- \* arises naturally from renormalization-group running
- \* large top Yukawa coupling  $\rightsquigarrow$  large mass splitting  $\rightsquigarrow$  light  $\tilde{t}_1$
- \* provides natural solution to finetuning problem
- \* light stop favoured by Baryogenesis

Carena eal; de Carlos, Espinosa; Huet,  
Nelson; Delepine eal; Losada; Cirigliano eal

- **Production** in  $\tilde{g}$  decays or direct  $\tilde{t}\tilde{t}$  production

---

## Stop Production at the $\mathcal{LHC}$

---

- **Example: Stop production**

- **Model assumptions (dilepton final state)**

→ T

- $\tilde{t}_1$  lightest squark, all other squarks heavier than 2 TeV
- direct stop pair production via  $\tilde{t}_1\tilde{t}_1$  and  $BR(\tilde{t}_1 \rightarrow b\tilde{\chi}_1^\pm) = 1$
- $m_{\tilde{\chi}_1^0} > 45$  GeV and  $m_{\tilde{\chi}_1^\pm} = 106$  GeV
- $BR(\tilde{\chi}_1^\pm \rightarrow \tilde{\chi}_1^0 l^\pm \nu) = 0.11$

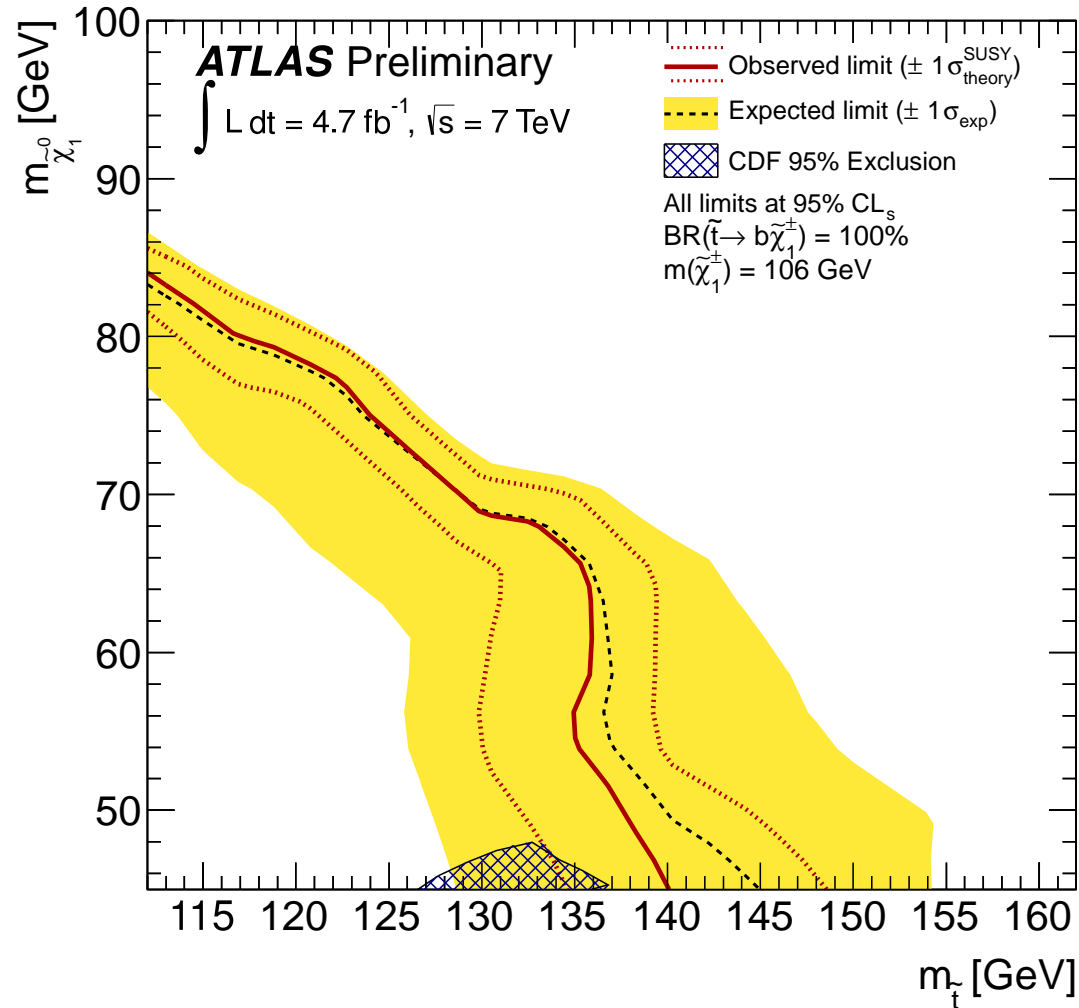
- **Production in this model:**

- direct production:

$$pp \rightarrow \tilde{t}_1\tilde{t}_1 \rightarrow (\tilde{\chi}_1^- \bar{b})(\tilde{\chi}_1^+ b) \rightarrow (W^{-(*)} \tilde{\chi}_1^0 \bar{b})(W^{+(*)} \tilde{\chi}_1^0 b) \rightarrow (l^- \nu \tilde{\chi}_1^0 \bar{b})(l^+ \nu \tilde{\chi}_1^0 b)$$

# Stop Production at the $\mathcal{LHC}$

ATLAS CONF-2012-059



Exclusion of  $m_{\tilde{t}_1} \lesssim 130 \text{ GeV}$  for  $m_{\tilde{\chi}_1^0} \lesssim 65 \text{ GeV}$

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# No Sign of SUSY

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Altarelli: *'The situation is depressing but not desperate.'*

Experimentalists: *'SUSY is simply not just around the corner.'*

Think of e.g.

- **Compressed SUSY:** suppressed  $\tilde{g}, \tilde{q}$  masses *i.e.*  $m_{\tilde{\chi}_1^0} \approx m_{\tilde{g}} \approx m_{\tilde{q}} \rightsquigarrow \tilde{q}, \tilde{g}$  difficult to detect  $\rightsquigarrow$  limits on  $\tilde{q}, \tilde{g}$  much weaker S.P.Martin'07
- **Split SUSY:** only light particles are  $\tilde{g}, \tilde{\chi}_i^0, \tilde{\chi}_j^\pm$  and  $\tilde{q}, \tilde{l}$  are very heavy;  $\tilde{\chi}_i^0, \tilde{\chi}_j^\pm$  difficult to access at the LHC,  $\tilde{g}$  is long-lived Wells;Arkani-Hamed,Dimopoulos;Giudice,Romanino
- **Long-lived SUSY** ( $\rightarrow$  R-parity violation): slowly moving particles, decays outside the detectors
- **Invisible SUSY:** only  $\tilde{\chi}_1^0$  accessible at LHC  $\rightsquigarrow$  monojet events

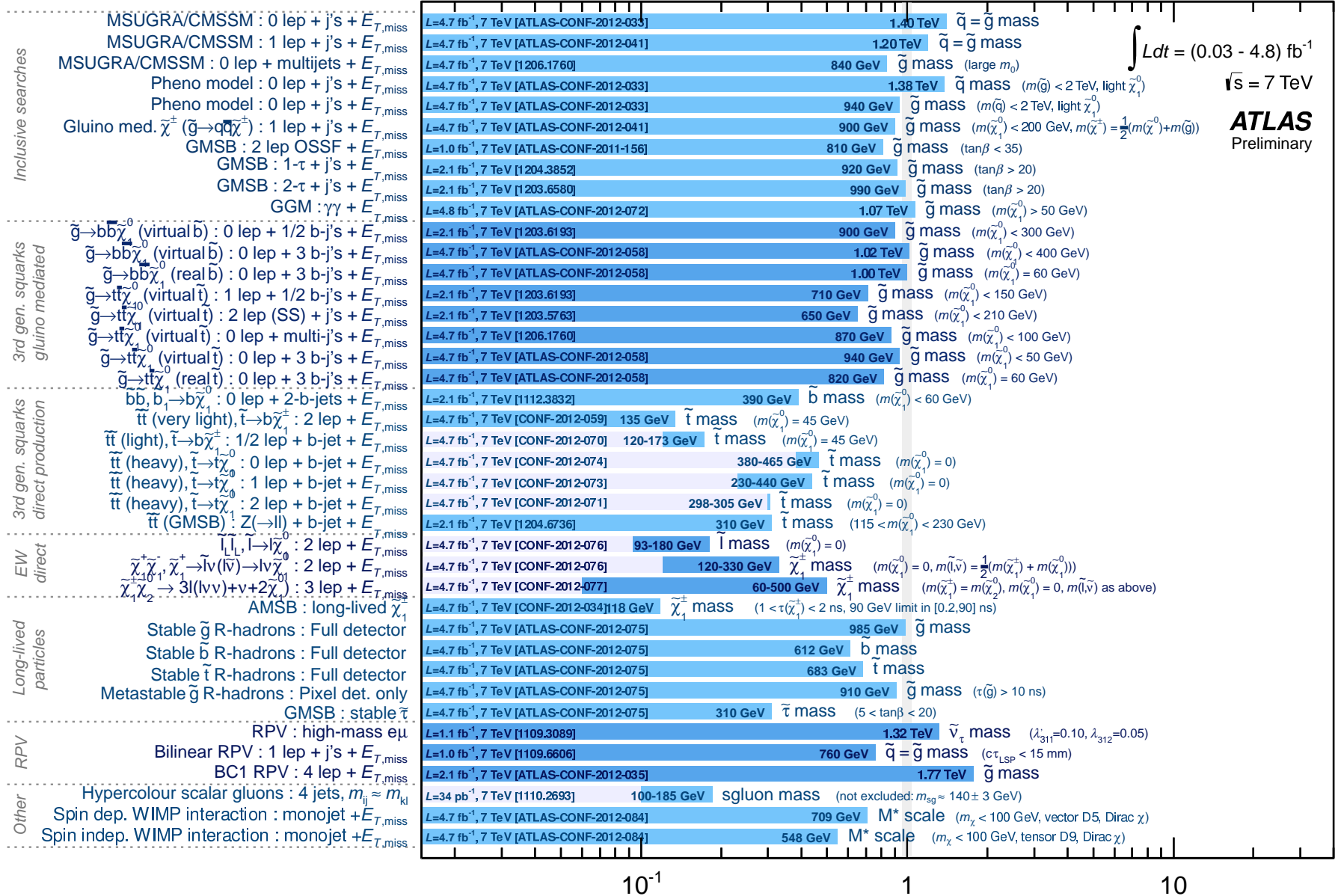
SUSY may hide very well!

- Still plenty of room for SUSY to hide.
- 2012 will provide more data.
- Experimentalists will turn around every stone!



# Summary *SUSY* Searches - ATLAS

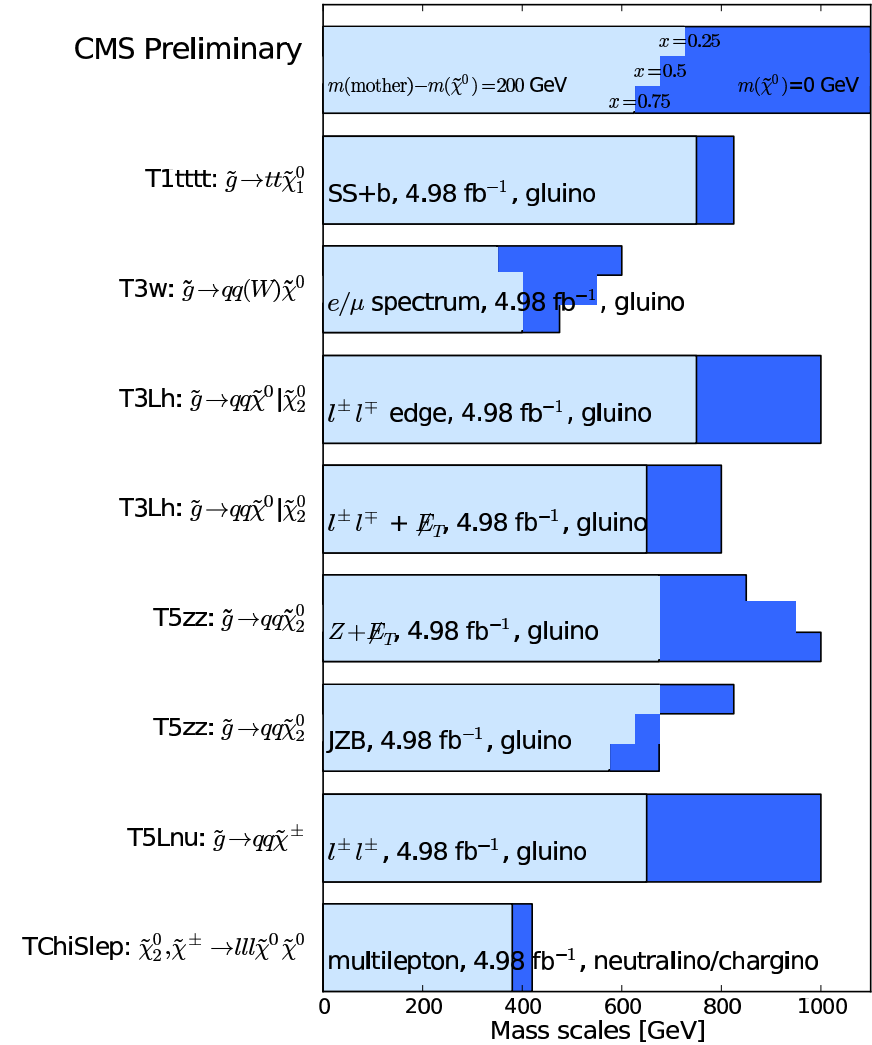
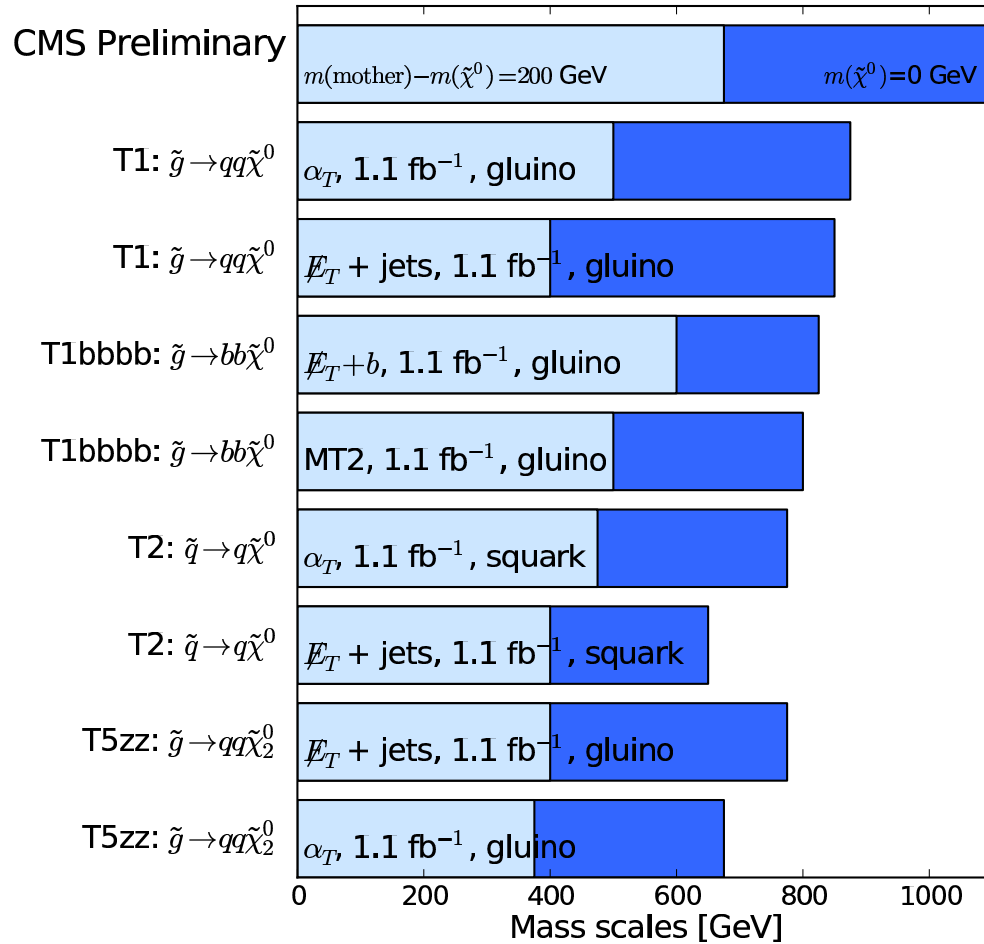
ATLAS SUSY Searches\* - 95% CL Lower Limits (Status: ICHEP 2012)



\* Only a selection of the available mass limits on new states or phenomena shown

Mass scale [TeV]

# Summary *SUSY* Searches - CMS



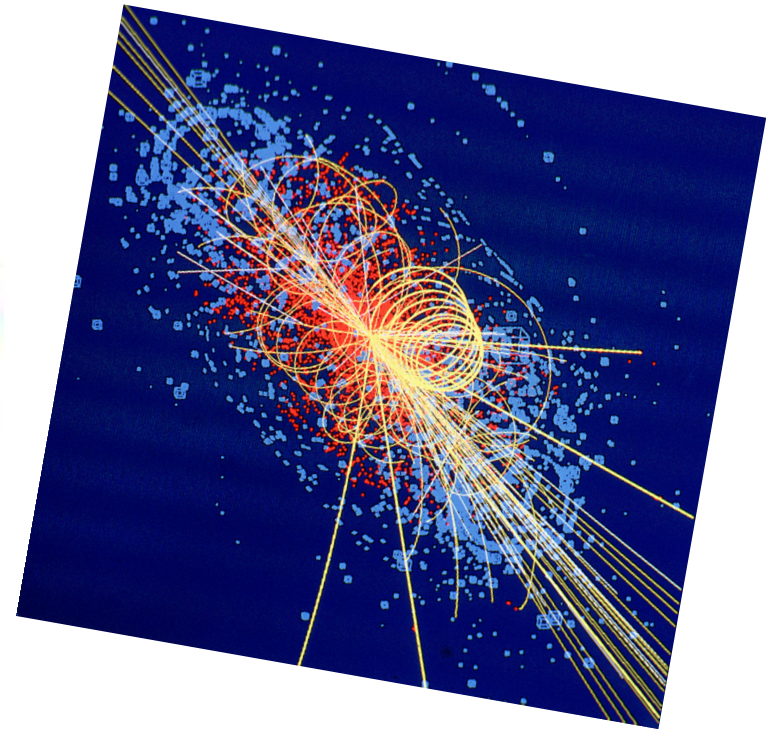
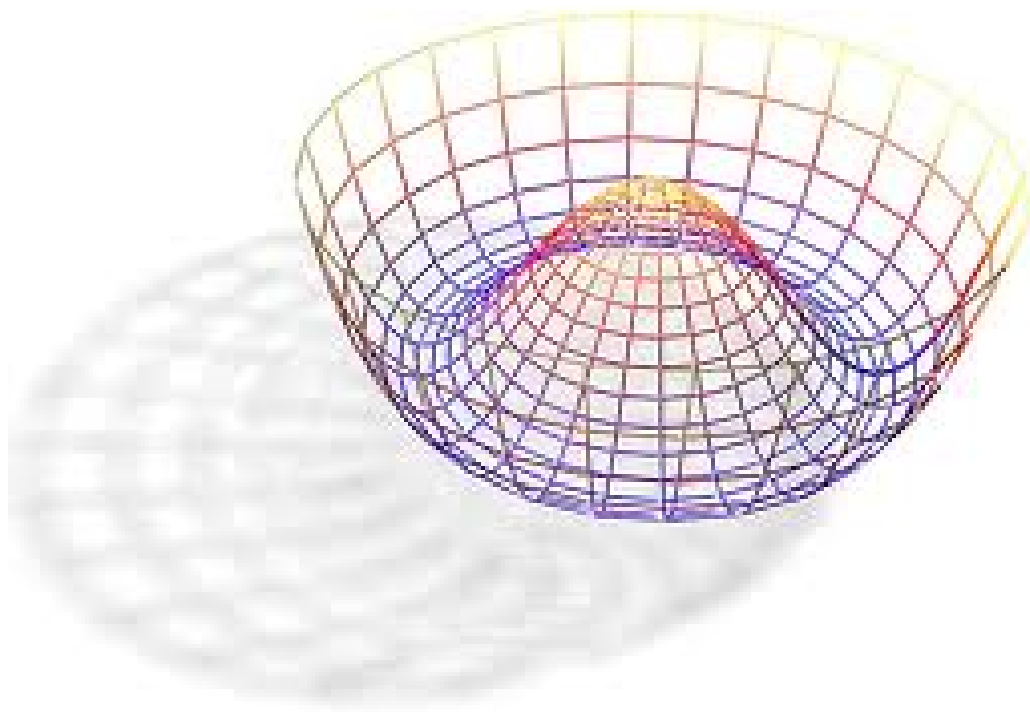
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# *Electroweak Symmetry Breaking ( $\mathcal{EWSB}$ ) and $\mathcal{LHC}$*

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Margarete Mühlleitner  
(KIT)

CALC 2012, Dubna, July/August 2012



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# Outline

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- **Introduction Higgs mechanism**  
**Standard Model Higgs Sector**
- **Experimental Verification of the Higgs Mechanism**  
**First Step: Higgs Searches**
- **MSSM Higgs Sector (Brief)**
- **Composite Higgs Sector**
- **Model-independent fits to SM Higgs Search Results**



# (I) Introduction Higgs Mechanism and Standard Model Higgs Sector

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## Electroweak Symmetry Breaking (*EW*SB)

---

**Why?** explain existence of massive particles consistently with the underlying symmetries of the SM

**How?** Higgs mechanism [SM, SUSY, ...]  
strong EW symmetry breaking [LH, “Higgsless”, extra Dims., ...]

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## From $WW$ Scattering to the Higgs Boson

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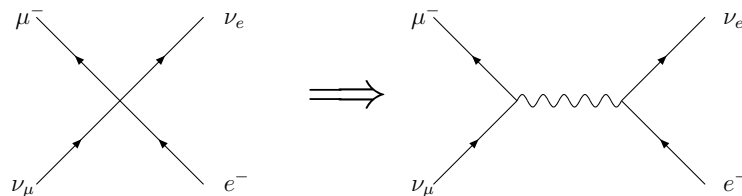
- **Fermi theory:** describes weak interaction with an effective Lagrangian

E.g.  $\mu$  decay:  $\mu^- \rightarrow e^- \bar{\nu}_e \nu_\mu$

$$\mathcal{L} = \frac{G_F}{\sqrt{2}} [\bar{\nu}_\mu \gamma_\lambda (1 - \gamma_5) \mu] [\bar{e} \gamma^\lambda (1 - \gamma_5) \nu_e]$$

$$G_F \approx 1.17 \times 10^{-5} \text{ GeV}^{-2} \text{ (Fermi coupling)}$$

- **Fermi theory at high energies:**  $\mathcal{M}[\nu_\mu e^- \rightarrow \mu^- \nu_e] \sim \frac{G_F}{2\sqrt{2}\pi} s \Rightarrow$  violates unitarity



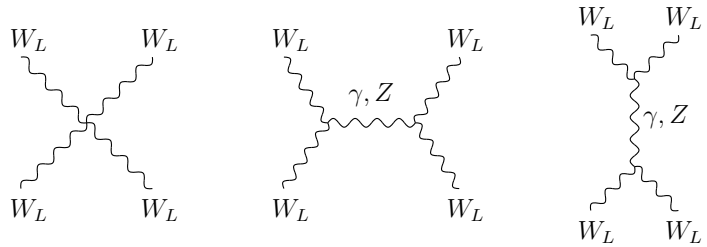
$$\mathcal{M}[\nu_\mu e^- \rightarrow \mu^- \nu_e] \rightarrow \frac{G_F s}{2\sqrt{2}\pi} \frac{M_W^2}{M_W^2 - s} \quad (\text{with } M_W \approx 100 \text{ GeV})$$

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# The Higgs Particle as $UV$ Regulator

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- Scattering of longitudinally polarized  $W$  bosons



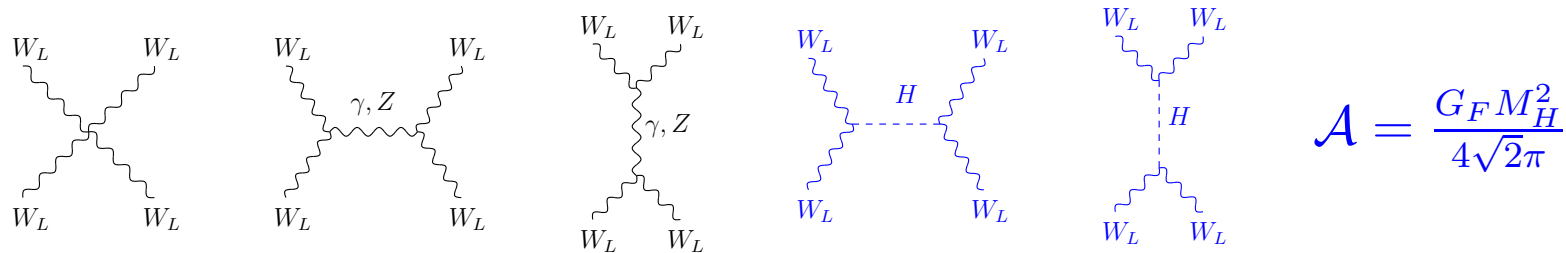
$$\mathcal{A} = \frac{G_F s}{8\pi\sqrt{2}}$$

---

# The Higgs Particle as UV Regulator

---

- Scattering of longitudinally polarized  $W$  bosons



Higgs particle guarantees unitarity of the  $W$  scattering

(if its mass  $\lesssim 1$  TeV,  $g_{XXH} \sim$  particle mass  $M_X$ ; also unitarity in  $WW \rightarrow hh$ ,  $WW \rightarrow ff$ )

A theory with massive gauge bosons and fermions, which is weakly coupled up to very high energies, requires, because of the demand for unitarity, the existence of a Higgs particle.

The Higgs particle is a scalar  $0^+$  particle, which couples to other particles with a coupling proportional to the mass of the particle.

---

## Electroweak Symmetry Breaking (EWSB)

---

**Goal: generate  $W$  and  $Z$  boson masses without violating gauge invariance. Toy model:**

▷ Local  $U(1)$  gauge theory with single spin-1 gauge field  $A_\mu$

$$\mathcal{L} = -\frac{1}{4}F_{\mu\nu}F^{\mu\nu} \quad \text{where} \quad F_{\mu\nu} = \partial_\mu A_\nu - \partial_\nu A_\mu$$

→ mass term  $\sim m^2 A^\mu A_\mu$  not gauge invariant  $\rightsquigarrow$  massless gauge boson  $A$

▷ Possible solution: add complex scalar field  $\phi$  ( $D_\mu = \partial_\mu - ieA_\mu$ )

$$\mathcal{L} = -\frac{1}{4}F_{\mu\nu}F^{\mu\nu} + |D_\mu\phi|^2 - V(\phi) \quad \text{where} \quad V(\phi) = \mu^2|\phi|^2 + \lambda|\phi|^4$$

if  $\mu^2 > 0$ : unique minimum at  $\phi = 0$  → QED with  $M_A = 0$  and  $M_\phi = \mu$

▷ Reverse sign of  $\mu^2$  so that  $V(\phi) = -\mu^2|\phi|^2 + \lambda|\phi|^4$

→ minimum of the potential at  $\sqrt{-\frac{\mu^2}{2\lambda}} \equiv \frac{v}{\sqrt{2}}$

▷ Expand  $\phi$  around the vacuum expectation value  $v$ :  $\phi = \frac{1}{\sqrt{2}}(v + H + i\chi) \Rightarrow$

---

## Electroweak Symmetry Breaking ( $\mathcal{EWSB}$ )

---

$$\begin{aligned}\mathcal{L} = & -\frac{1}{4}F_{\mu\nu}F^{\mu\nu} + \frac{1}{2}\partial_\mu H\partial^\mu H + \frac{1}{2}\partial_\mu\chi\partial^\mu\chi + \frac{1}{2}e^2v^2A_\mu A^\mu + evA^\mu\partial_\mu\chi \\ & -eA^\mu(\chi\partial_\mu H - H\partial_\mu\chi) + \frac{1}{2}e^2A_\mu A^\mu(H^2 + \chi^2) - \underbrace{(-\mu^2)}_{\frac{1}{2}m_H^2}H^2 + \text{interaction}(H^3, H^4)\end{aligned}$$

▷ The theory has now

- a photon of mass  $M_A = ev$
- a scalar field  $H$  with  $M_H^2 = -2\mu^2 > 0$
- a massless scalar field  $\chi$  (Goldstone boson)

▷ Mixed  $A - \chi$  propagator: can be removed by a gauge transformation

$$A_\mu \rightarrow A_\mu - \frac{1}{ev}\partial_\mu\chi \text{ and } \phi \rightarrow e^{-i\frac{\chi}{v}}\phi \text{ (unitary gauge)}$$

↪ the  $\chi$  field has been absorbed by a redefinition of  $A$   
(jargon:  $\chi$  has been “eaten” to give the photon mass)

▷ Degrees of freedom:

before symmetry breaking: massless gauge boson (2 dof) and complex scalar field (2 dof)  
after symmetry breaking: massive gauge boson (3 dof) and physical scalar (1 dof)

---

## The SM Higgs Sector

---

- Add complex Higgs doublet to  $\mathcal{L}$

$$\Phi = \begin{pmatrix} \phi^+ \\ \phi^0 \end{pmatrix} \quad \text{with} \quad \langle \Phi \rangle = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ v \end{pmatrix} \quad \text{and} \quad v = 246 \text{ GeV}$$

- Lagrangian of the Higgs doublet

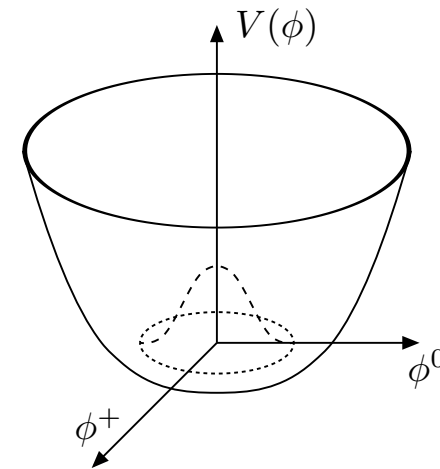
$$\mathcal{L}_\Phi = D_\mu \Phi D^\mu \Phi^\dagger - V(\Phi)$$

- The Higgs potential:

$$V(\Phi) = \lambda \left[ \Phi^\dagger \Phi - \frac{v^2}{2} \right]^2$$

The minimum of the potential is at  $v = 246 \text{ GeV}$

$\rightsquigarrow$  spontaneous symmetry breaking (SSB)





---

## The SM Higgs Sector

---

- Higgs field in the unitary gauge

$$\Phi = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ v+H \end{pmatrix} \Rightarrow$$

$$V(H) = \frac{1}{2} M_H^2 H^2 + \frac{M_H^2}{2v} H^3 + \frac{M_H^2}{8v^2} H^4$$

- $\Rightarrow$  Higgs mass and self-couplings:

|   |  |
|---|--|
| Higgs boson mass  | $M_H = \sqrt{2\lambda}v$                 |
| Trilinear coupling<br>[units $\lambda_0 = 33.8 \text{ GeV}$ ] | $\lambda_{HHH} = 3 \frac{M_H^2}{M_Z^2}$  |
| Quartic coupling<br>[units $\lambda_0^2$ ]                    | $\lambda_{HHHH} = 3 \frac{M_H^2}{M_Z^4}$ |

Higgs self-couplings in the SM  
uniquely determined by the Higgs mass!

# (II) Experimental Verification of the Higgs Mechanism

## First Step: Higgs Searches

# Electroweak Symmetry Breaking (EWSB)

**Why?** explain existence of massive particles consistently with the underlying symmetries of the SM

**How?** Higgs mechanism [SM, SUSY, ...]  
strong EW symmetry breaking [LH, “Higgsless”, extra dims., ...]

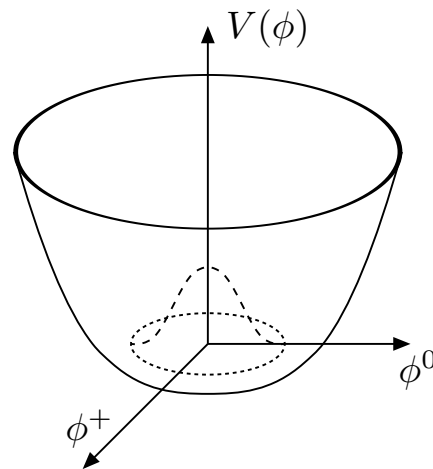
## Higgs mechanism

### Symmetry of the Lagrangian

$$SU(2)_L \times U(1)_Y$$

Higgs doublet

$$\Phi = \begin{pmatrix} H^+ \\ H^0 \end{pmatrix}$$



$$V(\Phi) = \lambda \left[ \Phi^\dagger \Phi - \frac{v^2}{2} \right]^2$$

### Symmetry of the vacuum

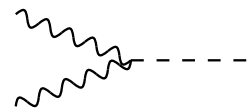
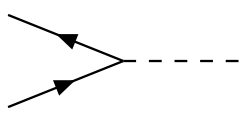
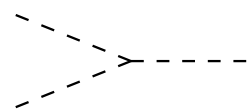
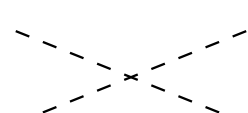
$$U(1)_{em}$$

vacuum expectation value

$$\langle \Phi \rangle = \begin{pmatrix} 0 \\ \frac{v}{\sqrt{2}} \end{pmatrix}$$

$$v = 246 \text{ GeV}$$

# The SM Higgs Sector

|   |   |  |
|---|---|--|
| Higgs boson mass  | $M_H = \sqrt{2\lambda}v$                |  |
| Gauge couplings   | $g_{VVH} = \frac{2M_V^2}{v}$            |   |
| Yukawa couplings  | $g_{ffH} = \frac{m_f}{v}$               |   |
| Trilinear coupling<br>[units $\lambda_0 = 33.8 \text{ GeV}$ ] | $\lambda_{HHH} = 3\frac{M_H^2}{M_Z^2}$  |   |
| Quartic coupling<br>[units $\lambda_0^2$ ]                    | $\lambda_{HHHH} = 3\frac{M_H^2}{M_Z^4}$ |  |

Only unknown parameter in the SM is the Higgs boson mass!

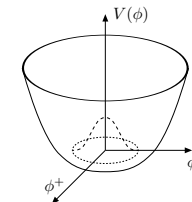
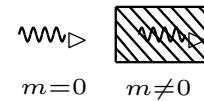
# Next Steps in Experimental Verification of the Higgs Mechanism

## Higgs mechanism:

Creation of particle masses without violating gauge symmetries

### Test of the Higgs mechanism

- Discovery –  $m$
- Interaction with a scalar Higgs with  $v = 246 \text{ GeV} \neq 0$   $\rightsquigarrow g_{HXX} \sim m_X$
- Spin and parity quantum numbers –  $J^{PC}$
- EWSB requires Higgs potential –  $\lambda_{HHH}, \lambda_{HHHH}$



Would require another lecture!

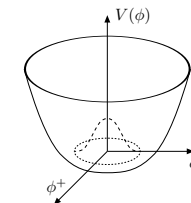
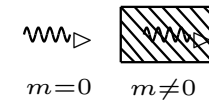
# Experimental Verification of the Higgs Mechanism

## Higgs mechanism:

Creation of particle masses without violating gauge symmetries

### Test of the Higgs mechanism

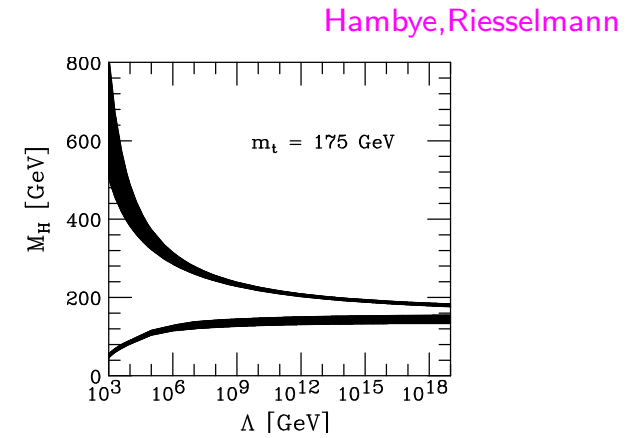
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- Interaction with a scalar Higgs  
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## SM Higgs Mass Limits

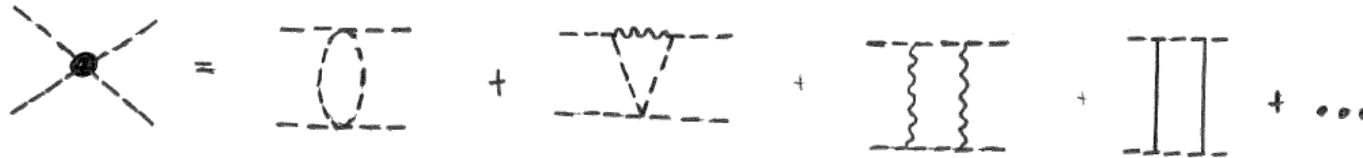
- Triviality → upper limit Cabibbo,...;Sher;  
Lindner;Hasenfratz,...;
- Vacuum stability → lower limit Lüscher, Weisz;  
Hambye,...;...

|   |   |
|---|---|
| $\Lambda = 1 \text{ TeV} :$             | $55 \text{ GeV} \lesssim M_H \lesssim 700 \text{ GeV}$  |
| $\Lambda_{GUT} = 10^{16} \text{ GeV} :$ | $130 \text{ GeV} \lesssim M_H \lesssim 190 \text{ GeV}$ |



## Triviality Bound

- **Quantum corrections to the Higgs potential:**  $V(\Phi) = \lambda[\Phi^\dagger\Phi - \frac{v^2}{2}]^2$
- **Corrections to coupling  $\lambda$**



- **Large mass**  $\rightsquigarrow$   $\lambda$  dominated renormalisation group equation (RGE):

$$16\pi^2 \frac{d\lambda}{d \ln Q} = 24\lambda^2 \quad \Longrightarrow \quad \lambda(Q) = \frac{M_H^2}{2v^2 - \frac{3}{2\pi^2} M_H^2 \ln(Q/v)}$$

$\lambda$  increases with  $Q$

- **Landau pole**

$$\Lambda \leq v e^{4\pi^2 v^2 / 3M_H^2}$$

New Physics must appear before this point to restore stability

$\Longrightarrow$  For  $\Lambda$  fixed upper bound on  $M_H$

- **Triviality** No quantum theory for  $\Lambda \rightarrow \infty$ : trivial theory  $\lambda = 0$ .



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---

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- **Corrections to coupling  $\lambda$**

$$16\pi^2 \frac{d\lambda}{d\ln Q} = 24\lambda^2 - (3g'^2 + 9g^2 - 12y_t^2)\lambda + \frac{3}{8}g'^4 + \frac{3}{4}g'^2g^2 + \frac{9}{8}g^4 - 6y_t^4 + \text{higher order}$$

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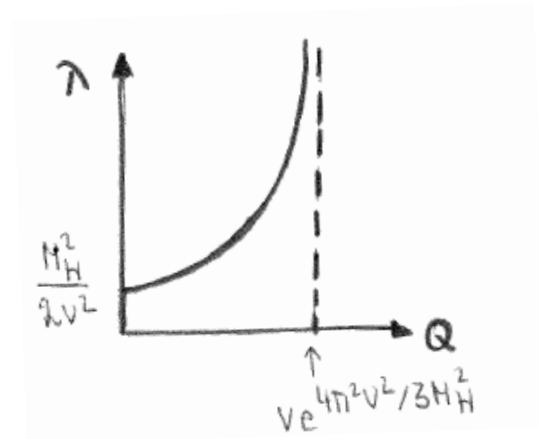
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# Vacuum Stability

- **Corrections to coupling  $\lambda$**

$$16\pi^2 \frac{d\lambda}{d \ln Q} = 24\lambda^2 - (3g'^2 + 9g^2 - 12y_t^2)\lambda + \frac{3}{8}g'^4 + \frac{3}{4}g'^2g^2 + \frac{9}{8}g^4 - 6y_t^4 + \text{higher order}$$

- **Small mass**  $\rightsquigarrow y_t$  dominated RGE:

$$16\pi^2 \frac{d\lambda}{d \ln Q} = -6y_t^4 \quad \Longrightarrow \quad \lambda(Q) = \lambda_0 - \frac{\frac{3}{8\pi^2}y_0^4 \ln \frac{Q}{Q_0}}{1 - \frac{9}{16\pi^2}y_0^2 \ln \frac{Q}{Q_0}}$$

$\lambda$  decreases with  $Q$ ;  $\lambda < 0 \rightsquigarrow$  potential unbounded from below

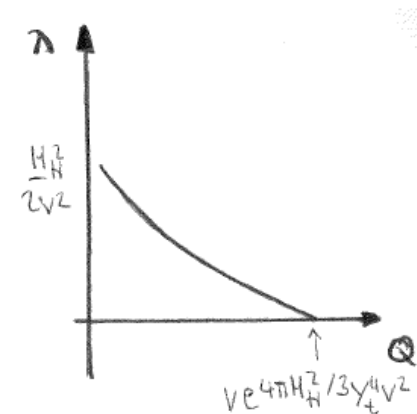
$$\lambda = 0 \text{ for } \lambda_0 \approx \frac{3}{8\pi^2} y_0^4 \ln \frac{Q}{Q_0}$$

- **Vacuum stability**

$$\Lambda \leq v e^{4\pi^2 M_H^2 / 3y_t^4 v^2}$$

New Physics must appear before this point to ensure vacuum stability

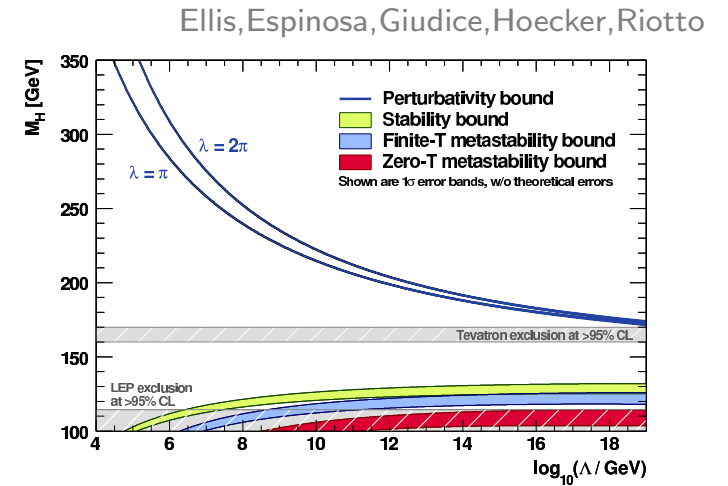
$\Longrightarrow$  For  $\Lambda$  fixed lower bound on  $M_H$



# SM Higgs Mass Constraints

- Triviality → upper bound Cabibbo,...; Sher; Lindner; Hasenfratz,...;
- Vacuum stability → lower bound Lüscher, Weisz; Hambye,...;...

|   |   |
|---|---|
| $\Lambda = 1 \text{ TeV} :$             | $55 \text{ GeV} \lesssim M_H \lesssim 700 \text{ GeV}$  |
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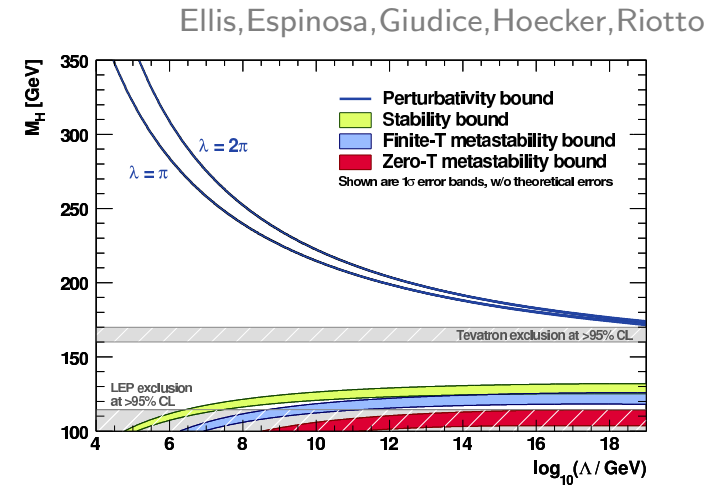


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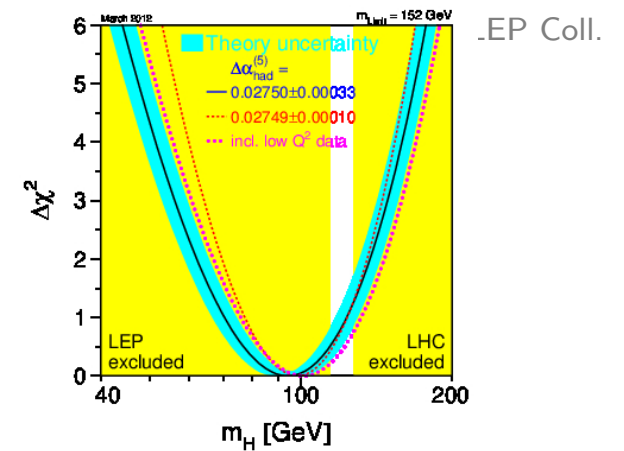
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- Fits to electroweak precision data

$$M_H = 94_{-24}^{+29} \text{ GeV}, \quad M_H \lesssim 171 \text{ GeV} @ 95\% \text{ CL}$$

EWWG



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## Precision Tests of the Standard Model

---

- Precision electroweak measurements, in particular at

LEP (Large Electron-Positron storage ring at CERN,  $M_Z \lesssim \sqrt{s} \lesssim 200$  GeV) and  
SLC (Stanford Linear Collider,  $\sqrt{s} = M_Z$ )

allow to test the SM at very high accuracy!

→ quantum corrections must be included

→ sensitive to energy scales beyond direct reach

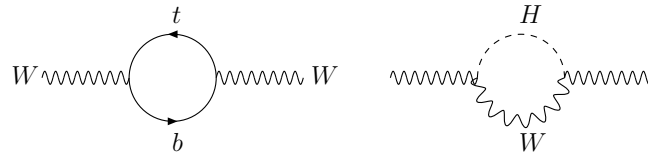
- indirect search for the Higgs

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## Indirect Search for the Higgs Boson

---

- **Quantum corrections to precision observables** give access to high mass scales:



Calculate  $M_W$  from  $M_Z$  and  $G_F$  including quantum corrections

$$\frac{M_W^2}{M_Z^2} \left( 1 - \frac{M_W^2}{M_Z^2} \right) = \frac{\pi\alpha}{\sqrt{2}G_F M_Z^2 (1 - \Delta r)}$$

where the quantum correction  $\Delta r$  is composed of

$$\Delta r = \Delta\alpha - \cot\theta_W \Delta\rho^{top} + \Delta r^{Higgs} + \dots$$

The leading top contribution is quadratic in  $m_{top}$

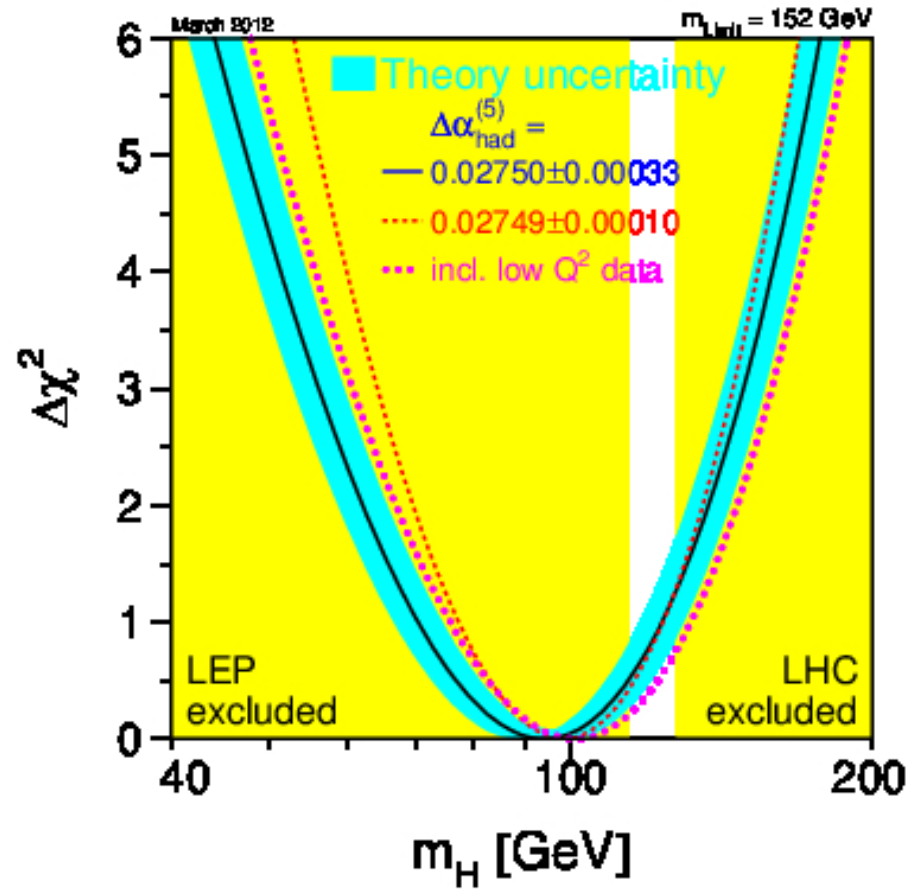
$$\Delta\rho^{top} = \frac{3G_F m_{top}^2}{8\pi^2 \sqrt{2}} + \dots$$

The Higgs contribution is screened, depending only logarithmically on  $M_H$

$$\Delta r^{Higgs} = \frac{G_F M_W^2}{8\pi^2 \sqrt{2}} \frac{1+9\sin^2\theta_W}{3\cos^2\theta_W} \ln\left(\frac{M_H^2}{M_W^2}\right) + \dots$$

# Higgs Mass from Combined Fit to $\mathcal{E}WPD$

LEPEWWG



Minimum at:  $M_H = 94^{+29}_{-24}$  GeV,  $M_H \lesssim 171$  GeV @ 95% CL

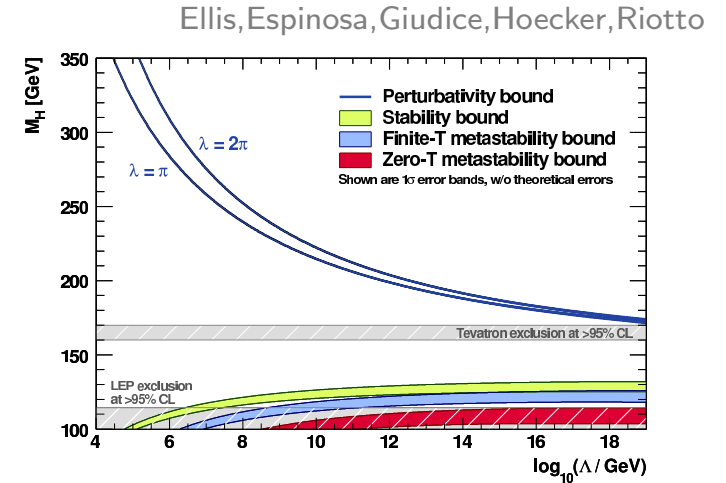


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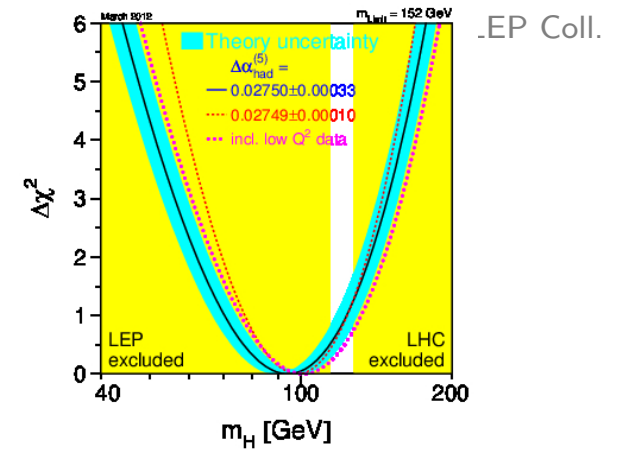
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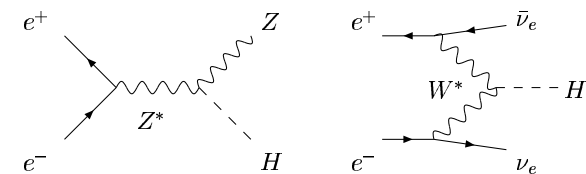
EWWG



- Direct search @ LEP: [ $M_H = 115.3 \text{ GeV}$ ]

$$M_H > 114.4 \text{ GeV @ 95% CL}$$

LEP Coll.

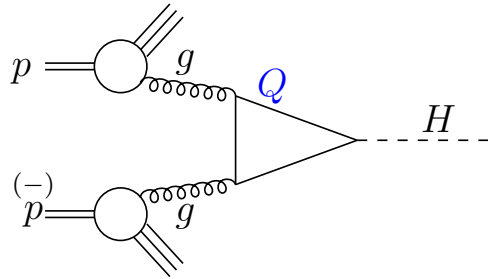


# Higgs Search at the $\mathcal{LHC}$

## Higgs boson production in the SM

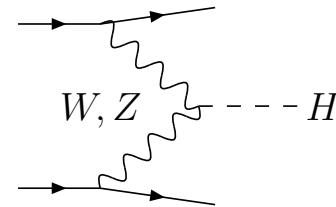
- **Gluon Fusion**

$$pp \rightarrow gg \rightarrow H$$



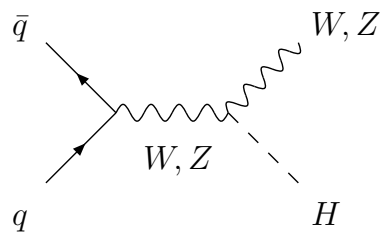
- **W/Z Fusion**

$$pp \rightarrow qq \rightarrow qq + WW/ZZ \rightarrow qq + H$$



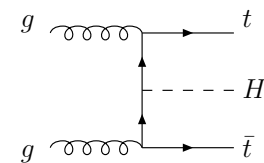
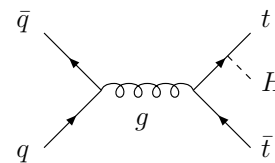
- **Higgs-strahlung**

$$pp \rightarrow W^*/Z^* \rightarrow W/Z + H$$



- **Associated Production**

$$pp \rightarrow t\bar{t} + H$$



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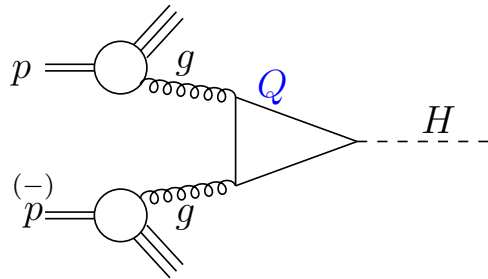
# Higgs Search at the $\mathcal{LHC}$

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## Higgs boson production in the SM

- Gluon Fusion

$$pp \rightarrow gg \rightarrow H$$

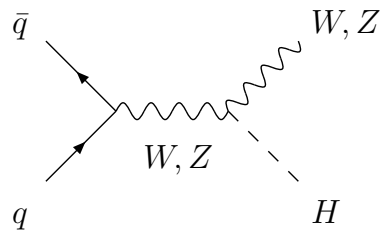


- LHC

$$gg \rightarrow \phi \quad \text{dominant}$$

- Higgs-strahlung

$$pp \rightarrow W^*/Z^* \rightarrow W/Z + H$$



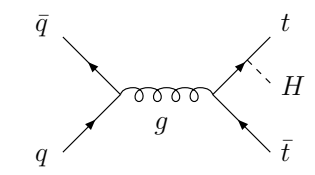
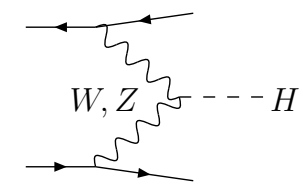
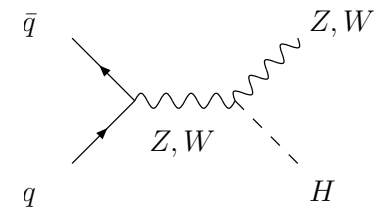
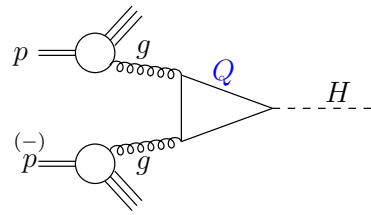
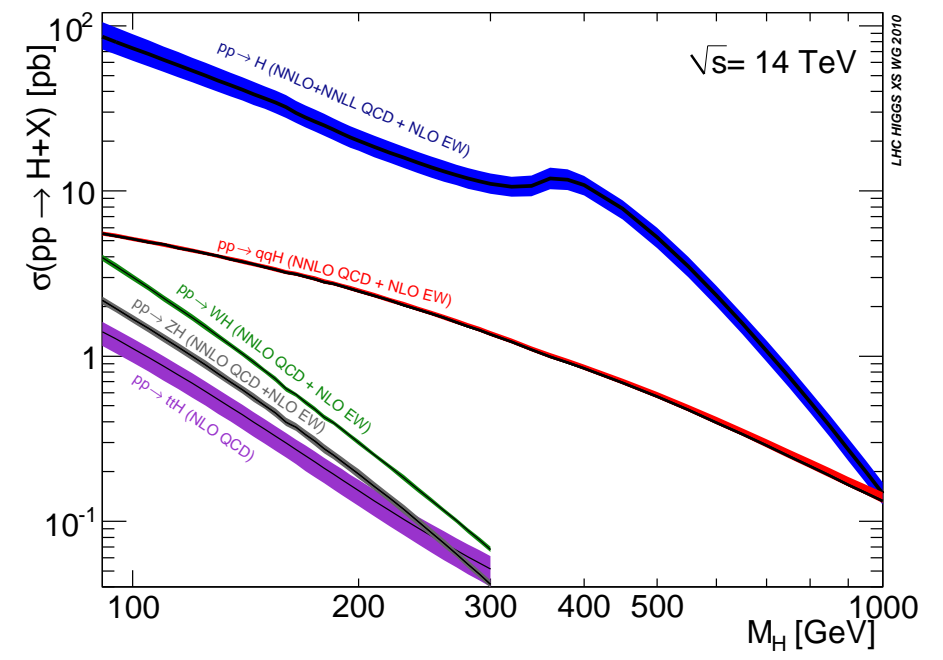
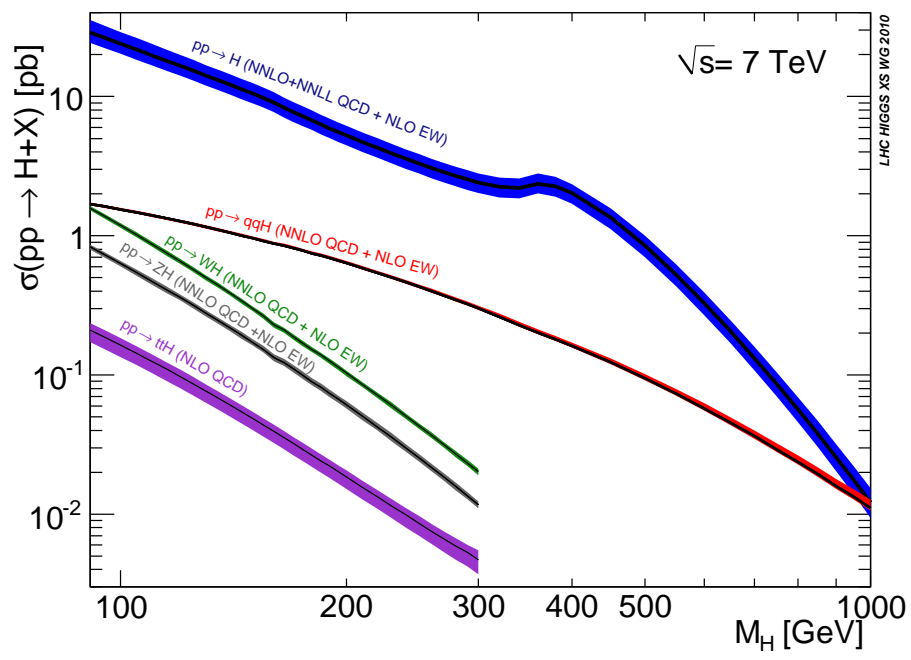
- Tevatron

$$gg \rightarrow \phi \quad \text{dominant}$$

$$q\bar{q}' \rightarrow \phi W \quad \text{most important}$$

# SM Higgs Boson Production at the LHC

LHC Higgs XS WG, arXiv:1101.0593



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## Higher Order Corrections

---

### Precision calculations needed for signal and background processes

- ◇ Higgs discovery in  $WW$  decay ← no reconstruction of the mass peak possible
- ◇ reliable extraction of the discovery/exclusion significances
- ◇ precise measurement of the Higgs couplings
- ◇ ...

⇒

- ▷ test of the Higgs mechanism
- ▷ discrimination between SM and SM extensions (e.g. SUSY)

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# Higgs Boson Decays

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- **Higgs boson coupling**  $\sim$  **particle mass**  $\rightsquigarrow$  most important decays: into heavy particles

## Fermions

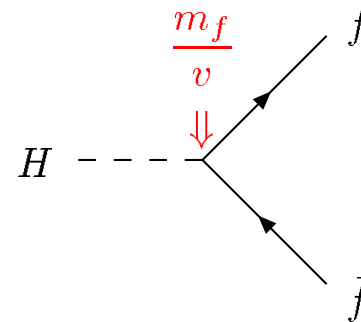
$$BR(H \rightarrow b\bar{b}) \quad \lesssim \quad 85\%$$

$$BR(H \rightarrow \tau^+\tau^-) \quad \lesssim \quad 8\%$$

$$BR(H \rightarrow c\bar{c}) \quad \lesssim \quad 4\%$$

$$BR(H \rightarrow t\bar{t}) \quad \lesssim \quad 20\%$$

large QCD corrections, up to -50%

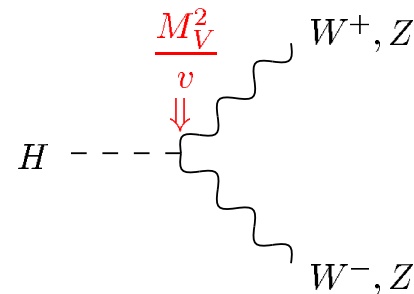


## Gauge bosons

$$BR(H \rightarrow W^+W^-) \quad \lesssim \quad 60 - 95\%$$

$$BR(H \rightarrow ZZ) \quad \lesssim \quad 30\%$$

EW corrections  $\mathcal{O}(5 - 20\%)$



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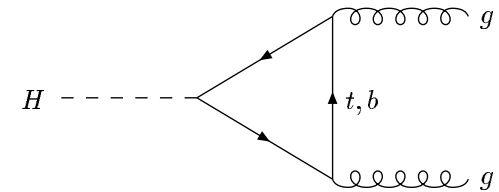
# Higgs Boson Decays

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## Gluons

$$BR(H \rightarrow gg) \lesssim 6\%$$

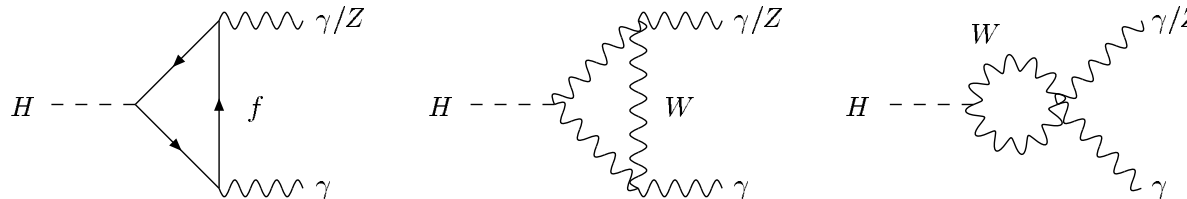
Loop-mediated decays, dominant contribution from top loops  
large QCD corrections, up to +70%



## $\gamma\gamma$ and $Z\gamma$

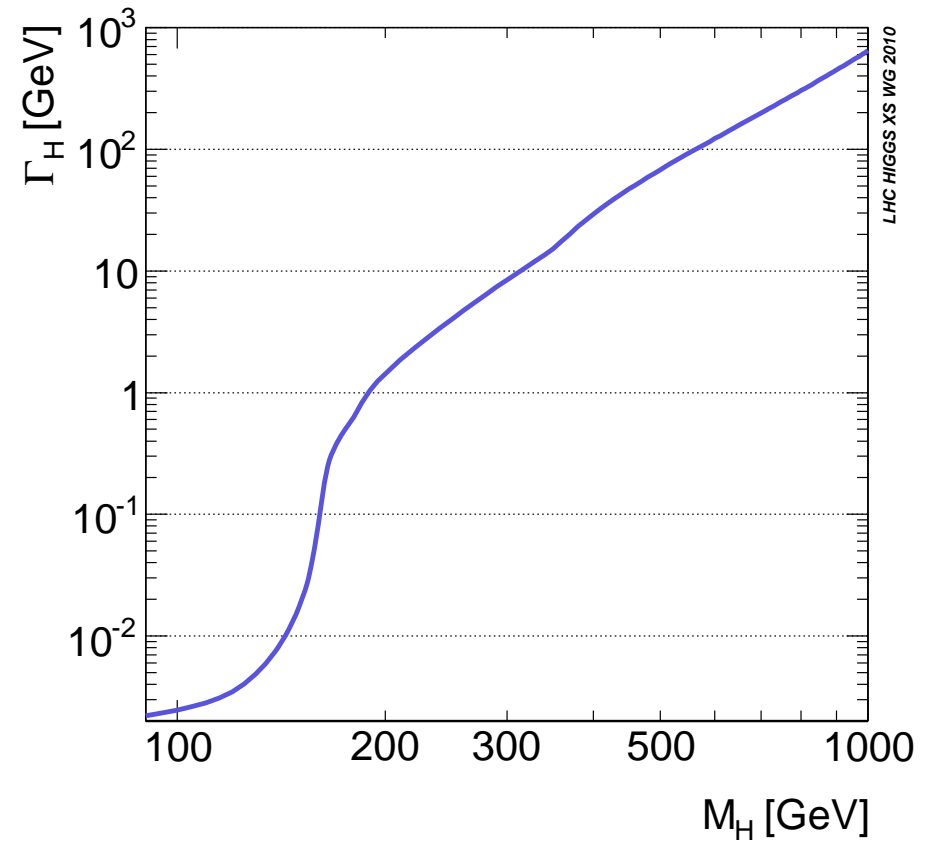
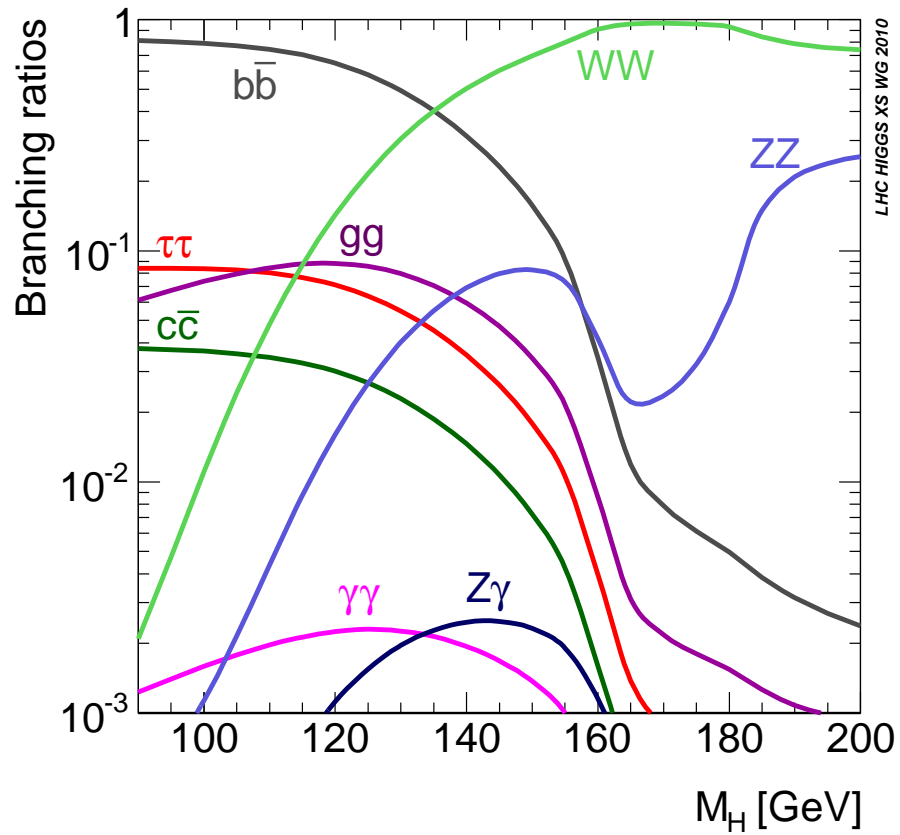
$$BR(H \rightarrow \gamma\gamma, Z\gamma) \lesssim 2 \times 10^{-3}$$

Loop-mediated decay via charged fermions and  $W$  bosons  
QCD corrections small



# Higgs Boson Decays

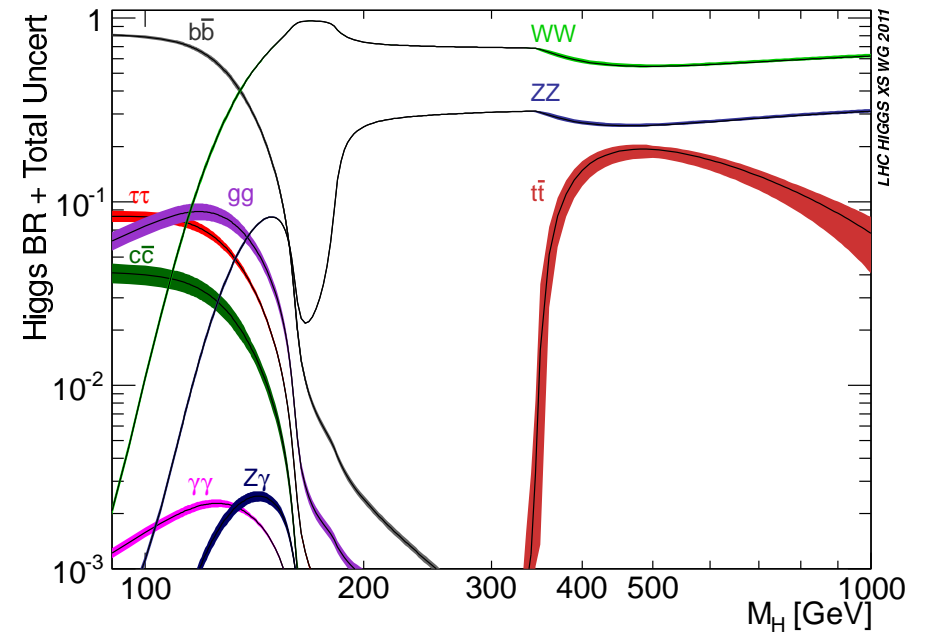
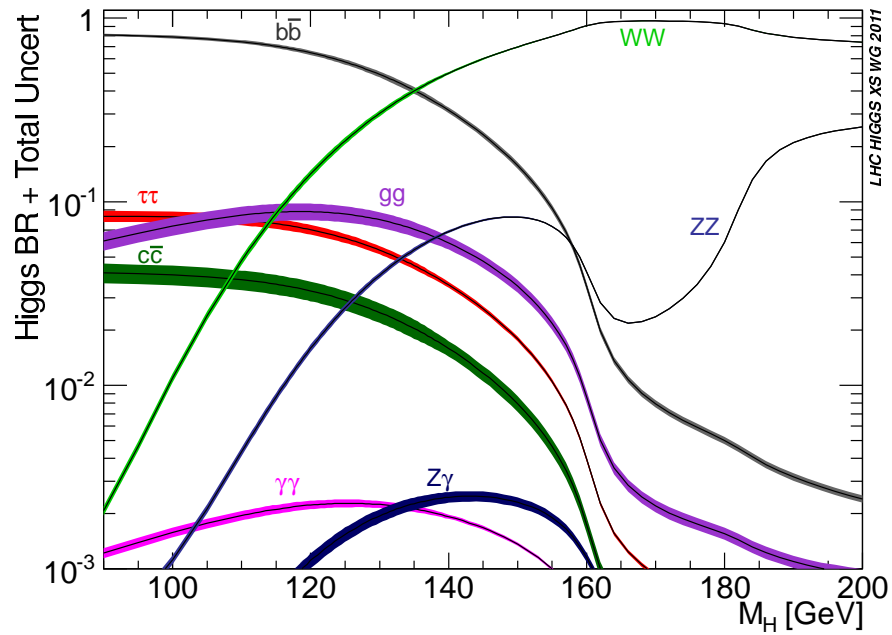
Higgs cxn working group



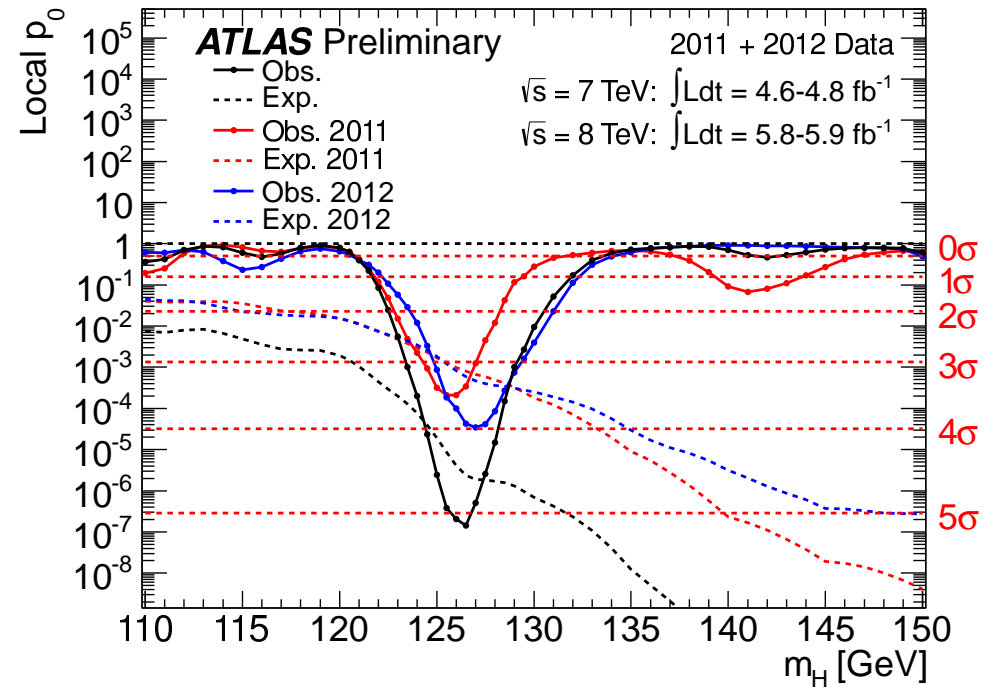
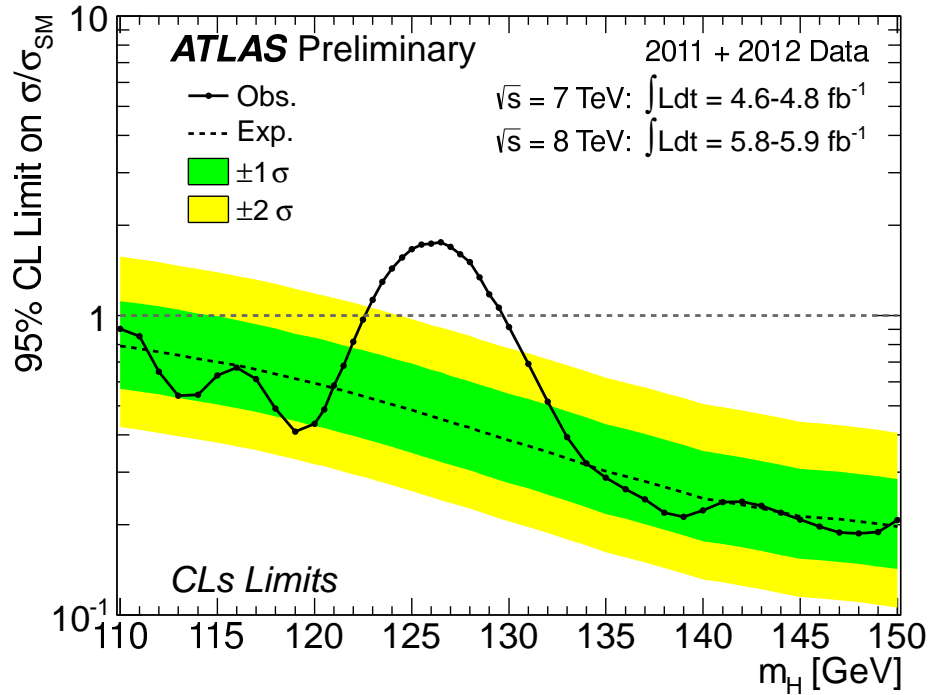


# Higgs Boson Decays

Higgs cxn working group



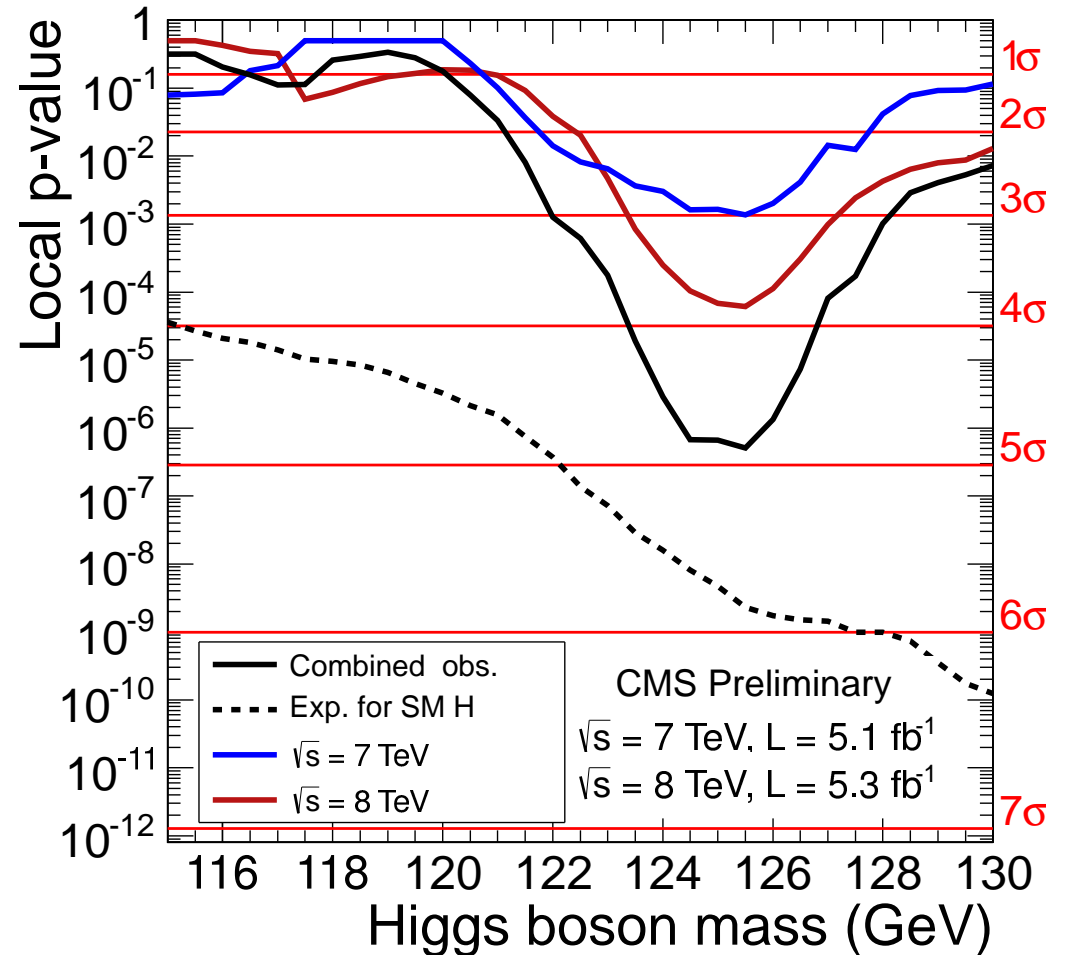
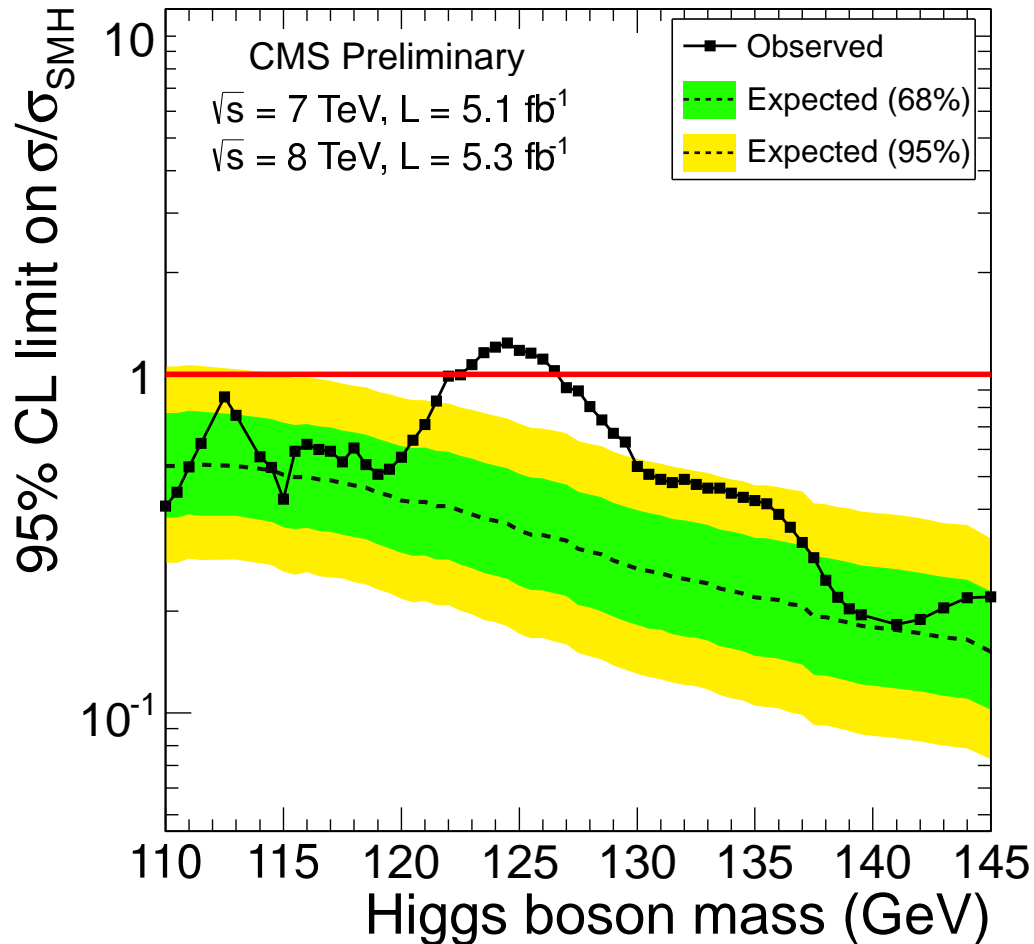
# LHC Higgs Search Results - ATLAS 4th July 2012



Observed exclusion at 95% CL: 110-122.6, 129.7-558 GeV

**Local significance of excess compatible with Higgs mass hypothesis near 126.5 GeV: 5 $\sigma$**

# LHC Higgs Search Results - CMS 4th July 2012



Observed exclusion at 95% CL: 110-122.5, 127-600 GeV

Local significance of excess compatible with Higgs mass hypothesis near 125 GeV:  $4.9\sigma$

# BSM Higgs Sectors

# The *MSSM* Higgs Sector

**MSSM Higgs sector** – supersymmetry & anomaly free theory  $\Rightarrow$  2 complex Higgs doublets

EWSB  
 $\rightarrow$

neutral, CP-even  $h, H$       neutral, CP-odd  $A$       charged  $H^+, H^-$

## Higgs masses

$$M_h \lesssim 140 \text{ GeV}$$

$$M_{A,H,H^\pm} \sim \mathcal{O}(v) \dots 1 \text{ TeV}$$

Ellis et al; Okada et al; Haber, Hempfling;  
Hoang et al; Carena et al; Heinemeyer et al;  
Zhang et al; Brignole et al; Harlander et al  
Degrassi et al; Kant et al; ...

## Decoupling limit:

$$M_A \sim M_H \sim M_{H^\pm} \gtrsim v$$

$M_h \rightarrow$  max. value,  $\tan\beta$  fixed;  $h$  becomes SM-like

**Modified couplings with respect to the SM:** (decoupling limit Gunion, Haber)

| $\Phi$ | $g_{\Phi u\bar{u}}$                             | $g_{\Phi d\bar{d}}$                           | $g_{\Phi VV}$                    |
|--------|---|---|----------------------------------|
| $h$    | $c_\alpha/s_\beta \rightarrow 1$                | $-s_\alpha/c_\beta \rightarrow 1$             | $s_{\beta-\alpha} \rightarrow 1$ |
| $H$    | $s_\alpha/s_\beta \rightarrow 1/\text{tg}\beta$ | $c_\alpha/c_\beta \rightarrow \text{tg}\beta$ | $c_{\beta-\alpha} \rightarrow 0$ |
| $A$    | $1/\text{tg}\beta$                              | $\text{tg}\beta$                              | 0                                |

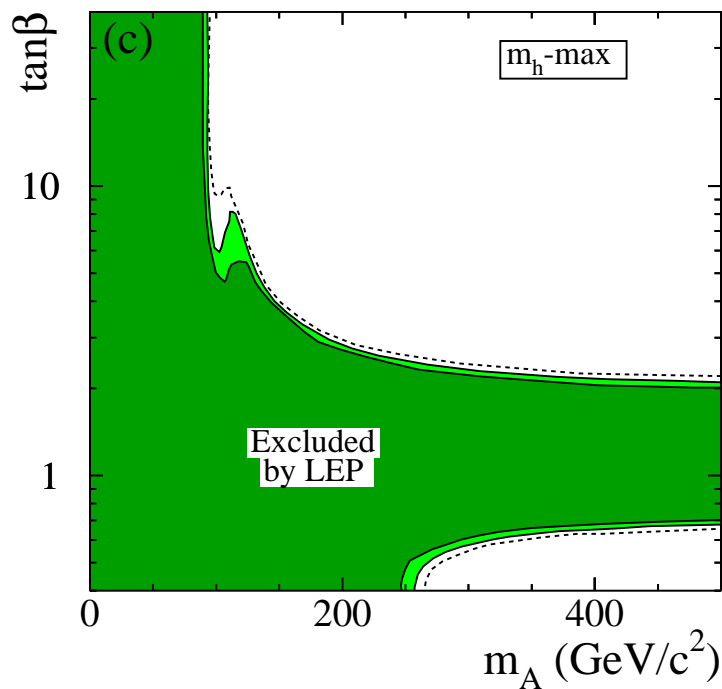
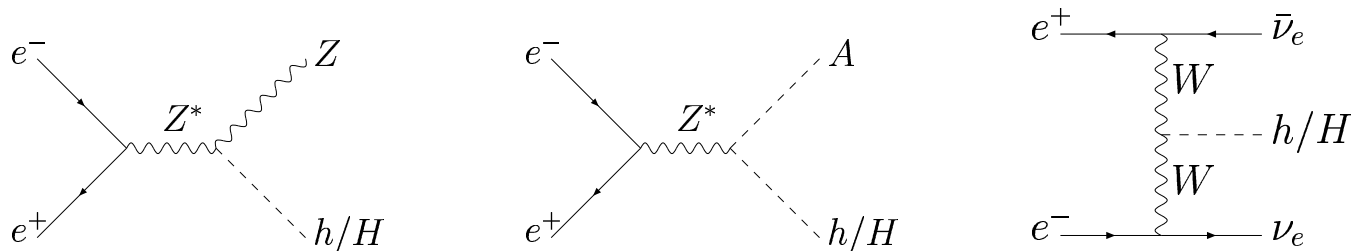
$$\tan\beta \uparrow \Rightarrow g_{\Phi uu} \downarrow$$

$$g_{\Phi dd} \uparrow$$

$$g_{\Phi VV}^{MSSM} \lesssim g_{\Phi VV}^{SM}$$

## Pre-LHC MSSM Higgs Mass Limits

▷ Direct Search at LEP  $e^+e^- \rightarrow Z + h/H, A + h/H, \nu_e\bar{\nu}_e + h/H$



$$M_{h/H} \gtrsim 92.6 \text{ GeV}$$

$$M_A \gtrsim 93.4 \text{ GeV}$$

$$M_{H^\pm} > 78.6 \text{ GeV}$$

$$0.6 < \tan \beta < 2.5 \text{ excluded}$$

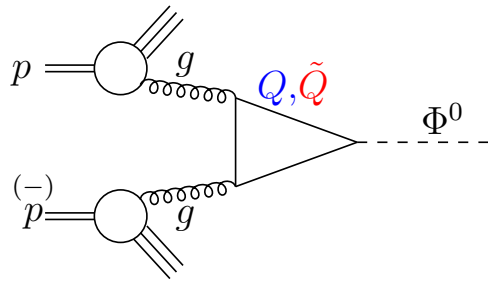
(only in this scenario,  $m_t = 174.3 \text{ GeV}$ !)

# Higgs Search at the $\mathcal{LHC}$

## Higgs boson production in the MSSM

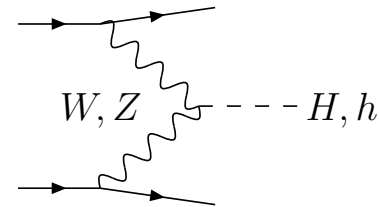
- **Gluon Fusion**

$$pp \rightarrow gg \rightarrow h, H, A$$



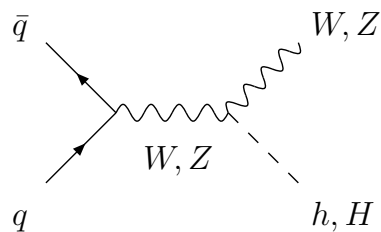
- **W/Z Fusion**

$$pp \rightarrow qq \rightarrow qq + WW/ZZ \rightarrow qq + h, H$$



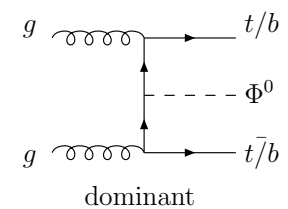
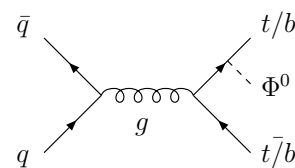
- **Higgs-strahlung**

$$pp \rightarrow W^*/Z^* \rightarrow W/Z + h, H$$



- **Associated Production**

$$pp \rightarrow t\bar{t}/b\bar{b} + h, H, A$$



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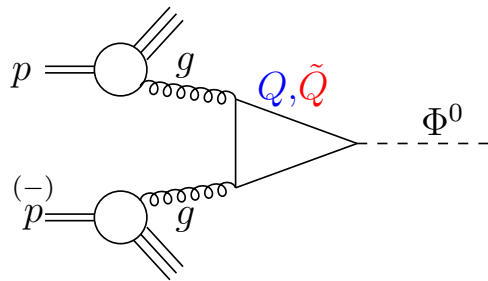
# Higgs Search at the $\mathcal{LHC}$

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## Higgs boson production in the MSSM

- Gluon Fusion

$$pp \rightarrow gg \rightarrow h, H, A$$



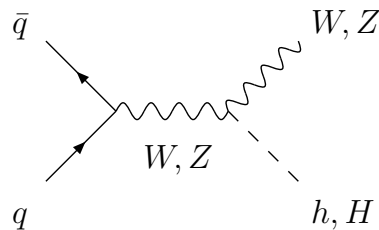
- LHC

$$gg \rightarrow \phi \quad \text{dominant for } \tan \beta \lesssim 10$$

$$gg \rightarrow \phi b \bar{b} \quad \text{dominant for } \tan \beta \gtrsim 10$$

- Higgs-strahlung

$$pp \rightarrow W^*/Z^* \rightarrow W/Z + h, H$$



- Tevatron

$$gg \rightarrow \phi \quad \text{dominant, for large } \tan \beta : \phi b \bar{b}$$

$$q \bar{q}' \rightarrow \phi W \quad \text{most important}$$

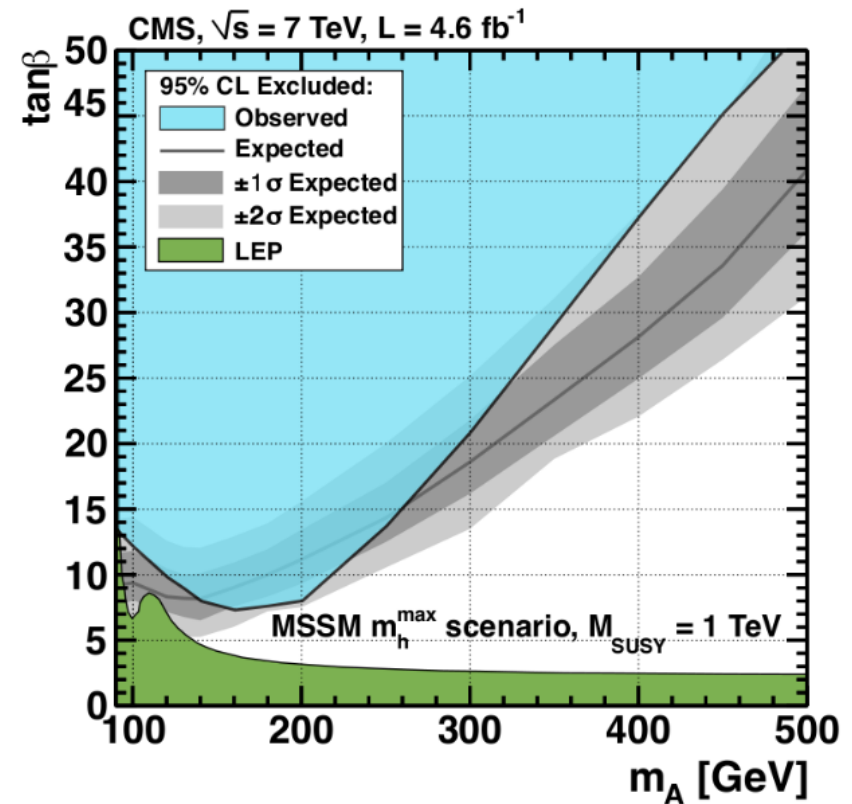
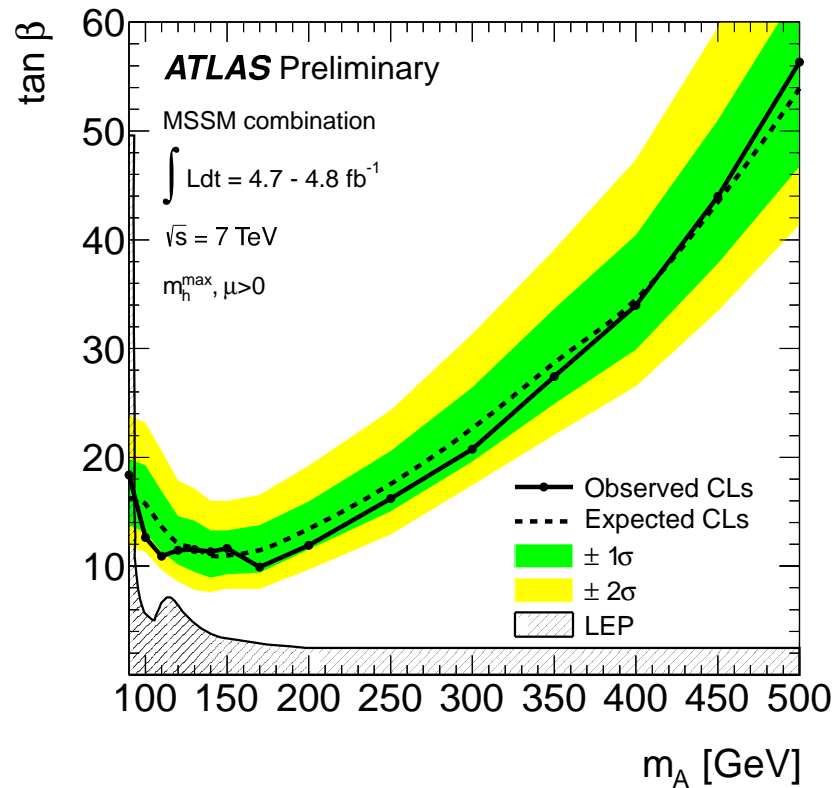


# Search for $MSSM$ Higgs Bosons at the $LHC$

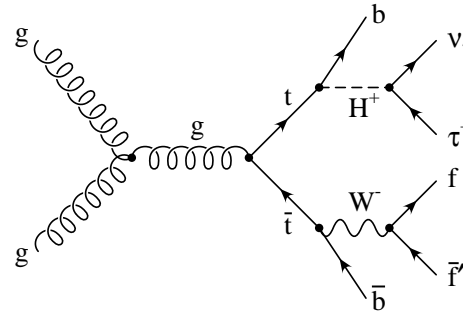
$$gg \rightarrow b\bar{b}\phi^0, \quad gg \rightarrow \phi^0, \quad \phi^0 \rightarrow \mu^+\mu^-, \quad \tau^+\tau^-$$

ATLAS-CONF-2012-094

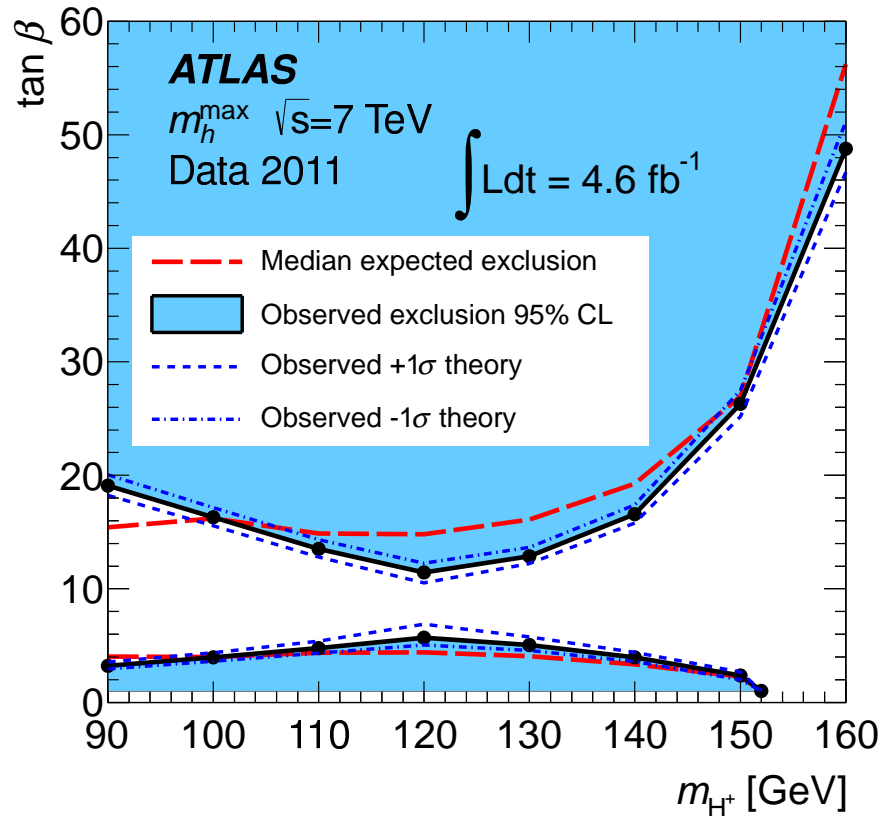
CMS 1202.4083



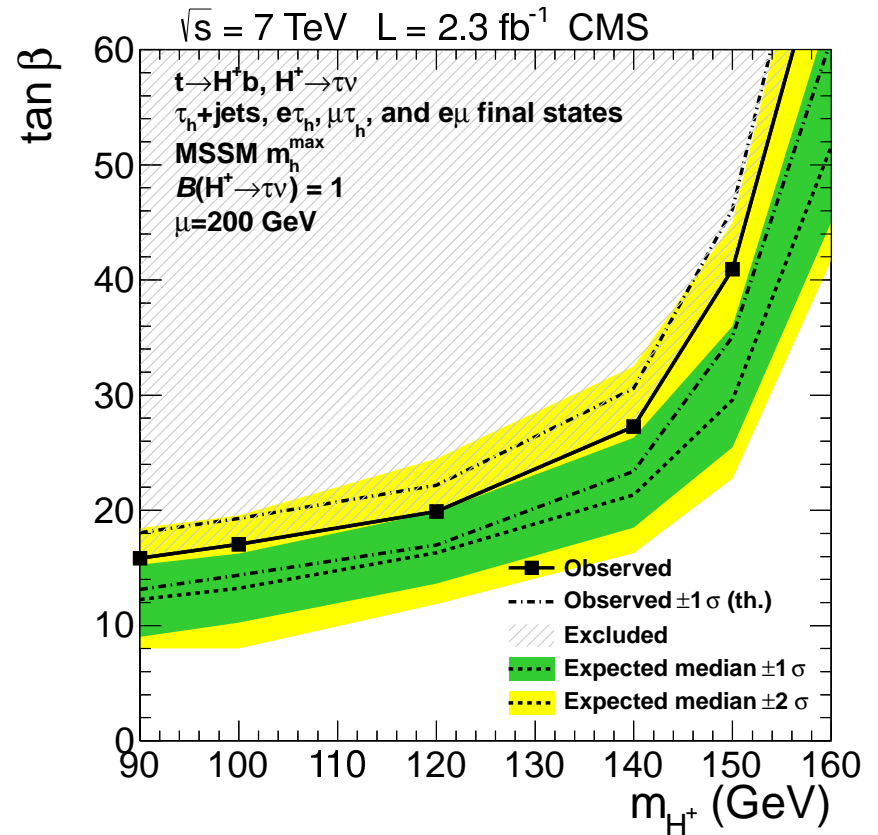
# Search for *MSSM* Higgs Bosons at the *LHC*



ATLAS arXiv:1204.2760



CMS arXiv:1205.5736



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## *MSSM Higgs Mass in View of the LHC Results*

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- **Vast literature on MSSM Higgs of  $\sim 122\dots 128$  GeV**

Arbey eal; Li eal; Feng eal; Baer eal; Hall eal; Albornoz Vasquez eal; Heinemeyer eal; Desai et al.;  
Draper eal; Carena eal; Cao eal; Christensen eal; Kadastik eal; Buchmuller eal; Arvanitaki eal; Ellis eal;  
Curtin eal; ...

- **MSSM Higgs mass corrections**

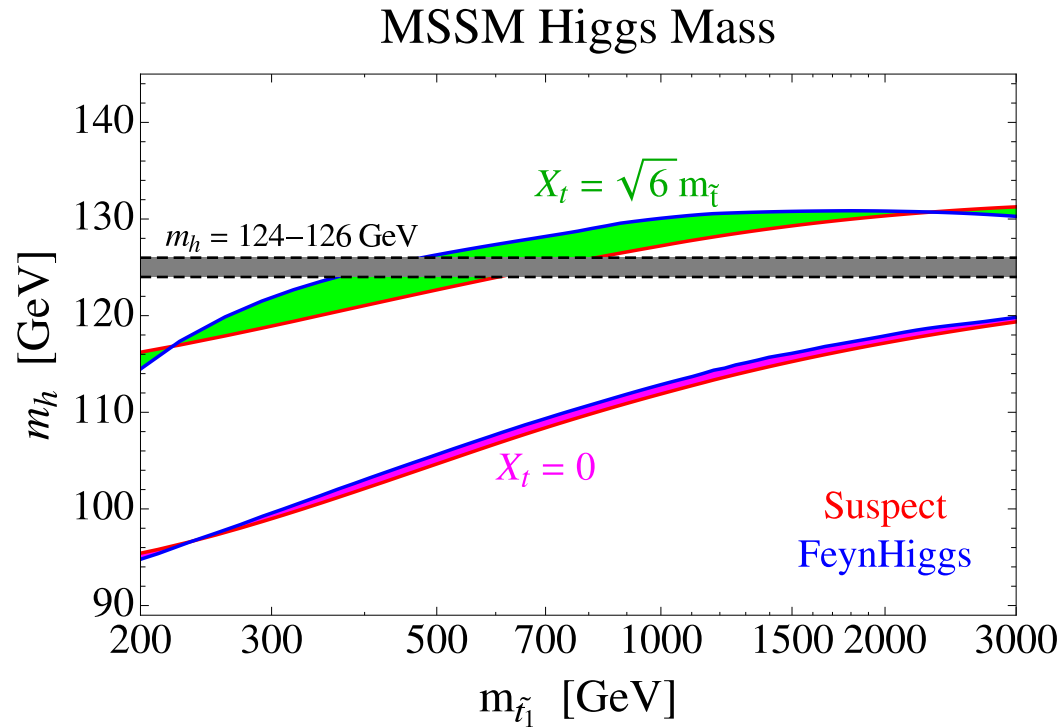
$$m_h^2 \approx M_Z^2 \cos^2 2\beta + \Delta m_h^2$$

$\Rightarrow M_H \approx 125$  GeV requires

$\Delta m_h \approx 85$  GeV ( $\tan \beta$  large)  $\Rightarrow$  large corrections  $\rightsquigarrow$  finetuning

# MSSM Higgs Mass in View of the LHC Results

Hall, Pinner, Ruderman 1112.2703



Maximal stop mixing:  
 $m_{\tilde{t}_1} \stackrel{!}{\gtrsim} 500$  GeV

## • Further remarks:

- next-lightest Higgs can be SM-like 122-128 GeV Higgs (low  $M_A$ , moderate  $\tan \beta$ )  
lightest Higgs below LEP limit see e.g. Heinemeyer eal '11
- enhanced diphoton rate can be achieved within MSSM w/ light staus Carena eal '11
- $\gamma\gamma$  excess, but no  $WW$  excess requires New Physics beyond MSSM Christensen eal '12

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# Which Higgs Boson?

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UnHiggs  
Gaugephobic Higgs  
Composite Higgs  
Gauge Higgs  
Simplest Higgs  
Private Higgs  
Intermediate Higgs  
Fat Higgs  
Twin Higgs  
Phantom Higgs  
Little Higgs  
Littlest Higgs  
Slim Higgs  
Higgsless  
Portal Higgs  
Lone Higgs

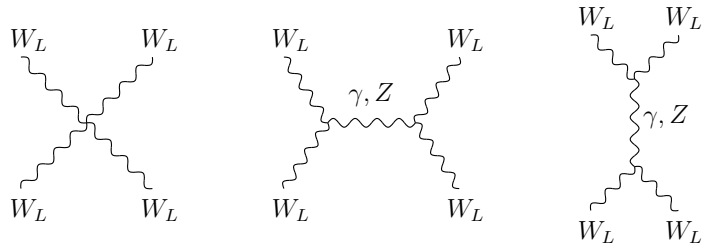
# Composite Higgs Boson

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# What is the $SM$ and what the *Composite Higgs Boson*?

---

- Higgs boson: creation of particle masses



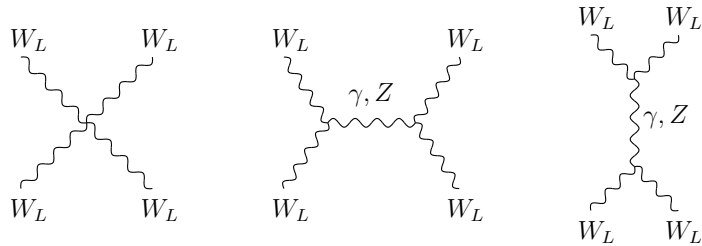
$$\mathcal{A} = \frac{s}{v^2}$$

---

# What is the $SM$ and what the Composite Higgs Boson?

---

- Higgs boson: creation of particle masses



$$\mathcal{A} = \frac{s}{v^2}$$

- Electroweak symmetry breaking  $\mathcal{L}$

Cornwall et al; Contino, Grojean, Moretti, Piccinini, Rattazzi

custodial symmetry and minimal flavour violation (MFV) built-in

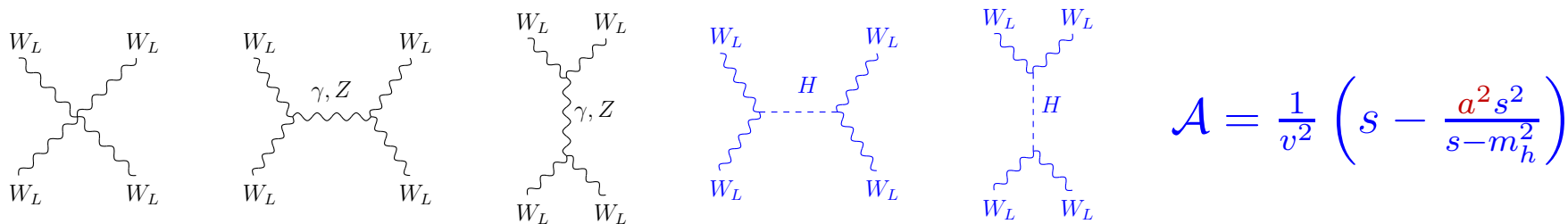
$$\mathcal{L}_{\text{EWSB}} = \frac{v^2}{4} \text{Tr}(D_\mu \Sigma^\dagger D^\mu \Sigma) \left( 1 + 2a \frac{h}{v} + b \frac{h^2}{v^2} \right) - \lambda \bar{\psi}_L \Sigma \psi_R \left( 1 + c \frac{h}{v} \right)$$

$\Sigma = e^{i\sigma^a \pi^a / v}$  Goldstone of  $SU(2)_L \times SU(2)_R / SU(2)_V$



# What is the $\mathcal{SM}$ and what the Composite Higgs Boson?

- Higgs boson: creation of particle masses



- Electroweak symmetry breaking  $\mathcal{L}$

Cornwall et al; Contino, Grojean, Moretti, Piccinini, Rattazzi

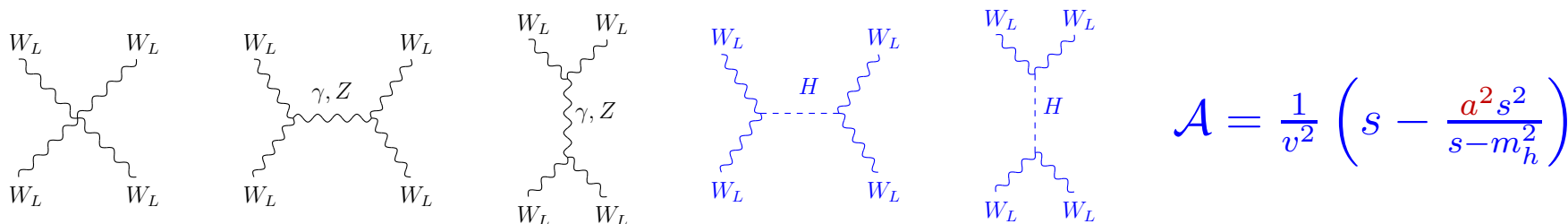
custodial symmetry and minimal flavour violation (MFV) built-in

$$\mathcal{L}_{\text{EWSB}} = \frac{v^2}{4} \text{Tr}(D_\mu \Sigma^\dagger D^\mu \Sigma) \left( 1 + 2a \frac{h}{v} + b \frac{h^2}{v^2} \right) - \lambda \bar{\psi}_L \Sigma \psi_R \left( 1 + c \frac{h}{v} \right)$$

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# What is the $\mathcal{SM}$ and what the Composite Higgs Boson?

- Higgs boson: creation of particle masses



- Electroweak symmetry breaking  $\mathcal{L}$

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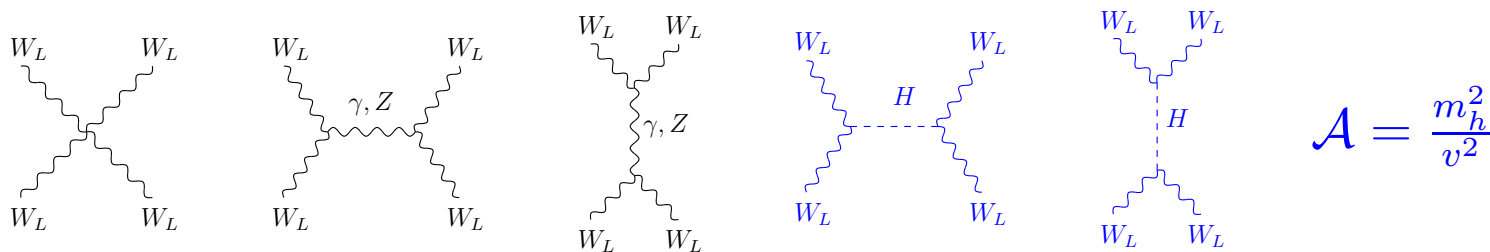
$a = 1$  perturbative unitarity in  $WW \rightarrow WW$

$b = a^2$  perturbative unitarity in  $WW \rightarrow hh$

$ac = 1$  perturbative unitarity in  $WW \rightarrow \psi\psi$

# What is the $\mathcal{SM}$ and what the Composite Higgs Boson?

- Higgs boson: creation of particle masses and UV regulator



- Electroweak symmetry breaking  $\mathcal{L}$

Cornwall et al; Contino, Grojean, Moretti, Piccinini, Rattazzi

custodial symmetry and minimal flavour violation (MFV) built-in

$$\mathcal{L}_{\text{EWSB}} = \frac{v^2}{4} \text{Tr}(D_\mu \Sigma^\dagger D^\mu \Sigma) \left( 1 + 2a \frac{h}{v} + b \frac{h^2}{v^2} \right) - \lambda \bar{\psi}_L \Sigma \psi_R \left( 1 + c \frac{h}{v} \right)$$

$a = 1$  perturbative unitarity in  $WW \rightarrow WW$

$b = a^2$  perturbative unitarity in  $WW \rightarrow hh$

$ac = 1$  perturbative unitarity in  $WW \rightarrow \psi\psi$

SM Higgs boson:  $a = b = c = 1$

Composite Higgs boson:  $a, b, c \neq 1$

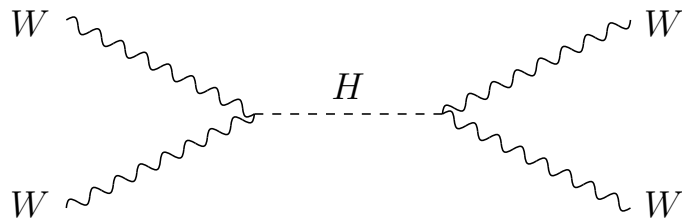
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# Composite Higgs

---

What guarantees the unitarity of the  $WW$  scattering amplitude?

Weakly coupled models

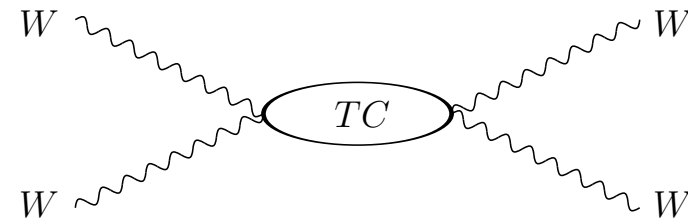


SUSY, ...

SUSY Partner  $\sim 100$  GeV

New particles necessary to  
stabilise the Higgs mass

Strongly coupled models



Technicolor

rho meson  $\sim 1$  TeV

Resonances for unitarity  
generate EW corrections

Composite Higgs

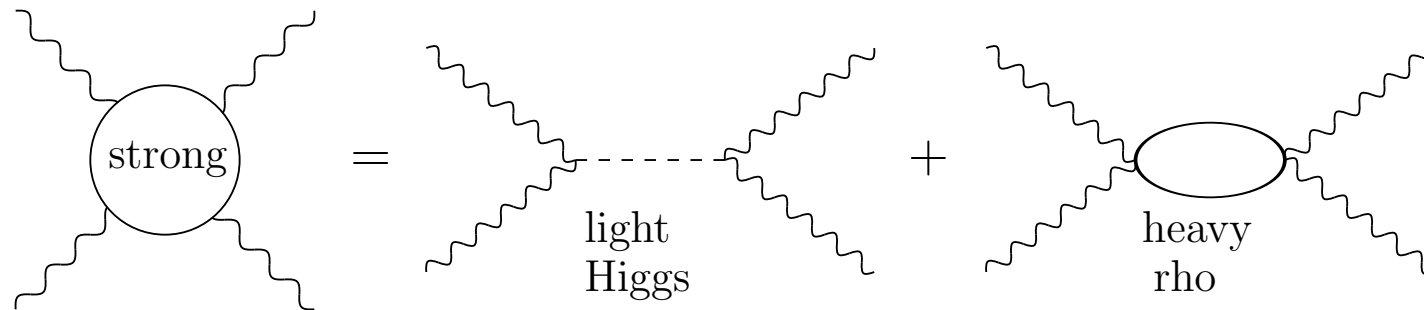
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# Composite Higgs

---

Georgi, Kaplan

**Higgs = Composite Object**    couplings deviate from pointlike scalar;  
pseudo-Goldstone boson of strong sector



## Unitarity restored half-way between weak and strong unitarity

- $\neq$  SUSY: composite particle  $\rightsquigarrow$  no naturalness problem  $\rightsquigarrow$  no new particles necessary for this
- $\neq$  Technicolor: amplitude partly cancelled by Higgs  $\rightsquigarrow$   $\rho$  heavier  $\rightsquigarrow$  smaller corrections to S, T-parameter

---

# Composite Higgs Boson

---

- How can we obtain a light composite Higgs?

Higgs: Pseudo-Goldstone boson of strongly interacting sector

Global symmetry of strong sector  $G$   $\xrightarrow[\text{broken at } f]{\text{spontaneously}}$  subgroup  $H$

$G/H$ : 4th Nambu-Goldstone Boson: Higgs boson

- Possible symmetry patterns

- \*  $H$  must contain SM gauge group
- \*  $G$  must contain an  $SU(2) \times SU(2) \sim SO(4)$  symmetry  $\rightsquigarrow$  PGB is a Higgs doublet

Examples:

- $SO(5)/SO(4) \rightsquigarrow$  PGB: one doublet
- $SO(6)/SO(5) \rightsquigarrow$  PGB: one doublet + singlet
- ...

---

# Composite Higgs Boson - Physics

---

- **SILH effective Lagrangian**

Giudice, Grojean, Pomarol, Rattazzi

(SILH=strongly interacting light Higgs)

- **Genuine strong operators** (sensitive to the scale  $f$ )

$$\frac{c_H}{2f^2}(\partial_\mu(|H|^2))^2 + \frac{c_T}{2f^2}(H^\dagger \overleftrightarrow{D}^\mu)^2 + \left( \frac{c_y y_f}{f^2} |H|^2 \bar{f}_L H f_R + h.c. \right) + \frac{c_6 \lambda}{f^2} |H|^6$$

- **Form factor operators** (sensitive to the scale  $m_\rho$ )

$$\frac{ic_w g}{2m_\rho^2} (H^\dagger \sigma^i \overleftrightarrow{D}^\mu H) (D^\nu W_{\mu\nu})^i + \frac{ic_B g'}{2m_\rho^2} (H^\dagger \overleftrightarrow{D}^\mu H) (\partial^\nu B_{\mu\nu}) + \dots$$

$c_H, c_T, \dots: \mathcal{O}(1),$  MFV built in (no FCNC)

- **Contribution to Higgs kinetic term:**  $\frac{c_H}{2f^2}(\partial_\mu(|H|^2))^2$

Rescale Higgs field  $\rightsquigarrow$   $g_{Hf\bar{f}} = g_{Hf\bar{f}}^{SM} \left( 1 - (c_y + c_H/2) \frac{v^2}{f^2} \right)$   $g_{HWW} = g_{HWW}^{SM} \left( 1 - c_H \frac{v^2}{f^2} \right)$

# Higgs Anomalous Couplings

- **SILH effective Lagrangian** Giudice, Grojean, Pomarol, Rattazzi
- **Large  $\xi$  5D MCHM** provides completion for large  $\frac{v}{f}$  ( $SO(5)/SO(4)$ ) Contino et al; Agashe et al
- **Fermion couplings** depend on embedding into representations of the bulk symmetry

spinorial representations of  $SO(5)$

fundamental representations of  $SO(5)$

MCHM4

MCHM5

| MCHM4  | MCHM5  |
|--|--|
| $g_{HVV} = g_{HVV}^{SM} \sqrt{1-\xi}$                | $g_{HVV} = g_{HVV}^{SM} \sqrt{1-\xi}$                  |
| $g_{Hff} = g_{Hff}^{SM} \sqrt{1-\xi}$                | $g_{Hff} = g_{Hff}^{SM} \frac{(1-2\xi)}{\sqrt{1-\xi}}$ |
| universal factor<br>$\rightsquigarrow$ BRs unchanged | $g_{Hff}$ coupling<br>vanishes for $\xi = 0.5$         |

In the following:  $\xi = 0.2, 0.5, 0.8$

- **Impact on** BR's,  $\Gamma_{\text{tot}}$ , production cross sections, Higgs search significances



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## Constraints

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- **EW precision observables:**

- \*  $\hat{T} = c_T \frac{v^2}{f^2} \Rightarrow |c_T \frac{v^2}{f^2}| < 2 \times 10^{-3}$

- \*  $\hat{S} = (c_W + c_B) \frac{m_W^2}{m_\rho^2}$

- ★ 1-loop IR effects

$$\Delta\epsilon_{1,3} = -c_{1,3}(1 - a^2) \log(m_\rho^2/m_h^2)$$

constrain only  $a$

removed by custodial symmetry

$$m_\rho \geq (c_W + c_B)^{1/2} 2.5 \text{ TeV}$$

constrains  $a$

Barbieri et al

- **Flavor constraints**

- \* no tree-level FCNC

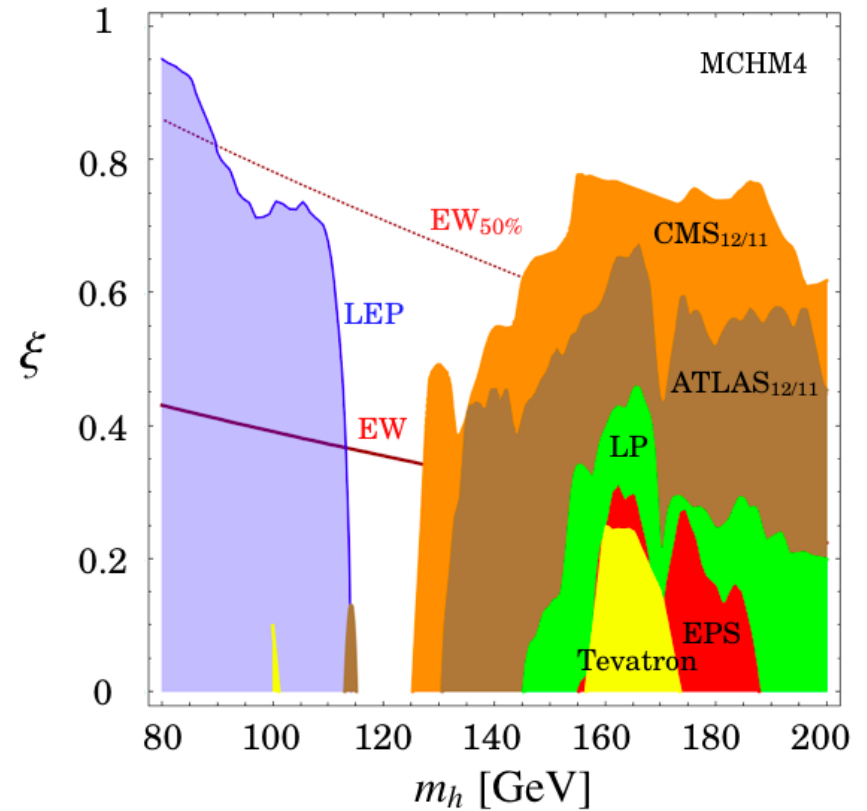
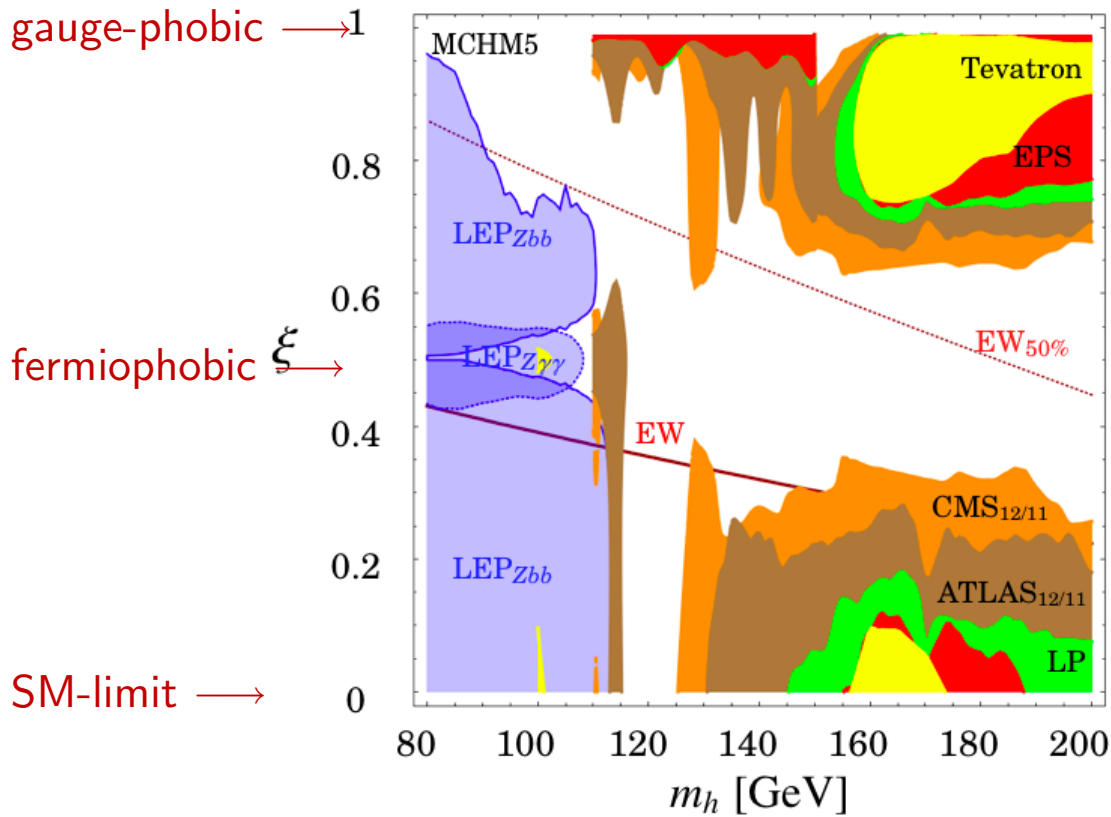
$c$  is flavor universal  $\rightarrow$  MFV built in

- **Direct searches LEP, Tevatron, LHC:** constrain  $a$  and  $c$

[rescale  $\sigma_{\text{prod}}$  and  $\Gamma_{\text{decay}}$ , add channels in quadrature]

# Constraints from EWPT, LEP, Tevatron, LHC - *Pre-Moriond '12*

Espinosa, Grojean, MMM



CMS 12/11

ATLAS 12/11

Lepton-Photon 11

LEP

EPS-HEP 11

Tevatron

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## How to test Composite Nature of the Higgs Boson?

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- Resonances

Production of heavy resonances  $m_\rho$

- Coupling modifications:

◇ modification of production and decay rates\*

LHC/300 fb<sup>-1</sup>:  $\delta g \approx 20 - 40\%$  Dührssen eal.  $\rightsquigarrow$  probe  $4\pi f = 5 - 7$  TeV

ILC/500 GeV  $\rightsquigarrow$  probe  $4\pi f \sim 30$  TeV,  $\delta\lambda_{HHH} \sim 10 - 20\%$  Barger eal

CLIC/3 TeV  $\rightsquigarrow$  improve sensitivity by factor 2

Composite Higgs model: accuracy of couplings 20-30% (30 fb<sup>-1</sup>) Bock eal

◇ strong  $WW$  scattering:  $W_L W_L \rightarrow W_L W_L$

difficult: disentangle  $L$  from  $T$  polarization Giudice eal; Han eal

◇ strong  $HH$  production:  $W_L W_L \rightarrow HH$

SLHC/5 ab<sup>-1</sup>:  $3l$  final state: rather clean signal  $\xi > 0.5$  Contino eal

\* no direct probe of strong sector at origin of EWSB

- Impact on Higgs boson searches at the LHC Espinosa, Grojean, Mühlleitner

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## Is it the SM Higgs Boson?

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- **Effective Lagrangian** valid at  $E \sim m_t$

- \* consider effective  $\mathcal{L}$  w/ a light scalar resonance and Goldstone bosons associated with EWSB and the SM field content

- \* minimal description: effective chiral  $\mathcal{L}$  w/ a nonlinear realisation of  $SU(2) \times U(1)_Y$

$$\begin{aligned}\mathcal{L} &= \frac{1}{2}(\partial_\mu h)^2 - V(h) + \frac{v^2}{4}\text{Tr}(D_\mu \Sigma^\dagger D^\mu \Sigma) \left[ 1 + 2a \frac{h}{v} + b \frac{h^2}{v^2} + b_3 \frac{h^3}{v^3} + \dots \right], \\ &\quad - \frac{v}{\sqrt{2}} (\bar{u}_L^i \bar{d}_L^i) \Sigma \left[ 1 + c \frac{h}{v} + c_2 \frac{h^2}{v^2} + \dots \right] \begin{pmatrix} y_{ij}^u u_R^j \\ y_{ij}^d d_R^j \end{pmatrix} + h.c., \quad \text{with} \\ V(h) &= \frac{1}{2} m_h^2 h^2 + \frac{d_3}{6} \left( \frac{3m_h^2}{v} \right) h^3 + \frac{d_4}{24} \left( \frac{3m_h^2}{v^2} \right) h^4 + \dots\end{aligned}$$

$a$  characterises deviation from SM Higgs coupling to the gauge bosons (SM:  $a=1$ )

$c$  characterises deviation from SM Higgs coupling to the fermions (SM:  $c=1$ )

☞ Incorporates  $SU(2)_L \times U(1)_Y \rightarrow U(1)_{em}$  symmetry breaking

☞ + custodial symmetry

☞  $y_{ij}^{u,d} \rightarrow y^{u,d} \delta_{ij}$ : no tree-level FCNC from  $h$  exchange

# Model-Independent Fit to (Moriond) LHC Data

Effective theory assuming: custodial symmetry & MFV

Espinosa, Grojean, MMM, Trott '12

Fit to LHC Higgs like data

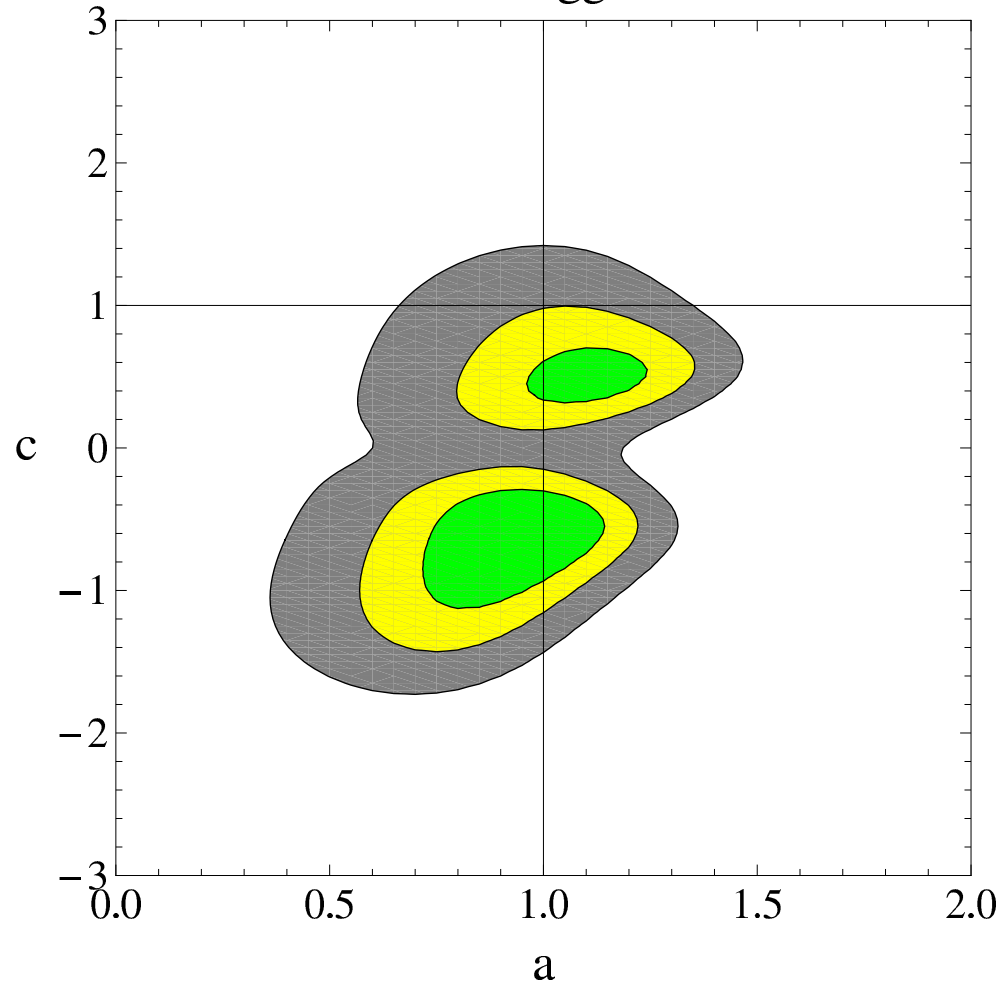
(green/yellow/gray)  
(65/90/99% CL)

SM 88%CL away  
from best fit point

Two minima:

$(a, c) = (1.18, 0.55)$   
 $\chi^2 = 7.5$

$(a, c) = (0.99, -0.64)$   
 $\chi^2 = 6.3$



Note: a fermiophobic  
Higgs is disfavoured  
by data

for similar analyses, see also

Azatov, Contino, Galloway '12  
Carmi, Falkowski, Kuflik, Volansky '12  
Ellis, You '12; Giardino et al '12

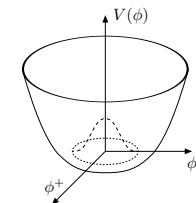
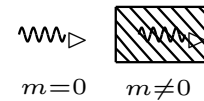
# Next Steps in Experimental Verification of the Higgs Mechanism

## Higgs mechanism:

Creation of particle masses without violating gauge symmetries

### Test of the Higgs mechanism

- Discovery –  $m$
- Interaction with a scalar Higgs with  $v = 246 \text{ GeV} \neq 0$   $\rightsquigarrow g_{HXX} \sim m_X$
- Spin and parity quantum numbers –  $J^{PC}$
- EWSB requires Higgs potential –  $\lambda_{HHH}, \lambda_{HHHH}$



Would require another lecture!

Thank you for your attention!