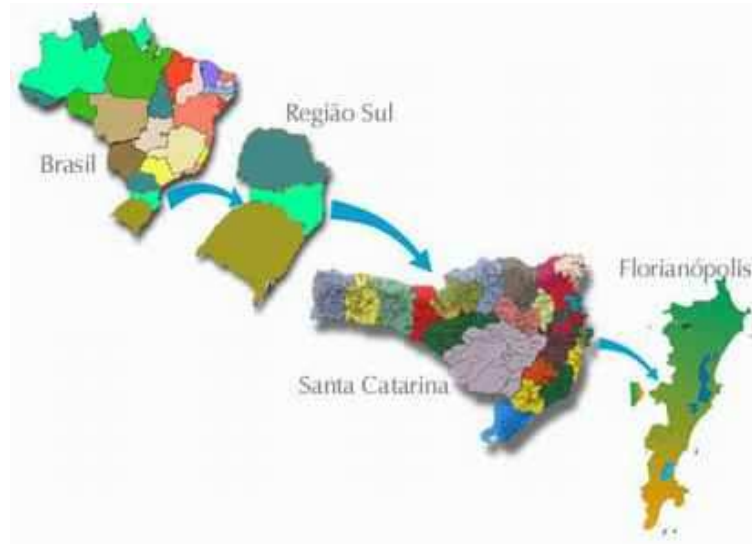


# Relativistic Mean-Field Hadronic Models under Nuclear Matter Constraints



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## Motivation

- EoS are essential for modeling compact astrophysical objects such as neutron stars, core-collapse supernovae and related phenomena including the creation of chemical elements in the Universe.
- No realistic and quantitative description of infinite hadronic matter and nuclei from first principles is available at present. Hence, too many models have been developed.
- It is important to determine the most realistic parameter sets and to use them consistently.
- Recently a set of constraints on properties of nuclear matter was formed and the performance of **240 non-relativistic Skyrme** parameterizations was assessed, in describing nuclear matter up to about 3 times nuclear saturation density. **16** were approved.
- We have also examined **263 Relativistic mean-field (RMF) models** in a comparable approach.

- **Three** different sets of constraints related to **symmetric nuclear matter, pure neutron matter, symmetry energy, and its derivatives** were used:
  - **SET1** -the same as used in assessing the Skyrme parameterizations. (M. Dutra, O. Lourenço, J. S. Sá Martins, A. Delfino, J. R. Stone, and P. D. Stevenson, Phys. Rev. C **85**, 035201 (2012))
  - **SET2a and SET2b (more restrictive)**, were more suitable for analysis of RMF and included, up-to-date theoretical, experimental and empirical information.

## Non-linear models

$$\mathcal{L}_{\text{NL}} = \mathcal{L}_{\text{nm}} + \mathcal{L}_{\sigma} + \mathcal{L}_{\omega} + \mathcal{L}_{\rho} + \mathcal{L}_{\delta} + \mathcal{L}_{\sigma\omega\rho}, \quad (1)$$

$$\mathcal{L}_{\text{nm}} = \bar{\psi}(i\gamma^{\mu}\partial_{\mu} - M)\psi + g_{\sigma}\sigma\bar{\psi}\psi - g_{\omega}\bar{\psi}\gamma^{\mu}\omega_{\mu}\psi - \frac{g_{\rho}}{2}\bar{\psi}\gamma^{\mu}\vec{\rho}_{\mu}\vec{\tau}\psi + g_{\delta}\bar{\psi}\vec{\delta}\vec{\tau}\psi, \quad (2)$$

$$\mathcal{L}_{\sigma} = \frac{1}{2}(\partial^{\mu}\sigma\partial_{\mu}\sigma - m_{\sigma}^2\sigma^2) - \frac{A}{3}\sigma^3 - \frac{B}{4}\sigma^4, \quad (3)$$

$$\mathcal{L}_{\omega} = -\frac{1}{4}F^{\mu\nu}F_{\mu\nu} + \frac{1}{2}m_{\omega}^2\omega_{\mu}\omega^{\mu} + \frac{C}{4}(g_{\omega}^2\omega_{\mu}\omega^{\mu})^2, \quad (4)$$

$$\mathcal{L}_{\rho} = -\frac{1}{4}\vec{B}^{\mu\nu}\vec{B}_{\mu\nu} + \frac{1}{2}m_{\rho}^2\vec{\rho}_{\mu}\vec{\rho}^{\mu}, \quad (5)$$

$$\mathcal{L}_{\delta} = \frac{1}{2}(\partial^{\mu}\vec{\delta}\partial_{\mu}\vec{\delta} - m_{\delta}^2\vec{\delta}^2), \quad (6)$$

$$\begin{aligned} \mathcal{L}_{\sigma\omega\rho} = & g_{\sigma}g_{\omega}^2\sigma\omega_{\mu}\omega^{\mu} \left( \alpha_1 + \frac{1}{2}\alpha_1'g_{\sigma}\sigma \right) + g_{\sigma}g_{\rho}^2\sigma\vec{\rho}_{\mu}\vec{\rho}^{\mu} \left( \alpha_2 + \frac{1}{2}\alpha_2'g_{\sigma}\sigma \right) \\ & + \frac{1}{2}\alpha_3'g_{\omega}^2g_{\rho}^2\omega_{\mu}\omega^{\mu}\vec{\rho}_{\mu}\vec{\rho}^{\mu}. \end{aligned} \quad (7)$$

**Mean-field approximation** (the meson fields are treated as classical fields):

$$\sigma \rightarrow \langle \sigma \rangle \equiv \sigma, \quad \omega_\mu \rightarrow \langle \omega_\mu \rangle \equiv \omega_0, \quad \vec{\rho}_\mu \rightarrow \langle \vec{\rho}_\mu \rangle \equiv \vec{\rho}_{0(3)}, \quad \vec{\delta} \rightarrow \langle \vec{\delta} \rangle \equiv \delta_{(3)}, \quad (8)$$

Euler-Lagrange equations  $\rightarrow$  equations of motion (translational and rotational invariance)  $\rightarrow$  energy-momentum tensor  $\rightarrow$  EoS

Dirac equation  $\rightarrow$  **vector and scalar potentials:**

$$V_{\tau \text{ NL}} = g_\omega \omega_0 + \frac{g_\rho}{2} \vec{\rho}_{0(3)} \tau_3 \quad (9)$$

$$S_{\tau \text{ NL}} = -g_\sigma \sigma - g_\delta \delta_{(3)} \tau_3, \quad (10)$$

$$M_\tau^* = M + S_{\tau \text{ NL}} \rightarrow$$

$$M_p^* = M - g_\sigma \sigma - g_\delta \delta_{(3)} \quad \text{and} \quad M_n^* = M - g_\sigma \sigma + g_\delta \delta_{(3)}. \quad (11)$$



- **type 1** (linear finite range models):  $A = B = C = \alpha_1 = \alpha_2 = \alpha'_1 = \alpha'_2 = \alpha'_3 = g_\delta = 0$  (linear Walecka model)
- **type 2** ( $\sigma^3 + \sigma^4$  models):  $C = \alpha_1 = \alpha_2 = \alpha'_1 = \alpha'_2 = \alpha'_3 = g_\delta = 0$ . (Boguta-Bodmer model)
- **type 3** ( $\sigma^3 + \sigma^4 + \omega_0^4$  models):  $\alpha_1 = \alpha_2 = \alpha'_1 = \alpha'_2 = \alpha'_3 = g_\delta = 0$ . (include a quartic self-interaction in the  $\omega$  field)
- **type 4** ( $\sigma^3 + \sigma^4 + \omega_0^4 +$  cross terms models):  $g_\delta = 0$  and at least one of the coupling constants,  $\alpha_1$ ,  $\alpha_2$ ,  $\alpha'_1$ ,  $\alpha'_2$ , or  $\alpha'_3$  is different from zero.

## Density dependent models

$$g_\sigma \rightarrow \Gamma_\sigma(\rho), \quad g_\omega \rightarrow \Gamma_\omega(\rho), \quad g_\rho \rightarrow \Gamma_\rho(\rho) \quad \text{and} \quad g_\delta \rightarrow \Gamma_\delta(\rho) \quad (12)$$

$$\begin{aligned} \mathcal{L}_{\text{DD}} = & \bar{\psi}(i\gamma^\mu\partial_\mu - M)\psi + \Gamma_\sigma(\rho)\sigma\bar{\psi}\psi - \Gamma_\omega(\rho)\bar{\psi}\gamma^\mu\omega_\mu\psi - \frac{\Gamma_\rho(\rho)}{2}\bar{\psi}\gamma^\mu\vec{\rho}_\mu\vec{\tau}\psi \\ & + \frac{1}{2}(\partial^\mu\sigma\partial_\mu\sigma - m_\sigma^2\sigma^2) - \frac{1}{4}F^{\mu\nu}F_{\mu\nu} + \frac{1}{2}m_\omega^2\omega_\mu\omega^\mu - \frac{1}{4}\vec{B}^{\mu\nu}\vec{B}_{\mu\nu} + \frac{1}{2}m_\rho^2\vec{\rho}_\mu\vec{\rho}^\mu \\ & + \Gamma_\delta(\rho)\bar{\psi}\vec{\delta}\vec{\tau}\psi + \frac{1}{2}(\partial^\mu\vec{\delta}\partial_\mu\vec{\delta} - m_\delta^2\vec{\delta}^2), \end{aligned} \quad (13)$$

$$\Gamma_i(\rho) = \Gamma_i(\rho_0)f_i(x), \quad f_i(x) = a_i \frac{1 + b_i(x + d_i)^2}{1 + c_i(x + d_i)^2} \quad i = \sigma, \omega, \quad (14)$$

$$\Gamma_\rho(\rho) = \Gamma_\rho(\rho_0)e^{-a(x-1)}, \quad x = \rho/\rho_0. \quad (15)$$

**the GDFM model:**

$$\Gamma_i(\rho) = a_i + (b_i + d_i x^3) e^{-c_i x}, \quad i = \sigma, \omega, \rho, \delta \quad (16)$$

and a correction to the coupling parameter for the meson  $\omega$  :

$$\Gamma_{\text{cor}}(\rho) = \Gamma_{\omega}(\rho) - a_{\text{cor}} e^{-\left(\frac{\rho - \rho_0}{b_{\text{cor}}}\right)^2}. \quad (17)$$

**DDH $\delta$  parameterization:** same coupling parameters as in Eq. (14) for  $\sigma$  and  $\omega$

$$f_i(x) = a_i e^{-b_i(x-1)} - c_i(x - d_i), \quad i = \rho, \delta \quad (18)$$

$$V_{\tau \text{ DD}} = \Gamma_{\omega}(\rho)\omega_0 + \frac{\Gamma_{\rho}(\rho)}{2}\bar{\rho}_{0(3)}\tau_3 + \Sigma_R(\rho), \quad (19)$$

$$\Sigma_R(\rho) = \frac{\partial \Gamma_{\omega}}{\partial \rho}\omega_0\rho + \frac{1}{2}\frac{\partial \Gamma_{\rho}}{\partial \rho}\bar{\rho}_{0(3)}\rho_3 - \frac{\partial \Gamma_{\sigma}}{\partial \rho}\sigma\rho_s - \frac{\partial \Gamma_{\delta}}{\partial \rho}\delta_{(3)}\rho_{s3} \quad (20)$$

- **type 5** (density dependent models): parameterizations obtained from Eq. (13) in which  $\Gamma_{\delta} = 0$ .

## Nonlinear point-coupling models

$$\begin{aligned}
 \mathcal{L}_{\text{NLPC}} = & \bar{\psi}(i\gamma^\mu\partial_\mu - M)\psi - \frac{\alpha_s}{2}(\bar{\psi}\psi)^2 - \frac{\beta_s}{3}(\bar{\psi}\psi)^3 - \frac{\gamma_s}{4}(\bar{\psi}\psi)^4 \\
 & - \frac{\alpha_V}{2}(\bar{\psi}\gamma^\mu\psi)^2 - \frac{\gamma_V}{4}(\bar{\psi}\gamma^\mu\psi)^4 - \frac{\alpha_{\text{TV}}}{2}(\bar{\psi}\gamma^\mu\vec{\tau}\psi)^2 - \frac{\gamma_{\text{TV}}}{4}(\bar{\psi}\gamma^\mu\vec{\tau}\psi)^4 \quad (21) \\
 & - \frac{\alpha_{\text{TS}}}{2}(\bar{\psi}\vec{\tau}\psi)^2 + [\eta_1 + \eta_2(\bar{\psi}\psi)](\bar{\psi}\psi)(\bar{\psi}\gamma^\mu\psi)^2 - \eta_3(\bar{\psi}\psi)(\bar{\psi}\gamma^\mu\vec{\tau}\psi)^2.
 \end{aligned}$$

$$\begin{aligned}
 V_{\text{T NLPC}} &= \alpha_V\rho + \alpha_{\text{TV}}\rho_3\tau_3 + \gamma_V\rho^3 + \gamma_{\text{TV}}\rho_3^3\tau_3 + 2(\eta_1 + \eta_2\rho_s)\rho_s\rho + 2\eta_3\rho_s\rho_3\tau_3, \\
 S_{\text{T NLPC}} &= \alpha_s\rho_s + \beta_s\rho_s^2 + \gamma_s\rho_s^3 + \eta_1\rho^2 + 2\eta_2\rho_s\rho^2 + \eta_3\rho_3^2 + \alpha_{\text{TS}}\rho_s\tau_3, \quad (22)
 \end{aligned}$$

$$M_p^* = M + \alpha_s\rho_s + \beta_s\rho_s^2 + \gamma_s\rho_s^3 + \eta_1\rho^2 + 2\eta_2\rho_s\rho^2 + \eta_3\rho_3^2 + \alpha_{\text{TS}}\rho_s, \quad (23)$$

$$M_n^* = M + \alpha_s\rho_s + \beta_s\rho_s^2 + \gamma_s\rho_s^3 + \eta_1\rho^2 + 2\eta_2\rho_s\rho^2 + \eta_3\rho_3^2 - \alpha_{\text{TS}}\rho_s. \quad (24)$$

- **type 6** (point-coupling models): parameterizations of the model described by Eq. (22) in which  $\alpha_{\text{TS}} = 0$ .
- **type 7** (delta meson models): parameterizations of finite range models presenting the meson  $\delta$ , i.e., models in which  $g_{\delta} \neq 0$ .

# Nuclear bulk matter quantities

$$S(\rho) = \frac{1}{8} \frac{\partial^2(\mathcal{E}/\rho)}{\partial y^2} \Big|_{\rho, y=1/2}, \quad (\text{symmetry energy}) \quad (25)$$

$$K_0 = 9 \left( \frac{\partial P}{\partial \rho} \right)_{\rho=\rho_0, y=1/2}, \quad (\text{incompressibility}) \quad (26)$$

$$Q_0 = 27 \rho_0^3 \frac{\partial^3(\mathcal{E}/\rho)}{\partial \rho^3} \Big|_{\rho=\rho_0, y=1/2}, \quad (\text{skewness coefficient}) \quad (27)$$

$$J = S(\rho_0), \quad (\text{symmetry energy at } \rho = \rho_0) \quad (28)$$

$$L_0 = 3 \rho_0 \left( \frac{\partial S}{\partial \rho} \right)_{\rho=\rho_0}, \quad (\text{slope of } S) \quad (29)$$

$$K_{\text{sym}}^0 = 9 \rho_0^2 \left( \frac{\partial^2 S}{\partial \rho^2} \right)_{\rho=\rho_0}, \quad (\text{curvature of } S) \quad (30)$$

$$Q_{\text{sym}}^0 = 27 \rho_0^3 \left( \frac{\partial^3 S}{\partial \rho^3} \right)_{\rho=\rho_0}, \quad (\text{skewness of } S) \quad (31)$$

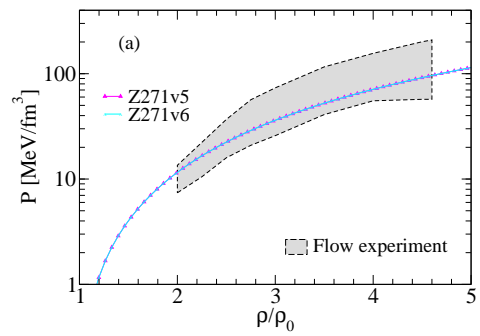
$$K_{\tau, \nu}^0 = \left( K_{\text{sym}}^0 - 6L_0 - \frac{Q_0}{K_0} L_0 \right). \quad (\text{vol part isospin incompressibility}) \quad (32)$$

# Constraints - SET 1

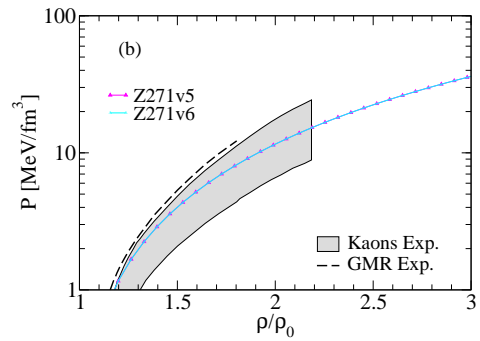
SET1 - 11 macroscopic constraints, range of their experimental/empirical values, density region in which they are valid and the corresponding range obtained using the approved RMF models (CRMf).

	Quantity	Density Region	Range of constraint (exp/emp)	Range of constraint from CRMf
SM1	$K_0$	$\rho_0$ (fm <sup>-3</sup> )	200-260 MeV	271.0 MeV
SM2	$K' = -Q_0$	$\rho_0$ (fm <sup>-3</sup> )	200-1200 MeV	733.6 MeV
SM3	$P(\rho)$	$2 < \frac{\rho}{\rho_0} < 4.6$	Band Region	see Fig.
SM4	$P(\rho)$	$1.2 < \frac{\rho}{\rho_0} < 2.2$	Band Region	see Fig.
PNM1	$\mathcal{E}_{\text{PNM}}/\rho$	$0.017 < \frac{\rho}{\rho_0} < 0.108$	Band Region	see Fig.
PNM2	$P(\rho)$	$2 < \frac{\rho}{\rho_0} < 4.6$	Band Region	see Fig.
MIX1	$J$	$\rho_0$ (fm <sup>-3</sup> )	30-35 MeV	33.8-34.0 MeV
MIX2	$L_0$	$\rho_0$ (fm <sup>-3</sup> )	40-76 MeV	70.9-73.9 MeV
MIX3	$K_{\tau, \nu}^0$	$\rho_0$ (fm <sup>-3</sup> )	-760/-372 MeV	-388.5/-388.4 MeV
MIX4	$\frac{S(\rho_0/2)}{J}$	$\rho_0$ (fm <sup>-3</sup> )	0.57-0.86	0.58
MIX5	$\frac{3P_{\text{PNM}}}{L_0\rho_0}$	$\rho_0$ (fm <sup>-3</sup> )	0.90-1.10	1.05-1.06

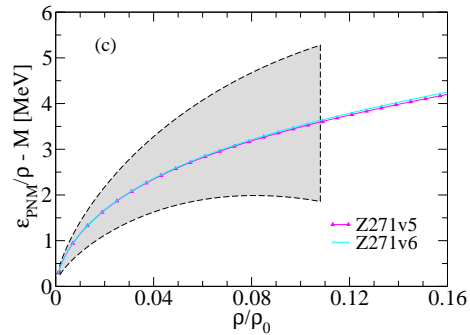




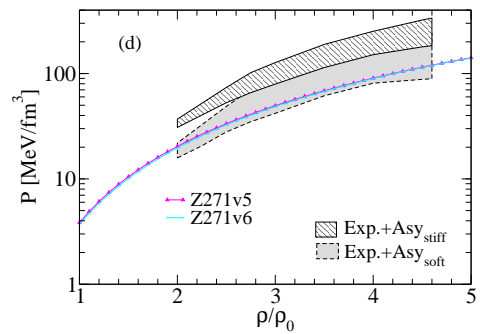
SM3 - symmetric matter



SM4 - Prog. Part. Nucl. Phys. **62**, 427 (2009)



PNM1 - Phys. Rev. C **85**, 035201 (2012)



PNM2 - pure neutron matter

A model is considered approved if its deviation obeys  $|\text{Dev}| \leq 1$ .

$$\text{Dev} = \frac{Q_{\text{mod}} - Q_{\text{const}}}{\Delta}, \quad (33)$$

$Q_{\text{mod}}$  is value of the quantity calculated in the model,  $Q_{\text{const}}$  the central value of the related constraint, and  $\Delta$  the error related to  $Q_{\text{const}}$ .

For the MIX1, MIX3 and MIX4 constraints, we define  $Q_{\text{const}} = (x_2 + x_1)/2$  and the error  $\Delta = x_2 - Q_{\text{const}} = Q_{\text{const}} - x_1$ , since they are given in the form of  $x_1 \leq X \leq x_2$ .

A graphic constraint is satisfied if the model is inside the corresponding band in 95% or more of the density region.

**None of the models** satisfies all constraints simultaneously.

List of parametrizations that **fail in only one** constraint of SET1:

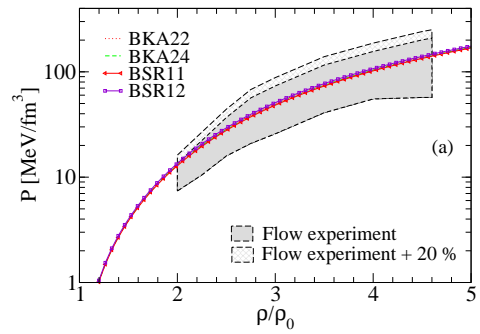
Model	Model value (MeV)	Deviation
SM1 not satisfied: $200 \leq K_0 \leq 260$ MeV		
Z271v5 (type 4)	271.00	1.37
Z271v6 (type 4)	271.00	1.37
MIX3 not satisfied: $-760 \leq K_{T,V}^0 \leq -372$ MeV		
BSR15 (type 4)	-252.54	1.62
BSR16 (type 4)	-258.75	1.58
FSUGold (type 4)	-276.07	1.49
FSUGZ06 (type 4)	-259.47	1.58
FSUGold4 (type 4)	-205.59	1.86
FSU-III (type 4)	-341.03	1.16
FSU-IV (type 4)	-210.68	1.83
TW99 (type 5)	-332.32	1.20
DD-F (type 5)	-285.54	1.45
DD-ME $\delta$ (type 7)	-258.28	1.59

## Constraints - SET2a and SET2b

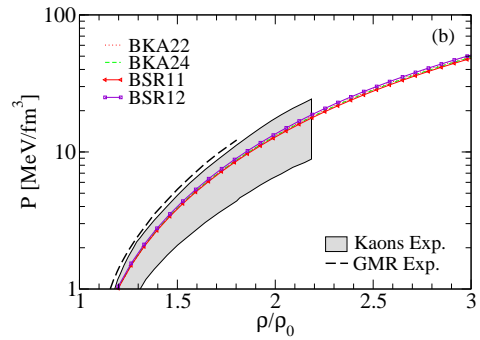
Updated constraints: SM1, SM3a, SM3b, MIX1a, MIX1b, MIX2a, MIX2b and MIX3. SM4, PNM1 and MIX4 constraints are the same as in SET1. SM2, PNM2 and MIX5 constraints were removed.

	Quantity	Density Region	Range of constraint (exp/emp)	Range of constraint from CRMF
SM1	$K_0$	$\rho_0$ (fm <sup>-3</sup> )	190-270 MeV	225.2-232.4 MeV
SM3a		the same as SM3b	plus 20% on upper limit	see Fig.
SM3b	$P(\rho)$	$2 < \frac{\rho}{\rho_0} < 5$	Band Region	see Fig.
SM4	$P(\rho)$	$1.2 < \frac{\rho}{\rho_0} < 2.2$	Band Region	see Fig.
PNM1	$\mathcal{E}_{\text{PNM}}/\rho$	$0.017 < \frac{\rho}{\rho_0} < 0.108$	Band Region	see Fig.
MIX1a	$J$	$\rho_0$ (fm <sup>-3</sup> )	25-35 MeV	33.2-34.2 MeV
MIX1b	$J$	$\rho_0$ (fm <sup>-3</sup> )	30-35 MeV	33.2-34.0 MeV
MIX2a	$L_0$	$\rho_0$ (fm <sup>-3</sup> )	25-115 MeV	77.9-84.8 MeV
MIX2b	$L_0$	$\rho_0$ (fm <sup>-3</sup> )	30-80 MeV	77.9-78.8 MeV
MIX3	$K_{\tau,v}^0$	$\rho_0$ (fm <sup>-3</sup> )	-700/-400 MeV	-421.6(a)/-414.3(b)/-382.5 MeV
MIX4	$\frac{S(\rho_0/2)}{J}$	$\rho_0$ (fm <sup>-3</sup> )	0.57 – 0.86	0.57(a)/0.59(b) – 0.59

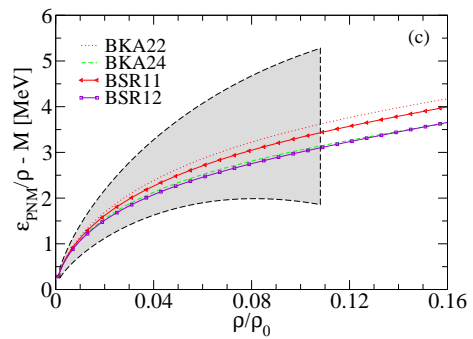
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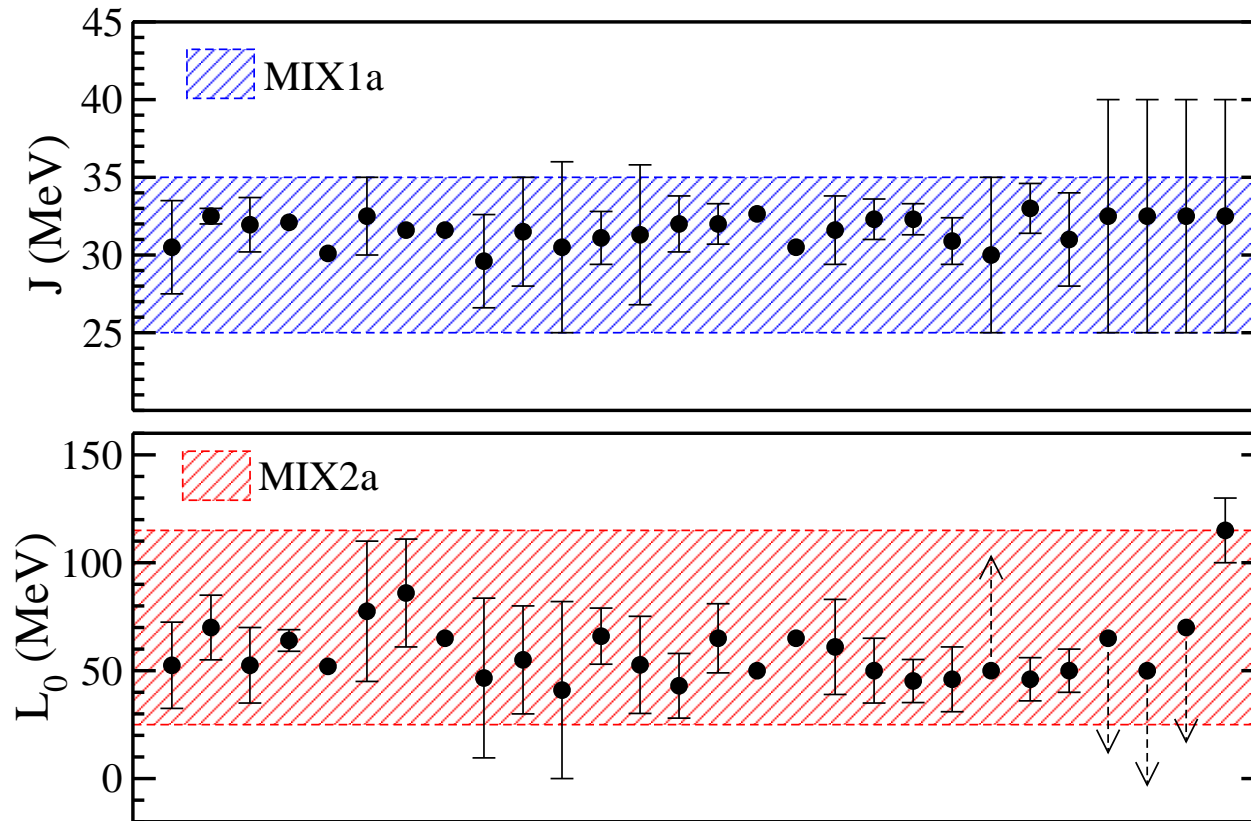
SM3



SM4



PNM1



**Comparison between the limits used in MIX1a and MIX2a constraints, and those from 28 different experimental/observational data collected in B.-A. Li and X. Han, Phys. Lett. B 727, 276 (2013): include analyses of isospin diffusion, neutron skins, pygmy dipole resonances, and decays, transverse flow, the mass-radius relation and torsional crust oscillations of neutron stars.**

## SET2

Constraints	SM1	SM3a	SM3b	SM4	PNM1		
Number of models	153	129	104	153	193		
Constraints	MIX1a	MIX1b	MIX2a	MIX2b	MIX3	MIX4	
Number of models	174	162	216	72	96	65	

**SET2a:** Only **2 type-4 models** satisfy all constraints: **BSR12** and **BKA24**.

**SET2b:** Only **1 model** satisfy all constraints: **BSR12**.

The models **FSUGold**, **FSUZG03**, **IU-FSU (type 4)** and **DD-ME $\delta$  (type 7)** are consistent with all constraints except MIX3, a constraint applicable in the region of saturation density. These parameter sets provide quite good global fits to binding energies, charge radii, isotopic shifts and neutron skin thicknesses

## Excluding MIX3 constraint

**SET2a:** 25 models are consistent with all 7 constraints: **BKA20, BKA22, BKA24, BSR8, BSR9, BSR10, BSR11, BSR12, BSR15, BSR16, BSR17, BSR18, BSR19, FSU-III, FSU-IV, FSUGold, FSUGold4, FSUGZ03, FSUGZ06, G2\*, IU-FSU (type 4), TW99, DD-F (type 5), DD-ME $\delta$ , DDH $\delta$  (type 7).**

48 models satisfy all but one of the constraints. In this group, 10 models fell outside the range of the constraint by less than 5%: **BSR20, FA3, Z271s2, Z271s3, Z271s4, Z271s5, Z271s6, Z271v4, Z271v5, Z271v6.**

**SET2b:** 22 models are consistent with all constraints: the same models approved in SET2a, **except** for the BKA24, IU-FSU and DDH $\delta$  models.

14 models satisfy only 7 constraints, and by applying the 5% criterium, 8 more models are approved. They are the same as in the corresponding case of SET2a, **except** for the BSR20 and FA3 models. Within SET2b analysis a total of 30 models are in the group of approved models.



## Saturation properties

Model	$\rho_0$	$E_0$	$K_0$	$m^*$	$K'$	$J$	$L_0$	$K_{\text{sy}}^0$
<b>linear finite range models ( type 1)</b>								
H1	0.148	-15.75	546.81	0.54	-2152.62	25.93	88.38	93
<b><math>\sigma^3 + \sigma^4</math> models (type 2)</b>								
CS	0.150	-16.17	187.21	0.58	292.63	40.91	131.42	136
<b><math>\sigma^3 + \sigma^4 + \omega_0^4</math> models (type 3)</b>								
BM-A	0.179	-15.17	188.32	0.61	436.32	19.62	51.88	-18
<b><math>\sigma^3 + \sigma^4 + \omega^4 +</math> cross terms models (type 4)</b>								
BKA20	0.146	-15.93	237.95	0.64	464.66	32.24	75.38	-15
<b>density dependent models (type 5)</b>								
DD	0.149	-16.02	239.99	0.56	-134.65	31.64	55.98	-95
<b>point-coupling models (type 6)</b>								
FA2	0.150	-16.03	287.24	0.60	812.70	33.53	99.38	-3
<b>delta meson models (type 7)</b>								
DD-ME $\delta$	0.152	-16.08	219.60	0.61	748.31	32.18	51.43	-124

**Status of each RMF model:** approved (+) or not (–) under SET2a and SET2b constraints.

Model	SM1	SM3a	SM3b	SM4	PNM1	MIX1a	MIX1b	MIX2a	MIX2b	MIX3
linear finite range models										
H1	–	–	–	–	+	+	–	+	–	–

## Deviation Table

Model	SM1	SM3a(%)	SM3b(%)	SM4(%)	PNM1(%)	MIX1a	MIX1b	MIX2a	MIX2b
linear finite range models									
H1	7.92	100U	100U	100U	0	–0.81	–2.63	0.41	

## Conclusions

- The sets of updated constraints (SET2a and SET2b) differed somewhat in the level of restriction but still yielded only 4 and 1 approved RMF models, respectively. A similarly small number of approved Skyrme parameterizations were found in the previous study with Skyrme models. An interesting feature of our analysis has been that the results change dramatically if the constraint on the volume part of the isospin incompressibility ( $K_{\tau,v}$ ) is eliminated. In this case, we have 35 approved models (SET2a) and 30 (SET2b).
- Our work faces the problematic proliferation of RMF models and our assessment should be used in future applications of RMF models.
- The reasons of many failures, even of the frequently used models, should lead to their improvement and to the identification of possible missing physics not included in present energy density functionals.

This work demanded a huge effort and took 4 years!

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**Thank you!**