

# Ising version of t-J model: Implications for underdoped cuprates

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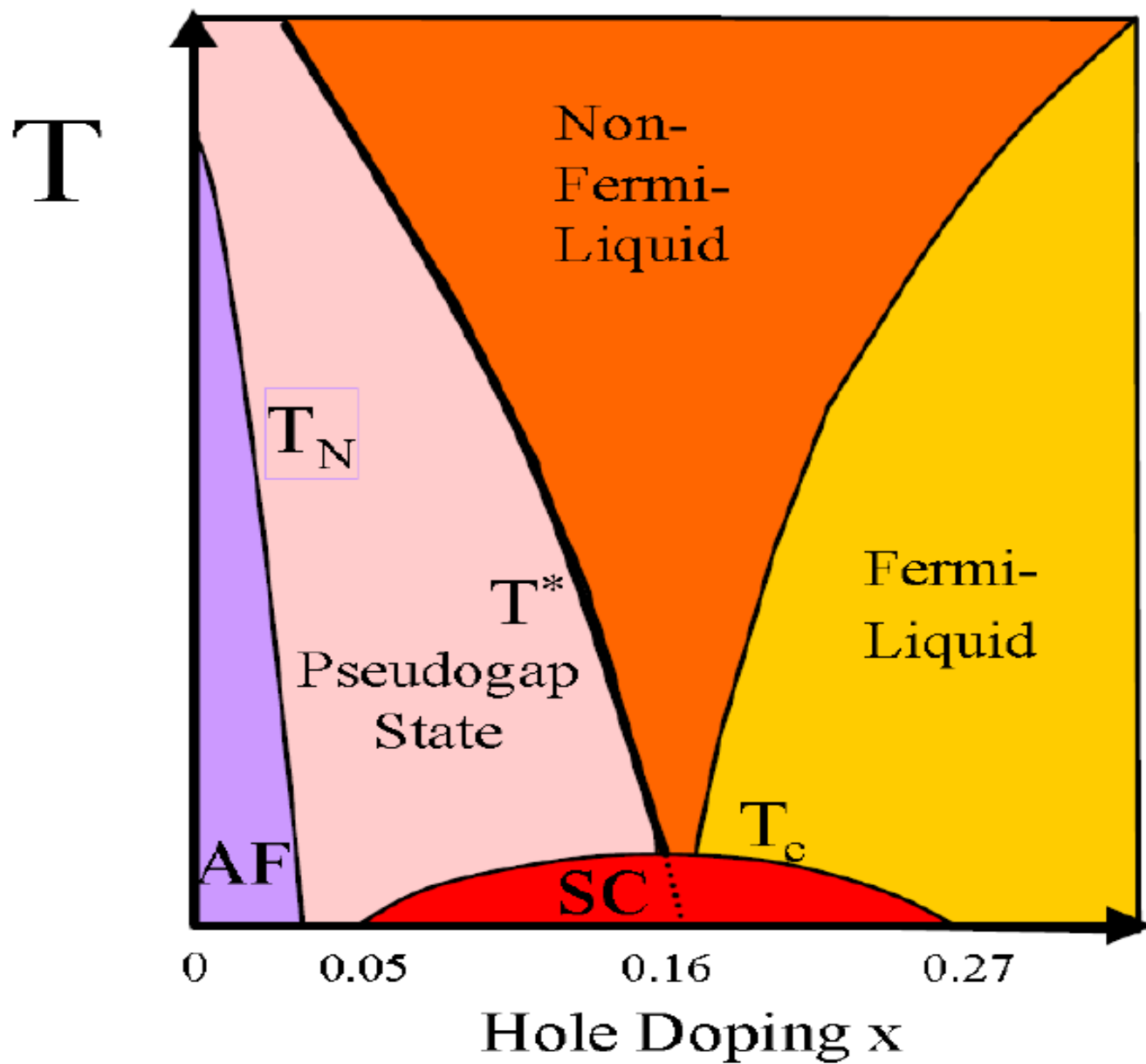
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# OUTLINE

Cuprate Phase Diagram

Doped Ising Model

Magnetic Correlations in Lightly  
Doped Cuprates



$t$ - $J$  model (SU(2) globally invariant)

$$H_{t-J} = - \sum_{ij\sigma} t_{ij} \tilde{c}_{i\sigma}^\dagger \tilde{c}_{j\sigma} + J \sum_{\langle ij \rangle} \left( Q_i Q_j - \frac{1}{4} \tilde{n}_i \tilde{n}_j \right)$$

where  $\tilde{c}_{i\sigma} = P c_{i\sigma} P = c_{i\sigma} (1 - n_{i,-\sigma})$  is the projected electron operator (to exclude the on-site double occupancy),

$$Q_i = \sum_{\sigma, \sigma'} c_{i\sigma}^\dagger \boldsymbol{\tau}_{\sigma\sigma'} c_{i\sigma'}$$

$t$ - $J_z$  model. (SU(2) globally invariant at  $J_z = 0$ )

$$H_{t-J_z} = - \sum_{ij\sigma} t_{ij} \tilde{c}_{i\sigma}^\dagger \tilde{c}_{j\sigma} + J_z \sum_{\langle ij \rangle} \left( Q_i^z Q_j^z - \frac{1}{4} \tilde{n}_i \tilde{n}_j \right)$$

## Slave spin-dopon repr:

Ribeiro, Wen, Phys. Rev. Lett. (2005), v.95, 057001:

$$\tilde{c}_{i\uparrow} = \frac{1}{\sqrt{2}} [S^+ S^- d_{i\downarrow} - S^- d_{i\uparrow}]$$

Ferraz, Kochetov, Uchoa, Phys. Rev. Lett. (2007), v.98, 069701:

$$\vec{S}_i \cdot \vec{s}_i + \frac{3}{4} n_i = 0$$

$$H_{tJ} = \sum_{ij\sigma} T_{ij} d_{i\sigma}^\dagger d_{j\sigma} + J \sum_{ij} \vec{S}_i \cdot \vec{S}_j + \lambda \sum_i \vec{S}_i \cdot \vec{s}_i$$

$$T_{ij} = 2t_{ij} + (3\lambda/4 - \mu)\delta_{ij}$$

$$\lambda \rightarrow +\infty$$

# Ising version of t-J model

Maska, Mierzejewski, Ferraz, Kochetov,  
J.Phys.C 21 , 045703 (2009)

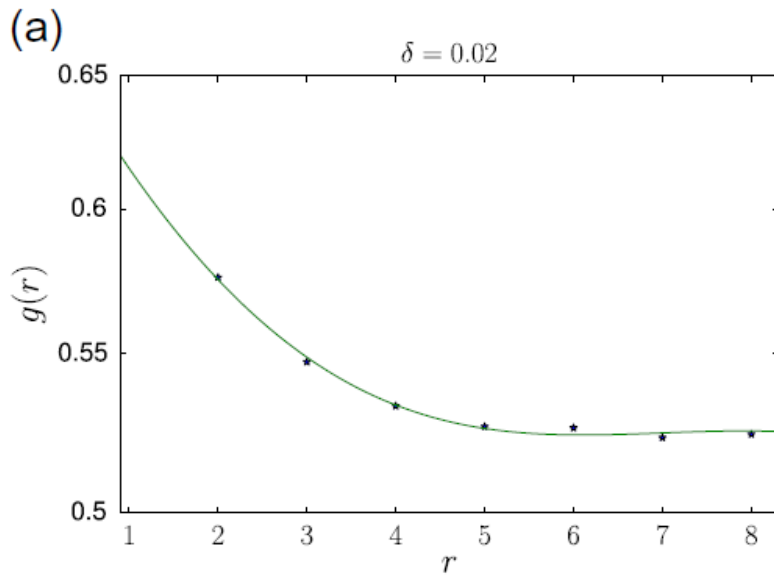
Maska, Mierzejewski, Kochetov, Vidmar,  
Bonca, Sushkov, Phys. Rev. B85 (2012) 245113

$$H_{t-J}^{Ising} = \sum_{ij\sigma} t_{ij} d_{i\sigma}^\dagger d_{j\sigma} + J \sum_{\langle ij \rangle} \left[ \left( S_i^z S_j^z - \frac{1}{4} \right) \right. \\ \left. + \lambda \sum_i \left( S_i^z M_i^z + \frac{1}{4} n_i^d \right) \right], \quad \lambda \rightarrow +\infty.$$

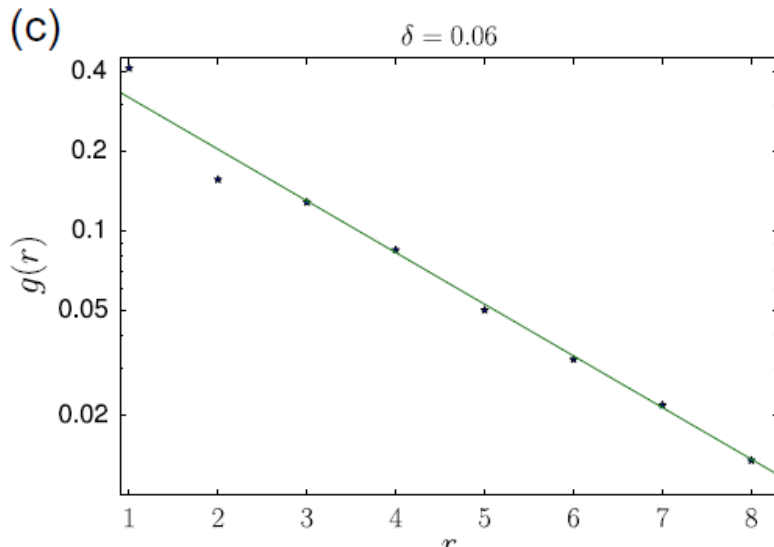
( $Z_2$  global symmetry at  $\forall t, J$ )

# No double occupancy constraint and magnetic correlations in cuprates

Maska, Mierzejewski, Kochetov, *Phil. Mag.* V.95 (2015), 583



The long-range AF order vanishes at hole concentration below 6 %, which remains in a perfect agreement with experimental data on high-temperatures superconductors. This is very impressive result, as many other techniques give much higher values of concentration, at which AF disappears. The main mechanism responsible for the destruction of the long-range



AF order has its origin in the interplay of the hole mobility and minimization of the spin-spin exchange energy.

This strong competition is strictly related to the constraint of no double occupancy.

Distance dependence of the spin-spin correlation function  $g(r)$  for different hole concentrations  $\delta$