Study of ¹⁷Ne in Coulomb/nuclear induced reactions

Yu. Parfenova, L. Grigorenko, I. Egorova, N. Shulgina, M. Zhukov



JINR, Dubna, Russia GSI, Darmstadt, Germany Kurchatov Institute, Moscow, Russia INP MSU, Moscow, Russia Chalmers University of Technology, Gothenburg, Sweden





- Introduction: why do we study ¹⁷Ne
- Combined model 2012
- Results of calculations;
- Conclusions
- Outlook

INTRODUCTION: why do we study ¹⁷Ne •History of ¹⁷Ne study

2p -radioactivity was predicted by V. I.Goldansky in 1960 as an essentially quantum-mechanical phenomenon. True three-body decay, in his terms, occurs when sequential emission of 2p is energetically prohibited and all the final-state fragments are emitted simultaneously. The examples are: ¹⁷Ne, ⁶Be, ⁴⁵Fe, ⁵⁴Zn, ¹⁹Mg, and, maybe, ⁴⁸Ni. All these decays exhibit specific correlation patterns. It is argued that <u>studies of these patterns could provide important information on structure of the decaying nuclei.</u>



Why do we study ¹⁷Ne?

CNO cycle: ${}^{12}C(p, \gamma){}^{13}N(e, v){}^{13}C(p, \gamma){}^{14}N(p, \gamma){}^{15}O(e, v){}^{15}N(p, \alpha){}^{12}C$

the nucleus ¹⁵O => a waiting point for the break-out of the CNO cycle

COMPETITION OF

 $^{15}O(\alpha,\gamma)^{19}Ne(p,\gamma)^{20}Na$

 $^{15}O(2p,\gamma)^{17}Ne(\beta)^{17}F(p,\gamma)^{18}Ne(2p,\gamma)^{20}Mg(\beta)^{20}Na$

				Mg ²⁰	Mg ²¹	Mg ²²	Mg ²³	Mg ²⁴
			Na ¹⁸	N a ¹⁹	Na ²⁰	Na ²¹	Na ²²	Na ²³
		Ne ¹⁶	Ne ¹⁷	Ne ¹⁸	Ne ¹⁹	Ne ²⁰	Ne ²¹	Ne ²²
Τ		F ¹⁵	F ¹⁶	F17	F ¹⁸	F ¹⁹	F ²⁰	F ²¹
	013	014	015	0 ¹⁶	017	O ¹⁸	O ¹⁹	O ²⁰
	N ¹²	N ¹³	N ¹⁴	N15	N ¹⁶	N ¹⁷	N ¹⁸	N ¹⁹
	C11	d	1 13	C14	C15	C ¹⁶	C17	C18
	B ¹⁰	B11	B ¹²	B ¹³	B ¹⁴	B ¹⁵	B ¹⁶	B ¹⁷
L							N	

According to the **detailed balance theorem,** this reaction can be accessed as time-reversal one for E1 Coulomb dissociation of ¹⁷Ne in lead target.

¹⁷Ne+γ -> ¹⁵O+2p

Where the "Soft E1" mode is supposed to be?

M.J. Chromik, et al., PRC 66 (2002) 024313.



The peak corresponds to transitions to the first excited states of ¹⁷Ne. There is no structure above 2 MeV.

In 2-neutron halo nuclei, such as ⁶He and ¹¹Li, the peak is placed at about 1 - 1.5 MeV. Theoretical predictions of L. Grigorenko et.al (PLB **641** (2006) 254) are: 4 MeV.



Where the "Soft E1" mode is supposed to be?

M.J. Chromik, et al., PRC 66 (2002) 024313.



In 2-neutron halo nuclei, such as ⁶He and ¹¹Li, the peak is placed at about 1 - 1.5 MeV. Theoretical predictions of L. Grigorenko et.al (PLB **641** (2006) 254) are: 4 MeV.



The peak corresponds to transitions to the first excited states of ¹⁷Ne. There is no structure above 2 MeV.

CLOSED

Where the "Soft E1" mode is supposed to be?

M.J. Chromik, et al., PRC **66** (2002) 024313. L.V. Grigorenko, et al., PLB **641** (2006) 254



In 2-neutron halo nuclei, such as ⁶He and ¹¹Li, the peak is placed at about 1 - 1.5 MeV. Theoretical predictions of L. Grigorenko et.al (PLB **641** (2006) 254) are: 4 MeV.



The astrophysical reaction rate can be enhanced by few orders of magnitude due to contributions of the non-resonant radiative 2p capture from continuum, for temperatures

T < 0.05-0.08 GK and T > 0.4-1.0 GK

Principally new experimental technique for exotic nucleus studies: LAND-R³B, ALADIN (GSI)

The experimental setup allows kinematically complete measurements. The excitation energy is reconstructed using the invariant mass method.

Low energy spectra in the Coulomb excitation of projectile is available. It was applied to •neutron-rich nuclei (⁶⁸Ni) •proton-rich nuclei (¹⁷Ne) 500 A MeV.



In such experiment an actual problem is how to separate the Coulomb and nuclear contributions, and whether there is the Coulomb/nuclear interference. It is necessary to take into account some exotic features of unstable nuclei that cannot be observed in their stable counterparts. In neutron-rich nuclei, one of these features is the appearance of electric-dipole strength at energies near the neutron separation threshold, located below the well-known Giant Dipole Resonance (GDR), well known in stable species. This new low-lying E1 strength distribution is called Soft E1 mode of excitation, referring to much smaller photoabsorption strength compared to that of the GDR.



⁸He SDM

INTRODUCTION: why do we study ¹⁷Ne?

•History of study of time reverse reaction ${}^{17}Ne+\gamma \longrightarrow {}^{15}O+2p$. Correlation patterns reveals structure.

•Astrophysical aspect of Soft E1 mode studies •Principally new experimental technique for exotic nucleus studies: LAND-R³B, ALADIN (GSI) and data.

•Absence of appropriate model for description of reaction where both Coulomb and nuclear mechanisms acts.

Combined MODEL 2012

- main ingredients
- free parameters are fixed

Model 2012



Assumptions

• in the Bertulani-Bauer model the stepwise function at grazing angle corresponding to nuclaer absorption is replaced by smooth absorption function (no free parameter any more) from the Glauber model.

• strength function for the Coulomb and nuclear excitation is supposed to be similar

• angular distribution in nuclear interaction corresponds to the Coulomb trajectories

 $\mathcal{F}_{abs} = \langle \psi_i | |S_1(\mathbf{b}, \mathbf{r}_1) S_2((\mathbf{b}, \mathbf{r}_2) S_3((\mathbf{b}, \mathbf{r}_3))|^2 |\psi_i \rangle$

<u>In use</u>

- 3-body wave function of ¹⁷Ne obtined with hyperspherical harmonics method
- Glauber model parameters are fitted ^[4] using available experimental data

^[2] Yu. Parfenova, Zhukov, M. V. (2006). *AIP Conf. Proc.*, *September 2005*, 526

Model: Eikonal approximation of the Glauber Model

Assumptions

- $a_V k_{proj} >> 1$, a_V is the range of the potential $V,\,k_{proj}$ is the momentum of projectile

- |V|<<E_{proj}
- Frozen Limit (stright-line trajectories)

Cross sections



Eikonal Approximation of the Glauber model

transition from the ground state with its total angular momentum J to the excited state J' is found as

$$\sigma_{JJ'} = \int d^2 \mathbf{b} \, (\hat{J})^{-2} \sum_{PQ} \sum_{L' l'_x l'_y SS_x} \int X^2 \, dX \int Y^2 \, dY \tag{9}$$

$$\left| \sum_{KL l_x l_y} R^J_{L l_x l_y SS_x}(X, Y) \sum_{\lambda \omega} B^{PQ}_{\lambda \omega}(X, Y, b) C^{l'_x 0}_{l_x 0 \lambda 0} C^{l'_y 0}_{l_y 0 \omega 0} \right|$$

$$\hat{l}_x \hat{l}_y \hat{\lambda} \hat{\omega} \hat{J}' \hat{L} \hat{L}' \hat{S}' \hat{P} \left\{ \begin{array}{cc} L & S & J \\ P & 0 & P \\ L' & S' & J' \end{array} \right\} \left\{ \begin{array}{cc} l_x & l_y & L \\ \lambda & \omega & P \\ l'_x & l'_y & L' \end{array} \right\} \right|^2 - \delta(J, J') \delta(\pi, \pi') \sigma_{JJ}$$

where the final state quantum numbers are denoted by prime. $B_{\lambda\omega}^{PQ} = \sum_{\omega\nu} C_{\lambda\mu\omega\nu}^{PQ} [Y_{\lambda}Y_{\omega}]_{PQ}$ are coefficients of expansion of profile functions in (...) into spherical harmonics.

$$S_{\nu}(b_{\nu}) = \exp\left[\frac{-i}{\hbar v} \int_{-\infty}^{\infty} dz' \ V_{\nu T}\left(\sqrt{b_{\nu}^{2} + z'^{2}}\right)\right]$$

$$\overline{V_{nT}}(r) = -\frac{i}{2}\hbar v \ A_{T} \ \rho_{T}\left(|\vec{r}|\right) \overline{\sigma_{NN}}.$$

$$V_{CT}(r) = \int d^{3} \vec{t} \ A_{C} \ \rho_{C}(|\vec{t}|) V_{\nu T}\left(|\vec{r} - \vec{t}|\right)$$

$$NN \ interaction \ potential$$

$$10 < E < 2000 \ MeV$$

$$S.K.Charagi \ et \ al \ PRC41(1990)1610$$

$$L.Ray \ PRC20(1979)1857$$

Eikonal Approximation of the Glauber model

transition from the ground state with its total angular momentum J to the excited state J' is found as

$$\sigma_{JJ'} = \int d^2 \mathbf{b} \, (\hat{J})^{-2} \sum_{PQ} \sum_{L' l'_x l'_y SS_x} \int X^2 \, dX \int Y^2 \, dY \tag{9}$$

$$\left| \sum_{KL l_x l_y} R^J_{L l_x l_y SS_x}(X, Y) \sum_{\lambda \omega} B^{PQ}_{\lambda \omega}(X, Y, b) C^{l'_x 0}_{l_x 0 \lambda 0} C^{l'_y 0}_{l_y 0 \omega 0} \right|_{\mathcal{I}} d\hat{J}' \hat{L} \hat{L}' \hat{S}' \hat{P} \left\{ \begin{array}{cc} L & S & J \\ P & 0 & P \\ L' & S' & J' \end{array} \right\} \left\{ \begin{array}{cc} l_x \ l_y \ L \\ \lambda \ \omega \ P \\ l'_x \ l'_y \ L' \end{array} \right\} \right|^2 - \delta(J, J') \delta(\pi, \pi') \sigma_{JJ}$$

where the final state quantum numbers are denoted by prime. $B_{\lambda\omega}^{PQ} = \sum_{\omega\nu} C_{\lambda\mu\omega\nu}^{PQ} [Y_{\lambda}Y_{\omega}]_{PQ}$ are coefficients of expansion of profile functions in (...) into spherical harmonics.

$$S_{\nu}(b_{\nu}) = \exp\left[\frac{-i}{\hbar v} \int_{-\infty}^{\infty} dz' \ V_{\nu T}\left(\sqrt{b_{\nu}^{2} + z'^{2}}\right)\right]$$

$$\overline{V_{nT}}(r) = -\frac{i}{2}\hbar v \ A_{T} \ \rho_{T}\left(|\vec{r}|\right) \overline{\sigma_{NN}}.$$

$$V_{CT}(r) = \int d^{3} \vec{t} \ A_{C} \ \rho_{C}(|\vec{t}|) V_{\nu T}\left(|\vec{r} - \vec{t}|\right)$$

$$NN \ interaction \ potential$$

$$10 < E < 2000 \ MeV$$

$$S.K.Charagi \ et \ al \ PRC41(1990)1610$$

$$L.Ray \ PRC20(1979)1857$$

Eikonal Approximation of the Glauber model PARAMETERS

Data of Ozawa, R. Kanungo etc.



¹⁷Ne wave function <u>3-cluster wave function</u> (¹⁵O+p+p)

(obtained with Schrödinger equation with nucleon-cluster potential) Reproduce the rms of ¹⁷Ne, magnetic moment, quadrupole model Reproduce the binding energy of ¹⁷Ne 0.963 MeV **Problems:** what is the s/d ratio in the partial waves? (we used 3 wave functions with s/d 7%,50%,70%)

Bertulani & Bauer Model of Coulomb excitation



Comparison with experimental data M.J. Chromik, et al., PRC 66 (2002) 024313.

Table 2: Population of the states $3/2^-$ ($E_T=1.228$ MeV) and $5/2^-$ ($E_T=1.764$ MeV) in the reaction ${}^{17}\text{Ne}+{}^{197}\text{Au}$ at the ${}^{17}\text{Ne}$ energy 48.4 A MeV, and theoretical estimates of the population in the reaction ${}^{17}\text{Ne}+{}^{208}\text{Pb}$ at the ${}^{17}\text{Ne}$ energy 500 A MeV.

	Energy	$1/2^- \to 3/2^-$		$1/2^{-} \rightarrow 5/2^{-}$
	of ^{17}Ne	E2, E_{γ} =1.288 MeV	M1, E_{γ} =1.288 MeV	E2, $E_{\gamma} = 1.764 \text{ MeV}$
	A MeV	σ mb	σ mb	σ mb
Our calc.	48.4	15.68	0.25	29.7
Chromik et al $[13]$	48.4	$11.9^{3.3}_{-4.5}$	0.24 ± 0.1	29.9 ± 4

Strength function in PWIA using Green Function method

$$\frac{dB_{E1}}{dE} = \frac{j(E)}{2\pi} = 2\frac{2J_f + 1}{2J_i + 1} \left(\frac{2}{\pi}\right)^2 \sqrt{\mu_X \mu_Y} \int_0^{\pi/2} d\vartheta |A(\varepsilon(\vartheta))|^2$$

where $|A(\varepsilon(\vartheta))|^2 = \sum_{SS_x} ||\sum_{KLl_x L_y} A_{KLl_x L_y SS_x}|^2|$ the amplitude is found as
 $A_{KLl_x L_y SS_x}(\varepsilon) = Z_{eff} < J_f ||Y_1(\hat{\mathbf{Y}})||J_i > C^{(n)} \int_0^{\infty} dX \int_0^{\infty} dY \phi_X(k_X, X) \phi_Y(k_Y, Y) Y \Psi_{KLl_x L_y SS_x}(X, Y)$

L.V. Grigorenko, et al., PLB 641 (2006) 254



Strength functions [sp] and [dp] in 17 Ne Resonances in 16 F (s,d waves) 0.535 MeV 0⁻ 0.738 MeV 1⁻ 0.959 MeV 2⁻ 1.256 MeV 3⁻ 5.856 MeV 2⁻

Comparison with other calculations Strength function

Collective model calculations 0.16 0.14 0.12 0.08E (MeV)

T.Oishi, et al PRC 84(2011) 057301

Sum rule $S_0=1.206$

¹⁷Ne

L.V. Grigorenko, et al., PLB 641 (2006) 254



Sum rule: WF08 S₀=0.822 fm² WF48 S₀=1.42 fm² WF70 S₀=1.62 fm²

RESULTS: excitation spectrum of ¹⁷Ne and correlations

There is a bump at 4-5 MeV
Energy spectra in different targets are not similar due to difference in s- and d- wave contributions (?)



Coulomb s/d 20 Nuclear s/d 1



Nuclear & Coulomb SDM in ¹⁷Ne: **cross sections** σ , mb (max at 4.0 MeV)

value	Pb target	Si target	C target
Coulomb total	415 17		3.2
Coulomb Soft E1	386	15	3.0
Coulomb s-wave	368	14.3	2.86
Coulomb d-wave	18	0.71	0.14
Nuclear total	35	13	12
Nuclear Soft N1	1.2	0.5	0.4
Nuclear s-wave	0.1	0.04	0.03
Nuclear d-wave	0.05	0.02	0.016
100 Pb target 00 C+N, s-wav 00 C-N s-wav 00 C-N d-wav 00 C+N total 00 C-N total	de do/dE1, mb/Me e do/dE1, mb/Me e do/dE1, mb/Me	Si target 1,0 - C+N, s-wave	C target C+N, s-wave C-N s-wave C+N d-wave C+N d-wave C-N d-wave C+N total C-N total

 E_{τ} , MeV

15

20

і 10

5

0,2

0,0

Ó

5

20

10

E_T, MeV

15

0

0

20

15

20

0

ò

5

10

 E_{T} , MeV

Nuclear & Coulomb SDM in ^{17}Ne : cross sections σ , mb

value	Pb target	Si target	C target
Coulomb total	415	17	3.2
Coulomb Soft E1	386	15	3.0
Coulomb s-wave	368	14.3	2.86
Coulomb d-wave	18	0.71	0.14
Nuclear total	35	13	12
Nuclear Soft N1	1.2	0.5	0.4
Nuclear s-wave	0.1	0.04	0.03
Nuclear d-wave	0.05	0.02	0.016
	1	1	



Coulomb SDM in ¹⁷Ne: energy spectrum







Excitation spectrum of ¹⁷Ne and correlations



Results and discussion

Important results

- The "Soft E1" mode shows to have maximum at 4 MeV. Here the result of theoretical calculaions and that after the MC simulation procedure.
- The excitation energy spectrum of ¹⁷Ne is well reproduced with d-wave contribution of the state at the energy 2.987 MeV.
- Mass number dependences of nuclear- and Coulomb dissociation is essentially different, that should be taken into account when separation their contribution.



Conclusions

• 2p- halo nucleus exhibits "**Soft E1**" **mode of excitation**, and the peak position is higher than that for the 2n- halo nuclei (GLOBAL conclusion).

- Contribution of the Coulomb **Soft E1** excitation in ¹⁷Ne in **C** target **dominates**.
- Due to negligibly small contribution of nuclear Soft N1 excitation the **Coulomb/nuclear interference** (if it is) in the Pb target is **less** than experimental errors (few percent). The interference is probable in the C target.
- In the Coulomb Soft E1 excitation, the s-wave states population dominates (by an order of magnitude) that for d-wave states. In the nuclear one, the s/d ratio is about unity.
- To reproduce the internal energy-angular correlation we need to suppose the excited ¹⁷Ne states with [dp] structure.
- The energy spectra of ¹⁷Ne excitation in C and Pb targets are not similar.

What is done

• We suggest a self-consistent approach for calculations of Coulomb/nuclear –induced dissociation of clustered nuclei for reactions at the nuclear surface.

• Mass number dependence of nuclear and Coulomb dissociation is essentially different, that should be taken into account when separation their contribution.

Nearest plans

•to analyze the angular distributions of fragments (we are working on now)

• to clarify the origin of the hypothetic states, we need for best description;

• to take into account for p-removal in 15O diffraction dissociation (estimated to be up to 30% of nuclear dissociation cross section)

• to calculate the strength function for nuclear- induced excitation of ¹⁷Ne



Nuclear & Coulomb SDM in ¹⁷Ne: angular distribution



Modes of two-proton radiative capture













Nuclear & Coulomb SDM in ^{17}Ne : cross sections σ , mb

value	Pb target	Si target	C target
Coulomb total	415 / 380	17 /16	3.2
Coulomb Soft E1	386/342	15 /14	3.0
Coulomb s-wave	368/326	14.3/13.3	2.86
Coulomb d-wave	18/16	0.71/0.67	0.14
Nuclear total	35	13	12
Nuclear Soft N1	1.2	0.5	0.4
Nuclear s-wave	0.1	0.04	0.03
Nuclear d-wave	0.05	0.02	0.016



Nuclear & Coulomb SDM in ^{17}Ne : cross sections σ , mb

value	Pb target	Si target	C target
Coulomb total	415 / 380	17 /16	3.2
Coulomb Soft E1	386/342	15 /14	3.0
Coulomb s-wave	368/326	14.3/13.3	2.86
Coulomb d-wave	18/16	0.71/0.67	0.14
Nuclear total	35	13	12
Nuclear Soft N1	1.2	0.5	0.4
Nuclear s-wave	0.1	0.04	0.03
Nuclear d-wave	0.05	0.02	0.016









2-body model of ¹⁷Ne



PRC84 e057301



Figure 1: Classification scheme of dipole excitations in ⁶He and ⁶Be prodused in charge-exchange reactions with ⁶Li [1]. The appearance of the soft dipole mode in the electromagnetic excitation of ⁶He is shown for comparison. Given is the illustration of difference between the cluster excitations (modes), i.e. the soft dipole mode (SDM) and isovector soft dipole mode (IVSDM), and the collective excitations (resonances), i.e. the giant dipole resonance (GDR) and spin-dipole resonance (SDR).



THANK YOU!!!

"Soft E1" mode in proton dripline nuclei

- Existence of "soft E1" mode now established in neutron-rich nuclei (⁶He, ¹¹Li).
- Cluster sum rule exhausted within several MeV above 2p threshold.
- > Possibility of "soft E1" in proton-dripline nuclei.
- > Calculations predict a strong and narrow E1 peak in 17 Ne.
- **The 2p capture rate is dominated by the nonresonant E1 for**

T < 0.05-0.08 GK and T > 0.4-1.0 GK

In 2p halo nuclei, the "soft E1" peak is placed higher in that in 2n halo nuclei (analogy with ⁶Be ⁶He and ⁶Be A.S. Fomichev et al PLB 708 (2012) 6







2-body model of ¹⁷Ne



