

Production of Tetraquark States in the e^+e^- Collisions

Makoto Oka
Tokyo Institute of Technology

July 15, 2013

**The 7th APCTP-BLTP JINR Joint Workshop Modern
Problems in Nuclear and Elementary Particle Physics**

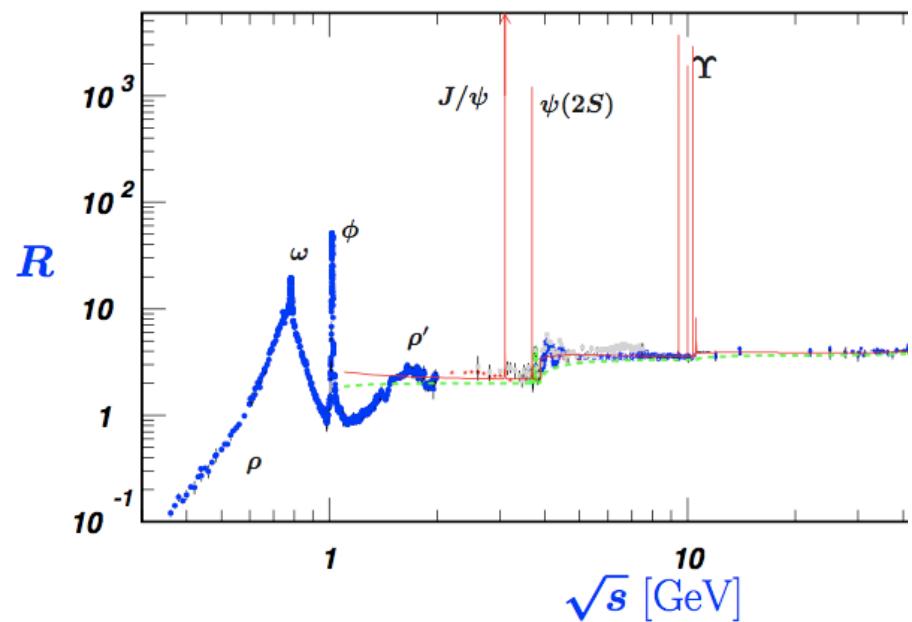
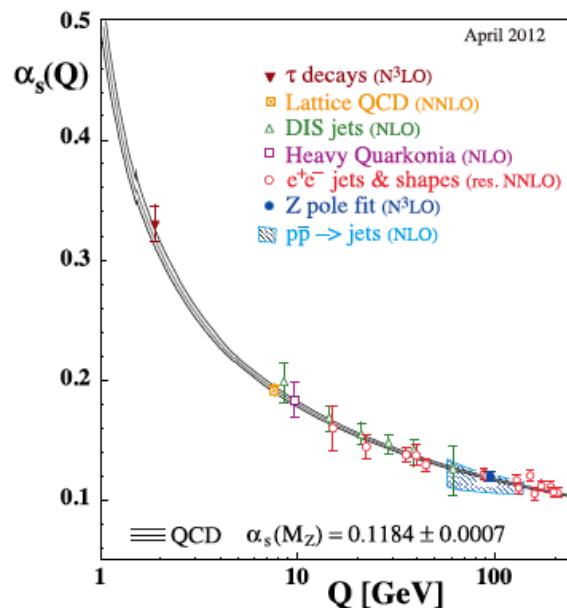
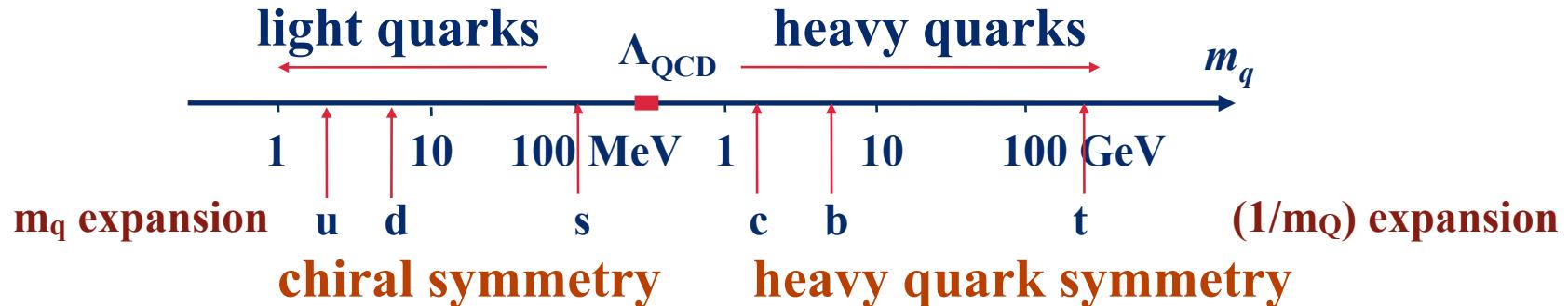
Irkutsk Region, Bolshiye Koty

Contents

- 1. Heavy quark dynamics**
- 2. Heavy baryon spectroscopy**
- 3. Heavy Tetraquark T_{cc}**
- 4. Production of Heavy Tetraquark in $e^+ e^-$ collisions**
- 5. Fragmentation of QQ into hadrons**

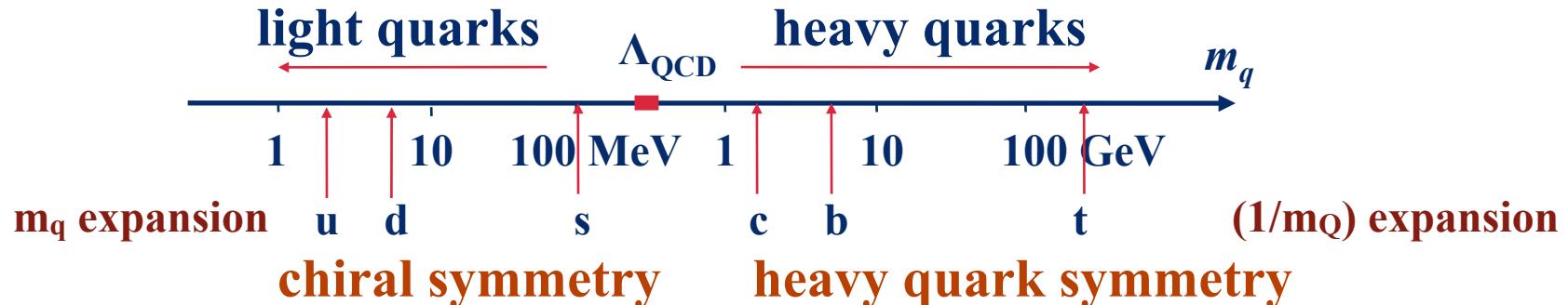
From Strangeness to Charm/Bottom

$\Lambda_{\text{QCD}}(\sim 300 \text{ MeV}) \ll m_c(\sim 1.3 \text{ GeV}) \ll m_b(\sim 4.2 \text{ GeV})$



From Strangeness to Charm/Bottom

- # $\Lambda_{\text{QCD}}(\sim 300 \text{ MeV}) \ll m_c(\sim 1.3 \text{ GeV}) \ll m_b(\sim 4.2 \text{ GeV})$

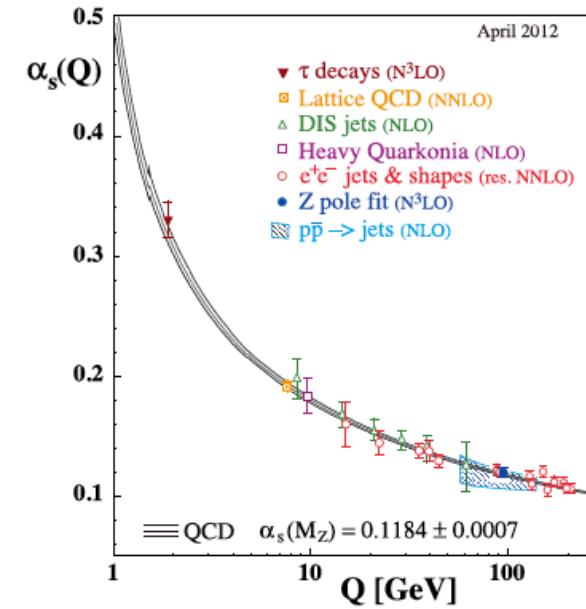


- # LQ: Dynamically generated mass

$$m_q \sim \Lambda_{\text{QCD}} \sim 300 \text{ MeV}$$

Strongly Correlated/ Non-perturbative

- # HQ: Small $\alpha_s \sim v/c \sim 0.3$ for charm
Perturbative/ Non-relativistic

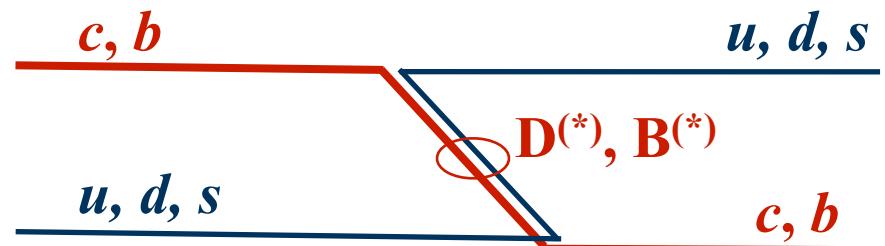


Dynamics of Heavy Quarks

Dynamics of Heavy Quarks

Several important properties of HQ interactions:

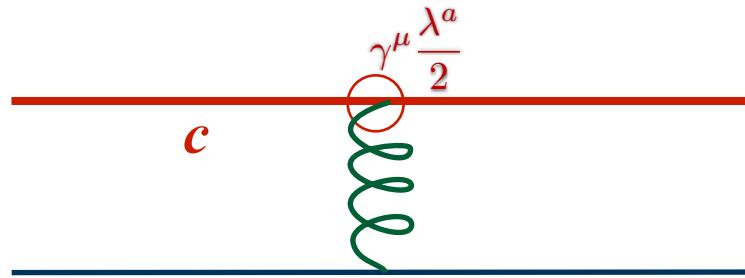
1. Heavy flavor exchanges are suppressed



The large masses of HQ mesons, $m(D, B) \gg m(\pi, K, \rho)$, make the HQ exchange forces suppressed by $O(1/m_Q)^2$. The interaction of the HQ hadrons is dominated by light hadron exchanges.

Dynamics of Heavy Quarks

2. Magnetic gluon coupling is suppressed



$$\bar{\Psi} \gamma^\mu \frac{\lambda^a}{2} \Psi A_\mu^a \sim \boxed{\Psi^\dagger \frac{\lambda^a}{2} \Psi A_0^a} - \boxed{\Psi^\dagger \sigma \frac{\lambda^a}{2} \Psi \cdot \frac{1}{m_Q} (\nabla \times A^a)}$$

(Color Electric coupling) \gg (Color Magnetic coupling)

HQ spin-flip amplitudes are suppressed by $(1/m_Q)$.

\Rightarrow Heavy Quark Spin Symmetry

Dynamics of Heavy Quarks

HQ spin symmetry

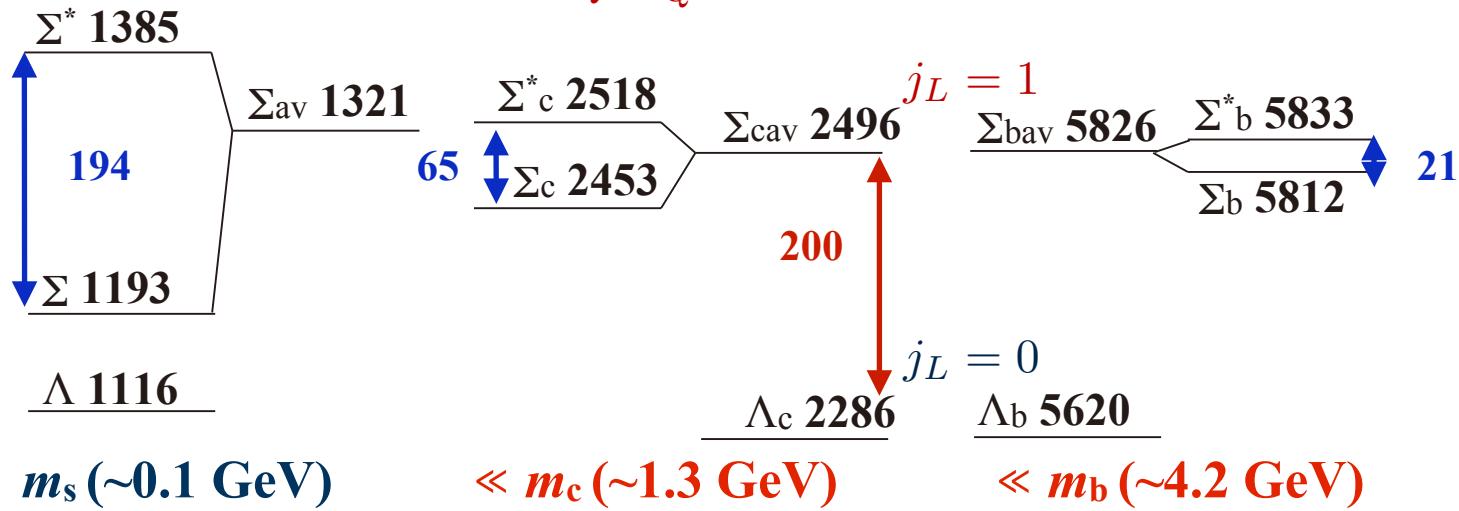
$$[S_Q, H] = O\left(\frac{1}{m_Q}\right)$$

$$\begin{matrix} Q \\ q \end{matrix} \quad \overline{\textcolor{red}{\rule{1cm}{0pt}}} \quad \} \quad \vec{J} = \vec{S}_Q + \vec{j}_L \quad \quad \vec{j}_L = \vec{S}_q + \vec{L}_q$$

$J = j_L \pm \frac{1}{2}$ states are degenerate in the HQ limit.

$$j_L = 0 \longrightarrow \Lambda_Q$$

$$j_L = 1 \longrightarrow \Sigma_Q, \Sigma_Q^*$$

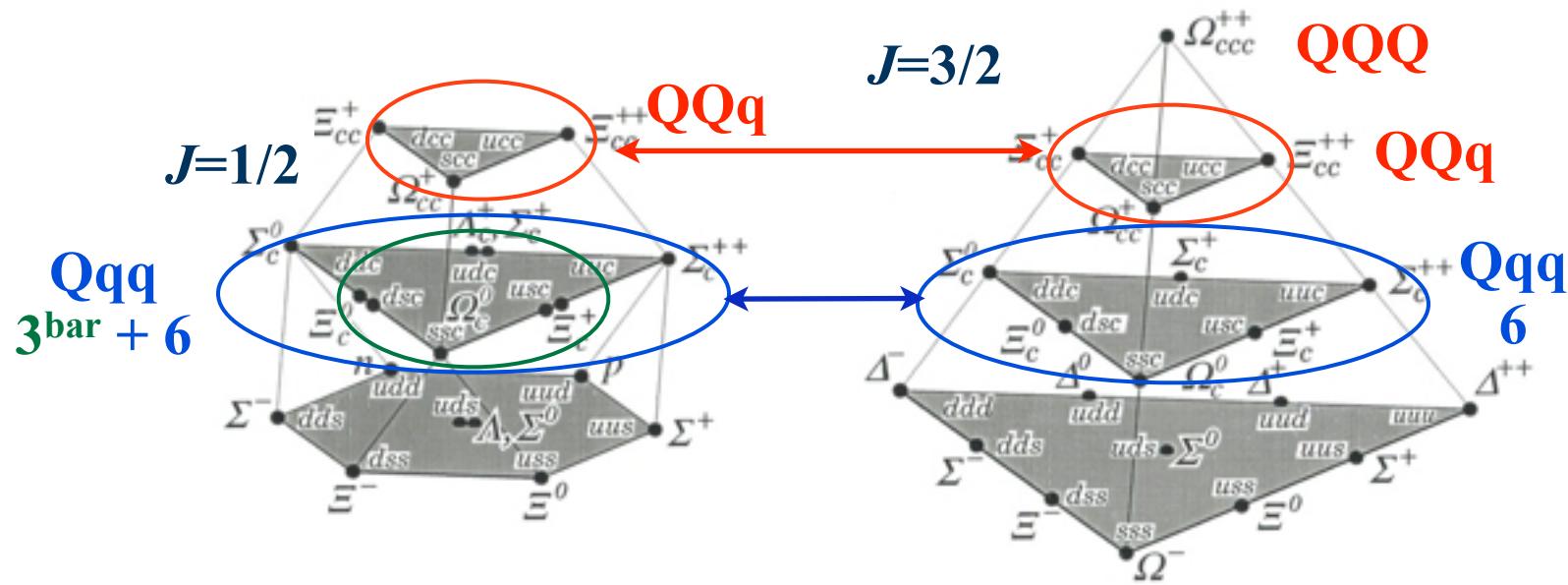


Dynamics of Heavy Quarks

- # Light Baryons: qqq color singlet (color antisymmetric)
 $SU(6)$ 56 dim. $L=0, (8, S=1/2) + (10, S=3/2)$
 - # Heavy Baryons: HQ spin symmetry

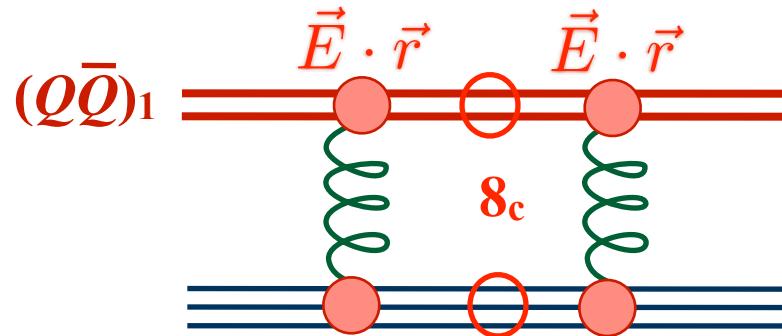
$$Q\bar{q}q \Rightarrow (3^{\text{bar}}, J=1/2) + (6, J=1/2) + (6, J=3/2)$$

$$\text{QQq} \Rightarrow \boxed{(3, J=1/2) + (3, J=3/2)}$$

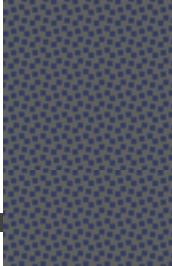


Dynamics of Heavy Quarks

3. Pure HQ hadrons have attractive interaction with matter.



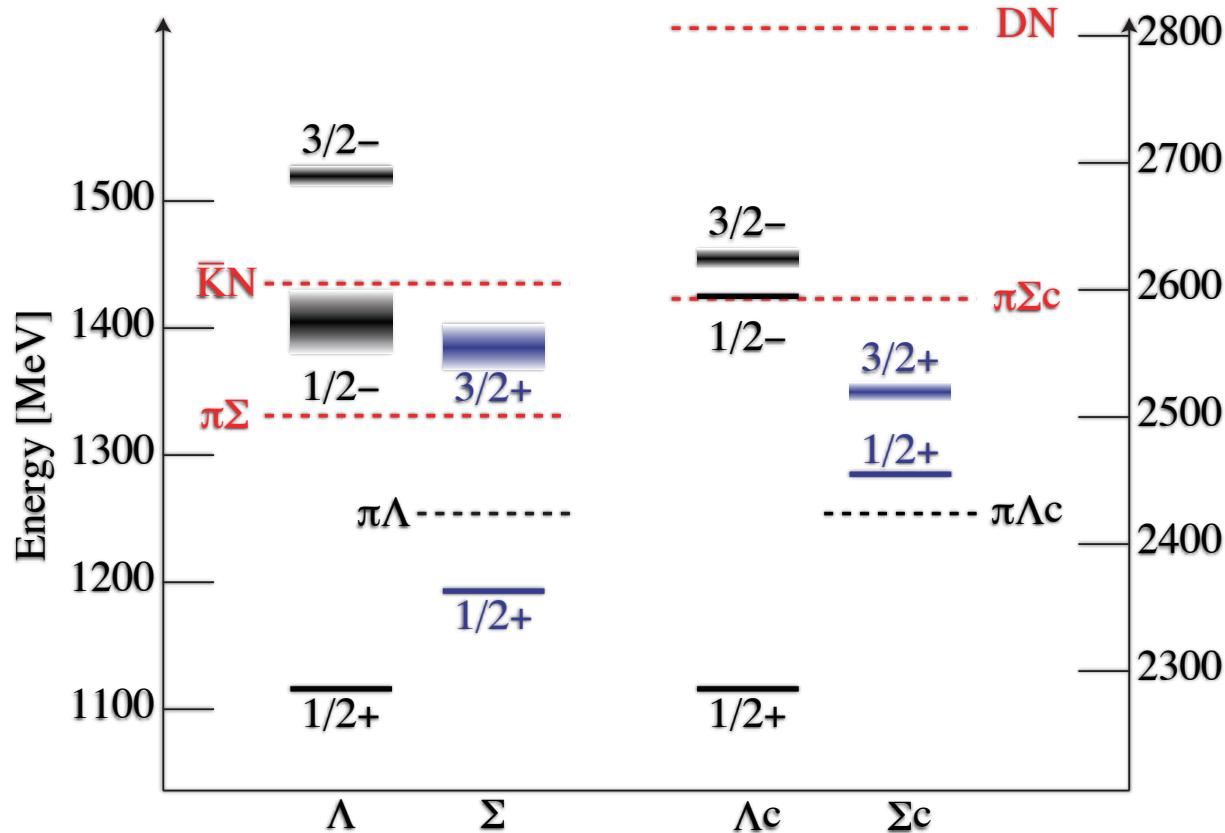
Color-van-der-Waals force \sim second order perturbation \sim
is (weakly) attractive. $V \sim -\frac{\alpha_s^2}{R^5}$



Heavy Baryon Spectroscopy

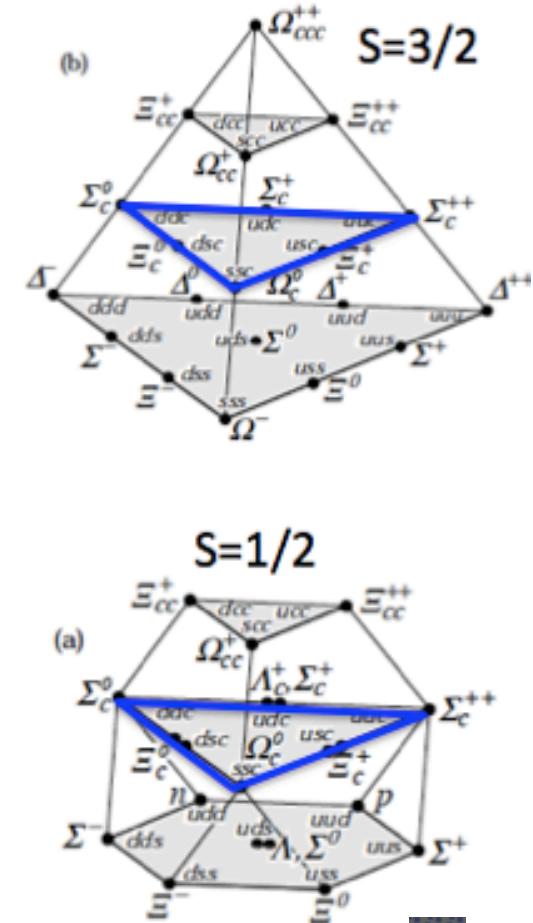
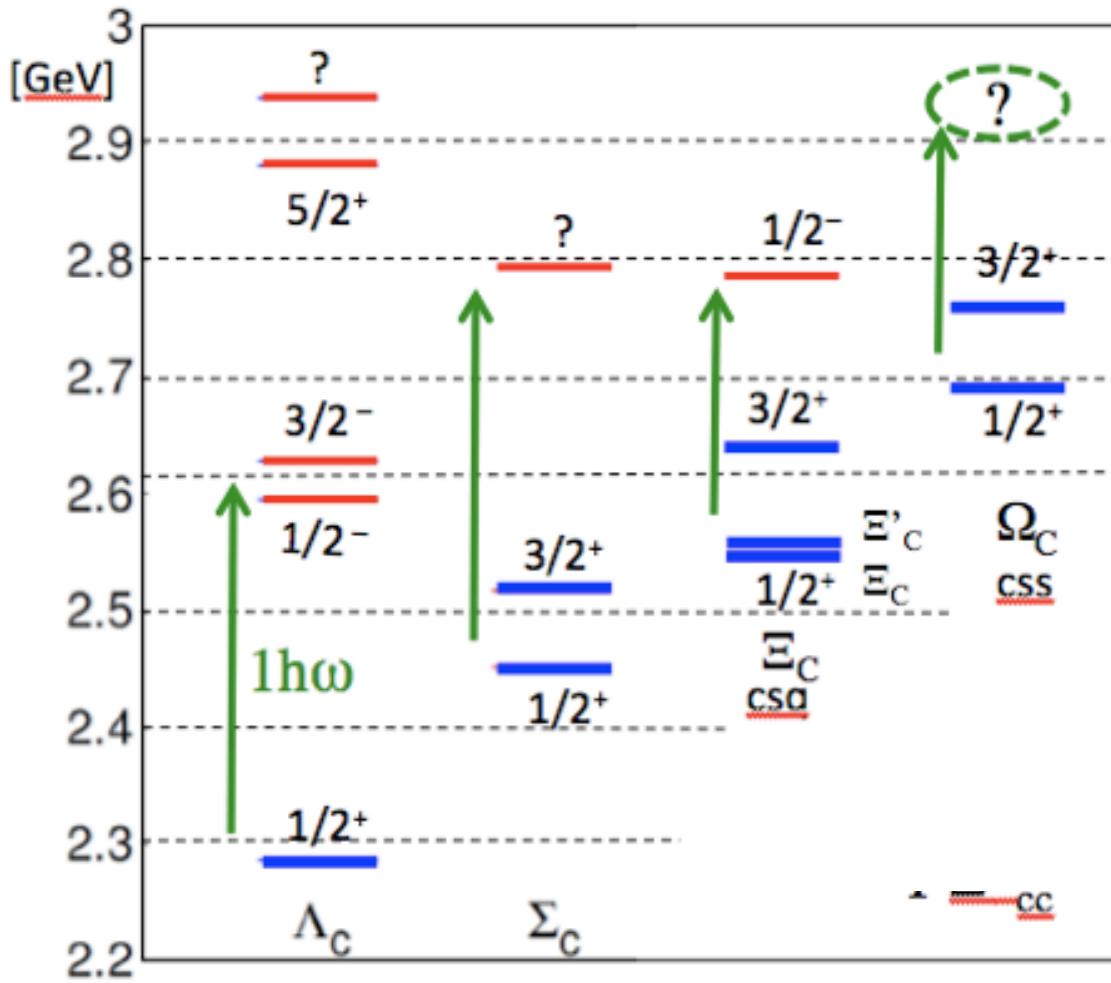
Heavy Baryon Spectroscopy

Heavy baryon spectrum looks simpler.
The higher thresholds make the heavy baryon excited states narrower. → No or small overlapping



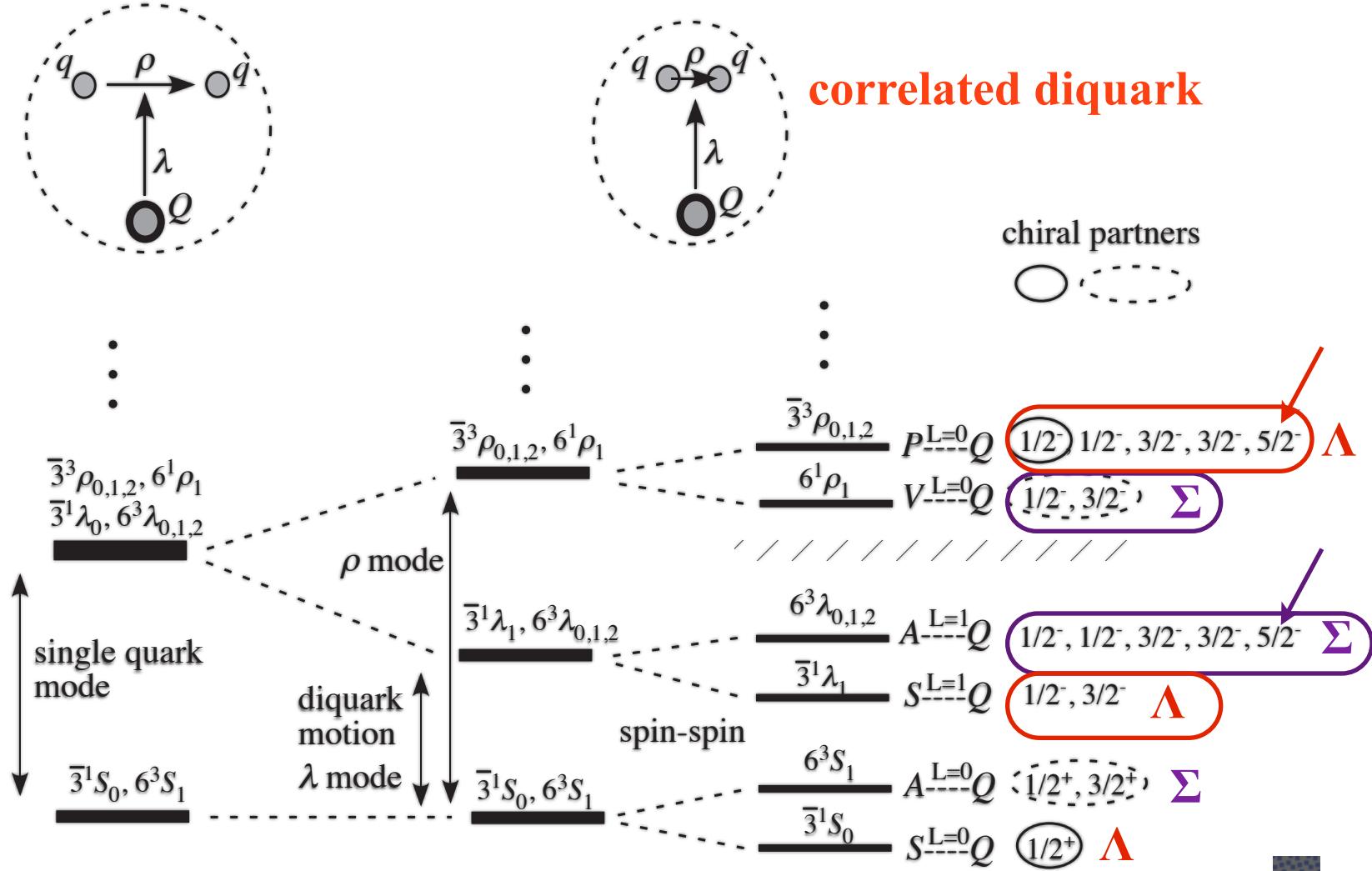
Heavy Baryon Spectroscopy

Many “*missing*” resonances



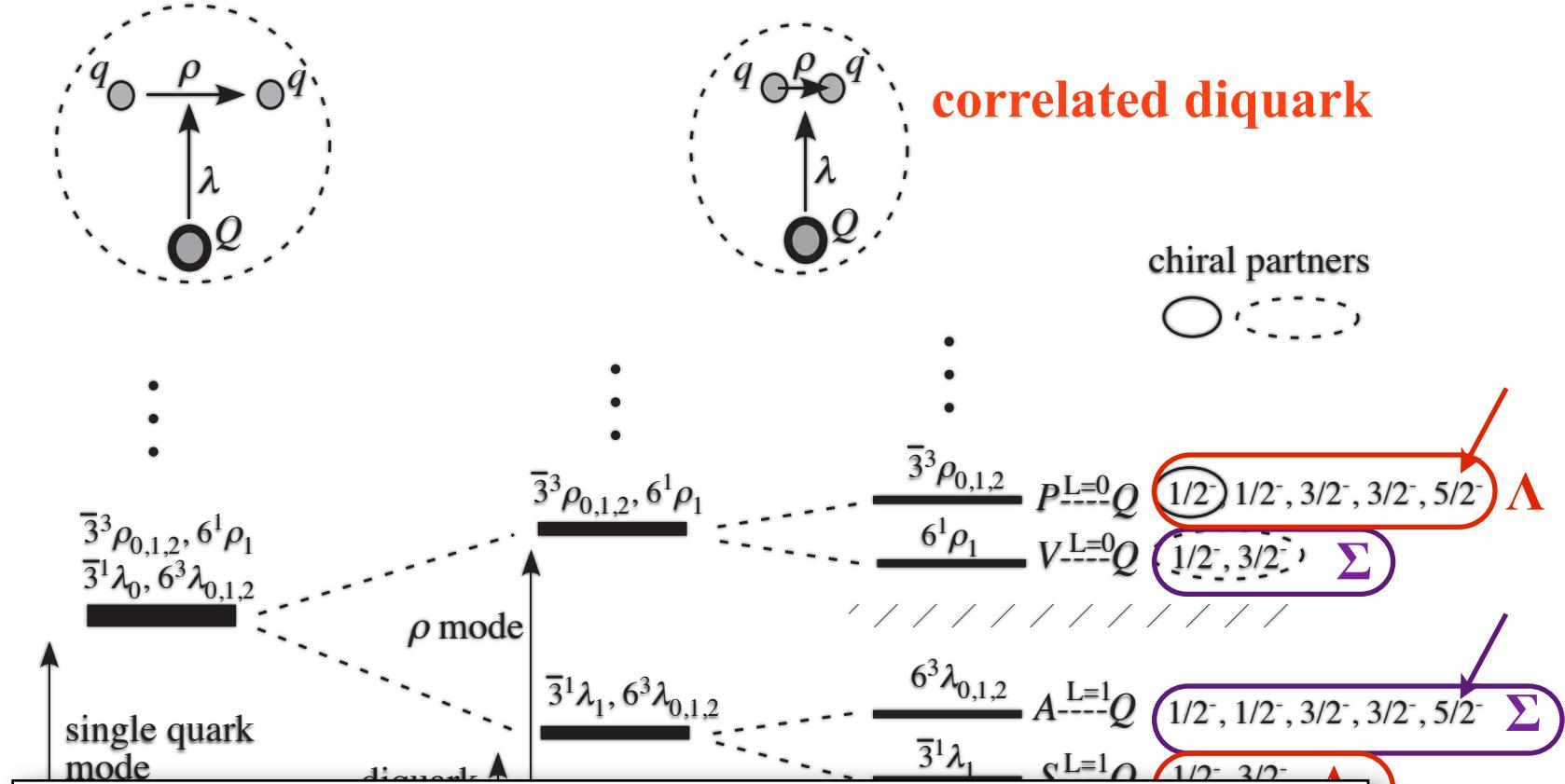
Heavy Baryon Spectroscopy

Two kinds of excitation modes



Heavy Baryon Spectroscopy

Two kinds of excitation modes



Similarly,
QQq baryons \rightarrow spectrum of a (constituent) quark

Diquarks in QCD

- # QCD predicts attraction in the channels:
 - PS meson $q\text{-}q^{\bar{}} : \text{color 1, spin-parity } 0^-, \text{ flavor 1+8}$
 - S *good* diquark $qq : \text{color 3}^{\bar{}} : \text{spin-parity } 0^+, \text{ flavor 3}^{\bar{}}$
- $U = [\bar{d}\bar{s}]_{C=3, J=0, F=3}, \quad D = [\bar{s}\bar{u}]_{3,0,3}, \quad S = [\bar{u}\bar{d}]_{3,0,3}$
- diquark “meson” d d^{bar} (tetra-quark)
- di-diquark “baryon” d-d-q (pentaquark)
- tri-diquark “dibaryon” d³ (6 quarks)
color 1, flavor 1, 0⁺⁺ H dibaryon
 $H = [\bar{U}\bar{D}\bar{S}]_A = [uddss]$
- diquark matter: color superconductivity
 $U^{\bar{}} + D^{\bar{}} + S^{\bar{}}$ condensates:
color-flavor locking (CFL)
 $S^{\bar{}} : \text{2SC} \quad (U^{\bar{}} : \text{uSC} \quad D^{\bar{}} : \text{dSC})$

Diquarks in QCD

		J^π	color	flavor
Pseudoscalar	$\epsilon_{abc}(u_a^T C d_b)$	0^-	$\bar{3}$	$\bar{3} \ (I = 0)$
Scalar (S)	$\epsilon_{abc}(u_a^T C \gamma^5 d_b)$ <i>good</i>	0^+	$\bar{3}$	$\bar{3} \ (I = 0)$
Vector	$\epsilon_{abc}(u_a^T C \gamma^\mu \gamma^5 d_b)$	1^-	$\bar{3}$	$\bar{3} \ (I = 0)$
Axial V. (A)	$\epsilon_{abc}(u_a^T C \gamma^\mu d_b)$ <i>bad</i>	1^+	$\bar{3}$	$6 \ (I = 1)$
	$\epsilon_{abc}(u_a^T C \sigma^{\mu\nu} d_b)$	$1^+, 1^-$	$\bar{3}$	$6 \ (I = 1)$
Color 6 only in Exotic Hadrons	$(u_a^T C d_b) + (a \leftrightarrow b)$	0^-	6	$6 \ (I = 1)$
	$(u_a^T C \gamma^5 d_b) + (a \leftrightarrow b)$	0^+	6	$6 \ (I = 1)$
	$(u_a^T C \gamma^\mu \gamma^5 d_b) + (a \leftrightarrow b)$	1^-	6	$6 \ (I = 1)$
	$(u_a^T C \gamma^\mu d_b) + (a \leftrightarrow b)$	1^+	6	$\bar{3} \ (I = 0)$
	$(u_a^T C \sigma^{\mu\nu} d_b) + (a \leftrightarrow b)$	$1^+, 1^-$	6	$\bar{3} \ (I = 0)$

Diquarks in QCD

- # Diquarks in some lattice calculations
 - Hess, Karsch, Laermann, Wetzorke, PR D58, 111502 (1998)
from the correlators in the Landau gauge
 $m_q \sim 342$ MeV, $M(S) \sim 694$ MeV, $M(A) \sim 810$ MeV
 - Alexandrou, de Forcrand, Lucini, PRL 97, 222002 (2006)
gauge invariant calculation inside a Qqq system
 $M(A) - M(S) \sim 100-150$ MeV, $R(S) \sim 1$ fm
 $M(PS) - M(S) \sim 600$ MeV
 - Babich, et al., PR D76, 074021 (2007)
diquark correlation and effective mass in the Landau gauge
 $M(S) - 2m_q \sim -200$ MeV, $M(A) - M(S) \sim 162$ MeV

Double Charm Exotics

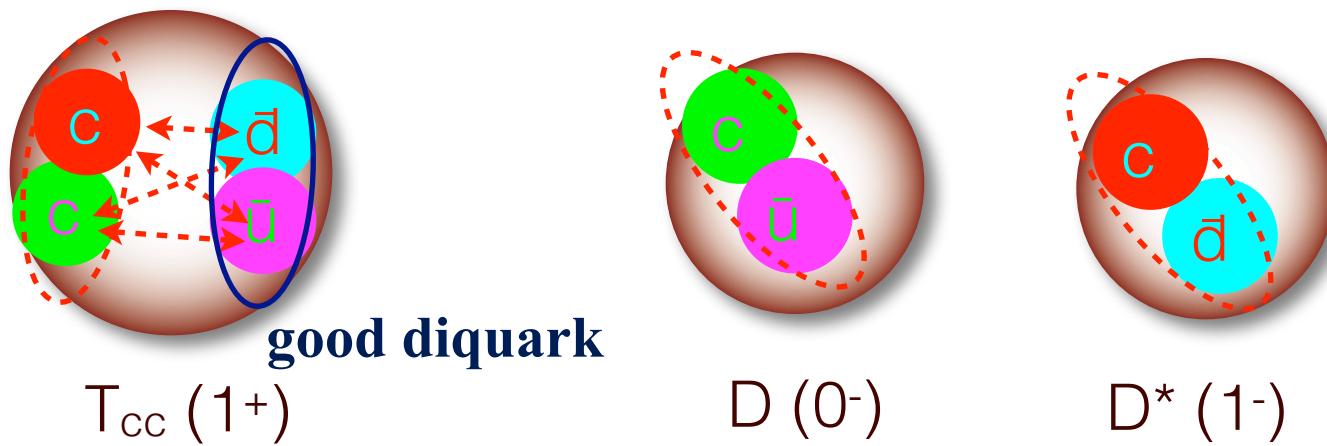
Tetraquark T_{cc}

Exotic Multiquark Heavy Hadrons

- # **New Exotic Multiquark states discovered at the B factories.**
 - X(3872): D-D* molecule with cc^{bar} component**
 - Y(4260): cc^{bar}g hybrid meson candidate**
 - Z_c(3900), Z_c(4430): charged charmonium-like tetraquarks**
 - Z_b(10610), Z_b(10650): bottom siblings**
- # **Prediction of Double charm meson i.e. c-c-q^{bar}-q^{bar} based on the diquark correlations**
 - S. H. Lee, S. Yasui, W. Liu, C. M. Ko, Eur. Phys. J. C54, 259-265 (2008),
 - S. H. Lee, S. Yasui , Eur. Phys. J. C64, 283-295 (2009).
- # **Various studies have been made.**
 - S. Zouzou, B. Silvestre-Brac, C. Gignoux, J.M. Richard,
Z. Phys. C30 (1986)457**
 - H.J. Lipkin, Phys. Lett. B172 (1986) 242, and so on.**

T_{cc} spectrum

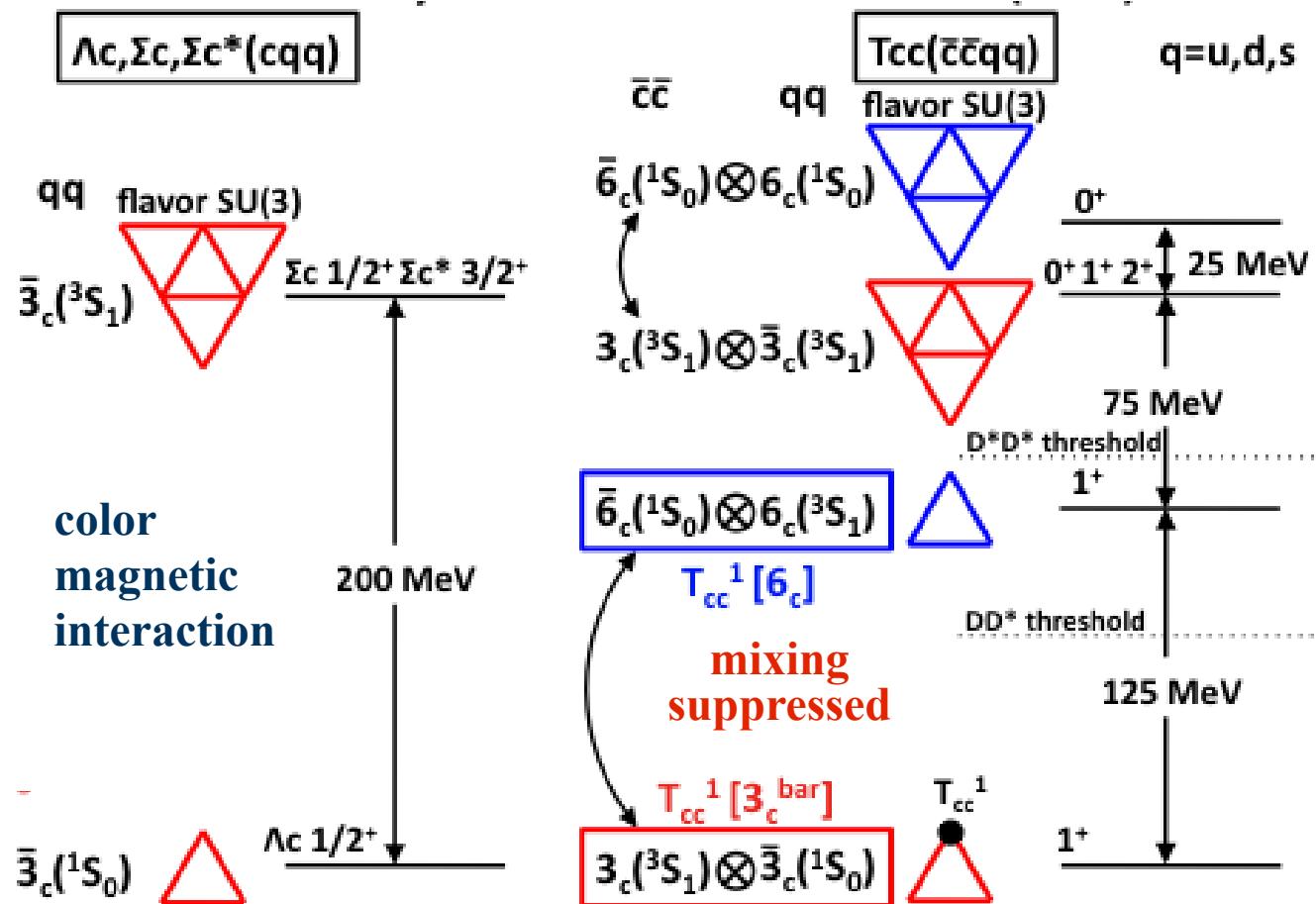
- # Double charm meson T_{cc} ($c\bar{c}c\bar{c}ud$, 1^+ , $I=0$)
 - stable against strong decay if $M(T_{cc}) < M(D) + M(D^*)$



- # Spin dependent force between the HQ and light quark is weak.

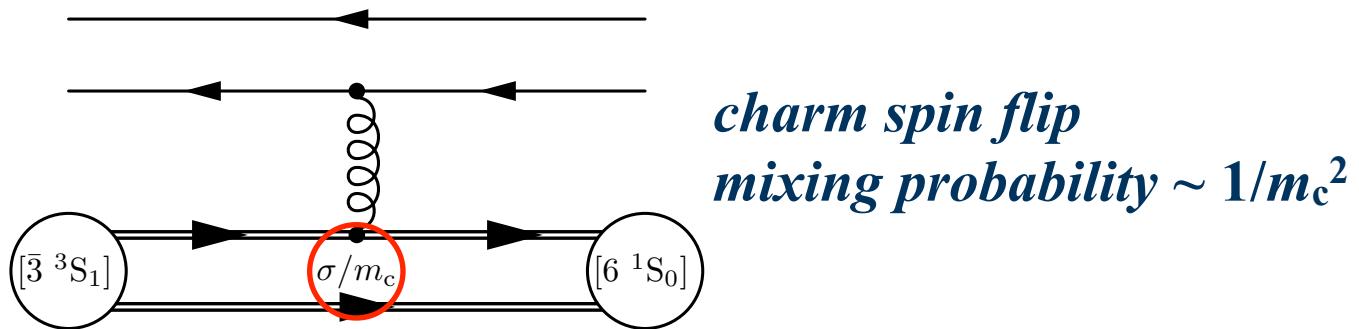
T_{cc} spectrum

Double charm meson T_{cc} ($c\bar{c}c\bar{c}ud$, 1⁺, I=0) spectrum



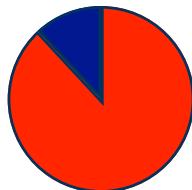
T_{cc} spectrum

- # The lowest two states, T_{cc}[3, ³S₁], T_{cc}[6, ¹S₀], have $I(J^P) = 0(1^+)$, and in principle mix with each other.
However, the mixing is suppressed in the HQ limit as $\sim 1/m_Q$.



- # Dynamical 4-quark calculation:
J. Vijande, A. Valcarce, PRC80, 035204

- Fraction: $\bar{3}$ (0.881) v.s. 6 (0.119) for the ground state.

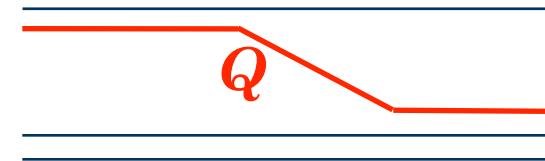


T_{cc}[3, ³S₁] and T_{cc}[6, ¹S₀] are well separated.

Production of T_{cc} in e^+e^- collisions

How can we produce them?

- # Charm (bottom) hadrons can be produced analogously to the *strangeness* hadron production flavor transfer, ex. (K^- , π)
 - (D , π), (D , N) etc.



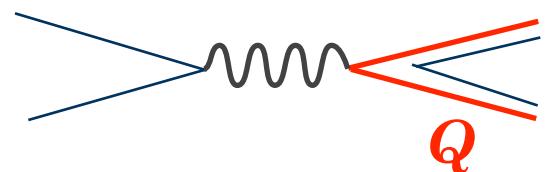
pair creation in hadronic reactions, ex. (π , K)

- (π , $D^{(*)}$), ($p^{\bar{b}ar}$, $D^{(*)}$) etc.



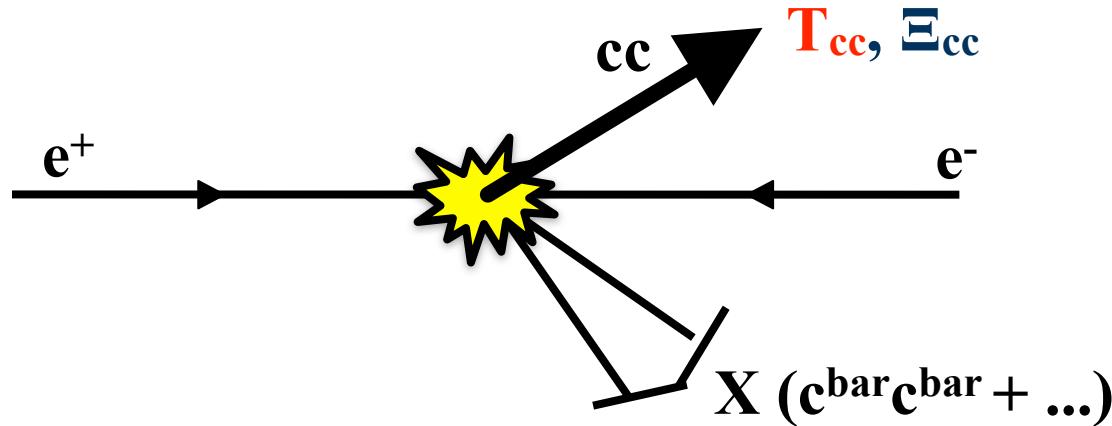
pair creation at high energy

- (e^+e^- , $QQ^{\bar{b}ar}$), ($qq^{\bar{b}ar}$, $QQ^{\bar{b}ar}$)



Production in $e^+ e^-$ collisions

- # $e^+ e^-$ collisions at Belle (KEKB; B-factory)
Double-charm productions ($J/\psi + \eta_c$, ...) have been observed.
K. Abe, et al, Belle Collaboration, Phys. Rev. Lett. 89, 142001 (2002)
- # Recombination of the charm quarks and antiquarks will produce double charmed mesons (T_{cc} 's) and baryons (Ξ_{cc}).



- # Calculate the cross sections of double charmed hadrons.

Cross section

- # Production of doubly charmed tetraquarks with exotic color configurations in electron-positron collisions,
T. Hyodo, Y.-R. Liu, M. Oka, K. Sudoh, S. Yasui
Physics Letters B721 (2013) 56-60,
and in preparation.
- # Formalism: NRQCD (factorization and expansion in v_Q)
hard process
 $e^+e^- \rightarrow cc [J^P]$ calculated perturbatively
soft process
representing the formation of T_{cc} as a matrix element

Cross section

- # **NRQCD** G.T. Bodwin, E. Braaten, G.P. Lepage, Phys. Rev. D51, 1125 (1995)
A. Petrelli, *et al*, Nucl. Phys. B514, 245 (1998)

Effective field theory in terms of HQ velocity = p/m_c .

Coefficients are computed by perturbative QCD in α_s .

Matrix element of NRQCD operator : nonperturbative

$$\sigma \sim \sum_k \frac{f_k(\alpha_s)}{\text{hard}} \frac{\left| \langle H | \mathcal{O}_k(v) | 0 \rangle \right|^2}{\text{soft}}$$

- # **NRQCD is applied to the double-charm productions**

E. Braaten, J. Lee, Phys. Rev. D67, 054007 (2003).

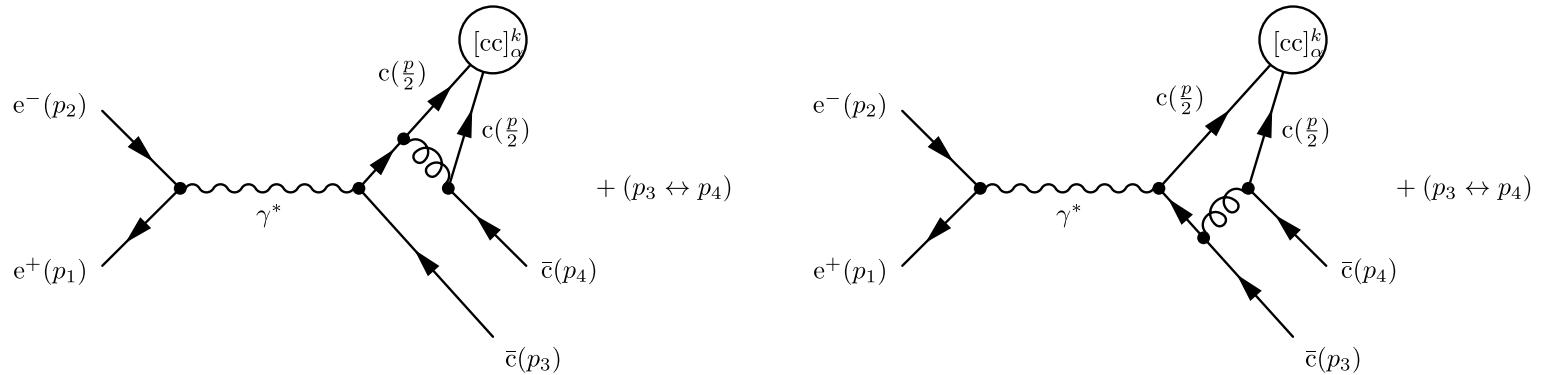
K.Y. Liu, Z.G. He, K.T. Chao, Phys. Lett. B557, 45 (2003), ...

Cross section

Cross section

$$d\sigma_\alpha(e^+e^- \rightarrow T_{cc}[\alpha] + X) = \sum_k \frac{d\hat{\sigma}(e^+e^- \rightarrow [cc]_\alpha^k + \bar{c} + \bar{c})}{k} \left| \langle T_{cc} + X | [cc]_\alpha^k | 0 \rangle \right|^2$$

**Hard part: leading order in α_s by pQCD calculation
cc with color-spin projection**



Soft part can be factorized: leading order in $v \rightarrow a number$.

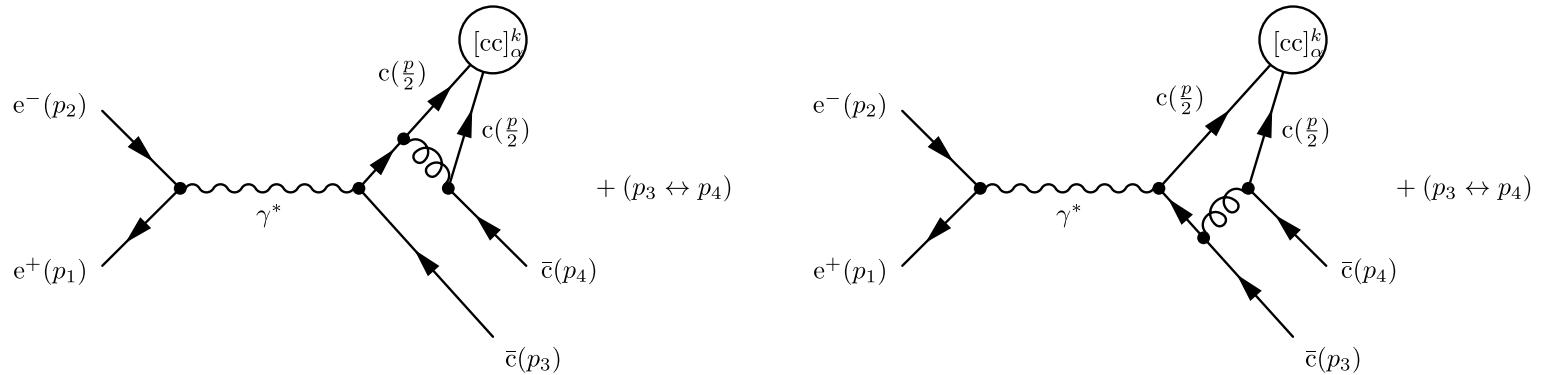
$$\left| \langle T_{cc} + X | [cc]_\alpha^k | 0 \rangle \right|^2 \Big|_{k=LO} = \begin{cases} h_3 & \text{for } \alpha = [\bar{\mathbf{3}}, {}^3S_1] \\ h_6 & \text{for } \alpha = [\mathbf{6}, {}^1S_0] \end{cases}$$

Cross section

Cross section

$$d\sigma_\alpha(e^+e^- \rightarrow T_{cc}[\alpha] + X) = \sum_k \frac{d\hat{\sigma}(e^+e^- \rightarrow [cc]_\alpha^k + \bar{c} + \bar{c})}{\text{Hard part}} \left| \langle T_{cc} + X | [cc]_\alpha^k | 0 \rangle \right|^2$$

**Hard part: leading order in α_s by pQCD calculation
cc with color-spin projection**



Soft part can be factorized: leading order in $v \rightarrow$ a number.

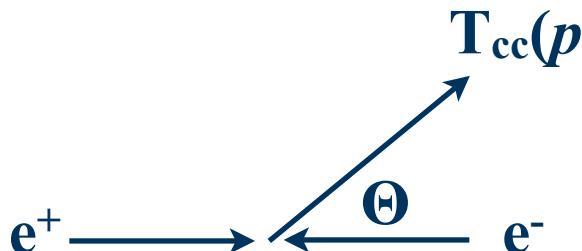
$$\left| \langle T_{cc} + X | [cc]_\alpha^k | 0 \rangle \right|^2 \Big|_{k=\text{LO}} = \begin{cases} h_3 & \text{for } \alpha = [\bar{\mathbf{3}}, {}^3S_1] \\ h_6 & \text{for } \alpha = [\mathbf{6}, {}^1S_0] \end{cases}$$

→ cancel when normalized by the total cross section $d\sigma/\sigma$

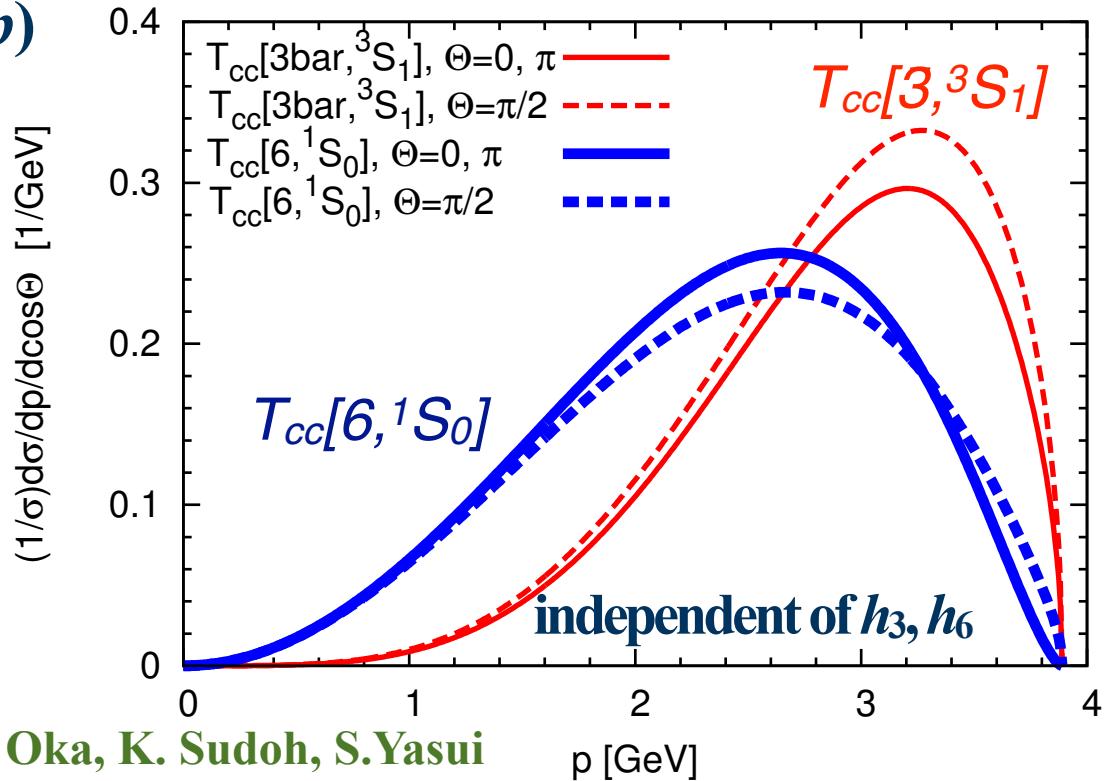
Cross section

Normalized differential cross sections

$$\frac{1}{\sigma} \frac{d\sigma_\alpha}{dp \, d\cos\Theta}$$



$$m_c = 1.8 \text{ GeV}$$
$$\alpha_s = 0.212$$
$$s^{1/2} = 10.6 \text{ GeV}$$



T. Hyodo, Y.R. Liu, M. Oka, K. Sudoh, S. Yasui

Momentum distribution depends on the **color** configurations.

Cross section

- # For absolute value, we need nonperturbative matrix elements.

Charmonium case: $c\bar{c}$ wave function at origin.

G.T. Bodwin, E. Braaten, G.P. Lepage, Phys. Rev. D51, 1125 (1995)

A. Petrelli, *et al*, Nucl. Phys. B514, 245 (1998)

$$|\langle J/\psi | \bar{c}c | 0 \rangle|^2 \sim \frac{1}{4\pi} |R_{\bar{c}c}(x=0)|^2$$

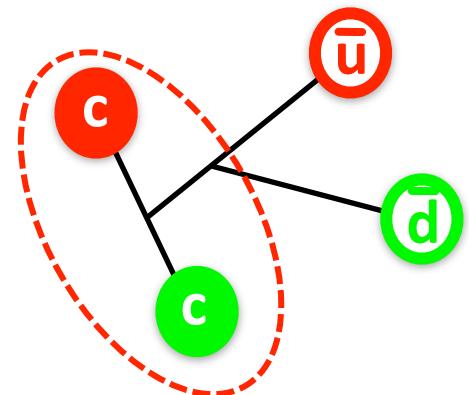
- # Constituent quark model for T_{cc} with harmonic confinement.

$$V = \sum_{i < j} \left(-\frac{3}{16} \right) \vec{\lambda}_i \cdot \vec{\lambda}_j \frac{k}{2} |\vec{r}_i - \vec{r}_j|^2$$

$T_{cc}[\bar{3}]$

$$h_3 = \frac{1}{4\pi} |R_{cc}^{\bar{3}_c(3S_1)}(0)|^2$$
$$\sim 0.089 \text{ GeV}^3$$

$$\sigma(T_{cc}[\bar{3}]) = 13.8 \text{ fb}$$



ref: Ξ_{cc} production with NRQCD formalism

- Ma, Si, PLB568, 135 (2003), - Jian, et al., arXiv:1208.3051

Cross section

- # For absolute value, we need nonperturbative matrix elements.

Charmonium case: $c\bar{c}$ wave function at origin.

G.T. Bodwin, E. Braaten, G.P. Lepage, Phys. Rev. D51, 1125 (1995)

A. Petrelli, *et al*, Nucl. Phys. B514, 245 (1998)

$$|\langle J/\psi | \bar{c}c | 0 \rangle|^2 \sim \frac{1}{4\pi} |R_{\bar{c}c}(x=0)|^2$$

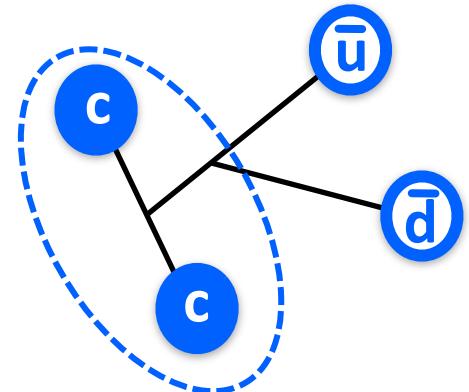
- # Constituent quark model for T_{cc} with harmonic confinement.

$$V = \sum_{i < j} \left(-\frac{3}{16} \right) \vec{\lambda}_i \cdot \vec{\lambda}_j \frac{k}{2} |\vec{r}_i - \vec{r}_j|^2$$

$T_{cc}[6]$

$$h_6 = \frac{1}{4\pi} |R_{cc}^{6_c(1S_0)}(0)|^2$$
$$\sim 0.053 \text{ GeV}^3$$

$$\sigma(T_{cc}[6]) = 4.1 \text{ fb}$$



ref: Ξ_{cc} production with NRQCD formalism

- Ma, Si, PLB568, 135 (2003), - Jian, et al., arXiv:1208.3051

Cross section

- # The present treatment assumes that the light quarks are supplied by the vacuum to form T_{cc} without a further factor.
- # The ratio of Ξ_{cc}/T_{cc} productions is about unity.

Fragmentation to T_{cc}

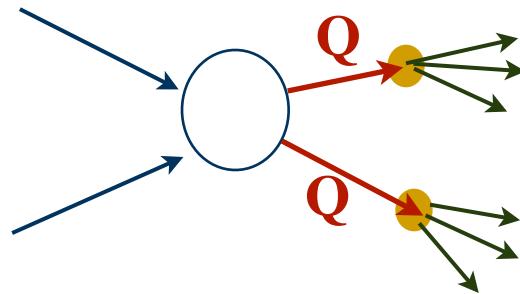
Fragmentation of heavy quark

- # HARD processes $e^+ + e^- \rightarrow QQ\bar{q}, Q^2Q\bar{q}^2, \dots$ are followed by SOFT hadronization

$$Q \rightarrow Qq\bar{q}, Qqq \text{ hadrons}$$

$$QQ \rightarrow QQq, QQq\bar{q}q\bar{q}$$

- # In high energy processes, the hard vertex with heavy quarks and the soft hadronization processes are “factorized”.



- # Productions with the common hard parts:
 - D/B ($Qq\bar{q}$) and Λ_Q , Σ_Q (Qqq)
 - D_s/B_s ($Qs\bar{s}$) and Ξ_Q (Qqs)
 - Ξ_{QQ} (QQq) and T_{QQ} ($QQq\bar{q}q\bar{q}$)

Experimental data

- # High energy production of b quark fragmented into B mesons and b-Baryons, eventually decaying via the weak interaction. Fragmentation probabilities of B_u , B_d , B_s , Λ_b productions are measured at LEP (Z decay), CDF ($pp^{\bar{}}$), and LHCb (pp).
- # Recent results

LHCb results (PR D85 (2012) 032008)

$$f_s/(f_u+f_d) = 0.134 \pm 0.004 \pm 0.001$$

$$f_B/(f_u+f_d) = (0.40 \pm 0.10) \times (1 - 0.031 p_T(\text{GeV}))$$

$f_{u, d, s, B}$: probability of b-quark fragmentation
into B^- (bu), B^0 (bd), B_s (bs), and Λ_b (bud)

- # Note that the preceding strong decays are not “measured”, so that the data include not only B and Λ_b , but also B^* and Σ_b^* .

$$f_u + f_d = B + B^* + (\text{some excited states})$$

$$f_B = \Lambda_b + \Sigma_b + \Sigma_b^* + (\text{some excited states})$$

LEP, CDF and LHCb

- # Lifetime and production rate of beauty baryons from Z decays,
DELPHI Collaboration, Z. Phys. C68 (1995) 375.
- # Measurement of the b baryon lifetime and branching fractions in Z decays, **The ALEPH Collaboration, Eur. Phys. J C2 (1998) 197.**
 $f_B = 0.101 \pm 0.040$
- # Measurement of b-Quark Fragmentation Fractions in $p\bar{p}$ collisions at $s^{1/2} = 1.8$ TeV,
CDF Collaboration, Phys. Rev. Lett. 84 (2000) 1663.
 $f_B / (f_u + f_d) = (0.090 \pm 0.029) / (0.750 \pm 0.046) = 0.118 \pm 0.042$
- # Measurement of ratios of fragmentation functions for bottom hadrons in $p\bar{p}$ collisions at $s^{1/2} = 1.96$ TeV,
CDF Collaboration, Phys. Rev. D77 (2008) 072003.
 $f_B / (f_u + f_d) = 0.281 \pm 0.10$
- # Measurement of b hadron production in 7 TeV $p\bar{p}$ collisions,
The LHCb Collaboration, Phys. Rev. D85 (2012) 032008.
 $f_B / (f_u + f_d) = (0.40 \pm 0.10) \times (1 - 0.031 p_T(\text{GeV}))$

Estimate the ratio by counting

- # Assume
 - (1) The leading HQ is picking up light quarks and forms a hadron.
 - (2) The light quarks are created as a quark-antiquark pair.
 - (3) The “probability” of creating a quark-antiquark pair is universal to all the processes.
 - (4) The hadrons are produced only when the HQ meets a light (anti-)quark with the *right* quantum numbers.
 - (5) The “sticking probability” is determined by the (valence) quark wave function (@ $R=0$) of the hadron.
- # More intuitively,
 $q\bar{q}$ can be created in the color singlet, spin singlet 0^+ state.
The pairs $u\bar{u}$ and $d\bar{d}$ are created with the same probability, while $s\bar{s}$ may be partially suppressed.

Estimate the ratio by counting

- # Suppose the probability of creating a $u\bar{u}$ pair is η_u .
Then

$$u\bar{u} (R\bar{u}, \downarrow) \rightarrow (1/6)\eta_u .$$

For a $Q(R, \uparrow)$ to form a $0^- Q\bar{q}\bar{u}$ (B_u) meson is then calculated so as to combine into color singlet and spin singlet

$$\rightarrow (1/3)(1/2)(1/6) \eta_u = (1/36) \eta_u$$

- # Similarly,
Vector $Q\bar{q}\bar{u}$ $1^- (B_u^*) \rightarrow (1/3)(3/2)(1/6) \eta_u = (1/12) \eta_u$

Same for B_d , and in total the probability of producing
 $B + B^* \rightarrow (8/36)\eta_q = (2/9)\eta_q$ (assuming $\eta_q = \eta_u = \eta_d$)

Estimate the ratio by counting

Baryons

$$\Lambda_b \quad (1/108) (\eta_q)^2$$

$$\Sigma_b \quad (1/36) (\eta_q)^2$$

$$\Sigma_b^* \quad (1/18) (\eta_q)^2$$

$$\text{in total } \Lambda_b + \Sigma_b + \Sigma_b^* = (5/54) (\eta_q)^2$$

The ratio of (Baryon)/(Meson) = $(5/12) \eta_q = 0.42 \eta_q$

Exp data $\sim 0.3\text{-}0.4 \Rightarrow \eta_q = 0.7\text{\textendash}1.0$

Estimate the ratio by counting

T_{QQ} and Ξ_{QQ}

$$\Xi_{QQ} \ (1/2) \rightarrow (1/3)(2/3)(1/6) \ \eta_q = (1/27) \ \eta_q$$

$$\Xi^*_{QQ} (3/2) \rightarrow (1/3)(4/3)(1/6) \ \eta_q = (2/27) \ \eta_q$$

$$T_{QQ} (1^+, \bar{3}) \rightarrow (1/108) (\eta_q)^2$$

$$T_{QQ} (1^+, 6) \rightarrow (1/72) (\eta_q)^2$$

$(T_{QQ})/(\Xi_{QQ})$

$$\bar{3} \quad 1/2 = (1/4) \ \eta_q = 0.15 \sim 0.25$$

$$6 \quad 1/2 = (3/8) \ \eta_q = 0.2 \sim 0.38$$

$T_{QQ}(6)/T_{QQ}(\bar{3}) = 1.5$ (indep. of η_q)

This is a primitive model, but gives some guidance on what happens at the production of exotic hadrons.

Conclusion

- # **New flavor-hadron physics will be open by the high-momentum proton beam line of J-PARC and other new experimental facilities: Charmed baryons, Charmed deuteron/nucleus, Heavy exotics, i.e. T_{cc} .**
- # **The charmed baryon spectroscopy may clarify the light-diquark correlations and their spectrum. Lattice QCD may help to make quantitative predictions on diquark correlations.**
- # **T_{cc} production in the e^+e^- collisions has been predicted. We have compared it with the Ξ_{cc} production by introducing the light quark production probability.**
- # **$T_{cc}(6_c)$ provides a new possibility to explore the colored force in hadrons. We compare the production of $T_{cc}(6_c)$ to $T_{cc}(3_c)$ and point out that the momentum dependence may distinguish them.**

Extra slides

Decay modes

- # **Decay of T_{cc}**
 - weak decay through $c \rightarrow s$: $T_{cc} \rightarrow D K \pi$**
 - radiative decay : $T_{cc} \rightarrow D^0 D^+ \gamma$**
- # **Belle group is analyzing (T. Iijima, private communication)**
exclusive mode (cross section is small)
 - $e^+ e^- \rightarrow D^- D^{0\bar{}} T_{cc}$ (missing mass)**
 - inclusive mode (large cross section, but resonance only)**
 - $e^+ e^- \rightarrow T_{cc} + X \rightarrow D^{*0} D^+ + X$ (invariant mass)**