

Photoproduction of multi-kaons in an effective Lagrangian approach

Huiyoung RYU



In Collaboration with
Atushi Hosaka (RCNP), A. I. Titov (JINR),
Hyun-Chul Kim (Inha Uni.) and Yongseok Oh (KNU)

The 7th APCTP-BLTP JINR Joint Workshop, July 14-19, 2013

*Bikal lake, 13 July, 2013
by Hee-jung Lee*

Contents

PART I. $\gamma p \rightarrow \phi p$

- Phi meson properties and photoproduction
- Effective Lagrangian method
- Formalism
- Numerical Results (Re+Im)
- Summary of part I

PART II. $\gamma p \rightarrow K^+ K^+ K^0 \Omega^-$

- Introduction
- Formalism
- Summary of part II





PART I. $\gamma p \rightarrow \phi p$

I. Introduction

Phi meson properties

$\phi(1020)$

$$J^{PC} = 0^{-}(1^{-})^{-}$$

Mass $m = 1019.455 \pm 0.020$ MeV (S = 1.1)

Full width $\Gamma = 4.26 \pm 0.04$ MeV (S = 1.4)

$\phi(1020)$ DECAY MODES	Fraction (Γ_i/Γ)	Scale factor/ Confidence level	p (MeV/c)
$K^+ K^-$	(48.9 \pm 0.5) %	S=1.1	127
$K_L^0 K_S^0$	(34.2 \pm 0.4) %	S=1.1	110

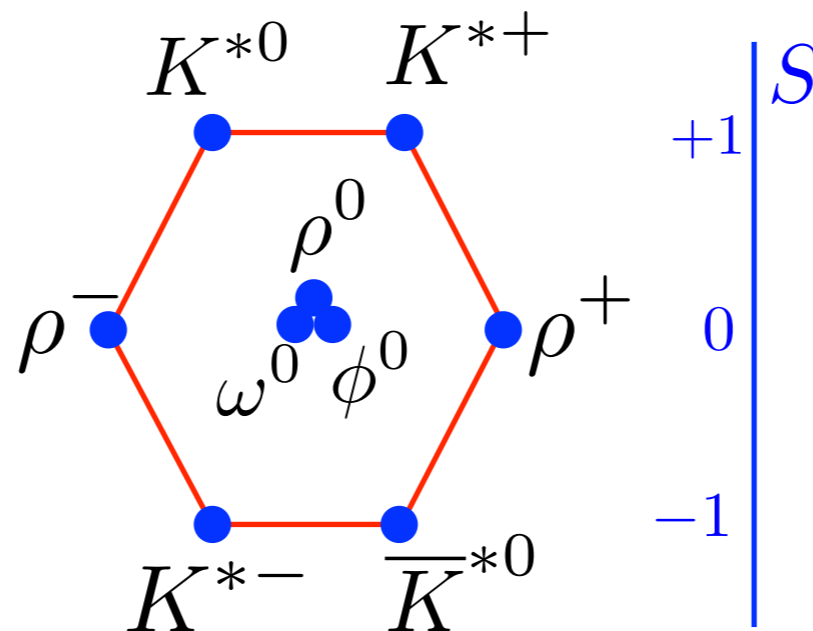
$$P = (-1)^J$$

: natural parity

$$P = (-1)^{J+1}$$

: unnatural parity

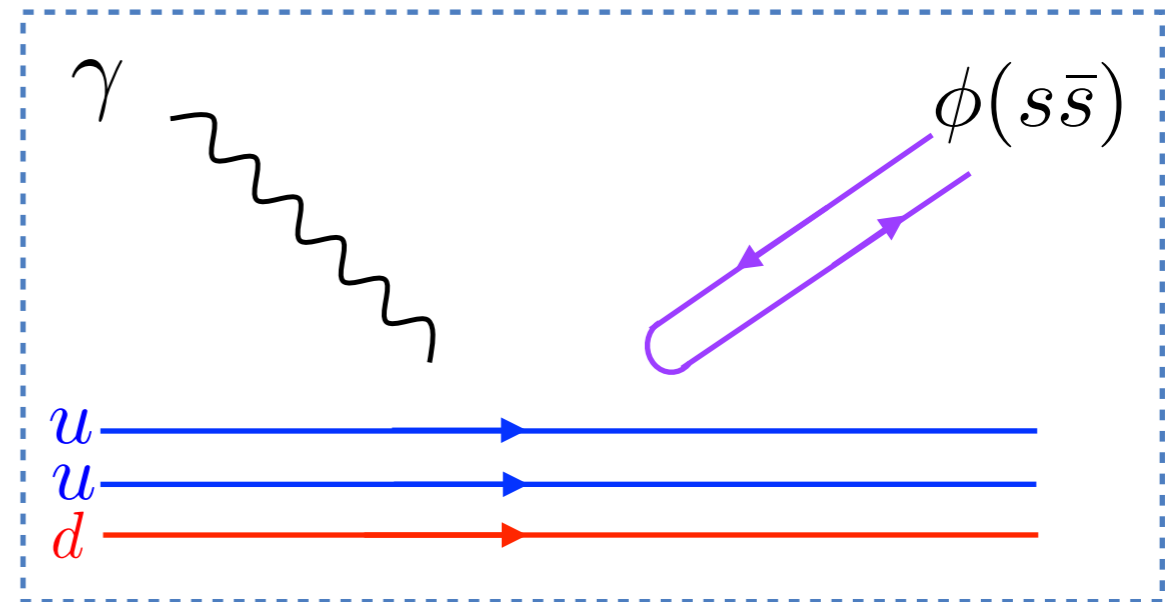
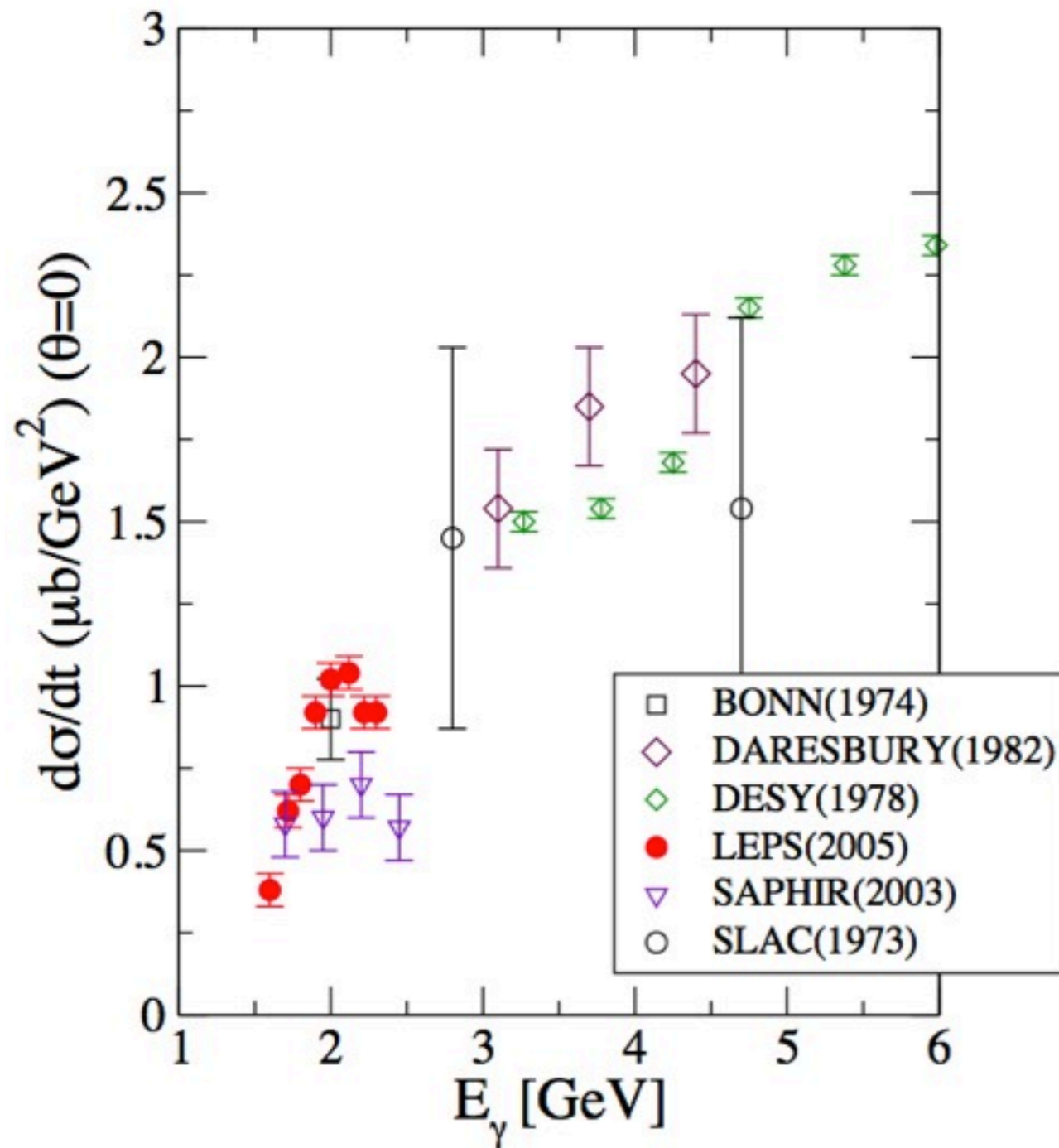
$$2S+1 L_J = {}^3S_1$$



$$\phi^0 = s\bar{s}$$



Phi meson photoproduction

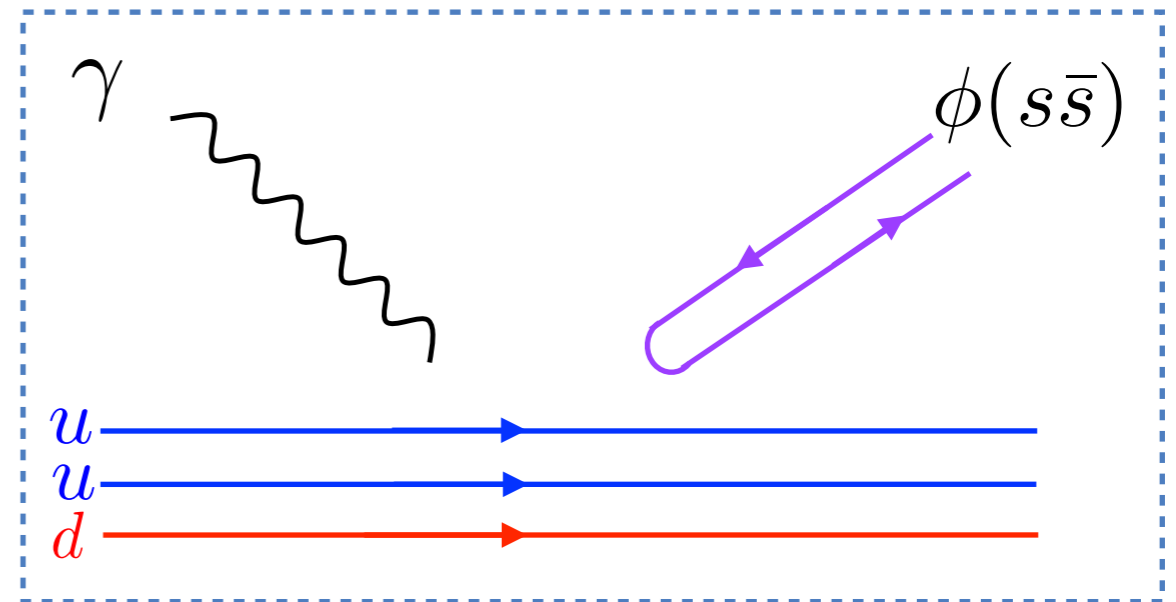
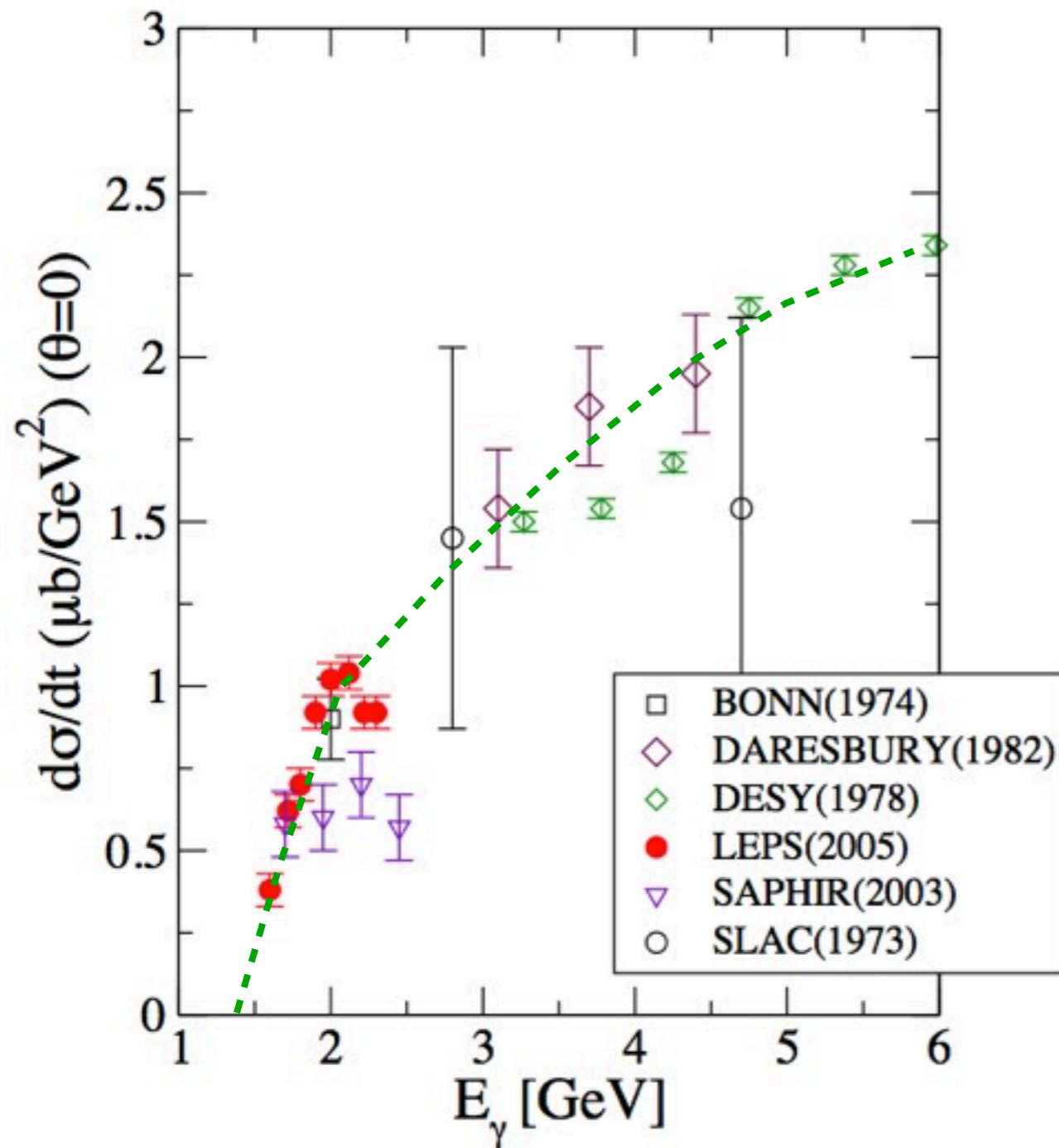


■ OZI rule violation

- Gluonic dynamics (Pomeron)
- Hidden strangeness



Phi meson photoproduction



■ OZI rule violation

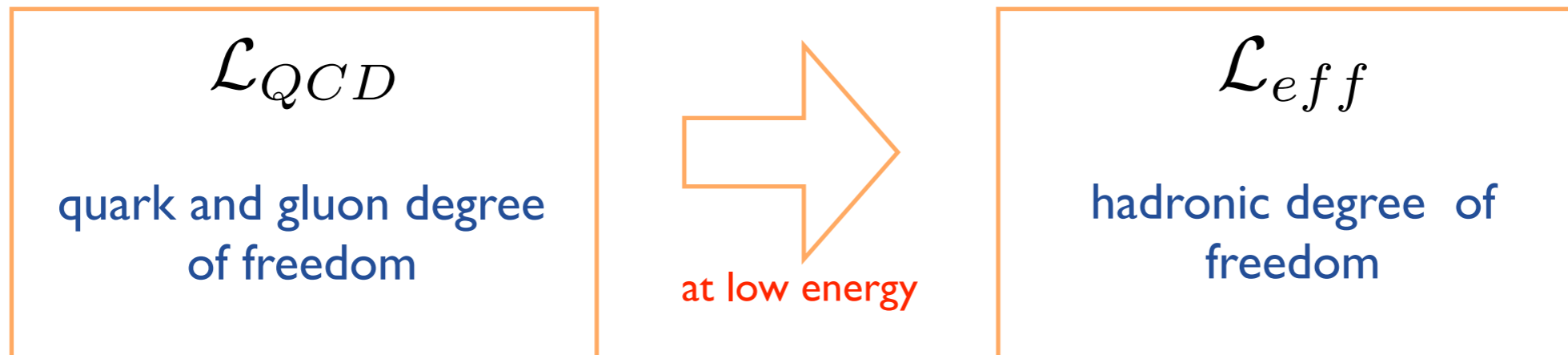
- Gluonic dynamics (Pomeron)
- Hidden strangeness



Effective Lagrangian method

$$\mathcal{L}_{QCD} = -\frac{1}{2} \text{tr}[G_{\mu\nu} G^{\mu\nu}] + \bar{q} i \gamma^\mu D_\mu q - \bar{q} \mathbf{m} q$$

$$G_{\mu\nu} = \partial_\mu A_\nu - \partial_\nu A_\mu - ig[A_\mu, A_\nu], \quad D_\mu = \partial_\mu - igA_\mu, \quad A_\mu = \sum_a T^a A_\mu^a$$



$$\exp[iZ] = \int \mathcal{D}q \mathcal{D}\bar{q} \mathcal{D}A \exp\left[i \int dx^4 \mathcal{L}_{QCD}\right] = \int \mathcal{D}U \exp\left[i \int dx^4 \mathcal{L}_{eff}\right]$$

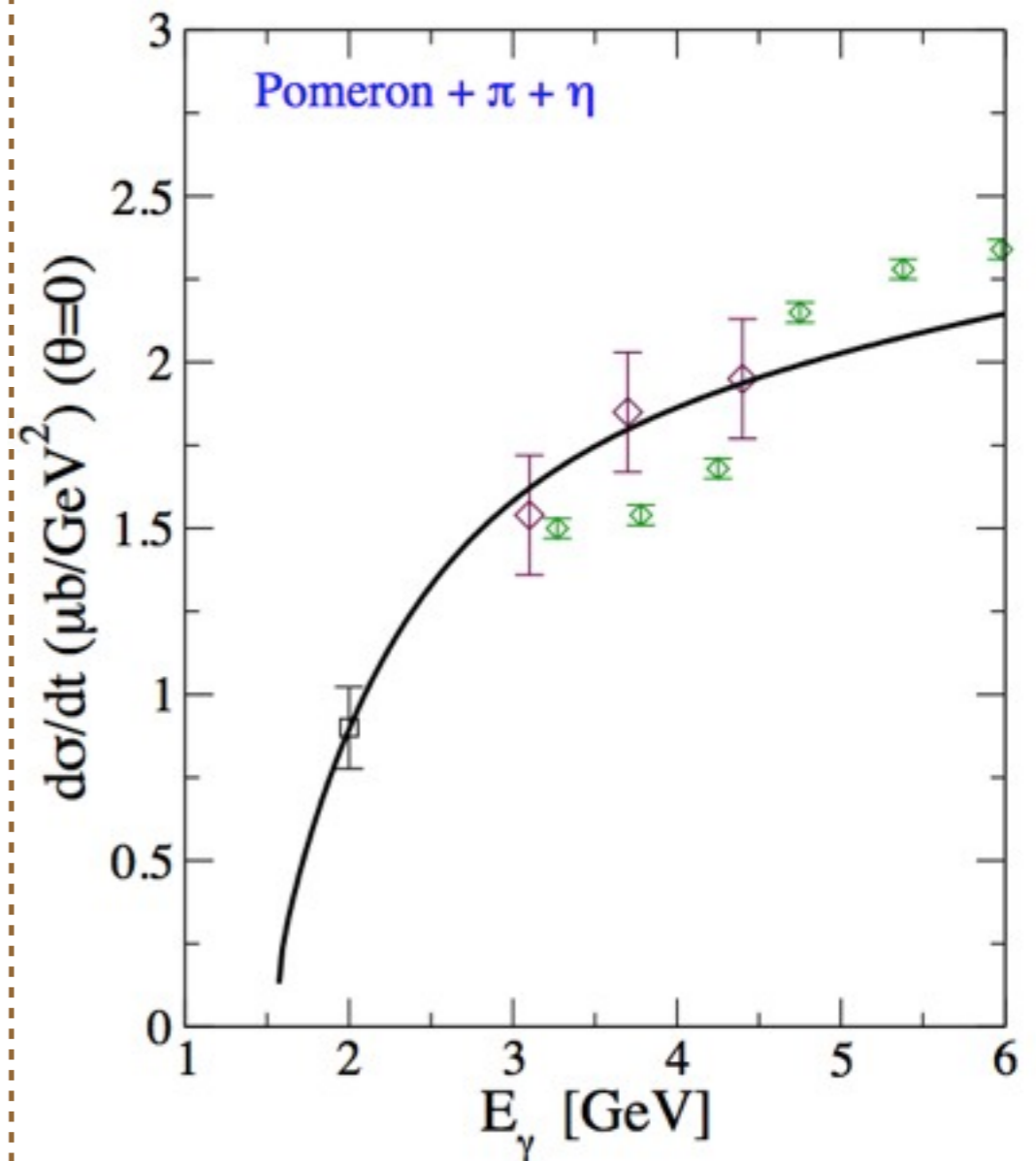
$$\mathcal{L}_{eff} = \mathcal{L}_{eff}(\underbrace{U, \partial_\mu U, V_\mu \dots}_{\text{Hadrons}}), \quad U = \exp\left[\frac{i\sqrt{2}\Phi}{f}\right]$$



II. Phi meson photoproduction

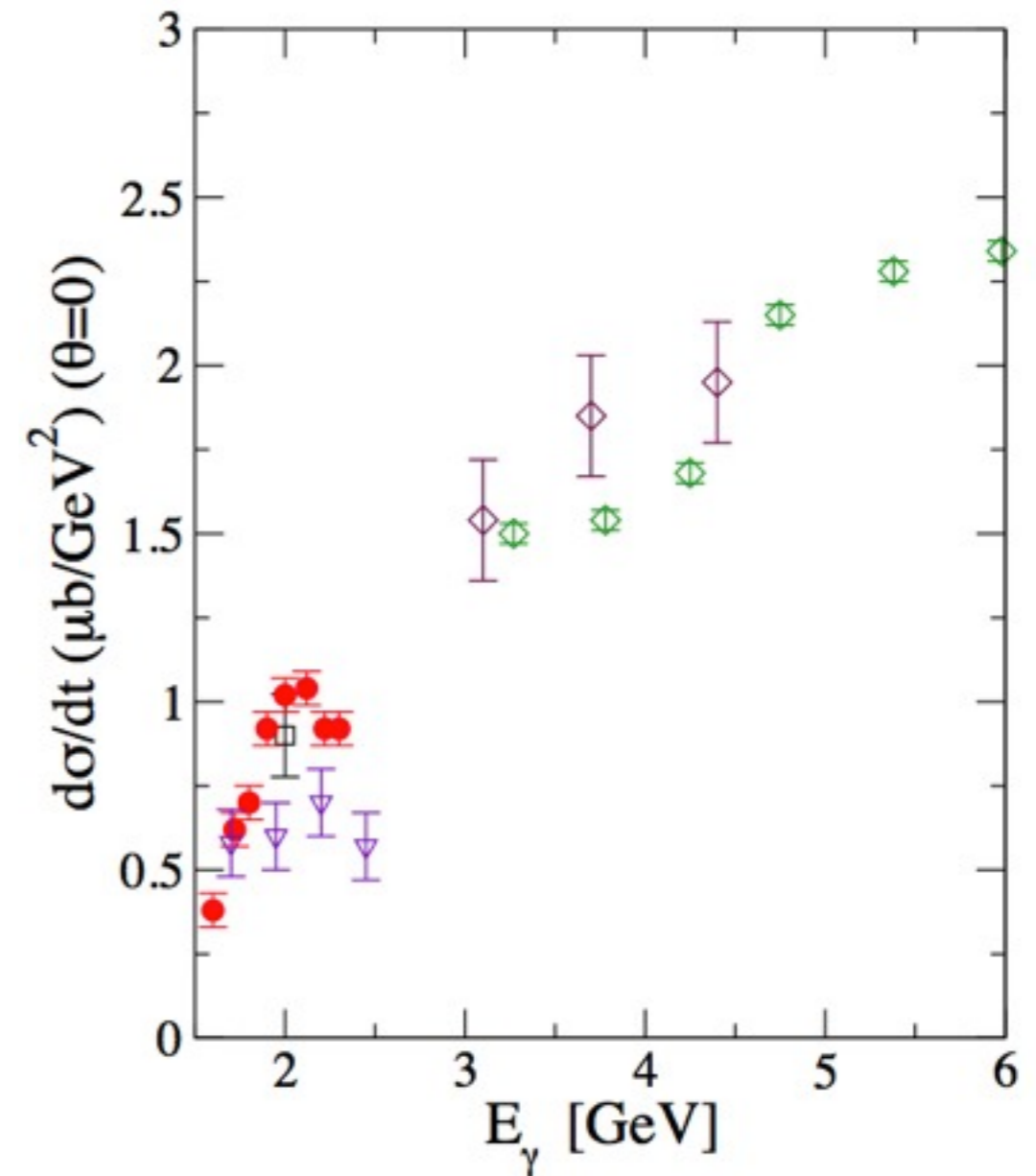
Previous works relevant to the present work

Author	Date	Their work
Titov <i>et al</i>	1999	Structure of the ϕ photoproduction at a few GeV
<hr style="border-top: 1px dashed red;"/>		
T. Mibe <i>et al</i>	2005	Near-Threshold Diffractive ϕ -Meson Photoproduction from the proton
S. Ozki <i>et al</i>	2009	Coupled-channel analysis for ϕ photoproduction with $\Lambda(1520)$
W. C. Chang <i>et al</i>	2010	Measurement of spin-density matrix elements for ϕ -meson photoproduction from protons and deuterons near threshold
A. Kiswandhi <i>et al</i>	2010	Is the nonmonotonic behavior in the cross section of ϕ photoproduction near threshold a signature of a resonance ?
H. Y. Ryu <i>et al</i>	2012	ϕ photoproduction with couple-channel effects



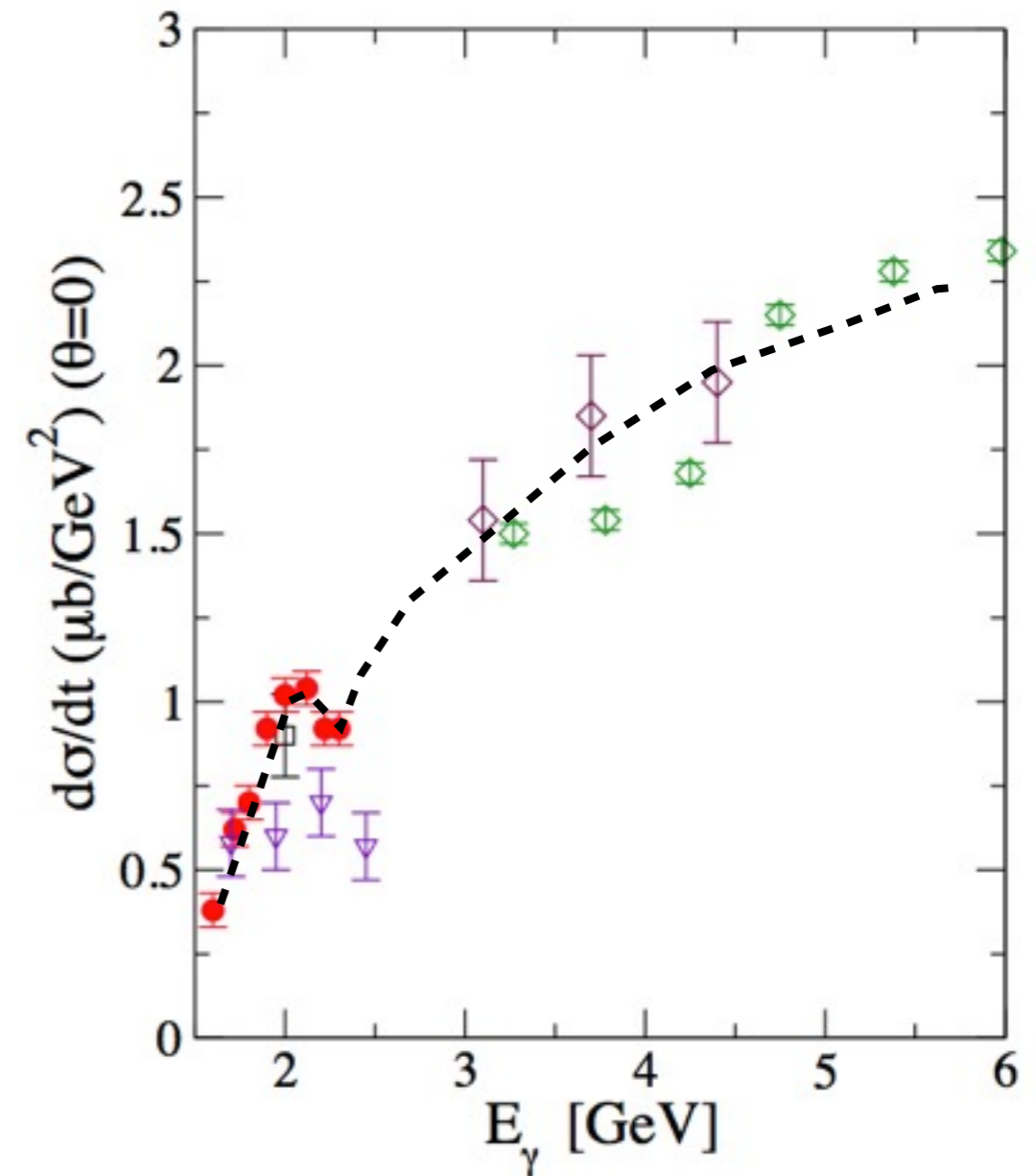
Previous works relevant to the present work

Author	Date	Their work
Titov <i>et al</i>	1999	Structure of the ϕ photoproduction at a few GeV
T. Mibe <i>et al</i>	2005	Near-Threshold Diffractive ϕ -Meson Photoproduction from the proton
S. Ozki <i>et al</i>	2009	Coupled-channel analysis for ϕ photoproduction with $\Lambda(1520)$
W. C. Chang <i>et al</i>	2010	Measurement of spin-density matrix elements for ϕ -meson photoproduction from protons and deuterons near threshold
A. Kiswandhi <i>et al</i>	2010	Is the nonmonotonic behavior in the cross section of ϕ photoproduction near threshold a signature of a resonance ?
H. Y. Ryu <i>et al</i>	2012	ϕ photoproduction with couple-channel effects



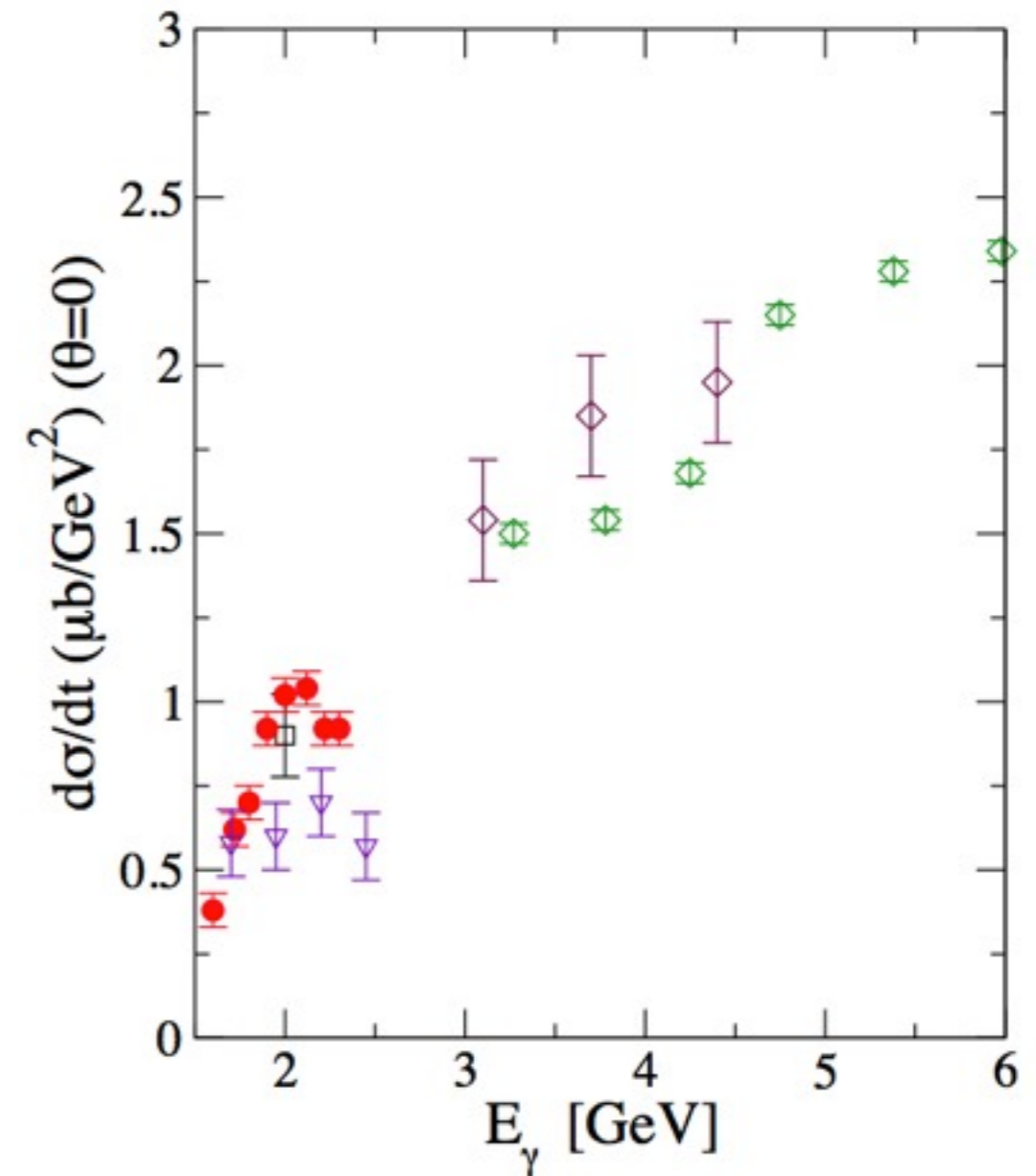
Previous works relevant to the present work

Author	Date	Their work
Titov <i>et al</i>	1999	Structure of the ϕ photoproduction at a few GeV
T. Mibe <i>et al</i>	2005	Near-Threshold Diffractive ϕ -Meson Photoproduction from the proton
S. Ozki <i>et al</i>	2009	Coupled-channel analysis for ϕ photoproduction with $\Lambda(1520)$
W. C. Chang <i>et al</i>	2010	Measurement of spin-density matrix elements for ϕ -meson photoproduction from protons and deuterons near threshold
A. Kiswandhi <i>et al</i>	2010	Is the nonmonotonic behavior in the cross section of ϕ photoproduction near threshold a signature of a resonance ?
H. Y. Ryu <i>et al</i>	2012	ϕ photoproduction with couple-channel effects



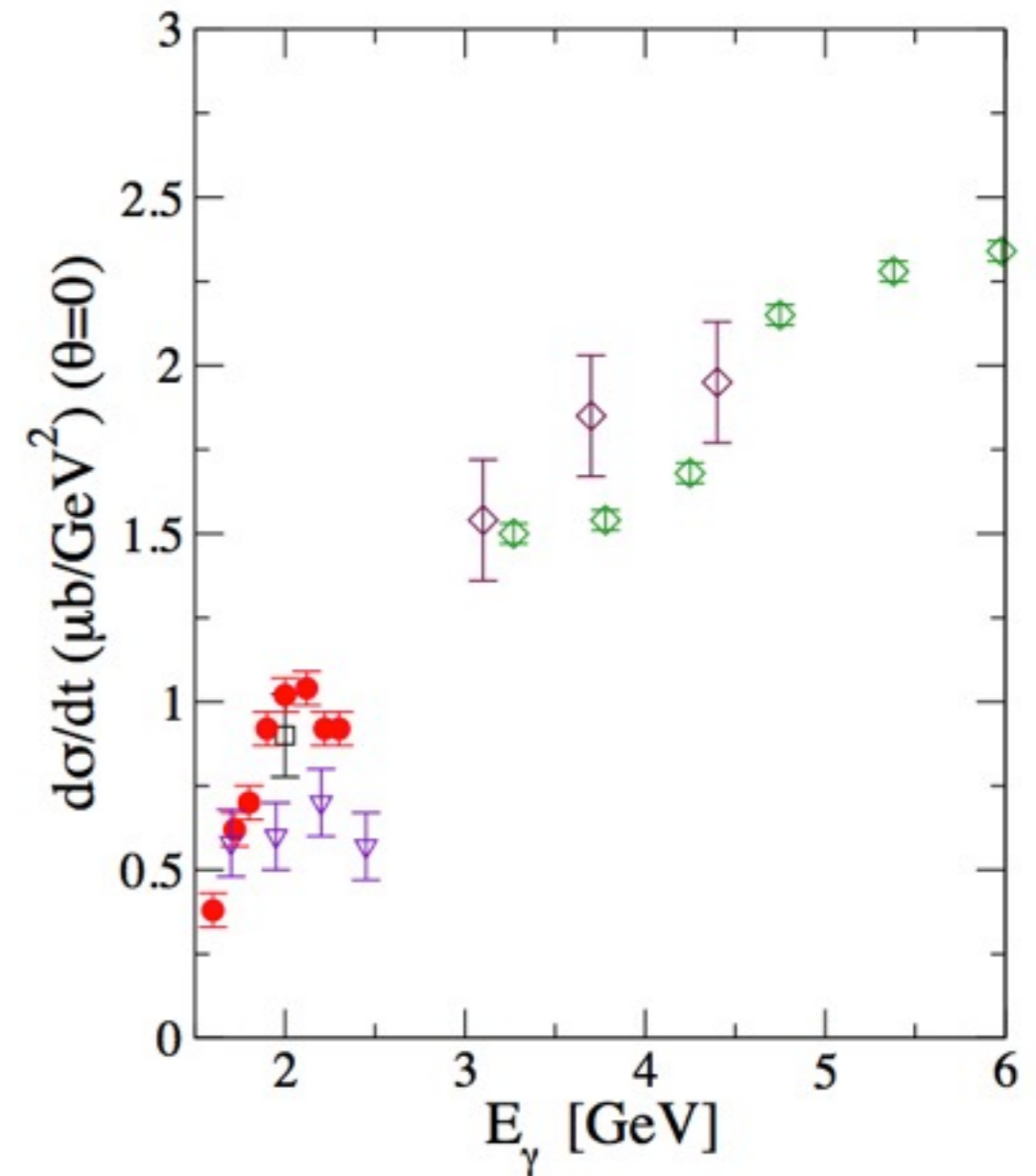
Previous works relevant to the present work

Author	Date	Their work
Titov <i>et al</i>	1999	Structure of the ϕ photoproduction at a few GeV
T. Mibe <i>et al</i>	2005	Near-Threshold Diffractive ϕ -Meson Photoproduction from the proton
S. Ozki <i>et al</i>	2009	Coupled-channel analysis for ϕ photoproduction with $\Lambda(1520)$
W. C. Chang <i>et al</i>	2010	Measurement of spin-density matrix elements for ϕ -meson photoproduction from protons and deuterons near threshold
A. Kiswandhi <i>et al</i>	2010	Is the nonmonotonic behavior in the cross section of ϕ photoproduction near threshold a signature of a resonance ?
H. Y. Ryu <i>et al</i>	2012	ϕ photoproduction with couple-channel effects



Previous works relevant to the present work

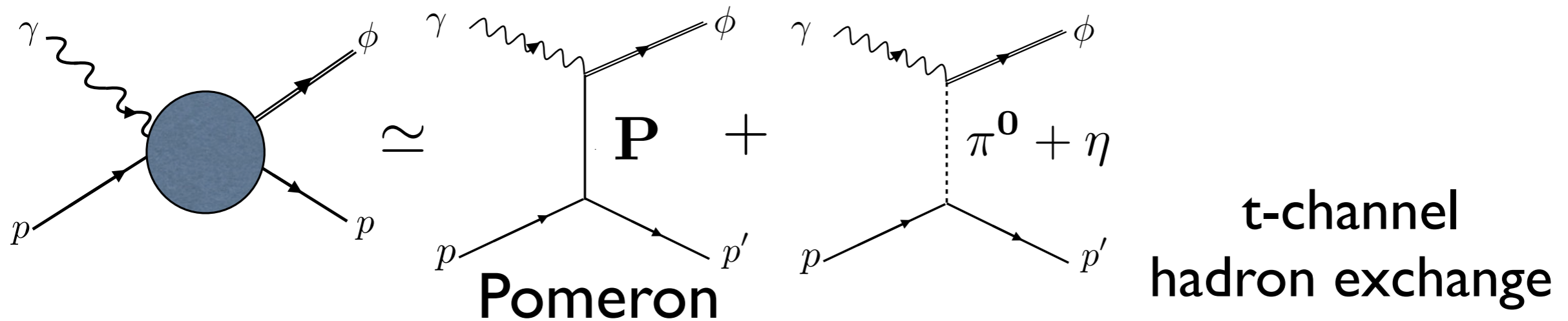
Author	Date	Their work
Titov <i>et al</i>	1999	Structure of the ϕ photoproduction at a few GeV
T. Mibe <i>et al</i>	2005	Near-Threshold Diffractive ϕ -Meson Photoproduction from the proton
S. Ozki <i>et al</i>	2009	Coupled-channel analysis for ϕ photoproduction with $\Lambda(1520)$
W. C. Chang <i>et al</i>	2010	Measurement of spin-density matrix elements for ϕ -meson photoproduction from protons and deuterons near threshold
A. Kiswandhi <i>et al</i>	2010	Is the nonmonotonic behavior in the cross section of ϕ photoproduction near threshold a signature of a resonance ?
H. Y. Ryu <i>et al</i>	2012	ϕ photoproduction with couple-channel effects



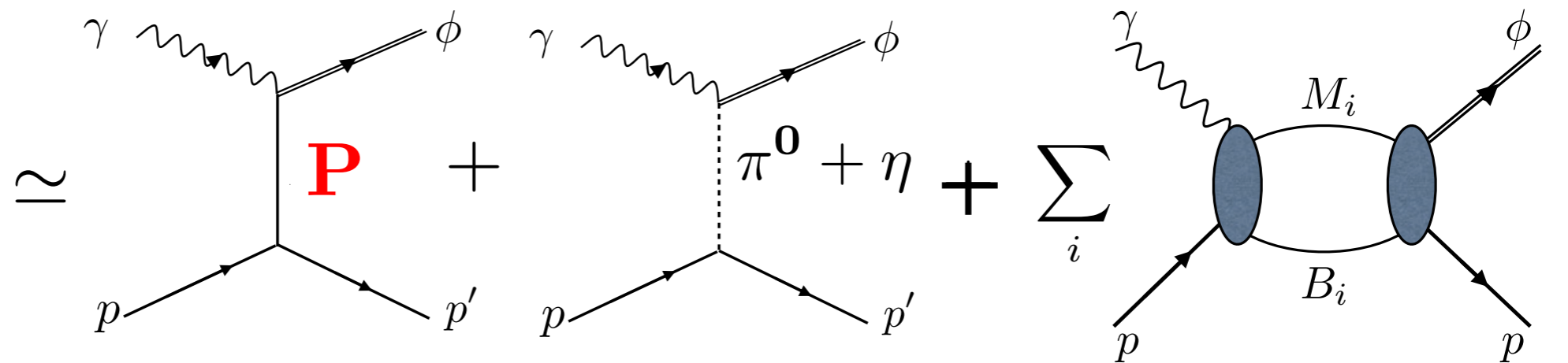
Mechanism for phi photoproduction

Conventional approach

A. I. Titov et al. phys. rev. 60, 035205 (1999)



This work



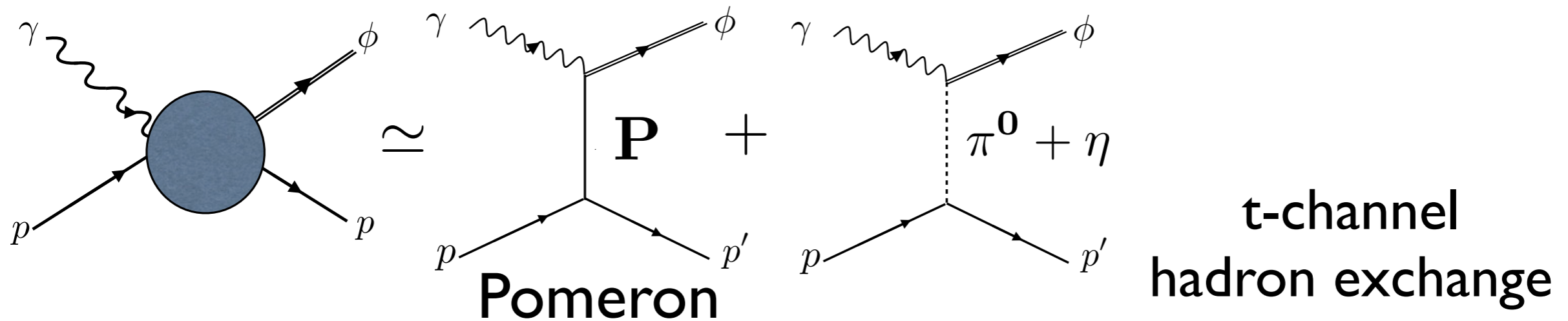
hadron rescatterings



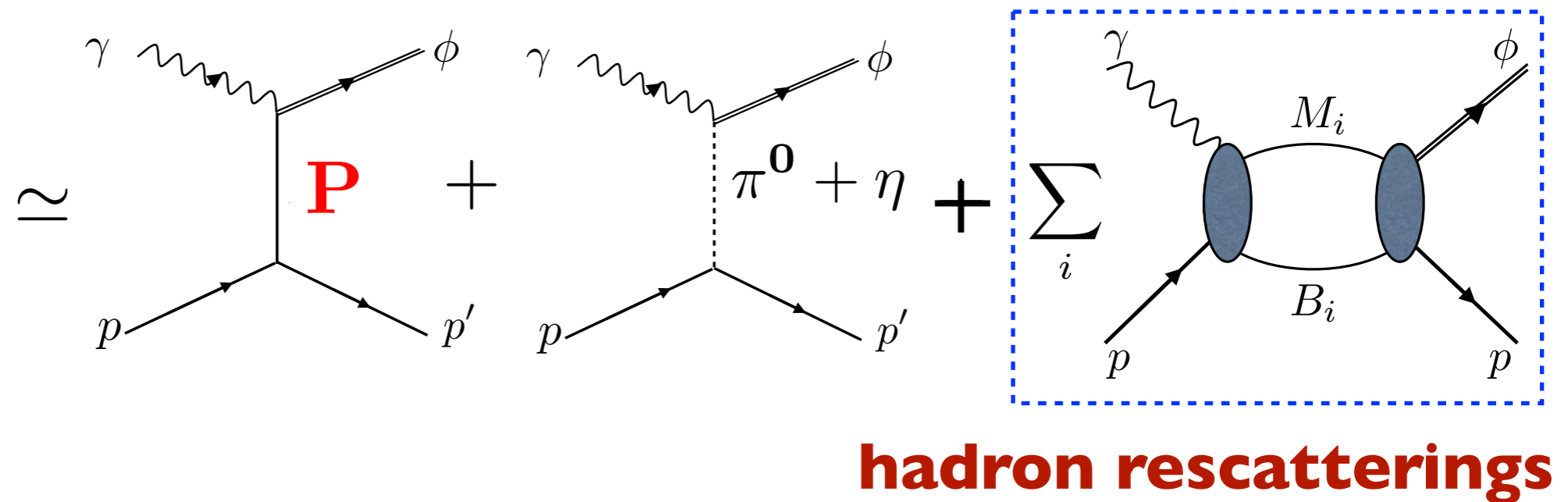
Mechanism for phi photoproduction

Conventional approach

A. I. Titov et al. phys. rev. 60, 035205 (1999)

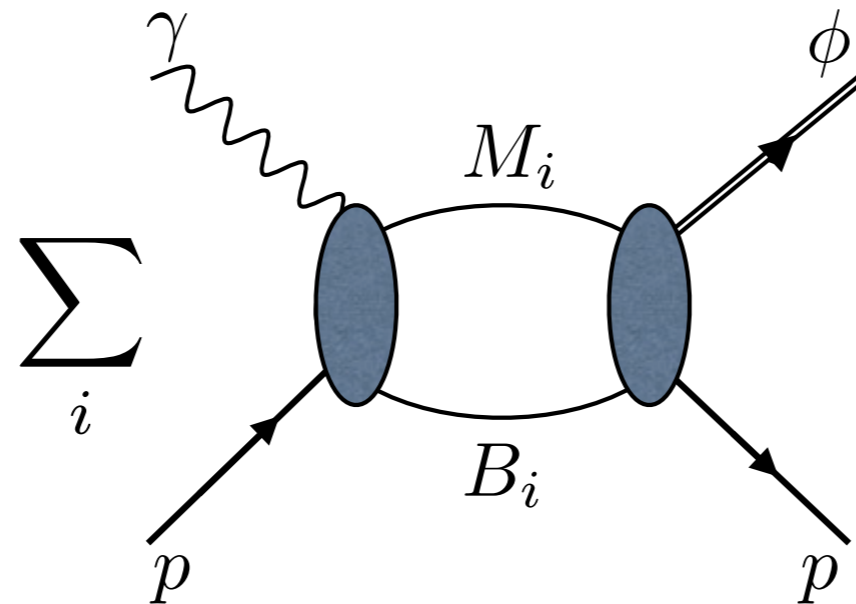


This work



Blankenbecler and Sugar Equation

R. Aaron, R. D. Amado and J. E. Young, phys. rev. 174, 5, 1968



$$T_{\gamma p \rightarrow \phi p} = V_{\gamma p \rightarrow \phi p} + \frac{1}{(2\pi)^3} \int \frac{dk^3}{2\omega_1 \omega_2} T_{M_i B_i \rightarrow \phi p} \frac{(\omega_1 + \omega_2)}{(\omega_1 + \omega_2)^2 - s + i\epsilon} T_{\gamma p \rightarrow M_i B_i}$$

M	ρ	ω	σ	π	K	K^*	K
B	p	p	p	p	$\Lambda(1116)$	$\Lambda(1116)$	$\Lambda(1520)$



$$T_{\gamma p \rightarrow \phi p} = V_{\gamma p \rightarrow \phi p} + \frac{1}{(2\pi)^3} \int \frac{dk^3}{2\omega_1 \omega_2} T_{M_i B_i \rightarrow \phi p} \frac{(\omega_1 + \omega_2)}{(\omega_1 + \omega_2)^2 - s + i\epsilon} T_{\gamma p \rightarrow M_i B_i}$$



$$T_{\gamma p \rightarrow \phi p} = V_{\gamma p \rightarrow \phi p} + \frac{1}{(2\pi)^3} \int \frac{dk^3}{2\omega_1 \omega_2} T_{M_i B_i \rightarrow \phi p} \frac{(\omega_1 + \omega_2)}{(\omega_1 + \omega_2)^2 - s + i\epsilon} T_{\gamma p \rightarrow M_i B_i}$$

$$\frac{1}{(\omega_1 + \omega_2)^2 - s + i\epsilon} = \text{P} \frac{1}{(\omega_1 + \omega_2)^2 - s} - i\pi \delta \left[(\omega_1 + \omega_2)^2 - s \right]$$



$$T_{\gamma p \rightarrow \phi p} = V_{\gamma p \rightarrow \phi p} + \frac{1}{(2\pi)^3} \int \frac{dk^3}{2\omega_1 \omega_2} T_{M_i B_i \rightarrow \phi p} \frac{(\omega_1 + \omega_2)}{(\omega_1 + \omega_2)^2 - s + i\epsilon} T_{\gamma p \rightarrow M_i B_i}$$

$$\frac{1}{(\omega_1 + \omega_2)^2 - s + i\epsilon} = \text{P} \frac{1}{(\omega_1 + \omega_2)^2 - s} - i\pi \delta \left[(\omega_1 + \omega_2)^2 - s \right]$$

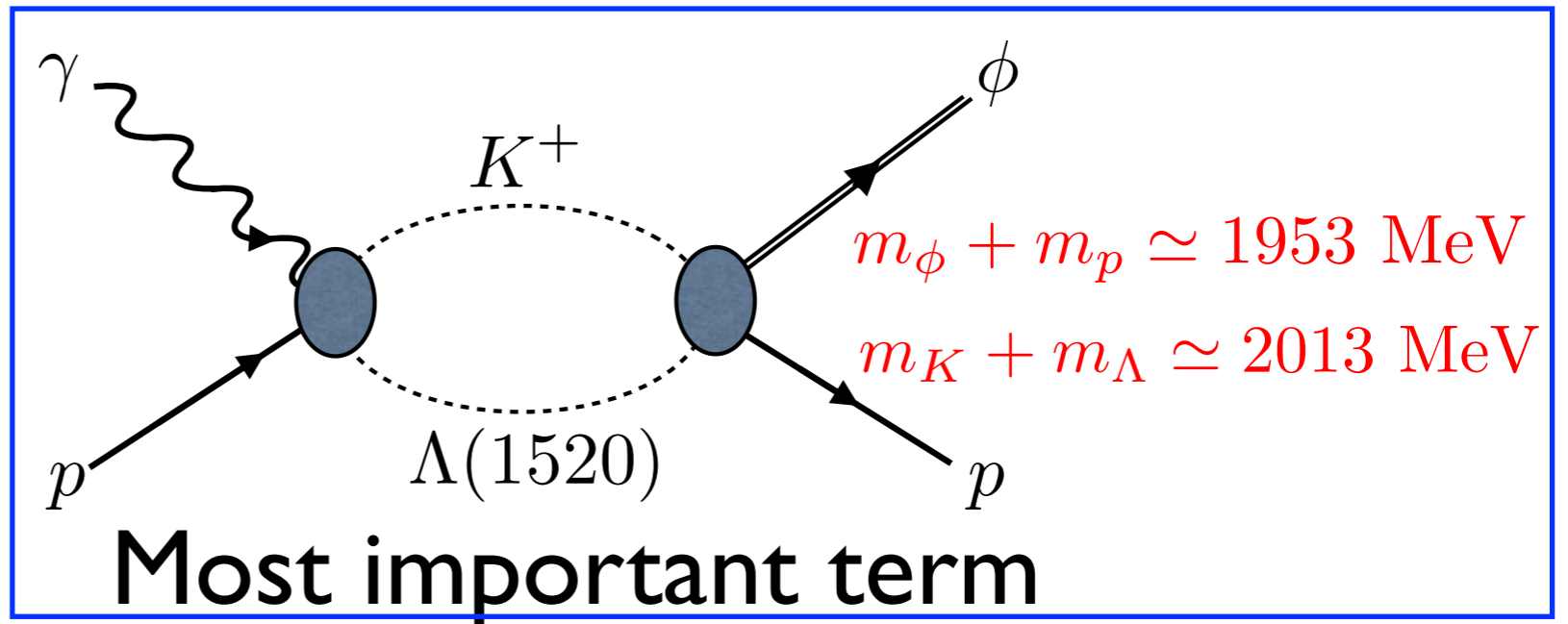
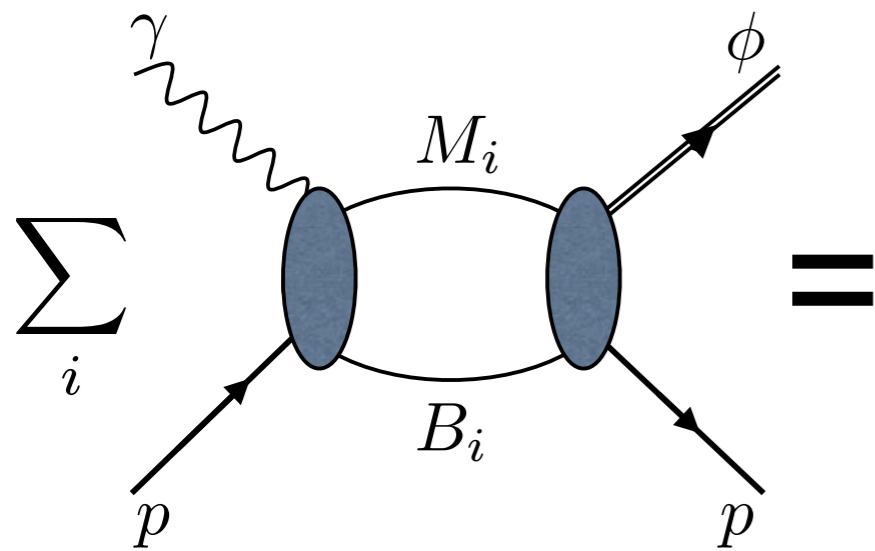
$$\text{Im} T_{\gamma p \rightarrow \phi p} = -\frac{h}{32\pi^2 \sqrt{s}} \int d\Omega T_{M_i B_i \rightarrow \phi p} T_{\gamma p \rightarrow M_i B_i}$$

$$\omega_1(h) + \omega_2(h) - \sqrt{s} = 0, \quad \omega_1(k) = \sqrt{M_{M_i}^2 + k^2}$$

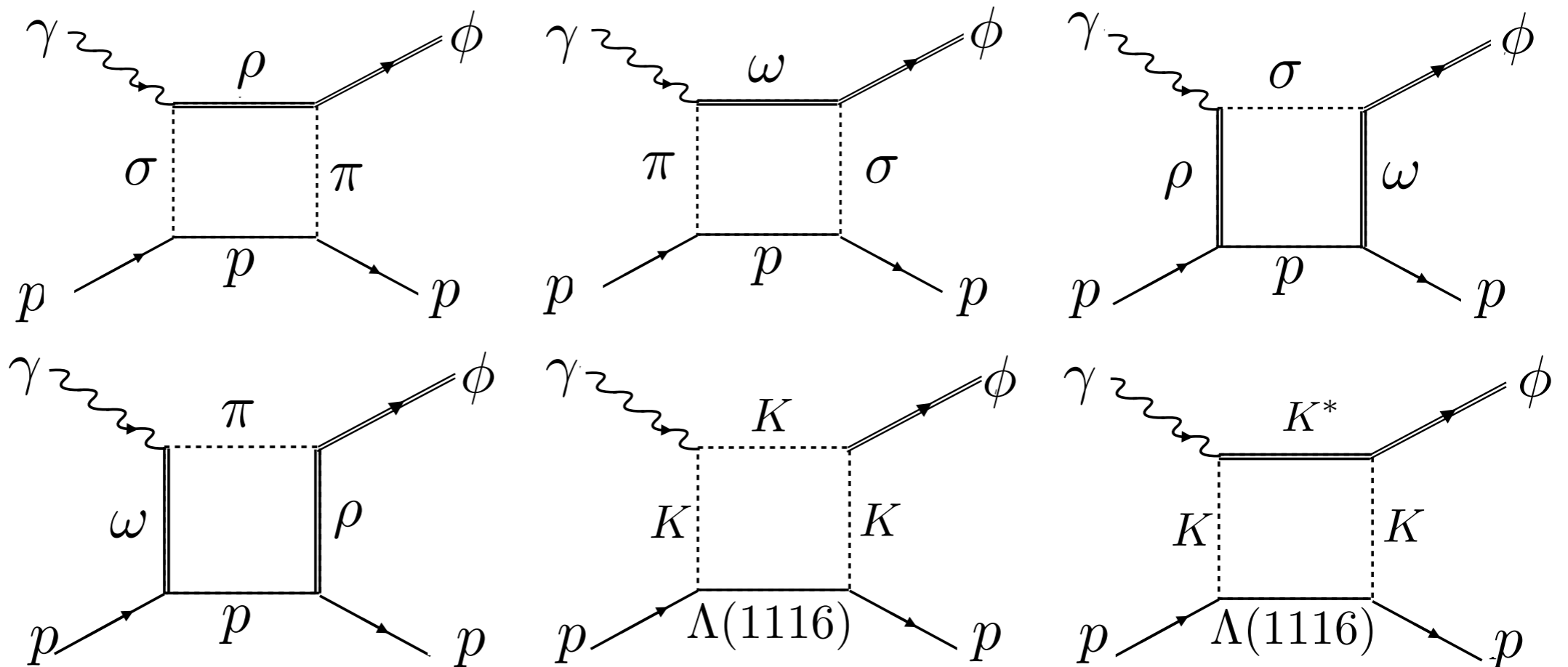
$$\omega_2(k) = \sqrt{M_{B_i}^2 + k^2}$$



Detail of contents of hadronic rescattering

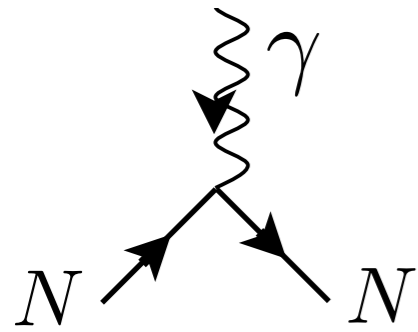


+

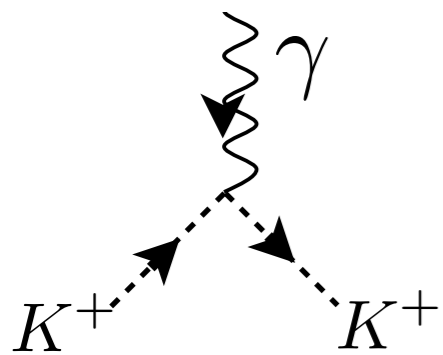


Effective Lagrangian

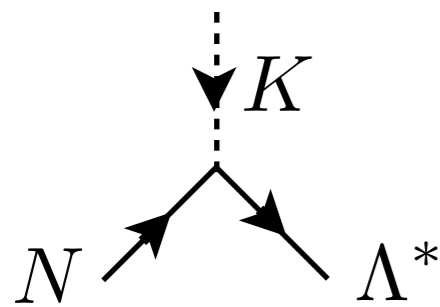
$$\Lambda^* = \Lambda(1520)$$



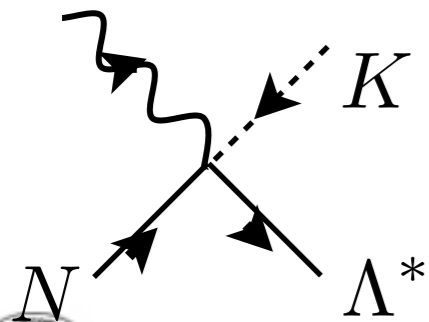
$$\mathcal{L}_{\gamma NN} = -e\bar{N} \left[\gamma^\mu - \frac{\kappa_N}{2M_N} \sigma_{\mu\nu} \partial_\nu \right] A_\mu N$$



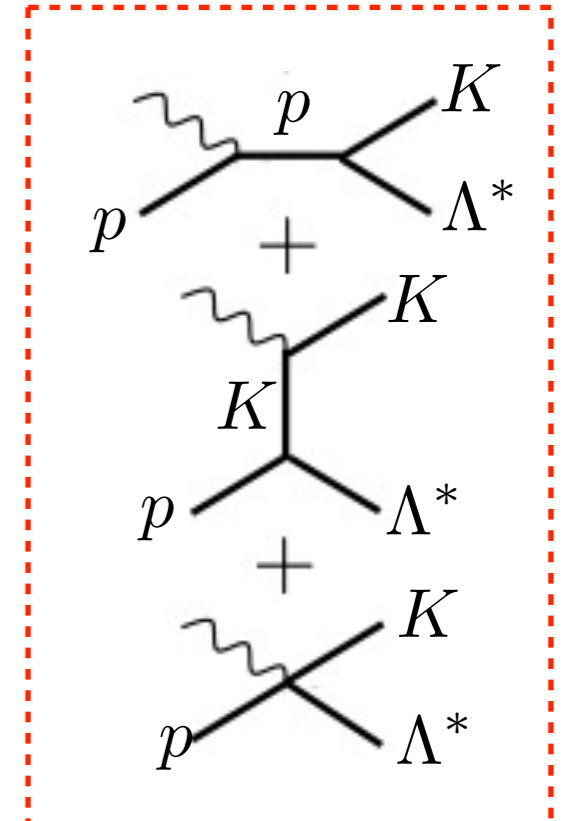
$$\mathcal{L}_{\gamma KK} = ie(\partial_\mu K^+ K^- - \partial_\mu K^- K^+) A^\mu$$



$$\mathcal{L}_{KN\Lambda^*} = \frac{g_{KN\Lambda^*}}{m_K} \bar{N} \gamma_5 \partial_\mu K^+ \Lambda^{*\mu}$$



$$\mathcal{L}_{\gamma KN\Lambda^*} = -i \frac{eg_{KN\Lambda^*}}{m_K} \bar{N} \gamma_5 A_\mu K^+ \Lambda^{*\mu}$$



$$\partial_\mu \rightarrow \partial_\mu - ieA_\mu$$



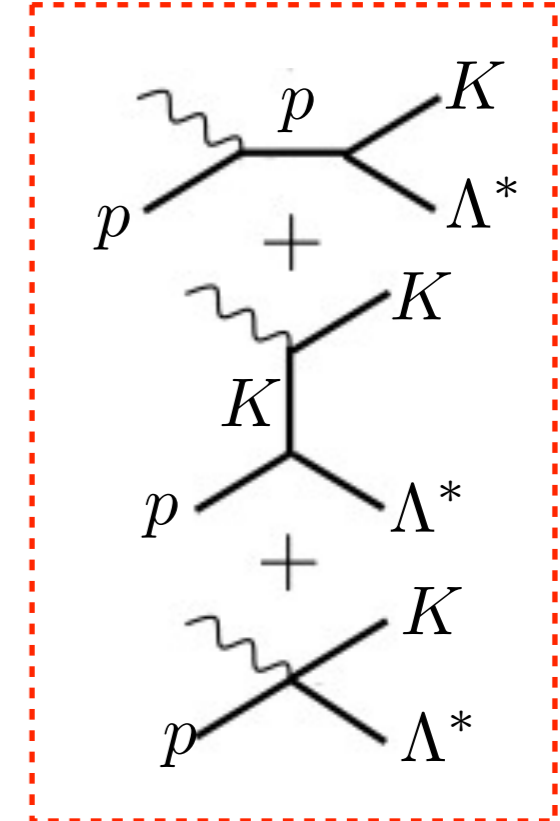
Invariant amplitude

$$\mathcal{M}_{L,s} = \frac{egKN\Lambda^*}{M_K} \bar{u}^\mu k_{2\mu} \gamma_5 \frac{k_1 + \not{q} + M_N}{q^2 - M_N^2} \not{\epsilon}_\gamma u(p_1),$$

$$+ \frac{e\kappa_p gKN\Lambda^*}{2M_N M_K} \bar{u}^\mu k_{2\mu} \gamma_5 \frac{\not{q} + M_N}{q^2 - M_p^2} \not{\epsilon}_\gamma \not{k}_1 u(p_1),$$

$$\mathcal{M}_{L,t} = -\frac{2egKN\Lambda^*}{M_K} \bar{u}^\mu \gamma_5 u(p_1) \frac{q_K^\mu}{t_K - M_K^2},$$

$$\mathcal{M}_{L,c} = \frac{egKN\Lambda^*}{M_K} \bar{u}^\mu \epsilon_\mu \gamma_5 u(p_1),$$



$$\mathcal{M}_L(\gamma p \rightarrow K^+ \Lambda^*) = (\mathcal{M}_{L,s} + \mathcal{M}_{L,t} + \mathcal{M}_{L,c}) F_L(s, t),$$

$$\mathcal{M}_R(K^+ \Lambda^* \rightarrow \phi p) = (\mathcal{M}_{R,s} + \mathcal{M}_{R,t} + \mathcal{M}_{R,c}) F_R(s, t),$$

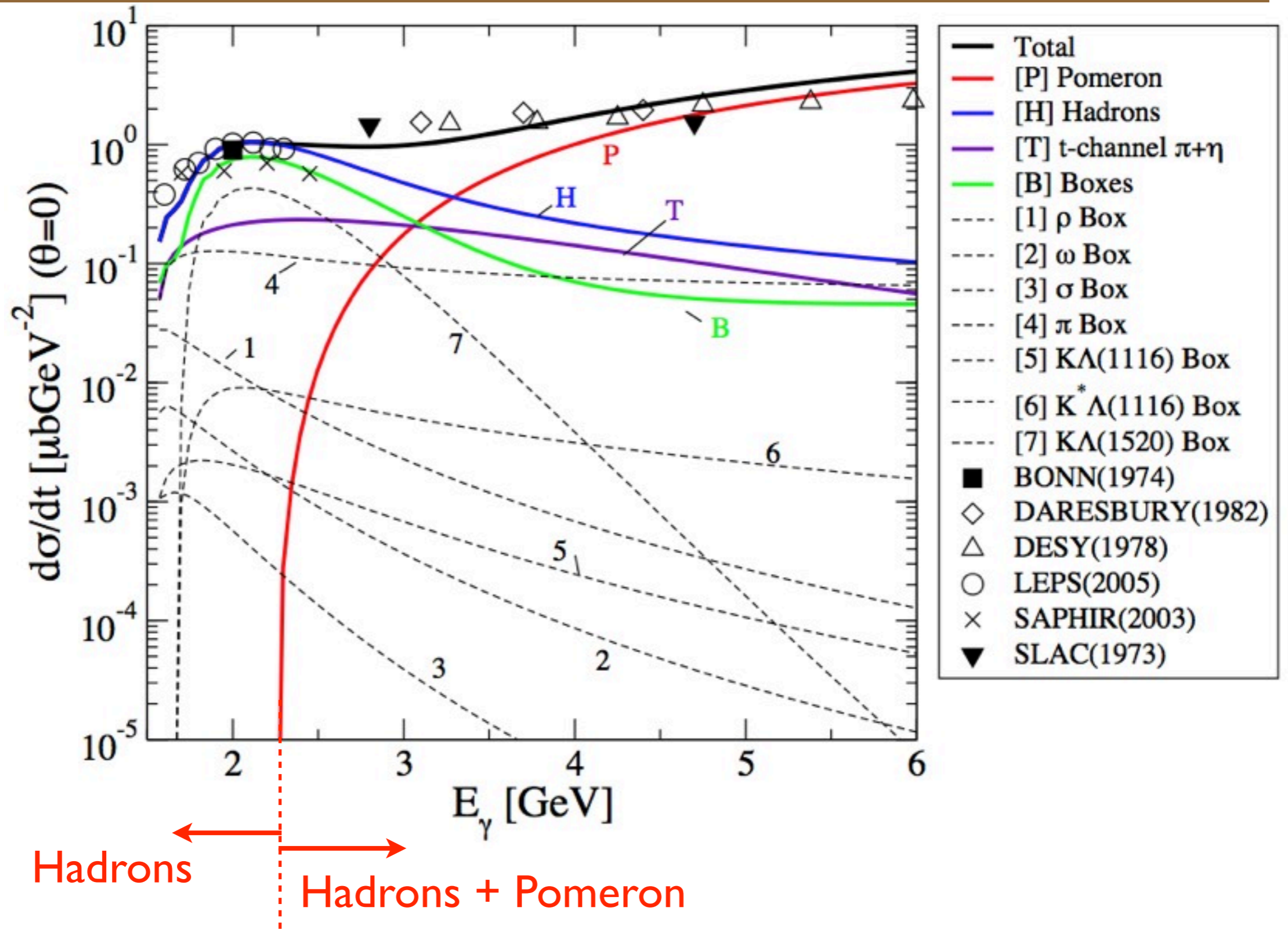
$$F_R(s, t) = \left[\frac{n_1 \Lambda_1^4}{n_1 \Lambda_1^4 + (s - M_p^2)^2} \right]^{n_1} \left[\frac{n_2 \Lambda_2^4}{n_2 \Lambda_2^4 + t^2} \right]^{n_2}$$

$$F_L(s, t) = \left[\frac{n_3 \Lambda_3^4}{n_3 \Lambda_3^4 + (s - M_p^2)^2} \right]^{n_3} \left[\frac{n_4 \Lambda_4^4}{n_4 \Lambda_4^4 + t^2} \right]^{n_4}$$

n_1	1
n_2	1
n_3	2
n_4	1
Λ_1	0.8 GeV
Λ_2	0.8 GeV
Λ_3	1.0 GeV
Λ_4	1.0 GeV

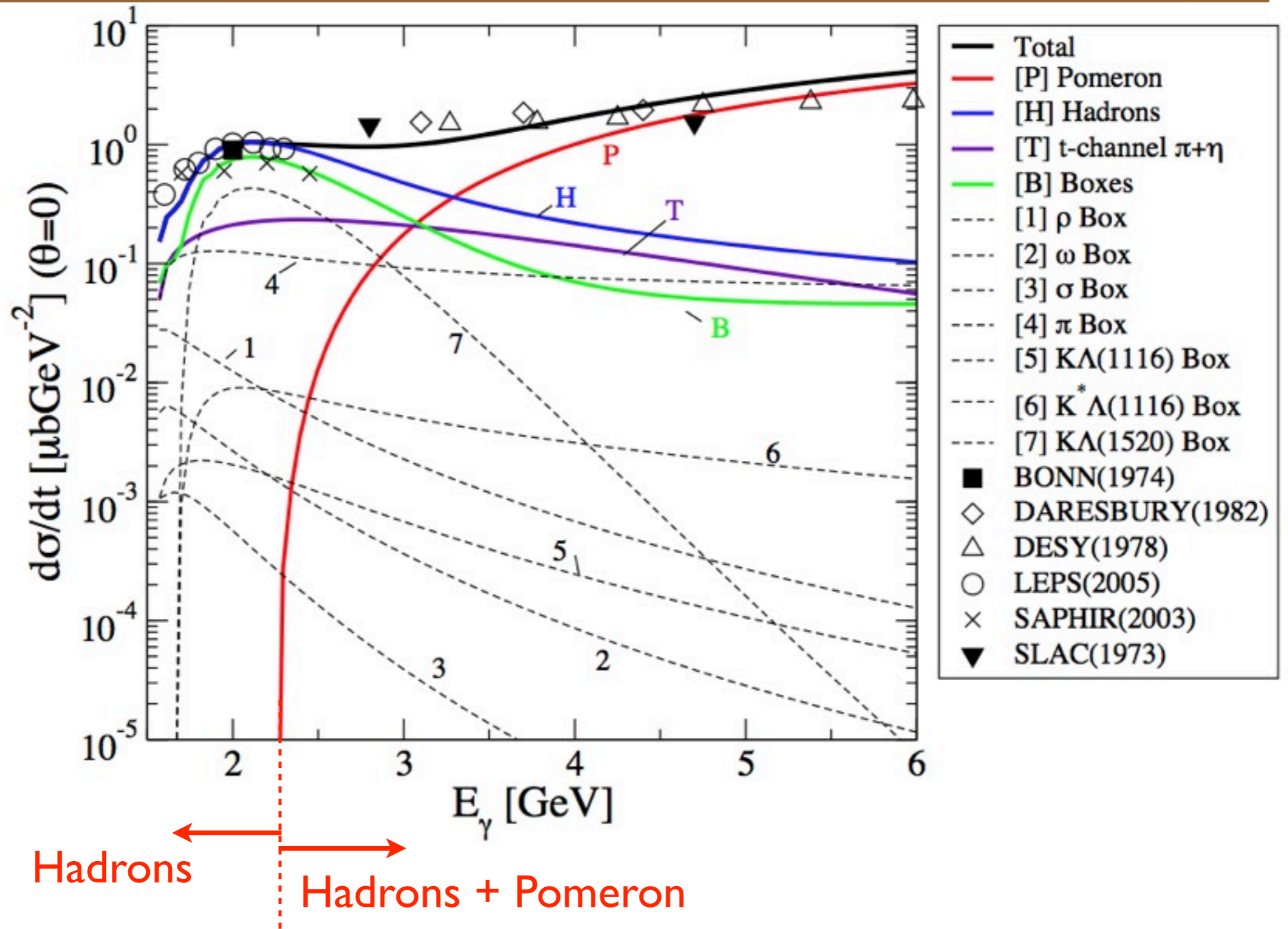


III. Numerical Result



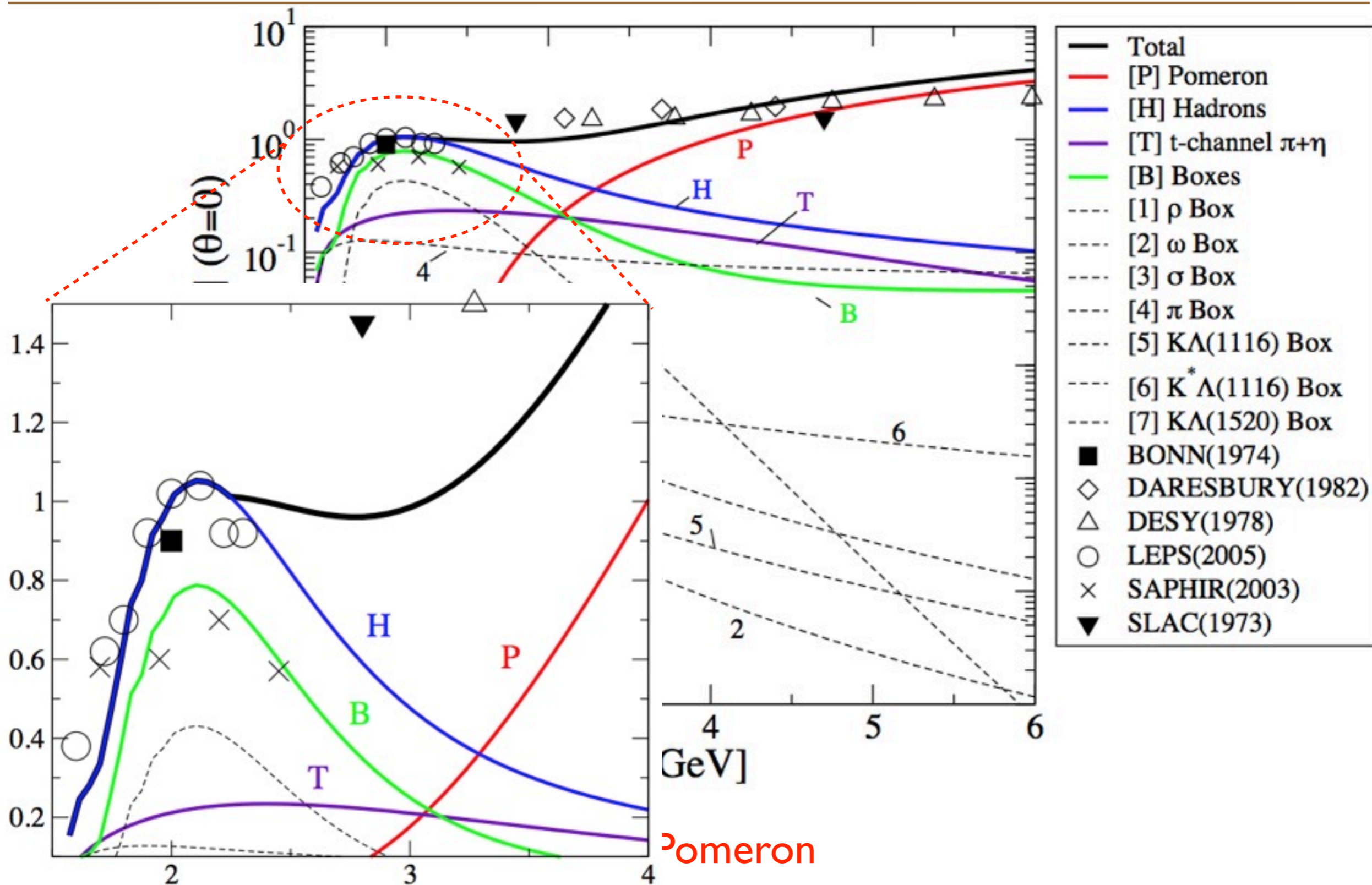
III. Numerical Result

$$M(s, t) = C_p F_N(t) F_\phi(t) \frac{1}{s} \left(\frac{s - s_{th}}{4} \right)^{\alpha_p(t)} \exp\left(-\frac{i\pi}{2} \alpha_p(t) \right)$$

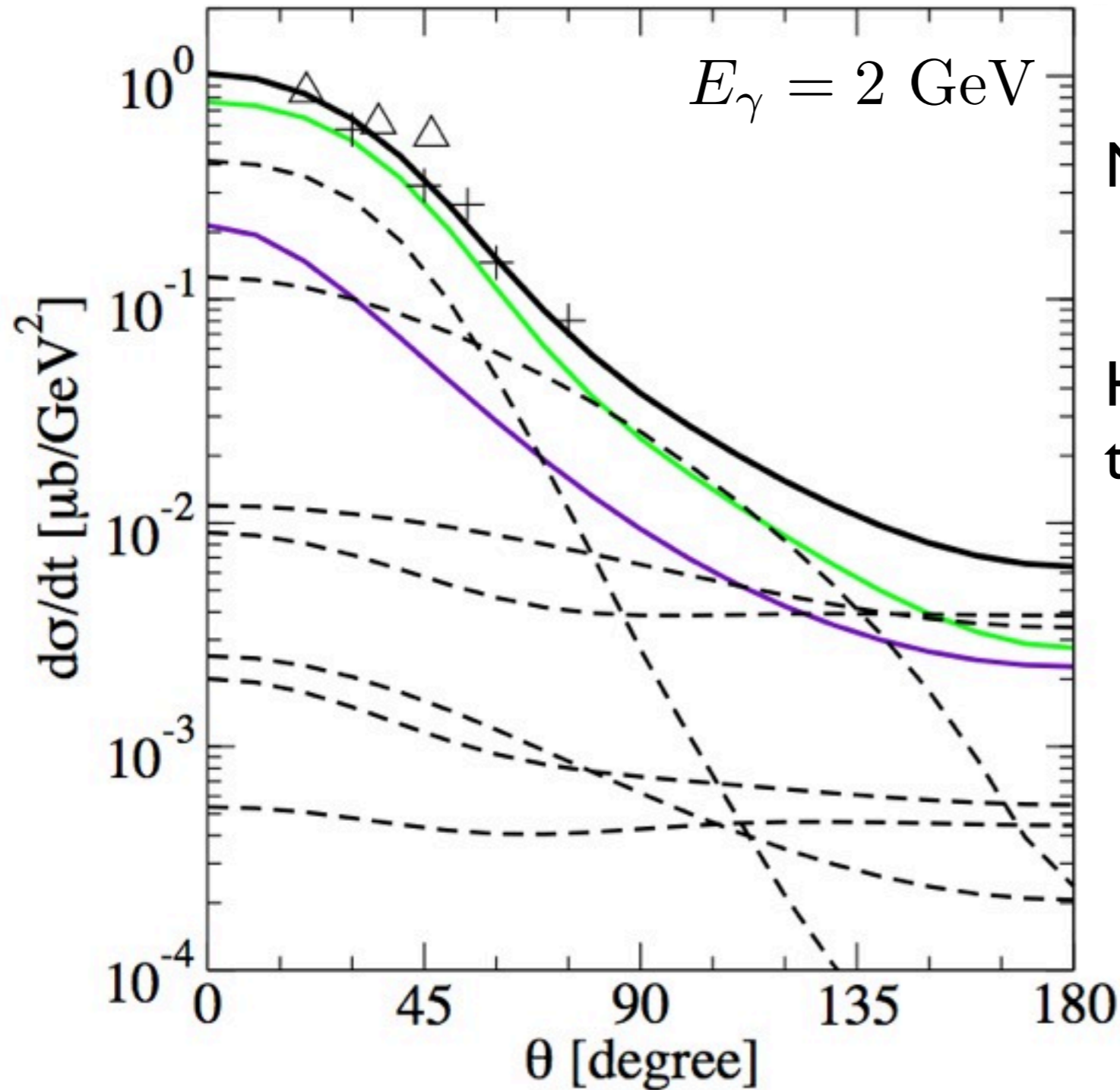


III. Numerical Result

$$M(s, t) = C_p F_N(t) F_\phi(t) \frac{1}{s} \left(\frac{s - s_{th}}{4} \right)^{\alpha_p(t)} \exp\left(-\frac{i\pi}{2} \alpha_p(t) \right)$$



Angular distribution



No Pomeron contribution.

Hadronic process can explain the angular distribution.



Spin density matrix and Decay angular distribution

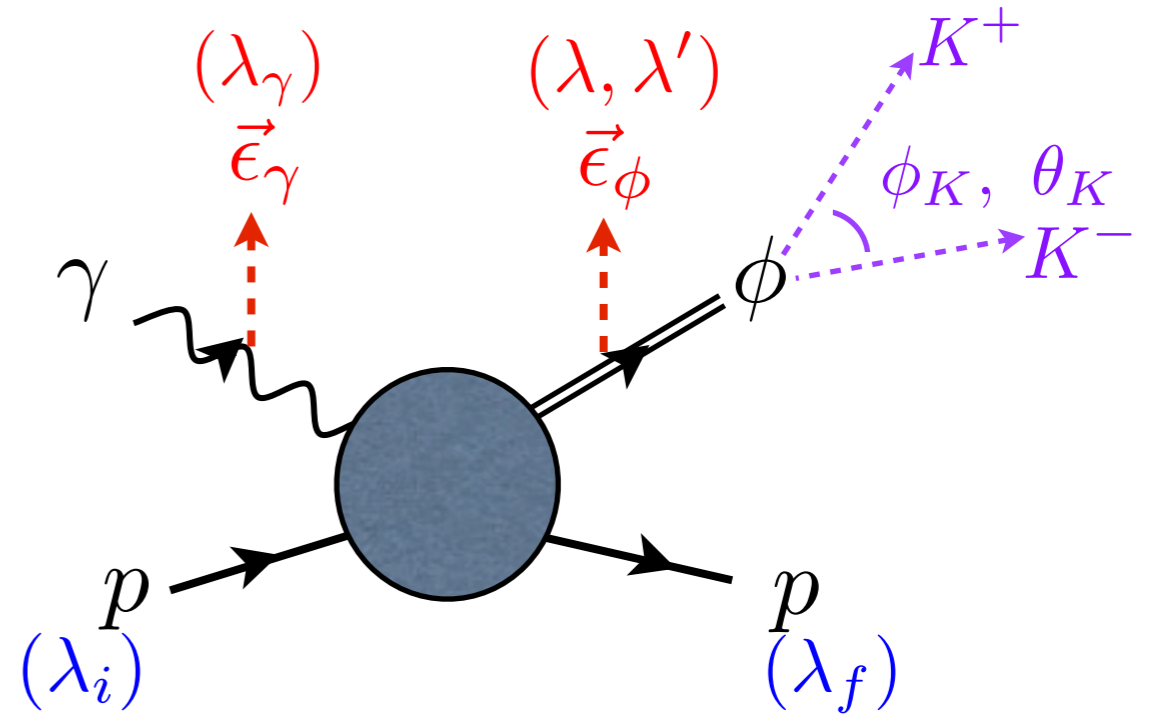
$$\rho_{\lambda\lambda'}^0 = \frac{1}{N} \sum_{\lambda_\gamma, \lambda_i, \lambda_f} T_{\lambda_f, \lambda; \lambda_i, \lambda_\gamma} T_{\lambda_f, \lambda'; \lambda_i, \lambda_\gamma}^*$$

$$\rho_{\lambda\lambda'}^1 = \frac{1}{N} \sum_{\lambda_\gamma, \lambda_i, \lambda_f} T_{\lambda_f, \lambda; \lambda_i, -\lambda_\gamma} T_{\lambda_f, \lambda'; \lambda_i, \lambda_\gamma}^*$$

$$\rho_{\lambda\lambda'}^2 = \frac{i}{N} \sum_{\lambda_\gamma, \lambda_i, \lambda_f} \lambda_\gamma T_{\lambda_f, \lambda; \lambda_i, -\lambda_\gamma} T_{\lambda_f, \lambda'; \lambda_i, \lambda_\gamma}^*$$

$$\rho_{\lambda\lambda'}^3 = \frac{1}{N} \sum_{\lambda_\gamma, \lambda_i, \lambda_f} \lambda_\gamma T_{\lambda_f, \lambda; \lambda_i, \lambda_\gamma} T_{\lambda_f, \lambda'; \lambda_i, \lambda_\gamma}^*$$

$$N = \sum |T_{\lambda_f, \lambda; \lambda_i, \lambda_\gamma}|^2$$



$$W_1(\cos \theta_K) = \frac{1}{2}(1 - \rho_{00}^0) + \frac{1}{2}(3\rho_{00}^0 - 1) \cos^2 \theta_K$$

$$2\pi W_2(\phi_K - \Phi) = 1 + 2p_\gamma \bar{\rho}_{1-1}^1 \cos 2(\phi_K - \Phi)$$

$$2\pi W_3(\phi_K + \Phi) = 1 + 2p_\gamma \Delta_{1-1} \cos 2(\phi_K + \Phi)$$

$$\bar{\rho}_{1-1}^1 = \frac{1}{2}(\rho_{1-1}^1 - \text{Im}\rho_{1-1}^2)$$

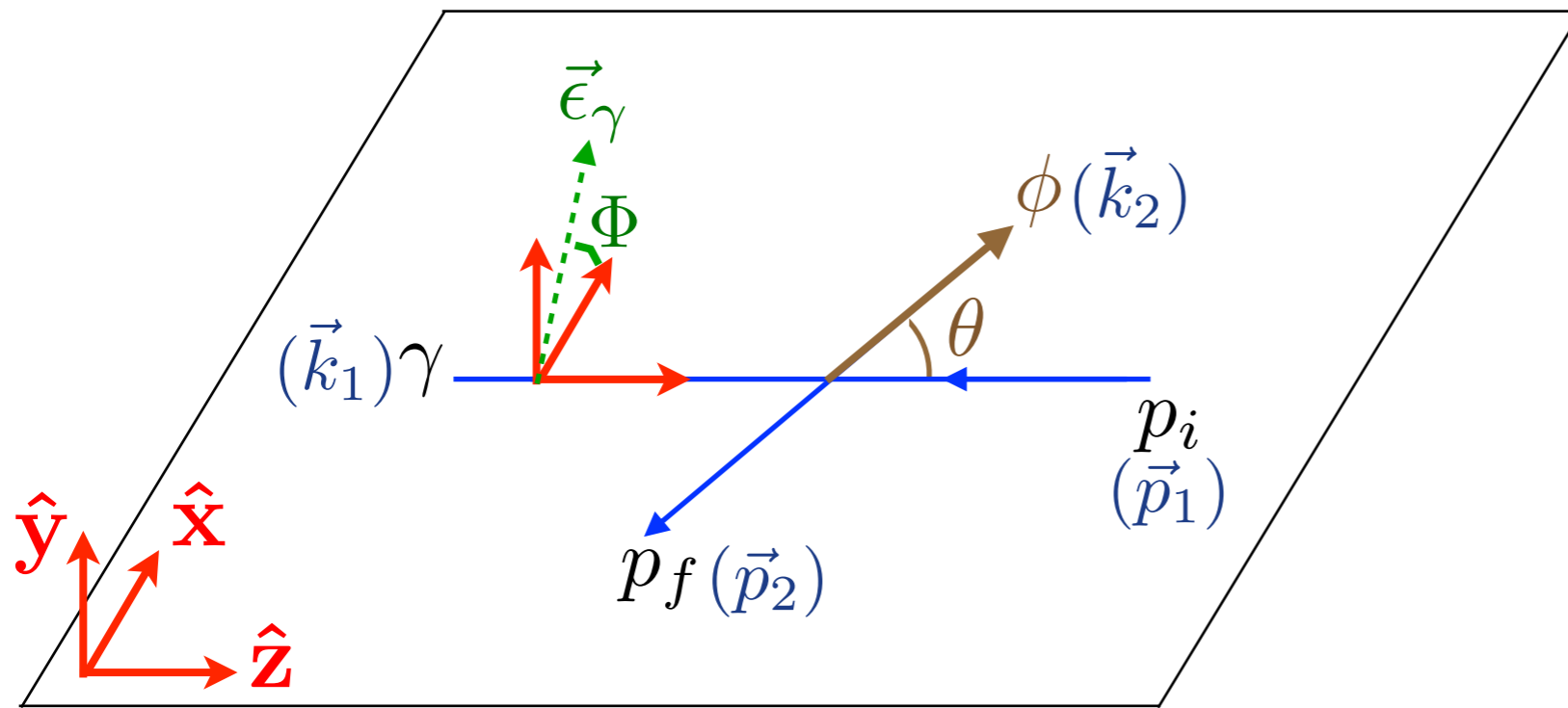
$$\Delta_{1-1} = \frac{1}{2}(\rho_{1-1}^1 + \text{Im}\rho_{1-1}^2)$$

(p_γ : polarization strength $\simeq 0.95$)



Definition of angles

Φ : azimuthal angle for the reaction plane



C.M. system

$$\vec{k}_1 + \vec{p}_1 = 0$$

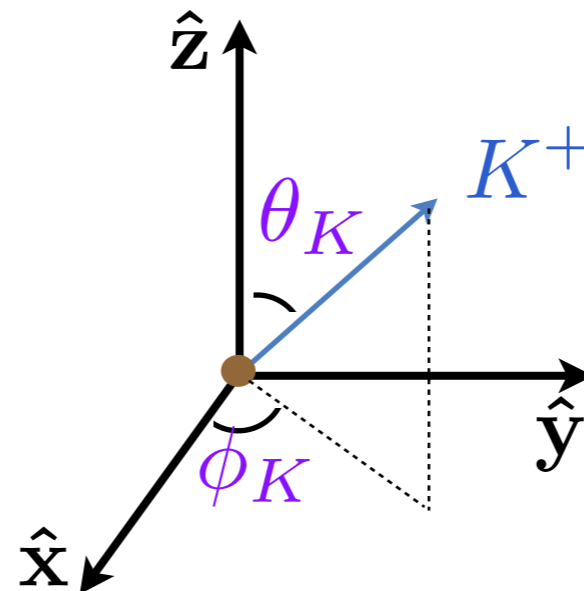
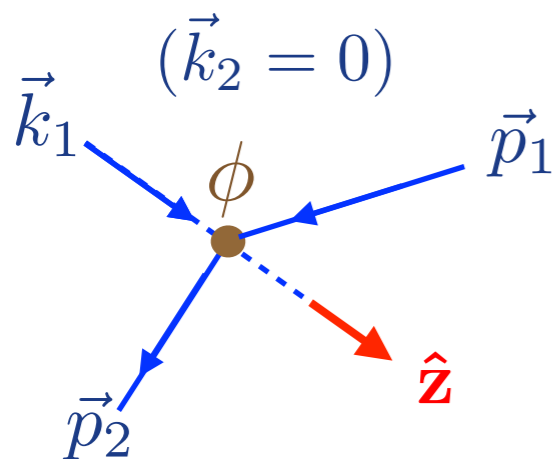
Rotation
Boost



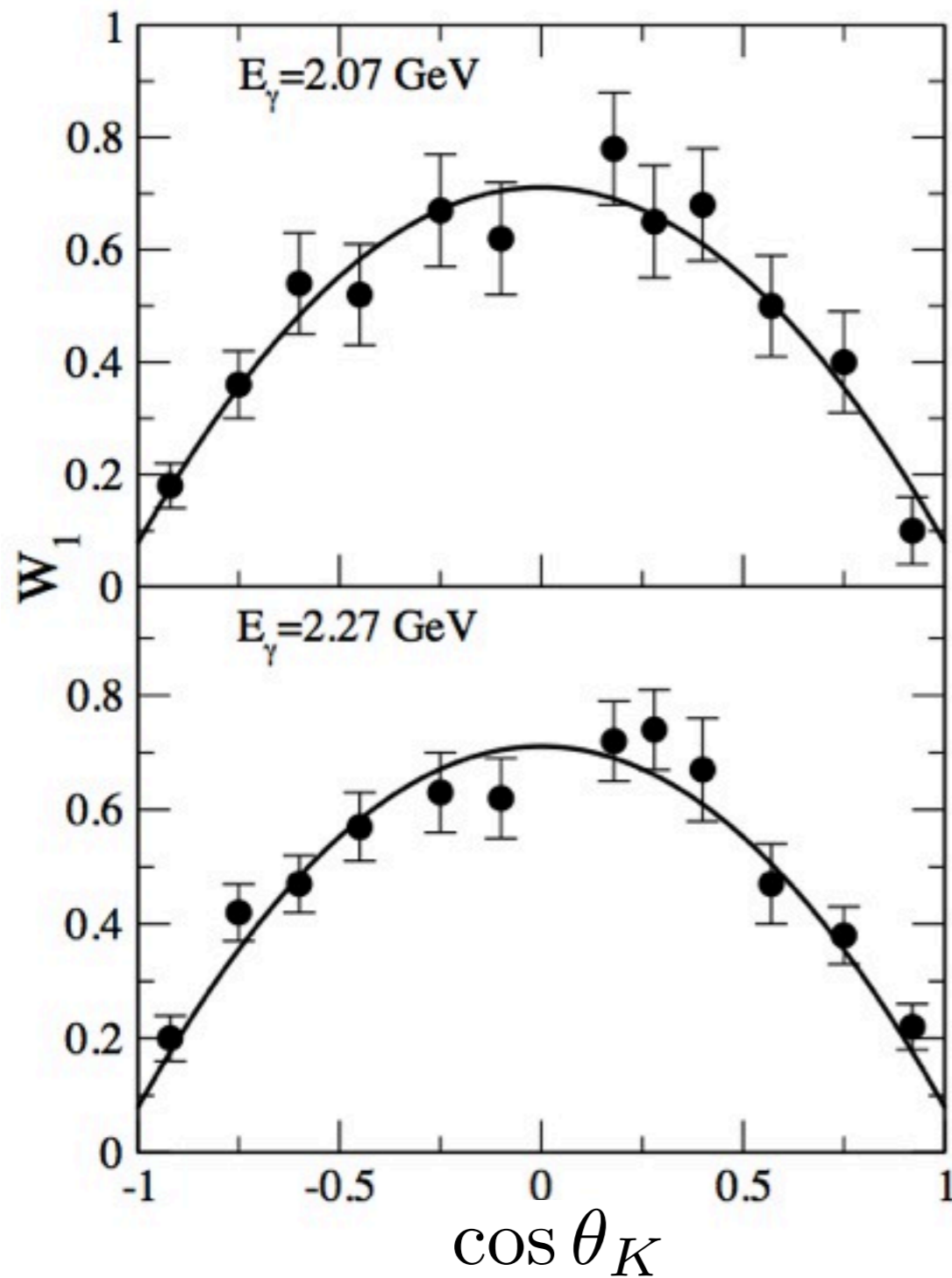
G.J. system

$$\vec{k}_2 = 0$$

$$\vec{k}_1 \parallel \hat{z}$$



$$\rho_{00}^0 = \frac{|T_{0,-1}|^2 + |T_{0,1}|^2}{|T_{-1,-1}|^2 + |T_{-1,1}|^2 + |T_{0,-1}|^2 + |T_{0,1}|^2 + |T_{1,-1}|^2 + |T_{1,1}|^2} \quad (T_{\lambda\phi\lambda\gamma})$$



$$W_1(\cos \theta_K) = \frac{1}{2}(1 - \rho_{00}^0) + \frac{1}{2}(3\rho_{00}^0 - 1) \cos^2 \theta_K$$

If $\rho_{00}^0 = 0$,

$$W_1(\cos \theta_K) = 0.5 + 0.5 \cos^2 \theta_K$$

If $\rho_{00}^0 = 0.5$,

$$W_1(\cos \theta_K) = 0.25 + 0.25 \cos^2 \theta_K$$

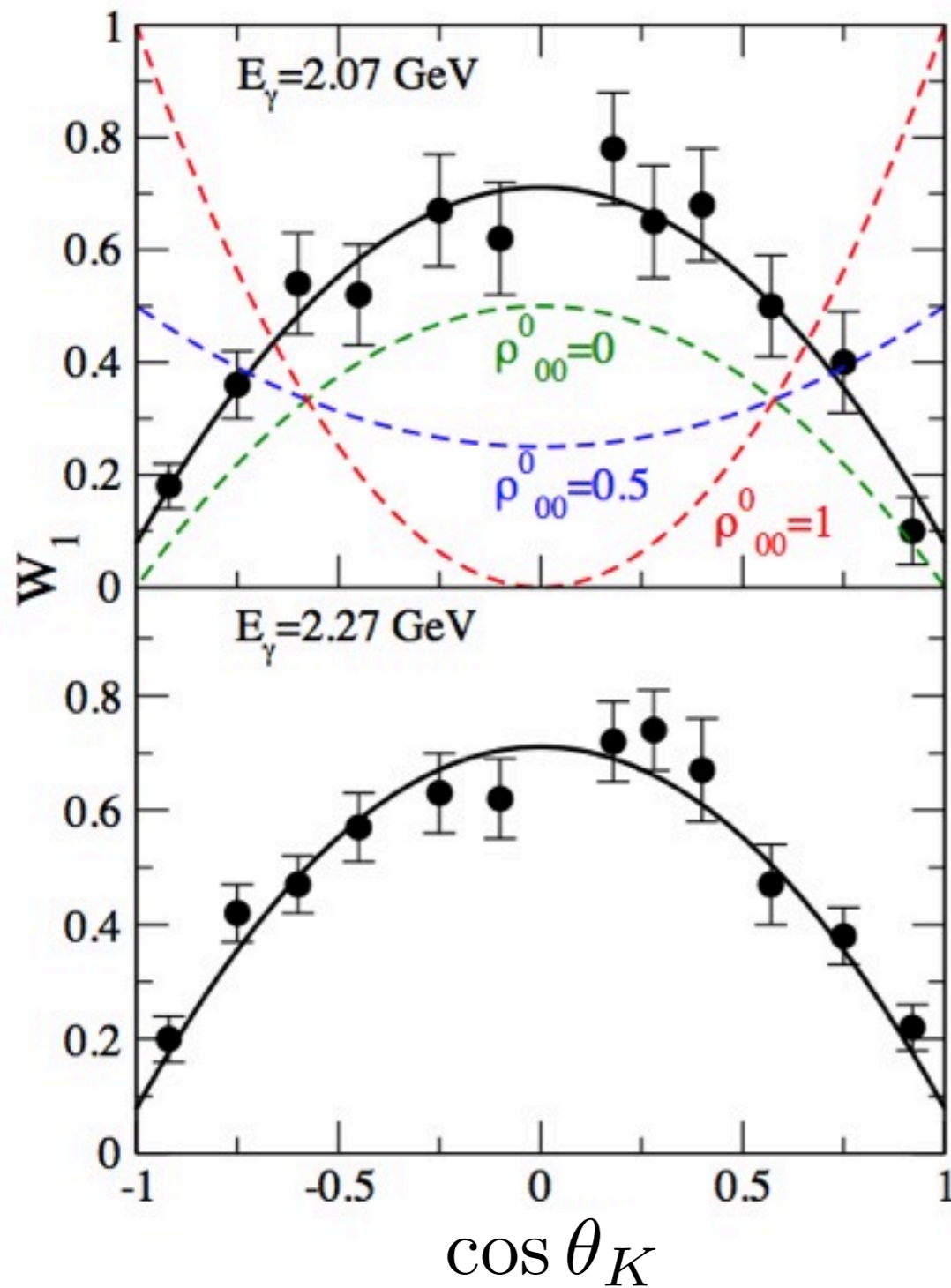
If $\rho_{00}^0 = 1$,

$$W_1(\cos \theta_K) = \cos^2 \theta_K$$

T. Mibe *et al.* [LEPS Collaboration], Phys. Rev. Lett. **95**, 182001 (2005)



$$\rho_{00}^0 = \frac{|T_{0,-1}|^2 + |T_{0,1}|^2}{|T_{-1,-1}|^2 + |T_{-1,1}|^2 + |T_{0,-1}|^2 + |T_{0,1}|^2 + |T_{1,-1}|^2 + |T_{1,1}|^2} \quad (T_{\lambda\phi\lambda\gamma})$$



$$W_1(\cos \theta_K) = \frac{1}{2}(1 - \rho_{00}^0) + \frac{1}{2}(3\rho_{00}^0 - 1) \cos^2 \theta_K$$

If $\rho_{00}^0 = 0$,

$$W_1(\cos \theta_K) = 0.5 + 0.5 \cos^2 \theta_K$$

If $\rho_{00}^0 = 0.5$,

$$W_1(\cos \theta_K) = 0.25 + 0.25 \cos^2 \theta_K$$

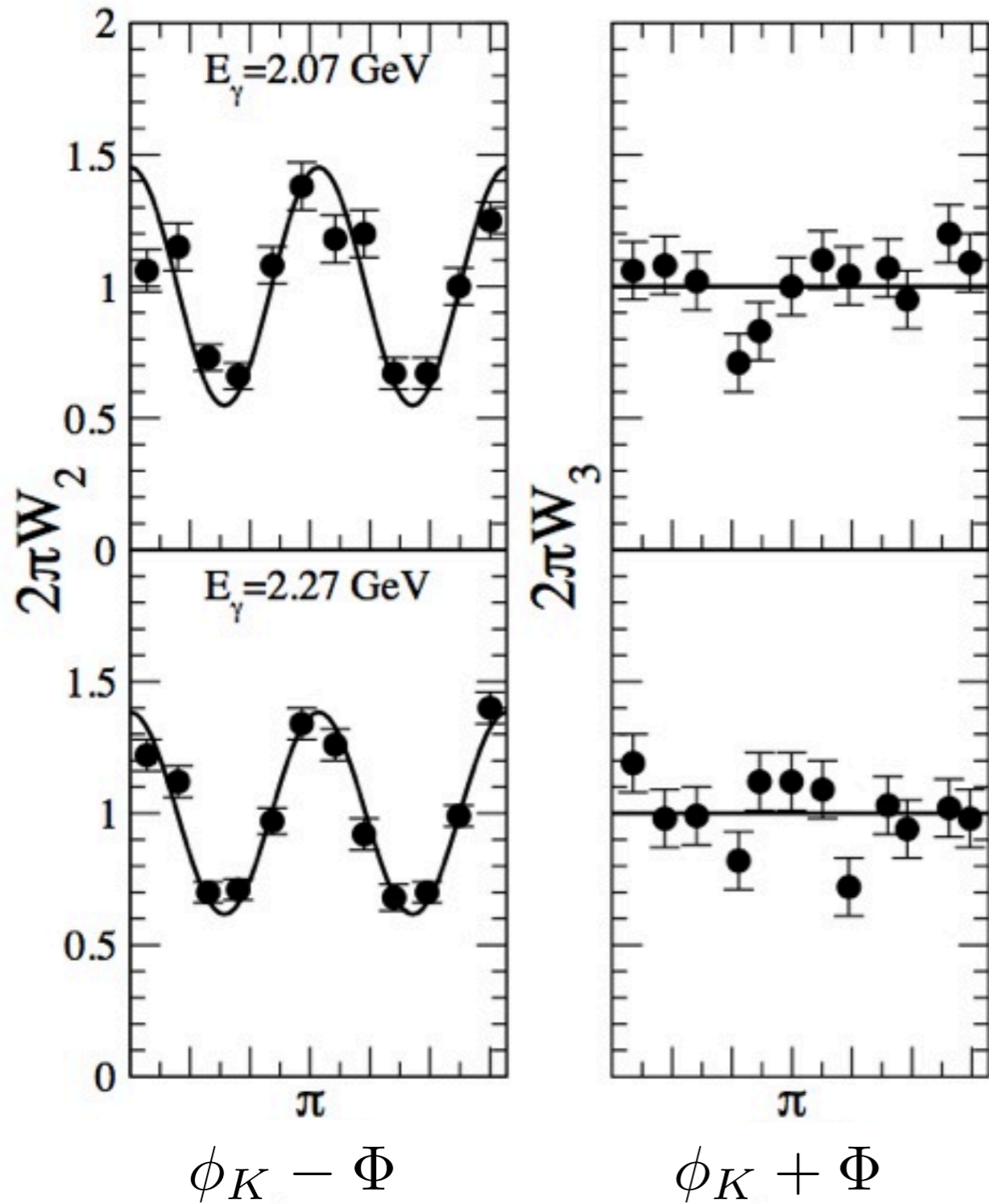
If $\rho_{00}^0 = 1$,

$$W_1(\cos \theta_K) = \cos^2 \theta_K$$

T. Mibe *et al.* [LEPS Collaboration], Phys. Rev. Lett. **95**, 182001 (2005)



T. Mibe et al. [LEPS Collaboration],
Phys. Rev. Lett. 95, 182001 (2005)



$$2\pi W_2(\phi_K - \Phi) = 1 + 2p_\gamma \bar{\rho}_{1-1}^1 \cos 2(\phi_K - \Phi)$$

$$2\pi W_3(\phi_K + \Phi) = 1 + 2p_\gamma \Delta_{1-1} \cos 2(\phi_K + \Phi)$$

$$\bar{\rho}_{1-1}^1 = \frac{1}{2}(\rho_{1-1}^1 - \text{Im}\rho_{1-1}^2)$$

$$\Delta_{1-1} = \frac{1}{2}(\rho_{1-1}^1 + \text{Im}\rho_{1-1}^2)$$

$$\rho_{1-1}^1 = \frac{1}{N} [T_{11}T_{-1-1}^* + T_{1-1}T_{-11}^*]$$

$$\rho_{1-1}^2 = \frac{i}{N} [-T_{11}T_{-1-1}^* + T_{1-1}T_{-11}^*]$$

$$T_{-\lambda-\lambda_\gamma}^{[N]} = \pm(-1)^{\lambda-\lambda_\gamma} T_{\lambda\lambda_\gamma} \text{ at high energy.}$$

$$\bar{\rho}_{1-1}^1 = \frac{1}{N} |T_{11}|^2$$

$$\Delta_{1-1} = \frac{1}{N} |T_{1-1}|^2$$

(natural)

$$\bar{\rho}_{1-1}^1 = -\frac{1}{N} |T_{11}|^2$$

$$\Delta_{1-1} = -\frac{1}{N} |T_{1-1}|^2$$

(unnatural)



Real part calculation

$$\begin{aligned} & \frac{1}{(2\pi)^3} \int \frac{dk^3}{2\omega_1\omega_2} \frac{(\omega_1 + \omega_2)}{(\omega_1 + \omega_2)^2 - s} T_{M_i B_i \rightarrow \phi p} T_{\gamma p \rightarrow M_i B_i} \\ &= \frac{1}{(2\pi)^3} \int d\Omega \int_0^\infty dk \frac{k(\omega_1 + \omega_2)}{2\omega_1\omega_2} \left[\frac{k f(k)}{(\omega_1 + \omega_2)^2 - s} - \frac{h f(h)}{(\omega_1 + \omega_2)^2 - s} \right] \\ & \quad + \frac{1}{(2\pi)^3} \frac{h f(h)}{2\sqrt{s}} \int d\Omega \ln \left| \frac{\mu + \sqrt{s}}{\mu - \sqrt{s}} \right| \end{aligned}$$

$$f(k) = T_{M_i B_i \rightarrow \phi p} T_{\gamma p \rightarrow M_i B_i}$$

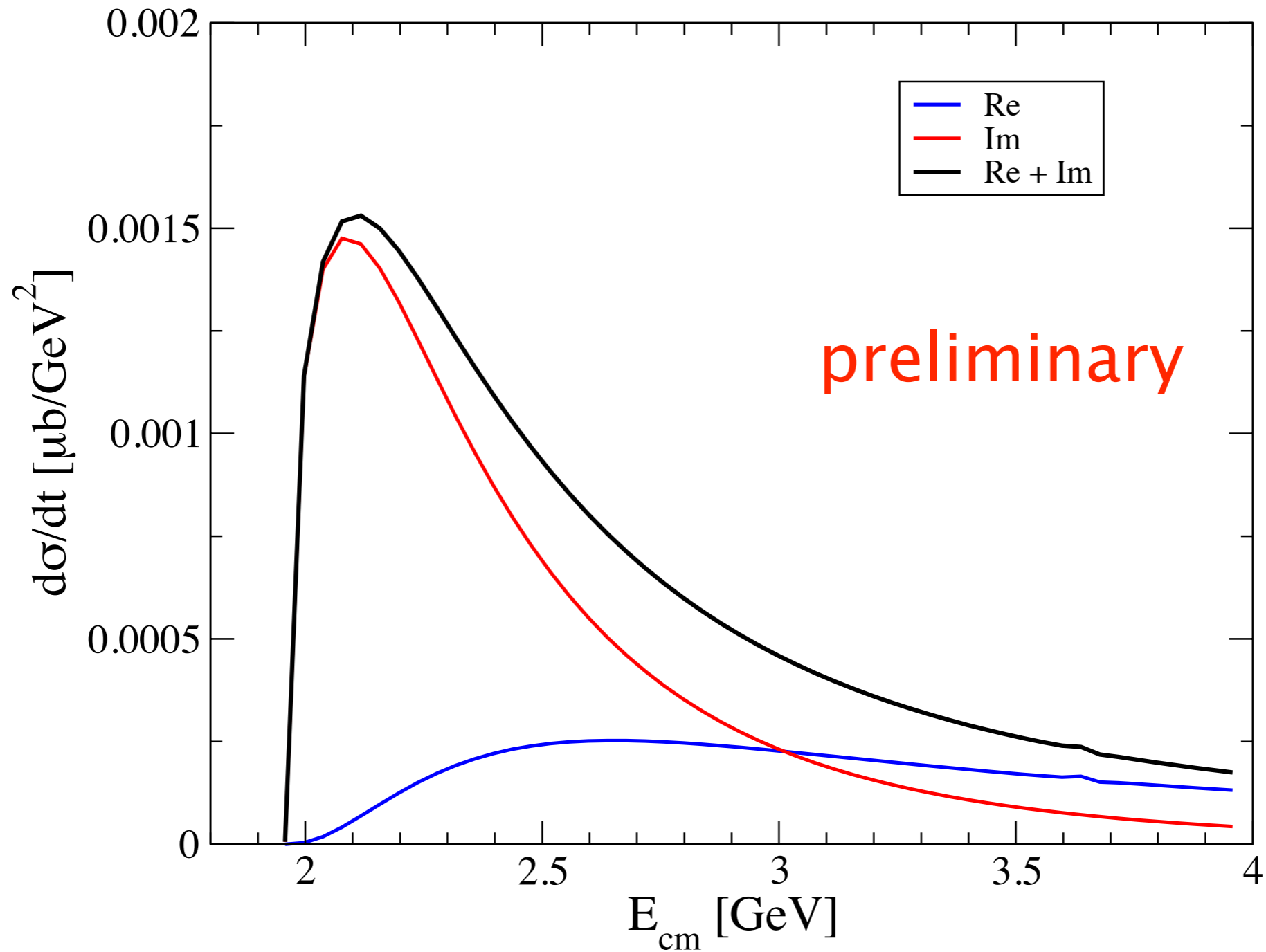
$$(\omega_1(h) + \omega_2(h))^2 - s = 0$$

$$\mu = M_{M_i} + M_{B_i}$$



Real part calculation

$(M_i, B_i) = (\rho, p)$ intermediate case



Summary of part I

■ **What's new ?**

- **Rescattering** contributions are essential to reproduce the bump structure near the threshold energy.

■ **What's questions ?**

- Application of **Pomeron** at low energy is still in ambiguities. We would like to determine the range of threshold energy of **Pomeron** by calculating other scattering processes.
- How to determine the parameters in form factors ?

■ **What's next ?**

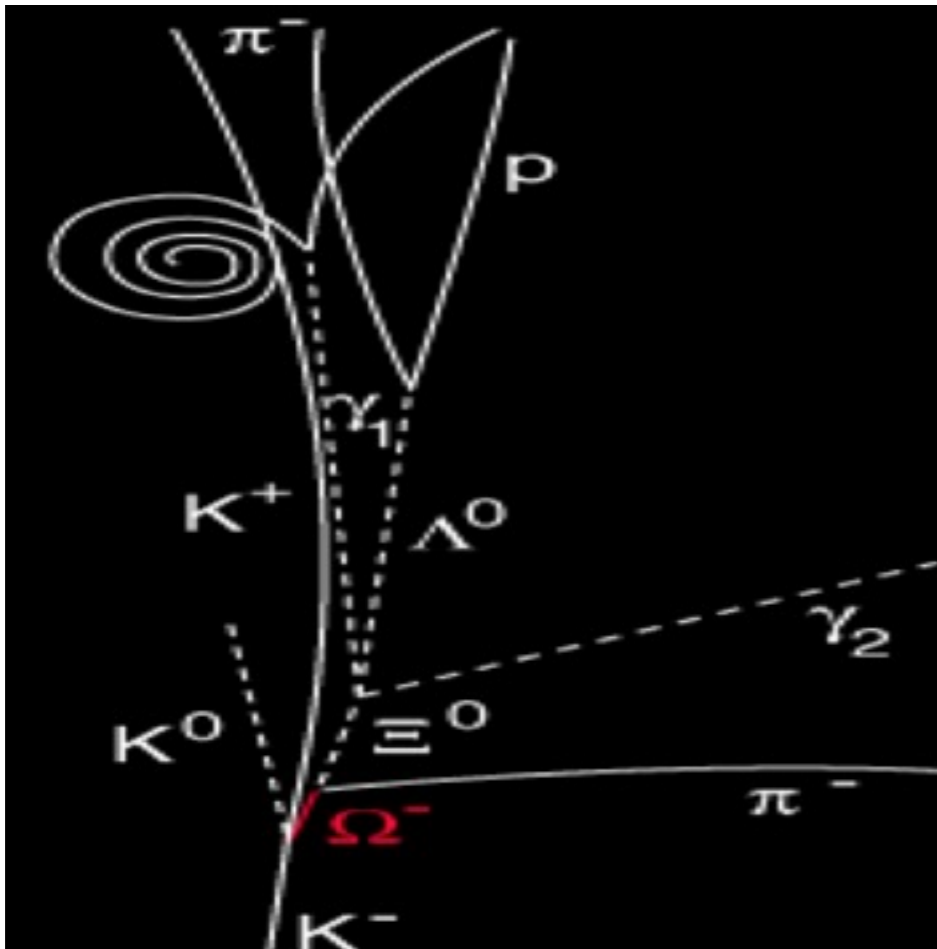
- Real part calculation and beam-, target- **asymmetry** are next work.
- We are going to calculate the **neutron target** process via similar rescattering processes. This is next project.



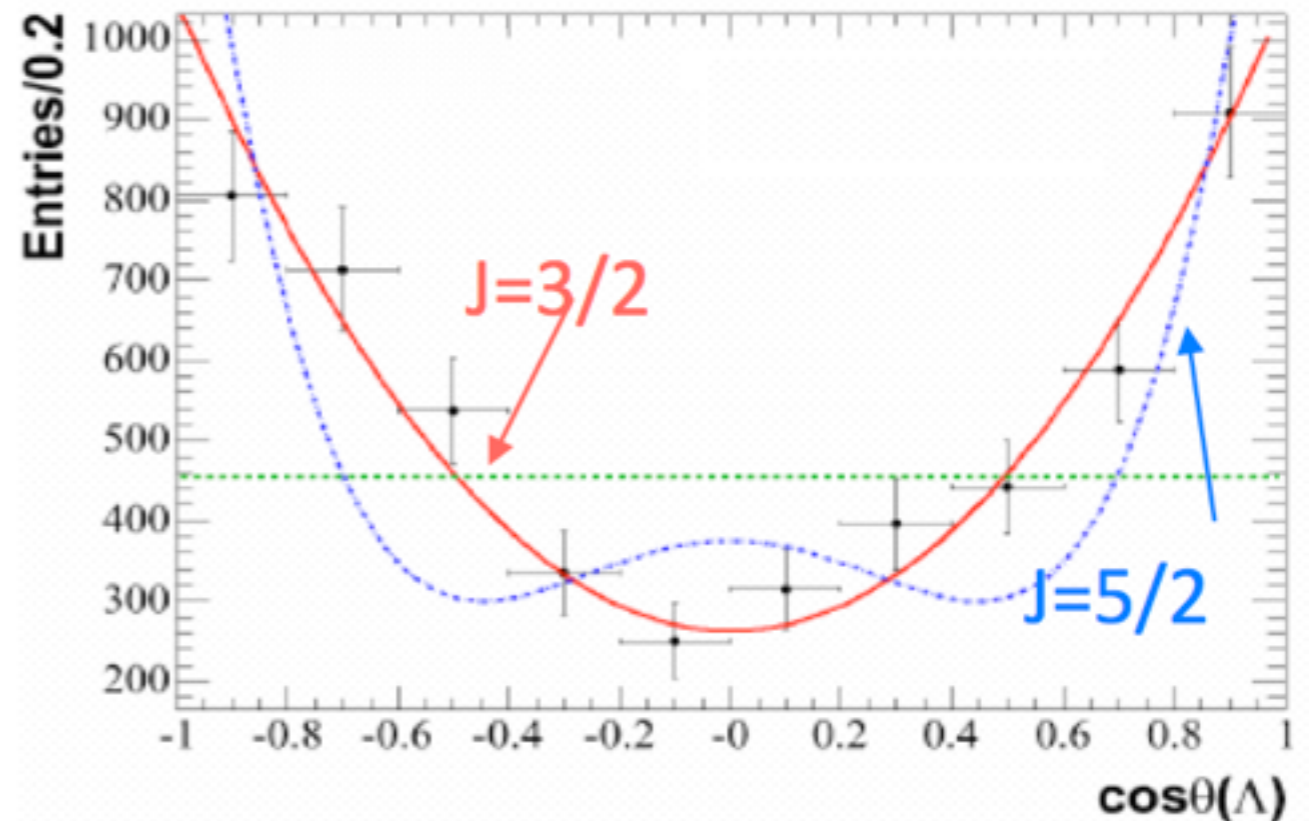


PART II. $\gamma p \rightarrow K^+ K^+ K^0 \Omega^-$

Introduction

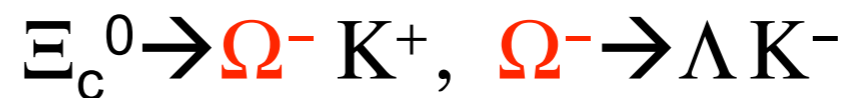


Barnes et al, PRL 12, 204 (1964)



Aubert et al, PRL.97, 112001 (2006)

First measurement of $J(\Omega^-)$ at SLAC



Introduction

Photoproduction of the Very Strangest Baryons on a Proton Target in CLAS12

A. Afanasev, W.J. Briscoe, H. Haberzettl, I.I. Strakovsky*, and R.L. Workman

The George Washington University, Washington, DC 20052, USA

M.J. Amarian, G. Gavalian, and M.C. Kunkel

Old Dominion University, Norfolk, VA 23529, USA

Ya.I. Azimov

Petersburg Nuclear Physics Institute, Gatchina, Russia 188300

•
•
•

V. Shklyar

Giessen University, D-35392 Giessen, Germany

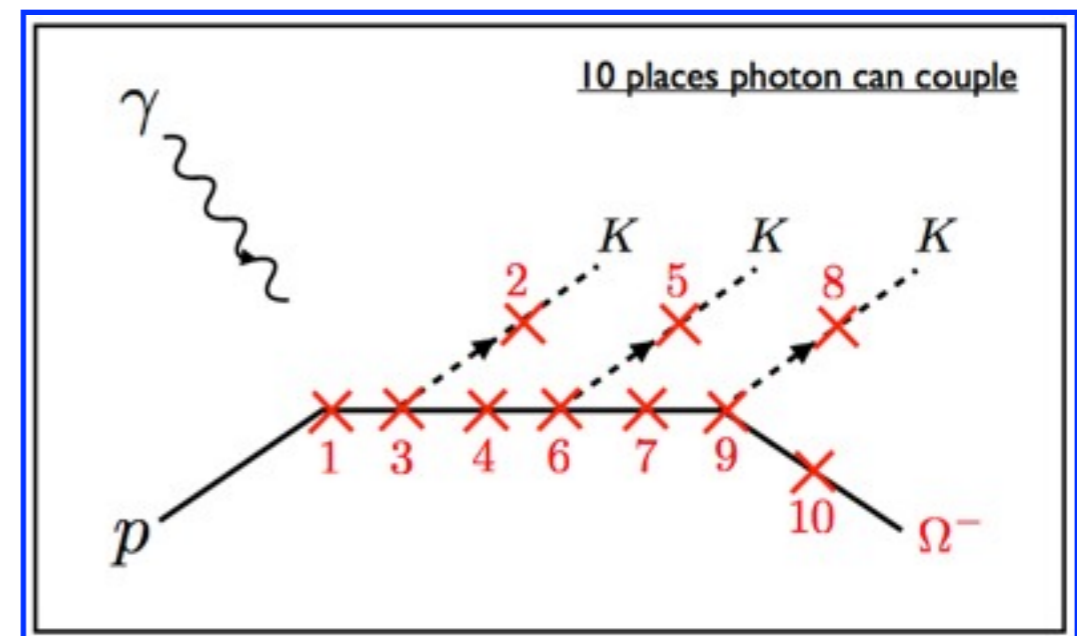
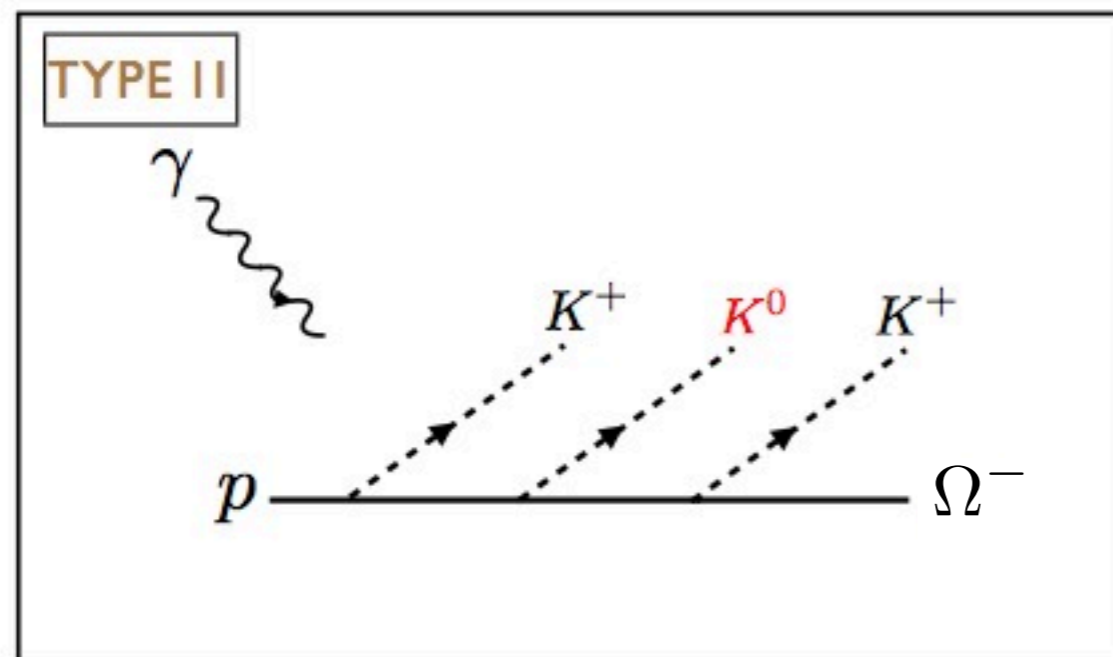
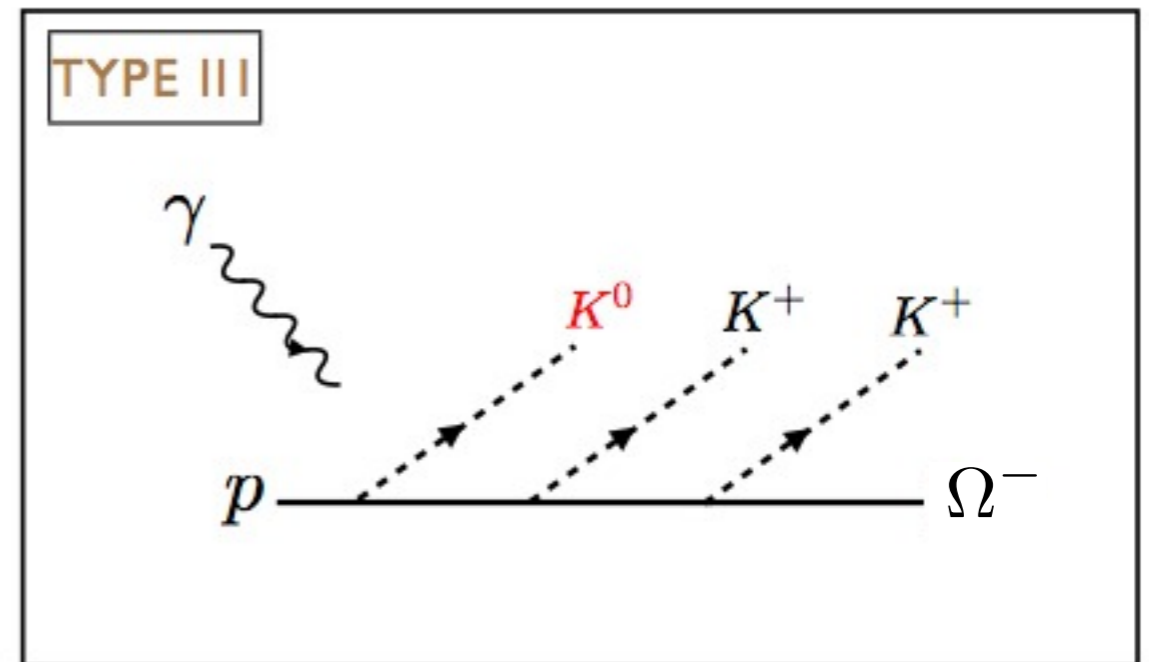
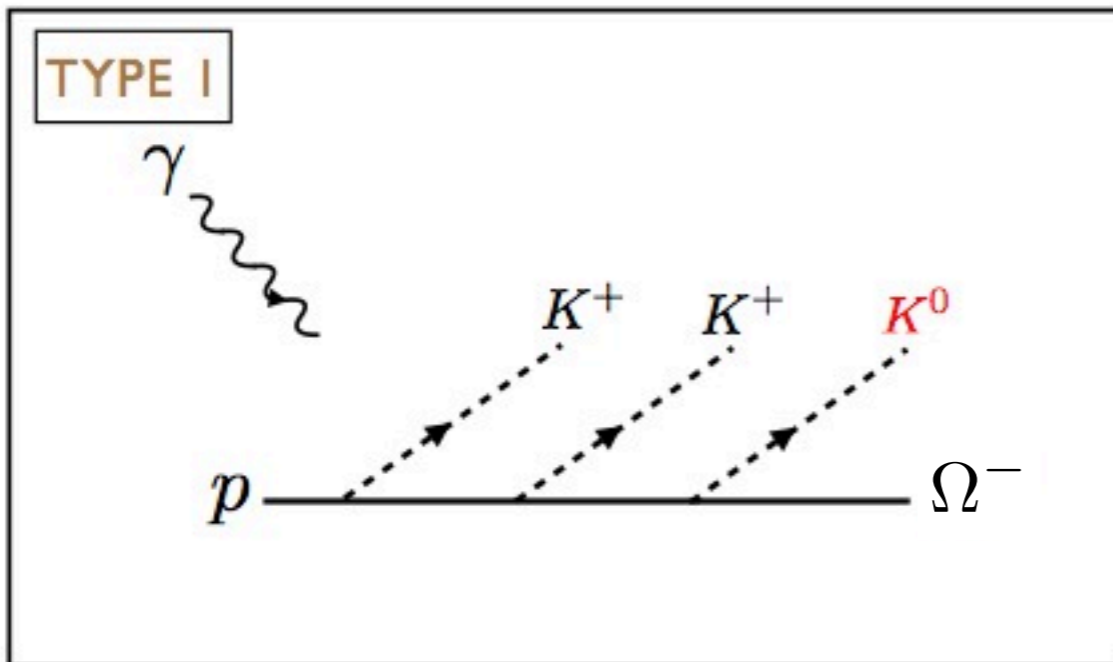
(The Very Strange Collaboration)

** - Contact person, * - Spokesperson

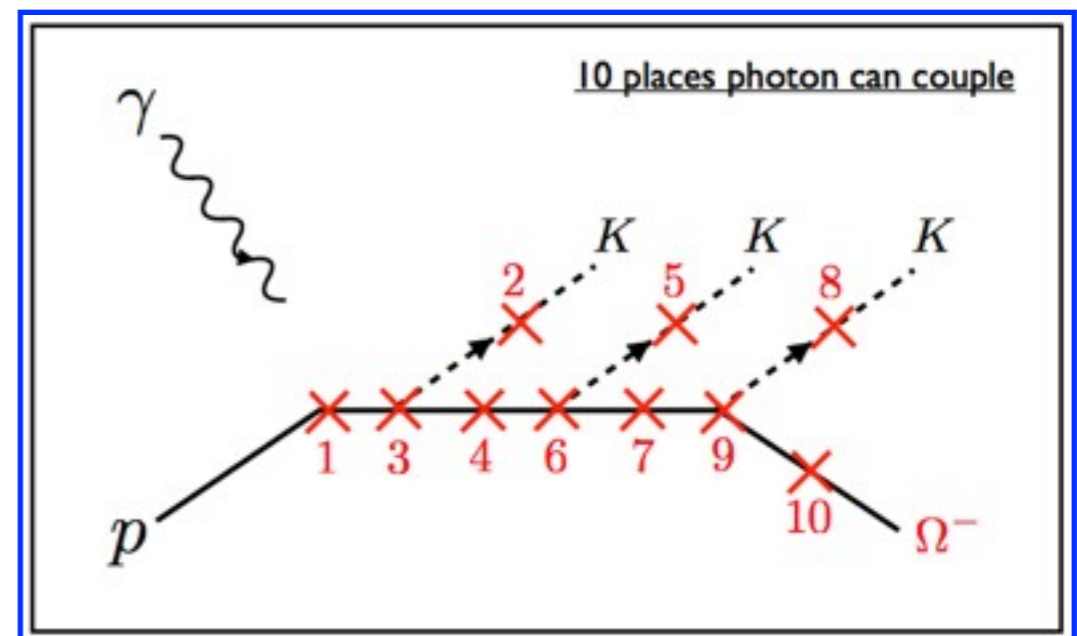
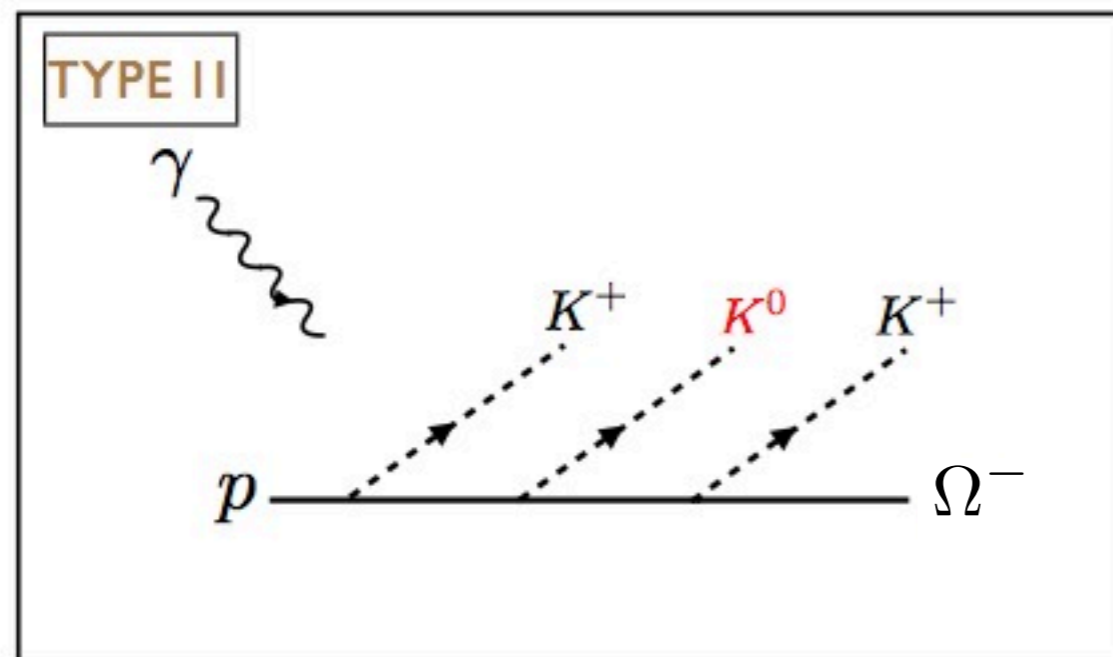
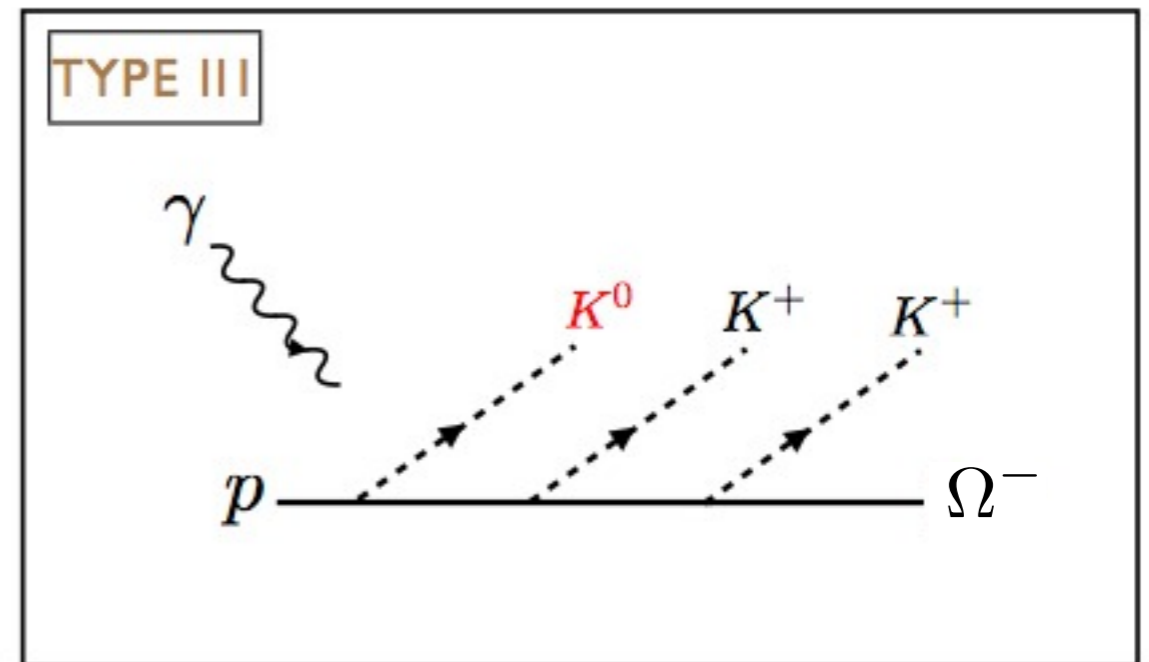
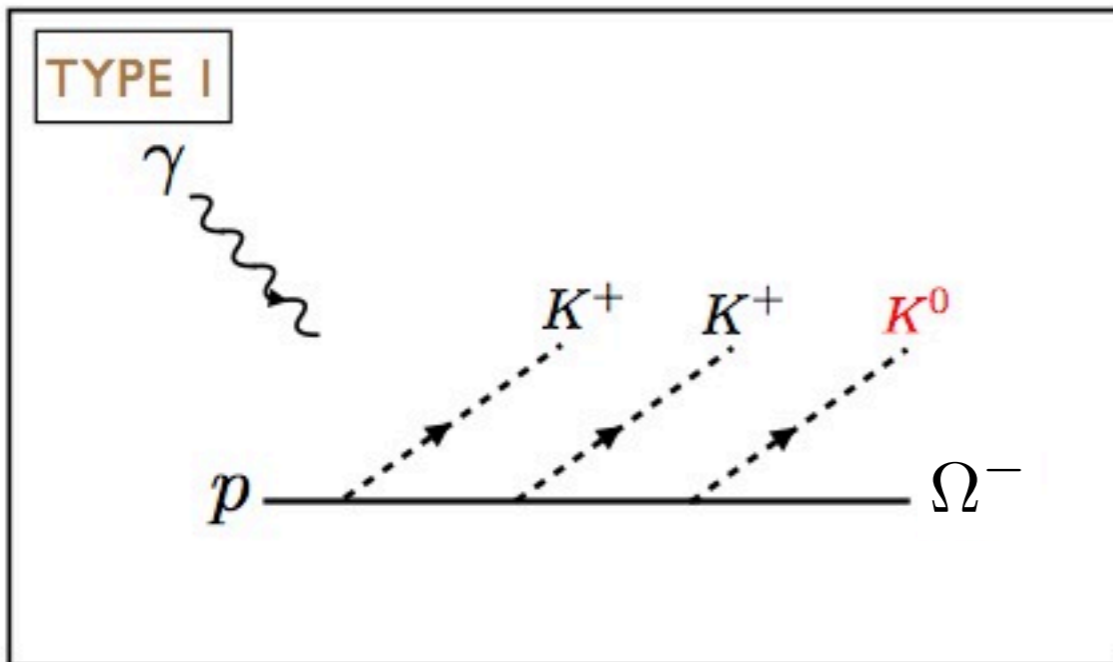
(Dated: May 4, 2012)



Diagrams



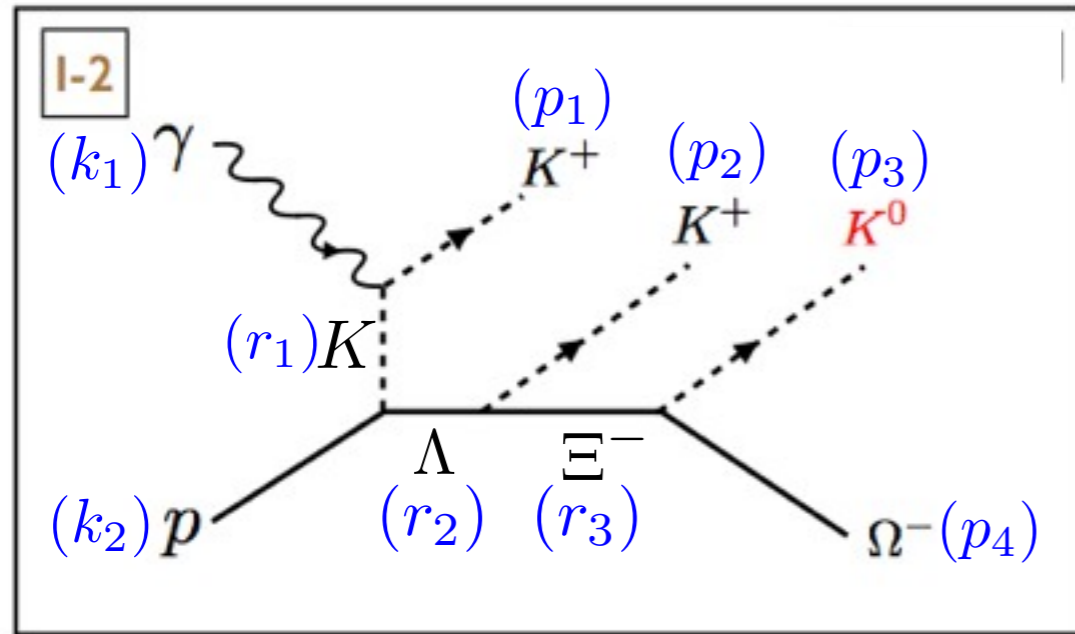
Diagrams



$$8 \times 3 = 24$$



one example : the 2nd diagram of type I set



$$\mathcal{L}_{\gamma NN} = -e\bar{N}\left[\gamma_\mu - \frac{\kappa_N}{2M_N}\sigma_{\mu\nu}\partial^\nu\right]A^\mu N$$

$$\mathcal{L}_{\gamma KK} = -ie[(\partial K^+)K^- - \partial(K^-)K^+]$$

$$\mathcal{L}_{K N \Lambda} = g_{K^+ N \Lambda}\bar{\Lambda}\gamma^\mu\gamma_5\partial_\mu K^- N$$

$$\mathcal{L}_{K \Lambda \Xi^-} = g_{K^+ \Lambda \Xi^-}\bar{\Xi}^-\gamma^\mu\gamma_5\partial_\mu\bar{K}^-\Lambda$$

$$\mathcal{L}_{K^0 \Xi^- \Omega^-} = g_{K^0 \Xi^- \Omega^-}\bar{\Omega}^-\gamma^\mu\gamma_5\partial_\mu\bar{K}^0\Xi^-$$

$$T_{I-2} = ieg_{KN\Lambda}g_{K\Lambda\Xi}g_{K\Xi\Omega}\bar{u}^\mu(p_4)p_{3\mu}\frac{\not{p}_3 - M_{\Xi^-}}{r_3^2 - M_{\Xi^-}^2}\not{p}_2\frac{\not{p}_2 + M_\Lambda}{r_2^2 - M_\Lambda^2}\not{p}_1\gamma_5 u(k_2)\frac{2p_1 \cdot \epsilon_\gamma}{r_1^2 - m_K^2} \times F_c$$

$$F_c = 1 - (1 - F_1)(1 - F_2)(1 - F_3)(1 - F_4)$$

$$F_2(r_1^2, r_2^2, r_3^2) = F_M(r_1^2)F_B(r_2^2)F_B(r_3^2)$$

$$F_M(r^2) = \frac{\Lambda_M^2 - m^2}{\Lambda_M^2 - r^2}$$

$$F_B(r^2) = \left[\frac{n\Lambda_B^4}{n\Lambda_B^2 + (r^2 - M^2)^2} \right]^n$$

$$T = T_1^{\text{inv}}F_1 + (T_1^{\text{viol}} + T_2 + T_3)F_c + T_4F_4 + \dots$$



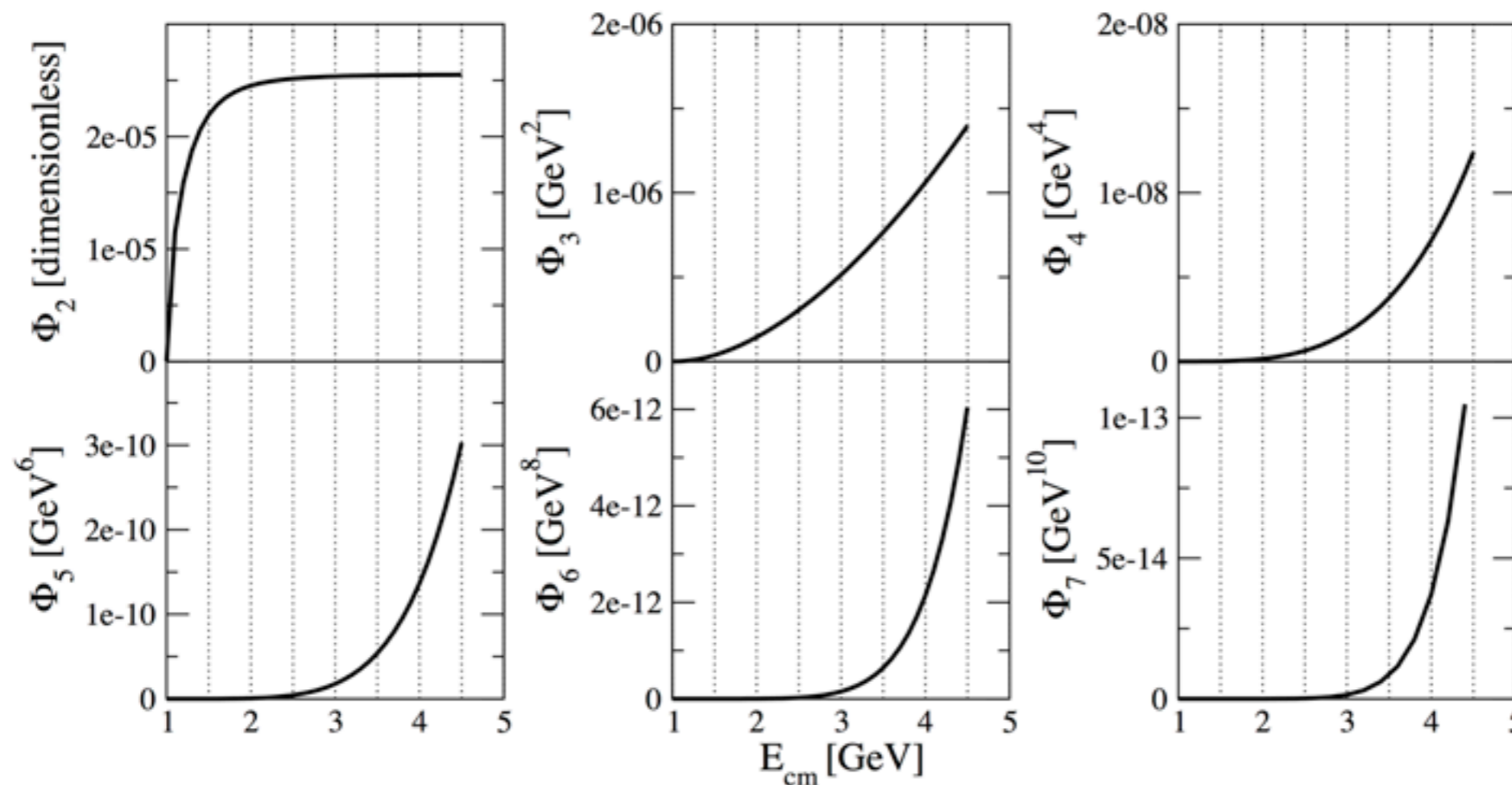
Some comments on the numerical calculation

$$\Phi_n(P; p_1, \dots, p_n) = \int_1 \dots \int_n \delta^4(P - \sum_i p_i) \prod_{i=1}^n \frac{d^3 p_i}{(2\pi)^3 2E_i}$$

of integration = $3n - 5$

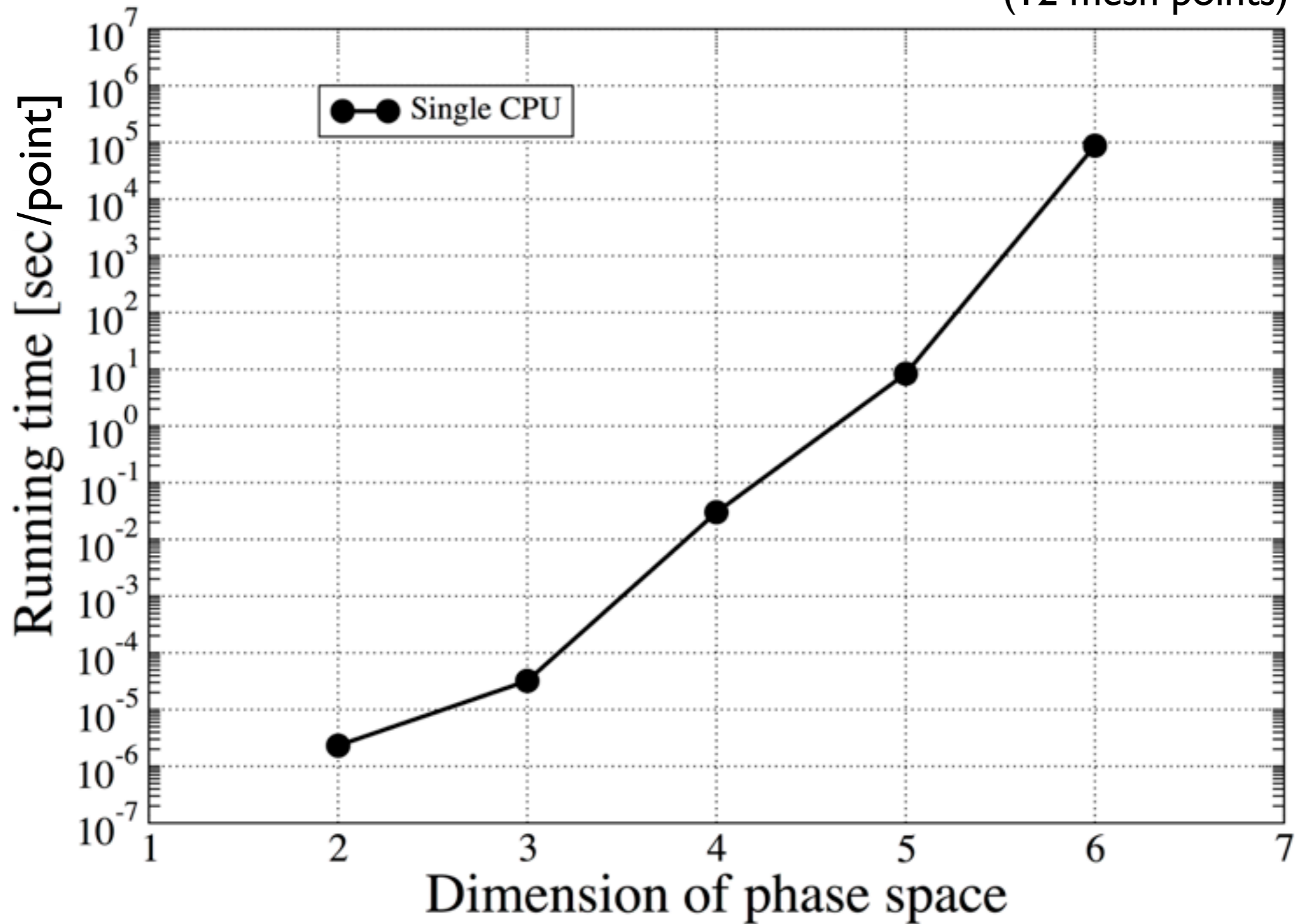
($m_1 = m_2 = \dots = m_n = 1\text{GeV}/n$)

n body Phase Space



Running time of one point calculation (E_{cm}, Φ_n)

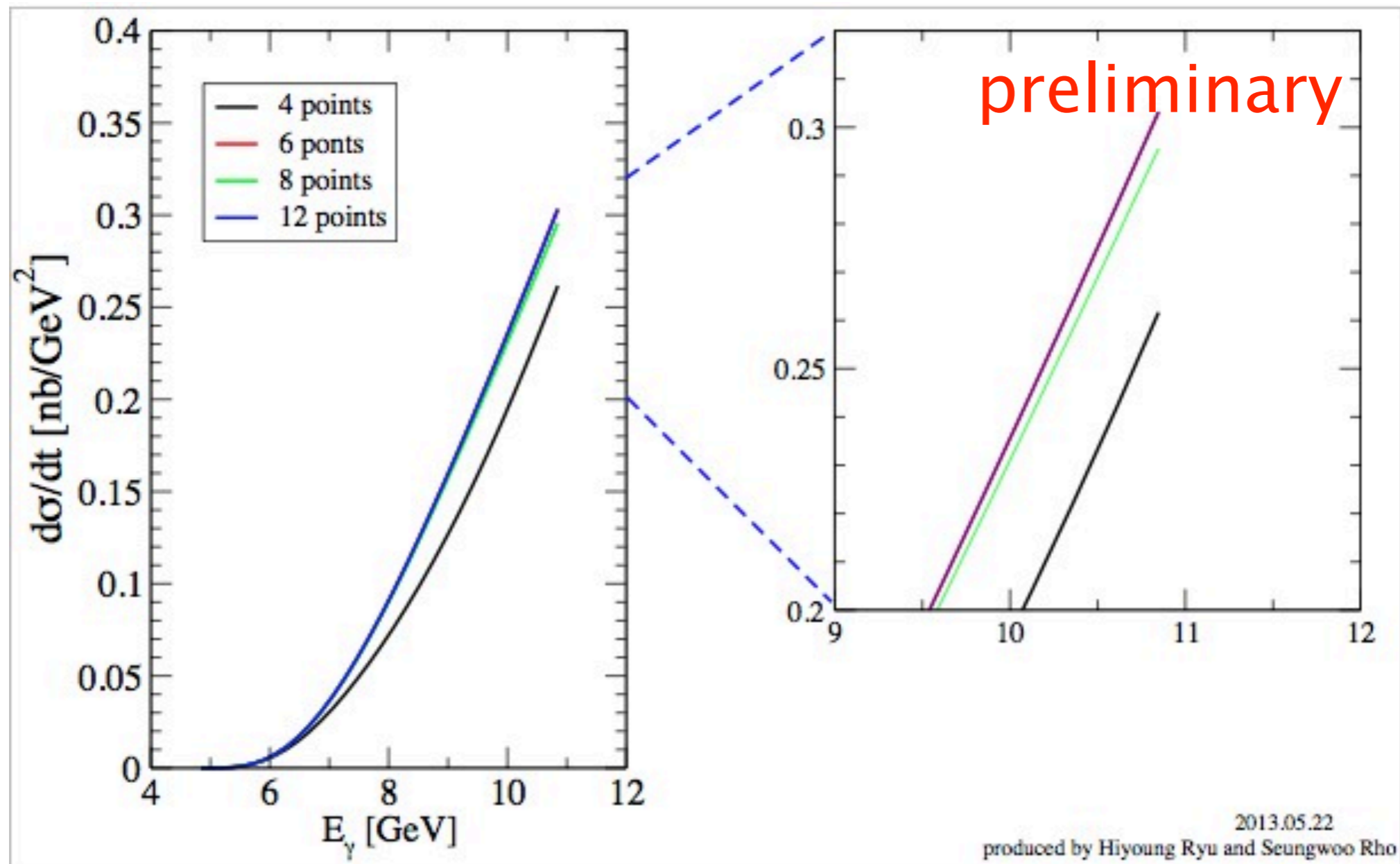
(12 mesh points)



Integration convergency check

STEP I : 4 mesh points calculation (single machine & HTCaaS with PLSI)

STEP II : convergency check for 6, 8 and 12 mesh points



Summary of part II

■ **What's new ?**

- There is no published paper for the Omega- photoproduction.
- We would like to suggest the minimum of the cross section.
- 4 body phase space calculation with the supercomputing power.

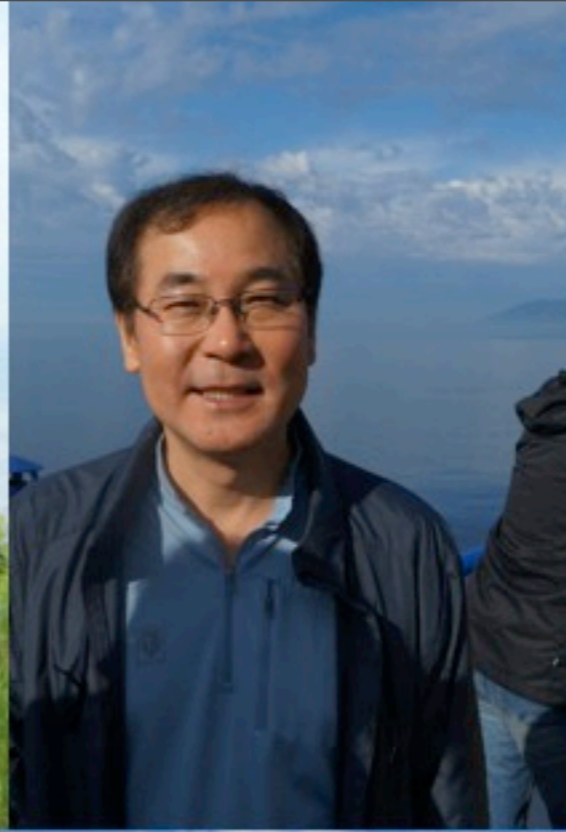
■ **What's questions ?**

- We are considering about which parameter we will use .
(coupling constant/ cut-off in the form factor)
- Are there other important diagrams ?

■ **What's next ?**

- The differential cross section as a function of the invariant mass.
- ...





Thank you very much ~

