

Neutron Star Equations of State and Gravitational Waves

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Astro-Hadron Group in Pusan Nat'l Univ

- Problems related to NS
 - dense matter physics/ NS equation of states
 - formation and evolution of NS
 - GW from NS binaries

- LSC(LIGO Scientific Collaboration) members
 - Dr. Hee-Suk Cho
 - Y.M. Kim (NIMS)
 - M.G. Kim (1st year in Ph.D., pre-LSC member)

- Non-LSC members (2 students)
 - working on hadron physics (dense matter physics)
 - dense matter physics / NS equation of states

From NS Equation of States

- NS Equation of States

- ✓ dense matter physics

- ✓ kaon condensation

- ✓ new approaches in hQCD

- Gravitational Waves

- ✓ sources : neutron star binaries

- ✓ GW waveform generation

- ✓ GW data analysis

Today

To Gravitational Waves

Contents

- Motivations
- Open problems in NS mass observations
- Possibilities of `NS + high-mass NS/BH` binaries
- A new approach to NS Equation of state in hQCD

Gravitation Wave from Binary Neutron Star

B1913+16

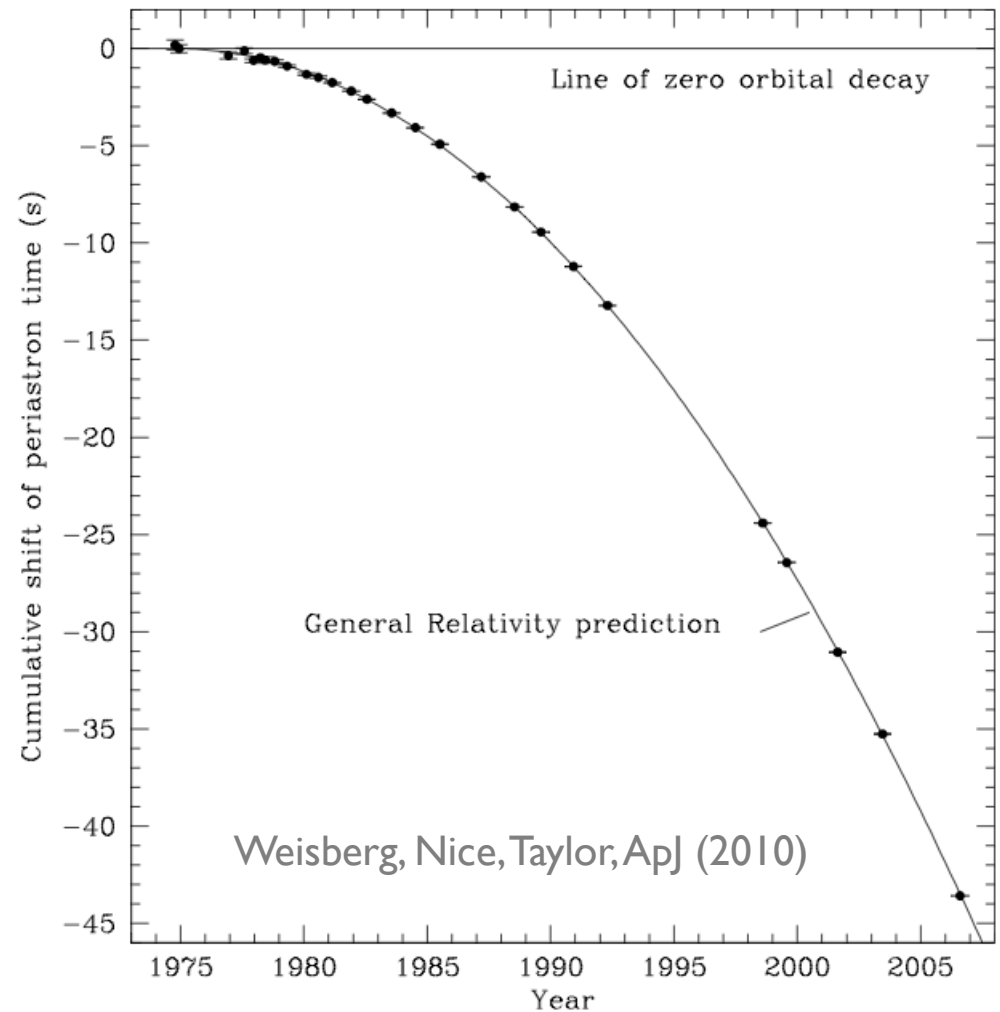
Hulse & Taylor (1975)



Effect of Gravitational
Wave Radiation

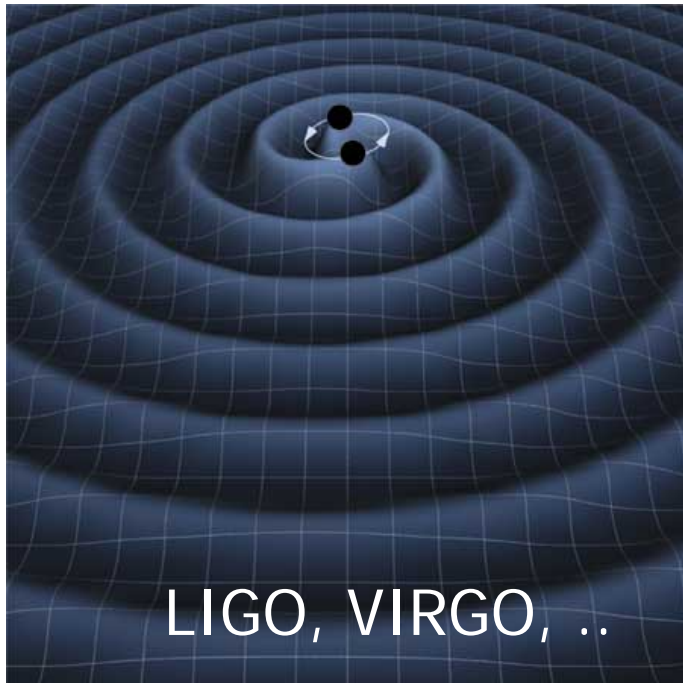
1993 Nobel Prize
Hulse & Taylor

Gravitational Wave
Observatory



Neutron Stars

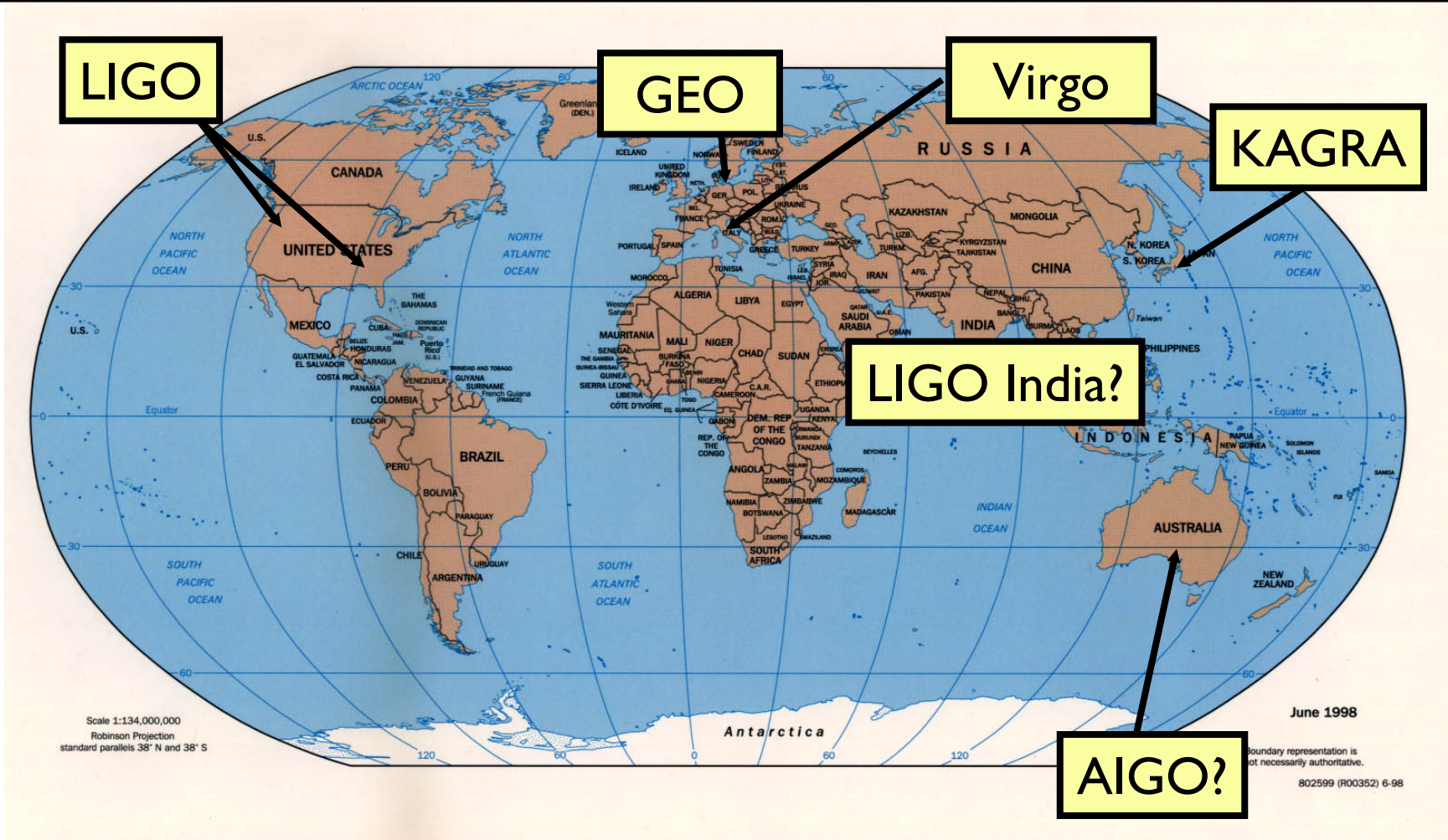
Cosmological Heavy Ion Collisions



Gravitational waves from
NS-NS and NS-BH Binaries



Network of Gravitational Wave Interferometers





Korean Gravitational-Wave Group



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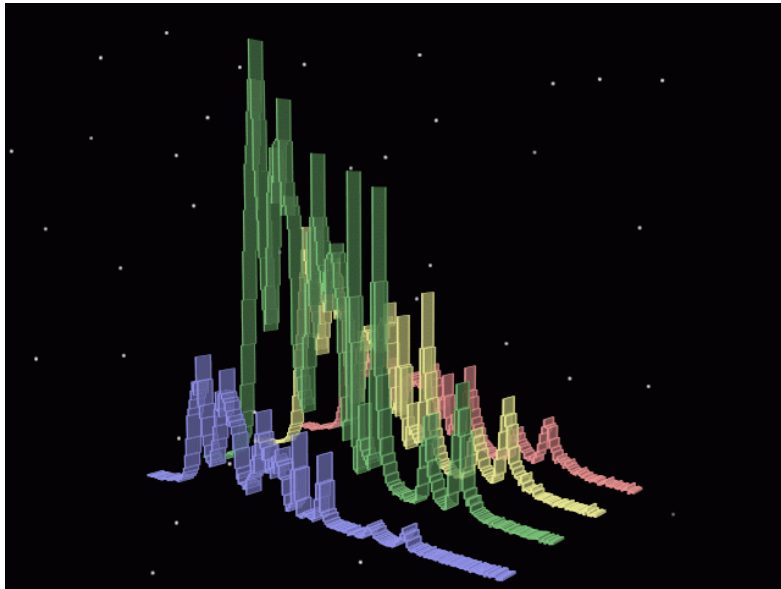
Worldwide Mega-Science Projects

Gravitational-wave detection is a global project of seeking a new window to the Universe. This will open an era of gravitational wave astronomy.



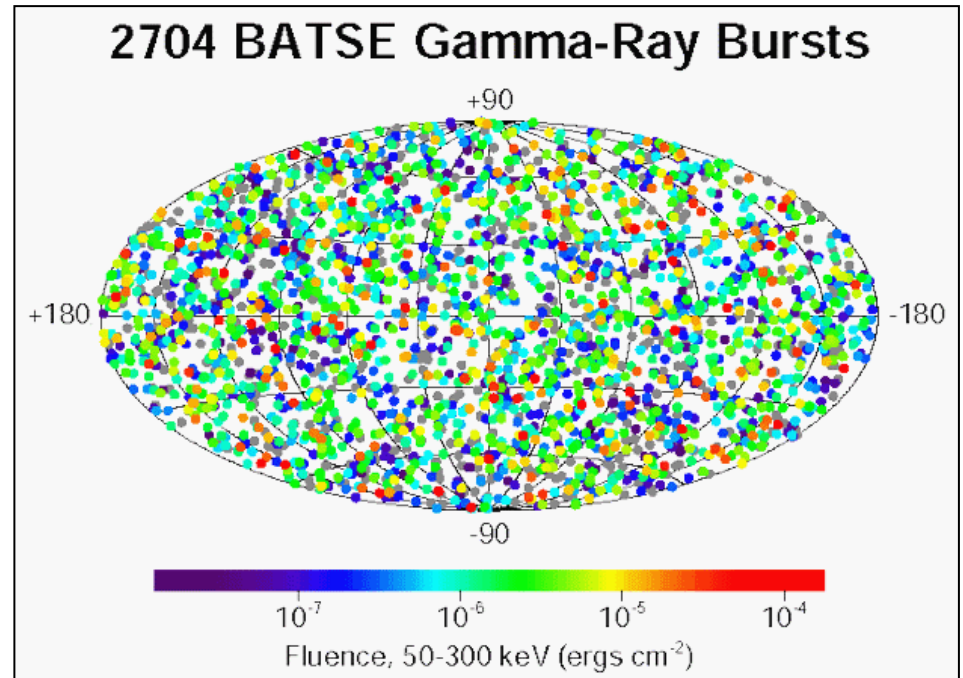
GRBs from NS Binaries

Origin of gamma-ray bursts (GRBs)



T_{90} = milli sec – min

Brightest event in
the Universe

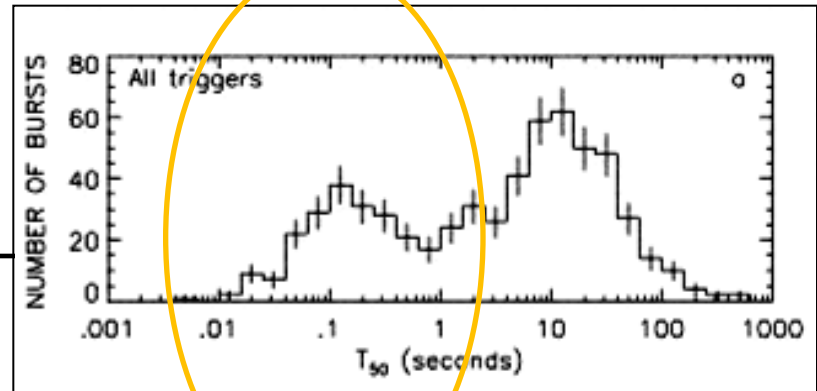


1970s : Vela Satellite

1990s: CGRO, Beppo-SAX

2000s: HETE-II, Swift

Two groups of GRBs



- Long-duration Gamma-ray Bursts:

⇒ HMBH Binaries

- Short Hard Gamma-ray Bursts:

Duration time < 2 sec

⇒ NS-NS, NS-BH Binaries

seen NS-NS binaries which will coalesce within Hubble time

PSR	P (ms)	P_b (hr)	e	Total Mass M_\odot	τ_c (Myr)	τ_{GW} (Myr)
J0737–3039A	22.70	2.45	0.088	2.58	210	87
J0737–3039B	2773	2.45	0.088	2.58	50	87
B1534+12	37.90	10.10	0.274	2.75	248	2690
J1756–2251	28.46	7.67	0.181	2.57	444	1690
B1913+16	59.03	7.75	0.617	2.83	108	310
B2127+11C	30.53	8.04	0.681	2.71	969	220
J1141–6545 [†]	393.90	4.74	0.172	2.30	1.4	590

Globular Cluster : no binary evolution

White Dwarf companion

Can we see BH-NS binaries as pulsars if they exist ?

Pulsar life time : $1/B$

Fresh pulsar : $B \sim 10^{12}$ G

Recycled pulsar : $B \sim 10^8$ G



$\sim 10^4$ times longer
lifetime
+ beaming effect

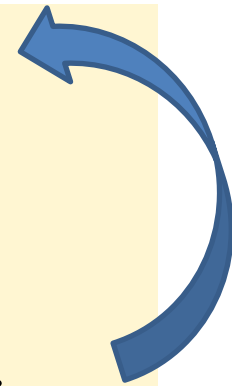
- NS(recycled)-NS(fresh)

- first-born NS is recycled by accretion

- NS(recycled) : longer pulsar life time

- BH-NS(fresh)

- one can see only NS(fresh) : short life time



$\sim 10^4$
bigger
chance

GW sources with NS

- NS-NS – already seen
 - NS-BH – no evidence yet
 - contribution to GW is still unknown
- Q) what is the boundary between NS & BH ?
- maximum mass of neutron stars

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1.97 Msun NS discovered in a NS-White Dwarf Binary

October 27, 2010

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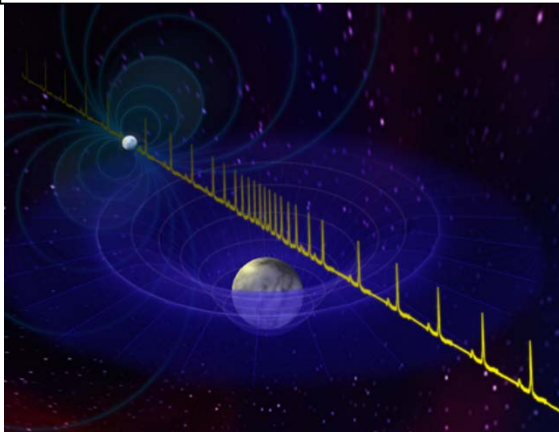
LETTER

doi:10.1038/nature09466

A two-solar-mass neutron star measured using Shapiro delay

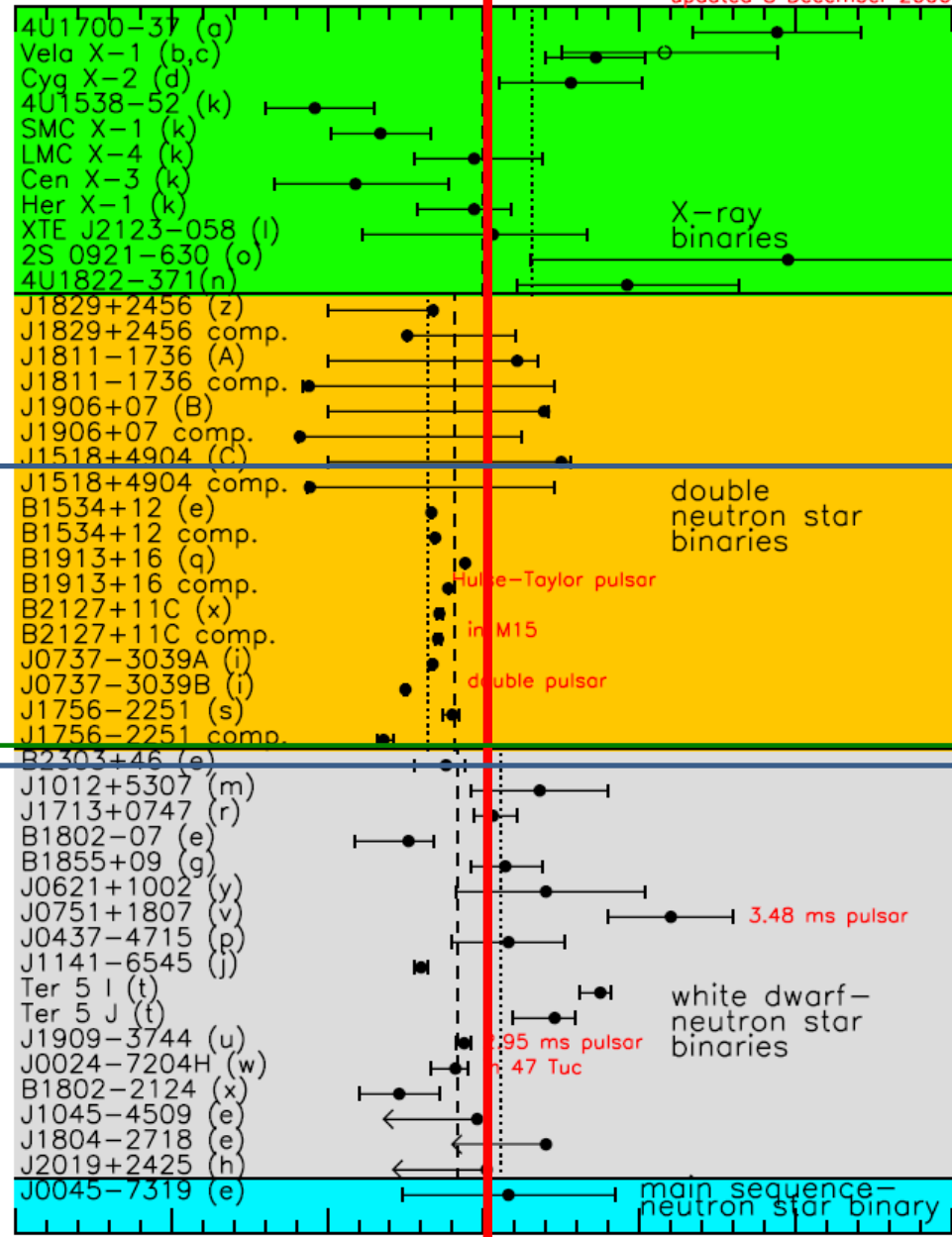
P. B. Demorest¹, T. Pennucci², S. M. Ransom¹, M. S. E. Roberts³ & J. W. T. Hessels^{4,5}

Astronomers Discover Most Massive Neutron Star Yet Known



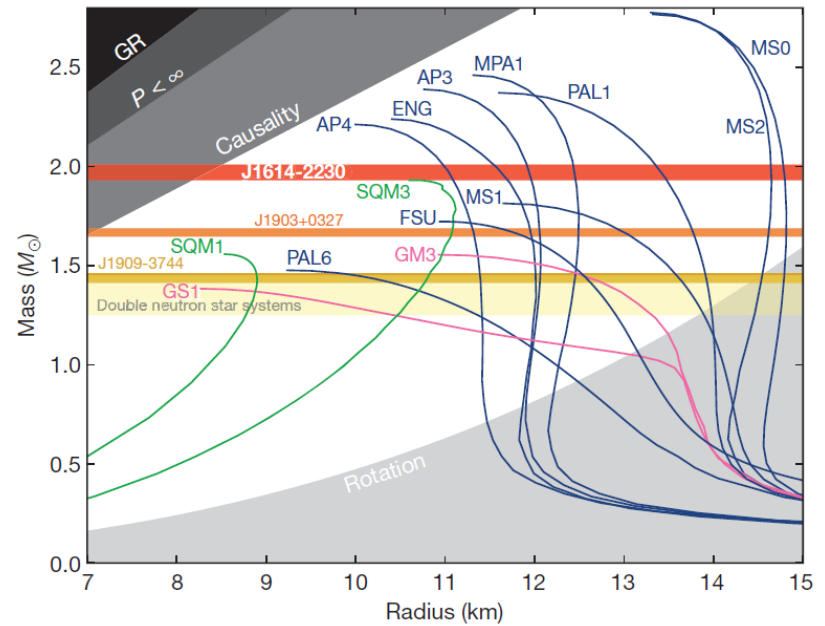
<http://www.nrao.edu/pr/2010/bigns/>

All well measured NS masses in NS-NS binaries are $< 1.5 M_{\odot}$



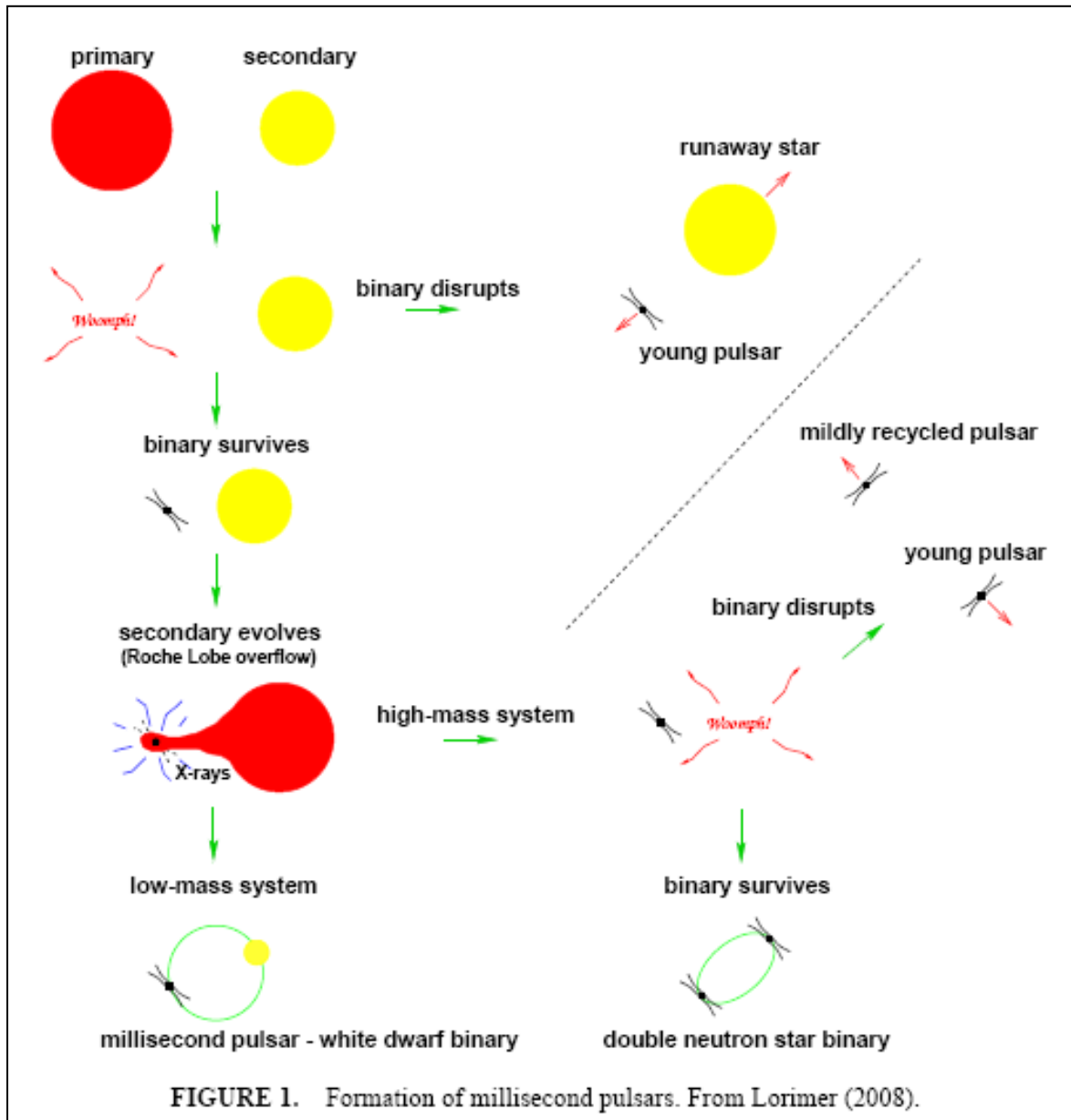
Lattimer & Prakash (2007)

Wanted



Nature 467, 1081

- 1.97 Msun NS was observed in a NS-WD binary
- Why all well-measured NS masses in NS-NS binaries are less than 1.5 Msun?
- NS mass may/should depend on the evolution process.



Accretion process
is essential in
understanding
NS binaries

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Eddington Luminosity & Eddington Limit

$$L_{\text{Edd}} = \frac{4\pi cGM}{\kappa} \approx 1.3 \times 10^{38} \frac{M}{M_{\odot}} \text{erg s}^{-1}$$

$$\kappa = \sigma_T N_A$$

Thomson scattering cross section σ_T

Avogadro's number N_A

$$L_{\text{Edd}} = \eta \dot{M}_{\text{Edd}} c^2$$

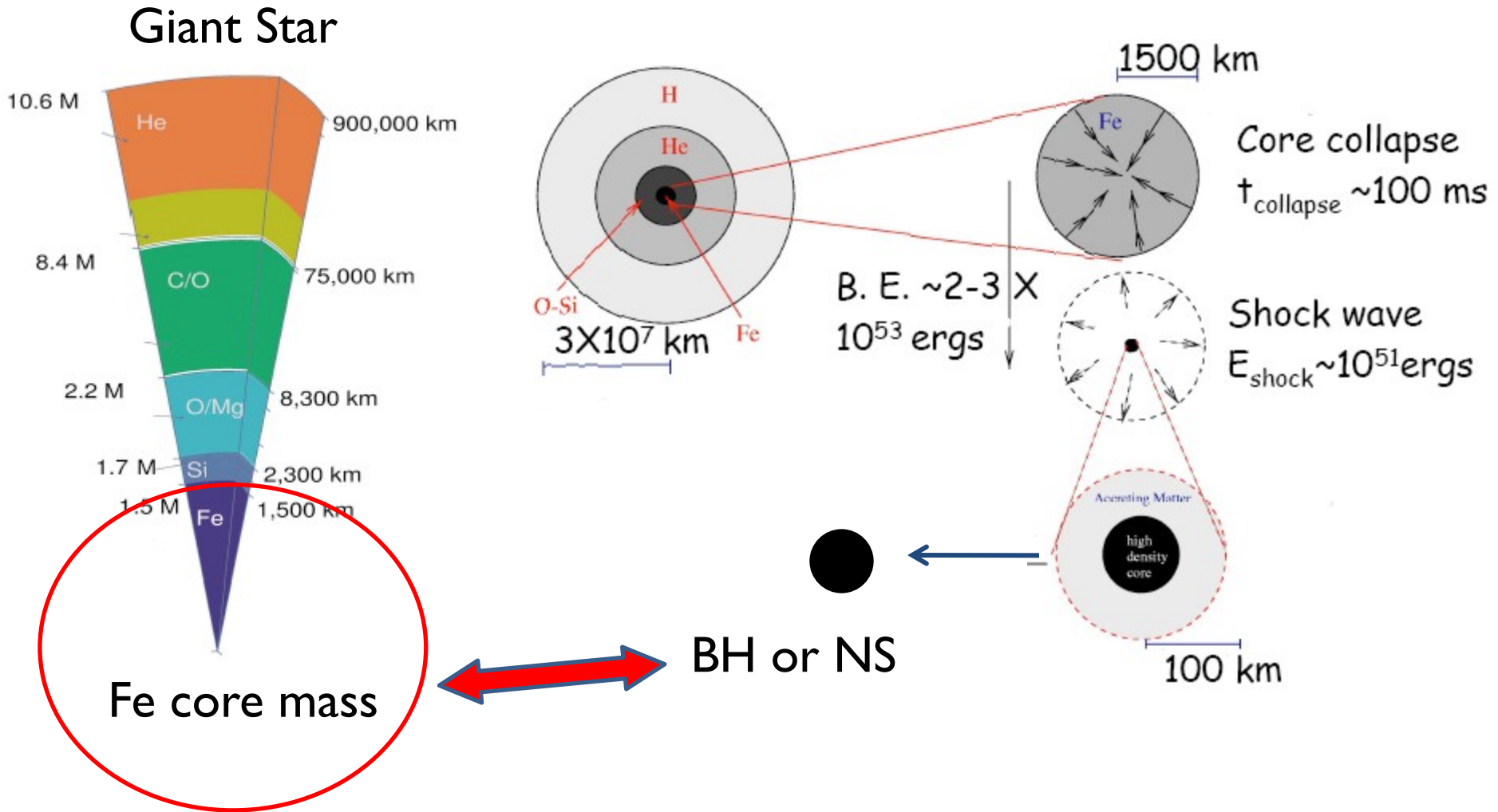
$$\dot{M}_{\text{Edd}} = \frac{4\pi GM}{\kappa c \eta} \approx \frac{1}{\eta} 0.45 \times 10^{-8} \left(\frac{M}{M_{\odot}} \right) M_{\odot} \text{yr}^{-1}$$

Supercritical Accretion onto first-born NS

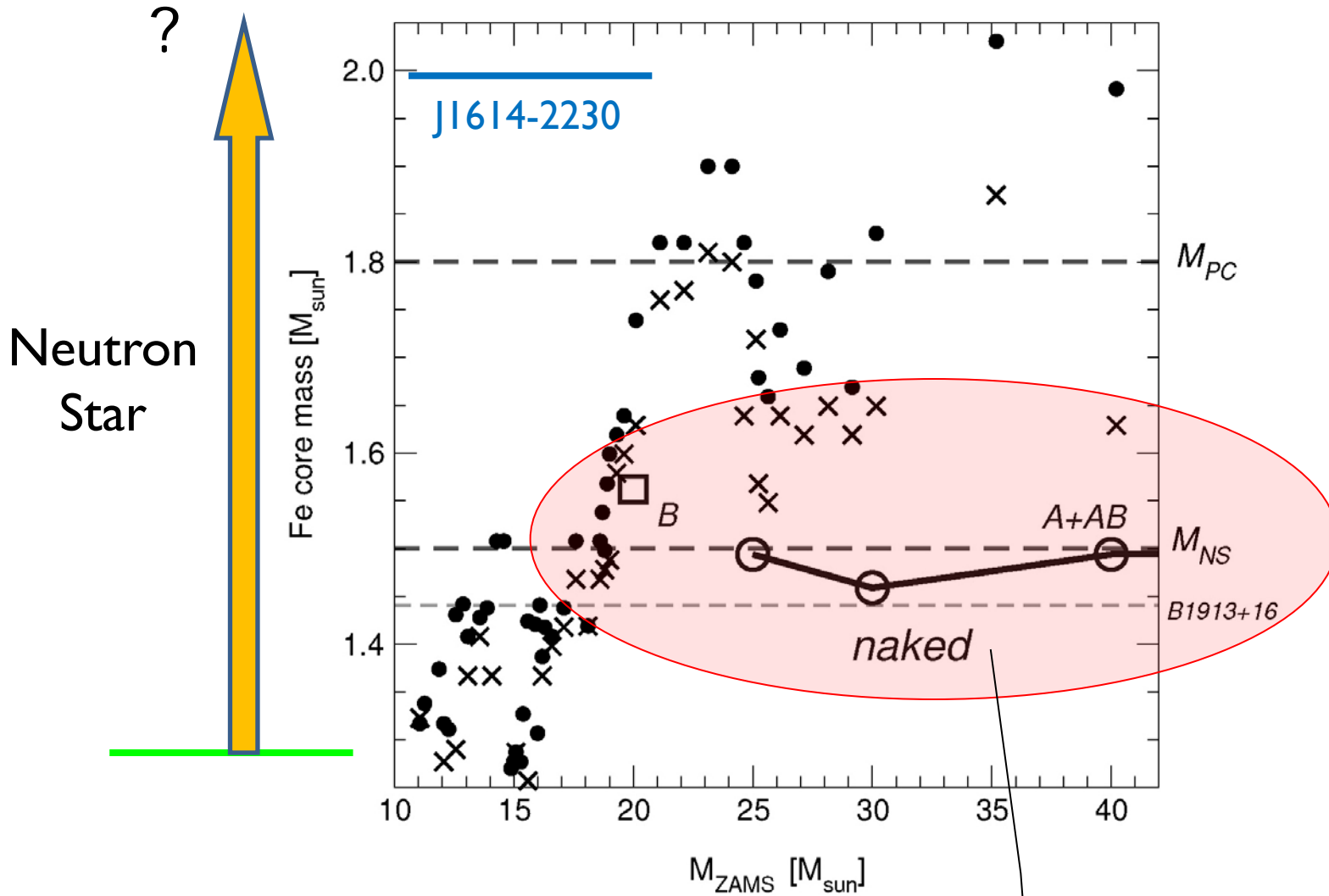
- Eddington Accretion Rate : photon pressure balances the gravitation attraction
- If this limit holds, neutron star cannot be formed from the beginning (e.g. SNI987A; 10^8 Eddington Limit).
- Neutrinos can take the pressure out of the system allowing the supercritical accretion when accretion rate is bigger than 10^4 Eddington limit !
($T > 1$ MeV :Thermal neutrinos dominates !)

Q) What is the implications of supercritical accretion ?

One has to understand formation of BH/NS



Fe core mass before collapse (Brown et al. New Aston. 6,457)



□ & ○ : evolution without H envelope

Fresh NS mass from Fe core collapse

In close binaries (evolution without H envelope)

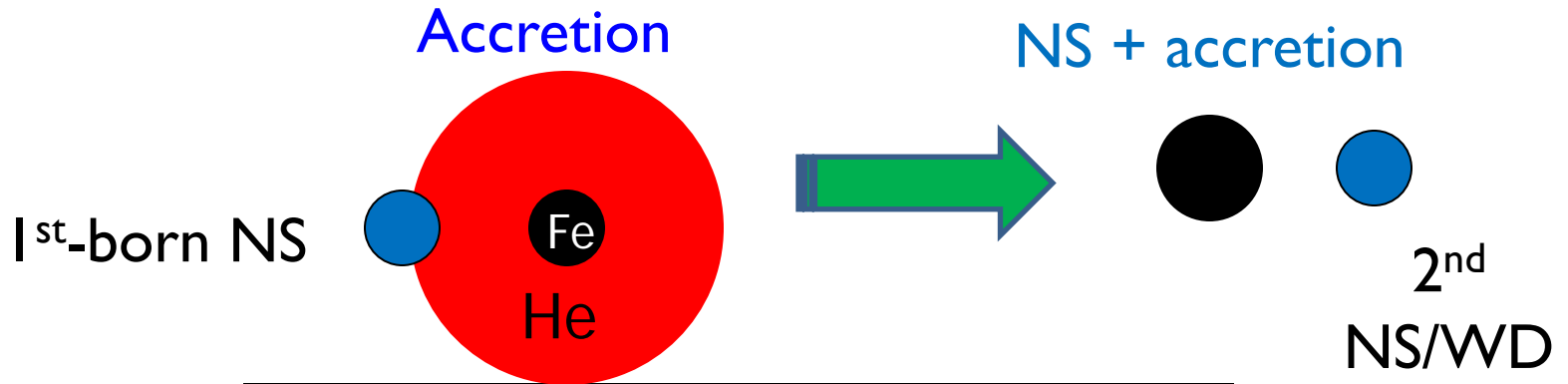
low Fe core mass  NS mass = 1.3 - 1.5 Msun

This value is independent of NS equation of state.

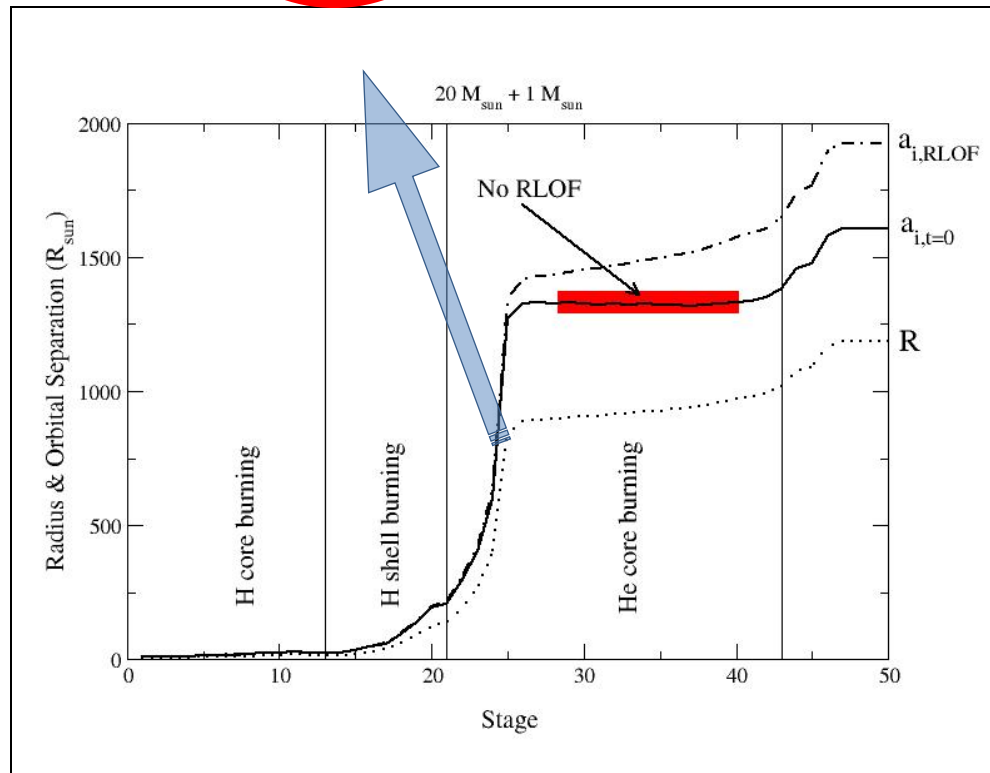
Q) What is the fate of primary (first-born) NS in binaries ?

Note: Accurate mass estimates of NS come from binaries

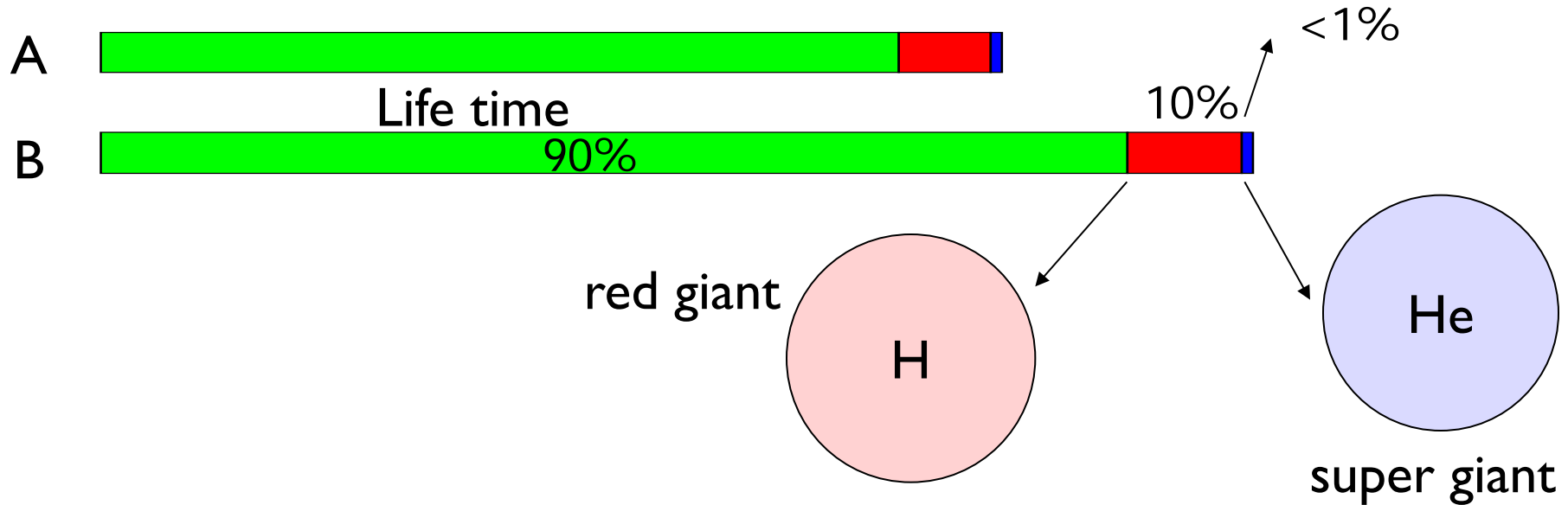
Final fate of first-born NS



Evolution of Companion



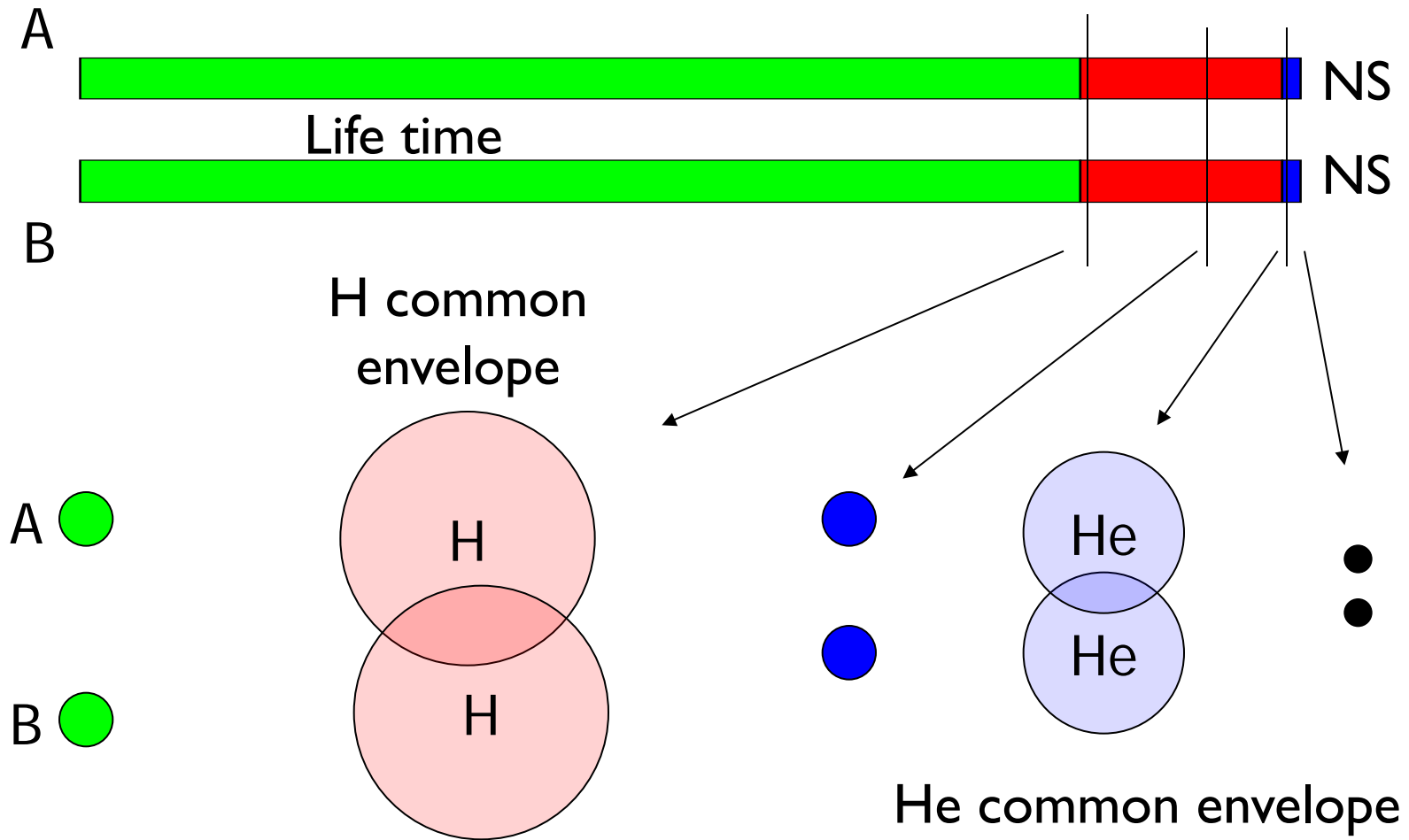
Evolution of binary stars



Original ZAMS(Zero Age Main Sequence) Stars

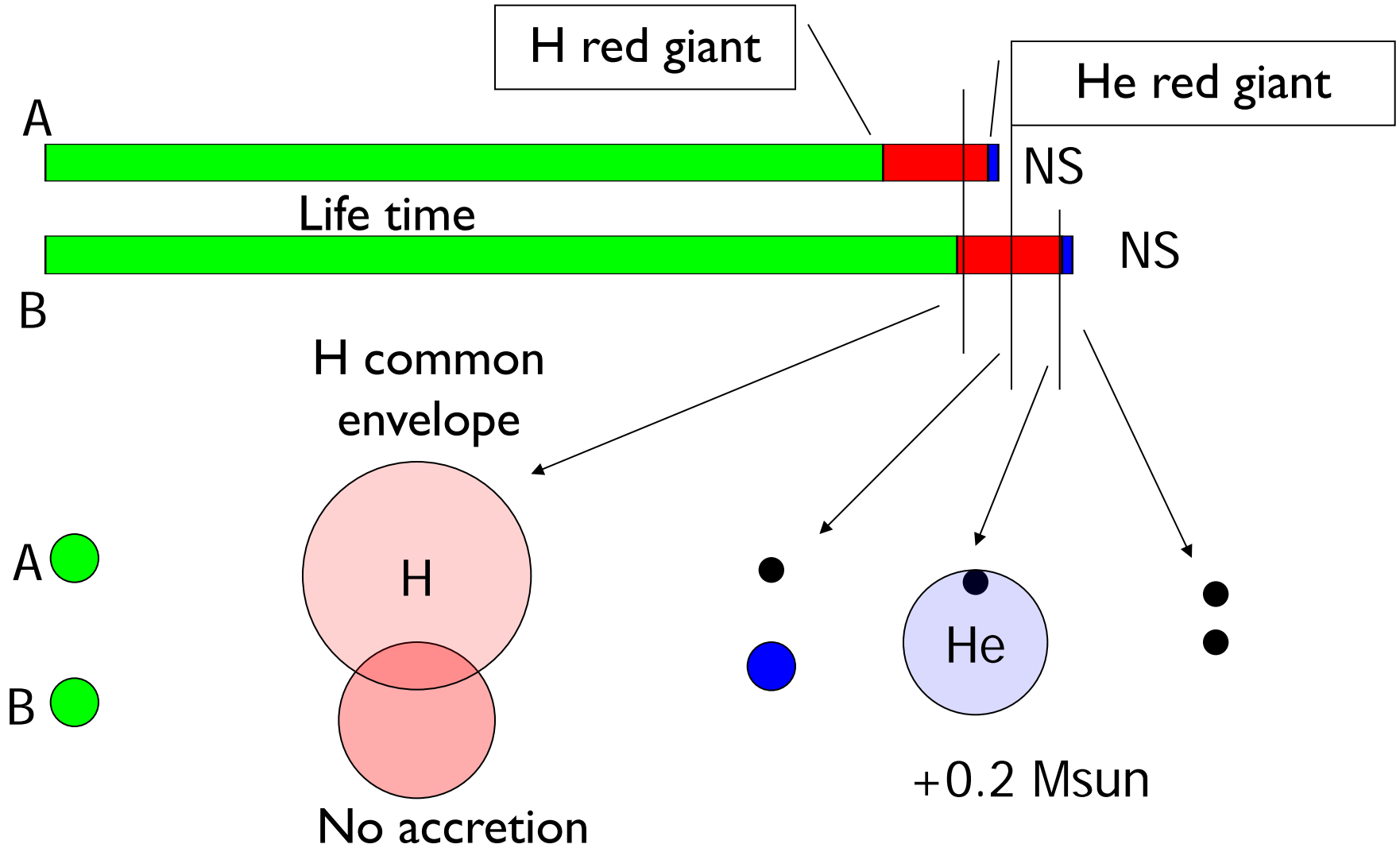
- Probability = $1/M^{2.5}$
- Life Time = $1/M^{2.5}$
- $\Delta M=4\%$,
 $\Delta T_{\text{life}}=(1 - 1/1.04^{2.5})= 10\%$,
 $\Delta P=10\%$ (population probability)

Case 1 : $\Delta T < 1\%$



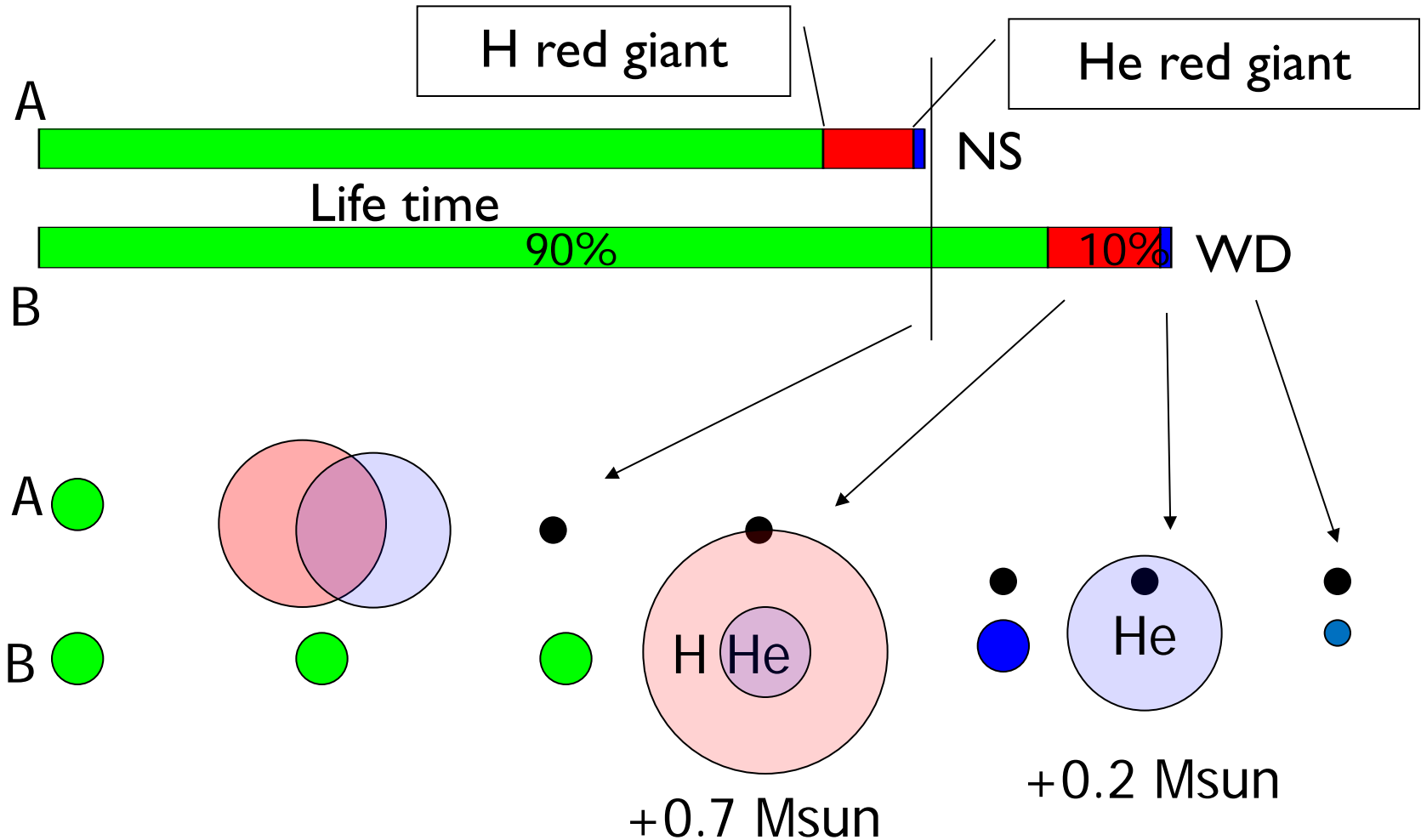
No accretion : nearly equal mass NS-NS binary!

Case 2 : $1\% < \Delta T < 10\%$



First born NS should accrete only $< 0.2 M_{\odot}$!

Case 3 : $\Delta T > 10\%$




Supercritical Accretion:
First born NS can accrete up to $0.9 M_{\odot}$!

How mass & orbit change during the evolution?

A few efficiencies (not calculable from first principles)

$$\dot{E}_{\text{acc}} = \frac{1}{2} c_d \frac{G(M_{\text{NS}} + M_{\text{giant}})}{a} \dot{M}_{\text{NS}}$$

$$-\dot{E}_{\text{orb}} = \frac{1}{2} \frac{GM_{\text{giant}}}{a} \dot{M}_{\text{NS}} + \frac{1}{2} \frac{GM_{\text{NS}}}{a} \dot{M}_{\text{giant}} - \frac{1}{2} \frac{GM_{\text{NS}}M_{\text{giant}}}{a^2} \dot{a}$$

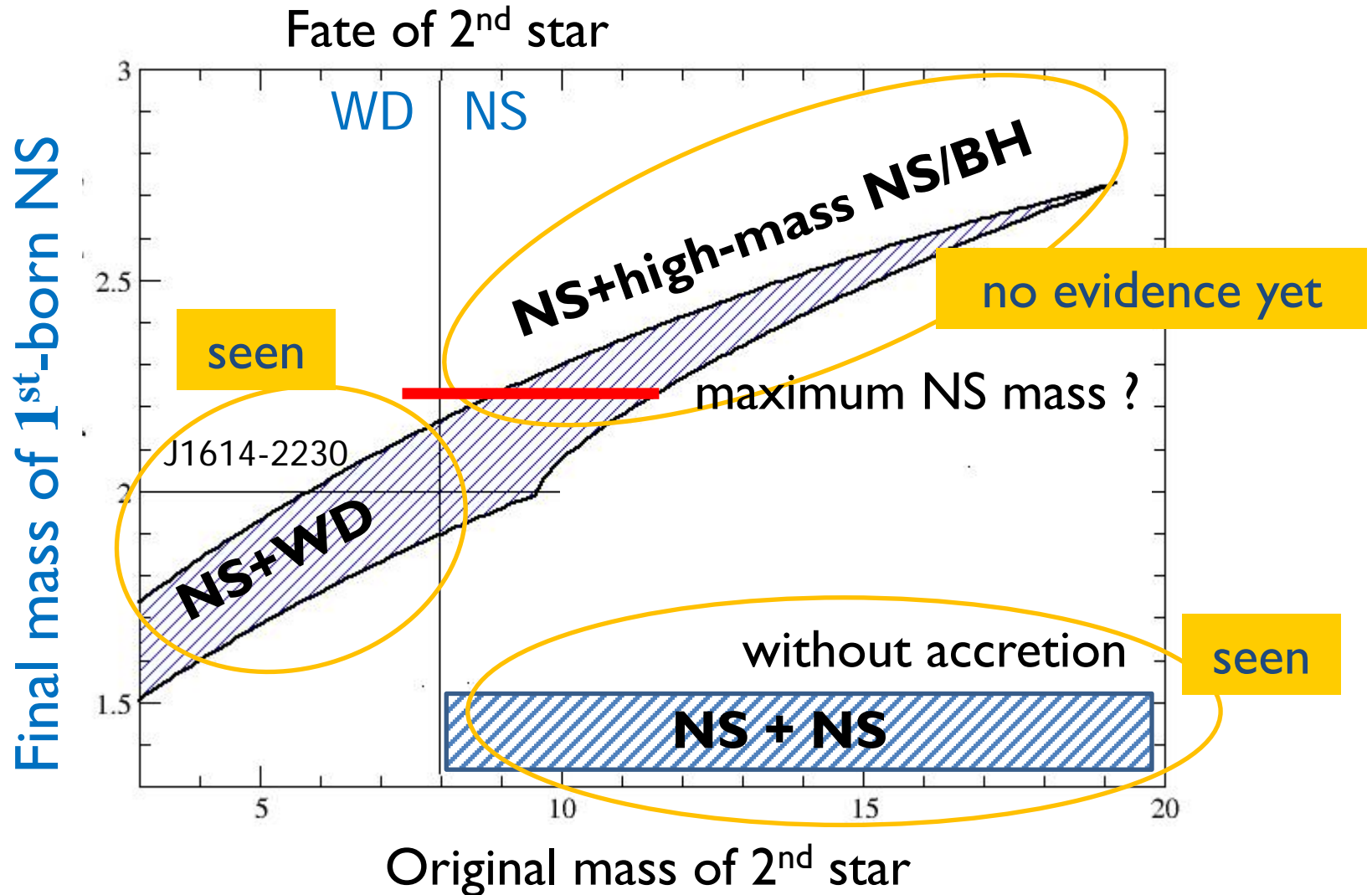

$$\dot{E}_{\text{acc}} = -\dot{E}_{\text{orb}}$$

$$\alpha_{\text{ce}} \frac{dE_{\text{orb}}}{dM_{\text{giant}}} = -\frac{dE_{\text{bind}}}{dM_c}$$

$c_d = 6$, $\alpha_{\text{ce}} \lambda = 0.2$
are consistent with
SXT (Soft X-ray Transient)
[Lee, Brown, Wijers, ApJ \(2002\)](#)

$$E_{\text{bind}} = \frac{1}{\lambda} \frac{GM_{\text{giant}}(M_{\text{giant}} - M_{\text{giant,core}})}{a}$$

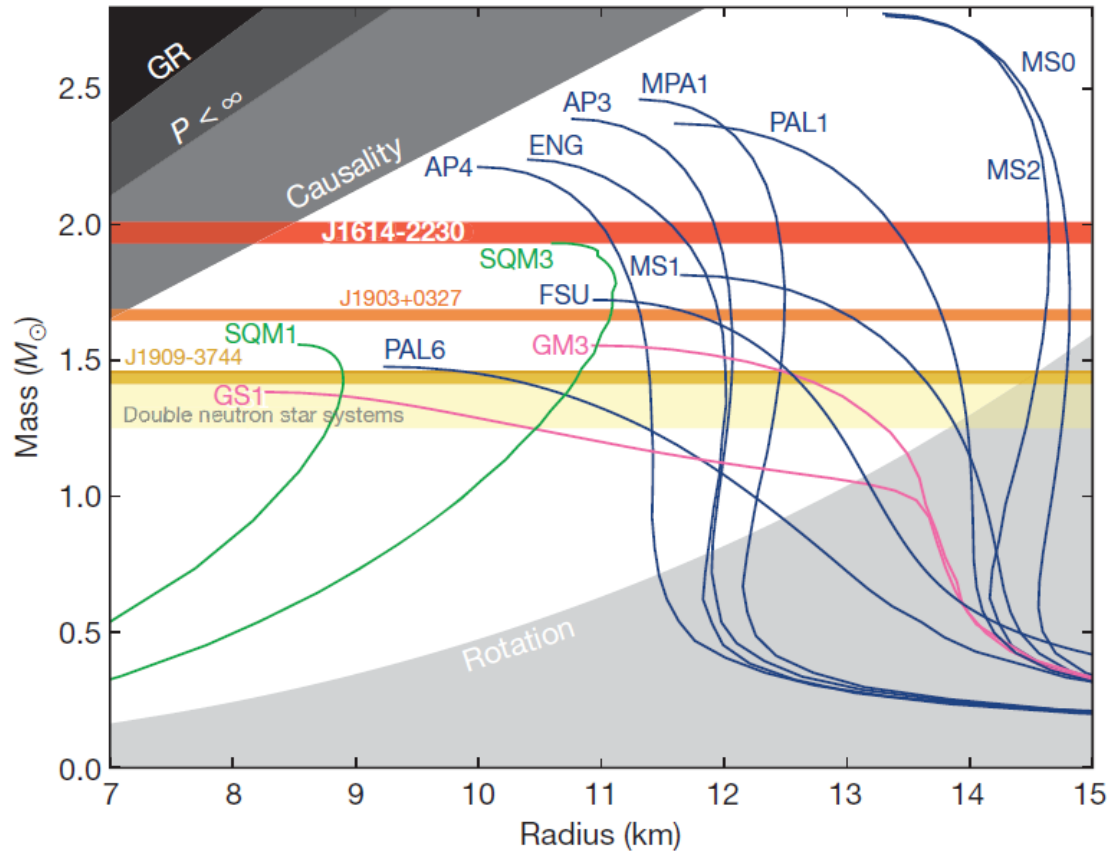
Final mass of first-born NS with supercritical accretion



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Which one is right EOS ?



refer talks by
M.G. Cheon (Tue) & H.K. Lee (Thu)

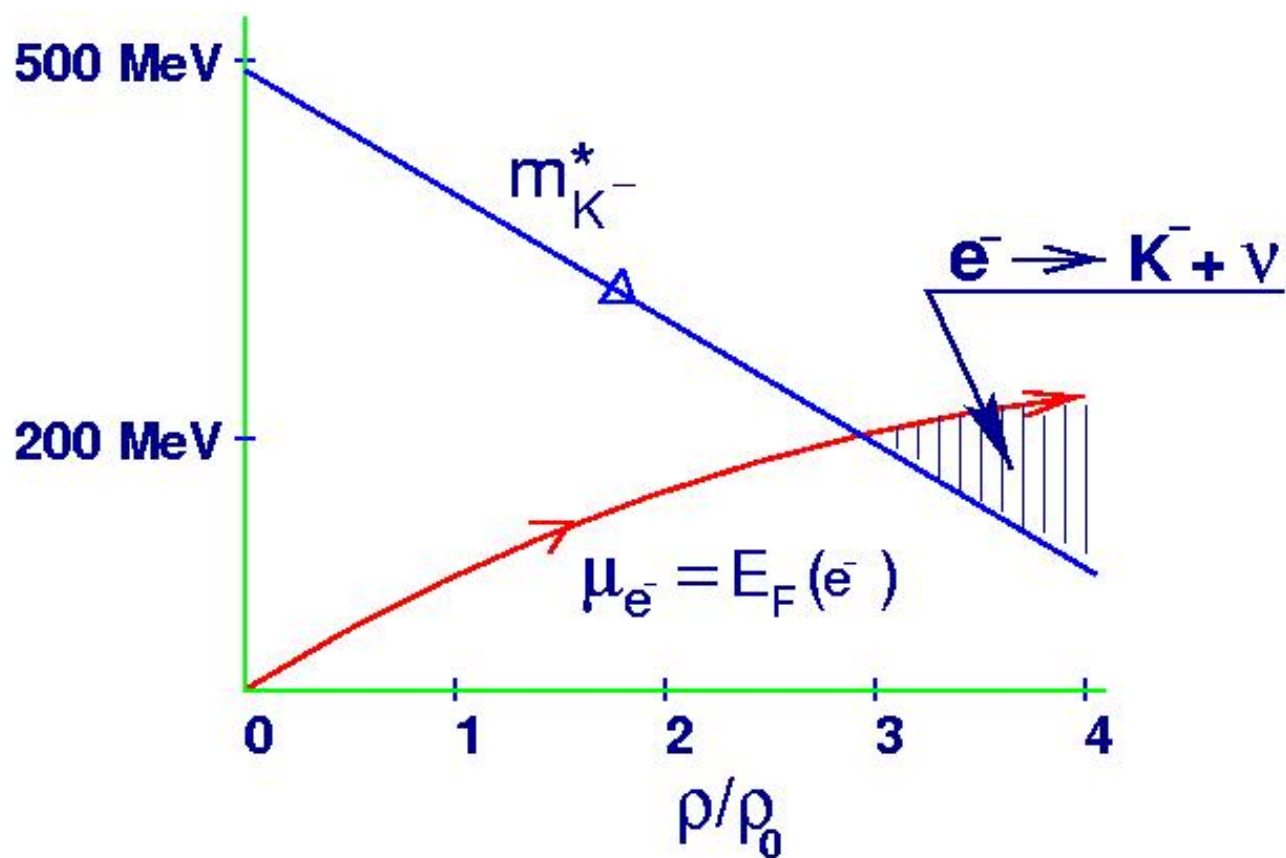
Nature 467, 1081

Why strange quarks in neutron stars ?

- ✓ proton, neutron: u, d quarks
- ✓ By introducing strange quark
 - we have one more degrees of freedom
 - energy of the system can be reduced!
- ✓ In what form ?
kaon, hyperons

Kaon is the lightest particle with strange quark !

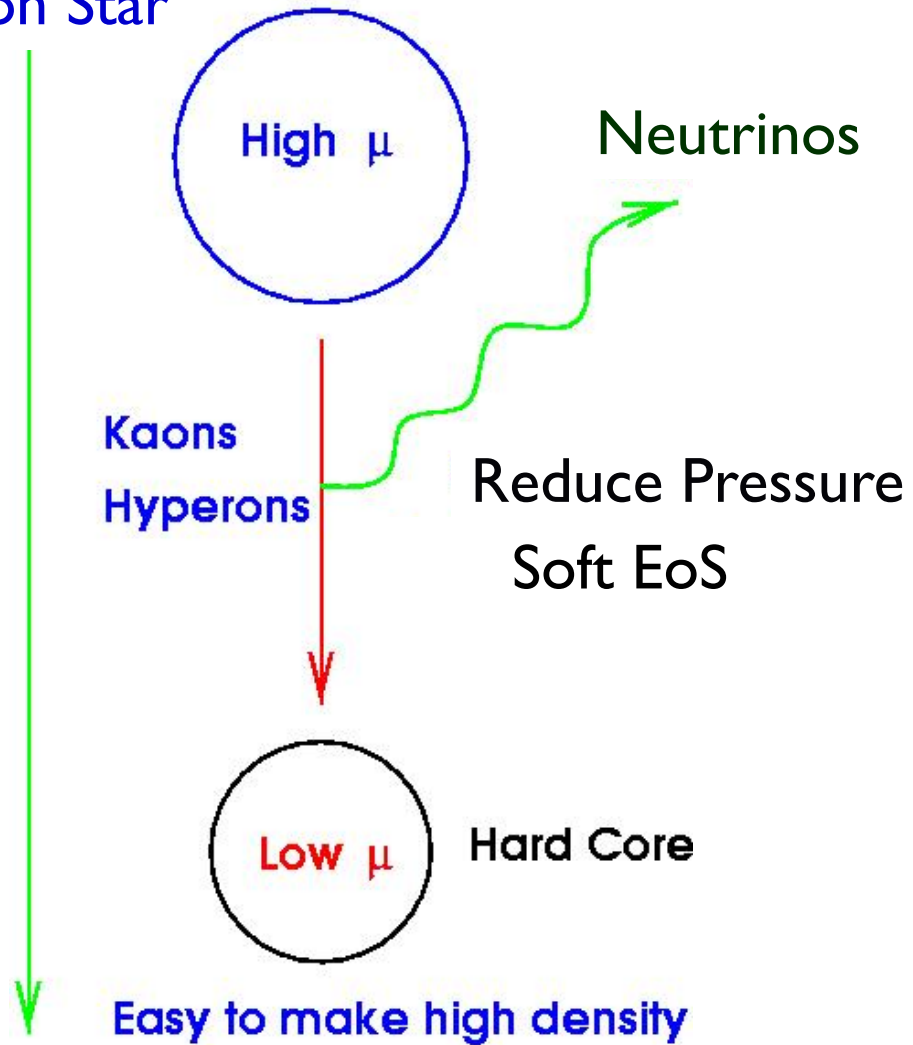
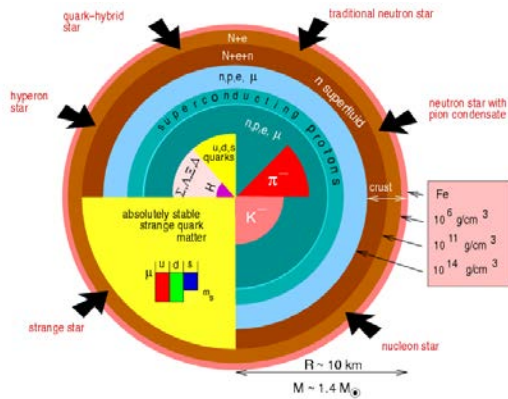
Kaon Condensation in Dense Matter



$\rho_0 =$ nuclear matter density

Astrophysical Implications

Neutron Star



Formation of low mass Black Hole

Two different approaches for kaon condensation

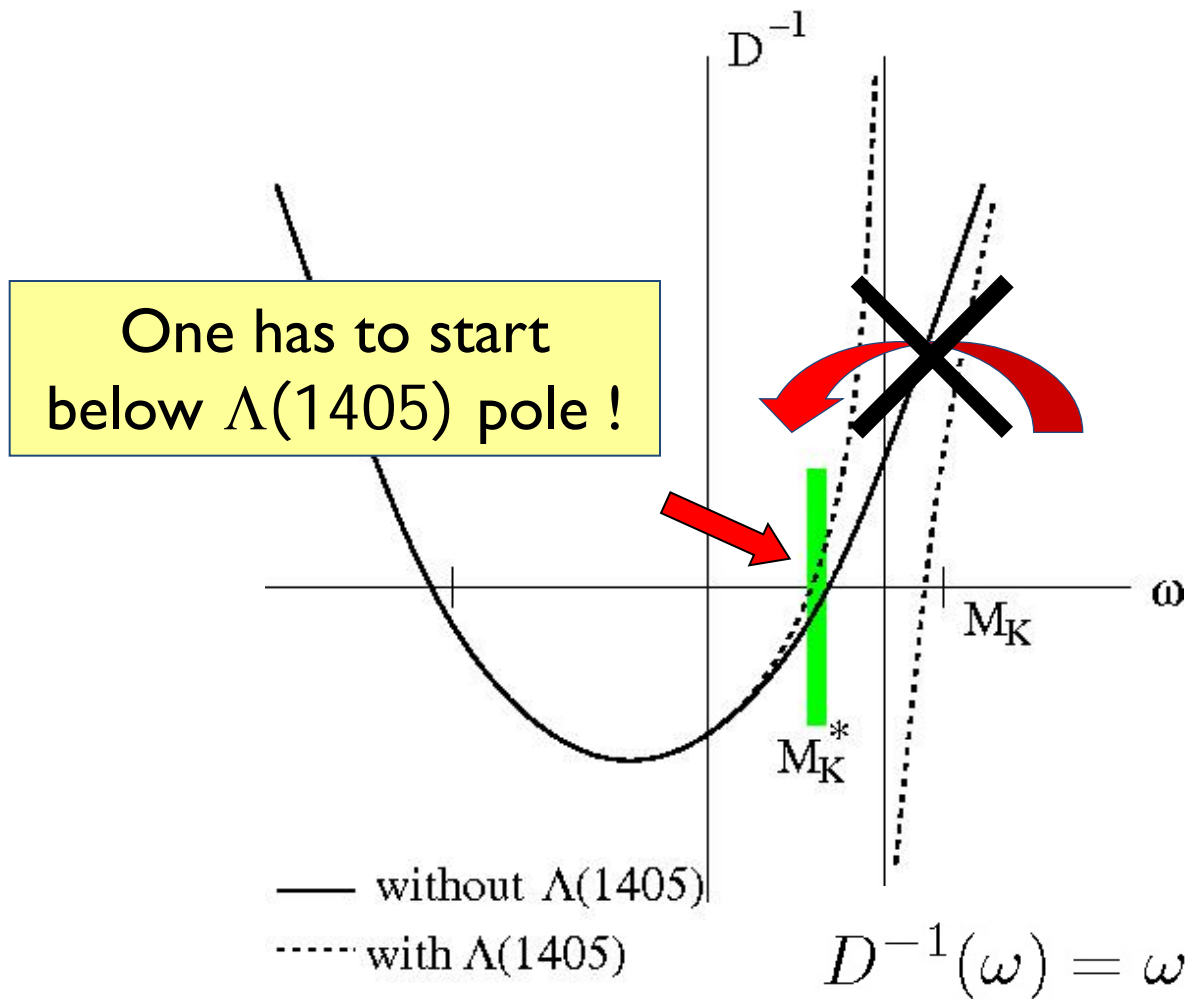
- ✓ Conventional approach :
 - from zero density to higher density
- ✓ Top-down approaches :
 - from high density where chiral symmetry is restored to lower density
 - possibilities in recent hQCD

Problems in conventional approaches

- ✓ Problem in K^-p Scattering amplitude:
experiment : - 0.65 + i 0.81 fm (repulsive)
chiral symmetry : + (**attractive !**)
- ✓ Problem of $\Lambda(1405)$
pole position of $\Lambda(1405)$
→ only 30 MeV below KN threshold

Perturbation breaks down in conventional approach !

Far below $\Lambda(1405)$ pole, $\Lambda(1405)$ is irrelevant !



$$D^{-1}(\omega) = \omega^2 - M_K^2 - \Pi(\omega)$$

Wanted : New Top-down approaches

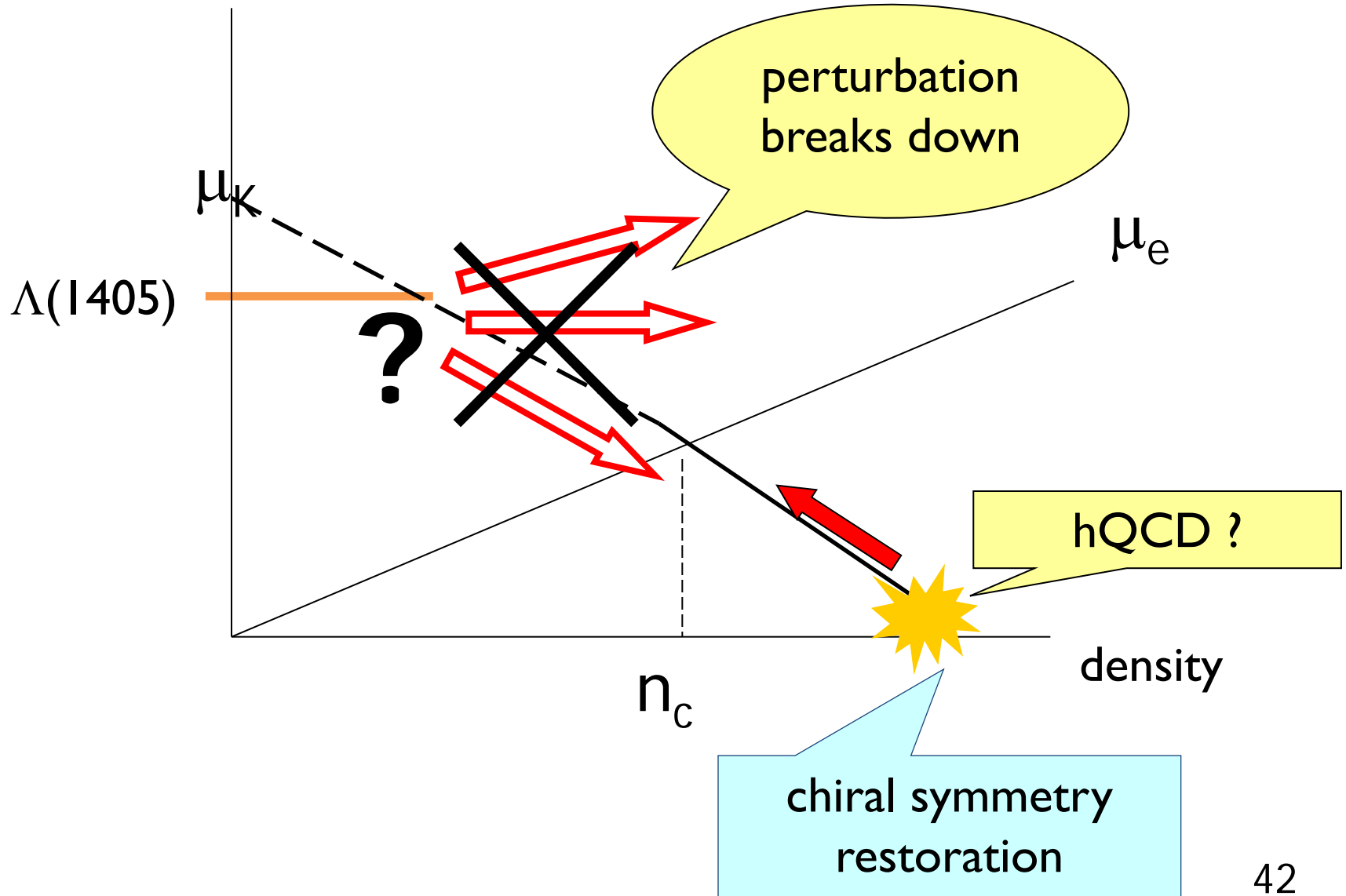
Q) Is there a proper way to treat strangeness in dense matter without problem of the irrelevant terms, e.g., $\Lambda(1405)$, from the beginning ?

Start from where the symmetry is fully restored !

- AdS/QCD, etc.

All irrelevant terms are out in the analysis from the beginning !

Goal: Strangeness in hQCD



- Bottom-up approach :
start from QCD and attempt to guess
its 5d holographic dual, AdS/CFT dictionaries
→ [hard-wall model](#), soft-wall model, ...
- Top-down approach :
start from string theory, set brane configuration with DBI
action, reproduce QCD-like theory
→ D3/D7, [D4/D6](#), Sakai-Sugimoto ...



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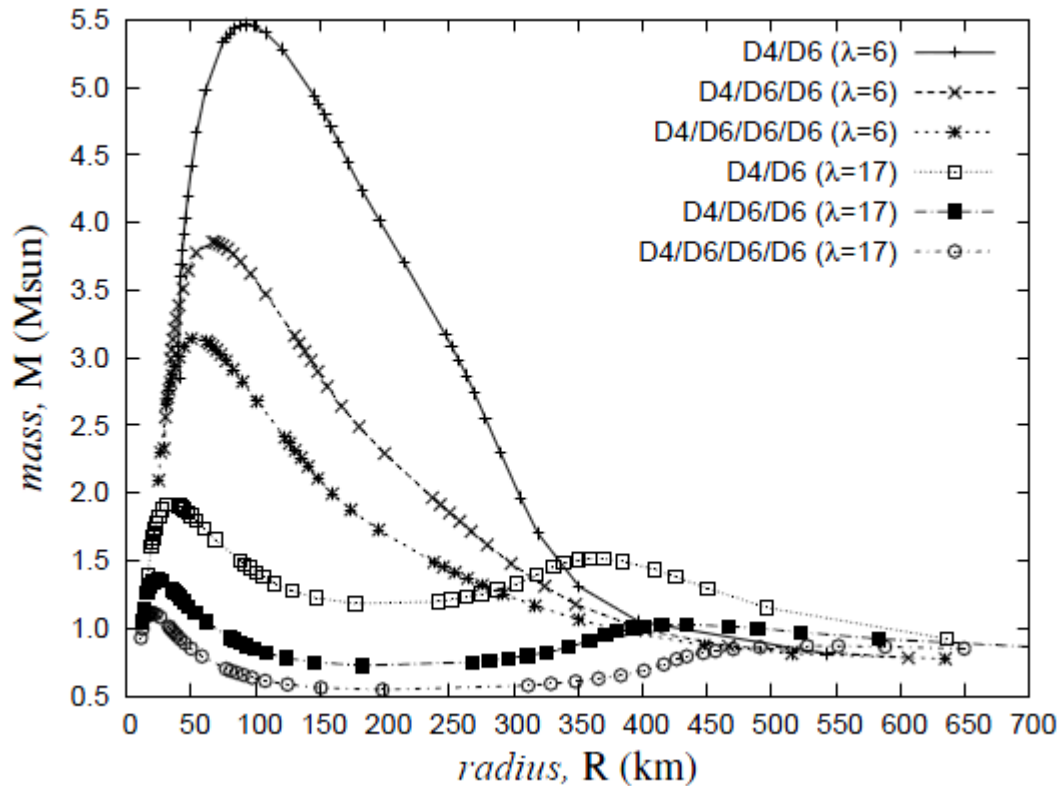
PUBLISHED: October 24, 2011

Holographic equations of state and astrophysical compact objects

Youngman Kim,^{a,b} Chang-Hwan Lee,^c Ik Jae Shin^a and Mew-Bing Wan^a

Related works by S.-J. Sin et al. JHEP 03(2010)074, 04(2008)010, 06(2011)011

Mass-radius relation



Far from realistic : what is the problem ?

hQCD: What is still missing ?

- proper attraction is missing
in large N_c limit & large t'Hooft coupling limit
- mass of scalar field is bigger than that of vector field
- strangeness in hQD

more details of hQCD itself
→ talk by Bumhoon Lee (Fri)

Prospect

- possibilities of different class of NS binaries
 - typical NS + high-mass NS/BH (> 2 solar mass)
 - could be hidden GW sources
- new approaches to NS EoS in hQCD
 - still far from realistic
 - how to put strangeness



Many Thanks

