Multi-layer scintillation detector for the MOON double beta decay experiment: Scintillation photon responses studied by a prototype detector MOON-1


Abstract

An ensemble of multi-layer scintillators is discussed as an option of the high-sensitivity detector Mo Observatory Of Neutrinos (MOON) for spectroscopic measurements of neutrino-less double beta decays. A prototype detector MOON-1, which consists of 6 layer plastic-scintillator plates, was built to study the sensitivity of the MOON-type detector. The scintillation photon collection and the energy resolution, which are key elements for the high-sensitivity experiments, are found to be 1835±30 photo-electrons for 976 keV electrons and $\sigma = 2.9\pm0.1\%$ ($\Delta E/E = 6.8\pm0.3\%$ in FWHM) at the $Q_{\beta\beta} \sim 3$ MeV region, respectively. The multi-layer plastic-scintillator structure with good energy resolution as well as good background suppression of $\beta-\gamma$ rays is crucial for the MOON-type detector to achieve the inverted hierarchy neutrino mass sensitivity.

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1. Introduction

Double beta decays (DBD) are sensitive and realistic probes to study the Majorana nature of neutrinos ($\nu$), the absolute $\nu$–mass scale and the $\nu$–mass spectrum. Recent neutrino-studies suggest that the effective $\nu$-mass to be studied by neutrino-less double beta decay ($0\nu\beta\beta$) is of the orders of 100–1 meV, depending on the mass spectrum, if the neutrino is a Majorana particle. Actually, it may be of the order of 100, 30, or 2 meV, if the mass spectrum is with quasi-degenerate (QD), inverted hierarchy (IH), or normal
hierarchy (NH). Thus it is of great interest to study $0\nu\beta\beta$ with the mass sensitivity of the order of 10 meV.

Current detectors for $0\nu\beta\beta$ experiments are limited by the mass sensitivity of the order of 200 meV in the QD region because of the limited total $\beta\beta$ isotopes to be used for their experiments. High-sensitivity $0\nu\beta\beta$ experiments with mass sensitivities of the QD mass of 100 meV and the IH mass of 30 meV may require quantities of $\beta\beta$ isotopes on the orders of 0.1-ton and 1-ton, respectively.

Several experiments are planned to study the effective mass in the QD and IH mass regions. Majorana/GERDA, CUORE/CUORICINO, EXO, XMASS CANDLES and others use calorimetric detectors, which are themselves made of $\beta\beta$ isotopes. On the other hand, MOON, NEMO/Super-NEMO and DCBA use spectroscopic detectors, with $\beta\beta$ sources that are positioned within but not an integral part of the detection system. Detailed discussions on v-masses to be studied by DBD, v-masses suggested by v-oscillations and present and future DBD experiments are found in review articles and references therein [1], [2], [3], [4], [5], [6].

The present paper is concerned with the MOON-type spectroscopic detector [7]. Mo Observatory Of Neutrinos (MOON) is based essentially on the ELEGANT V detector [8], but is expanded to improve the mass sensitivity by 2 orders of magnitudes for studying the effective mass in the QD and IH mass regions. Merits of the MOON-type spectroscopic experiment are as follows.

1. Spectroscopic studies of $\beta\beta$ energy and angular correlations enable one to identify the v-mass term.

2. Since $\beta\beta$ sources are separated from detectors, one can select such $\beta\beta$ isotopes with large $Q_{\beta\beta}$ values and nuclear responses (matrix elements) that give sufficient nuclear sensitivity to enhance the $0\nu\beta\beta$ signal rate and to place the $0\nu\beta\beta$ signal well above most BG ones.

3. It is realistic to build a high-sensitivity detector with mass sensitivity of the order of 10 meV using ton-scale $\beta\beta$ isotopes provided that it has energy resolution better than about $\sigma = 3\% \ (\Delta E/E \approx 7\% \ \text{in FWHM})$ at the $^{100}\text{Mo}$ $Q_{\beta\beta}$ value (3.034-MeV).

A prototype detector, MOON-1, was built to study the v-mass sensitivity of the MOON-type detector. In the present report, we discuss mainly the photon responses, i.e. the scintillation photon collection, the energy resolution and the energy calibration, which are key elements for high-sensitivity experiments. Other options of the MOON detector will be discussed elsewhere.

The v-mass sensitivity is discussed briefly in section 2. The MOON detector configuration and the prototype detector, MOON-1, are described in section 3. The scintillation photon collection, the energy resolution and the energy calibration are discussed in detail in section 4. Concluding remarks are given in section 5.

2. Neutrino mass sensitivity and $\beta\beta$ detector

The limiting effective v-mass $<m>$ which can be studied by $0\nu\beta\beta$ experiments with $^{100}\text{Mo}$ over a 5 year period is known to be given by the $0\nu\beta\beta$ nuclear sensitivity $S_N$ as follows [1].

\[
\langle m \rangle = 12\sqrt{S} \text{ meV} \tag{1}
\]

\[
S = S_N \times \frac{n_{\beta\beta}}{\sqrt{B \times \varepsilon}} \tag{2}
\]

where $n_{\beta\beta}$ is the $\beta\beta$ isotopes in unit of ton, $B$ are the BG rates per ton per year of the $\beta\beta$ isotopes at the $^{100}\text{Mo}$ $Q_{\beta\beta}$ value (3.034-MeV), and $\varepsilon$ is the detection efficiency of the $0\nu\beta\beta$ event after all kinds of hard and soft cuts. The nuclear sensitivity $S_N$ in unit of $10^{-24} \text{ y}^{-1} \text{eV}^{-2}$ is expressed as $S_N = GM[2$ with $G$ and $M$ being the phase-space factor and the nuclear matrix element in unit of the electron mass, respectively. The mass sensitivity in equation (1) in ref [1] is based on the 2$\sigma$ confidence level to describe detector sensitivity, yet a 4.5$\sigma$ confidence level will be required for $0\nu\beta\beta$ claims. In case of MOON with the detection efficiency of around $\varepsilon \approx 0.3$ and the nuclear sensitivity $S_N \approx 1$, one gets $<m> \approx 22 (Bn_{\beta\beta})^{1/4}$ meV. Then one needs low-background ($B \approx 1$ per ton year) and large-scale detectors with ton-scale $\beta\beta$ isotopes ($n_{\beta\beta} \approx 1$) to achieve the IH sensitivity of $<m> \approx 30$ meV. Since the energies of $0\nu\beta\beta$ signals for these $\beta\beta$ isotopes exceed the energies of most $\beta-\gamma$ signals from the natural and cosmogenic R1 impurities, their BG rates may not be sufficiently realistic. Then major BG events are due to the tail of the 2$\nu\beta\beta$ spectrum in the $0\nu\beta\beta$ window, which depend strongly on the $0\nu\beta\beta$ energy window and thus on the energy resolution.

Key points of spectroscopic experiments with the mass sensitivity of an order of IH mass ($\sim 30$ meV) are to build a large low-background detector to accommodate $\beta\beta$ isotopes of the order of $n_{\beta\beta} \approx 1$ (ton) and to achieve the sufficient energy resolution with $\sigma = 3\% \ (\Delta E/E \approx 7\% \ \text{in FWHM})$ at the $^{100}\text{Mo}$ $Q_{\beta\beta}$ value (3.034-MeV) regions to reduce the 2$\nu\beta\beta$ BG rate to the order of $B \approx 5$ (per ton year). It is really a challenge to meet these conditions in the few-MeV energy region.

3. MOON detector concept

MOON consists of multi-layer detector modules [7], [9], [10]. Each module of the plastic-scintillator option MOON is composed of a plastic-scintillator plate, two thin detector planes for position and particle identifications, a thin $\beta\beta$ source film interleaved between the two planes. The $\beta\beta$ vertex point is identified by the detector planes for position and particle identification, while energies of the two $\beta$ rays are measured by two adjacent plastic-scintillator plates. All other modules (layers) are used as active shields to reject $\gamma$ rays in the MOON detector. Scintillation photons are collected by photo-multiplier tubes (PMT) around the plastic-scintillator plate. Assuming one module is composed of one plastic-scintillator with $\sim 1 \times 1 \times 0.01$ m$^3$ and a thin $\beta\beta$ source film with $100 \times 100$ cm$^2$ and 20 mg/cm$^2$, the detector has 0.2 kg of $\beta\beta$ isotopes per module. Thus one unit made of 200 modules at $\sim 1$cm intervals has 40 kg of $\beta\beta$ isotopes with the total detector volume of the order of $\sim 1 \times 1 \times 4$ m$^3$ in case of scintillation-fiber planes for particle identification. The MOON-type spectroscopic experiment has several unique features.
1. Individual $\beta\beta$ rays emitted in opposite directions are measured in coincidence by two adjacent plastic-scintillator plates to confirm the $v$-mass term in the $0v\beta\beta$.

2. The multi-module structure makes it realistic to build a compact detector of the order of $\sim 0.1$ m$^3$ per kg $\beta\beta$ isotopes to accommodate a ton scale of $\beta\beta$ isotopes.

3. Good energy resolution of $\sigma \approx 3\%$ ($\Delta E/E \approx 7\%$ in FWHM) at the $^{100}$Mo $Q_{\beta\beta}$ value (3.034-MeV) can be obtained by efficient scintillation photon collection to reduce the $2\nu\beta\beta$ contribution down to the order of 5 per ton year.

4. The multi-layer module structure with a good position resolution enables one to select $0v\beta\beta$ signals and reject RI-background signals [11], [7], [9], [10]. Then BG’s from RI isotopes in $\beta\beta$ source with realistic ppt (parts per trillion) purity-level may be quite small.

5. Since the source is separated from detector, one can select the best one or two $\beta\beta$ nuclides from view points of the nuclear matrix element, the phase space, the signal energy, and the $2\nu\beta\beta$ rate.

Accordingly it is realistic to carry out high-sensitivity $\beta\beta$ experiments in the QD-IH mass region. The present paper aims at demonstrating experimentally the key points of 2 and 3 given above using a prototype MOON-1 detector [10], [11], [12], [13], [14].

4. A prototype MOON-1 detector

4.1. MOON-1 detector configuration

A prototype MOON-1 detector was constructed to study the scintillation photon responses (photon collection and energy resolution), the feasibility of the multi-layer structures of plastic-scintillator plates and $\beta\beta$-source films, and the BG-rejection capability. These are crucial points for the high-sensitivity experiment, and thus the results of MOON-1 can be used to prove feasibility of MOON with the mass sensitivity of around 30 meV.

The MOON-1 detector consists of 6-layer plastic-scintillator plates, each with $53 \times 53 \times 1$ cm$^3$, as shown schematically in Fig. 1 [13], [14]. RP-408 (BC-408 equivalent) plastic-scintillator plates were provided by REXON. The plastic-scintillator plates are realistic detectors from view points of the low RI impurity, the good photon yield of around $10^4$ per MeV, and the low-cost of a large quantity on the order of 10 tons.

The 94.5 % enriched $^{100}$Mo films [15], each having dimensions of 48x48 cm$^2 \times 40$ mg/cm$^2$, are interleaved between two plastic-scintillator plates. The total amount of the $^{100}$Mo films is 142 g. The plastic scintillator plates are viewed by square-type PMT (R6236-01-KM1D provided by Hamamatsu Photonics). The 56 PMTs are coupled to the four sides of the 6-layer plastic-scintillator plates.

4.2. Photon response of plastic-scintillator

Photon response for the same plastic-scintillator as used for the MOON-1 detector was studied using RI sources. The 32 PMTs are coupled to the four sides of plastic-scintillator plates to get the same coverage as in MOON-1. As the first step, the photon response for each PMT was measured using photons from LED (NSPB500S, 475 nm, NICHA). The measured spectrum was analyzed in terms of the Poisson distribution for the photo-electron fluctuation and the Gaussian distribution for the PMT gain fluctuation. The PMT response is obtained to be $3.6 \pm 0.07$ ADC channels per photo-electron. The error is due to statistical fluctuations estimated via peak fitting.

The photon response for each of the plastic-scintillators was measured using the 976-keV K conversion-electron from a $^{208}$Bi source at the center of each plastic-scintillator. The number of photo-electrons for each PMT was deduced from the observed 976-keV peak channel using the measured response of 3.6 channels per photo-electron. The number of photo-electrons depends upon the geometrical...
position (solid angle) of the PMT with respect to the source, as shown in Fig. 2 (a), (b), (c), and (d). They are plotted for 4 PMT geometries in Fig. 3. The number of photo-electrons are nearly the same among PMTs in approximately the same relative geometrical position ((a), (b), (c), or (d) in Fig. 2). They scatter little around the average value (line in Fig. 3), depending on the photo contact between PMT and plastic-scintillator. Then slight adjustments were made among the 8 PMTs having the same relative geometry.

Fig. 2. PMT geometry. (a), (b), (c) and (d) shows 4 kinds of the PMT geometrical positions. 8 PMTs in each geometry are symmetrical with respect to the test source at the center. PMT ID numbers are attached on PMT.

Fig. 3. Photo-electron numbers obtained by each PMT. The $^{207}$Bi source with 976-keV K conversion-electrons is set at the center of plastic-scintillator.

Then the energy spectrum is obtained for the K and L conversion-lines from $^{207}$Bi by summing up the energy signals from the 32 PMTs with the two-Gaussian peak fit and the individual K and L peak fits.

Fig. 4. Energy spectrum of the K and L conversion-electrons from $^{207}$Bi by summing up the energy signals from the 32 PMTs with the two-Gaussian peak fit and the individual K and L peak fits.

Fig. 5. Position dependence of the total number of photo-electrons from the 976-keV $^{207}$Bi K-line. The source position (x axis) gives the distance along the x axis (x = 0, y = 0).

4.3. MOON-1 detector setting

The MOON-1 detector was set in the active and passive shields of ELEGANT V [8], [18], as shown in Fig. 6. The drift chamber was replaced by the multi-layer plastic-scintillator plates with $^{108}$Mo films. The active shields of 14 NaI(Tl) detectors, each having dimensions of 102×10.2×10.2 cm$^3$, were used to veto $\gamma$ rays associated with RI backgrounds. The passive shields are 10 cm thick copper bricks (Oxygen Free High Conductivity) and 15 cm thick lead bricks. The MOON-1 and the NaI(Tl) detectors were set in an air-tight box (69.6 cm high and 147.0 cm by
200.0 cm) in order to keep the radon (Rn) concentration low by flushing it with Rn free N2 gas. The experiment was carried out at the Oto underground laboratory with 1400 m water-equivalent depth.

Data taking is made using four kinds of trigger signals from plastic-scintillator, LED, Clock, and NaI(Tl). The first three triggers were taken simultaneously. The plastic-scintillator trigger with the threshold less than 200-keV is used to measure the two β rays by plastic-scintillators. The UV LED trigger is used to monitor the MOON-1 detector. The Clock trigger is used to obtain the pedestal for each PMT. The NaI(Tl) trigger is used to measure γ ray backgrounds. The data are recorded by ORed triggers. The ORed rate is around 11 Hz, with 8 Hz, 2 Hz and 1 Hz from plastic-scintillators, LED, and Clock, respectively. The dead time is 1.2 msec (~ 1 %).

The front end of the data acquisition system is designed using CAMAC at the Oto underground laboratory. The CC/NET (TOYO) [19], which has an internal CPU, is used as the CAMAC crate controller. The Linux OS is installed in the CC/NET. The collected-data program runs on the Linux OS. The data, which are saved in the server computer, are transferred to the computer in RCNP (Research Center for Nuclear Physics) of Osaka University and the quality of which may be checked via the network.

The High Voltage (HV) are supplied from CAEN SY 527 [20] and SY 403 [21] for the PMTs in the MOON-1 plastic-scintillators and the NaI(Tl) detector, respectively. They can be controlled and monitored by the Linux server through RS232C. Therefore, one can access the server from Osaka university.

The experimental setup is shown in Fig. 7. The 1.274-MeV γ rays from a 22Na source are set at 90 mm above the top of plastic-scintillator. One PMT collects photons from 2 or 3 layers of plastic-scintillators. The selection of the single-layer PL3 event is made by requiring signals from PMTs viewing the PL3 which are not vetoed by signals from other PMTs, as shown schematically in Fig. 8. The energy deposit on PL3 is obtained by summing up signals from PMTs viewing PL3. Here the threshold for the summed signal is set at 200-keV, while that for the veto signal at 50-keV.

![Fig. 7. The experiment setup is shown to perform the energy calibration using 22Na source at 90 mm above the top of the plastic scintillator.](image)

![Fig. 8. Plastic-scintillator and PMT configuration. Single-layer hit events are selected by requiring signals from all PMT2, PMT3 and PMT4 in coincidence and veto signals from any PMT1, PMT5, or PMT6.](image)

5. Results of MOON-1 detector responses

5.1. Beta event selection

The present work demonstrates the feasibility of the multi-layer plastic-scintillator modules in terms of having both sufficient scale and energy resolution, which are key elements for such a high-sensitivity experiment. Here, single-layer hit events at the PL3 (the third layer from the top) are selected to estimate the energy resolution of the MOON-1 plastic-scintillator plates.

5.2. γ ray reconstruction and energy calibration

Compton-scattering is a dominant process for γ rays in plastic-scintillator. Thus the full energy of the gamma peak may be reconstructed by summation of the energy of the Compton-scattered electron deposited in a plastic-scintillator with the corresponding energy of the Compton-scattered γ ray deposited in one of the NaI(Tl). Coincidence between a single-layer hit at PL3 and corresponding energy deposited within NaI(Tl) ID4 is required for each of the 1.274-MeV γ rays from the 22Na source shown in Fig. 9. The other NaI(Tl) detectors are used as veto counters. Therefore, the two 511-keV γ rays from the source are emitted outside the MOON-1 detector.

The line in the plot of PL3 versus NaI(Tl) ID4 in Fig. 10 is indicative of correlated signals having a total energy of
1.274-MeV. The reconstructed 1.274-MeV γ ray spectrum is obtained by summing the two signals from PL3 and NaI(Tl) ID4, as shown in Fig. 11.

Here, the relative and absolute energy calibrations are obtained via two distinct procedures. One is the relative calibration. The other one is the absolute energy calibration. The relative gains for PMTs are calibrated using the Compton edge of 1.274-MeV γ rays from the $^{22}$Na source. Their signals obey the measured distribution as obtained in the section 4.2. The energy calibration of NaI(Tl) ID4 is performed using the γ rays from the source ($^{22}$Na 511-keV, 1.274-MeV) and the radioactive isotopes ($^{40}$K 1.461-MeV, $^{208}$Tl 2.615-MeV). The reconstructed total energy peaks are used for the absolute energy calibrations of the plastic-scintillators. This method is used for other plastic-scintillator layers as well.

**Fig. 9.** Compton-scattering of $^{22}$Na γ rays. The γ ray source is set on the rough center of a plastic scintillator. The single-layer hit event of the plastic scintillator (PL3) with NaI(Tl) detector (ID4) is selected for the 1.274-MeV γ rays from $^{22}$Na source.

**Fig. 10.** The energy deposit on the plastic scintillator (PL3) and the NaI(Tl) ID4 detector is shown for the event of the 1.274-MeV γ rays from $^{22}$Na source. The line shows that the sum energy of 1.274-MeV.

5.3. **Energy resolution of plastic-scintillator**

The reconstructed γ peaks from the plastic-scintillator and the NaI(Tl) signals are used to evaluate the energy resolution of the MOON-1 plastic-scintillator plates. Here, the energy and the energy resolution for the reconstructed γ ray are expressed as

$$E_\gamma = E_{PL} + E_{NaI}$$

$$\Delta E_\gamma^2 = \Delta E_{PL}^2 + \Delta E_{NaI}^2$$

where $E_\gamma$, $E_{PL}$, and $E_{NaI}$ are the energy of the reconstructed γ ray, the energy deposit on the plastic-scintillator and the energy deposit on the NaI(Tl), respectively, and $\Delta E_{PL}$, $\Delta E_{NaI}$ are their respective fluctuations.

First, the energy resolutions of the NaI(Tl) detector were found to be $\sigma = 4.5\pm0.2\% \ (\Delta E/E = 10.5\pm0.4\% \ in \ FWHM)$, $2.8\pm0.1\% \ (6.6\pm0.2\% \ in \ FWHM)$ for the γ rays from the source ($^{22}$Na 511-keV, 1.274-MeV) and to be $\sigma = 2.7\pm0.1\% \ (\Delta E/E = 6.4\pm0.2\% \ in \ FWHM)$, $2.0\pm0.1\% \ (4.6\pm0.3\% \ in \ FWHM)$ for the radioactive isotopes ($^{40}$K 1.461-MeV, $^{208}$Tl 2.615-MeV) respectively.

The energy window of NaI(Tl) is selected in order to estimate the energy resolution of plastic-scintillator. Requiring a coincidence between the 511-keV energy deposited on the NaI(Tl) ID4 with the 763-keV energy deposit from the Compton-scattered electron on the PL3, the energy resolution of the PL3 at the 763-keV may thus be obtained. The energy window is shown for 1.274-MeV γ rays in Fig. 12.
The γ ray peaks from the source ($^{22}$Na 1.274-MeV) and the radioactive isotopes ($^{208}$Tl 2.615-MeV) are shown at the energy window $E_{\text{NaI}} = 511$-keV of the NaI(Tl) detector in Fig. 13 and Fig. 14. They are fitted by a Gaussian peak with an exponential background tail. The measured energy deposit at PL3 agrees with the expected value of $E_{\text{PL}} = E_{\gamma} - E_{\text{NaI}}$, as shown in Fig. 15. Here the energy scale of plastic-scintillator is calibrated using the 1.461-MeV γ rays from the $^{40}$K radioactive isotope.

The energy resolution for PL3 is found to be well reproduced by $\sigma/\sqrt{E}$ with $\sigma = 5.0\pm0.2$ % ($\Delta E/E = 11.9\pm0.5$ % in FWHM) in the energy region from 0.5-MeV to 2.1-MeV, as shown in Fig. 16. This energy region covers β ray energies in most spectroscopic ββ experiments. The energy resolutions obtained for the conversion-electrons from the source ($^{137}$Cs 624-keV, $^{207}$Bi 976-keV) agree well with those derived from the reconstructed γ peaks, as shown in Fig. 16. The energy resolution at the $^{100}$Mo Q$_{\beta\beta}$ value (3.034-MeV) is $\sigma = 2.9\pm0.1$ % ($\Delta E/E = 6.8\pm0.3$ % in FWHM), which is the energy resolution required for MOON with the IH mass sensitivity.

6. Concluding remarks
1. MOON is a spectroscopic $\beta\beta$ experiment with a v-mass sensitivity in the IH mass region (30 meV). It has a multi-layer structure of plastic scintillator plates to accommodate a ton-scale $\beta\beta$ source, a good energy resolution of $\sigma \approx 3\%$ ($\Delta E/E \approx 7\%$ in FWHM) at the $0\beta\beta$ peak energy, and a good BG rejection capability. These are crucial for achieving the IH mass sensitivity.

2. A prototype detector MOON-1 was built to demonstrate the feasibility and the sensitivity of MOON. It consists of 6 layers of plastic-scintillator plates with dimensions of 53x53x1 cm$^3$. Photons are collected by 56 PMTs positioned along the 4 sides of the plate covering about 82 % of the plastic-scintillator side-face.

3. The number of total photo-electrons is 1830±35 for the 976-keV electron line. This is just what is expected from the total reflection rate for the case of the total number of $10^4$ photons per MeV for the present plastic-scintillator, the amount of coverage by PMTs, and the photo-electron conversion coefficient of 0.25 for the PMTs.

4. The energy resolution, which is one of the key elements for the large-scale spectroscopic $\beta\beta$ experiments, was measured using conversion-electrons from RI sources as well as Compton-scattering electrons from RI $\gamma$ rays. A new method of checking the plastic-scintillator response for low-energy electrons is carried out using reconstructed $\gamma$ peaks via summing the energy of the Compton-scattered electrons in the plastic-scintillators with the energy from the coincident Compton-scattered $\gamma$ rays in the NaI(Tl).

5. The measured energy resolution is found to be well reproduced by $\sigma/\sqrt{E}$ with $\sigma \approx 5.0\pm0.2\%$ ($\Delta E/E = 11.9\pm0.5\%$ in FWHM) in the energy region from 0.5-MeV to 2.1-MeV. This leads to the energy resolution of $\sigma = 2.9\pm0.1\%$ ($\Delta E/E = 6.8\pm0.3\%$ in FWHM) at the $^{100}$Mo $Q_{\beta\beta}$ value (3.034-MeV). This is just what is required for the IH mass sensitivity of around 30 meV.

6. The energy resolution of $\sigma = 5.0\%$ ($\Delta E/E = 11.9\%$ in FWHM) for 1-MeV is worse than $\sigma = 2.3\%$ ($\Delta E/E = 5.4\%$ in FWHM) due to the statistical fluctuation of photo-electrons, since the observed resolution includes the intrinsic (non-statistical) component [22] and others. Proper choice of the plastic-scintillator material and production process may improve the resolution quite a bit.

7. The MOON-1 with 53 cm x 53 cm plastic-scintillator plates works well and can be expanded by a factor 2 to the MOON scale ($\approx 100$ cm x 100 cm) since the photon attenuation in the plastic-scintillator plate is less than a few percent.

In short, the present work demonstrates the feasibility of the multi-layer plastic-scintillator modules for a high-sensitivity MOON detector in terms of having both sufficient scale and energy resolution, which are key elements for such a high-sensitivity experiment. Another important feature of the detector is the capability of RI background rejection, which is studied experimentally using the MOON-1. MOON is a spectroscopic detector, where $\beta\beta$ source is within but not an integral part of the detector. Thus the MOON-type detector with the multi-layer structure of plastic-scintillator plates can be universally used for $\beta\beta$ decays of other isotopes as well as for other low-energy rare decays.

Experimental studies of the RI-background rejections, the position-sensitive detector plane and others relevant to MOON detectors are reported elsewhere.

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