Search for SUSY in the AMSB scenario with the DELPHI detector

The DELPHI Collaboration

Abstract. The DELPHI experiment at the LEP $e^+e^-$ collider collected almost 700 pb$^{-1}$ at centre-of-mass energies above the $Z^0$ mass pole and up to 208 GeV. Those data were used to search for SUSY in the Anomaly Mediated SUSY Breaking (AMSB) scenario with a flavour independent common sfermion mass parameter. The searches covered several possible signatures experimentally accessible at LEP, with either the neutralino, the sneutrino or the stau being the Lightest Supersymmetric Particle (LSP). They included: the search for nearly mass-degenerate chargino and neutralino, which is a typical feature of AMSB; the search for Standard-Model-like or invisibly decaying Higgs boson; the search for stable staus; the search for cascade decays of SUSY particles resulting in the LSP and a low multiplicity final state containing neutrinos. No evidence of a signal was found, and thus constraints were set in the space of the parameters of the model.

1 Introduction

There are several theoretical motivations to believe that nature could be supersymmetric. However, after many years of searching in collider experiments, no evidence was found for the existence of supersymmetric particles. The negative results of the searches constrains the spectrum of the SUSY particles and of the parameters of the model. The mechanism of SUSY breaking itself is unclear. In the gravity mediated scenario (SUGRA) [1], SUSY is broken in a hidden sector and the breaking is transmitted gravitationaly to the observable sector. This mechanism is elegant, since it only requires already existing fields and interactions, like gravity. It suffers, however, from the so called SUSY flavour problem, since it requires a large amount of fine tuning in the squark and slepton mass matriced to avoid unobserved large flavour-changing neutral current effects.

To cope with the SUSY flavour problem, different SUSY breaking mechanisms have been proposed. In the Gauge Mediated SUSY Breaking scenario (GMSB) [2] the breaking is transmitted via gauge forces. This model predicts a very characteristic mass spectrum, with a light gravitino as the lightest supersymmetric particle (LSP), and typically long-lived next-to-lightest supersymmetric particles (NLSP).

Anomaly Mediated Supersymmetry Breaking (AMSB) [3,4] is another interesting solution to the flavour problem of mSUGRA. Rescaling anomalies in the supergravity Lagrangian always give rise to soft mass parameters in the observable sector. It follows that anomalies contribute to SUSY breaking in any case, irrespective of the main symmetry breaking mechanism. We shall refer to AMSB as the model in which all other components that mediate the SUSY breaking are suppressed and the anomaly mediation is the dominant mechanism.

The minimal AMSB is very predictive: all the low energy phenomenology can be derived by adding to the Standard Model (SM) only two extra parameters and one sign. Unfortunately, the minimal AMSB model would imply negative squared masses (tachyons) for the sleptons at the electroweak scale. One way of getting rid of tachyons is to suppose additional, non-anomaly, contributions to the SUSY breaking which can generate a positive contribution to the soft masses squared. There are a few string-motivated solutions that generate such a positive contribution without spoiling the renormalization group (RG) invariance of the soft terms. In most cases, such a contribution is universal for all sfermion masses and, in practice, it is enough to add just one extra parameter to the model. This arises, for instance, when the visible and the hidden sectors lie in separate branes that communicate only through gravity [3]. There are other solutions [5] that lead to flavour dependent mass terms; such possibilities are less predictive, since the sfermion spectrum depends on more parameters, and they will not be investigated further in this paper. In the following, the minimal AMSB with a single, flavour independent, sfermion mass parameter will be considered, as implemented in version 7.63 of the program ISAJET (see below). However, the characteristic gaugino spectrum of AMSB is the same even for models without such an universal sfermion mass term, and most of the considerations that follow can be applied also to them.

The paper is organized as follows. In Sect. 2 the phenomenology of AMSB relevant to the search at LEP is shortly reviewed. Section 3 lists the data and the event generators used to simulate the signal. Section 4 describes the results of the searches for the AMSB signatures in DELPHI. In some cases, searches already performed in DELPHI were just reinterpreted in the context of AMSB. The descriptions of those searches can be found in the relevant papers cited in that section. In other cases, which are described here in more detail, it was necessary to adapt the original techniques to the requirements specific to the AMSB scenarios. With no evidence of excesses above the SM expectations, in Sect. 5 the results of the searches are combined to constrain the parameters of the model and the spectrum of some SUSY particles.

2 Phenomenology of AMSB

If there is only one common squared mass term for all scalars, all masses and couplings can be derived in terms of just three parameters and one sign:

- the mass of the gravitino, $m_{3/2}$;
- the ratio of the vacuum expectation values of the Higgs fields, $\tan \beta$;
- the common scalar mass parameter $m_0$;
- the sign of the Higgs term, $\text{sign}(\mu)$. 

In this context, \( m_0 \) can even be considered as a phenomeno-
logical term that parameterizes the lack of knowledge of the
method with which the sleptons acquire physical masses.

Low-energy gaugino masses \( (M_\lambda) \), scalar masses \( (M_Q) \),
and trilinear couplings \( (A_y) \) in AMSB are given by:

\[
M_\lambda = \frac{\beta_\lambda}{\gamma} m_{3/2}
\]
\[
M_Q^2 = -\frac{1}{4} \left( \frac{\partial \gamma}{\partial \beta_\gamma} + \frac{\partial \lambda}{\partial \beta_\gamma} \right) m_{3/2}^2 + m_0^2
\]
\[
A_y = \frac{\beta_y}{\gamma} m_{3/2}
\]

where \( g \) are the gauge couplings, \( y \) the Yukawa couplings
and \( \gamma \) and \( \beta \) are RG functions. This soft mass spectrum
has distinctive features [4] which can differ from the usual
SUGRA or GMSB scenarios.

- The gravitino is heavy (this has several advantages for
cosmology [4]).
- The ratios of gaugino masses at the electroweak scale
are determined by the ratios of the corresponding \( \beta \)
functions. Therefore, they assume in a natural way dif-
ferent values with respect to the theories with gaugino
mass unification at a Grand Unification (GUT) Scale:

\[
M_1 : M_2 : M_3 \simeq 2.8 : 1 : -8
\]

These ratios have been computed by including the
largest next-to-leading corrections [4]. Small deviations
from these ratios can occur as a result of varying the
parameters of the model. Typical values of \( \mu \) allowed
by the model imply \( M_2 < M_1 < |\mu| \). As a conse-
quence, the chargino \( (\tilde{\chi}_i^\pm, i = 1, 2) \) and neutralino \( (\tilde{\chi}_j^0, j = 1, 4) \)
mass eigenstates are rather well approximated by ei-
ther pure gaugino or pure higgsino states, with \( M_{\tilde{\chi}_1^0} \sim
M_{\tilde{\chi}_2^0} \sim M_2, M_{\tilde{\chi}_3^0} \sim M_1, M_{\tilde{\chi}_4^0} \sim M_{\tilde{\chi}_2^\pm} \sim |\mu| \).
Therefore, the lightest chargino and neutralino are always a
nearly mass-degenerate doublet of gauginos, with never-
thless \( M_{\tilde{\chi}_1^0} \sim M_{\tilde{\chi}_1^\pm} \); the second lightest neutralino
is a gaugino of intermediate mass; and the heaviest
chargino and neutralinos are heavy and higgsino-like.

- Squark masses are rather insensitive to \( m_0 \). AMSB im-
plies squarks and gluinos much heavier than the LSP,
and completely out of reach at LEP.
- In the slepton sector, if both the right and the left
chiral states receive the same \( m_0^2 \) contribution, the
diagonal entries of the mass matrix are accidentally
highly degenerate. Nearly mass-degenerate and highly
mixed same flavour sleptons are a distinctive feature of
the minimal AMSB with a flavour-independent \( m_0 \).
The lightest stau is always the lightest charged slepton.
The sneutrinos can be lighter than all charged sleptons,
and typically the stau sneutrino is the lightest sneutrino.
- The CP-odd neutral Higgs, \( A \), is usually much heavier
than the \( Z \), and the lightest CP-even neutral Higgs, \( h^0 \)
is analogous to the SM one [6]. Also the mass of the \( h^0 \)
is still more tightly bound than in the usual SUSY sce-
narios, since it should lie below 120 GeV/c^2 [6]. There-
fore, the lower limit obtained at LEP for the SM Higgs
mass already strongly constrains the AMSB parameter
space. Moreover, if such a light Higgs is not to be found
at the Tevatron or, later, at the LHC, the AMSB model
itself will be completely ruled out.

In the model considered here, only the slepton mass
spectrum and, to some extent, the Higgs depend on the
assumptions of a common scalar term \( m_0 \). All other features
are characteristic of any AMSB scenario, independently of
the procedure used to cope with the tachyonic masses of the
sleptons.

Since \( m_0 \) is a free parameter, according to its value
there are three possible candidates for the LSP: the nearly
mass-degenerate \( \tilde{\chi}_1^0/\tilde{\chi}_1^+ \), the \( \tilde{\tau} \) (for relatively small values
of \( \tan \beta \) and \( m_{3/2} \)) or the \( \tilde{\tau} \). Scenarios with any of the
above as LSP are explored in the following.

### 3 Data and simulation samples

The results listed in this paper come from searches per-
formed in the DELPHI experiment [7] at the electron-
positron collider LEP of CERN, and interpreted in the
context of AMSB. Some of these searches were originally
prepared for different analyses and used unmodified here.
Others, were instead optimized to search specifically for the
AMSB signatures. If not otherwise specified in the text,
the reader should refer to the papers cited for the descrip-
tion of the samples of the data and of the SM background
simulation used in the different analyses.

DELPHI collected a total of approximately 116 pb\(^{-1}\)
while running at the \( Z^0 \) pole in the years from 1989 to 1995 (LEP1).
About 694 pb\(^{-1}\) of integrated luminosity
were harvested in the LEP2 phase, with centre-of-mass
energies ranging from 130 to 208 GeV.

SUSYGEN [8] was used for the simulation of the signal.
As it does not allow for the calculation of the particle spec-
trum of the AMSB models, the input parameters were set
so as to correspond to a spectrum close to the one result-
ing from the precise calculations in the AMSB framework
of [4].

ISAJET [9], since version 7.47, allows the calculation
of the particle masses and decay branching modes of the
AMSB model of [3, 4] as a function of the four parameters
\( m_0, m_{3/2}, \tan \beta \) and \( \text{sign}(\mu) \). To constrain the allowed space
of the parameters, the result of the searches were compared
with the prediction of mass spectra, cross-sections and
decay modes as given by ISAJET 7.63 \(^1\). In that version of
ISAJET only one loop contributions are considered in the
Higgs sector, while all two loops terms are included for the
running of the gauge couplings. The program was run with
the following SM parameters in input: \( \alpha_s(M_Z) = 0.118 \) and
the mass of the top quark at the mean value of [11], i.e.
\( m_t = 174.3 \text{ GeV}/c^2 \). Since \( m_t \) is relevant in the definition
of the Higgs mass spectrum, also samples with \( m_t = 169.2 \)
and \( m_t = 179.4 \text{ GeV}/c^2 \) were generated, which corresponds

\(^1\) In the code used for the scan some of the later correc-
tions were applied by hand, as implemented in the subsequent
versions of the program [10]
4 Searches used to investigate the AMSB scenario

In this section, the searches for topologies predicted by the AMSB model at LEP are reviewed.

4.1 LEP1 limits

The precise measurement of the $Z^0$ width at LEP1 [11] was used to place severe constraints on all possible non-SM contributions. Given the good agreement between the measured total width and the one predicted by the SM, non-standard contributions are expected to be smaller than 3.2 MeV/$c^2$ at the 95% confidence level (CL). In particular, this rules out charginos with mass smaller than 45 GeV/$c^2$ at the same CL, independently of their field composition and decay modes. Such lower bound on the mass of the chargino is not going to be affected even if the more conservative method of [12] is used to fit the amount of allowed non-SM $Z$ width. The upper limit on the non-SM invisible width is more model independent, and evaluated to be 2.0 MeV/$c^2$ at the 95% CL [11]. Sneutrinos with mass below 43 GeV/$c^2$ are incompatible with that limit. Limits for other sparticles depend both on mass and couplings.

4.2 Search for nearly mass-degenerate chargino-neutralino

One of the key features of AMSB is the very small difference between the masses of the lightest chargino and neutralino. Therefore, the results of the search for nearly mass-degenerate chargino and neutralino [13] can be used to investigate AMSB.

When the masses of the lightest chargino and neutralino are very close, the visible products of the decay $\tilde{\chi}_1^\pm \rightarrow \tilde{\chi}_0^{ff'}$ carry little momentum. Therefore, they are both difficult to select and trigger on, and they can become almost indistinguishable from the huge background of two-photon events at LEP2. Dedicated techniques were used for this search. If there is a sneutrino lighter than the chargino two-body leptonic decay modes dominate: this case is treated in Sect. 4.3.

For $\Delta M = M_{\tilde{\chi}_1^\pm} - M_{\tilde{\chi}_1^0}$ below approximately 200 MeV/$c^2$, the phase space available for the decay is limited, and the lifetime can be so long that the chargino produced at the interaction point is seen as either a heavy stable charged particle in the detector, or as a kink in the reconstructed track. Long-lived charginos are searched for in DELPHI as single tracks with no signal (veto) in the gas or liquid radiator of the Cherenkov counter, and/or with an anomalously high ionization loss in the Time Projection Chamber (TPC). Kinks with both the mother chargino and the daughter charged decay particle reconstructed in the tracking devices were also searched for.

For $\Delta M$ larger than about 200 MeV/$c^2$, or even less if there are light sneutrinos which increase the leptonic decay width of the chargino, the lifetime tags are no longer effective. It was however observed that the signature of a photon with high transverse momentum radiated from the initial state (ISR), together with the few soft particles from the decay of the chargino, improves both the trigger efficiency of the signal and the rejection of the two-photon background.

Nearly mass-degenerate chargino and neutralino are possible in SUSY only if $M_2 \gg |\mu|$, that is $\tilde{\chi}_1^\pm$ and $\tilde{\chi}_1^0$ are both almost pure higgsinos, but this case does not concern AMSB, or if $M_2 \ll |\mu|$, that is $\tilde{\chi}_1^\pm$ and $\tilde{\chi}_1^0$ are both almost pure gauginos. To maximize the sensitivity to AMSB scenarios, the analysis of [13] was redone taking further into account additional scenarios with light sneutrinos. The search was done under the following hypotheses: heavy sneutrinos, that is $M_{\tilde{\nu}} \geq 500$ GeV/$c^2$; 100 GeV/$c^2$ sneutrinos; sneutrinos with mass between $M_{\tilde{\nu}}^+ + 1$ GeV/$c^2$ and 100 GeV/$c^2$; sneutrinos lighter than $M_{\tilde{\nu}}^+ + 1$ GeV/$c^2$. In the last case, where all charginos decay promptly, a stricter requirement on the extrapolation to the main event vertex of the charged particle tracks was required: the event was accepted only if at least two charged particles in it were compatible with coming from the primary $e^+e^-$ interaction vertex.

With respect to the scenario explored in [13], if there is a light sneutrino, either lighter than the chargino or not more than a couple of GeV/$c^2$ heavier, the leptonic width gets strongly enhanced, and the lifetime shortens. In that case, the efficiencies at the smallest $\Delta M$ explored with the ISR tag, turned out to be larger than the ones computed in [13] for the same $\Delta M$. On the other hand, as the lifetime shortens, the searches that explicitly rely on it (stable particles and kinks) lose efficiency.

Since there was no evidence of an excess in the number of events observed above the SM expectations, regions in the plane $(M_{\tilde{\chi}_1^\pm}, \Delta M)$ could be excluded at the 95% CL. Figure 1 shows the regions excluded by the different techniques used in the search for degenerate charginos. Figure 1a is the same plot with the gaugino exclusion as in [13], and includes AMSB scenarios when $M_{\tilde{\nu}} \geq 500$ GeV/$c^2$. In Fig. 1b the exclusion was computed for $M_{\tilde{\nu}} = 100$ GeV/$c^2$, and therefore it gives conservative predictions in case of heavier sneutrinos. Figure 1c was obtained with the minimal chargino cross-section (with respect to $M_{\tilde{\nu}}$) and with the lifetime corresponding to $M_{\tilde{\nu}} = M_{\tilde{\chi}_1^\pm} + 1$ GeV/$c^2$. This exclusion is conservative for all AMSB scenarios with $M_{\tilde{\chi}_1^\pm} + 1$ GeV/$c^2 < M_{\tilde{\nu}} < 100$ GeV/$c^2$, since as $M_{\tilde{\nu}}$ increases the s-t channels interference weakens and the cross-section gets larger; moreover, also the lifetime increases, thus improving the sensitivity of all searches for long-lived charginos. Finally, Fig. 1d was computed using the minimal chargino cross-section (again with respect to $M_{\tilde{\nu}}$) and for short lived charginos. It can be used to constrain AMSB scenarios with $M_{\tilde{\nu}} < M_{\tilde{\chi}_1^\pm} + 1$ GeV/$c^2$ (see also Sect. 4.3).

To compute these excluded regions, the different channels were combined using the multichannel Bayesian
4.3 Search for $\tilde{\chi}_1^\pm \rightarrow \tilde{\nu} t^\pm$ decays

If the sneutrino is lighter than the chargino, the chargino decays with practically 100% branching ratio into a sneutrino and a charged lepton. Since the upper limits on the chargino cross-section in the SUGRA scenario were obtained assuming the chargino decaying into $\chi_1^0 W^{\pm}$ [13], those limits cannot be translated directly into limits in the AMSB scenario. Hence, only the “leptonic” search for charginos described in [13] was used to explore the region with $\Delta M_\ell = M_{\tilde{\chi}_1^\pm} - M_\chi^0$ larger than 3 GeV/c².

The analysis selected events with low charged multiplicity and without any reconstructed isolated photon: events were discarded if they had more than five reconstructed charged particles and if there was a photon with more than 5 GeV, and isolated by more than 15 degrees from any other charged or neutral particle. After a preselection obtained with sequential cuts, the final selection was performed using likelihood ratio functions [16] $\mathcal{L}_R(\{x_i\})$ built as follows: for a set of variables $\{x_i\}$ (e.g. multiplicities, visible energy, acoplanarity, total transverse momentum, fraction of energy in the forward cone, etc.), the probability distribution functions of these variables were estimated by normalized frequency distributions for the signal (with a $\chi_1^0$ LSP) and the background samples. These probability distribution functions were denoted $f^S(x_i)$ for the signal, and $f^B(x_i)$ for the background events that passed the same selection criteria. Six likelihood ratio functions, one per $\Delta M_\ell$ region defined as in Table 1, were defined as

$$\mathcal{L}_R = \prod_{i=1}^n \frac{f^S(x_i)}{f^B(x_i)}.$$  \hspace{1cm} (5)

Events with $\mathcal{L}_R > \mathcal{L}_{R\text{CUT}}$ were selected as candidate signal events. The choice of variables and the value of $\mathcal{L}_{R\text{CUT}}$ were optimized using samples of simulated events, by minimizing the signal cross-section that was expected to be excluded at 95% CL in the absence of a signal. This procedure was repeated for every investigated centre-of-mass energy. Basically after the final selection, the remaining set of events consisted of low-multiplicity events with high acoplanarity and high missing energy.

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Additional text:

The effect of the systematics uncertainties on the signal efficiency and on the expected background content was taken into account according to [15].
Table 1. The number of events observed in data and the expected number of background events in the search for a pair of charginos both decaying into a sneutrino and a charged lepton, at the centre-of-mass energies collected by DELPHI in 1999 and 2000. The last column corresponds to the data collected in the year 2000 with the TPC not fully operational (at their mean centre-of-mass energy)

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Table 1 summarizes the number of events observed and expected, and the luminosities used at the different centre-of-mass energies. The data collected during the year 2000 with and without the TPC fully operational (see [13]) were treated as different channels in the analyses.

The efficiencies at the centre-of-mass energy of 208 GeV of the fully leptonic selection are plotted in Fig. 2a as function of the chargino and sneutrino masses. Since up to five visible charged particles were allowed and no leptonic identification was required, those efficiencies had only very little dependence on the flavour of the charged lepton in the final state. The efficiencies of Fig. 2a were computed using events simulated with three body $\tilde{\chi}_1^\pm \rightarrow l^\pm \ell \tilde{\nu}$ decays. It was however verified with samples of fully simulated events with the two body decay $\tilde{\chi}_1^\pm \rightarrow l^\pm \tilde{\nu}$ searched for in AMSB, that the efficiencies used in the analysis were never larger than the ones expected for the two body decays. This was expected, since the momentum of the visible charged particles is on average larger in the two body sample than in the three body one. In particular, the efficiencies are used are fully compatible with the true ones at large $\Delta M_{\tilde{g}}$, and they become up to one and a half times smaller when $\Delta M_{\tilde{g}}$ approaches 3 GeV/$c^2$. Therefore, the limits obtained are never overestimated, and possibly conservative at small $\Delta M_{\tilde{g}}$.

No significant excess was observed above the SM expectations. After having combined all channels with the multichannel Bayesian method of [14], Fig. 2b displays the 95% CL upper limit of the chargino cross-section at the reference centre-of-mass energy of 208 GeV, as function of the masses of the chargino and of the sneutrino, and assuming BR($\tilde{\chi}_1^\pm \rightarrow l^\pm \ell \tilde{\nu}$) = 1. If that exclusion is compared with the theoretical expectation of the same cross-section (in Fig. 2c the minimal expected $e^+e^- \rightarrow \tilde{\chi}_1^+ \tilde{\chi}_1^-$ cross-section is shown as function of $M_{\tilde{\chi}_1^+}$), a region in the plane ($M_{\tilde{\chi}_1^+}, M_{\tilde{\chi}_1^0}$) can be excluded at the same confidence level. Such excluded region is shown in Fig. 2d.

The exclusion when $0 < \Delta M_{\tilde{g}} < 3$ GeV/$c^2$, as obtained with the results of the search for nearly mass-degenerate charginos, can be derived from Fig. 1d, by simply substituting $\Delta M$ with $\Delta M_{\tilde{g}}$ in the ordinate. The same observation on the conservativeness of the limits obtained when the chargino decays into two bodies also holds for the search at $\Delta M_{\tilde{g}} < 3$ GeV/$c^2$, since the efficiencies are estimated from samples of three body decays. For $M_{\tilde{\chi}_1^+} < 55$ GeV/$c^2$, only the narrow band $0 < \Delta M_{\tilde{g}} < 200$ MeV/$c^2$ cannot be excluded.

If also the stau, or some other charged slepton, has a mass which is intermediate between the mass of the chargino and that of the sneutrino, Fig. 2b should be interpreted as the 95% CL upper limit of the chargino cross-section times its branching ratio into $l^\pm \ell \tilde{\nu}$. 

Table 1. The number of events observed in data and the expected number of background events in the search for a pair of charginos both decaying into a sneutrino and a charged lepton, at the centre-of-mass energies collected by DELPHI in 1999 and 2000. The last column corresponds to the data collected in the year 2000 with the TPC not fully operational (at their mean centre-of-mass energy)
Fig. 2. a Chargino pair production detection efficiencies (%) for the fully leptonic decay channel at $\sqrt{s}=208.2$ GeV in the $(M_{\tilde{\chi}^\pm_1}, M_{\tilde{\nu}})$ plane; a 100% branching ratio of $\tilde{\chi}^\pm_1 \rightarrow \tilde{\nu} l^\pm$ is assumed. b Equivalent excluded cross-section at the 95% CL (in pb) at 208.2 GeV. c Minimal expected $e^+ e^- \rightarrow \tilde{\chi}^+_1 \tilde{\chi}_1^-$ cross-section in AMSB, as function of the mass of the chargino. d Region excluded at the 95% CL in the plane $(M_{\tilde{\chi}^\pm_1}, M_{\tilde{\nu}})$ by the search described in the text. Sneutrinos lighter than 43 GeV/c$^2$ were already excluded at LEP1. The dotted lines in figures a and b bound the range of $\Delta M = M_{\tilde{\chi}^\pm_1} - M_{\tilde{\nu}}$ searched for by this channel.
4.4 Search for $e^+e^- \rightarrow \tilde{\chi}_1^0\tilde{\chi}_2^0$

Searches for $\tilde{\chi}_1^0\tilde{\chi}_2^0$ production with $\tilde{\chi}_2^0 \rightarrow q\bar{q}\tilde{\chi}_1^0$, $\tilde{\chi}_2^0 \rightarrow \mu^+\mu^-\tilde{\chi}_1^0$, $\tilde{\chi}_2^0 \rightarrow e^+e^-\tilde{\chi}_1^0$, $\tilde{\chi}_2^0 \rightarrow Z\tilde{\chi}_1^0$, and $\tilde{\chi}_2^0 \rightarrow \tau\tau$ decays have been presented in [13]. Limits for production cross-section times branching ratio to the corresponding final state ranged typically from 0.05 pb to 0.2 pb, depending primarily on the mass difference $M_{\tilde{\chi}_2^0} - M_{\tilde{\chi}_1^0}$.

Since in AMSB $M_1/M_2 \sim 2.8$, and $M_{\tilde{\chi}_1^0} \sim M_{\tilde{\chi}_1^\pm} \sim M_2$ and $M_{\tilde{\chi}_2^0} \sim M_1$, there is relatively little phase space available for the production of $\tilde{\chi}_1^0\tilde{\chi}_2^0$ at LEP energies. Only if $\tilde{\chi}_1^0$ is sufficiently light a $\tilde{\chi}_2^0$, which is almost three times as heavy as the $\tilde{\chi}_1^0$, can be produced in association, as $M_{\tilde{\chi}_2^0} + M_{\tilde{\chi}_1^0}$ must be below the centre-of-mass energy available in the $e^+e^-$ collision. In this case, the $\tilde{\chi}_2^0$ decays mainly to $\tilde{\chi}_1^0Z$ and $\tilde{\chi}_1^0W^\mp$ [9]. For the $\tilde{\chi}_2^0 \rightarrow \tilde{\chi}_1^0Z$ decay, the results of the neutralino searches presented in [13] can be directly used. Since in AMSB scenarios the chargino is nearly mass-degenerate with the neutralino, the decay $\tilde{\chi}_2^0 \rightarrow \tilde{\chi}_1^0W^\mp$, with $\tilde{\chi}_1^\pm \rightarrow \pi^\pm\tilde{\chi}_1^0$ and $W \rightarrow q\bar{q}'$, results in the same visible final state as $\tilde{\chi}_2^0 \rightarrow \tilde{\chi}_1^0q\bar{q}$. Also in this case, the limits on $\tilde{\chi}_1^0\tilde{\chi}_2^0$ production with the above final state presented in [13] can be used. On the other hand, when the $W$ decays leptonically, the visible objects in the final states are different from those of the standard search for neutralinos, because of the soft particles from the chargino decay, which can be relevant in a low-multiplicity environment.

A dedicated search would be needed, but is not considered in the present paper.

If there are sleptons with a mass between $M_{\tilde{\chi}_1^0}$ and $M_{\tilde{\chi}_2^0}$, cascade decays of $\tilde{\chi}_2^0$ can take place: $\tilde{\chi}_2^0 \rightarrow l\bar{l}$, $\tilde{\chi}_2^0 \rightarrow \tilde{\chi}_1^0l$. In this case there are two mass differences ($\Delta M_{\tilde{l}}$) characterizing the process: $M_{\tilde{\chi}_2^0} - M_{\tilde{l}}$ and $M_{\tilde{\chi}_2^0} - M_{\tilde{\chi}_1^0}$. It was verified that if $\tilde{l} = (\tilde{\mu}, \tilde{\tau})$ the results of the searches for $e^+e^- \rightarrow \tilde{\chi}_2^0\tilde{\chi}_1^0$, where $\tilde{\chi}_2^0 \rightarrow \mu^+\mu^-\tilde{\chi}_1^0$ or $\tilde{\chi}_2^0 \rightarrow e^+e^-\tilde{\chi}_1^0$, can be used, provided that from the $\Delta M_{\tilde{l}}$ definitions above the one giving the more conservative result is used in place of $M_{\tilde{\chi}_2^0} - M_{\tilde{\chi}_1^0}$.

The lightest stau, $\tilde{\tau}_1$, is typically the lightest charged slepton in AMSB. For $\tilde{\tau}_1$ as the intermediate slepton, the tau cascade search described in [13] was studied in a wider range of $M_{\tilde{\tau}_2} - M_{\tilde{\chi}_1^0}$. The tau cascade search is sensitive to $\tilde{\chi}_1^0\tilde{\chi}_2^0$ production with $\tilde{\chi}_2^0 \rightarrow \tilde{\tau}\tau$ and $\tilde{\tau} \rightarrow \tilde{\chi}_1^0\tau$, where the second $\tau$ produced has very low energy. At the preselection level, well reconstructed low-multiplicity events with missing energy, missing mass, and no more than two reconstructed jets were selected. In particular, the total visible energy including badly reconstructed tracks was required to be less than 140 GeV, the number of charged particles was required to be at least two and at most eight, and the number of neutral particles to be less than five. Two or more of the charged particles also had to satisfy stricter criteria on reconstruction and impact parameters. There was no evidence of excess above the SM expectations after the selection (see [13]). The resulting cross-section upper limits at the 95% CL are shown in Fig. 3.

![Fig. 3. Cross-section limits at the 95% CL for the $\tilde{\chi}_1^0\tilde{\chi}_2^0$ production when $\tilde{\chi}_2^0$ decays entirely to $\tilde{\tau}\tau$. The upper limits are shown for several ranges of $\Delta M = M_{\tilde{\tau}_2} - M_{\tilde{\chi}_1^0}$ in GeV/$c^2$. The widths of the bands are due to dependence of the limit on $\Delta M$ and to statistical fluctuations of the efficiency due to limited Monte Carlo statistics.](image)

4.5 Search for a charged slepton as the LSP

In a scan of the parameter space performed with ISAJET 7.63 [9] no points were obtained where a charged slepton is lighter than the $\tilde{\chi}_1^0$. However, the calculations in [4] still allow a small region in the space of the AMSB parameters with the $\tilde{\tau}_1$ being the LSP. In this case, if R-parity is conserved, the stau must be stable. The DELPHI results of the search for heavy stable charged particles in DELPHI can exclude a stable $\tilde{\tau}_1$ with mass below 96 GeV/$c^2$ at the 95% CL, even at the level of mixing that gives the lowest $\tilde{\tau}_1^+\tilde{\tau}_1^-$ production cross-section.

4.6 Search for cascades from sleptons

The decay $\tilde{l}^+ \rightarrow \tilde{\chi}_1^+\nu_l$ is practically undetectable, due to the softness of the visible decay products of the chargino. It accounts, however, for two thirds of the total decay width, if the chargino and the neutralino are the only SUSY particles lighter than the charged slepton. The only visible cascades originating from that slepton (in particular a stau, since it is expected to be the lightest) in AMSB are therefore:
In the case of sneutrino production, the decay $\tilde{\nu} \rightarrow \tilde{\chi}_1^{0} \nu$ is clearly invisible. On the other hand, $\tilde{\nu} \rightarrow \tilde{\chi}_1^{\pm} l^-$ is observable using techniques similar to those used in the usual searches for sleptons [13]. No optimization by means of a dedicated study of those cascades was attempted for the present paper.

### 4.7 Search for the SUSY Higgs boson

Since in the range of the AMSB parameters explored in this paper $M_A \gg M_Z$, the lightest supersymmetric neutral Higgs $h^0$ has the same couplings as the SM Higgs boson, and the limits obtained on the mass of the Higgs in the SM can be translated into the same lower limits on the mass of the $h^0$ in AMSB, provided that the decay branching fractions of the Higgs into supersymmetric particles are negligible.

If $M_A \gg M_Z$, the $h^0$ can be produced at LEP only in association with the $Z$ (higgsstrahlung), and with the same cross-section as in the SM. When there are SUSY particles lighter than $M_{h^0}/2$, decays of the $h^0$ into those particles are allowed. This is the case for AMSB, when there are light winos, sneutrinos or charged sleptons. Possible SUSY decays of the $h^0$ are:

- $h^0 \rightarrow \tilde{\chi}_1^{0} \tilde{\chi}_1^{0}, \tilde{\chi}_1^{\pm} \tilde{\chi}_1^{\mp}, \tilde{\nu} \tilde{\nu}$, all invisible or practically invisible in AMSB, apart from some possible cascades;
- $h^0 \rightarrow \tilde{\nu} \tilde{\nu}$, the visibility of which depends on the mass difference between the slepton and the LSP.

The DELPHI bound on the SM Higgs mass is $M_H > 114.1 \text{ GeV}/c^2$ at the 95% CL [18]. DELPHI measured also the upper limit on the production cross-section of an invisibly decaying Higgs boson [19]. This leads to exclude a Higgs boson with mass below 112.1 GeV/$c^2$, if it has a 100% branching ratio into invisible particles. [19] shows how the lower limit on the mass of the lightest supersymmetric Higgs boson depends on the branching fraction into invisible states, assuming that the production cross-section and all other decay modes are SM-like. That limit starts from 114.1 GeV/$c^2$ when $\text{BR}(h^0 \rightarrow \text{inv.}) = 0$, that is when the $h^0$ decays as the SM Higgs; it reaches a minimum of 111.8 GeV/$c^2$ when both visible and invisible decay modes are present simultaneously; and it goes up again to 112.1 GeV/$c^2$ when $\text{BR}(h^0 \rightarrow \text{inv.}) = 1$. The same limits on $M_{h^0}$ apply in AMSB, provided there are no visible SUSY decays with sizeable branching fractions.

### 5 Constraints on the AMSB spectrum

The negative results of the searches described in this paper were used to constrain the AMSB parameter space. To do so, the experimental exclusions measured were compared with the mass spectra produced by ISAJET 7.63 [9]. A scan over the AMSB parameters was carried out by varying them in the following ranges: $1 < m_{3/2} < 50 \text{ TeV}/c^2$; $0 < m_0 < 1000 \text{ GeV}/c^2$; $1.5 < \tan \beta < 35$; both positive and negative $\mu$. 900,000 SUSY points were generated by choosing at random the parameters within the bounds above. 500,000 of those points were generated with the mass of the top quark at 174.3 GeV/$c^2$, the others having been divided between $m_t = 169.2$ and 179.4 GeV/$c^2$, as explained in Sect. 3. A bigger density of points was allowed in the regions of the space of the parameters where the expected limits lied as well as in the regions where some structure was observed.

With the AMSB model as implemented in that version of ISAJET, only the negative results from the search for nearly mass-degenerate chargino and neutralino, the search for neutral SM-like and invisibly decaying Higgs, the search for charginos decaying into a sneutrino and a charged lepton, and the limit on the non-SM $Z$ width from LEP1 were used to constrain the model parameters. The other searches described in this paper were found to provide no additional constraints to the model. They have been listed all together as well, in order to allow tests of any deviations from the implementation of AMSB as coded in ISAJET.

The following Figs. 4, 5 and 6 refer to the scan done for the central value of $m_t$. Similar figures were obtained in

**DELPHI**

![Fig. 4. a physically allowed $m_0$ and $m_{3/2}$ parameters in AMSB, as obtained in a scan of the AMSB parameter space with ISAJET, as described in the text. b points remaining after applying the chargino and sneutrino mass bounds of LEP1. c set of points from the scan remaining after considering all the results of the searches described in this work.](image-url)
correspondence of the two other values of $m_t$ considered, and their outcomes are summarized in Table 2.

Figure 4a shows the points in the plane $(m_0, m_{3/2})$ generated with ISAJET. The region of the space with no points was not allowed, because one or more sparticles would be tachyonic. This implies a certain degree of correlation between $m_0$ and $m_{3/2}$, since by cutting away slices at low $m_{3/2}$ the value of the lowest admissible $m_0$ increases. Figure 4b shows the points that remain after the application of the model-independent bounds on the chargino and sneutrino masses obtained at LEP1. Finally, in Fig. 4c the points that remain after having applied all the results of the searches described in this paper are displayed.

Since the model prefers a light Higgs, most of the exclusion in the space of the AMSB parameters arises from the negative results of the searches for the SM and the invisibly decaying Higgs boson. The negative results of the other searches enlarged further the rejection, especially at low $m_{3/2}$ (chargino searches) and low $m_0$ (searches with sleptons). The effect of the search for the standard and invisible Higgs can be seen in Fig. 5. Figure 5a shows all the points generated with ISAJET in the plane $(M_{h^0}, \tan \beta)$. Figure 5b shows all the points remaining after the LEP1 chargino and sneutrino bounds, and the exclusions obtained with the searches for SUSY particles, but excluding the Higgs, at LEP2. Figure 5c shows the points surviving after the negative results of the SM and invisibly decaying Higgs searches in DELPHI. One can notice how the search for the Higgs boson and the search for the other SUSY particles at LEP are complementary in excluding certain regions in the space of the AMSB parameters. Figure 5d shows that, after applying the full set of results presented in this paper to constrain AMSB, no point with a mass of the lightest Higgs below the SM limit of 114.1 GeV/$c^2$ survived.

It is interesting to observe the impact of the searches for AMSB on some sparticle masses. Figure 6 shows the number of points generated by ISAJET and passing the three steps of selection as in Fig. 4, as a function of the mass of the lightest neutralino and of the lightest sneutrino. Neutralinos lighter than 66 GeV/$c^2$ and sneutrinos lighter than 95 GeV/$c^2$ are excluded in AMSB.

Table 2 summarizes the bounds on the AMSB parameters and on the mass of some sparticles obtained by applying the 95% CL exclusions from the searches described in the previous paragraphs to the ISAJET spectra. They are listed separately as function of the sign of $\mu$ and of the value of the mass of the top quark used in the simulation. Small shifts of those bounds are still possible, in principle, when applying the full next-to-leading order corrections to the model.
Table 2. Bounds on the AMSB parameters and on the sparticle masses, as a function of sign(μ), obtained by applying the 95% CL limits derived in the searches for AMSB scenarios. Given the small mass splitting, at the level of few hundred MeV/c², ξ is can be viewed both as ξ or ξ. ξ is the mass of the lightest sneutrino, always the tau sneutrino in the model. M_f refers to the lightest charged slepton, which is always the stau in AMSB. Within parenthesis are listed the same bounds obtained with m_t respectively below and above one standard deviation, as from [11], from the central value of 174.3 GeV/c²

<table>
<thead>
<tr>
<th>Parameter</th>
<th>μ &lt; 0</th>
<th>μ &gt; 0</th>
</tr>
</thead>
<tbody>
<tr>
<td>m₀</td>
<td>183 (211, 174) GeV/c²</td>
<td>156 (181, 147) GeV/c²</td>
</tr>
<tr>
<td>mₙ/2</td>
<td>26.3 (30.0, 24.5) TeV/c²</td>
<td>23.0 (26.1, 21.4) TeV/c²</td>
</tr>
<tr>
<td>tan β</td>
<td>&gt; 5.7 (7.0, 4.9)</td>
<td>&gt; 3.8 (4.6, 3.4)</td>
</tr>
<tr>
<td>M_ξ</td>
<td>&gt; 73 (83, 67) GeV/c²</td>
<td>&gt; 66 (74, 63) GeV/c²</td>
</tr>
<tr>
<td>M_ν</td>
<td>&gt; 114 (131, 104) GeV/c²</td>
<td>&gt; 95 (116, 85) GeV/c²</td>
</tr>
<tr>
<td>M_f</td>
<td>&gt; 75 (90, 70) GeV/c²</td>
<td>&gt; 68 (78, 66) GeV/c²</td>
</tr>
</tbody>
</table>

Given the bounds listed in Table 2, the possible AMSB explanation for a light sneutrino (M_0 ≤ 80 GeV/c²), which was suggested to cure some of the discrepancies in the fit of precision electroweak data [20], is likely to be ruled out by the results of this analysis.

6 Conclusions

The results of the searches performed using the data collected with the DELPHI detector at LEP, and relevant to explore AMSB scenarios, have been presented. An interpretation of the limits obtained in searches motivated by other SUSY breaking scenarios was used whenever appropriate. In addition, some of the searches were developed specifically to improve the sensitivity to AMSB. There is no evidence for a signal beyond the Standard Model, and limits are set on the sparticle production in the AMSB framework.

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