Determination of α_s using the next-to-leading-log approximation of QCD

DELPHI Collaboration

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Received 12 March 1993

Abstract. A new measurement of α_s is obtained from the distributions in thrust, heavy jet mass, energy-energy correlation and two recently introduced jet broadening variables following a method proposed by Catani, Trentadue, Turnock and Webber. This method includes the full calculation of $\mathscr{O}(\alpha_s^2)$ terms and leading and next-to-leading logarithms resummed to all orders of α_s . The analysis is based on data taken with the DELPHI detector at LEP during 1991. I its found that the inclusion of the resummed leading and next-to-leading logarithms reduces the scale dependence of α_s and allows an extension of the fit range towards the infrared limit of the kinematical range. The combined value for α_s obtained at the scale $\mu^2 = M_Z^2$ is:

 $\alpha_s(M_Z^2) = 0.123 \pm 0.006$.

1 Introduction

During the last two years accurate measurements of the running coupling constant, α_s , of quantum chromodynamics at e^+e^- colliders have been obtained from the analysis of event shape distributions measured in hadronic Z^0 decays [1-3]. In these publications, distributions in infrared and collinear safe observables are compared to QCD predictions in fixed order perturbation theory. The dominant uncertainty in the measurement of α_s results from the renormalization scale dependence of the coefficient of the second order term in α_s .

Recently a resummation of leading and next-to-leading logarithmic contributions (NLLA) has been performed to all orders of perturbation theory for the distributions in thrust, heavy jet masses and jet broadening variables, and for the back-to-back energy-energy correlation [4–7]. In consequence the uncertainty of α_s due to the renormalization scale is reduced. Also the quantitative comparison between data and theory can be extended towards the 2-jet region, where gluons are emitted close to the directions of the produced quarks (infrared limit) and where the statistics are high. For some of the distributions studied in this paper, the resummed expressions have been applied to LEP data [2, 8, 9]. In the following analysis α_s is determined using two methods. Method 1 concentrates on the 2-jet region where the cross-section can be reliably expressed as a power series in α_s containing only the leading and next-to-leading contributions of large logarithms. Values of α_s are determined from the distributions in thrust, heavy jet mass and jet broadening variables. Method 2 extends the comparison with theory into the region dominated by 3jet events. Here the resumed expression has to be matched with the full $\mathscr{O}(\alpha_s^2)$ expression for the different distributions. The corresponding α_s values, including the one from the analysis of the energy-energy correlation, are compared to the results of method 1.

In this paper Sect. 2 briefly describes the DELPHI detector while Sect. 3 introduces the relevant event shape variables and describes the data selection and corrections. In Sect. 4 the theoretical expressions used to determine α_s are evaluated. Section 5 describes the hadronization correction. Also the sources of different systematic uncertainties and fit results are discussed, and finally the procedure to obtain a combined result for α_s including the correlation of the individual results is presented.

2 The detector

A detailed description of the DELPHI apparatus has been presented in [10]. Here the components relevant for this analysis are briefly described.

The main part of the tracking system is a 2.7 m long time projection chamber (TPC) which measures the tracks of charged particles with a resolution of about 250 µm in the $R\phi$ -projection (transverse to the beam direction) and 0.9 mm along the z direction (beam direction). The space between the TPC and the beam pipe contains the inner detector (ID) and a silicon microstrip vertex detector (VD). Each 15° sector of the ID consists of a 24 wire jet chamber surrounded by a 5 layer proportional chamber. The vertex detector is built from three concentric shells of 24 silicon microstrip detector modules each 24 cm long. In the barrel region (polar angle θ relative to the beam axis between 43° and 137°) the quality of tracking is further improved by the outer detector containing 5 layers of drift tubes. Each layer measures the $R\phi$ -coordinate with a resolution of about 110 µm. Three layers also provide an approximate z measurement.

In the forward and backward regions (θ in the range 11-33° or 147-169°) two additional drift chamber systems improve the tracking. Forward chamber A (FCA) consists of three pairs of wire planes rotated by 120° with respect to each other, in order to resolve ambiguities internally. Forward chamber B (FCB) consists of 12 wire planes twice repeating the orientation of FCA and positioned directly in front of the forward electromagnetic calorimeter (FEMC).

Electromagnetic clusters are measured in the barrel region (θ between 43° and 137°) by a high density projection chamber (HPC), and in the forward region (θ in the range 10-36.5° or 143.5-170°) by the FEMC, a matrix of 4522 lead glass blocks. The HPC consists of 144 modules arranged in 6 rings around the beam axis. It is finely grained in 3 dimensions and thus allows a good two-shower separation and some particle identification from the shower shape.

3 Data analysis and corrections

For this analysis charged particles were used if they fulfilled the following criteria:

- momentum larger than $0.4 \, \text{GeV/c}$;
- over 30 cm measured track length;
- polar angle θ between 20° and 160°;

• projection of impact parameter relative to the fitted main vertex below 4 cm in the plane transverse to the beam direction, and below 10 cm along the beam direction.

Photon showers were included if they were detected in the HPC or the FEMC with an energy larger than 0.4 GeV and if their polar angle was between 20° and 160°.

Hadronic events were selected by requiring 5 or more charged particles, a total energy of all selected charged particles larger than 12% of the centre-of-mass energy, and larger than 3% in each hemisphere. To ensure that the event was well contained in the detector it was required that the angle between the sphericity axis and the beam axis exceeded 40°. A total of 177 925 events survived these selections for the 1991 data.

All distributions have been obtained from the analysis of charged and neutral particles except for the distribution of the back-to-back energy-energy correlation (EEC) where only charged particles were used. In order to correct the measured distributions for detector effects such as losses of charged and neutral particles, measurement errors and secondary interactions, events were generated with the JETSET 7.3 parton shower program [11] combined with the DYMU3 event generator [12] to simulate initial state photon radiation (QED), and followed by a detailed simulation of the detector (DELSIM) [13]. The simulated data were processed in the same way as the real data. For a quantity X the correction factor C_X was calculated bin-by-bin as:

$$C_{X} = \frac{\left(\frac{\mathrm{d}\sigma}{\mathrm{d}_{X}}\right)_{\text{generated}}^{\text{DELSIM}}}{\left(\frac{\mathrm{d}\sigma}{\mathrm{d}X}\right)_{\text{reconstructed}}^{\text{DELSIM}}} \cdot \frac{\left(\frac{\mathrm{d}\sigma}{\mathrm{d}X}\right)^{\text{no QED}}}{\left(\frac{\mathrm{d}\sigma}{\mathrm{d}X}\right)^{\text{QED}}}$$
(1)

where 'generated' includes all particles with a lifetime larger than 10^{-9} s without detector simulation, and 'reconstructed' indicates the full detector simulation and reconstruction of the simulated raw data.

In this analysis experimental distribution for six quantities are presented, namely for thrust T, two different definitions of normalized heavy jet mass squared ρ , two jet broadening measures B, B_W and back-to-back energyenergy correlation EEC. For these distributions leading and next-to-leading logarithms have been resummed to all orders of α_s in [4-7]. The definitions of these event shape variables are:

$$T = \max_{\mathbf{n}_{\text{thr}}} \frac{\sum_{i} |\mathbf{p}_{i} \cdot \mathbf{n}_{\text{thr}}|}{\sum_{i} |\mathbf{p}_{i}|}$$
(2)

$$\rho^{(T)} = \frac{1}{E_{\text{vis}}^2} \cdot \max\left[\left(\sum_{\mathbf{p}_i \cdot \mathbf{n}_{\text{thr}} > 0} p_i \right)^2, \left(\sum_{\mathbf{p}_i \cdot \mathbf{n}_{\text{thr}} < 0} p_i \right)^2 \right] \quad (3)$$

where *i* runs over all final state particles, \mathbf{n}_{thr} is the thrust axis, and E_{vis} the total energy of all visible particles with four-momentum p_i . In (3) charged particles are assumed to have the pion mass while neutrals are assumed to be massless.

Among all possible ways to divide the particle system into two groups *a* and *b* the one which minimizes the sum of the squared invariant masses $M_a^2 + M_b^2$ was selected in order to get the alternative jet mass $\rho^{(M)}$ [14]:

$$\rho^{(M)} = \frac{1}{E_{\text{vis}}^2} \cdot \max(M_a^2, M_b^2).$$
(4)

In [7] two new e^+e^- event shape variables were introduced which measure the jet broadening by summing up the transverse momenta of the final state particles relative to the thrust axis. The total jet broadening *B* and wide jet broadening B_W are defined as follows:

$$B = B_+ + B_- \tag{5}$$

$$B_W = \max\left(B_+, B_-\right) \tag{6}$$

with

$$B_{\pm} = \frac{\sum_{\substack{\pm \mathbf{p}_i \cdot \mathbf{n}_{\text{thr}} > 0}} |\mathbf{p}_i \times \mathbf{n}_{\text{thr}}|}{2 \sum_i |\mathbf{p}_i|}$$
(7)

where *i* again runs over all final state particles.

The back-to-back energy-energy correlation is defined from the distribution of angles χ between all particle pairs in an event weighted by their energies:

$$EEC(\chi) = \frac{1}{N} \frac{1}{\Delta \chi} \sum_{\text{events}}^{N} \sum_{i,j}^{N \text{particles}} \sum_{i,j}^{N \text{particles}} \chi + \frac{E_i E_j}{E_{\text{vis}}^2} \int_{\chi - \frac{\Delta \chi}{2}}^{\chi + \frac{\Delta \chi}{2}} \delta(\chi - \chi_{ij}) \, \mathrm{d}\chi \tag{8}$$

(17)

where χ is taken larger than 90° and $\Delta \chi$ is the bin width of the histogram.

4 OCD predictions in NLLA

Pure second order QCD predictions can describe the distribution of an infrared and collinear safe shape variable only in a limited kinematic region dominated by the 3jet rate, where higher order effects are negligible. On the other hand in the 2-jet region higher order terms grow in the case of exponentiation [15] like $\ln^{n+1} y \alpha_s^n$ as the shape variable y is close to its infrared limit $y \rightarrow 0$. Therefore in this region any fixed order expansion of the crosssection must fail. To extend the range towards the infrared limit it is essential to calculate at least the leading higher order terms. The expansion of the integrated crosssection

$$R(\tilde{y}, \alpha_{s}) = \frac{1}{\sigma_{tot}} \sigma(y < \tilde{y})$$
(9)

at the scale $Q^2 \equiv s$ can be written in the form [4-7]:

$$cR(y,\alpha_{s}(Q^{2})) = (1 + C_{1}\alpha_{s}(Q^{2}) + C_{2}\alpha_{s}^{2}(Q^{2}) + ...) \cdot \Sigma(L,\alpha_{s}(Q^{2})) + F_{1}(y)\alpha_{s}(Q^{2}) + F_{2}(y)\alpha_{s}^{2}(Q^{2}) + ...(10)$$
with

with

$$L = \ln y \tag{11}$$

$$c = \begin{cases} 1: & T, \rho^{(T)}, \rho^{(M)}, B, B_W \\ 2: & \text{back-to-back EEC} \end{cases}$$
(12)

where the C_i are constant and the $F_i(y)$ vanish in the infrared limit $y \rightarrow 0$. Here y stands for (1-T), $\rho^{(T)}$, $\rho^{(M)}$, B, B_W or $(1 + \cos \chi)/2$, respectively. All logarithmic divergencies can be included in the function $\Sigma(L, \alpha_s(Q^2))$. In the case of exponentiation which holds for thrust, heavy jet masses, jet broadening variables and back-to-back energy-energy correlation, the logarithm of the function Σ can be written in the form:

$$\ln (\Sigma (L, \alpha_{s})) = (G_{12}L^{2} + G_{11}L)\alpha_{s}$$

$$+ (G_{23}L^{3} + G_{22}L^{2} + G_{21}L)\alpha_{s}^{2}$$

$$+ (G_{34}L^{4} + G_{33}L^{3} + ...)\alpha_{s}^{3}$$

$$+ ...$$
(13)

Once exponentiation is established the leading and nextto-leading terms, denoted in (13) as LL and NLL, can be resummed to all orders of α_s . Logarithms weaker than next-to-leading, such as the $(G_{21}L)\alpha_s^2$ term, are called subleading. At present subleading terms higher than $\mathscr{O}(\alpha_s^2)$ remain uncalculated and have to be estimated or neglected. A transition from the scale Q^2 to a scale μ^2 induces a $f = \mu^2/Q^2$ dependence of the next-to-leading terms, i.e. $\ln \Sigma$ explicitly depends on f.

Apart from the combination of the second order calculation and the resummed logarithms as suggested in (10), alternative matching schemes have been proposed [8, 16], which differ in terms of the order $\mathscr{O}(\alpha_s^3 \ln^2 y)$. If the first and second order coefficients A and B, which can be taken from reference [14] or computed by using the EVENT program [14, 17], are defined through

$$cR(y,\alpha_s) = 1 + A(y)\alpha_s + B(y)\alpha_s^2$$
(14)

and the functions g_1 and g_2 as

$$g_1(L) = G_{12}L^2 + G_{11}L \tag{15}$$

$$g_2(L) = G_{23}L^3 + G_{22}L^2 + G_{21}L$$
(16)

the following matching schemes can be defined:

 $+H_2(y)\alpha_s^2$

In *R*-matching scheme. This scheme follows from [4, 5]:

 $\ln cR(y,\alpha_s) = \ln \left(\Sigma(L,\alpha_s) \right) + H_1(y)\alpha_s$

with

$$H_1(y) = A(y) - g_1(L)$$
(18)

$$H_2(y) = B(y) - \frac{1}{2}A^2(y) - g_2(L).$$
(19)

 $R-G_{21}$ -matching scheme. This scheme follows from (10) and is suggested in [6]:

$$cR(y,\alpha_{s}) = (1 + C_{1}\alpha_{s} + C_{2}\alpha_{s}^{2})\Sigma(L,\alpha_{s})$$

$$+F_{1}(y)\alpha_{s} + F_{2}(y)\alpha_{s}^{2}$$
(20)
with

with

$$F_1(y) = A(y) - g_1(L) - C_1$$
(21)

$$F_{2}(y) = B(y) - \frac{1}{2}g_{1}^{2}(L) - g_{2}(L) - C_{1}g_{1}(L) - C_{2}$$
(22)

where the coefficient G_{21} is known from the full second order calculation [14, 18].

R-matching scheme. This scheme also follows from (10), but now with g_2 and $\ln \Sigma$ in NLLA only, i.e. without the $G_{21}L$ term.

In this analysis the ambiguity introduced by these different matching schemes is used for evaluating one source of theoretical uncertainties. From a theoretical point of view the $\ln R$ - and R- G_{21} -schemes are preferred, since in both schemes all known logarithms are exponentiated, while the *R*-matching suffers from the fact that the known logarithmic term $G_{21}L$ is only included in second order and not exponentiated. This leads to large differences between the $\ln R$ - or R- G_{21} -scheme and the R-scheme if this term is large. Nevertheless the R-scheme can be used in a restricted fit range to estimate the influence of uncalculated terms. This is discussed in more detail in the next section.

When combining second order theory with resummed logarithms one has to take into account that the resummed terms do not vanish at the upper kinematic boundary. Therefore the resummed logarithms are redefined in the following form [16]:

$$L = \ln(1/y - 1/y_{\max} + 1).$$
(23)

Here y_{max} is the upper kinematic boundary for each variable and is listed in Table 7.

As a consequence of the explicit inclusion of higher order terms in the theoretical prediction a reduced scale dependence is expected. The small scales found in former pure second order α_s measurements [2, 3], which were necessary to compensate unknown higher order terms, are not needed in the resummed calculation and are even forbidden, since such small scales introduce additional terms of the type $\ln^n f$ to all orders of α_s . This would lead to some double counting of the higher order terms.

5 Confrontation of QCD in NLLA and data

Before theoretical expressions describing parton distributions can be compared with the experimental data, corrections must be made for hadronization effects, i.e. effects resulting from the transition of the parton state into the observable hadronic state. For the global event shape variables, thrust, jet broadening and heavy jet masses, it is assumed that hadronization effects can be described by a correlation matrix C which connects the parton state with the hadronic final state:

$$\frac{\Delta \sigma}{\Delta y_i}\Big|_{\text{Hadron}} = \sum_j C_{ij} \frac{\Delta \sigma}{\Delta y_i}\Big|_{\text{Parton}}.$$
(24)

In the case of the back-to-back energy-energy correlation, which is defined for each pair of charged particles, had-ronization effects are described by a linear bin-by-bin correction vector C_i :

$$\frac{\Delta R(\chi_i)}{\Delta \chi_i}\Big|_{\text{Hadron}} = C_i \frac{\Delta R(\chi_i)}{\Delta \chi_i}\Big|_{\text{Parton}}.$$
(25)

These corrections were determined using 1 000 000 Monte Carlo events produced with JETSET 7.3 tuned to the DELPHI data [19]. In addition to this Monte Carlo sample, different tunings and models were used for the hadronization correction yielding an estimate of the systematic uncertainty of this correction, as detailed later.

For the confrontation of QCD with data and the determination of α_s two approaches have been used:

1. Following the suggestion of [7, 20] to consider two distinct theories, each applicable in certain kinematic regions (namely the resummed leading and next-to-leading logarithms (NLLA) on one side, and pure $\mathscr{O}(\alpha_s^2)$ theory on the other side), α_s is extracted from one measured bin in the extreme 2-jet region, where y is small, using pure NLLA without combination with second order theory. Figure 1a shows the ratio ω of the resummed logarithms (first two columns of (13), denoted as $\ln \Sigma^{(NLLA)}$ and the non-exponentiating second order contributions:

$$\omega = \frac{\ln \Sigma^{(\text{NLLA})}}{H_1 \alpha_{\text{s}} + H_2 \alpha_{\text{s}}^2}.$$
(26)

In the extreme 2-jet region where the ratio ω becomes large, the theory should be completely dominated by the resummed logarithms signalling the reliability of this approach. This method, which will be denoted as *method* 1, is complementary to pure second order α_s determinations using data in the 3-jet region. It offers the possibility of comparing a theory which is known to all orders of α_s in NLLA with the data. However, this approach is not applicable to the back-to-back energy-energy correlation due to the fact that here the ratio ω (Fig. 2a) does not



Fig. 1. a Ratio of the resummed leading and next-to-leading logarithms to $H_1 \alpha_s + H_2 \alpha_s^2$ of (18) and (19) versus 1-T. For low values of 1-T, where this ratio becomes large, the theory is dominated by resummed logarithms. **b** Ratio of the next-toleading logarithms to the leading logarithms. If this ratio is small NLLA should be reliable. **c** Ratio of the only known subleading logarithm $G_{21} \ln y$ and $G_{22} \ln^2 y$. If this ratio is small one expects a small matching scheme ambiguity



Fig. 3. Upper plot: Measured thrust distribution corrected for acceptance and initial state radiation. The histogram presents the result of a fit to the data of the combined theory with ln R-matching scheme at $\mu^2 = M_Z^2$ as described in the text. Middle plot: Bin-bybin detector correction including effects due to initial state radiation. Lower plot: Size of the hadronization correction. The width of the band indicates the uncertainty of the correction

become sufficiently large in the accessible range, which is limited towards small y-values by the pole in the resummed next-to-leading logarithms as visible in Fig. 2b [6].

to-back energy-energy correlation



Fig 4. As Fig. 3 but for the heavy jet mass (thrust definition)

2. While the first method aims to measure α_s to all orders in NLLA, the second method tests a combined NLLA and $\mathscr{O}(\alpha_s^2)$ theory over a wide kinematical range including the 3-jet region. Therefore expressions (24-25) are confronted with the experimental distributions by means of a least square fit supplying a measurement of $\Lambda_{\overline{MS}}$ which can be translated into $\alpha_s(M_Z^2)$. For the fit only statistical errors are considered. Figures 3 to 8 show the



Fig. 5. As Fig. 3 but for the heavy jet mass (mass definition)



Fig. 6. As Fig. 3 but for the total jet broadening variable



Fig. 7. As Fig. 3 but for the wide jet broadening variable



Fig. 8. As Fig. 3 but for the back-to-back energy-energy correlation EEC

hadron data compared with the fit result of the ln *R*-matching scheme at the renormalization scale $\mu^2 = Q^2 \equiv s$. The fit range is chosen in such a way that:

• Acceptance corrections are below about 20% and hadronization corrections below about 40%.

• One keeps away from the pole of the ratio of the nextto-leading logarithms and the leading logarithms (Fig. 1b and 2b) at small y values. Otherwise subleading terms cannot be neglected.

• The data can be well described by the theoretical prediction.

These criteria lead to the following fit ranges

(1 - T)	:[0.06,	0.30]		
$\rho^{(T)}$:	[0.03,	0.24]		
$ ho^{(M)}$:	[0.02,	0.15]		(27)
B :]	0.06,	0.24]		(27)
B_W :	[0.04,	0.20]		
$\chi_{\rm EEC}$:	[1	04.4°, 1	62.0°].		

For all variables the fit ranges have been extended towards the infrared limit in comparison to the more restricted fit ranges used for the determination of α_s in $\mathscr{O}(\alpha_s^2)$ [3]. Below the lower limit of the fit range, hadronization corrections increase strongly for 1 - T, $\rho^{(T)}$, $\rho^{(M)}$, B and B_W . For the R-scheme, which is used in this analysis only to estimate the theoretical uncertainty, a fit range restricted to the 3-jet region is used. This is necessary due to the one logarithmic divergent term $G_{21}L$, which is not exponentiated in the R-scheme and so leads to an unphysical divergency of the predicted cross-section in the 2-jet limit. The size of this term can be seen from Figs. 1c and 2c, where the ratio $G_{21} \ln y/G_{22} \ln^2 y$ is plot-

 Table 1. Thrust distribution corrected for detector acceptance and initial state photon radiation

Т	$\frac{1}{\sigma_{\rm tot}} \frac{\Delta \sigma}{\Delta T} \pm ({\rm stat}) \pm ({\rm exp})$	Т	$\frac{1}{\sigma_{\rm tot}} \frac{\Delta \sigma}{\Delta T} \pm ({\rm stat}) \pm ({\rm exp})$
0.605	$0.012 \pm 0.007 \pm 0.007$	0.805	$0.77 \pm 0.04 \pm 0.02$
0.615	$0.006 \pm 0.003 \pm 0.003$	0.815	$0.89 \pm 0.04 \pm 0.04$
0.625	$0.010 \pm 0.004 \pm 0.004$	0.825	$1.07 \pm 0.04 \pm 0.03$
0.635	$0.021 \pm 0.006 \pm 0.007$	0.835	$1.13 \pm 0.04 \pm 0.05$
0.645	$0.07 \pm 0.01 \pm 0.02$	0.845	$1.32 \pm 0.05 \pm 0.03$
0.655	$0.07 \pm 0.01 \pm 0.03$	0.855	$1.42 \pm 0.05 \pm 0.03$
0.665	$0.10 \pm 0.01 \pm 0.01$	0.865	$1.71 \pm 0.06 \pm 0.05$
0.675	$0.12 \pm 0.01 \pm 0.01$	0.875	$1.92 \pm 0.06 \pm 0.03$
0.685	$0.15 \pm 0.02 \pm 0.02$	0.885	$2.28 \pm 0.06 \pm 0.04$
0.695	$0.18 \pm 0.02 \pm 0.02$	0.895	$2.71 \pm 0.07 \pm 0.11$
0.705	$0.23 \pm 0.02 \pm 0.01$	0.905	$2.99 \pm 0.07 \pm 0.06$
0.715	$0.27 \pm 0.02 \pm 0.03$	0.915	$3.90 \pm 0.08 \pm 0.13$
0.725	$0.33 \pm 0.02 \pm 0.03$	0.925	$4.62 \pm 0.09 \pm 0.11$
0.735	$0.36 \pm 0.03 \pm 0.02$	0.935	$5.7 \pm 0.1 \pm 0.1$
0.745	$0.40 \pm 0.03 \pm 0.03$	0.945	$7.4 \pm 0.1 \pm 0.2$
0.755	$0.48 \pm 0.03 \pm 0.02$	0.955	$9.7 \pm 0.1 \pm 0.4$
0.765	$0.51 \pm 0.03 \pm 0.02$	0.965	$13.6 \pm 0.2 \pm 0.2$
0.775	$0.55 \pm 0.03 \pm 0.03$	0.975	$16.2 \pm 0.2 \pm 0.8$
0.785	$0.62 \pm 0.03 \pm 0.03$	0.985	$10.1 \pm 0.1 \pm 0.5$
0.795	$0.76\ \pm 0.04\ \pm 0.03$	0.995	$1.40 \pm 0.04 \pm 0.14$

 Table 2. Heavy jet mass distribution (thrust definition) corrected for detector acceptance and initial state photon radiation

$\rho^{(T)}$	$\frac{1}{\sigma_{\text{tot}}} \frac{\Delta \sigma}{\Delta \rho^{(T)}} \pm (\text{stat}) \\ \pm (\text{exp})$	$\rho^{(T)}$	$\frac{1}{\sigma_{\text{tot}}} \frac{\Delta \sigma}{\Delta \rho^{(T)}} \pm (\text{stat}) \\ \pm (\exp)$
0.005	$1.84 \pm 0.04 \pm 0.58$	0.205	$0.47 \pm 0.03 \pm 0.04$
0.015	$15.2 \pm 0.1 \pm 1.3$	0.215	$0.39 \pm 0.03 \pm 0.02$
0.025	$20.2 \pm 0.2 \pm 0.5$	0.225	$0.34 \pm 0.03 \pm 0.03$
0.035	$14.1 \pm 0.2 \pm 0.8$	0.235	$0.29 \pm 0.02 \pm 0.02$
0.045	$9.9 \pm 0.1 \pm 0.5$	0.245	$0.23 \pm 0.02 \pm 0.02$
0.055	$7.1 \pm 0.1 \pm 0.4$	0.255	$0.18 \pm 0.02 \pm 0.02$
0.065	5.5 ± 0.1 ± 0.3	0.265	$0.166 \pm 0.017 \pm 0.006$
0.075	$4.30 \pm 0.09 \pm 0.22$	0.275	$0.13 \pm 0.01 \pm 0.01$
0.085	$3.47 \pm 0.08 \pm 0.17$	0.285	$0.088 \pm 0.012 \pm 0.006$
0.095	$2.78 \pm 0.07 \pm 0.16$	0.295	$0.062 \pm 0.009 \pm 0.003$
0.105	$2.30 \pm 0.07 \pm 0.12$	0.305	$0.048 \pm 0.008 \pm 0.012$
0.115	$1.99 \pm 0.06 \pm 0.09$	0.315	$0.035 \pm 0.007 \pm 0.005$
0.125	$1.69 \pm 0.06 \pm 0.05$	0.325	$0.024 \pm 0.006 \pm 0.007$
0.135	$1.37 \pm 0.05 \pm 0.05$	0.335	$0.022 \pm 0.006 \pm 0.003$
0.145	$1.18 \pm 0.05 \pm 0.07$	0.345	$0.011 \pm 0.003 \pm 0.002$
0.155	$1.05 \pm 0.05 \pm 0.06$	0.355	$0.007 \pm 0.003 \pm 0.003$
0.165	$0.89 \pm 0.04 \pm 0.10$	0.365	$0.006 \pm 0.003 \pm 0.001$
0.175	$0.77 \pm 0.04 \pm 0.06$	0.375	$0.002 \pm 0.002 \pm 0.002$
0.185	$0.67 \pm 0.04 \pm 0.02$	0.385	$0.002 \pm 0.002 \pm 0.001$
0.195	$0.54 \pm 0.03 \pm 0.03$	0.395	$0.0014 \pm 0.0015 \pm 0.0007$

 Table 3. Heavy jet mass distribution (mass definition) corrected for detector acceptance and initial state photon radiation

ρ ^(M)	$\frac{1}{\sigma_{\text{tot}}} \frac{\Delta \sigma}{\Delta \rho^{(M)}} \pm (\text{stat}) \\ \pm (\exp)$	ρ ^(M)	$\frac{1}{\sigma_{\text{tot}}} \frac{\Delta \sigma}{\Delta \rho^{(M)}} \pm (\text{stat}) \\ \pm (\exp)$
0.005	$1.87 \pm 0.05 \pm 0.58$	0.155	$1.11 \pm 0.05 \pm 0.10$
0.015	$15.5 \pm 0.2 \pm 1.4$	0.165	$0.86 \pm 0.04 \pm 0.06$
0.025	$20.6 \pm 0.2 \pm 0.7$	0.175	$0.64 \pm 0.03 \pm 0.03$
0.035	$14.4 \pm 0.2 \pm 0.9$	0.185	$0.56 \pm 0.03 \pm 0.04$
0.045	$10.0 \pm 0.1 \pm 0.6$	0.195	$0.41 \pm 0.03 \pm 0.03$
0.055	$7.2 \pm 0.1 \pm 0.4$	0.205	$0.35 \pm 0.03 \pm 0.03$
0.065	$5.5 \pm 0.1 \pm 0.2$	0.215	$0.23 \pm 0.02 \pm 0.02$
0.075	$4.34 \pm 0.09 \pm 0.29$	0.225	$0.20 \pm 0.02 \pm 0.02$
0.085	$3.54 \pm 0.08 \pm 0.20$	0.235	$0.105 \pm 0.014 \pm 0.009$
0.095	$2.90 \pm 0.07 \pm 0.12$	0.245	$0.044 \pm 0.008 \pm 0.015$
0.105	$2.40 \pm 0.07 \pm 0.12$	0.255	$0.034 \pm 0.009 \pm 0.003$
0.115	$2.09 \pm 0.06 \pm 0.08$	0.265	$0.008 \pm 0.003 \pm 0.006$
0.125	$1.70 \pm 0.06 \pm 0.12$	0.275	$0.003 \pm 0.002 \pm 0.002$
0.135	$1.47 \pm 0.05 \pm 0.07$	0.285	$0.004 \pm 0.004 \pm 0.002$
0.145	$1.26 \pm 0.05 \pm 0.07$		

ted for thrust and for back-to-back energy-energy correlation. This ratio is one order of magnitude larger for EEC than for thrust, indicating the large matching scheme ambiguity of the EEC.

The data can be described well by the combined theory over a wide kinematic region. Note that the value of χ^2/NDF is evaluated from statistical errors only. These are very small, in particular in the case of the EEC.

5.1 Systematic uncertainties

To estimate the systematic error of α_s , three sources of uncertainties are investigated:

 Table 4. Total jet broadening distribution corrected for detector acceptance and initial state photon radiation

B	$\frac{1}{\sigma_{\rm tot}} \frac{\Delta \sigma}{\Delta B} \pm ({\rm stat}) \pm ({\rm exp})$	В	$\frac{1}{\sigma_{\rm tot}} \frac{\Delta \sigma}{\Delta B} \pm ({\rm stat}) \pm ({\rm exp})$
0.015 0.025 0.035 0.045 0.055 0.065	$\begin{array}{c} 0.04 \pm 0.01 \pm 0.02 \\ 0.30 \pm 0.02 \pm 0.09 \\ 1.95 \pm 0.06 \pm 0.16 \\ 5.66 \pm 0.09 \pm 0.07 \\ 9.4 \pm 0.1 \pm 0.3 \\ 10.6 \pm 0.1 \pm 0.2 \\ 10.0 \pm 0.1 \pm 0.1 \\ \end{array}$	0.165 0.175 0.185 0.195 0.205 0.215	$\begin{array}{c} 2.53 \pm 0.07 \pm 0.05 \\ 2.24 \pm 0.06 \pm 0.07 \\ 2.01 \pm 0.06 \pm 0.05 \\ 1.79 \pm 0.06 \pm 0.06 \\ 1.60 \pm 0.05 \pm 0.04 \\ 1.41 \pm 0.05 \pm 0.07 \\ 1.21 \pm 0.05 \pm 0.06 \end{array}$
0.075 0.085 0.095 0.105 0.115 0.125 0.125 0.135 0.145 0.155	$\begin{array}{c} 10.0 \pm 0.1 \pm 0.1 \\ 8.2 \pm 0.1 \pm 0.2 \\ 7.1 \pm 0.1 \pm 0.1 \\ 5.86 \pm 0.10 \pm 0.08 \\ 5.32 \pm 0.10 \pm 0.13 \\ 4.49 \pm 0.09 \pm 0.07 \\ 3.88 \pm 0.08 \pm 0.11 \\ 3.34 \pm 0.08 \pm 0.08 \\ 3.07 \pm 0.07 \pm 0.05 \end{array}$	0.223 0.235 0.245 0.255 0.265 0.275 0.285 0.285 0.295	$\begin{array}{c} 1.21 \pm 0.03 \pm 0.06 \\ 1.03 \pm 0.04 \pm 0.03 \\ 0.90 \pm 0.04 \pm 0.03 \\ 0.79 \pm 0.04 \pm 0.03 \\ 0.65 \pm 0.03 \pm 0.01 \\ 0.61 \pm 0.03 \pm 0.06 \\ 0.50 \pm 0.03 \pm 0.03 \\ 0.40 \pm 0.03 \pm 0.02 \end{array}$

 Table 5. Wide jet broadening distribution corrected for detector acceptance and initial state photon radiation

B _W	$\frac{1}{\sigma_{\rm tot}} \frac{\Delta \sigma}{\Delta B_W} \pm ({\rm stat})$	B _W	$\frac{1}{\sigma_{\rm tot}} \frac{\Delta \sigma}{\Delta B_W} \pm ({\rm stat})$
	\pm (exp)		$\pm(\exp)$
0.005	$0.017 \pm 0.007 \pm 0.013$	0.155	$1.77 \pm 0.06 \pm 0.06$
0.015	$0.88 \pm 0.04 \pm 0.12$	0.165	$1.47 \pm 0.05 \pm 0.04$
0.025	$8.9 \pm 0.1 \pm 0.3$	0.175	$1.28 \pm 0.05 \pm 0.03$
0.035	$15.9 \pm 0.2 \pm 0.3$	0.185	$1.10 \pm 0.04 \pm 0.04$
0.045	$13.7 \pm 0.2 \pm 0.3$	0.195	$0.87 \pm 0.04 \pm 0.07$
0.055	$10.3 \pm 0.1 \pm 0.2$	0.205	$0.69 \pm 0.03 \pm 0.03$
0.065	$8.3 \pm 0.1 \pm 0.1$	0.215	$0.61 \pm 0.03 \pm 0.04$
0.075	$6.65 \pm 0.11 \pm 0.08$	0.225	$0.49 \pm 0.03 \pm 0.02$
0.085	$5.51 \pm 0.10 \pm 0.07$	0.235	$0.34 \pm 0.02 \pm 0.02$
0.095	$4.65 \pm 0.09 \pm 0.09$	0.245	$0.25 \pm 0.02 \pm 0.03$
0.105	$3.91 \pm 0.08 \pm 0.07$	0.255	$0.16 \pm 0.02 \pm 0.01$
0.115	$3.36 \pm 0.08 \pm 0.05$	0.265	$0.11 \pm 0.01 \pm 0.01$
0.125	$2.80 \pm 0.07 \pm 0.06$	0.275	$0.043 \pm 0.007 \pm 0.011$
0.135	$2.34 \pm 0.06 \pm 0.03$	0.285	$0.018 \pm 0.005 \pm 0.005$
0.145	$2.02 \pm 0.06 \pm 0.08$	0.295	$0.009 \pm 0.004 \pm 0.002$

1 Experimental uncertainty. Several data samples with different selections were used to calculate the acceptance corrections and to estimate all other experimental uncertainties. In addition an analysis using only charged particles was performed with events selected to be fully contained in the barrel part of DELPHI. The bin-by-bin systematic experimental errors are quoted in Tables 1 to 6.

2 Hadronization correction. In addition to the JETSET 7.3 Monte Carlo sample, yielding the central value of the analysis, the HERWIG 5.4 and ARIADNE 3.1 models tuned to LEP data [21] were used to evaluate the hadronization correction. All three models differ in parton state generation. Although JETSET and HERWIG both follow the parton shower model, they differ in some details:

• JETSET includes the full $\mathscr{O}(\alpha_s)$ matrix element for hard gluon radiation,

 Table 6. Distribution of the back-to-back energy-energy correlation

 corrected for detector acceptance and initial state photon radiation

ίεεc	$EEC(\chi_{EEC}) \pm (stat) \pm (exp)$	
91.8	$0.0785 \pm 0.0007 \pm 0.0020$	
95.4	$0.0800 \pm 0.0007 \pm 0.0015$	
99.0	$0.0814 \pm 0.0008 \pm 0.0015$	
102.6	$0.0839 \pm 0.0008 \pm 0.0010$	
106.2	$0.0863 \pm 0.0008 \pm 0.0018$	
109.8	$0.0899 \pm 0.0008 \pm 0.0009$	
113.4	$0.0956 \pm 0.0009 \pm 0.0012$	
117.0	$0.1001 \pm 0.0009 \pm 0.0017$	
120.6	$0.1061 \pm 0.0009 \pm 0.0016$	
124.2	$0.115 \pm 0.001 \pm 0.002$	
127.8	$0.124 \pm 0.001 \pm 0.001$	
131.4	$0.137 \pm 0.001 \pm 0.002$	
135.0	$0.152 \pm 0.001 \pm 0.001$	
138.6	$0.169 \pm 0.001 \pm 0.002$	
142.2	$0.194 \pm 0.001 \pm 0.003$	
145.8	$0.225 \pm 0.001 \pm 0.003$	
149.4	$0.264 \pm 0.002 \pm 0.004$	
153.0	$0.317 \pm 0.002 \pm 0.004$	
156.6	$0.390 \pm 0.002 \pm 0.004$	
160.2	$0.492 \pm 0.003 \pm 0.004$	
163.8	$0.632 \pm 0.003 \pm 0.008$	
167.4	$0.832 \pm 0.004 \pm 0.012$	
171.0	$1.086 \pm 0.005 \pm 0.017$	
174.6	$1.269 \pm 0.007 \pm 0.012$	
178.2	$0.750 \pm 0.006 \pm 0.051$	

• HERWIG takes into account interference phenomena within the shower to full leading order.

While JETSET and HERWIG formulate the QCD shower in terms of partons, ARIADNE used the colour dipole formalism. For fragmentation JETSET and ARIADNE both use the JETSET string fragmentation, while HER-WIG incorporates cluster fragmentation.

To estimate the uncertainty originating from the parameter tuning, two alternative tunings of JETSET, performed by the DELPHI collaboration, were used in addition. Furthermore the parton virtuality $Q_0 = 1$ GeV which limits the shower evolution in JETSET, was varied between $Q_0 = 0.2$ and 5.0 GeV. The systematic hadronization error is then estimated as the variance of the fitted α_s values obtained by using all hadronization corrections as mentioned above.

3 Theoretical uncertainties. To estimate the theoretical uncertainties, fits at different values of μ^2/Q^2 ranging from 0.5 to 2.0 were performed. In addition for method 1 the bin selected for the determination of α_s was slightly shifted towards the 3-jet region. For method 2, two different fit ranges were used for each variable. One of these fit ranges was shifted towards the 2-jet region and the other towards the 3-jet region. A further uncertainty of method 2 originates from the selection of the matching scheme, and was estimated by evaluating α_s with the *R*-scheme instead of the ln *R*-scheme. The variance of the α_s values obtained yields an estimate for the theoretical uncertainty.

5.2 Results

Table 8 presents the bin edges and bin contents used for method 1 and the results obtained at scale $\mu^2 = M_Z^2$. For each variable the bin selected for the evaluation of α_s is chosen in such a way, that the ratio plotted in Fig. 1a becomes as large as allowed by the data. Here larger hadronization and acceptance corrections are accepted than for the fit range of method 2.

The results found with method 2 from χ^2 fits to the particular variables at the scale $\mu^2 = M_Z^2$ using the different matching schemes as defined in Sect. 4, are summarized in Table 9. The errors quoted there are the full experimental and theoretical errors evaluated as described in Sect. 5.1. The fits in the ln *R*- and *R*-G₂₁-schemes are performed over the full range including the 2-jet region, while for the fits in the *R*-scheme a range restricted to the 3-jet region is used as detailed in Sect. 5. The values found with the ln *R*- and the *R*-G₂₁-schemes agree well. Regarding the larger difference between the results from these two schemes and the *R*-scheme one has also to note the different fit range used for the fits in the latter scheme.

Table 7. Upper kinematic boundary limits. For the jet broadening variables the limits were estimated numerically with a Monte Carlo simulation

Variable	y _{max}
$\overline{1-T}$	$\frac{1}{2}$
$\rho^{(T)}$	$\frac{1}{2}$
$\rho^{(M)}$	$\frac{1}{3}$
В	0.5
B _W	0.33
$(1+\cos\chi)/2$	$\frac{1}{2}$

Table 8. Bin edges and contents used for method 1 and results for α_s at the scale $\mu^2 = M_Z^2$. The quoted errors of the data points include statistical and experimental uncertainties, and the errors of the α_s values include theoretical uncertainties additionally

Variable	Bib Δy	$\frac{1}{\boldsymbol{\sigma}_{\rm tot}} \frac{\boldsymbol{\Delta}\boldsymbol{\sigma}}{\boldsymbol{\Delta}\boldsymbol{y}}$	α _s
1-T	0.020.03	16.2 ± 0.8	0.122 ± 0.008
$\rho^{(T)}$	0.020.03	20.2 ± 0.5	0.117 ± 0.008
$\rho^{(M)}$	0.020.03	20.6 ± 0.7	0.119 ± 0.007
B	0.050.06	9.4 ± 0.3	0.116 ± 0.007
B_W	0.040.05	13.7 ± 0.4	0.113 ± 0.010



Fig. 9. Upper plot: Values of $\alpha_s(M_Z^2)$ obtained at different scales μ^2/M_Z^2 from fits to the distributions in thrust, heavy jet masses, jet broadening variables and back-to-back energy-energy correlation. All fits are performed by using the ln *R*-scheme. Lower plot: Combined α_s values as a function of the scale μ^2/M_Z^2 using the ln *R*-scheme. The width of the band corresponds to the full experimental and theoretical error of the combined value

The results of method 1 (Table 8) and those of method 2 (Table 9) agree if the ln R- or the R- G_{21} -scheme are used in method 2. Due to the unphysical divergency of the R-scheme the ln R-scheme is chosen to be the central matching scheme in method 2. This scheme is preferred also in [4, 5]. The upper plot of Fig. 9 shows the dependence of α_s on the scale μ^2/Q^2 of each particular variable investigated in method 2. With the exception of the EEC and the wide jet broadening B_W , all variables agree well and behave similarly.

5.3 Combined result

To combine the results from the fits to the individual variables, statistical correlations are taken into account.

Table 9. Results of method 2 for the scale $\mu^2 = M_Z^2$. The quoted errors are the total errors including theoretical uncertainties as found in an analysis using each event shape variable separately. For the *R*-scheme, which is used in this analysis only to estimate the systematic uncertainty, a restricted fit range is used

Variable	Fit range	$\alpha_{s}(\ln R)$	$\alpha_{s}(R-G_{21})$	Fit range	$\alpha_{\rm s}(R)$
$\overline{1-T}$	0.06 0.30	0.122 ± 0.006	0.123 ± 0.007	0.10 0.30	0.128 ± 0.006
$\rho^{(T)}$	0.03 0.24	0.123 ± 0.009	0.124 ± 0.009	0.08 0.24	0.125 ± 0.009
$\rho^{(M)}$	0.02 0.15	0.124 ± 0.007	0.126 + 0.009	0.08 0.15	0.128 + 0.011
B	0.06 0.24	0.121 ± 0.009	0.117 ± 0.009	0.10 0.24	0.133 ± 0.013
B_{W}	0.04 0.20	0.110 + 0.008	0.107 + 0.008	0.08 0.20	0.122 ± 0.008
EËC	104.4°162.0°	0.134 ± 0.007	0.135 ± 0.007	104.4°136.8°	0.126 ± 0.007

Therefore a covariance matrix $\hat{\sigma}$, which itself is the sum of four matrices, is calculated:

$$\hat{\sigma} = \hat{\sigma}^{(\text{stat})} + \hat{\sigma}^{(\text{exp})} + \hat{\sigma}^{(\text{hadr})} + \hat{\sigma}^{(\text{theo})}.$$
(28)

 $\hat{\sigma}^{(\text{stat})}$ is obtained by splitting the full data sample in 10 subsamples. To each subsample and each variable a fit is performed yielding 10×6 values $\alpha_{s(ik)}$, $i=1,\ldots,6$; $k=1,\ldots,10$, from which, $\hat{\sigma}^{(\text{stat})}$ is computed:

$$\hat{\sigma}_{ij}^{(\text{stat})} = \frac{1}{N(N-1)} \sum_{k=1}^{N=10} (\alpha_{s(ik)} - \bar{\alpha}_{s(i)}) \times (\alpha_{s(ik)} - \bar{\alpha}_{s(j)})$$
(29)

with

$$\bar{\alpha}_{s(i)} = \frac{1}{N} \sum_{k=1}^{N=10} \alpha_{s(ik)}.$$
(30)

 $\hat{\sigma}^{(exp)}$, $\hat{\sigma}^{(hadr)}$ and $\hat{\sigma}^{(theo)}$ are obtained similarly but now with the α_s values obtained in the estimation of the experimental, hadronization and theoretical systematic uncertainties, respectively, instead of the values obtained from the data subsamples. Since correlations of systematic uncertainties are hard to work out reliably, in these latter categories the non-diagonal covariances are set to zero. Once the covariance matrix $\hat{\sigma}$ has been calculated, a combined average value for α_s and the errors can be computed.

The combined result obtained at the scale $\mu^2 = M_Z^2$ with analysis method 1 is:

$$\alpha_{\rm s} = 0.118 \pm 0.002 \,(\text{stat} + \exp) \pm 0.003 \,(\text{hadr}) + 0.006 \,(\text{theo}).$$

The first error quoted is the experimental uncertainty, which includes the statistical error and the uncertainty of the detector simulation. The second error is due to hadronization correction and the third error is an estimate of all theoretical uncertainties.

For method 2, combined α_s -values using the ln *R*-scheme are quoted for several values of the renormalization scale, as shown in the lower plot of Fig. 9. The band corresponds to the total error of the combined values. Since the correlation matrices are expected to be scale independent, they were calculated only at the scale $\mu^2 = M_Z^2$ but applied to all investigated renormalization scales.

The value obtained with analysis method 2 at $\mu^2 = M_Z^2$ is:

$$\alpha_s = 0.123 \pm 0.002 (\text{stat} + \text{exp}) \pm 0.002 (\text{hadr})$$

where the errors are again the combined statistical and experimental error, and the uncertainty due to hadronization correction. From the remaining scale dependence (estimated using the range $0.5 \le \mu^2/Q^2 \le 2.0$) and matching ambiguits, the theoretical uncertainty of method 2 is estimated to: It should be pointed out that this theoretical error is estimated as an "one standard deviation error". The uncertainty due to a certain arbitrariness in the choice of the fit range is estimated to:

$$\Delta \alpha_s = \pm 0.002$$
 (fit range).

This yields a total theoretical error of:

$$\Delta \alpha_s = \pm 0.005$$

6 Conclusions

From 178 000 Z^0 hadronic decays collected in 1991 with the DELPHI detector at the LEP collider, a new measurement of the strong coupling constant α_s has been performed, using the next-to-leading logarithm approximation (NLLA) of QCD.

Using theoretical expressions including resummation of leading and next-to-leading logarithms to all orders of α_s , which describe parton distributions for thrust, heavy jet mass, jet broadening and back-to-back energy-energy correlation, α_s was determined following two different approaches. The first method concentrates on the extreme 2-jet region where the resummed logarithms dominate, and is in some sense complementary to a pure second order α_s determination which is restricted to the 3-jet region. This method can only be applied to thrust, the heavy jet mass and the jet broadening measures.

The second method confronts the combined NLLA and $\mathscr{O}(\alpha_s^2)$ calculation with data. The values of α_s obtained from both methods agree within errors if the ln *R*or *R*-*G*₂₁-matching schemes are used for method 2. While the first approach should be reliable to determine α_s only from the 2-jet region, the second tests whether a combined calculation is able to describe the experimental distributions over a wide kinematical range including the 3-jet region. Therefore the result obtained with method 1 is considered as a consistency check, and the final result:

 $\alpha_{\rm s} = 0.123 \pm 0.006$ at the scale $\mu^2 = M_Z^2$

is based on method 2 only.

If in method 2 the R- G_{21} -scheme is chosen instead of the ln R-scheme, the final value is $\alpha_s = 0.122 \pm 0.006$. In a previous paper [3] based on $\mathscr{O}(\alpha_s^2)$ perturbation theory, a value of $\alpha_s(M_Z^2) = 0.115 \pm 0.007$ was determined. This result was obtained from a combined analysis of eight distributions of event shape variables, where hadronization corrections were performed by using parton shower models. Within errors the results of the $\mathscr{O}(\alpha_s^2)$ and the NLLA analysis are consistent.

Acknowledgements. We are greatly indebted to our technical collaborators and to the funding agencies for their support in building and operating the DELPHI detector, and to the members of the CERN-SL Division for the excellent performance of the LEP collider. We would like to thank S. Catani, G. Turnock and B.R. Webber for useful discussions.

$$\Delta \alpha_{\rm s} = \pm 0.005$$
 (scale + matching ambiguity).

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