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ЯДЕРНЫХ  
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ДУБНА

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**TABLES AND GRAPHS  
OF OSCILLATOR SPHEROIDAL FUNCTIONS**

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## 1. Introduction

In ref. <sup>1/1</sup> the problem has been studied of an isotropic quantum oscillator in prolate and oblate spheroidal coordinates and a new class of special functions has been introduced, the class of prolate and oblate spheroidal functions of the oscillator. These functions are related to spheroidal and Coulomb spheroidal functions which have found application in radiophysics, optics and quantum mechanics <sup>x)</sup>. Unlike the classical special functions the oscillator spheroidal functions do not obey recurrence formulae and have no integral representations. This "anomaly" can be explained by a specific feature of the spheroidal coordinate system <sup>2/</sup>: there cannot be made expansions of the group of motion of a three-dimensional space into one-parameter subgroups. This peculiarity much complicates the study and application of spheroidal functions and puts forward the problem of compilation of tables and graphs of appropriate effective calculation algorithms at computer. In this paper, tables and graphs of prolate and oblate spheroidal functions of the oscillator are obtained only for several of the first values of quantum numbers of these functions. A more complete solution to this problem is still to be looked for.

## 2. Prolate angular spheroidal functions of the oscillator

Let us introduce the operator  $\hat{A}(n, m, c; \eta)$  dependent on the variable  $\eta \in [-1, 1]$ , quantum numbers  $n$ ,  $m$  and parameter  $c$ :

$$\hat{A}(n, m, c; \eta) = \frac{d}{d\eta}(\eta^2 - 1) \frac{d}{d\eta} + 2(n + \frac{1}{2})c\eta^2 - \frac{m^2}{\eta^2 - 1} - c^2\eta^2(\eta^2 - 1) \quad (1)$$

The quantum number  $n$  assumes only integer nonnegative values,  $|m|$  may equal  $0, 1, 2, \dots, n$ , and parameter  $c \in [0, \infty)$ . The prolate angular spheroidal functions  $Y_q(n, m, c; \eta)$  are defined as solutions to the following Sturm-Liouville equation:

$$\hat{A}(n, m, c; \eta) Y_q(n, m, c; \eta) = A_q(n, m, c) Y_q(n, m, c; \eta) \quad (2)$$

The quantum number  $q$  enumerates eigenvalues  $A_q$  and coincides with the number of zeros of the functions  $Y_q$  in the interval  $(-1, 1)$ .

<sup>x)</sup> Theory and methods of the calculation of spheroidal and Coulomb spheroidal functions and their most important applications can be found in monograph <sup>2/</sup>.

In ref.<sup>1/1</sup> it has been shown that the functions  $Y_q$  are divided into two classes,  $Y_q^{(+)}$  and  $Y_q^{(-)}$ , with positive and negative parity in variable  $q$  and are determined by the expressions:

$$Y_q^{(+)}(n, m, c; \eta) = e^{-\frac{c\eta^2}{2}} (1-\eta^2)^{\frac{|m|}{2}} \sum_S a_{2S}(n, m, c) \eta^{2S} \quad (3)$$

$$Y_q^{(-)}(n, m, c; \eta) = e^{-\frac{c\eta^2}{2}} (1-\eta^2)^{\frac{|m|}{2}} \sum_S a_{2S+1}(n, m, c) \eta^{2S+1} \quad (4)$$

Summation in (3) and (4) runs over  $S = 0, 1, \dots, \frac{n-|m|}{2}$  and  $S = 0, 1, \dots, \frac{n-|m|-1}{2}$  (in the first case  $n-|m|$  is even; in the second, odd). From the meaning of the quantum number  $q$  it is clear that for  $Y_q^{(+)}$  and  $Y_q^{(-)}$   $q = 0, 2, \dots, n-|m|$  and  $q = 1, 3, \dots, n-|m|$ , respectively. Coefficients  $a_{2S}$  and  $a_{2S+1}$  obey trinomial recurrence formulae:

$$-(2S+1)(2S+2)a_{2S+2} + \{(2S+1m)(2S+1m+1) + 4cS - Aq + c\}a_{2S} + 2c(n-1m+2-2S)a_{2S-2} = 0 \quad (5)$$

$$-(2S+2)(2S+3)a_{2S+3} + \{(2S+1m+1)(2S+1m+2) + 2c(2S+1) - Aq + c\}a_{2S+1} + 2c(n-1m+1-2S)a_{2S-1} = 0 \quad (6)$$

and the boundary conditions

$$a_{-2} = a_{-1} = 0, \quad a_0 = a_1 = 1 \quad (7)$$

normalizing the function  $Y_q^{(\pm)}$ .

Therefore, the tables and graphs we are interested in are constructed by solving two systems of homogeneous equations (5) and (6) with boundary conditions (7). Results for particular cases  $0 \leq n-|m| \leq 5$  are given in Table 1 and graphs in Fig. 1.

### 3. Prolate radial spheroidal functions of the oscillator

Let us redenote the variable in operator (1) by  $\xi$  and assume the  $\xi \in [1, \infty)$ . Prolate radial spheroidal functions of

the oscillator will be defined as solutions to the Sturm-Liouville problem:

$$\hat{A}(n, m, c; \xi) X_{\kappa}(n, m, c; \xi) = \mathcal{B}_{\kappa}(n, m, c) X_{\kappa}(n, m, c; \xi) \quad (8)$$

The quantum number  $\kappa$  enumerates eigenvalues  $\mathcal{B}_{\kappa}$  and coincides with the number of zeros of the function  $X_{\kappa}$  in the interval  $(1, \infty)$ . According to <sup>11/</sup> equation (8) has two classes of solutions, even and odd in the variable  $\xi$ . These solutions can be represented by polynomials:

$$X_{\kappa}^{(+)}(n, m, c; \xi) = e^{-\frac{\xi}{2}(\xi^2-1)} (\xi^2-1)^{\frac{|m|}{2}} \sum_S b_S(n, m, c) (\xi^2-1)^S \quad (9)$$

$$X_{\kappa}^{(-)}(n, m, c; \xi) = e^{-\frac{\xi}{2}(\xi^2-1)} (\xi^2-1)^{\frac{|m|}{2}} \xi \sum_S g_S(n, m, c) (\xi^2-1)^S \quad (10)$$

The range of summation in (9) and (10) is the same as in (3) and (4). The coefficients  $b_S$  and  $g_S$  satisfy the trinomial recurrence relations:

$$4(S+1)(S+|m|+1)b_{S+1} + \{(2S+|m|)(2S+|m|+1) + 2c(n-|m|-2S) - \mathcal{B}_{\kappa}^{(+)} + c\} b_S + 2c(n-|m|+2-2S)b_{S-1} = 0 \quad (11)$$

$$4(S+1)(S+|m|+1)g_{S+1} + \{(2S+|m|+1)(2S+|m|+2) + 2c(n-|m|-2S) - \mathcal{B}_{\kappa}^{(-)} + c\} g_S + 2c(n-|m|+1-2S)g_{S-1} = 0 \quad (12)$$

and the boundary conditions

$$b_{-1} = g_{-1} = 0, \quad b_0 = g_0 = 1 \quad (13)$$

fixing the normalization of functions  $X_{\kappa}^{(\pm)}$ . Results of the solution of two systems of homogeneous equations (11) and (12) with the boundary condition (13) for  $0 \leq n-|m| \leq 5$  are collected in Tables 2 and graphs in Fig. 2.

#### 4. Oblate spheroidal functions of the oscillator

We shall not here discuss these functions in detail; rather we shall note that according to ref. <sup>11/</sup> these functions follow from analogous functions in prolate spheroidal coordinates by using the formulae

$$\tilde{Y}_t^{(+)}(n, m, \rho; \bar{\eta}) = (-1)^{\frac{|m|}{2}} X_{\frac{n-t-|m|}{2}}^{(+)}(n, m, -\rho; \bar{\eta}) \quad (14)$$

$$\tilde{X}_2^{(+)}(n, m, \rho; \bar{\xi}) = Y_{n-2l-|m|}^{(+)}(n, m, -\rho; i\bar{\xi}) \quad (15)$$

$$\tilde{X}_2^{(-)}(n, m, \rho; \bar{\xi}) = -i Y_{n-2l-|m|}^{(-)}(n, m, -\rho; i\bar{\xi}) \quad (16)$$

$$\bar{\eta} \in [-1, 1], \quad \bar{\xi} \in [0, \infty)$$

i.e. they represent analytic continuations of prolate spheroidal oscillator functions into an "unphysical" region of the variables  $\eta$ ,  $\xi$  and parameter  $C$ . Tables 3, 4 and graphs in Figs. 3, 4 are compiled by formulae (14)-(16).

### 5. Particular cases

The explicit form of spheroidal oscillator functions for arbitrary  $n$  and  $|m|$ , when  $0 \leq n-|m| \leq 3$ , is as follows:

$$Y_0^{(+)}(n, n, c; \eta) = \exp\left(-\frac{C\eta^2}{2}\right) (1-\eta^2)^{\frac{n}{2}}$$

$$Y_1^{(-)}(n, n-1, c; \eta) = \exp\left(-\frac{C\eta^2}{2}\right) (1-\eta^2)^{\frac{n-1}{2}} \eta$$

$$Y_0^{(+)}(n, n-2, c; \eta) = \exp\left(-\frac{C\eta^2}{2}\right) (1-\eta^2)^{\frac{n-2}{2}}$$

$$\left\{ 1 - \frac{(2n-1)+2c - \sqrt{(2n-1)^2 + 4c(2n-3) + 4c^2}}{2} \eta^2 \right\}$$

$$Y_2^{(+)}(n, n-2, c; \eta) = \exp\left(-\frac{C\eta^2}{2}\right) (1-\eta^2)^{\frac{n-2}{2}}$$

$$\left\{ 1 - \frac{(2n-1)+2c + \sqrt{(2n-1)^2 + 4c(2n-3) + 4c^2}}{2} \eta^2 \right\}$$

$$Y_1^{(-)}(n, n-3, c; \eta) = \exp\left\{-\frac{C\eta^2}{2}\right\} (1-\eta^2)^{\frac{n-3}{2}} \eta$$

$$\left\{ 1 - \frac{(2n-1)+2c - \sqrt{(2n-1)^2 + 4c(2n-7) + 4c^2}}{6} \eta^2 \right\}$$

$$Y_3^{(+)}(n, n-3, c; \eta) = \exp\left(-\frac{c\eta^2}{2}\right) (1-\eta^2)^{\frac{n-3}{2}} \eta.$$

$$\left\{1 - \frac{(2n-1) - 2c + \sqrt{(2n-1)^2 + 4c(2n-7) + 4c^2}}{6} \eta^2\right\}$$

$$X_0^{(+)}(n, n, c; \xi) = \exp\left[-\frac{c}{2}(\xi^2-1)\right] (\xi^2-1)^{\frac{n}{2}}$$

$$X_0^{(-)}(n, n-1, c; \xi) = \exp\left[-\frac{c}{2}(\xi^2-1)\right] (\xi^2-1)^{\frac{n-1}{2}} \xi$$

$$X_0^{(+)}(n, n-2, c; \xi) = \exp\left[-\frac{c}{2}(\xi^2-1)\right] (\xi^2-1)^{\frac{n-2}{2}}.$$

$$\left\{1 + \frac{(2n-1) - 2c + \sqrt{(2n-1)^2 + 4c(2n-3) + 4c^2}}{4(n-1)} (\xi^2-1)\right\}$$

$$X_1^{(+)}(n, n-2, c; \xi) = \exp\left[-\frac{c}{2}(\xi^2-1)\right] (\xi^2-1)^{\frac{n-2}{2}}.$$

$$\left\{1 + \frac{(2n-1) - 2c - \sqrt{(2n-1)^2 + 4c(2n-3) + 4c^2}}{4(n-1)} (\xi^2-1)\right\}$$

$$X_0^{(-)}(n, n-3, c; \xi) = \exp\left[-\frac{c}{2}(\xi^2-1)\right] (\xi^2-1)^{\frac{n-3}{2}} \xi.$$

$$\left\{1 + \frac{(2n-1) - 2c + \sqrt{(2n-1)^2 + 4c(2n-7) + 4c^2}}{4(n-2)} (\xi^2-1)\right\}$$

$$X_1^{(-)}(n, n-3, c; \xi) = \exp\left[-\frac{c}{2}(\xi^2-1)\right] (\xi^2-1)^{\frac{n-3}{2}} \xi.$$

$$\left\{1 + \frac{(2n-1) - 2c - \sqrt{(2n-1)^2 + 4c(2n-7) + 4c^2}}{4(n-2)} (\xi^2-1)\right\}$$

$$\tilde{Y}_0^{(+)}(n, n, \rho; \bar{\eta}) = \exp\left[-\frac{\rho}{2}(1-\bar{\eta}^2)\right](1-\bar{\eta}^2)^{\frac{n}{2}}$$

$$\tilde{Y}_1^{(-)}(n, n-1, \rho; \bar{\eta}) = \exp\left[-\frac{\rho}{2}(1-\bar{\eta}^2)\right](1-\bar{\eta}^2)^{\frac{n-1}{2}}$$

$$\tilde{Y}_0^{(+)}(n, n-2, \rho; \bar{\eta}) = \exp\left[-\frac{\rho}{2}(1-\bar{\eta}^2)\right](1-\bar{\eta}^2)^{\frac{n-2}{2}}$$

$$\cdot \left\{1 - \frac{(2n-1)+2\rho - \sqrt{(2n-1)^2 - 4\rho(2n-3) + 4\rho^2}}{4(n-1)} (1-\bar{\eta}^2)\right\}$$

$$\tilde{Y}_2^{(+)}(n, n-2, \rho; \bar{\eta}) = \exp\left[-\frac{\rho}{2}(1-\bar{\eta}^2)\right](1-\bar{\eta}^2)^{\frac{n-2}{2}}$$

$$\cdot \left\{1 - \frac{(2n-1)+2\rho + \sqrt{(2n-1)^2 - 4\rho(2n-3) + 4\rho^2}}{4(n-1)} (1-\bar{\eta}^2)\right\}$$

$$\tilde{Y}_1^{(-)}(n, n-3, \rho; \bar{\eta}) = \exp\left[-\frac{\rho}{2}(1-\bar{\eta}^2)\right](1-\bar{\eta}^2)^{\frac{n-3}{2}}$$

$$\cdot \left\{1 - \frac{(2n-1)+2\rho - \sqrt{(2n-1)^2 - 4\rho(2n-7) + 4\rho^2}}{4(n-2)} (1-\bar{\eta}^2)\right\}$$

$$\tilde{Y}_3^{(-)}(n, n-3, \rho; \bar{\eta}) = \exp\left[-\frac{\rho}{2}(1-\bar{\eta}^2)\right](1-\bar{\eta}^2)^{\frac{n-3}{2}}$$

$$\cdot \left\{1 - \frac{(2n-1)+2\rho + \sqrt{(2n-1)^2 - 4\rho(2n-7) + 4\rho^2}}{4(n-2)} (1-\bar{\eta}^2)\right\}$$

$$\tilde{X}_0^{(+)}(n, n, \rho; \bar{\xi}) = \exp\left(-\frac{\rho\bar{\xi}^2}{2}\right)(\bar{\xi}^2+1)^{\frac{n}{2}}$$

$$\tilde{X}_1^{(-)}(n, n-1, \rho; \bar{\xi}) = \exp\left(-\frac{\rho\bar{\xi}^2}{2}\right)(\bar{\xi}^2+1)^{\frac{n-1}{2}}$$

$$\tilde{X}_0^{(+)}(n, n-2, \rho; \bar{\xi}) = \exp\left(-\frac{\rho\bar{\xi}^2}{2}\right)(\bar{\xi}^2+1)^{\frac{n-2}{2}}$$

$$\cdot \left\{1 + \frac{(2n-1) - 2\rho + \sqrt{(2n-1)^2 - 4\rho(2n-3) + 4\rho^2}}{2} \bar{\xi}^2\right\}$$

$$\begin{aligned} \tilde{X}_1^{(+)}(n, n-2, \rho; \bar{\xi}) &= \exp\left(-\frac{\rho \bar{\xi}^2}{2}\right) (\bar{\xi}^2 + 1)^{\frac{n-2}{2}} \\ &\cdot \left\{ 1 + \frac{(2n-1) - 2\rho - \sqrt{(2n-1)^2 - 4\rho(2n-3) + 4\rho^2}}{2} \bar{\xi}^{-2} \right\} \\ \tilde{X}_0^{(-)}(n, n-3, \rho; \bar{\xi}) &= \exp\left(-\frac{\rho \bar{\xi}^2}{2}\right) (\bar{\xi}^2 + 1)^{\frac{n-3}{2}} \bar{\xi}^{-1} \\ &\cdot \left\{ 1 + \frac{(2n-1) - 2\rho + \sqrt{(2n-1)^2 - 4\rho(2n-7) + 4\rho^2}}{6} \bar{\xi}^{-2} \right\} \\ \tilde{X}_1^{(-)}(n, n-1, \rho; \bar{\xi}) &= \exp\left(-\frac{\rho \bar{\xi}^2}{2}\right) (\bar{\xi}^2 + 1)^{\frac{n-3}{2}} \bar{\xi}^{-1} \\ &\cdot \left\{ 1 + \frac{(2n-1) - 2\rho - \sqrt{(2n-1)^2 - 4\rho(2n-7) + 4\rho^2}}{6} \bar{\xi}^{-2} \right\} \end{aligned}$$

## 6. Eigenvalues $A_q^{(\pm)}$ and $B_\kappa^{(\pm)}$

Eigenvalues  $A_q^{(\pm)}$  and  $B_\kappa^{(\pm)}$  are determined from the requirement that the determinants for homogeneous systems of equations (5), (6), and (11), (12) equal zero. The dependence of  $A_q^{(\pm)}$  and  $B_\kappa^{(\pm)}$  on  $C$  at given  $n$  and  $|m|$  is shown in Tables 5, 6 and graphs in Figs. 5. There is also given their analytic continuation into a "physical" region of oblate functions. Note that the quantum numbers  $q$  and  $\kappa$  are related by  $n - |m| - q = 2\kappa / 11$ , and

$$A_q^{(\pm)}(n, m, c) = B_\kappa^{(\pm)}(n, m, c)$$

## 7. Conclusion

The functions studied above naturally arise when the variables are separated in the Schrödinger equation for an isotropic oscillator in prolate and oblate spheroidal coordinates. The latter are connected with rectangular coordinates as follows:

$$x = \frac{R}{2} \sqrt{(\xi^2 - 1)(1 - \eta^2)} \cos \varphi, \quad y = \frac{R}{2} \sqrt{(\xi^2 - 1)(1 - \eta^2)} \sin \varphi, \quad z = \frac{R}{2} \xi \eta$$



$$X = \frac{\bar{R}}{2} \sqrt{(\bar{\xi}^2 + 1)(1 - \bar{\eta}^2)} \cos \varphi, \quad Y = \frac{\bar{R}}{2} \sqrt{(\bar{\xi}^2 + 1)(1 - \bar{\eta}^2)} \sin \varphi, \quad Z = \frac{\bar{R}}{2} \bar{\xi} \bar{\eta}.$$

Here the angle  $\varphi$  changes within the interval  $0 \leq \varphi < 2\pi$ ; the range of variation of the coordinates  $(\bar{\xi}, \bar{\eta})$  and  $(\bar{\xi}, \bar{\eta})$  has been indicated in the main body of the manuscript. The parameter  $\bar{R}$  is expressed through  $C$  by the formula

$$C = \frac{\mu \omega}{4\pi} \bar{R}^2$$

in which  $\mu$  is the mass,  $\omega$  is a cyclic velocity of an isotropic oscillator. An analogous relation is valid for parameters  $\bar{R}$  and  $\rho$ . Total wave functions of an isotropic oscillator in prolate spheroidal coordinates have the form

$$\psi_{nqkm}^{(\pm)}(\bar{\xi}, \bar{\eta}, \varphi; C) = N_{nqm}^{(\pm)}(C) Y_q^{(\pm)}(n, m, c; \bar{\eta}) X_\kappa(n, m, c; \bar{\xi}) \frac{e^{im\varphi}}{\sqrt{2\pi}}$$

where  $N_{nqm}^{(\pm)}(C)$  is a normalization constant. The oblate basis follows from this formula by the change  $\bar{\eta} \rightarrow \bar{\eta}$ ,  $\bar{\xi} \rightarrow \bar{\xi}$ ,  $C \rightarrow \rho$ . Indices of the total wave functions of the oscillator are related by  $n = 2\kappa + |m| + q$ .

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#### References

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2. I.V. Komarov, L.I. Ponomarev, S.Yu. Slavyanov. Spheroidal and Coulomb Spheroidal Functions, Nauka, Moscow, 1976 (in Russian).

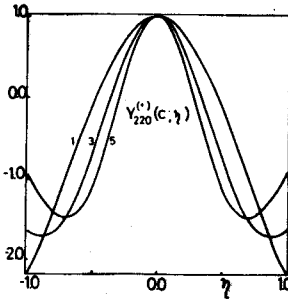
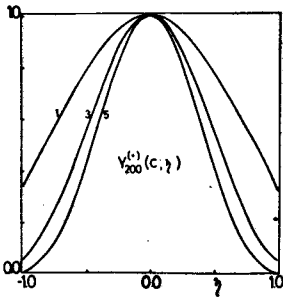
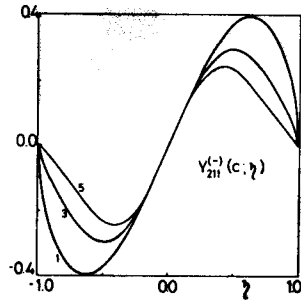
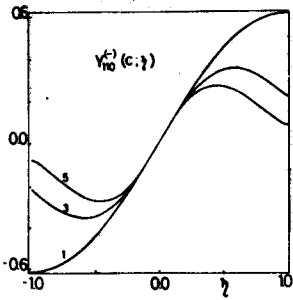
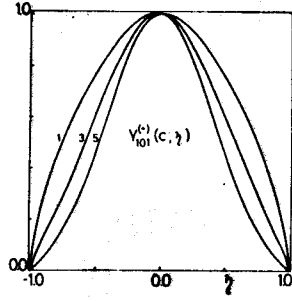
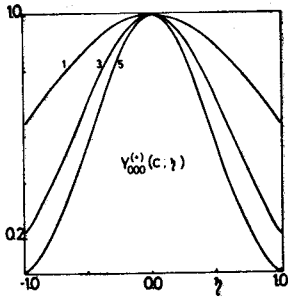


Fig. 1a. Prolate angular spheroidal functions  $Y_{nqm}^{(\pm)}(c; \eta) = Y_q(n, m, c; \eta)$ ,  $c = 1, 3, 5$

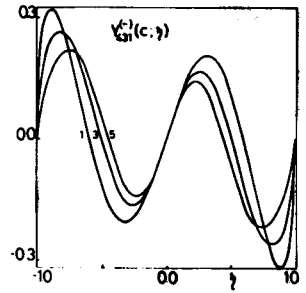
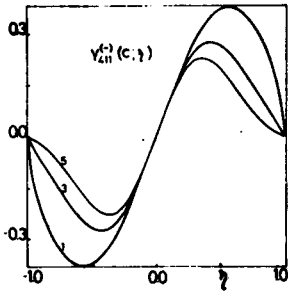
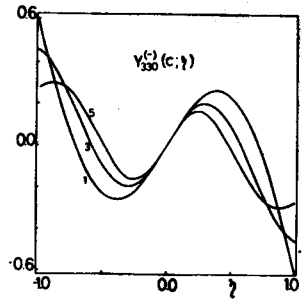
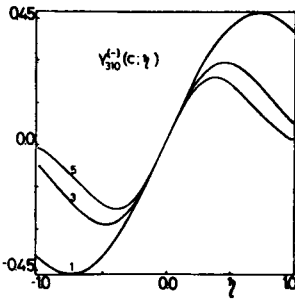
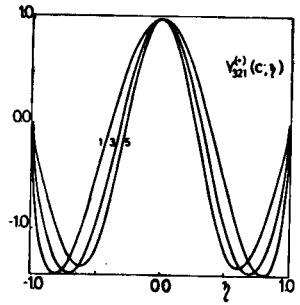
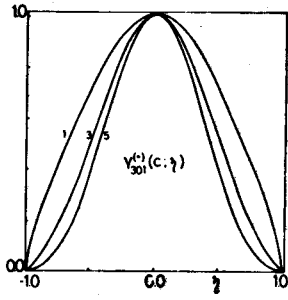


Fig. 1b. Prolate angular spheroidal functions  
 $Y_{nqm}(c, \eta) \equiv Y_q(n, m, c; \eta)$ ,  $c = 1, 3, 5$

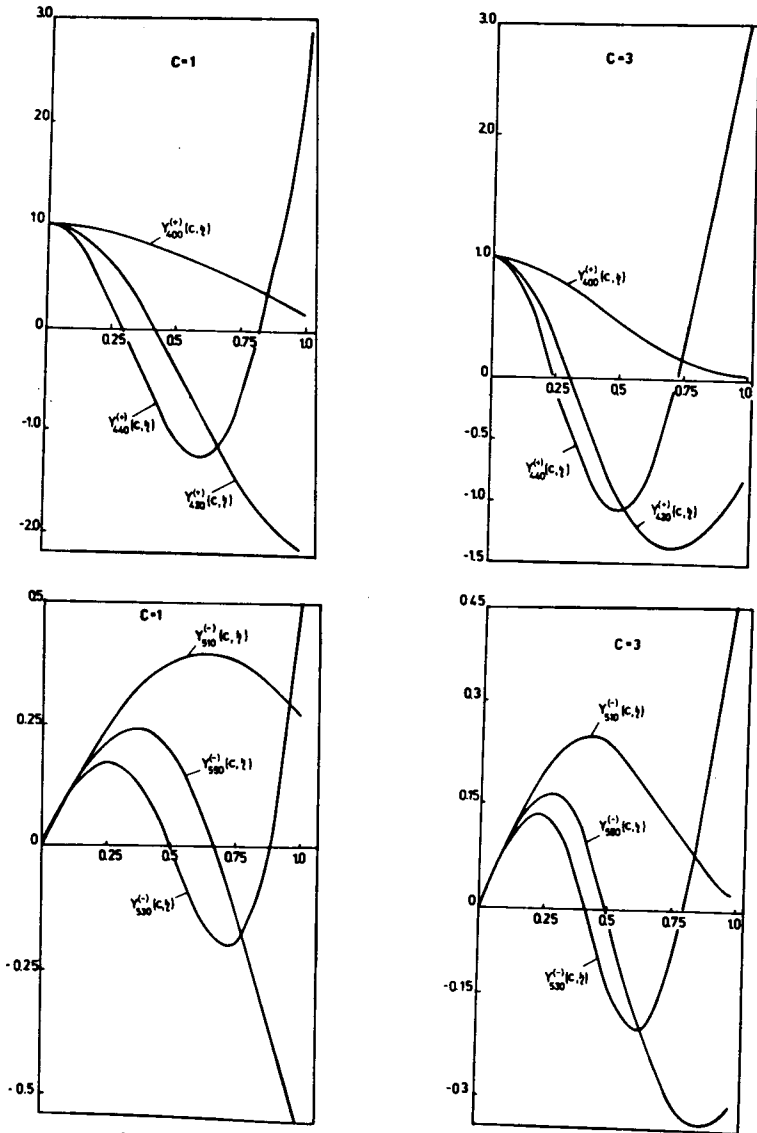


Fig. 1c. Prolate angular spheroidal functions  
 $Y_{nqm}^{(-)}(c; \eta) \equiv Y_q(n, m, c; \eta)$

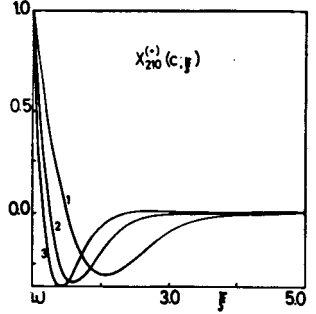
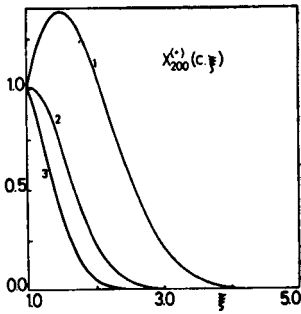
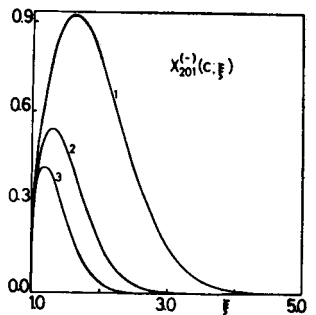
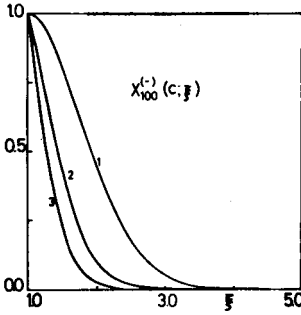
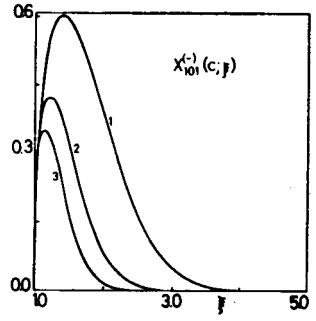
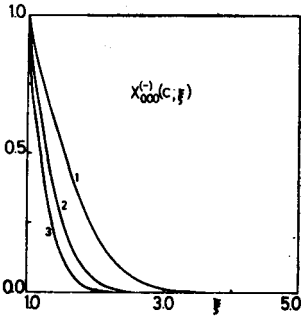


Fig. 2a. Prolate radial spheroidal functions  
 $X_{nkm}^{(-)}(c; \xi) \equiv X_k(n, m, c; \xi)$ ;  $c = 1, 2, 3$

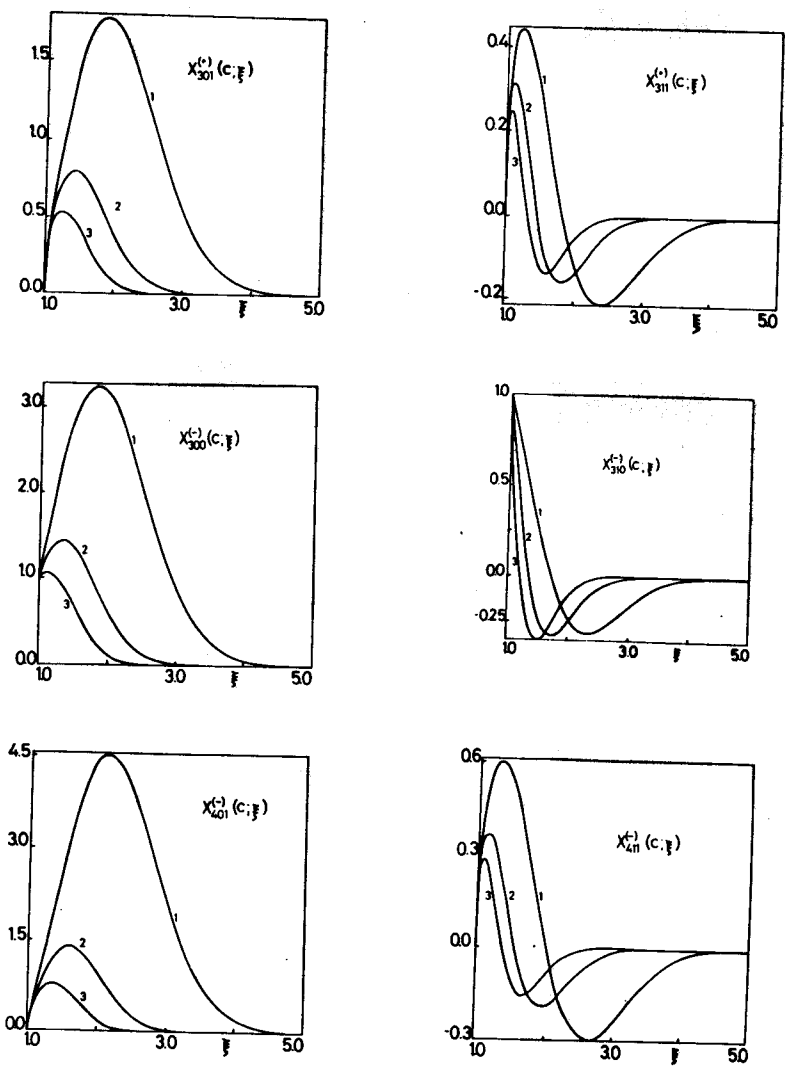


Fig. 2b. Prolate radial spheroidal functions  $X_{nkm}^{(c)}(c; \xi) \equiv X_k(n, m, c; \xi)$ ;  $c = 1, 2, 3$

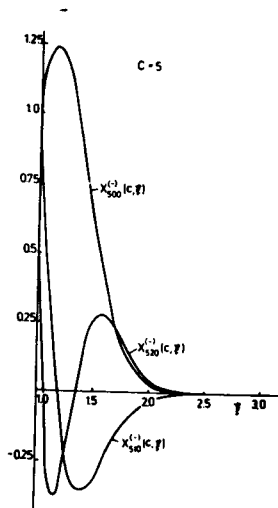
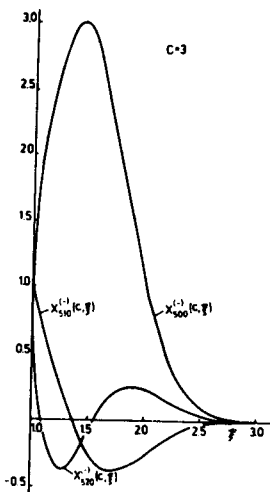
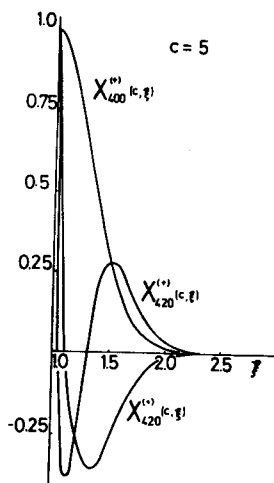
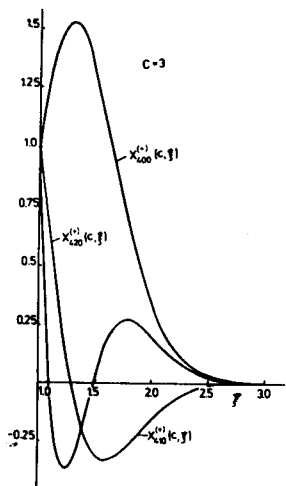


Fig. 2c. Prolate radial spheroidal functions  
 $X_{nkm}(c; \xi) \equiv X_k(n, m, c; \xi)$

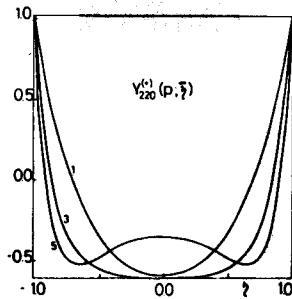
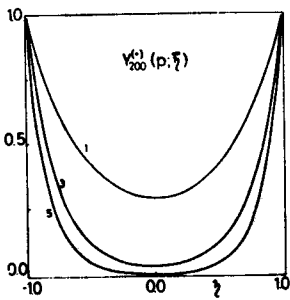
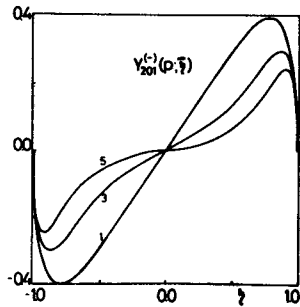
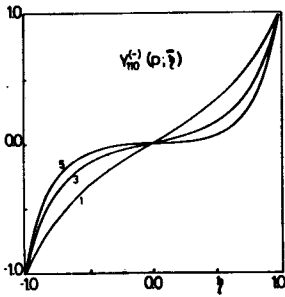
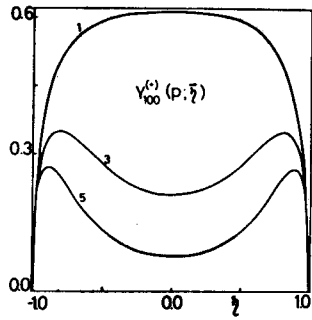
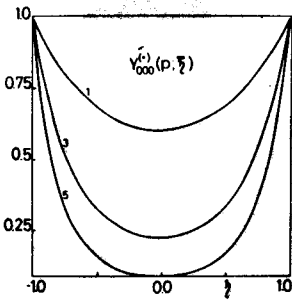


Fig. 3a. Oblate angular spheroidal functions  
 $Y_{ntm}^{(c)}(p; \bar{\eta}) \equiv \tilde{Y}_t^{(c)}(n, m, p; \bar{\eta})$ ,  $p = 1, 3, 5$



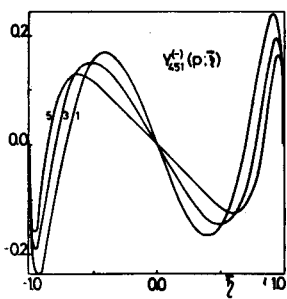
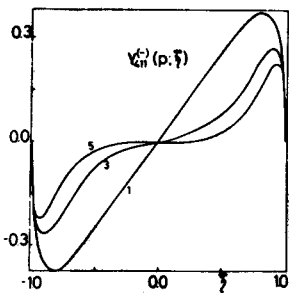
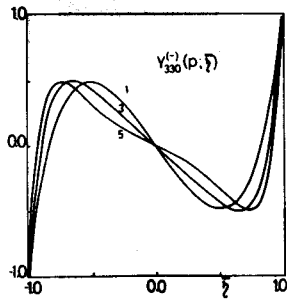
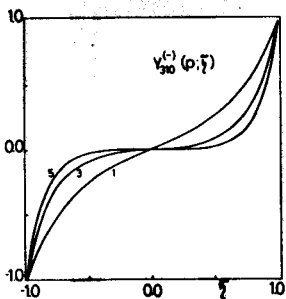
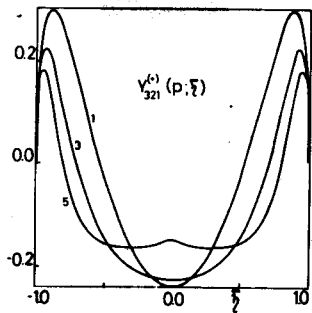
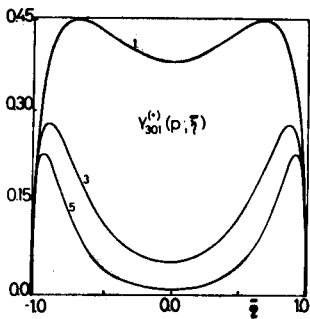


Fig. 3b. Oblate angular spheroidal functions  
 $Y_{ntm}^{(c)}(\rho; \bar{\eta}) \equiv \tilde{Y}_t(n, m, p; \bar{\eta})$ ,  $p = 1, 3, 5$

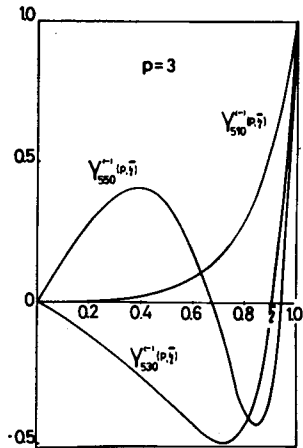
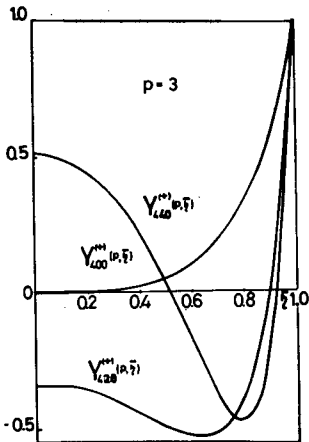
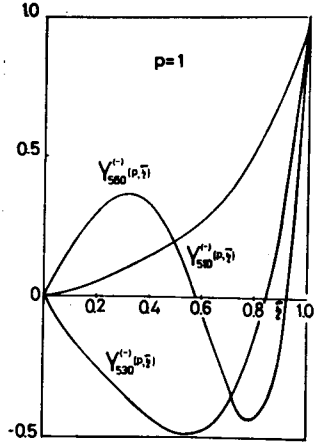
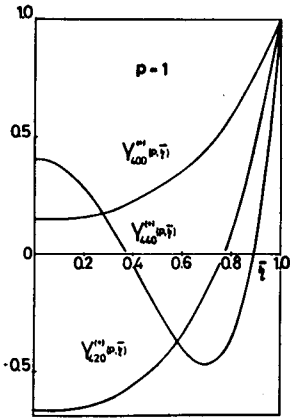


Fig. 3c. Oblate angular spheroidal functions  
 $Y_{ntm}(p; \bar{\eta}) = \tilde{Y}_t(n, m, p; \bar{\eta})$

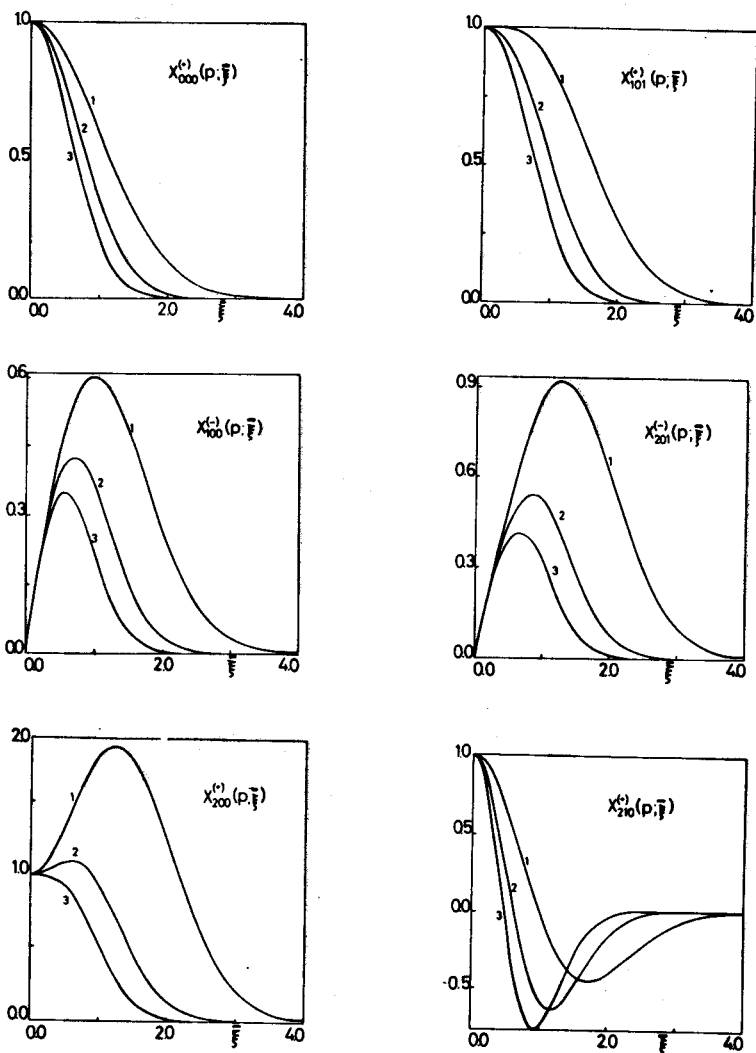


Fig. 4a. Oblate radial spheroidal functions  
 $X_{lm}^{(p)}(\rho; \bar{\xi}) \equiv \tilde{X}_r(n, m, p; \bar{\xi})$ ;  $p = 1, 2, 3$

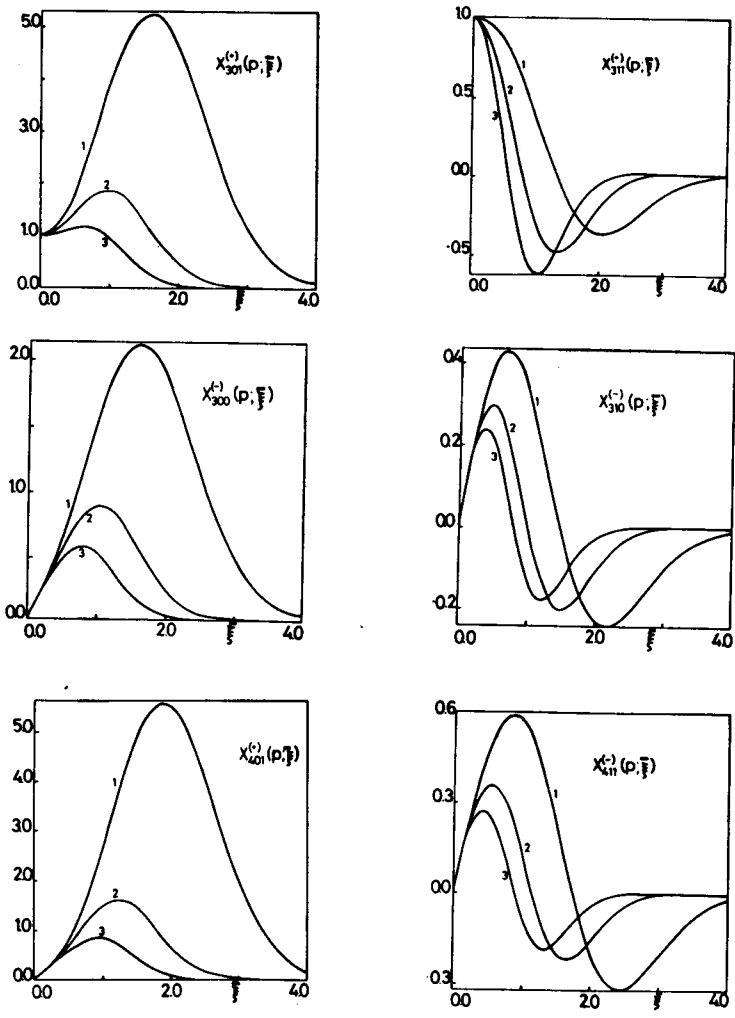


Fig. 4b. Oblate radial spheroidal functions  $X_{nrm}^{(-)}(p; \bar{\xi}) \equiv \tilde{X}_r(n, m, p; \bar{\xi})$ ;  $p = 1, 2, 3$

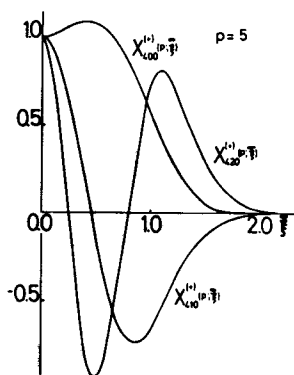
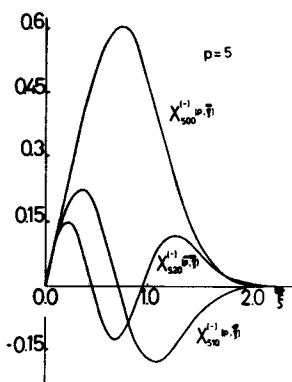
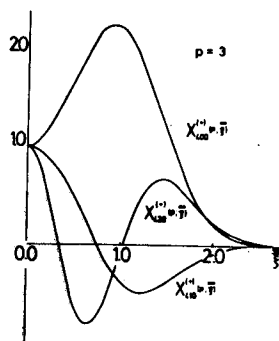
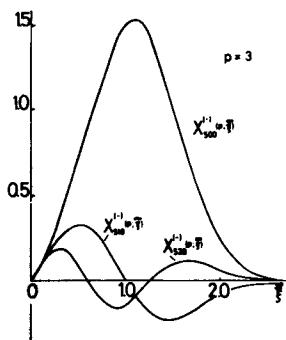


Fig. 4c. Oblate radial spheroidal functions  $X_{nrm}(p; \xi)$   $\tilde{X}_r(n, m, p; \xi)$ ;

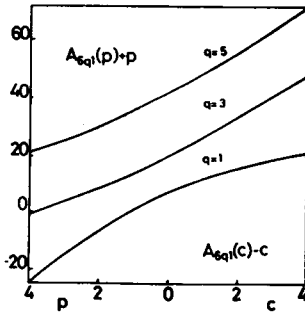
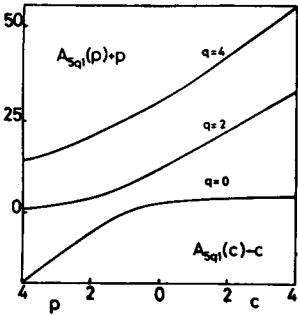
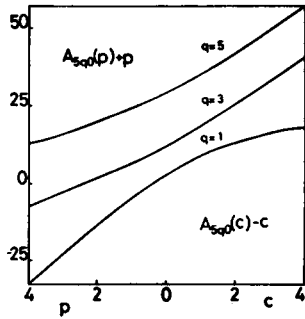
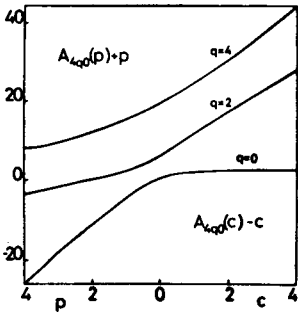
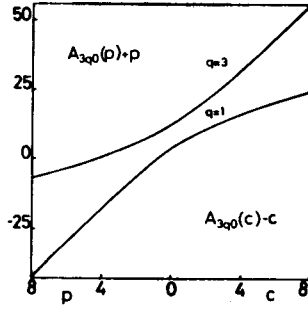
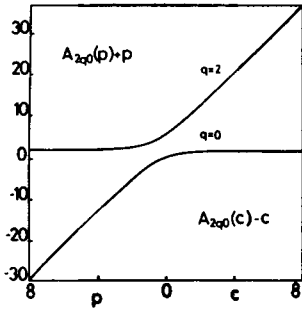


Fig. 5. Eigenvalues of the separation constants  $A_{nqm}(c) \equiv A_q(n, m, 0) \bar{\xi}$  and  $A_{nqm}(p) \equiv A_q(n, m, p)$

Table 1a. Prolate angular spheroidal functions  $Y_0^{(+)}(n, n, c; \eta)$

$n$	$c \setminus \eta$	0.0	.1	.2	.3	.4	.5	.6	.7	.8	.9	1.0
0	1	1.0000	.9950	.9882	.9768	.9591	.9255	.8353	.7027	.5281	.6670	.6165
	3	1.0000	.9900	.9606	.9139	.8521	.7768	.6977	.6126	.5273	.4449	.3679
	5	1.0000	.9851	.9418	.8737	.7866	.6883	.5829	.4995	.4233	.3521	.2967
1	1	1.0000	.9900	.9604	.9120	.8461	.7643	.6682	.5590	.4377	.2907	0.0000
	3	1.0000	.9851	.9421	.8718	.7810	.6782	.5681	.4524	.3307	.1939	0.0000
	5	1.0000	.9802	.9277	.8535	.7510	.6352	.5121	.3824	.2527	.1293	0.0000
2	1	1.0000	.9851	.9410	.8700	.7754	.6619	.5344	.3992	.2614	.1267	0.0000
	3	1.0000	.9801	.9224	.8317	.7158	.5841	.4465	.3124	.1828	.0565	0.0000
	5	1.0000	.9753	.9041	.7951	.6608	.5155	.3730	.2445	.1378	.0564	0.0000
3	1	1.0000	.9801	.9220	.8299	.7107	.5732	.4277	.2951	.1868	.0952	0.0000
	3	1.0000	.9752	.9037	.7934	.6560	.5058	.3572	.2331	.1439	.0736	0.0000
	5	1.0000	.9704	.8958	.7855	.6486	.4964	.3484	.2280	.1466	.0746	0.0000
4	1	1.0000	.9752	.9034	.7917	.6514	.4964	.3421	.2336	.1491	.0741	0.0000
	3	1.0000	.9703	.8955	.7868	.6433	.4881	.3360	.2293	.1483	.0761	0.0000
	5	1.0000	.9655	.8907	.7835	.6405	.4865	.3365	.2327	.1524	.0787	0.0000
5	1	1.0000	.9703	.8951	.7852	.6414	.4899	.3381	.2354	.1555	.0785	0.0000
	3	1.0000	.9655	.8904	.7820	.6411	.4914	.3406	.2394	.1598	.0811	0.0000
	5	1.0000	.9607	.8856	.7792	.6407	.4937	.3448	.2438	.1639	.0837	0.0000
6	1	1.0000	.9655	.8902	.7804	.6401	.4923	.3419	.2439	.1659	.0860	0.0000
	3	1.0000	.9607	.8855	.7792	.6408	.4941	.3448	.2466	.1687	.0886	0.0000
	5	1.0000	.9559	.8807	.7752	.6384	.4958	.3476	.2498	.1719	.0912	0.0000
7	1	1.0000	.9606	.8854	.7772	.6397	.4941	.3454	.2463	.1703	.0899	0.0000
	3	1.0000	.9558	.8806	.7740	.6395	.4958	.3481	.2490	.1736	.0925	0.0000
	5	1.0000	.9511	.8759	.7708	.6392	.4975	.3508	.2522	.1769	.0951	0.0000
8	1	1.0000	.9558	.8806	.7740	.6395	.4958	.3481	.2490	.1736	.0925	0.0000
	3	1.0000	.9511	.8759	.7708	.6392	.4975	.3508	.2522	.1769	.0951	0.0000
	5	1.0000	.9463	.8711	.7679	.6389	.4992	.3535	.2554	.1804	.0976	0.0000
9	1	1.0000	.9510	.8758	.7707	.6394	.4974	.3507	.2521	.1768	.0950	0.0000
	3	1.0000	.9463	.8711	.7679	.6389	.4992	.3535	.2554	.1804	.0976	0.0000
	5	1.0000	.9416	.8664	.7632	.6384	.5009	.3562	.2582	.1837	.0999	0.0000

Table 1b. Prolate angular spheroidal functions  $Y_1^{(-)}(n, n-1, c; \eta)$

n	c \eta	0.0	0.1	0.2	0.3	0.4	0.5	0.6	0.7	0.8	0.9	1.0
1	1 2 3	0.0000	.0995	.1950	.2868	.3692	.4412	.5012	.5479	.5809	.6083	.6265
2	1 2 3	0.0000	.0985	.1922	.2742	.3409	.3934	.4366	.4688	.4910	.5074	.5181
3	1 2 3	0.0000	.0990	.1921	.2736	.3384	.3821	.4099	.4273	.4356	.4345	0.0000
4	1 2 3	0.0000	.0980	.1845	.2500	.2984	.3372	.3599	.3697	.3698	.3604	0.0000
5	1 2 3	0.0000	.0985	.1802	.2305	.2610	.2739	.2799	.2794	.2701	.2511	0.0000
6	1 2 3	0.0000	.0975	.1645	.2085	.2345	.2421	.2398	.2287	.2119	.1861	0.0000
7	1 2 3	0.0000	.0970	.1500	.1885	.2063	.2077	.2008	.1712	.1303	.0897	0.0000
8	1 2 3	0.0000	.0975	.1444	.1790	.1943	.1966	.1866	.1425	.0911	.0497	0.0000
9	1 2 3	0.0000	.0970	.1371	.1675	.1782	.1790	.1653	.1115	.0662	.0332	0.0000
10	1 2 3	0.0000	.0965	.1307	.1571	.1642	.1633	.1452	.0873	.0457	.0217	0.0000
		0.0000	.0960	.1242	.1471	.1500	.1477	.1253	.0733	.0397	.0196	0.0000
		0.0000	.0955	.1173	.1371	.1370	.1329	.1146	.0623	.0328	.0163	0.0000
		0.0000	.0950	.1100	.1266	.1235	.1174	.1046	.0522	.0238	.0122	0.0000
		0.0000	.0945	.1030	.1166	.1100	.1013	.0877	.0414	.0184	.0094	0.0000
		0.0000	.0940	.0966	.1075	.0982	.0863	.0733	.0377	.0177	.0091	0.0000
		0.0000	.0935	.0900	.0985	.0870	.0726	.0586	.0310	.0163	.0088	0.0000
		0.0000	.0930	.0833	.0884	.0748	.0586	.0441	.0227	.0122	.0068	0.0000
		0.0000	.0925	.0750	.0775	.0610	.0425	.0300	.0159	.0086	.0049	0.0000
		0.0000	.0920	.0685	.0685	.0500	.0356	.0241	.0129	.0071	.0038	0.0000
		0.0000	.0915	.0630	.0610	.0400	.0287	.0198	.0107	.0051	.0025	0.0000
		0.0000	.0910	.0585	.0555	.0325	.0232	.0163	.0087	.0042	.0021	0.0000
		0.0000	.0905	.0540	.0495	.0275	.0198	.0142	.0075	.0038	.0019	0.0000
		0.0000	.0900	.0500	.0445	.0245	.0177	.0130	.0068	.0033	.0016	0.0000
		0.0000	.0895	.0465	.0400	.0215	.0155	.0115	.0059	.0028	.0014	0.0000
		0.0000	.0890	.0435	.0360	.0195	.0140	.0105	.0052	.0025	.0012	0.0000
		0.0000	.0885	.0410	.0330	.0180	.0130	.0095	.0048	.0022	.0011	0.0000
		0.0000	.0880	.0385	.0300	.0165	.0120	.0085	.0042	.0019	.0009	0.0000
		0.0000	.0875	.0365	.0275	.0155	.0110	.0075	.0038	.0017	.0008	0.0000
		0.0000	.0870	.0350	.0255	.0145	.0105	.0070	.0033	.0015	.0007	0.0000
		0.0000	.0865	.0340	.0245	.0140	.0100	.0065	.0030	.0014	.0006	0.0000
		0.0000	.0860	.0335	.0240	.0135	.0095	.0060	.0028	.0013	.0005	0.0000
		0.0000	.0855	.0330	.0235	.0130	.0090	.0055	.0026	.0012	.0005	0.0000
		0.0000	.0850	.0325	.0230	.0125	.0085	.0050	.0024	.0011	.0004	0.0000
		0.0000	.0845	.0320	.0225	.0120	.0080	.0045	.0022	.0010	.0003	0.0000
		0.0000	.0840	.0315	.0220	.0115	.0075	.0040	.0020	.0009	.0002	0.0000
		0.0000	.0835	.0310	.0215	.0110	.0070	.0035	.0018	.0008	.0002	0.0000
		0.0000	.0830	.0305	.0210	.0105	.0065	.0030	.0016	.0007	.0002	0.0000
		0.0000	.0825	.0300	.0205	.0100	.0060	.0025	.0014	.0006	.0002	0.0000
		0.0000	.0820	.0295	.0200	.0095	.0055	.0020	.0012	.0005	.0002	0.0000
		0.0000	.0815	.0290	.0195	.0090	.0050	.0015	.0010	.0004	.0002	0.0000
		0.0000	.0810	.0285	.0190	.0085	.0045	.0010	.0008	.0003	.0002	0.0000
		0.0000	.0805	.0280	.0185	.0080	.0040	.0005	.0006	.0002	.0002	0.0000
		0.0000	.0800	.0275	.0180	.0075	.0035	.0000	.0004	.0001	.0001	0.0000



Table 1c. Prolate angular spheroidal functions  $Y_q^{(+)}(n, m=2, c; \eta)$

$n$	$q$	$c \backslash \eta$	0.0	0.1	0.2	0.3	0.4	0.5	0.6	0.7	0.8	0.9	1.0	
2	0	1	1.0000	0.956	0.9630	0.9183	0.8504	0.7659	0.6334	0.4145	0.2244	0.101	0.3406	
		2	1.0000	0.368	0.337	0.623	0.666	0.566	0.540	0.422	0.287	0.155	0.087	0.1370
		3	1.0000	0.3780	0.914	0.8167	0.6954	0.527	0.306	0.091	0.000	0.000	0.000	0.0613
2	2	1	1.0000	0.496	0.033	0.5635	0.494	0.139	0.3364	0.9660	1.3938	1.7974	2.1602	2.1602
		2	1.0000	0.373	0.7159	0.398	0.273	0.159	0.028	0.9028	1.6231	1.8231	1.8513	1.9764
		3	1.0000	0.3736	0.6330	0.2230	0.0549	0.000	0.000	0.000	0.000	0.000	0.000	0.000
3	0	1	1.0000	0.871	0.9409	0.875	0.8057	0.7372	0.5964	0.4772	0.3525	0.2214	0.0800	0.0000
		2	1.0000	0.935	0.9237	0.8350	0.7224	0.5954	0.4639	0.3370	0.2114	0.0900	0.0000	0.0000
		3	1.0000	0.9745	0.9015	0.7903	0.6546	0.5096	0.3696	0.2459	0.1451	0.0690	0.0000	0.0000
3	2	1	1.0000	0.2277	0.7029	0.3619	0.0611	0.5162	0.9439	1.3765	1.8330	2.2814	2.7374	3.1000
		2	1.0000	0.3013	0.6204	0.2024	0.000	0.7840	1.1560	1.5600	1.9914	2.4110	2.8160	3.1800
		3	1.0000	0.3793	0.5330	0.0515	0.000	0.9360	1.2833	1.6067	1.8030	1.9627	2.0000	2.0000
4	0	1	1.0000	0.828	0.9334	0.8521	0.7471	0.6241	0.4907	0.3546	0.2233	0.0933	0.0000	0.0000
		2	1.0000	0.9585	0.9085	0.8035	0.6721	0.5391	0.4060	0.2840	0.1641	0.0441	0.007	0.0000
		3	1.0000	0.9706	0.8868	0.7608	0.6101	0.4737	0.3086	0.1871	0.0956	0.0345	0.0000	0.0000
4	2	1	1.0000	0.897	0.810	0.631	0.3129	0.096	0.1536	0.1166	0.0062	0.0000	0.0000	0.0000
		2	1.0000	0.8532	0.4533	0.000	0.000	0.9472	1.3512	1.7590	2.1000	2.3800	2.6000	2.7374
		3	1.0000	0.9283	0.7709	0.5161	0.297	0.167	0.000	0.3922	0.692	1.000	1.300	1.5000
5	0	1	1.0000	0.9564	0.873	0.7304	0.568	0.4095	0.2542	0.1394	0.0609	0.0164	0.0000	0.0000
		2	1.0000	0.8415	0.4432	0.000	0.000	0.9766	1.3740	1.7256	2.0000	2.2000	2.3000	2.3000
		3	1.0000	0.828	0.3689	0.000	0.000	1.1317	1.5137	1.7330	1.8695	1.9000	1.9000	1.9000
6	0	1	1.0000	0.9337	0.876	0.7806	0.6351	0.4771	0.3229	0.1860	0.0847	0.0210	0.0000	0.0000
		2	1.0000	0.9620	0.8554	0.7000	0.5230	0.4003	0.2577	0.1381	0.0562	0.0000	0.0000	0.0000
		3	1.0000	0.890	0.4322	0.000	0.000	0.9916	1.3298	1.6000	1.8000	1.9000	1.9000	1.9000
6	2	1	1.0000	0.874	0.3686	0.000	0.000	1.1538	1.2998	1.4906	1.595	1.6000	1.6000	1.6000
		2	1.0000	0.8049	0.2903	0.000	0.000	1.2216	1.1911	1.2922	1.3922	1.4000	1.4000	1.4000
		3	1.0000	0.8049	0.2903	0.000	0.000	1.2216	1.1911	1.2922	1.3922	1.4000	1.4000	1.4000

Table 1d. Prolate angular spheroidal functions  $Y_q(n, n-3, c; \eta)$

$n$	$q$	$c/\eta$	0.0	.1	.2	.3	.4	.5	.6	.7	.8	.9	1.0		
3	1	1	0.0000	.0392	.1934	.2782	.3196	.4845	.4410	.4584	.4570	.4382	.6044		
		2	0.0000	.0395	.1899	.2606	.3113	.3496	.3965	.3529	.3448	.2756	.2248	.1683	
		3	0.0000	.0399	.1863	.2480	.2859	.3160	.3404	.3684	.3908	.4074	.4188	.4244	
3	3	1	0.0000	.0775	.1604	.2352	.2811	.2916	.1403	.1110	.1575	.1527	.1722	.6065	
		2	0.0000	.0776	.1573	.2135	.2468	.2611	.2641	.1403	.1110	.1576	.1527	.1722	.6065
		3	0.0000	.0776	.1558	.2013	.2306	.2456	.2506	.1403	.1110	.1576	.1527	.1722	.6065
4	1	1	0.0000	.0988	.1902	.2676	.3253	.3590	.3449	.3449	.2946	.2946	.2104	0.0000	
		2	0.0000	.0988	.1852	.2519	.2919	.3027	.2855	.2655	.2468	.1858	.1167	0.0000	
		3	0.0000	.0975	.1807	.2382	.2641	.2565	.2268	.2268	.1780	.1220	.0669	0.0000	
4	3	1	0.0000	.0953	.1709	.2057	.1891	.1166	.1028	.1028	.1376	.2568	.3229	0.0000	
		2	0.0000	.0953	.1637	.1849	.1496	.0626	.0578	.0578	.1266	.2745	.2659	0.0000	
		3	0.0000	.0943	.1564	.1643	.1127	.0143	.1038	.1038	.2076	.2541	.2426	0.0000	
5	1	1	0.0000	.0933	.1668	.2565	.3006	.3151	.2986	.2532	.1835	.1835	.0963	0.0000	
		2	0.0000	.0977	.1620	.2420	.2710	.2677	.2358	.1930	.1344	.1135	.0555	0.0000	
		3	0.0000	.0971	.1776	.2291	.2458	.2295	.1885	.1434	.0793	.0793	.0327	0.0000	
5	3	1	0.0000	.0941	.1620	.1794	.1371	.0435	.0805	.1179	.1963	.2550	.2070	0.0000	
		2	0.0000	.0941	.1550	.1597	.1031	0.1000	.1179	.1179	.2400	.2100	.2100	0.0000	
		3	0.0000	.0931	.1478	.1406	.0714	.0362	.1437	.1437	.2114	.2117	.1367	0.0000	
6	1	1	0.0000	.0979	.1832	.2454	.2770	.2752	.2418	.1839	.1127	.0433	0.0000		
		2	0.0000	.0972	.1787	.2320	.2505	.2351	.1925	.1346	.0746	.0256	0.0000		
		3	0.0000	.0967	.1745	.2198	.2276	.2021	.1546	.0996	.0501	.0153	0.0000		
6	3	1	0.0000	.0933	.1536	.1554	.0944	.0124	.1289	.1289	.2085	.2037	.1184	0.0000	
		2	0.0000	.0929	.1466	.1370	.0844	.0454	.1497	.1497	.2448	.2040	.0935	0.0000	
		3	0.0000	.0919	.1397	.1192	.0373	.0719	.1618	.1618	.1945	.1578	.0726	0.0000	
7	1	1	0.0000	.0974	.1797	.2346	.2548	.2397	.1951	.1329	.0637	.0193	0.0000		
		2	0.0000	.0968	.1734	.2205	.2310	.2056	.1563	.0981	.0461	.0116	0.0000		
		3	0.0000	.0962	.1713	.2105	.2202	.1772	.1260	.0730	.0312	.0070	0.0000		
7	3	1	0.0000	.0928	.1455	.1335	.0378	.0535	.0541	.1371	.1590	.1590	.0637	0.0000	
		2	0.0000	.0928	.1387	.1163	.0318	.0775	.1631	.1631	.1971	.1350	.0490	0.0000	
		3	0.0000	.0908	.1319	.0998	.0089	.1967	.1661	.1661	.1694	.1117	.0372	0.0000	

Table 1e. Prolate angular spheroidal functions  $Y_q^{(+)}(n, n-4, c; \eta)$

$n$	$q$	$c \backslash \eta$	0.0	.1	.2	.3	.4
4	4	1	1.00000	.4727	.5171	.0092	-.5352
		2	1.00000	.3411	.4083	-.1765	-.7416
		3	1.00000	.3069	.2942	-.3563	-.9099
		4	1.00000	.2701	.1784	-.5223	-1.0265
		5	1.00000	.7323	.1643	-.6681	-1.0958
4	2	1	1.00000	.3373	.7565	.4710	.1050
		2	1.00000	.9049	.6343	.2338	-.2450
		3	1.00000	.3744	.5255	.0297	-.5084
		4	1.00000	.3462	.4284	-.1381	-.7052
		5	1.00000	.3133	.3403	-.2810	-.8543
4	0	1	1.00000	.3873	.9438	.8838	.8137
		2	1.00000	.3793	.9192	.8260	.7089
		3	1.00000	.3727	.8946	.7767	.6345
		4	1.00000	.3667	.8727	.7343	.5738
		5	1.00000	.3611	.8525	.6964	.5218
5	4	1	1.00000	.8264	.3580	-.2596	-.8196
		2	1.00000	.7597	.2434	-.4237	-.9556
		3	1.00000	.7281	.1431	-.5735	-1.0474
		4	1.00000	.7213	.0325	-.7051	-1.0941
		5	1.00000	.5843	-.0717	-.8165	-1.0981
5	2	1	1.00000	.3146	.6694	.2963	-.1554
		2	1.00000	.3843	.5601	.0911	-.4319
		3	1.00000	.3554	.4594	-.0864	-.6468
		4	1.00000	.3231	.3663	-.3333	-.8119
		5	1.00000	.3017	.2813	-.5729	-.9333
5	0	1	1.00000	.3845	.9389	.8664	.7715
		2	1.00000	.3756	.9031	.8053	.6765
		3	1.00000	.3699	.8842	.7561	.6041
		4	1.00000	.3637	.8623	.7138	.5447
		5	1.00000	.3593	.8415	.6760	.4941
6	4	1	1.00000	.7823	.2143	-.4719	-.9767
		2	1.00000	.7481	.1132	-.6086	-1.0435
		3	1.00000	.7129	.0373	-.7282	-1.0703
		4	1.00000	.6774	-.0926	-.8293	-1.0593
		5	1.00000	.6444	-.1883	-.9110	-1.0147
6	2	1	1.00000	.3942	.5846	.3358	-.3717
		2	1.00000	.3674	.4836	-.3431	-.5896
		3	1.00000	.3375	.3895	-.4995	-.7598
		4	1.00000	.3113	.3023	-.6359	-.8909
		5	1.00000	.2813	.2232	-.7653	-.9905
6	0	1	1.00000	.3813	.9250	.8362	.7284
		2	1.00000	.3732	.8972	.7836	.6445
		3	1.00000	.3655	.8733	.7333	.5857
		4	1.00000	.3593	.8517	.6939	.5334
		5	1.00000	.3547	.8316	.6635	.4885
7	4	1	1.00000	.7314	.2026	-.6457	-1.0578
		2	1.00000	.7038	.0179	-.7534	-1.0770
		3	1.00000	.6833	-.1147	-.8551	-1.0608
		4	1.00000	.6633	-.2081	-.9326	-1.0131
		5	1.00000	.5981	-.2963	-.9919	-.9385
7	2	1	1.00000	.3673	.5010	-.3168	-.5657
		2	1.00000	.8394	.4056	-.1781	-.7467
		3	1.00000	.9123	.3162	-.3231	-.8879
		4	1.00000	.7855	.2324	-.4447	-.9262
		5	1.00000	.7623	.1536	-.5541	-1.0776
7	0	1	1.00000	.3736	.9087	.8032	.6702
		2	1.00000	.3633	.8824	.7507	.5939
		3	1.00000	.3521	.8582	.7059	.5316
		4	1.00000	.3537	.8366	.6662	.4795
		5	1.00000	.3513	.8164	.6334	.4344

	.5	.6	.7	.8	.9	1.0
-1.9751	-1.1624	-.9600	-.2598	1.0040	2.0846	2.8460
-1.1404	-1.1138	-.6789	-.2085	1.4757	2.0985	2.9850
-1.1493	-1.9452	-.2862	-.7223	1.3945	3.0190	2.0190
-1.1072	-.6798	-.1606	1.1973	2.1767	2.8918	2.0190
-.9902	-.3555	-.5978	1.5661	2.2841	2.6125	2.6125
-.3117	-.7461	-1.1645	-1.5358	-1.8340	-2.0401	-2.0401
-.7232	-1.4380	-1.4374	-1.5905	-1.5904	-1.4521	-1.4521
-.9826	-1.4098	-1.4464	-1.3927	-1.1856	-.8842	-.8842
-1.1388	-1.3569	-1.3446	-1.1462	-.8401	-.5099	-.5099
-1.1282	-1.3369	-1.2053	-.9205	-.5874	-.2906	-.2906
.7169	.6135	.5057	.3987	.2972	.2050	.2050
.5788	.4668	.3229	.2146	.1268	.0613	.0613
.4853	.3446	.2240	.1299	.0635	.0222	.0222
.4138	.2727	.1614	.0831	.0345	.0090	.0090
.3562	.2190	.1189	.0549	.0197	.0039	.0039
-1.1403	-.9384	-.2687	.7697	1.6989	0.0000	0.0000
-1.1022	-.7338	-.0996	1.1313	1.8230	0.0000	0.0000
-1.1305	-.4639	.4801	1.4298	1.8560	0.0000	0.0000
-.8985	-.1570	.8341	1.6381	1.7991	0.0000	0.0000
-.7209	.1592	1.1332	1.7481	1.6694	0.0000	0.0000
-.6239	-1.0406	-1.3342	-1.4300	-1.2260	0.0000	0.0000
-.9090	-1.2515	-1.3957	-1.3088	-.9733	0.0000	0.0000
-1.0914	-1.3289	-1.3256	-1.1039	-.7175	0.0000	0.0000
-1.1998	-1.3256	-1.1987	-.8942	-.5107	0.0000	0.0000
-1.2565	-1.2762	-1.0545	-.7092	-.3577	0.0000	0.0000
.6601	.5388	.4139	.2907	.1708	.0600	.0600
.5359	.3966	.2697	.1628	.0792	.0300	.0300
.4479	.3047	.1865	.0987	.0405	.0100	.0100
.3802	.2396	.1333	.0626	.0220	.0080	.0080
.3259	.1912	.0974	.0409	.0124	.0000	.0000
-1.0331	-.5245	.4185	1.3534	1.5524	0.0000	0.0000
-.9306	-.2408	.7609	1.5558	1.4994	0.0000	0.0000
-.7803	.0598	1.0587	1.6663	1.3925	0.0000	0.0000
-.5941	.3571	1.2971	1.6966	1.2500	0.0000	0.0000
-.3848	.6345	1.4695	1.6593	1.0894	0.0000	0.0000
-.8402	-1.1729	-1.2888	-1.1356	-.6978	0.0000	0.0000
-1.0260	-1.2530	-1.2240	-.9543	-.5122	0.0000	0.0000
-1.1394	-1.2536	-1.1042	-.7677	-.3610	0.0000	0.0000
-1.1999	-1.2069	-.9664	-.6024	-.2488	0.0000	0.0000
-1.2227	-1.1340	-.8301	-.4658	-.1693	0.0000	0.0000
.6348	.4761	.3492	.2281	.1128	.0000	.0000
.5086	.3772	.2619	.1639	.0799	.0000	.0000
.4377	.3095	.2053	.1254	.0591	.0000	.0000
.3820	.2591	.1659	.0986	.0451	.0000	.0000
.3362	.2197	.1370	.0783	.0344	.0000	.0000
-.8810	-.1175	.6810	1.4894	1.1060	0.0000	0.0000
-.7309	.1575	1.1164	1.5272	.9949	0.0000	0.0000
-.5489	.4275	1.3010	1.5099	.8726	0.0000	0.0000
-.3463	.6781	1.4802	1.4468	.7477	0.0000	0.0000
-.1338	.8993	1.5050	1.3497	.6273	0.0000	0.0000
-1.0149	-1.2518	-1.2100	-.8938	-.4010	0.0000	0.0000
-1.1847	-1.2723	-1.1131	-.7391	-.2948	0.0000	0.0000
-1.2183	-1.2386	-.9884	-.5928	-.2108	0.0000	0.0000
-1.2804	-1.1729	-.6581	-.4655	-.1481	0.0000	0.0000
-1.2525	-1.0950	-.7338	-.3626	-.1031	0.0000	0.0000
.5226	.3738	.2367	.1225	.0401	.0000	.0000
.4319	.2832	.1613	.0736	.0208	.0000	.0000
.3628	.2196	.1135	.0460	.0112	.0000	.0000
.3081	.1730	.0815	.0295	.0063	.0000	.0000
.2637	.1378	.0595	.0194	.0036	.0000	.0000

Table 1f. Prolate angular spheroidal functions  $Y_q^{(-)}(n, n-5, c; \eta)$

$n$	$q$	$c$	$\eta$	0.0	.1	.2	.3
5	5	1	0.0000	.00000	.3953	.1560	.1616
		2	0.0000	.00000	.3931	.1475	.1387
		3	0.0000	.00000	.0918	.4385	.1156
		4	0.0000	.00000	.3984	.1292	.0627
		5	0.0000	.00000	.3883	.1196	.0706
5	3	1	0.0000	.00000	.3971	.1774	.2261
		2	0.0000	.00000	.3953	.1672	.1955
		3	0.0000	.00000	.3944	.1572	.1667
		4	0.0000	.00000	.3930	.1478	.1411
		5	0.0000	.00000	.3913	.1391	.1187
5	1	1	0.0000	.00000	.0939	.1911	.2707
		2	0.0000	.00000	.0980	.1847	.2504
		3	0.0000	.00000	.0973	.1795	.2348
		4	0.0000	.00000	.0967	.1750	.2216
		5	0.0000	.00000	.0962	.1708	.2099
6	5	1	0.0000	.00000	.3924	.1425	.1247
		2	0.0000	.00000	.3911	.1337	.1027
		3	0.0000	.00000	.3837	.1247	.0814
		4	0.0000	.00000	.3883	.1156	.0611
		5	0.0000	.00000	.3868	.1066	.0420
6	3	1	0.0000	.00000	.0959	.1685	.1985
		2	0.0000	.00000	.0947	.1591	.1715
		3	0.0000	.00000	.0934	.1499	.1464
		4	0.0000	.00000	.0921	.1412	.1237
		5	0.0000	.00000	.0909	.1329	.1033
6	1	1	0.0000	.00000	.3935	.1885	.2622
		2	0.0000	.00000	.3973	.1825	.2437
		3	0.0000	.00000	.0971	.1774	.2285
		4	0.0000	.00000	.3964	.1728	.2154
		5	0.0000	.00000	.3953	.1687	.2038
7	5	1	0.0000	.00000	.3955	.1300	.0929
		2	0.0000	.00000	.3892	.1212	.0727
		3	0.0000	.00000	.3878	.1124	.0536
		4	0.0000	.00000	.3854	.1037	.0387
		5	0.0000	.00000	.3843	.0950	.0192
7	3	1	0.0000	.00000	.3943	.1600	.1735
		2	0.0000	.00000	.3935	.1511	.1492
		3	0.0000	.00000	.3923	.1425	.1266
		4	0.0000	.00000	.3911	.1342	.1061
		5	0.0000	.00000	.3899	.1263	.0874
7	1	1	0.0000	.00000	.3981	.1854	.2523
		2	0.0000	.00000	.3974	.1738	.2353
		3	0.0000	.00000	.3957	.1748	.2209
		4	0.0000	.00000	.3951	.1704	.2084
		5	0.0000	.00000	.3955	.1662	.1971
8	5	1	0.0000	.00000	.3833	.1133	.0654
		2	0.0000	.00000	.3874	.1097	.0472
		3	0.0000	.00000	.3850	.1011	.0302
		4	0.0000	.00000	.3846	.0927	.0146
		5	0.0000	.00000	.3831	.0844	.0004
8	3	1	0.0000	.00000	.3937	.1519	.1507
		2	0.0000	.00000	.3924	.1434	.1285
		3	0.0000	.00000	.3912	.1352	.1080
		4	0.0000	.00000	.3900	.1273	.0893
		5	0.0000	.00000	.3889	.1197	.0722
8	1	1	0.0000	.00000	.3977	.1821	.2420
		2	0.0000	.00000	.3970	.1768	.2264
		3	0.0000	.00000	.3963	.1720	.2129
		4	0.0000	.00000	.3957	.1677	.2008
		5	0.0000	.00000	.3951	.1636	.1900

.4	.5	.6	.7	.8	.9	1.0	I
.1041	-.0208	-.1229	-.2012	-.1694	.0444	.5063	I
.0657	-.0458	-.1494	-.1890	-.1137	.1087	.4828	I
.3300	-.0803	-.1608	-.1605	-.0502	.1674	.4590	I
-.0021	-.1052	-.1578	-.1194	.0151	.2152	.4294	I
-.0298	-.1204	-.1424	-.0710	.0750	.2465	.3895	I
.2321	.1896	.0984	-.0361	-.2031	-.3886	-.5761	I
.1710	.0958	-.0180	-.1504	-.2785	-.3811	-.4429	I
.1177	.0222	-.0951	-.2050	-.2825	-.3129	-.2948	I
.0739	-.0310	-.1393	-.2190	-.2509	-.2334	-.1792	I
.0387	-.0682	-.1614	-.2114	-.2095	-.1667	-.1043	I
.3328	.3739	.3926	.3891	.3654	.3249	.2720	I
.2892	.2989	.2820	.2439	.1926	.1364	.0828	I
.2575	.2485	.2147	.1661	.1135	.0660	.0252	I
.2321	.2108	.1685	.1182	.0713	.0349	.0115	I
.2106	.1808	.1345	.0863	.0465	.0195	.0048	I
.0415	-.0723	-.1575	-.1494	-.0106	.2112	0.0000	I
.0098	-.0981	-.1563	-.1120	.0422	.2284	0.0000	I
-.0181	-.1151	-.1442	-.1691	.0891	.2354	0.0000	I
-.0417	-.1239	-.1236	-.0247	.1271	.2323	0.0000	I
-.0668	-.1252	-.0972	-.0174	.1544	.2203	0.0000	I
.1752	.0983	-.0202	-.1550	-.2720	-.3104	0.0000	I
.1251	.0296	-.0903	-.2015	-.2682	-.2539	0.0000	I
.0818	-.0233	-.1344	-.2155	-.2399	-.1940	0.0000	I
.0456	-.0621	-.1583	-.2097	-.2023	-.1418	0.0000	I
.0156	-.0896	-.1682	-.1935	-.1648	-.1010	0.0000	I
.3135	.3386	.3359	.3061	.2509	.1705	0.0000	I
.2749	.2750	.2476	.2001	.1417	.0804	0.0000	I
.2449	.2290	.1892	.1374	.0852	.0408	0.0000	I
.2204	.1937	.1480	.0976	.0535	.0219	0.0000	I
.1995	.1655	.1176	.0708	.0347	.0123	0.0000	I
-.0049	-.1085	-.1462	-.0691	.0998	.2195	0.0000	I
-.0297	-.1202	-.1289	-.0283	.1308	.2086	0.0000	I
-.0514	-.1246	-.1056	.0111	.1531	.1929	0.0000	I
-.0670	-.1226	-.0785	.0467	.1665	.1738	0.0000	I
-.0795	-.1154	-.0498	.0767	.1715	.1528	0.0000	I
.1273	.0299	-.0928	-.1018	-.2511	-.1955	0.0000	I
.0853	-.0210	-.1337	-.2119	-.2223	-.1494	0.0000	I
.0492	-.0595	-.1569	-.2055	-.1876	-.1101	0.0000	I
.0189	-.0874	-.1669	-.1897	-.1531	-.0791	0.0000	I
-.00863	-.1068	-.1680	-.1695	-.1222	-.0558	0.0000	I
.2918	.3306	.2788	.2302	.1616	.117	0.0000	I
.2577	.2470	.2094	.1549	.0954	.0412	0.0000	I
.2302	.2066	.1613	.1078	.0587	.0218	0.0000	I
.2072	.1750	.1265	.0769	.0372	.0120	0.0000	I
.1875	.1494	.1004	.0558	.0242	.0068	0.0000	I
-.0389	-.1225	-.1132	.0054	.1529	.1697	0.0000	I
-.0574	-.1236	-.1884	.0396	.1638	.1509	0.0000	I
-.0719	-.1192	-.0613	.0692	.1676	.1317	0.0000	I
-.0827	-.1104	-.0337	.0933	.1654	.1127	0.0000	I
-.0900	-.0981	-.1070	.1114	.1583	.0948	0.0000	I
.0866	-.0214	-.1351	-.2083	-.2031	-.1114	0.0000	I
.0511	-.0589	-.1565	-.2003	-.1705	-.0822	0.0000	I
.0209	-.0865	-.1559	-.1843	-.1391	-.0592	0.0000	I
-.0045	-.1059	-.1658	-.1846	-.1141	-.0290	0.0000	I
-.0256	-.1189	-.1620	-.1439	-.0874	-.0284	0.0000	I
.2702	.2645	.2283	.1699	.1014	.0378	0.0000	I
.2399	.2193	.1739	.1152	.0517	.0199	0.0000	I
.2148	.1843	.1350	.0752	.0387	.0109	0.0000	I
.1936	.1564	.1062	.0590	.0248	.0061	0.0000	I
.1752	.1337	.0845	.0430	.0162	.0035	0.0000	I

Table 2a. Prolate radial spheroidal functions  $x_0^{(+)}(n, n, c; \xi)$

$n$	$c$	1.0	1.2	1.4	1.6	1.8	2.0	2.2	2.4	2.6	2.8	3.0
0	1	1.000	.619	.456	.326	.223	.147	.093	.056	.033	.018	.010
0	2	1.000	.644	.481	.351	.250	.174	.119	.082	.059	.036	.020
0	3	1.000	.517	.337	.206	.111	.063	.033	.019	.010	.005	.002
1	1	0.000	.606	.573	.488	.386	.287	.202	.135	.086	.051	.032
1	2	0.000	.343	.262	.180	.109	.066	.036	.020	.010	.005	.002
1	3	0.000	.353	.288	.215	.149	.083	.041	.024	.012	.006	.003
1	4	0.000	.283	.227	.150	.088	.033	.012	.004	.001	.000	.000
2	1	0.000	.234	.188	.116	.058	.024	.012	.006	.002	.001	.000
2	2	0.000	.180	.133	.073	.037	.017	.008	.004	.002	.001	.000
2	3	0.000	.151	.104	.053	.025	.012	.006	.003	.001	.000	.000
2	4	0.000	.125	.077	.037	.017	.008	.004	.002	.001	.000	.000
2	5	0.000	.100	.052	.023	.010	.005	.002	.001	.000	.000	.000
3	1	0.000	.103	.059	.026	.011	.005	.002	.001	.000	.000	.000
3	2	0.000	.083	.043	.018	.008	.004	.002	.001	.000	.000	.000
3	3	0.000	.066	.033	.013	.006	.003	.001	.000	.000	.000	.000
3	4	0.000	.056	.027	.010	.005	.002	.001	.000	.000	.000	.000
3	5	0.000	.044	.020	.008	.004	.002	.001	.000	.000	.000	.000
4	1	0.000	.055	.025	.010	.005	.002	.001	.000	.000	.000	.000
4	2	0.000	.044	.020	.008	.004	.002	.001	.000	.000	.000	.000
4	3	0.000	.033	.015	.006	.003	.001	.000	.000	.000	.000	.000
4	4	0.000	.025	.011	.004	.002	.001	.000	.000	.000	.000	.000
4	5	0.000	.019	.008	.003	.001	.000	.000	.000	.000	.000	.000
5	1	0.000	.020	.009	.003	.001	.000	.000	.000	.000	.000	.000
5	2	0.000	.015	.006	.002	.001	.000	.000	.000	.000	.000	.000
5	3	0.000	.010	.004	.001	.000	.000	.000	.000	.000	.000	.000
5	4	0.000	.007	.003	.001	.000	.000	.000	.000	.000	.000	.000
5	5	0.000	.005	.002	.001	.000	.000	.000	.000	.000	.000	.000
6	1	0.000	.005	.002	.001	.000	.000	.000	.000	.000	.000	.000
6	2	0.000	.004	.001	.000	.000	.000	.000	.000	.000	.000	.000
6	3	0.000	.003	.001	.000	.000	.000	.000	.000	.000	.000	.000
6	4	0.000	.002	.001	.000	.000	.000	.000	.000	.000	.000	.000
6	5	0.000	.001	.000	.000	.000	.000	.000	.000	.000	.000	.000
7	1	0.000	.002	.001	.000	.000	.000	.000	.000	.000	.000	.000
7	2	0.000	.001	.000	.000	.000	.000	.000	.000	.000	.000	.000
7	3	0.000	.001	.000	.000	.000	.000	.000	.000	.000	.000	.000
7	4	0.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000
7	5	0.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000
8	1	0.000	.001	.000	.000	.000	.000	.000	.000	.000	.000	.000
8	2	0.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000
8	3	0.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000
8	4	0.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000
8	5	0.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000
9	1	0.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000
9	2	0.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000
9	3	0.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000
9	4	0.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000
9	5	0.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000

Table 2b. Prolate radial spheroidal functions  $x^{(-)}(n, n-1, c; \xi)$

$n$	$c \backslash \xi$	1.0	1.2	1.4	1.6	1.8	2.0	2.2	2.4	2.6	2.8	3.0
1	1	1.000	.963	.866	.733	.587	.446	.323	.222	.146	.092	.055
	2	1.000	.773	.536	.336	.192	.100	.047	.021	.008	.003	.001
	3	1.000	.620	.332	.154	.063	.022	.007	.002	.000	.000	.000
2	1	0.000	.639	.899	.916	.879	.773	.632	.485	.350	.240	.155
	2	0.000	.411	.535	.420	.287	.172	.093	.045	.020	.008	.003
	3	0.000	.111	.325	.493	.609	.638	.514	.384	.240	.100	.000
3	1	0.000	.124	.892	1.144	1.316	1.339	1.239	1.057	.847	.627	.440
	2	0.000	.279	.518	.624	.610	.539	.427	.308	.207	.120	.060
	3	0.000	.000	.318	.524	.640	.667	.527	.389	.263	.160	.080
4	1	0.000	.281	.815	1.429	1.969	2.319	2.457	2.307	2.010	1.639	1.233
	2	0.000	.561	.949	1.655	2.462	3.177	3.556	3.213	2.733	2.213	1.684
	3	0.000	.000	.312	.530	.710	.815	.852	.820	.706	.562	.400
5	1	0.000	.186	.738	1.285	2.047	2.816	3.255	3.033	2.642	2.285	1.917
	2	0.000	.450	.830	1.375	2.161	2.906	3.267	2.956	2.466	2.015	1.604
	3	0.000	.000	.220	.375	.514	.600	.612	.543	.415	.285	.160
6	1	0.000	.164	.782	1.222	1.839	2.552	2.920	2.516	2.016	1.520	1.128
	2	0.000	.380	.730	1.065	1.470	1.946	2.200	1.904	1.521	1.128	.803
	3	0.000	.000	.080	.165	.240	.280	.280	.200	.104	.037	.012
7	1	0.000	.082	.766	1.276	1.801	2.389	2.677	2.217	1.566	.959	.515
	2	0.000	.253	.693	1.085	1.473	1.960	2.333	2.050	1.588	.931	.409
	3	0.000	.000	.054	.104	.154	.180	.180	.120	.060	.031	.012
8	1	0.000	.054	.751	1.594	2.223	2.870	3.268	2.678	1.840	1.080	.572
	2	0.000	.154	.655	1.594	2.223	2.870	3.268	2.678	1.840	1.080	.572
	3	0.000	.000	.035	.073	.102	.110	.110	.073	.035	.012	.007
9	1	0.000	.036	.736	1.991	2.824	3.647	4.022	3.054	2.054	1.128	.633
	2	0.000	.082	.622	1.913	2.824	3.647	4.022	3.054	2.054	1.128	.633
	3	0.000	.000	.023	.046	.069	.073	.073	.046	.023	.010	.006
10	1	0.000	.024	.721	2.425	3.430	4.269	4.269	2.878	1.655	.847	.453
	2	0.000	.049	.646	2.425	3.430	4.269	4.269	2.878	1.655	.847	.453
	3	0.000	.005	.276	1.140	2.356	3.117	3.117	2.131	1.215	.561	.224



Table 2c. Prolate radial spheroidal functions  $X_k^{(+)}(n, n-2, c; \xi)$

$n$	$k$	$\xi$	1.0	1.2	1.4	1.6	1.8	2.0	2.2	2.4	2.6	2.8	3.0	
2	0	1	1.000	1.255	1.380	1.374	1.262	1.080	.868	.657	.470	.319	.206	
		2	1.000	.980	.819	.599	.286	.277	.219	.119	.057	.025	.010	.004
		3	1.000	.776	.496	.267	.123	.049	.017	.005	.001	.000	.000	.000
3	1	1	1.000	.527	.155	-.100	-.244	.300	-.293	-.251	-.196	-.142	-.086	
		2	1.000	.166	-.343	-.300	-.296	-.282	-.118	-.069	-.027	-.011	-.004	
		3	1.000	-.083	-.303	-.300	-.170	-.077	-.029	-.009	-.003	-.001	-.000	
3	0	1	0.000	.878	1.290	1.622	1.774	1.749	1.584	1.332	1.047	.773	.539	
		2	0.000	.640	.783	.726	.564	.379	.225	.119	.033	.017	.010	.000
		3	0.000	.510	.479	.328	.181	.083	.032	.011	.003	.001	.000	.000
4	1	1	0.000	.433	.359	.193	.023	-.107	-.182	-.207	-.195	-.163	-.124	
		2	0.000	.261	.057	-.099	-.156	-.142	-.101	-.060	-.031	-.014	-.006	
		3	0.000	.138	-.070	-.134	-.106	-.089	-.026	-.009	-.003	-.001	-.000	
4	0	1	0.000	.528	1.289	1.974	2.579	2.936	3.003	2.887	2.425	1.951	1.478	
		2	0.000	.421	.757	.892	.828	.644	.432	.255	.124	.063	.026	
		3	0.000	.336	.465	.405	.267	.142	.063	.023	.007	.002	.000	
4	1	1	0.000	.307	.426	.386	.247	.076	-.075	-.179	-.227	-.228	.200	
		2	0.000	.209	.154	.019	-.083	-.142	-.109	-.076	-.045	-.027	-.023	.010
		3	0.000	.135	.037	-.065	-.083	-.059	-.031	-.013	-.004	-.001	-.000	
5	0	1	0.000	.378	1.198	2.428	3.794	4.982	5.771	6.082	5.791	4.996	4.068	
		2	0.000	.222	.753	1.103	1.523	1.801	.936	.549	.316	.161	.074	
		3	0.000	.147	.453	.502	.396	.244	.121	.059	.016	.005	.001	
5	1	1	0.000	.211	.455	.577	.538	.370	.142	-.077	-.238	-.323	.338	
		2	0.000	.104	.273	.415	-.066	-.093	-.124	-.106	-.087	-.072	-.041	
		3	0.000	.073	.073	-.017	-.086	-.083	-.087	-.087	-.087	-.087	-.087	
6	0	1	0.000	.284	1.164	3.063	5.614	8.541	11.164	12.921	13.596	12.883	11.342	
		2	0.000	.147	.716	1.367	1.618	1.909	.951	.549	.316	.161	.074	
		3	0.000	.104	.441	.624	.590	.419	.236	.109	.042	.017	.004	
6	1	1	0.000	.143	.469	.795	.961	.697	.337	.256	.116	.040	.557	
		2	0.000	.104	.227	.408	.088	-.063	-.129	-.050	-.030	-.013	-.043	
		3	0.000	.075	.100	.028	-.046	-.069	-.054	-.030	-.013	-.005	-.001	

Table 2d. Prolate radial spheroidal functions  $X_K^{(-)}(n, n-3, c; \xi)$

$n$	$k$	$\xi$	1.0	1.2	1.4	1.5	1.6	1.8	2.0	2.2	2.4	2.6	2.8	3.0	
3	0	1.000	1.810	2.530	3.022	3.216	3.124	2.800	2.337	1.827	1.345	.934	.535	.15	
		1.000	1.316	1.404	1.221	.916	.624	.353	.047	.186	.068	.038	.015	.001	.000
		1.000	1.030	.809	.515	.273	.122	.047	.015	.015	.004	.001	.000	.000	.000
3	1	1.000	.751	.450	.161	-.070	-.223	-.297	-.307	-.274	-.222	-.165	-.021	-.000	
		1.000	.369	-.074	-.327	-.318	-.255	-.168	-.046	-.016	-.048	-.001	-.000	-.000	-.000
		1.000	.074	-.305	-.327	-.318	-.255	-.168	-.046	-.016	-.048	-.001	-.000	-.000	-.000
4	0	0.000	1.080	2.127	3.158	3.960	4.411	4.439	4.103	3.515	2.810	2.106	1.386	.805	
		0.000	.838	1.253	1.365	1.214	.919	.606	.353	.031	.183	.003	.000	.000	.000
		0.000	.657	.748	.600	.378	.195	.084	.031	.010	.110	.003	.000	.000	.000
4	1	0.000	.549	.589	.461	.251	.034	-.142	-.251	-.293	-.283	-.241	-.203	-.163	
		0.000	.356	.176	-.034	-.158	-.186	-.154	-.059	-.018	-.059	-.029	-.013	-.000	-.000
		0.000	.211	-.020	-.140	-.138	-.089	-.044	-.018	-.018	-.006	-.002	-.000	-.000	-.000
5	0	0.000	.686	1.953	3.650	5.453	6.978	7.916	8.124	7.644	6.643	5.377	4.207	3.094	
		0.000	.540	1.173	1.615	1.711	1.494	1.111	.719	.419	.240	.127	.074	.044	
		0.000	.427	.710	.721	.542	.323	.158	.064	.022	.022	.007	.000	.000	.000
5	1	0.000	.273	.642	.720	.646	.385	.109	-.137	-.309	-.391	-.395	-.350	-.304	
		0.000	.179	.268	.115	-.056	-.149	-.109	-.035	-.025	-.009	-.003	-.001	-.000	-.000
		0.000	.179	.080	-.052	-.175	-.089	-.053	-.025	-.009	-.009	-.003	-.001	-.000	-.000
6	0	0.000	.444	1.844	4.361	7.769	11.467	15.683	16.747	17.301	16.370	14.324	12.319	10.517	
		0.000	.352	1.118	1.952	2.469	2.487	2.090	1.583	1.136	.941	.819	.754	.700	
		0.000	.279	.681	.870	.789	.543	.299	.136	.052	.022	.017	.005	.000	.000
6	1	0.000	.258	.666	1.005	1.331	.996	.655	.219	-.192	-.492	-.648	-.648		
		0.000	.186	.313	.252	.073	-.094	-.183	-.307	-.407	-.444	-.492	-.549	-.606	
		0.000	.133	.130	.015	-.076	-.095	-.070	-.037	-.016	-.016	-.006	-.002	-.000	-.000
7	0	0.000	.290	1.793	5.290	11.257	19.185	27.747	35.390	39.954	41.185	38.932	36.032	33.232	
		0.000	.230	1.076	2.368	3.682	4.193	3.980	3.484	2.889	2.192	1.516	.946	.519	
		0.000	.183	.658	1.077	1.457	1.573	1.221	.829	.421	.121	.042	.016	.000	.000
7	1	0.000	.173	.677	1.343	1.898	2.102	1.854	1.237	.711	.371	.171	.093	.053	
		0.000	.139	.339	.403	.268	.019	-.176	-.257	-.359	-.441	-.473	-.504	-.534	
		0.000	.094	.159	.083	-.038	-.100	-.094	-.059	-.029	-.029	-.011	-.004	-.000	-.000

Table 2e. Prolate radial spheroidal functions  $X_k^{(+)}(n, n-4, c; \xi)$

$n$	$k$	$c/\xi$	1.0	1.2	1.4	1.6	1.8
4	0	1	1.0	2.837	5.693	7.322	9.051
		2	1.0	2.013	2.693	2.813	2.447
		3	1.0	1.477	1.468	1.116	.684
		4	1.0	1.109	.826	.498	.198
		5	1.0	.848	.477	.194	.059
4	1	1	1.0	1.049	.905	.625	.289
		2	1.0	.919	.470	-.164	-.317
		3	1.0	.278	-.192	-.331	-.271
		4	1.0	.019	-.334	-.290	-.153
		5	1.0	-.165	-.353	-.202	-.073
4	2	1	1.0	.288	-.138	-.303	-.279
		2	1.0	-.141	-.339	-.129	.111
		3	1.0	-.335	-.179	.154	.260
		4	1.0	-.374	.135	.270	.212
		5	1.0	-.323	.192	.263	.128
5	0	1	0.0	1.517	3.745	6.612	9.583
		2	0.0	1.152	2.143	2.769	2.835
		3	0.0	.885	1.245	1.179	.854
		4	0.0	.686	.733	.510	.261
		5	0.0	.536	.436	.223	.081
5	1	1	0.0	.716	.976	.986	.783
		2	0.0	.484	.369	.107	-.124
		3	0.0	.308	.060	-.127	-.178
		4	0.0	.178	-.066	-.146	-.107
		5	0.0	.083	-.112	-.110	-.052
5	2	1	0.0	.344	.177	-.017	-.139
		2	0.0	.137	-.080	-.121	-.043
		3	0.0	.014	-.106	-.022	.064
		4	0.0	-.059	-.061	.047	.073
		5	0.0	-.076	-.009	.067	.050
6	0	1	0.0	.922	3.241	7.151	12.269
		2	0.0	.716	1.910	3.097	3.761
		3	0.0	.559	1.136	1.354	1.465
		4	0.0	.439	.680	.597	.364
		5	0.0	.346	.410	.265	.115
6	1	1	0.0	.482	1.001	1.366	1.442
		2	0.0	.343	.452	.310	.055
		3	0.0	.233	.163	-.012	-.127
		4	0.0	.159	.032	-.081	-.092
		5	0.0	.101	-.027	-.073	-.047
6	2	1	0.0	.266	.293	.171	.007
		2	0.0	.147	.034	-.069	-.074
		3	0.0	.071	-.040	-.046	.009
		4	0.0	-.024	-.044	-.022	.033
		5	0.0	-.063	-.026	.020	.027
7	0	1	0.0	.583	2.958	8.216	16.758
		2	0.0	.457	1.770	3.619	5.234
		3	0.0	.360	1.065	1.565	1.646
		4	0.0	.285	.644	.715	.521
		5	0.0	.225	.391	.320	.166
7	1	1	0.0	.323	1.009	1.809	2.409
		2	0.0	.236	.494	.517	.293
		3	0.0	.173	.222	.087	-.074
		4	0.0	.121	.083	-.032	-.082
		5	0.0	.083	.017	-.049	-.046
7	2	1	0.0	.189	.350	.351	.210
		2	0.0	.118	.098	-.009	-.073
		3	0.0	.069	.004	-.042	-.018
		4	0.0	.037	-.021	-.017	.014
		5	0.0	.017	-.020	.002	.017

2.0	2.2	2.4	2.6	2.8	3.0
9.965	9.968	9.173	7.833	6.246	4.672
1.829	1.196	.692	.358	.166	.065
.347	.148	.054	.017	.005	.001
.068	.019	.004	.001	.000	.000
.014	.003	.000	.000	.000	.000
-.022	-.257	-.391	-.434	-.407	-.340
-.322	-.248	-.160	-.189	-.043	-.019
-.160	-.075	-.029	-.010	-.003	-.001
-.059	-.018	-.004	-.001	-.000	-.000
-.019	-.004	-.001	-.000	-.000	-.000
-.153	-.005	.116	.186	.207	.192
.229	.228	.169	.103	.053	.024
.241	.110	.047	.016	.005	.001
.188	.034	.009	.002	.000	.000
.039	.009	.001	.000	.000	.000
12.037	13.488	13.721	12.821	11.095	8.946
2.423	1.773	1.139	.644	.324	.146
.497	.239	.096	.033	.010	.002
.104	.033	.008	.002	.000	.000
.022	.005	.001	.000	.000	.000
.447	.081	-.231	-.436	-.525	-.518
-.238	-.243	-.188	-.120	-.066	-.032
-.138	-.078	-.035	-.013	-.004	-.001
-.091	-.018	-.005	-.001	-.000	-.000
-.016	-.004	-.001	-.000	-.000	-.000
-.165	-.119	-.039	.039	.095	.120
.046	.091	.090	.066	.040	.020
.081	.057	.029	.012	.004	.001
.046	.019	.006	.001	.000	.000
.019	.005	.001	.000	.000	.000
17.692	22.302	25.155	25.775	24.246	21.102
3.696	3.054	2.170	1.347	.737	.359
.781	.423	.189	.071	.023	.006
.166	.059	.017	.004	.001	.000
.036	.008	.001	.000	.000	.000
1.208	.746	.197	-.300	-.650	-.820
-.160	-.257	-.249	-.185	-.145	-.061
-.138	-.095	-.059	-.021	-.007	-.002
-.055	-.023	-.007	-.002	-.000	-.000
-.018	-.005	-.001	-.000	-.000	-.000
-.115	-.159	-.129	-.057	.023	.085
-.017	.040	.065	.061	.043	.025
.043	.042	.026	.012	.004	.001
.031	.016	.006	.001	.000	.000
.014	.004	.001	.000	.000	.000
27.819	39.526	49.499	55.676	56.981	53.562
5.326	5.234	4.359	2.970	1.770	.931
1.271	.777	.387	.160	.055	.018
.274	.110	.035	.009	.002	.000
.060	.016	.003	.000	.000	.000
2.557	2.173	1.368	.380	-.538	-1.199
-.020	-.252	-.336	-.300	-.212	-.125
-.143	-.125	-.076	-.036	-.014	-.004
-.064	-.032	-.011	-.003	-.001	-.000
-.022	-.007	-.001	-.000	-.000	-.000
-.016	-.140	-.205	-.175	-.085	.021
-.056	-.000	.046	.061	.053	.035
-.021	.035	.027	.015	.006	.002
.023	.015	.006	.002	.000	.000
.012	.004	.001	.000	.000	.000

Table 2f. Prolate radial spheroidal functions  $X_k^{(-)}(n, n-5, c; \xi)$

n	k	$\Delta$	1.	1.2	1.4	1.6	1.8
5	0	1	1.	4.641	17.752	18.568	26.609
		2	1.	3.234	5.560	6.987	7.053
		3	1.	2.286	2.919	2.668	1.897
		4	1.	1.651	1.567	1.043	.522
		5	1.	1.214	.864	.419	.148
5	1	1	1.	1.549	1.815	1.720	1.305
		2	1.	.955	-.571	-.088	-.274
		3	1.	.535	-.004	-.306	-.342
		4	1.	.221	-.260	-.328	-.210
		5	1.	-.017	-.344	-.250	-.106
5	2	1	1.	.548	.128	-.163	-.288
		2	1.	.050	-.313	-.242	-.014
		3	1.	-.240	-.271	.049	.232
		4	1.	-.358	-.373	.232	.236
		5	1.	-.360	.112	.271	.159
6	0	1	0.	2.221	6.924	14.586	24.420
		2	0.	1.655	3.874	5.954	7.350
		3	0.	1.245	2.195	2.472	2.063
		4	0.	.948	1.260	1.039	.613
		5	0.	.723	.732	.443	.185
6	1	1	0.	.973	1.687	2.127	2.143
		2	0.	.657	.708	.419	.021
		3	0.	.441	.224	-.073	-.226
		4	0.	.271	-.002	-.165	-.156
		5	0.	.153	-.095	-.140	-.080
6	2	1	0.	.466	.380	.162	-.055
		2	0.	.220	-.015	-.141	-.105
		3	0.	.077	-.112	-.066	.042
		4	0.	-.018	-.083	.024	.079
		5	0.	-.064	-.036	.064	.061
7	0	1	0.	1.281	5.609	14.574	28.985
		2	0.	.954	3.249	6.233	8.708
		3	0.	.754	1.899	2.573	2.643
		4	0.	.587	1.118	1.157	.810
		5	0.	.458	.664	.505	.250
7	1	1	0.	.632	1.629	2.582	3.399
		2	0.	.452	.767	.717	.356
		3	0.	.313	.323	.088	-.137
		4	0.	.210	.102	-.075	-.132
		5	0.	.145	-.000	-.090	-.073
7	2	1	0.	.333	.484	.416	.206
		2	0.	.207	.111	-.047	-.110
		3	0.	.163	-.323	-.068	-.014
		4	0.	.048	-.043	-.019	.032
		5	0.	.011	-.337	.314	.033
8	0	1	0.	.736	4.918	16.120	37.750
		2	0.	.610	2.904	6.394	11.600
		3	0.	.475	1.724	3.355	3.590
		4	0.	.373	1.030	1.343	1.119
		5	0.	.297	.618	.593	.351
8	1	1	0.	.417	1.586	3.333	5.286
		2	0.	.364	.795	1.043	.828
		3	0.	.221	.375	.241	-.030
		4	0.	.153	.157	-.002	-.111
		5	0.	.111	.050	-.054	-.070
8	2	1	0.	.237	.539	.583	.584
		2	0.	.152	.180	.351	-.080
		3	0.	.084	.033	-.049	-.041
		4	0.	.057	-.015	-.030	.008
		5	0.	.021	-.023	-.005	.119

2.0	2.2	2.4	2.6	2.8	3.0	I
33.200	37.039	37.563	35.020	30.254	24.361	I
5.978	4.362	2.783	1.573	.789	.355	I
1.092	.521	.209	.071	.021	.005	I
.204	.064	.016	.003	.001	.000	I
.039	.008	.001	.000	.000	.000	I
-.703	-.076	-.441	-.772	-.907	-.883	I
-.429	-.411	-.307	-.192	-.104	-.049	I
-.243	-.131	-.057	-.021	-.006	-.002	I
-.094	-.032	-.008	-.000	-.000	-.000	I
-.031	-.007	-.001	-.000	-.000	-.000	I
-.267	-.156	-.017	.103	.177	.204	I
.164	.226	.199	.138	.079	.040	I
.226	.143	.068	.026	.008	.002	I
.129	.049	.014	.003	.001	.000	I
.055	.013	.002	.000	.000	.000	I
34.694	43.303	48.503	49.444	46.331	40.200	I
6.813	5.566	3.925	2.422	1.320	.641	I
1.357	.726	.322	.120	.039	.010	I
.274	.096	.027	.006	.001	.000	I
.056	.013	.002	.000	.000	.000	I
1.728	1.014	-.206	-.504	-.990	-1.214	I
-.280	-.400	-.370	-.269	-.164	-.086	I
-.220	-.144	-.073	-.030	-.010	-.003	I
-.087	-.035	-.011	-.003	-.000	-.000	I
-.029	-.007	-.001	-.000	-.000	-.000	I
-.189	-.216	-.155	-.051	.052	.126	I
-.000	.082	.110	.095	.065	.037	I
.089	.076	.044	.021	.007	.002	I
.061	.029	.010	.002	.001	.000	I
.028	.008	.002	.000	.000	.000	I
47.171	66.140	82.054	91.655	93.309	87.350	I
9.651	8.865	6.928	4.686	2.777	1.454	I
1.995	1.201	.591	.242	.084	.024	I
.417	.164	.051	.013	.003	.000	I
.088	.023	.004	.001	.000	.000	I
3.485	2.872	1.733	-.390	-.824	-1.678	I
-.081	-.383	-.475	-.412	-.286	-.167	I
-.217	-.179	-.105	-.049	-.018	-.006	I
-.095	-.045	-.016	-.004	-.001	-.000	I
-.032	-.010	-.002	-.000	-.000	-.000	I
-.033	-.203	-.255	-.200	-.082	.046	I
-.067	.015	.073	.088	.072	.047	I
.042	.056	.041	.021	.009	.003	I
.040	.024	.010	.003	.001	.000	I
.020	.007	.002	.000	.000	.000	I
70.598	111.437	153.364	187.928	208.043	210.263	I
14.786	15.299	13.268	9.848	6.347	3.589	I
3.120	2.116	1.157	.520	.195	.062	I
.663	.295	.102	.028	.006	.001	I
.142	.041	.009	.001	.000	.000	I
6.584	6.710	5.505	3.277	.640	-1.753	I
-.282	-.275	-.601	-.651	-.522	-.341	I
-.209	-.230	-.162	-.085	-.035	-.012	I
-.110	-.063	-.025	-.008	-.002	-.000	I
-.039	-.014	-.003	-.001	-.000	-.000	I
.296	-.044	-.296	-.383	-.307	-.131	I
-.108	-.045	.037	.085	.090	.068	I
.012	.044	.043	.027	.012	.005	I
.029	.023	.011	.004	.001	.000	I
.017	.007	.002	.000	.000	.000	I

Table 3a. Oblate angular spheroidal functions  $\tilde{Y}_0(n, n, \pi; \bar{\eta})$

$n$	$\bar{\eta}$	.0	.1	.2	.3	.4	.5	.6	.7	.8	.9	1.0
0	1	6055	6096	6188	6344	6570	6873	7261	7749	8353	9094	1.0000
	2	3679	3716	3829	4025	4317	4724	5273	6005	6977	8270	1.0000
	3	2231	2255	2369	2554	2837	3247	3829	4653	5887	7520	1.0000
1	1	6055	6055	6063	6052	6022	5952	5809	5534	5012	3964	0.0000
	2	3679	3679	3752	3840	3957	4091	4218	4288	4186	3605	0.0000
	3	2231	2254	2321	2436	2600	2812	3063	3323	3486	3278	0.0000
2	1	6055	6035	5940	5773	5519	5155	4677	3952	3012	1728	0.0000
	2	3679	3679	3679	3663	3626	3543	3417	3233	2822	1571	0.0000
	3	2231	2242	2275	2324	2393	2485	2451	2373	2238	1429	0.0000
3	1	6055	6025	5820	5508	5088	4464	3718	2822	1804	0753	0.0000
	2	3679	3679	3679	3679	3679	3604	3400	3087	2587	1625	0.0000
	3	2231	2231	2229	2217	2222	2109	1960	1767	1259	0623	0.0000
4	1	6055	5974	5703	5254	4636	3865	2974	2016	1083	0328	0.0000
	2	3679	3679	3679	3633	3406	2957	2160	1562	0974	0299	0.0000
	3	2231	2222	2220	2215	2201	1826	1568	1110	0755	0271	0.0000
5	1	6055	5944	5587	5012	4232	3348	2379	1439	0650	0143	0.0000
	2	3679	3620	3457	3180	2732	2301	1728	1115	0533	0130	0.0000
	3	2231	2209	2139	2017	1834	1582	1255	0964	0443	0118	0.0000
6	1	6055	5915	5475	4781	3894	2900	1904	1028	0390	0062	0.0000
	2	3679	3605	3388	3033	2559	1993	1382	0797	0326	0057	0.0000
	3	2231	2198	2096	1924	1651	1370	1004	0617	0272	0052	0.0000
7	1	6055	5885	5364	4561	3569	2511	1523	0734	0234	0027	0.0000
	2	3679	3587	3319	2894	2339	1726	1106	0569	0195	0025	0.0000
	3	2231	2187	2054	1836	1541	1186	0803	0441	0163	0022	0.0000
8	1	6055	5856	5255	4351	3271	2175	1218	0524	0140	0012	0.0000
	2	3679	3569	3252	2760	2183	1495	0885	0408	0117	0011	0.0000
	3	2231	2176	2012	1751	1472	1027	0642	0315	0098	0010	0.0000
9	1	6055	5826	5149	4150	2988	1883	0975	0374	0084	0005	0.0000
	2	3679	3555	3242	2633	1994	1299	0700	0370	0070	0005	0.0000
	3	2231	2173	1976	1671	1244	0860	0514	0225	0059	0004	0.0000

Table 3b. Oblate angular spheroidal functions  $\tilde{Y}_1(n, n-1, p; \tilde{\eta})$

$n$	$p \setminus \tilde{\eta}$	0.0	.1	.2	.3	.4	.5	.6	.7	.8	.9	1.0	
1	1	0.0000	.0610	.1230	.1903	.2628	.3336	.4057	.4824	.5582	.6384	.7184	1.0000
	2	0.0000	.0372	.0766	.1208	.1727	.2362	.3068	.3824	.4603	.5481	.6443	1.0000
	3	0.0000	.0277	.0574	.0966	.1435	.1972	.2562	.3197	.3857	.4622	.5486	1.0000
2	1	0.0000	.0607	.1213	.1816	.2409	.2976	.3606	.4274	.4989	.5750	.6567	0.0000
	2	0.0000	.0370	.0750	.1132	.1593	.2083	.2641	.3226	.3849	.4509	.5244	0.0000
	3	0.0000	.0225	.0484	.0731	.1040	.1406	.1838	.2326	.2877	.3497	.4200	0.0000
3	1	0.0000	.0603	.1188	.1732	.2208	.2717	.3288	.3926	.4626	.5386	.6200	0.0000
	2	0.0000	.0350	.0735	.1099	.1543	.2027	.2595	.3244	.3976	.4780	.5646	0.0000
	3	0.0000	.0224	.0455	.0697	.0933	.1217	.1570	.1981	.2444	.2969	.3558	0.0000
4	1	0.0000	.0600	.1164	.1652	.2073	.2532	.3021	.3541	.4094	.4680	.5290	0.0000
	2	0.0000	.0356	.0720	.1048	.1379	.1734	.2120	.2537	.2986	.3466	.3976	0.0000
	3	0.0000	.0223	.0446	.0665	.0874	.1054	.1217	.1366	.1507	.1643	.1776	0.0000
5	1	0.0000	.0597	.1141	.1576	.1948	.2293	.2717	.3121	.3506	.3872	.4220	0.0000
	2	0.0000	.0364	.0700	.1000	.1248	.1529	.1826	.2141	.2473	.2822	.3189	0.0000
	3	0.0000	.0222	.0437	.0634	.0801	.0913	.0941	.0847	.0664	.0295	.0244	0.0000
6	1	0.0000	.0524	.1077	.1504	.1790	.1974	.1928	.1006	.0520	.0119	.0000	0.0000
	2	0.0000	.0362	.0691	.0954	.1117	.1151	.1037	.0781	.0434	.0129	.0000	0.0000
	3	0.0000	.0221	.0428	.0605	.0734	.0791	.0753	.0605	.0363	.0107	.0000	0.0000
7	1	0.0000	.0521	.1095	.1434	.1558	.1450	.1142	.0720	.0312	.0056	.0000	0.0000
	2	0.0000	.0323	.0637	.0837	.0912	.0906	.0829	.0602	.0360	.0051	.0000	0.0000
	3	0.0000	.0219	.0419	.0577	.0672	.0685	.0602	.0432	.0287	.0020	.0000	0.0000
8	1	0.0000	.0519	.1073	.1368	.1428	.1255	.0914	.0514	.0187	.0022	.0000	0.0000
	2	0.0000	.0359	.0664	.0868	.0938	.0866	.0663	.0398	.0156	.0022	.0000	0.0000
	3	0.0000	.0219	.0411	.0551	.0616	.0593	.0482	.0309	.0131	.0020	.0000	0.0000
9	1	0.0000	.0516	.1051	.1305	.1308	.1087	.0731	.0367	.0112	.0011	.0000	0.0000
	2	0.0000	.0357	.0650	.0828	.0860	.0747	.0531	.0284	.0078	.0000	.0000	0.0000
	3	0.0000	.0218	.0402	.0525	.0565	.0514	.0385	.0220	.0078	.0000	.0000	0.0000
10	1	0.0000	.0513	.1030	.1245	.1199	.0942	.0685	.0262	.0067	.0005	.0000	0.0000
	2	0.0000	.0353	.0637	.0790	.0788	.0647	.0425	.0203	.0056	.0004	.0000	0.0000
	3	0.0000	.0216	.0394	.0501	.0518	.0445	.0306	.0157	.0047	.0004	.0000	0.0000



Table 3c. Oblate angular spheroidal functions  $\tilde{Y}_l(n, n-2, p; \bar{\eta})$

$n$	$l$	$p$	$\bar{\eta}$	0.0	.1	.2	.3	.4	.5	.6	.7	.8	.9	1.0
2	0	1	1	.3033	.3078	.3218	.3458	.3811	.4296	.4938	.5773	.6849	.8230	1.0000
2	1	2	1	.1033	.1070	.1185	.1391	.1709	.2176	.2846	.3602	.4570	.5740	1.0000
2	2	3	1	.0415	.0440	.0518	.0662	.0897	.1265	.1835	.2722	.4120	.6357	1.0000
2	2	3	2	.6655	.5974	.5693	.5202	.4468	.3436	.2033	.1155	.0308	.0000	0.0000
2	2	3	3	.5994	.6001	.6015	.6013	.5946	.5729	.4411	.2511	.0936	.0000	0.0000
3	0	1	1	.3984	.3906	.3970	.4072	.4203	.4347	.4472	.4519	.4563	.4593	0.0000
3	1	2	1	.1296	.1256	.1256	.1270	.1291	.1250	.2373	.2955	.2667	.3497	0.0000
3	2	3	1	.0598	.0580	.0630	.0773	.0962	.1250	.1593	.2052	.2552	.2811	0.0000
3	2	3	2	.2368	.2283	.2158	.1605	.1011	.0255	.0540	.1610	.2503	.2117	0.0000
3	2	3	3	.2321	.2229	.2138	.1892	.1768	.0952	.0210	.0701	.0979	.2191	0.0000
3	2	3	4	.2231	.2114	.2013	.1996	.1768	.1406	.0858	.0686	.0979	.2191	0.0000
4	0	1	1	.4420	.4414	.4393	.4348	.4261	.4106	.3848	.3405	.2713	.1839	0.0000
4	1	2	1	.1839	.1858	.1911	.1996	.2103	.2214	.2295	.2282	.2060	.1532	0.0000
4	2	3	1	.0744	.0782	.0819	.0914	.1048	.1217	.1485	.1566	.1594	.1426	0.0000
4	2	3	2	.1387	.1306	.1067	.0682	.0177	.0404	.0933	.1476	.1677	.1324	0.0000
4	2	3	3	.1116	.1177	.1209	.1281	.1435	.0000	.0495	.0980	.1306	.1122	0.0000
4	2	3	4	.1116	.1088	.1081	.1048	.10620	.0384	.0098	.0558	.0965	.1122	0.0000
5	0	1	1	.4757	.4733	.4615	.4427	.4142	.3742	.3205	.2512	.1664	.0722	0.0000
5	1	2	1	.2192	.2166	.2176	.2183	.2173	.2119	.1987	.1727	.1283	.0731	0.0000
5	2	3	1	.0941	.0953	.0991	.1050	.1123	.1194	.1235	.1195	.0997	.0554	0.0000
5	2	3	2	.0967	.0887	.0658	.0303	.0322	.0582	.0959	.1154	.1051	.0987	0.0000
5	2	3	3	.0822	.0733	.0591	.0362	.0062	.0278	.0604	.0834	.0849	.0927	0.0000
5	2	3	4	.0662	.0633	.0545	.0399	.0195	.0068	.0334	.0574	.0671	.0669	0.0000
6	0	1	1	.4984	.4920	.4727	.4401	.3942	.3349	.2635	.1832	.0813	.0117	0.0000
6	1	2	1	.2007	.1961	.1934	.1921	.1906	.1866	.1688	.1286	.0791	.0279	0.0000
6	2	3	1	.1116	.1121	.1135	.1153	.1161	.1151	.1066	.0902	.0619	.0246	0.0000
6	2	3	2	.0944	.0850	.0638	.0318	.0268	.0544	.0839	.0863	.0545	.0158	0.0000
6	2	3	3	.0663	.0560	.0438	.0264	.0164	.0389	.0564	.0643	.0445	.0158	0.0000
6	2	3	4	.0446	.0347	.0232	.0119	.0016	.0283	.0460	.0470	.0229	.0010	0.0000
6	2	3	5	.0446	.0332	.0213	.0105	.0016	.0313	.0486	.0470	.0229	.0010	0.0000

Table 3d. Oblate angular spheroidal functions  $\tilde{Y}_t(n, n-3, p; \eta)$

$n$	$l$	$p$	$\eta$	0.0	0.1	0.2	0.3	0.4	0.5	0.6	0.7	0.8	0.9	1.0
3	1	1	1	0.0000	0.420	0.865	1.360	1.935	2.628	3.482	4.556	5.927	7.596	1.0000
3	3	1	1	0.0000	0.188	0.398	0.658	1.002	1.476	2.151	3.132	4.577	6.396	1.0000
3	3	3	1	0.0000	0.089	0.195	0.338	0.549	0.816	1.395	2.237	3.632	5.379	1.0000
4	1	1	1	0.0000	0.313	0.2548	0.3615	0.4806	0.4775	0.4527	0.3390	0.982	3.230	1.0000
4	3	1	1	0.0000	0.100	0.2175	0.3186	0.4075	0.4775	0.4935	0.372	0.2456	0.885	1.0000
4	3	3	1	0.0000	0.089	0.1749	0.2640	0.322	0.4325	0.4667	0.4859	0.3538	0.885	1.0000
4	1	1	3	0.0000	0.656	0.922	1.003	1.003	0.448	0.2928	0.380	0.3648	0.398	0.0000
4	3	1	3	0.0000	0.212	0.340	0.4700	0.593	0.704	0.785	0.742	0.529	0.278	0.0000
4	3	3	1	0.0000	0.101	0.216	0.360	0.533	0.819	1.163	1.665	2.336	3.238	0.0000
4	1	1	5	0.0000	0.594	1.116	1.489	1.730	1.858	0.976	1.077	1.233	1.512	0.0000
4	3	1	5	0.0000	0.179	0.320	0.4860	0.670	0.872	1.225	1.644	2.145	2.715	0.0000
4	3	3	1	0.0000	0.375	0.6736	1.066	1.512	1.934	2.330	2.669	3.0085	3.241	0.0000
5	1	1	1	0.0000	0.481	0.955	1.409	1.826	2.182	2.423	2.478	2.228	1.495	0.0000
5	3	1	1	0.0000	0.233	0.473	0.728	0.968	1.278	1.544	1.738	1.741	1.474	0.0000
5	3	3	1	0.0000	0.113	0.237	0.380	0.553	0.751	1.0	1.238	1.376	1.164	0.0000
5	1	1	3	0.0000	0.370	0.659	0.935	1.173	1.344	0.918	0.469	0.995	1.074	0.0000
5	3	1	3	0.0000	0.266	0.532	0.772	1.033	1.314	1.609	1.811	1.832	1.479	0.0000
5	3	3	1	0.0000	0.220	0.419	0.572	0.646	0.614	0.302	0.033	0.0470	0.092	0.0000
6	1	1	1	0.0000	0.398	0.972	1.394	1.731	1.944	1.985	1.802	1.354	0.656	0.0000
6	3	1	1	0.0000	0.249	0.496	0.741	0.970	1.164	1.286	1.280	1.066	0.579	0.0000
6	3	3	1	0.0000	0.124	0.254	0.395	0.546	0.701	0.840	0.916	0.845	0.513	0.0000
6	1	1	3	0.0000	0.263	0.460	0.632	0.846	1.020	1.156	0.912	0.688	0.491	0.0000
6	3	1	3	0.0000	0.197	0.354	0.533	0.705	0.823	0.810	0.310	0.532	0.362	0.0000
6	3	3	1	0.0000	0.148	0.272	0.351	0.356	0.273	0.087	0.171	0.399	0.362	0.0000
7	1	1	1	0.0000	0.510	1.079	1.364	1.624	1.719	1.616	1.304	0.820	0.367	0.0000
7	3	1	1	0.0000	0.262	0.515	0.743	0.930	1.047	1.062	0.936	0.650	0.309	0.0000
7	3	3	1	0.0000	0.134	0.269	0.404	0.532	0.659	0.700	0.674	0.517	0.226	0.0000
7	1	1	3	0.0000	0.202	0.340	0.363	0.252	0.027	0.240	0.438	0.444	0.220	0.0000
7	3	1	3	0.0000	0.147	0.255	0.293	0.208	0.014	0.120	0.303	0.354	0.196	0.0000
7	3	3	1	0.0000	0.108	0.192	0.232	0.208	0.094	0.138	0.199	0.278	0.175	0.0000

Table 3e. Oblate angular spheroidal functions  $\tilde{Y}_t^{(+)}(n, n-4, p; \bar{\eta})$

$n$	$t$	$p/\bar{\eta}$	0.0	.1	.2	.3	.4
4	4	1	.4064	.3796	.2994	.1524	-.0206
		2	.4515	.4234	.3593	.2455	.0912
		3	.5104	.4935	.4416	.3520	.2211
		4	.5610	.5571	.5155	.4519	.3505
		5	.5737	.5684	.5507	.5142	.4475
4	2	1	-.6424	-.6383	-.6192	-.5867	-.5342
		2	-.5361	-.5383	-.5464	-.5551	-.5624
		3	-.3276	-.3343	-.3541	-.3864	-.4288
		4	-.1766	-.1835	-.2046	-.2410	-.2936
		5	-.0934	-.0993	-.1167	-.1486	-.1981
4	0	1	.1603	.1647	.1783	.2022	.2383
		2	.0386	.0411	.0493	.0644	.0892
		3	.0125	.0134	.0183	.0270	.0424
		4	.0047	.0054	.0079	.0129	.0224
		5	.0019	.0023	.0037	.0066	.0125
5	4	1	.1196	.1061	.0677	.0111	-.0521
		2	.1173	.1028	.0776	.0316	-.0238
		3	.1183	.1108	.0885	.0523	.0047
		4	.1217	.1154	.1002	.0725	.3333
		5	.1243	.1203	.1099	.0901	.0596
5	2	1	-.2341	-.2314	-.2112	-.1767	-.1267
		2	-.2228	-.2277	-.2139	-.2005	-.1778
		3	-.1641	-.1649	-.1669	-.1687	-.1673
		4	-.0999	-.1013	-.1078	-.1169	-.1275
		5	-.0650	-.0571	-.0635	-.0741	-.0887
5	0	1	.2448	.2479	.2571	.2723	.2932
		2	.0995	.1021	.0637	.0834	.1040
		3	.0179	.0193	.0238	.0323	.0461
		4	.0064	.0071	.0097	.0146	.0234
		5	.0025	.0029	.0043	.0072	.0127
6	4	1	.0552	.0467	.0233	-.0086	-.0396
		2	.0498	.0436	.0261	.0007	-.0264
		3	.0461	.0416	.0285	.0087	-.0146
		4	.0437	.0405	.0309	.0218	-.0038
		5	.0423	.0401	.0333	.0258	.0060
6	2	1	-.1327	-.1259	-.1059	-.0731	-.0290
		2	-.1163	-.1137	-.1034	-.0864	-.0640
		3	-.0956	-.0927	-.0915	-.0881	-.0788
		4	-.0667	-.0670	-.0677	-.0680	-.0681
		5	-.0405	-.0413	-.0437	-.0470	-.0504
6	0	1	.3176	.3155	.3211	.3244	.3269
		2	.0895	.0916	.0979	.1085	.1231
		3	.0263	.0277	.0321	.0398	.0516
		4	.0089	.0097	.0122	.0170	.0249
		5	.0034	.0033	.0052	.0081	.0131
7	4	1	.0313	.0252	.0090	-.0116	-.0283
		2	.0266	.0222	.0103	-.0057	-.0205
		3	.0231	.0200	.0113	-.0011	-.0133
		4	.0205	.0133	.0120	.0024	-.0084
		5	.0187	.0111	.0126	.0053	-.0036
7	2	1	-.0904	-.0830	-.0638	-.0329	.0060
		2	-.0714	-.0573	-.0575	-.0402	.0166
		3	-.0587	-.0511	-.0522	-.0434	.0130
		4	-.0450	-.0445	-.0439	-.0396	.0135
		5	-.0304	-.0306	-.0308	-.0308	.0129
7	0	1	.3700	.3694	.3633	.3536	.3376
		2	.1229	.1237	.1283	.1338	.1404
		3	.0384	.0397	.0435	.0500	.0589
		4	.0126	.0114	.0159	.0203	.0271
		5	.0046	.0053	.0065	.0092	.0137

.5	.6	.7	.8	.9	1.0
-.2059	-.3660	-.4421	-.3438	.0671	1.0000
-.0927	-.2816	-.4238	-.4170	-.0651	1.0000
.0485	-.1551	-.3555	-.4477	-.1851	1.0000
.2012	-.0018	-.2419	-.4318	-.2867	1.0000
.3337	.1532	-.1018	-.3732	-.3628	1.0000
-.4541	-.3346	-.4590	.0967	.4668	1.0000
-.5555	-.5177	-.4186	-.2050	.2148	1.0000
-.4749	-.5097	-.4997	-.3730	.0219	1.0000
-.3616	-.4368	-.4919	-.4506	-.1162	1.0000
-.2683	-.3587	-.4522	-.4791	-.2159	1.0000
.2895	.3502	.4563	.5864	.7621	1.0000
.1279	.1877	.2800	.4232	.6470	1.0000
.0687	.1138	.1916	.3273	.5677	1.0000
.1401	.0734	.1368	.2600	.5044	1.0000
.0244	.0488	.0999	.2095	.4512	1.0000
-.1054	-.1279	-.0972	.0023	.1489	0.0000
-.0784	-.1150	-.1093	-.0343	.1124	0.0000
-.0482	-.0941	-.1101	-.0614	.0781	0.0000
-.0156	-.0667	-.1008	-.0793	.0464	0.0000
-.0171	-.0349	-.0825	-.0878	.0178	0.0000
-.0601	.0228	.1186	.2151	.2731	0.0000
-.1410	-.0844	-.0025	.1045	.2090	0.0000
-.1577	-.1316	-.0767	.0197	.1499	0.0000
-.1358	-.1341	-.1078	-.0346	.1020	0.0000
-.1053	-.1183	-.1140	-.0646	.0649	0.0000
.3189	.3472	.3726	.3832	.3460	0.0000
.1331	.1717	.2192	.2686	.2894	0.0000
.0676	.0997	.1455	.2039	.2517	0.0000
.0382	.0628	.1023	.1604	.2227	0.0000
.0228	.0413	.0740	.1285	.1986	0.0000
-.0575	-.0511	-.0144	.0435	.0820	0.0000
-.0467	-.0498	-.0261	.0238	.0690	0.0000
-.0355	-.0452	-.0329	.0079	.0568	0.0000
-.0240	-.0381	-.0354	-.0043	.0454	0.0000
-.0126	-.0293	-.0344	-.0134	.0349	0.0000
.0236	.0794	.1285	.1540	.1271	0.0000
-.0264	-.0170	-.0650	.1052	.1866	0.0000
-.0544	-.0248	-.0163	.0627	.0863	0.0000
-.0593	-.0435	-.0137	.0304	.0680	0.0000
-.0516	-.0465	-.0285	.0086	.0528	0.0000
.3258	.3170	.2936	.2452	.1556	0.0000
.1409	.1596	.1739	.1720	.1301	0.0000
.0680	.0889	.1149	.1279	.1120	0.0000
.0369	.0544	.0770	.0994	.0985	0.0000
.0215	.0351	.0551	.0796	.0876	0.0000
-.0326	-.0191	.0097	.0386	.0394	0.0000
-.0276	-.0210	.0004	.0274	.0343	0.0000
-.0223	-.0209	-.0060	.0182	.0295	0.0000
-.0172	-.0193	-.0099	.0107	.0251	0.0000
-.0122	-.0167	-.0119	.0048	.0210	0.0000
.0474	.0837	.1048	.0987	.0569	0.0000
.0119	.0419	.0664	.0738	.0493	0.0000
-.0113	.0119	.0363	.0522	.0419	0.0000
-.0230	-.0069	.0142	.0341	.0349	0.0000
-.0250	-.0156	.0004	.0204	.0287	0.0000
.3127	.2758	.2234	.1535	.0693	0.0000
.1458	.1465	.1370	.1099	.0584	0.0000
.0698	.0805	.0870	.0809	.0500	0.0000
.0364	.0477	.0586	.0519	.0437	0.0000
.0206	.0301	.0412	.0486	.0387	0.0000

Table 3f. Oblate angular spheroidal functions  $\tilde{Y}_t^{(-)}(n, n-5, p; \bar{\eta})$

$h$	$t$	$h-t$	0.0	.1	.2	.3	.4
5	5	1	0.0000	.1733	.3023	.3639	.3273
		2	0.0000	.1537	.2928	.3726	.3732
		3	0.0000	.1456	.2763	.3687	.4012
		4	0.0000	.1355	.2535	.3505	.4082
5	3	1	0.0000	-.1219	-.2378	-.3429	-.4278
		2	0.0000	-.1884	-.1753	-.2646	-.3533
		3	0.0000	-.1593	-.1165	-.1846	-.2628
		4	0.0000	-.1343	-.0736	-.1222	-.1854
5	1	1	0.0000	.0295	.0616	.0931	.1454
		2	0.0000	.1102	.1222	.1385	.1623
		3	0.0000	.1707	.1094	.1169	.1300
		4	0.0000	.1617	.1043	.1081	.1159
6	5	1	0.0000	.0517	.0863	.0924	.0624
		2	0.0000	.1423	.0737	.0933	.0735
		3	0.0000	.1422	.0724	.0883	.0809
		4	0.0000	.1343	.0647	.0834	.0844
6	3	1	0.0000	-.0553	-.1042	-.1414	-.1596
		2	0.0000	-.1333	-.0777	-.1113	-.1364
		3	0.0000	-.1253	-.0539	-.0811	-.1068
		4	0.0000	-.1111	-.0353	-.0557	-.0783
6	1	1	0.0000	.0344	.0703	.1088	.1511
		2	0.0000	.1135	.1255	.1438	.1654
		3	0.0000	.1633	.1133	.1191	.1316
		4	0.0000	.1631	.1047	.1090	.1161
7	5	1	0.0000	.0241	.0381	.0351	.0145
		2	0.0000	.1203	.0335	.0339	.0196
		3	0.0000	.1122	.0294	.0322	.0133
		4	0.0000	.1145	.0256	.0301	.0225
7	3	1	0.0000	-.1342	-.0624	-.0792	-.0793
		2	0.0000	-.1243	-.0459	-.0619	-.0684
		3	0.0000	-.1167	-.0325	-.0463	-.0559
		4	0.0000	-.1139	-.0220	-.0329	-.0427
7	1	1	0.0000	.0333	.0767	.1147	.1515
		2	0.0000	.1148	.1077	.1486	.1694
		3	0.0000	.1633	.1127	.1214	.1333
		4	0.0000	.1625	.1035	.1100	.1168
8	5	1	0.0000	.0176	.0297	.0156	.0014
		2	0.0000	.1111	.0172	.0150	.0047
		3	0.0000	.1131	.0146	.0142	.0069
		4	0.0000	.1074	.0125	.0132	.0084
8	3	1	0.0000	-.1203	-.0429	-.0535	-.0437
		2	0.0000	-.1163	-.0308	-.0389	-.0383
		3	0.0000	-.1073	-.0219	-.0293	-.0290
		4	0.0000	-.1023	-.0151	-.0214	-.0254
8	1	1	0.0000	.0443	.0814	.1174	.1480
		2	0.0000	.1471	.1347	.1524	.1709
		3	0.0000	.1871	.1447	.1237	.1346
		4	0.0000	.1873	.1054	.1111	.1175
8	5	1	0.0000	.0176	.0297	.0156	.0014
		2	0.0000	.1111	.0172	.0150	.0047
		3	0.0000	.1131	.0146	.0142	.0069
		4	0.0000	.1074	.0125	.0132	.0084

.5	.6	.7	.8	.9	1.0
.1854	.0453	.2980	.4274	.5566	1.0000
.2739	.0700	.2026	.4174	.5346	1.0000
.3467	.1821	.0891	.3737	.5121	1.0000
.3963	.2790	.0298	.3028	.4871	1.0000
.4192	.3520	.1415	.2138	.4193	1.0000
-.4789	-.4758	-.3873	-.4656	-.2608	1.0000
-.4332	-.4867	-.4773	-.3344	-.0753	1.0000
-.3499	-.4354	-.4880	-.4284	-.0715	1.0000
-.2668	-.3644	-.4572	-.4701	-.1835	1.0000
-.1980	-.2949	-.4094	-.4793	-.2681	1.0000
.2049	.2835	.3889	.5322	.7286	1.0000
.1985	.1549	.2444	.3877	.5200	1.0000
.0926	.0927	.1648	.2966	.4507	1.0000
.0300	.0585	.1157	.2329	.4777	1.0000
.0178	.0381	.0832	.1858	.4253	1.0000
.0025	-.0664	-.1057	-.0652	.0815	0.0000
.0260	-.0397	-.0929	-.0805	.0508	0.0000
.0459	-.0131	-.0746	-.0875	.0234	0.0000
.0613	.0116	-.0528	-.0872	-.0001	0.0000
.0715	.0327	-.0298	-.0809	-.0196	0.0000
-.1513	-.1087	-.0267	.0908	.2070	0.0000
-.1465	-.1318	-.0795	.0214	.1553	0.0000
-.1265	-.1315	-.1060	.0280	.1110	0.0000
-.1012	-.1179	-.1135	-.0596	.0738	0.0000
-.0774	-.0996	-.1098	-.0779	.0436	0.0000
.1976	.2474	.2966	.3335	.3245	0.0000
.0965	.1365	.1872	.2433	.2761	0.0000
.0510	.0808	.1250	.1848	.2399	0.0000
.0286	.0503	.0869	.1441	.2112	0.0000
.0168	.0324	.0620	.1144	.1876	0.0000
-.0159	-.0400	-.0372	.0041	.0579	0.0000
-.0056	-.0306	-.0370	.0071	.0466	0.0000
-.0031	-.0212	-.0341	.0151	.0362	0.0000
-.0100	-.0121	-.0293	.0262	.0269	0.0000
.0152	-.0038	-.0233	-.0228	.0187	0.0000
-.0592	-.0185	.0371	.0904	.1031	0.0000
-.0621	-.0383	.0038	.0560	.0852	0.0000
-.0576	-.0466	-.0176	.0291	.0690	0.0000
-.0489	-.0468	-.0292	.0095	.0548	0.0000
-.0390	-.0424	-.0339	-.0039	.0427	0.0000
.1849	.2109	.2223	.2068	.1438	0.0000
.0933	.1192	.1425	.1522	.1228	0.0000
.0493	.0704	.0949	.1152	.1065	0.0000
.0274	.0434	.0654	.0894	.0935	0.0000
.0159	.0277	.0463	.0705	.0828	0.0000
-.0153	-.0221	-.0105	.0162	.0302	0.0000
-.0094	-.0185	-.0129	.0090	.0256	0.0000
-.0047	-.0146	-.0136	.0035	.0215	0.0000
-.0009	-.0108	-.0132	-.0006	.0177	0.0000
.0020	-.0071	-.0119	-.0036	.0144	0.0000
-.0220	.0111	.0455	.0644	.0476	0.0000
-.0271	-.0051	.0233	.0459	.0407	0.0000
-.0276	-.0142	.0079	.0310	.0334	0.0000
-.0251	-.0180	-.0022	.0194	.0288	0.0000
-.0212	-.0185	-.0079	.0107	.0239	0.0000
.1693	.1767	.1645	.1271	.0635	0.0000
.0886	.1026	.1075	.0947	.0545	0.0000
.0474	.0610	.0718	.0718	.0473	0.0000
.0263	.0375	.0493	.0553	.0414	0.0000
.0151	.0237	.0347	.0436	.0366	0.0000

Table 4a. Oblate radial spheroidal functions  $\tilde{Y}_0^{(+)}(n, n, p; \xi)$

$n$	$p/\xi$	0.0	0.3	0.6	0.9	1.2	1.5	1.8	2.1	2.4	2.7	3.0
0	1.000	0.954	0.874	0.805	0.667	0.497	0.285	0.166	0.100	0.059	0.026	0.011
	1.000	0.974	0.933	0.893	0.797	0.637	0.434	0.269	0.162	0.093	0.041	0.000
	1.000	0.974	0.933	0.893	0.797	0.637	0.434	0.269	0.162	0.093	0.041	0.000
1	1.000	0.998	0.974	0.948	0.899	0.820	0.706	0.561	0.388	0.246	0.146	0.075
	1.000	0.998	0.974	0.948	0.899	0.820	0.706	0.561	0.388	0.246	0.146	0.075
	1.000	0.998	0.974	0.948	0.899	0.820	0.706	0.561	0.388	0.246	0.146	0.075
2	1.000	1.042	1.036	1.033	1.007	0.958	0.885	0.782	0.656	0.514	0.361	0.211
	1.000	0.996	0.993	0.993	0.957	0.908	0.835	0.732	0.606	0.464	0.311	0.161
	1.000	0.952	0.953	0.953	0.917	0.868	0.795	0.692	0.566	0.424	0.271	0.121
3	1.000	1.088	1.085	1.085	1.024	0.965	0.892	0.789	0.663	0.521	0.368	0.218
	1.000	1.040	1.037	1.037	0.963	0.904	0.831	0.728	0.602	0.460	0.307	0.157
	1.000	0.994	0.994	0.994	0.923	0.864	0.791	0.688	0.562	0.420	0.267	0.117
4	1.000	1.136	1.135	1.135	1.045	0.986	0.913	0.810	0.684	0.542	0.389	0.239
	1.000	1.086	1.086	1.086	1.000	0.941	0.868	0.765	0.639	0.497	0.344	0.194
	1.000	1.038	1.038	1.038	0.947	0.888	0.815	0.712	0.586	0.444	0.291	0.141
5	1.000	1.186	1.186	1.186	1.072	1.013	0.940	0.837	0.711	0.569	0.416	0.266
	1.000	1.134	1.134	1.134	1.039	0.980	0.907	0.804	0.678	0.536	0.383	0.233
	1.000	1.084	1.084	1.084	1.000	0.941	0.868	0.765	0.639	0.497	0.344	0.194
6	1.000	1.238	1.238	1.238	1.107	1.048	0.975	0.872	0.746	0.604	0.451	0.301
	1.000	1.184	1.184	1.184	1.082	1.023	0.950	0.847	0.721	0.579	0.426	0.276
	1.000	1.131	1.131	1.131	1.036	0.977	0.904	0.801	0.675	0.533	0.380	0.230
7	1.000	1.293	1.293	1.293	1.152	1.093	1.020	0.917	0.791	0.649	0.496	0.346
	1.000	1.236	1.236	1.236	1.130	1.071	1.000	0.897	0.771	0.629	0.476	0.326
	1.000	1.181	1.181	1.181	1.075	1.016	0.943	0.840	0.714	0.572	0.419	0.269
8	1.000	1.349	1.349	1.349	1.199	1.140	1.067	0.964	0.838	0.696	0.543	0.393
	1.000	1.290	1.290	1.290	1.183	1.124	1.051	0.948	0.822	0.680	0.527	0.377
	1.000	1.233	1.233	1.233	1.167	1.108	1.035	0.932	0.806	0.664	0.511	0.361
9	1.000	1.409	1.409	1.409	1.231	1.172	1.099	0.996	0.870	0.728	0.575	0.425
	1.000	1.347	1.347	1.347	1.215	1.156	1.083	0.980	0.854	0.712	0.559	0.409
	1.000	1.288	1.288	1.288	1.199	1.140	1.067	0.964	0.838	0.696	0.543	0.393

Table 4b. Oblate radial spheroidal functions  $\tilde{X}_0^{(-)}(n, m-1, p; \xi)$

$n$	$m$	0.0	.2	.6	.9	1.2	1.5	1.8	2.1	2.4	2.7	3.0
1	1	0.000	.287	.501	.608	.584	.487	.356	.232	.135	.071	.033
	2	0.000	.274	.419	.490	.284	.156	.070	.026	.006	.002	.000
	3	0.000	.262	.350	.267	.138	.051	.014	.003	.000	.000	.000
2	1	0.000	.299	.584	.888	.912	.878	.733	.539	.358	.283	.195
	2	0.000	.286	.468	.539	.444	.285	.145	.057	.020	.008	.000
	3	0.000	.274	.408	.359	.216	.093	.029	.007	.001	.000	.000
3	1	0.000	.313	.682	1.087	1.425	1.803	1.518	1.253	.911	.585	.333
	2	0.000	.299	.569	.725	.694	.514	.299	.138	.051	.015	.004
	3	0.000	.286	.476	.483	.338	.167	.059	.015	.003	.000	.000
4	1	0.000	.329	.795	1.462	2.226	2.953	3.110	2.943	2.368	1.683	1.054
	2	0.000	.312	.664	.975	1.084	.826	.615	.321	.133	.044	.012
	3	0.000	.298	.555	.650	.527	.381	.222	.035	.007	.001	.000
5	1	0.000	.341	.927	1.974	3.478	5.144	6.404	6.776	6.157	4.847	3.333
	2	0.000	.326	.774	1.412	1.693	1.670	1.267	.747	.346	.127	.037
	3	0.000	.311	.647	.875	.824	.542	.351	.082	.019	.003	.000
6	1	0.000	.359	1.081	2.646	5.432	9.273	13.187	15.761	16.007	13.956	10.539
	2	0.000	.349	.903	1.765	2.644	3.040	2.610	1.738	.899	.365	.117
	3	0.000	.325	.754	1.177	1.287	.877	.516	.192	.050	.010	.001
7	1	0.000	.371	1.261	3.559	8.485	16.717	27.153	36.668	40.618	40.101	33.327
	2	0.000	.359	.880	1.803	4.130	5.827	5.373	4.042	2.336	1.050	.370
	3	0.000	.339	.780	1.503	2.010	1.762	1.063	.446	.131	.027	.004
8	1	0.000	.388	1.470	4.789	13.254	30.337	55.911	85.269	100.287	115.691	105.339
	2	0.000	.371	1.226	2.330	5.452	9.801	11.065	9.401	6.074	3.022	1.171
	3	0.000	.354	1.026	1.730	3.140	2.190	1.036	.441	.141	.079	.013
9	1	0.000	.425	1.714	6.443	20.704	54.330	115.127	198.330	261.339	333.183	333.270
	2	0.000	.407	1.432	3.297	10.070	17.838	22.784	21.793	15.733	8.701	3.702
	3	0.000	.370	1.196	2.866	4.905	5.726	4.509	2.411	.887	.227	.041
10	1	0.000	.423	1.999	8.068	32.340	97.946	237.862	461.304	731.431	959.882	1050.00
	2	0.000	.404	1.691	3.978	11.781	21.678	26.959	21.062	14.042	7.553	3.178
	3	0.000	.386	1.395	3.056	7.682	10.323	9.284	5.607	2.305	.654	.110



Table 4c. Oblate radial spheroidal functions  $\tilde{X}_l^{(+)}(n, n-2, p; \bar{\xi})$

$n$	$l$	$\bar{\xi}$	0.0	.3	.6	.9	1.2	1.5	1.8	2.1	2.4	2.7	3.0	
2	0	1	1.000	1.028	1.437	1.747	1.889	1.786	1.480	1.063	.703	.407	.211	
		1	1.000	1.042	1.090	1.008	1.770	3.343	.476	.237	.096	.031	.008	.000
		1	1.000	.982	.671	.627	.343	.140	.042	.009	.000	.000	.000	.000
2	1	1	1.000	.870	.535	.127	-.214	-.406	-.443	-.376	-.267	-.164	-.089	
		1	1.000	.853	.533	-.478	-.611	-.502	-.266	-.125	-.042	-.001	-.000	
		1	1.000	.533	-.335	-.754	-.611	-.302	-.102	-.024	-.004	.000	.000	
3	0	1	1.000	1.318	2.223	3.486	4.660	5.275	5.110	4.284	3.140	2.028	1.161	
		1	1.000	1.174	1.564	1.840	1.785	1.505	1.150	.740	.348	.129	.039	
		1	1.000	1.076	1.169	1.046	1.699	3.334	.119	.031	.006	.001	.000	
3	1	1	1.000	.918	.777	.489	-.146	-.154	-.327	-.379	-.326	-.233	-.142	
		1	1.000	.620	.356	-.169	-.590	-.478	-.327	-.159	-.038	-.007	-.000	
		1	1.000	.620	-.054	-.571	-.590	-.355	-.139	.000	.000	.000	.000	
4	0	1	1.000	1.546	3.333	5.461	10.376	13.809	15.444	14.738	12.122	8.697	5.482	
		1	1.000	1.355	2.315	3.414	3.908	3.425	2.818	1.226	.812	.512	.306	
		1	1.000	1.209	1.646	1.842	1.497	1.062	.552	.103	.022	.003	.000	
4	1	1	1.000	1.007	.984	.843	-.551	.171	-.173	.383	.434	.371	.261	
		1	1.000	.907	.607	-.153	-.254	-.428	-.372	-.224	-.101	-.036	-.010	
		1	1.000	.781	.222	-.333	-.529	-.369	-.160	-.057	-.013	.000	.000	
5	0	1	1.000	1.800	4.794	11.195	21.290	33.038	42.453	45.896	42.330	33.690	23.352	
		1	1.000	1.574	3.378	5.281	9.317	16.540	6.558	3.999	1.674	.693	.204	
		1	1.000	1.386	2.379	3.281	3.207	2.173	1.026	.342	.081	.014	.002	
5	1	1	1.000	1.061	1.194	1.262	1.121	.726	.189	.295	.576	.626	.518	
		1	1.000	.974	.627	-.468	-.089	-.357	-.335	-.320	-.168	-.067	-.021	
		1	1.000	.871	.468	-.881	-.429	-.419	-.333	-.085	-.021	.004	.000	
6	0	1	1.000	2.078	6.671	18.548	41.361	74.543	109.803	134.307	138.753	122.416	93.263	
		1	1.000	1.822	3.763	5.296	10.706	19.241	17.048	12.077	6.397	2.965	.749	
		1	1.000	1.599	2.806	3.496	6.619	5.241	3.048	1.077	.287	.065	.000	
6	1	1	1.000	1.114	1.424	1.801	1.992	1.755	1.056	.478	.641	1.045	1.059	
		1	1.000	.945	.690	-.305	-.302	-.217	-.058	-.134	-.038	-.000	-.000	
		1	1.000	.945	.690	-.305	-.302	-.217	-.058	-.134	-.038	-.000	-.000	

Table 4d. Oblate radial spheroidal functions  $\tilde{X}_n^{(-)}(n, n-3, p; \xi)$

$n$	$2$	$1$	$0$	$0.0$	$0.3$	$0.6$	$0.9$	$1.2$	$1.5$	$1.8$	$2.1$	$2.4$	$2.7$	$3.0$
3	0	327	327	0.000	1.309	1.800	2.084	2.030	1.720	1.266	0.820	0.478	0.200	0.000
3	1	292	292	0.000	1.353	1.830	2.097	2.035	1.716	1.266	0.820	0.478	0.200	0.000
4	0	275	275	0.000	1.378	1.820	2.097	2.035	1.716	1.266	0.820	0.478	0.200	0.000
4	1	225	225	0.000	1.378	1.820	2.097	2.035	1.716	1.266	0.820	0.478	0.200	0.000
5	0	333	333	0.000	1.305	1.820	2.097	2.035	1.716	1.266	0.820	0.478	0.200	0.000
5	1	290	290	0.000	1.305	1.820	2.097	2.035	1.716	1.266	0.820	0.478	0.200	0.000
5	2	243	243	0.000	1.305	1.820	2.097	2.035	1.716	1.266	0.820	0.478	0.200	0.000
5	3	385	385	0.000	1.305	1.820	2.097	2.035	1.716	1.266	0.820	0.478	0.200	0.000
5	4	337	337	0.000	1.305	1.820	2.097	2.035	1.716	1.266	0.820	0.478	0.200	0.000
6	0	305	305	0.000	1.305	1.820	2.097	2.035	1.716	1.266	0.820	0.478	0.200	0.000
6	1	283	283	0.000	1.305	1.820	2.097	2.035	1.716	1.266	0.820	0.478	0.200	0.000
6	2	260	260	0.000	1.305	1.820	2.097	2.035	1.716	1.266	0.820	0.478	0.200	0.000
6	3	385	385	0.000	1.305	1.820	2.097	2.035	1.716	1.266	0.820	0.478	0.200	0.000
6	4	329	329	0.000	1.305	1.820	2.097	2.035	1.716	1.266	0.820	0.478	0.200	0.000
6	5	277	277	0.000	1.305	1.820	2.097	2.035	1.716	1.266	0.820	0.478	0.200	0.000
7	0	425	425	0.000	1.305	1.820	2.097	2.035	1.716	1.266	0.820	0.478	0.200	0.000
7	1	396	396	0.000	1.305	1.820	2.097	2.035	1.716	1.266	0.820	0.478	0.200	0.000
7	2	325	325	0.000	1.305	1.820	2.097	2.035	1.716	1.266	0.820	0.478	0.200	0.000
7	3	293	293	0.000	1.305	1.820	2.097	2.035	1.716	1.266	0.820	0.478	0.200	0.000

Table 4e. Oblate radial spheroidal functions  $\tilde{X}_x^{(+)}(n, n-4, p; \frac{1}{2})$

$n$	$l$	$p$	0.	.3	.6	.9	1.2
4	0	1	1.	1.699	4.112	8.590	14.465
		2	1.	1.462	2.773	4.385	5.245
		3	1.	1.281	1.909	2.274	1.925
		4	1.	1.151	1.373	1.237	.741
		5	1.	1.058	1.036	.713	.304
4	1	1	1.	1.068	1.180	1.145	.848
		2	1.	.943	.705	.257	-.203
		3	1.	.815	.302	-.266	-.505
		4	1.	.669	-.372	-.576	-.520
		5	1.	.513	-.388	-.707	-.415
4	2	1	1.	.767	.220	-.306	-.535
		2	1.	.476	-.440	-.710	-.223
		3	1.	.200	-.781	-.438	.408
		4	1.	-.045	-.864	.031	.726
		5	1.	-.257	-.774	.449	.752
5	0	1	1.	2.155	6.961	18.391	37.836
		2	1.	1.836	4.723	9.553	14.037
		3	1.	1.577	3.205	4.936	5.166
		4	1.	1.373	2.202	2.569	1.910
		5	1.	1.221	1.560	1.379	.728
5	1	1	1.	1.241	1.851	2.464	2.589
		2	1.	1.066	1.590	.800	.177
		3	1.	.937	.631	.061	-.399
		4	1.	.810	.247	-.352	-.504
		5	1.	.669	-.097	-.582	-.448
5	2	1	1.	.887	.562	.117	-.262
		2	1.	.651	-.100	-.583	-.419
		3	1.	.386	-.583	-.594	.142
		4	1.	.132	-.811	-.226	.589
		5	1.	-.096	-.832	.212	.736
6	0	1	1.	2.678	11.016	35.775	88.441
		2	1.	2.279	7.533	18.770	33.147
		3	1.	1.944	5.112	9.711	12.202
		4	1.	1.666	3.451	4.950	4.397
		5	1.	1.444	2.337	2.501	1.555
6	1	1	1.	1.462	2.822	4.662	5.819
		2	1.	1.223	1.605	1.430	.254
		3	1.	1.053	.906	.144	-.824
		4	1.	.921	.444	-.414	-.870
		5	1.	.793	.075	-.640	-.705
6	2	1	1.	.967	.775	.245	-.737
		2	1.	.785	-.158	-.577	-1.264
		3	1.	.552	-.410	-.370	-.695
		4	1.	.302	-.784	-.743	.016
		5	1.	.063	-.936	-.295	.437
7	0	1	1.	3.280	16.818	66.515	196.604
		2	1.	2.804	11.741	35.365	76.435
		3	1.	2.398	8.149	19.340	29.446
		4	1.	2.053	5.626	10.277	11.236
		5	1.	1.765	3.874	5.435	4.252
7	1	1	1.	1.720	4.257	9.333	14.969
		2	1.	1.432	2.581	3.619	3.183
		3	1.	1.214	1.546	1.248	.147
		4	1.	1.055	.920	.241	-.473
		5	1.	.925	.489	-.230	-.517
7	2	1	1.	1.032	1.060	.931	.552
		2	1.	.895	.533	-.119	-.397
		3	1.	.709	-.001	-.311	-.298
		4	1.	.483	-.453	-.543	.169
		5	1.	.243	-.721	-.255	.542

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1.5	1.8	2.1	2.4	2.7	3.0	I
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13.847	22.651	21.900	18.202	13.153	8.335	I
4.727	3.258	1.745	.735	.247	.666	I
1.137	.473	.140	.033	.005	.001	I
.287	.072	.012	.004	.000	.000	I
.077	.012	.001	.000	.000	.000	I
.355	-.147	-.484	-.595	-.528	-.380	I
-.434	-.403	-.251	-.116	-.041	-.012	I
-.392	-.187	-.060	-.013	-.002	-.000	I
-.241	-.066	-.012	-.001	-.000	-.000	I
-.123	-.020	-.002	-.000	-.000	-.000	I
-.418	-.109	.187	.344	.354	.276	I
.351	.541	.409	.213	.090	.023	I
.647	.398	.146	.034	.006	.001	I
.518	.175	.034	.004	.000	.000	I
.314	.062	.007	.001	.000	.000	I
61.762	82.064	90.768	85.074	68.506	47.501	I
15.096	12.136	7.441	3.538	1.323	.393	I
3.656	1.777	.604	.146	.025	.003	I
.988	.261	.049	.008	.000	.000	I
.222	.039	.004	.000	.000	.000	I
1.964	.784	-.439	-1.244	-1.477	-1.276	I
-.393	-.595	-.474	-.261	-.107	-.034	I
-.460	-.275	-.104	-.027	-.005	-.001	I
-.296	-.098	-.020	-.003	-.000	-.000	I
-.161	-.031	-.003	-.000	-.000	-.000	I
-.406	-.295	-.050	.171	.278	.273	I
.382	.407	.405	.248	.108	.035	I
.563	.440	.191	.053	.015	.001	I
.561	.227	.051	.007	.001	.000	I
.379	.087	.011	.001	.000	.000	I
169.994	261.236	329.071	346.714	317.416	239.091	I
41.969	39.813	27.240	14.563	6.052	1.979	I
10.152	5.699	2.203	.597	.115	.016	I
2.394	.809	.173	.024	.002	.000	I
.550	.111	.013	.001	.000	.000	I
4.964	1.788	-2.518	-6.075	-7.610	-7.086	I
-1.293	-2.115	-1.889	-1.166	-.526	-.183	I
-1.158	-.812	-.355	-.104	-.021	-.003	I
-.634	-.248	-.058	-.008	-.001	-.000	I
-.312	-.071	-.000	-.001	-.000	-.000	I
-2.050	-3.322	-4.122	-4.206	-3.838	-2.715	I
-1.305	-.934	-.495	-.200	-.063	-.015	I
-.153	.097	.989	.034	.008	.001	I
.318	.185	.051	.008	.001	.000	I
.338	.096	.014	.001	.000	.000	I
443.612	736.863	1127.303	1333.899	1726.901	1125.214	I
114.035	122.849	97.557	56.675	27.099	9.761	I
29.331	18.927	8.357	2.551	.548	.084	I
7.315	2.890	.708	.113	.011	.001	I
1.826	.437	.059	.005	.000	.000	I
18.935	17.650	10.578	.724	-7.564	-11.545	I
1.024	-1.312	-2.278	-1.871	-1.028	-.413	I
-.796	-.885	-.494	-.172	-.040	-.006	I
-.565	-.283	-.079	-.013	-.001	-.000	I
-.299	-.033	-.012	-.001	-.000	-.000	I
.031	-.376	-.467	-.259	.059	.295	I
-.313	.046	.294	.297	.180	.077	I
.221	.002	.260	.098	.024	.004	I
.511	.315	.397	.017	.002	.000	I
.474	.154	.025	.002	.000	.000	I
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Table 4f. Oblate radial spheroidal functions  $\tilde{X}_r^{(-)}(n, n-5, p; \xi)$

n	l	p	0.	.3	.6	.9	1.2
5	0	1	.471	1.471	3.373	8.257	
		2	.373	1.132	2.362	3.512	
		3	.346	.984	1.429	1.522	
		4	.322	.703	.880	.674	
		5	.305	.561	.552	.304	
5	1	1	.315	.685	1.020	1.125	
		2	.291	.485	.439	.146	
		3	.267	.328	.117	-.145	
		4	.241	.202	-.052	-.189	
		5	.213	.104	-.130	-.155	
5	2	1	.263	.341	.201	-.029	
		2	.225	.145	-.089	-.160	
		3	.199	.115	-.147	-.035	
		4	.155	-.063	-.166	.068	
		5	.127	-.101	-.039	.107	
5	0	1	.455	2.115	7.165	18.175	
		2	.413	1.605	4.196	7.621	
		3	.387	1.231	2.486	3.233	
		4	.369	.955	1.493	1.392	
		5	.335	.750	.911	.610	
6	1	1	.344	.913	1.718	2.424	
		2	.315	.650	.796	.525	
		3	.289	.454	.304	-.062	
		4	.264	.302	.042	-.197	
		5	.247	.183	-.089	-.186	
6	2	1	.281	.446	.403	.171	
		2	.246	.237	-.001	-.174	
		3	.211	.182	-.138	-.093	
		4	.173	-.023	-.134	.330	
		5	.147	-.183	-.076	.196	
7	0	1	.517	2.987	12.483	38.211	
		2	.475	2.254	7.282	15.984	
		3	.433	1.712	4.277	6.729	
		4	.405	1.311	2.534	2.859	
		5	.371	1.014	1.519	1.229	
7	1	1	.377	1.211	2.821	4.931	
		2	.347	.864	1.363	1.293	
		3	.314	.612	.596	.133	
		4	.283	.423	.191	-.180	
		5	.263	.277	-.018	-.216	
7	2	1	.293	.557	.560	.500	
		2	.266	.336	.131	-.141	
		3	.237	.161	-.098	-.147	
		4	.208	.035	-.148	-.120	
		5	.183	-.146	-.111	.073	
8	0	1	.597	4.154	21.444	77.486	
		2	.545	3.129	12.350	32.509	
		3	.485	2.366	7.238	15.680	
		4	.445	1.799	4.264	8.785	
		5	.411	1.378	2.531	3.464	
8	1	1	.417	1.592	4.521	9.604	
		2	.377	1.141	2.359	2.809	
		3	.347	.814	1.158	.556	
		4	.317	.534	.326	-.106	
		5	.293	.393	.097	-.240	
8	2	1	.311	.677	.994	1.033	
		2	.274	.443	.313	-.039	
		3	.237	.251	-.023	-.186	
		4	.208	.104	-.140	-.077	
		5	.183	-.033	-.178	.139	

	1.5	1.8	2.1	2.4	2.7	3.0	I
13.562	18.093	20.867	18.845	15.197	10.637	I	I
3.801	3.268	1.887	.899	.337	.100	I	I
1.087	.531	.181	.044	.008	.001	I	I
.318	.194	.018	.002	.000	.000	I	I
.095	.017	.002	.000	.000	.000	I	I
.382	.372	-.172	-.538	-.650	-.566	I	I
-.170	-.303	-.254	-.143	-.059	-.019	I	I
-.221	-.145	-.058	-.015	-.003	-.000	I	I
-.133	-.048	-.010	-.001	-.000	-.000	I	I
-.065	-.014	-.002	-.000	-.000	-.000	I	I
-.181	-.180	-.068	.061	.137	.147	I	I
-.033	.101	.130	.088	.040	.014	I	I
.106	.110	.353	.016	.003	.000	I	I
.112	.053	.313	.002	.000	.000	I	I
.075	.020	.003	.000	.000	.000	I	I
35.520	55.188	70.043	74.190	65.679	51.506	I	I
9.821	9.236	6.501	3.495	1.458	.478	I	I
2.748	1.564	.611	.167	.032	.004	I	I
.781	.269	.058	.008	.001	.000	I	I
.226	.047	.006	.000	.000	.000	I	I
2.539	1.832	.573	-.662	-1.406	-1.546	I	I
-.016	-.417	-.479	-.325	-.156	-.056	I	I
-.282	-.242	-.115	-.035	-.001	-.001	I	I
-.199	-.083	-.020	-.003	-.000	-.000	I	I
-.097	-.024	-.003	-.000	-.000	-.000	I	I
-.100	-.241	-.198	-.042	.109	.184	I	I
-.112	.054	.140	.120	.065	.025	I	I
.077	.127	.075	.020	.006	.001	I	I
.120	.072	.021	.003	.000	.000	I	I
.191	.029	.004	.000	.000	.000	I	I
88.187	158.777	229.805	273.882	273.872	233.150	I	I
24.354	26.560	21.328	12.906	5.993	2.167	I	I
3.767	4.470	1.991	.612	.132	.020	I	I
1.398	.759	.188	.029	.003	.000	I	I
.539	.130	.018	.001	.000	.000	I	I
6.463	6.197	3.848	.422	-2.531	-3.998	I	I
.481	-.471	-.899	-.758	-.423	-.172	I	I
-.334	-.411	-.238	-.085	-.020	-.003	I	I
-.273	-.147	-.042	-.007	-.001	-.000	I	I
-.147	-.043	-.007	-.001	-.000	-.000	I	I
.132	-.221	-.353	-.232	.009	.205	I	I
-.191	-.023	.135	.161	.104	.046	I	I
.129	.136	.103	.042	.011	.002	I	I
.120	.093	.032	.006	.001	.000	I	I
.107	.041	.007	.001	.000	.000	I	I
211.129	436.966	719.616	963.493	1070.726	1003.741	I	I
28.264	73.452	67.147	45.662	23.572	9.386	I	I
16.201	12.378	6.280	2.169	.520	.088	I	I
4.526	2.095	.590	.103	.012	.001	I	I
1.273	.357	.056	.005	.000	.000	I	I
15.309	18.181	15.400	7.380	-2.212	-3.218	I	I
1.836	-.145	-1.588	-1.753	-1.151	-.530	I	I
-.316	-.695	-.502	-.208	-.056	-.040	I	I
-.389	-.267	-.191	-.018	-.002	-.000	I	I
-.223	-.080	-.014	-.001	-.000	-.000	I	I
.653	.021	-.477	-.559	-.264	.141	I	I
-.254	-.140	.098	.208	.163	.087	I	I
-.041	.132	.138	.067	.020	.004	I	I
.106	.117	.048	.010	.001	.000	I	I
.121	.057	.012	.001	.000	.000	I	I

Table 5a. Eigenvalues of the separation constant  $\Lambda_0(n, n-2, c) - c$

$c \backslash n$	2	3	4	5	6
.00	0.0000	2.0000	6.0000	12.0000	20.0000
.20	.2441	1.5733	6.1039	12.0735	20.0704
.40	.4474	2.2823	6.2233	12.1646	20.1364
.60	.6167	2.4077	6.2933	12.2381	20.1983
.80	.7581	2.5041	6.3305	12.3063	20.2586
1.00	.8769	2.5969	6.4560	12.3699	20.3114
1.20	.9773	2.6773	6.5255	12.4291	20.3631
1.40	1.0629	2.7544	6.5891	12.4835	20.4119
1.60	1.1364	2.8217	6.6480	12.5336	20.4581
1.80	1.2000	2.8825	6.7025	12.5850	20.5018
2.00	1.2554	2.9377	6.7530	12.6337	20.5432
2.20	1.3041	2.9881	6.8033	12.6776	20.5824
2.40	1.3471	3.0342	6.8537	12.7141	20.6197
2.60	1.3853	3.0763	6.8984	12.7523	20.6552
2.80	1.4195	3.1153	6.9427	12.7884	20.6899
3.00	1.4512	3.1511	6.9854	12.8226	20.7242
3.20	1.4779	3.1837	7.0233	12.8549	20.7571
3.40	1.5030	3.2137	7.0593	12.8856	20.7882
3.60	1.5259	3.2413	7.0931	12.9147	20.8190
3.80	1.5466	3.2673	7.1251	12.9424	20.8360
4.00	1.5660	3.2913	7.1576	12.9688	20.8616
4.20	1.5837	3.3136	7.1826	12.9939	20.8862
4.40	1.6000	3.3343	7.2062	13.0179	20.9098
4.60	1.6151	3.3531	7.2287	13.0417	20.9324
4.80	1.6291	3.3703	7.2500	13.0626	20.9541
5.00	1.6422	3.3865	7.2223	13.0835	20.9750

$$\{\Lambda_0(n, n-2, c) - c\} / c$$

$(1/c) \backslash n$	2	3	4	5	6
.20	.3284	.6797	1.4441	2.6167	4.1950
.19	.3150	.6500	1.3766	2.4308	3.9902
.18	.3013	.6193	1.3389	2.2647	3.7852
.17	.2874	.5895	1.2408	2.2382	3.5799
.16	.2731	.5533	1.1724	2.1114	3.3743
.15	.2585	.5276	1.1335	1.9342	3.1687
.14	.2437	.4961	1.0343	1.8566	2.9619
.13	.2285	.4644	.9645	1.7285	2.7551
.12	.2131	.4311	.8944	1.6000	2.5479
.11	.1972	.3939	.8237	1.4713	2.3401
.10	.1810	.3555	.7525	1.3414	2.1318
.09	.1646	.3143	.6806	1.2112	1.9229
.08	.1477	.2723	.6082	1.0813	1.7133
.07	.1306	.2295	.5351	.9487	1.5039
.06	.1130	.2263	.4623	.8263	1.2918
.05	.0961	.1477	.3867	.6933	1.0797
.04	.0769	.1567	.3113	.5488	.8655
.03	.0582	.0784	.2350	.4135	.6524
.02	.0396	.0714	.1577	.2777	.4357
.01	.0219	.0376	.0794	.1392	.2190
.00	.0000	.0000	.0000	.0000	.0000

Table 5b. Eigenvalues of the separation constant  $\Lambda_2(n, n-2, c) - c$

$c \setminus n$	2	3	4	5	6
.00	6.00000	12.00000	20.00000	30.00000	42.00000
.20	5.55599	12.64398	21.69111	30.71445	42.72966
.40	7.15226	13.31722	21.39221	31.43544	43.46336
.60	7.78333	14.00000	22.10199	32.16119	44.20117
.80	8.44419	14.69593	22.81995	32.89337	44.94334
1.00	9.12331	15.40331	23.54440	33.63001	45.68936
1.20	9.82227	16.12011	24.27477	34.37099	46.43699
1.40	10.53771	16.84566	25.01099	35.11559	47.18819
1.60	11.26336	17.57833	25.75200	35.86336	47.94119
1.80	12.00000	18.31775	26.49755	36.61500	48.69882
2.00	12.74446	19.06223	27.24700	37.36993	49.45668
2.20	13.49599	19.81119	28.00000	38.12264	50.21776
2.40	14.25229	20.56588	28.75633	38.88599	50.98003
2.60	15.01447	21.32336	29.51555	39.64777	51.74448
2.80	15.78005	22.08447	30.27733	40.41116	52.51110
3.00	16.54998	22.84833	31.04116	41.17774	53.27888
3.20	17.32221	23.61577	31.80888	41.94551	54.04881
3.40	18.09770	24.38693	32.57666	42.71444	54.81888
3.60	18.87441	25.15933	33.34669	43.48553	55.59008
3.80	19.65332	25.92996	34.11899	44.25776	56.36340
4.00	20.43440	26.70447	34.89224	45.03112	57.13884
4.20	21.21663	27.48114	35.66674	45.80661	57.91738
4.40	22.00000	28.25999	36.44338	46.58333	58.69802
4.60	22.78449	29.03999	37.22110	47.36111	59.48076
4.80	23.57009	29.81997	38.00000	48.13774	60.26559
5.00	24.35778	30.60115	38.77337	48.91665	61.05250

$$\{ \Lambda_2(n, n-2, 0) - c \} / c$$

$(1/c) \Lambda n$	2	3	4	5	6
.20	4.87116	6.01203	7.75599	9.78333	12.20500
.19	4.82500	6.01000	7.56334	9.48999	11.78998
.18	4.77877	5.98001	7.37111	9.19553	11.37448
.17	4.73226	5.97900	7.17922	8.90118	10.96001
.16	4.68669	5.96811	6.98776	8.60886	10.54557
.15	4.64115	5.95724	6.79669	8.31558	10.13117
.14	4.59563	5.94639	6.60555	8.02334	9.71811
.13	4.55115	5.93553	6.41415	7.73115	9.30449
.12	4.50770	5.92468	6.22256	7.44000	8.89221
.11	4.46526	5.91412	6.03063	7.14900	8.47999
.10	4.42390	5.90345	5.83875	6.85886	8.06882
.09	4.37954	4.89233	5.64718	6.56888	7.65771
.08	4.33333	4.88222	5.45594	6.27997	7.24667
.07	4.28844	4.77177	5.26449	5.99133	6.83770
.06	4.24470	4.66132	5.07387	5.70337	6.42882
.05	4.20449	4.55333	4.91333	5.41770	6.02003
.04	4.16331	4.44060	4.72337	5.13112	5.61335
.03	4.12188	4.33034	4.54550	4.84665	5.20779
.02	4.08088	4.22016	4.36223	4.56330	4.80337
.01	4.04000	4.10004	4.18006	4.28008	4.40000
.00	4.00000	4.00000	4.00000	4.00000	4.00000



Table 5c. Eigenvalues of the separation constant  $\Lambda_1(n, n-3, c) - c$

$c \setminus n$	3	4	5	6	7
.00	2.00000	6.00000	12.00000	20.00000	30.00000
.20	2.86644	6.73188	12.69889	21.61125	30.58003
.40	3.49669	7.44133	13.30227	21.21400	31.15223
.60	3.49669	8.13119	13.93222	21.80522	31.71644
.80	3.26444	8.80000	14.54881	22.38664	32.27300
1.00	5.00000	9.45000	15.15111	22.95884	32.82226
1.20	5.70449	10.08225	15.74222	23.52216	33.36553
1.40	7.38088	10.69881	16.32119	24.07664	33.90117
1.60	8.02977	11.29881	16.89116	24.62335	34.43200
1.80	8.65338	11.88338	17.45011	25.16331	34.95666
2.00	9.25544	12.45667	18.00000	25.69559	35.47558
2.20	9.83668	13.01533	18.54122	26.22221	35.98999
2.40	10.40000	13.56455	19.07444	26.74422	36.49991
2.60	10.94711	14.10227	19.60300	27.25655	37.00337
2.80	11.47999	14.63113	20.11886	27.76653	37.50339
3.00	12.00000	15.15111	20.63007	28.26991	38.00000
3.20	12.50889	15.66223	21.13677	28.76880	38.49222
3.40	13.00779	16.16774	21.63700	29.26225	38.98007
3.60	13.49881	16.66550	22.13220	29.75226	39.46557
3.80	13.98005	17.15664	22.62221	30.23888	39.94773
4.00	14.45660	17.64222	23.10776	30.72212	40.42558
4.20	14.92553	18.12227	23.58887	31.20200	40.90113
4.40	15.38991	18.59883	24.06555	31.67755	41.37440
4.60	15.84880	19.06995	24.53993	32.14778	41.84339
4.80	15.30225	19.53667	25.00992	32.61171	42.31113
5.00	16.75330	20.00000	25.47558	33.08335	42.77663

$$\{\Lambda_1(n, n-3, c) - c\}/c$$

$(1/c) \setminus n$	3	4	5	6	7
.20	3.35006	4.00000	5.03522	6.61667	8.55553
.19	3.29447	3.91443	4.95662	6.43117	8.24331
.18	3.23776	3.82885	4.81662	6.18558	7.93001
.17	3.17994	3.74111	4.67500	5.96900	7.61662
.16	3.12000	3.65332	4.53227	5.75510	7.30114
.15	3.05994	3.56660	4.38991	5.53339	6.98552
.14	2.99776	3.47774	4.24422	5.31115	6.66885
.13	2.93445	3.37774	4.09777	5.08998	6.35002
.12	2.87022	3.28223	3.93997	4.86665	6.03005
.11	2.80447	3.18666	3.80000	4.64416	5.70993
.10	2.73779	3.08887	3.64885	4.41449	5.38662
.09	2.66998	2.99220	3.49350	4.18661	5.06443
.08	2.60004	2.89774	3.33994	3.95522	4.73442
.07	2.52998	2.79333	3.18216	3.72220	4.40446
.06	2.45779	2.67997	3.02213	3.48661	4.07223
.05	2.38447	2.57770	2.85885	3.24773	3.73700
.04	2.31022	2.46660	2.69330	3.00554	3.39883
.03	2.23445	2.35337	2.52446	2.76000	3.05557
.02	2.15776	2.23773	2.35330	2.51999	2.70889
.01	2.07994	2.11993	2.17662	2.27577	2.35771
.00	2.00000	2.00000	2.00000	2.00000	2.00000

Table 5d. Eigenvalues of the separation constant  $\Lambda_3(n, n-3, c) - 0$

$c \setminus n$	3	4	5	6	7
.00	12.00000	20.00000	30.00000	42.00000	56.00000
.20	12.73556	20.86882	30.94411	42.98875	57.01997
.40	13.50331	21.75882	31.88973	43.98860	58.04777
.60	14.30331	22.66911	32.86788	44.99448	59.08336
.80	15.13556	23.60000	33.85119	46.01336	60.12770
1.00	16.00000	24.54998	34.84889	47.04116	61.17774
1.20	17.89551	25.51775	35.85778	48.07884	62.23447
1.40	17.81923	26.50113	36.88781	49.12336	63.29883
1.60	18.77703	27.50113	37.90990	50.17665	64.36880
1.80	19.74622	28.51622	38.94999	51.23669	65.44334
2.00	20.74446	29.54444	40.00000	52.30441	66.52442
2.20	21.76322	30.58441	41.05338	53.37779	67.61001
2.40	22.80000	31.63555	42.12556	54.44578	68.70009
2.60	23.85229	32.69773	43.20330	55.51435	69.79663
2.80	24.92201	33.76887	44.28114	56.58347	70.89961
3.00	25.00000	34.84889	45.36933	57.73309	72.00000
3.20	27.09111	35.93771	46.46333	58.83220	73.10778
3.40	28.19222	37.03226	47.56330	59.93775	74.21993
3.60	29.30111	38.13350	48.66936	61.04774	75.33443
3.80	30.41999	39.24336	49.77779	62.14912	76.45227
4.00	31.54440	40.35779	50.88924	63.27888	77.57442
4.20	32.67477	41.47773	51.99333	64.40000	78.69887
4.40	33.81099	42.59501	53.09331	65.52225	79.82660
4.60	34.95200	43.71305	54.18807	66.65222	80.95664
4.80	35.09975	44.83333	55.28008	67.78229	82.08887
5.00	37.24770	46.00000	56.52442	68.91665	83.22337

$$\{\Lambda_3(n, n-3, 0) - 0\}/0$$

$(1/C) \setminus n$	3	4	5	6	7
.20	7.44994	9.20000	11.10448	13.79333	16.64447
.19	7.36823	9.02222	11.02338	13.67833	16.49969
.18	7.28652	8.85111	10.94338	13.57442	16.35499
.17	7.20481	8.67999	10.86500	13.47110	16.21038
.16	7.12310	8.50773	10.78773	13.36888	16.06578
.15	7.04139	8.33333	10.71000	13.26666	15.92117
.14	6.95968	8.16333	10.63333	13.16444	15.77657
.13	6.87797	8.00000	10.55666	13.06222	15.63196
.12	6.79626	7.83333	10.48000	12.96000	15.48736
.11	6.71455	7.67333	10.40333	12.85778	15.34275
.10	6.63284	7.51113	10.32666	12.75556	15.19815
.09	6.55113	7.35113	10.25000	12.65334	15.05354
.08	6.46942	7.19222	10.17333	12.55112	14.90894
.07	6.38771	7.03333	10.09666	12.44890	14.76433
.06	6.30600	6.88115	10.02000	12.34668	14.61973
.05	6.22429	6.72991	9.94333	12.24446	14.47512
.04	6.14258	6.57877	9.86666	12.14224	14.33052
.03	6.06087	6.43000	9.79000	12.04002	14.18591
.02	5.97916	6.28113	9.71333	11.93780	14.04131
.01	5.89745	6.14112	9.63666	11.83558	13.89670
.00	5.81574	6.00000	9.56000	11.73336	13.75210

Table 5e. Eigenvalues of the separation constant  $\{\Lambda_0(n, n-4, c) - c\}$

c \ n	4	5	6	7	8
0.00	.0000	2.0000	6.0000	12.0000	20.0000
.20	.4718	2.2954	6.2156	12.4598	20.4807
.40	.8400	2.5430	6.4080	12.9251	20.9703
.60	1.1313	2.7660	6.5806	12.4676	20.3915
.80	1.3664	2.9558	6.7362	12.5989	20.5048
1.00	1.5602	3.1225	6.8774	12.7202	20.6107
1.20	1.7236	3.2702	7.0060	12.8326	20.7102
1.40	1.8623	3.4021	7.1237	12.9372	20.8036
1.60	1.9831	3.5207	7.2318	13.0347	20.8917
1.80	2.0893	3.6273	7.3315	13.1258	20.9748
2.00	2.1835	3.7255	7.4238	13.2111	21.0533
2.20	2.2679	3.8147	7.5096	13.2913	21.1277
2.40	2.3441	3.8967	7.5894	13.3667	21.1982
2.60	2.4133	3.9722	7.6640	13.4379	21.2652
2.80	2.4765	4.0422	7.7339	13.5051	21.3290
3.00	2.5346	4.1072	7.7995	13.5687	21.3897
3.20	2.5881	4.1678	7.8611	13.6290	21.4476
3.40	2.6376	4.2244	7.9193	13.6862	21.5029
3.60	2.6836	4.2774	7.9742	13.7406	21.5557
3.80	2.7265	4.3272	8.0262	13.7925	21.6063
4.00	2.7666	4.3741	8.0754	13.8419	21.6547
4.20	2.8041	4.4183	8.1222	13.8890	21.7012
4.40	2.8394	4.4601	8.1666	13.9341	21.7458
4.60	2.8725	4.5096	8.2090	13.9772	21.7886
4.80	2.9038	4.5571	8.2493	14.0185	21.8298
5.00	2.9334	4.5727	8.2878	14.0581	21.8694

$\{\Lambda_0(n, n-4, c) - c\}/c$

(1/c) \ n	4	5	6	7	8
.20	.5867	.9145	1.6576	2.8116	4.3739
.19	.5643	.8772	1.5838	2.6805	4.1647
.18	.5414	.8393	1.5095	2.5488	3.9550
.17	.5179	.8008	1.4346	2.4165	3.7447
.16	.4939	.7617	1.3590	2.2837	3.5339
.15	.4693	.7218	1.2828	2.1501	3.3225
.14	.4440	.6813	1.2057	2.0158	3.1103
.13	.4181	.6410	1.1279	1.8807	2.8974
.12	.3915	.5993	1.0493	1.7448	2.6836
.11	.3642	.5548	.9697	1.6079	2.4690
.10	.3361	.5103	.8891	1.4700	2.2533
.09	.3072	.4653	.8073	1.3310	2.0364
.08	.2774	.4193	.7244	1.1907	1.8183
.07	.2467	.3727	.6402	1.0490	1.5988
.06	.2150	.3243	.5546	.9057	1.3776
.05	.1822	.2745	.4673	.7607	1.1546
.04	.1484	.2232	.3793	.6137	.9295
.03	.1133	.1702	.2873	.4645	.7019
.02	.0770	.1173	.1941	.3128	.4715
.01	.0392	.0588	.0985	.1581	.2377
.00	.0000	.0000	.0000	.0000	.0000

Table 5f. Eigenvalues of the separation constant  $\{\Lambda_2(n, n-4, c) - c\}$

$c \setminus n$	4	5	6	7	8
0.00	6.00000	12.00000	20.00000	30.00000	42.00000
0.20	7.00004	13.02667	21.01118	30.99223	42.97442
0.40	8.07773	14.07733	22.02294	31.98553	43.94711
0.60	9.20355	15.13355	23.04995	32.97775	44.91911
0.80	10.35779	16.19995	24.06699	33.96779	45.88866
1.00	11.52553	17.26722	25.08886	34.95556	46.85222
1.20	12.69446	18.33333	26.11442	35.94000	47.81146
1.40	13.85889	19.39999	27.11554	36.92005	48.77735
1.60	15.01223	20.46888	28.12115	37.89666	49.74247
1.80	16.15115	21.49447	29.12118	38.86882	50.68801
2.00	17.27441	22.55322	30.11559	39.83550	51.62276
2.20	18.37886	23.62990	31.10333	40.79668	52.53711
2.40	19.46443	24.72990	32.08445	41.75337	53.43100
2.60	20.53110	25.85889	33.05888	42.70556	54.44452
2.80	21.57889	26.98887	34.02664	43.65225	55.37779
3.00	22.60886	27.57116	34.98774	44.59345	56.30556
3.20	23.62009	28.54333	35.94449	45.52317	57.22335
3.40	24.61667	29.51113	36.89330	46.44641	58.14996
3.60	25.59771	30.47883	37.83119	47.36318	59.06611
3.80	26.56331	31.43333	38.76779	48.27151	59.97991
4.00	27.51559	32.37766	39.69882	49.17339	60.88833
4.20	28.45555	33.30021	40.62238	50.06885	61.79443
4.40	29.38558	34.21333	41.54322	50.95991	62.69669
4.60	30.30550	35.11885	42.45565	51.84656	63.59663
4.80	31.21448	36.01733	43.36000	52.72884	64.49227
5.00	32.11622	36.98113	44.27007	53.60675	65.38550

$$\{\Lambda_2(n, n-4, c) - c\}/c$$

$(1/c) \setminus n$	4	5	6	7	8
0.20	5.42332	7.39664	8.85441	10.75335	13.07772
0.19	5.32552	7.25227	8.63064	10.43396	12.64558
0.18	5.22247	7.10557	8.41171	10.12244	12.21335
0.17	5.12116	6.95777	8.19611	9.80779	11.77999
0.16	5.01559	6.80663	7.97333	9.48899	11.34522
0.15	4.90766	6.65333	7.74066	9.17003	10.90999
0.14	4.79677	6.49333	7.52100	8.84887	10.47112
0.13	4.68331	6.33443	7.29233	8.52522	10.03316
0.12	4.56669	6.17553	7.06665	8.19993	9.59300
0.11	4.44881	6.01113	6.82556	7.87339	9.14661
0.10	4.32668	5.84335	6.58881	7.53397	8.69996
0.09	4.20330	5.67334	6.34442	7.20553	8.25022
0.08	4.07668	5.50113	6.10228	6.86675	7.79771
0.07	3.94885	5.32883	5.85446	6.52255	7.34111
0.06	3.81880	5.14882	5.60226	6.17302	6.88005
0.05	3.68556	4.96447	5.34663	5.82299	6.41522
0.04	3.55113	4.77881	5.08359	5.47448	5.94446
0.03	3.41544	4.58779	4.82113	5.11444	5.46883
0.02	3.27881	4.39448	4.55117	4.74886	4.98557
0.01	3.13966	4.19333	4.27880	4.37772	4.49664
0.00	3.00000	4.00000	4.00000	4.00000	4.00000

Table 5g. Eigenvalues of the separation constant  $\{A_4(n, n-4, c) - c\}$

$c \setminus n$	4	5	6	7	8
0.00	20.00000	30.00000	42.00000	56.00000	72.00000
.20	20.92779	31.07133	43.17255	57.23379	73.28557
.40	21.88277	32.17333	44.36266	58.48896	74.58206
.60	22.86552	33.30055	45.63999	59.75499	75.92854
.80	23.87556	34.44447	46.79338	61.03332	77.20887
1.00	24.91445	35.61003	48.03440	62.32441	78.53770
1.20	25.98222	36.79603	49.28998	63.62733	79.87552
1.40	27.07888	38.00441	50.56669	64.94233	81.22229
1.60	28.20446	39.23443	51.84667	66.26675	82.57996
1.80	29.35992	40.48773	53.14667	67.60061	83.94551
2.00	30.54224	41.74233	54.46033	68.95339	85.31991
2.20	31.75555	43.02533	55.78669	70.31119	86.70112
2.40	32.99916	44.32544	57.12660	71.67555	88.09111
2.60	34.25557	45.64119	58.47772	73.05665	89.48885
2.80	35.52446	46.97441	59.83997	74.44424	90.89332
3.00	36.85669	48.32442	61.21332	75.83368	92.30447
3.20	38.19110	49.68233	62.59770	77.23394	93.72229
3.40	39.54557	51.05667	63.99077	78.64977	95.14775
3.60	40.91993	52.44337	65.39339	80.06675	96.57882
3.80	42.31104	53.84224	66.80559	81.49225	98.01448
4.00	43.71775	55.25233	68.22664	82.92422	99.45770
4.20	45.13994	56.67336	69.65558	84.36224	100.90445
4.40	46.57748	58.10226	71.09111	85.80668	102.35733
4.60	48.02244	59.54113	72.53445	87.25772	103.81550
4.80	49.48113	60.99006	73.98447	88.71331	105.27775
5.00	50.95004	62.44555	75.44445	90.17444	106.74445

$$\{A_4(n, n-4, c) - c\}/c$$

$(1/c) \setminus n$	4	5	6	7	8
.20	10.19001	12.48331	15.08863	18.03349	21.34889
.19	10.05005	12.23008	14.69998	17.51000	20.64995
.18	9.91440	11.97443	14.31334	16.96668	19.95116
.17	9.78005	11.72133	13.92933	16.43355	19.25553
.16	9.65002	11.47115	13.54777	15.90664	18.56009
.15	9.52311	11.22447	13.16887	15.37996	17.86886
.14	9.39933	10.98117	12.79226	14.85555	17.17885
.13	9.27888	10.73333	12.41777	14.33341	16.49110
.12	9.16116	10.49233	12.05333	13.81559	15.80664
.11	9.04777	10.25777	11.68845	13.30302	15.12550
.10	9.93772	10.02225	11.32228	12.79903	14.44771
.09	8.82299	9.81117	10.96555	12.28337	13.77334
.08	8.72556	9.59551	10.61228	11.78118	13.10442
.07	8.52499	9.37333	10.26522	11.28551	12.44002
.06	8.52270	9.15115	9.92229	10.79441	11.78220
.05	8.43222	8.96003	9.58864	10.30994	11.13003
.04	8.34003	8.75333	9.25229	9.83315	10.48559
.03	8.25113	8.55113	8.93117	9.36110	9.84998
.02	8.16449	8.35333	8.61442	8.89886	9.22228
.01	8.08112	8.15113	8.30336	8.44447	8.60558
.00	8.00000	8.00000	8.00000	8.00000	8.00000

Table 5h. Eigenvalues of the separation constant  $\Lambda_1(n, n-5, c) - c$

$c \setminus n$	5	6	7	8	9
0.00	2.00000	6.00000	12.00000	20.00000	30.00000
0.20	3.5197	7.0587	12.9156	20.8233	30.7595
0.40	4.5566	8.0643	13.7949	21.6217	31.5004
0.60	5.7098	9.0217	14.6421	22.3967	32.2239
0.80	6.7819	9.9322	15.4587	23.1499	32.9309
1.00	7.7781	10.8002	16.2471	23.8828	33.6226
1.20	8.7057	11.6294	17.0095	24.5969	34.2999
1.40	9.5725	12.4232	17.7479	25.2934	34.9636
1.60	10.3865	13.1853	18.4644	25.9736	35.6148
1.80	11.1552	13.9180	19.1607	26.6386	36.2541
2.00	11.8849	14.6263	19.8384	27.2895	36.8824
2.20	12.5814	15.3177	20.4931	27.9275	37.5002
2.40	13.2494	15.9743	21.1442	28.5532	38.1083
2.60	13.8928	16.6193	21.7750	29.1677	38.7072
2.80	14.5149	17.2473	22.3926	29.7716	39.2975
3.00	15.1185	17.8601	22.9980	30.3657	39.8798
3.20	15.7060	18.4592	23.5923	30.9506	40.4544
3.40	16.2791	19.0457	24.1762	31.5270	41.0218
3.60	16.8397	19.6200	24.7496	32.0953	41.5826
3.80	17.3890	20.1856	25.3161	32.6552	42.1369
4.00	17.9283	20.7433	25.8734	33.2101	42.6853
4.20	18.4585	21.2975	26.4231	33.7574	43.2279
4.40	18.9800	21.8482	26.9657	34.2986	43.7652
4.60	19.4933	22.3957	27.5017	34.8340	44.2975
4.80	20.0033	22.9402	28.0316	35.3639	44.8249
5.00	20.5052	23.4804	28.5557	35.8886	45.3478

$$\{\Lambda_1(n, n-5, c) - c\} / c$$

$(1/c) \setminus n$	5	6	7	8	9
0.20	4.1010	4.6801	5.7111	7.1777	9.0696
0.19	4.0198	4.5741	5.5521	6.9436	8.7456
0.18	3.9368	4.4650	5.3972	6.7179	8.4201
0.17	3.8519	4.3560	5.2374	6.4854	8.0930
0.16	3.7650	4.2433	5.0755	6.2510	7.7642
0.15	3.6760	4.1234	4.9114	6.0145	7.4334
0.14	3.5848	4.0125	4.7449	5.7757	7.1006
0.13	3.4913	3.8931	4.5758	5.5344	6.7653
0.12	3.3954	3.7703	4.4039	5.2914	6.4275
0.11	3.2969	3.6458	4.2290	5.0435	6.0869
0.10	3.1958	3.5175	4.0508	4.7932	5.7430
0.09	3.0919	3.3853	3.8690	4.5393	5.3955
0.08	2.9850	3.2507	3.6833	4.2813	5.0440
0.07	2.8749	3.1115	3.4932	4.0189	4.6888
0.06	2.7615	2.9683	3.2985	3.7514	4.3268
0.05	2.6446	2.8205	3.0986	3.4784	3.9598
0.04	2.5239	2.6677	2.8930	3.2000	3.5860
0.03	2.3994	2.5033	2.6810	2.9126	3.2046
0.02	2.2707	2.3263	2.4621	2.6180	2.8141
0.01	2.1376	2.1465	2.2354	2.3143	2.4132
0.00	2.0000	2.0000	2.0000	2.0000	2.0000

Table 51. Eigenvalues of the separation constant  $\Lambda_3(n, n-5, c) - c$

$c \setminus M$	5	6	7	8	9
0.00	12.00000	20.00000	30.00000	42.00000	56.00000
.20	13.15666	21.25774	31.29099	43.30200	57.30433
.40	14.37099	22.54449	32.56800	44.61133	58.61400
.60	15.64355	23.85966	33.91964	45.93244	59.92822
.80	16.97168	25.19885	35.25229	47.25581	61.24660
1.00	18.35033	26.55779	36.59666	48.58922	62.56669
1.20	19.77177	27.93444	37.94855	49.92466	63.88999
1.40	21.22755	29.32455	39.30700	51.26333	65.21455
1.60	22.70997	30.72557	40.67033	52.60444	66.54933
1.80	24.21066	32.13337	42.03771	53.94771	67.88666
2.00	25.72334	33.54667	43.40600	55.29055	69.19331
2.20	27.24233	34.96155	44.77559	56.63342	70.51933
2.40	28.76666	36.37777	46.14558	57.97744	71.84449
2.60	30.29996	37.79228	47.51448	59.31977	73.16995
2.80	31.79008	39.20554	48.88221	60.66007	74.49330
3.00	33.29333	40.61444	50.24773	62.00000	75.81550
3.20	34.78522	42.01833	51.60997	63.33373	77.13554
3.40	36.26566	43.41133	52.96889	64.66723	78.45440
3.60	37.73316	44.81122	54.32466	66.00049	79.77007
3.80	39.18455	46.21932	55.67666	67.33348	81.08553
4.00	40.62322	47.57866	57.02455	68.66620	82.39779
4.20	42.04477	48.93166	58.36844	69.99866	83.70882
4.40	43.45882	50.28166	59.70811	71.33075	85.01624
4.60	44.85550	51.62799	61.04344	72.66258	86.32250
4.80	46.23866	53.03224	62.37455	73.94411	87.62254
5.00	47.60966	54.37889	63.70144	75.25333	88.92665

$$\{\Lambda_3(n, n-5, c) - c\}/c$$

$(1/c) \setminus M$	5	6	7	8	9
.20	9.5219	10.87553	12.74337	15.0507	17.7853
.19	9.3851	10.66667	12.4337	14.6253	17.2206
.18	9.2442	10.45774	12.1257	14.1988	16.6551
.17	9.0990	10.2445	11.8159	13.7711	16.0886
.16	8.9493	10.0247	11.5041	13.3419	15.5210
.15	8.7947	9.8047	11.1901	12.9110	14.9520
.14	8.6353	9.5813	10.8735	12.4781	14.3814
.13	8.4709	9.3544	10.5541	12.0430	13.8030
.12	8.3016	9.1228	10.2314	11.6052	13.2344
.11	8.1275	8.8871	9.9051	11.1645	12.6574
.10	7.9488	8.6469	9.5748	10.7204	12.0774
.09	7.7658	8.4017	9.2404	10.2724	11.4941
.08	7.5788	8.1514	8.9037	9.8204	10.9066
.07	7.3883	7.8973	8.5562	9.3629	10.3151
.06	7.1948	7.6373	8.2065	8.9005	9.7182
.05	5.9987	7.3732	7.8513	8.4322	9.1155
.04	5.8007	7.1047	7.4906	7.9579	8.5064
.03	5.6012	6.8325	7.1246	7.4773	7.8905
.02	5.4009	6.5573	6.7538	6.9905	7.2673
.01	5.2003	6.2795	6.3786	6.4974	6.6370
.60	6.0000	6.0000	6.0000	6.0000	6.0000

Table 5j. Eigenvalues of the separation constant  $\Lambda_5(n, n-5, c) - c$

$c \setminus n$	5	6	7	8	9
0.00	30.00000	42.00000	56.00000	72.00000	90.00000
.20	31.12337	43.28733	57.39441	73.47446	91.53551
.40	32.27255	44.59372	58.83771	74.96551	93.08556
.60	33.44666	45.91337	60.23886	76.47099	94.64330
.80	34.64662	47.26933	61.68884	77.99220	96.22331
1.00	35.87115	48.64113	63.15663	79.52220	97.81066
1.20	37.12227	50.03333	64.64220	81.07335	99.41133
1.40	38.40000	51.44523	66.14551	82.64433	101.02449
1.60	39.70338	52.88977	67.66533	84.22220	102.64449
1.80	41.03342	54.34883	69.20223	85.81143	104.27922
2.00	42.39117	55.82273	70.75566	87.41999	105.92445
2.20	43.77633	57.31273	72.32550	89.03833	107.58339
2.40	45.18883	58.84880	73.91330	90.66994	109.24668
2.60	46.62277	60.38881	75.51022	92.31226	110.92333
2.80	48.09443	61.94473	77.12533	93.96577	112.60995
3.00	49.58882	63.52255	78.75447	95.63343	114.30353
3.20	51.10888	65.12221	80.39880	97.31121	116.01102
3.40	52.65559	66.73554	82.05449	99.00007	117.72444
3.60	54.22887	68.36881	83.72448	100.69998	119.44668
3.80	55.82665	70.01662	85.43774	102.43990	121.17779
4.00	57.44885	71.68775	87.18211	104.21279	122.93169
4.20	59.09338	73.38602	88.96885	106.02563	124.66339
4.40	60.76112	75.10546	90.79262	107.86939	126.41855
4.60	62.44497	76.84633	92.62548	109.74402	128.18805
4.80	64.14581	78.60855	93.93339	111.64951	129.94966
5.00	65.86553	80.39227	95.74229	112.85881	131.72556

$$\{\Lambda_5(n, n-5, c) - c\} / c$$

$(1/c) \setminus n$	5	6	7	8	9
.20	13.17771	16.04441	19.14886	22.57716	26.34551
.19	12.95551	15.67933	18.63122	21.88661	25.47338
.18	12.73990	15.31956	18.11771	21.20333	24.60448
.17	12.52291	14.96225	17.60657	20.52335	23.73884
.16	12.32558	14.61115	17.10007	19.84771	22.87448
.15	12.12933	14.26553	16.59885	19.17445	22.01446
.14	11.93999	13.92622	16.10116	18.51622	21.15881
.13	11.75778	13.59223	15.61011	17.84226	20.30557
.12	11.58336	13.26553	15.12447	17.18443	19.45880
.11	11.41555	12.94441	14.64559	16.53220	18.61558
.10	11.25553	12.63556	14.17444	15.88664	17.77996
.09	11.10223	12.33223	13.71099	15.24883	16.95444
.08	10.95552	12.03375	13.25661	14.61886	16.12991
.07	10.81668	11.75114	12.81055	13.99882	15.31669
.06	10.68337	11.47543	12.37550	13.38881	14.51559
.05	10.55557	11.20663	11.95022	12.78944	13.72447
.04	10.43334	10.94474	11.53365	12.20331	12.94775
.03	10.31994	10.69775	11.13344	11.63022	12.18550
.02	10.20884	10.45555	10.74422	11.07155	11.43888
.01	10.10221	10.22221	10.36666	10.52800	10.70998
.00	10.00000	10.00000	10.00000	10.00000	10.00000



Table 6a. Eigenvalues of the separation constant  $\Lambda_0(n, n-2, p) + p$

$p \setminus n$	2	3	4	5	6
.00	0.0000	2.0000	6.0000	12.0000	20.0000
.20	-.2914	1.8223	5.8739	11.9375	19.9248
.40	-.6355	1.6343	5.7471	11.8071	19.8443
.60	-1.0355	1.4117	5.6010	11.6981	19.7581
.80	-1.4914	1.1621	5.4368	11.5795	19.6655
1.00	-2.0000	.8763	5.2554	11.4502	19.5660
1.20	-2.5559	.5533	5.0538	11.3089	19.4589
1.40	-3.1526	.1953	4.8297	11.1454	19.3434
1.60	-3.7833	-.2053	4.5888	10.9585	19.2186
1.80	-4.4419	-.6447	4.3044	10.8000	19.0838
2.00	-5.1233	-1.1233	4.0000	10.5969	18.9377
2.20	-5.8227	-1.6373	3.6664	10.3742	18.7795
2.40	-6.5371	-2.1869	3.2936	10.1304	18.6079
2.60	-7.2636	-2.7653	2.8969	9.8637	18.4217
2.80	-8.0000	-3.3737	2.4644	9.5725	18.2195
3.00	-8.7446	-4.0000	2.0000	9.2554	18.0000
3.20	-9.4959	-4.6433	1.5049	8.9114	17.7619
3.40	-10.2529	-5.3117	1.0008	8.5396	17.5037
3.60	-11.0147	-6.0000	.4997	8.1396	17.2243
3.80	-11.7800	-6.6953	-.1462	7.7114	16.9223
4.00	-12.5498	-7.4031	-.7446	7.2554	16.5969
4.20	-13.3221	-8.1211	-1.3632	6.7725	16.2470
4.40	-14.0970	-8.8456	-2.0000	6.2637	15.8723
4.60	-14.8741	-9.5753	-2.6529	5.7304	15.4723
4.80	-15.6532	-10.3115	-3.3201	5.1742	15.0470
5.00	-15.4340	-11.0623	-4.0000	4.5969	14.5969

$$\{\Lambda_0(n, n-2, p) + p\}/p$$

$(1/p) \setminus n$	2	3	4	5	6
.20	-3.2868	-2.2125	-.8000	.9194	2.9194
.19	-3.3181	-2.2234	-.8332	.7235	2.6538
.18	-3.3499	-2.2367	-1.0698	.5213	2.3799
.17	-3.3821	-2.2447	-1.2039	.3127	2.0966
.16	-3.4148	-2.2529	-1.3533	.0976	1.8035
.15	-3.4480	-2.2612	-1.5000	-.1238	1.5000
.14	-3.4817	-2.2695	-1.6498	-.3514	1.1861
.13	-3.5158	-2.2781	-1.8027	-.5849	.8617
.12	-3.5504	-2.2868	-1.9584	-.8240	.5274
.11	-3.5854	-2.2957	-2.1169	-1.0684	.1836
.10	-3.6209	-3.0410	-2.2780	-1.3177	-.1689
.09	-3.6569	-3.1315	-2.4415	-1.5715	-.4521
.08	-3.6933	-3.2233	-2.6073	-1.8294	-.7896
.07	-3.7301	-3.3163	-2.7753	-2.0911	-1.1269
.06	-3.7674	-3.4103	-2.9452	-2.3560	-1.4685
.05	-3.8051	-3.5051	-3.1171	-2.6241	-2.0319
.04	-3.8433	-3.6000	-3.2906	-2.8948	-2.4194
.03	-3.8818	-3.6958	-3.4658	-3.1680	-2.7304
.02	-3.9208	-3.7926	-3.6426	-3.4434	-3.0044
.01	-3.9602	-3.8903	-3.8206	-3.7208	-3.2600
.00	-4.0000	-4.0000	-4.0000	-4.0000	-4.0000

Table 6b. Eigenvalues of the separation constant  $\Lambda_2(n, n-2, p) + p$

$p \setminus n$	2	3	4	5	6
.60	6.06000	12.00000	20.00000	30.00000	42.00000
.80	4.49144	11.37377	19.32000	29.03325	41.27552
1.00	3.03555	10.75551	18.65552	28.36929	40.55557
1.20	1.62914	9.63773	17.00000	27.22055	39.84119
1.40	4.06000	9.12311	16.74466	26.54998	38.43440
1.60	3.75599	8.64477	16.14622	25.89111	37.74111
1.80	3.55226	8.20511	15.57033	25.24656	37.15666
2.00	3.38333	7.80511	15.01922	24.61447	36.38114
2.20	3.24119	7.44447	14.49551	24.03000	35.71622
2.40	3.12311	7.12311	14.00000	23.40331	35.06223
2.60	3.02227	6.83773	13.53556	22.82558	34.42055
2.80	2.93771	6.58663	13.10331	22.28696	33.79221
3.00	2.86336	6.36551	12.70331	21.79363	33.17833
3.20	2.80000	6.17077	12.33556	21.22775	32.58005
3.40	2.74466	6.00000	12.00000	20.74466	32.00000
3.60	2.69599	5.84998	11.69351	20.28886	31.43881
3.80	2.65229	5.71772	11.41922	19.86004	30.89663
4.00	2.61477	5.60000	11.17666	19.46004	30.37557
4.20	2.58005	5.49466	10.94662	19.09886	29.87777
4.40	2.54998	5.40331	10.74466	18.74466	29.40331
4.60	2.52221	5.32000	10.56333	18.42275	28.95330
4.80	2.49770	5.24556	10.40000	18.13363	28.52777
5.00	2.47441	5.17333	10.25222	17.86996	28.12777
5.20	2.45332	5.11175	10.12000	17.62558	27.75330
5.40	2.43440	5.06223	10.00000	17.40331	27.40331

$$\{\Lambda_2(n, n-2, p) + p\} / p$$

$(1/p) \setminus n$	2	3	4	5	6
.20	4.8668	1.0125	2.00000	3.48006	5.48006
.19	4.5811	.94944	1.87332	3.25565	5.12622
.18	4.2999	.88773	1.74996	3.03387	4.78022
.17	4.0221	.82773	1.62299	2.82273	4.44334
.16	3.7488	.76922	1.51333	2.62224	4.11655
.15	3.4800	.71221	1.40000	2.42338	3.80000
.14	3.2117	.65573	1.28998	2.23114	3.49339
.13	2.9558	.60133	1.18227	2.04449	3.19833
.12	2.7034	.54933	1.07884	1.86640	2.91226
.11	2.4544	.49911	.97669	1.68884	2.63664
.10	2.2099	.44664	.87800	1.51777	2.36889
.09	1.9669	.39711	.78155	1.35155	2.10991
.08	1.7333	.34833	.68733	1.18994	1.85664
.07	1.5011	.30188	.59533	1.03311	1.60998
.06	1.2774	.25553	.50522	.87660	1.36885
.05	1.0551	.21133	.41711	.72411	1.13119
.04	.8333	.16633	.33066	.57488	.89994
.03	.6118	.12733	.24588	.42880	.67004
.02	.4008	.08166	.16222	.28334	.44444
.01	.2020	.04444	.08996	.14008	.22110
.00	.0000	.00000	.00000	.00000	.00000

Table 6c. Eigenvalues of the separation constant  $\Lambda_1(n, n-3, p) + p$

$p \setminus n$	3	4	5	6	7
.00	2.00000	6.00000	12.00000	20.00000	30.00000
.20	1.10449	5.24599	11.32533	19.37760	29.41009
.40	-.18088	4.46889	10.63482	18.73980	28.81277
.60	-.77033	3.66833	9.92559	18.09910	28.20488
.80	-1.74623	2.84559	9.20000	17.42889	27.58669
1.00	-2.74446	2.00000	8.45660	16.75330	26.95884
1.20	-3.76332	1.13133	7.69335	16.06229	26.31889
1.40	-4.80000	-.24778	6.91244	15.35881	25.66880
1.60	-5.85229	-.66661	6.11244	14.63881	25.00522
1.80	-6.92011	-1.60000	5.29335	13.90025	24.33000
2.00	-8.00000	-2.54333	4.45660	13.15111	23.64222
2.20	-9.09111	-3.51778	3.60330	12.38337	22.94122
2.40	-10.19211	-4.50199	2.72559	11.60000	22.22680
2.60	-11.30199	-5.50199	1.83422	10.80000	21.49886
2.80	-12.41995	-6.51622	.92533	9.98337	20.75664
3.00	-13.54440	-7.54440	.00000	9.15111	20.00000
3.20	-14.67477	-8.58441	-.94111	8.30225	19.22911
3.40	-15.81009	-9.63555	-1.89733	7.43881	18.44437
3.60	-16.95220	-10.69733	-2.86678	6.55911	17.64337
3.80	-18.09975	-11.76667	-3.85199	5.66629	16.82691
4.00	-19.24770	-12.84889	-4.84889	4.75330	16.00000
4.20	-20.40000	-13.93771	-5.85778	3.82289	15.15664
4.40	-21.55663	-15.03226	-6.87881	2.89910	14.29886
4.60	-22.71555	-16.13500	-7.90900	1.93988	13.42668
4.80	-23.87773	-17.24466	-8.94339	.97660	12.54122
5.00	-25.04166	-18.35778	-10.00000	.00000	11.64222

$$\{\Lambda_1(n, n-3, p) + p\} / p$$

$(1/p) \setminus n$	3	4	5	6	7
.20	-5.00883	-3.67116	-2.00000	-.00000	2.32884
.19	-5.04991	-3.76881	-2.16500	-.24733	1.98335
.18	-5.09111	-3.86663	-2.33339	-.49886	1.63339
.17	-5.13443	-3.96663	-2.50339	-.75411	1.27922
.16	-5.17776	-4.06631	-2.67680	-1.01442	.91888
.15	-5.22211	-4.17113	-2.85556	-1.27994	.55220
.14	-5.26722	-4.27777	-3.03668	-1.54999	.17822
.13	-5.31332	-4.38556	-3.22116	-1.82660	-.20333
.12	-5.36000	-4.49556	-3.41114	-2.10882	-.59332
.11	-5.40677	-4.60779	-3.60331	-2.39667	-.99199
.10	-5.45664	-4.72224	-3.80000	-2.69116	-1.40000
.09	-5.50660	-4.83332	-4.00111	-3.09333	-1.81779
.08	-5.55666	-4.95884	-4.20664	-3.50117	-2.24557
.07	-5.60882	-5.08880	-4.41660	-3.91669	-2.68335
.06	-5.66005	-5.20443	-4.62999	-4.33988	-3.13133
.05	-5.71446	-5.33335	-4.84334	-4.76673	-3.58885
.04	-5.76994	-5.45995	-5.07004	-5.19322	-4.05449
.03	-5.82537	-5.59339	-5.29669	-5.62032	-4.52999
.02	-5.88224	-5.72442	-5.52774	-6.04901	-5.01222
.01	-5.94006	-5.86112	-5.76278	-6.47825	-5.50331
.00	-5.00000	-6.00000	-6.00000	-6.00000	-6.00000

Table 6d. Eigenvalues of the separation constant  $A_3(n, n-3, p) + p$

$p \setminus n$	3	4	5	6	7
.00	12.00000	20.00000	30.00000	42.00000	56.00000
.20	11.29511	19.15411	29.07477	41.02440	54.98991
.40	10.61922	18.33311	28.16588	40.06602	53.98773
.60	9.97033	17.53311	27.27411	39.10990	52.99552
.80	9.34662	16.75411	26.40000	38.17111	52.01331
1.00	8.74446	16.00000	25.54440	37.24770	51.04116
1.20	8.16332	15.26822	24.70000	36.33771	50.08111
1.40	7.60000	14.55822	23.88776	35.44119	49.13200
1.60	7.05229	13.86911	23.08876	34.56119	48.19448
1.80	6.52011	13.20000	22.30065	33.69775	47.27000
2.00	6.00000	12.54440	21.54440	32.84889	46.35778
2.20	5.49111	11.91111	20.80000	32.01633	45.45888
2.40	4.99221	11.30333	20.07771	31.20000	44.57322
2.60	4.50119	10.70119	19.35558	30.40000	43.70114
2.80	4.01915	10.11662	18.67477	29.61633	42.84336
3.00	3.54440	9.54440	18.00000	28.84889	42.00000
3.20	3.07477	8.98441	17.33333	28.09775	41.17009
3.40	2.61009	8.43555	16.66667	27.36119	40.35563
3.60	2.15119	7.89773	16.00000	26.64119	39.55563
3.80	1.69775	7.36877	15.45119	25.93771	38.77009
4.00	1.24776	6.84889	14.84440	25.24770	38.00000
4.20	0.80000	6.33776	14.25778	24.57111	37.24336
4.40	0.35633	5.83226	13.67881	23.90990	36.50114
4.60	-0.08445	5.33553	13.10990	23.26332	35.77332
4.80	-0.52227	4.84445	12.54440	22.62440	35.05888
5.00	-0.95844	4.35773	12.00000	22.00000	34.35778

$$\{A_3(n, n-3, p) + p\} / p$$

$(1/p) \setminus n$	3	4	5	6	7
.20	-.19171	.87116	2.40000	4.40000	6.87116
.19	-.29044	.70811	2.14550	4.02733	6.35665
.18	-.38844	.54533	1.83229	3.65886	5.84661
.17	-.48577	.38633	1.46439	3.29441	5.34008
.16	-.58222	.22311	1.39800	2.93342	4.84112
.15	-.67779	.07113	1.15556	2.57994	4.34880
.14	-.77228	-.08233	.91666	2.22999	3.86118
.13	-.86668	-.23444	.68226	1.88669	3.38333
.12	-.96000	-.38444	.45000	1.54882	2.91332
.11	-1.05223	-.53221	.22311	1.21667	2.45119
.10	-1.14336	-.67776	-.00000	.89116	2.00000
.09	-1.23440	-.82233	-.24669	.57333	1.55779
.08	-1.32334	-.96116	-.43336	.26117	1.12577
.07	-1.41118	-1.10000	-.64440	-.04331	.70335
.06	-1.49991	-1.23333	-.85551	-.34112	.29113
.05	-1.58854	-1.36335	-1.05220	-.63227	-.11115
.04	-1.67706	-1.50000	-1.24996	-.91778	-.50511
.03	-1.75447	-1.62231	-1.44331	-1.19668	-.89001
.02	-1.83776	-1.75553	-1.63226	-1.46999	-1.26771
.01	-1.91994	-1.87888	-1.81882	-1.73775	-1.63669
.00	-2.00000	-2.00000	-2.00000	-2.00000	-2.00000

Table 6e. Eigenvalues of the separation constant  $\Lambda_0(n, n-4, p) + p$

$p \setminus n$	4	5	6	7	8
6.00	0.0000	2.0000	6.0000	12.0000	20.0000
.20	-.5039	1.6538	5.7569	11.8135	19.8433
.40	-1.3607	1.2333	5.4815	11.6380	19.6851
.60	-2.2726	.7483	5.1676	11.3805	19.5074
.80	-3.3221	.1693	4.8087	11.1277	19.3139
1.00	-4.4821	-.5031	4.3970	10.8458	19.1026
1.20	-5.7254	-1.2905	3.9248	10.5303	18.8710
1.40	-7.0308	-2.1722	3.3845	10.1763	18.6165
1.60	-8.3826	-3.1478	2.7626	9.7792	18.3360
1.80	-9.7695	-4.2043	2.0758	9.3332	18.0261
2.00	-11.1838	-5.3311	1.3019	8.8289	17.6831
2.20	-12.6199	-6.5295	-.4493	8.2668	17.3028
2.40	-14.0737	-7.7433	-1.4774	7.6406	16.8810
2.60	-15.5421	-8.9223	-2.4720	6.9481	16.4135
2.80	-17.0229	-10.3296	-3.5275	6.1883	15.8960
3.00	-18.5140	-11.6646	-4.6365	5.3625	15.3252
3.20	-20.0143	-13.0233	-5.7922	4.4732	14.6980
3.40	-21.5234	-14.4033	-6.9883	3.5246	14.0129
3.60	-23.0374	-15.8000	-8.2196	2.5213	13.2691
3.80	-24.5585	-17.2132	-9.4615	1.4623	12.4674
4.00	-26.0850	-18.6396	-9.7730	-.3709	11.6095
4.20	-27.6164	-20.0781	-11.0820	-1.7662	10.6981
4.40	-29.1523	-21.5273	-12.3417	-3.1428	9.7367
4.60	-30.6930	-22.9865	-13.5657	-4.5048	8.7289
4.80	-32.2394	-24.4544	-14.7332	-5.8319	7.6786
5.00	-33.7821	-25.9301	-16.5153		6.5896

$$\{\Lambda_0(n, n-4, p) + p\}/p$$

$(1/p) \setminus n$	4	5	6	7	8
.20	-6.7564	-5.1863	-3.3031	-1.1264	1.3179
.19	-6.8061	-5.2977	-3.4873	-1.3908	.9697
.18	-6.8568	-5.4113	-3.6758	-1.6623	.6103
.17	-6.9085	-5.5232	-3.8686	-1.9440	.2396
.16	-6.9612	-5.6442	-4.0660	-2.2271	-.1427
.15	-7.0151	-5.7533	-4.2681	-2.5207	-.5365
.14	-7.0701	-5.8632	-4.4750	-2.8220	-.9422
.13	-7.1264	-6.0227	-4.6869	-3.1312	-1.3597
.12	-7.1839	-6.1536	-4.9041	-3.4487	-1.7893
.11	-7.2427	-6.2844	-5.1268	-3.7746	-2.2314
.10	-7.3030	-6.4200	-5.3552	-4.1094	-2.6862
.09	-7.3647	-6.5535	-5.5835	-4.4533	-3.1542
.08	-7.4279	-6.7042	-5.8299	-4.8066	-3.6357
.07	-7.4928	-6.8513	-6.0768	-5.1697	-4.1312
.06	-7.5594	-7.0062	-6.3303	-5.5429	-4.6411
.05	-7.6278	-7.1573	-6.5907	-5.9264	-5.1654
.04	-7.6981	-7.3174	-6.8581	-6.3204	-5.7043
.03	-7.7703	-7.4812	-7.1327	-6.7248	-6.2577
.02	-7.8447	-7.6435	-7.4145	-7.1397	-6.8251
.01	-7.9212	-7.8224	-7.7036	-7.5649	-7.4061
.00	-8.0000	-8.0000	-8.0000	-8.0000	-8.0000

Table 6f. Eigenvalues of the separation constant  $\Lambda_2(n, n-4, p) + p$

$p \setminus n$	4	5	6	7	8
0.00	6.00000	12.00000	20.00000	30.00000	42.00000
0.20	6.00488	12.00359	20.00376	30.00400	42.00250
0.40	6.01357	12.00469	20.00734	30.00844	42.00513
0.60	6.02649	12.01487	20.04039	30.05157	42.03790
0.80	6.04647	12.03143	20.09884	30.07669	42.07099
1.00	6.07173	12.05563	20.18944	30.12144	42.14557
1.20	6.10200	12.08722	20.32113	30.13333	42.18855
1.40	6.13653	12.12743	20.50144	30.22672	42.24066
1.60	6.17414	12.17411	20.73599	30.37682	42.30447
1.80	6.21489	12.22641	21.02886	30.52216	42.38339
2.00	6.25933	12.28314	21.38066	30.72344	42.48188
2.20	6.30749	12.34307	21.78339	30.92254	42.60200
2.40	6.35971	12.40512	22.25166	31.19953	42.74885
2.60	6.41631	12.46837	22.75589	31.51111	42.92552
2.80	6.47884	12.53205	23.30433	31.87663	43.13660
3.00	6.54743	12.59522	23.89797	32.28844	43.38411
3.20	6.62113	12.65825	24.53776	32.74422	43.60200
3.40	6.69999	12.72197	25.22316	33.23933	43.80111
3.60	6.78359	12.78793	25.95339	33.76685	44.07177
3.80	6.87183	12.85619	26.72844	34.32261	44.37826
4.00	6.96473	12.92673	27.54866	34.90644	44.70118
4.20	7.06226	12.99951	28.41466	35.51844	45.04118
4.40	7.16449	13.07451	29.32683	36.15944	45.40118
4.60	7.27149	13.15163	30.28533	36.83044	45.77444
4.80	7.38326	13.23088	31.29133	37.53233	46.16118
5.00	7.50000	13.31226	32.34466	38.26533	46.56118

$$\{\Lambda_2(n, n-2, p) + p\}/p$$

$(1/p) \setminus n$	4	5	6	7	8
0.20	-1.39884	-0.32210	0.99004	2.59445	4.58447
0.19	-1.50255	-0.45044	0.82776	2.36837	4.28553
0.18	-1.61066	-0.58732	0.65774	2.17399	3.99291
0.17	-1.72288	-0.73233	0.47811	1.99822	3.68045
0.16	-1.83888	-0.88555	0.28880	1.66448	3.27990
0.15	-1.95884	-1.04669	0.08566	1.41227	2.94995
0.14	-2.08114	-1.21622	-0.13655	1.14644	2.61118
0.13	-2.20766	-1.39331	-0.36666	0.86623	2.26066
0.12	-2.33866	-1.57667	-0.63444	0.56578	1.88994
0.11	-2.46833	-1.76663	-0.96110	0.23316	1.49221
0.10	-2.60222	-1.96110	-1.12877	-0.11544	1.06444
0.09	-2.73811	-2.15999	-1.20594	-0.48055	0.60660
0.08	-2.87566	-2.36110	-1.28883	-0.85988	0.12110
0.07	-3.01444	-2.56661	-1.37773	-1.24422	-0.38337
0.06	-3.15444	-2.77119	-1.46885	-1.64445	-0.96007
0.05	-3.29500	-2.97884	-1.56669	-2.04266	-1.42337
0.04	-3.43651	-3.18843	-1.65331	-2.44077	-1.94777
0.03	-3.57755	-3.39939	-1.74444	-2.83667	-2.46692
0.02	-3.71897	-3.60957	-1.83225	-3.22933	-2.98559
0.01	-3.85996	-3.79889	-1.91861	-3.61172	-3.49664
0.00	-4.00000	-4.00000	-4.00000	-4.00000	-4.00000

Table 6g. Eigenvalues of the separation constant  $\Lambda_4(n, n-4, p) + p$

$p \setminus n$	4	5	6	7	8
0.00	20.00000	30.00000	42.00000	56.00000	72.00000
0.20	19.09991	28.94477	40.09991	54.77654	70.72558
0.40	18.22250	27.91211	39.09991	53.56766	69.46336
0.60	17.37777	26.9024	38.5915	52.37738	68.2136
0.80	16.5574	25.9153	37.4929	51.1954	66.9762
1.00	15.7648	24.9523	36.4136	50.0329	65.7517
1.20	15.00000	24.0133	35.3539	48.8864	64.5405
1.40	14.26555	23.0979	34.3141	47.7564	63.3429
1.60	13.55611	22.2066	33.2946	46.6433	62.1593
1.80	12.86886	21.3404	32.2956	45.5472	60.9899
2.00	12.20955	20.4997	31.3175	44.4686	59.8351
2.20	11.57400	19.6853	30.3598	43.4068	58.6955
2.40	10.95952	18.8981	29.4256	42.3615	57.5703
2.60	10.36333	18.1393	28.5131	41.3340	56.4593
2.80	9.79133	17.4099	27.6232	40.3254	55.3679
3.00	9.24949	16.7094	26.7568	39.3349	54.2907
3.20	8.73222	16.0411	25.9146	38.3626	53.2300
3.40	8.23433	15.4052	25.0973	37.4081	52.1892
3.60	7.75999	14.8008	24.3059	36.4715	51.1690
3.80	7.30266	14.2263	23.5411	35.5525	50.1590
4.00	6.86403	13.6997	22.8040	34.6522	49.1587
4.20	6.44158	13.2000	22.0954	33.7711	48.1657
4.40	6.03047	12.7345	21.4163	32.9088	47.1831
4.60	5.63569	12.3025	20.7674	32.0653	46.2067
4.80	5.25463	11.9031	20.1496	31.2422	45.2416
5.00	4.89339	11.5340	19.5632	30.4393	44.2870

$$\{\Lambda_4(n, n-4, p) + p\}/p$$

$(1/p) \setminus n$	4	5	6	7	8
0.20	1.3548	2.3070	3.9126	6.1319	8.8974
0.19	1.2486	2.1081	3.5797	5.6421	8.2350
0.18	1.1474	1.9191	3.2583	5.1623	7.5805
0.17	1.0513	1.7405	2.9505	4.6948	6.9360
0.16	0.9600	1.5727	2.6580	4.2422	6.3037
0.15	0.8735	1.4157	2.3825	3.8100	5.6871
0.14	0.7915	1.2695	2.1255	3.3956	5.0903
0.13	0.7145	1.1335	1.8875	3.0089	4.5191
0.12	0.6405	1.0073	1.6686	2.6509	3.9799
0.11	0.5710	0.8901	1.4678	2.3230	3.4793
0.10	0.5052	0.7815	1.2839	2.0248	3.0218
0.09	0.4427	0.6804	1.1148	1.7538	2.6082
0.08	0.3835	0.5825	0.9589	1.5064	2.2347
0.07	0.3273	0.4915	0.8141	1.2783	1.8949
0.06	0.2738	0.4146	0.6788	1.0675	1.5818
0.05	0.2228	0.3363	0.5516	0.8690	1.2891
0.04	0.1742	0.2623	0.4312	0.6831	1.0120
0.03	0.1273	0.1921	0.3167	0.5116	0.7469
0.02	0.0838	0.1252	0.2070	0.3520	0.4910
0.01	0.0408	0.0612	0.1017	0.1621	0.2426
0.00	0.0000	0.0000	0.0000	0.0000	0.0000

Table 6h. Eigenvalues of the separation constant  $\Lambda_1(n, n-5, p) + p$

$p \setminus n$	5	6	7	8	9
0.00	2.00006	6.00033	12.00090	20.00233	31.00433
.20	.80115	4.80577	11.00476	19.00713	29.00717
.40	-.86933	3.71733	10.00359	18.00713	27.00717
.60	-2.40447	2.40416	9.00229	17.00636	27.00716
.80	-3.9964	1.21131	7.9471	16.04238	26.07212
1.00	-5.6365	-.1254	6.8275	15.4509	25.9800
1.20	-7.3179	-1.5126	5.6635	14.4437	24.9826
1.40	-9.0346	-2.9435	4.4549	13.4008	24.0578
1.60	-10.7811	-4.4235	3.2021	12.3214	23.1043
1.80	-12.5531	-5.9522	1.9056	11.2047	22.1211
2.00	-14.3469	-7.5123	-.5677	10.0504	21.1071
2.20	-16.1596	-9.1081	-2.0109	8.8583	20.0616
2.40	-17.9885	-10.7345	-3.4281	7.6287	18.9839
2.60	-19.8317	-12.3891	-4.8316	6.3621	17.8733
2.80	-21.6872	-14.0691	-6.2197	5.0592	16.7297
3.00	-23.5536	-15.7713	-7.6036	3.7211	15.5529
3.20	-25.4306	-17.4955	-8.9734	2.3488	14.3431
3.40	-27.3149	-19.2376	-10.3168	-.9439	13.1075
3.60	-29.2075	-20.9967	-11.6416	-3.2222	11.8256
3.80	-31.1071	-22.7711	-13.0465	-6.4958	10.5199
4.00	-33.0129	-24.5594	-14.6351	-9.7519	9.1817
4.20	-34.9245	-26.3633	-16.3640	-13.0724	7.8146
4.40	-36.8411	-28.1733	-18.0954	-16.4517	6.4186
4.60	-38.7625	-29.9951	-19.7561	-19.8367	4.9959
4.80	-40.6883	-31.8233	-21.4768	-23.2377	3.5449
5.00	-42.6179	-33.6737	-23.2122	-26.6392	2.0694

$\{\Lambda_1(n, n-5, p) + p\}/p$

$(1/p) \setminus n$	5	6	7	8	9
.20	-8.5236	-6.7341	-4.6424	-2.2578	.4139
.19	-8.5809	-6.8613	-4.8481	-2.5534	.3174
.18	-8.6393	-6.9891	-5.0582	-2.8554	-.3873
.17	-8.6991	-7.1203	-5.2732	-3.1643	-.8310
.16	-8.7601	-7.2554	-5.4931	-3.4806	-1.2243
.15	-8.8226	-7.3933	-5.7184	-3.8046	-1.6580
.14	-8.8865	-7.5344	-5.9494	-4.1370	-2.1031
.13	-8.9519	-7.6773	-6.1863	-4.4783	-2.5602
.12	-9.0190	-7.8225	-6.4295	-4.8290	-3.0303
.11	-9.0878	-7.9733	-6.6794	-5.1896	-3.5142
.10	-9.1585	-8.1365	-6.9364	-5.5608	-4.0128
.09	-9.2312	-8.2975	-7.2039	-5.9433	-4.5271
.08	-9.3059	-8.4633	-7.4733	-6.3377	-5.0580
.07	-9.3829	-8.6342	-7.7543	-6.7447	-5.6064
.06	-9.4623	-8.8112	-8.0342	-7.1649	-6.1732
.05	-9.5443	-8.9923	-8.3435	-7.5992	-6.7594
.04	-9.6290	-9.1793	-8.6529	-8.0470	-7.3658
.03	-9.7167	-9.3743	-8.9728	-8.5082	-7.9929
.02	-9.8076	-9.5755	-9.3137	-8.9822	-8.6410
.01	-9.9020	-9.7833	-9.6660	-9.4800	-9.3131
.00	-10.0000	-10.0000	-10.0000	-10.0000	-10.0000



Table 61. Eigenvalues of the separation constant  $\Lambda_3(n, n-5, p) + p$

$p \backslash n$	5	6	7	8	9
0.00	12.00000	20.00000	30.00000	42.00000	56.00000
0.20	10.89715	18.77443	28.47274	40.73866	55.70199
0.40	9.84155	17.53323	27.27449	39.48291	55.41111
0.60	8.82554	16.42323	26.24422	38.16330	52.12855
0.80	7.84008	15.38373	25.30365	36.94117	50.85552
1.00	6.87977	14.20677	23.85228	35.67664	49.59221
1.20	5.93511	13.14119	22.09335	34.45822	48.34055
1.40	5.00111	12.10223	21.05585	33.25581	47.10111
1.60	4.07252	11.08663	20.04473	32.07668	45.87511
1.80	3.14552	10.08873	19.35590	30.94488	44.66632
2.00	2.21559	9.10447	18.29221	29.77223	43.46663
2.20	1.28220	8.13330	17.24448	28.64442	42.28449
2.40	0.34144	7.16977	16.21551	27.54551	41.11195
2.60	-0.60744	6.21116	15.20008	26.44494	39.97705
2.80	-1.56555	5.25664	14.19997	25.39410	38.85579
3.00	-2.53335	4.30115	13.20995	24.33889	37.72216
3.20	-3.51221	3.33451	12.22880	23.33116	36.62214
3.40	-4.50133	2.38555	11.25229	22.27777	35.53667
3.60	-5.50133	1.42113	10.28224	21.26557	34.46669
3.80	-6.51420	0.45113	9.31444	20.26338	33.41111
4.00	-7.53330	-0.52253	8.34775	19.27004	32.36684
4.20	-8.55644	-1.50092	7.37999	18.28339	31.33377
4.40	-9.60090	-2.50011	6.41055	17.30026	30.31178
4.60	-10.65551	-3.50113	5.43779	16.32252	29.30074
4.80	-11.71141	-4.50395	4.46113	15.35092	28.30052
5.00	-12.78114	-5.52664	3.47977	14.37661	27.31011

$$\{\Lambda_3(n, n-5, p) + p\}/p$$

$(1/p) \backslash n$	5	6	7	8	9
0.20	2.55563	-1.10573	0.69599	2.87522	5.46622
0.19	2.69766	-1.30677	0.44411	2.48799	4.92417
0.18	2.84116	-1.51112	0.13000	2.09999	4.42229
0.17	2.98884	-1.71991	-0.15722	1.71007	3.90511
0.16	3.13833	-1.93311	-0.44800	1.31933	3.38776
0.15	3.29133	-2.14772	-0.74333	0.92477	2.86693
0.14	3.44788	-2.36322	-1.04441	0.52566	2.34889
0.13	3.60788	-2.57945	-1.35111	0.12055	1.82247
0.12	3.77144	-2.79622	-1.66554	-0.29221	1.29944
0.11	3.93888	-3.01333	-1.98776	-0.71441	0.75553
0.10	4.10999	-3.23077	-2.31883	-1.14668	0.20477
0.09	4.28488	-3.45566	-2.65880	-1.59914	-0.36000
0.08	4.46334	-3.68131	-3.00665	-2.04486	-0.94100
0.07	4.64555	-3.90777	-3.35334	-2.50122	-1.53889
0.06	4.83111	-4.13333	-3.72281	-2.99991	-2.15330
0.05	5.01999	-4.36000	-4.09922	-3.48896	-2.78110
0.04	5.21116	-4.58833	-4.47554	-3.98873	-3.41194
0.03	5.40558	-4.81666	-4.85552	-4.48897	-4.06411
0.02	5.60223	-5.04333	-5.23669	-4.99941	-4.71113
0.01	5.80000	-5.27133	-5.61990	-5.49882	-5.35775
0.00	-6.00000	-6.00000	-6.00000	-6.00000	-6.00000

Table 6j. Eigenvalues of the separation constant  $A_5(n, n-5, p) + p$

$p \setminus n$	5	6	7	8	9
0.00	30.60000	42.60000	56.00000	72.00000	91.10100
0.20	29.90114	41.73333	55.62222	71.50000	89.47774
0.40	27.82799	39.49999	53.26666	69.33333	86.36886
0.60	26.77333	38.28333	51.93333	67.67333	85.47339
0.80	25.75556	37.08333	50.61666	66.26444	83.49366
1.00	24.75668	35.91333	49.31000	64.37222	82.52778
1.20	23.78288	34.77777	48.04333	63.43811	81.37669
1.40	22.83334	33.66666	46.79666	62.44111	79.26411
1.60	21.90885	32.56666	45.55333	60.83111	78.22255
1.80	21.00000	31.46666	44.33333	59.43000	76.81557
2.00	20.13110	30.40000	43.13333	58.17773	75.42666
2.20	19.27776	29.37500	41.96666	56.93222	74.35333
2.40	18.44771	28.36666	40.83333	55.69666	72.69966
2.60	17.63991	27.37500	39.73333	54.47885	71.39566
2.80	16.85227	26.41222	38.66666	53.27498	70.33224
3.00	16.08773	25.47000	37.64000	51.94411	69.72554
3.20	15.34221	24.55555	36.64111	50.74966	68.45555
3.40	14.61622	23.66666	35.66333	49.57933	66.66666
3.60	13.90889	22.77777	34.70000	48.42966	64.30778
3.80	13.21991	21.91111	33.73333	47.29343	62.36668
4.00	12.54559	21.08888	32.77777	46.17166	60.24477
4.20	11.88886	20.26999	31.83333	45.06333	58.24778
4.40	11.24961	19.44777	30.90000	44.06166	56.90936
4.60	10.61776	18.62999	29.95111	42.95111	55.38676
4.80	10.00223	17.83333	28.61555	41.93275	53.74999
5.00	9.39994	17.19777	27.73224	40.91131	56.62005

$$\{A_5(n, n-5, p) + p\}/p$$

$(1/p) \setminus n$	5	6	7	8	9
0.20	1.87999	3.43394	5.54666	8.10266	11.32441
0.19	1.63885	3.08885	5.15444	7.52555	10.48009
0.18	1.44009	2.82222	4.86666	6.86777	9.64444
0.17	1.16775	2.39999	4.09333	6.23336	8.31558
0.16	0.93884	2.06664	3.62211	5.60313	7.99667
0.15	0.71339	1.74222	3.16118	4.37999	7.48887
0.14	0.49443	1.42222	2.74335	3.47114	6.39441
0.13	0.27997	1.11333	2.27744	2.77773	5.61955
0.12	0.07044	0.81333	1.85448	3.20111	4.85660
0.11	-0.13344	0.52333	1.44669	2.64437	4.11889
0.10	-0.33166	0.24333	1.05477	2.10766	3.40881
0.09	-0.52466	-0.24333	0.67888	1.59947	2.72777
0.08	-0.71007	-0.28444	0.31222	1.10063	2.07888
0.07	-0.89125	-0.33333	0.42222	0.62229	1.46883
0.06	-1.06666	-0.77000	-0.34778	0.29441	0.88662
0.05	-1.23558	-0.99333	-0.65773	-0.21122	0.34005
0.04	-1.53994	-1.21666	-0.95117	-0.63445	-0.17448
0.03	-1.55775	-1.42221	-1.23220	-0.97880	-0.66330
0.02	-1.71011	-1.62249	-1.49994	-1.33337	-1.42777
0.01	-1.85776	-1.81663	-1.75550	-1.67337	-1.57224
0.00	-2.00000	-2.00000	-2.00000	-2.00000	-2.00000

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Кульчицкий Ю.А. и др.  
Таблицы и графики сфероидальных  
функций осциллятора

E2-86-432

В работе подытожены - в виде таблиц и графиков - результаты вычислений на ЭВМ угловых и радиальных функций изотропного осциллятора в вытянутых и в сплюснутых сфероидальных координатах. Установлена зависимость сфероидальных констант разделения от дополнительного параметра входящего в определение сфероидальных координат.

Работа выполнена в Лаборатории теоретической физики ОИЯИ.

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Kulchitsky Yu.A. et al.  
Tables and Graphs of  
Oscillator Spheroidal Functions

E2-86-432

In the paper, we summarize, in the form of tables and graphs, the results of calculations at computer and radial functions of an oscillator in prolate and oblate spheroidal coordinates. The dependence is established for separation spheroidal constants on an extra parameter defining the spheroidal coordinates.

The investigation has been performed at the Laboratory of Theoretical Physics, JINR.

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