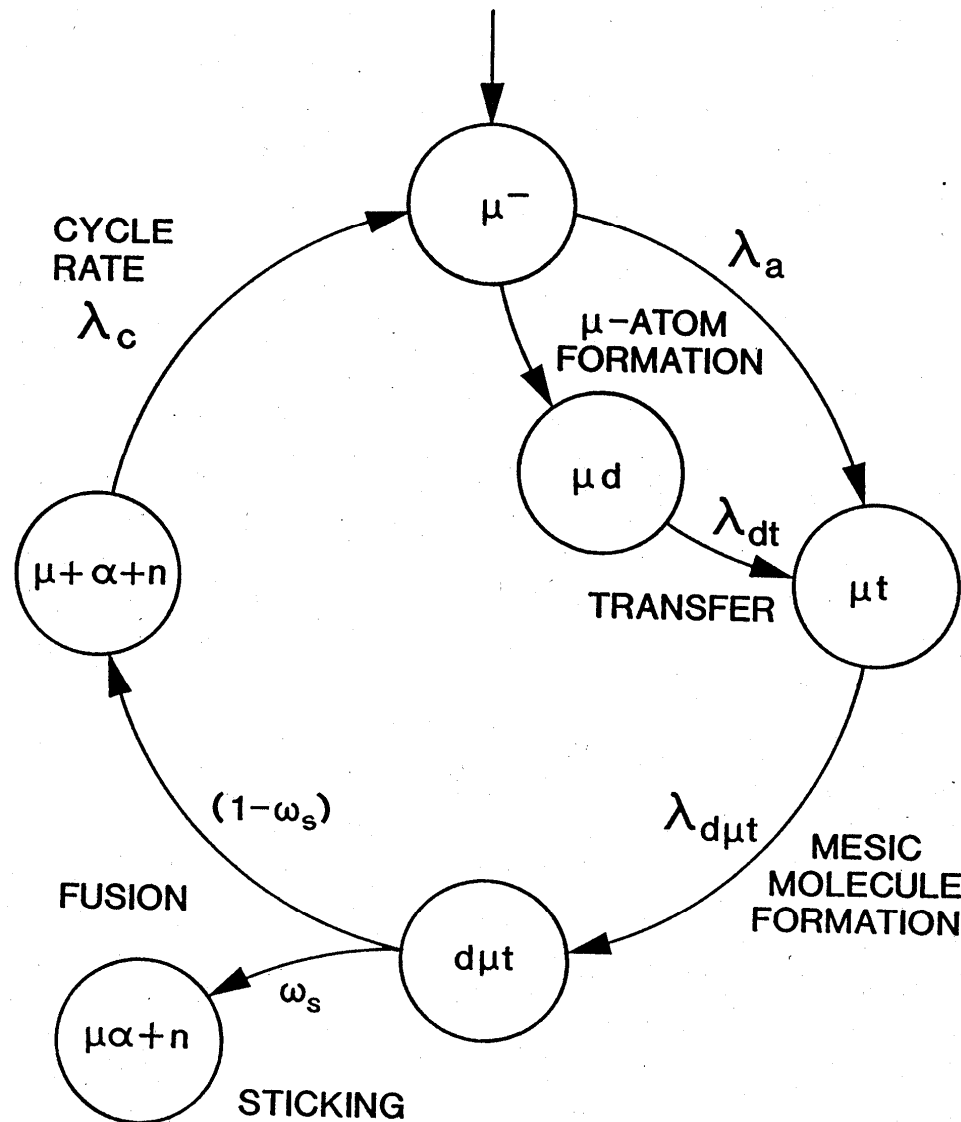


Review of Muon-Catalyzed Deuterium-Tritium Experiments



International Conference
on Muon Catalyzed Fusion
and Related Topics

MCF-07

Dubna, June 18-21 2007

presented by

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Paul Scherrer Institute

outline of talk

- review of important D-T μ CF experiments & results 1979 – 2005 from DUBNA, LAMPF, PSI, KEK/Tokyo, TRIUMF, RIKEN/RAL (presented in historical order)

(I) cycle & molecular formation rates

λ_c , $\lambda_{dt\mu}$, etc. are „reduced rates“ normalized to

liquid hydrogen density ($\varphi = 1 \rightarrow 4.25 \cdot 10^{22}$ atoms/cm³)

observed rates are defined as $\Lambda_c = \varphi \lambda_c$, $\Lambda_{dt\mu} = \varphi c_d \lambda_{dt\mu}$, etc.

(II) the $\mu\alpha$ sticking experiments & methods

w_s is the final sticking probability after dt μ fusion

w is the „effective sticking“ = observed muon loss per cycle

- comparison of results & open problems – discussion – conclusions

I. the fast dtμ fusion: discovery

- **1977 Dubna** theorists (S.S.Gerstein, L.I.Ponomarev, Phys Lett. 72B (1977) 80 Vinitiskii et al., JETP 47 (1978) 444.) predict existence of dtμ analogue process to resonant ddμ formation:

$[d\mu t_{(1,1)}dee]$ molecular state with ultra-fast kinetic rates

$$\lambda_{dt\mu} \sim 10^8 s^{-1}, \lambda_f \sim 10^{11} s^{-1}, \omega_s \sim 1\% \rightarrow Y_f \sim 100 \text{ fusions}/\mu$$

- **1979 Dubna** experimenters (V.P. Dzhelepov, V.M. Bystritsky et al., JETP Lett. 31 (1980) 228, Phys. Lett. 94B (1980) 476.) confirm prediction by first D-T experiment (c_+ , $\varphi < 0.1$ - T: 93K - 613K):

mesomolecule formation rate $\lambda_{dt\mu} > 10^8 s^{-1}$

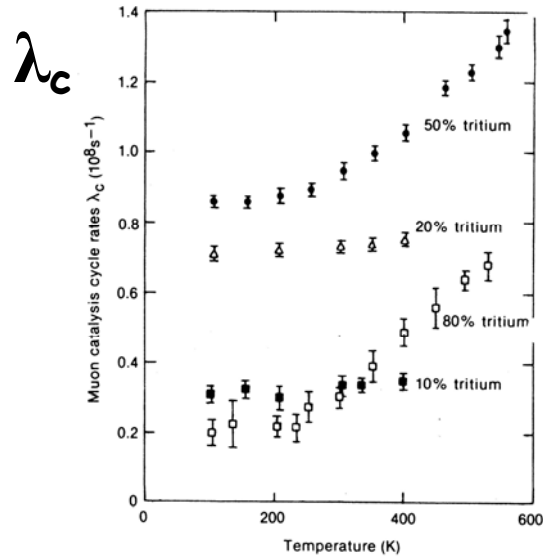
$\mu d \rightarrow \mu t$ transfer rate $\lambda_{dt} = 2.9 \pm 0.4 \cdot 10^8 s^{-1}$

- **1981 LAMPF** and **PSI** laboratories prepare large dtμ experiments

LAMPF 1983:

first dtμ fusion results

cycle rate



S.E. Jones et al., PRL 51 (1983) 1757, PRL 56 (1986) 58.

first high yield D-T experiments at
 $\phi = 0.45 - 0.60$, $T = 100-540 \text{ K}$

strong temperature effects observed!

cycle rates: $\lambda_c^{\text{max}} = 1.4 \cdot 10^8 \text{ s}^{-1}$

effective sticking: $w = 0.77 \pm .08 \%$

projected max. fusion yield ($\phi=1$, 540K) :

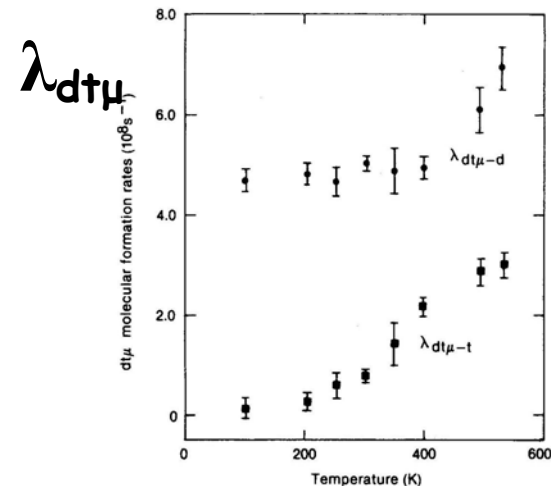
$Y_f \sim 90 \text{ fusions}/\mu$

meso-molecular formation rates on

D₂ molecule: $\lambda_{dt\mu-d}(T) \quad 4 \rightarrow 7 \cdot 10^8 \text{ s}^{-1}$

DT molecule: $\lambda_{dt\mu-t}(T) \quad 0 \rightarrow 3 \cdot 10^8 \text{ s}^{-1}$

molecular formation



temperature T (K)

PSI 1983: first dtμ fusion results

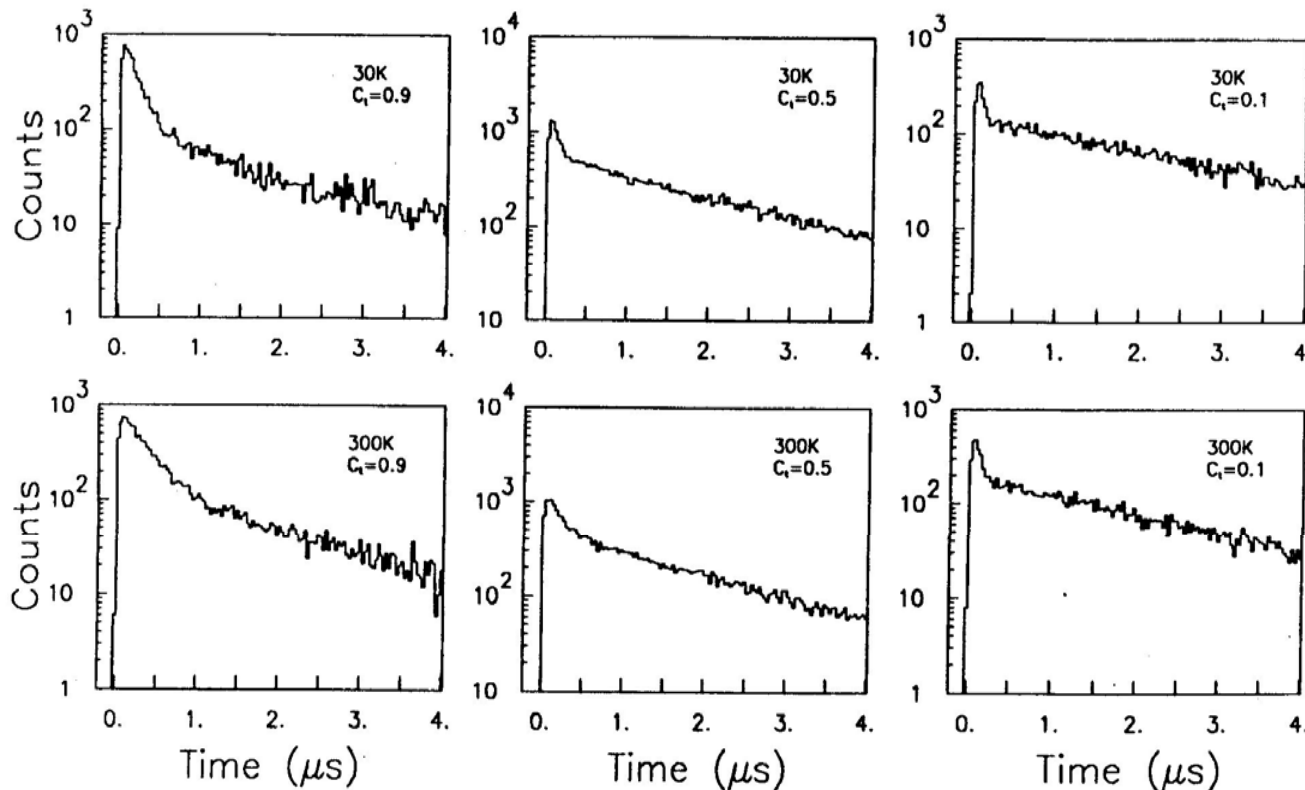
fusion rates at low density $\varphi = 0.01$, $T = 30\text{-}300\text{ K}$

W.H. Breunlich et al., PRL 53 (1984) 1137, MCF 1 (1987) 67.

M. Jeitler et al., Phys. Rev. A51 (1995) 2881.

steady state: $\lambda_c^{\max} = 0.55 \cdot 10^8 \text{ s}^{-1}$ $\lambda_{\text{dt}\mu\text{-d}} = 1.0\text{-}1.3 \cdot 10^8 \text{ s}^{-1}$

initial peaks: $\lambda_{\text{dt}\mu} \gg 10^8 \text{ s}^{-1}$ at epithermal μt energies ($\varepsilon_{\mu\text{t}} \sim \text{eV}$)



time spectra of
dt fusion neutrons
with
steady state slopes
and
initial peaks due to
thermalisation
during first μs !

PSI 1984: first high yield data in D-T liquid & gas

W.H. Breunlich et al., PRL 58 (1987) 329, MCF 1 (1987) 67

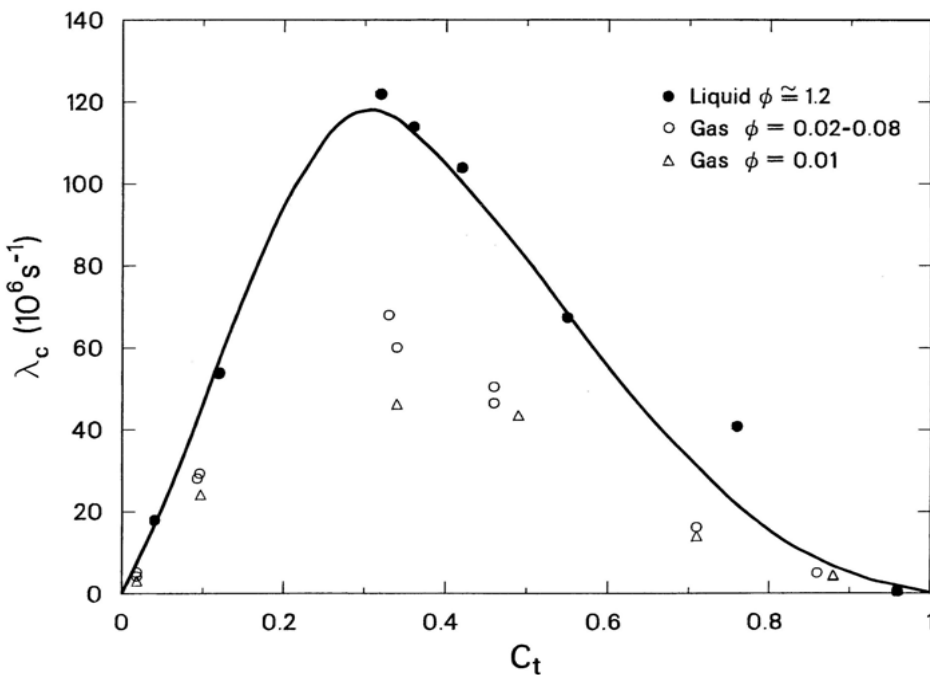
P. Ackerbauer et al., Nucl. Phys. A 652 (1999) 311

strong density effects at low temperature observed

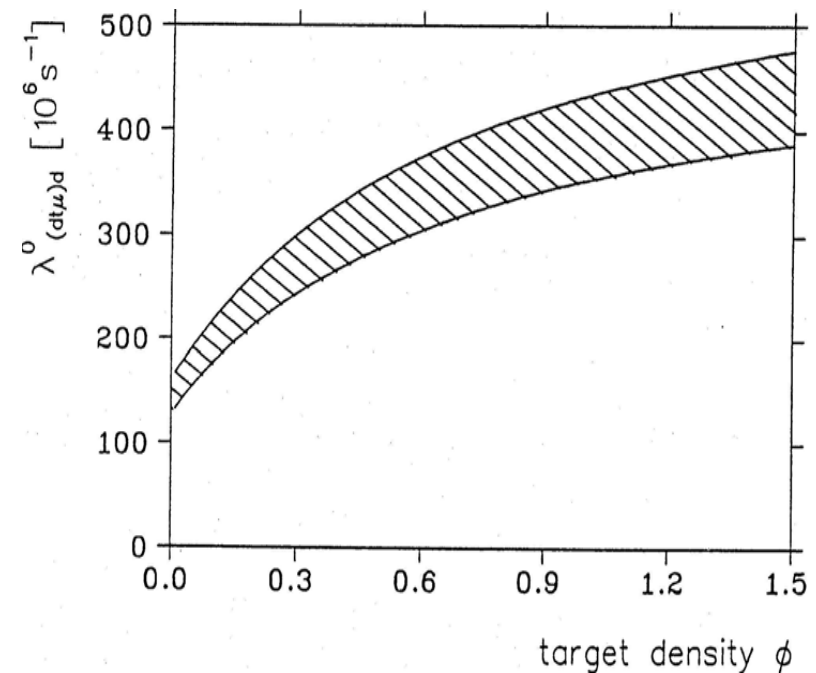
in liquid D-T at 20K, density $\phi = 1.2$: $\lambda_c^{\max} = 1.2 \cdot 10^8 \text{ s}^{-1}$

$$Y_f = 113 \text{ fusions}/\mu$$

$$\lambda_{dt\mu-d}(\phi) = 1.5 - 4 \cdot 10^8 \text{ s}^{-1}$$



λ_c vs. c_t at various ϕ



$\lambda_{dt\mu-d}$ vs. ϕ

LAMPF 1985/86: S.E. Jones reports new surprises

record cycle rates & yields S.E. Jones et al., PRL 56 (1986) 588.

ϕ : 0.1 $\rightarrow$ 1.2, T: 20 K $\rightarrow$ 600 K

strong temperature & density effects seen

$$\lambda_c^{\max} = 1.5 \cdot 10^8 \text{ s}^{-1} \quad (600\text{K})$$

$$\lambda_{dt\mu-d}(\phi) = 2 - 7 \cdot 10^8 \text{ s}^{-1}$$

highest observed
yield published:

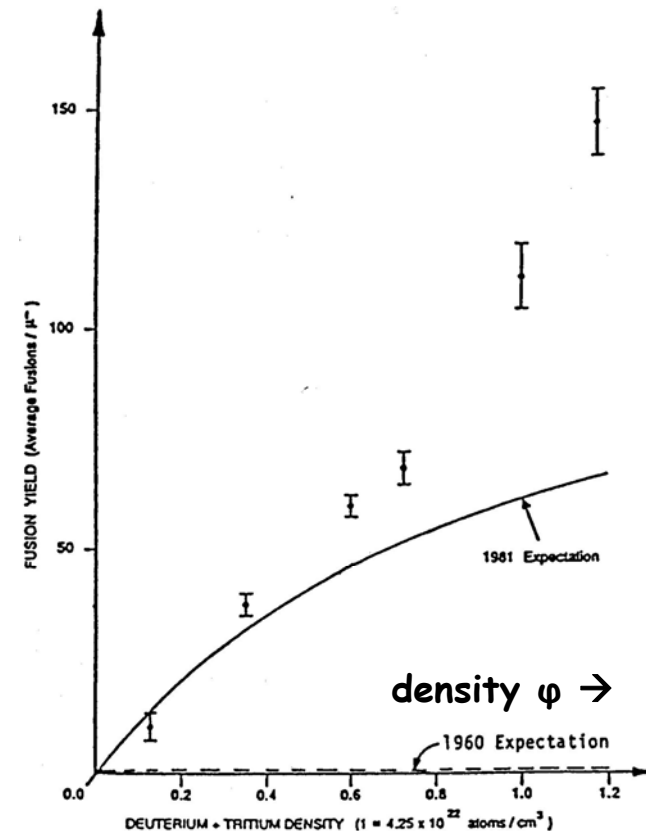
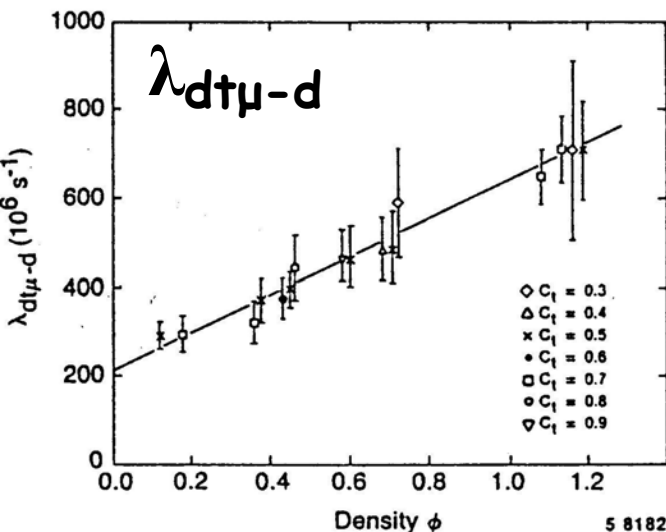
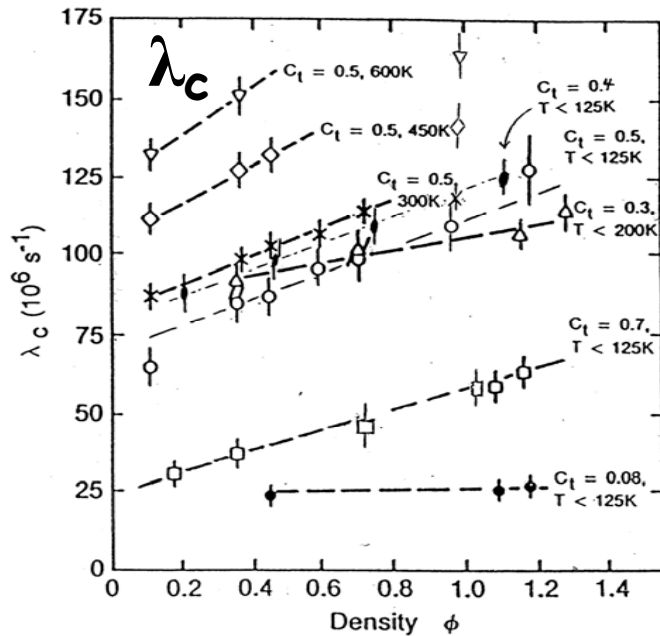
$$Y_f \sim 150 \pm 20 \text{ f}/\mu$$

in liquid D-T with
 $\phi = 1.2$, $c_t = 0.3$

$$\lambda_c = 1.1 \cdot 10^8 \text{ s}^{-1}$$

$$w = 0.35 \% (?)$$

start of sticking
controversy!



PSI 1987: new survey in solid, liquid & gaseous D-T

$\phi = 0.1-1.45$, $T = 12-30$ K, non-equilibrated D_2+T_2

C. Petitjean et al., MCF 2 (1988) 37, Hyp.Int.82 (1993) 273,

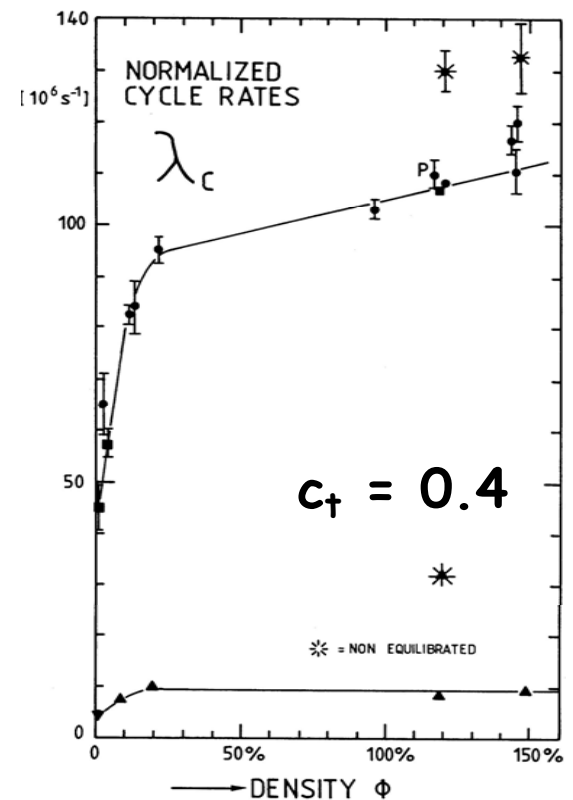
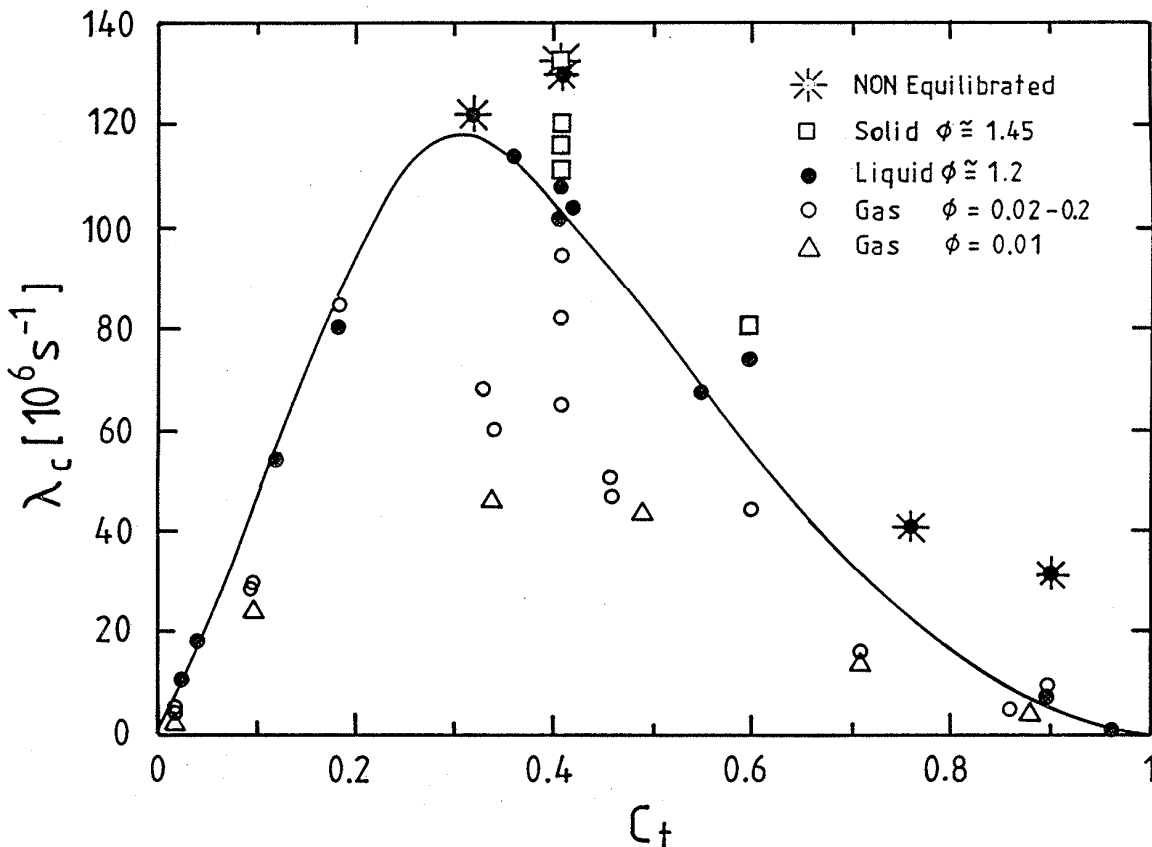
P. Ackerbauer et al., Nucl. Phys. A 652 (1999) 311.

$$\lambda_c^{\max} = 1.3 \cdot 10^8 \text{ s}^{-1}$$

strong density effects confirmed!

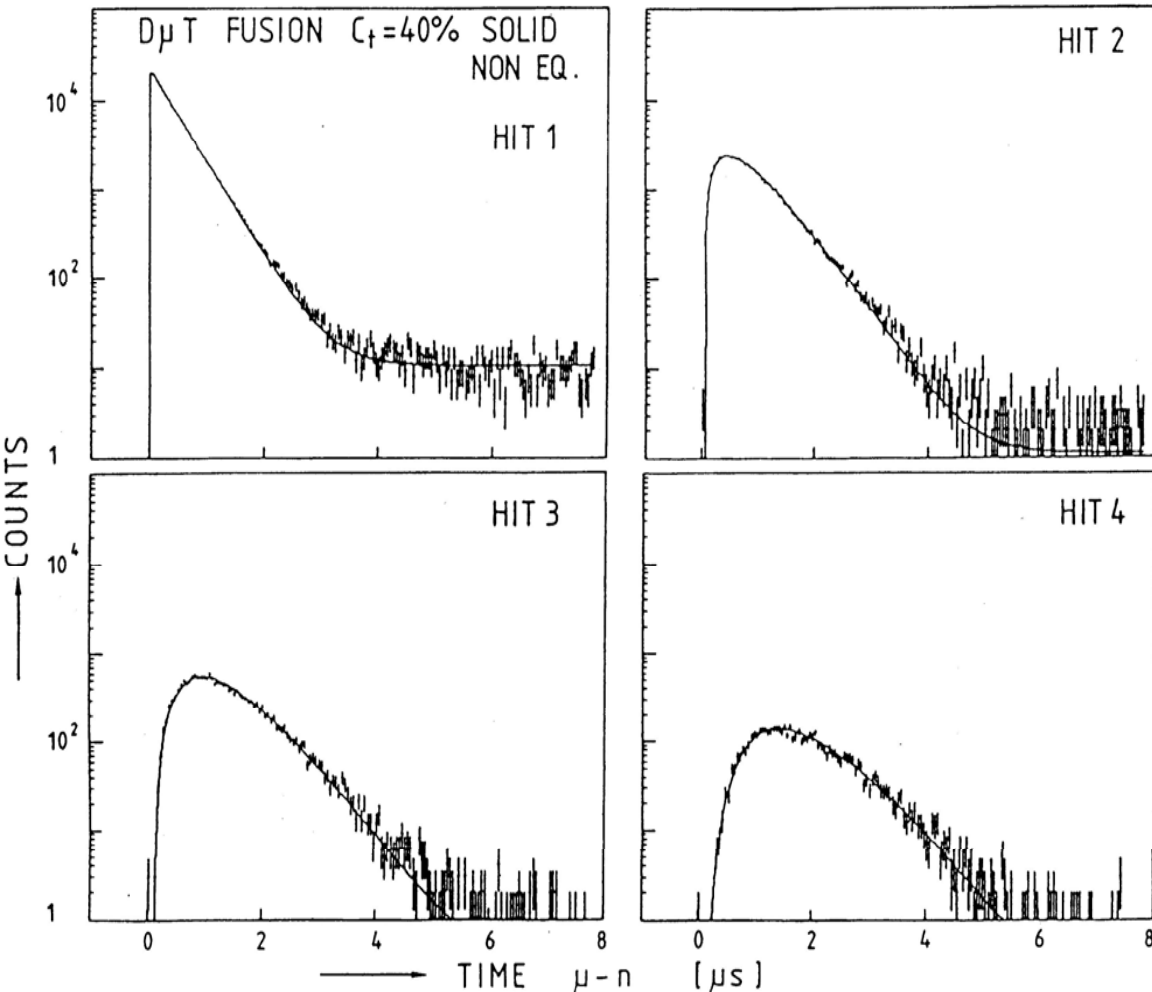
$$Y_f = 124 \text{ fusions}/\mu$$

in solid non-equilibrated mixture



PSI 1987: the highest observed fusion yield

14-MeV neutron spectra from ultra-fast dμt cycle



multi-hit time distributions after μ stop

solid $\text{D}_2\text{-T}_2$ at 12K
non-equilibrated
40%-60% mixture

$$\Lambda_c = 1.95 \cdot 10^8 \text{ s}^{-1}$$

$$\varphi = 1.45$$

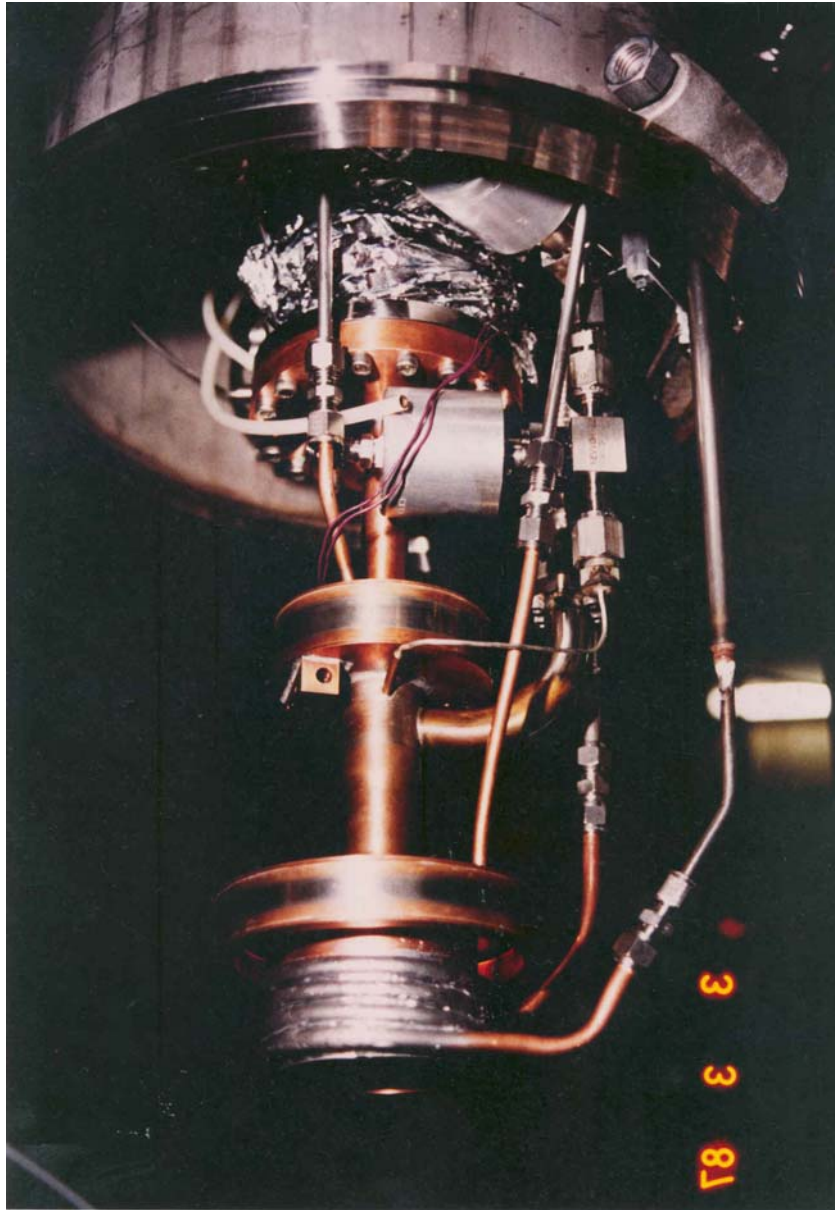
$$w = 0.568 \%$$

$$\omega_s = 0.48(4) \%$$

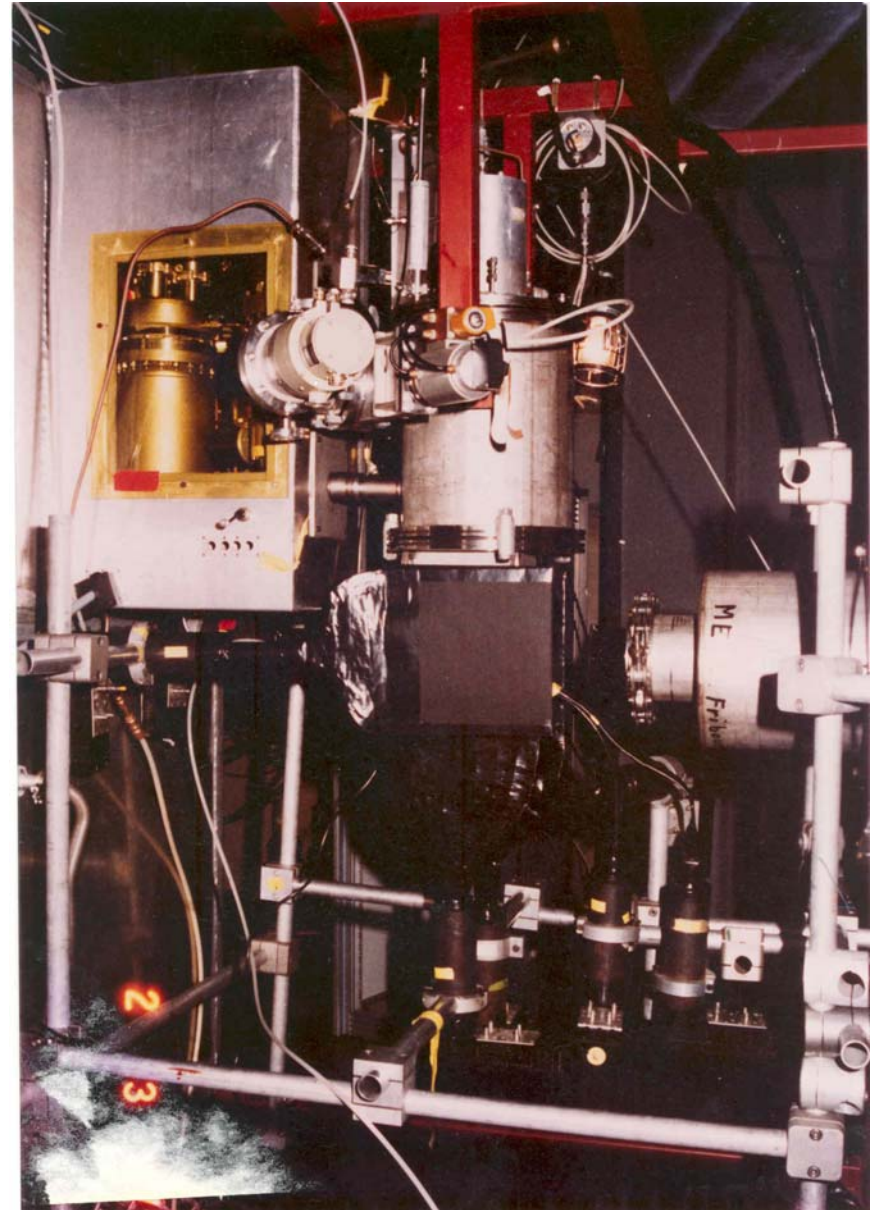
$$Y_f = 124 \pm 10$$

(presented 1987 at
Gatchina μCF conference)

PSI apparatus in 1987



tritium cryotarget (20 cm^3)



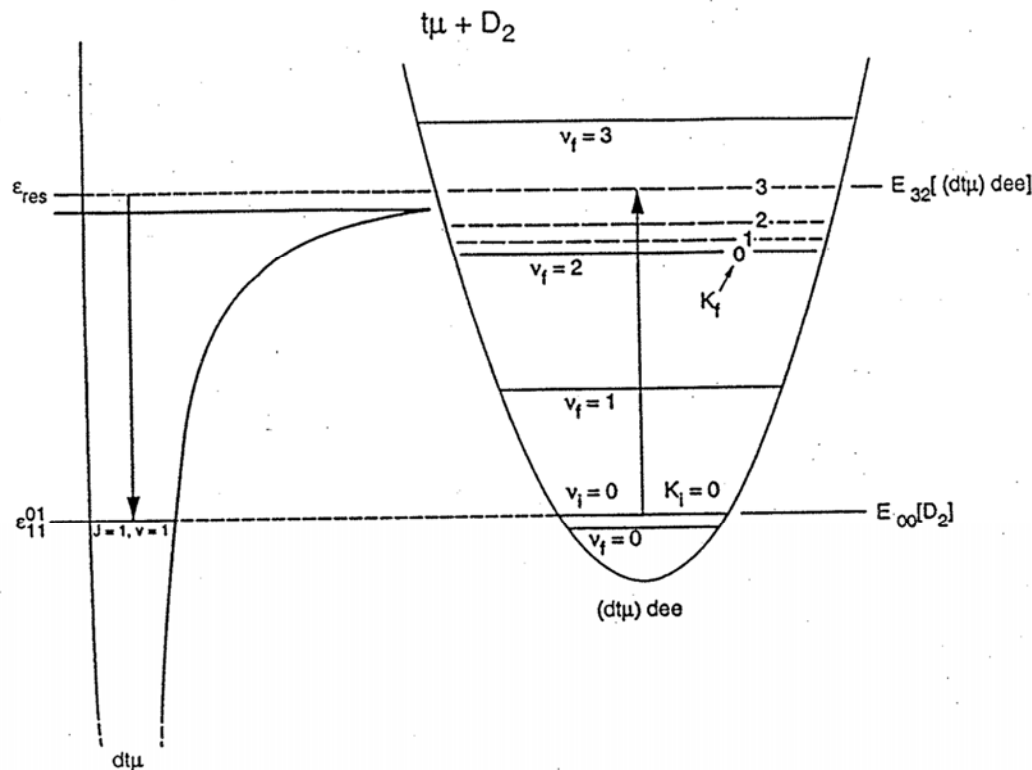
scint-counters & gas system (part)

interpretation of $\lambda_{dt\mu-d} - \lambda_{dt\mu-t}$ behaviour

main $v_f=2$ resonances $t\mu + D_2 \rightarrow [dt\mu_{(1,1)}dee]$ are just below threshold
 (-14 meV, -4.3 meV)

- increased in non-equilibrated D_2+T_2 mixtures
- density dependence due to triple collisions
- $\lambda_{dt\mu-d}$ large at low temperature

on the other hand: $t\mu + DT \rightarrow [dt\mu_{(1,1)}tee]$ $v_f=3$ resonant at +164 meV
 → $\lambda_{dt\mu-t}$ large at high temperatures (~ 1000 K)



level schemes showing
 Vesman mechanism
 in the $t\mu + D_2$ system

← $\epsilon_{11} = -596$ meV
 (Faifman)

(figure by Cohen, LEMS'93)

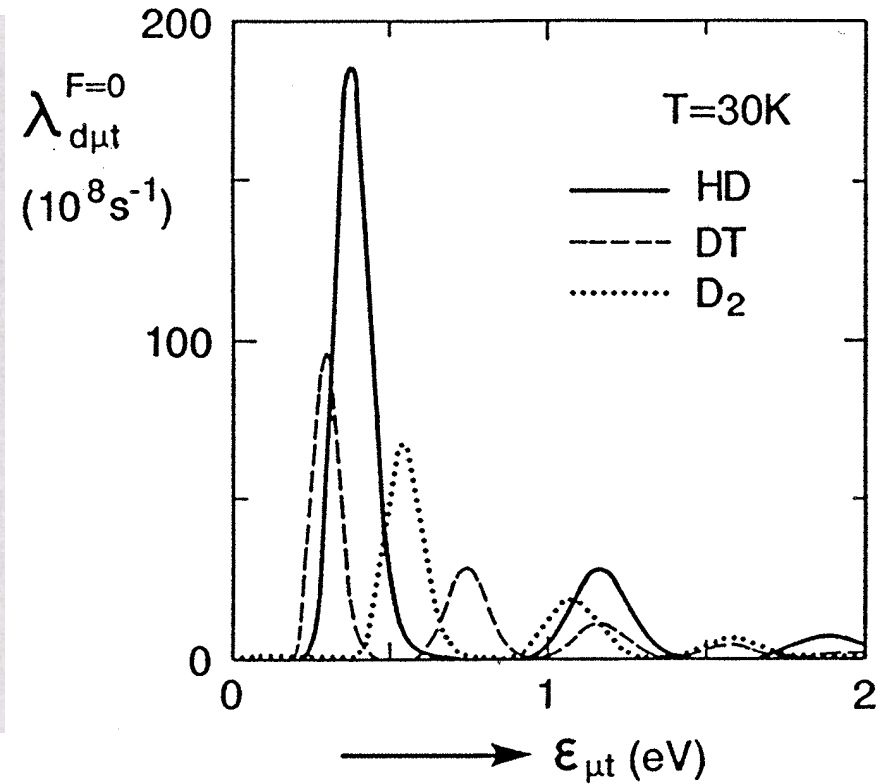
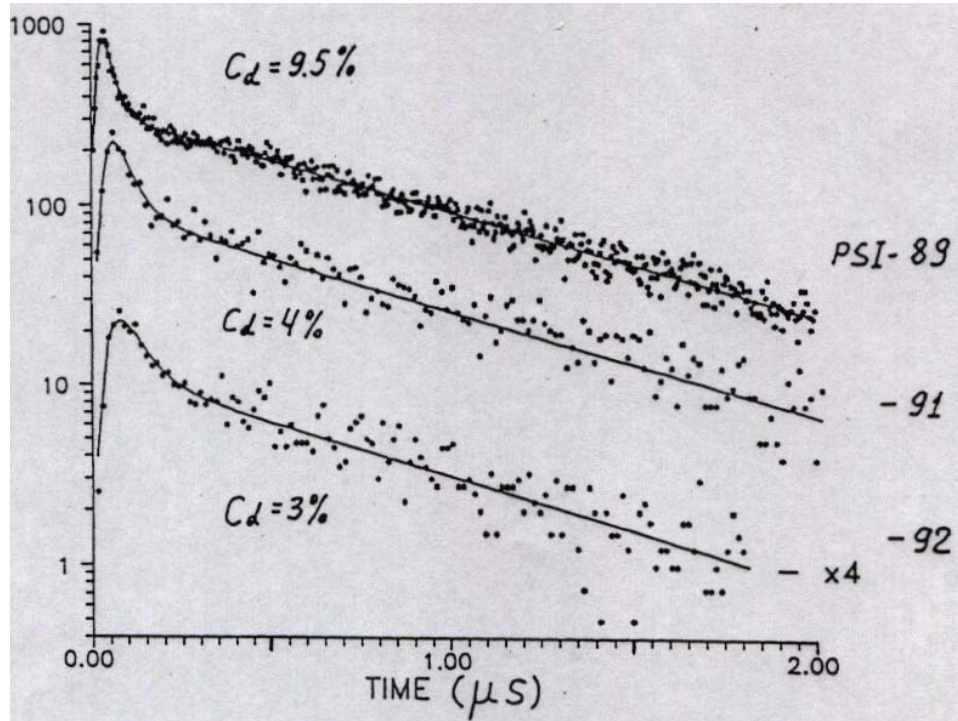
PSI 1989: epithermal resonances in HDT-mixtures

experiment:

theory:

T. Case et al., MCF 5/6 (1990/91) 327

M.P. Faifman and L.I. Ponomarev, Phys. Lett. B (1991) 201



PSI experiments 1989-92 using Gatchina ionisation chamber:

fusion time distribution in H-D-T gas with $\varphi=0.17$, $c_p=0.9-0.97$, $c_t=0.036\%$ shows **initial peak from epithermal μ t**

theory 1991:

plot of $\lambda_{d\mu t}$ vs. μ t energy

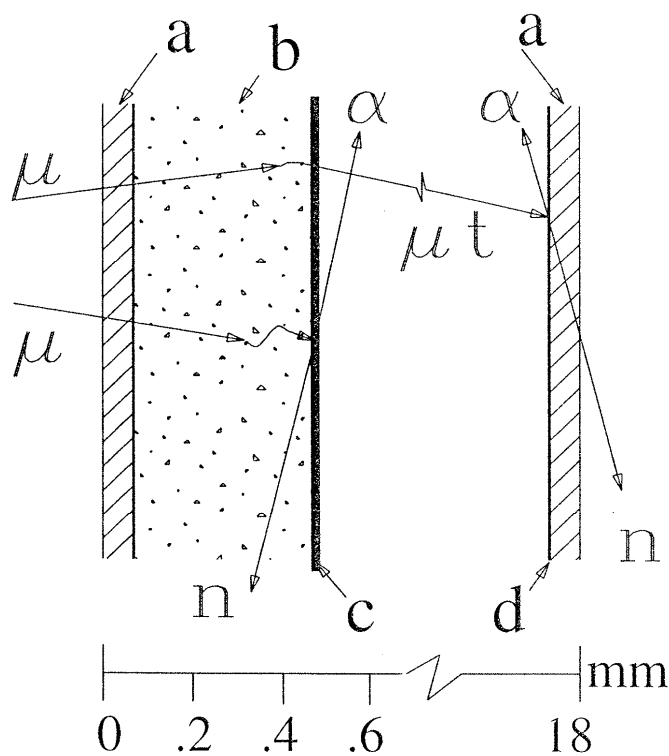
$$\lambda_{d\mu t}^{\text{max}} \sim 10^{10} \text{ s}^{-1} !$$

TRIUMF 1990th: experiments in T-doped solid H₂

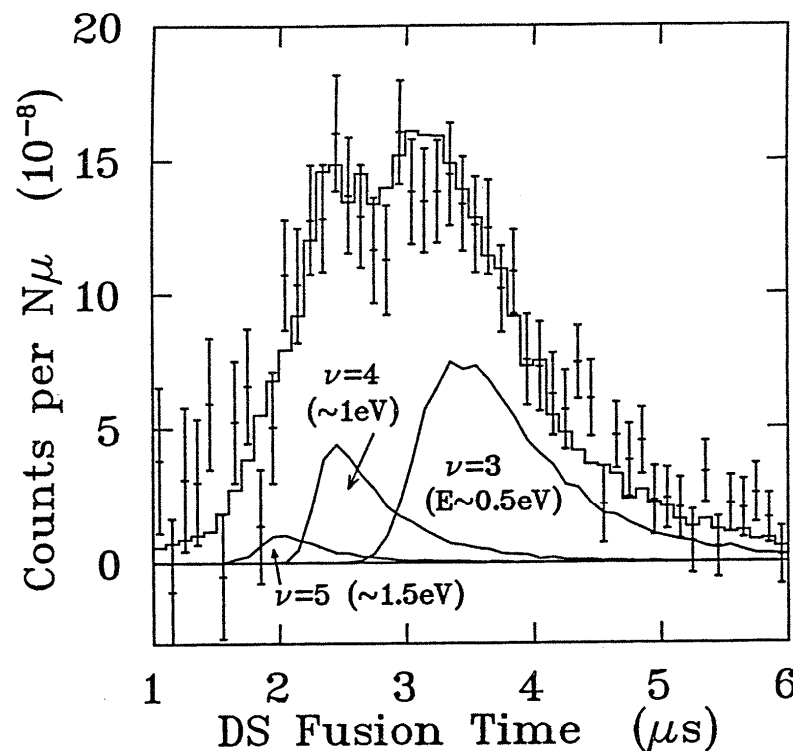
M.C. Fujiwara et al., PRL 85 (2000) 1642,
G.M. Marshall et al., Hyp.Int. 138 (2001) 203.

diffusion of epithermal μ t atoms due to Ramsauer-Townsend effect!

→ direct observation of reactions with epithermal μ t atoms on D₂ or HD



setup of solid H₂(T) target for
 μ t TOF measurement detecting
 α & n from $d\mu$ fusion in D₂, HD

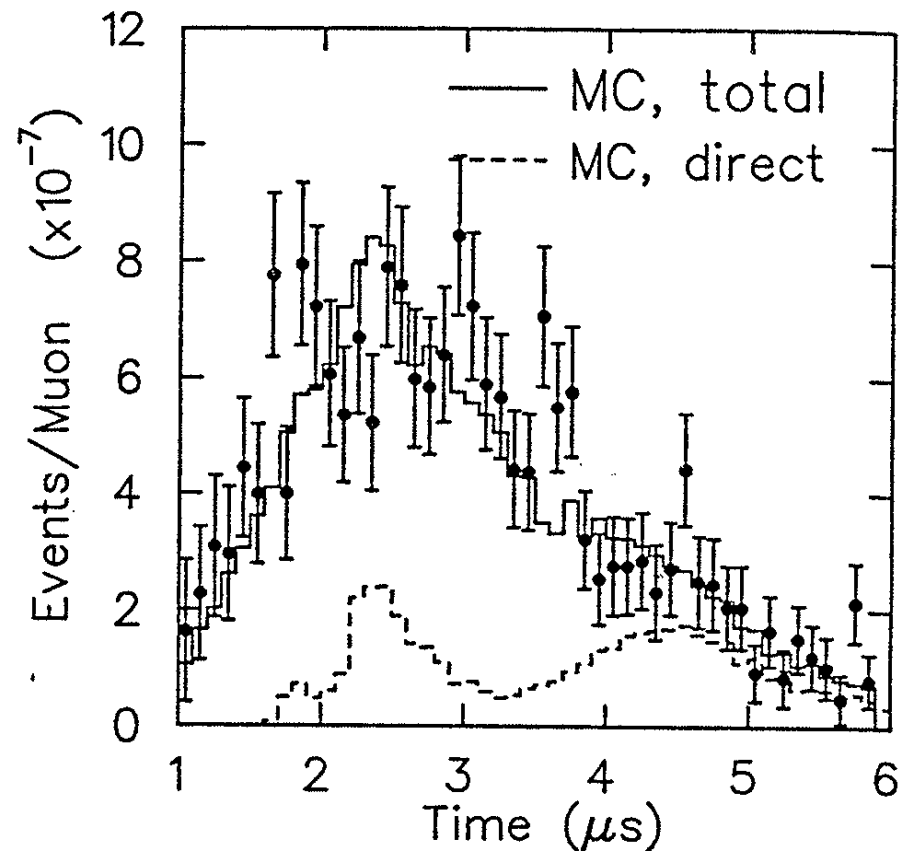
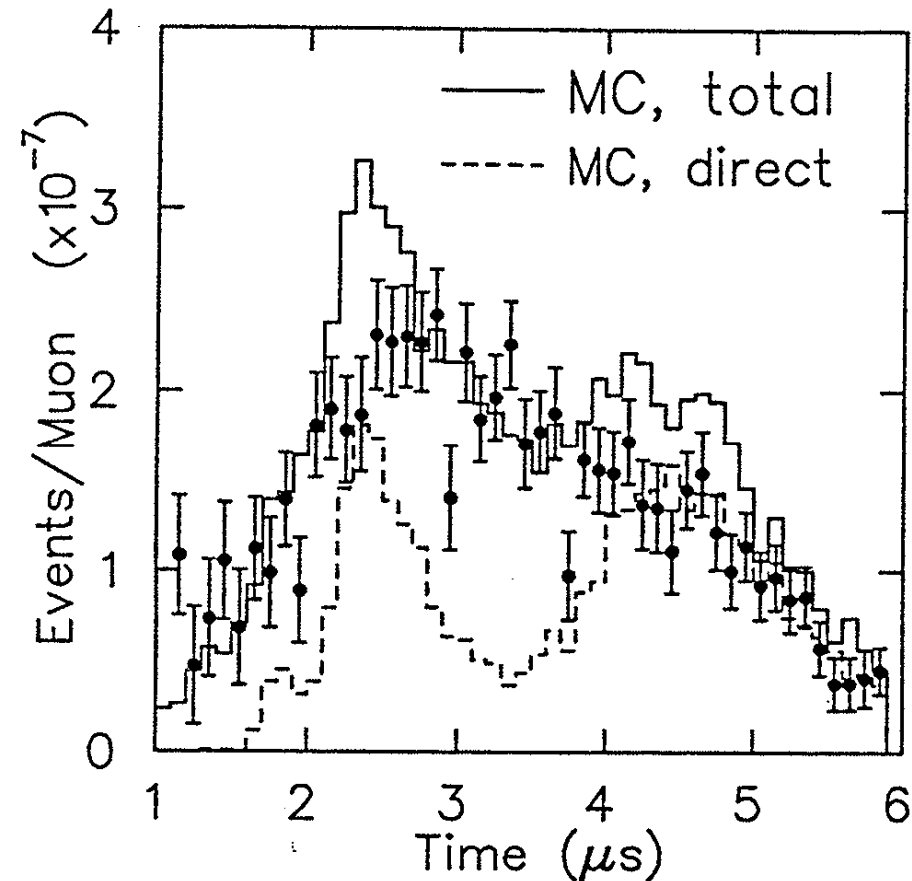


μ t + D₂ → [d μ -dee]
showing **epithermal resonances**

TRIUMF run on $\mu t + HD \rightarrow [dt\mu_{(1,1)}p2e]$

T.A.Porcelli et al., PRL 86 (2001) 3763.

qualitative agreement with Faifman-Ponomarev theory
of epithermal resonances

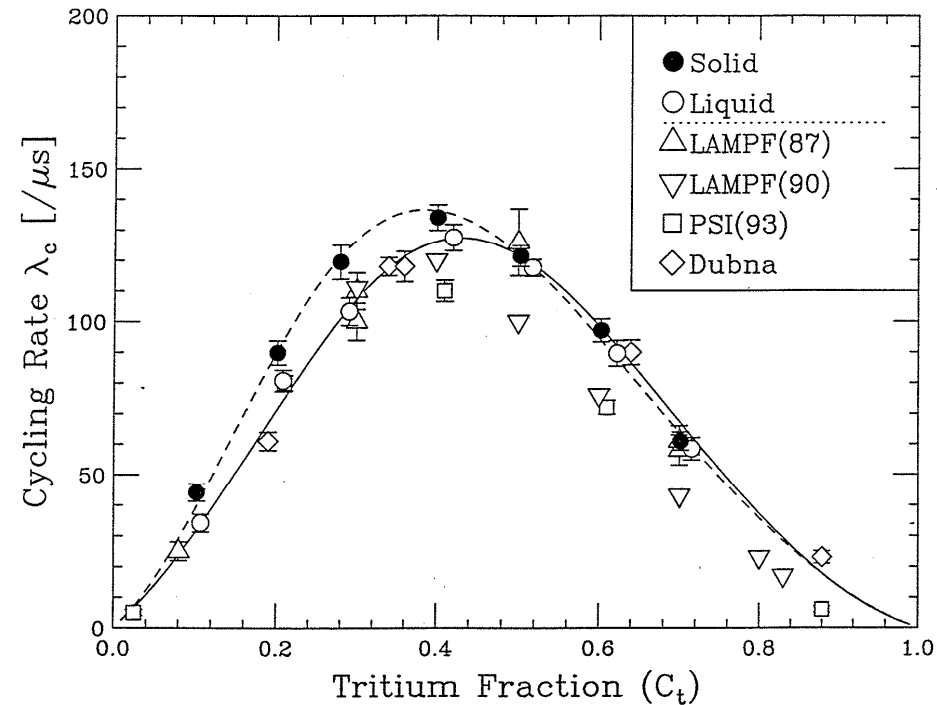
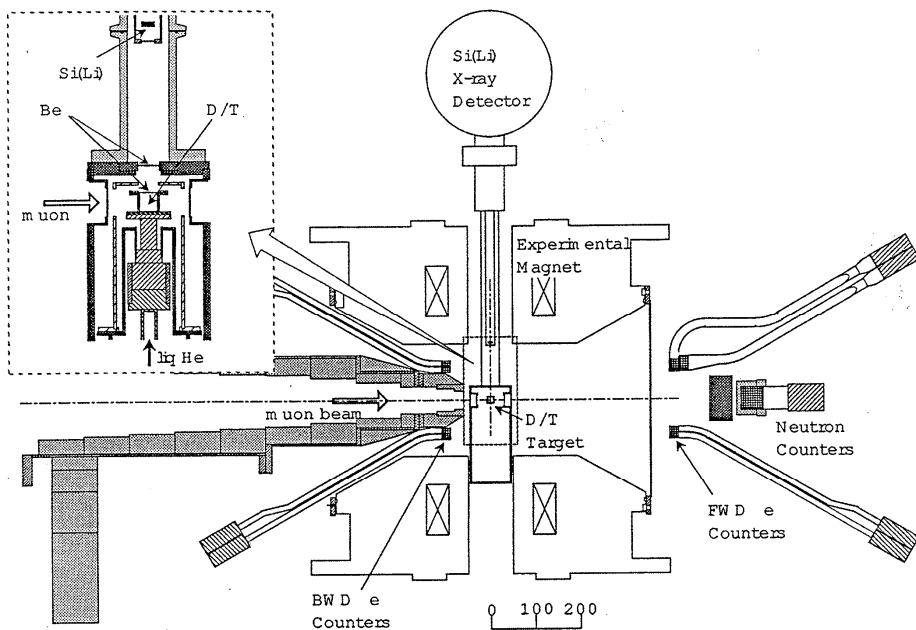


RIKEN-RAL 1990th dtμ fusion in solid & liquid D-T

K. Ishida et al., Hyp.Int.118 (1999) 203

ϕ : 1.2 - 1.45, T: 16K / 20 K

$$\lambda_c^{\max} = 1.3 \cdot 10^8$$



RIKEN-RAL apparatus for neutron
& X-ray measurements in D-T targets

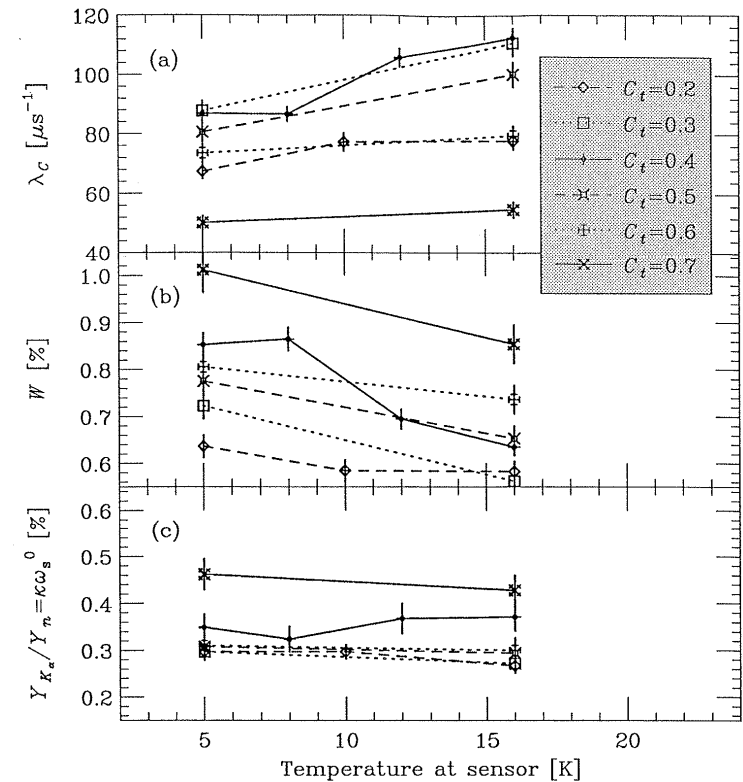
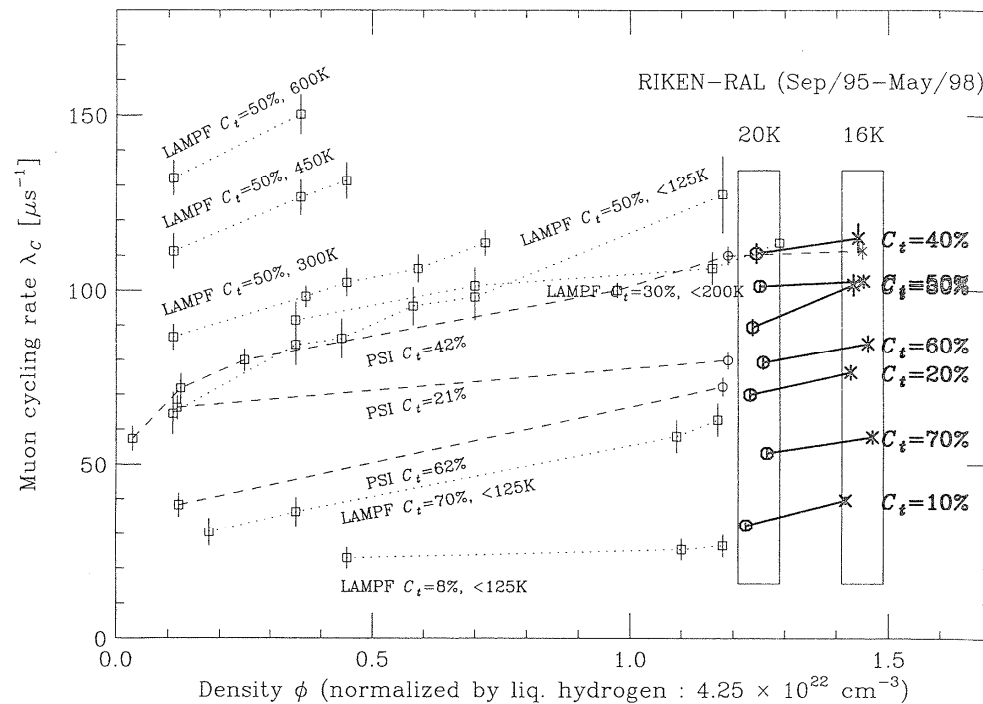
cycle rates λ_c
in solid & liquid D-T

RIKEN-RAL 1995/96: temperature and density effects in solid D-T mixtures

K. Nagamine, Hyp.Int. 138 (2001) 5, N. Kawamura et al., ibid. p. 235.

ϕ : 1.2 - 1.45,

T: 5K - 20 K



density effects at low temperature
comparison with LAMPF & PSI data

explained by $\epsilon_{\text{res}} < 0$

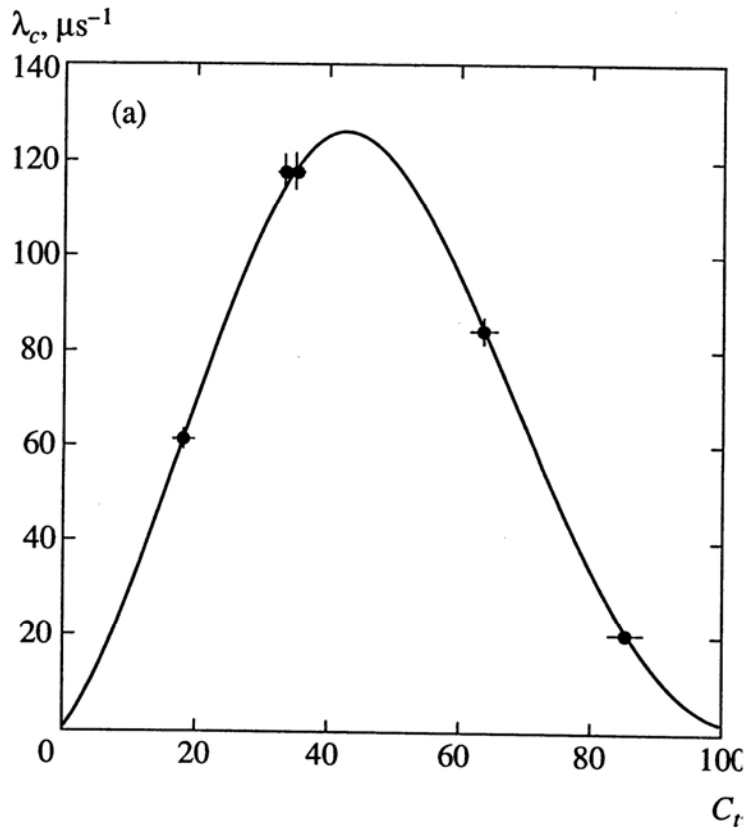
temperature effects in solid D-T
unexplained! - due to solid state?

Dubna 1997-2005: new $d\mu t$ experimental survey

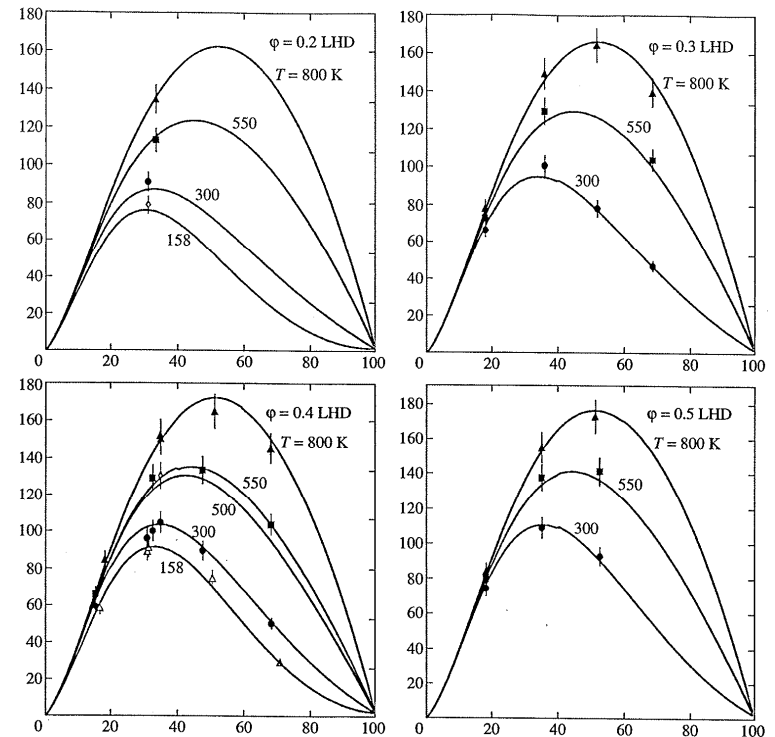
Yu.P. Averin et al., Hyp.Int.118 (1999) 101 V.R.Bom et al., Hyp.Int.118 (1999) 103,
Hyp.Int. 138 (2001) 213, JETP 127 (2005) 752

φ : 0.2-1.2 T : 22K - 800K 81 λ_c - data points

$\lambda_c^{\max} = 1.25 \cdot 10^8 s^{-1}$ (liquid DT) - $1.73 \cdot 10^8 s^{-1}$ ($T=800K$)



λ_c in liquid D-T

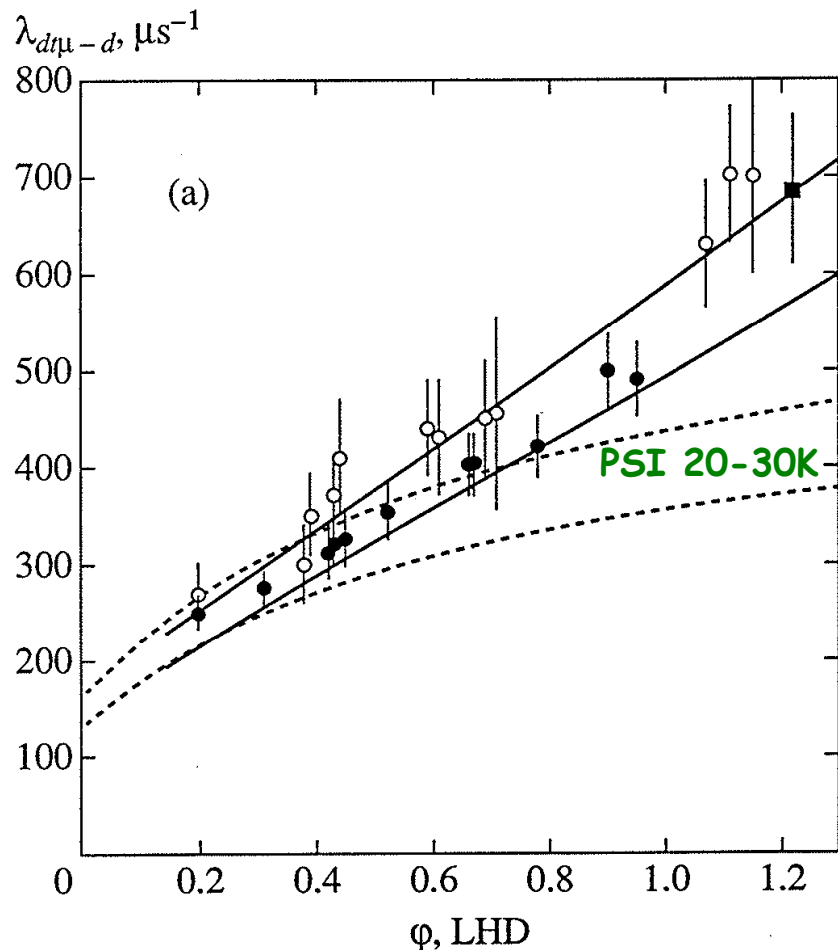


sample in D-T gas $T = 158K-800K$

Dubna 2005 vs. LAMPF 1986

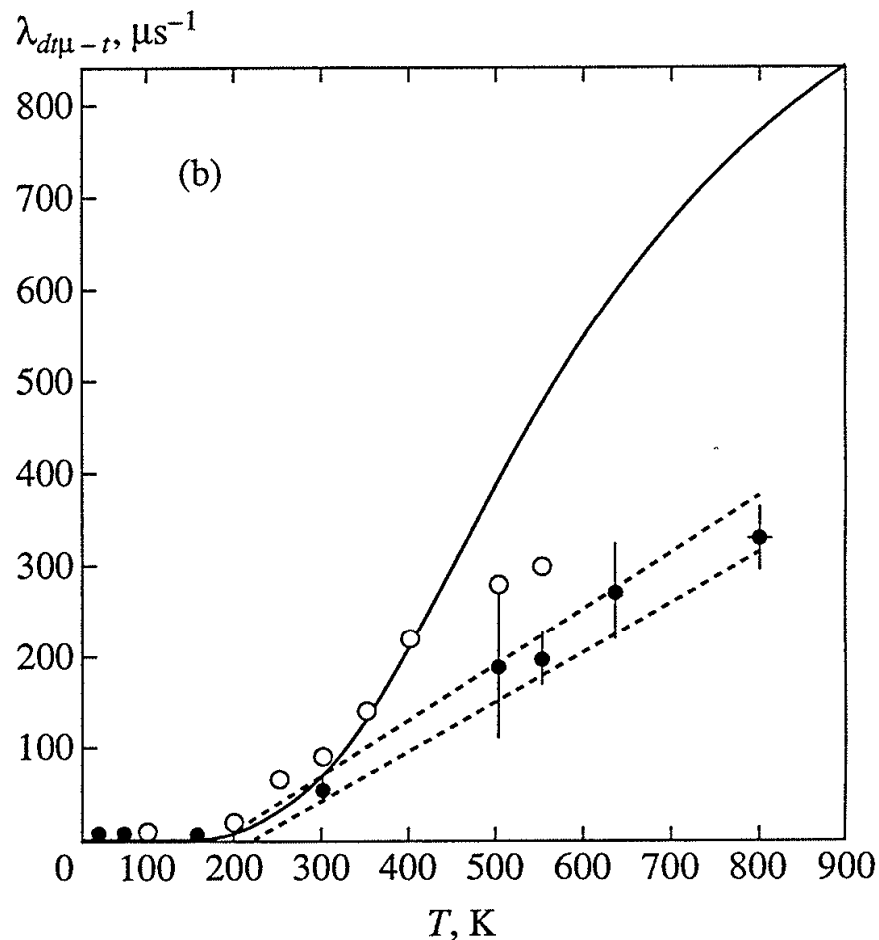
comparison of mesomolecule formation rates (open circles Dubna
full circles LAMPF)

$\lambda_{dt\mu-d}(\varphi)$ on D_2



density effect of $\lambda_{dt\mu-d}$ ($T < 300K$)

$\lambda_{dt\mu-t}(T)$ on DT



temperature effect of $\lambda_{dt\mu-t}$

Dubna 91:

can the D-T fusion yields get enhanced in triple mixture H-D-T?

Yu.P. Averin et al., Hyp. Int. 138 (2001) 249

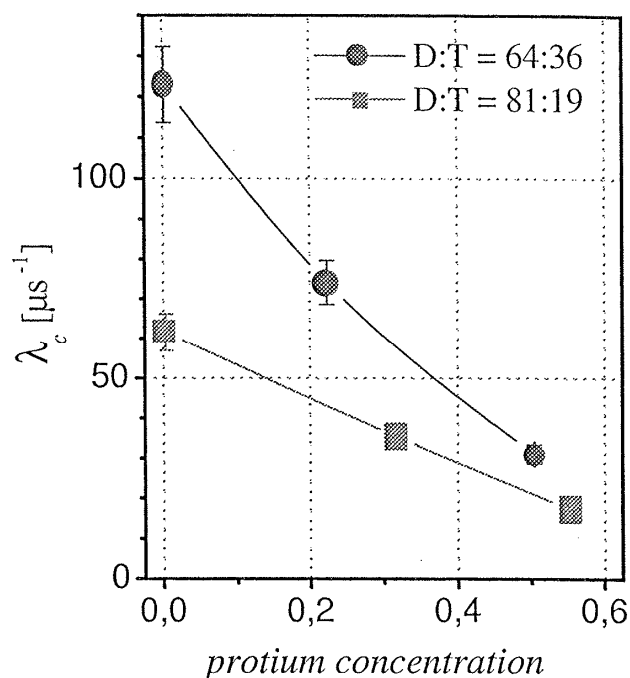
favorable:

more epithermal μ t near the big mmf resonances due to Ramsauer-Townsend effect

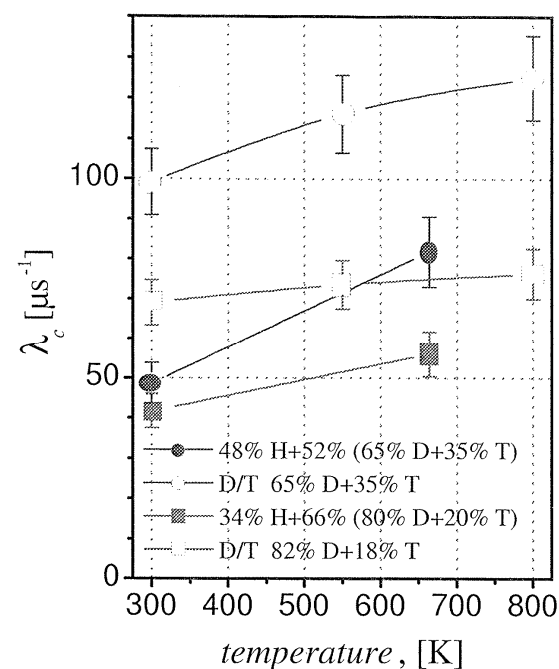
disfavorable:

reduced c_t & c_d concentrations and $pt\mu$ formation ($\lambda_{pt\mu} \sim 6 \cdot 10^6 s^{-1}$) cut the $dt\mu$ cycle

Dubna result:
 H^1 admixture
reduces λ_c
in liquid phase
and as well at
higher Temp.!



liquid phase 20K



gaseous phase 300-800K

conclusions I on μ CF rates

- exp. cycle & molecule formation rates agree $\pm 10\%$ among all labs (Dubna - LAMPF - PSI - RIKEN/RAL)

e.g. $\lambda_c^{\max}$ (liquid D-T) = $(1.2 \pm 0.1) 10^8 \text{ s}^{-1}$

- low temperature resonance is $\mu\text{t}+\text{D}_2$ ($\lambda_{\text{dt}\mu\text{-d}}$); density effects due to sub-threshold resonances are corroborated (LAMPF-PSI-Dubna)
- epithermal resonances (Faifman, Ponomarev) confirmed by all measurements sensitive to it (Dubna-PSI-TRIUMF-LAMPF)

$\mu\text{t}+\text{D}_2$ ($\lambda_{\text{dt}\mu\text{-d}}$): good agreement with theory (TRIUMF TOF, PSI low ϕ)

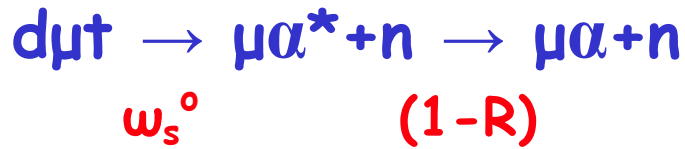
$\mu\text{t}+\text{HD}$ ($\lambda_{\text{dt}\mu\text{-p}}$): qualitative agreement with theory (TRIUMF & PSI)

$\mu\text{t}+\text{DT}$ ($\lambda_{\text{dt}\mu\text{-t}}$): smaller rate increase with T than predicted by theory (LAMPF & Dubna)

- μ CF in solid D-T: rates $\sim$ same as in liquid (RIKEN/RAL- PSI), cf. solid state theory by A. Adamczak, Hyp.Int. 119 (1999) 23.

The RIKEN/RAL experiment has reported strange temperature effects (16 K $\rightarrow$ 5K) K. Nagamine, Hyp.Int. 138 (2001) 5.

II $\mu\alpha$ - sticking



theory

ω_s^0 initial sticking

$\sim 0.92\%$

R reactivation ($\mu\alpha$ -stripping)
slightly density dependent!

0.30-0.36

$\omega_s = \omega_s^0 (1-R)$ final sticking

0.59-0.65%

w „effective sticking“

$= \omega_s + \text{other muon loss terms}$

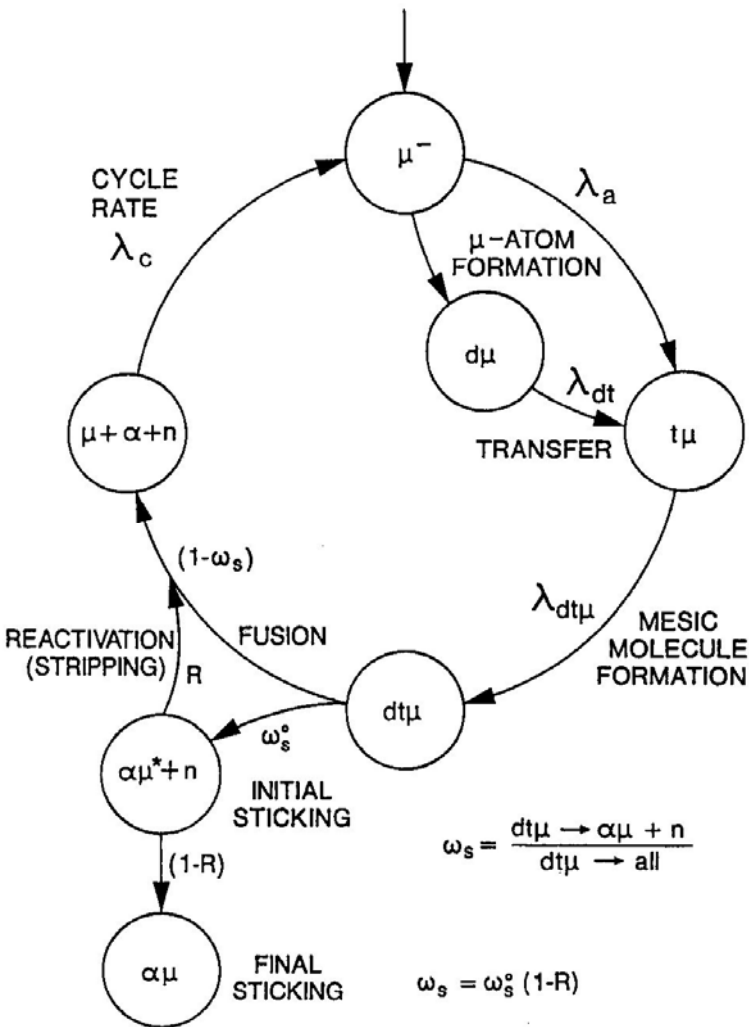
e.g. dd, hd, tt, ht channels, μ transfers

fusion time curve & yield:

$$N_f(t) = \Lambda_c e^{-(\lambda_\mu + w\Lambda_c)t}$$

$$Y_f = \int N_f = \Lambda_c / (\lambda_\mu + w\Lambda_c) < w^{-1} < \omega_s^{-1}$$

Gerstein et al., JETP 51 (1981) 1053



theory: $Y_f^{\text{th}} < 170$ D-T fusions/muon

methods of sticking measurements

1) neutron time spectra

$$N_n(t) = \varepsilon_n \Lambda_c e^{-(\lambda_n * t)} \quad \text{neutron time distribution}$$

$$\lambda_n = \lambda_\mu + w \Lambda_c \quad \text{neutron disappearance rate}$$

$$\lambda_\mu \quad \text{muon decay rate}$$

$$w = \omega_s + \text{other loss channels} = \text{muon loss per cycle}$$

$$\Lambda_c = \varphi \lambda_c \quad \text{effective cycle rate}$$

$$Y_f = \Lambda_c / (\lambda_\mu + w \Lambda_c) \quad \text{fusion yield per muon}$$

$$\omega_s = w - \omega_{tt} \frac{\Lambda_{t\mu t} \lambda_f^{tt}}{\Lambda_{d\mu t} (\lambda_f^{tt} + \Lambda_{t\mu t})} - \frac{P_{1s} (\bar{\omega}_{dd} \Lambda_{d\mu d} + \omega_{pd} \Lambda_{p\mu d})}{\Lambda_{dt} + (1 - P_{1s}) \Lambda_{d\mu d}} - \omega_{pt} \frac{\Lambda_{p\mu t}}{\Lambda_{d\mu t}}$$

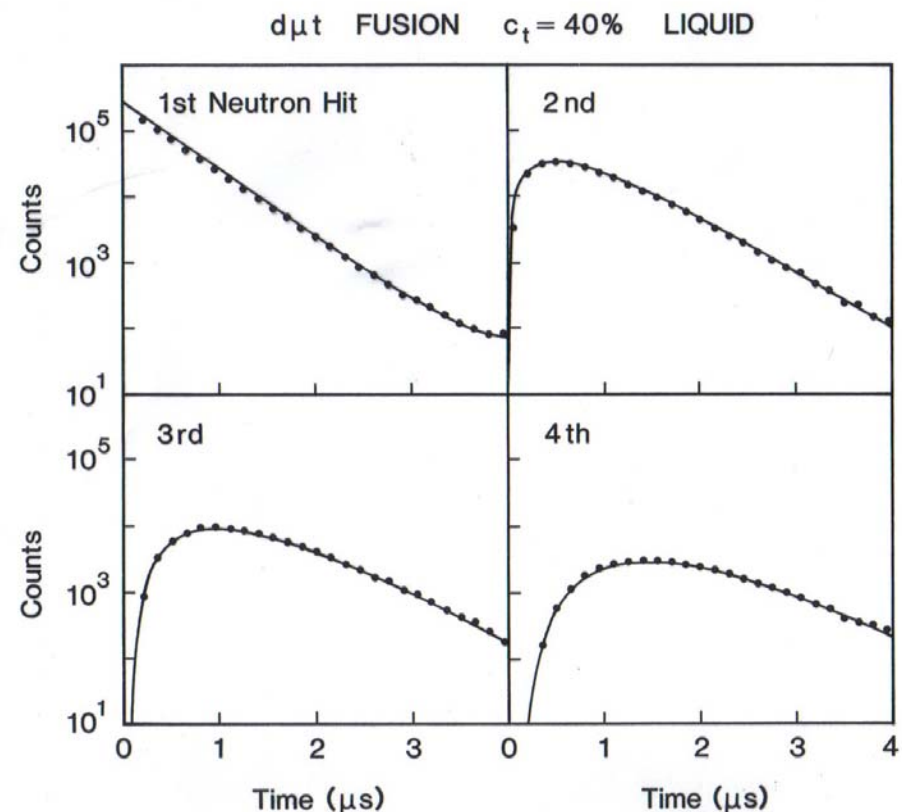
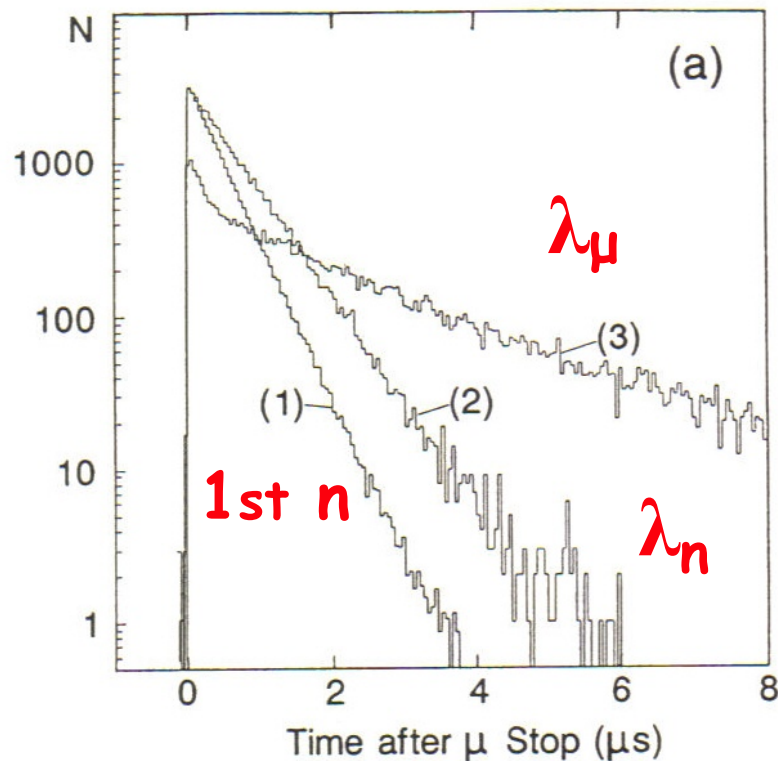
slope of neutron time spectra

$$\text{disappearance rate } \lambda_n = - (\lambda_\mu + w \Lambda_c)$$

→ w most sensitive to large Λ_c ($\gg \lambda_\mu$)
all observed in liquid and solid D-T mixtures !

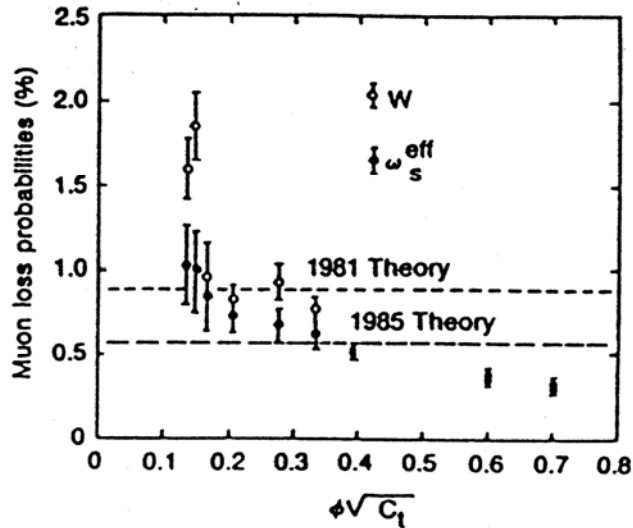
solid non-eq DT $\Lambda_c = 2 * 10^8 \text{ s}^{-1}$

liquid DT $\Lambda_c = 1.5 * 10^8 \text{ s}^{-1}$

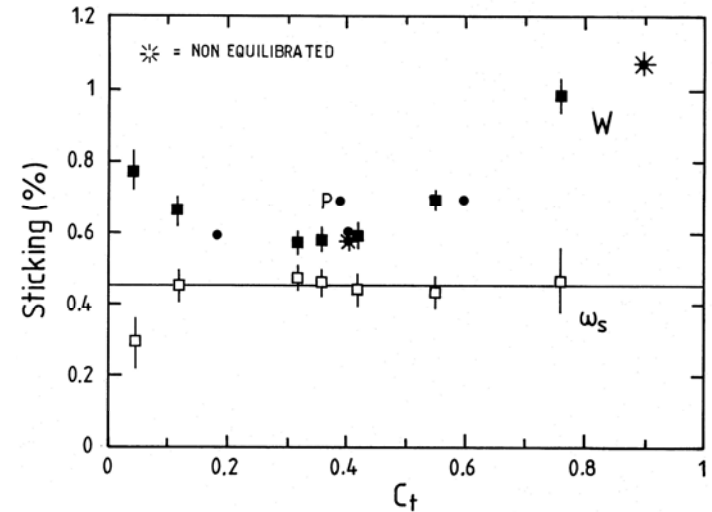


world results on w from high-yield n-disappearance data

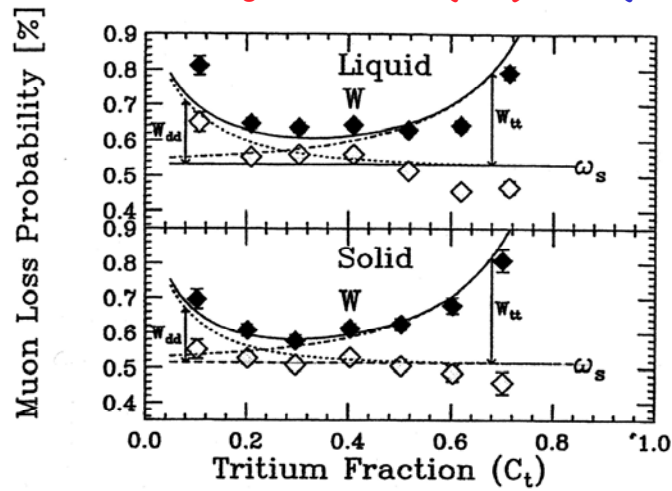
LAMPF 1986: $\omega_s = 0.32(3) \%$
(liquid D-T)



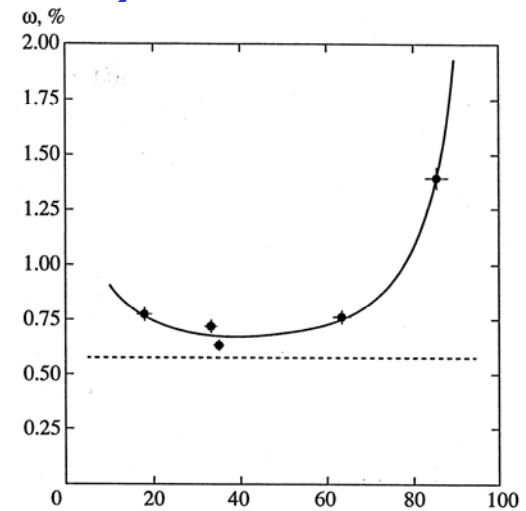
PSI 1987/93: $\omega_s = 0.485(17) \%$
(liquid & solid D-T)



RIKEN-RAL: $\omega_s = 0.515(30) \%$ (liquid D-T)
2001 $\omega_s = 0.532(30) \%$ (solid D-T)



Dubna 2005: $\omega_s = 0.574(22) \%$
(liquid D-T)



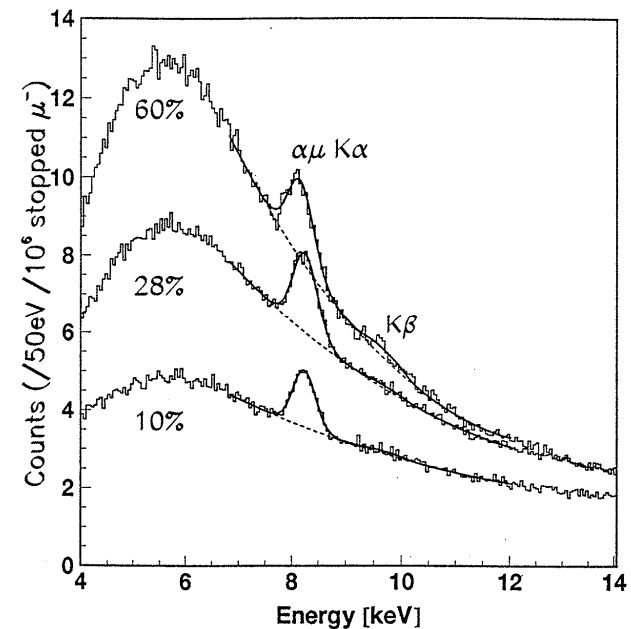
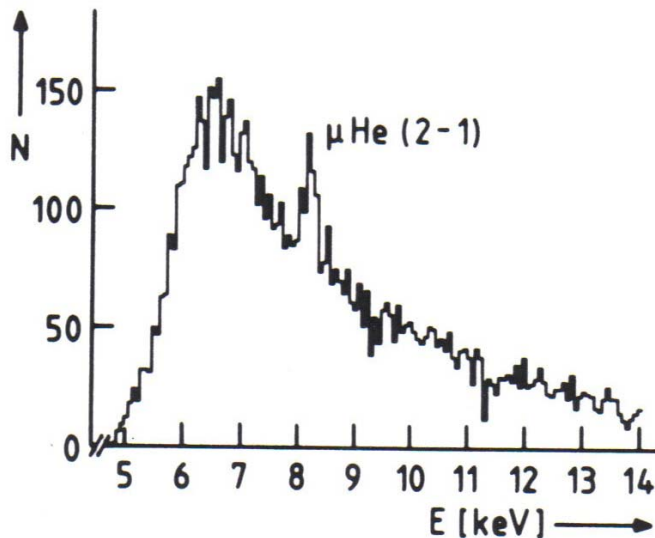
summary table of w & ω_s from neutron slope data (the worlds high-yield data in liquid & solid D-T)

Lab	references	condition	c_t	λ_c	Λ_c	w	Y_f	ω_s	comments
LAMPF 1984	S.E. Jones et al. PRL 56 (1986) 558	liquid $\varphi=1.2$	0.3	120	144	0.35(3)	150	0.32(3)	inconsistent!
	Hyp.Int.82(1993)303	liquid $\varphi=1.14$ non eq.	0.7	102	117	0.70(3)	92	0.43(5)	
PSI 1984	W. Breunlich et al. PRL 58 (1987) 329	liquid 23K $\varphi=1.20$	0.32	122	145	0.57(3)	113	0.45(5)	global fit
1987	C. Petitjean et al. Hyp.Int.82(1993) 273	solid 12K $\varphi=1.45$ non eq.	0.41	134	195	0.568(12)	124	0.485(17)	8% calib.
		liquid 23K $\varphi=1.21$ non eq.	0.41	134	162	0.554(14)	120	0.466(21)	8% calib
RIKEN -RAL 1996	K.Nagamine et al. & K. Ishida et al. Hyp.Int.138(2001) 5 & Hyp.Int.138(2001)225	solid 16K $\varphi=1.45$	0.3	~100	~145	0.57(3)	~113	0.515(30)	global fit
		liquid 20K $\varphi=1.25$	0.3	~110	~137	0.62(3)	~105	0.532(30)	global fit
JINR Dubna 2003	V.R. Bom et al. JETP 100 (2005) 663	liquid 22K $\varphi=1.20$	0.334	118	141	0.72(6)	97	0.574(22)	global fit
			0.352	118	140	0.63(5)	103		

2) X ray method



Lab	ref.	c_+	K_α -yield	sticking
PSI	H. Bossy et al. PRL 59 (1987) 2864	0.0004	0.19(5)%	0.42(14)%
RIKEN- RAL	K. Ishida et al. Hyp.Int.138(2001) 225	0.1-0.7 0.1-0.7	0.273(17) 0.279(17)	(0.532 %) liquid D-T (0.515 %) solid D-T



3) direct observations of sticking

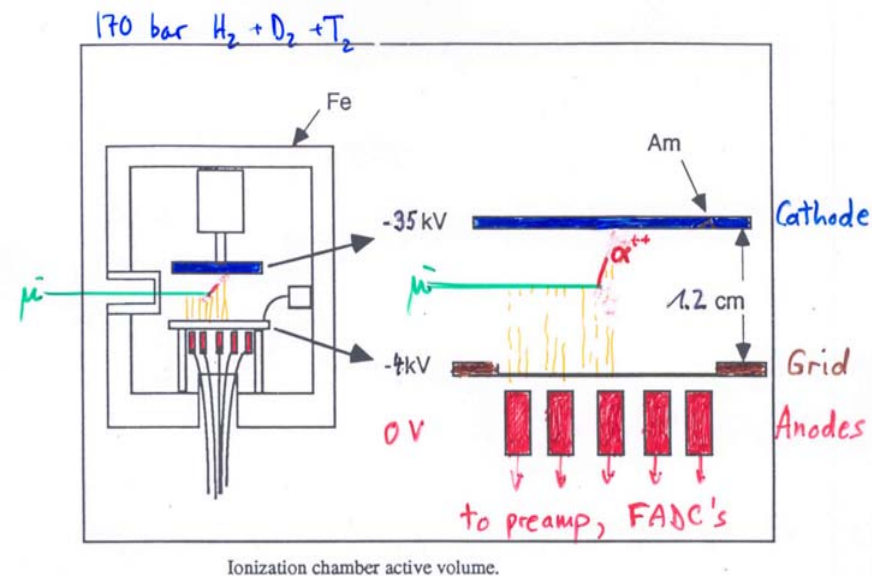
PSI T.Case, K. Lou et al.

H/D/T mixture at 70 bar ($c_t=0.036\%$)

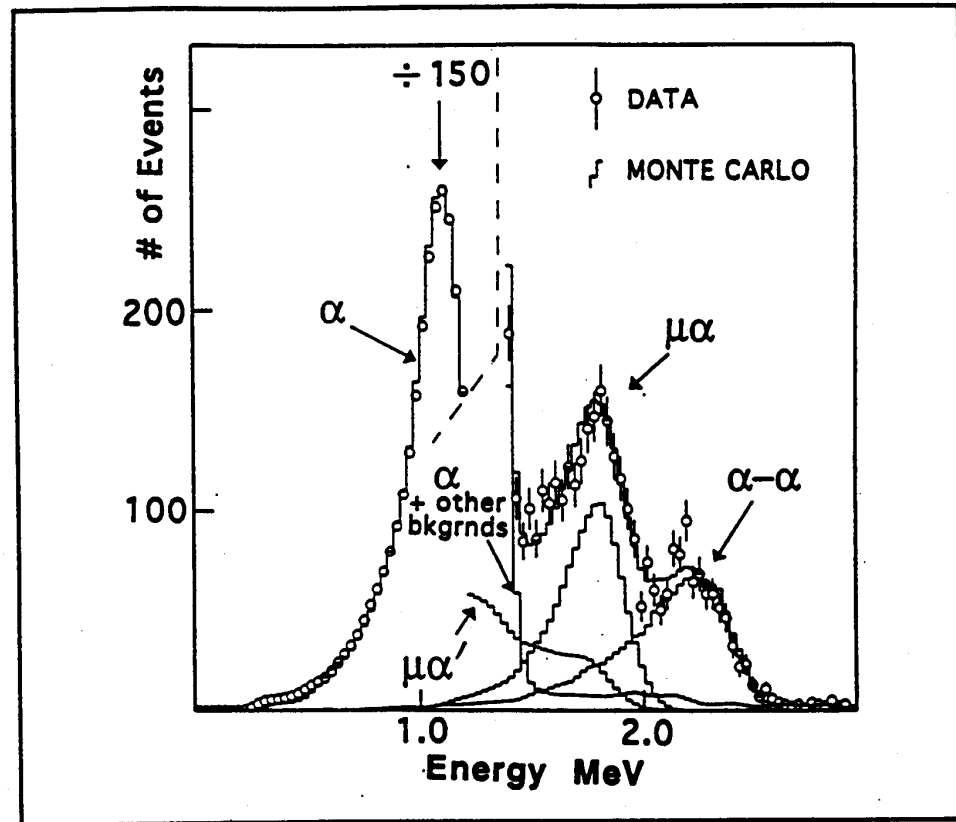
1992 Hyp.Int. 82 (1993) 295
Hyp.Int. 118 (1999) 197

final result:

$$\omega_s = 0.57 \pm 0.04 \%$$



**Gatchina ionisation chamber
using recombination effect !**



survived muon method (developed by Gatchina)

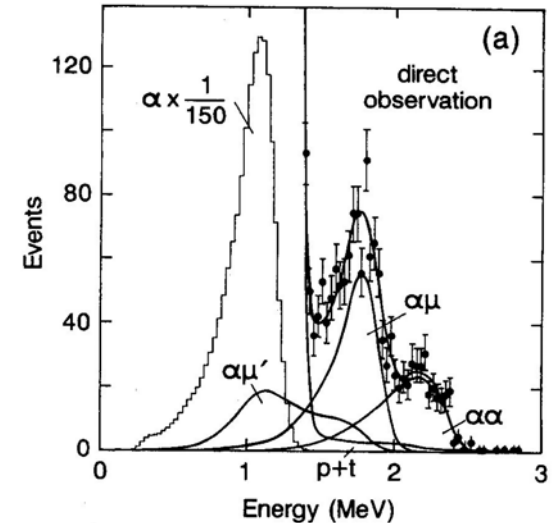
K. Lou et al., Hyp.Int. 82 (1993) 313 and thesis

C. Petitjean et al., Hyp.Int. 82 (1993) 273

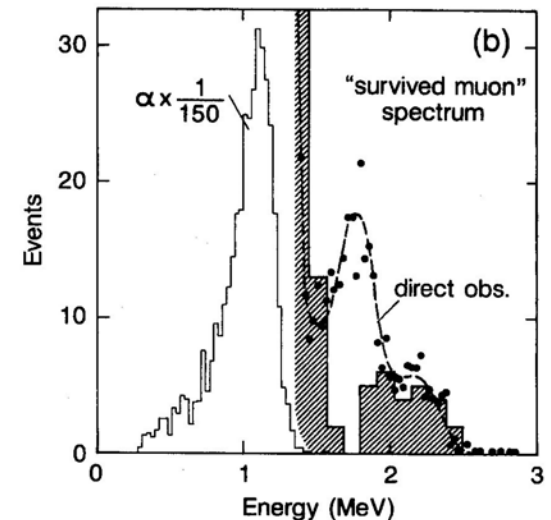
$$\omega_s = 0.565 \pm 0.052 \%$$

proves beyond any doubt presence of sticking !

(a) direct observation
with sticking & stripping



(b) events with 2nd fusion
sticking peak absent !



direct observation of initial sticking ω_s^0

LAMPF
1988

M.A. Paciotti et al.

AIP Conf.Proc 181 (1989) 38

S.E. Jones, AIP 181 (1989) 2

D-T mixture at 2.4 bar ($c_T=40\%$)

$$\omega_s^0 = (0.80 \pm 0.15 \pm 0.12)\%$$

$$\text{theory: } (0.92 \pm 0.02)\%$$

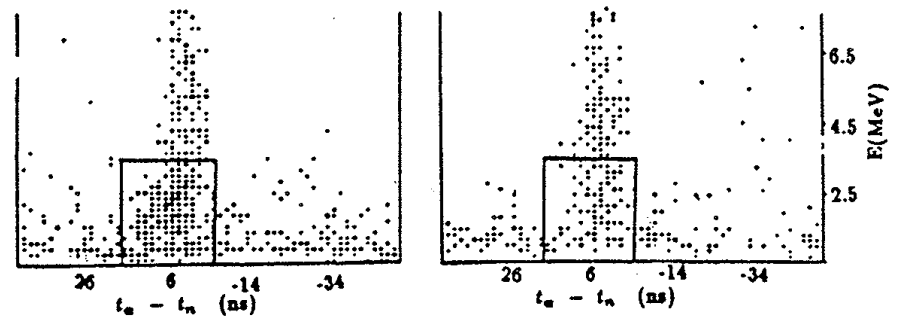
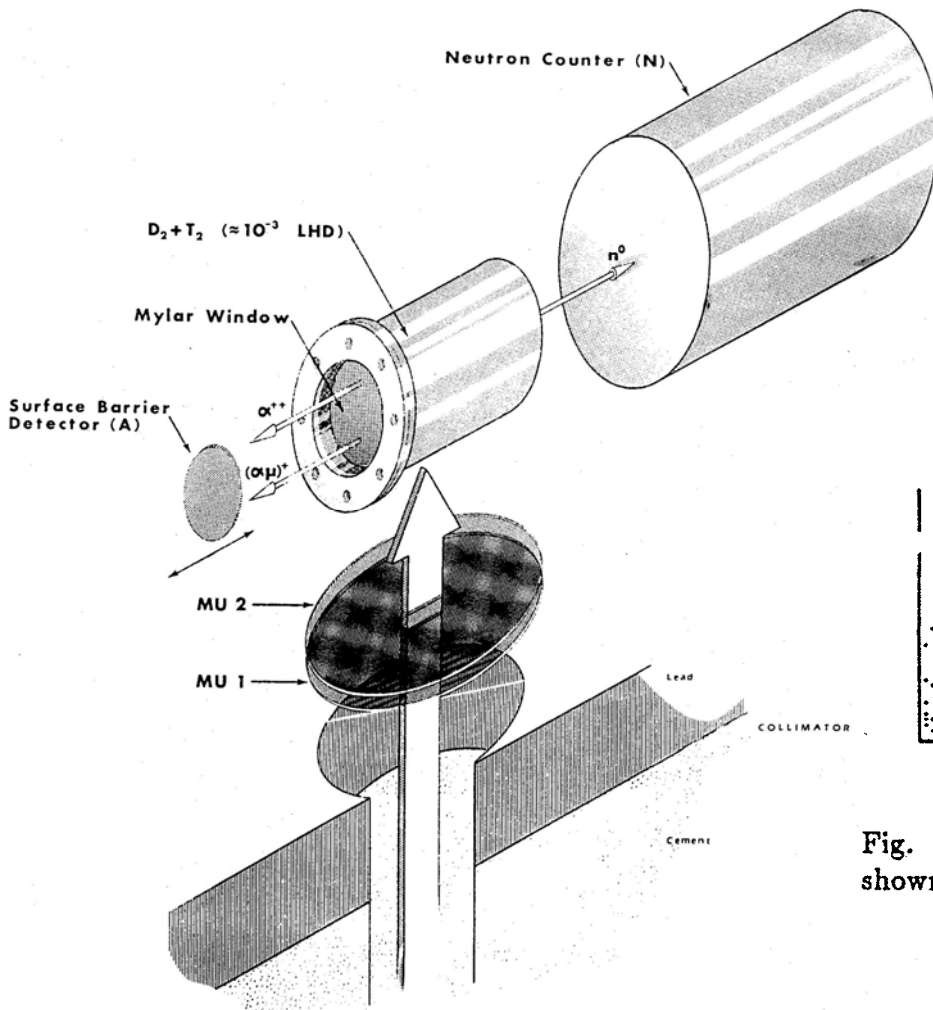


Fig. 6. The $(\alpha\mu)^+$ spectrum for all data taken at 1800 Torr. Background is shown on the right for 3/4 number of incident muons.

conclusions II on $\mu\alpha$ sticking

- the **slope** results scatter $\pm 14\%$ around a "world average" $w_s = 0.5\%$ that is $\sim 2-3$ times the estimated systematic errors (without S.E. Jones inconsistent 1984 data - 6 std. deviations off) perhaps it reflects the difficulty of absolute neutron calibrations! this average is **20%** below theory
- however the recent Dubna slope data are $\approx$ consistent with theory $(0.574 \pm 0.022)\%^{exp}$ vs. $(0.60 \pm 0.02)\%^{th}$
- the **X ray** method (RIKEN/RAL) experiment observes **10-20%** lower X ray yields and there are some inconsistencies with K_β , K_γ yields
- the w_s direct observation (PSI) experiment agrees nicely with theory $(0.57 \pm 0.04)\%^{exp}$ vs. $(0.62 \pm 0.02)\%^{th}$
- the w_s^0 direct observation (LAMPF) experiment also agrees with theory, though within large errors $(0.80 \pm 0.15 \pm 0.12)\%^{exp}$ vs. $0.92\%^{th}$
- question: **can sticking be overcome?**
the exp. answer is: **no evidence!** It looks very difficult to go beyond $\mu\alpha$ fusion yields of ≈ 130 per $\mu\alpha$.

what can we experimentally do in the future?

- understand better the **d₂t kinetics**, especially at the **epithermal resonances** → more measurements at high temperatures ($T = 1000\text{--}2000\text{ K}$) are needed.

(goal proposed by the Dubna group)

- understand better the lowest temperature physics
(**solid state effects, ortho/para effects** in D_2 molecules)

(proposal of the Japanese group for the J-PARK facility)

we wish for these upcoming experiments good luck!